

Lighting Electroweak-Violating ALP-Lepton Interactions at CEPC

Chih-Ting Lu 卢致廷 ctlu@njnu.edu.cn



NNU · 南京师范大学
NANJING NORMAL UNIVERSITY

Ref : 2210.15648 [hep-ph]

17/08/2023

CEPC味物理-新物理和相关探测技术研讨会

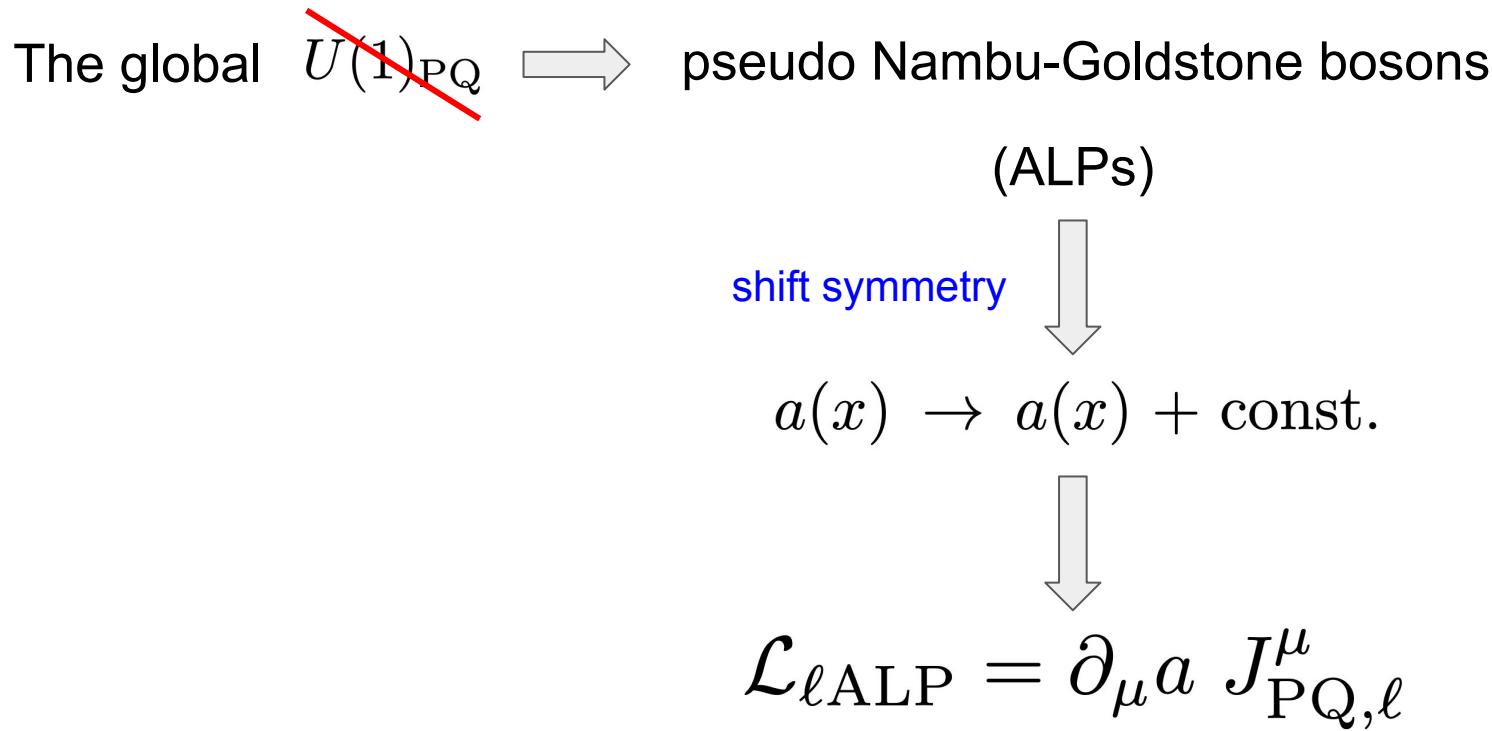
Content

1. ALP-lepton interactions
2. Energy enhancement behaviors in $e^+e^- \rightarrow \nu_e a \bar{\nu}_e$
3. The signal-to-background analysis at CEPC
4. Conclusion

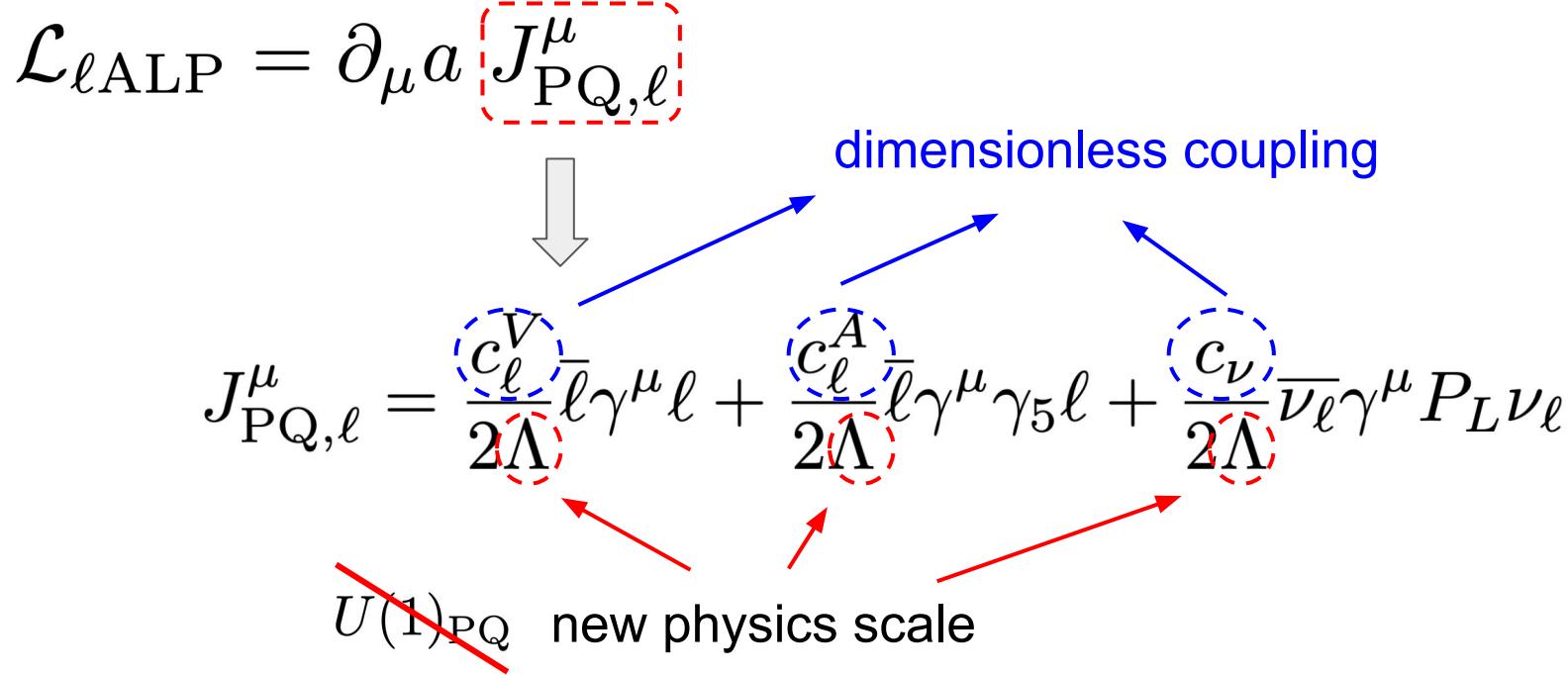
Content

1. **ALP-lepton interactions**
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ALP-lepton interactions



