

Tau Physics at Belle II

Current Status and Prospects

CEPC味物理-新物理和相关探测技术研讨会



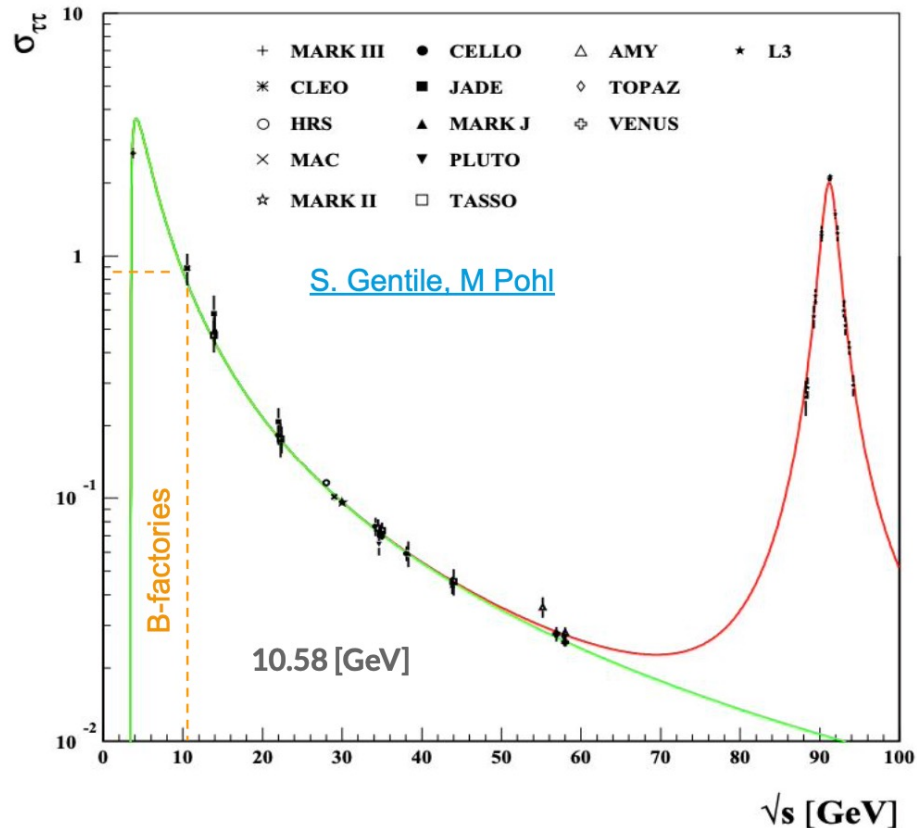
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2023/06/18

B factory is also τ factory

$$\sigma(e^+e^- \rightarrow \tau^+\tau^-)$$



@10.58 GeV:

$$\sigma(e^+e^- \rightarrow \tau^+\tau^-) = 0.92 \text{ nb}$$

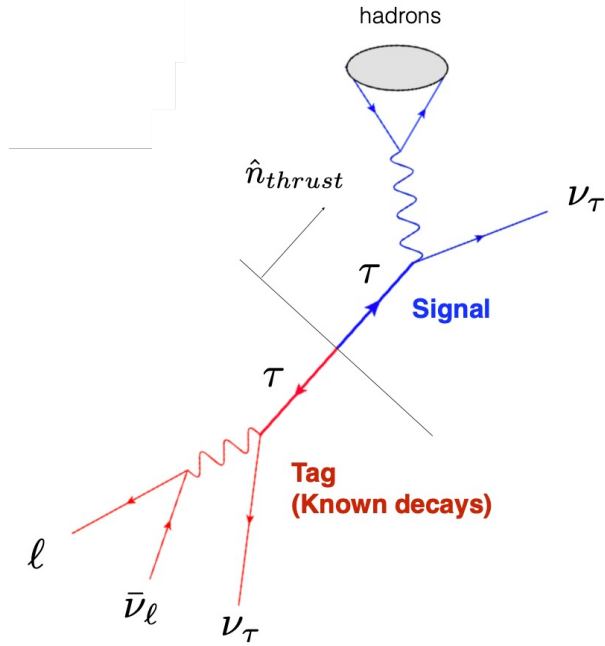
$$\sigma(e^+e^- \rightarrow \Upsilon(4S)) = 1.11 \text{ nb}$$

Features of a B-Factory (super τ -charm Factory):

- High luminosity.
- Well-defined initial state.
- High vertex resolution.
- Excellent calorimetry.
- Sophisticated particle ID.
- Ability to trigger low-multiplicity event

Also see Nishida-san's talk

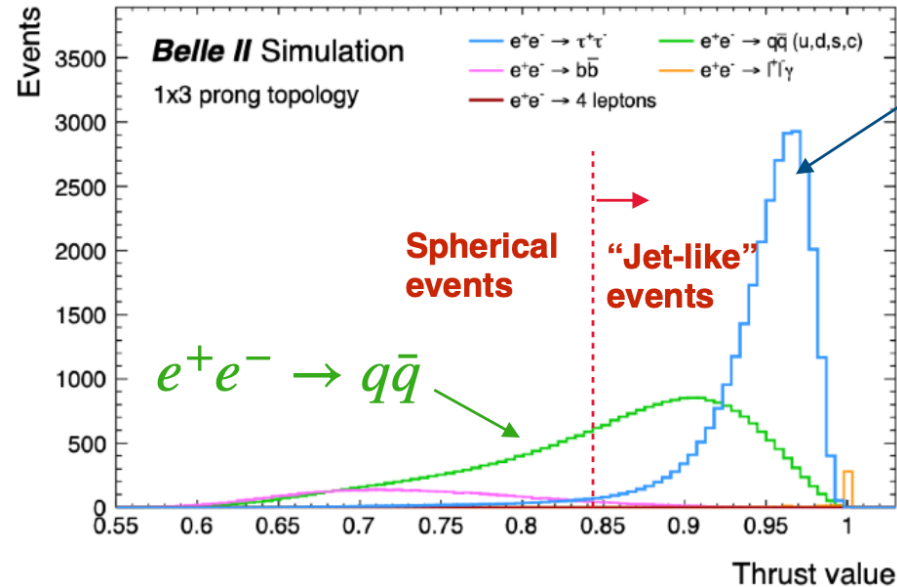
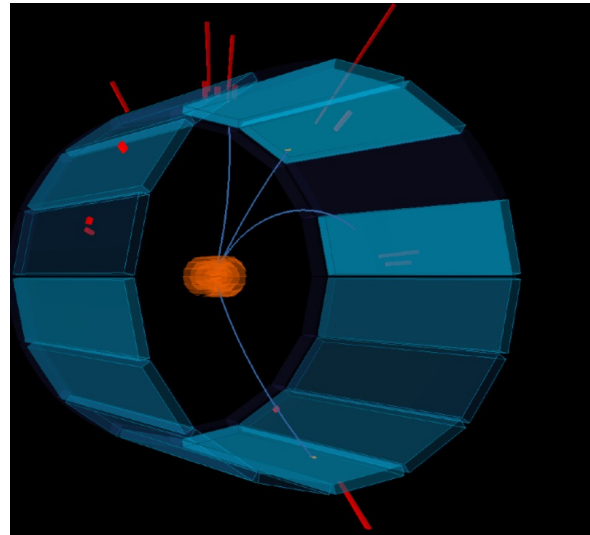
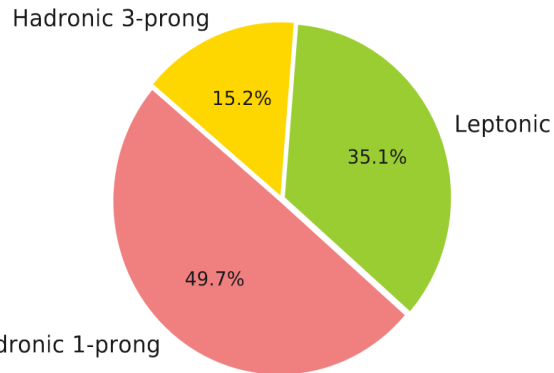
How we reconstruct τ at Belle II (in general cases)



- $e^+e^- \rightarrow \tau^+\tau^-$ decays are reconstructed
- Event separated based on **thrust** axis (\hat{n}_{thrust})

$$V_{thrust} = \frac{\sum_i |\vec{p}_i^{cm} \cdot \hat{n}_{thrust}|}{\sum_i |\vec{p}_i^{cm}|}$$

- \vec{p}_i^{cm} : momenta of detectable tracks
- \hat{n}_{thrust} : values maximize V_{thrust}



Current status of Belle II



Current:

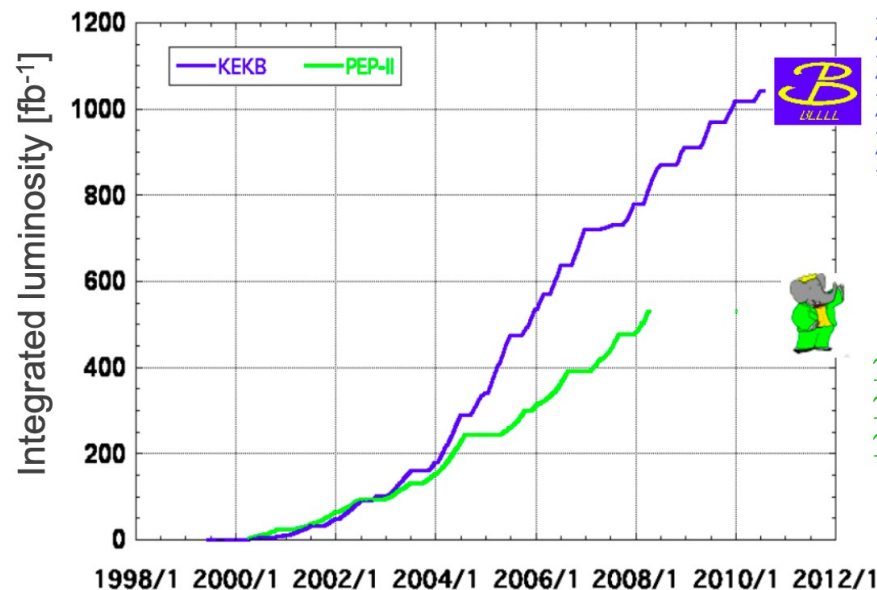
peak \mathcal{L} : $4.7 \times 10^{34} \text{ cm}^{-2} \text{ s}^{-1}$ (world-record)

integral \mathcal{L} : 428 fb^{-1}

Goal:

peak \mathcal{L} : $6 \times 10^{35} \text{ cm}^{-2} \text{ s}^{-1}$

integral \mathcal{L} : 50 ab^{-1}



The Belle II's integral luminosity is only half those of Belle/Babar. **But** some results are better!

