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NANJING NORMAL UNIVERSITY

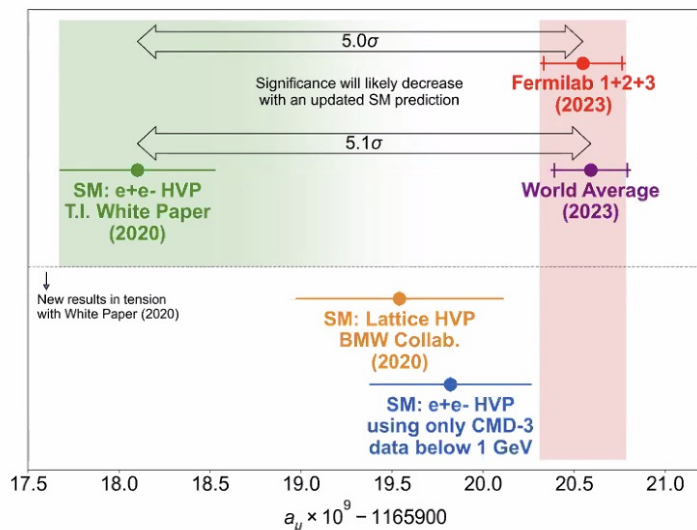
Muon $g-2$
SUSY vs non-SUSY explanations

Peter Athron
(Nanjing Normal University)

As you heard earlier today there is now an updated muon g-2 measurement...

Experiment vs Theory Comparison

- Theory prediction is less clear now, but we can still compare



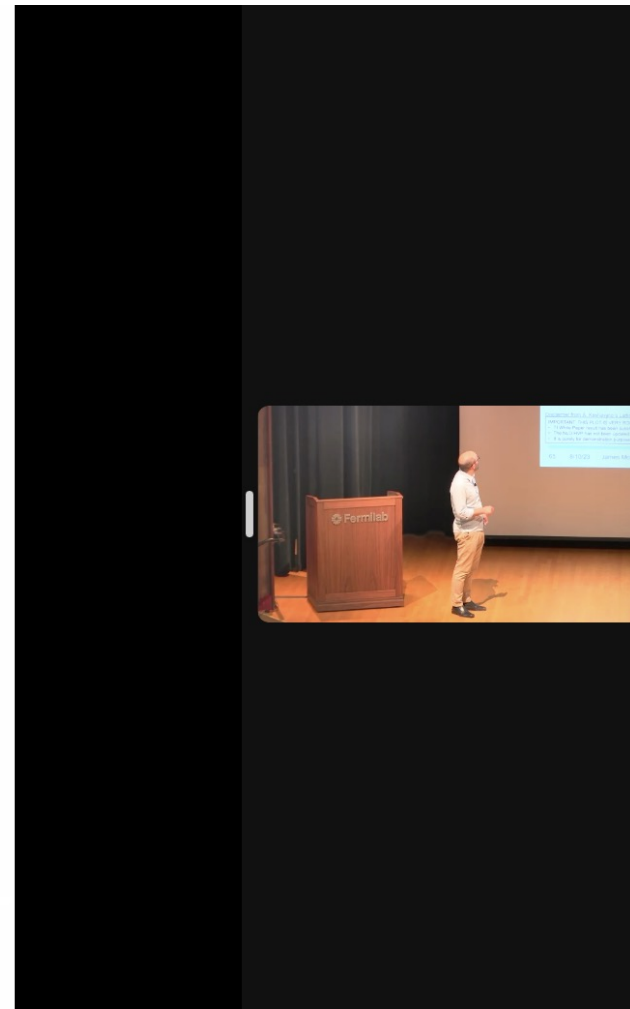
Disclaimer from A. Keshavarzi's Lattice 2023 talk:

IMPORTANT: THIS PLOT IS VERY ROUGH!

- T.I White Paper result has been substituted by CMD-3 only for 0.33 \rightarrow 1.0 GeV.
- The NLO HVP has not been updated.
- It is purely for demonstration purposes \rightarrow should not be taken as final!

Following A. Keshavarzi at Lattice 2023...

- Substitute **CMD-3** data for HVP below 1 GeV
- Cherry-picking one experiment but gives a bounding case
- **SND2k** cannot be processed in this way, but would fall closer to WP (2020).
- Many **parallel efforts are underway** to resolve the theoretical ambiguity



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New world average $a_{\mu}^{2023} = (116592059 \pm 22) \times 10^{-11}$

Deviation to SM estimates

$$\Delta a_{\mu}^{2021} = (25.1 \pm 5.9) \times 10^{-10} \Rightarrow 4.2\sigma \text{ deviation}$$

$$\Delta a_{\mu}^{2023-\text{WP}} = (24.9 \pm 4.8) \times 10^{-10} \Rightarrow 5.1\sigma \text{ deviation}$$

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central value didn't change much, so results would just become sharper

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I can't help much here, but...

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Regardless of the outcome muon $g-2$ has **very important** implications for **new physics**

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Scenarios where we **explain muon g-2** would be **precisely** those that are **ruled out** only by muon g-2 if the lattice results agree with the measurement.

Minimal models for muon g-2: 1 field extensions

Model	Spin	$SU(3)_C \times SU(2)_L \times U(1)_Y$	Result for $\Delta a_\mu^{\text{BNL}}, \Delta a_\mu^{2021}$
1	0	(1, 1, 1)	Excluded: $\Delta a_\mu < 0$
2	0	(1, 1, 2)	Excluded: $\Delta a_\mu < 0$
3	0	(1, 2, -1/2)	Updated in Sec. 3.2
4	0	(1, 3, -1)	Excluded: $\Delta a_\mu < 0$
5	0	($\bar{3}$, 1, 1/3)	Updated Sec. 3.3.
6	0	($\bar{3}$, 1, 4/3)	Excluded: LHC searches
7	0	($\bar{3}$, 3, 1/3)	Excluded: LHC searches
8	0	(3, 2, 7/6)	Updated Sec. 3.3.
9	0	(3, 2, 1/6)	Excluded: LHC searches
10	1/2	(1, 1, 0)	Excluded: $\Delta a_\mu < 0$
11	1/2	(1, 1, -1)	Excluded: Δa_μ too small
12	1/2	(1, 2, -1/2)	Excluded: LEP lepton mixing
13	1/2	(1, 2, -3/2)	Excluded: $\Delta a_\mu < 0$
14	1/2	(1, 3, 0)	Excluded: $\Delta a_\mu < 0$
15	1/2	(1, 3, -1)	Excluded: $\Delta a_\mu < 0$
16	1	(1, 1, 0)	Special cases viable
17	1	(1, 2, -3/2)	UV completion problems
18	1	(1, 3, 0)	Excluded: LHC searches
19	1	($\bar{3}$, 1, -2/3)	UV completion problems
20	1	($\bar{3}$, 1, -5/3)	Excluded: LHC searches
21	1	($\bar{3}$, 2, -5/6)	UV completion problems
22	1	($\bar{3}$, 2, 1/6)	Excluded: $\Delta a_\mu < 0$
23	1	($\bar{3}$, 3, -2/3)	Excluded: proton decay

2HDM →

Scalar
leptoquarks {

Dark
photon →

EXCLUDED

From:
JHEP 09 (2021) 080,
[PA, C.Balázs, D.H.J. Jacob,
W. Kotlarski, D. Stöckinger,
H. Stöckinger-Kim]

Builds on:

- JHEP 05 (2014) 145 [A. Freitas, J. Lykken, S. Kell & S. Westhoff],
- Phys. Rev. D 89 (2014) 095024 [F. S. Queiroz & W. Shepherd]
- JHEP 10 (2016) 002 [C. Biggio, M. Bordone, L. Di Luzio & G. Ridolfi],
- JHEP 10 (2016) 002 [C. Biggio & M. Bordone],
- JHEP 09 (2017) 112 [K. Kowalska & E. M. Sessio]

Minimal models for muon g-2: 2 fields, different spin

$(SU(3)_C \times SU(2)_L \times U(1)_Y)_{\text{spin}}$	$+\mathbb{Z}_2$	Result for $\Delta a_\mu^{\text{BNL}}, \Delta a_\mu^{2021}$
$(\mathbf{1}, \mathbf{1}, 0)_0 - (\mathbf{1}, \mathbf{1}, -1)_{1/2}$	No Yes	Projected LHC 14 TeV exclusion, not confirmed Updated Sec. 4.2
$(\mathbf{1}, \mathbf{1}, -1)_0 - (\mathbf{1}, \mathbf{1}, 0)_{1/2}$	Both	Excluded: $\Delta a_\mu < 0$
$(\mathbf{1}, \mathbf{2}, -1/2)_0 - (\mathbf{1}, \mathbf{1}, 0)_{1/2}$	Both	Excluded: $\Delta a_\mu < 0$
$(\mathbf{1}, \mathbf{1}, 0)_0 - (\mathbf{1}, \mathbf{2}, -1/2)_{1/2}$	No Yes	Excluded: LHC searches Updated Sec. 4.2
$(\mathbf{1}, \mathbf{2}, -1/2)_0 - (\mathbf{1}, \mathbf{1}, -1)_{1/2}$	No Yes	Excluded: LEP contact interactions Viable with under abundant DM
$(\mathbf{1}, \mathbf{1}, -1)_0 - (\mathbf{1}, \mathbf{2}, -1/2)_{1/2}$	Both	Excluded: $\Delta a_\mu < 0$
$(\mathbf{1}, \mathbf{2}, -1/2)_0 - (\mathbf{1}, \mathbf{2}, -1/2)_{1/2}$	Both	Excluded: LEP search
$(\mathbf{1}, \mathbf{2}, -1/2)_0 - (\mathbf{1}, \mathbf{3}, 0)_{1/2}$	No Yes	Excluded: LHC searches Viable with under abundant DM
$(\mathbf{1}, \mathbf{2}, -1/2)_0 - (\mathbf{1}, \mathbf{3}, -1)_{1/2}$	No Yes	Excluded: LHC searches + LEP contact interactions Viable with under abundant DM
$(\mathbf{1}, \mathbf{3}, 0)_0 - (\mathbf{1}, \mathbf{2}, -1/2)_{1/2}$	Both	Excluded: $\Delta a_\mu < 0$
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$(\mathbf{1}, \mathbf{1}, -1)_{1/2} - (\mathbf{1}, \mathbf{1}, 0)_1$	No	Excluded: $\Delta a_\mu < 0$
$(\mathbf{1}, \mathbf{2}, -1/2)_{1/2} - (\mathbf{1}, \mathbf{1}, 0)_1$	No	Excluded: $\Delta a_\mu < 0$
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Why so difficult?

Many extensions **ruled out** by: I) **wrong sign**: corrections **only decrease** muon g-2
II) Tension with collider experiments

$$\Delta a_{\mu}^{2021} = (25.1 \pm 5.9) \times 10^{-10}$$

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Typically $C_{\text{BSM}} \rightarrow$ loop suppression $\times \mathcal{O}(1)$ function of mass ratios.

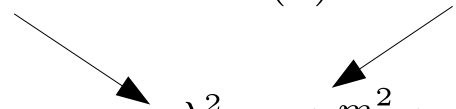
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e.g. scalar leptoquark with
 $L_{LQ} = -\lambda Q_3 \cdot L_2 S_1 + \text{h.c.}$

$$C_{\text{SLQ}} = \frac{\lambda^2}{64\pi^2} E\left(\frac{m_t^2}{m_{S_1}^2}\right)$$


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For $\lambda = 3, E = 1$
 $\Rightarrow M_{\text{BSM}} \approx 250 \text{ GeV}$

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→ Generic scale of BSM physics explaining muon g-2 already probed by LHC, etc

Naive solutions have big tension between muon g-2 and collider limits

Try to evade limits with compressed spectra

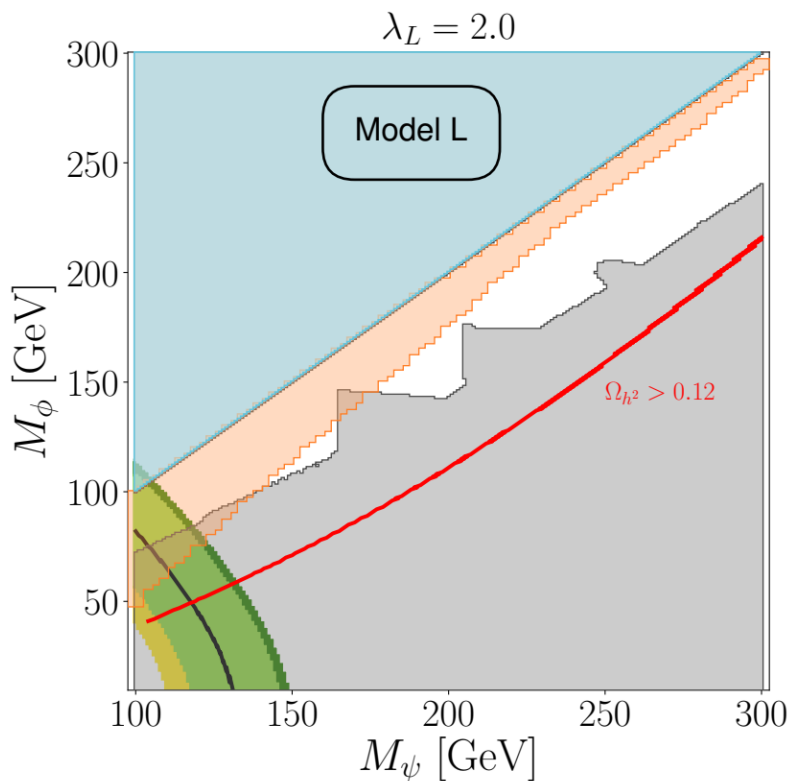
Simple extension with scalar singlet and charged fermion doublet

$$\mathcal{L}_L = (\lambda_L L \cdot \psi_d \phi - M_\psi \psi_d^c \psi_d + h.c.) - \frac{M_\phi^2}{2} |\phi|^2, \quad C_{\text{BSM}} = \frac{\lambda^2}{3 \times 64 \Pi^2} E\left(\frac{m_\psi^2}{m_\phi^2}\right)$$

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Fitting
2021 Muon g-2

Now Ruled Out

Still viable

Now viable

**FlexibleSUSY 2.5.0
for muon g-2**

For $\lambda_L = 2, E = 1$

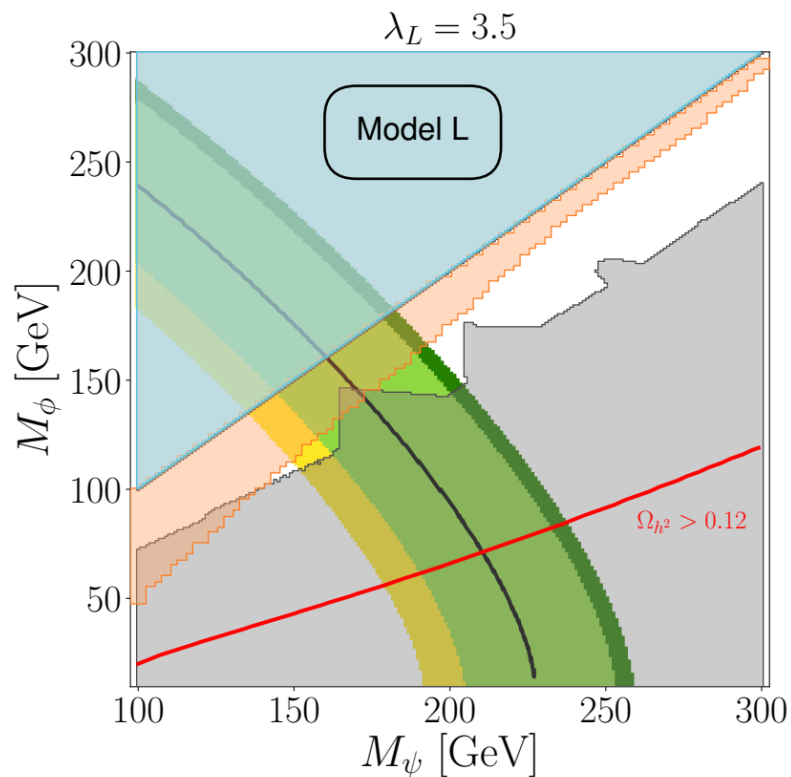
$\Rightarrow M_{\text{BSM}} \approx 100 \text{ GeV}$

Excluded by compressed
spectra searches

Try to evade limits with compressed spectra

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For $\lambda_L = 3.5, E = 1$

$\Rightarrow M_{\text{BSM}} \approx 170 \text{ GeV}$

Just finds gaps in exclusion
for compressed spectra?

