



南京理工大学
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Testing **EWPT** at the **lifetime** and **energy** frontiers

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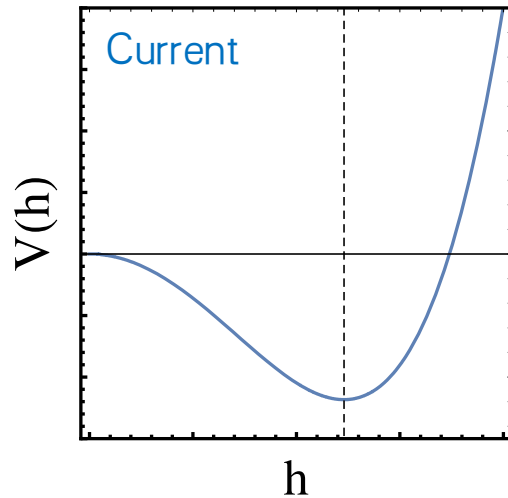
Nanjing University of Science and Technology

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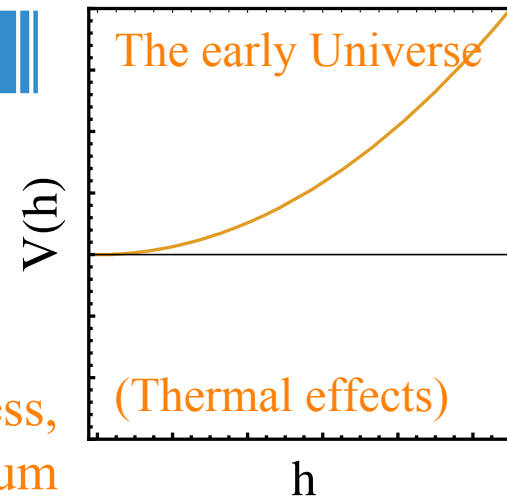
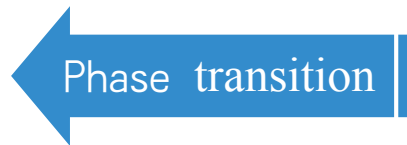
CEPC 2023

Phase transition in electroweak theory

EW symmetry restoration in the early Universe



W & Z bosons are massive;
Photon is massless,
Mexican-hat like



$SU(2)_L$ & $U(1)_Y$ bosons are massless,
True vacuum

What is the pattern of EW phase transition (PT)?

It could be –

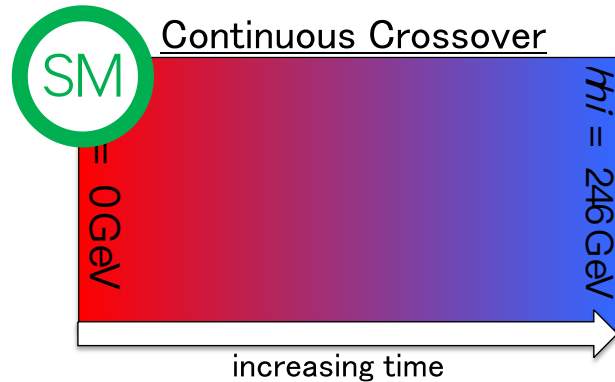
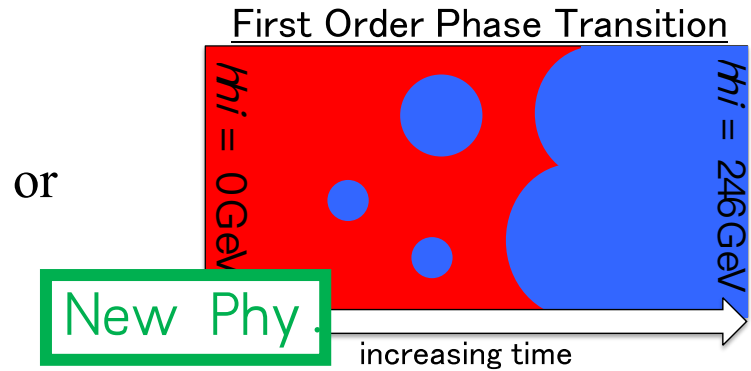


