

# Flavor changing *H* and *Z* decays

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arXiv: 2306.17520 with

J. F. Kamenik & A. Korajac (JSI), M. Szewc & J. Zupan (U. Cincinnati)



- **Goal:** assess the potential of  $e^+e^-$  colliders to explore FC decays
- **Ingredients:**
  - Clean environment of  $e^+e^-$  colliders
  - State-of-the-art and future flavor taggers
  - Analysis technique we propose
- **Take home messages:**
  - Upper limits at FCC-ee are above the SM level
  - Improve limits on Higgs FC couplings
  - Results depend on taggers performances
- **Disclaimer:** projections for FCC-ee, we expect very similar results at CepC

# Current status

Decay	SM prediction	exp. bound	indir. constr.
$\mathcal{B}(h \rightarrow bs)$	$(8.9 \pm 1.5) \cdot 10^{-8}$	0.16 ▲	$2 \times 10^{-3}$ ★
$\mathcal{B}(h \rightarrow bd)$	$(3.8 \pm 0.6) \cdot 10^{-9}$	0.16 ▲	$10^{-3}$ ★
$\mathcal{B}(h \rightarrow cu)$	$(2.7 \pm 0.5) \cdot 10^{-20}$	0.16 ▲	$2 \times 10^{-2}$ ★
$\mathcal{B}(Z \rightarrow bs)$	$(4.2 \pm 0.7) \cdot 10^{-8}$	$2.9 \times 10^{-3}$ ■	$6 \times 10^{-8}$ ●
$\mathcal{B}(Z \rightarrow bd)$	$(1.8 \pm 0.3) \cdot 10^{-9}$	$2.9 \times 10^{-3}$ ■	$6 \times 10^{-8}$ ●
$\mathcal{B}(Z \rightarrow cu)$	$(1.4 \pm 0.2) \cdot 10^{-18}$	$2.9 \times 10^{-3}$ ■	$4 \times 10^{-7}$ ●

▲  $h \rightarrow$  BSM (CMS+ATLAS, 2207.00043)

■  $\Gamma(Z \rightarrow \text{had})$  (hep-ex/0012018)

★ Meson mixings

● Global fits (mostly semi-leptonic)

## Z pole running

$$\sqrt{s} = m_Z$$

$$e^+e^- \rightarrow Z \rightarrow qq'$$

Parameters	Nominal value	Rel. uncert. (in %)
$\mathcal{B}(Z \rightarrow uu + dd)$	27.01%	5.0
$\mathcal{B}(Z \rightarrow ss)$	15.84%	3.8
$\mathcal{B}(Z \rightarrow cc)$	12.03%	1.7
$\mathcal{B}(Z \rightarrow bb)$	15.12%	0.33
$N_Z$	$5 \times 10^{12}$	$10^{-3}$
$\mathcal{A}$	0.994	$10^{-3}$

1905.03764

FCC Conceptual Design Reports

G. Marchiori's talk at "Higgs Performance meeting"  
([indico.cern.ch/event/1221257](https://indico.cern.ch/event/1221257))

## hZ running

$$\sqrt{s} = 240 \text{ GeV}$$

$$e^+e^- \rightarrow Z^* \rightarrow hZ (Z \rightarrow \ell^+\ell^-, h \rightarrow qq')$$

Parameters	Nominal Value	Rel. uncert. (%)
$\mathcal{B}(h \rightarrow gg)$	1.4%	1.2
$\mathcal{B}(h \rightarrow ss)$	0.024%	160
$\mathcal{B}(h \rightarrow cc)$	2.9%	2.8
$\mathcal{B}(h \rightarrow bb)$	56%	0.4
$N_h$	$6.7 \times 10^5$	0.5
$\mathcal{A}$	0.70	0.1

Other backgrounds ( $\tau^+\tau^-$  for Z, DY, WW, ZZ for h) are negligible

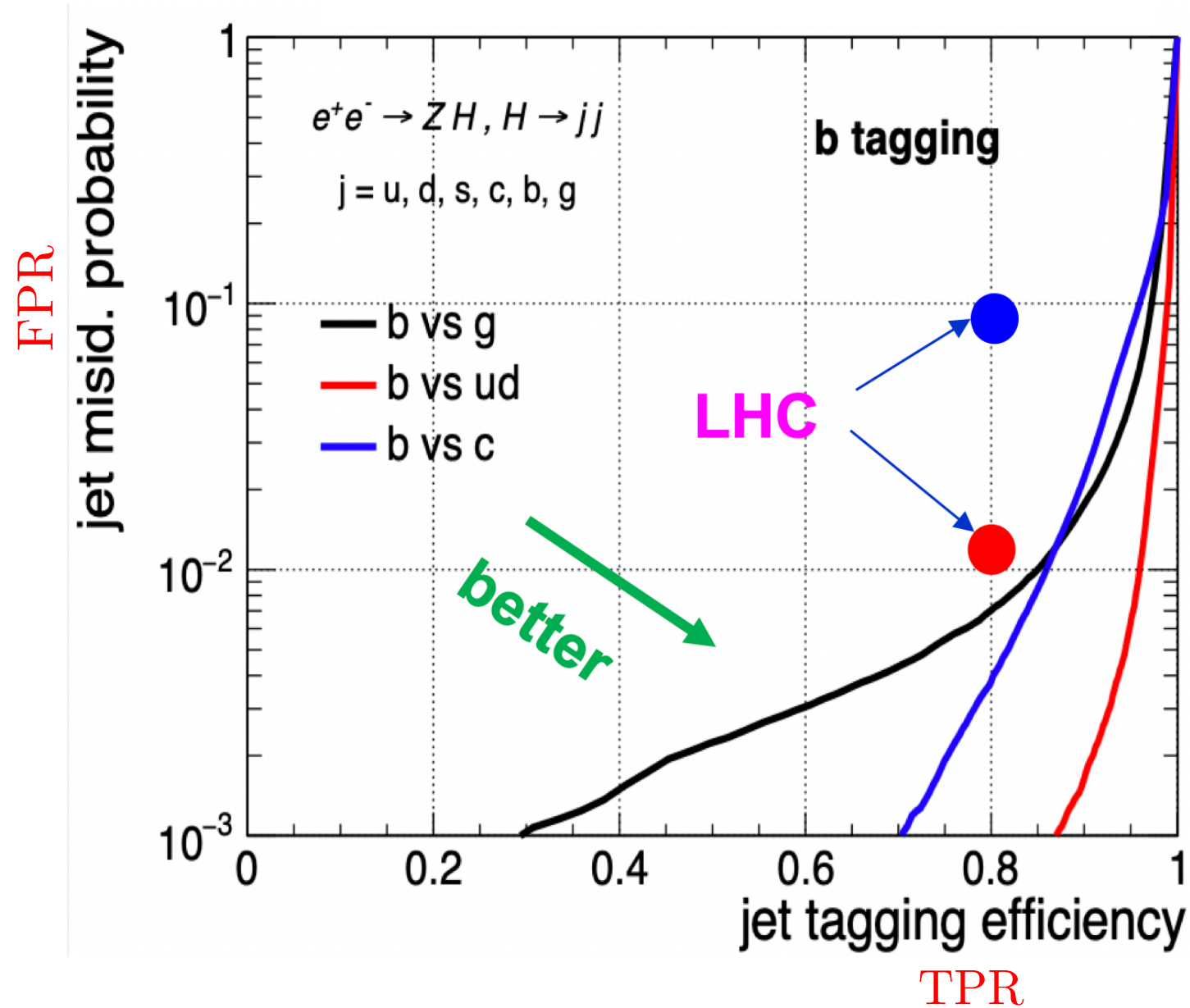
G. Marchiori's talk at "FCC Physics  
Workshop" ([indico.cern.ch/event/1176398/](https://indico.cern.ch/event/1176398/))



