Time-dependent Measurements at LHCb & Belle(II)

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Outline

- Recap of CKM and CP violation
- Flavour tagging at LHCb & Belle II
- $\sin 2\beta$ measurements
- ϕ_s measurements
- $B^0_{(s)} \rightarrow h^+ h^- \& \tau_L$
- Prospects & summary



* Due to time limits, focusing on B decays only

CKM matrix

$$V_{CKM} = \begin{pmatrix} |V_{ud}| & |V_{us}| & |V_{ub}|e^{-i\gamma} \\ -|V_{cd}| & |V_{cs}| & |V_{cb}| \\ |V_{td}|e^{-i\beta} & -|V_{ts}|e^{i\beta_s} & |V_{tb}| \end{pmatrix} + \mathcal{O}(\lambda^5) \sim \begin{pmatrix} 1 & 0.2 & 0.004 \\ 0.2 & 1 & 0.04 \\ 0.008 & 0.04 & 1 \end{pmatrix}$$

1.5

excluded area has CL > 0.95

• Key test of the SM: Verify unitarity of CKM matrix

- Magnitudes: branching fractions or mixing frequencies
- Phases: CP violation measurement
- Sensitive probe for new physics



Neutral meson oscillation

Neutral mesons can oscillate through box diagrams



Mixing and decay can be described by Schrödinger-like equation $i\frac{d}{dt}\left(\frac{B}{B}\right) = \tilde{\mathbf{H}}\left(\frac{B}{B}\right) = \begin{bmatrix} m - \frac{i}{2}\Gamma & m_{12} - \frac{i}{2}\Gamma_{12} \\ m_{12}^* - \frac{i}{2}\Gamma_{12}^* & m - \frac{i}{2}\Gamma \end{bmatrix} \begin{pmatrix} B \\ \overline{B} \end{pmatrix}$



 $\Delta m_s = (17.7656 \pm 0.0057) \ ps^{-1}$

• Decay rate of initial B or \bar{B}

$$\begin{split} |\langle f|H|B\rangle|^2 &= \frac{1}{2}e^{-\Gamma t}|A_f|^2 \Big\{ \mathcal{D}\cosh\left(\frac{\Delta\Gamma}{2}t\right) + \mathcal{A}_{\Delta\Gamma}\sinh\left(\frac{\Delta\Gamma}{2}t\right) \\ &\pm \mathcal{C}\cos(\Delta mt) \mp S\sin(\Delta mt) \Big\} \\ &\text{direct } \mathcal{A}_{CP} \qquad CP \text{ in mixing} \end{split}$$

• Mass difference $\Delta m_{(s)} = M_H - M_L = 2 |M_{12}| \rightarrow \text{oscillation frequency}!$

• Decay-width difference $\Delta \Gamma_{(s)} = \Gamma_L - \Gamma_H = 2 |\Gamma_{12}| \cos \phi_{12}$

Opportunities for new physics



• New physics (NP) short-distance contributions can influence mixing $m_{12}^q = m_{12}^{SM,q} \cdot \Delta_q^{NP}$ [PRD 86(2012)033008]

 Through B mixing, NP energy scales of up to 20 TeV for tree-level NP or 2 TeV for NP in loops can be probed
 [PRD 89(2014)033016]



Time-dependent CP asymmetry

$$A_{CP}(t) = \frac{\Gamma(\bar{B}^0_{(s)} \to f) - \Gamma(B^0_{(s)} \to f)}{\Gamma(\bar{B}^0_{(s)} \to f) + \Gamma(B^0_{(s)} \to f)} \propto C_f \cos(\Delta m_{(s)}t) + \eta_f S_f \sin(\Delta m_{(s)}t)$$

• Tree diagram dominant: NP in mixing $S_f \approx \frac{\sin 2\beta_{(s)}}{\sin 2\beta_{(s)}}$

- $\sin 2\beta: B^0 \to \psi K_S^0 / K_L^0: CP-odd/even component$
- $\phi_s \approx \sin 2\beta_s : B_s^0 \to J/\psi\phi$: a mixture of CP-even (L = 0,2) & CP-odd (L = 1)
- Penguin dominant: NP contributions in mixing & penguin diagrams
 - $\sin 2\beta \colon B^0 \to \phi K^0_S, \ K^0_S K^0_S K^0_S, \ K^0_S \pi^0$
 - $\phi_s^{s\bar{s}s}: B_s^0 \to \phi\phi, K^{*0}K^{*0}$
 - Experimentally