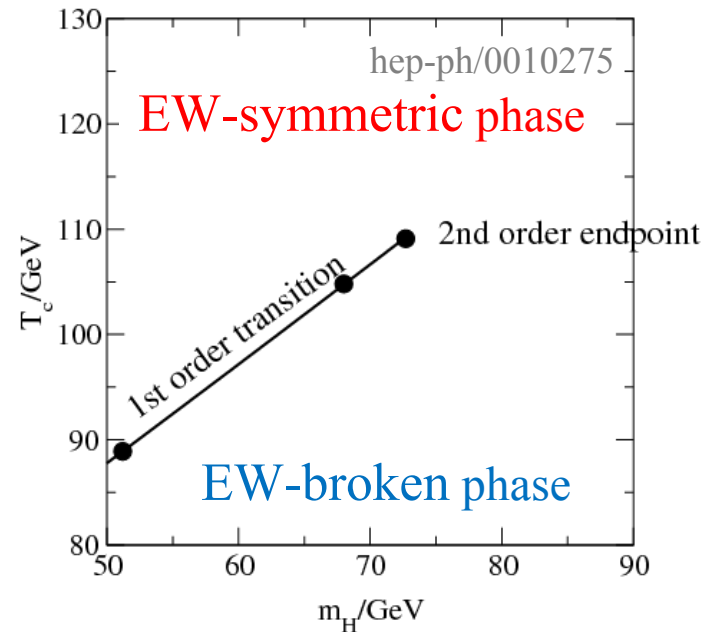
Figure from L.-T. Wang's talk in IHEP workshop



Lattice calculation shows the phase diagram \implies

Thus in the SM it is a crossover, since $M_h = 125 \text{ GeV} > 75 \text{ GeV}$;

However, a 1st-order EWPT is more interesting.
(Needs **new physics**)



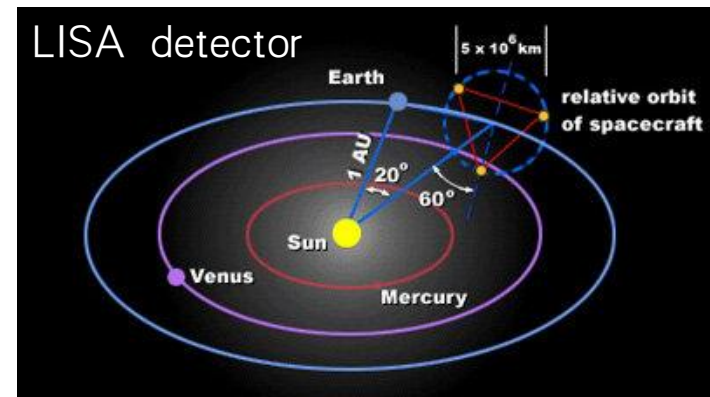
Why is a 1st-order EWPT interesting?

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- It's the essential ingredient of the **EW baryogenesis**.
- Acting as the background of very rich **dark matter** mechanisms
- Sources of the stochastic GWs:

- Collision of the bubbles
- Sound waves in plasma
- Turbulence in plasma

EWPT GWs typically peak in mHz.



How to achieve a 1st-order EWPT?

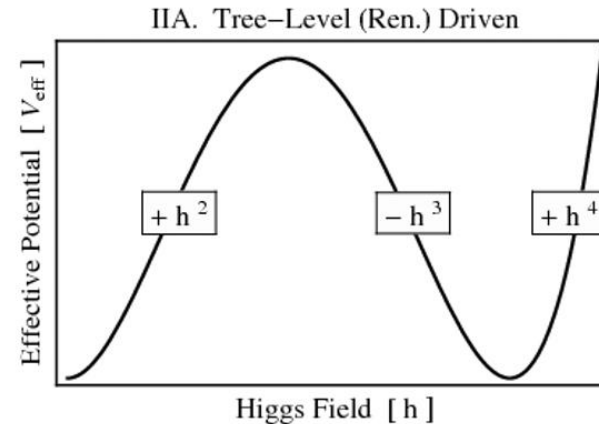
Adding a barrier for the Higgs potential via new physics!

The decay between two vacua separated by a barrier.

The VEV of the Higgs field *jumps*.

Getting a barrier via the help of additional **scalar field(s)**:

- SM + real singlet (xSM);
- 2HDM;
- Georgi-Machacek model;
-



We choose the **xSM** as the benchmark model.

