

# Global fit of the SMEFT at future lepton colliders

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Based on

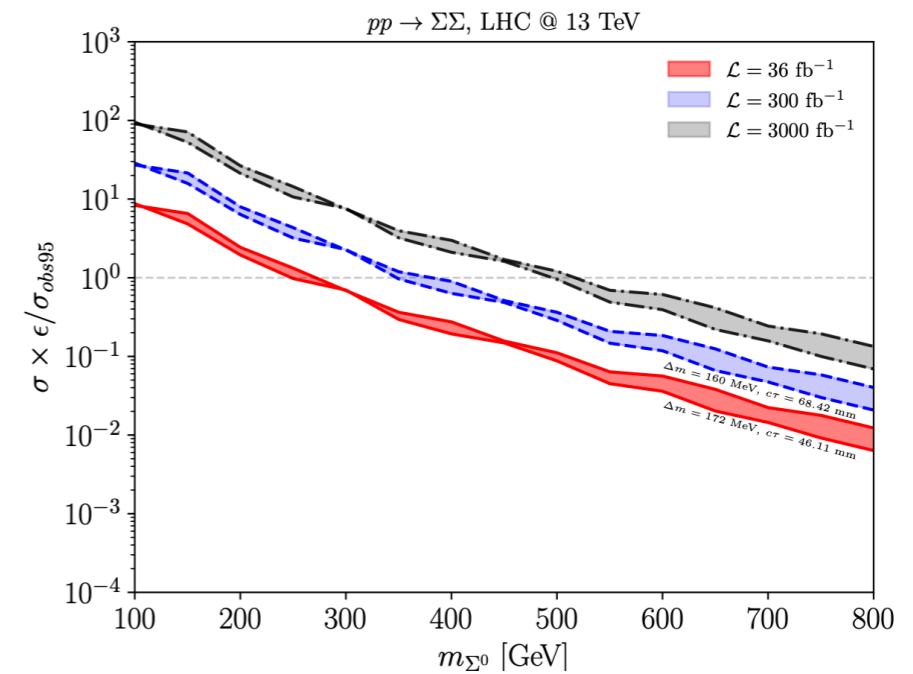
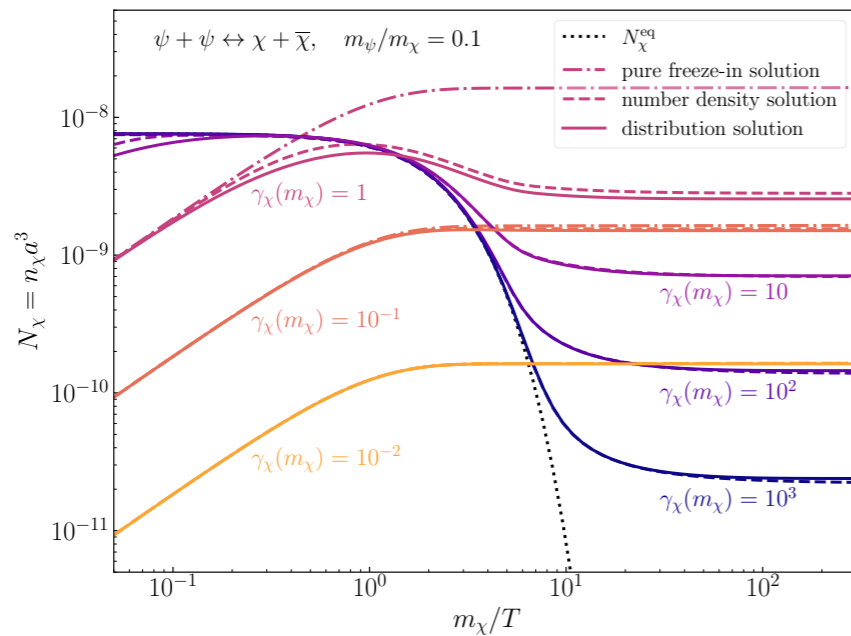
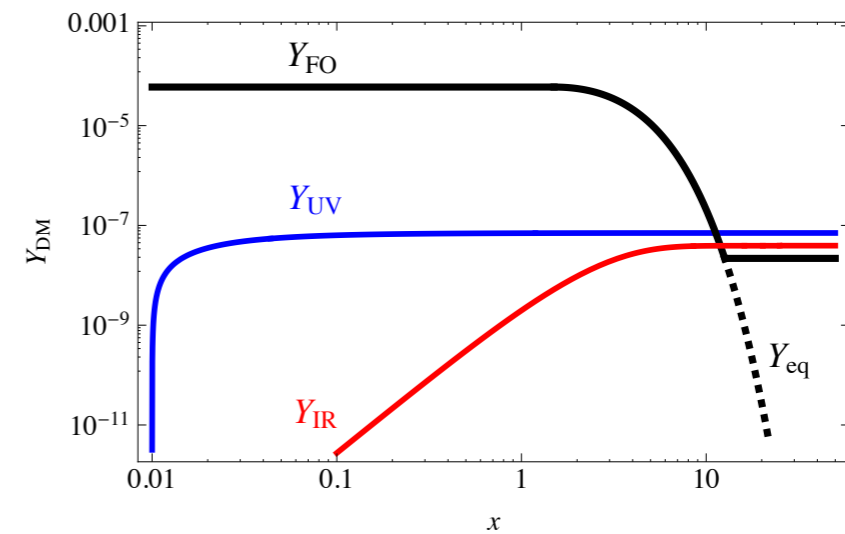
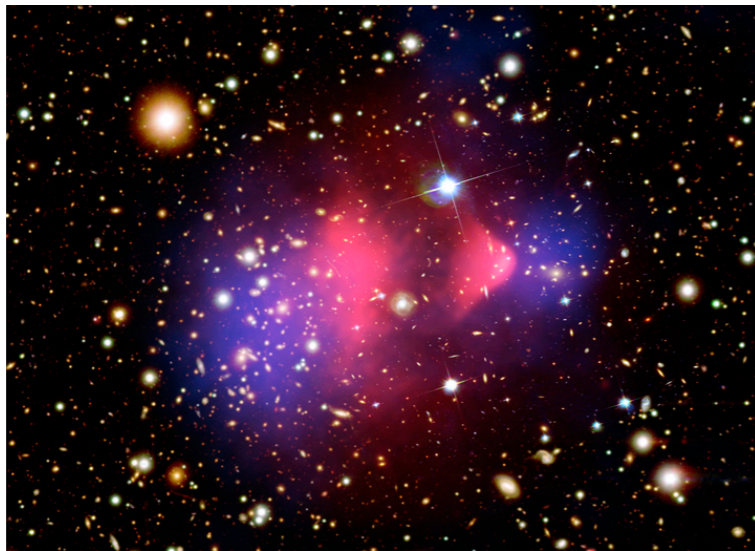
2206.08326, with Jorge de Blas, Christophe Grojean, Jiayin Gu, Victor Miralles, Michael Peskin, Junping Tian, Marcel Vos, Eleni Vryonidou



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The SM, up to now, is very successful. But there are some flaws:

Elahi et al, 1410.6157

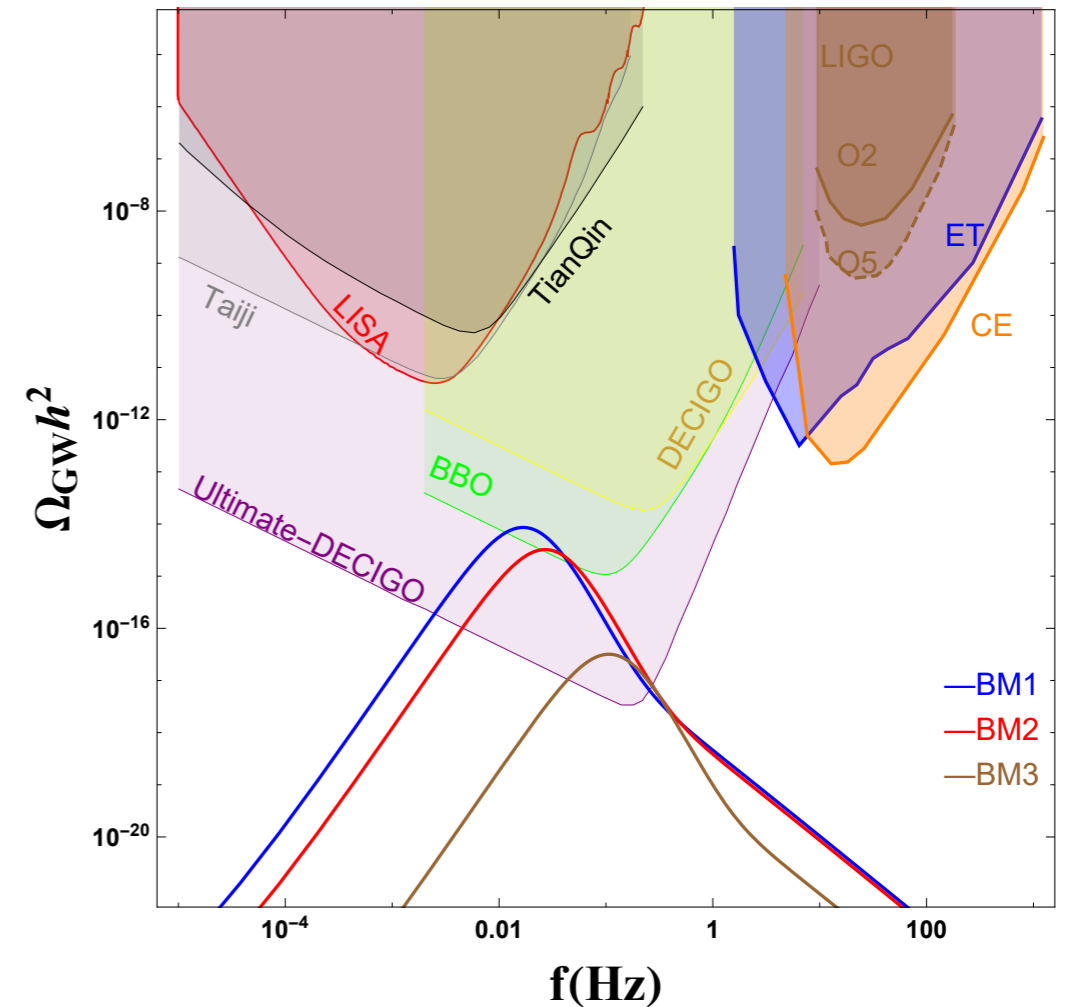
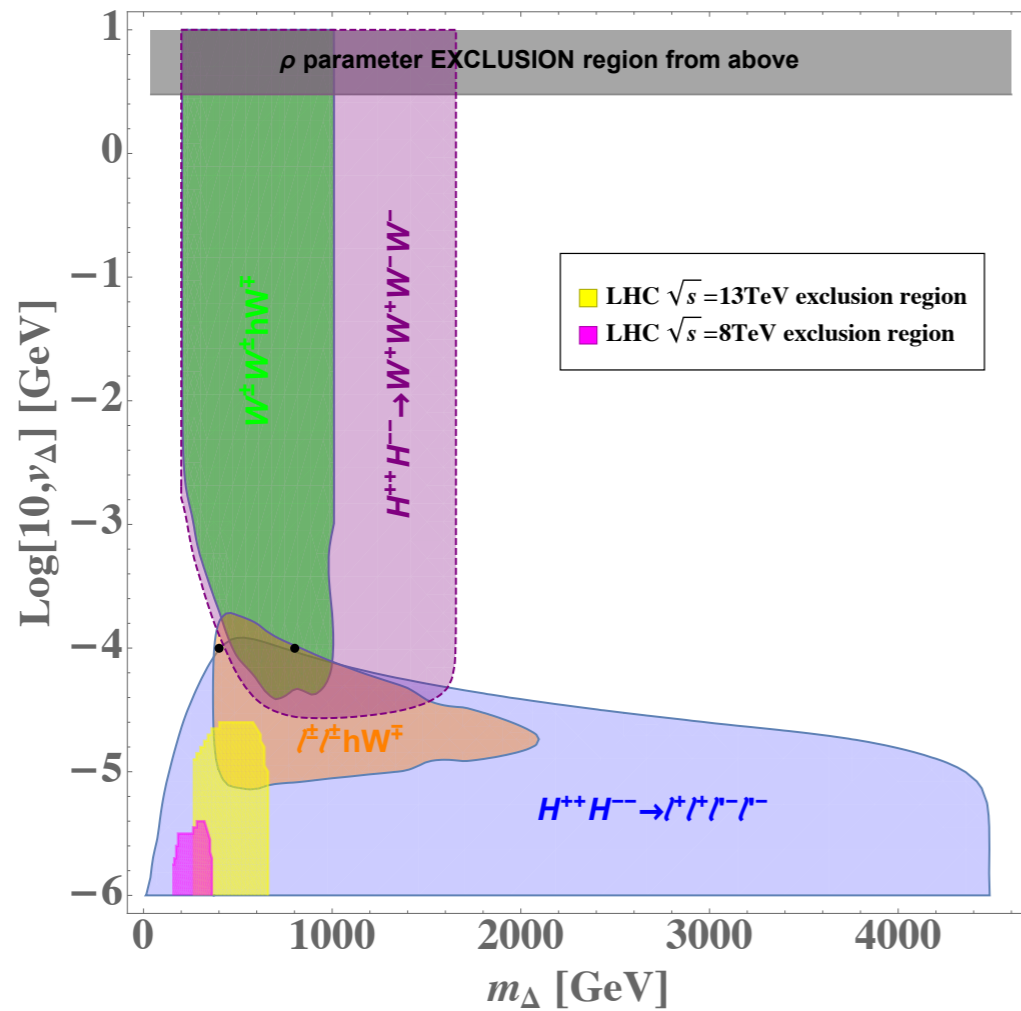
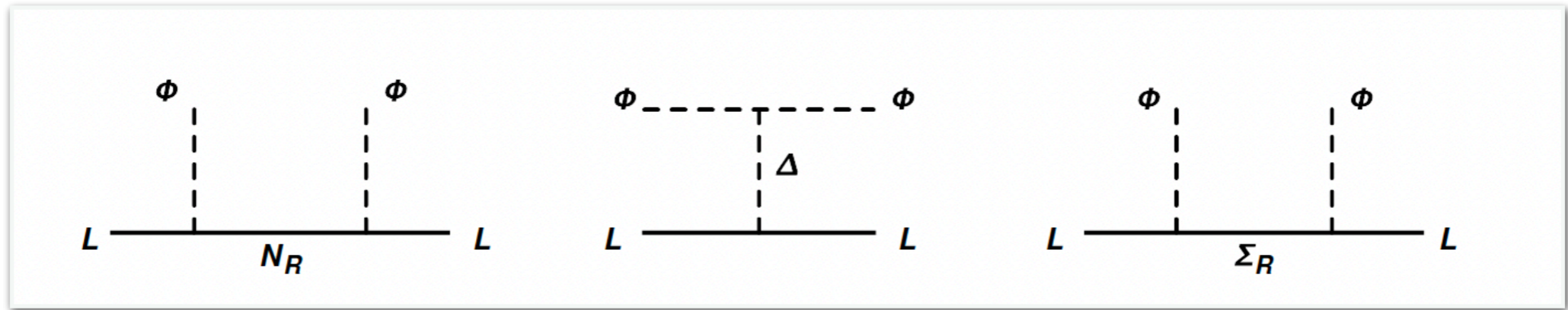


**YD**, Huang, Li, Yu, 2005.01717 (JHEP)

**YD**, Huang, Li, Li, Yu, 2111.01267 (JCAP)

Chiang, Cottin, **YD**, Fuyuto, Ramsey-Musolf, 2003.07867 (JHEP)

On the other hand, neutrinos oscillate



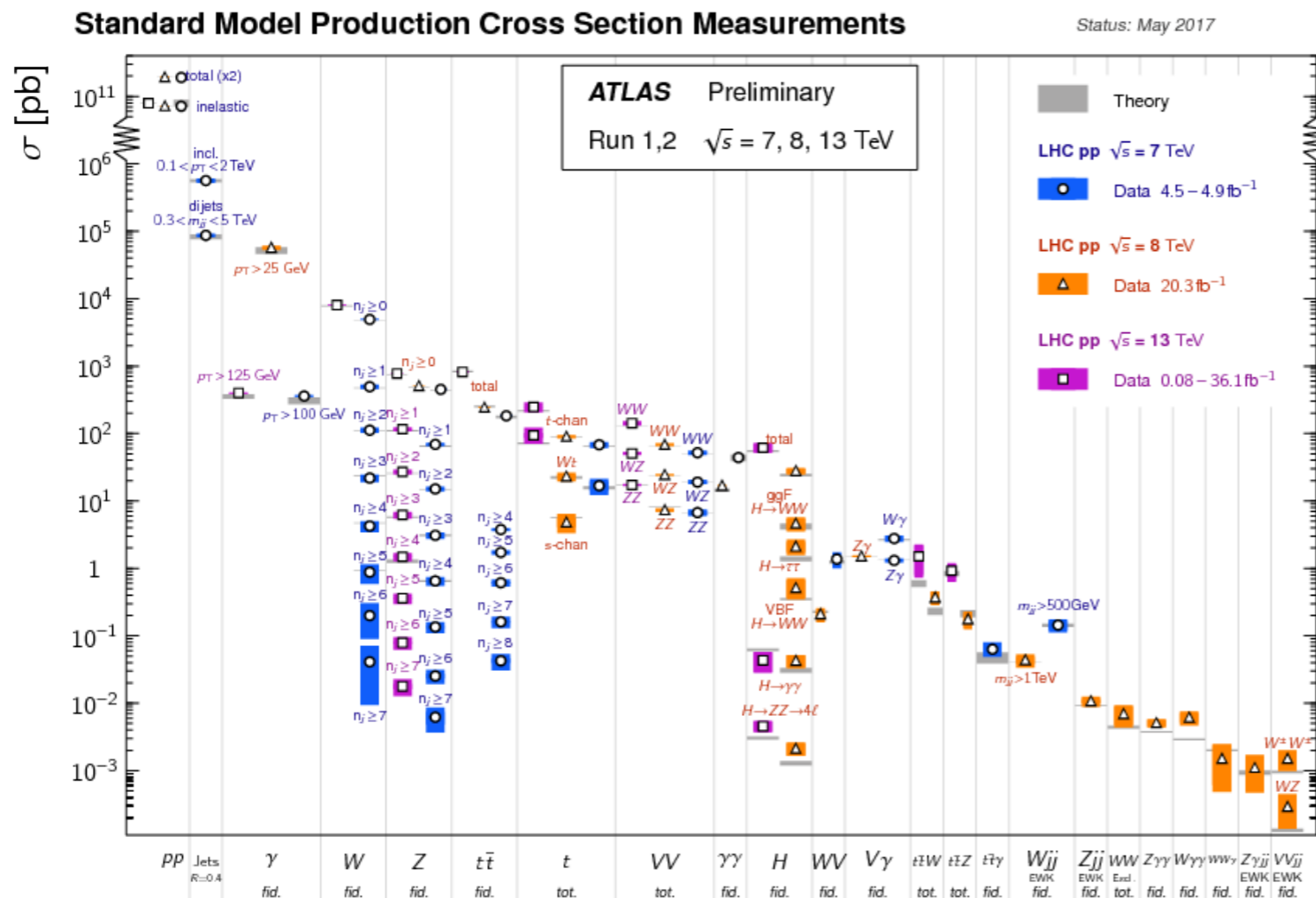
**YD**, Dunbrack, Ramsey-Musolf, Yu, 1810.09450 (JHEP)

Zhou, Bian, **YD**, 2203.01561 (JHEP)

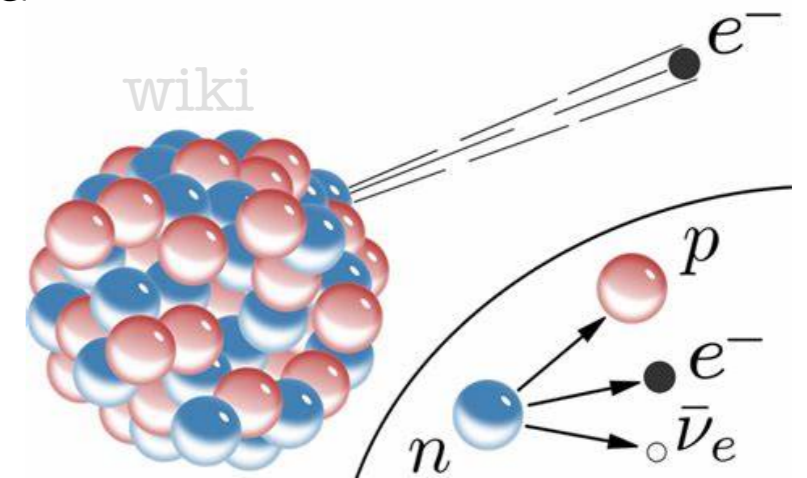
While there are many models for dark matter, neutrinos and other topics as you prefer, the direct experimental observation of any new particle is still null.