# Jet flavor taggers @FCC-ee

Tools to classify flavor of jets from input data

ParticleNet: 1902.08570  
 Jet-Flavor tagging at FCC-ee: 2210.10322



*q*-tagger rates

$$\epsilon_{\beta}^q \quad \beta = \{g(ud), s, c, b\}$$

WPs for *h* decays

$$\epsilon_{\beta; \text{Loose}}^b = \{0.02, 0.001, 0.02, 0.90\}$$

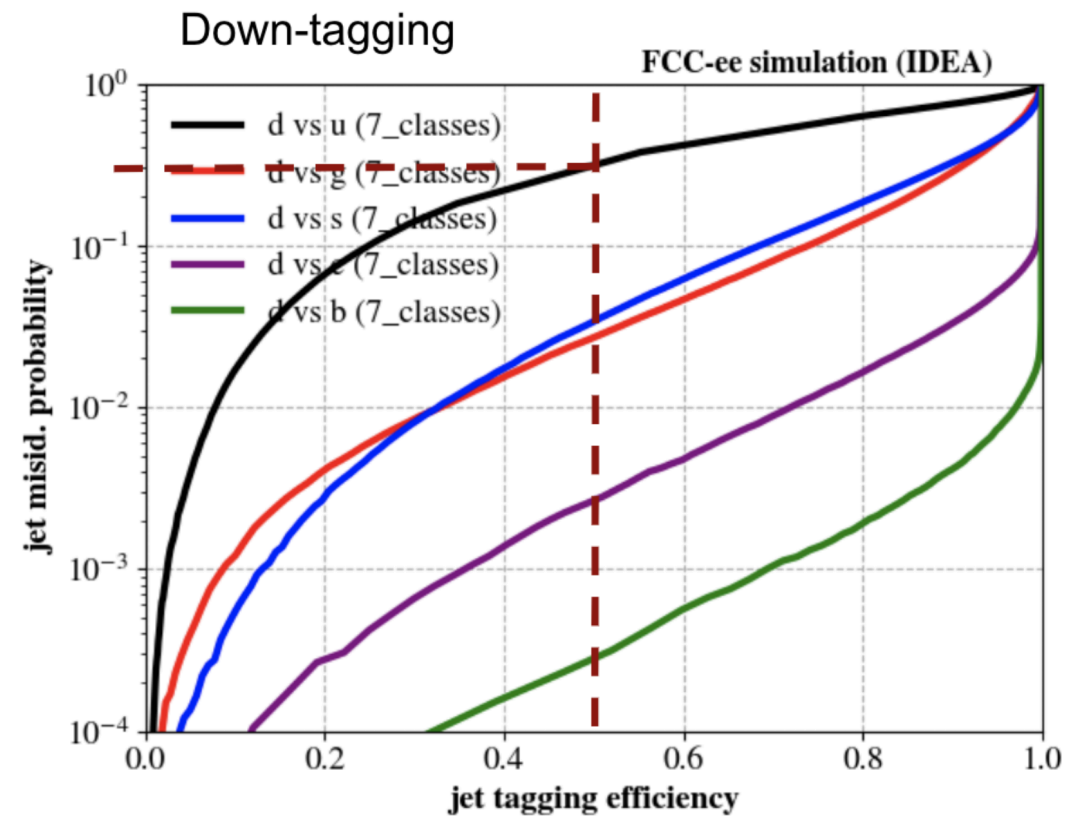
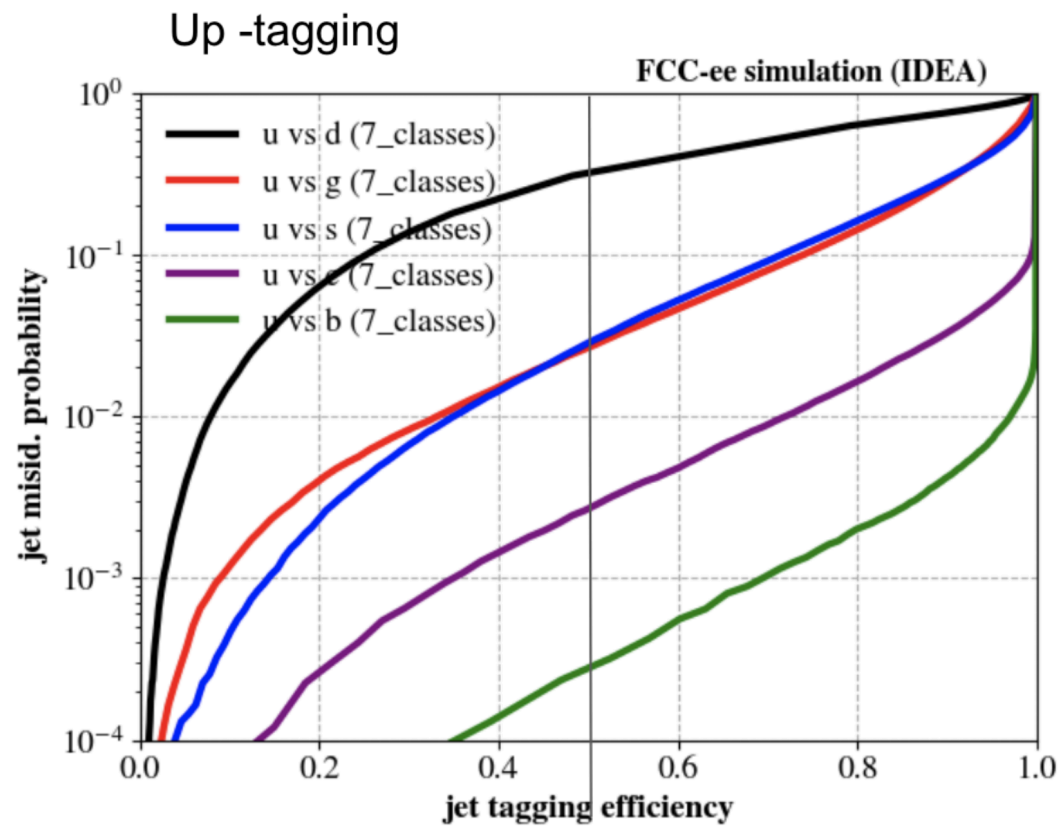
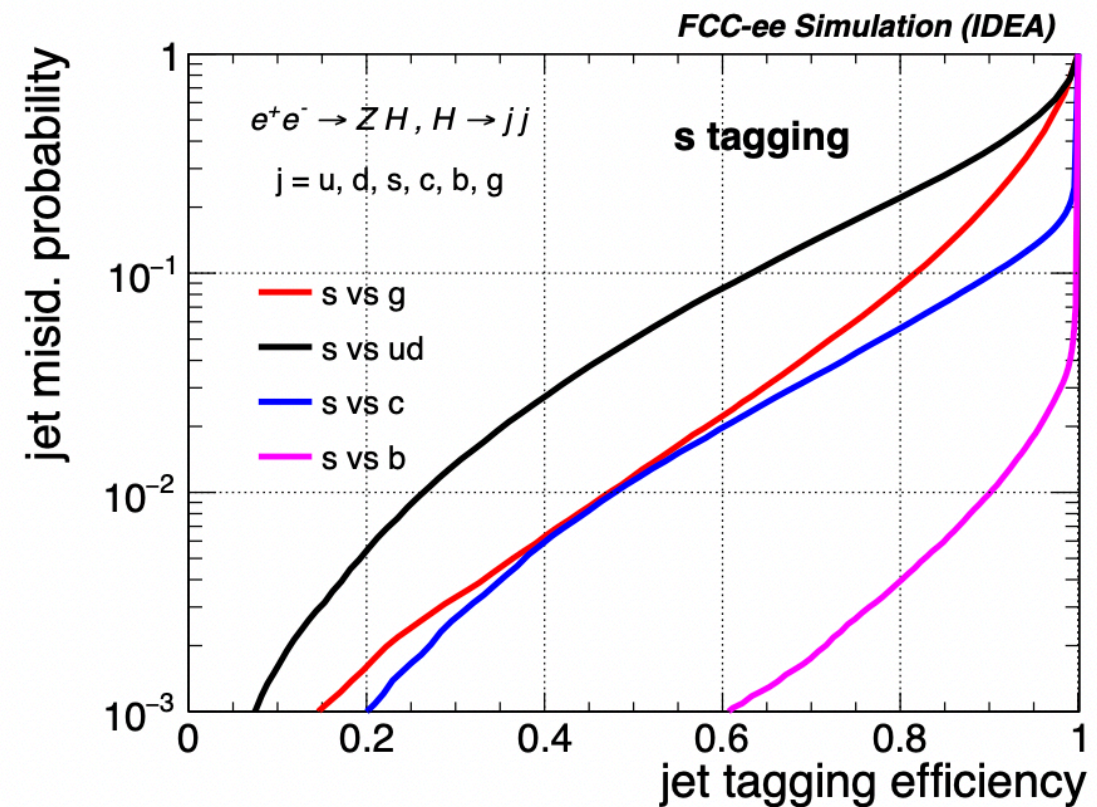
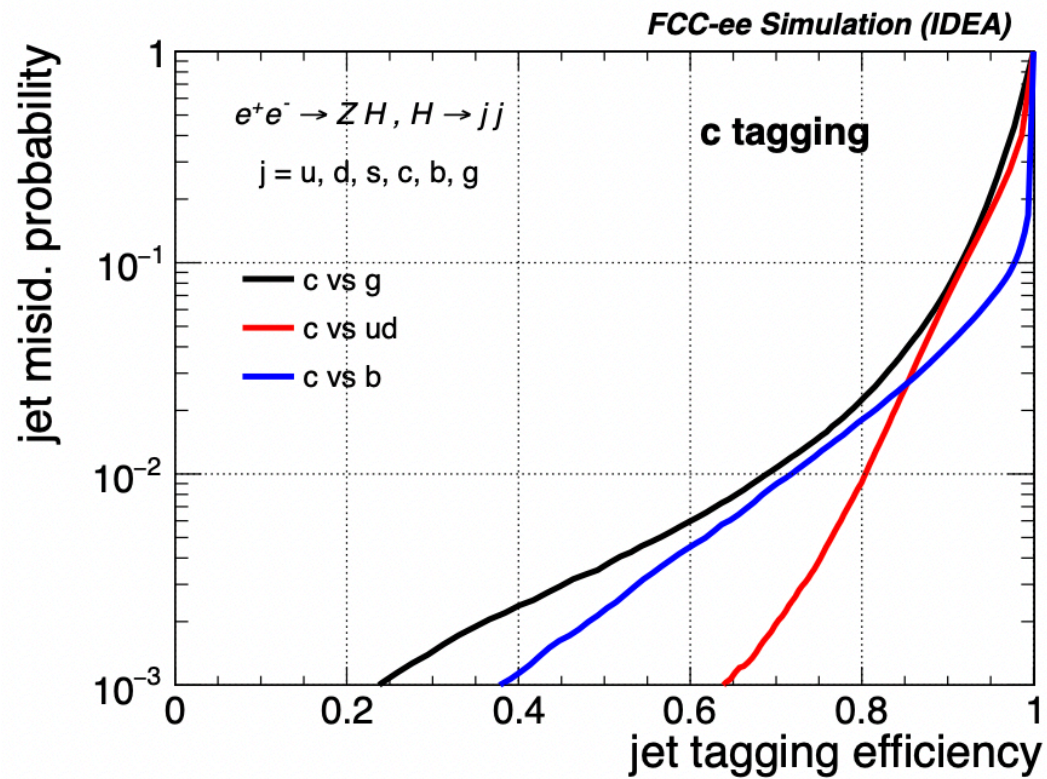
$$\epsilon_{\beta; \text{Med}}^b = \{0.007, 0.0001, 0.003, 0.80\}$$

Currently  $\mathcal{O}(\text{few})\%$  syst. on  $\epsilon_{\beta}^q$

ATLAS: 1907.05120  
 CMS: 1712.07158

Bedeschi, Gouskos, Selvaggi: 2202.03285  
 Gouskos' talk at "FCC Physics Workshop" ([indico.cern.ch/event/1176398/](https://indico.cern.ch/event/1176398/))

