



Single Transverse Spin Asymmetry as a New Probe of SMEFT Dipole Operators

Xin-Kai Wen (文新锴 Bhung Sing-Kai)

Peking University

In collaboration with Bin Yan, Zhite Yu and C.-P. Yuan

Basing on arXiv: 2307.05236 and works in progress

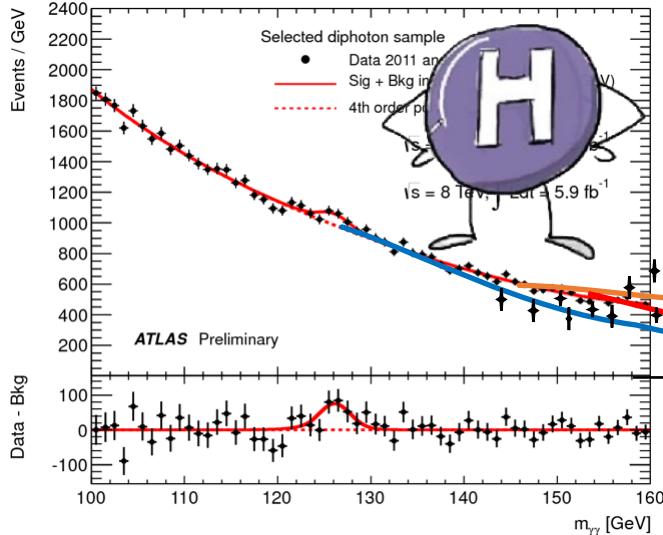
Thanks a lot to the organizers of Fudan University
Shanghai, China

2023/08/18



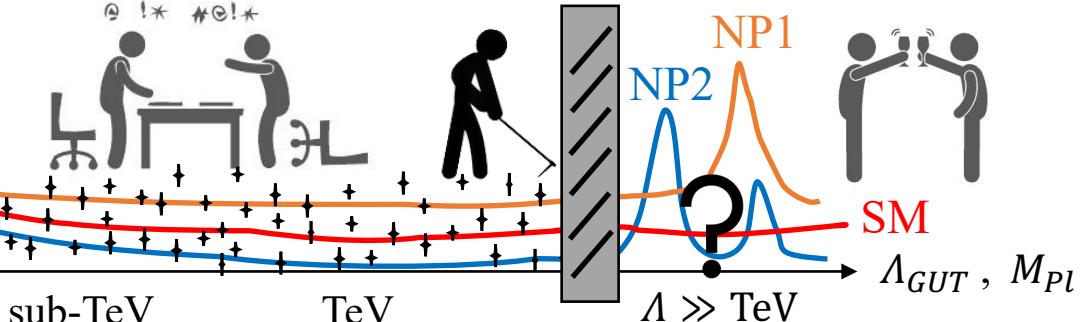
New Physics and SMEFT

None new fundamental resonance since 2012 but anomalies bursting



“5W1H”: Where, What, Why, When, Who, How NP

NP might hide within the current scale



ATLAS Heavy Particle Searches* - 95% CL Upper Exclusion Limits

Status: March 2023

ATLAS Preliminary

$\sqrt{s} = 13 \text{ TeV}$

Reference

Model	ℓ, γ	Jets †	E_T^{miss}	$f_L dt [fb^{-1}]$	Limit					
ADD Gau, 1/q	0 e, \mu, \gamma	1-4 j	Yes	139	$\Lambda = 2$ 8.6 TeV 9.4 TeV 9.55 TeV					
ADD non-resonant $\gamma\gamma$	-	2 j	-	36.7	M_ϕ					
ADD OBH	-	-	-	139	M_ϕ					
ADD multi-jet	-	3 j	-	139	M_ϕ					
RS1 $G_{\phi\phi} \rightarrow \gamma\gamma$	-	-	-	139	$\Lambda_{\phi\phi}$ mass					
Bulk RS $G_{\phi\phi} \rightarrow WW/ZZ$	-	-	-	36.1	$\Lambda_{\phi\phi}$ mass					
Bulk RS $G_{\phi\phi} \rightarrow tt$	1 e, \mu	$\geq 1 t \geq 1 J/2$	Yes	139	$\Lambda \gg \text{TeV}$					
2UED / RPP	1 e, \mu	$\geq 2 b \geq 3 j$	Yes	36.1	$\Lambda \gg \text{TeV}$					
	2 e, \mu	-	-	36.1	$\Lambda \gg \text{TeV}$					
SSM $Z' \rightarrow \ell\ell$	2 e, \mu	-	-	36.1	$\Lambda \gg \text{TeV}$					
Lepto-phobic $Z' \rightarrow bb$	-	2 b	-	36.1	$\Lambda \gg \text{TeV}$					
Lepto-phobic $Z' \rightarrow tt$	0 e, \mu	$\geq 2 b \geq 2 J$	Yes	139	$\Lambda \gg \text{TeV}$					
SSM $W' \rightarrow \ell\nu$	1 e, \mu	-	-	139	$\Lambda \gg \text{TeV}$					
SSM $W' \rightarrow \nu\nu$	1 e, \mu	-	-	139	$\Lambda \gg \text{TeV}$					
HVT $Z' \rightarrow WZ$ model B	0 e, \mu	$\geq 1 b \geq 1 J$	Yes	139	$\Lambda \gg \text{TeV}$					
HVT $Z' \rightarrow WW$ model B	0 e, \mu	$\geq 1 b \geq 1 J$	Yes	139	$\Lambda \gg \text{TeV}$					
URSM $W_2 \rightarrow \mu/N_R$	2 \mu	1 J	-	80	$\Lambda \gg \text{TeV}$					
<hr/>										
SMEFT	\rightarrow Global Fitting									
Many excellent works										
<hr/>										
<i>See talks of Jiayin Gu, Yong Du, Peter Athron and so on</i>										
<hr/>										
EWPo										
<hr/>										
Table 2: Dimension-six operators other than the four-fermion ones.										
<hr/>										
Table 3: Four-fermion operators.										
<hr/>										
B. Grzadkowski, et al. <i>JHEP</i> 10 (2010).										
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but some constrained poorly because of non-interference effect										
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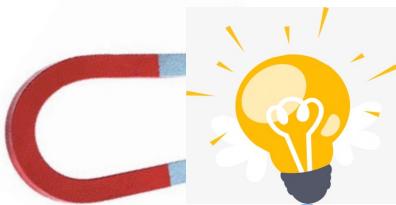
*Only a selection of the available mass limits on new states or phenomena is shown.