 $A_{CP}(t) \propto e^{-\frac{1}{2}\Delta m_s^2 \sigma_t^2} \cdot (1 - 2\omega) \cdot (C_f \cos(\Delta m_{(s)}t) + \eta_f S_f \sin(\Delta m_{(s)}t))$

- Flavour tagging of $B_{(s)}^0$: probability of wrong tag ω
- Excellent decay-time resolution (vertex resolution)
- CP eigenvalue of the final state η_f



LHCb & Belle(II) detectors

LHCD

• Daughters of b & c hadron decays: $p_T \sim \mathcal{O}(1 \text{ GeV}/c)$, flight distance L~1mm



pp collision: 3 fb⁻¹ (7,8 TeV) + 6 fb⁻¹ (13 TeV)
 σ(bb̄)(7TeV) = 72.0 ± 0.3 ± 6.8 μb,
 σ(bb̄)(13TeV) = 144 ± 1 ± 21 μb

• Asymmetric collider: e^- of 7 GeV with e^+ of 4 GeV KL and muon detector Resistive Plate Counter (barrel outer layers) Scintillator + WLSF + MPPC (end-caps, inner 2 barrel layers)



• e^+e^- collision: 362 fb⁻¹ at $\Upsilon(4S)$ • $N(B\bar{B}) = 387 \times 10^6$

Flavour tagging



- Same-side (SS) tagging: Use charge of K/ π produced in the fragmentation
- Opposite-side (OS) tagging: charge of
 leptons or hadrons from the other *b* hadrons
- Tagging power = $(4 \sim 6)\%$ (mode-dependent) = $\varepsilon_{tag} \cdot (1 - \omega)^2$ (ω is mistag rate)

Coherent production of $B^0 \overline{B}^0$





 Category-FT: Use inputs of kinematic, track hit and PID from the remaining tracks apart from the signal

• Tagging efficiency = $(30\pm1.3)\%$

• wrong tagging probability
$$\omega = \frac{1}{2}$$

Δm_d and τ_{B^0} in $B^0 \to D^{(*)-}\pi^+$



- 190 fb⁻¹ $e^+e^- \rightarrow \Upsilon(4S) \rightarrow B\bar{B}: N(B\bar{B}) = 200 \times 10^6$
- Entangled quantum states: knowledge of the B^0 tag flavour determines the B_{CP} flavour at that time $\Delta t \equiv t_{CP} t_{tag}$
- Benchmark for time-dependent measurements
- Fit to background-subtracted Δt distribution to extract Δm_d and au_{B^0}





 $\sin 2\beta$ in $B^0 \to J/\psi K_S^0$



- 190 fb⁻¹ $e^+e^- \to \Upsilon(4S) \to B\bar{B}: N(B\bar{B}) = 200 \times 10^6$
- Entangled quantum states: Fit to background-subtracted $\Delta t \equiv t_{CP} t_{tag}$

$$P(\Delta t, q) = \frac{e^{-|\Delta t|/\tau_{B^0}}}{2\tau_{B^0}} \{1 + q[S_{CP}\sin(\Delta m_d\Delta t) + A_{CP}\cos(\Delta m_d\Delta t)]\}$$



 $S_{CP} = 0.720 \pm 0.062 \text{(stat)} \pm 0.016 \text{(syst)}$ $A_{CP} = 0.094 \pm 0.044 \text{(stat)} + 0.042 \text{(syst)}$ - 0.017 (syst)

(Statistical uncertainty dominant!)

Consistent with Belle results:

 $S_{CP} = 0.667 \pm 0.023 (\text{stat}) \pm 0.012 (\text{syst})$

 $A_{CP} = 0.006 \pm 0.016 (\text{stat}) \pm 0.012 (\text{syst})$

Agree with the World average:

 $A_{CP} = 0.699 \pm 0.017, \ S_{CP} = 0.005 \pm 0.015$

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$\sin 2\beta$ in $B^0 \to \psi K_S^0$