No simultaneous solution with DM

Only solutions hide in the gaps

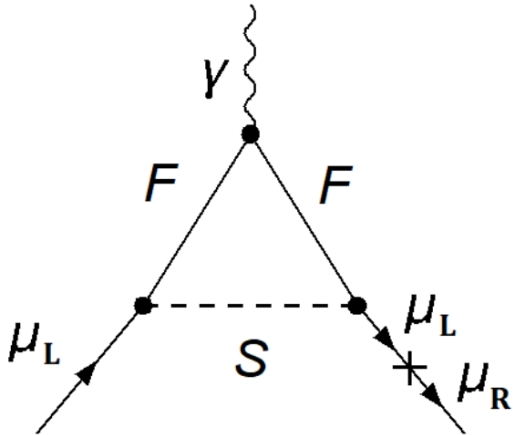
Chirality flipping enhancements

Muon g-2 is a chirality flipping operator

$$\Delta a_{\mu}^{\text{BSM}} \approx C_{\text{BSM}} \frac{m_{\mu}^2}{M_{\text{BSM}}^2}$$

← One factor of muon mass for chirality flip on outgoing muon

e.g.



Chirality flipping enhancements

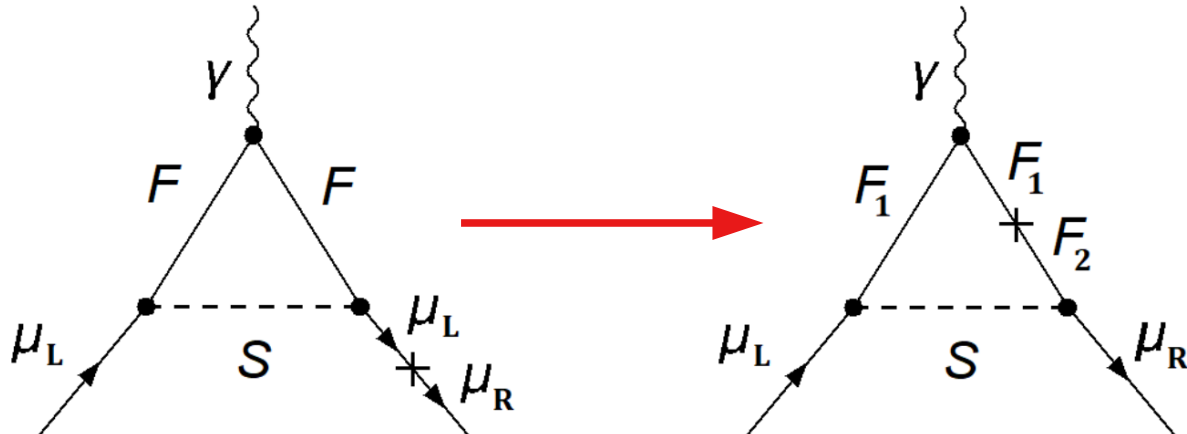
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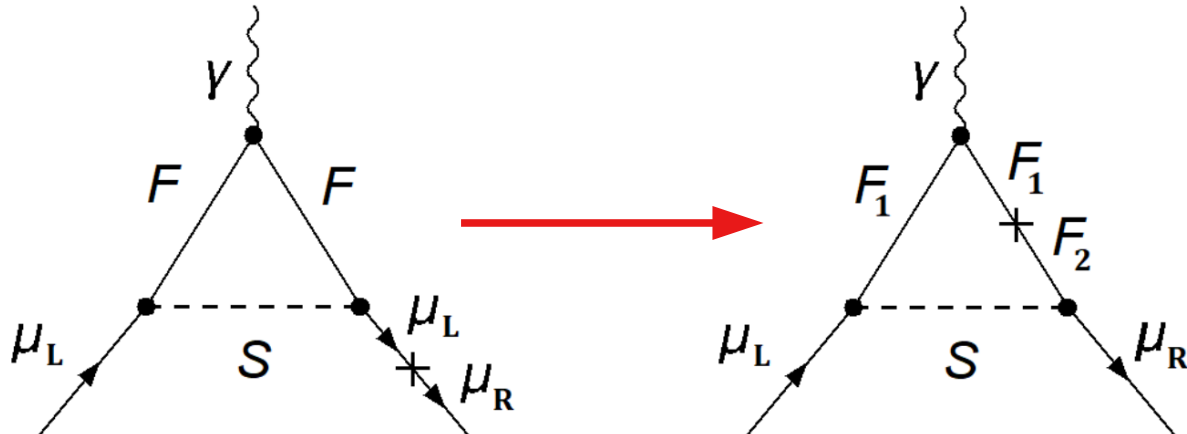
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→ Enhancement to BSM corrections from an internal chirality flip $C_{\text{BSM}} \propto \frac{M_{CF}}{m_{\mu}}$

e.g.



$$m_{\mu} \rightarrow M_{CF}$$

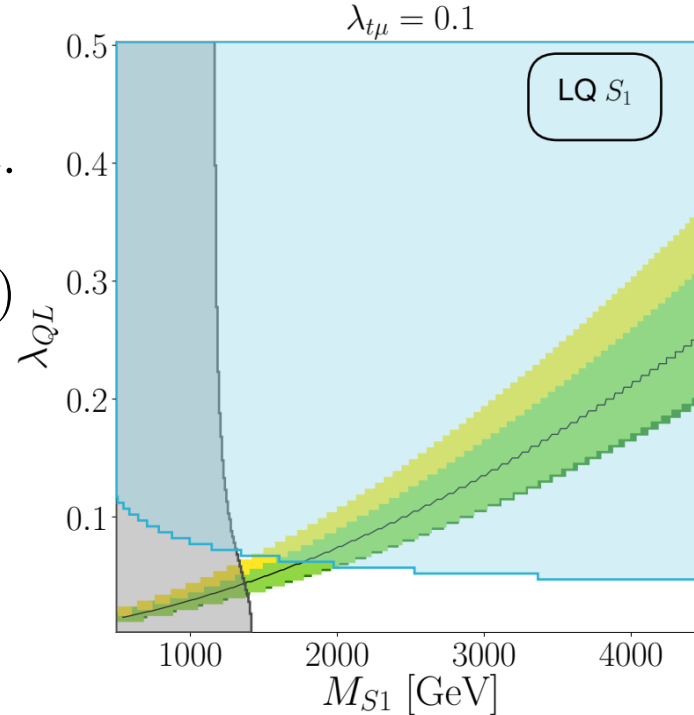
Chirality flipping enhancements

Scalar leptoquark with left and right couplings

$$\mathcal{L}_{SLQ-S_1} = -\lambda_{QL} Q_3 \cdot L_2 S_1 - \lambda_{t\mu} t\mu S_1^* + h.$$

$\longrightarrow C_{\text{BSM}} \approx Q_t \lambda_L \lambda_R m_t / (8\pi^2 m_\mu)$
 $m_t / m_\mu \approx 1600$

Huge chirality flipping enhancement:
easy to explain muon g-2 with large masses



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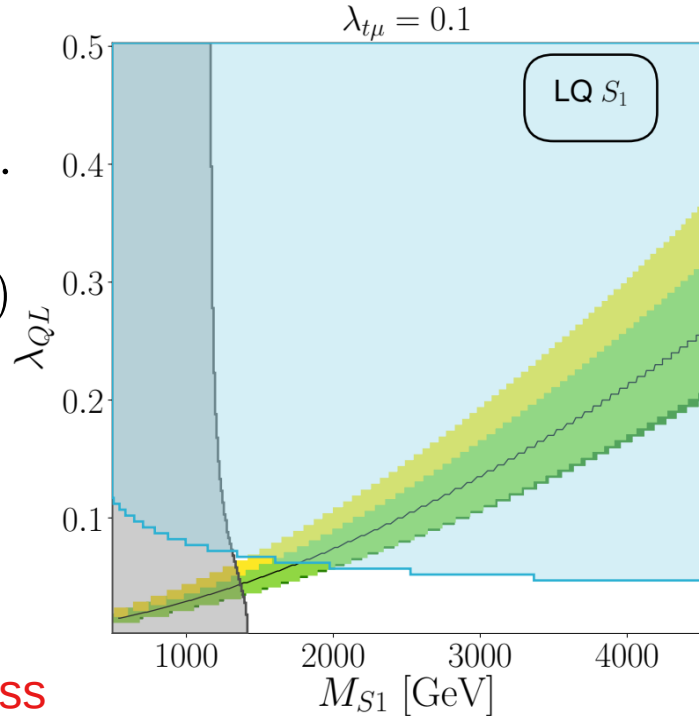
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But hard to avoid fine tuning in the muon mass

Typically $\Delta a_\mu^{\text{BSM}} \approx \mathcal{O}(\Delta m_\mu / m_\mu) \frac{m_\mu^2}{M_{\text{BSM}}^2}$

Enhancement in muon mass
 corrections too

**FlexibleSUSY 2.5.0
 for muon g-2**



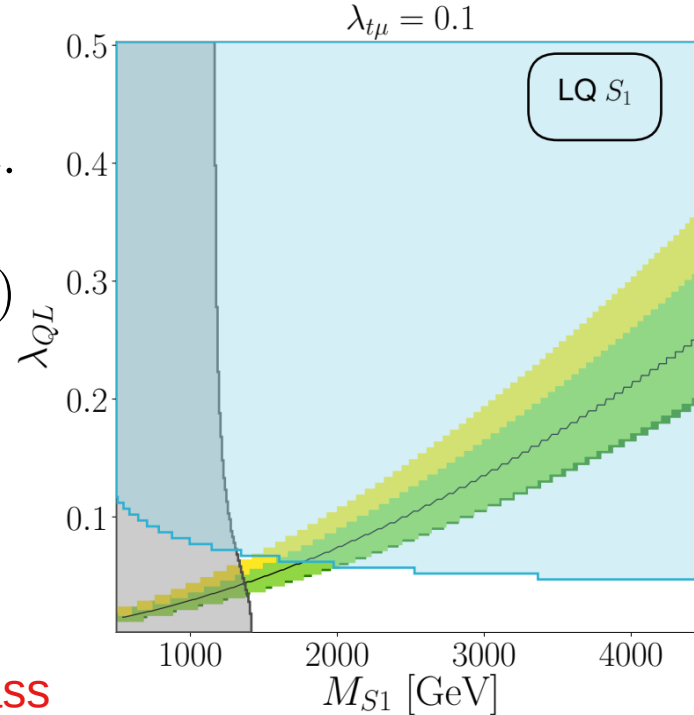
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Testable with $BR(h \rightarrow \mu^+ \mu^-)$ at the CEPC

Enhancement in muon mass
corrections too

**FlexibleSUSY 2.5.0
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Muon $g-2$ and CDF MW?

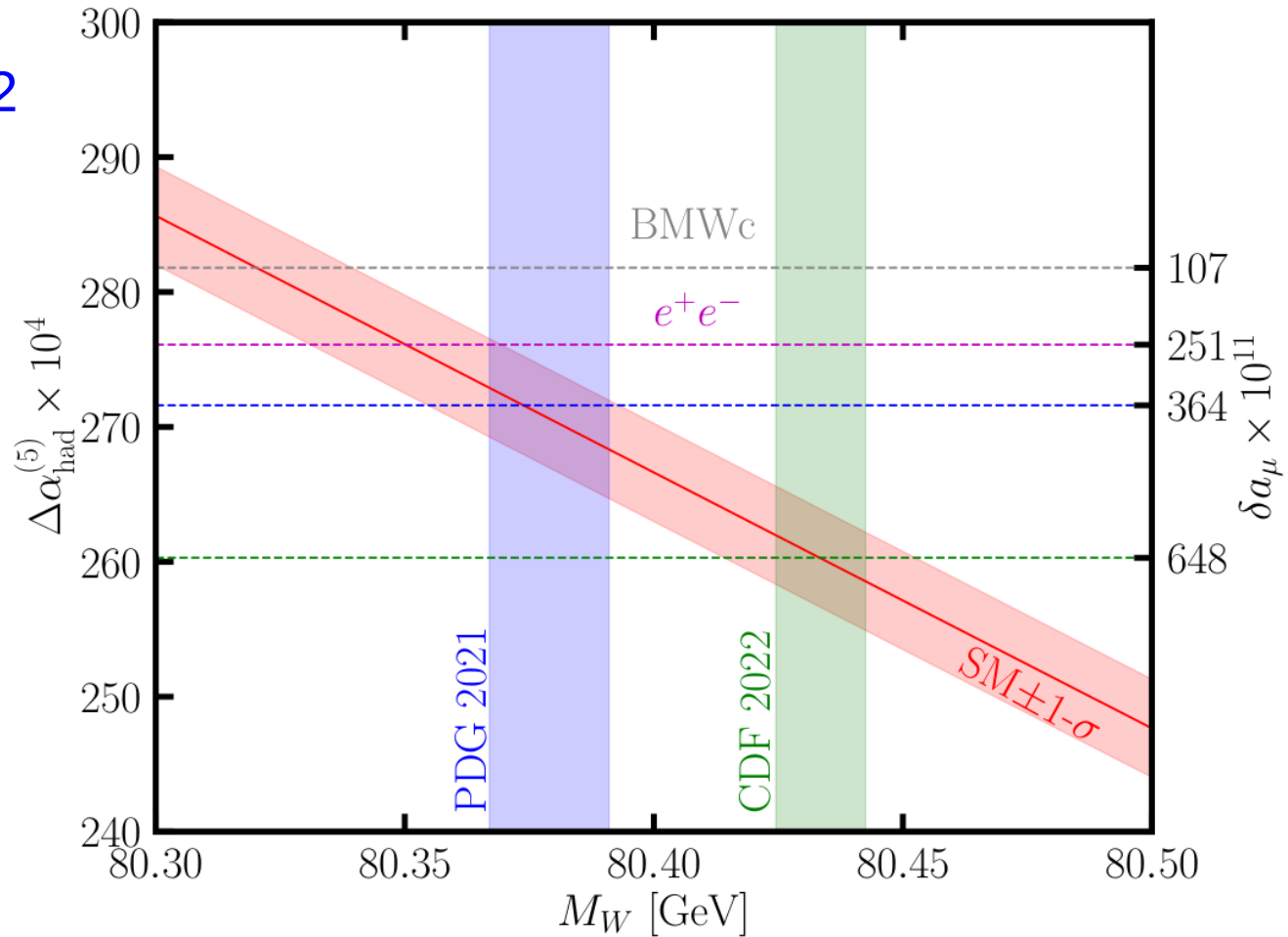
Global EW fit Tension

[Nature Commun. 14 (2023) 659, PA, A. Fowlie, C.-T. Lu, L. Wu, Y. Wu, B. Zhu]

The W mass and muon $g-2$ pull in opposite directions

Red EW fit band cannot agree with both muon $g-2$ and CDF M_W

Very hard for a change in the hadronic cross section to explain both



Simultaneous BSM explanation of MW and muon g-2

[arXiv:2204.03996,PA, A. Fowlie, C.-T. Lu, L. Wu, Y. Wu, B. Zhu]

Two scalar leptoquarks that mix together (proof of principle)