[†]Small-radius (large-radius) jets are denoted by the letter (J).

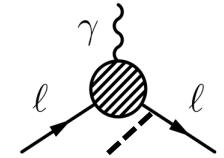
Multi-Tev

No.2

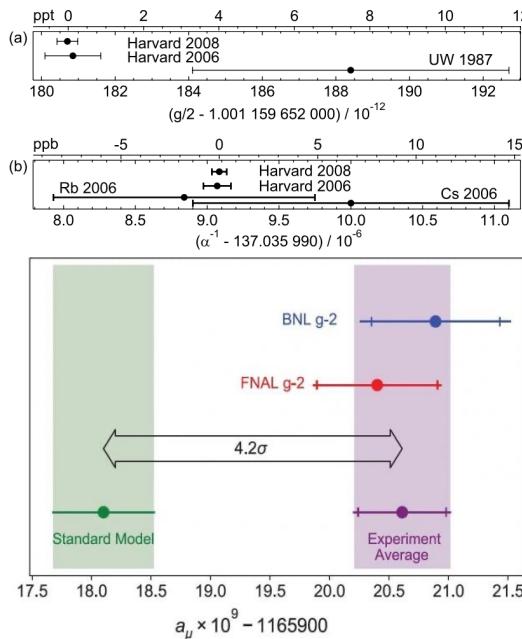
Dipole Operator



- ✓ Connect Mass and E/M Dipole Moment
- ✓ Loop-induced by the UV BSM
- ✓ Cause Chirality Flip



especially for the “ 4.2σ ”
Direct & Dominant



D. Hanneke et al., *Phys.Rev.Lett.* 100,(2008)
G.W. Bennett et al. *Phys.Rept.* 887 (2020)
B. Abi et al. *Phys.Rev.Lett.* 126 (2021)

New results from Muon g-2

Liang Li

C108, 物理樓

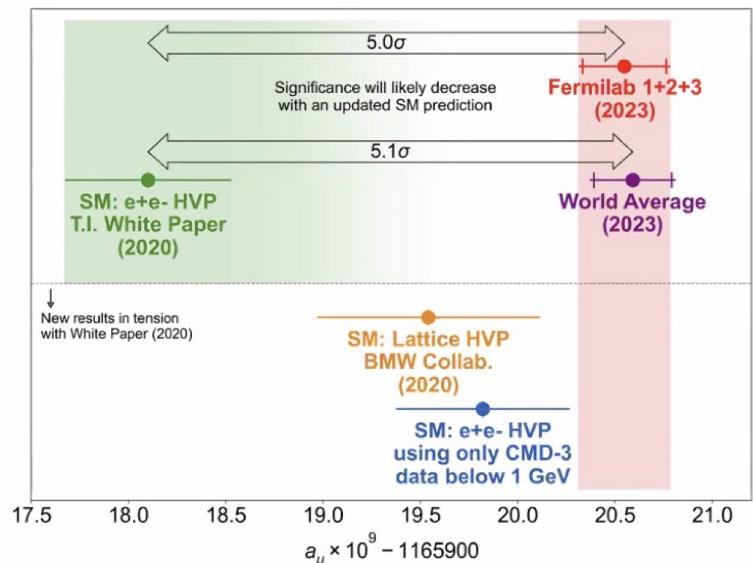
09:40 - 10:05

Experiment vs Theory Comparison

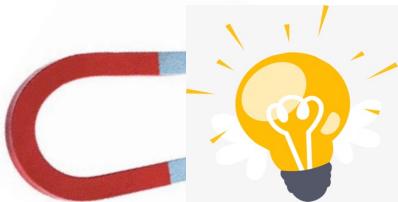
- Theory prediction is less clear now, but we can still compare

See talks of Liang Li and
Fermilab papers and so on

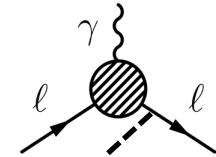
 Fermilab



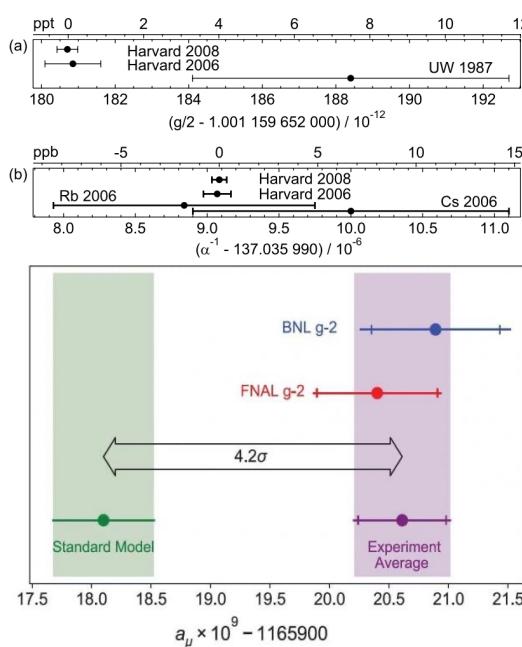
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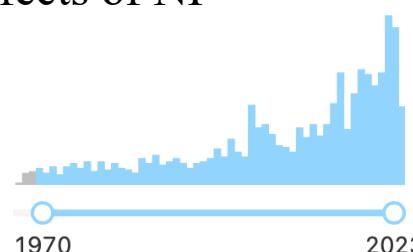
D. Hanneke et al., *Phys.Rev.Lett.* 100,(2008)
G.W. Bennett et al. *Phys.Rept.* 887 (2020)
B. Abi et al. *Phys.Rev.Lett.* 126 (2021)

Loop-induced by the BSM

- Encode information about heavy particle interactions
- Indirect probes of quantum effects of NP

See talks of Fei Wang, Peter Athron and so on

Implications of muon and electron g-2 anomalies for NMSSM		Fei Wang
C108, 物理樓		16:55 - 17:10
Muon g-2: SUSY vs non-SUSY explanations	Peter Athron	
C108, 物理樓		17:25 - 17:40



Z' and dark photon model NMSSM (SUSY) Scalar extension.....