ALP-lepton interactions



ALP-lepton interactions

$$\mathcal{L}_{\ell \text{ALP}} = \partial_\mu a \boxed{J_{\text{PQ},\ell}^\mu}$$

Are the previous statements
in the literature correct ?

$$J_{\text{PQ},\ell}^\mu = \boxed{\frac{c_\ell^V}{2\Lambda} \bar{\ell} \gamma^\mu \ell} + \boxed{\frac{c_\ell^A}{2\Lambda} \bar{\ell} \gamma^\mu \gamma_5 \ell} + \boxed{\frac{c_\nu}{2\Lambda} \bar{\nu}_\ell \gamma^\mu P_L \nu_\ell}$$

“The vector coupling
is unphysical”

“The neutrino coupling is
suppressed by its mass”

$$\boxed{\frac{1}{2} \partial_\mu a \bar{\ell} \gamma^\mu \gamma_5 \ell = m_\ell a \bar{\ell} i \gamma_5 \ell}$$

ALP-lepton interactions

$$J_{\text{PQ},\ell}^{\mu} = \frac{c_{\ell}^V}{2\Lambda} \bar{\ell} \gamma^{\mu} \ell + \frac{c_{\ell}^A}{2\Lambda} \bar{\ell} \gamma^{\mu} \gamma_5 \ell + \frac{c_{\nu}}{2\Lambda} \bar{\nu}_{\ell} \gamma^{\mu} P_L \nu_{\ell}$$

More generally, each lepton coupling term in the above can arise independently in a electroweak invariant theory by including the following currents,

$$\overline{(HL)} \gamma_{\mu} (HL), \bar{e}_R \gamma_{\mu} e_R, \text{ and } \overline{(H^\dagger L)} \gamma_{\mu} (H^\dagger L),$$

New Opportunities for Detecting Axion-Lepton Interactions

Wolfgang Altmannshofer, Jeff A. Dror, and Stefania Gori

Phys. Rev. Lett. **130**, 241801 – Published 13 June 2023

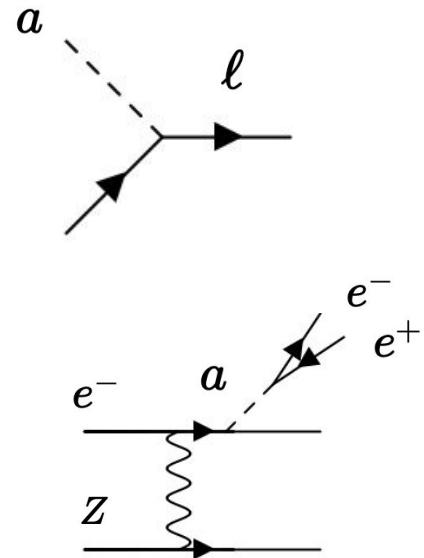
ABSTRACT

We revisit the theory and constraints on axionlike particles (ALPs) interacting with leptons. We clarify some subtleties in the constraints on ALP parameter space and find several new opportunities for ALP detection. We identify a qualitative difference between weak-violating and weak-preserving ALPs, which dramatically change the current constraints due to possible “energy enhancements” in various processes. This new understanding leads to additional opportunities for ALP detection through charged meson decays (e.g., $\pi^+ \rightarrow e^+ \nu a$, $K^+ \rightarrow e^+ \nu a$) and W boson decays. The new bounds impact both weak-preserving and weak-violating ALPs and have implications for the QCD axion and addressing experimental anomalies using ALPs.

ALP-lepton interactions

After integration by parts of $\partial_\mu a J_{\text{PQ},\ell}^\mu$, the $\mathcal{L}_{\ell\text{ALP}}$ can be represented as

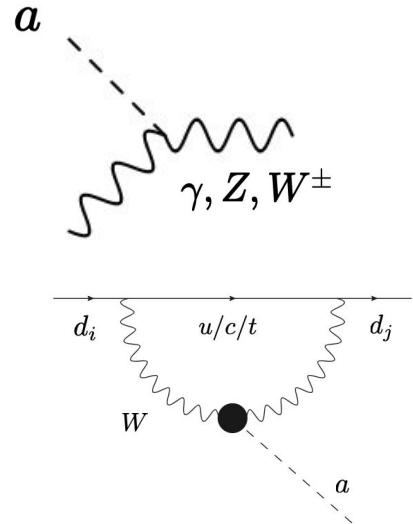
$$\begin{aligned}
 a \partial_\mu J_{\text{PQ},\ell}^\mu &= \boxed{i c_\ell^A \frac{m_\ell}{\Lambda} a \bar{\ell} \gamma_5 \ell} \\
 &+ \frac{\alpha_{\text{em}}}{4\pi\Lambda} \left[\frac{c_\ell^V - c_\ell^A + c_\nu}{4s_W^2} a W_{\mu\nu}^+ \tilde{W}^{-,\mu\nu} \right. \\
 &+ \frac{c_\ell^V - c_\ell^A (1 - 4s_W^2)}{2s_W c_W} a F_{\mu\nu} \tilde{Z}^{\mu\nu} - c_\ell^A a F_{\mu\nu} \tilde{F}^{\mu\nu} + \\
 &\left. \frac{c_\ell^V (1 - 4s_W^2) - c_\ell^A (1 - 4s_W^2 + 8s_W^4) + c_\nu}{8s_W^2 c_W^2} a Z_{\mu\nu} \tilde{Z}^{\mu\nu} \right] \\
 &+ \frac{ig_W}{2\sqrt{2}\Lambda} (c_\ell^A - c_\ell^V + c_\nu) a (\bar{\ell} \gamma^\mu P_L \nu) W_\mu^- + \text{h.c.},
 \end{aligned}$$