- Better vertex resolution
- Better trigger efficiency
-

What Belle II has done:

τ properties:

- mass: [arXiv:2305.19116](#)
- lifetime (Sensitivity study)

Beyond Standard Model

--LFV

- $\tau^- \rightarrow \ell^- \phi$ [arXiv:2305.04759](#)
- $\tau^- \rightarrow \ell^- \alpha$ [PRL 130, 181803](#)

Electroweak sector

--Lepton Universality

$$R_\mu = \frac{B(\tau^- \rightarrow \mu^- \bar{\nu}_\mu \nu_\tau)}{B(\tau^- \rightarrow e^- \bar{\nu}_e \nu_\tau)} \text{ (Sensitivity study)}$$

PS: Works on Trigger logical, Particle Identification, Photon calibration ... are still ongoing for better performance.

a little background:

$$\Gamma(L^- \rightarrow \ell^- \bar{\nu}_\ell \nu_L(\gamma)) = \frac{\mathcal{B}(L^- \rightarrow \ell^- \bar{\nu}_\ell \nu_L(\gamma))}{\tau_L} = \frac{g_L^2 g_\ell^2}{32M_W^4} \frac{m_L^5}{192\pi^3} f\left(\frac{m_\ell^2}{m_L^2}\right) F_{\text{corr}}(m_L, M_\ell)$$

$$f(x) = 1 - 8x + 8x^3 - x^4 - 12x^2 \ln(x)$$

$$F_{\text{corr}}(m_L, M_\ell) = f\left(\frac{m_\ell}{m_L}\right) \left(1 + \frac{3m_\ell^2}{5M_W^2}\right) \left(1 + \frac{\alpha(m_L)}{2\pi} \left(\frac{25}{4} - \pi^2\right)\right)$$

W. Marciano and A. Sirlin PRL. 61, 1815 (1988)

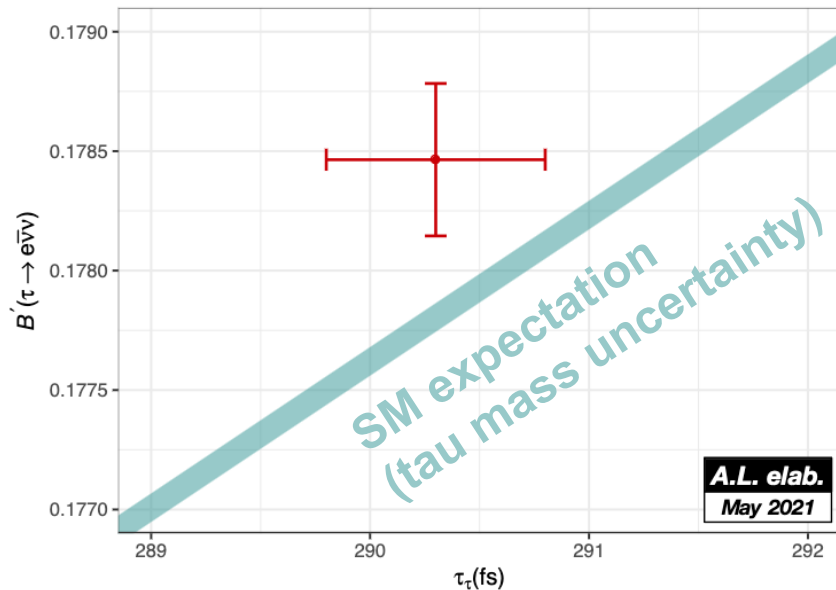
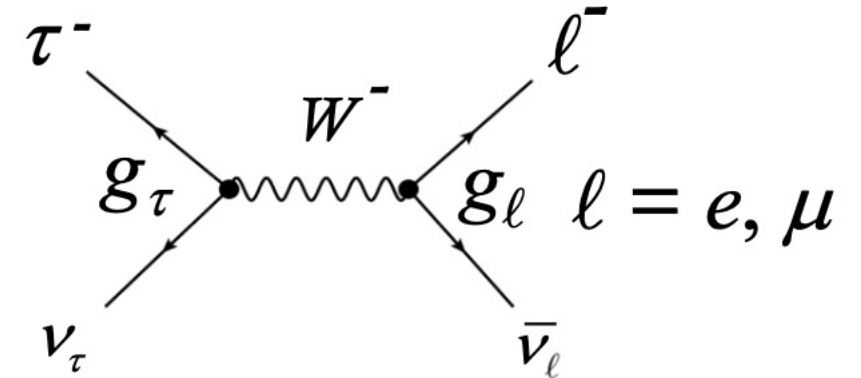
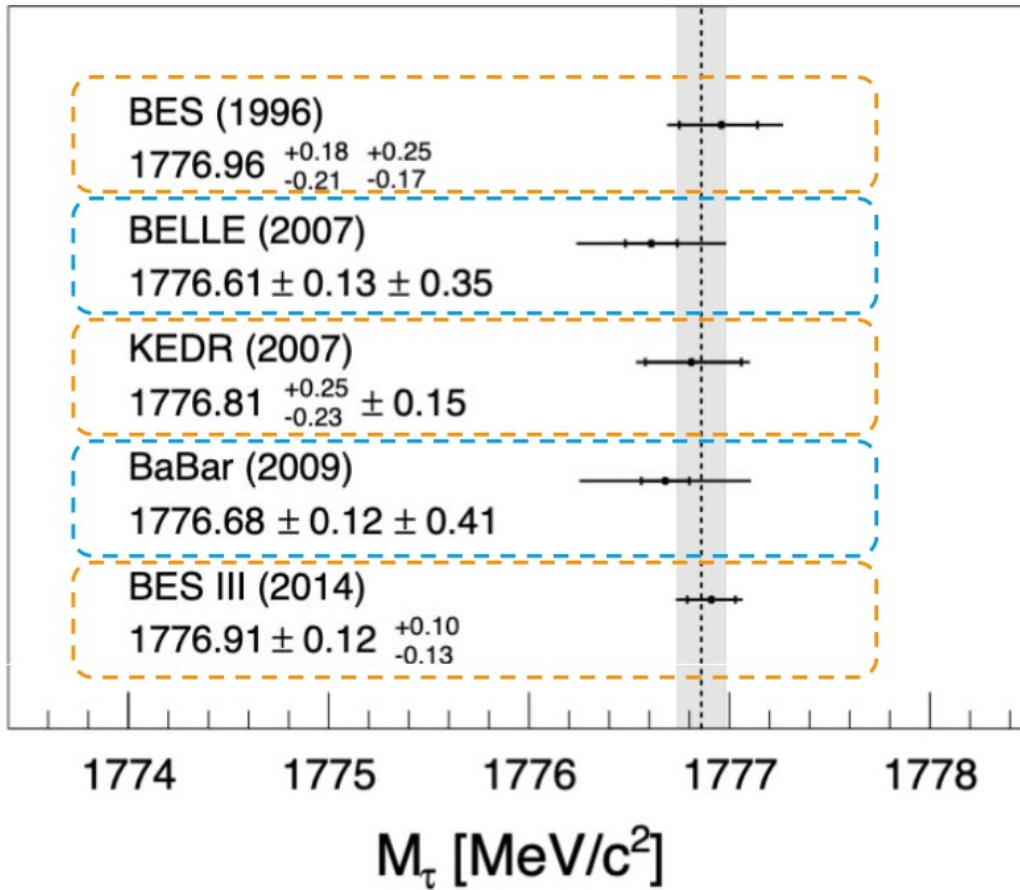


Fig from Alberto Lusiani

| input | Uncertainty (%) | Best Measurement |
|--|-----------------|------------------|
| $\mathcal{B}(\tau^- \rightarrow \ell^- \bar{\nu}_\ell \nu_\tau(\gamma))$ | 0.180 | ALEPH |
| τ_L | 0.172 | Belle |
| m_L^5 | 0.007 | BES III |

Measurement of τ mass

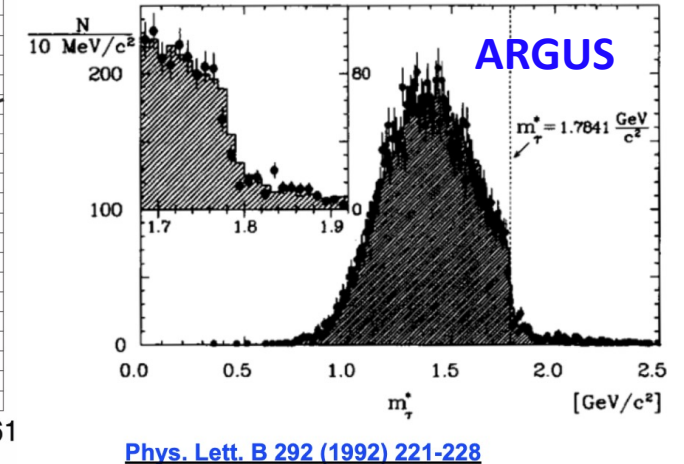
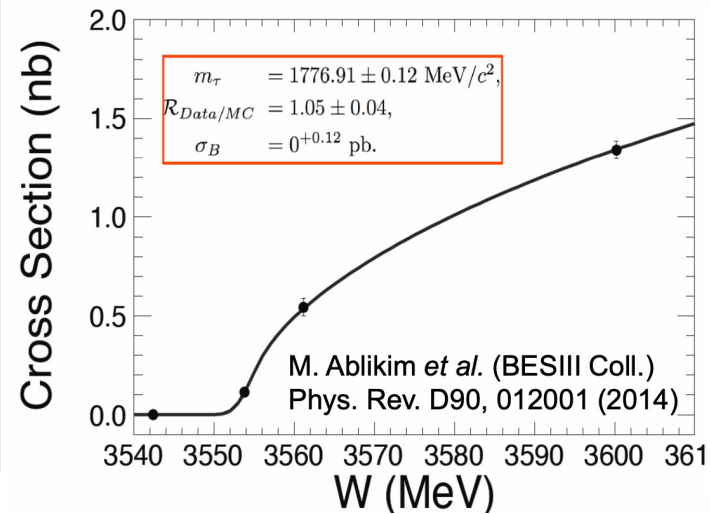
PDG Average (2022)
 1776.86 ± 0.12