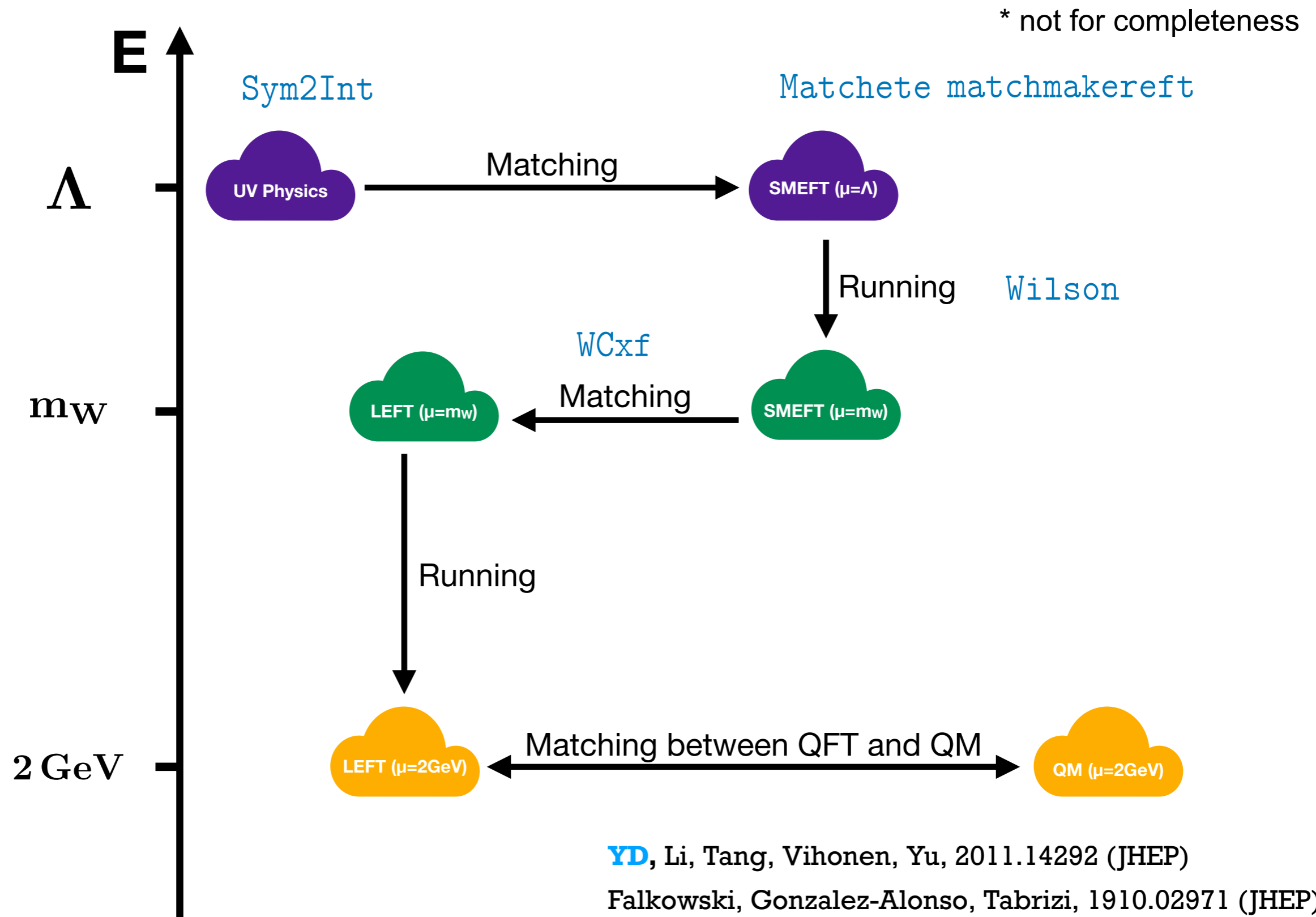
**Q: How to approach new physics beyond the Standard Model?**

**A: ...**



The experimental data are suggesting that the SM is an effective low-energy theory of some UV model above the weak scale.





## Operators in the Warsaw basis:

$X^3$		$\varphi^6$ and $\varphi^4 D^2$		$\psi^2 \varphi^3$	
$Q_G$	$f^{ABC} G_\mu^{A\nu} G_\nu^{B\rho} G_\rho^{C\mu}$	$Q_\varphi$	$(\varphi^\dagger \varphi)^3$	$Q_{e\varphi}$	$(\varphi^\dagger \varphi)(\bar{l}_p e_r \varphi)$
$Q_{\tilde{G}}$	$f^{ABC} \tilde{G}_\mu^{A\nu} G_\nu^{B\rho} G_\rho^{C\mu}$	$Q_{\varphi\Box}$	$(\varphi^\dagger \varphi)\Box(\varphi^\dagger \varphi)$	$Q_{u\varphi}$	$(\varphi^\dagger \varphi)(\bar{q}_p u_r \tilde{\varphi})$
$Q_W$	$\varepsilon^{IJK} W_\mu^{I\nu} W_\nu^{J\rho} W_\rho^{K\mu}$	$Q_{\varphi D}$	$(\varphi^\dagger D^\mu \varphi)^* (\varphi^\dagger D_\mu \varphi)$	$Q_{d\varphi}$	$(\varphi^\dagger \varphi)(\bar{q}_p d_r \varphi)$
$Q_{\tilde{W}}$	$\varepsilon^{IJK} \tilde{W}_\mu^{I\nu} W_\nu^{J\rho} W_\rho^{K\mu}$				
$X^2 \varphi^2$		$\psi^2 X \varphi$		$\psi^2 \varphi^2 D$	
$Q_{\varphi G}$	$\varphi^\dagger \varphi G_{\mu\nu}^A G^{A\mu\nu}$	$Q_{eW}$	$(\bar{l}_p \sigma^{\mu\nu} e_r) \tau^I \varphi W_{\mu\nu}^I$	$Q_{\varphi l}^{(1)}$	$(\varphi^\dagger i \overleftrightarrow{D}_\mu \varphi)(\bar{l}_p \gamma^\mu l_r)$
$Q_{\varphi \tilde{G}}$	$\varphi^\dagger \varphi \tilde{G}_{\mu\nu}^A G^{A\mu\nu}$	$Q_{eB}$	$(\bar{l}_p \sigma^{\mu\nu} e_r) \varphi B_{\mu\nu}$	$Q_{\varphi l}^{(3)}$	$(\varphi^\dagger i \overleftrightarrow{D}_\mu^I \varphi)(\bar{l}_p \tau^I \gamma^\mu l_r)$
$Q_{\varphi W}$	$\varphi^\dagger \varphi W_{\mu\nu}^I W^{I\mu\nu}$	$Q_{uG}$	$(\bar{q}_p \sigma^{\mu\nu} T^A u_r) \tilde{\varphi} G_{\mu\nu}^A$	$Q_{\varphi e}$	$(\varphi^\dagger i \overleftrightarrow{D}_\mu \varphi)(\bar{e}_p \gamma^\mu e_r)$
$Q_{\varphi \tilde{W}}$	$\varphi^\dagger \varphi \tilde{W}_{\mu\nu}^I W^{I\mu\nu}$	$Q_{uW}$	$(\bar{q}_p \sigma^{\mu\nu} u_r) \tau^I \tilde{\varphi} W_{\mu\nu}^I$	$Q_{\varphi q}^{(1)}$	$(\varphi^\dagger i \overleftrightarrow{D}_\mu \varphi)(\bar{q}_p \gamma^\mu q_r)$
$Q_{\varphi B}$	$\varphi^\dagger \varphi B_{\mu\nu} B^{\mu\nu}$	$Q_{uB}$	$(\bar{q}_p \sigma^{\mu\nu} u_r) \tilde{\varphi} B_{\mu\nu}$	$Q_{\varphi q}^{(3)}$	$(\varphi^\dagger i \overleftrightarrow{D}_\mu^I \varphi)(\bar{q}_p \tau^I \gamma^\mu q_r)$
$Q_{\varphi \tilde{B}}$	$\varphi^\dagger \varphi \tilde{B}_{\mu\nu} B^{\mu\nu}$	$Q_{dG}$	$(\bar{q}_p \sigma^{\mu\nu} T^A d_r) \varphi G_{\mu\nu}^A$	$Q_{\varphi u}$	$(\varphi^\dagger i \overleftrightarrow{D}_\mu \varphi)(\bar{u}_p \gamma^\mu u_r)$
$Q_{\varphi WB}$	$\varphi^\dagger \tau^I \varphi W_{\mu\nu}^I B^{\mu\nu}$	$Q_{dW}$	$(\bar{q}_p \sigma^{\mu\nu} d_r) \tau^I \varphi W_{\mu\nu}^I$	$Q_{\varphi d}$	$(\varphi^\dagger i \overleftrightarrow{D}_\mu \varphi)(\bar{d}_p \gamma^\mu d_r)$
$Q_{\varphi \tilde{W}B}$	$\varphi^\dagger \tau^I \varphi \tilde{W}_{\mu\nu}^I B^{\mu\nu}$	$Q_{dB}$	$(\bar{q}_p \sigma^{\mu\nu} d_r) \varphi B_{\mu\nu}$	$Q_{\varphi ud}$	$i(\tilde{\varphi}^\dagger D_\mu \varphi)(\bar{u}_p \gamma^\mu d_r)$

$(\bar{L}L)(\bar{L}L)$		$(\bar{R}R)(\bar{R}R)$		$(\bar{L}L)(\bar{R}R)$	
$Q_{ll}$	$(\bar{l}_p \gamma_\mu l_r)(\bar{l}_s \gamma^\mu l_t)$	$Q_{ee}$	$(\bar{e}_p \gamma_\mu e_r)(\bar{e}_s \gamma^\mu e_t)$	$Q_{le}$	$(\bar{l}_p \gamma_\mu l_r)(\bar{e}_s \gamma^\mu e_t)$
$Q_{qq}^{(1)}$	$(\bar{q}_p \gamma_\mu q_r)(\bar{q}_s \gamma^\mu q_t)$	$Q_{uu}$	$(\bar{u}_p \gamma_\mu u_r)(\bar{u}_s \gamma^\mu u_t)$	$Q_{lu}$	$(\bar{l}_p \gamma_\mu l_r)(\bar{u}_s \gamma^\mu u_t)$
$Q_{qq}^{(3)}$	$(\bar{q}_p \gamma_\mu \tau^I q_r)(\bar{q}_s \gamma^\mu \tau^I q_t)$	$Q_{dd}$	$(\bar{d}_p \gamma_\mu d_r)(\bar{d}_s \gamma^\mu d_t)$	$Q_{ld}$	$(\bar{l}_p \gamma_\mu l_r)(\bar{d}_s \gamma^\mu d_t)$
$Q_{lq}^{(1)}$	$(\bar{l}_p \gamma_\mu l_r)(\bar{q}_s \gamma^\mu q_t)$	$Q_{eu}$	$(\bar{e}_p \gamma_\mu e_r)(\bar{u}_s \gamma^\mu u_t)$	$Q_{qe}$	$(\bar{q}_p \gamma_\mu q_r)(\bar{e}_s \gamma^\mu e_t)$
$Q_{lq}^{(3)}$	$(\bar{l}_p \gamma_\mu \tau^I l_r)(\bar{q}_s \gamma^\mu \tau^I q_t)$	$Q_{ed}$	$(\bar{e}_p \gamma_\mu e_r)(\bar{d}_s \gamma^\mu d_t)$	$Q_{qu}^{(1)}$	$(\bar{q}_p \gamma_\mu q_r)(\bar{u}_s \gamma^\mu u_t)$
		$Q_{ud}^{(1)}$	$(\bar{u}_p \gamma_\mu u_r)(\bar{d}_s \gamma^\mu d_t)$	$Q_{qu}^{(8)}$	$(\bar{q}_p \gamma_\mu T^A q_r)(\bar{u}_s \gamma^\mu T^A u_t)$
		$Q_{ud}^{(8)}$	$(\bar{u}_p \gamma_\mu T^A u_r)(\bar{d}_s \gamma^\mu T^A d_t)$	$Q_{qd}^{(1)}$	$(\bar{q}_p \gamma_\mu q_r)(\bar{d}_s \gamma^\mu d_t)$
				$Q_{qd}^{(8)}$	$(\bar{q}_p \gamma_\mu T^A q_r)(\bar{d}_s \gamma^\mu T^A d_t)$
$(\bar{L}R)(\bar{R}L)$ and $(\bar{L}R)(\bar{L}R)$		$B$ -violating			
$Q_{ledq}$	$(\bar{l}_p^j e_r)(\bar{d}_s q_t^j)$	$Q_{duq}$	$\varepsilon^{\alpha\beta\gamma} \varepsilon_{jk} [(d_p^\alpha)^T C u_r^\beta] [(q_s^{\gamma j})^T C l_t^k]$		
$Q_{quqd}^{(1)}$	$(\bar{q}_p^j u_r) \varepsilon_{jk} (\bar{q}_s^k d_t)$	$Q_{ququ}$	$\varepsilon^{\alpha\beta\gamma} \varepsilon_{jk} [(q_p^{\alpha j})^T C q_r^{\beta k}] [(u_s^\gamma)^T C e_t]$		
$Q_{quqd}^{(8)}$	$(\bar{q}_p^j T^A u_r) \varepsilon_{jk} (\bar{q}_s^k T^A d_t)$	$Q_{qqq}$	$\varepsilon^{\alpha\beta\gamma} \varepsilon_{jn} \varepsilon_{km} [(q_p^{\alpha j})^T C q_r^{\beta k}] [(q_s^{\gamma m})^T C l_t^n]$		
$Q_{lequ}^{(1)}$	$(\bar{l}_p^j e_r) \varepsilon_{jk} (\bar{q}_s^k u_t)$	$Q_{duu}$	$\varepsilon^{\alpha\beta\gamma} [(d_p^\alpha)^T C u_r^\beta] [(u_s^\gamma)^T C e_t]$		
$Q_{lequ}^{(3)}$	$(\bar{l}_p^j \sigma_{\mu\nu} e_r) \varepsilon_{jk} (\bar{q}_s^k \sigma^{\mu\nu} u_t)$				

59 operators (+ 4 B-violating ones)

2499 operators: 1350 (CP-even) + 1149 (CP-odd)

No flavor assumptions are made.