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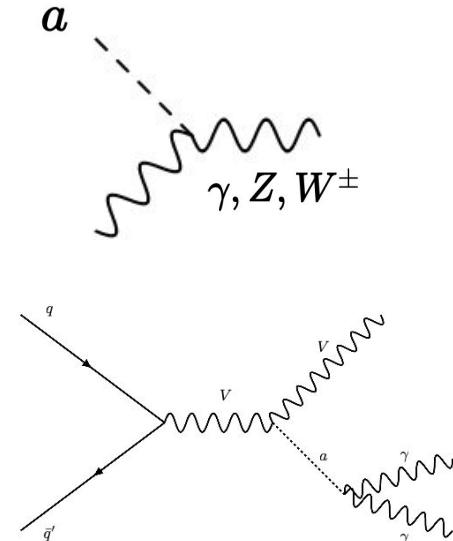
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 + \frac{c_\ell^V - c_\ell^A(1 - 4s_W^2)}{2s_W c_W} &a F_{\mu\nu} \tilde{Z}^{\mu\nu} - c_\ell^A a F_{\mu\nu} \tilde{F}^{\mu\nu} + \\
 \frac{c_\ell^V(1 - 4s_W^2) - c_\ell^A(1 - 4s_W^2 + 8s_W^4) + c_\nu}{8s_W^2 c_W^2} &a Z_{\mu\nu} \tilde{Z}^{\mu\nu} \Big] \\
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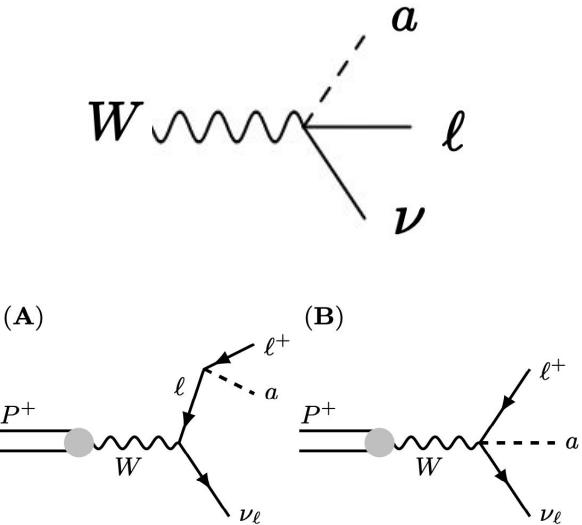
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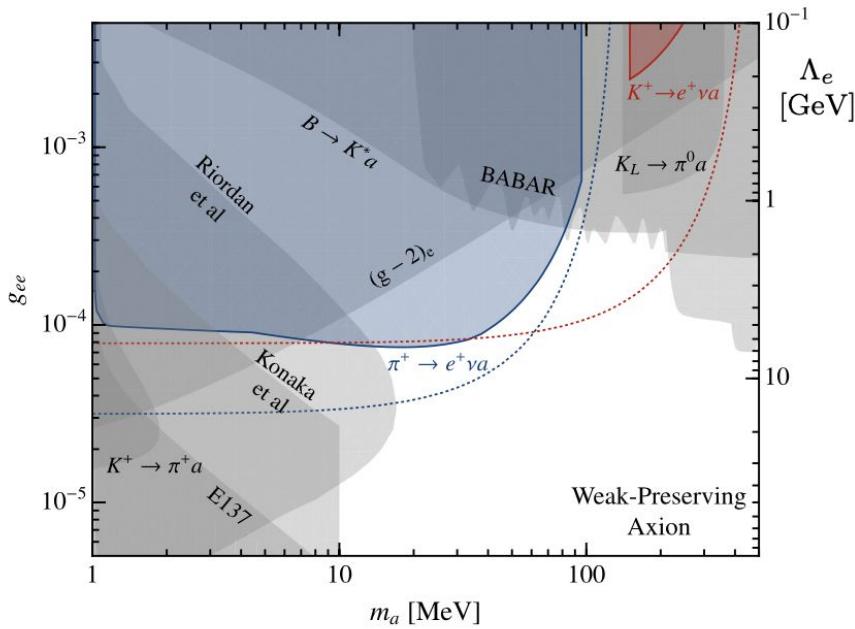


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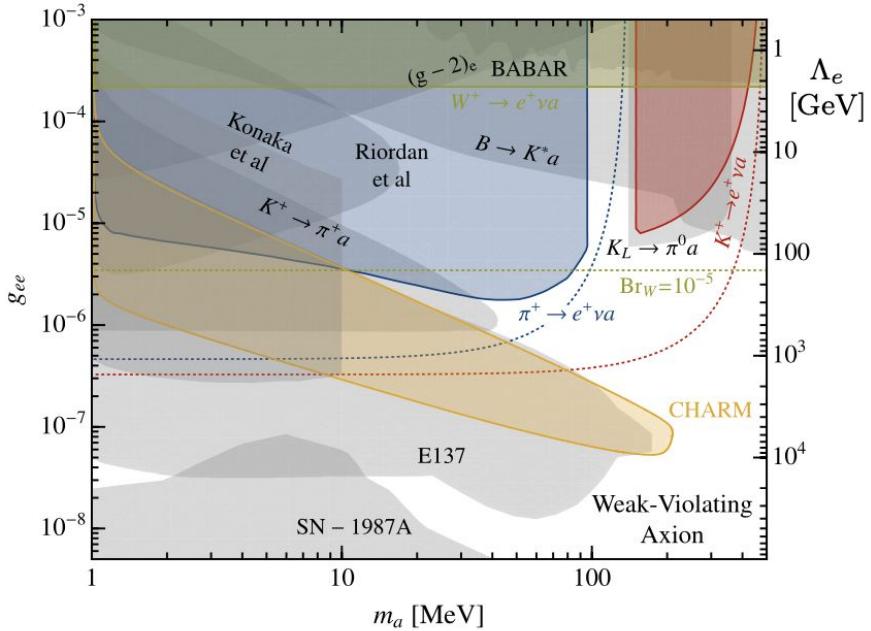
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 &+ \boxed{\frac{i g_W}{2\sqrt{2}\Lambda} (c_\ell^A - c_\ell^V + c_\nu) a (\bar{\ell} \gamma^\mu P_L \nu) W_\mu^- + \text{h.c.}}
 \end{aligned}$$





$$j_{\text{PQ}}^\mu = \frac{\bar{g}_{\ell\ell}}{2m_\ell} \bar{\ell} \gamma^\mu \ell + \frac{g_{\ell\ell}}{2m_\ell} \bar{\ell} \gamma^\mu \gamma_5 \ell + \frac{g_{\nu_\ell}}{2m_\ell} \bar{\nu}_\ell \gamma^\mu P_L \nu_\ell .$$

$$\Lambda_e \equiv m_e / g_{ee}$$

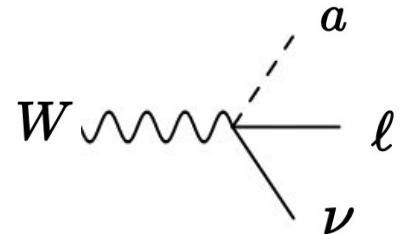


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 &+ \frac{c_\ell^V - c_\ell^A (1 - 4s_W^2)}{2s_W c_W} a F_{\mu\nu} \tilde{Z}^{\mu\nu} - c_\ell^A a F_{\mu\nu} \tilde{F}^{\mu\nu} + \\
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 &+ \boxed{\frac{i g_W}{2\sqrt{2}\Lambda} (c_\ell^A - c_\ell^V + c_\nu) a (\bar{\ell} \gamma^\mu P_L \nu) W_\mu^- + \text{h.c.}}
 \end{aligned}$$