Two main methods for measuring the mass:

1: pair production cross section:

- energy scan around the tau pair production threshold
- extract the mass from the dependence of cross section on collision energy



2: Pseudomass method:

developed by ARGUS, and used at BaBar, Belle and Belle II

Measurement of τ mass

Pseudomass method:

$$m_\tau^2 = (p_h + p_\nu)^2$$

$$= 2 E_h (E_\tau - E_h) + m_h^2 - 2|\vec{p}_h|(E_\tau - E_h)\cos(\vec{p}_h, \vec{p}_\nu)$$

The direction of the neutrino is not known, since $\cos(\vec{p}_h, \vec{p}_\nu) \leq 1$

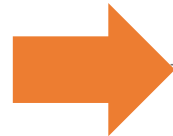
Pseudomass: $\sqrt{2 E_h (E_\tau - E_h) + m_h^2 - 2|\vec{p}_h|(E_\tau - E_h)} \leq m_\tau$

Belle (414 fb⁻¹) [arXiv:hep-ex/0608046](https://arxiv.org/abs/hep-ex/0608046)

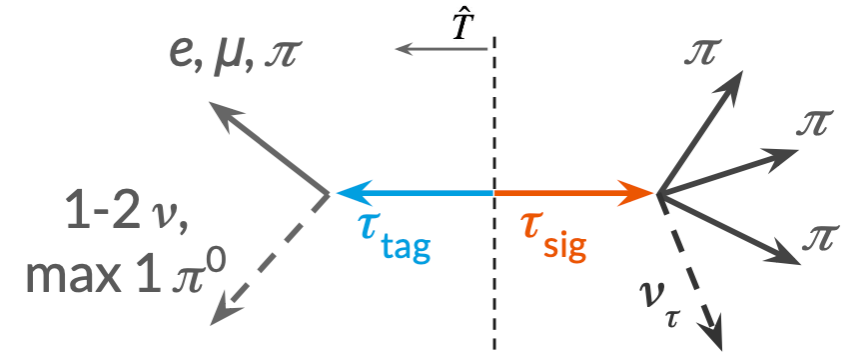
TABLE I: Summary of systematic uncertainties

| Source of systematics | σ , MeV/c ² |
|--|-------------------------------|
| Beam energy and tracking system | 0.26 |
| Edge parameterization | 0.18 |
| Limited MC statistics | 0.14 |
| Fit range | 0.04 |
| Momentum resolution | 0.02 |
| Model of $\tau \rightarrow 3\pi\nu_\tau$ | 0.02 |
| Background | 0.01 |
| Total | 0.35 |

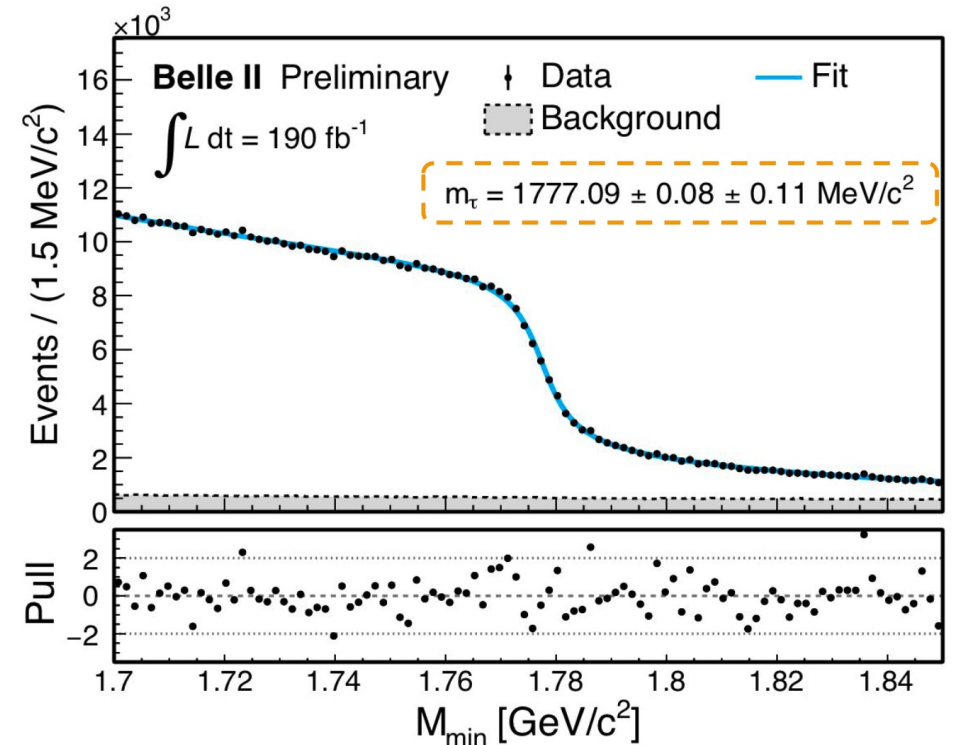
stat: 0.13 MeV



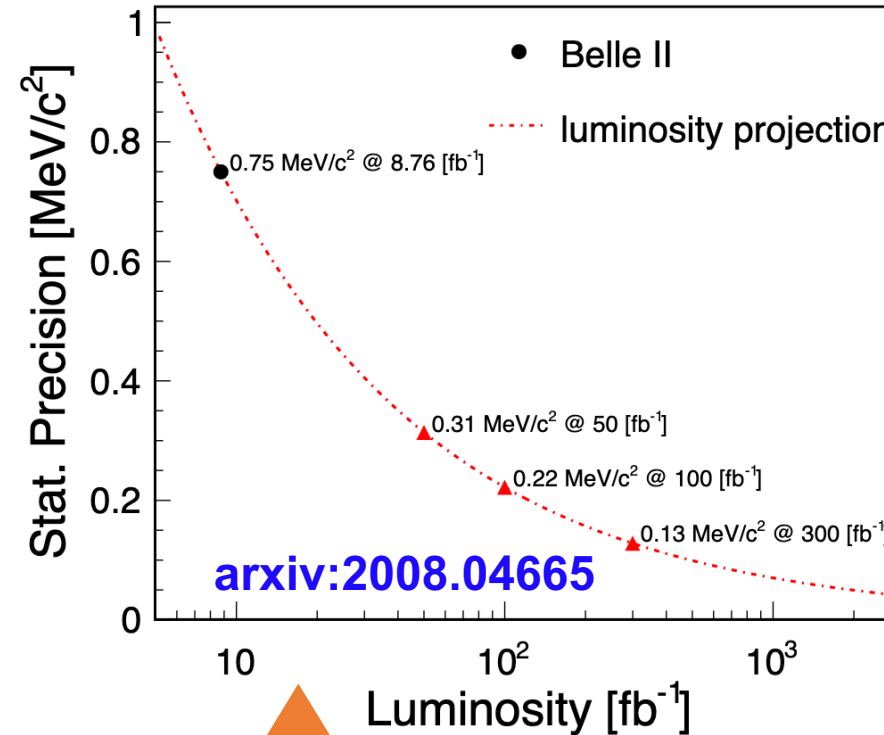
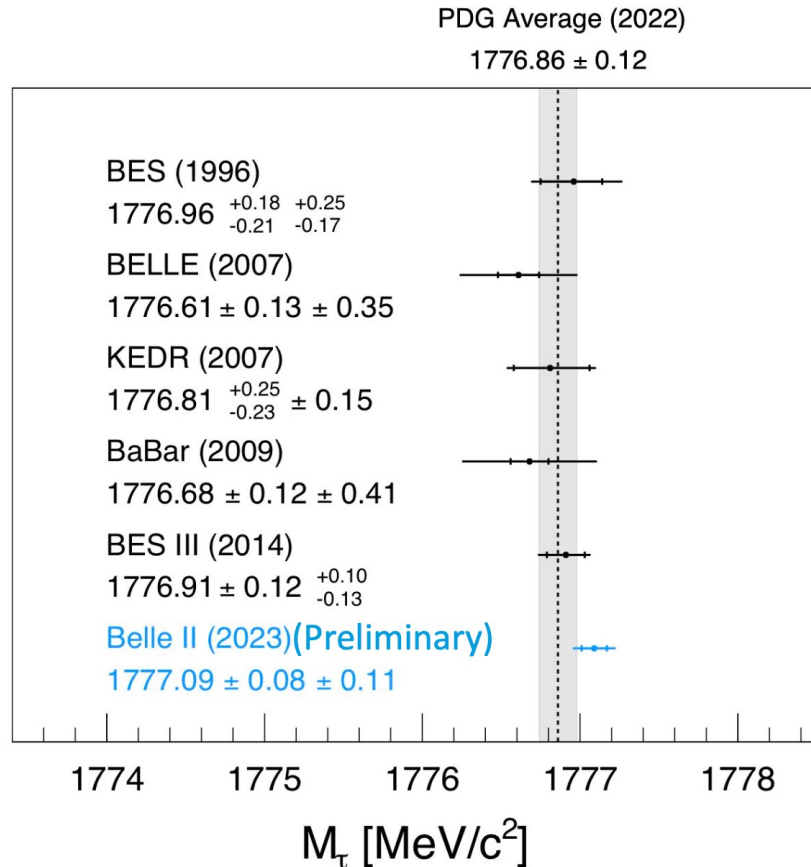
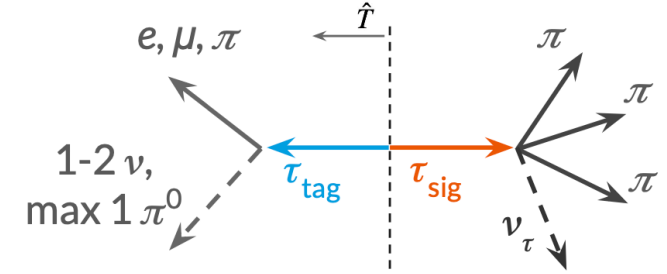
| Source | Belle II (190 fb ⁻¹) | Uncertainty [MeV/c ²] |
|--------------------------------------|----------------------------------|-----------------------------------|
| Knowledge of the colliding beams: | | |
| Beam energy correction | | 0.07 |
| Boost vector | | ≤ 0.01 |
| Reconstruction of charged particles: | | |
| Charged particle momentum correction | | 0.06 |
| Detector misalignment | | 0.03 |
| Fitting procedure: | | |
| Estimator bias | | 0.03 |
| Choice of the fit function | | 0.02 |
| Mass dependence of the bias | | ≤ 0.01 |
| Imperfections of the simulation: | | |
| Detector material budget | | 0.03 |
| Modeling of ISR and FSR | | 0.02 |
| Total | | 0.11 |



[arXiv:2305.19116](https://arxiv.org/abs/2305.19116)



Measurement of τ mass



World's best measurement of the τ mass!