LHCb-PAPER-2023-013 In preparation



• Three decay modes in $B^0 \to \psi K_S^0$

Simultaneous fits to the decay time of B^0



 $egin{aligned} S^{ ext{Run 2}}_{\psi K^0_{ ext{S}}} &= 0.716 \pm 0.013 \, (ext{stat}) \pm 0.008 \, (ext{syst}) \ C^{ ext{Run 2}}_{\psi K^0_{ ext{S}}} &= 0.012 \pm 0.012 \, (ext{stat}) \pm 0.003 \, (ext{syst}) \end{aligned}$

 The most precise measurement in single measurement to date

$$B^{0} \to J/\psi(\mu^{+}\mu^{-})K_{s}^{0}(\to \pi^{+}\pi^{-}) \\ B^{0} \to \psi(2S)(\mu^{+}\mu^{-})K_{s}^{0}(\to \pi^{+}\pi^{-}) \\ B^{0} \to J/\psi(e^{+}e^{-})K_{s}^{0}(\to \pi^{+}\pi^{-})$$



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$\sin 2\beta$ combinations



*Belle II results is not included, which should not affect the current WA significantly

- Consistent with other measurements, still statistical uncertainty limited
- LHCb results dominate the latest World Average



- Good agreement with the WA, more data needed!
- Belle II is in the unique position to measurements involving neutral particles



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 $\phi_{\rm s}$ in $B_{\rm s}^0 \to J/\psi KK$

arXiv: 2308.01468 submitted to PRL





- The most precise measurement in single channel to date
- Compatible with prediction assuming the SM $-\beta_s^{SM} = -0.0368^{+0.0009}_{-0.0006}$ rad
- No evidence of CP violation
- Consistent and combined with all LHCb measurements $(B_s^0 \rightarrow J/\psi hh, D_s^+ D_s^-, \psi(2S)KK) \quad \phi_s = -0.031 \pm 0.018 \text{ rad}$

ϕ_s combinations in $b \rightarrow c\bar{c}s$ transition

 Previous World Average:
 New World Average: (preliminary)

 $\phi_s^{c\bar{c}s} = -0.049 \pm 0.019$ rad
 $\phi_s^{c\bar{c}s} = -0.050 \pm 0.016$ rad (16%)

 $\phi_s^{J/\psi KK} = -0.070 \pm 0.022$ rad
 $\phi_s^{c\bar{c}s} = -0.039 \pm 0.017$ rad (23%)

Consistent with the Global fits with SM assumption

 $\phi_s^{\text{CKMFitter}} \approx -2\beta_s = (-0.0368^{+0.0006}_{-0.0009}) \text{ rad} \quad \phi_s^{\text{UTFitter}} = (-0.0370 \pm 0.0010) \text{ rad}$



ϕ_s in $b \rightarrow s\bar{s}s$ transition

- Penguin dominant decay $B^0_s
 ightarrow \phi \phi$
- Similar time-dependent flavour-tagged angular analysis as $B_s^0 \rightarrow J/\psi KK$

 $\phi_s^{s\bar{s}s} = -0.042 \pm 0.075 \pm 0.009$ rad, $|\lambda| = 1.004 \pm \pm 0.030 \pm 0.009$

- The most precise measurement in any penguin dominated B decays
- No polarisation dependence is observed



_HCb-PAPER-2023-001

accepted by PRL

CP asymmetry in $B_{(s)}^0 \rightarrow h^+h^-$

JHEP03(2021)075

- Simultaneous fit to the invariant mass, $B_{(s)}^0$ decay time and tagging decision for $B^0 \to \pi^+\pi^-$, $B_s^0 \to K^+K^-$, $B_{(s)}^0 \to K\pi$, providing inputs to α , γ , $\sin 2\beta_s$
- The first observation of time-dependent *CP* violation in B_s^0 decay



Effective lifetime measurements in $B_s^0 \rightarrow J/\psi \eta$

- *CP*-even decay $B_s^0 \to J/\psi(\mu^+\mu^-)\eta(\gamma\gamma)$ allows to determine $\tau_L = 1/\Gamma_L$
- Simultaneous fit to invariant mass and decay time





Better reconstruction of η and $J/\psi(e^+e^-)$ at CEPC? $+ B_s^0 \rightarrow J/\psi \eta'(\pi^0)$