We choose to work in the Higgs basis

$$\begin{aligned}
 \mathcal{L} \supset & eA^\mu \sum_{f=u,d,e} Q_f (\bar{f}_I \bar{\sigma}_\mu f_I + f_I^c \sigma_\mu \bar{f}_I^c) \\
 & + \frac{g_L}{\sqrt{2}} \left[ W^{\mu+} \bar{\nu}_I \bar{\sigma}_\mu (\delta_{IJ} + [\delta g_L^{W\ell}]_{IJ}) e_J + W^{\mu+} \bar{u}_I \bar{\sigma}_\mu \left( V_{IJ} + [\delta g_L^{Wq}]_{IJ} \right) d_J + \text{h.c.} \right] \\
 & + \frac{g_L}{\sqrt{2}} \left[ W^{\mu+} u_I^c \sigma_\mu [\delta g_R^{Wq}]_{IJ} \bar{d}_J^c + \text{h.c.} \right] \\
 & + \sqrt{g_L^2 + g_Y^2} Z^\mu \sum_{f=u,d,e,\nu} \bar{f}_I \bar{\sigma}_\mu \left( (T_3^f - s_w^2 Q_f) \delta_{IJ} + [\delta g_L^{Zf}]_{IJ} \right) f_J \\
 & + \sqrt{g_L^2 + g_Y^2} Z^\mu \sum_{f=u,d,e} f_I^c \sigma_\mu \left( -s_w^2 Q_f \delta_{IJ} + [\delta g_R^{Zf}]_{IJ} \right) \bar{f}_J^c,
 \end{aligned}$$

We choose to work in the Higgs basis

$$\begin{aligned}
 \delta g_{LWe} &\rightarrow c_{\text{HL3}}^{\text{Warsaw}} v^2 - \frac{c_{\text{HD}}^{\text{Warsaw}} g_L^2 v^2}{4 (g_L^2 - g_Y^2)} - \frac{c_{\text{HWB}}^{\text{Warsaw}} g_L g_Y v^2}{g_L^2 - g_Y^2} - \frac{g_L^2 v^2 \Delta\text{GF}}{2 (g_L^2 - g_Y^2)} \\
 \delta g_{LZe} &\rightarrow -\frac{c_{\text{HL1}}^{\text{Warsaw}} v^2}{2} - \frac{c_{\text{HL3}}^{\text{Warsaw}} v^2}{2} + \frac{c_{\text{HWB}}^{\text{Warsaw}} g_L g_Y v^2}{g_L^2 - g_Y^2} + \frac{c_{\text{HD}}^{\text{Warsaw}} (g_L^2 + g_Y^2) v^2}{8 (g_L^2 - g_Y^2)} + \frac{(g_L^2 + g_Y^2) v^2 \Delta\text{GF}}{4 (g_L^2 - g_Y^2)} \\
 \delta g_{RZe} &\rightarrow -\frac{c_{\text{He1}}^{\text{Warsaw}} v^2}{2} + \frac{c_{\text{HD}}^{\text{Warsaw}} g_Y^2 v^2}{4 g_L^2 - 4 g_Y^2} + \frac{c_{\text{HWB}}^{\text{Warsaw}} g_L g_Y v^2}{g_L^2 - g_Y^2} + \frac{g_Y^2 v^2 \Delta\text{GF}}{2 g_L^2 - 2 g_Y^2} \\
 \delta g_{LZu} &\rightarrow -\frac{c_{\text{Hq1}}^{\text{Warsaw}} v^2}{2} + \frac{c_{\text{Hq3}}^{\text{Warsaw}} v^2}{2} - \frac{2 c_{\text{HWB}}^{\text{Warsaw}} g_L g_Y v^2}{3 (g_L^2 - g_Y^2)} - \frac{c_{\text{HD}}^{\text{Warsaw}} (3 g_L^2 + g_Y^2) v^2}{24 (g_L^2 - g_Y^2)} - \frac{(3 g_L^2 + g_Y^2) v^2 \Delta\text{GF}}{12 (g_L^2 - g_Y^2)} \\
 \delta g_{LZd} &\rightarrow -\frac{c_{\text{Hq1}}^{\text{Warsaw}} v^2}{2} - \frac{c_{\text{Hq3}}^{\text{Warsaw}} v^2}{2} + \frac{c_{\text{HWB}}^{\text{Warsaw}} g_L g_Y v^2}{3 g_L^2 - 3 g_Y^2} + \frac{c_{\text{HD}}^{\text{Warsaw}} (3 g_L^2 - g_Y^2) v^2}{24 (g_L^2 - g_Y^2)} + \frac{(3 g_L^2 - g_Y^2) v^2 \Delta\text{GF}}{12 (g_L^2 - g_Y^2)} \\
 \delta g_{RZu} &\rightarrow -\frac{c_{\text{Hu}}^{\text{Warsaw}} v^2}{2} - \frac{2 c_{\text{HWB}}^{\text{Warsaw}} g_L g_Y v^2}{3 (g_L^2 - g_Y^2)} + \frac{c_{\text{HD}}^{\text{Warsaw}} g_Y^2 v^2}{6 (-g_L^2 + g_Y^2)} + \frac{g_Y^2 v^2 \Delta\text{GF}}{3 (-g_L^2 + g_Y^2)} \\
 \delta g_{RZd} &\rightarrow -\frac{c_{\text{Hd}}^{\text{Warsaw}} v^2}{2} + \frac{c_{\text{HWB}}^{\text{Warsaw}} g_L g_Y v^2}{3 g_L^2 - 3 g_Y^2} + \frac{c_{\text{HD}}^{\text{Warsaw}} g_Y^2 v^2}{12 (g_L^2 - g_Y^2)} + \frac{g_Y^2 v^2 \Delta\text{GF}}{6 g_L^2 - 6 g_Y^2}
 \end{aligned}$$



We only consider flavor conserving 4-fermion operators

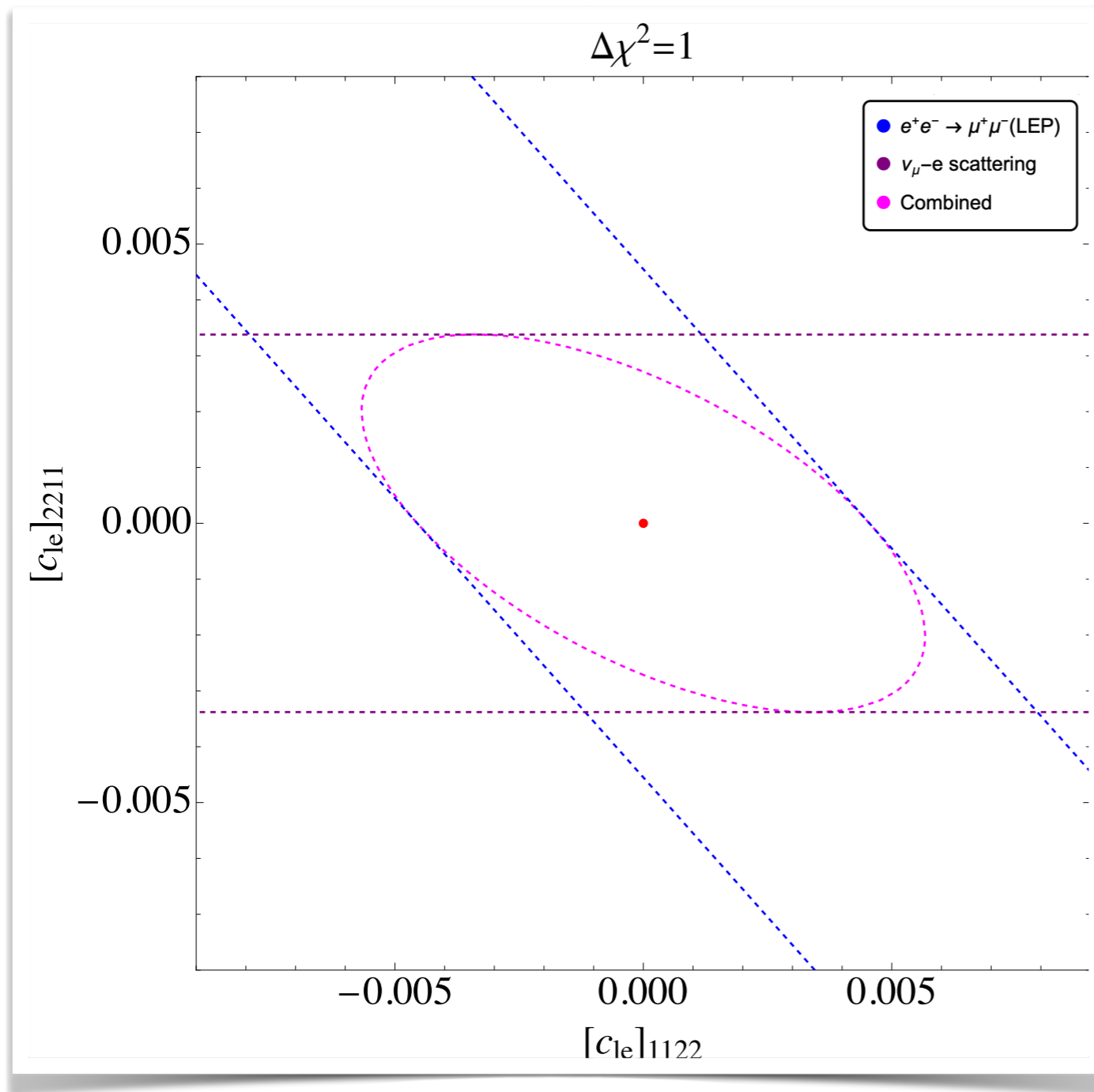
$2\ell 2q$ operators ( $p, r = 1, 2, 3$ )	$4\ell$ operators ( $p < r = 1, 2, 3$ )
Chirality conserving	Two flavors
$[\mathcal{O}_{\ell q}]_{pprr} = (\bar{\ell}_p \bar{\sigma}_\mu \ell_p)(\bar{q}_r \bar{\sigma}^\mu q_r)$	$[\mathcal{O}_{\ell\ell}]_{pprr} = (\bar{\ell}_p \bar{\sigma}_\mu \ell_p)(\bar{\ell}_r \bar{\sigma}^\mu \ell_r)$
$[\mathcal{O}_{\ell q}^{(3)}]_{pprr} = (\bar{\ell}_p \bar{\sigma}_\mu \sigma^i \ell_p)(\bar{q}_r \bar{\sigma}^\mu \sigma^i q_r)$	$[\mathcal{O}_{\ell\ell}]_{prrp} = (\bar{\ell}_p \bar{\sigma}_\mu \ell_r)(\bar{\ell}_r \bar{\sigma}^\mu \ell_p)$
$[\mathcal{O}_{\ell u}]_{pprr} = (\bar{\ell}_p \bar{\sigma}_\mu \ell_p)(u_r^c \sigma^\mu \bar{u}_r^c)$	$[\mathcal{O}_{\ell e}]_{pprr} = (\bar{\ell}_p \bar{\sigma}_\mu \ell_p)(e_r^c \sigma^\mu \bar{e}_r^c)$
$[\mathcal{O}_{\ell d}]_{pprr} = (\bar{\ell}_p \bar{\sigma}_\mu \ell_p)(d_r^c \sigma^\mu \bar{d}_r^c)$	$[\mathcal{O}_{\ell e}]_{rrpp} = (\bar{\ell}_r \bar{\sigma}_\mu \ell_r)(e_p^c \sigma^\mu \bar{e}_p^c)$
$[\mathcal{O}_{eq}]_{pprr} = (e_p^c \sigma_\mu \bar{e}_p^c)(\bar{q}_r \bar{\sigma}^\mu q_r)$	$[\mathcal{O}_{\ell e}]_{prrp} = (\bar{\ell}_p \bar{\sigma}_\mu \ell_r)(e_r^c \sigma^\mu \bar{e}_p^c)$
$[\mathcal{O}_{eu}]_{pprr} = (e_p^c \sigma_\mu \bar{e}_p^c)(u_r^c \sigma^\mu \bar{u}_r^c)$	$[\mathcal{O}_{ee}]_{pprr} = (e_p^c \sigma_\mu \bar{e}_p^c)(e_r^c \sigma^\mu \bar{e}_r^c)$
$[\mathcal{O}_{ed}]_{pprr} = (e_p^c \sigma_\mu \bar{e}_p^c)(d_r^c \sigma^\mu \bar{d}_r^c)$	
Chirality violating	One flavor
$[\mathcal{O}_{lequ}]_{pprr} = (\bar{\ell}_p^j \bar{e}_p^c) \epsilon_{jk} (\bar{q}_r^k \bar{u}_r^c)$	$[\mathcal{O}_{\ell\ell}]_{pppp} = \frac{1}{2} (\bar{\ell}_p \bar{\sigma}_\mu \ell_p)(\bar{\ell}_p \bar{\sigma}^\mu \ell_p)$
$[\mathcal{O}_{lequ}^{(3)}]_{pprr} = (\bar{\ell}_p^j \bar{\sigma}_{\mu\nu} \bar{e}_p^c) \epsilon_{jk} (\bar{q}_r^k \bar{\sigma}_{\mu\nu} \bar{u}_r^c)$	$[\mathcal{O}_{\ell e}]_{pppp} = (\bar{\ell}_p \bar{\sigma}_\mu \ell_p)(e_p^c \sigma^\mu \bar{e}_p^c)$
$[\mathcal{O}_{ledq}]_{pprr} = (\bar{\ell}_p^j \bar{e}_p^c)(d_r^c q_r^j)$	$[\mathcal{O}_{ee}]_{pppp} = \frac{1}{2} (e_p^c \sigma_\mu \bar{e}_p^c)(e_p^c \sigma^\mu \bar{e}_p^c)$

Full list of observables and different collider options are summarized in great detail in our snowmass paper [2206.08326](#)

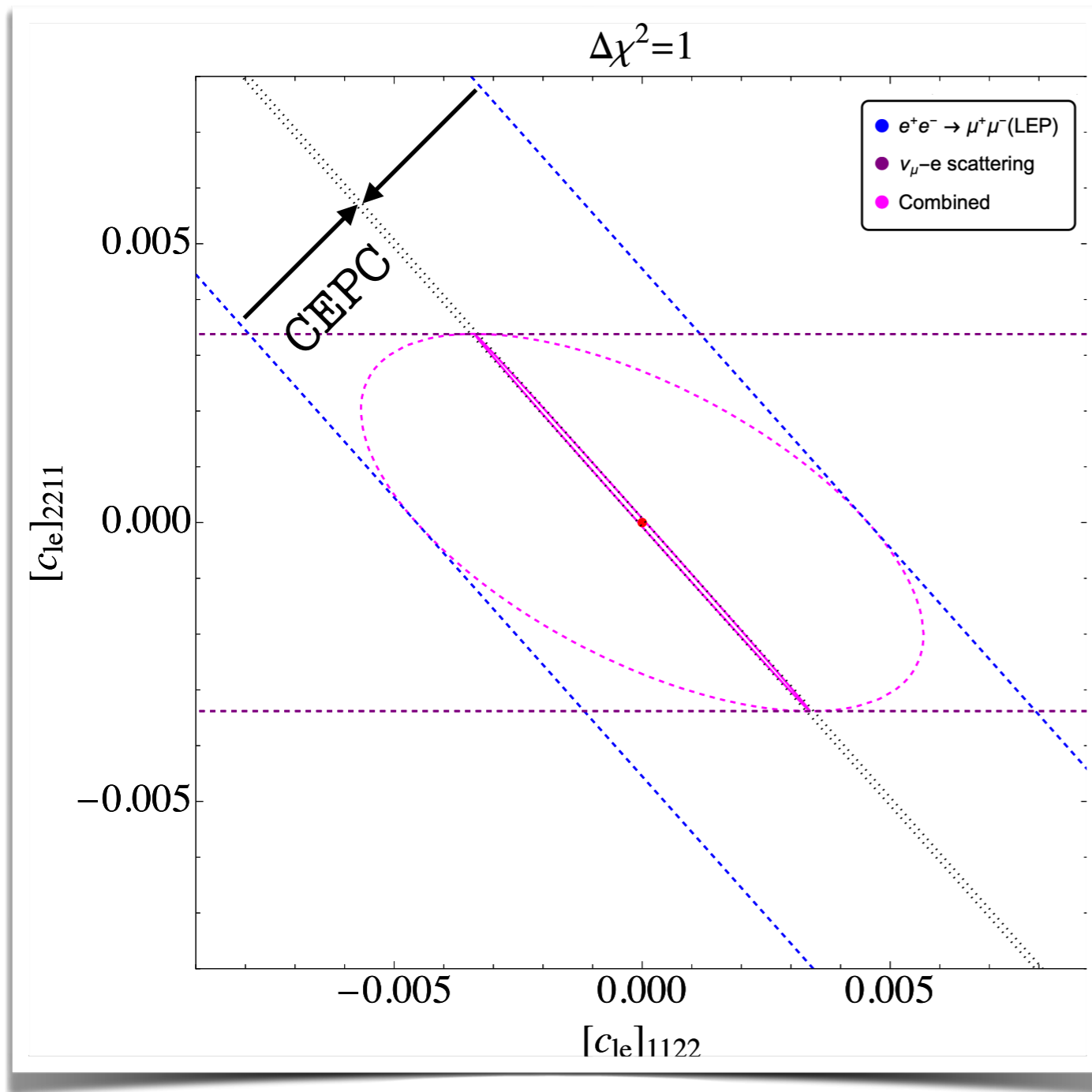
de Blas, **YD**, Grojean, Gu, Miralles, Peskin, Tian, Vos, Vryonidou, 2206.08326

Process	Observable	Experimental value	Ref.	SM prediction	
$\nu_{\mu}^{-} - e^{-}$ scattering	$g_{LV}^{\nu_{\mu}e}$	$-0.035 \pm 0.017$	CHARM-II [47]	$-0.0396$ [48]	
	$g_{LA}^{\nu_{\mu}e}$	$-0.503 \pm 0.017$		$-0.5064$ [48]	
$\tau$ decay	$\frac{G_{\tau e}^2}{G_F^2}$	$1.0029 \pm 0.0046$	PDG2014 [49]	1	
	$\frac{G_{\tau \mu}^2}{G_F^2}$	$0.981 \pm 0.018$			
Neutrino scattering	$R_{\nu_{\mu}}$	$0.3093 \pm 0.0031$	CHARM ( $r = 0.456$ ) [50]	$0.3156$ [50]	
	$R_{\bar{\nu}_{\mu}}$	$0.390 \pm 0.014$		$0.370$ [50]	
	$R_{\nu_{\mu}}$	$0.3072 \pm 0.0033$	CDHS ( $r = 0.393$ ) [51]	$0.3091$ [51]	
	$R_{\bar{\nu}_{\mu}}$	$0.382 \pm 0.016$		$0.380$ [51]	
	$\kappa$	$0.5820 \pm 0.0041$	CCFR [52]	$0.5830$ [52]	
	$R_{\nu_e \bar{\nu}_e}$	$0.406^{+0.145}_{-0.135}$	CHARM [53]	$0.33$ [54]	
Parity-violating scattering	$(s_w^2)^{\text{Møller}}$	$0.2397 \pm 0.0013$	SLAC-E158 [55]	$0.2381 \pm 0.0006$ [56]	
	$Q_W^{\text{Cs}}(55, 78)$	$-72.62 \pm 0.43$	PDG2016 [54]	$-73.25 \pm 0.02$ [54]	
	$Q_W^{\text{P}}(1, 0)$	$0.064 \pm 0.012$	QWEAK [57]	$0.0708 \pm 0.0003$ [54]	
	$A_1$	$(-91.1 \pm 4.3) \times 10^{-6}$	PVDIS [58]	$(-87.7 \pm 0.7) \times 10^{-6}$ [58]	
	$A_2$	$(-160.8 \pm 7.1) \times 10^{-6}$		$(-158.9 \pm 1.0) \times 10^{-6}$ [58]	
	$g_{VA}^{eu} - g_{VA}^{ed}$		$-0.042 \pm 0.057$	SAMPLE ( $\sqrt{Q^2} = 200$ MeV) [59]	$-0.0360$ [54]
			$-0.12 \pm 0.074$	SAMPLE ( $\sqrt{Q^2} = 125$ MeV) [59]	$0.0265$ [54]
$b_{\text{SPS}}$		$-(1.47 \pm 0.42) \times 10^{-4} \text{ GeV}^{-2}$	SPS ( $\lambda = 0.81$ ) [60]	$-1.56 \times 10^{-4} \text{ GeV}^{-2}$ [60]	
		$-(1.74 \pm 0.81) \times 10^{-4} \text{ GeV}^{-2}$	SPS ( $\lambda = 0.66$ ) [60]	$-1.57 \times 10^{-4} \text{ GeV}^{-2}$ [60]	
$\tau$ polarization	$\mathcal{P}_{\tau}$	$0.012 \pm 0.058$	VENUS [61]	$0.028$ [61]	
	$\mathcal{A}_{\mathcal{P}}$	$0.029 \pm 0.057$		$0.021$ [61]	
Neutrino trident production	$\frac{\sigma}{\sigma^{\text{SM}}}(\nu_{\mu} \gamma^* \rightarrow \nu_{\mu} \mu^+ \mu^-)$	$0.82 \pm 0.28$	CCFR [62–64]	1	
$d_I \rightarrow u_J \ell \bar{\nu}_{\ell}(\gamma)$	$\epsilon_{L,R,S,P,T}^{deJ}$	See text	[65]	0	
$e^+e^- \rightarrow f\bar{f}$	$\delta A_{LR}^e$	2.0%	SuperKEKB [66]	0.00015	
	$\delta A_{LR}^{\mu}$	1.5%		-0.0006	
	$\delta A_{LR}^{\tau}$	2.4%		-0.0006	
	$\delta A_{LR}^c$	0.5%		-0.005	
	$\delta A_{LR}^b$	0.4%		-0.020	