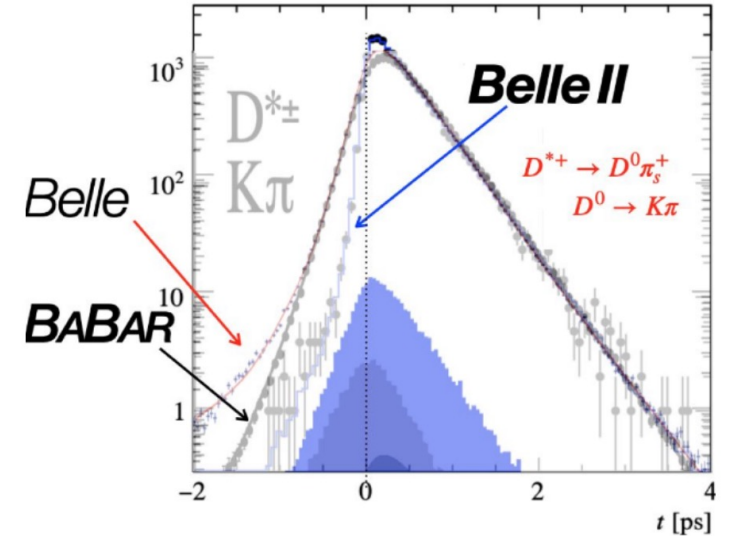
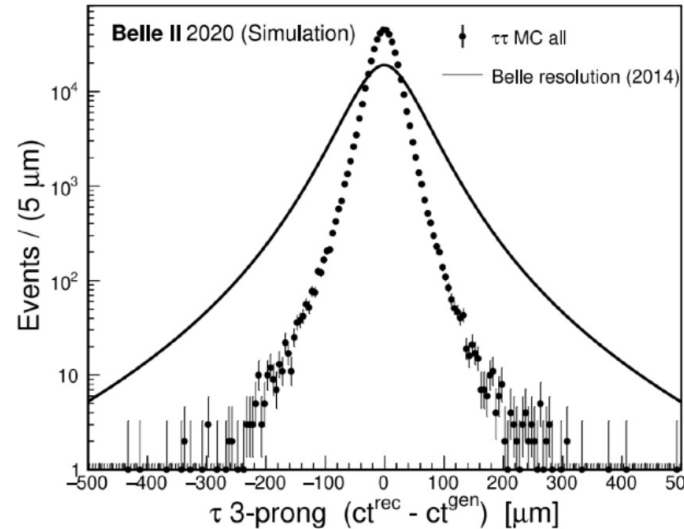
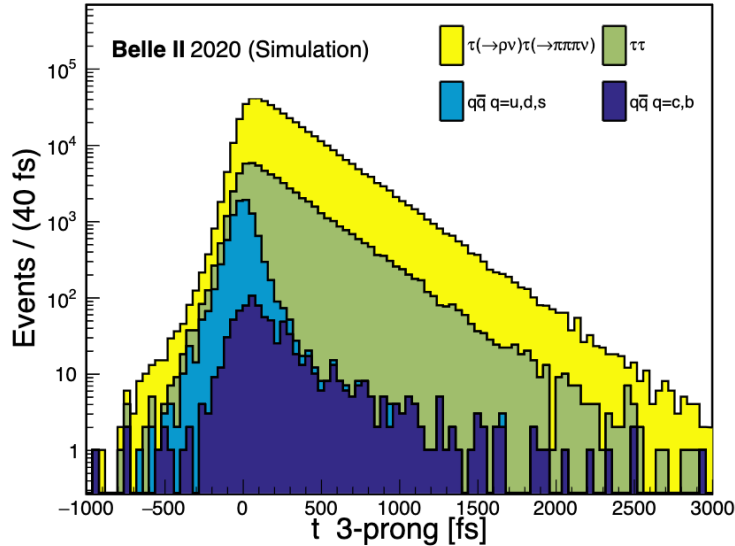
half data size as Belle and BaBar,
BUT better statistical precision!

**Even better than our estimation
when using 8.75 fb¹ data!**

Sensitivity study of τ lifetime

proper decay time: $t = \ell_\tau \frac{m_\tau}{|\vec{p}_\tau| c}$

Proper decay time resolution:



In MC simulations, the Belle II proper time resolution is **~2x better than Belle**.

-- Due to PXD and smaller beam pipe diameter.

Input $\tau_\tau = 290.57$ fs
 Output $\tau_\tau = 287.2 \pm 0.5$ (stat) fs } 3 fs bias

Same statistical uncertainty of Belle. (200 fb⁻¹ vs 711 fb⁻¹)

Next step:

- Revisiting the 3x3 topology
- Consider the ISR/FSR effect
-

Lepton Flavor Universality Violation

$$\left(\frac{g_\mu}{g_e}\right)_\tau = \sqrt{\frac{BF[\tau^- \rightarrow \mu^- \bar{\nu}_\mu \nu_\tau] f(m_e^2/m_\tau^2)}{BF[\tau^- \rightarrow e^- \bar{\nu}_e \nu_\tau] f(m_\mu^2/m_\tau^2)}}$$

In the SM: $\left(\frac{g_\mu}{g_e}\right)_\tau = 1$

| | μ |
|--|--------|
| N^D | 731102 |
| Purity | 97.3% |
| Total Efficiency | 0.485% |
| Particle ID Efficiency | 74.5% |
| Systematic uncertainties: | |
| Particle ID | 0.32 |
| Detector response | 0.08 |
| Backgrounds | 0.08 |
| Trigger | 0.10 |
| $\pi^- \pi^- \pi^+$ modelling | 0.01 |
| Radiation | 0.04 |
| $\mathcal{B}(\tau^- \rightarrow \pi^- \pi^- \pi^+ \nu_\tau)$ | 0.05 |
| $\mathcal{L}\sigma_{e^+e^- \rightarrow \tau^+\tau^-}$ | 0.02 |
| Total [%] | 0.36 |

Base measurement from Babar: 467 fb⁻¹, [PRL.105.051602](#)

Need to improve systematic uncertainty uncertainties due to **PID** and **trigger**

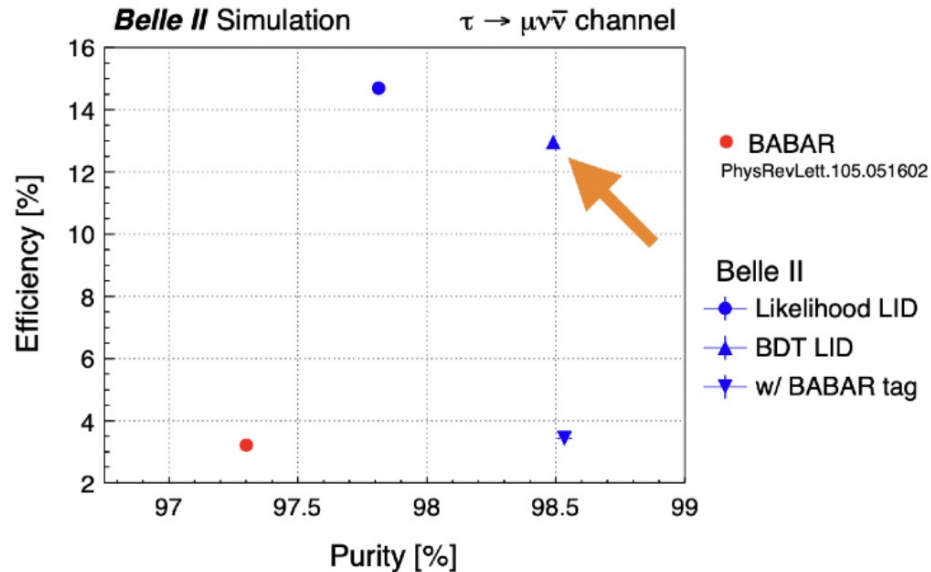
➤ **Belle II can do it!**

Lepton Flavor Universality Violation

tests with 3x1 topology: same method as Babar

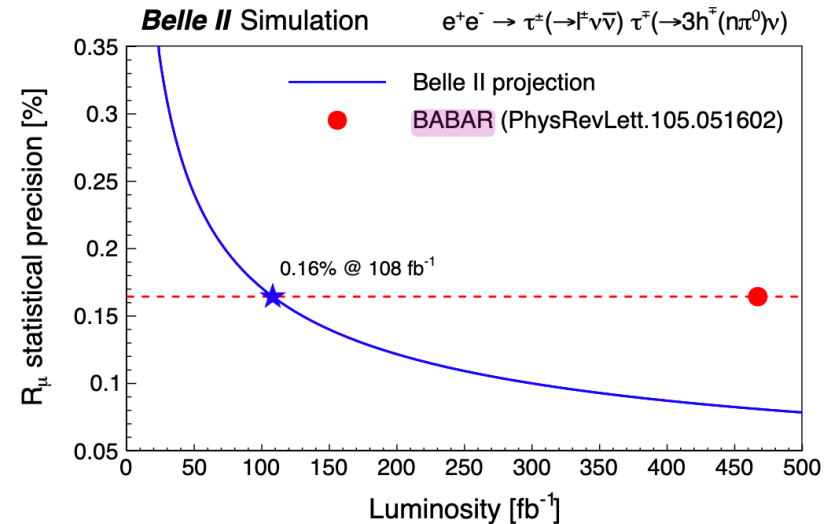
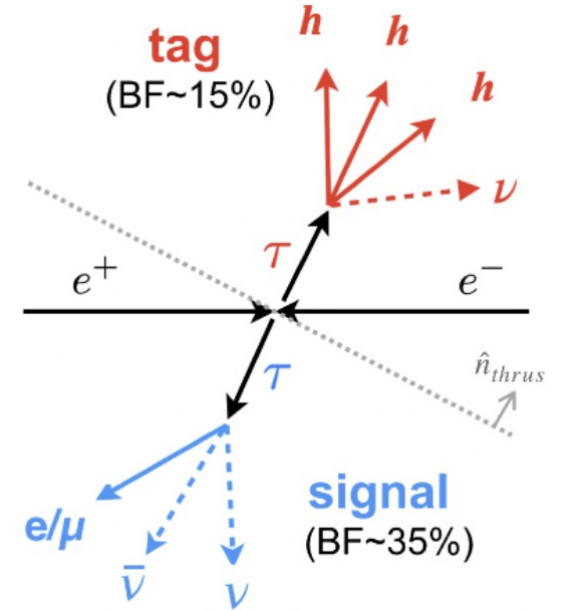
Cut-based performance