EPJC83 (2023) 629

Looking at future

see Lingfeng Li's talk

Particle	Belle II	LHCb (300 fb^{-1})	CEPC $(4 \times \text{Tera-}Z)$
B^0, \bar{B}^0	$5.4 \times 10^{10} (50 \text{ ab}^{-1} \text{ on } \Upsilon(4S))$	$3 imes 10^{13}$	4.8×10^{11}
B^{\pm}	$5.7 \times 10^{10} (50 \text{ ab}^{-1} \text{ on } \Upsilon(4S))$	3×10^{13}	4.8×10^{11}
B_s^0, \bar{B}_s^0	$6.0 \times 10^8 \text{ (5 ab}^{-1} \text{ on } \Upsilon(5S))$	1×10^{13}	1.2×10^{11}
B_c^{\pm}	-	1×10^{11}	7.2×10^8
$\Lambda_b^0, ar{\Lambda}_b^0$	-	2×10^{13}	1×10^{11}

see Mingrui Zhao's talk

	Belle II	LHCb	CEPC
tagging power	(30~35)%	(4~6)%	20 %
time resolution		43 fs	4.7 fs
e/neutral particles	***	*	***

- Belle II, LHCb & CEPC compensate each other
- CEPC & Belle II have advantages in decays with neutral particles \rightarrow See <u>Yuexin Wang's talk</u> for α measurement with $B^0 \rightarrow \pi^0 \pi^0$

Looking at future for $\sin 2\beta$

• Belle II good at $J/\psi \rightarrow e^+e^-$, K_L^0 , π^0 reconstruction than LHCb

Could CEPC make great contributions for these with η' and π^0 ?



Looking at future for ϕ_s

- B_s^0 production at Belle II is limited
- Significant contribution from CEPC possible!



Control of penguin contribution

- $\sigma(\phi_s) \sim 0.016$ comparable with the estimation of $\Delta \phi_s^{penguin} \sim 1^\circ \approx 0.017$, better control of penguin effect necessary
- Combined analysis of penguin contributions in ϕ_s and ϕ_d (sin 2 β), using SU(3) flavor symmetry



Could be good opportunity for CEPC?

Summary

- LHCb & Belle II are leading the efforts in the time-dependent measurements of CP violation
- ✓ Most of the measurements are / will be statistical limited
- ✓ CEPC & Belle II have advantages in measurements with neutral particles, e.g. $B^0 \rightarrow \pi^0 \pi^0$, $B^0 \rightarrow J/\psi \pi^0$ etc
- ✓ With higher flavor tagging & better time resolution than LHCb, CEPC could definitely make significant contribution to such time-dependent measurements
- Looking forward to further test of the SM and search for new physics



Thanks for your attention!

Back up slides

Fit pdf at Belle II

arXiv:2302.12898

Fit to Δt distribution in 7 bins of tag quality r:

$$P_{CP}(\Delta t, q) = \frac{e^{-|\Delta t|/\tau_{B^0}}}{2\tau_{B^0}} \{ 1 - q\Delta w + q\mu(1 - 2w) \text{ flavor tagging} \\ + [q(1 - 2w) + \mu(1 - q\Delta w)] [S_{CP}\sin(\Delta m_d\Delta t) + A_{CP}\cos(\Delta m_d\Delta t)] \}$$

convolved by decay-time resolution

$$\begin{aligned} \mathcal{R}(\mathrm{d}\Delta\tau;\sigma_{\Delta t}) &= f_{\mathrm{core}}G(\mathrm{d}\Delta\tau;m_{\mathrm{core}}\sigma_{\Delta t},s_{\mathrm{core}}\sigma_{\Delta t}) \\ &+ f_{\mathrm{tail}}\mathcal{R}_{\mathrm{tail}}(\mathrm{d}\Delta\tau;m_{\mathrm{tail}}\sigma_{\Delta t},s_{\mathrm{tail}}\sigma_{\Delta t},c/\sigma_{\Delta t},f_{>},f_{<}) \\ &+ f_{\mathrm{OL}}G(\mathrm{d}\Delta\tau;0,\sigma_{\mathrm{OL}}), \end{aligned}$$

Flavor tagging calibrated with $D^0 \rightarrow D^{(*)-}\pi^+$:

$$P_{\text{flav}}(\Delta t, q, q_{\pi}) = \frac{e^{-|\Delta t|/\tau_{B^{0}}}}{4\tau_{B^{0}}} \{1 - q\Delta w + q\mu(1 - 2w) - q_{\pi}[q(1 - 2w) + \mu(1 - q\Delta w)]\cos(\Delta m_{d}\Delta t)\}$$

Systematic uncertainties



TABLE II. Summary of the individual sources of uncertainties

Dominant contribution due to samples size, could be reduced with more data!