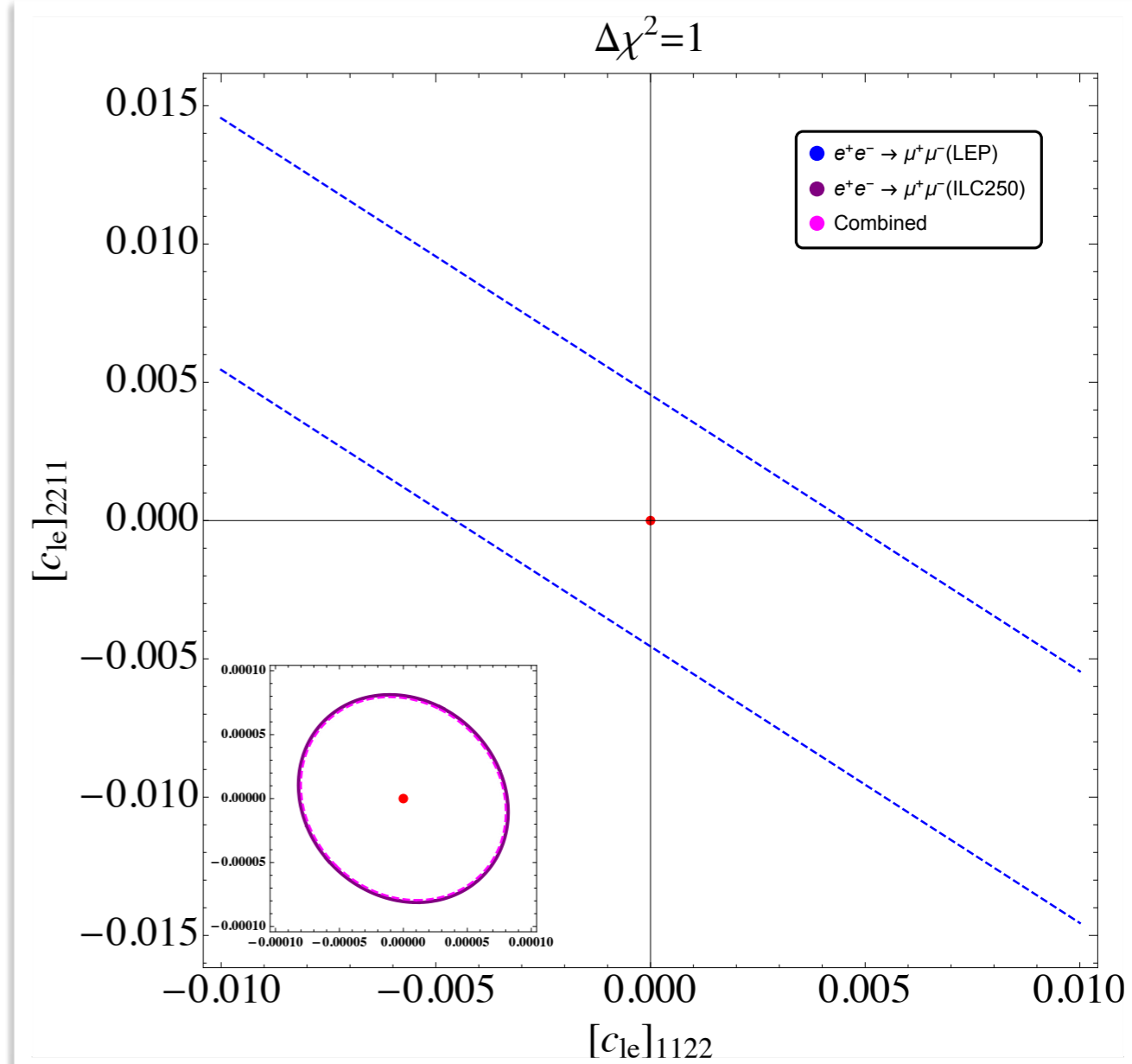
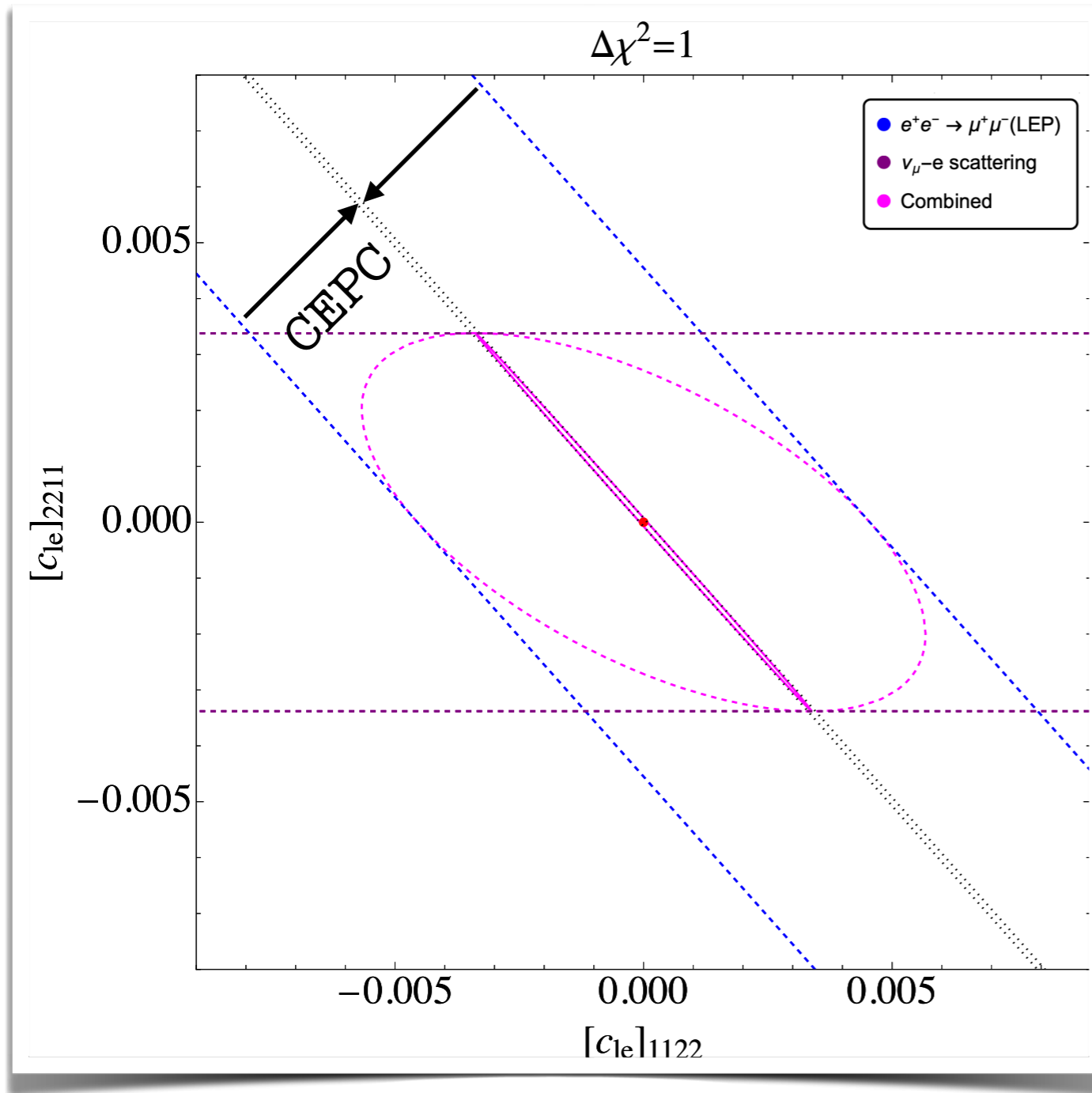
Flat direction lifted by low-energy experiments: **muon sector example**



Flat direction lifted by low-energy experiments: **muon sector example**

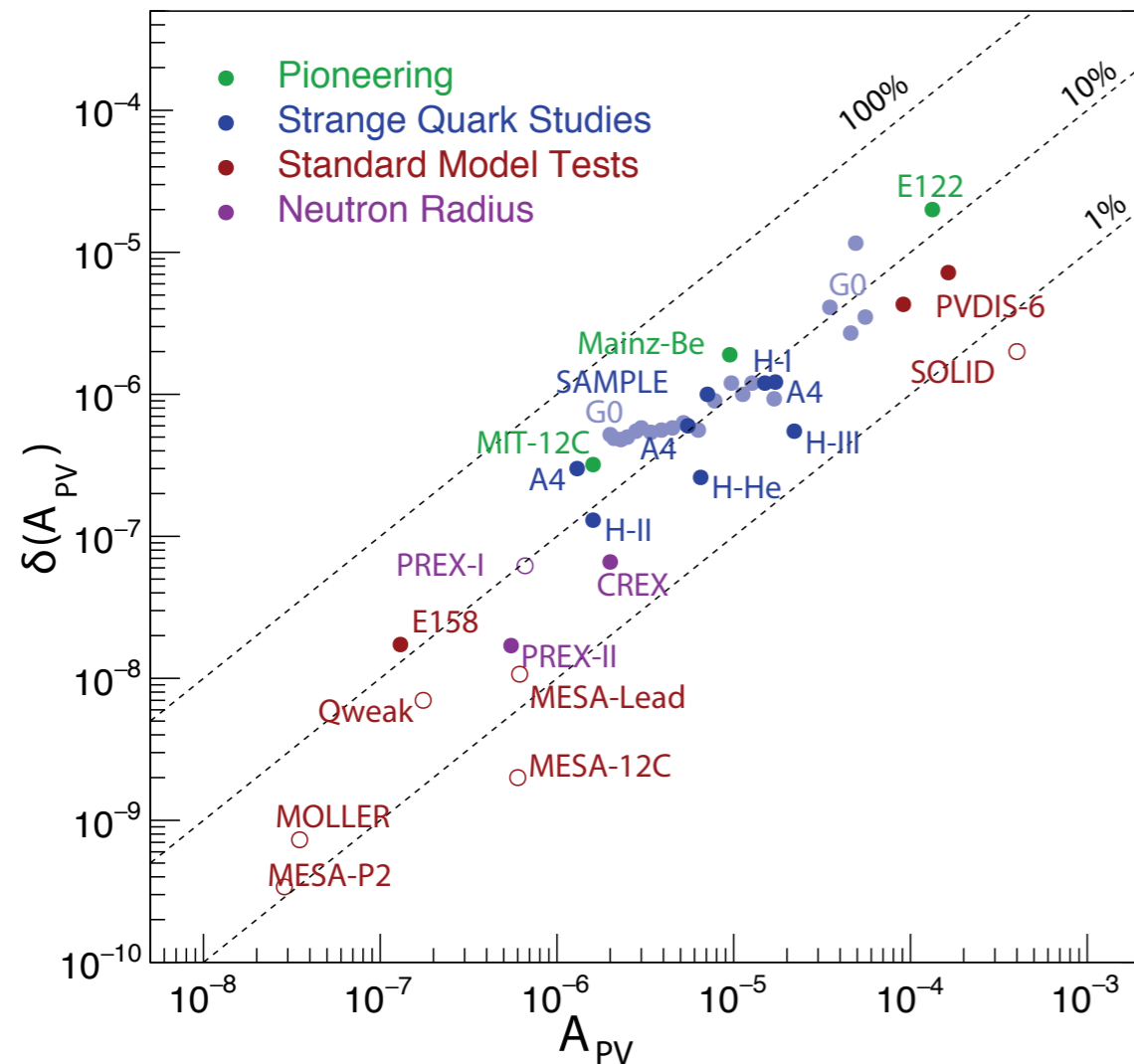


Flat direction lifted by low-energy experiments: **muon sector example**



Flat direction lifted by low-energy experiments: **electron sector example**

Bhabha alone is not enough to close the fit,  $A_{PV}$  from PVES is the key



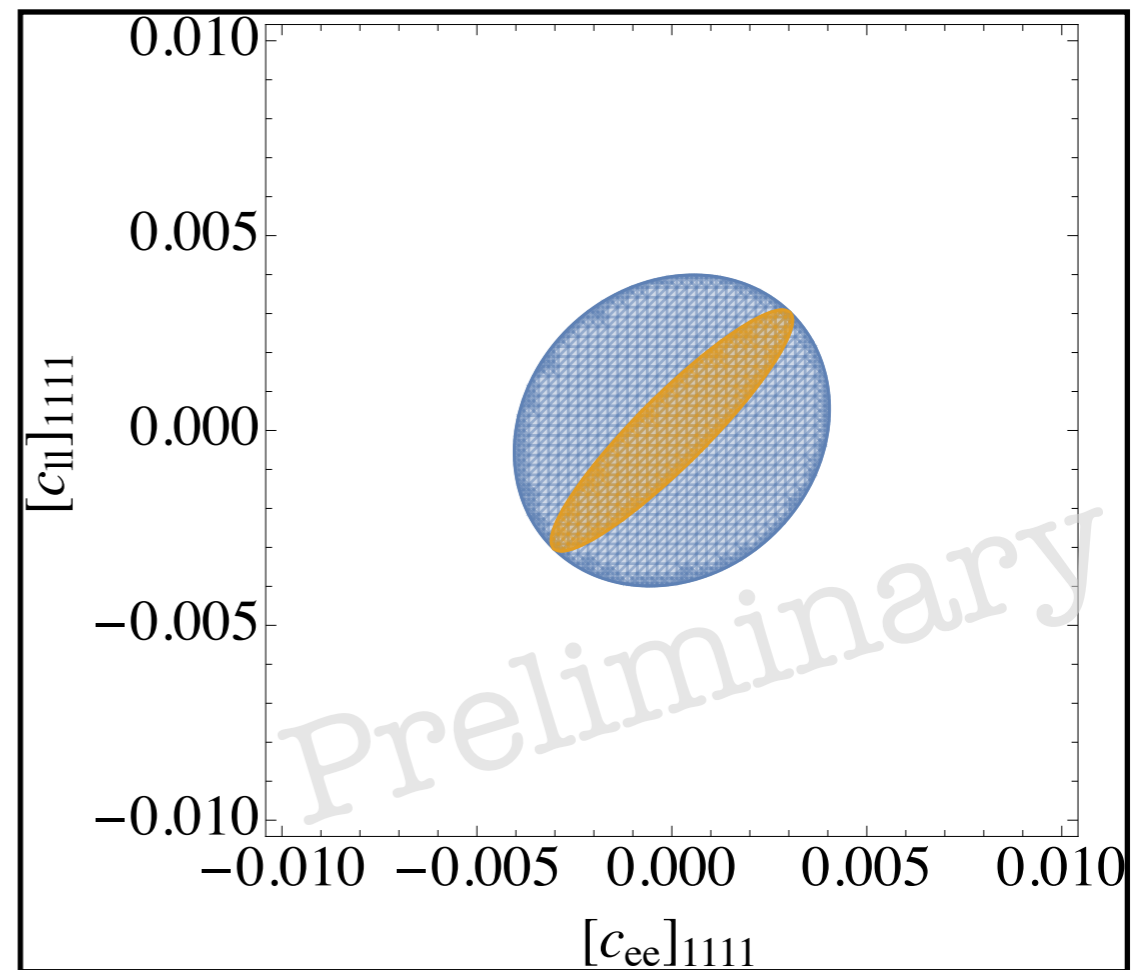
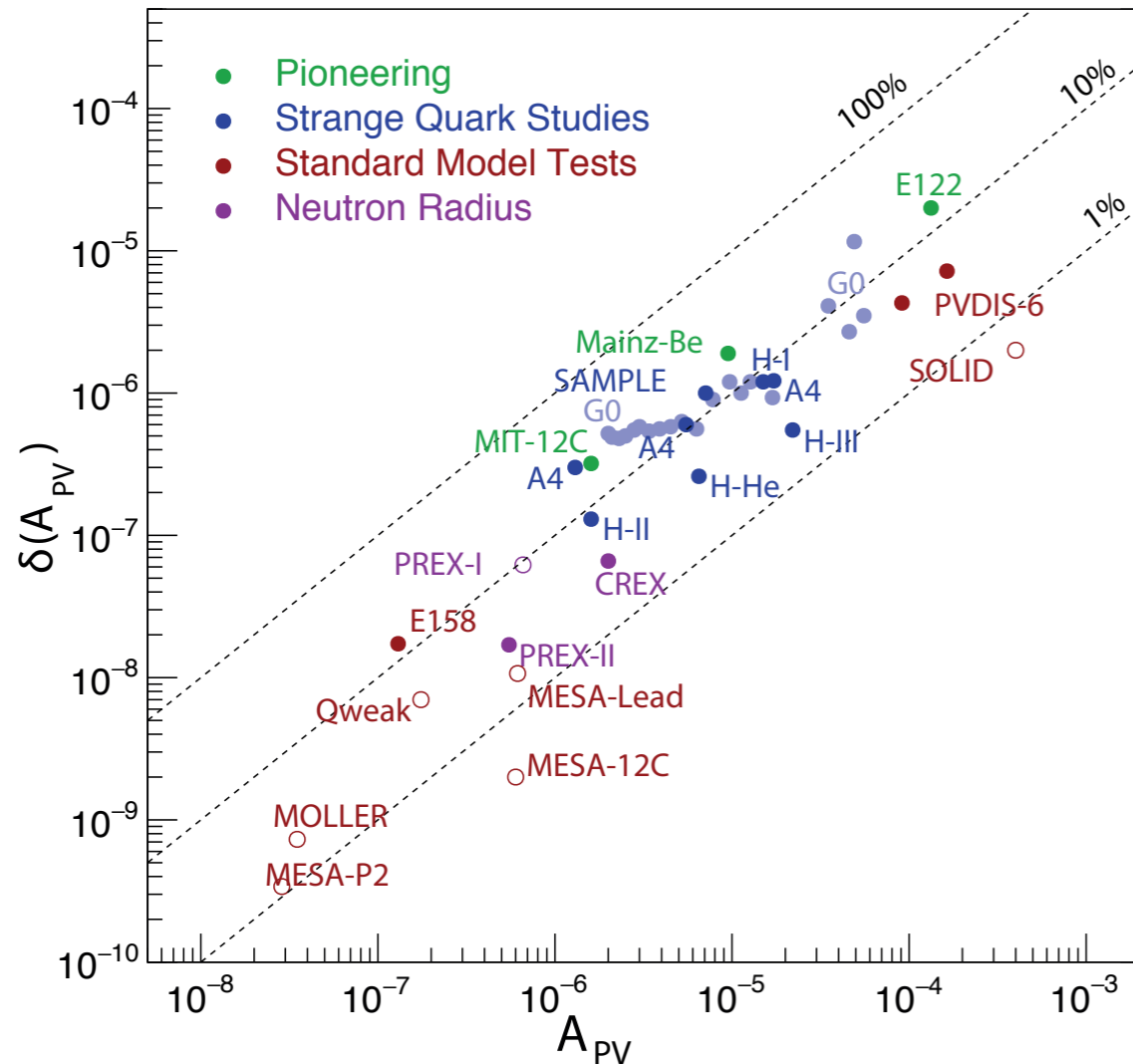
P2 collaboration, 1802.04759 (EPJA)