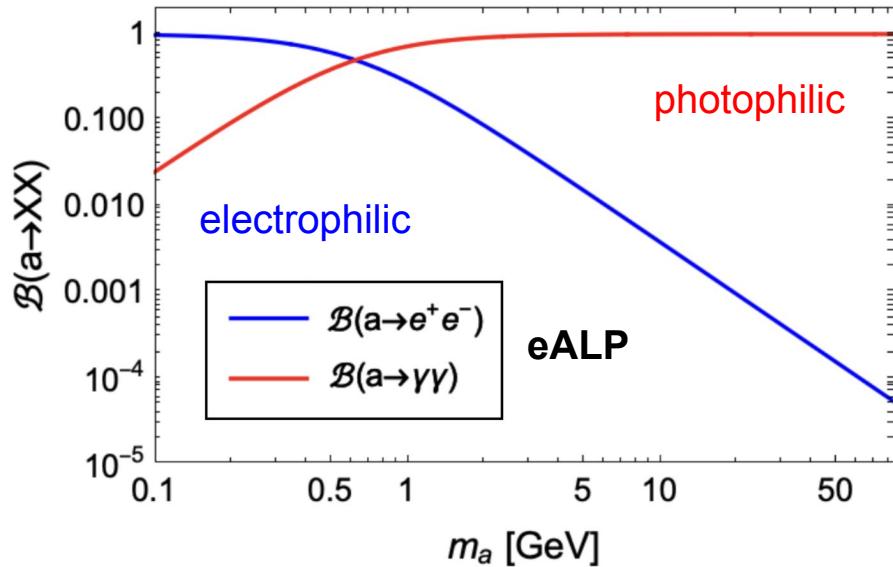
How about the scenario for heavy leptophilic ALPs ?

Leptophilic ALP decay modes

$$\Gamma_{a \rightarrow \ell^+ \ell^-} = \frac{(c_\ell^A)^2 m_\ell^2 m_a}{8\pi \Lambda^2} \sqrt{1 - \frac{4m_\ell^2}{m_a^2}}, \quad \Gamma_{a \rightarrow \gamma\gamma} = \frac{g_{a\gamma\gamma}^2 m_a^3}{64\pi},$$

$$g_{a\gamma\gamma} = \frac{\alpha_{\text{em}}}{\pi} \frac{c_\ell^A}{\Lambda} \left| 1 - \mathcal{F}\left(\frac{m_a^2}{4m_\ell^2}\right) \right|$$

$$\mathcal{F}(z > 1) = \frac{1}{z} \arctan^2 \left(\frac{1}{\sqrt{1/z-1}} \right)$$



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Electroweak Violating and Electroweak Preserving scenarios

Electroweak Violating (**EWV**) : $c_\ell^V = c_\nu = 0, c_\ell^A \neq 0,$

Electroweak Preserving (**EWP**) : $c_\nu = 0, c_\ell^V = c_\ell^A \neq 0$

$$J_{\text{PQ},\ell}^\mu = \frac{c_\ell^V}{2\Lambda} \bar{\ell} \gamma^\mu \ell + \frac{c_\ell^A}{2\Lambda} \bar{\ell} \gamma^\mu \gamma_5 \ell + \frac{c_\nu}{2\Lambda} \bar{\nu}_\ell \gamma^\mu P_L \nu_\ell$$

EWP :

1. PQ charges are electroweak symmetric
2. The lepton current is pure right-handed coupling current

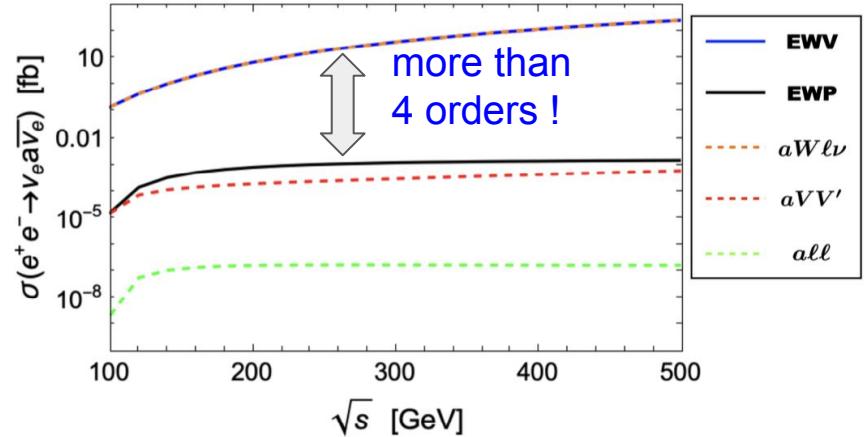
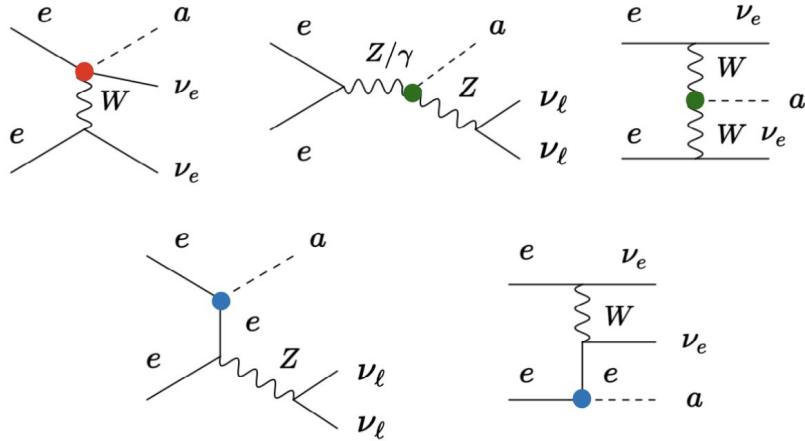
$$J_{\text{PQ},\ell}^\mu = \frac{c_\ell^A}{\Lambda} \bar{\ell} \gamma_\mu P_R \ell$$

EWV :