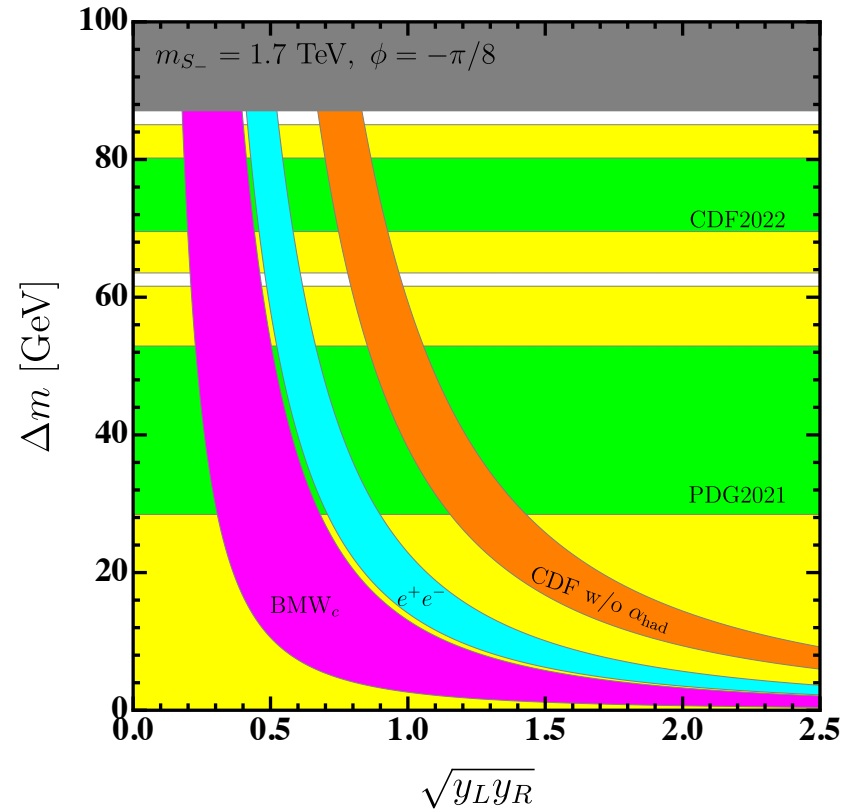
$$S_1 (\bar{\mathbf{3}}, \mathbf{1}, 1/3)$$

$$S_3 (\bar{\mathbf{3}}, \mathbf{3}, 1/3)$$

$$\mathcal{L}_{S_1 \& S_3} = \mathcal{L}_{\text{mix}} + \mathcal{L}_{\text{LQ}},$$

$$\mathcal{L}_{\text{mix}} = \lambda H^\dagger \left(\vec{\tau} \cdot \vec{S}_3 \right) H S_1^* + \text{h.c.}$$

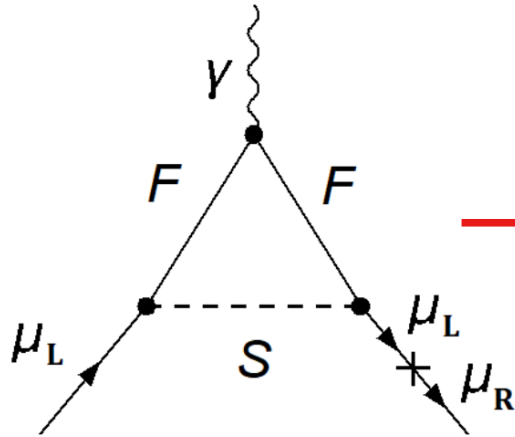
$$\begin{aligned} \mathcal{L}_{\text{LQ}} &= y_R^{ij} \bar{u}_{Ri}^C e_{Rj} S_1 \\ &+ y_L^{ij} \bar{Q}_i^C i\tau_2 \left(\vec{\tau} \cdot \vec{S}_3 \right) L_j + \text{h.c.} \end{aligned}$$



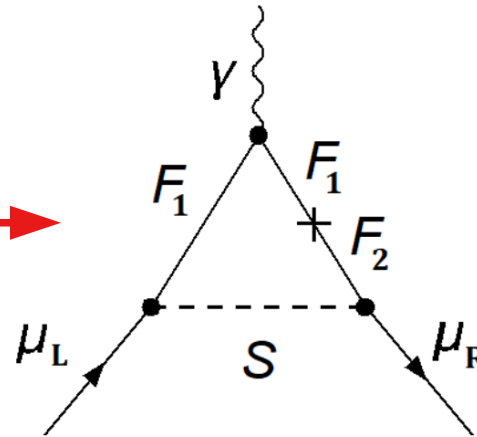
Muon $g-2$ and Dark Matter?

Chirality flipping enhancements

To explain DM and have a chirality flipping enhancement,
need 3 BSM fields



2 fields of opposite sign
(no internal chirality flip)



Add third field
(internal chirality flip)

$$m_\mu \rightarrow M_{CF}$$

Heavy new physics for DM and muon g-2

Scalar doublet

Scalar singlet

Charged fermion singlet

Example:

$$\mathcal{L}_{2S1F} = (a_H H \cdot \phi_d \phi_s^0 + \lambda_L \phi_d \cdot L \psi_s + \lambda_R \phi_s^0 \mu \psi_s^c - M_\psi \psi_s^c \psi_s + h.c.) - M_{\phi_d}^2 |\phi_d|^2 - \frac{M_{\phi_s}^2}{2} |\phi_s^0|^2.$$

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Mass Mixing between scalars

Left and right couplings to muons

Mass eigenstate coupling to left muon and right muon

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Scalar doublet \rightarrow H
 Scalar singlet \rightarrow ϕ_d, ϕ_s^0
 Charged fermion singlet \rightarrow ψ_s^c

Mass Mixing between scalars \rightarrow a_H
 Left and right couplings to muons \rightarrow λ_L, λ_R

Mass eigenstate coupling to left muon and right muon

$$\Rightarrow \text{Non-zero } a_H + \lambda_L + \lambda_R$$

Heavy new physics for DM and muon g-2

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Scalar doublet \rightarrow ϕ_d
 Scalar singlet \rightarrow ϕ_s^0
 Charged fermion singlet \rightarrow ψ_s^c

Mass Mixing between scalars \rightarrow $a_H H \cdot \phi_d \phi_s^0$
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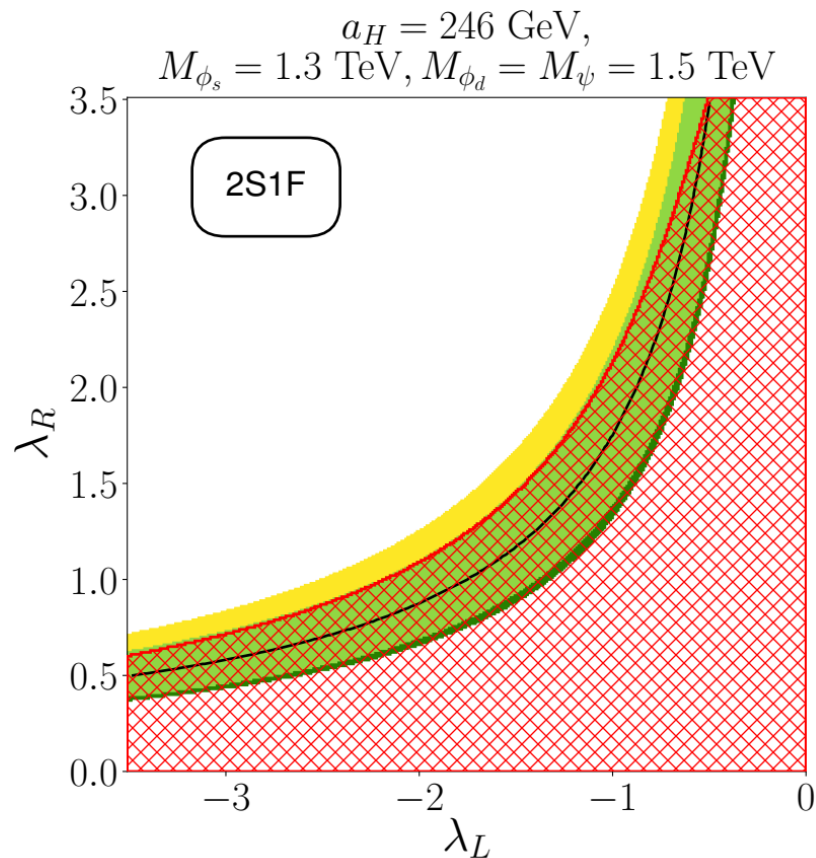
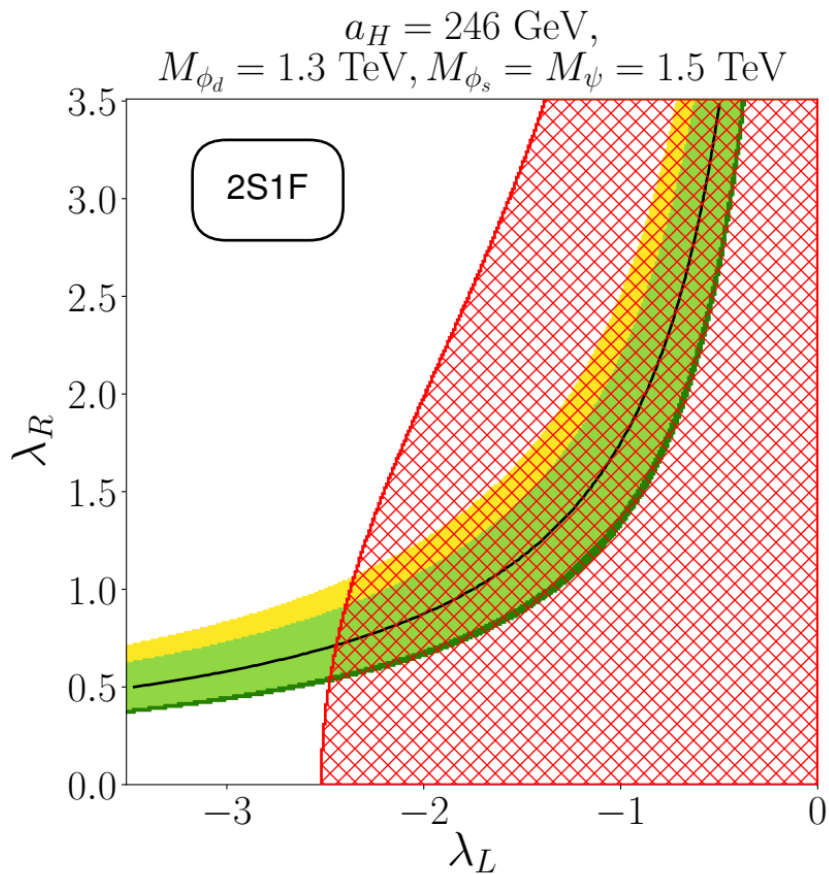
Chirality flip enhancement $\frac{\lambda_L \lambda_R v}{m_\mu} \frac{a_H}{M_\psi}$

Heavy new physics for DM and muon g-2

FlexibleSUSY 2.5.0
for muon g-2

Many params influence relic density (and muon g-2)

→ many situations are possible e.g.



Fitting
2021 Muon g-2

Now Ruled Out

Still viable

Now viable

Exclusions:

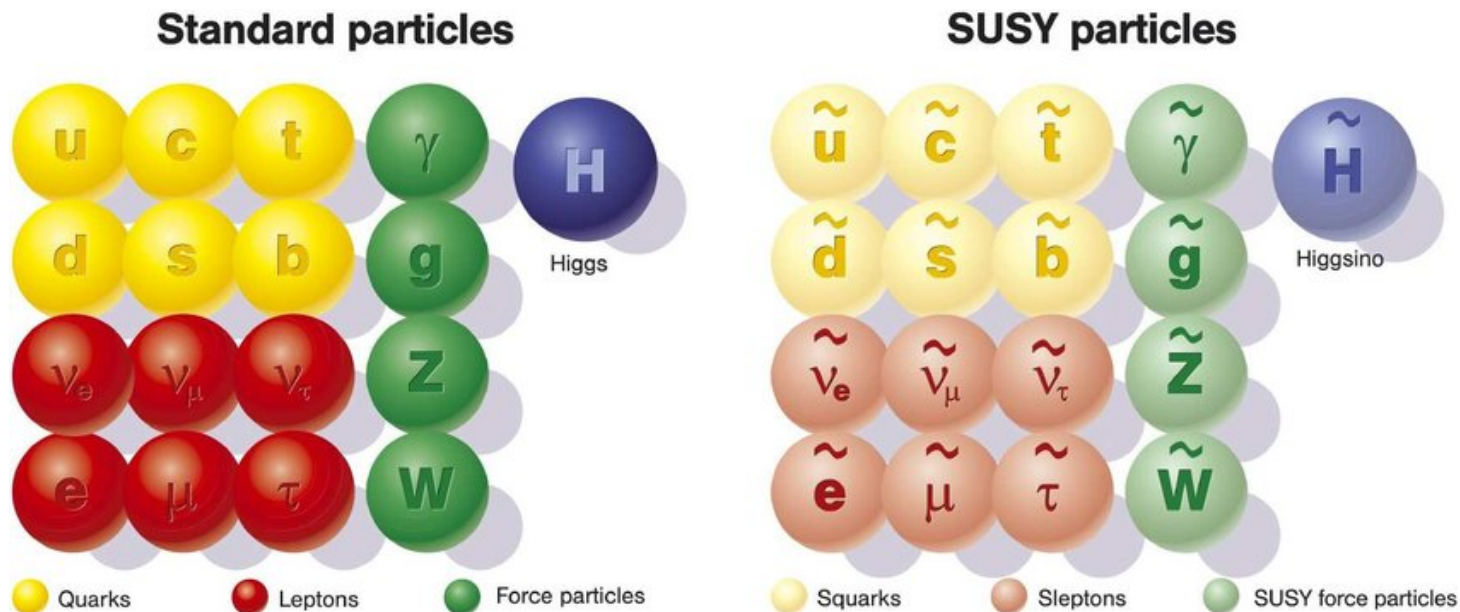
Over Abundant

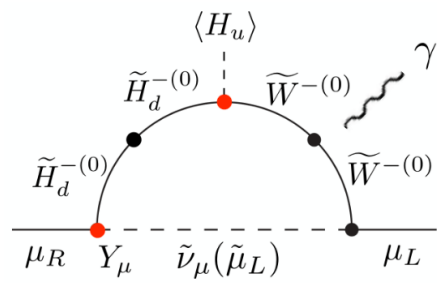
Minimal SUSY (MSSM) solutions

Interest:

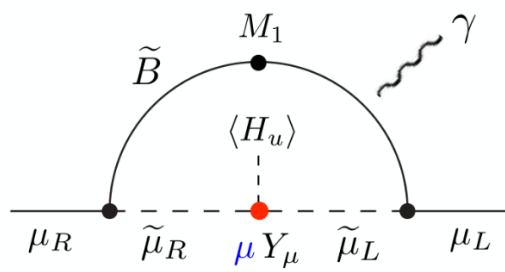
- Well motivated
- Solves Hierarchy Problem
- Has chirality flipping enhancement via $\tan \beta = v_u/v_d$

One-loop contributions from EWinos, smuons and smuon neutrinos

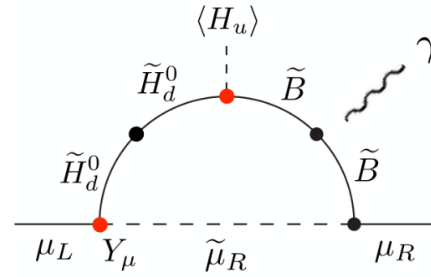




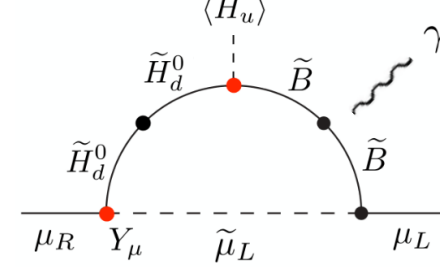
WHL



BLR



BHR



BHL

Four main diagrams with internal chirality flip

All are linear in tan beta

BLR is also linear in mu

WHL and BLR most important for phenomenology

$$a_\mu^{\text{WHL}} \approx 21 \times 10^{-10} \text{sign}(\mu M_2) \left(\frac{500 \text{ GeV}}{M_{\text{SUSY}}} \right)^2 \frac{\tan \beta}{40},$$

$$a_\mu^{\text{BLR}} \approx 2.4 \times 10^{-10} \text{sign}(\mu M_1) \left(\frac{500 \text{ GeV}}{M_{\text{SUSY}}} \right)^2 \frac{\tan \beta}{40} \frac{\mu}{500 \text{ GeV}},$$

$$a_\mu^{\text{BHR}} \approx -2.4 \times 10^{-10} \text{sign}(\mu M_1) \left(\frac{500 \text{ GeV}}{M_{\text{SUSY}}} \right)^2 \frac{\tan \beta}{40}$$

$$a_\mu^{\text{BHL}} \approx 1.2 \times 10^{-10} \text{sign}(\mu M_1) \left(\frac{500 \text{ GeV}}{M_{\text{SUSY}}} \right)^2 \frac{\tan \beta}{40},$$

MSSM solutions

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The main four diagrams could map to three field EFTs similar to previous model but...