Minimal models for muon g-2: 1 field extensions

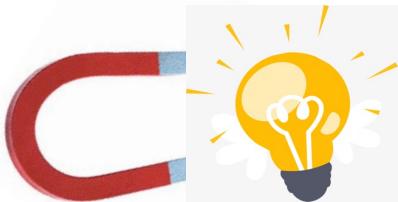
Model	Spin	$SU(3)_C \times SU(2)_L \times U(1)_Y$	Result for $\Delta a_\mu^{\text{BNL}}, \Delta a_\mu^{2021}$	EXCLUDED
1	0	(1, 1, 1)	Excluded: $\Delta a_\mu < 0$	
2	0	(1, 1, 2)	Excluded: $\Delta a_\mu < 0$	
3	0	(1, 2, -1/2)	Updated in Sec. 3.2	
4	0	(1, 3, -1)	Excluded: $\Delta a_\mu < 0$	
5	0	(3, 1, 1/3)	Updated Sec. 3.3	
6	0	(3, 1, 4/3)	Excluded: LHC searches	
7	0	(3, 3, 1/3)	Excluded: LHC searches	
8	0	(3, 2, 7/6)	Updated Sec. 3.3	
9	0	(3, 2, 1/6)	Excluded: LHC searches	
10	1/2	(1, 1, 0)	Excluded: $\Delta a_\mu < 0$	
11	1/2	(1, 1, -1)	Excluded: Δa_μ too small	
12	1/2	(1, 2, -1/2)	Excluded: LEP lepton mixing	
13	1/2	(1, 2, -3/2)	Excluded: $\Delta a_\mu < 0$	
14	1/2	(1, 3, 0)	Excluded: $\Delta a_\mu < 0$	
15	1/2	(1, 3, -1)	Excluded: $\Delta a_\mu < 0$	
16	1	(1, 1, 0)	Special cases viable	
17	1	(1, 2, -3/2)	UV completion problems	
18	1	(1, 3, 0)	Excluded: LHC searches	
19	1	(3, 1, -2/3)	UV completion problems	
20	1	(3, 1, -5/3)	Excluded: LHC searches	
21	1	(3, 2, -5/6)	UV completion problems	
22	1	(3, 2, 1/6)	Excluded: $\Delta a_\mu < 0$	
23	1	(3, 3, -2/3)	Excluded: proton decay	

From:
JHEP 09 (2021) 080.
[PA. C. Balázs, D.H.J. Jacob,
W. Kotarski, D. Stöckinger,
H. Stöckinger-Kim]

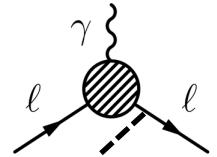
Builds on:
- JHEP 05 (2014) 145
[A. Freitas, J. Lykken, S. Kell
& S. Westhoff].
- Phys. Rev. D 89 (2014) 095024
[F. S. Queiroz & W. Shepherd].
- JHEP 10 (2016) 002
[C. Biggio, M. Bordone,
L. Di Luzio & G. Ridolfi].
- JHEP 10 (2016) 002
[C. Biggio & M. Bordone].
- JHEP 09 (2017) 112
[K. Kowalska & E. M. Sestilo]

F. Wang et al. *Nucl.Phys.B* 970 (2021)
Peter Athron et al., *JHEP* 09 (2021) 080
.....

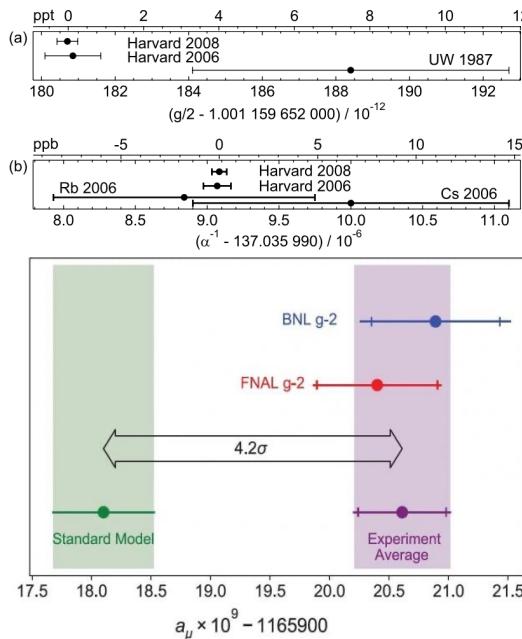
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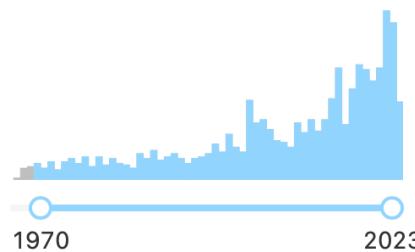


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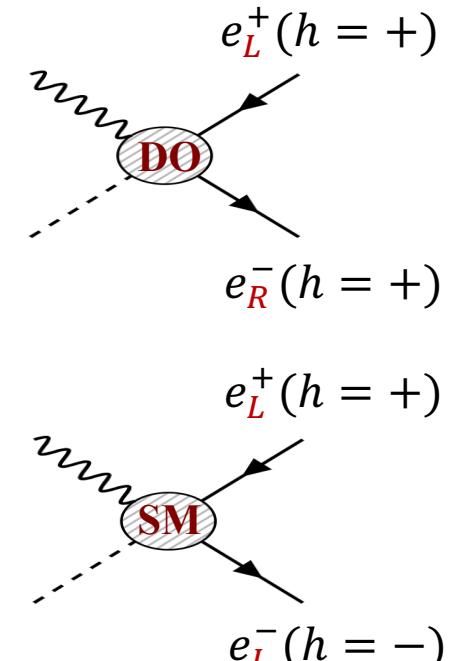
Loop-induced by the BSM

- Encode information about heavy particle interactions
- Indirect probes of quantum effects of NP



Z' and dark photon model
NMSSM (SUSY)
Scalar extension.....