1. Generated through RG flow
2. Also by $\overline{(HL)} \gamma_\mu (HL)$
3. The lepton current is pure axial-vector current

$$J_{\text{PQ},\ell}^\mu = \frac{c_\ell^A}{2\Lambda} \bar{\ell} \gamma_\mu \gamma_5 \ell$$

$$e^+ e^- \rightarrow \nu_e a \bar{\nu}_e$$

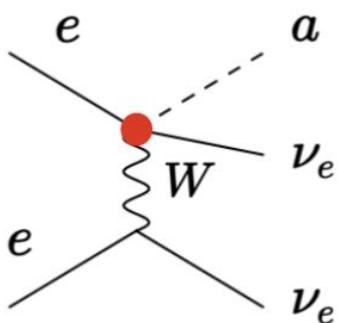


$$c_e^A / \Lambda = 0.01 \text{ GeV}^{-1}$$

$$e^+ e^- \rightarrow \nu_e a \bar{\nu}_e$$

$$e^-(p_1)e^+(p_2) \rightarrow \nu_e(q_1)a(q_2)\bar{\nu}_e(q_3), \quad |\mathcal{M}|^2 = \quad (3.1)$$

$$\begin{aligned} & \frac{g_W^4 (c_\ell^A - c_\ell^V + c_\nu)^2}{32\Lambda^2} \left(\frac{1}{k^2 - M_W^2} + \frac{1}{k'^2 - M_W^2} \right)^2 \\ & \times (s - 2m_e^2) [s - m_a^2 - 2q_2 \cdot (q_1 + q_3)] , \end{aligned}$$



where $s = (p_1 + p_2)^2 = (q_1 + q_2 + q_3)^2$, $k = p_2 - q_3$ and $k' = p_1 - q_1$. It's clear to see this amplitude square can be enhanced when the momentum transferring in this t -channel process is large enough and it is estimated to be smaller than

$$|\mathcal{M}|^2 < \frac{g_W^4 (c_\ell^A - c_\ell^V + c_\nu)^2}{16\Lambda^2 (s - M_W^2)^2} (s - 2m_e^2) (\sqrt{s} - m_a)^2 .$$

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Exploring $e^+e^- \rightarrow \nu_e a \bar{\nu}_e$ at CEPC

1. We choose the CEPC with $\sqrt{s} = 240$ GeV
2. Benchmark point : $m_a = 50$ GeV with $c_e^A/\Lambda = 1$ TeV $^{-1}$.
3. The signal process $e^+e^- \rightarrow \nu_e a \bar{\nu}_e$, $a \rightarrow \gamma\gamma$

signature : 2 isolated photons plus missing energy

4. Possible SM backgrounds :

$$e^+e^- \rightarrow \gamma\gamma\nu_\ell\bar{\nu}_\ell$$

$$e^+e^- \rightarrow \nu_\ell\bar{\nu}_\ell h \rightarrow \nu_\ell\bar{\nu}_\ell(\gamma\gamma)$$

Exploring $e^+e^- \rightarrow \nu_e a\bar{\nu}_e$ at CEPC

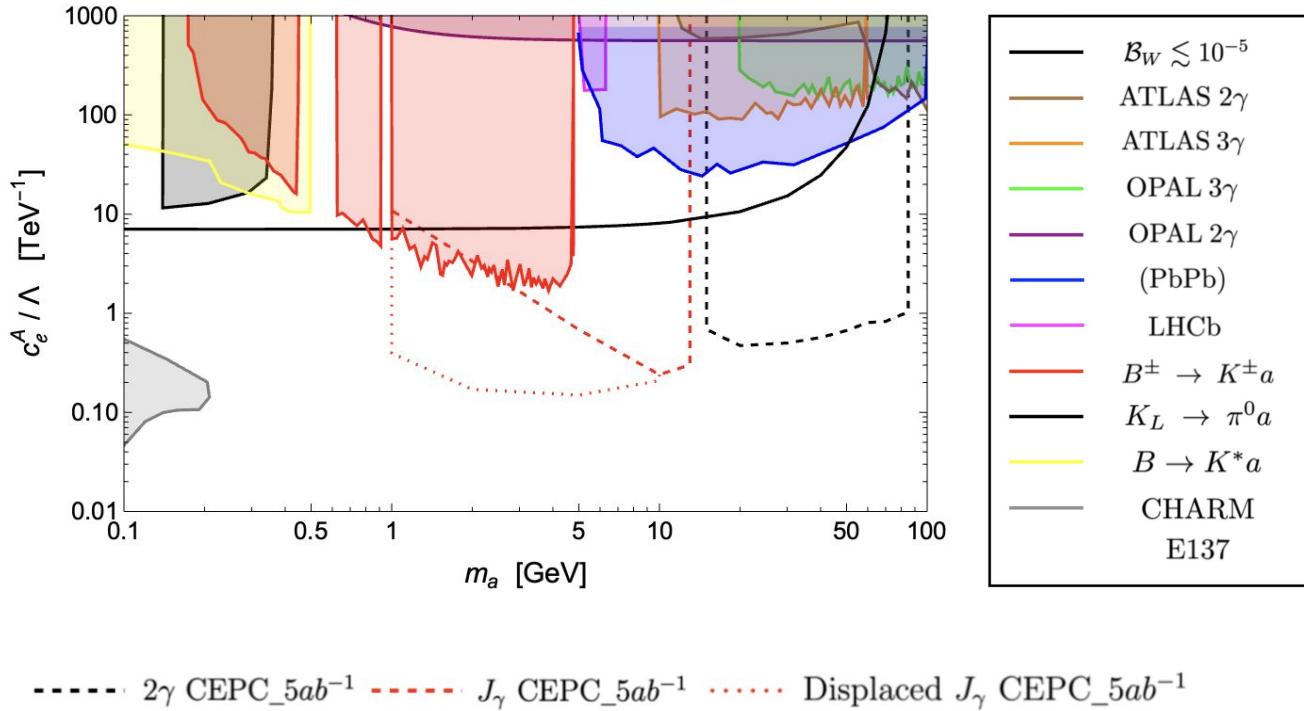
- (1) $N(\gamma) \geq 2$ with $30 < E_{\gamma_1} < 90$ GeV, $E_{\gamma_2} > 15$ GeV, $|\eta_{\gamma_1}| < 1.5$ and $|\eta_{\gamma_2}| < 2.0$,
- (2) $\cancel{E} > 120$ GeV and $|\eta_{\cancel{E}}| < 2.0$,
- (3) Veto $85 < M_{\cancel{E}} < 95$ GeV,
- (4) $|M_{\gamma_1\gamma_2} - m_a| < 3$ GeV,
- (5) $\Delta\phi_{\gamma_1, \cancel{E}} > 2.5$ and $\Delta\phi_{\gamma_2, \cancel{E}} > 1.8$,
- (6) $2.2 < \cancel{E}/M_{\gamma_1\gamma_2} < 3.6$,

Exploring $e^+e^- \rightarrow \nu_e a\bar{\nu}_e$ at CEPC

cut flow in σ [fb]	signal	$\nu_\ell \bar{\nu}_\ell \gamma\gamma$	$\nu_\ell \bar{\nu}_\ell (h \rightarrow \gamma\gamma)$
Generator	0.11	263.60	7.67×10^{-2}
cut-(1)	7.10×10^{-2}	32.23	5.47×10^{-2}
cut-(2)	6.62×10^{-2}	21.85	3.84×10^{-5}
cut-(3)	6.02×10^{-2}	12.62	3.84×10^{-5}
cut-(4)	5.96×10^{-2}	1.17	7.67×10^{-7}
cut-(5)	5.01×10^{-2}	0.68	0
cut-(6)	4.99×10^{-2}	0.64	0

pre-selection cuts ($E_\gamma > 5$ GeV and $|\eta_\gamma| < 3.0$)

Main results and existing bounds



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Conclusion

1. The less discussed four-point interaction, W-l-v-a, in electroweak-violating (EWV) scenario plays an important role to explore leptophilic ALPs :

Light eALPs : charged mesons and W boson exotic decays.