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Challenge: Much less freedom than a generic three field model for DM:

→ Interactions fixed to gauge couplings

→ Can't just make the coupling 1 or larger

→ Large $\tan \beta \gtrsim 70$ leads to non-perturbative Yukawas

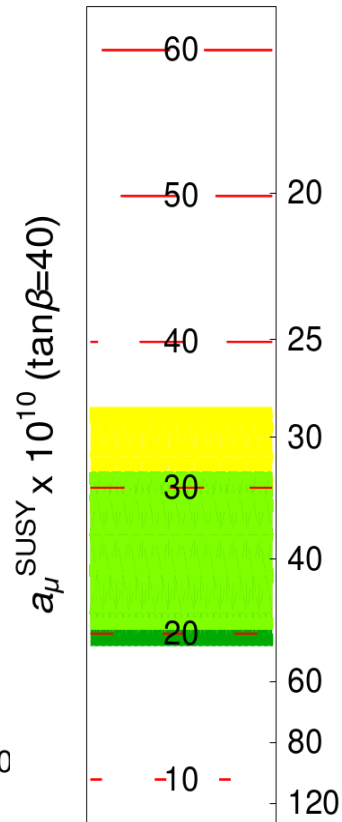
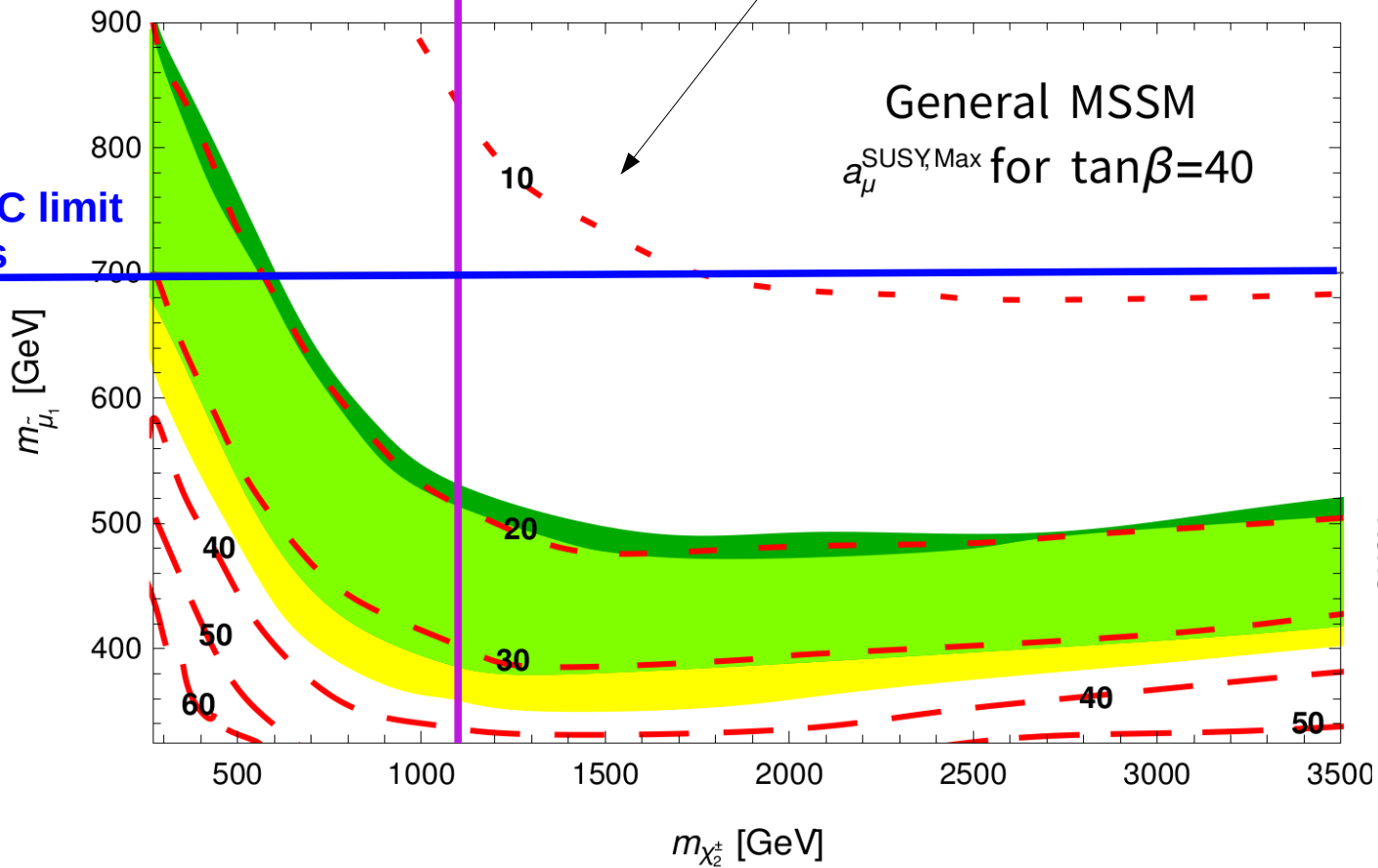
Use GM2Calc for all
MSSM results
State-of-the-art
2-loop corrections

Maximum LHC limit
Chargino mass < 1.1 TeV

“Obviously allowed” region has either:

Too low $\Delta a_\mu^{\text{BSM}}$
Or very large $\tan\beta \gg 40$

Maximum LHC limit
Slepton mass
< 700 GeV



Evading limits on sleptons and charginos

Idea 1: Make sleptons light but close in mass to LSP (compressed spectra again)

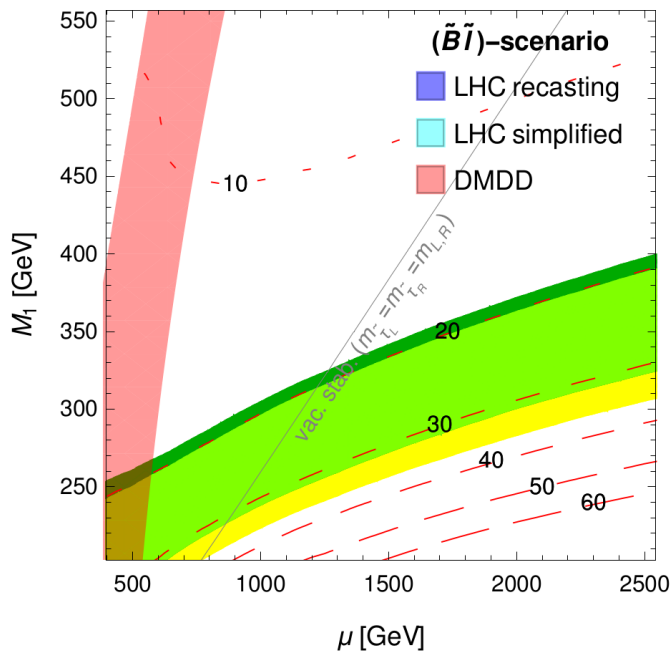
If you accept this tuning to evade collider limits (and deplete DM relic density)

→ Plenty of viable parameter space:

DM also explained

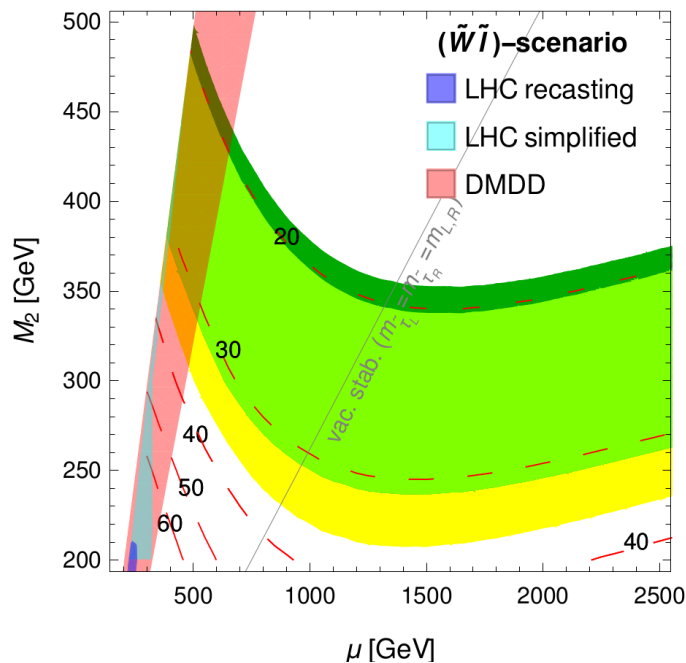
Bino LSP

$m_{L,R} = M_1 + 50 \text{ GeV}$, $M_2 = 1200 \text{ GeV}$, $\tan\beta = 40$



Wino LSP

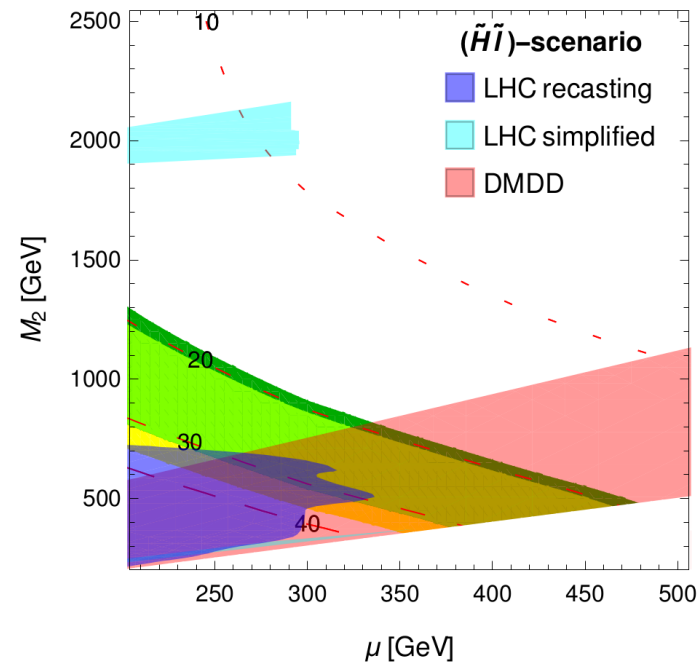
$m_{L,R} = M_2 + 50 \text{ GeV}$, $M_1 = 600 \text{ GeV}$, $\tan\beta = 40$



No DM explanation

Higgsino LSP

$m_{L,R} = \mu + 50 \text{ GeV}$, $M_1 = 2000 \text{ GeV}$, $\tan\beta = 40$

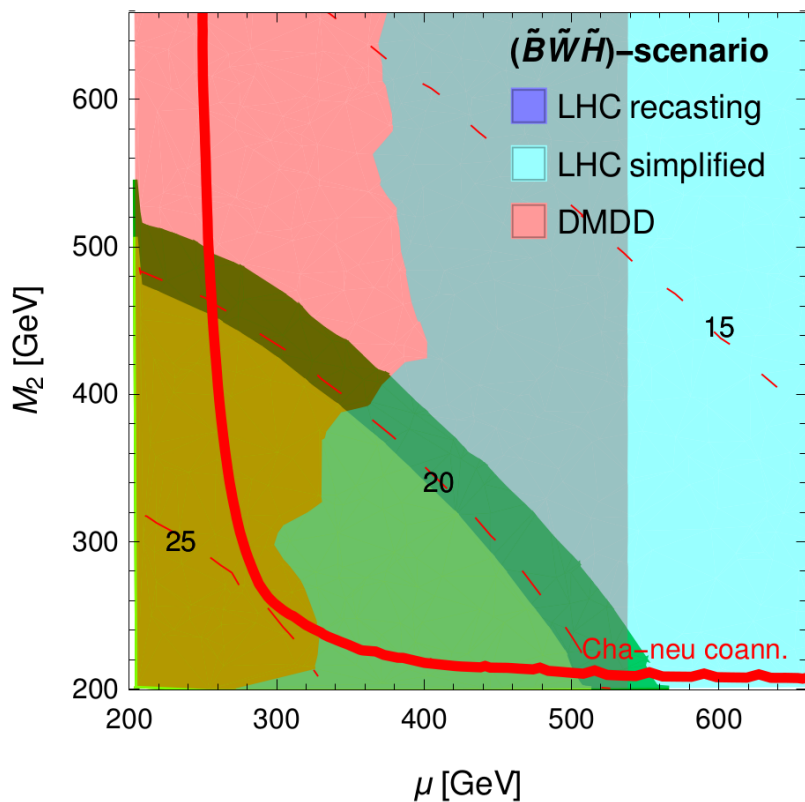


Evading broad limits on sleptons and charginos

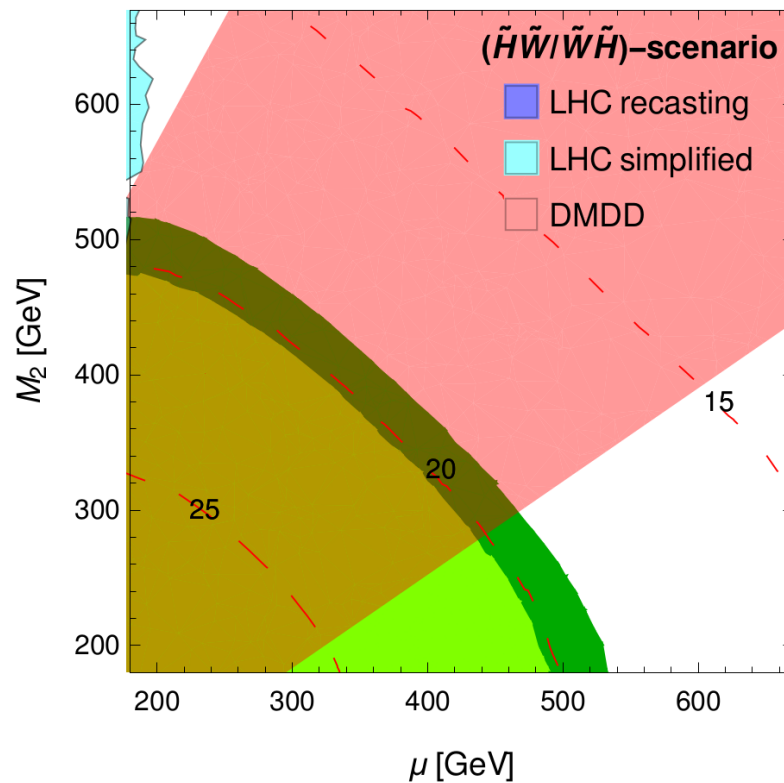
Idea 2: Make charginos lighter than sleptons

Does not assume tuning, but the parameter space is quite constrained

$m_{L,R} = 700 \text{ GeV}$, $M_1 = 200 \text{ GeV}$, $\tan\beta = 40$



$m_{L,R} = 700 \text{ GeV}$, $M_1 = 2000 \text{ GeV}$, $\tan\beta = 40$



Although restrictive there are many ways to explain a large muon $g-2$ deviation

MSSM muon $g-2$ solutions

- Scrape into 2σ region with large $\tan\beta$ close to 50.
- Very large $\tan\beta \gg 50$
- Tune slepton masses so $m_{\tilde{l}} < m_{\text{LSP}} + \Delta m_{\text{LHC-gap}}$
- Choose $m_{\chi_{1,2}^{\pm}} < m_{\tilde{l}}$

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Non-SUSY solutions

- Chirality flip enhancement e.g. leptoquarks,
- Hide from LHC with compressed spectra
- DM can be comfortably explained with 3 or more fields

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My Conclusions and Outlook

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 - There is a large tuning in the muon mass and significant corrections to $h \rightarrow \mu\mu$ that may be targeted with precision Higgs measurements
- Many reasonable models can fit muon $g-2$, but there is still room for new ideas

Back Up Slides

Other Possibilities

There are many other possibilities not covered here.

e.g.