Source	$\sigma(S_{CP})$	$\sigma(A_{CP})$
Statistical	0.0622	0.0439
Calibration with $B^0 \to D^{(*)-}\pi^+ {\rm decays}$		
$B^0 \to D^{(*)-} \pi^+$ sample size	0.0111	0.0093
Signal charge-asymmetry	0.0027	0.0126
$w_6^+ = 0$ limit	0.0014	0.0001
Fit model		
Analysis bias	0.0080	0.0020
Fixed resolution parameters	0.0039	0.0008
$\sigma_{\Delta t}$ binning	0.0050	0.0051
$ au_{B^0},\Delta m_d$	0.0007	0.0002
Δt measurement		
Alignment	0.0020	0.0042
Beam spot	0.0024	0.0020
Momentum scale	0.0005	0.0013
$B^0 \to J/\psi K_S^0 \ \Delta E$ background shape	0.0037	0.0015
Multiple candidates	0.0005	0.0008
CP violation in B_{tag}^0 decays	0.0020	$+0.0380 \\ -0.0000$
Total systematic	0.0163	$+0.0418 \\ -0.0174$

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$\sin 2\beta$ in $B^0 \to J/\psi K_S^0$

PRL108(2012)171802

Asymmetry Events / 0.5 ps	$ \begin{array}{c} 00\\ 00\\ 00\\ 00\\ 00\\ 50\\ 00\\ 50\\ 00\\ 50\\ 0\\ 0\\ 0\\ 0\\ 0\\ 0\\ 0\\ 0\\ 0\\ 0\\ 0\\ 0\\ 0$	$ \begin{array}{c} 250 \\ 200 \\ 150 \\ 100 \\ 50 \\ 0.6 \\ 0.4 \\ 0.2 \\ 0.4 \\ 0.2 \\ 0.4 \\ 0.6 \\ 0.4 \\ 0.2 \\ 0.4 \\ 0.6 \\ 0.4 \\ 0.2 \\ 0.4 \\ 0.6 \\ 0.4 \\ 0.2 \\ 0.4 \\ 0.6 \\ 0.4 \\ 0.2 \\ 0.4 \\ 0.6 \\ 0.4 \\ 0.2 \\ 0.4 \\ 0.6 \\ 0.4 \\ 0.2 \\ 0.4 \\ 0.6 \\ 0.4 \\ 0.2 \\ 0.4 \\ 0.6 \\ 0.4 \\ 0.6 \\ 0.4 \\ 0.2 \\ 0.4 \\ 0.6 \\ 0.4 \\ 0.2 \\ 0.4 \\ 0.6 \\ 0.4 \\ 0.2 \\ 0.4 \\ 0.6 \\ 0.4 \\ 0.2 \\ 0.4 \\ 0.6 \\ 0.4 \\ 0.6 \\ 0.4 \\ 0.2 \\ 0.4 \\ 0.6 \\ 0.4 \\ 0.2 \\ 0.4 \\ 0.6 \\ 0.4 \\ 0.2 \\ 0.4 \\ 0.6 \\ 0.4 \\ 0.4 \\ 0.6 \\ 0.4 \\ 0.4 \\ 0.4 \\ 0.4 \\ 0.4 \\ 0.4 \\ 0.4 \\ 0.4 \\ 0.4 \\ 0.4 \\ 0.4 \\ 0.4 \\ 0.4 \\ 0.4 \\ 0.4 \\$	
Decay mode	e $\sin 2\phi_1 \equiv -$	$ar{\xi_f}\mathcal{S}_f \qquad \mathcal{A}_f$	
$J/\psi K_S^0$	$+0.670 \pm 0.029$	$\pm 0.013 -0.015 \pm 0.021$	+0.045 -0.023
$\psi(2S)K_S^0$	$+0.738 \pm 0.079$	$\pm 0.036 + 0.104 \pm 0.055$	+0.047 -0.027
$\chi_{c1}K_S^0$	$+0.640 \pm 0.117$	$\pm 0.040 -0.017 \pm 0.083$	$+0.046 \\ -0.026$
$J/\psi K_L^0$	$+0.642 \pm 0.047$	$\pm 0.021 + 0.019 \pm 0.026$	+0.017 -0.041
All modes	$+0.667 \pm 0.023$	$\pm 0.012 + 0.006 \pm 0.016 \pm$	± 0.012