Dev, Ramsey-Musolf, Zhang, 1806.08499 (PRD)

**YD**, Freitas, Patel, Ramsey-Musolf, 1912.08220 (PRL)

Flat direction lifted by low-energy experiments: **electron sector example**

Bhabha alone is not enough to close the fit,  $A_{PV}$  from PVES is the key



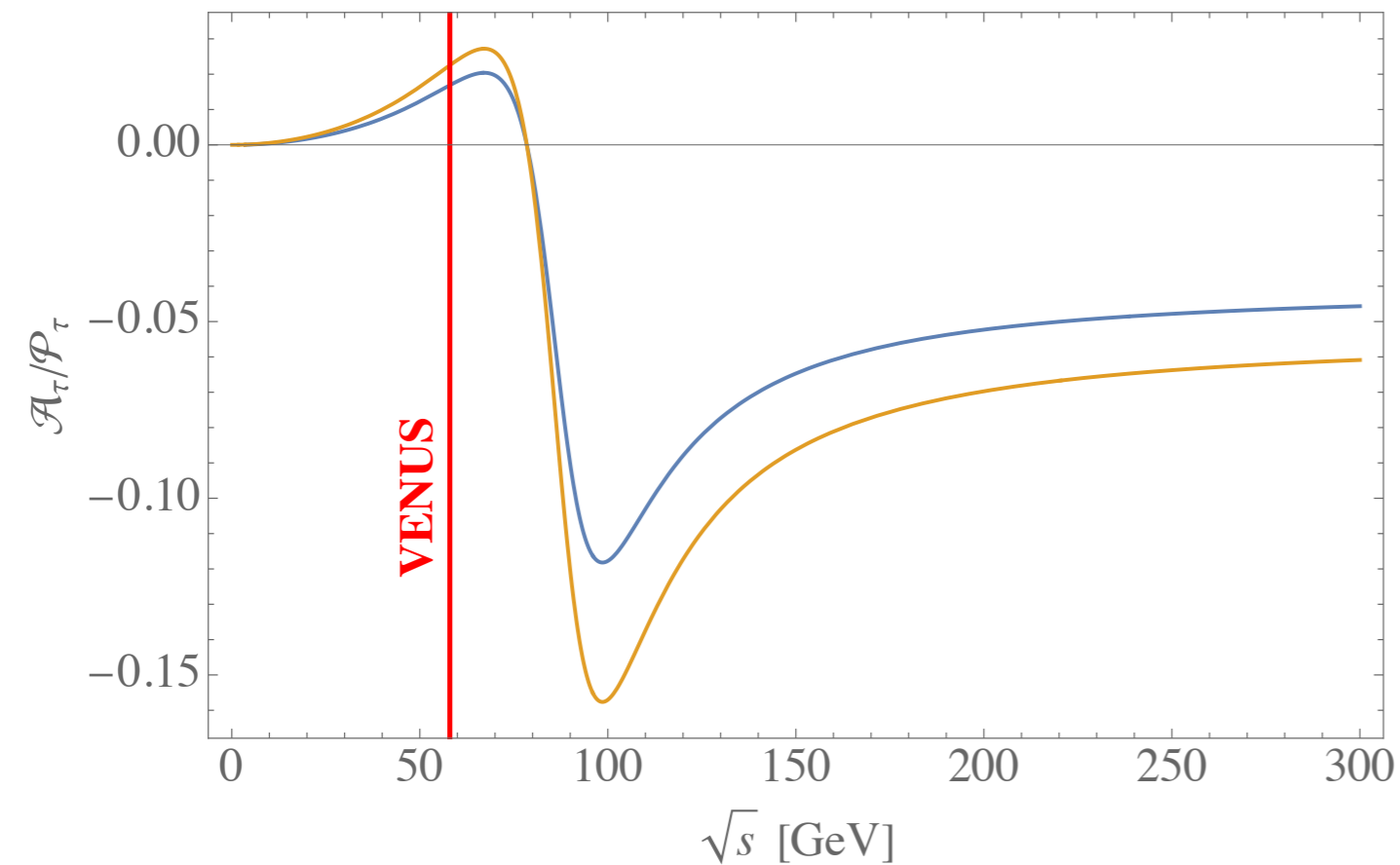
P2 collaboration, 1802.04759 (EPJA)

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**YD**, Freitas, Patel, Ramsey-Musolf, 1912.08220 (PRL)

Flat direction lifted by low-energy experiments: **tau sector example**

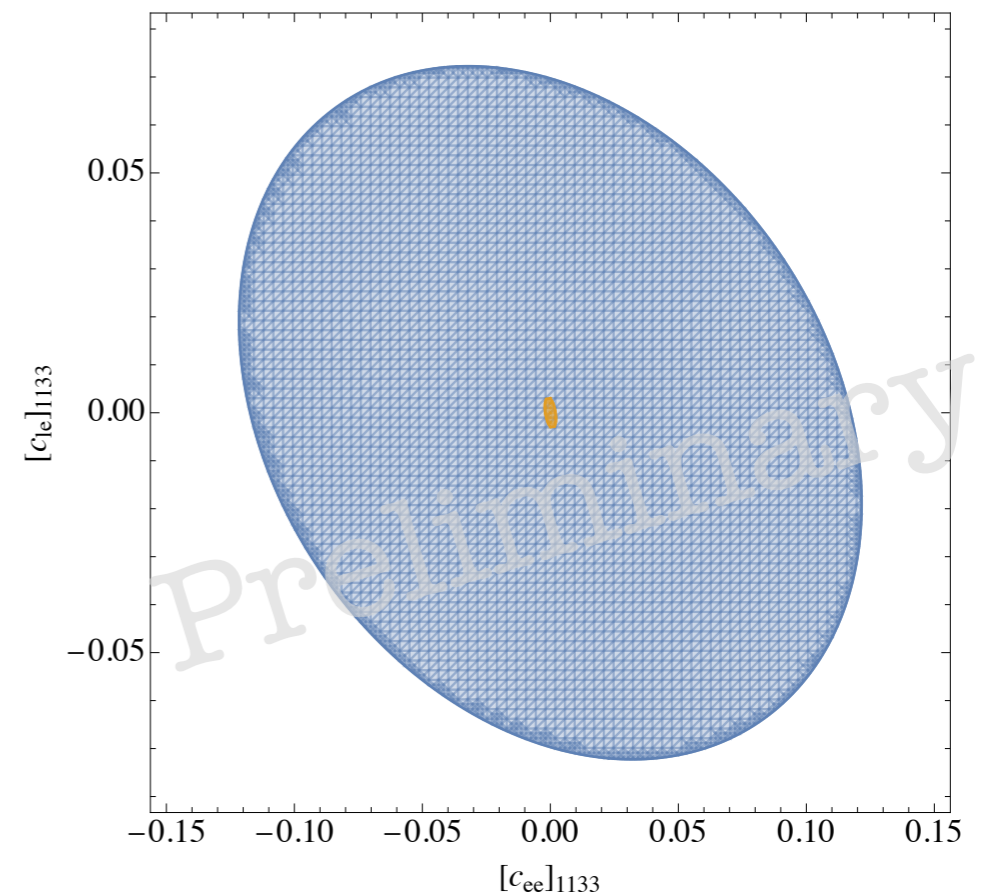
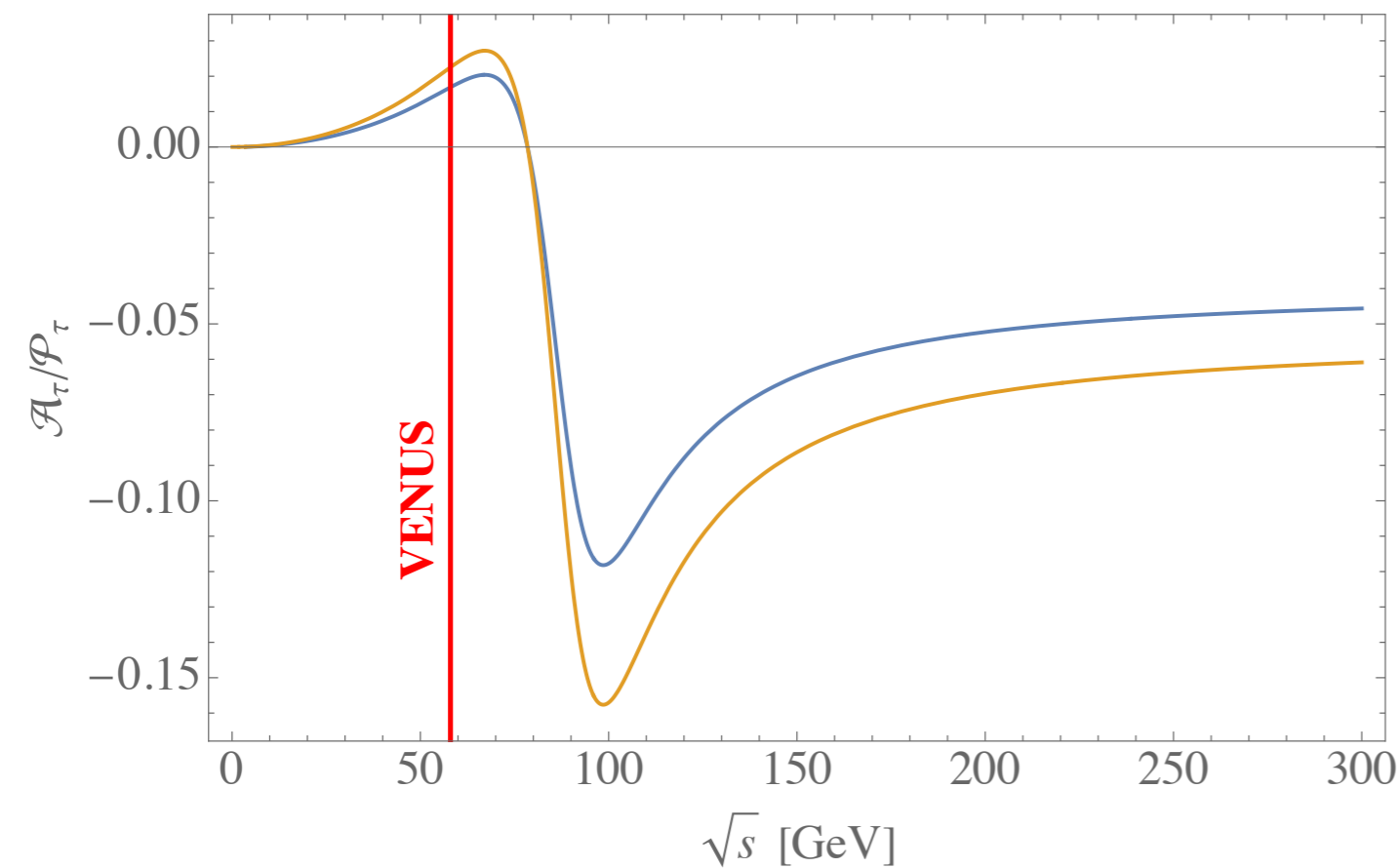
$\tau$  polarization measurement at VENUS is limited by statistics ( $\mathcal{L} = 271 \text{ pb}^{-1}$ ). CEPC at 240GeV will have better sensitivity with much more statistics (let alone STCF).



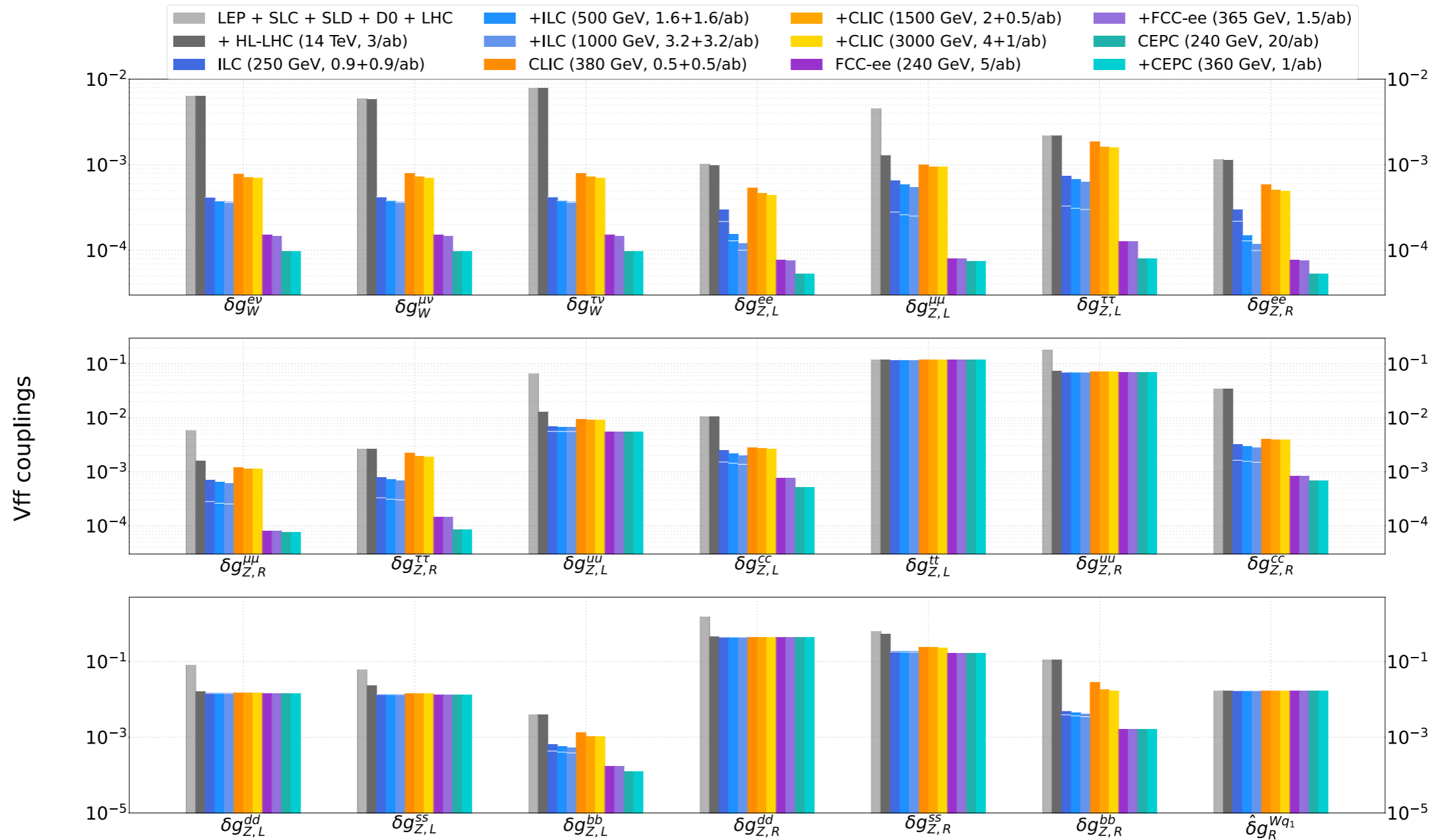


Flat direction lifted by low-energy experiments: **tau sector example**

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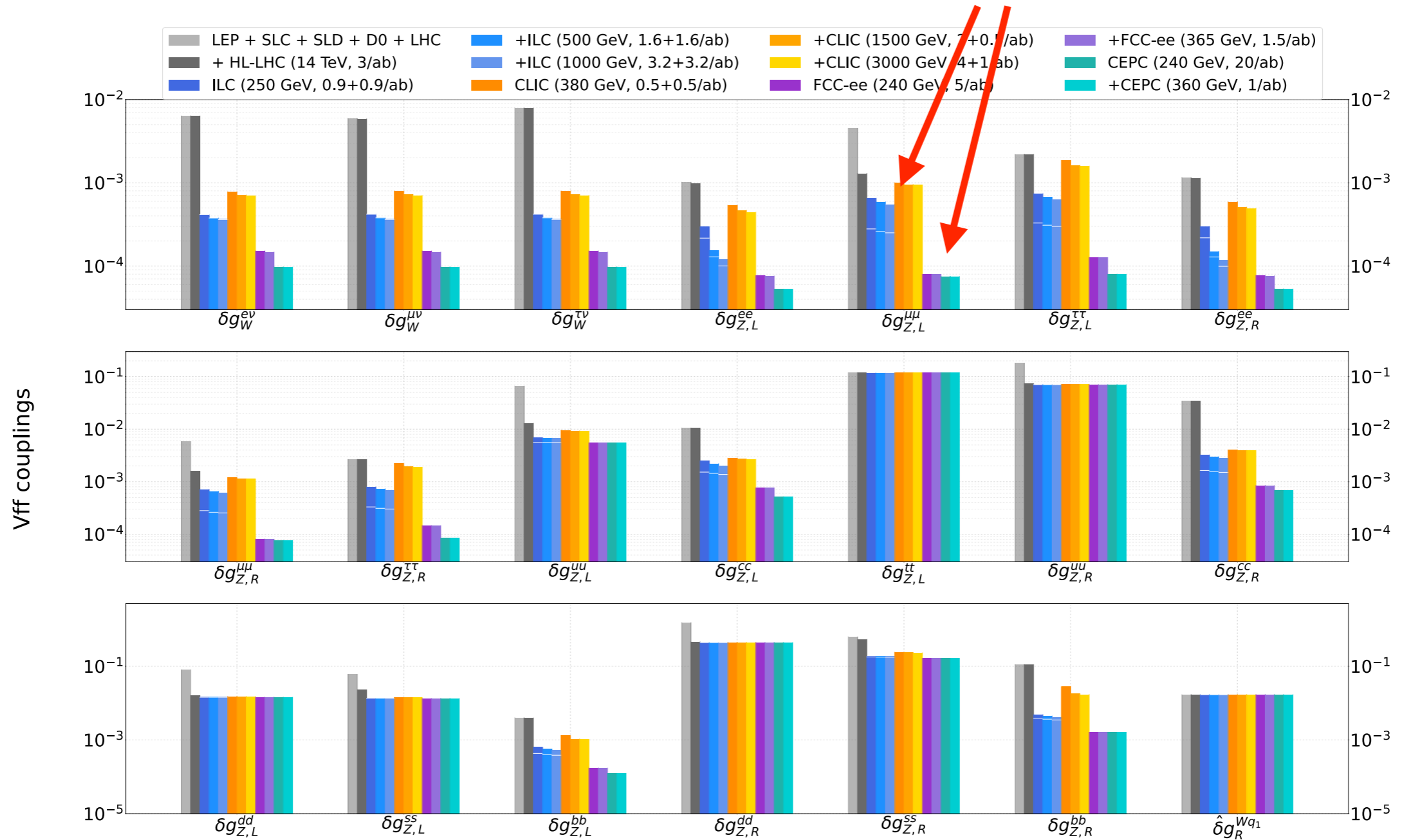
## Global fit results: Vff couplings



de Blas, [YD](#), Grojean, Gu, Miralles, Peskin, Tian, Vos, Vryonidou, 2206.08326