- Axion Like Particles
- Dark Z
- Gauged $U_{(L_\mu - L_\tau)}$
- Vector like leptons (similar to leptoquark solution)
- Next-to-Minimal Supersymmetric Standard Model (NMSSM),
- Flavourful Supersymmetric Standard Model (larger chirality flipping enhancement)
-

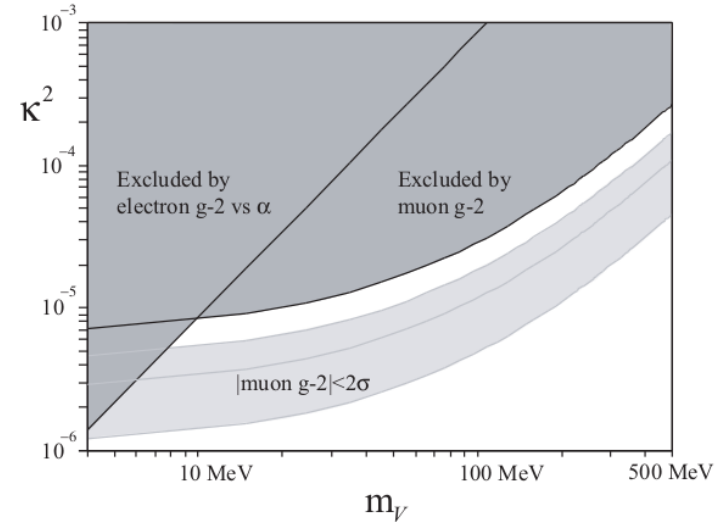
Dark Photon

Original idea: Dark $U(1)_d$ [PRD 80 (2009) 095002]

Kinetic mixing between $U(1)_d$, $U(1)_Y$: $\frac{1}{2}\kappa\tilde{F}^{\mu\nu}F_{\mu\nu}$

Diagonalise $A_\mu \rightarrow A_\mu + \kappa Z_{d\mu}$

→ Induced SM couplings $-e\kappa J_{e.m.}^\mu Z_{d\mu}$



[PRD 80(2009) 095002, M. Pospelov,

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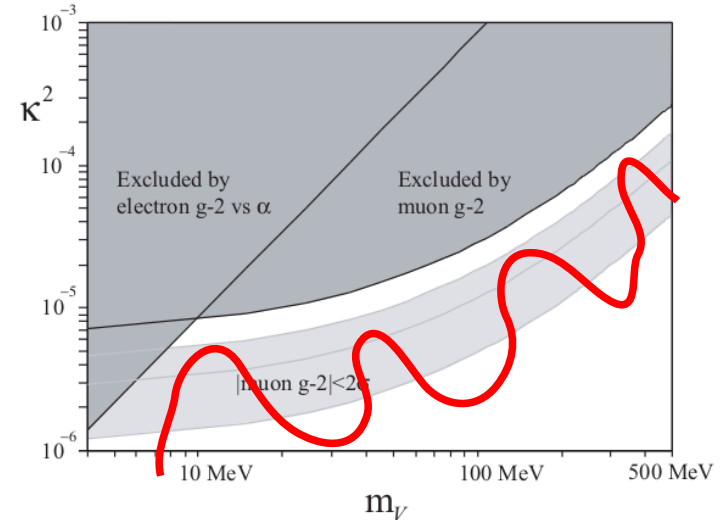
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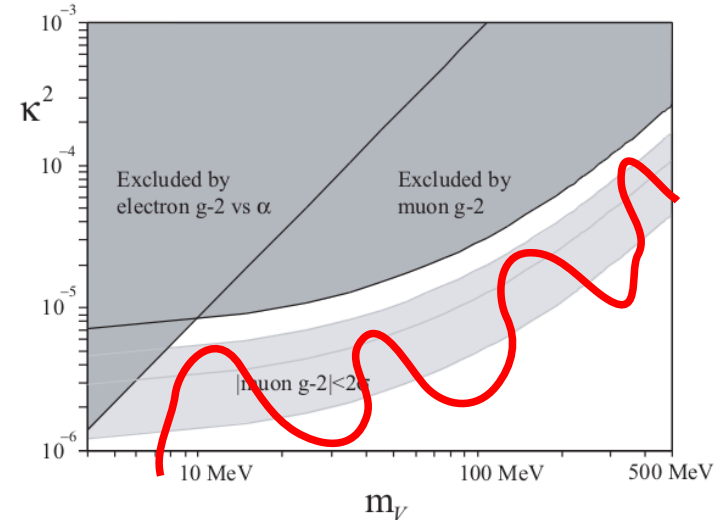
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Extensions of this still viable, e.g.

Dark Z: Include $Z-Z_d$ mixing through EWSB if the Higgs is also charged under $U(1)_d$
[PRL 109(2012) 031802, PRD 86(2012) 095009 Davoudiasl et al, PRD 104(2021) 1, 011701 Cadeddu et al]



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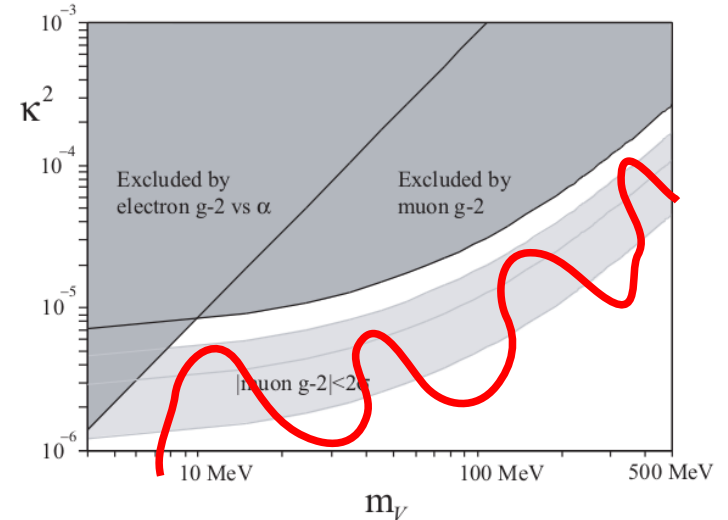
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Semi-visible decays: Dark photon/Z decays into invisible dark sector states + visible SM states
 [PRD 99 (2019) 115001, G. Mohlabeng]



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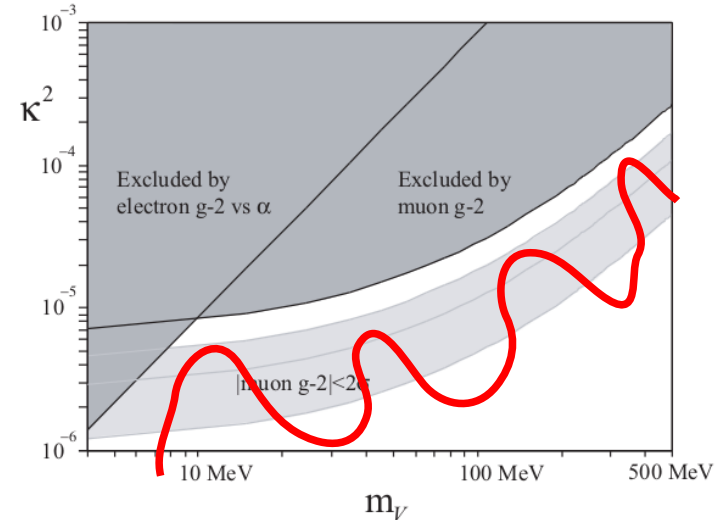
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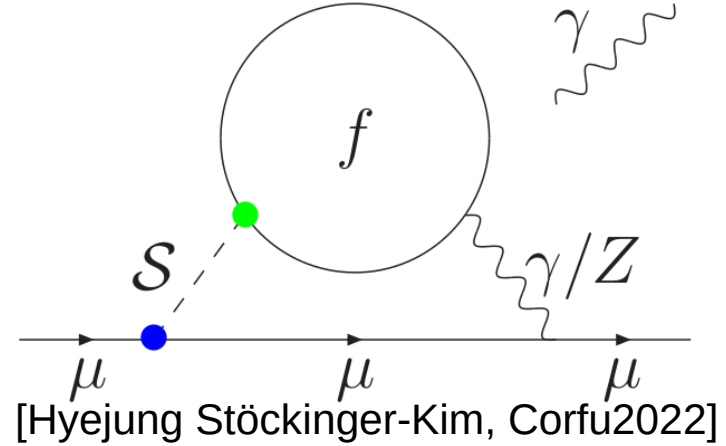
Z' / Gauged $U_{(L_\mu - L_\tau)}$ It could have direct couplings to visible states
 [e.g. PRD 84 (2011) 075007, PRL 113 (2014) 091801, PLB 762 (2016) 389, PRD 103 (2021) 9, 095005]



[PRD 80(2009) 095002, M. Pospelov, + My indicative red overlay]

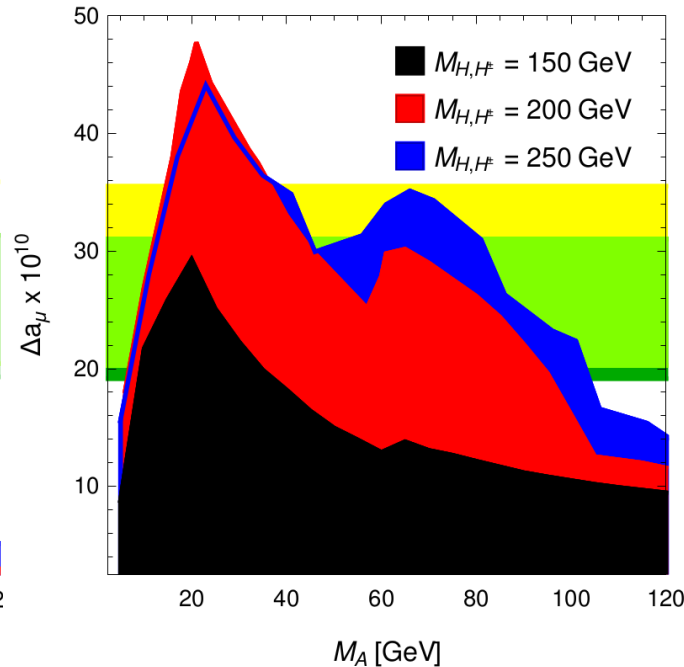
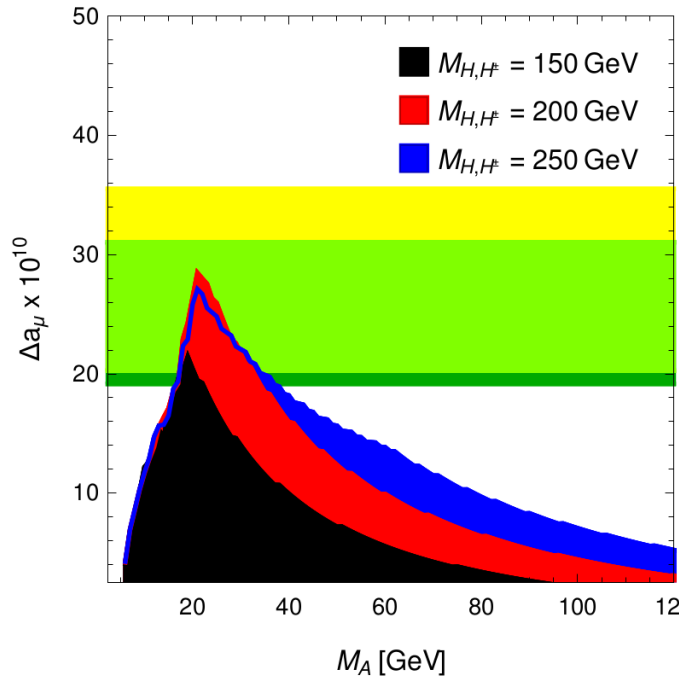
2HDM

- Light pseudoscalar can explain muon g-2 in 2HDM
- Internal chirality flipping via Yukawa coupling
- Two-loop Barr-Zee diagrams are essential, e.g.



Type X 2HDM

Flavour aligned 2HDM



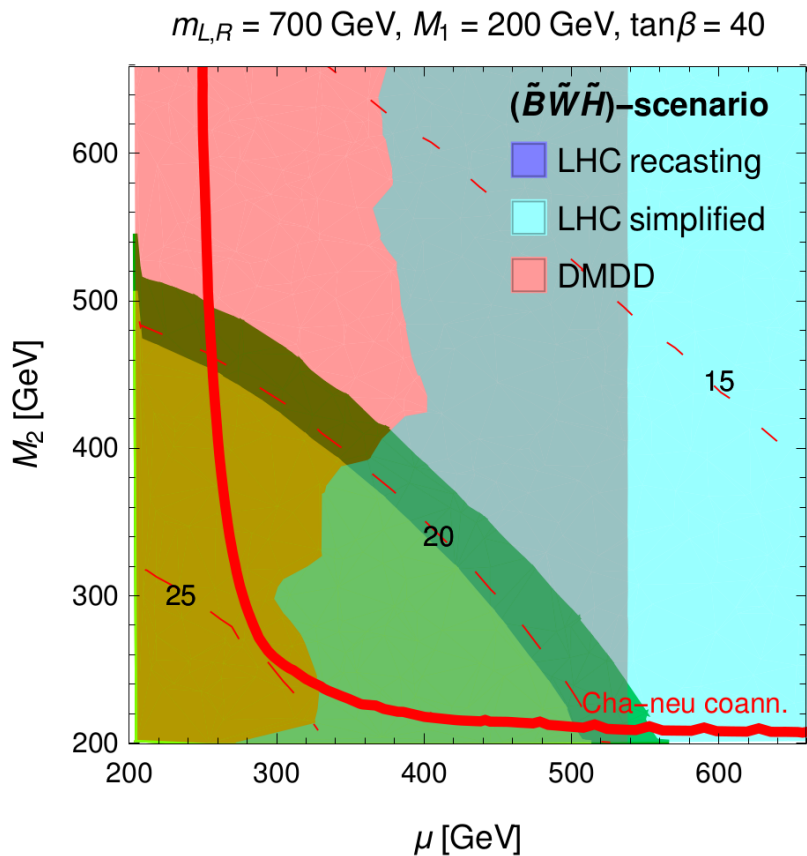
Small regions in Type X still viable

More scenarios possible in flavour aligned 2HDM

Evading broad limits on sleptons and charginos

Idea 2: Make charginos lighter than sleptons

Does not assume tuning, but the parameter space is quite constrained

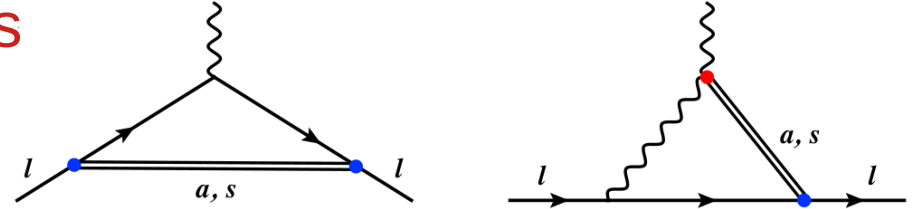


Since the overlapping colors make this hard to read...