- Matches BaBar stat. uncertainty with 100 fb^{-1} of data.
 - Achieved with asymmetric p_t thresholds on lead, sublead and third track on tag side.
 - x4 higher efficiency** with better purity:



BDT performance

- Training of a XGBoost classifier for combined signal (e or μ in final state).
- 1.7x improvement in efficiency w.r.t. cut-based selection (**x7 than BaBar**), with a purity of 98%.



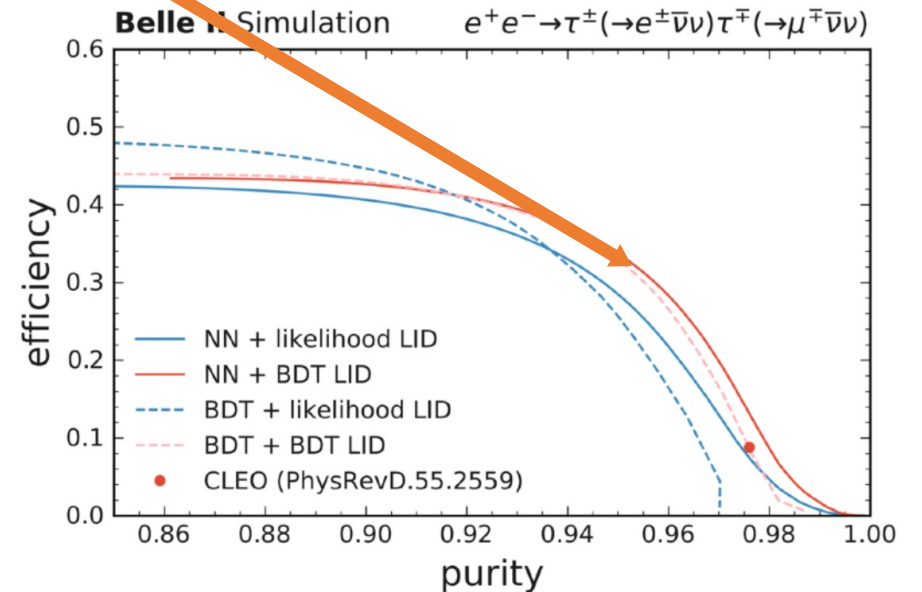
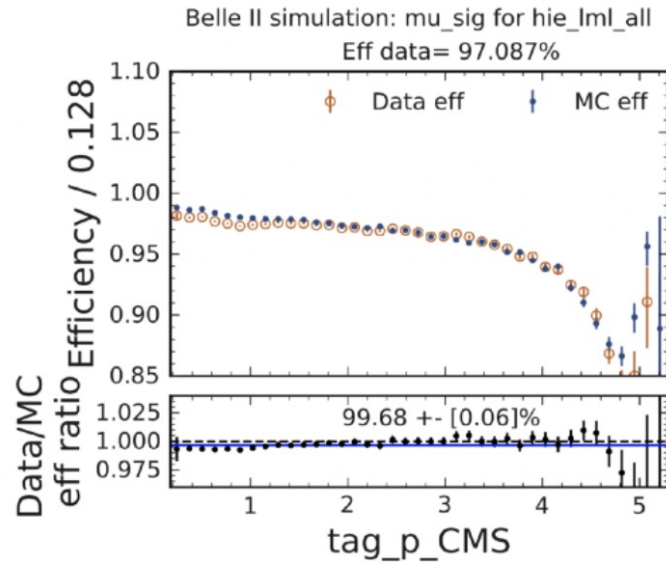
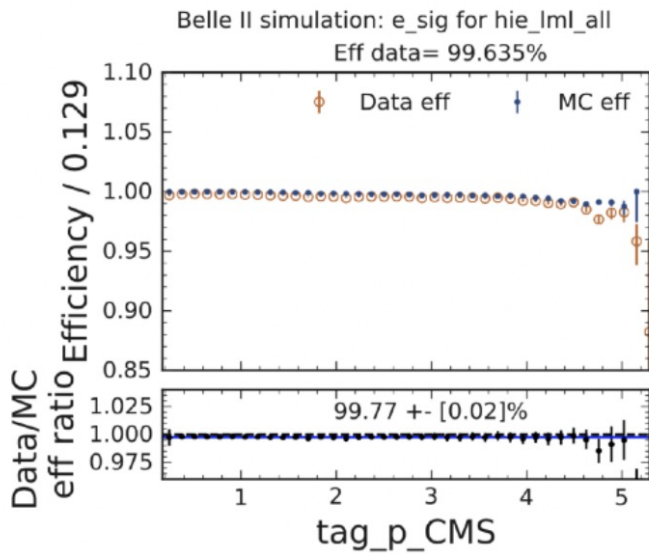
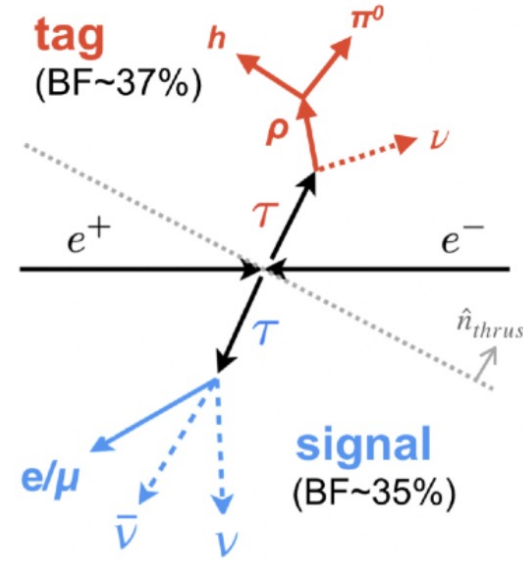
Lepton Flavor Universality Violation

tests with 1x1 topology: same method as CLEO (only 3.56 fb^{-1})

- Trigger:**

- $\epsilon_{\text{trg}} = 96 - 100\%$ for e-channel.
- $\epsilon_{\text{trg}} = 85 - 99\%$ for μ -channel.