Chirality flip
Disappear in massless SM

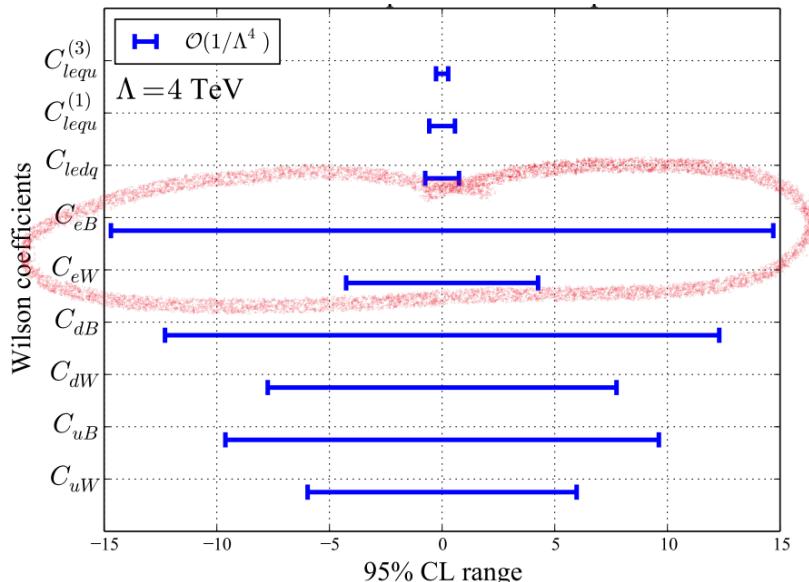


D. Hanneke et al., *Phys.Rev.Lett.* 100,(2008)
G.W. Bennett et al. *Phys.Rept.* 887 (2020)
B. Abi et al. *Phys.Rev.Lett.* 126 (2021)

F. Wang et al. *Universe* 9 (2023), 2305.04623
Peter Athron et al., *JHEP* 09 (2021) 080
J. Liu et al., *JHEP* 03 (2019), 1810.11028

Proposal and Data for Dipole Operator

In Global Analyses, EW dipole couplings constrained poorly



Single-Parameter-Analysis from
recent Drell-Yan Data at LHC
(R. Boughezal et al. *Phys.Rev.D* 104 (2021)...)

only small non-interfering effect with $\left| \frac{c_{\text{dipole}}}{\Lambda^2} \right|^2$

LHC Drell-Yan: $\mathcal{O}(10^{-2} \sim 10^{-1})$

(R. Boughezal et al. *Phys.Rev.D* 104 (2021)...) Even if HL-LHC, lifting at most five times better

LEP Z-boson partial width: $\mathcal{O}(10^{-2} \sim 10^{-1})$

(R. Escribano et al. *Nucl.Phys.B* 429 (1994), S. Schael et al. *Phys.Rept.* 427 (2006)...)

EFT running for interpretation $(g - 2)_e$: $\mathcal{O}(10^{-6} \sim 10^{-2})$

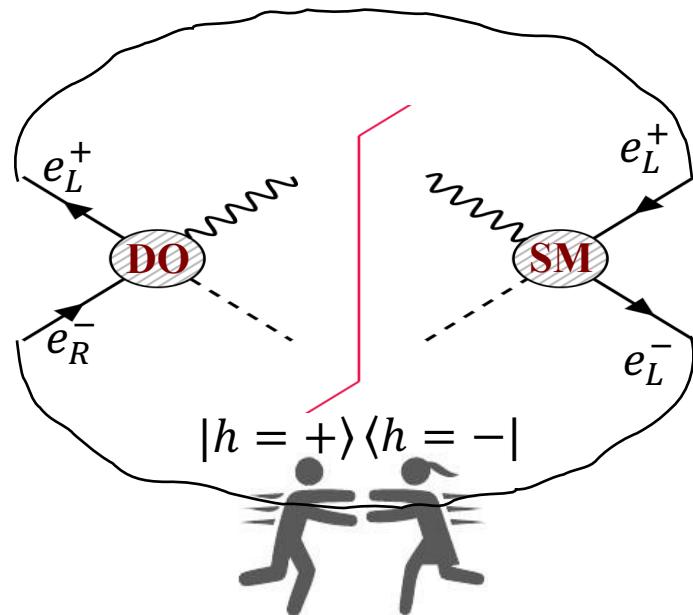
(A. V. Manohar et al. *JHEP* 07 (2021), T. Giani et al. 2302.06660, J. J. Ethier et al. *JHEP* 11 (2021)...)

How to Probe Dipole Operator

Our proposal:

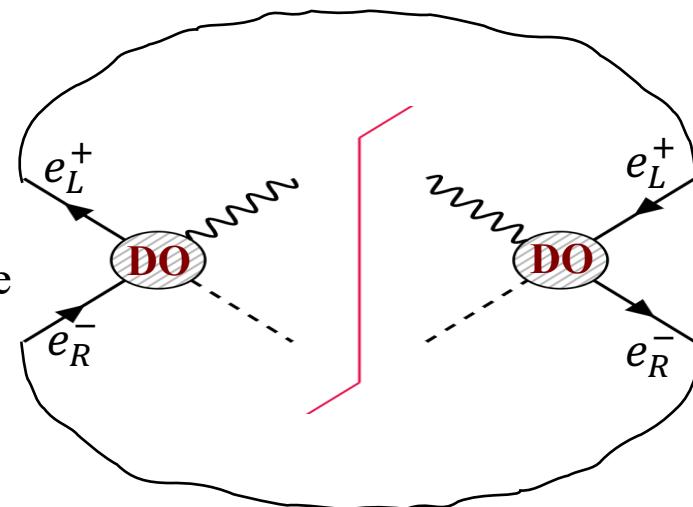
- ✓ C_{dipole}/Λ^2 , interfering with the massless SM
- ✓ Without depending on other NP operators
- ✓ Transverse polarization effect
- ✓ Non-trivial azimuthal angular distribution

Single Transverse Spin Azimuthal Asymmetries



Traditional method via cross section and width

- $|C_{dipole}|^2/\Lambda^4$, small effect from non-interference
- Bothered by other operators and assumptions



Transverse Spin Polarization

Transverse polarization effect → Interference of helicity amplitudes

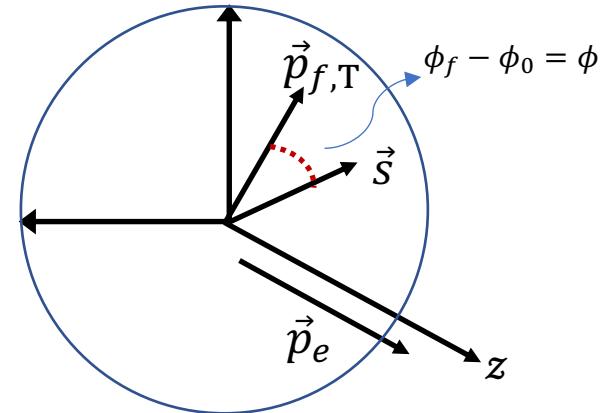
Breaking the rotational invariance & A nontrivial azimuthal behavior