## Global fit results: Vff couplings

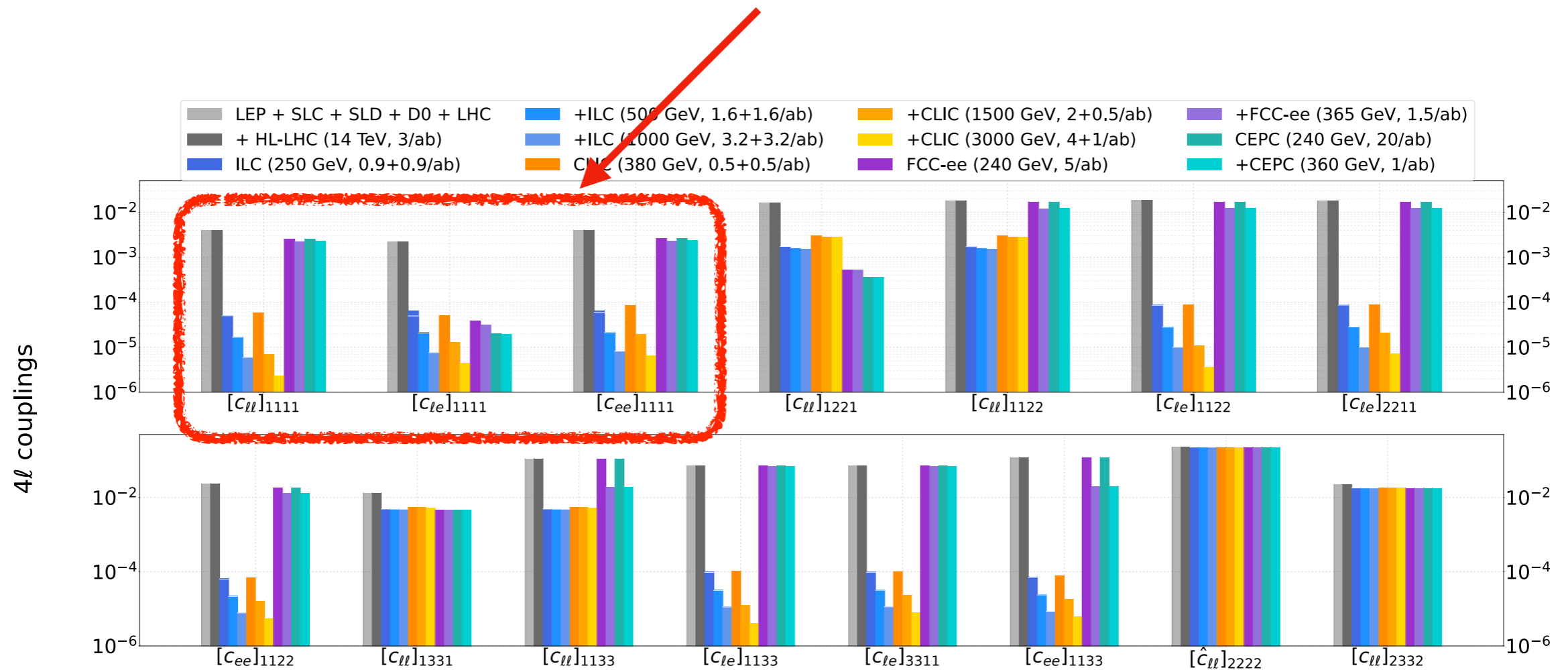
Luminosity wins (through radiative return)



de Blas, [YD](#), Grojean, Gu, Miralles, Peskin, Tian, Vos, Vryonidou, 2206.08326

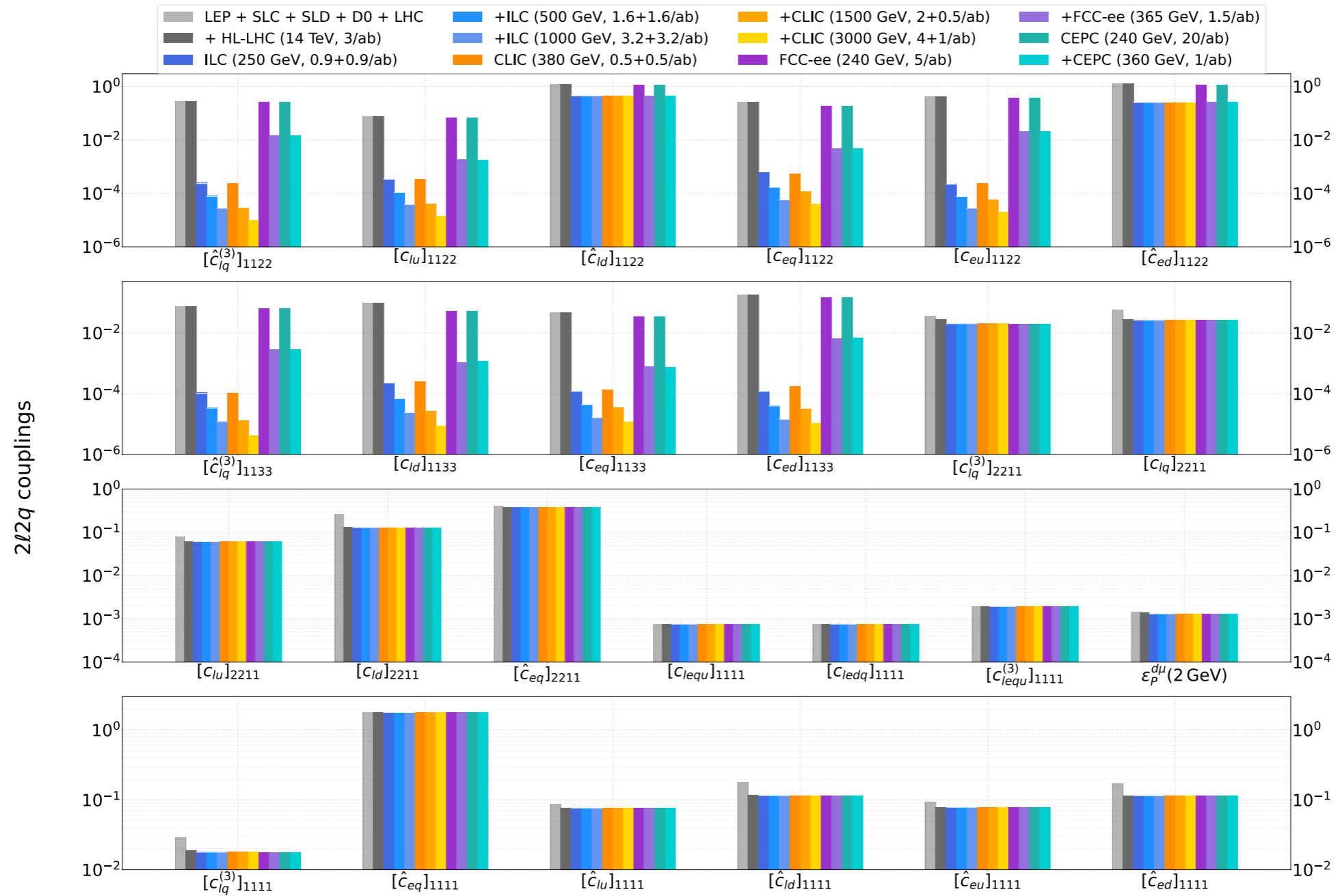
Global fit results:  $4\ell$  couplings

Beam polarization is the key in beating the (HL-)LHC and also circular colliders.



de Blas, **YD**, Grojean, Gu, Miralles, Peskin, Tian, Vos, Vryonidou, 2206.08326

## Global fit results: $2\ell 2q$ couplings



de Blas, **YD**, Grojean, Gu, Miralles, Peskin, Tian, Vos, Vryonidou, 2206.08326

Purely bosonic CPV operators: 6 in total, in Warsaw basis

$$\mathcal{O}_{\tilde{G}} = f^{ABC} \tilde{G}_{\mu}^{A\nu} G_{\nu}^{B\rho} G_{\rho}^{C\mu}$$

$$\mathcal{O}_{\varphi\tilde{G}} = \varphi^{\dagger} \varphi \tilde{G}_{\mu\nu}^A G^{A\mu\nu}$$

$$\mathcal{O}_{\varphi\tilde{W}} = \varphi^{\dagger} \varphi \tilde{W}_{\mu\nu}^I W^{I\mu\nu}$$

$$\mathcal{O}_{\varphi\tilde{B}} = \varphi^{\dagger} \varphi \tilde{B}_{\mu\nu} B^{\mu\nu}$$

$$\mathcal{O}_{\varphi\tilde{W}B} = \varphi^{\dagger} \tau^I \varphi \tilde{W}_{\mu\nu}^I B^{\mu\nu}$$

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Not included (gluon free) — strong constraints from neutron/chromo-EDMs

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Cirigliano et al, Phys.Rev.D 94 (2016) 3, 034031

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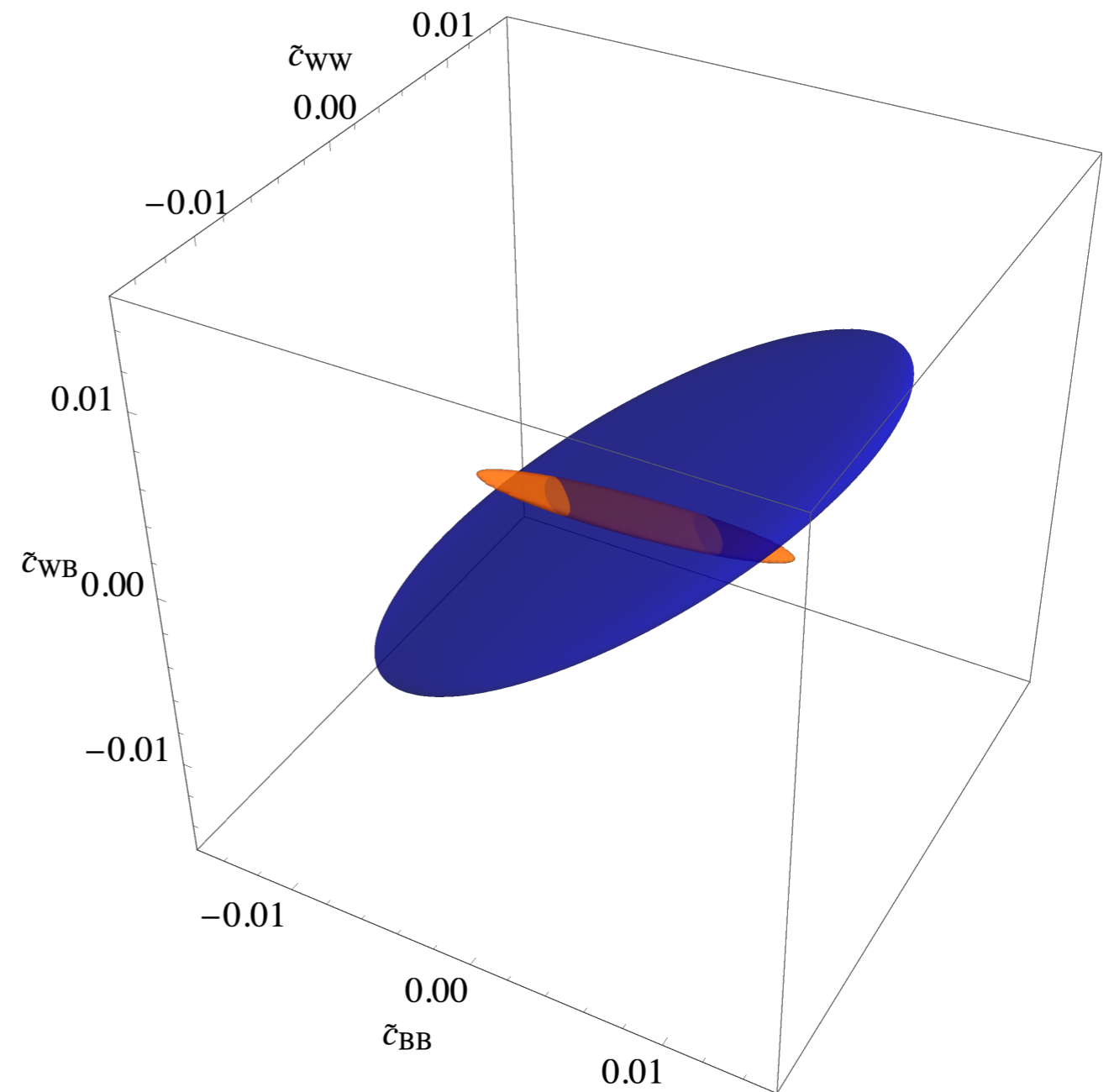
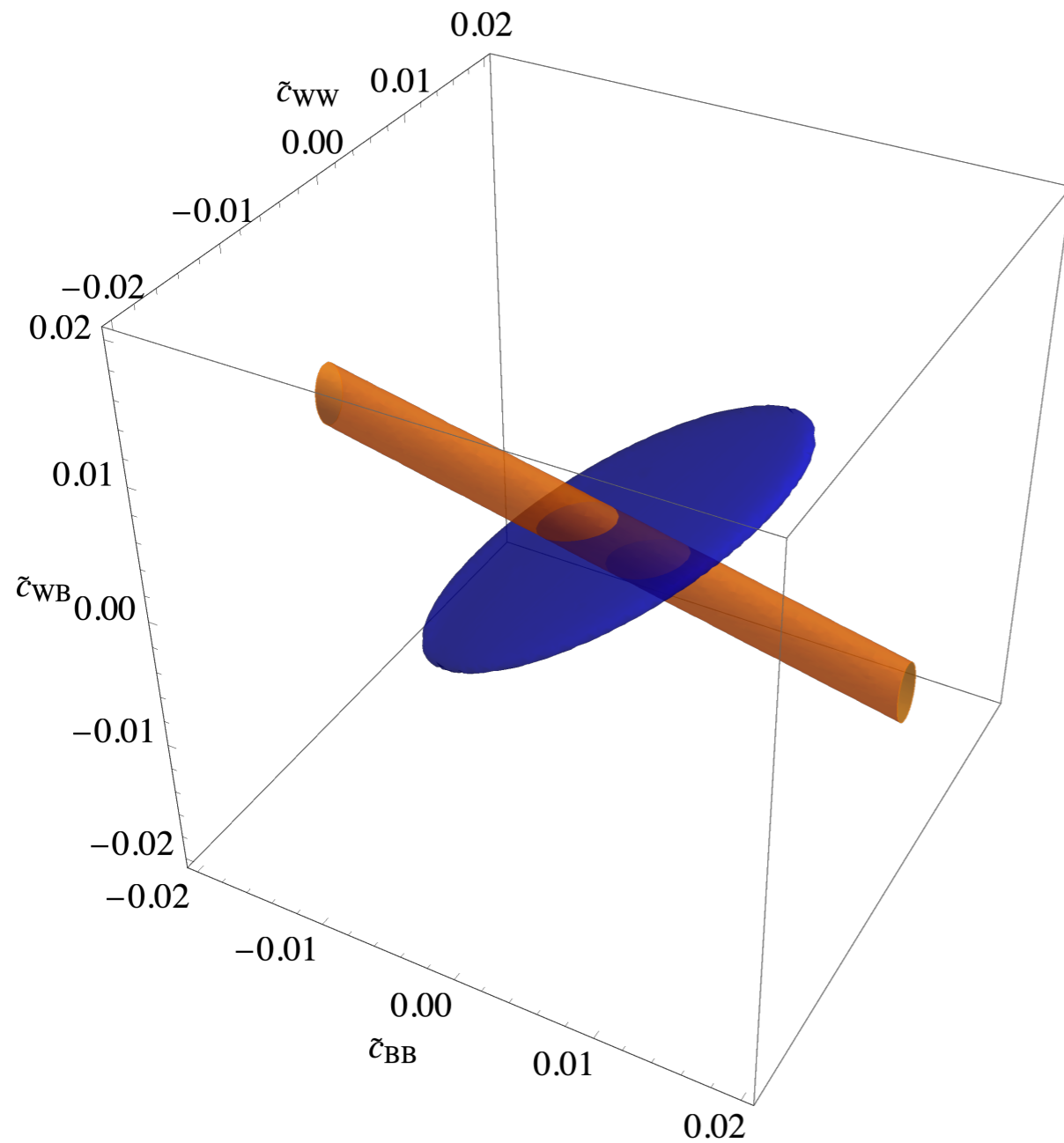
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$$\mathcal{O}_{\tilde{W}} = \epsilon^{IJK} \tilde{W}_{\mu}^{I\nu} W_{\nu}^{J\rho} W_{\rho}^{K\mu}$$

1. Determination of **two anomalous triple gauge couplings (aTGC)** from  $e^+e^- \rightarrow W^+W^-$
2. Another **two anomalous Higgs couplings (aHC)** from  $e^+e^- \rightarrow Zh$  (dominant production channel of ILC at low energies) using angular asymmetries.