# Jet flavor taggers @FCC-ee

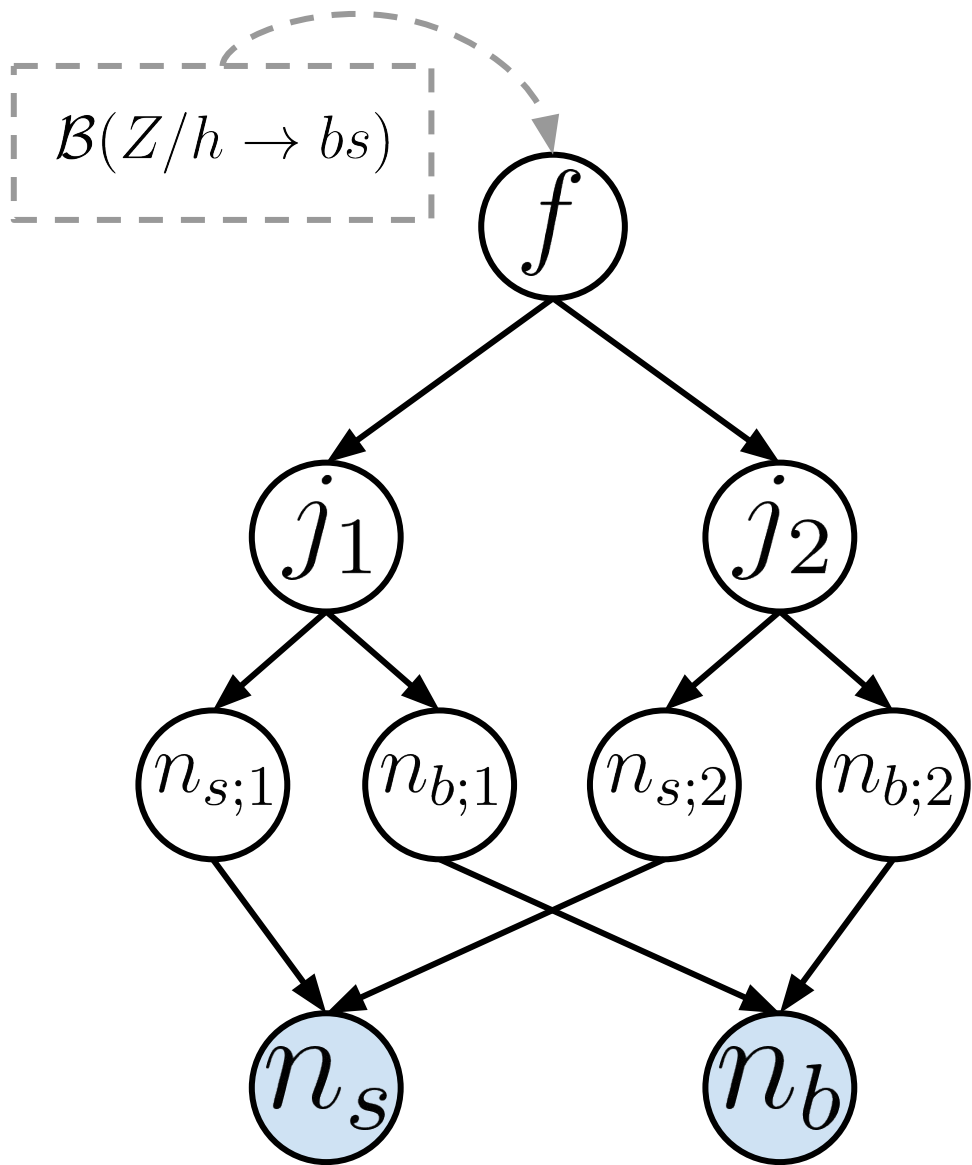


# Probabilistic model

ATLAS: 2201.11428

CMS: 2004.12181

Faroughy, Kamenik, Szewc, Zupan: 2209.01222



Distribute events into tag bins

$$(n_b, n_s) = \{(0, 0), (0, 1), (1, 0), (2, 0), (0, 2), (1, 1)\}$$

Expected number of events per channel

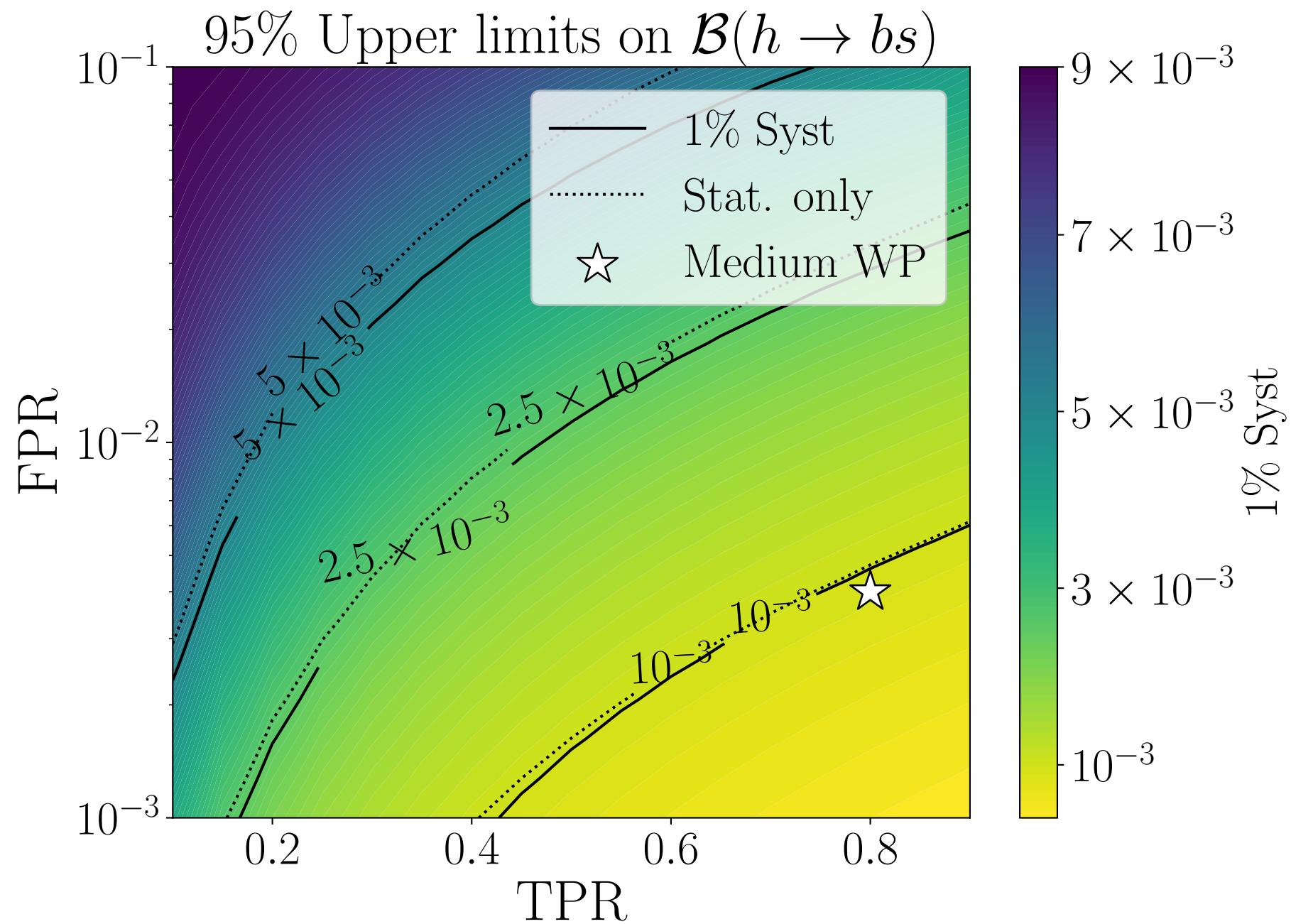
$$\bar{N}_f = \mathcal{B}(Z/h \rightarrow f) N_{Z/h} \mathcal{A}$$



Expected number of events per tag bin

$$\bar{N}_{(n_b, n_s)} = \sum_f p(n_b, n_s | f, \nu) \bar{N}_f(\nu)$$





Take common TPR and FPR (for plots)

Medium WP

$(\text{TPR}, \text{FPR}) = (0.8, 0.004)$

$\text{FPR} = \max(\epsilon_s^b, \epsilon_b^s)$

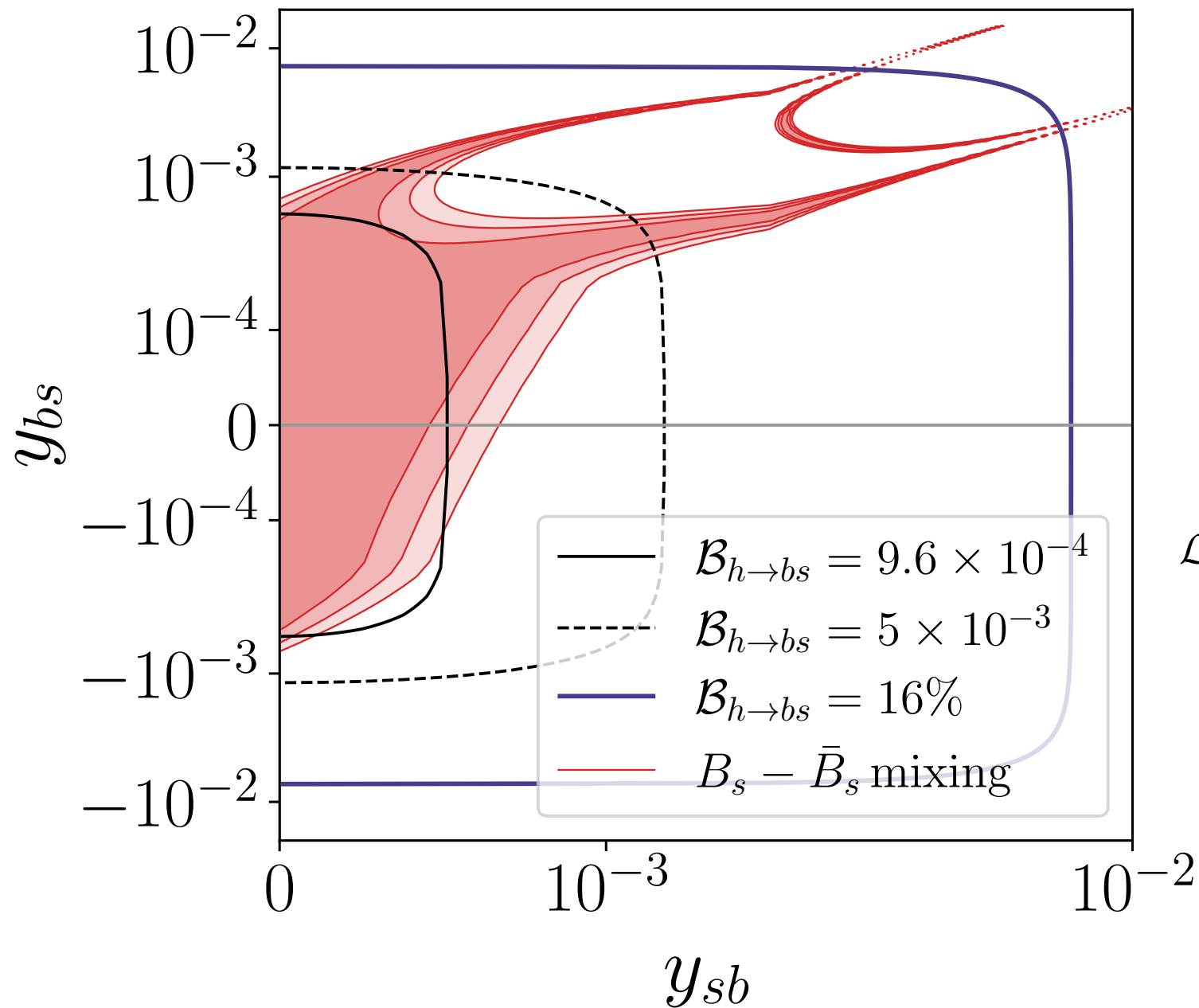
FCC-ee reach

$$\mathcal{B}(h \rightarrow bs) \lesssim 9.6 \times 10^{-4}$$

Indirect constraints

$$\mathcal{B}(h \rightarrow bs) \lesssim 1.6 \times 10^{-3}$$

$$\mathcal{L} \supset y_{sb}(\bar{s}_L b_R)h + y_{bs}(\bar{b}_L s_R)h + \text{h.c.}$$



Match to WET + wilson + flavio

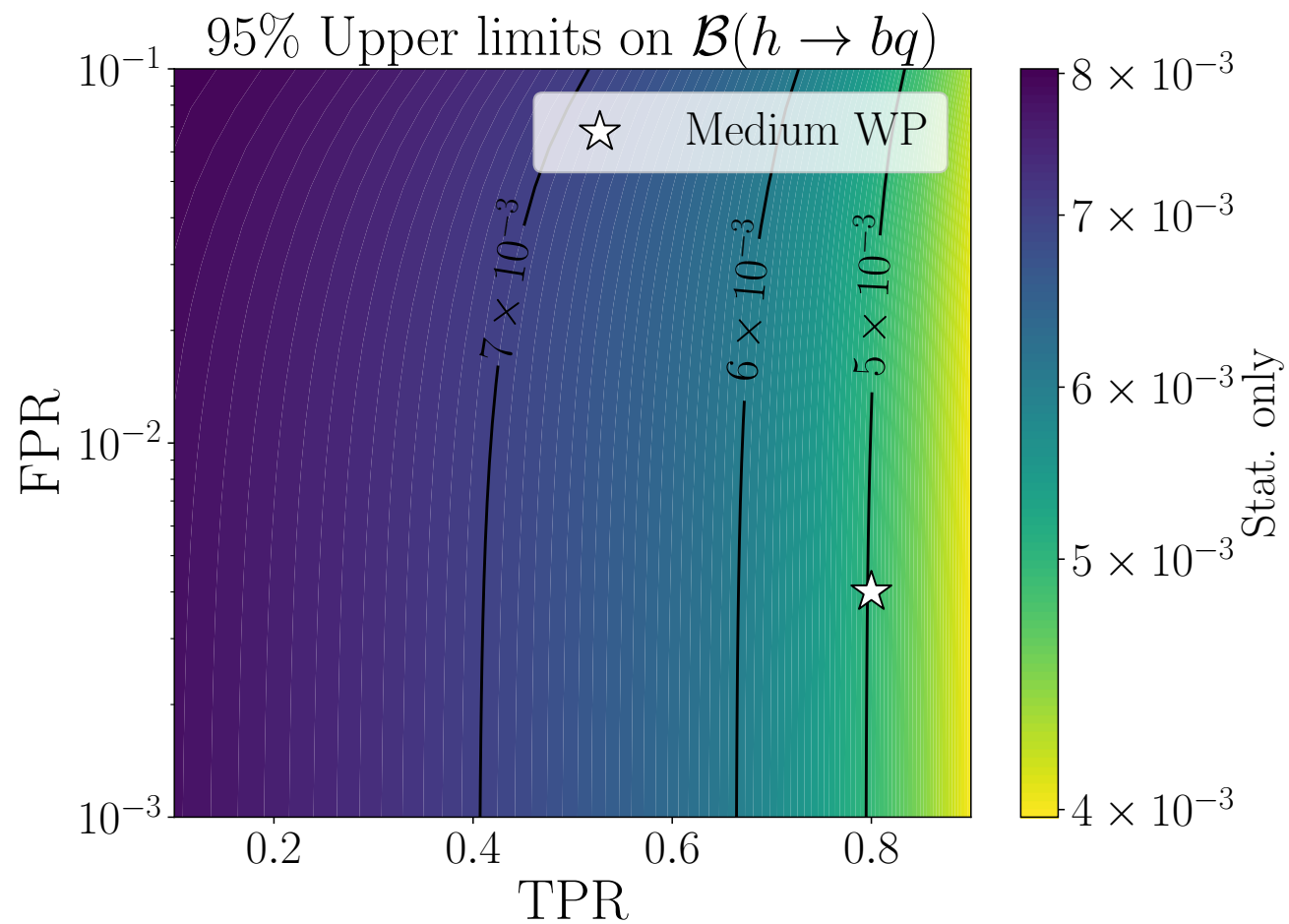
$$\mathcal{L}_{\text{WET}} \supset C_2(\bar{s}_R b_L)^2 + C'_2(\bar{s}_L b_R)^2 + C_4(\bar{s}_L b_R)(\bar{s}_R b_L)$$