Ken-ichi Hikasa, *Phys.Rev.D* 33 (1986) 3203, *PhysRevD*.38 (1988) 1439

$$|\mathcal{M}|^2 = \rho_{\alpha_1 \alpha'_1}(\mathbf{s}) \rho_{\alpha_2 \alpha'_2}(\bar{\mathbf{s}}) \mathcal{M}_{\alpha_1 \alpha_2}(\phi) \mathcal{M}_{\alpha'_1 \alpha'_2}^*(\phi)$$

$$\mathbf{s} = (b_1, b_2, \lambda) = (b_T \cos \phi_0, b_T \sin \phi_0, \lambda)$$

$$\rho = \frac{1}{2} (1 + \boldsymbol{\sigma} \cdot \mathbf{s}) = \frac{1}{2} \begin{pmatrix} 1 + \lambda & b_T e^{-i\phi_0} \\ b_T e^{i\phi_0} & 1 - \lambda \end{pmatrix}$$

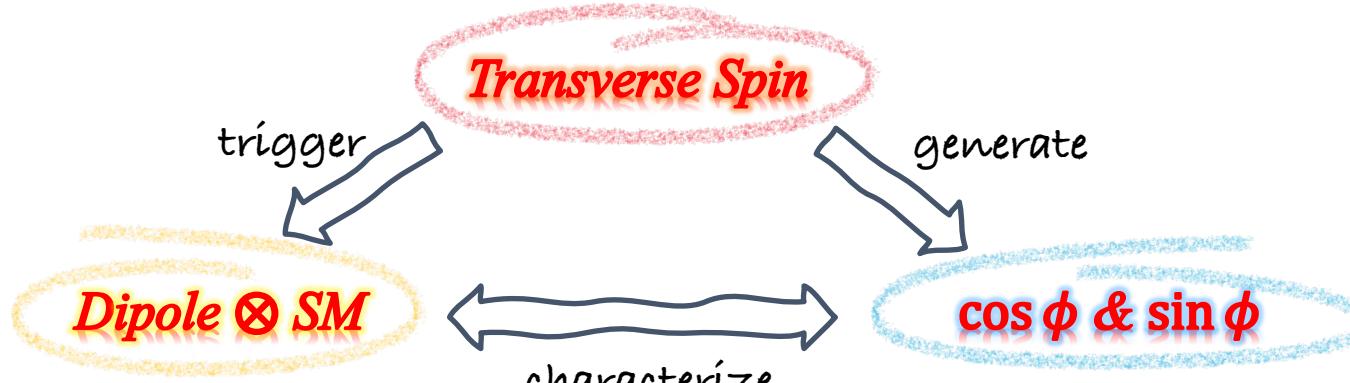


Only the azimuthal difference between initial \vec{s} and final \vec{p}_f physical meaningful

Only dipole operator contribute to $\mathcal{M}_{\pm\pm}$ while $\mathcal{M}_{\mp\mp}^{\text{SM}} = 0$, massless SM only $\mathcal{M}_{\pm\mp} \neq 0$

	<i>U</i>	<i>L</i>	<i>T</i>
<i>U</i>	$ \mathcal{M} _{UU}^2 \rightarrow 1$	$ \mathcal{M} _{UL}^2 \rightarrow 1$	$ \mathcal{M} _{UT}^2 \rightarrow \cos \phi, \sin \phi$
<i>L</i>	$ \mathcal{M} _{LU}^2 \rightarrow 1$	$ \mathcal{M} _{LL}^2 \rightarrow 1$	$ \mathcal{M} _{LT}^2 \rightarrow \cos \phi, \sin \phi$
<i>T</i>	$ \mathcal{M} _{TU}^2 \rightarrow \cos \phi, \sin \phi$	$ \mathcal{M} _{TL}^2 \rightarrow \cos \phi, \sin \phi$	$ \mathcal{M} _{TT}^2 \rightarrow 1, \cos 2\phi, \sin 2\phi$

A New Probe of Dipole Operators



$$\frac{2\pi d\sigma^i}{\sigma^i d\phi} = 1 + \frac{A_R^i(b_T, \bar{b}_T) \cos \phi}{\text{Re}[C_{dipole}]} + \frac{A_I^i(b_T, \bar{b}_T) \sin \phi}{\text{Im}[C_{dipole}]} + \frac{b_T \bar{b}_T B^i \cos 2\phi}{\text{SM \& other NP}} + \mathcal{O}(1/\Lambda^4)$$

$$\vec{s} \cdot \vec{p}_f \propto \cos \phi$$

CP-conserving

$$\vec{s} \times \vec{p}_f \propto \sin \phi$$

CP-violation

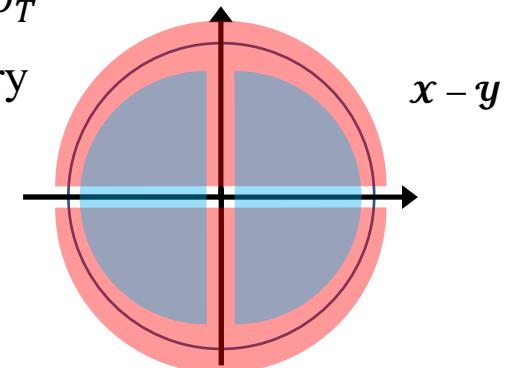
X.-K.W, BY, ZY, C.-P.Y, 2307.05236

Linearly dependent on the dipole couplings C_{dipole} and spin b_T

Using azimuthal asymmetry instead of polarization asymmetry

■ $A_{LR}^i = \frac{\sigma^i(\cos \phi > 0) - \sigma^i(\cos \phi < 0)}{\sigma^i(\cos \phi > 0) + \sigma^i(\cos \phi < 0)} = \frac{2}{\pi} A_R^i$

■ $A_{UD}^i = \frac{\sigma^i(\sin \phi > 0) - \sigma^i(\sin \phi < 0)}{\sigma^i(\sin \phi > 0) + \sigma^i(\sin \phi < 0)} = \frac{2}{\pi} A_I^i$,