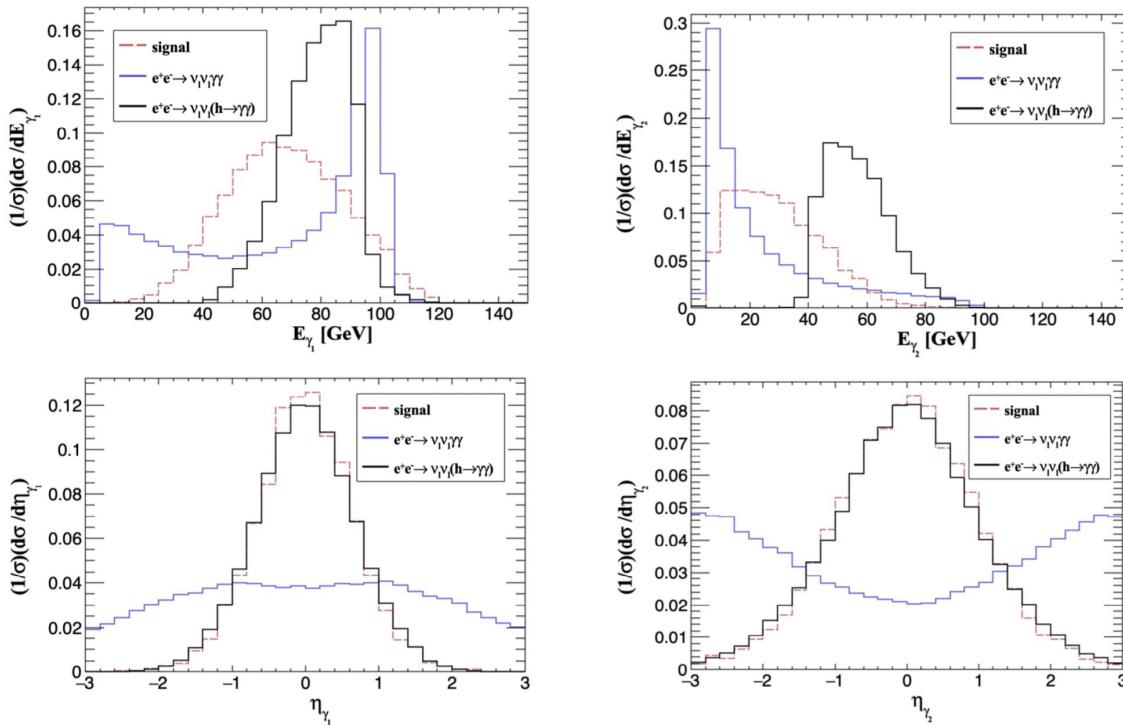
Heavy eALPs : t-channel ALP production modes : $e^+e^- \rightarrow \nu_e a \bar{\nu}_e$

2. Taking CEPC with $\mathcal{L} = 5ab^{-1}$ as an examples, we find the possible future bounds of c_e^A/Λ can be lower than about $0.1 - 1.0 \text{ TeV}^{-1}$ for $1 \text{ GeV} \lesssim m_a \lesssim M_W$ which is much stronger than existing bounds.

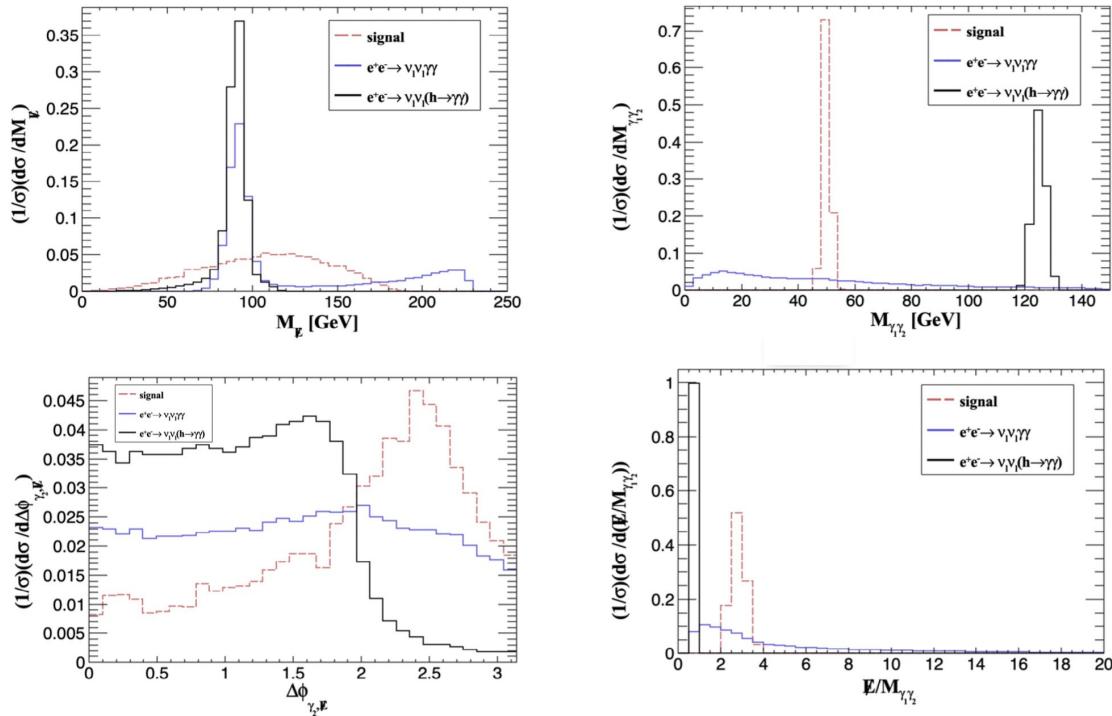
Thank you
for your attention

Back-up

Exploring $e^+e^- \rightarrow \nu_e a\bar{\nu}_e$ at CEPC



Exploring $e^+e^- \rightarrow \nu_e a\bar{\nu}_e$ at CEPC



Exploring $e^+e^- \rightarrow \nu_e a\bar{\nu}_e$ at CEPC

When the ALP is light, it will be **highly boosted**, generating two photons in the final state that are **too collimated to pass the photon isolation criteria**, resulting in a novel '**photon-jet**' signature. Additionally, the light ALP can become a **long-lived particle (LLP)**. Further details on these studies can be found in my paper.