- It's simple, but has captured the most important feature of EWPT;
- It can be treated as the prototype of many new physics EWPT models.

EWPT in the xSM (SM + real singlet)

We choose the **xSM** as the benchmark model.

It's simple, but has captured the most important feature of EWPT.

The scalar potential of the xSM

$$V = -\mu^2 |H|^2 + \lambda |H|^4 + \frac{a_1}{2} |H|^2 S + \frac{a_2}{2} |H|^2 S^2 \\ + b_1 S + \frac{b_2}{2} S^2 + \frac{b_3}{3} S^3 + \frac{b_4}{4} S^4$$

8 input parameters:

1 unphysical, 2 fixed by Higgs mass & VEV; 5 *free* parameters.

Expansion around the VEV

$$H = \frac{1}{\sqrt{2}} \begin{pmatrix} 0 \\ v + h \end{pmatrix}, \quad S = v_s + s, \quad \begin{pmatrix} h \\ s \end{pmatrix} = \begin{pmatrix} \cos \theta & -\sin \theta \\ \sin \theta & \cos \theta \end{pmatrix} \begin{pmatrix} h_1 \\ h_2 \end{pmatrix}$$

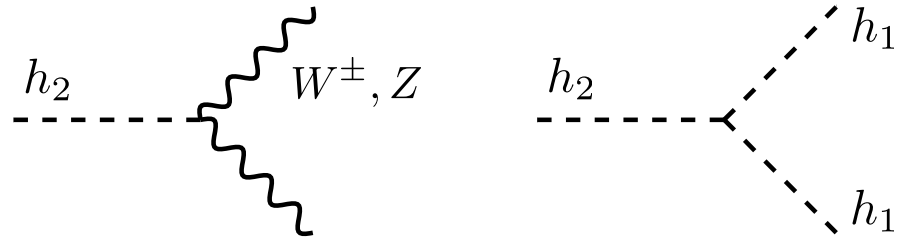
Mass eigenstates & the mixing angle.

Probing EWPT of the xSM at colliders

Feature of the xSM

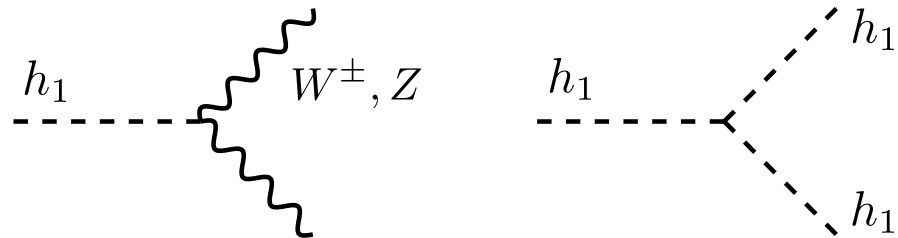
Two neutral scalars: h_1 (Higgs-like) and h_2 (singlet-like, TeV), with mixing angle θ ;

$$\begin{aligned}
 g_{h_2 V V} &= g_{h V V}^{\text{SM}} \sin \theta \\
 g_{h_2 f \bar{f}} &= g_{h f \bar{f}}^{\text{SM}} \sin \theta \\
 \lambda_{h_2 h_1 h_1} &\propto \sin \theta
 \end{aligned}$$



Direct searches at the pp colliders

$$\begin{aligned}
 g_{h_1 V V} &= g_{h V V}^{\text{SM}} \cos \theta \\
 g_{h_1 f \bar{f}} &= g_{h f \bar{f}}^{\text{SM}} \cos \theta \\
 \lambda_{h_1 h_1 h_1} &= \lambda_{h h h}^{\text{SM}} f(\theta)
 \end{aligned}$$



Indirect searches at the e^+e^- colliders

Muon collider!

Precision and Energy Frontier!