FCC-ee reach

Indirect constraints

$$\mathcal{B}(h \rightarrow bs) \lesssim 9.6 \times 10^{-4}$$

$$\mathcal{B}(h \rightarrow bs) \lesssim 1.6 \times 10^{-3}$$



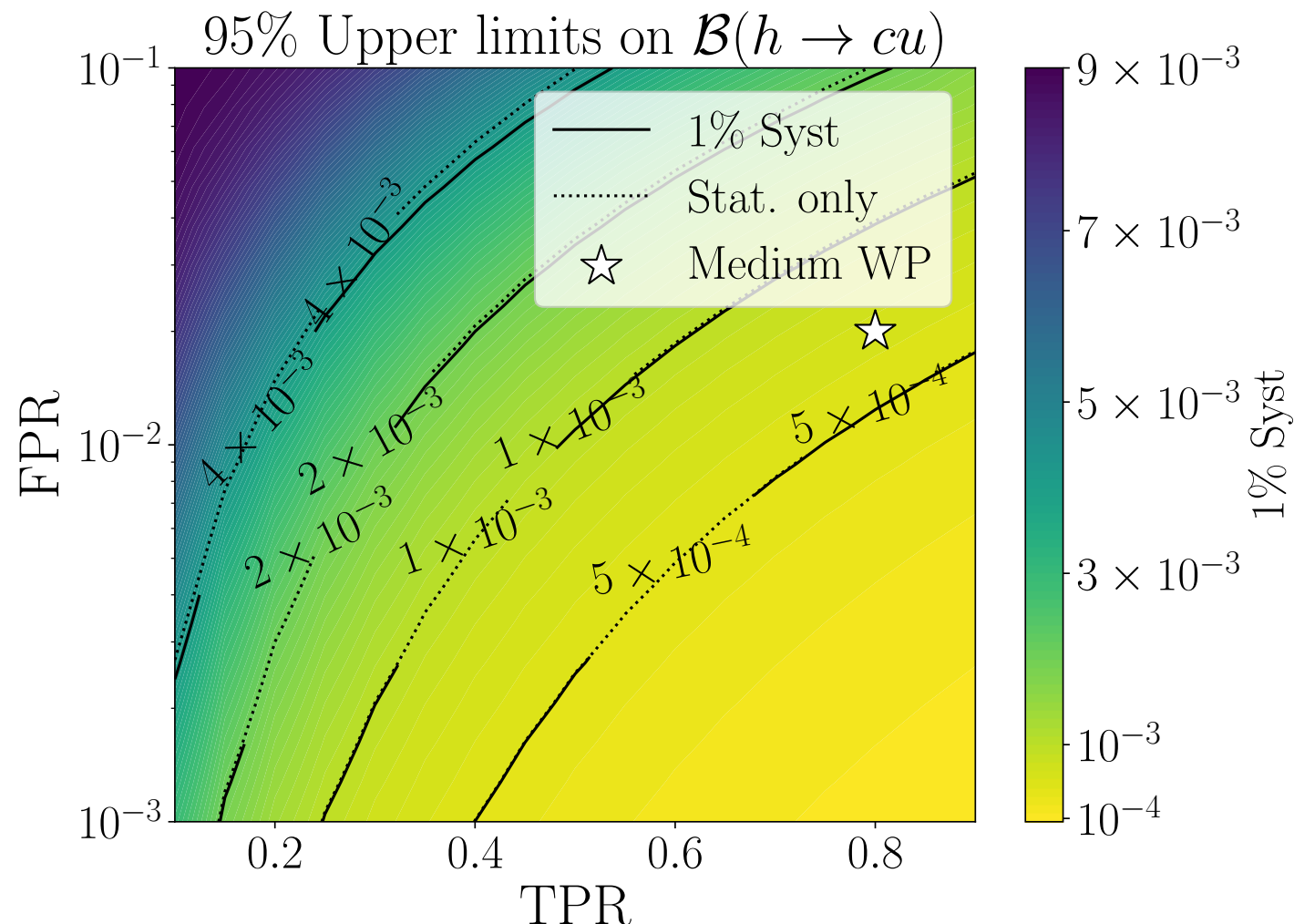
$$\mathcal{B}(h \rightarrow bq) = \mathcal{B}(h \rightarrow bs) + \mathcal{B}(h \rightarrow bd)$$

Medium WP

$$(\text{TPR}, \text{FPR}) = (0.8, 0.004)$$

FCC-ee reach (no d-tagger)

$$\mathcal{B}(h \rightarrow bq) \lesssim 5 \times 10^{-3}$$



Medium WP

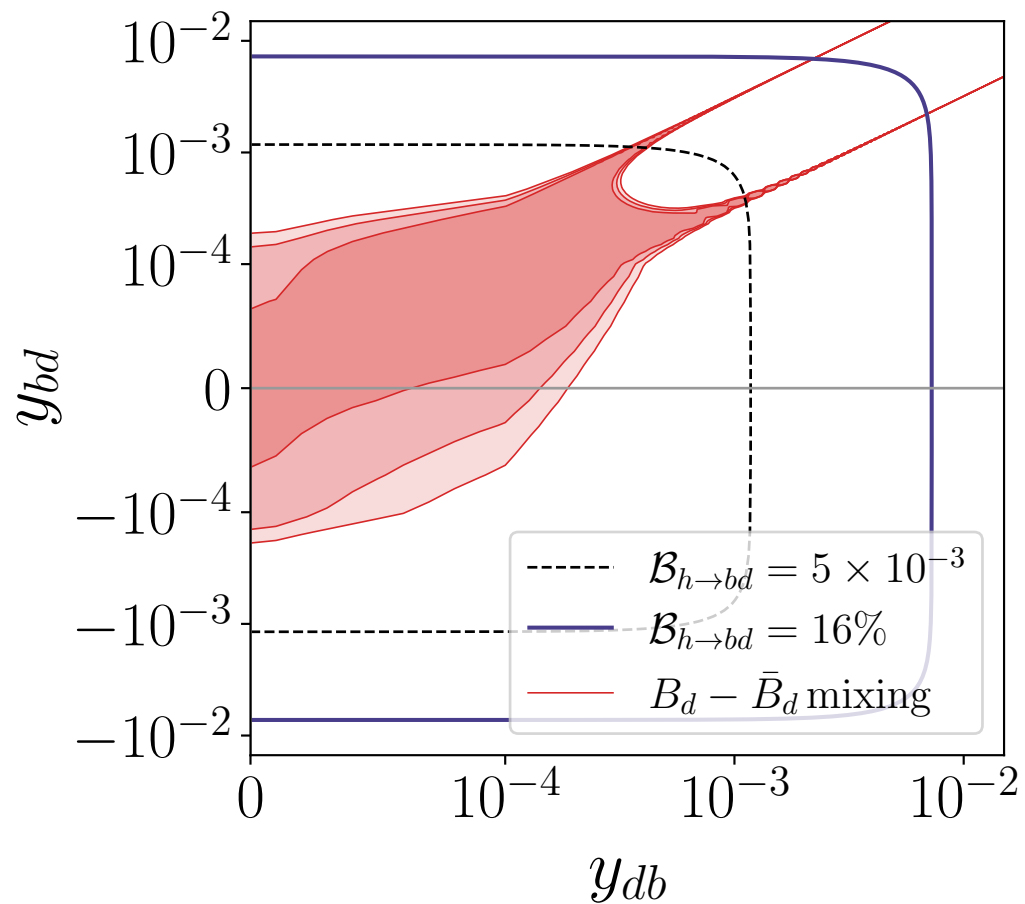
$$(\text{TPR}, \text{FPR}) = (0.8, 0.02)$$

FCC-ee reach (no u-tagger)

$$\mathcal{B}(h \rightarrow cu) \lesssim 2.5 \times 10^{-3}$$

FCC-ee reach (with u-tagger)

$$\mathcal{B}(h \rightarrow cu) \lesssim 6.6 \times 10^{-4}$$

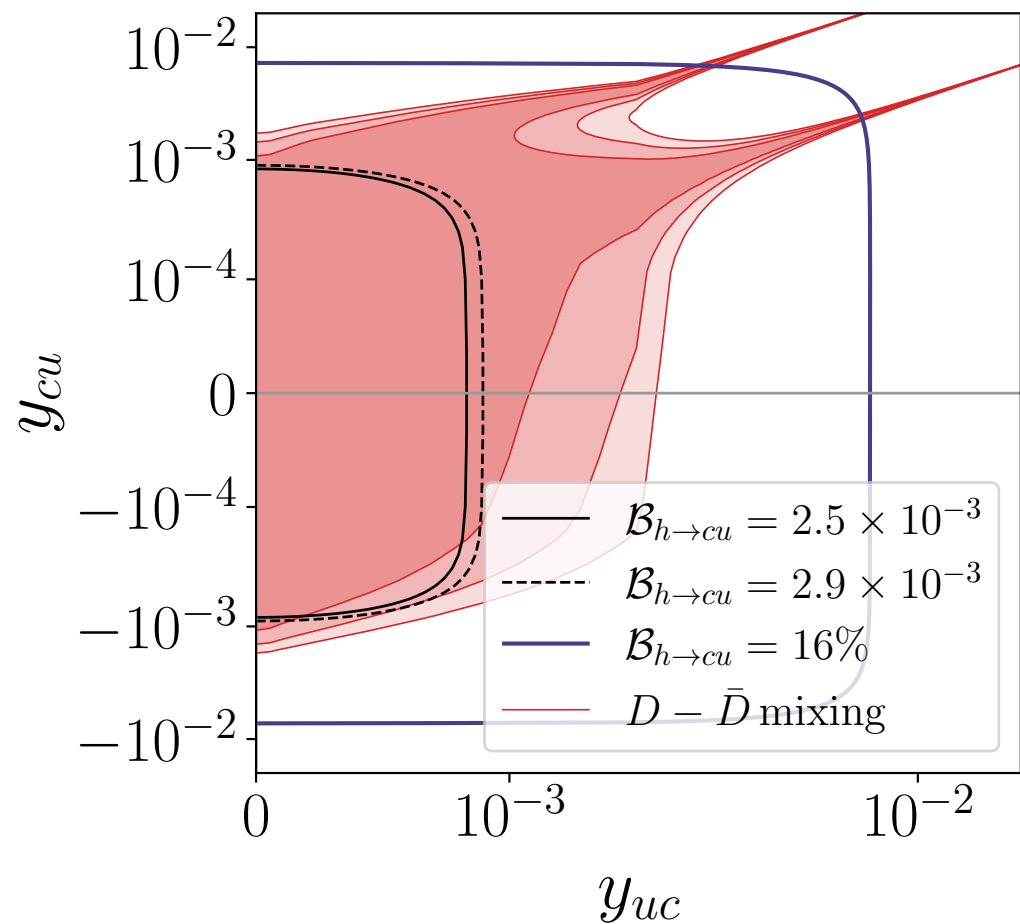


Indirect constraints

$$\mathcal{B}(h \rightarrow bd) \lesssim 10^{-3}$$

FCC-ee reach

$$\mathcal{B}(h \rightarrow bq) \lesssim 5 \times 10^{-3}$$



Indirect constraints

$$\mathcal{B}(h \rightarrow cu) \lesssim 2 \times 10^{-2}$$

FCC-ee reach (no u-tagger)

$$\mathcal{B}(h \rightarrow cu) \lesssim 2.5 \times 10^{-3}$$

FCC-ee reach (with u-tagger)

$$\mathcal{B}(h \rightarrow cu) \lesssim 6.6 \times 10^{-4}$$





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- **Ingredients:**
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  - State-of-the-art and improved flavor taggers
  - Analysis technique we propose
  
- **Take home messages:**
  - Upper limits at FCC-ee are above the SM level
  - Improve limits on Higgs FC couplings
  - Results depend on taggers performances