- The shaded red DMDD region is all $\mu < 550 \text{ GeV}$
- Cyan is everywhere with $\mu \gtrsim 350 \text{ GeV}$ and gives the jagged vertical line roughly around this value of μ .
- the cyan exclusion only applies whenever stau co-annihilation is needed to deplete the relic density,
- However that is everywhere except the red line where we get chargino co-annihilation
- So we have a tiny region of viable explanations in the bottom right of the plot where the red line overlaps with the green

Axions

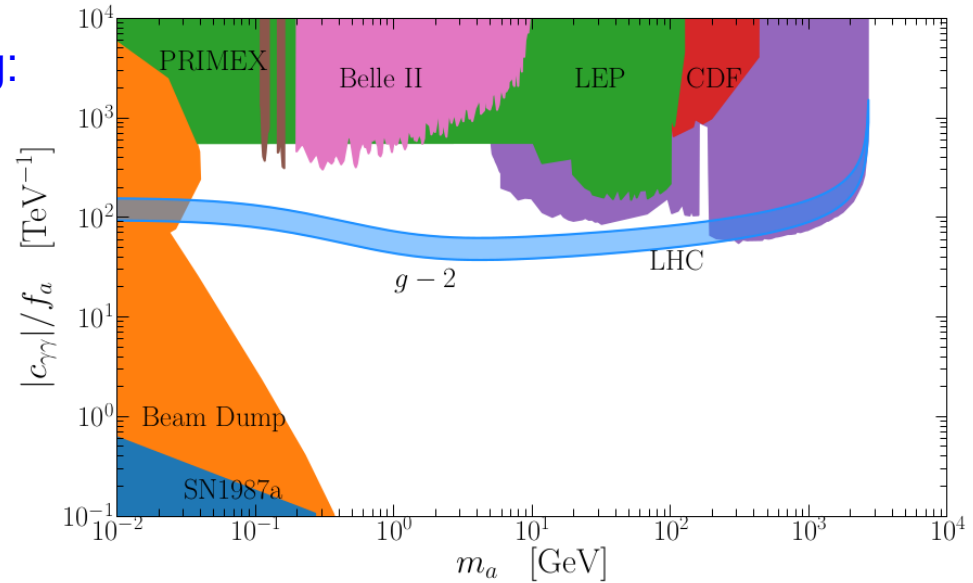
Axion Like Particles (ALPs) appear from the breaking of the approximate U(1) PQ symmetry



[Phys.Rev.D 94 (2016) 11, 115033,
W.J. Marciano, A. Masiero, P. Paradisi & M. Passera]

Axions solve the strong CP problem,
but ALPs are more general

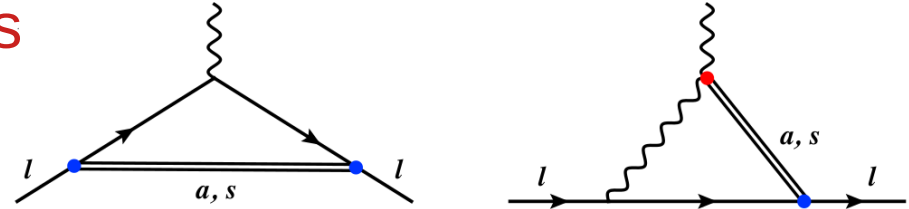
Naively the EFT ALP picture looks very promising:



[JHEP 09 (2021) 101, M.A. Buen-Abad, J. Fan, M. Reece & C. Sun]

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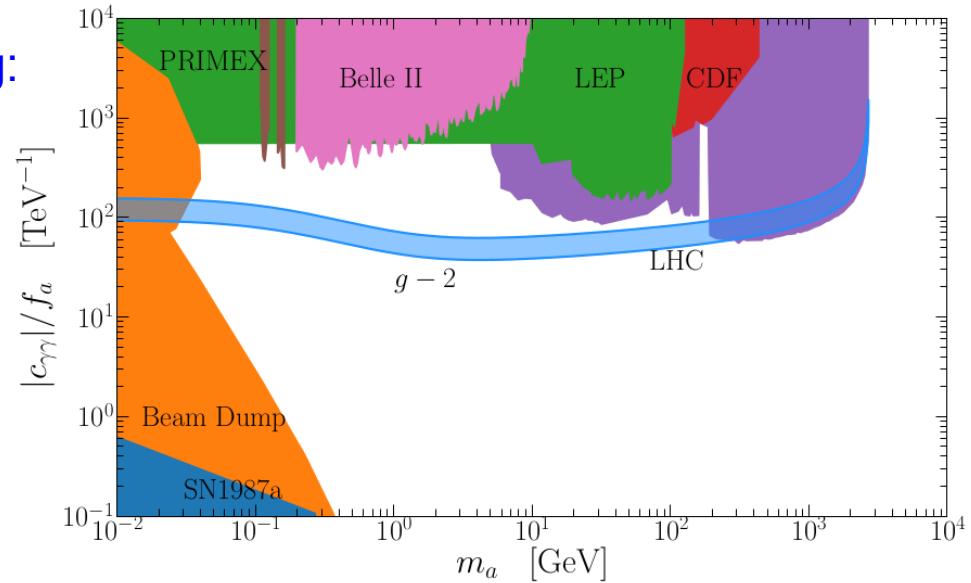
Naively the EFT ALP picture looks very promising:

But need very large couplings

Sober analysis of possible UV
completions in JHEP 09 (2021) 101

Usually need light new degrees of
freedom with masses $\mathcal{O}(10-100)$ GeV

Less room in specific models but
needs more study



[JHEP 09 (2021) 101, M.A. Buen-Abad, J. Fan, M. Reece & C. Sun]

Chirality flipping enhancements

Scalar leptoquark with left and right couplings, e.g. \longrightarrow $C_{\text{BSM}} \approx Q_t \lambda_L \lambda_R m_t / (8\pi^2 m_\mu)$
 $\mathcal{L}_{SLQ-S_1} = -\lambda_{QL} Q_3 \cdot L_2 S_1 - \lambda_{t\mu} t\mu S_1^* + h.c.$ $m_t/m_\mu \approx 1600$

Vector-like Leptons that mix, e.g.

$$\mathcal{L} \supset -Y_{\psi^\pm} \bar{L}_L H \psi_R^- - Y_{\psi_D} \bar{\psi}_{D,L} H \ell_R \\ - Y_{LR} \bar{\psi}_{D,L} H \psi_R^- - Y_{RL} \bar{\psi}_L H^\dagger \psi_{D,R} + h.c.$$

$$\longrightarrow C_{\text{BSM}} \approx \frac{M_{LR}}{m_\mu}$$

[JHEP 02 (2012) 106, K. Kannike, M. Raidal, D.M. Straub & A. Strumia,
Phys.Rev.D 88 (2013) 013017, R. Dermíšek, A. Raval,
Phys.Rev.D 104 (2021) 5, 053008, P.M. Ferreira, B.L. Gonçalves, F.R. Joaquim, & M. Sher]

Similar to scalar leptoquark case

Solutions with heavy masses well beyond LHC

But may have issues with muon mass fine tuning.

Heavy new physics for DM and muon g-2

Example:

$$\mathcal{L}_{2S1F} = (a_H H \cdot \phi_d \phi_s^0 + \lambda_L \phi_d \cdot L \psi_s + \lambda_R \phi_s^0 \mu \psi_s^c - M_\psi \psi_s^c \psi_s + h.c.) - M_{\phi_d}^2 |\phi_d|^2 - \frac{M_{\phi_s}^2}{2} |\phi_s^0|^2.$$

Scalar doublet (points to ϕ_d)
 Scalar singlet (points to ϕ_s^0)
 Charged fermion singlet (points to ψ_s^c)

Mass Mixing between scalars (points to $a_H H \cdot \phi_d \phi_s^0$)
 Left and right couplings to muons (points to $\lambda_L \phi_d \cdot L \psi_s$ and $\lambda_R \phi_s^0 \mu \psi_s^c$)
 Scalar doublet mass (points to $M_{\phi_d}^2 |\phi_d|^2$)
 Scalar singlet mass (points to $\frac{M_{\phi_s}^2}{2} |\phi_s^0|^2$)

Scalar DM:

Relic density (co)annihilations mech.

- scalar singlet DM \longrightarrow via Higgs portal, λ_R t-channel exchange ψ_s
- inert doublet scalar DM \longrightarrow SU(2) co-ann, λ_L t-channel exchange of ψ_s
- Mixed singlet-doublet scalar DM \longrightarrow All of the above
+ a_H driven singlet-doublet co-ann

Direct detection of dark matter via a_H

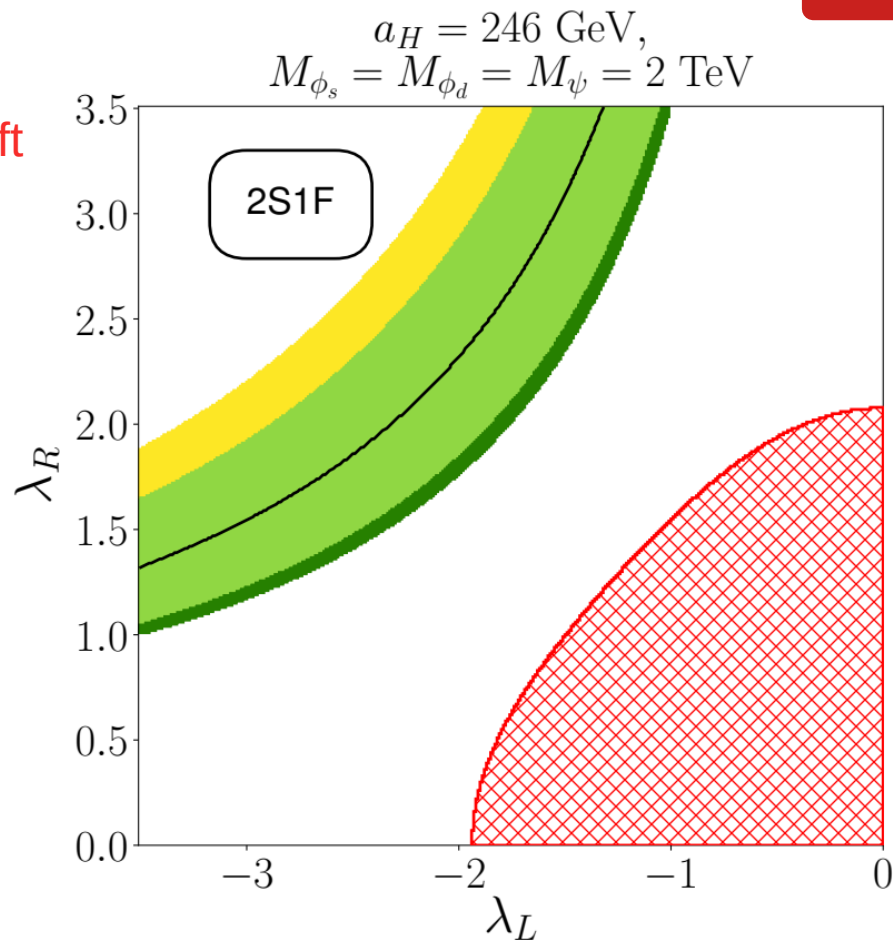
Heavy new physics for DM and muon g-2

Many params influence relic density (and muon g-2)

→ many situations are possible

- Annihilations so effective little DM left when muon g-2 is explained

FlexibleSUSY 2.5.0
for muon g-2



Fitting
2021 Muon g-2

Now Ruled Out

Still viable

Now viable

Exclusions:

Over Abundant

Heavy new physics for DM and muon g-2

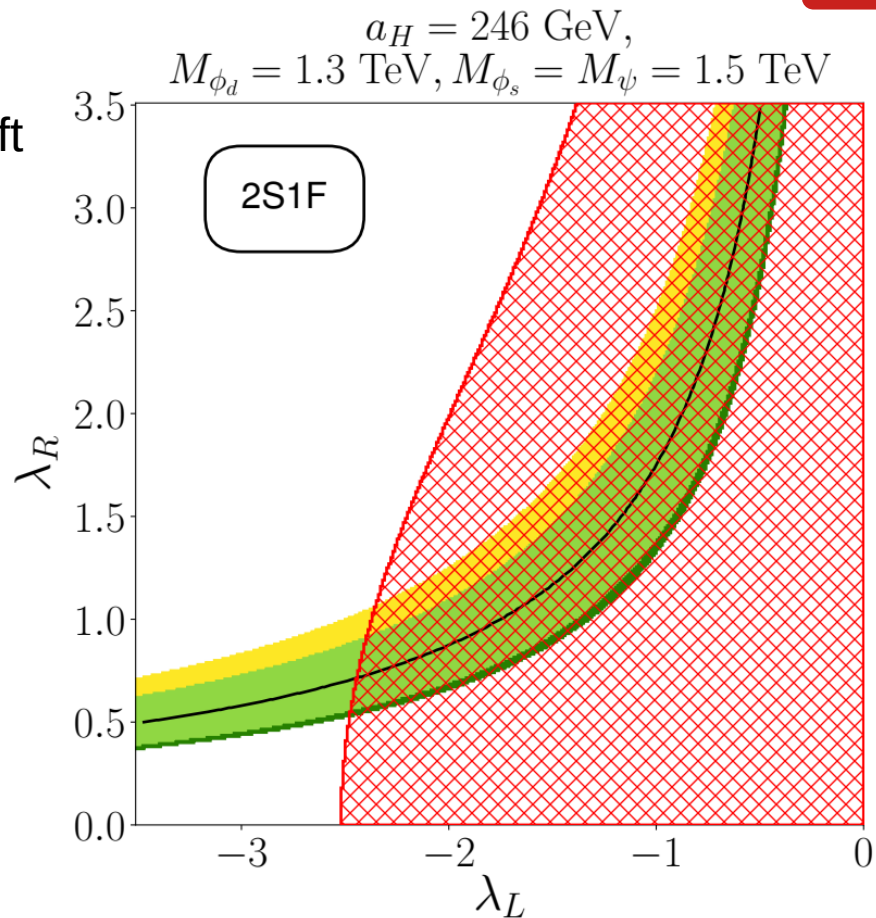
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- RD depends much more on λ_L
→ point where g-2 and RD explained simultaneously



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Exclusions:

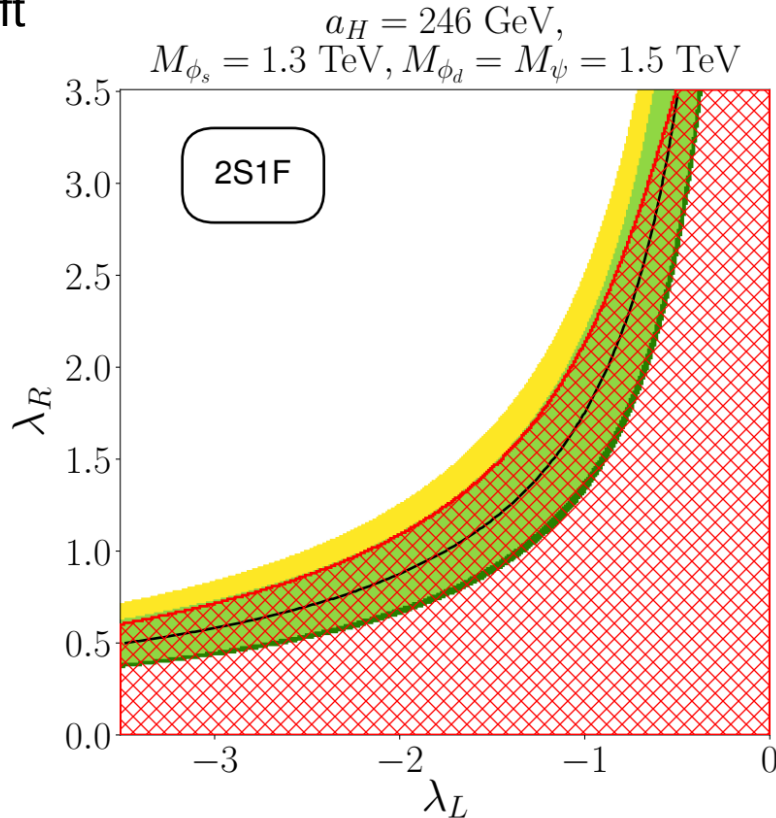
Over Abundant

Heavy new physics for DM and muon g-2

Many params influence relic density (and muon g-2)

→ many situations are possible

- Annihilations so effective little DM left when muon g-2 is explained
- RD depends much more on λ_L
→ point where g-2 and RD explained simultaneously
- Dependency on muon couplings just right for simultaneous solution along the allowed curve



FlexibleSUSY 2.5.0
for muon g-2

Fitting
2021 Muon g-2

Now Ruled Out

Still viable

Now viable

Exclusions:

Over Abundant

The W mass

A very Surprising New Result..

New experimental result

$$M_W^{\text{CDF}} = 80.4335 \pm 0.0094 \text{ GeV}$$

Previous world average

$$M_W^{2021} = 80.379 \pm 0.012 \text{ GeV}$$

Theory predictions

$$M_W^{\text{SM,OS}} = 80.355 \pm 0.006 \text{ GeV}$$

$$M_W^{\text{SM},\overline{\text{MS}}} = 80.351 \pm 0.006 \text{ GeV}$$

$$M_W^{\text{SM, EW fit}} = 80.3591 \pm 0.0052 \text{ GeV}$$

Good agreement

$\Rightarrow \approx 7\sigma$ deviation!

But in **significant tension** with previous measurements...