A high-energy muon collider is able to execute both the

- **direct search**
- **indirect search**

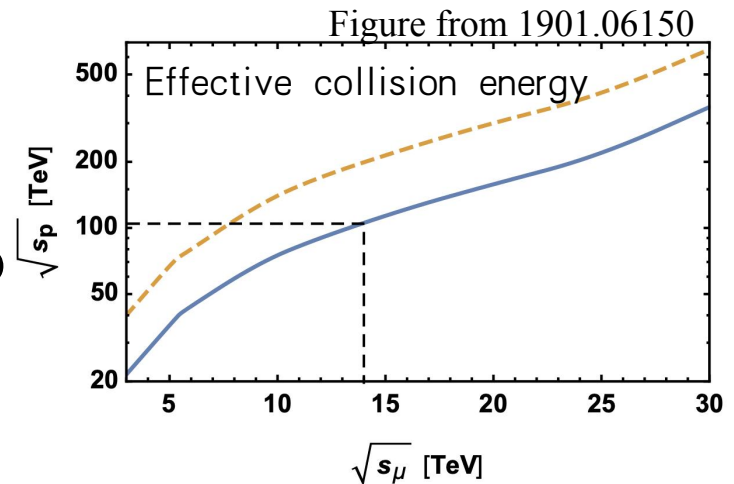
strategies for EWPT in xSM!

Compared to the e^+e^- machine:

- Synchrotron radiation is **suppressed by 10^9** since $M_\mu \gg M_e$, hence the collision energy can reach O(10) TeV;
- Also **very clean**, as long as the beam-induced-background is controllable (main challenge).

Compared to the pp machine:

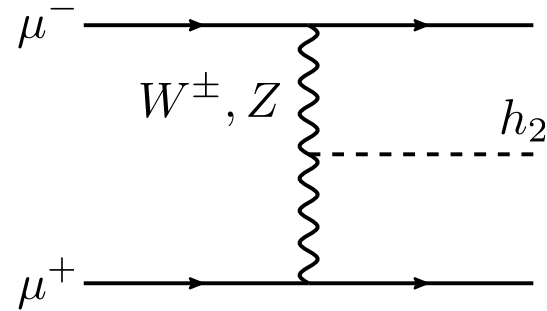
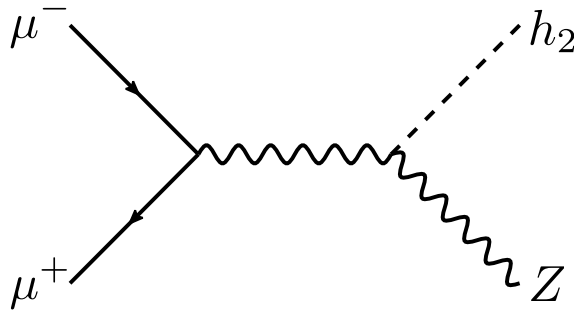
- The **entire collision energy** can be used to probe hard process;
- Much **cleaner** due to the small QCD background.



Muon collider: direct search

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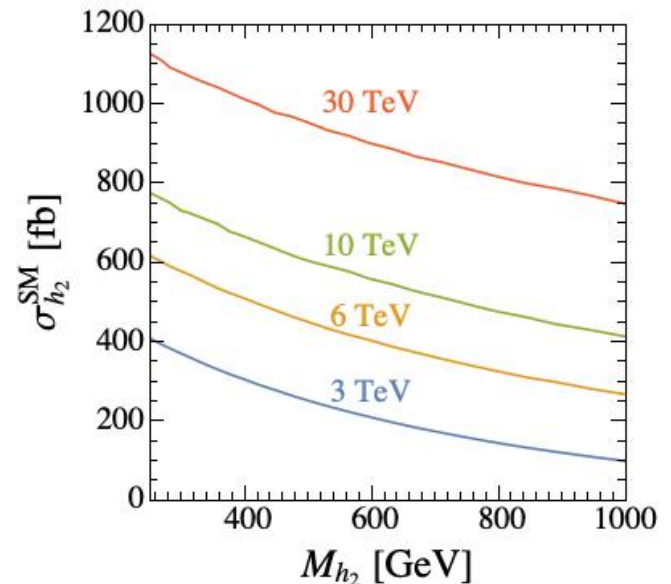
Producing the h_2 at a muon collider



Zh_2 associated production & Vector Boson Fusion (VBF).

At a multi-TeV collider, the dominant channel is VBF, in which W^+W^- fusion dominates (90%);

$\sigma^{\text{SM}}(h_2)$: rate obtained by assuming a Higgs-like coupling for the h_2 .