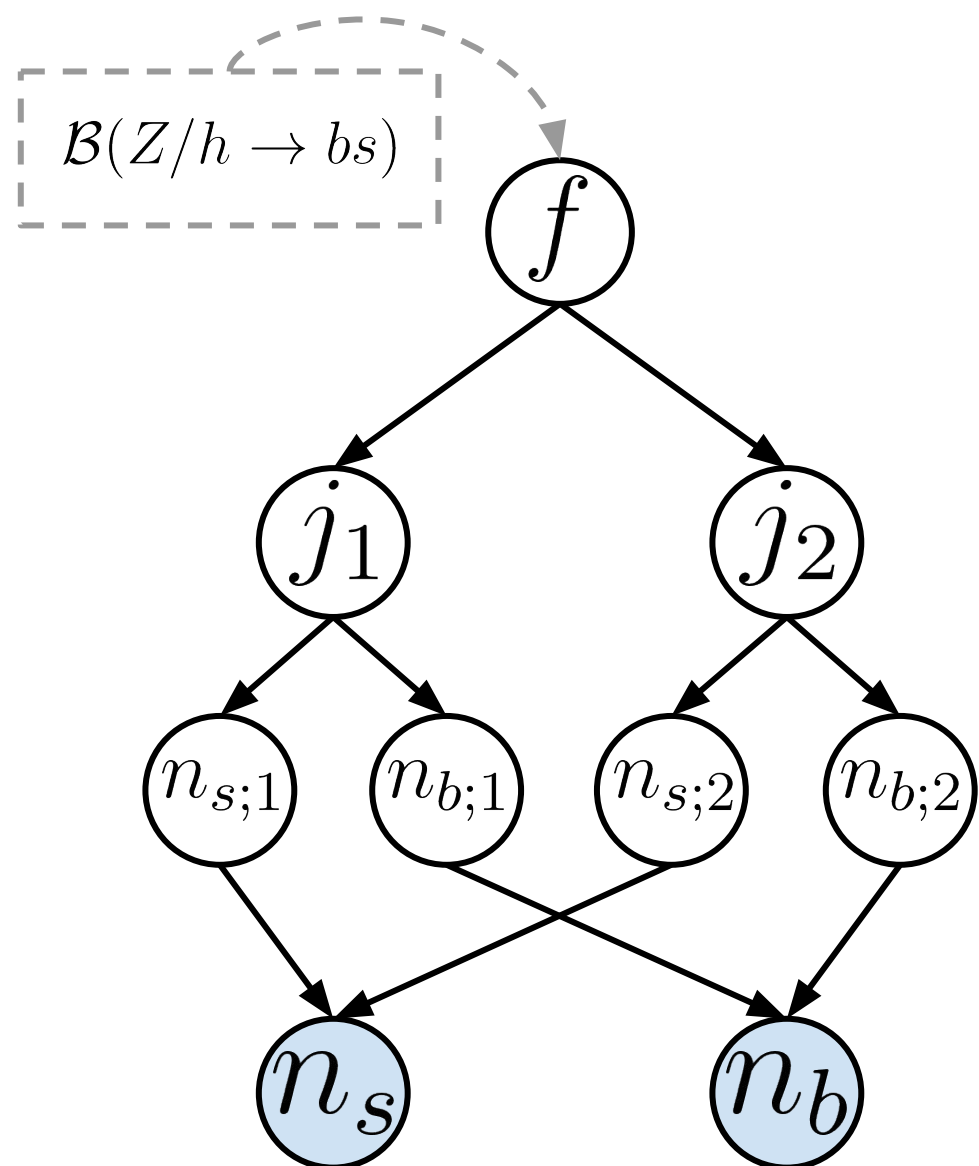
# **Backup slides**

# Probabilistic model

$$p(n_b, n_s | f, \nu) = \sum_{n_{b;1}=0}^{\min(n_b, 1)} \sum_{n_{s;1}=0}^{\min(n_s, 1 - n_{b;1})} p(n_{b;1} | j_1) p(n_{s;1} | j_1, n_{b;1}) p(n_{b;2} | j_2) p(n_{s;2} | j_2, n_{b;2})$$

$$p(n_{b;1} | j_1) = \text{Binom}(n_{b;1}, 1, \epsilon_1^b)$$

$$p(n_{s;1} | j_1, n_{b;1}) = \text{Binom}\left(n_{s;1}, 1 - n_{b;1}, \frac{\epsilon_1^s}{1 - \epsilon_1^b}\right)$$



Flavor conserving decays

$$p(n_b, n_s | f, \nu) = \text{Binom}(n_b, 2, \epsilon_1^b) \text{Binom}\left(n_s, 2 - n_b, \frac{\epsilon_1^s}{1 - \epsilon_1^b}\right)$$

Efficiencies are implicit function of the nuisance parameters

$$\nu = \{\mathcal{B}(h \rightarrow f), \mathcal{B}(Z \rightarrow f'), \epsilon_\beta^\alpha, N_{Z/h}, \mathcal{A}\}$$

# Likelihood

Poisson dist.  $\mathcal{P}(k|\lambda) = \frac{\lambda^k e^{-\lambda}}{k!}$

$$\mathcal{L}(\mu, \nu) = \mathcal{P}(N_{(n_b, n_s)} | \bar{N}_{(n_b, n_s)}(\mu, \nu)) p(\nu)$$

↓ Constrained to nominal values by other measurements

$$p(\nu) = \prod_i \mathcal{N}(\nu_{i,0}; \nu_i, \sigma_i)$$

## Profile likelihood ratio

Cowan, Cranmer, Gross, Vitells: 1007.1727

$$\lambda(\mu) = \frac{\mathcal{L}(\mu, \hat{\nu}(\mu))}{\mathcal{L}(\hat{\mu}, \hat{\nu})}$$

$\hat{\nu}(\mu), \hat{\mu}, \hat{\nu}$  are maximum likelihood estimates (MLE)

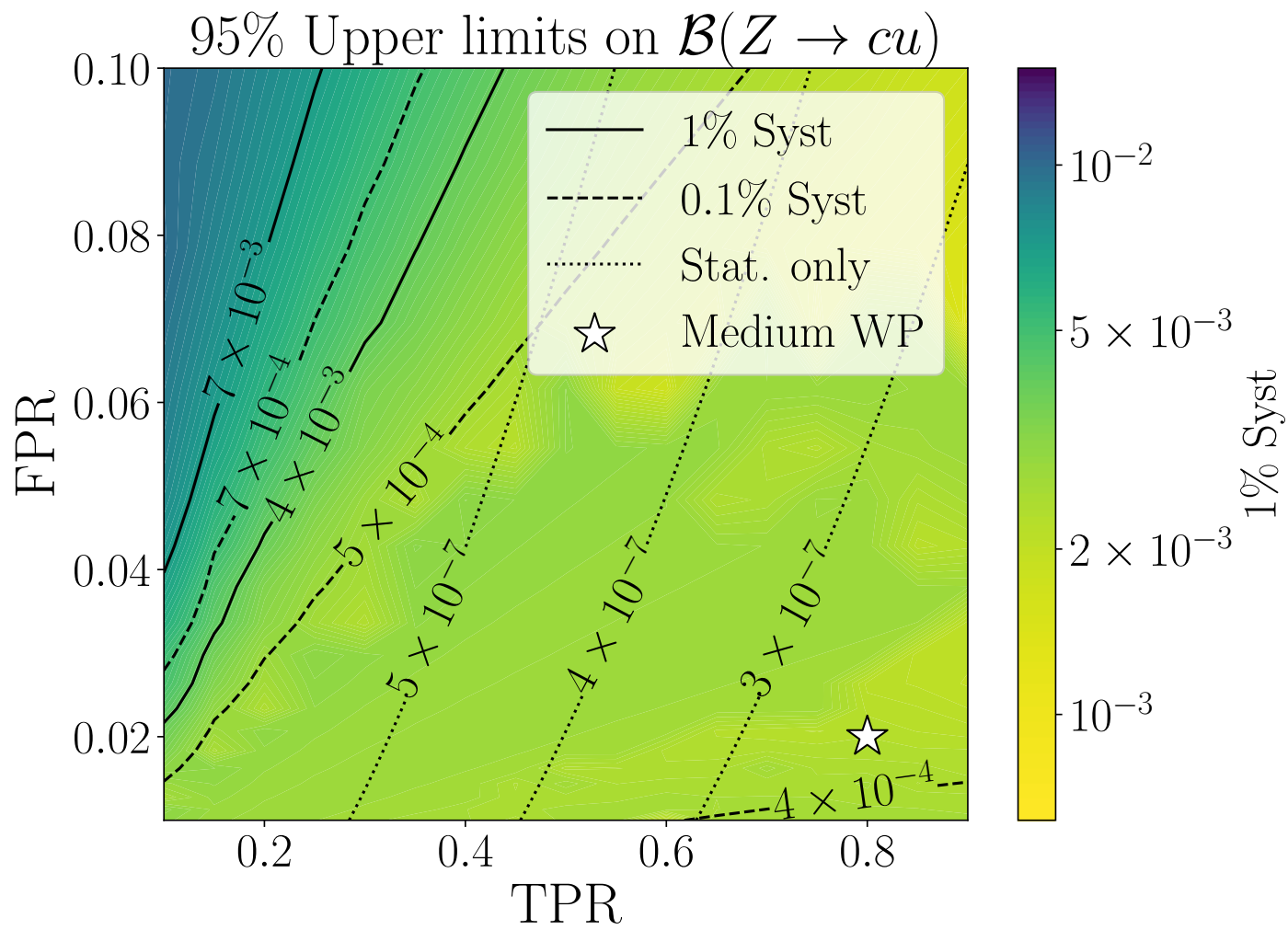
## Test statistics

$$t_\mu = -2 \text{Ln } \lambda(\mu)$$

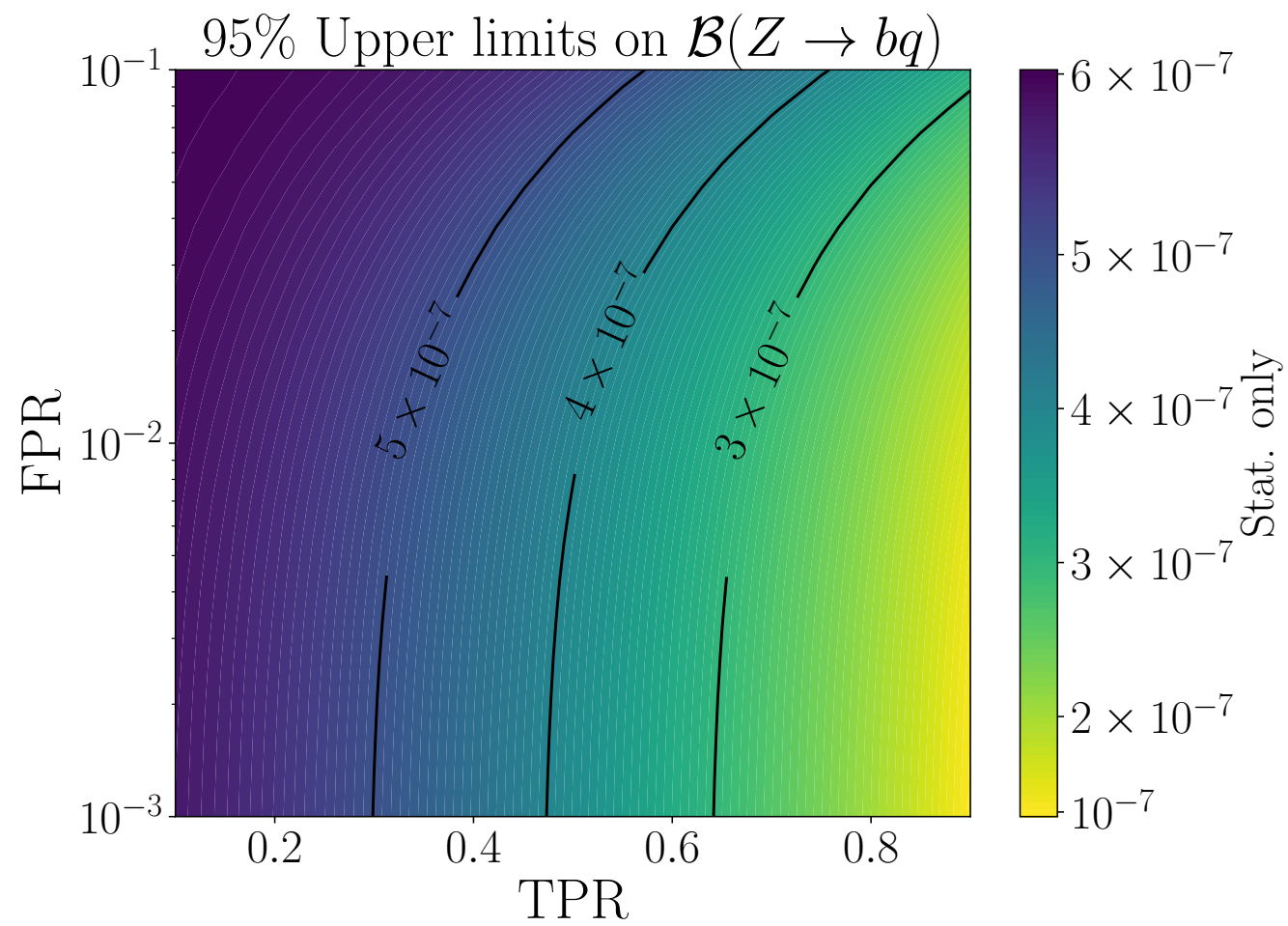
Confidence interval  $\mu_{\text{true}} = 1$ , solve for  $t_\mu = 1$  (68%)