Naive Combination

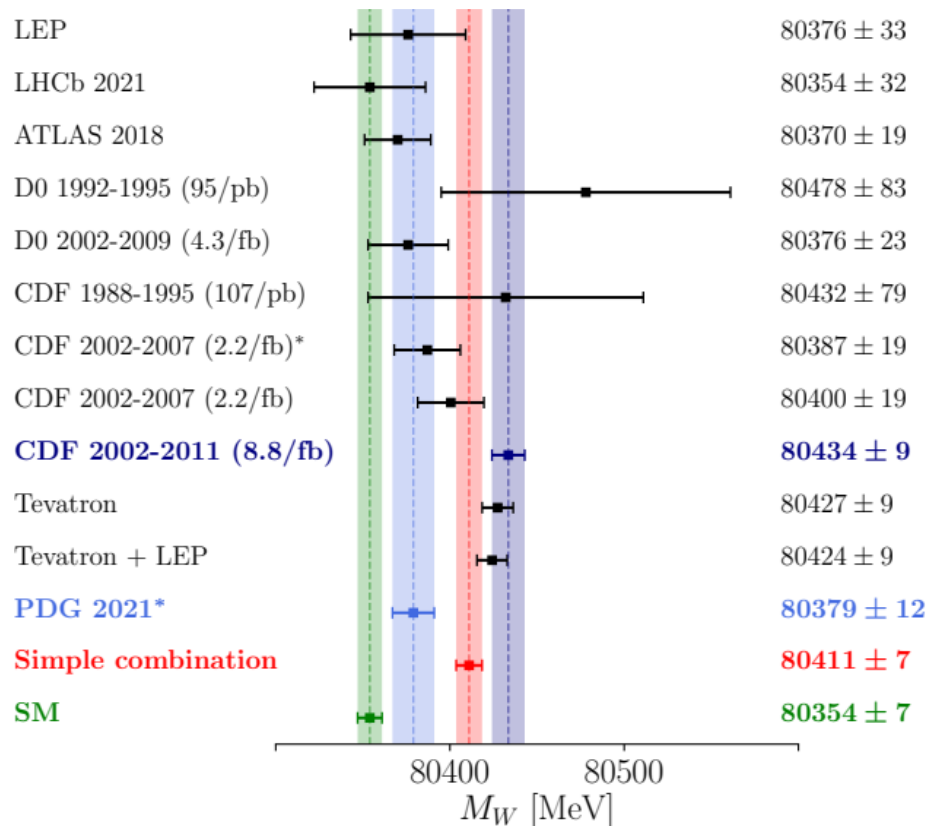
[arXiv:2204.03996,PA, A. Fowlie, C.-T. Lu, L. Wu, Y. Wu, B. Zhu]

Naively combine **all** measurements,
avoiding double counting
of old CDF results

$$\bar{x} \pm \Delta x = \frac{\sum_{i=1}^N w_i x_i}{\sum_{i=1}^N w_i} \pm \left(\sum_{i=1}^N w_i \right)^{-1/2}$$

$$\Rightarrow M_W^{\text{simple comb.}} = 80.411 \pm 0.007 \text{ GeV}$$

With **tension: 2.5σ**



Predicting MW

Electroweak sector $\{M_W, M_Z, G_F, \sin \theta_W, \alpha_e\} \xrightarrow{\text{Choose}} \{M_Z, G_F, \alpha_e\}^{\text{EW inputs}}$

Redundancy amongst these quantities

$$M_W^2 = \frac{1}{4}g^2v^2 \quad M_Z^2 = \frac{1}{4}\sqrt{(g^2 + g'^2)}v^2 \quad \sin^2 \theta_W = \frac{g'^2}{g^2 + g'^2}$$

$$\alpha_e = \frac{e^2}{4\pi} \quad e = \frac{gg'}{g^2 + g'^2} = g' \sin \theta_W = g \cos \theta_W$$

$$G_F = \frac{\pi\alpha}{\sqrt{2}M_W^2 \sin^2 \theta_W}$$

The Fermi constant is very precisely measured

Tree-level EW relations in SM

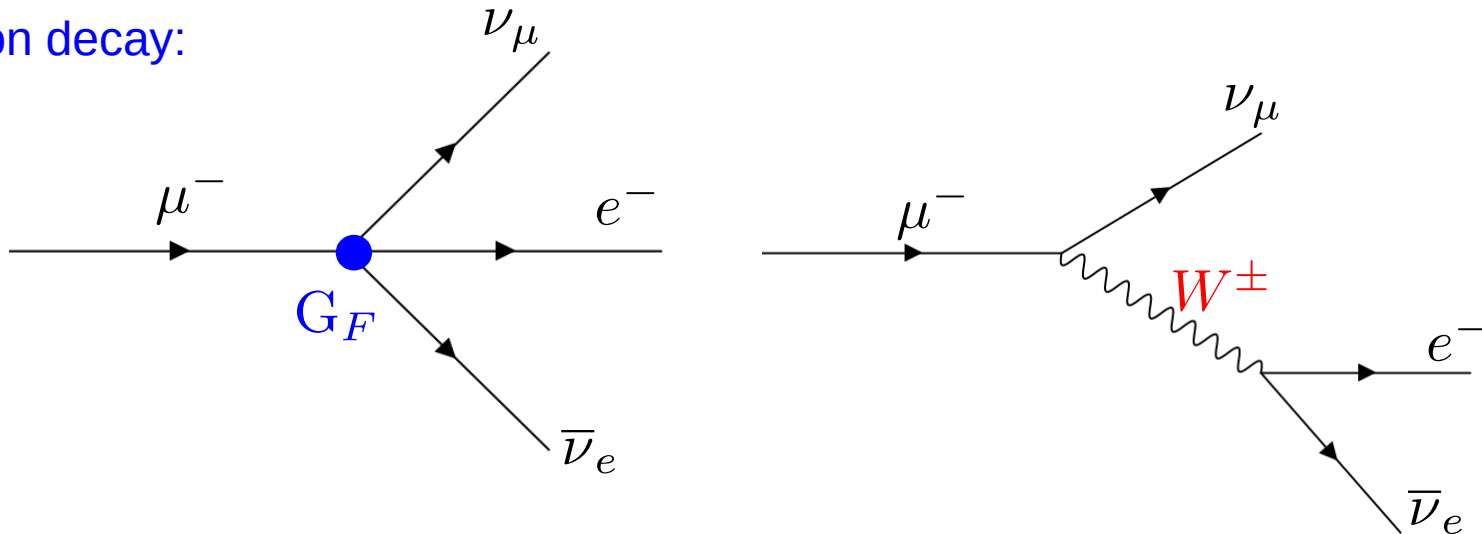
\Rightarrow **Predict M_W from G_F**

Predicting MW from muon decay

Just calculate corrections from W self energy?

$$M_W^2 = M_W^{\text{tree}} + \Pi_{WW}(M_W^2) \quad \times$$

Predict through muon decay:



Muon lifetime:

$$\tau_\mu^{-1} = G_F \frac{m_\mu^5}{192\pi^3} (1 + \dots)$$

$$G_F^{\text{tree}} = \frac{\pi\alpha}{\sqrt{2}M_W^2 \sin^2 \theta_W}$$

OS calculation of MW

Calculate from muon decay:

$$G_F = \frac{\pi\alpha}{\sqrt{2}M_W^{2\text{OS}} \sin^2 \theta_W} \left(1 + \Delta r\right)$$

$$M_W^{2\text{OS}} = M_Z^2 \left\{ \frac{1}{2} + \sqrt{\frac{1}{4} - \frac{\pi\alpha}{\sqrt{2}G_F M_Z^2} (1 + \Delta r)} \right\}$$

At one loop: $\Delta r^{(\alpha)} = \Delta\alpha - \frac{c_W^2}{s_W^2} \Delta\rho + \Delta r^{\text{remainder}}$

Charge renormalisation

$$\begin{aligned} \Delta\alpha &:= \Pi_{AA}^{\text{light}}(0) - \Pi_{AA}^{\text{light}}(M_Z^2) \\ &= \Delta\alpha^{\text{had}} + \Delta\alpha^{\text{lep}} \end{aligned}$$

Correction to the ρ parameter

$$\rho = \frac{M_W^2}{M_Z^2 c_W^2}$$

OS calculation of MW

Calculate from muon decay:

$$G_F = \frac{\pi\alpha}{\sqrt{2}M_W^{2\text{OS}} \sin^2 \theta_W} \left(1 + \Delta r\right)$$

$$M_W^{2\text{OS}} = M_Z^2 \left\{ \frac{1}{2} + \sqrt{\frac{1}{4} - \frac{\pi\alpha}{\sqrt{2}G_F M_Z^2} (1 + \Delta r)} \right\} \leftarrow \begin{array}{l} \text{Assumes no} \\ \text{tree-level} \\ \text{correction to} \\ \rho \text{ parameter} \end{array}$$

At one loop: $\Delta r^{(\alpha)} = \Delta\alpha - \frac{c_W^2}{s_W^2} \Delta\rho + \Delta r^{\text{remainder}}$

Charge renormalisation

$$\begin{aligned} \Delta\alpha &:= \Pi_{AA}^{\text{light}}(0) - \Pi_{AA}^{\text{light}}(M_Z^2) \\ &= \Delta\alpha^{\text{had}} + \Delta\alpha^{\text{lep}} \end{aligned}$$

Correction to the ρ parameter

$$\rho = \frac{M_W^2}{M_Z^2 c_W^2}$$

$\overline{\text{MS}}$ calculation of MW

Calculate from muon decay:

$$G_F = \frac{\pi \hat{\alpha}(M_Z)}{\sqrt{2} M_W^2 \hat{s}_{\theta W}} \left(1 + \Delta \hat{r}_W \right)$$

$$M_W^2 = M_Z^2 \hat{\rho} \left\{ \frac{1}{2} + \sqrt{\frac{1}{4} - \frac{\pi \hat{\alpha}(M_Z)}{\sqrt{2} G_F M_Z^2 \hat{\rho}} (1 + \Delta r_W)} \right\}$$

$$\hat{\alpha}(M_Z) = \frac{\alpha}{1 - \Delta \hat{\alpha}(M_Z)}$$

You may see other formulations,
many subtleties.

Also Includes $\Delta \alpha^{\text{had}} + \Delta \alpha^{\text{lep}}$

Again hadronic contributions
to charge renormalisation
play a role

Hadronic uncertainties in muon g-2

Skepticism exists
because:

- Extraordinary claims require extraordinary evidence
- a_{μ}^{HVP} (and $\Delta\alpha^{\text{had}}$) are hard to calculate
- The new BMW Lattice result does not agree
(and some parts agreement in 2206.06582, arXiv:2206.15084)

Early lattice results (at this precision)

—► need for caution, but increases concerns

Muon g-2 situation already motivated comparison to EW fits with $\Delta\alpha^{\text{had}}$

If BMW result is correct —► tension in EW fits

[A. Crivellin, M. Hoferichter, C. A. Manzari, and M. Montull, PRL 125, 091801 (2020)]

But what about the new W mass measurement?

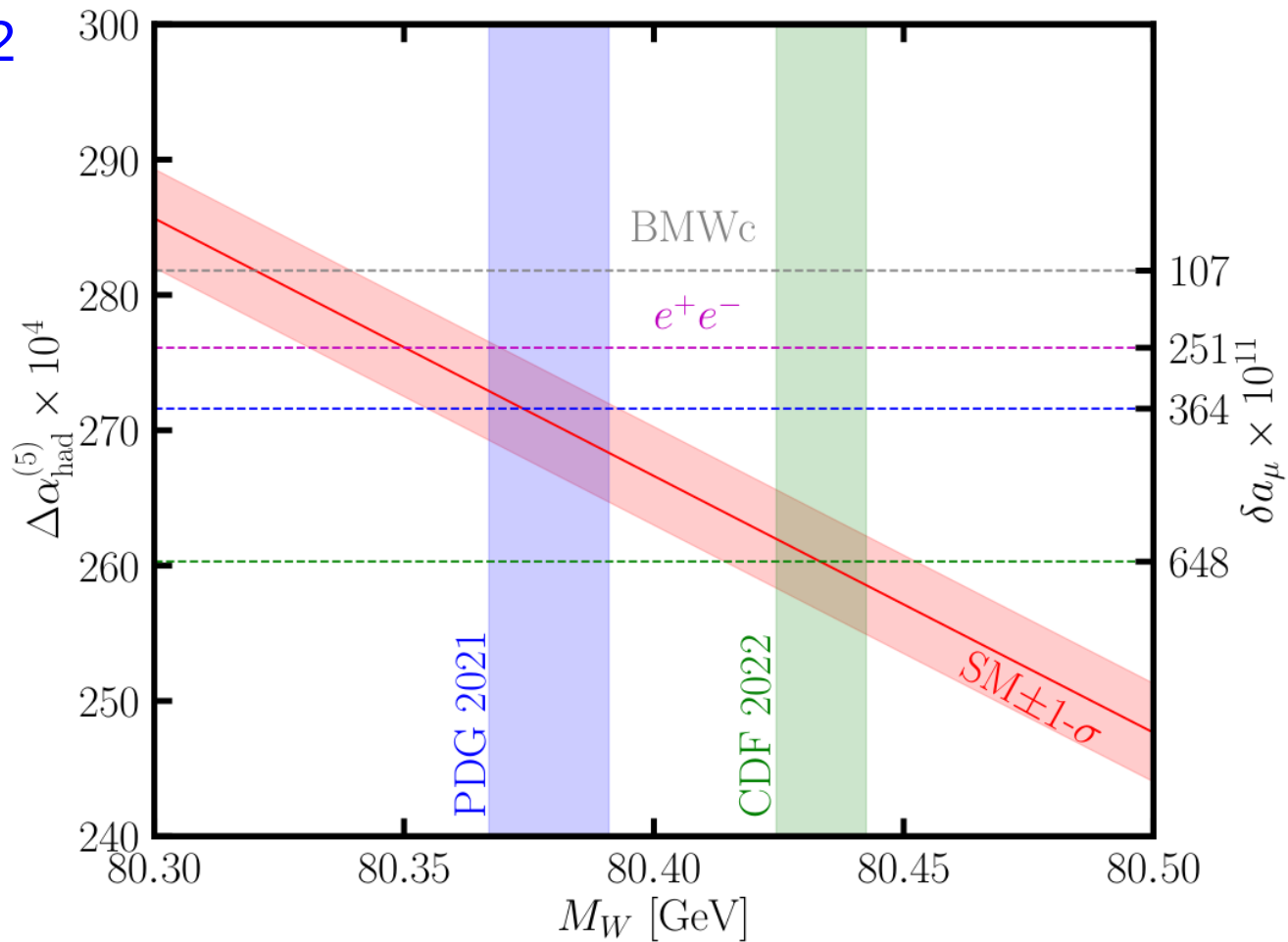
Global EW fit Tension

[arXiv:2204.03996,PA, A. Fowlie, C.-T. Lu, L. Wu, Y. Wu, B. Zhu]

The W mass and muon $g-2$ pull in opposite directions

Red EW fit band cannot agree with both muon $g-2$ and CDF M_W

Very hard for a change in the hadronic cross section to explain both



Global EW fit Tension

[arXiv:2204.03996,PA, A. Fowlie, C.-T. Lu, L. Wu, Y. Wu, B. Zhu]

Input $\Delta\alpha^{\text{had}}$

$\Delta\alpha_{\text{had}}$ Data	BMWc	e^+e^-
Input $\Delta\alpha_{\text{had}} \times 10^4$	281.8(1.5)	276.1(1.1)
χ^2/dof	18.32/15	16.01/15
M_W [GeV]	80.348(6)	80.357(6)
$\Delta\alpha_{\text{had}} \times 10^4$	280.9(1.4)	275.9(1.1)
δM_W [MeV]	86(11)	77(11)
Tension	7.8 σ	7.0 σ

a_μ deviation 1.7 σ

a_μ deviation 4.2 σ

Inputting BMW data increases tension with
CDF W mass measurement

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Input M_W

M_W Data	PDG 2021	CDF 2022
Input M_W [GeV]	80.379(12)	80.4335(94)
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M_W [GeV]	80.367(7)	80.396(7)
$\Delta\alpha_{\text{had}} \times 10^4$	271.7(3.8)	260.9(3.6)
$\delta a_\mu \times 10^{11}$	364(145)	648(137)
Tension	2.5 σ	4.7 σ
δM_W [MeV]	67(12)	38(12)
Tension	5.6 σ	3.2 σ

Inputting CDF W mass increases tension with muon g-2

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Inputting CDF W mass increases tension with muon g-2

And we have a bad EW fit

Global EW fit Tension

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Inputting CDF W mass increases tension with muon g-2

And there is still a tension in the W mass

In general:

For *any* choice to constrain $\Delta\alpha^{\text{had}}$ via
CDF-MW, 2021 PDG-MW, e+e- or BMW lattice data

Reducing the ΔM_W^{CDF} anomaly increases Δa_μ anomaly
and vice versa

... and every choice has: $\sqrt{(\Delta M_W^{\text{CDF}})^2 + (\Delta a_\mu)^2} > 5\sigma$

Big Caveat: this all depends on our assumptions about
energy dependence of the hadronic cross-section

(we applied universal scaling over the full integration range)

Alternative hypothesis:

cross section only changes at low energies $m_{\pi_0} \leq \sqrt{s} \leq 1.937 \text{ GeV}$,

Input $\Delta\alpha^{\text{had}}$

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BMW doesn't increase tension
with MW as much

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$\delta a_\mu \times 10^{11}$	748(339)	1997(320)
Tension	2.2 σ	6.2 σ
δM_W [MeV]	67(12)	38(12)
Tension	5.6 σ	3.2 σ

CDF data makes muon
g-2 anomaly even worse

Alternative hypothesis:

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Tension	2.2 σ	6.2 σ
δM_W [MeV]	67(12)	38(12)
Tension	5.6 σ	3.2 σ

And the EW fit is still
bad!