Muon collider: direct search

Decay of h_2 to SM particles (X = vector boson or fermion)

$$\Gamma(h_2 \rightarrow XX) = \sin^2 \theta \times \Gamma^{\text{SM}}(h_2 \rightarrow XX),$$

$$\Gamma(h_2 \rightarrow h_1 h_1) \propto \lambda_{h_2 h_1 h_1}^2$$

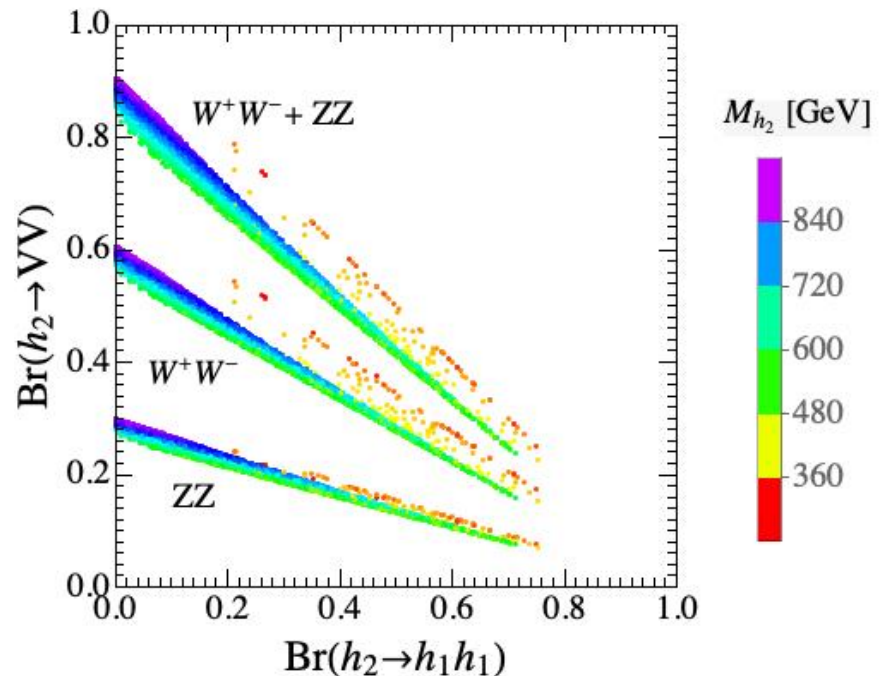
Dominant channels: di-boson (W^+W^- , ZZ), tt , and $h_1 h_1$.

The $h_1 h_1$ channel can reach a branching ratio of 80%;

For heavy h_2 , the VV channel dominates;

We choose

- $h_2 \rightarrow ZZ \rightarrow l^+l^-l^+l^-$
 - $h_2 \rightarrow h_1 h_1 \rightarrow bbbb$
- for a detailed simulation.



Muon collider: direct search

The $h_2 \rightarrow h_1 h_1 \rightarrow bbbb$ channel:

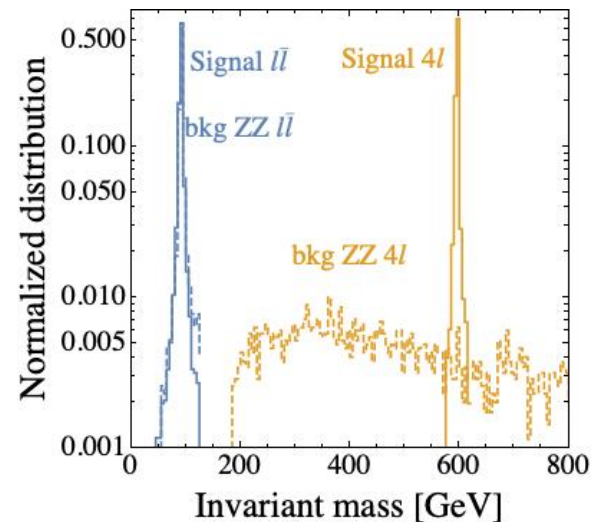
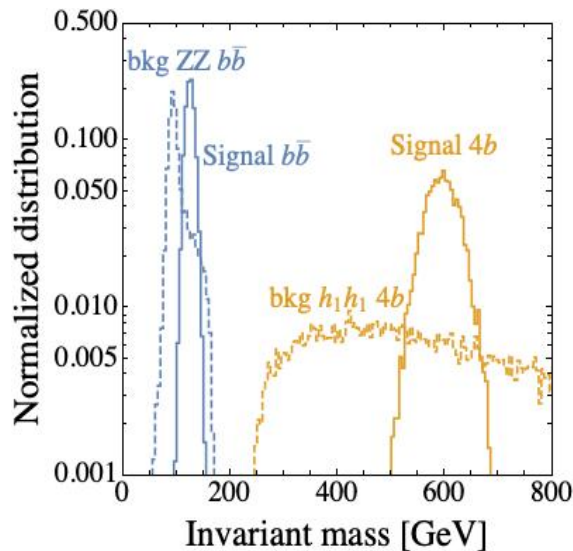
Main background:

- Vector Boson Scattering $ZZ \rightarrow bbbb$
- $h_1 h_1 \rightarrow bbbb$.

The $h_2 \rightarrow ZZ \rightarrow l^+ l^- l^+ l^-$ channel:

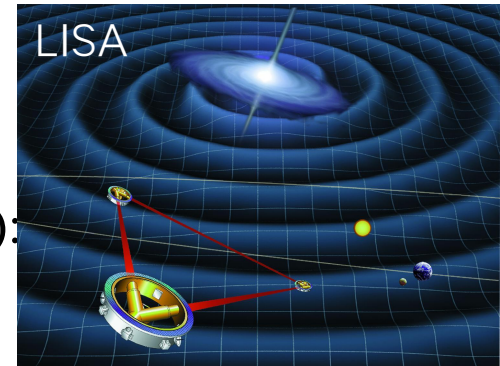
Main background:

- Vector Boson Scattering $ZZ \rightarrow l^+ l^- l^+ l^-$.



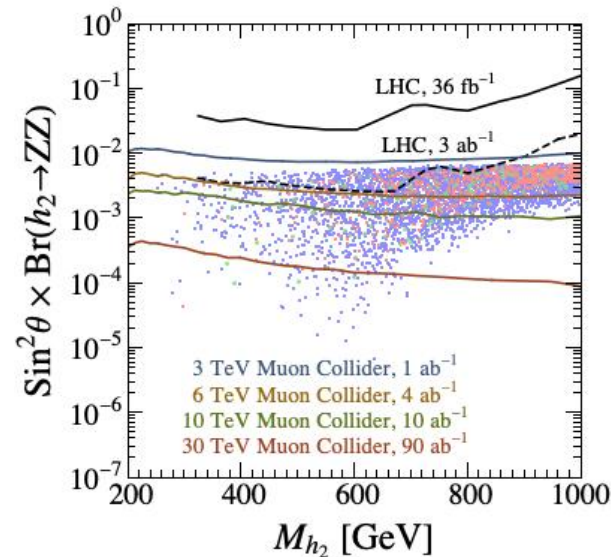
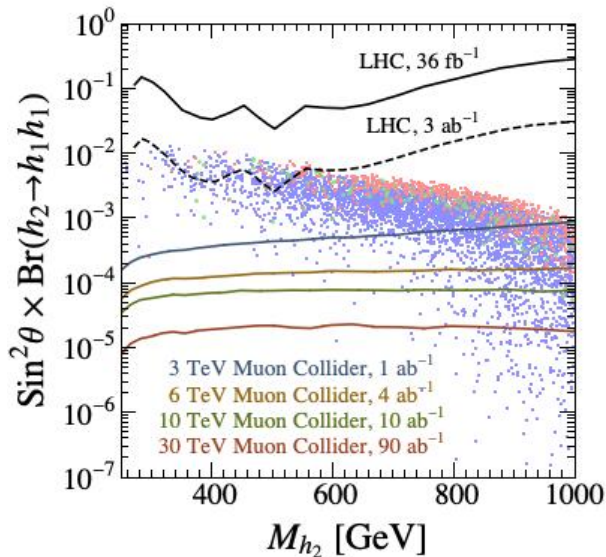
Muon collider: direct search

The collider search and gravitational wave detection are complementary!