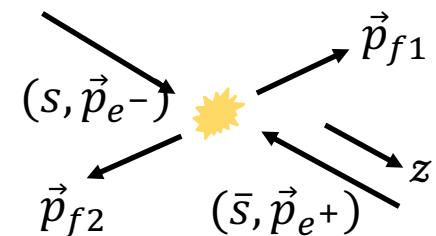
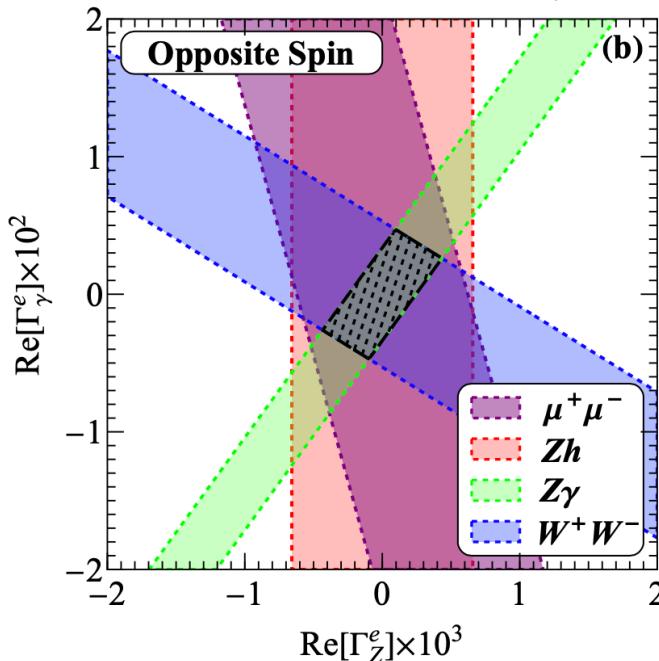
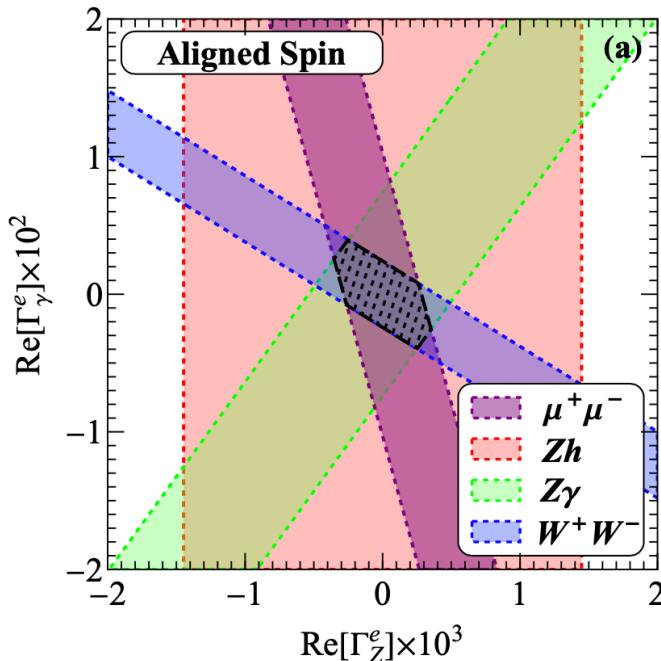
Pinning down Dipole Operators

$$\mathcal{L}_{\text{eff}} = -\frac{1}{\sqrt{2}} \bar{\ell}_L \sigma^{\mu\nu} (g_1 \Gamma_B^e B_{\mu\nu} + g_2 \Gamma_W^e \sigma^a W_{\mu\nu}^a) \frac{H}{v^2} e_R + \text{h.c.}$$

$$A_{LR}^i = \frac{\sigma^i(\cos \phi > 0) - \sigma^i(\cos \phi < 0)}{\sigma^i(\cos \phi > 0) + \sigma^i(\cos \phi < 0)} = \frac{2}{\pi} A_R^i$$

Aligned Spin
 $\phi_0 = \bar{\phi}_0 = 0$
 Opposite Spin
 $(\phi_0, \bar{\phi}_0) = (0, \pi)$

$\sqrt{s} = 250 \text{ GeV}, \mathcal{L} = 5 \text{ ab}^{-1}$



CP property

$$e^+ e^- : |e^-(s)e^+(\bar{s})\rangle \xrightarrow{\mathcal{CP}} |e^-(\bar{s})e^+(s)\rangle$$

$$A^i(s_T, \bar{s}_T; \Gamma_{Z,\gamma}^e) = \pm A^i(\bar{s}_T, s_T; \Gamma_{Z,\gamma}^{e*})$$

$$Zh, Z\gamma : |\phi, \theta\rangle \xrightarrow{\mathcal{CP}} |\phi + \pi, \pi - \theta\rangle$$

$$(A_R^{WW, \mu\mu}, A_I^{Zh, Z\gamma}) \propto s_T + \bar{s}_T$$

$$W^+W^-, \mu^+\mu^- : |\phi, \theta\rangle \xrightarrow{\mathcal{CP}} |\phi, \theta\rangle$$

$$(A_I^{WW, \mu\mu}, A_R^{Zh, Z\gamma}) \propto s_T - \bar{s}_T$$

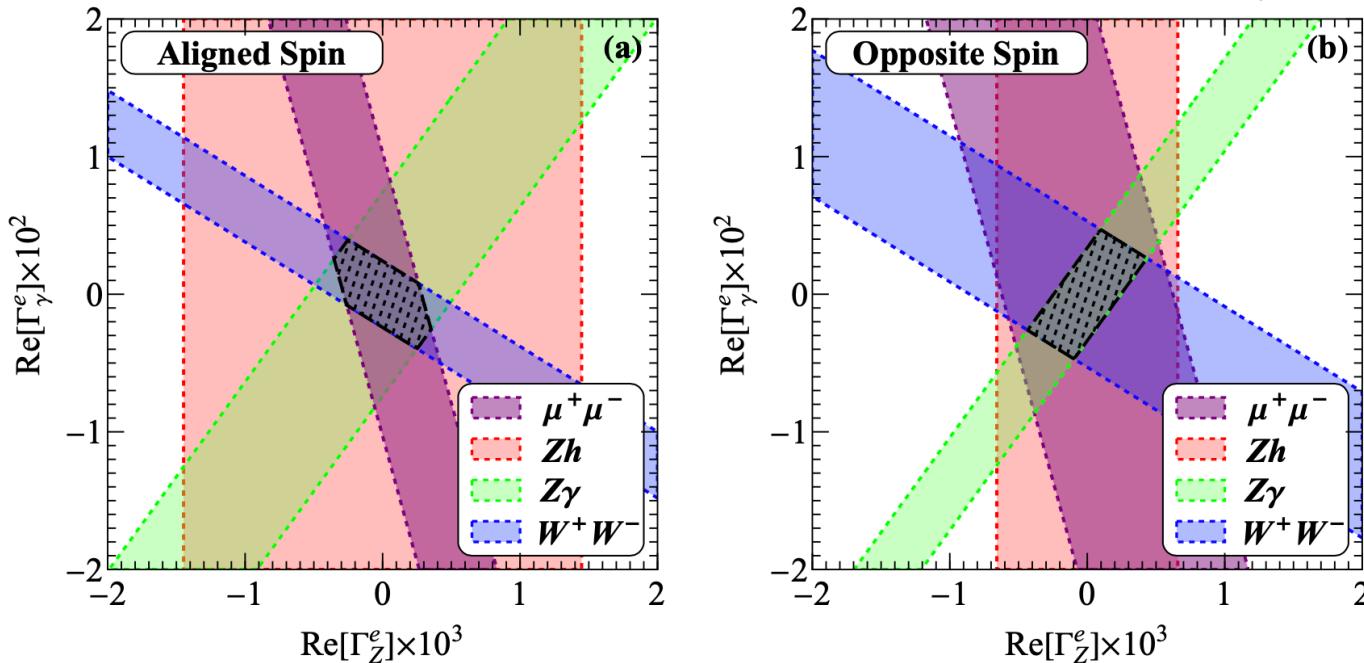
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Parity property