Lighting Electroweak-Violating ALP-Lepton Interactions at e^+e^- and ep Colliders

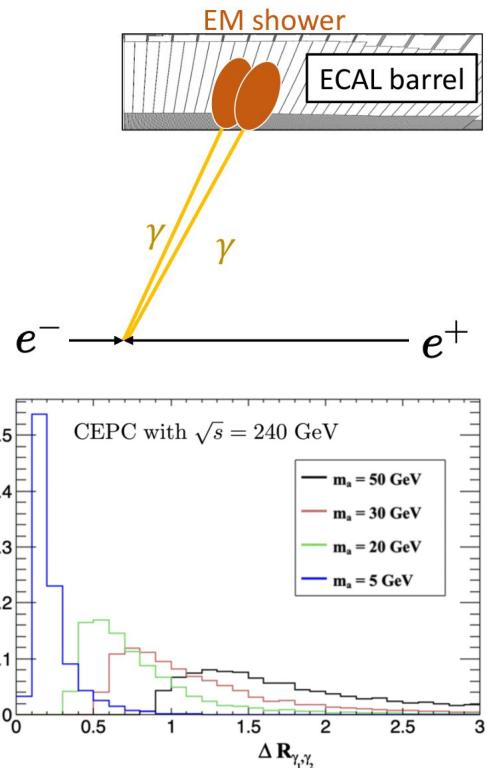
Chih-Ting Lu ([Nanjing Normal U.](#)) (Oct 27, 2022)

e-Print: [2210.15648](#) [hep-ph]

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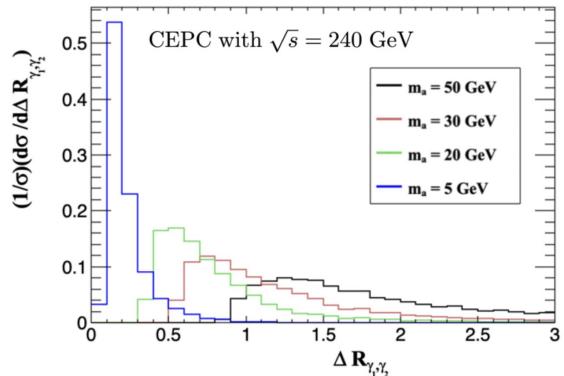
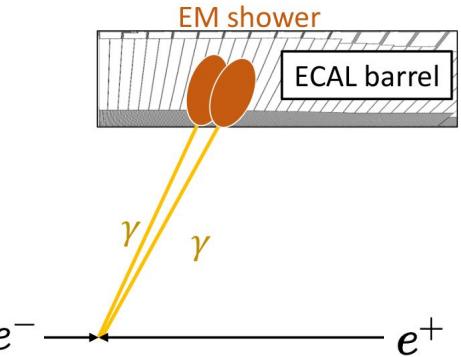
$$e^+e^- \rightarrow \nu_\ell \bar{\nu}_\ell \gamma$$



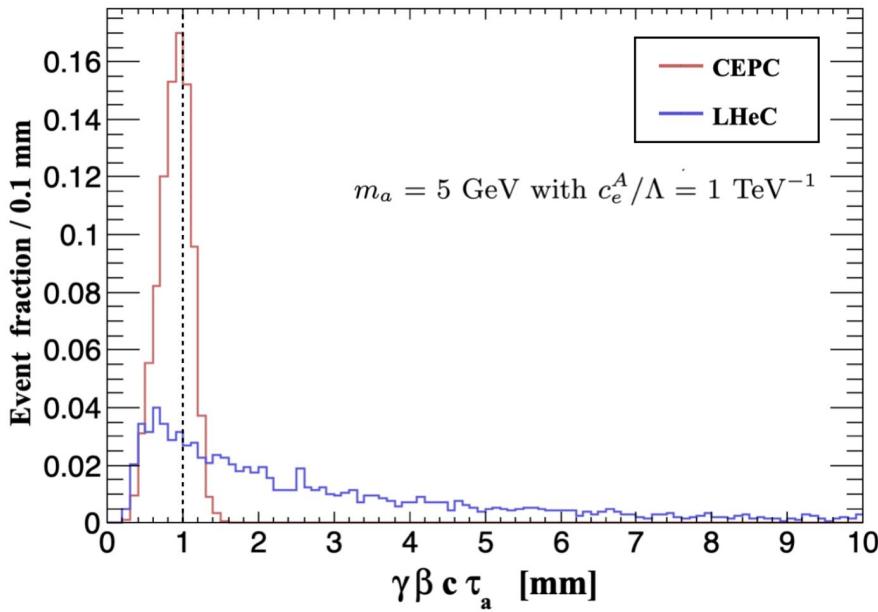
Exploring $e^+e^- \rightarrow \nu_e a\bar{\nu}_e$ at CEPC

1. We apply the C/A jet clustering algorithm with a cone size $R = 0.4$ for a photon-jet candidate.
2. Then the hadronic energy fraction is required to satisfy $\log\theta_J < -2$

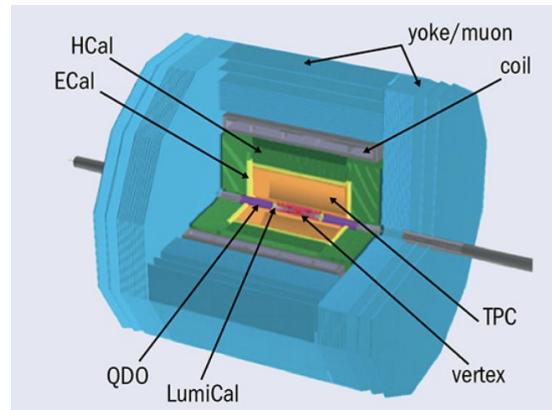
$$\theta_J = \frac{E_{J,\text{HCAL}}}{E_J},$$