**By using the neural network,
Belle II achieve better performance for
electron channel**



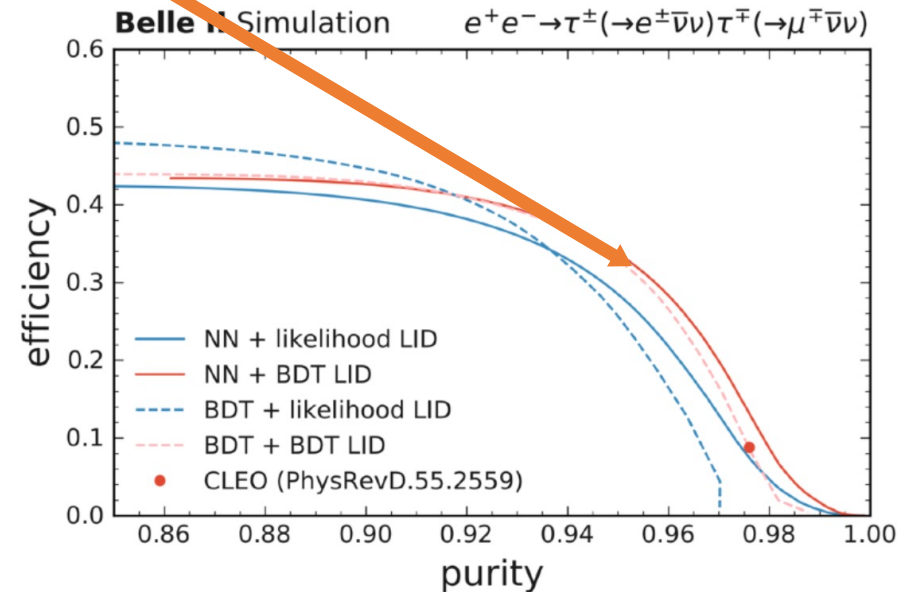
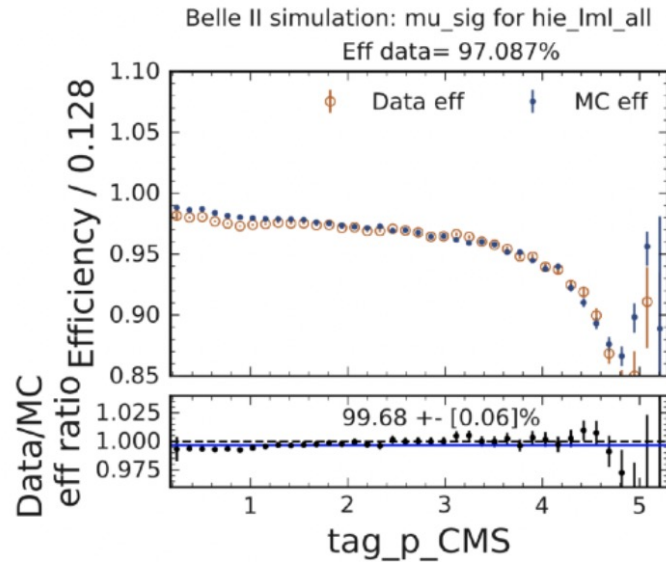
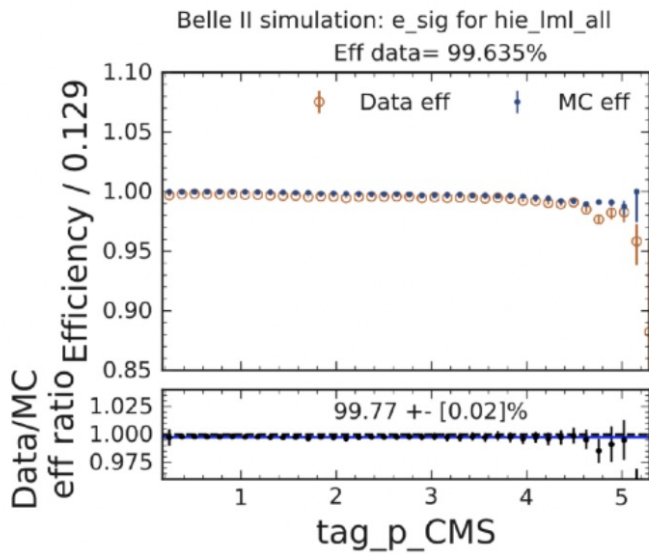
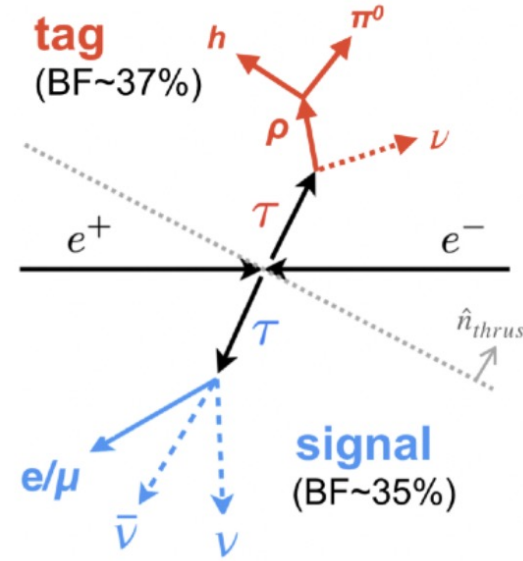
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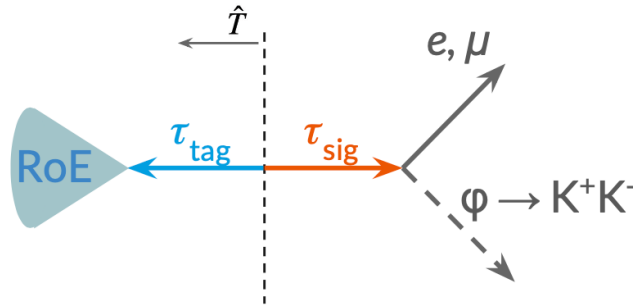
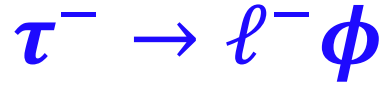
**By using the neural network,
Belle II achieve better performance for
electron channel**



New results coming soon! (Maybe in ESP2023 meeting)

Charged Lepton Flavor Violation

arXiv:2305.04759

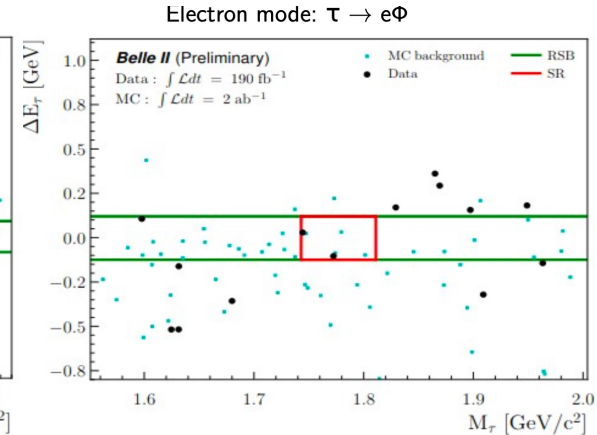
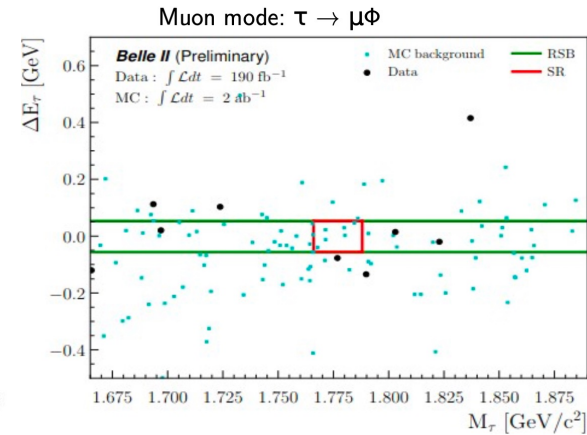
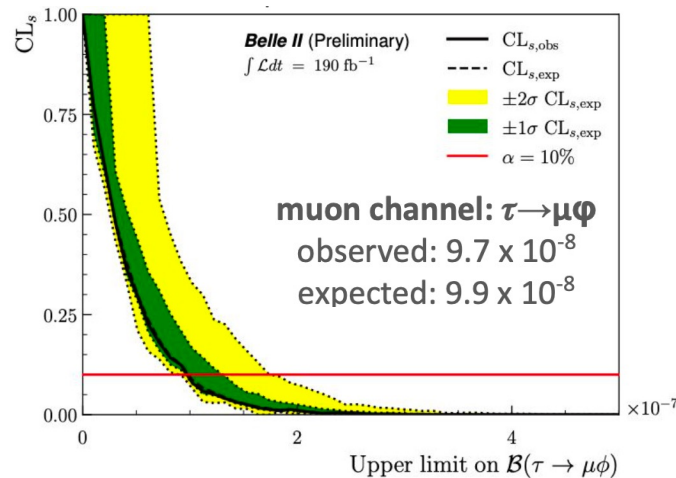
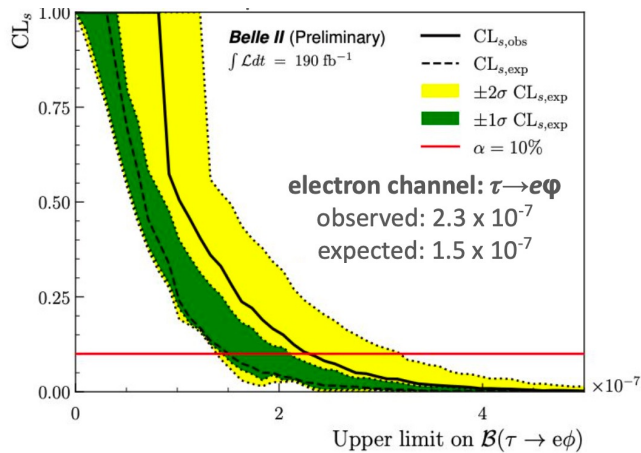


- highly suppressed in SM ($\sim 10^{-50}$)
- leptoquark models predict BF of up to $10^{-8} \sim 10^{-10}$

Poisson counting experiment approach in **signal regions** in M_τ and $\Delta E_\tau = E_{\text{sig}}^* - \sqrt{s}/2$ plane

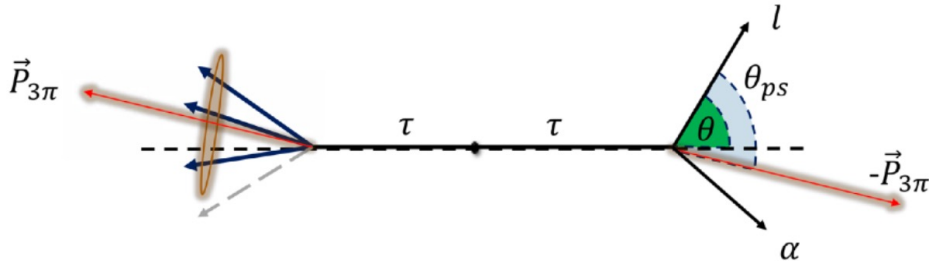
→ expected background evaluated from data **reduced sidebands** with scaling from simulation

not yet competitive with Belle/BaBar... (only 190 fb⁻¹ data samples are used)
But a successful first application of inclusive tagging at Belle II