Even if we remove **all four** of these constraints on $\Delta\alpha^{\text{had}}$
(i.e. extractions from MW and from e+e- data or BMW lattice data)

We find

$$\Delta M_W^{\text{CDF}} = (75 \pm 13) \text{ MeV}, \Rightarrow 5.8\sigma \text{ Tension}$$

EW observables are very sensitive to $\alpha(M_Z)$

No way to explain CDF measurement even without any data driven estimates from hadronic cross sections

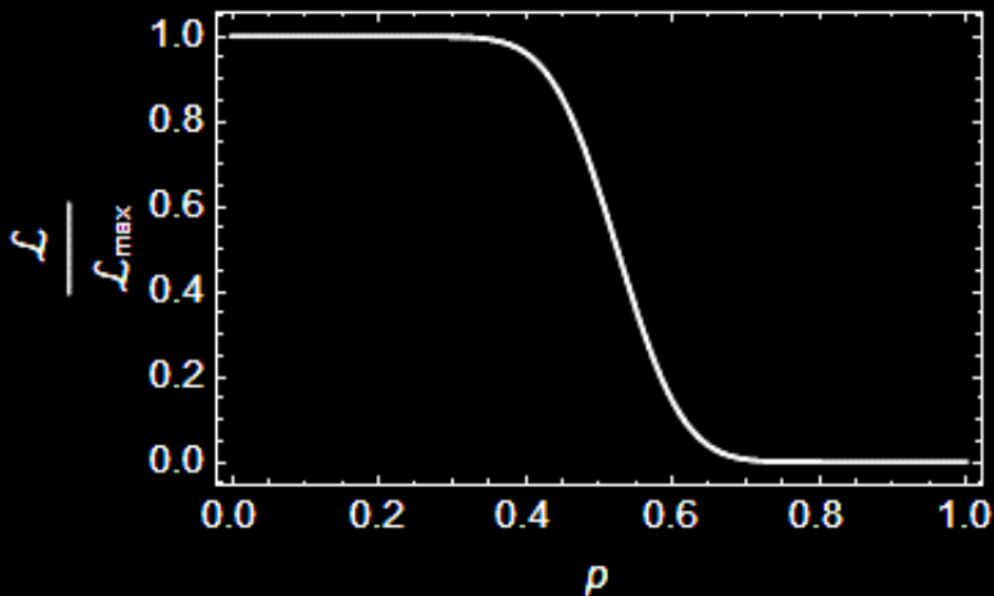
Conversely Δa_μ does depend on the data driven estimates

But inputting a heavy MW pulls us further away from the BMW prediction and the measured value

Naturalness in Bayesian statistics

Slide nicked from Csaba Balazs

Consider hypothesis 1 quantified by a single parameter p .
This theory postdicts an observable o .

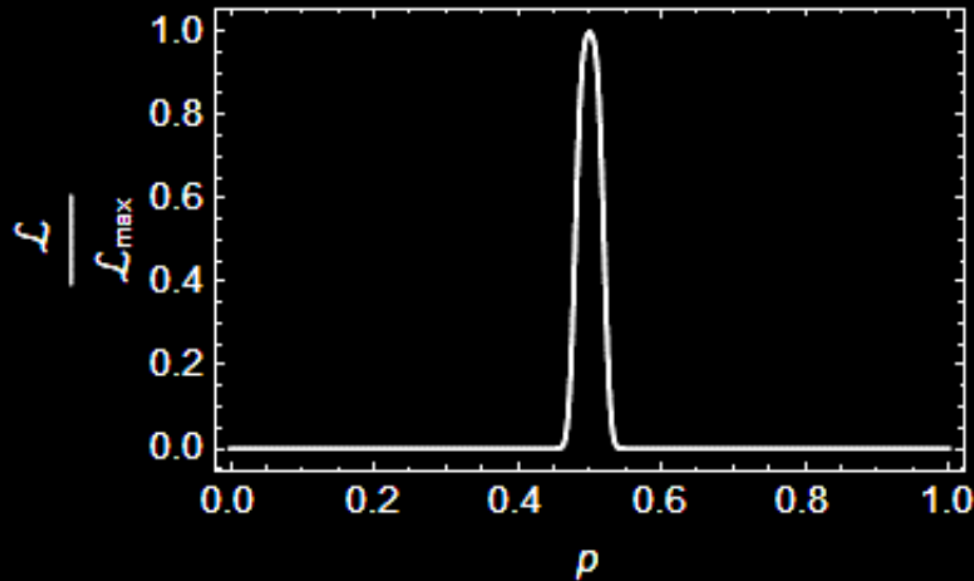


Is this model fine-tuned?

Naturalness in Bayesian statistics

Slide nicked from Csaba Balazs

Consider hypothesis 2 quantified by the parameter p .
This theory also postdicts the observable o .

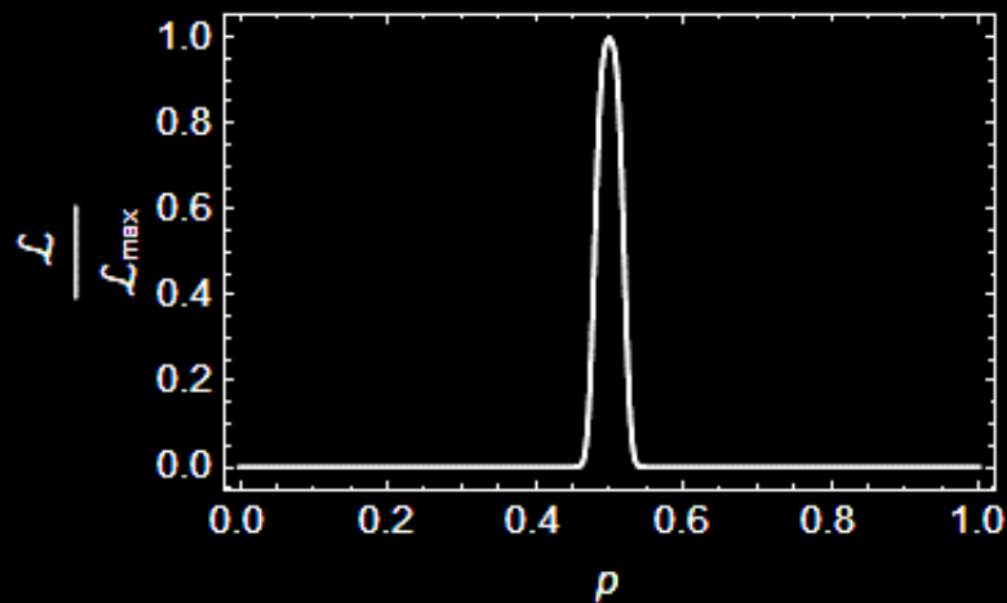
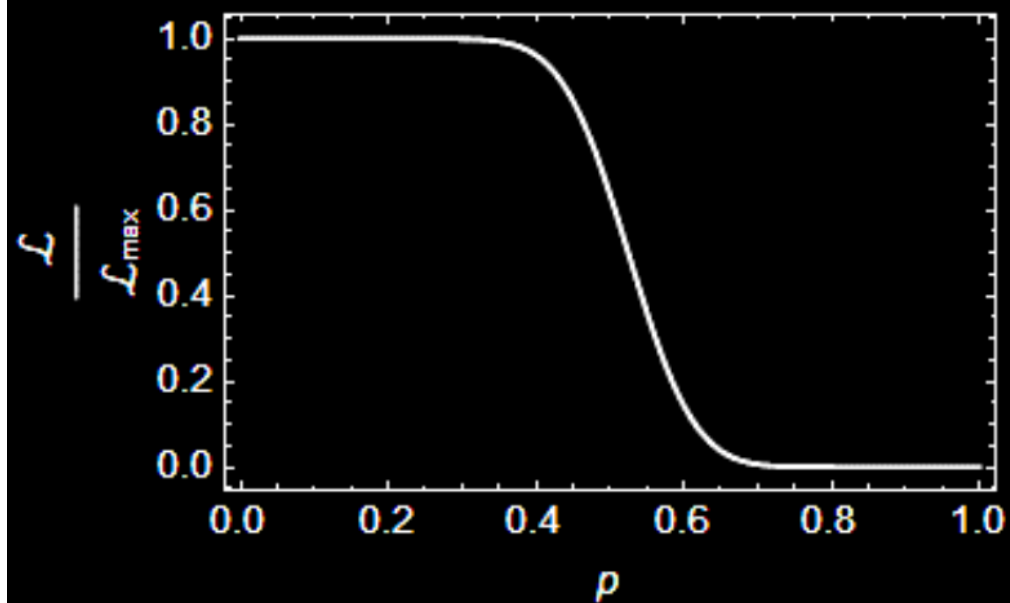


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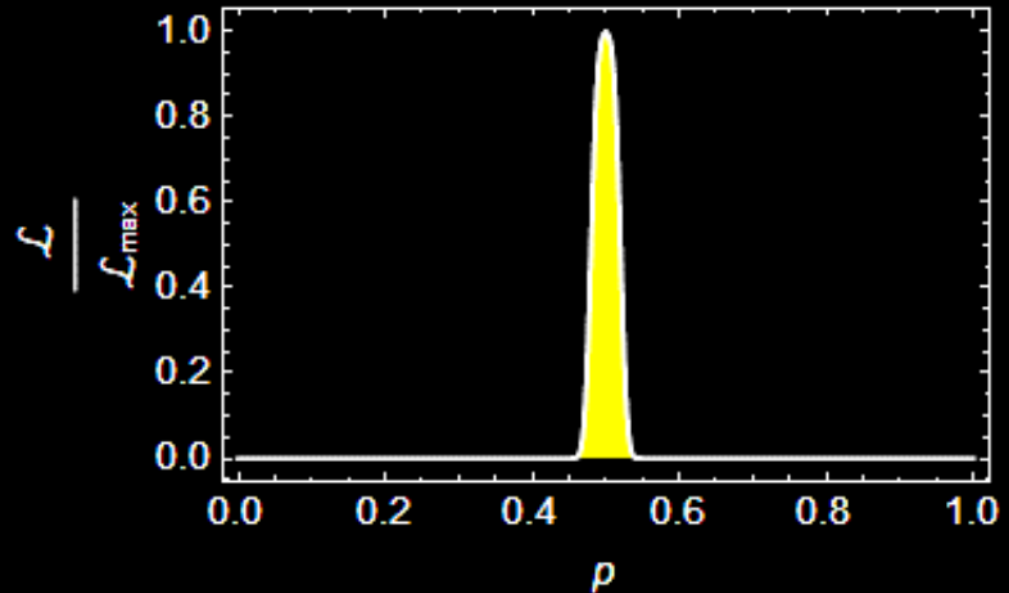
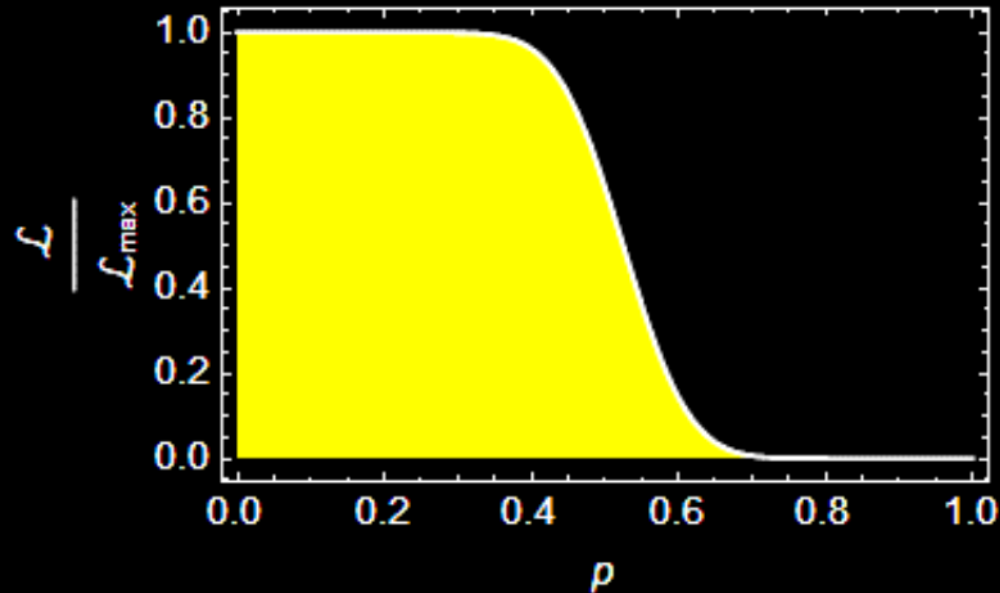
Why does the first model look less fine-tuned?



Naturalness in Bayesian statistics

Slide nicked from Csaba Balazs

Why does the first model look less fine-tuned?



Because it has a higher evidence. (Assume flat prior:)

Naturalness in Bayesian statistics

Slide nicked from Csaba Balazs

Bayesian evidence is

$$\mathcal{E} = \int \mathcal{L}(o, p) \pi(p) dp$$

- the plausibility that hypothesis reproduces observation,
 - proportional to ‘global’ fine-tuning.

My Conclusions and Outlook

- The muon $g-2$ deviation is a powerful discriminator amongst BSM theories and scenarios
- Many reasonable models can fit muon $g-2$, many ways to combine with DM
- No solution in survey is obviously perfect, hard to explain without some tuning, hiding in some corner of parameter space, or going to special cases
- Usually large muon $g-2$ corrections need light solution in survey is obviously perfect, hard to explain without some tuning, hiding in some corner of parameter space, or going to special cases
- Motivates proper Bayesian studies checking the plausibility of explanations, accounting for naturalness questions
- Still room for new ideas, more natural/plausible explanations

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Give a broad overview of physics beyond the standard model that can explain a large deviation from the SM prediction in muon $g-2$

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Give a broad overview of physics beyond the standard model that can explain a large deviation from the SM prediction in muon $g-2$

Not just “ambulance chasing”  Important stress test

Existence of plausible hypotheses must impact on how seriously we take this as a new physics signal

By the end of this talk I hope you will understand:

- the challenges to explaining muon $g-2$ with BSM physics,
- the advantages and drawbacks of most obvious solutions
- what overcoming them implies for future experiments like the CEPC

Note I will use SM prediction from the theory initiative white paper

$$\text{This gives: } \Delta a_\mu = (25.1 \pm 5.9) \times 10^{-10} \Rightarrow 4.2\sigma \text{ deviation}$$

But this is based on:

$$a_\mu^{\text{HVP,LO}} \times 10^{10} = 694.0 \pm 4 \quad [\text{KNT, PRD 101 (2020) 1, 014029}]$$

$$692.78 \pm 2.42 \quad [\text{BHMZ, EPJC 80 (2020) 3, 241}]$$

$$693.1 \pm 4 \quad [\text{White Paper, Phys.Rept. 887 (2020) 1-166}]$$

$$707.5 \pm 5.5 \quad [\text{BMW Lattice, Nature 593, 51 (2021)}] \text{ (not included SM Estimate above)}$$

There seems to be a tension between data driven estimates and early lattice results.

I am not an expert on computing hadronic contributions

and I mostly won't comment on this, but...