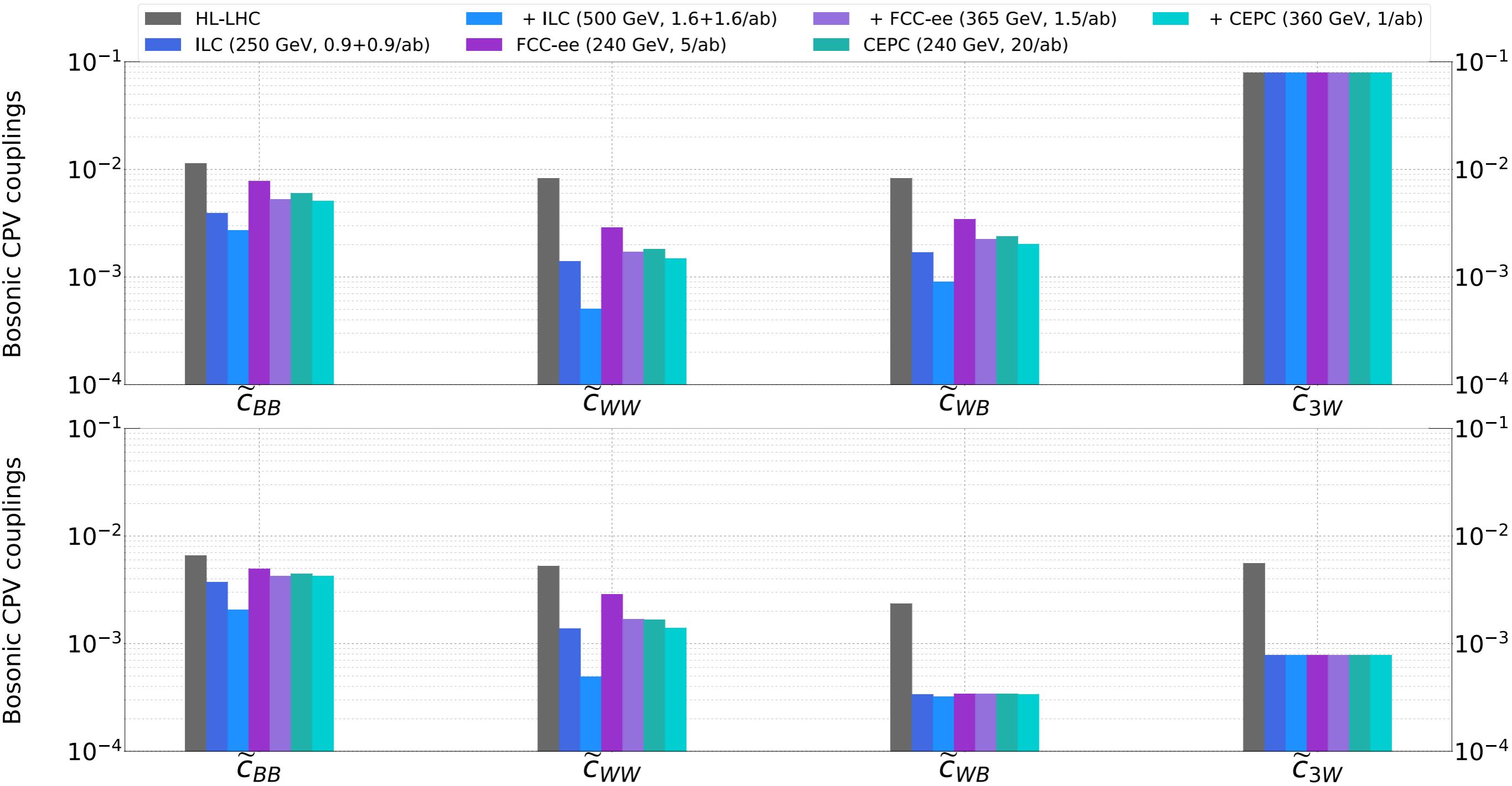


## Complementarity of hadron and lepton colliders in probing CP violation



de Blas, [YD](#), Grojean, Gu, Miralles, Peskin, Tian, Vos, Vryonidou, 2206.08326

de Blas, **YD**, Grojean, Gu, Miralles, Peskin, Tian, Vos, Vryonidou, 2206.08326



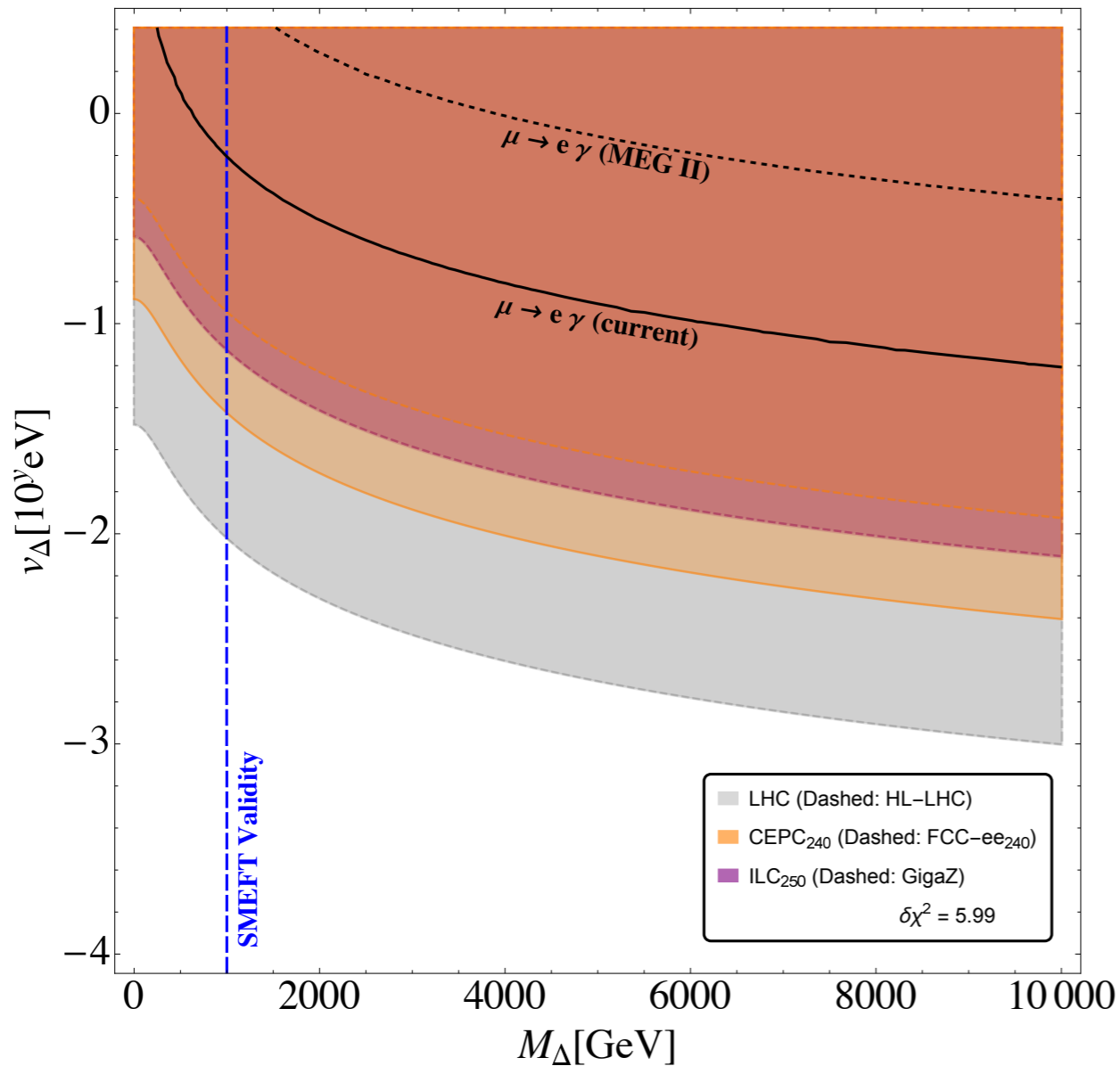


# Benchmark: Type-II seesaw model

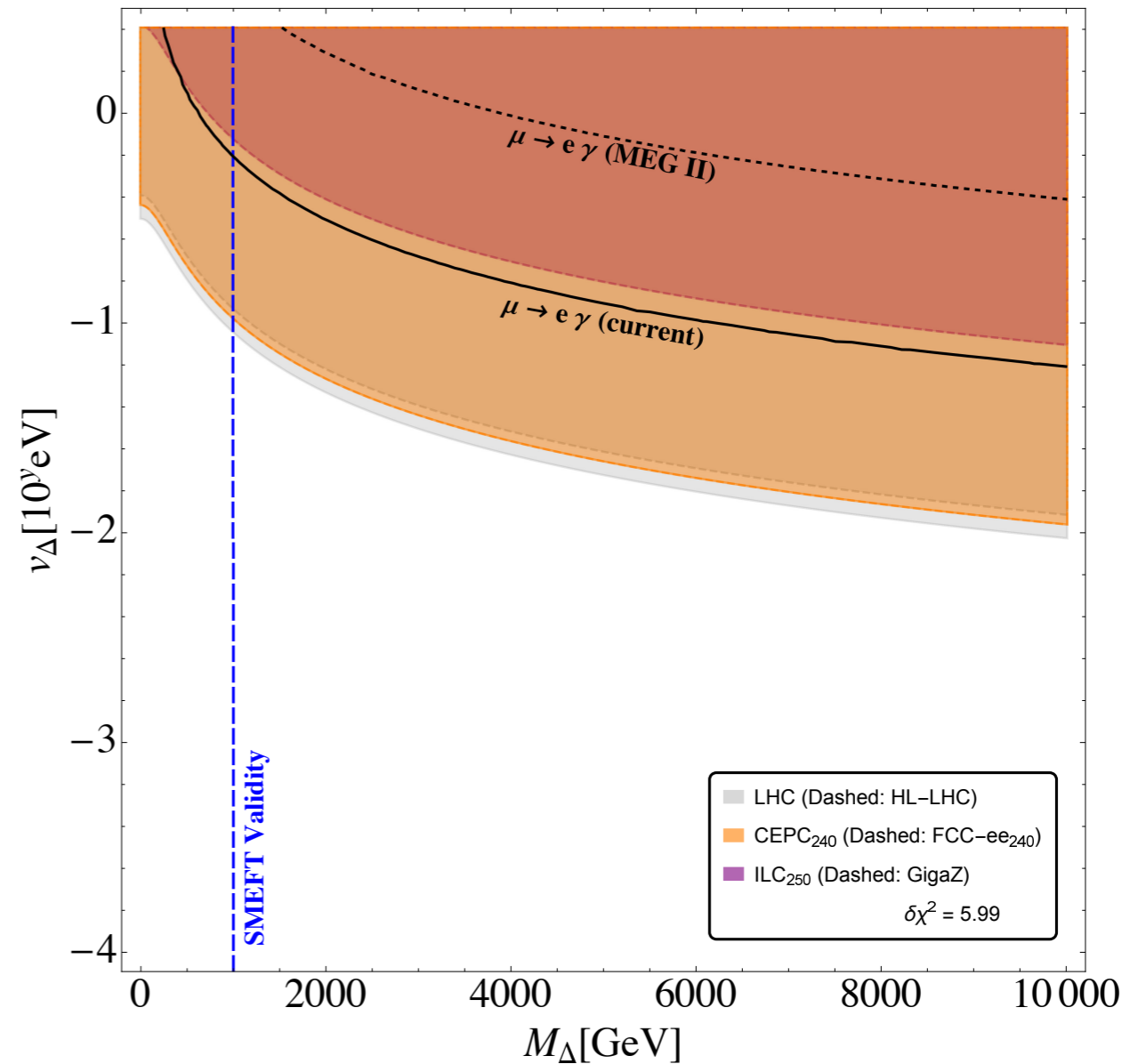
$$V(\Phi, \Delta) \supset \lambda_4(\Phi^\dagger \Phi) \text{Tr}(\Delta^\dagger \Delta) + \lambda_5 \Phi^\dagger \Delta \Delta^\dagger \Phi$$

$$\mathcal{L}_Y = (y_\nu)_{\alpha\beta} \bar{L}_\alpha^c i\tau_2 \Delta L_\beta h . c .$$

95% CL limits on the type-II seesaw model (NO)



95% CL limits on the type-II seesaw model (NO)



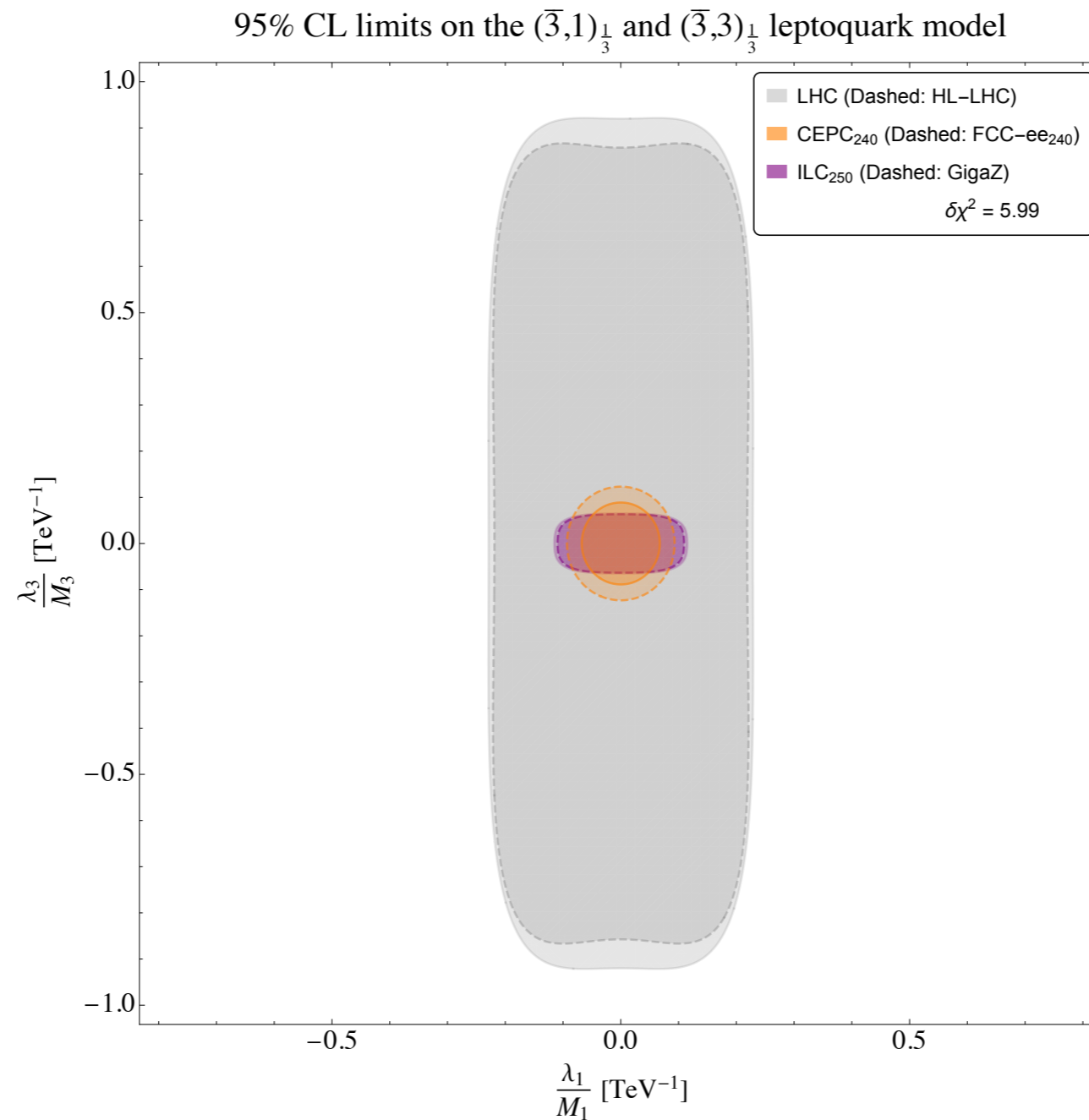
$m_{\text{light}} = 0$  vs  $m_{\text{light}} = 0.1 \text{ eV}$

**YD**, 2303.16400

**YD**, Li, Yu, 2201.04646 (JHEP)

Li, Zhang, Zhou, 2201.05082 (JHEP)

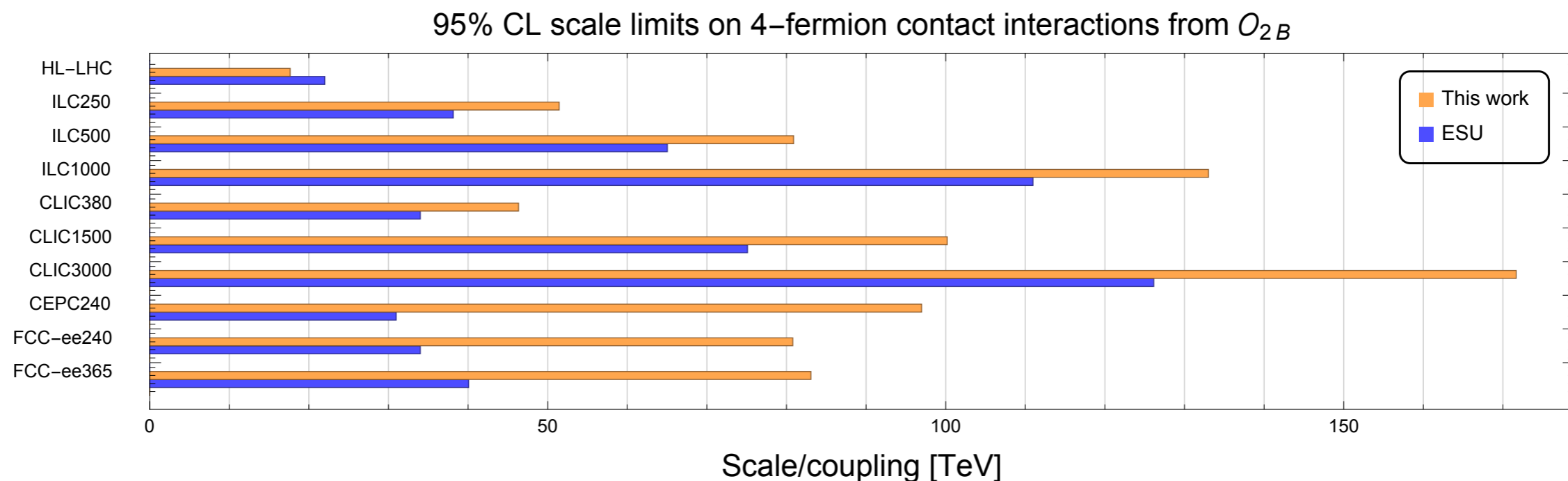
$$\mathcal{L}_{\text{LQ}} \supset (\lambda_{i\alpha}^{1L} \bar{q}_i^c \epsilon \ell_\alpha + \lambda_{i\alpha}^{1R} \bar{u}_i^c e_\alpha) S_1 + \lambda_{i\alpha}^{3L} \bar{q}_i^c \epsilon \sigma^I \ell_\alpha S_3^I + \text{h.c.}$$