Charged Lepton Flavor Violation

$$\tau^- \rightarrow \ell^- \alpha$$

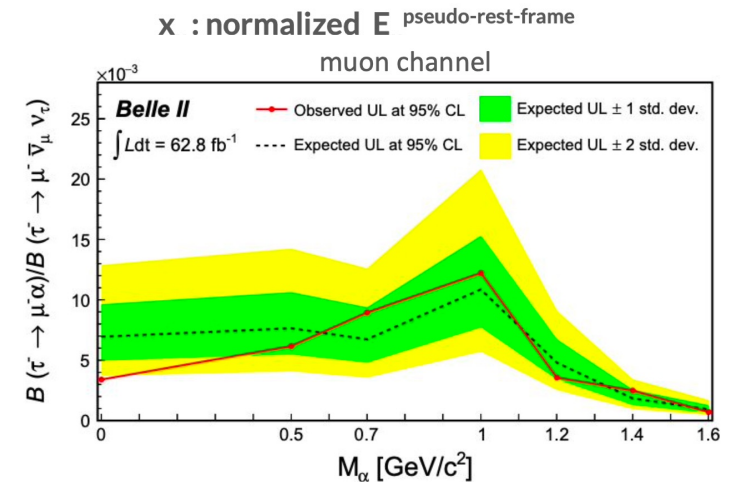
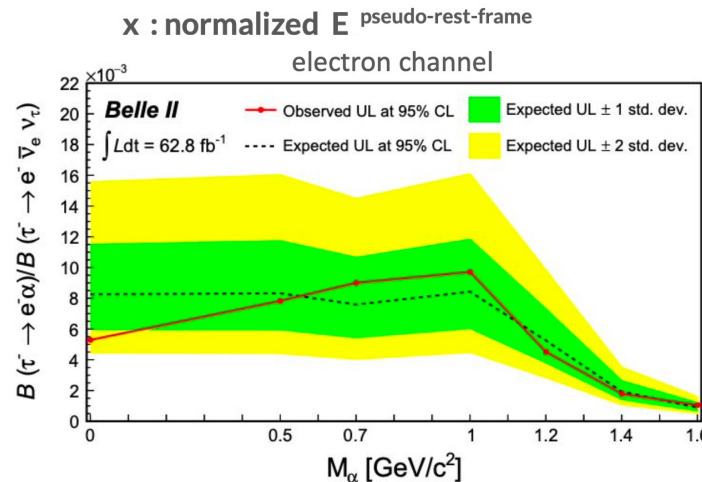
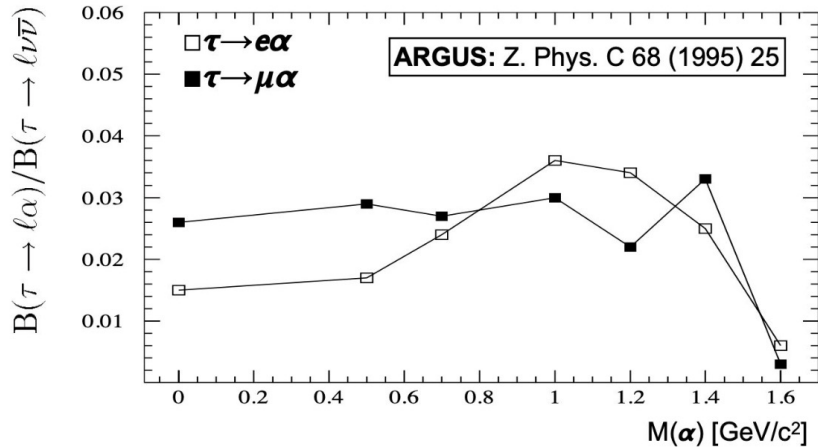
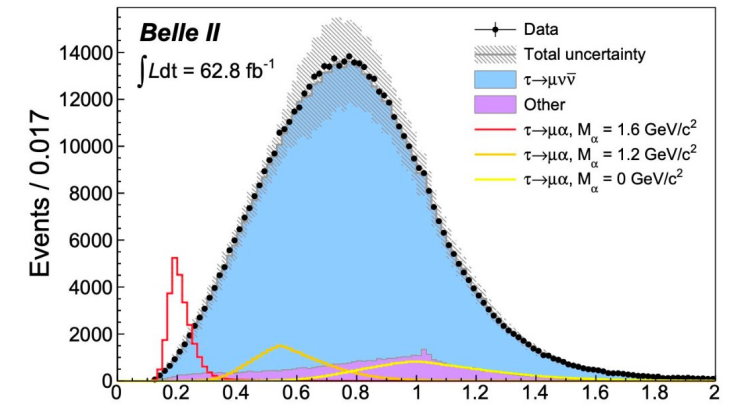
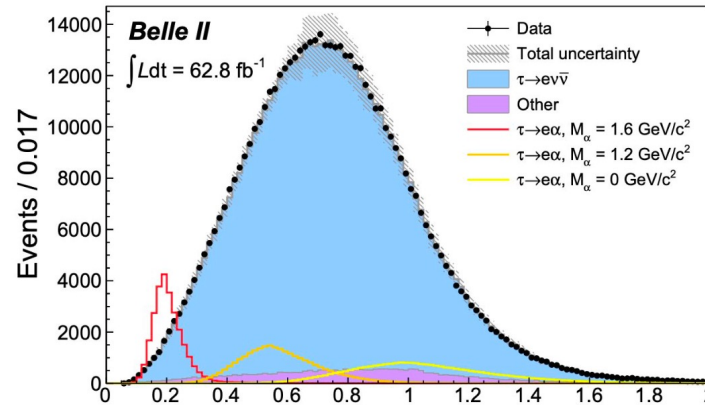


$$E_\tau = E_{\text{cms}}/2, \quad \hat{p}_\tau \approx \vec{p}_{\text{tag}} / |\vec{p}_{\text{tag}}|$$

It probes the existence of a **long-lived invisible gauge boson** α .

- Possible DM candidate.

[PRL 130, 181803](#)



Most stringent limits in these channels to date! (2-14 times more constraining than Argus)

Summary

Belle II has **advantages in τ decays studies**

- ❖ Has collected 424 fb-1 data samples
- ❖ Lots of works on the way!

τ properties:

-- mass: [arXiv:2305.19116](https://arxiv.org/abs/2305.19116)

-- lifetime

-- CKM (V_{us}): $\tau^- \rightarrow K^- (\dots) \nu$

Electroweak sector

--Lepton Universality

Beyond Standard Model

--LFV

• $\tau^- \rightarrow \ell^- \phi$ [arXiv:2305.04759](https://arxiv.org/abs/2305.04759)

• $\tau^- \rightarrow \ell^- \alpha$ [PRL 130, 181803](https://arxiv.org/abs/1803.18180)

• $\tau \rightarrow 3\ell, \ell \gamma, \ell \rho, \ell^- K_S^0, \Lambda \pi$

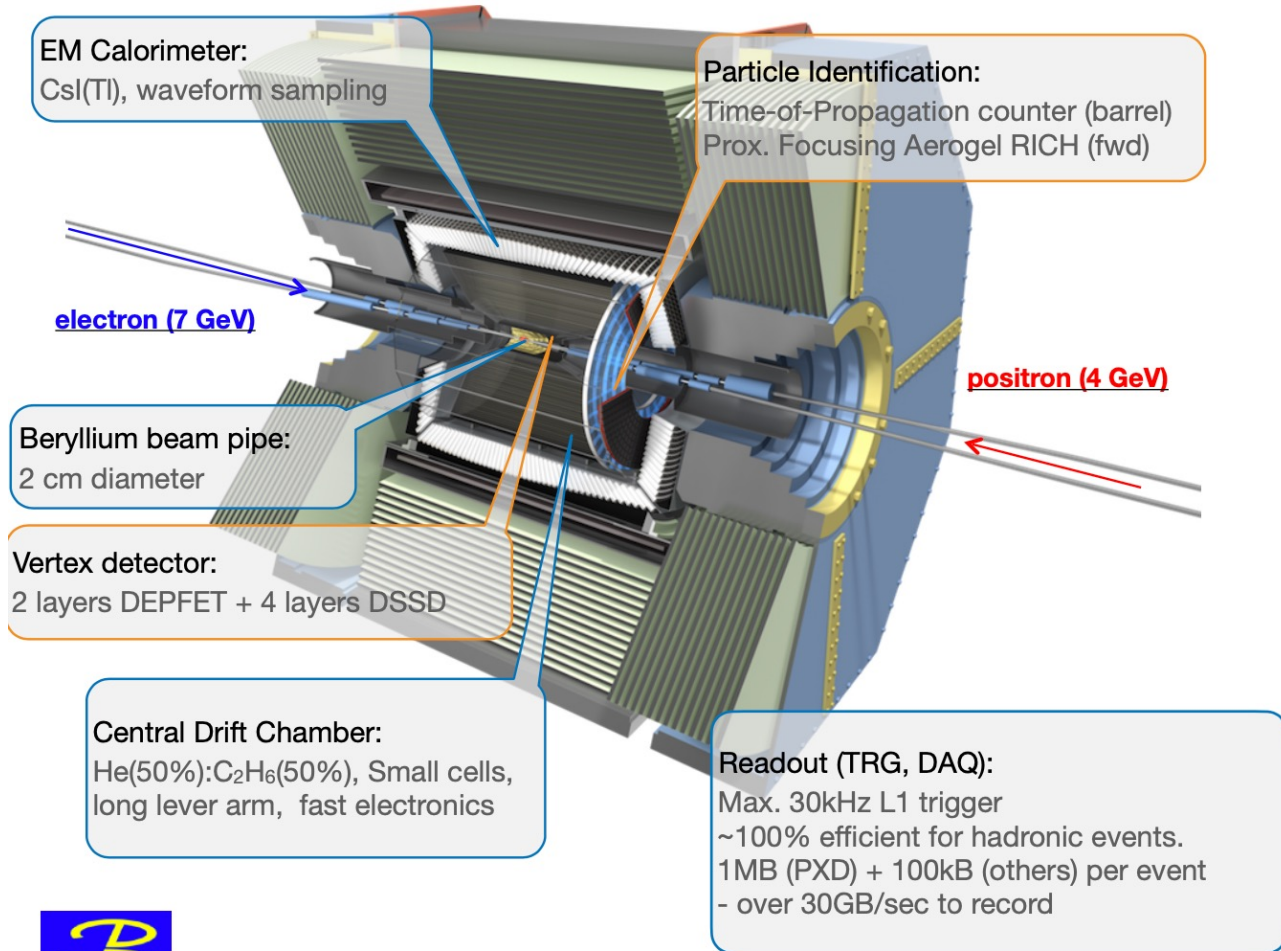
-- CP Violation

$\tau \rightarrow K_S^0 \pi \nu, 3h\nu$

-- CP/T: EDM and MDM

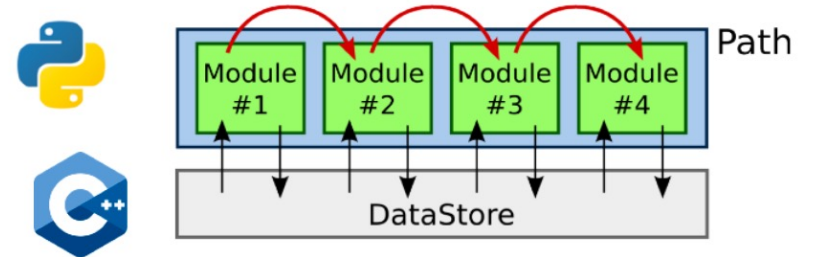
Backup:

In a nutshell

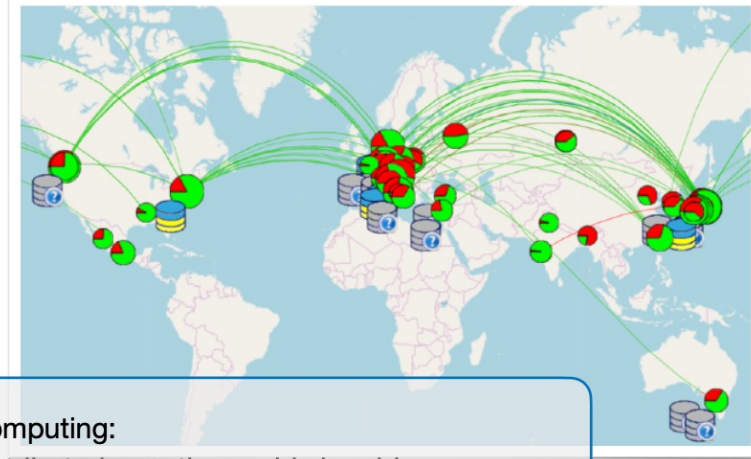


[arXiv:1011.0352 \[physics.ins-det\]](https://arxiv.org/abs/1011.0352)

Software:
Open-source sophisticated algorithms for simulation, reconstruction, visualization, and analysis.