Upper limits

$\mu_{\text{true}} = 0$ , solve for  $t_\mu = (\Phi^{-1}(1 - 0.05))^2$  (95%)



Similar backgrounds and tagger performances



# New Physics fits ( $Z$ )

$$\Delta B = \Delta S = 1$$

$$-\mathcal{H}_{\text{WET}} = \frac{4G_F}{\sqrt{2}} \frac{\alpha_{\text{em}}}{4\pi} V_{tb}^* V_{ts} \sum_{\ell} \left( C_9 \mathcal{O}_9 + C'_9 \mathcal{O}'_9 + C_{10} \mathcal{O}_{10} + C'_{10} \mathcal{O}'_{10} + C_{\nu} \mathcal{O}_{\nu} + C'_{\nu} \mathcal{O}'_{\nu} + \dots \right)$$

$$\mathcal{O}_9^{(\prime)} = (\bar{s}\gamma_{\mu}b_{L(R)}) (\bar{\ell}\gamma^{\mu}\ell)$$

$$\mathcal{O}_{10}^{(\prime)} = (\bar{s}\gamma_{\mu}b_{L(R)}) (\bar{\ell}\gamma^{\mu}\gamma_5\ell)$$

$$\mathcal{O}_{\nu}^{(\prime)} = (\bar{s}\gamma_{\mu}b_{L(R)}) (\bar{\nu}_{\ell}\gamma^{\mu}(1 - \gamma_5)\nu_{\ell})$$

$$\Delta F = 2$$

$$-\mathcal{H}_{\Delta F=2} = C_{VL} (\bar{s}\gamma_{\mu}b_L)^2 + C_{VR} (\bar{s}\gamma_{\mu}b_R)^2 + C_{VLR} (\bar{s}\gamma_{\mu}b_L) (\bar{s}\gamma_{\mu}b_R)$$

**Wilson coefficients**  $C_i = C_i^{\text{SM}} + \delta C_i$

$$\delta C_{9,\ell\ell}^{(\prime)} = \mathcal{N} g_{sb}^{L(R)} g_{Z\ell\ell,\text{vec}} \simeq 6.04 \times 10^3 g_{sb}^{L(R)}$$

$$\delta C_{10,\ell\ell}^{(\prime)} = \mathcal{N} g_{sb}^{L(R)} g_{Z\ell\ell,\text{ax}} \simeq -5.67 \times 10^4 g_{sb}^{L(R)}$$

$$\delta C_{\nu}^{(\prime)} = \mathcal{N} g_{sb}^{L(R)} g_{Z\nu\nu}$$

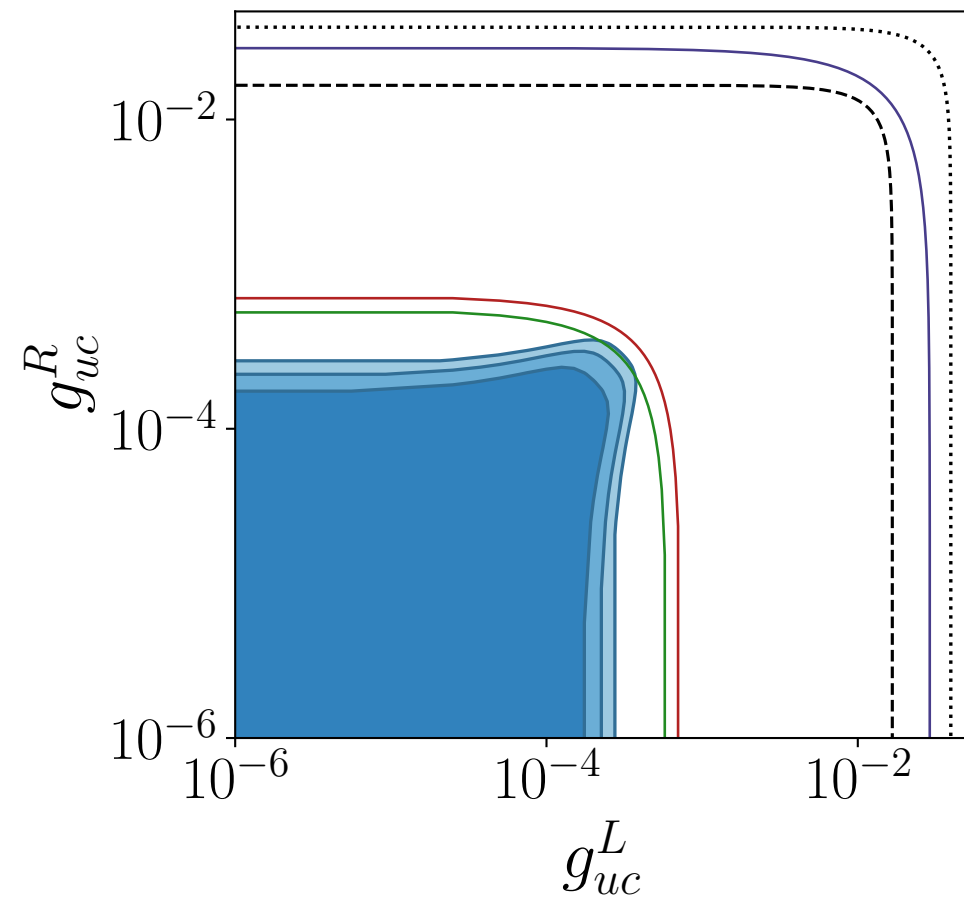
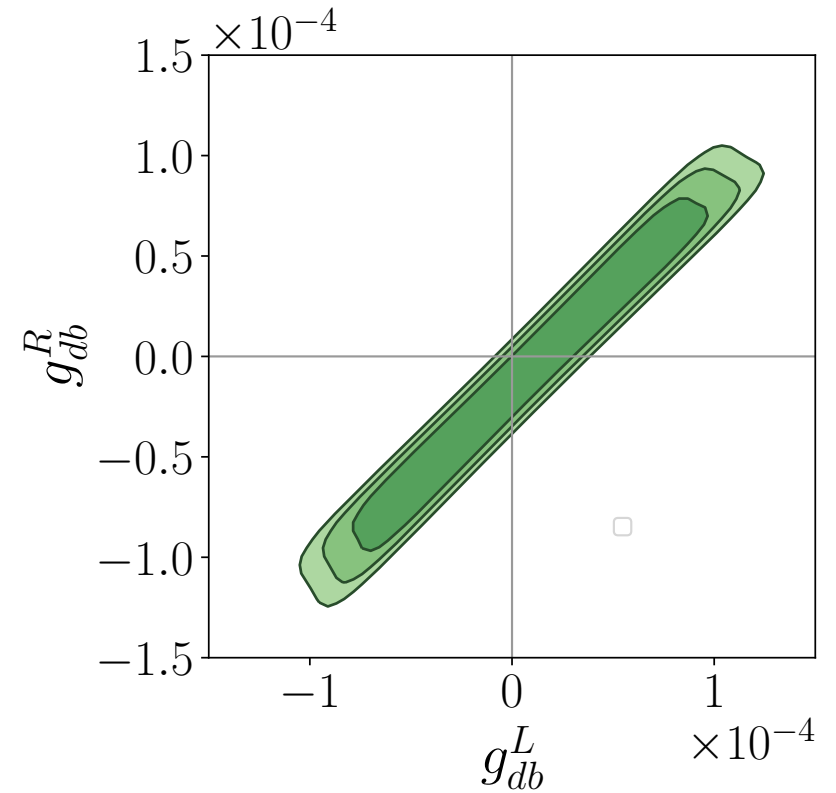
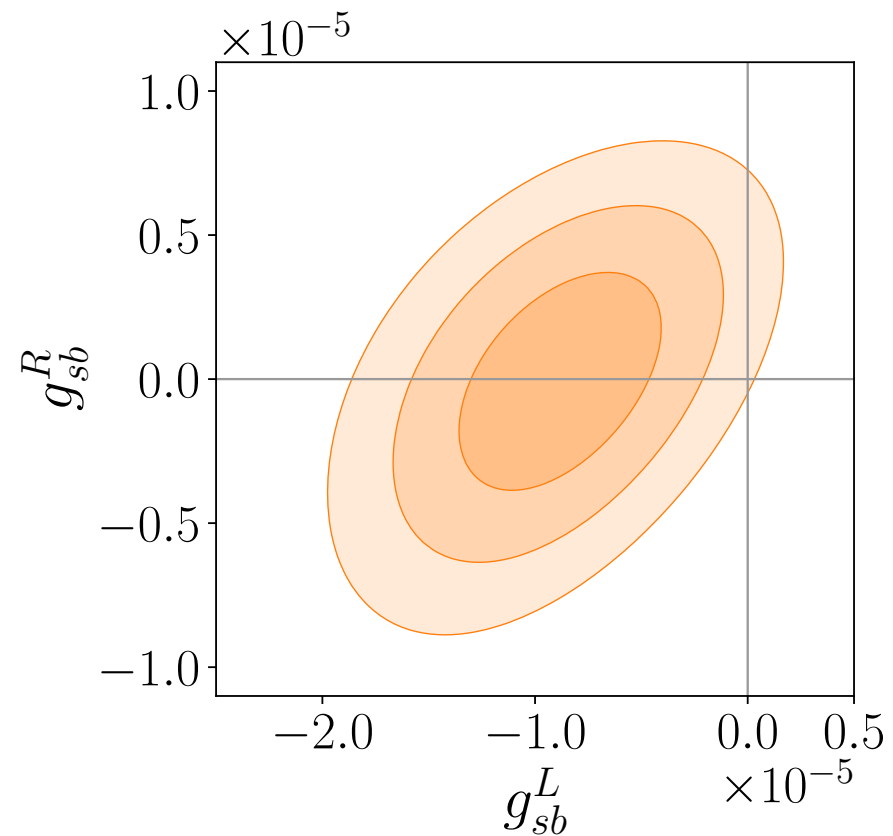
$$C_{VL} = \frac{(g_{sb}^L)^2}{2m_Z^2}$$

$$C_{VR} = \frac{(g_{sb}^R)^2}{2m_Z^2}$$

$$C_{VLR} = \frac{g_{sb}^L g_{sb}^R}{m_Z^2}$$

Lepton couplings are assumed to be SM

# New Physics fits (Z)



- $\mathcal{B}(Z \rightarrow cu) = 4.04 \times 10^{-4}$
- .....  $\mathcal{B}(Z \rightarrow cu) = 2.28 \times 10^{-3}$
- Combined  $D$  decays fit
- $\mathcal{B}(D^+ \rightarrow \pi^+ \mu^+ \mu^-)$ , full region
- $\mathcal{B}(D^+ \rightarrow \pi^+ \mu^+ \mu^-)$ , high  $q^2$
- $\mathcal{B}(D^0 \rightarrow \pi^0 \nu \bar{\nu})$