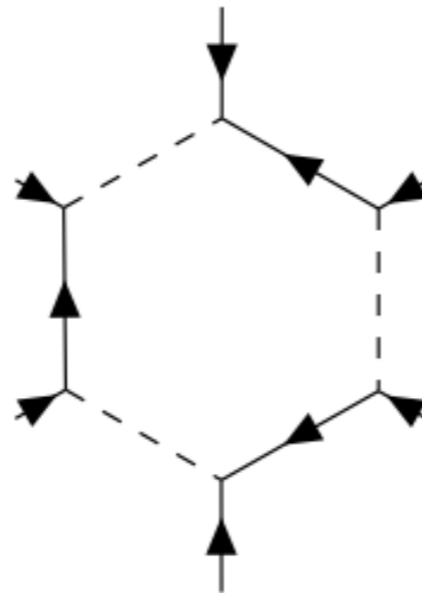
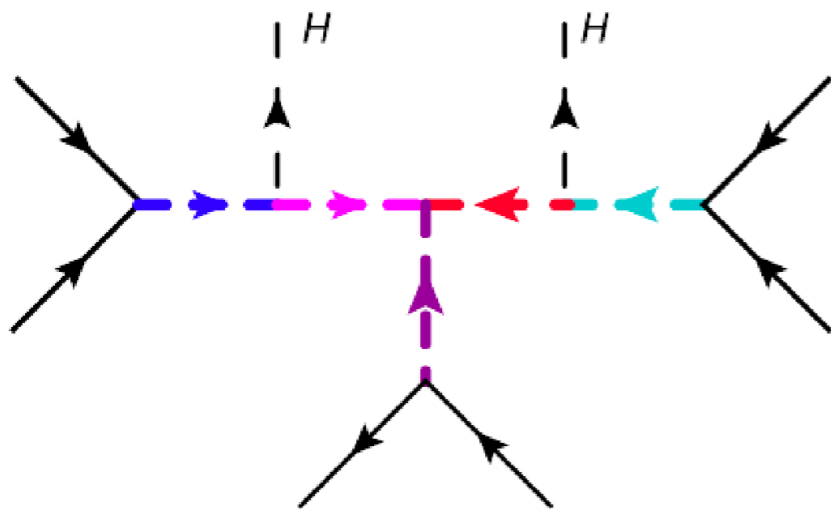
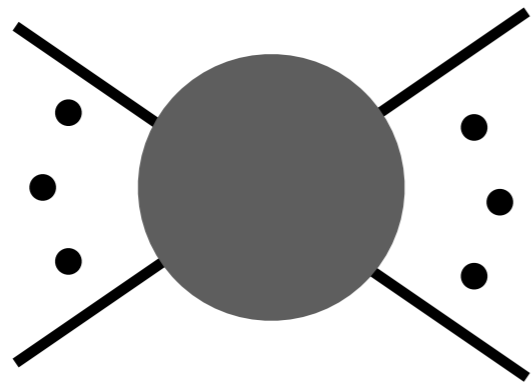
de Blas, **YD**, Grojean, Gu, Miralles, Peskin, Tian, Vos, Vryonidou, 2206.08326

Extend the SM by  $U(1)_Z$  but without introducing kinetic mixing and off-diagonal gauge couplings

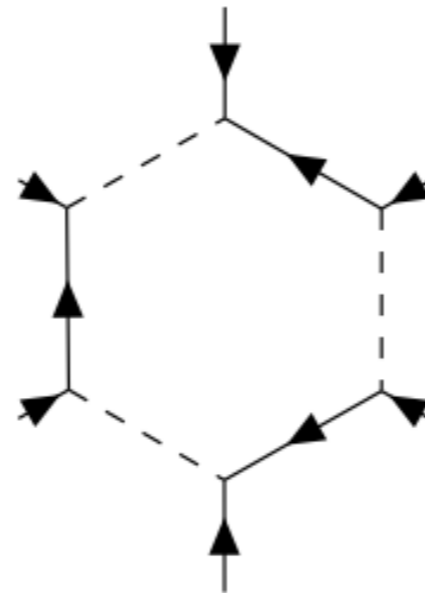
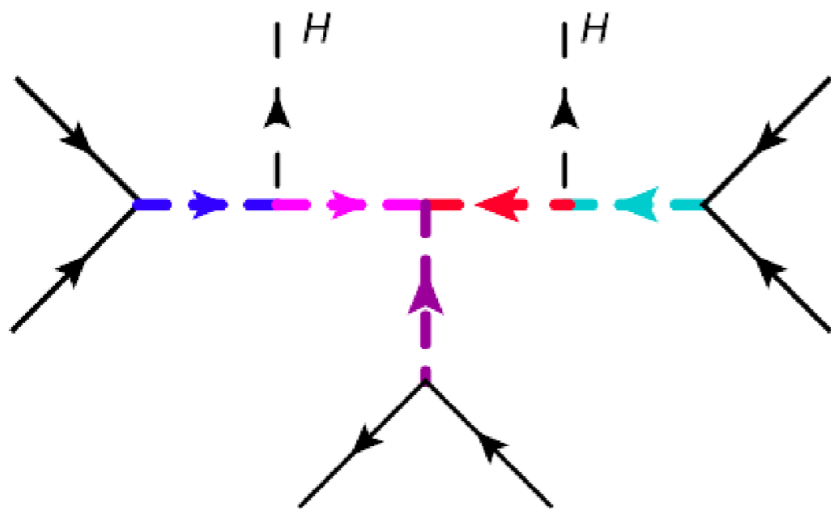
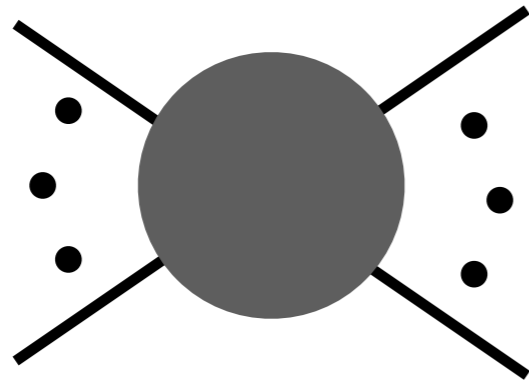
$$\frac{c_{2B}}{\Lambda^2} = \frac{g_{Z'}^2}{g_1^4 M^2}$$



de Blas, **YD**, Grojean, Gu, Miralles, Peskin, Tian, Vos, Vryonidou, 2206.08326



Find the UV models for any operator and any topology ([UVBuilder](#)).

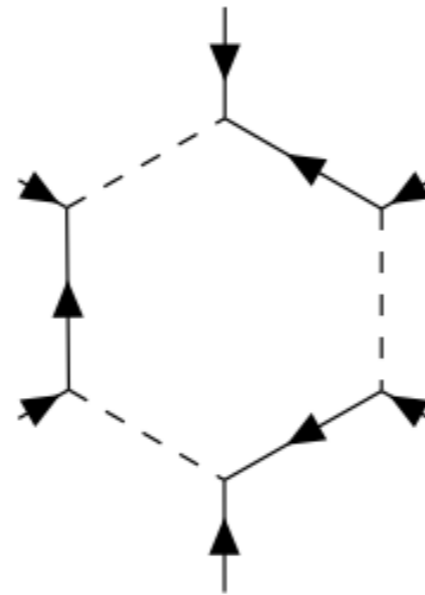
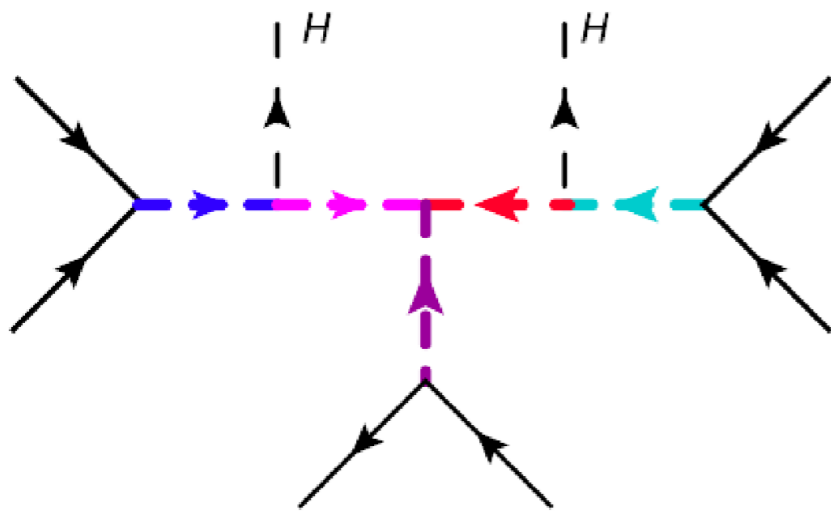
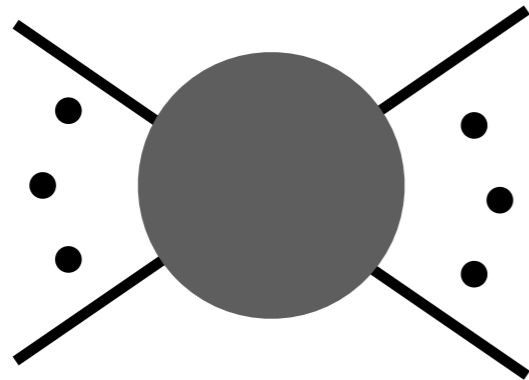


Find the UV models for any operator and any topology ([UVBuilder](#)).

Internal fields				
I1	I2	I3	I4	I5
HyperCharges				
$-\frac{2}{3}$	$-\frac{5}{3}$	$\frac{1}{3}$	$-\frac{2}{3}$	$\frac{4}{3}$
Gauge information {SU3, SU2}				
{3, 1}	{3, 2}	{3, 2}	{3, 1}	{3, 1}
{3, 1}	{3, 2}	{3, 2}	{3, 1}	{6, 1}
{3, 1}	{3, 2}	{3, 2}	{6, 1}	{3, 1}
{3, 1}	{3, 2}	{3, 2}	{6, 1}	{6, 1}
{3, 1}	{3, 2}	{6, 2}	{3, 1}	{3, 1}
{3, 1}	{3, 2}	{6, 2}	{6, 1}	{3, 1}
{3, 1}	{6, 2}	{3, 2}	{3, 1}	{3, 1}
{3, 1}	{6, 2}	{3, 2}	{6, 1}	{3, 1}
{3, 1}	{6, 2}	{6, 2}	{3, 1}	{6, 1}
{3, 1}	{6, 2}	{6, 2}	{6, 1}	{6, 1}
{6, 1}	{3, 2}	{3, 2}	{3, 1}	{3, 1}
{6, 1}	{3, 2}	{3, 2}	{3, 1}	{6, 1}
{6, 1}	{3, 2}	{3, 2}	{6, 1}	{3, 1}
{6, 1}	{3, 2}	{3, 2}	{6, 1}	{6, 1}
{6, 1}	{3, 2}	{6, 2}	{3, 1}	{3, 1}
{6, 1}	{3, 2}	{6, 2}	{6, 1}	{3, 1}
{6, 1}	{6, 2}	{3, 2}	{3, 1}	{3, 1}
{6, 1}	{6, 2}	{3, 2}	{6, 1}	{3, 1}
{6, 1}	{6, 2}	{6, 2}	{3, 1}	{6, 1}
{6, 1}	{6, 2}	{6, 2}	{6, 1}	{6, 1}

YD, Ma, Liao, 2308.XXXXXX





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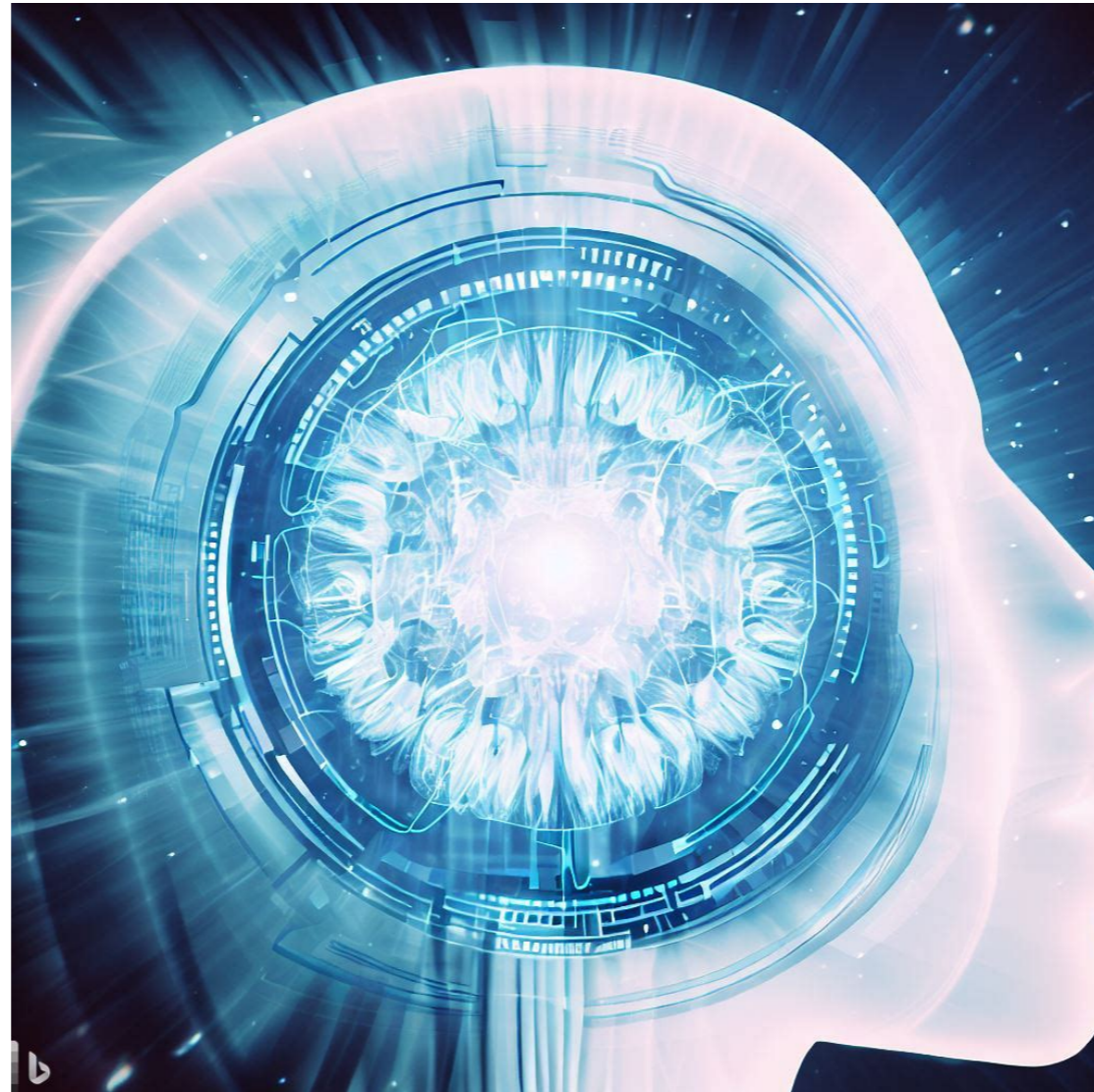
Internal fields				
I1	I2	I3	I4	I5
HyperCharges				
$-\frac{2}{3}$	$-\frac{5}{3}$	$\frac{1}{3}$	$-\frac{2}{3}$	$\frac{4}{3}$
Gauge information {SU3, SU2}				
{3, 1}	{3, 2}	{3, 2}	{3, 1}	{3, 1}
{3, 1}	{3, 2}	{3, 2}	{3, 1}	{6, 1}
{3, 1}	{3, 2}	{3, 2}	{6, 1}	{3, 1}
{3, 1}	{3, 2}	{3, 2}	{6, 1}	{6, 1}
{3, 1}	{3, 2}	{6, 2}	{3, 1}	{3, 1}
{3, 1}	{3, 2}	{6, 2}	{6, 1}	{3, 1}
{3, 1}	{6, 2}	{3, 2}	{3, 1}	{3, 1}
{3, 1}	{6, 2}	{3, 2}	{6, 1}	{3, 1}
{3, 1}	{6, 2}	{6, 2}	{3, 1}	{6, 1}
{3, 1}	{6, 2}	{6, 2}	{6, 1}	{6, 1}
{6, 1}	{3, 2}	{3, 2}	{3, 1}	{3, 1}
{6, 1}	{3, 2}	{3, 2}	{3, 1}	{6, 1}
{6, 1}	{3, 2}	{3, 2}	{6, 1}	{3, 1}
{6, 1}	{3, 2}	{3, 2}	{6, 1}	{6, 1}
{6, 1}	{3, 2}	{6, 2}	{3, 1}	{3, 1}
{6, 1}	{3, 2}	{6, 2}	{6, 1}	{3, 1}
{6, 1}	{6, 2}	{3, 2}	{3, 1}	{3, 1}
{6, 1}	{6, 2}	{3, 2}	{6, 1}	{3, 1}
{6, 1}	{6, 2}	{6, 2}	{3, 1}	{6, 1}
{6, 1}	{6, 2}	{6, 2}	{6, 1}	{6, 1}

Q: Which benchmark model for CEPC?

YD, Ma, Liao, 2308.XXXXXX

# Summary

- ✦ I discussed the global fit of 4f and CPV SMEFT operators at future colliders:
  - ✦ Beam polarization is the key to surpass circular colliders in studying 4f ints.
  - ✦ Luminosity largely wins otherwise for circular colliders;
  - ✦ aTGCs will be the key to improve the sensitivity of the bosonic CPV operators.
  - ✦ Several benchmark models are discussed (type-II seesaw, leptoquark models, etc)



**Backup**