[Comput. Softw. Big Sci. 3 1 \(2019\)](#)



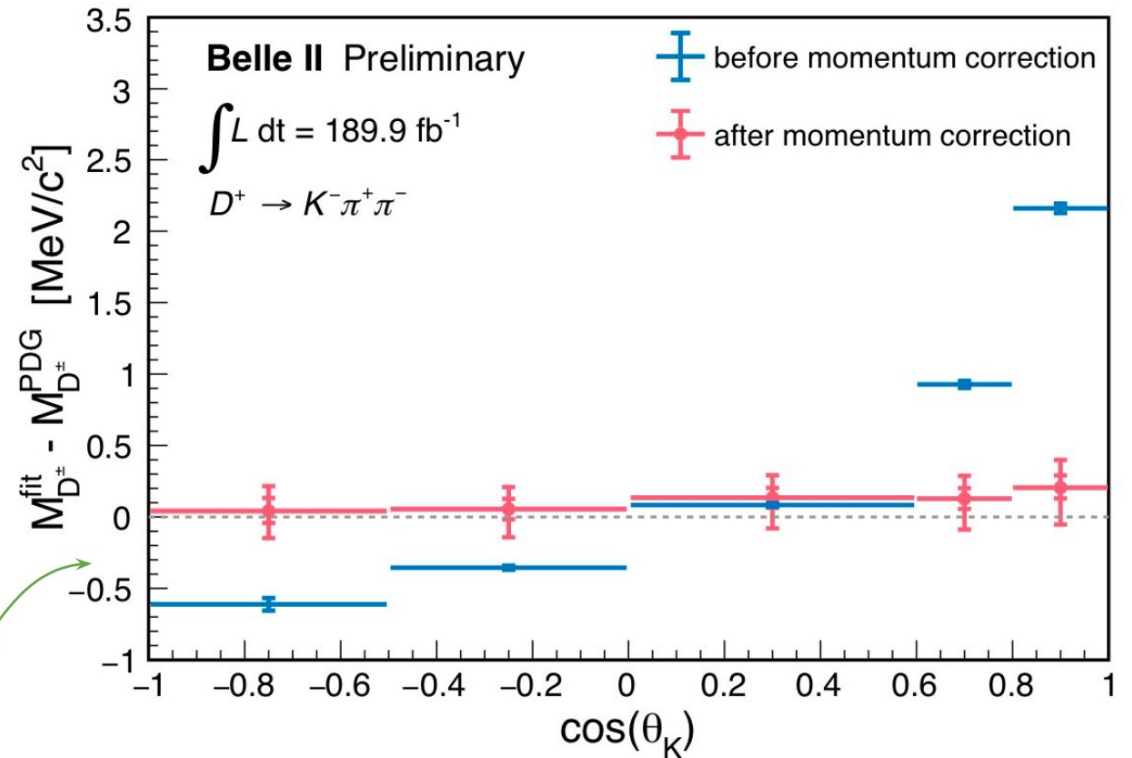
Computing:
Distributed over the world via grid.

Backup:

Tau mass systematics: momentum scale

$$M_{\min} = \sqrt{M_{3\pi}^2 + 2(\sqrt{s}/2 - E_{3\pi}^*)(E_{3\pi}^* - P_{3\pi}^*)}$$

- Momentum of the 3π 's is an important ingredient in the M_{\min} !
- We use $D^0 \rightarrow K\pi$ as a standard candle!
 - get scale factors (SF) for K and π based on difference in peak position and PDG value of D^0
 - phase-space dependent SFs: as a function of charge and $\cos(\theta)$ of the tracks
 - various systematic effects included for the SF's:
 - $m(D^0)$ PDG uncertainty
 - peak position modelling
 - additional kinematical dependence
 - detector misalignment
- Use other mass peaks as cross check:
 $D^0 \rightarrow K\pi\pi\pi, J/\psi \rightarrow \mu\mu, K_S^0 \rightarrow \pi\pi, D^\pm \rightarrow K\pi\pi$



⇒ impact on tau mass: 0.06 MeV

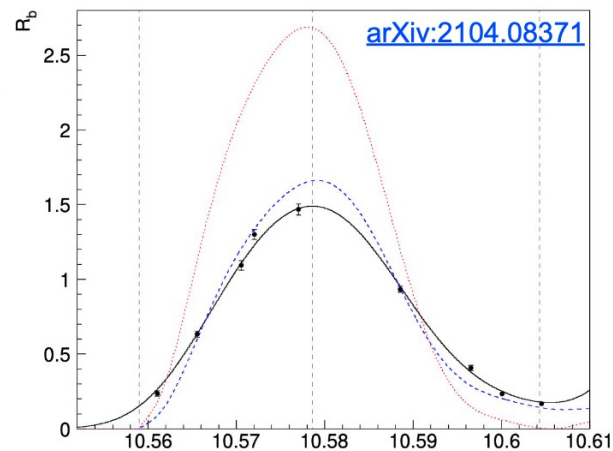
Backup:

Tau mass systematics: energy scale

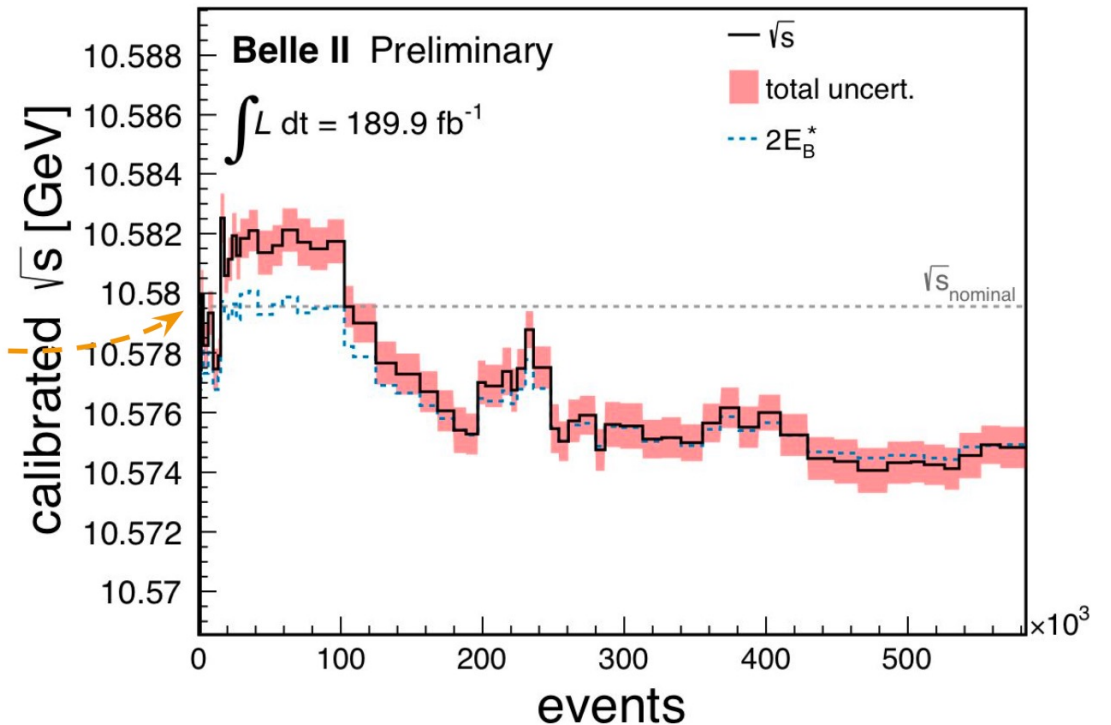
- Center-of-mass collision energy (\sqrt{s}):
 - used to approximate the energy of the tau
- Use energy of fully reconstructed B mesons (E_B^*) to calibrate \sqrt{s}
 - E_B^* only approximately equals \sqrt{s} , need extra corrections due to subtle effects from:
 - ISR photons
 - spread of the beam energy
 - dependence of $\Upsilon(4S)$ cross section on the beam energy:

e.g when \sqrt{s} is below the $\Upsilon(4S)$ peak, due to the beam-energy spread, we produce:

- less low energy B mesons
 - more high energy B's
- ⇒ resulting in a bias in E_B^* values towards the $\Upsilon(4S)$ peak



$$M_{\min} = \sqrt{M_{3\pi}^2 + 2(\sqrt{s}/2 - E_{3\pi}^*)(E_{3\pi}^* - P_{3\pi}^*)}$$



⇒ impact on tau mass: 0.07 MeV

Backup:

- The method:

- Use an empirical fit function to extract the mass:

$$F(M_{\min}) = 1 - P_3 \cdot \arctan\left(\frac{M_{\min} - P_1}{P_2}\right) + P_4(M_{\min} - P_1) + P_5(M_{\min} - P_1)^2$$

- P_1 : depends on the position of threshold
- P_2 : the slope of the threshold
- P_3 - P_5 : the shape away the threshold

- P_1 is an estimator of tau mass!

- This is a biased estimator of 0.40 MeV, determined from simulation samples, with various generated tau masses
- **~3x smaller bias** compare to Belle and BaBar (they had slightly different parameterizations)
- The bias can also depend on the overall shape of the distribution as well