Systematics for $\sin 2\beta$



Source	$\sigma(S)$	$\sigma(C)$
Fitter validation	0.0004	0.0006
$\Delta \Gamma_d$ uncertainty	0.0055	0.0017
FT calibration portability	0.0053	0.0001
FT $\Delta \epsilon_{\text{tag}}$ portability	0.0014	0.0017
Decay-time bias model	0.0007	0.0013

$$\begin{split} S^{\mathrm{Run}\;2}_{J/\psi(\to\mu^+\mu^-)K^0_{\mathrm{S}}} &= & 0.714 \pm 0.015 \,(\mathrm{stat}) \pm 0.0074 \,(\mathrm{syst}) \\ C^{\mathrm{Run}\;2}_{J/\psi(\to\mu^+\mu^-)K^0_{\mathrm{S}}} &= & 0.013 \pm 0.014 \,(\mathrm{stat}) \pm 0.0025 \,(\mathrm{syst}) \\ S^{\mathrm{Run}\;2}_{\psi(2S)K^0_{\mathrm{S}}} &= & 0.647 \pm 0.053 \,(\mathrm{stat}) \pm 0.018 \quad(\mathrm{syst}) \\ C^{\mathrm{Run}\;2}_{\psi(2S)K^0_{\mathrm{S}}} &= -0.083 \pm 0.048 \,(\mathrm{stat}) \pm 0.0053 \,(\mathrm{syst}) \\ S^{\mathrm{Run}\;2}_{J/\psi(\to e^+e^-)K^0_{\mathrm{S}}} &= & 0.752 \pm 0.037 \,(\mathrm{stat}) \pm 0.084 \quad(\mathrm{syst}) \\ C^{\mathrm{Run}\;2}_{J/\psi(\to e^+e^-)K^0_{\mathrm{S}}} &= & 0.046 \pm 0.034 \,(\mathrm{stat}) \pm 0.0077 \,(\mathrm{syst}) \end{split}$$

Mass fit



(a) LHCb 6 fb^{-1}

5500

5600

sPlot technique to subtract combinatorial background: \rightarrow perform fits to invariant mass distribution

- $B^0 \to J/\psi(\mu^+\mu^-)K_s^0$ (85%) • $B^0 \to J/\psi(e^+e^-)K_s^0$ (12%)
- $B^0 \to \psi(2S)(\mu^+\mu^-)K_s^0$ (6%)

•
$$B_s^0 \to J/\psi K^+ K^-$$

•
$$B_s^0 \to \phi \phi$$



Total signal candidates ~306090 + 42700 + 23560

> LHCb-PAPER-2023-013 In preparation

Total signal candidates ~349000

LHCb-PAPER-2023-016 In preparation

Total signal candidates ~15840

LHCb-PAPER-2023-001

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ϕ_s polarisation dependent fit



- New physics effects can vary in different polarisation states
 - Allow $|\lambda|$ and ϕ_s differ in polarisation states
 - Shows no evidence for any polarisation dependence

LHCb-PAPER-2023-016

$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	Parameters	Values (stat. unc. only)
	$\begin{array}{l} \phi_s^0 \; [rad] \\ \phi_s^{\parallel} - \phi_s^0 \; [rad] \\ \phi_s^{\perp} - \phi_s^0 \; [rad] \\ \phi_s^{S} - \phi_s^0 \; [rad] \\ \lambda^0 \\ \lambda^0 \\ \lambda^{\parallel}/\lambda^0 \\ \lambda^{\perp}/\lambda^0 \\ \lambda^S/\lambda^0 \end{array}$	$\begin{array}{c} -0.034 \pm 0.023 \\ -0.002 \pm 0.021 \\ -0.001 \stackrel{+ \ 0.020}{_{- \ 0.021}} \\ 0.022 \stackrel{+ \ 0.027}{_{- \ 0.026}} \\ 0.969 \stackrel{+ \ 0.025}{_{- \ 0.024}} \\ 0.982 \stackrel{+ \ 0.055}{_{- \ 0.052}} \\ 1.107 \stackrel{+ \ 0.081}{_{- \ 0.075}} \\ 1.121 \stackrel{+ \ 0.085}{_{- \ 0.078}} \end{array}$

Systematics for ϕ_s



* Uncertainties (×0.01) Dominated sys. S

Sub-dominated sys.