LHCb: 2212.11203, 1304.6365  
 Belle: 1003.2345  
 BESIII: 2112.14236  
 Bause, Golz, Hiller, Tayduganov: 1909.11108

# NP model: Vector-like Quarks (1)

Introduce  $SU_L(2)$  singlets  $(D_L, D_R)$  with  $Y = -1/3$

$$-\mathcal{L}_{\text{int}} \supset y_d^{ij} \bar{q}_L^i H d_R^j + y_u^{ij} \bar{q}_L^i \tilde{H} u_R^j + y_D^i \bar{q}_L^i H D_R + M_D \bar{D}_L D_R + \text{h.c.},$$



$$\mathcal{L}_{\text{VLQ}}^D \supset \frac{g}{2c_W} X_{ij}^d (\bar{d}^i \gamma^\mu P_L d^j) Z_\mu + X_{ij}^d \frac{m_j}{v} (\bar{d}^i P_R d^j) h + \text{h.c.},$$

$$g_{sb}^L = \frac{g}{2c_W} (X_{sb}^d + X_{bs}^{d*}), \quad g_{sb}^R = 0, \quad y_{sb} = X_{sb}^d m_b/v, \quad y_{bs} = X_{bs}^d m_s/v$$

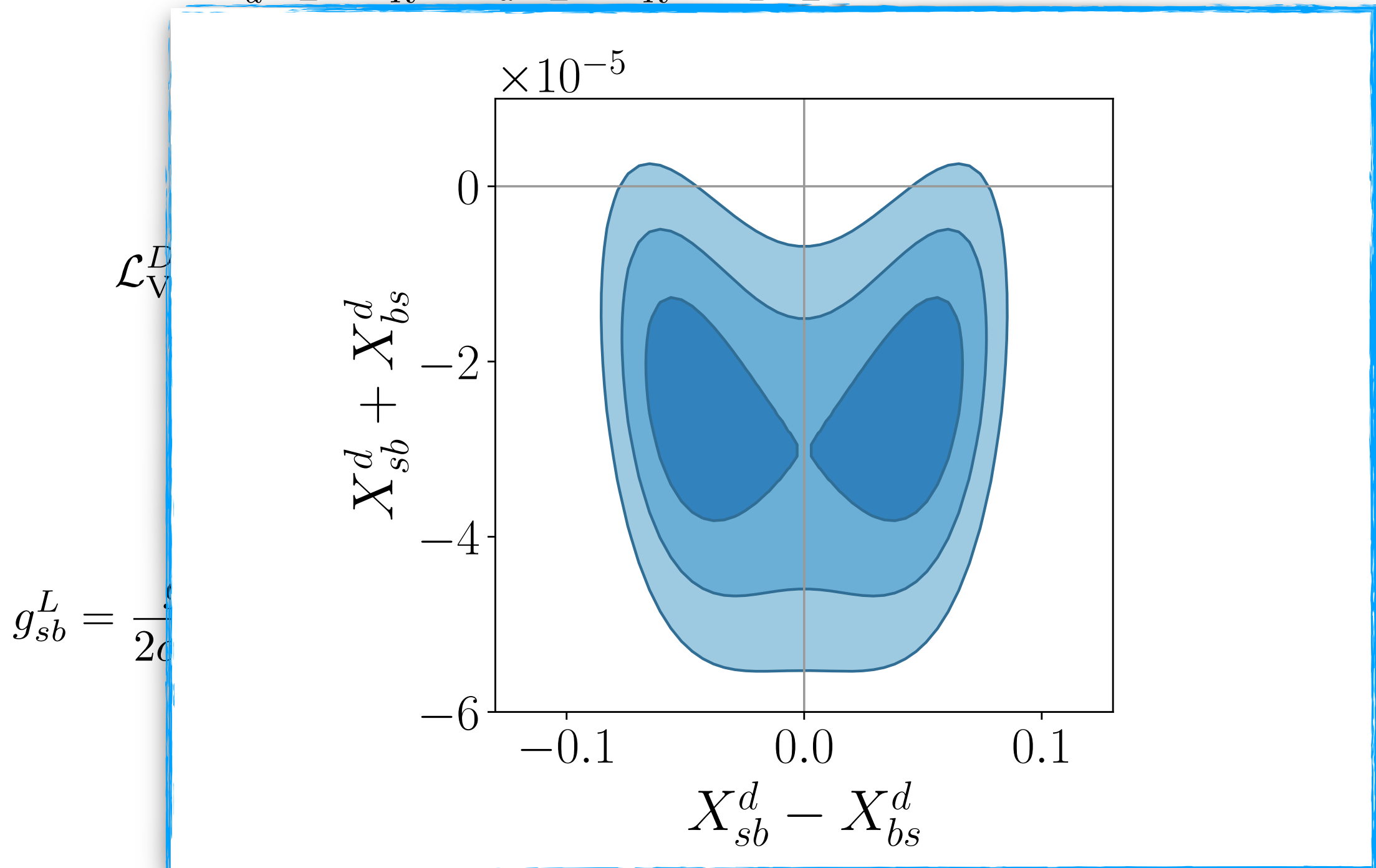
Both  $h$  and  $Z$  couplings generated



# NP model: Vector-like Quarks (1)

Introduce  $SU_L(2)$  singlets  $(D_L, D_R)$  with  $Y = -1/3$

$$-\mathcal{L}_{\text{int}} \supset y_d^{ij} \bar{q}_L^i H d_R^j + y_u^{ij} \bar{q}_L^i \tilde{H} u_R^j + y_D^i \bar{q}_L^i H D_R + M_D \bar{D}_L D_R + \text{h.c.},$$



# NP model: Vector-like Quarks (2)

Introduce  $SU_L(2)$  doublets  $(Q_L, Q_R)$  with  $Y = 1/6$

$$-\mathcal{L}_Q = y_d^{ij} \bar{q}_L^i H d_R^j + y_u^{ij} \bar{q}_L^i \tilde{H} u_R^j + y_D^i \bar{Q}_L H d_R^i + y_U^i \bar{Q}_L \tilde{H} u_R^i + M_Q \bar{Q}_L Q_R + \text{h.c.}$$



$$\mathcal{L}_{\text{VLQ}}^Q \supset \frac{g}{2c_W} X_{ij}^Q (\bar{d}^i \gamma^\mu P_R d^j) Z_\mu + X_{ij}^Q \frac{m_j}{v} (\bar{d}^i P_R d^j) h + \text{h.c.}$$

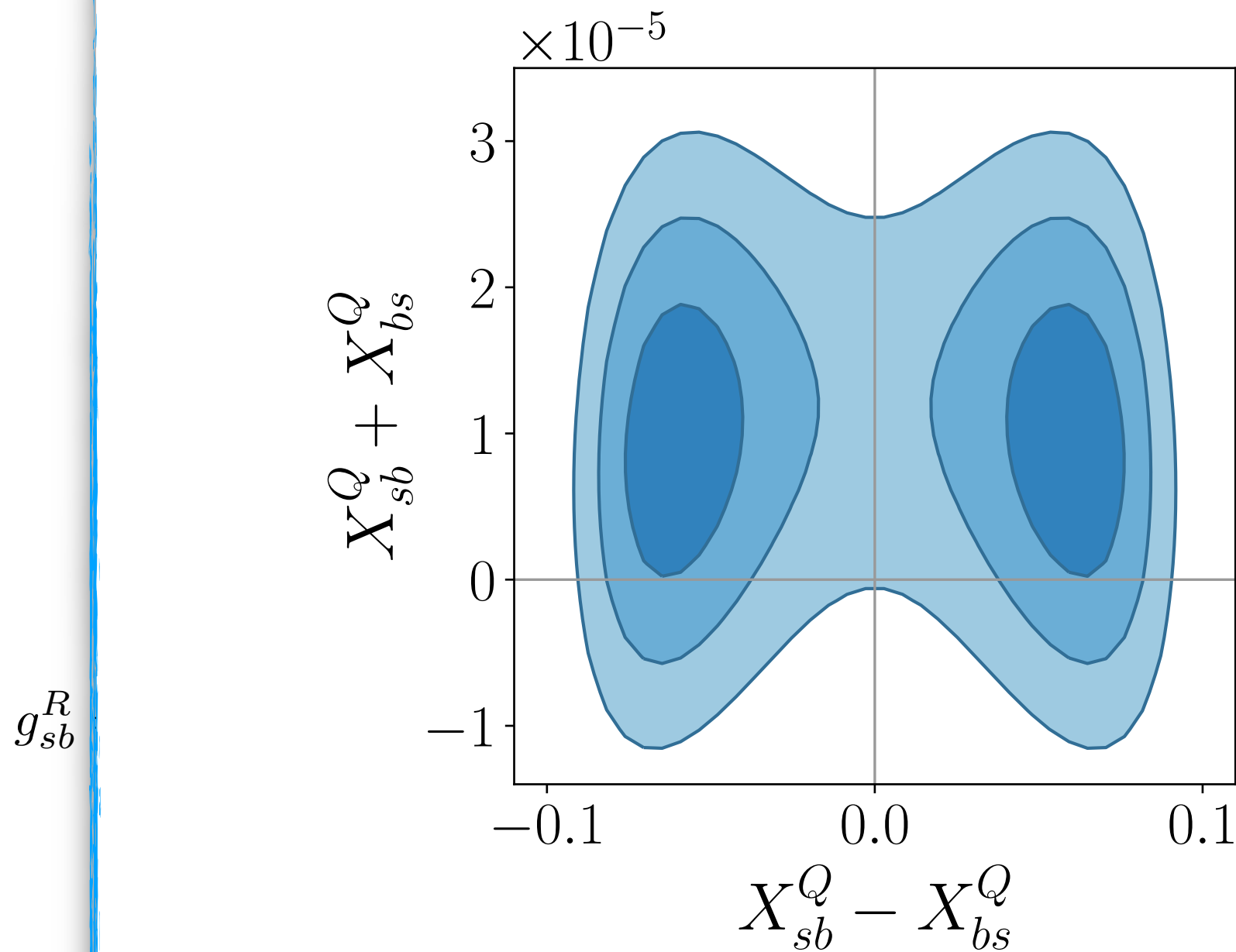
$$g_{sb}^R = \frac{g}{2c_W} (X_{sb}^Q + X_{bs}^{Q*}), \quad g_{sb}^L = 0, \quad y_{sb} = X_{sb}^Q m_b/v, \quad y_{bs} = X_{bs}^Q m_s/v$$

Both  $h$  and  $Z$  couplings generated

# NP model: Vector-like Quarks (2)

Introduce  $SU_L(2)$  doublets  $(Q_L, Q_R)$  with  $Y = 1/6$

$$-\mathcal{L}_Q = \alpha^{ij} \bar{q}^i H d^j + \alpha^{ij} \bar{q}^i \tilde{H} u^j + \alpha^i \bar{Q}_L H d^i + \alpha^i \bar{Q}_L \tilde{H} u^i + M_Q \bar{Q}_L Q_R + \text{h.c.}$$



$g_{sb}^R$

# NP model: Two Higgs Doublet Model

Type III: no discrete symmetry preventing FCNCs

$$\mathcal{L}_{2\text{HDM}} \supset -\frac{\sqrt{2}m_i}{v}\delta_{ij}\bar{q}_L^i H_1 d_R^j - \sqrt{2}Y_{ij}^d \bar{q}_L^i H_2 d_R^j - \frac{\sqrt{2}m_i}{v}\delta_{ij}\bar{q}_L^i \tilde{H}_1 u_R^j - \sqrt{2}Y_{ij}^u \bar{q}_L^i \tilde{H}_2 u_R^j$$

$$H_1 = \begin{pmatrix} G^+ \\ \frac{1}{\sqrt{2}}(v + h_1 + iG^0) \end{pmatrix}$$

$$H_2 = \begin{pmatrix} H^+ \\ \frac{1}{\sqrt{2}}(h_2 + iA) \end{pmatrix}$$

$$\begin{pmatrix} h_1 \\ h_2 \end{pmatrix} = \begin{pmatrix} c_\alpha & s_\alpha \\ -s_\alpha & c_\alpha \end{pmatrix} \begin{pmatrix} h \\ H \end{pmatrix}$$

$$C_2 = -\frac{(Y_{bs}^{d*})^2}{2} \left( \frac{s_\alpha^2}{m_h^2} + \frac{c_\alpha^2}{m_H^2} - \frac{1}{m_A^2} \right),$$