Exploring $e^+e^- \rightarrow \nu_e a\bar{\nu}_e$ at CEPC



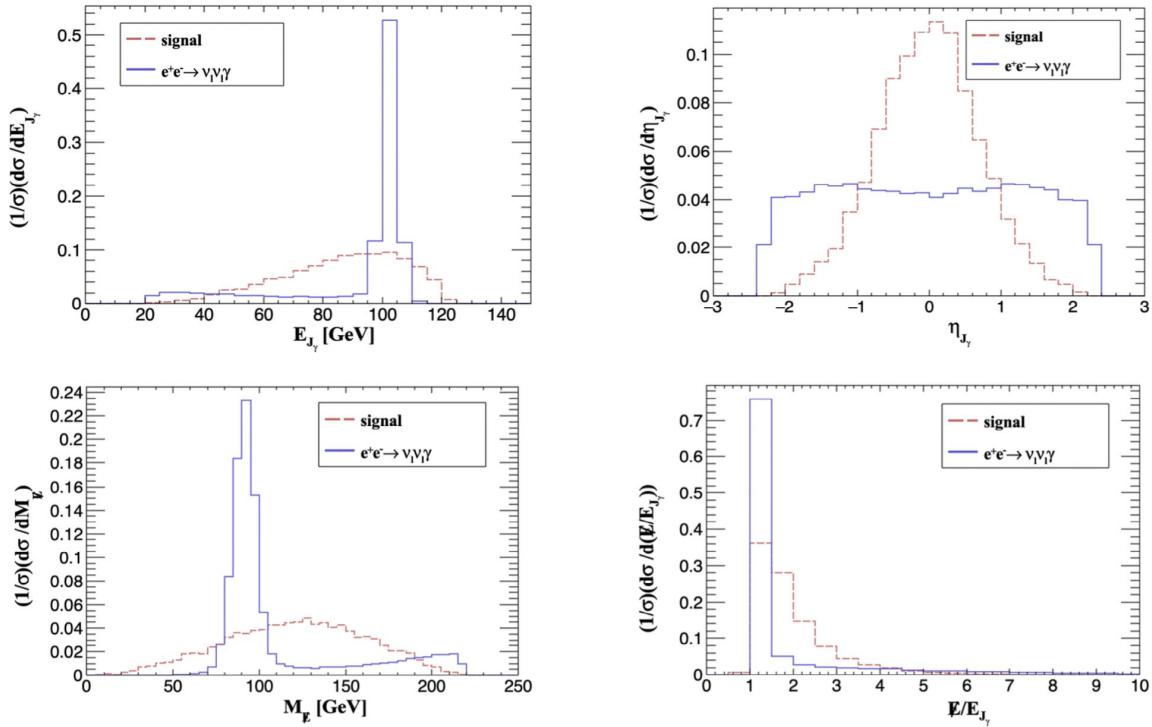
1. $16 \leq R_{\text{vertex}} \leq 60 \text{ mm,}$
2. $0.15 \leq R_{\text{ECAL}} \leq 1.81 \text{ m,}$
3. $2.30 \leq R_{\text{HCAL}} \leq 3.34 \text{ m,}$
4. $2.30 \leq R_{\text{muon}} \leq 3.34 \text{ m}$



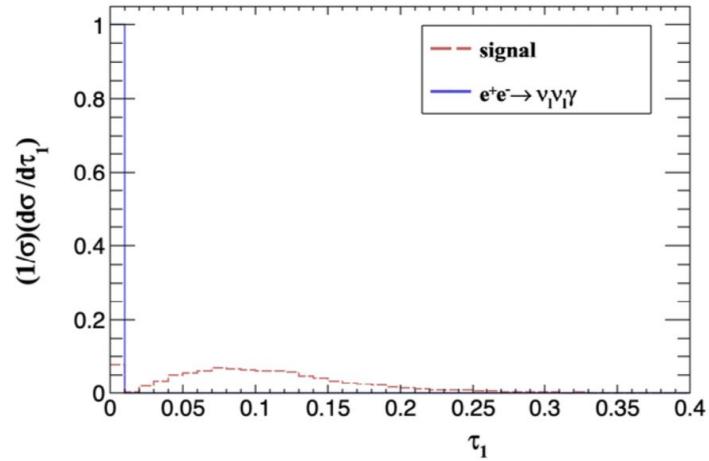
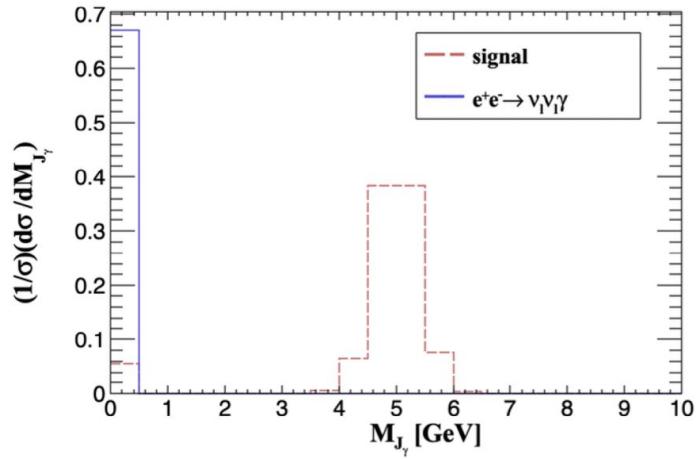
Exploring $e^+e^- \rightarrow \nu_e a\bar{\nu}_e$ at CEPC

- (1) $N(J_\gamma) \geq 1$ with $\log\theta_J < -2$, $30 < E_{J_\gamma} < 100$ GeV, and $|\eta_{J_\gamma}| < 1.5$,
- (2) $\cancel{E} > 140$ GeV and $|\eta_{\cancel{E}}| < 1.5$,
- (3) Veto $75 < M_{\cancel{E}} < 105$ GeV,
- (4) $\cancel{E}/E_{J_\gamma} > 1.5$,
- (5) $|M_{J_\gamma} - m_a| < 1$ GeV,
- (6) $\tau_1(J_\gamma) > 0.03$.

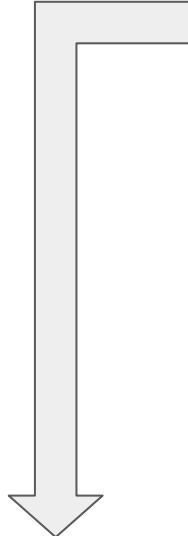
Exploring $e^+e^- \rightarrow \nu_e a\bar{\nu}_e$ at CEPC



Exploring $e^+e^- \rightarrow \nu_e a\bar{\nu}_e$ at CEPC



Exploring $e^+e^- \rightarrow \nu_e a\bar{\nu}_e$ at CEPC



cut flow in σ [fb]	signal	$\nu_\ell\bar{\nu}_\ell\gamma$
Generator	0.16	4266.80
$\gamma\beta c\tau_a < 1$ mm	0.10	–
cut-(1)	8.49×10^{-2}	520.29
cut-(2)	8.49×10^{-2}	520.29
cut-(3)	8.10×10^{-2}	387.77
cut-(4)	7.92×10^{-2}	373.39
cut-(5)	7.76×10^{-2}	0
cut-(6)	7.67×10^{-2}	0

The pre-selection cuts in parton-level are similar as before, except for $E_\gamma > 1$ GeV ($E_\gamma > 10$ GeV) for the signal (background).