Stat. limited

Source	$ A_0 ^2$	$ A_{\perp} ^2$	ϕ_s [rad]	$ \lambda $	$\delta_{\perp} - \delta_0 \ [ext{rad}]$	$\delta_{\parallel} - \delta_0 \ [ext{rad}]$	$\Gamma_s - \Gamma_d$ $[ps^{-1}]$	$\Delta \Gamma_s$ [ps ⁻¹]	Δm_s [ps ⁻¹]
Mass parametrization	0.04	0.03	0.03	0.02	0 15	0.12	0.02	0.04	0.03
Mass: shape statistical	0.04	0.04	0.05	0.09	0.62	0.33	0.02	0.01	0.11
Mass factorization	0.11	0.10	0.42	0.19	0.54	0.60	0.12	0.16	0.18
B^+ contamination	0.04	0.05	_	0.02	_	0.17	(0.07)	(0.03)	_
D–wave component	0.04	0.04	0.02	_	0.07	0.13	0.01	0.03	0.02
Bkgcat 60	0.07	0.04	0.02	0.10	0.18	0.18	0.02	_	0.01
Multiple candidates	0.01	_	0.27	0.22	0.90	0.41	0.01	0.01	0.24
Particle identification	0.06	0.09	0.27	0.27	1.31	0.51	0.05	0.15	0.46
$\mathcal{C}_{\mathrm{SP}}$ factors	_	0.01	0.01	0.03	0.73	0.41	_	0.01	0.04
DTR model portability	_	—	0.08	0.03	0.26	0.09	_	—	0.09
DTR calibration	_	_	0.03	0.02	0.11	0.07	_	_	0.05
Time bias correction	0.04	0.05	0.06	0.05	0.77	0.11	0.03	0.05	0.44
Angular efficiency	0.05	0.14	0.25	0.32	0.42	0.44	0.01	0.02	0.13
Angular resolution	0.01	0.01	0.02	0.01	0.02	0.08	_	0.01	0.02
Kinematic weighting	0.24	0.09	0.01	0.01	0.98	0.86	0.02	0.03	0.31
Momentum uncertainty	0.08	0.04	0.04	_	0.07	0.11	0.01	_	0.13
Longitudinal scale	0.07	0.04	0.04	_	0.10	0.09	0.02	_	0.31
Neglected correlations	_	—	_	_	4.20	4.96	—	—	—
Total sys. unc.	0.32	0.24	0.6	0.5	4.8	5.2	0.14	0.24	0.9
Stat. unc.	0.17	0.23	2.2	1.1	7.5	6.0	0.14	0.44	3.3

• ϕ_s , $|\lambda|$, $\Delta\Gamma_s$, Δm_s are statistically limited

Systematics for $\phi_s^{s\bar{s}s}$



Source	$\phi^{s\overline{s}s}_{s}$	$ \lambda $	$ A_0 ^2$	$ A_{\perp} ^2$	$\delta_{\parallel}-\delta_{0}$	$\delta_{\perp} - \delta_0$
Time resolution	4.9	2.6	0.8	0.8	0.1	3.4
Flavor tagging	4.8	4.7	0.9	1.3	1.2	9.7
Angular acceptance	3.9	4.9	1.4	1.7	4.7	1.2
Time acceptance	2.3	1.7	0.1	0.1	5.6	0.7
Mass fit & factorization	2.2	4.4	1.9	2.3	2.3	2.5
MC truth match	1.1	0.2	0.1	0.1	0.2	0.3
Fit bias	0.8	0.7	0.9	0.3	3.6	0.7
Candidate multiplicity	0.3	0.2	0.1	0.8	0.2	0.1
Total	8.8	8.6	2.7	3.3	8.5	10.7

Parameter	Result
$\phi_s^{s\overline{s}s}$ [rad]	$-0.042 \pm 0.075 \pm 0.009$
$ \lambda $	$1.004 \pm 0.030 \pm 0.009$
$ A_0 ^2$	$0.384 \pm 0.007 \pm 0.003$
$ A_{\perp} ^2$	$0.310 \pm 0.006 \pm 0.003$
$\delta_{\parallel} - \delta_0 \; \; [{ m rad} \;]$	$2.463 \pm 0.029 \pm 0.009$
$\delta_{\perp}^{-} - \delta_{0} \; \; [{ m rad} \;]$	$2.769 \pm 0.105 \pm 0.011$