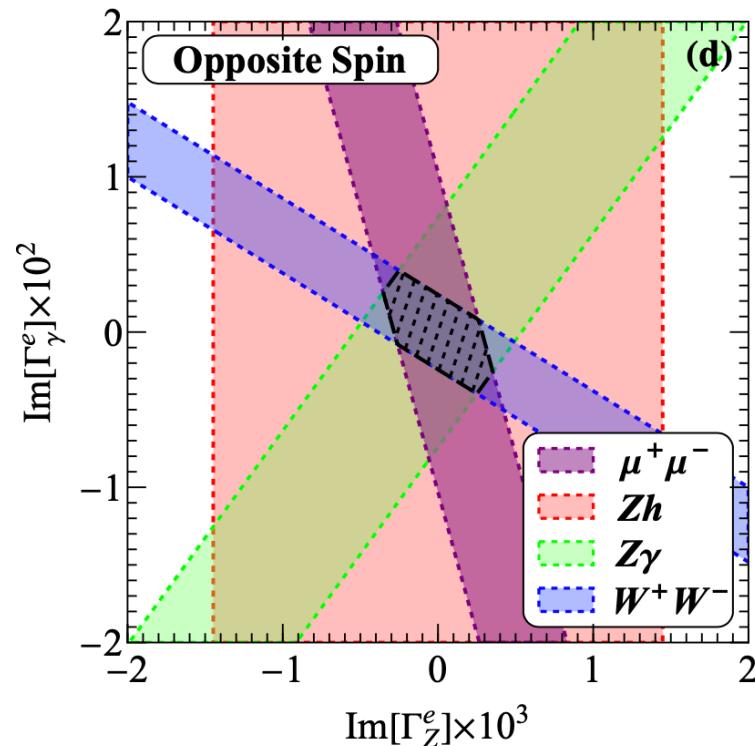
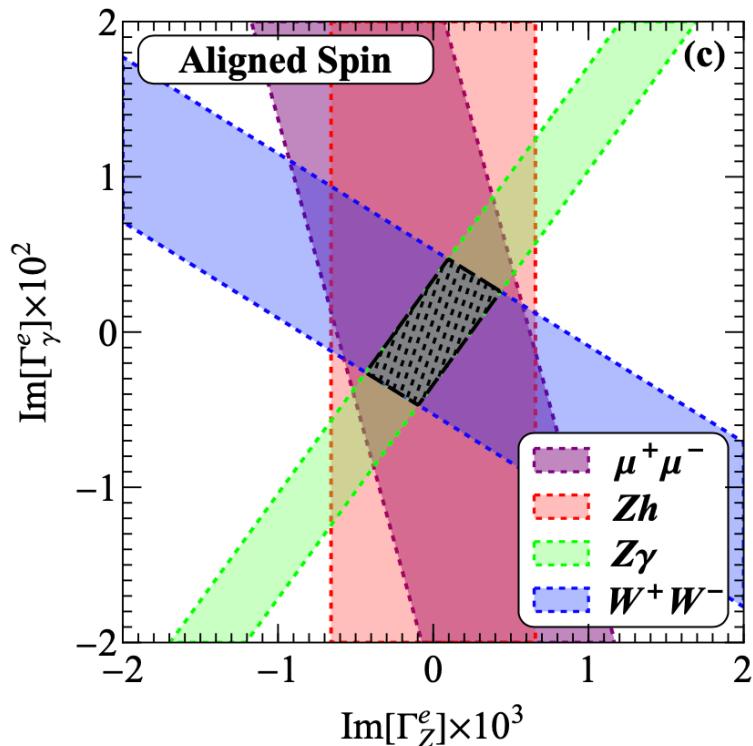
$$\mathcal{M}_{++}^* \mathcal{M}_{-+} = -\mathcal{M}_{+-}^* \mathcal{M}_{--}(g_L \leftrightarrow g_R) \quad |\mathcal{M}|_{1\phi}^2 \sim (g_L - g_R)[(g_L^e + g_R^e)\Gamma_\gamma^e + \Gamma_Z^e]$$

Pinning down Dipole Operators

For the imaginary parts of dipole couplings, things are similar

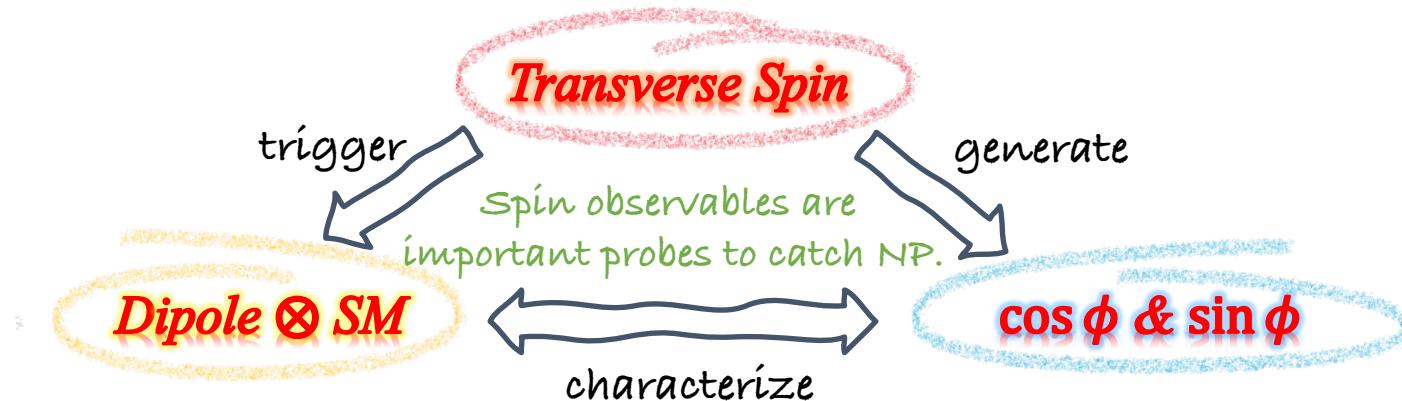
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 $\sqrt{s} = 250 \text{ GeV}, \mathcal{L} = 5 \text{ ab}^{-1}$



Offering a new opportunity for directly probing potential CP-violating effects.