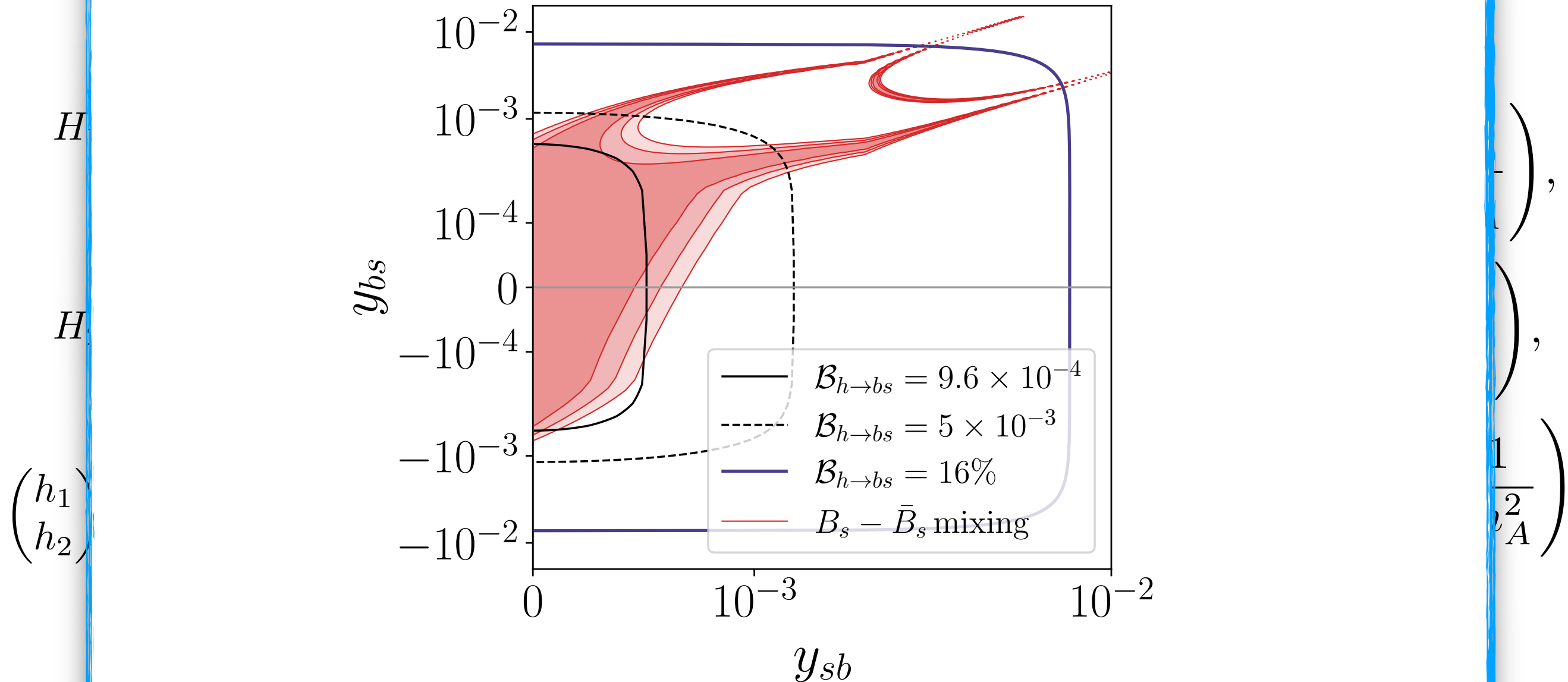
$$C'_2 = -\frac{(Y_{sb}^d)^2}{2} \left( \frac{s_\alpha^2}{m_h^2} + \frac{c_\alpha^2}{m_H^2} - \frac{1}{m_A^2} \right),$$

$$C_4 = -(Y_{bs}^{d*} Y_{sb}^d) \left( \frac{s_\alpha^2}{m_h^2} + \frac{c_\alpha^2}{m_H^2} + \frac{1}{m_A^2} \right)$$

# NP model: Two Higgs Doublet Model

Type III: no discrete symmetry preventing FCNCs

$$m_{H,A} \rightarrow \infty \quad y_{ij} = Y_{ij}^q \sin \alpha$$

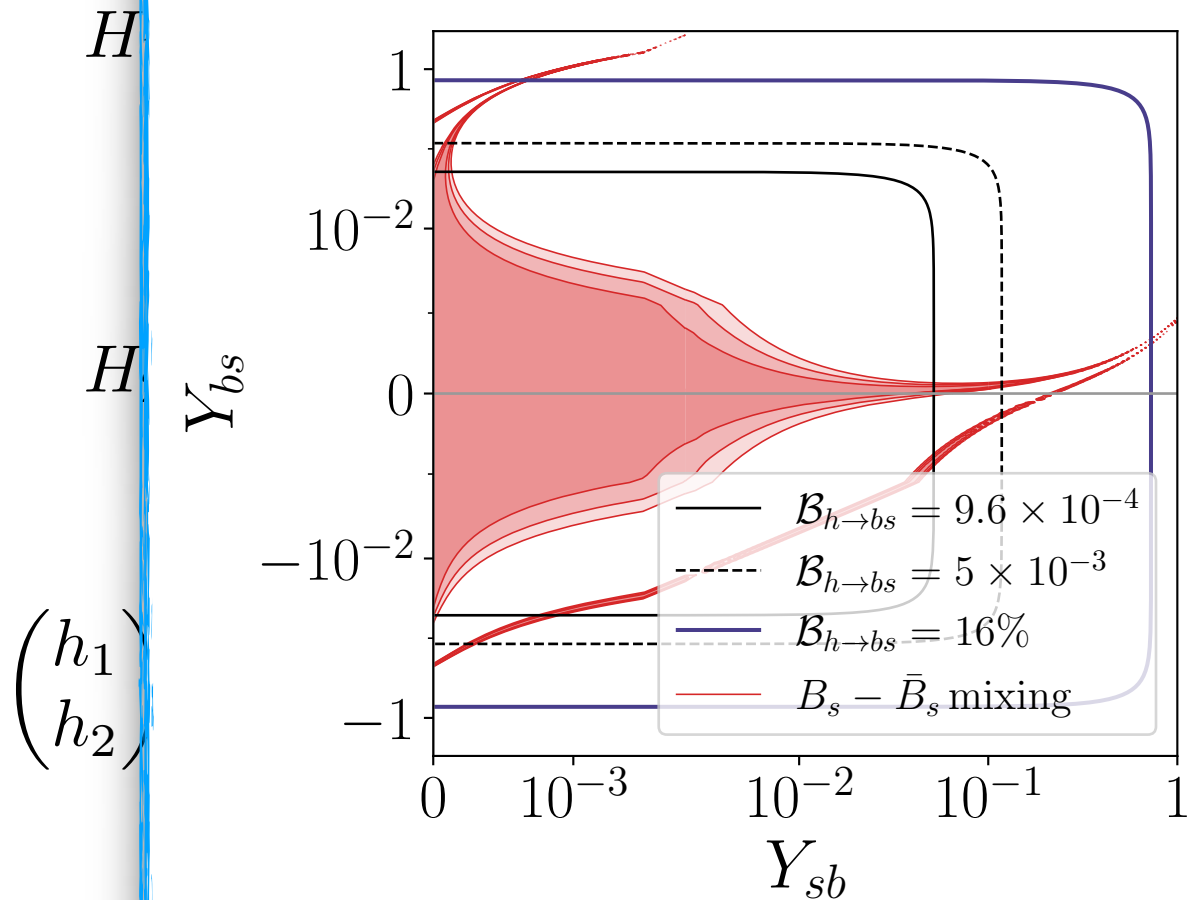


# NP model: Two Higgs Doublet Model

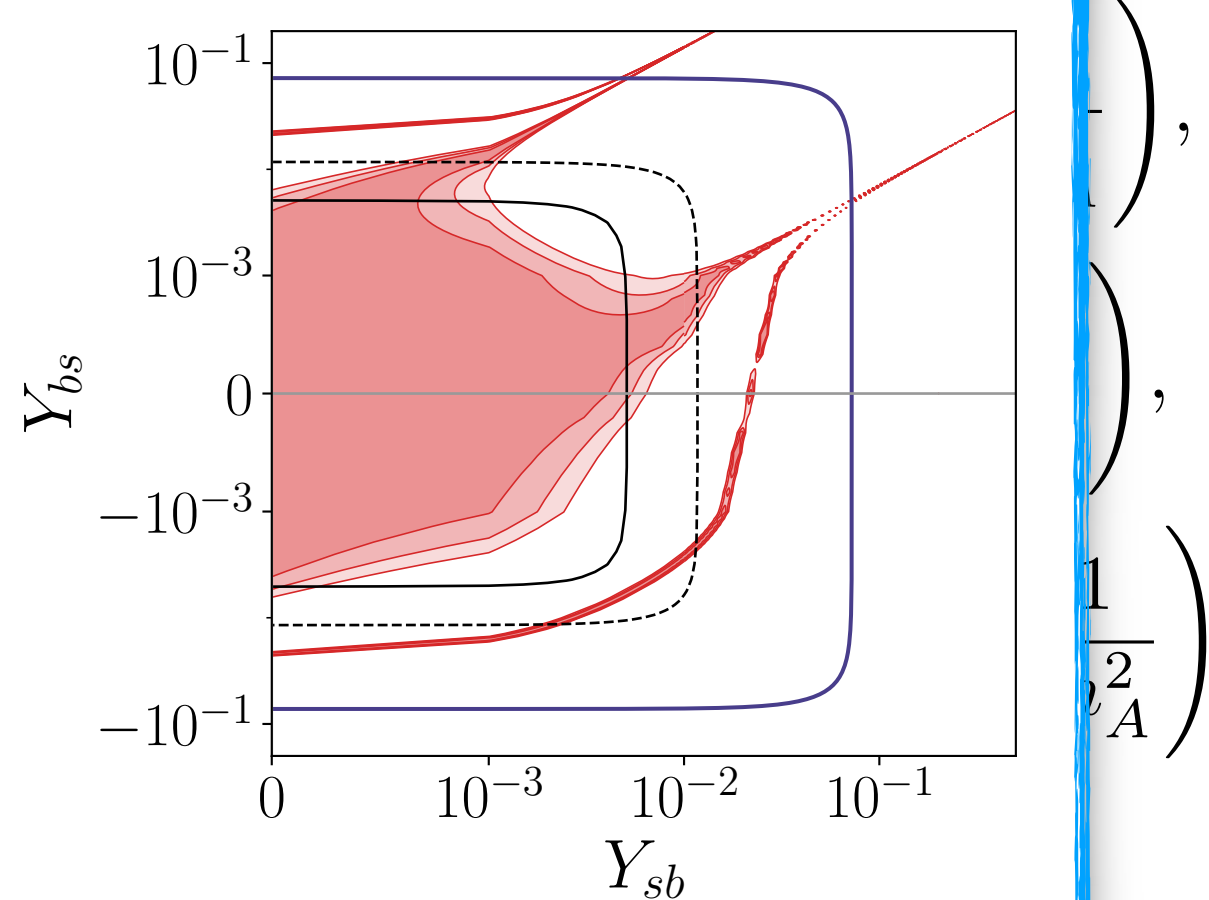
Type III: no discrete symmetry preventing FCNCs

$$m_{H,A} = 1 \text{ TeV}$$

$\sin \alpha = 0.01$



$\sin \alpha = 0.1$



# NP model: Two Higgs Doublet Model

Type III: no discrete symmetry preventing FCNCs

$$m_{H,A} = 1 \text{ TeV}$$

$\sin \alpha = 0.01$

$\sin \alpha = 0.1$