Time-dependent angular fit

$$\mathscr{P}(t,\theta_K,\theta_\mu,\phi_h|\delta_t) \propto \sum_{k=1}^{10} N_k h_k(t) f_k(\theta_K,\theta_\mu,\phi_h) \to \phi_s, \Delta m_s, \Delta \Gamma_s, \Gamma_s - \Gamma_d$$

$$\mathcal{P}\left(t, \Omega | \mathfrak{q}^{\mathrm{OS}}, \mathfrak{q}^{\mathrm{SSK}}, \eta^{\mathrm{OS}}, \eta^{\mathrm{SSK}}, \delta_{t}\right)$$

$$\propto \sum_{k=1}^{10} \mathcal{C}_{\mathrm{SP}}^{k} N_{k} f_{k}(\Omega) \varepsilon_{\mathrm{data}}^{B_{s}^{0}}(t)$$

$$\cdot \left\{ \left[\mathcal{Q}\left(\mathfrak{q}^{\mathrm{OS}}, \mathfrak{q}^{\mathrm{SSK}}, \eta^{\mathrm{OS}}, \eta^{\mathrm{SSK}}\right) h_{k}\left(t | B_{s}^{0}\right) + \bar{\mathcal{Q}}\left(\mathfrak{q}^{\mathrm{OS}}, \mathfrak{q}^{\mathrm{SSK}}, \eta^{\mathrm{OS}}, \eta^{\mathrm{SSK}}\right) h_{k}\left(t | \overline{B}_{s}^{0}\right) \right\}$$

Angular amplitudes

$$C_{SP}^k$$
 account for the interference
between P- and S- wave
flavor tagging

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time-dependent oscillation decay-time efficiency

decay-time resolution

$$h_k(t|B_s^0) = \frac{3}{4\pi} e^{-\Gamma t} \left(a_k \cosh \frac{\Delta \Gamma t}{2} + b_k \sinh \frac{\Delta \Gamma t}{2} + c_k \cosh(\Delta m t) + d_k \sin(\Delta m t) \right),$$
$$+c_k \cos(\Delta m t) + d_k \sin(\Delta m t) \right),$$
$$h_k(t|\bar{B}_s^0) = \frac{3}{4\pi} e^{-\Gamma t} \left(a_k \cosh \frac{\Delta \Gamma t}{2} + b_k \sinh \frac{\Delta \Gamma t}{2} - c_k \cos(\Delta m t) - d_k \sin(\Delta m t) \right),$$

 a_k, b_k, c_k, d_k involve strong and weak phases (δ, ϕ_s) of each component

k	A_k	$f_k(heta_\mu, heta_K,arphi_h)$
1	$ A_0 ^2$	$2\cos^2 heta_K\sin^2 heta_\mu$
2	$ A_{\ } ^{2}$	$\sin^2 heta_k(1-\sin^2 heta_\mu\cos^2arphi_h)$
3	$ A_{\perp} ^2$	$\sin^2 heta_k(1-\sin^2 heta_\mu\sin^2arphi_h)$
4	$ A_{\parallel}A_{\perp} $	$\sin^2 heta_k \sin^2 heta_\mu \sin 2arphi_h$
5	$ A_0A_{\parallel} $	$\frac{1}{2}\sqrt{2}\sin 2 heta_k\sin 2 heta_\mu\cos arphi_h$
6	$ A_0A_\perp $	$-\frac{1}{2}\sqrt{2}\sin 2\theta_k \sin 2\theta_\mu \sin \varphi_h$
7	$ A_{S} ^{2}$	$rac{2}{3}\sin^2 heta_\mu$
8	$ A_S A_{\parallel} $	$\frac{1}{3}\sqrt{6}\sin\theta_k\sin2\theta_\mu\cos\varphi_h$
9	$ A_S A_\perp $	$-\frac{1}{3}\sqrt{6}\sin\theta_k\sin2\theta_\mu\sin\varphi_h$
10	$ A_S A_0 $	$\frac{4}{3}\sqrt{3}\cos\theta_K\sin^2\theta_\mu$