Summary



- ✓ Dipole operators flip fermion helicities being ideally studied at $1/\Lambda^2$ through--

Single Transverse Spin Azimuthal Asymmetries

- ✓ STSAA simultaneously determining both Re & Im parts *without impact from other NP*, offering a new opportunity for directly probing potential CP-violating effects.
- ✓ Our bound could be reached around $O(0.01\% \sim 0.1\%)$, much stronger sensitivity than other approaches by 1~2 orders of magnitude

	$ \Gamma_Z^e $	$ \Gamma_A^e $
Our Study	0.0002	0.005
LHC Drell-Yan	0.0765	0.197
Z Partial Width	0.0582	0.093
$(g - 2)_e$	10^{-2}	10^{-6}

Thank you

Backup

BACKUP

Backup: Some Formulae

$$|\theta, \chi\rangle_1 = \cos\frac{\theta}{2}|h=+\rangle + \sin\frac{\theta}{2}e^{i\chi}|h=-\rangle \quad \text{Superposition of the two helicity states along polarization } \vec{s}(\theta, \chi)$$

$$T_{h\bar{h}} = \langle \phi, \dots | T | \chi, \bar{\chi} \rangle = \langle \phi = 0, \dots | T | \chi - \phi, \bar{\chi} - \phi \rangle \quad \text{2-to-2 rotational invariance}$$

Ken-ichi Hikasa, *Phys.Rev.D* 33 (1986) 3203, *PhysRevD*.38 (1988) 1439

$$|\mathcal{M}|^2(s, \bar{s}, \theta, \phi) = \sum_{\alpha_1, \alpha_2, \alpha'_1, \alpha'_2} \rho_{\alpha_1, \alpha'_1}(s) \bar{\rho}_{\alpha_2, \alpha'_2}(\bar{s}) \mathcal{M}_{\alpha_1, \alpha_2}(i \rightarrow f; \theta, \phi) \mathcal{M}_{\alpha'_1, \alpha'_2}^\dagger(i \rightarrow f; \theta, \phi)$$

$$\mathbf{s} = (b_1, b_2, \lambda) = (b_T \cos \phi_0, b_T \sin \phi_0, \lambda) \quad \rho = \frac{1}{2} (1 + \boldsymbol{\sigma} \cdot \mathbf{s})$$

$$\begin{aligned} \mathcal{M}_{\lambda_1, \lambda_2}(\theta, \phi) &= e^{i(\lambda_1 - \lambda_2)\phi} \mathcal{T}_{\lambda_1, \lambda_2}(\theta) & |M|^2 &= |M|_{\text{unpol}}^2 - \frac{1}{2} \lambda_T \bar{\lambda}_T \text{Re}[T_{++}^* T_{--}] \\ |\mathcal{M}|_{TU}^2 &= \frac{1}{2} b_T \text{Re} \left[e^{i(\phi - \phi_0)} \left(\mathcal{T}_{++} \mathcal{T}_{-+}^\dagger + \mathcal{T}_{+-} \mathcal{T}_{--}^\dagger \right) \right] & & - \frac{1}{2} \lambda_T \bar{\lambda}_T \text{Re}[e^{-2i\phi} T_{+-}^* T_{-+}] \\ T_{-\lambda_a, -\lambda_b, -\lambda_c, -\lambda_d}(\theta) &= \eta \cdot (-1)^{\lambda - \mu} \cdot T_{\lambda_a, \lambda_b, \lambda_c, \lambda_d}(\theta) & & + \frac{1}{2} \lambda_T \text{Re} [e^{-i\phi} (T_{+-}^* T_{--} + T_{++}^* T_{-+})] \\ \eta &= \frac{\eta_c \eta_d}{\eta_a \eta_b} \cdot (-1)^{s_a + s_b - s_c - s_d} & & - \frac{1}{2} \bar{\lambda}_T \text{Re} [e^{-i\phi} (T_{+-}^* T_{++} + T_{--}^* T_{-+})] \end{aligned}$$

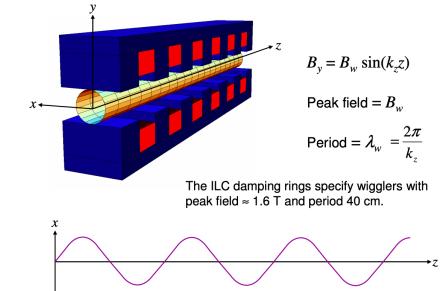
X.-K.W, BY, ZY, C.-P.Y, works in progress

Backup: Polarized beam realization

Transverse polarization is more natural

Sokolov-Ternov effect (92.4%, minutes-hours, 50GeV)

Laser-assistant
Spin-precession



Photon-based scheme:

Polarized positrons are produced via pair production in a thin target from circularly-polarized photons with energy of multi-MeV (up to about 100 MeV). The cost difference between an polarized source and an upgrade from a unpolarized source is small ($\sim 1\%$). At 500 GeV, loss of polarization $<1\%$, at IP $<0.25\%$.

Polarized electron source consists of a polarized high-power laser beam and a high- voltage dc gun with a semiconductor photocathode.

Only polarization parallel or anti-parallel to the guide fields of the damping ring is preserved.
Need to avoid spin-orbit coupling resonance depolarizing effects.

The spin rotator systems between the damping rings and the main linacs permit the setting of arbitrary polarization vector orientations at the IP.

Polarized-photons source:

- I. a high-energy electron beam ($>\sim 150$ GeV) passing through a short period, helical undulator.
(E-166, SLAC)
- II. Compton backscattering of laser light off a GeV energy-range electron beam. (KEK)
In both schemes a polarization of about $|Pe+| \geq 90\%$ is reported.