For the LISA detector, signal-to-noise ratio (SNR):

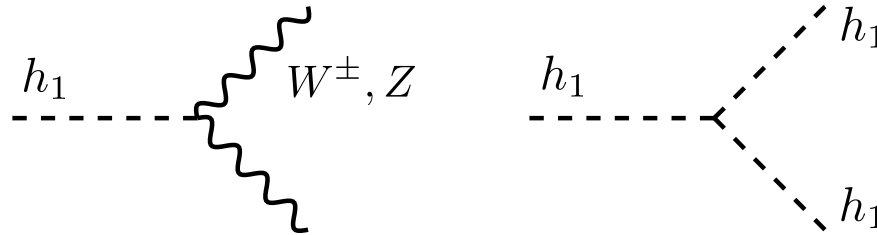
$$\text{SNR} = \sqrt{\mathcal{T} \int_{f_{\min}}^{f_{\max}} df \left(\frac{\Omega_{\text{GW}}(f)}{\Omega_{\text{LISA}}(f)} \right)^2}$$



The diHiggs & diboson channels are complementary as well

Muon collider: indirect search

The gauge boson coupling & triple Higgs coupling. Making use of the results in [Han, Liu, Low and Wang, 2008.12204].

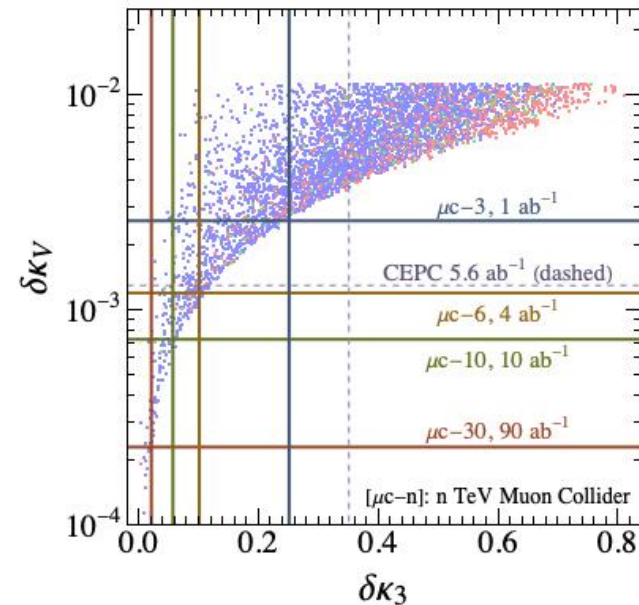


Defining deviations

$$\delta\kappa_V = \left| \frac{g_{h_1 VV}}{g_{h_1 VV}^{\text{SM}}} - 1 \right|,$$

$$\delta\kappa_3 = \frac{\lambda_{h_1 h_1 h_1}}{\lambda_{h_1 h_1 h_1}^{\text{SM}}} - 1$$

We can obtain the projections.



LLP EWPT

From J. Kozaczuk, M. Ramsey-Musolf, J. Shelton, Phys.Rev.D
101 (2020) 11, 115035

The Higgs mixing is small

Approximate **Z_2 symmetry**

EWPT can happen as **two-step transition**

$$(h = 0, s \simeq 0) \rightarrow (h = 0, s \neq 0) \rightarrow (h \neq 0, s \simeq 0),$$

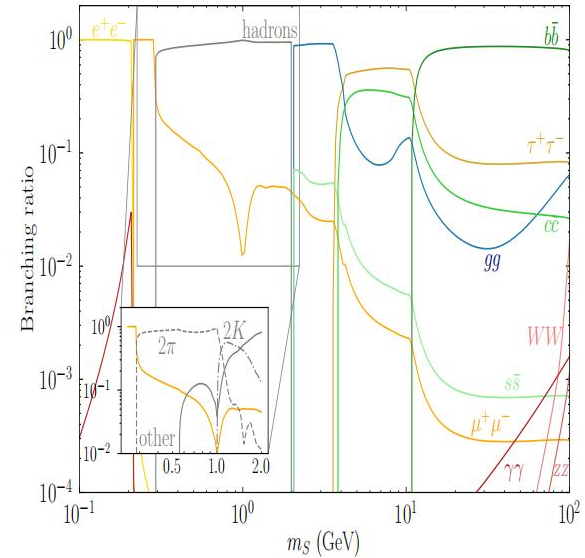
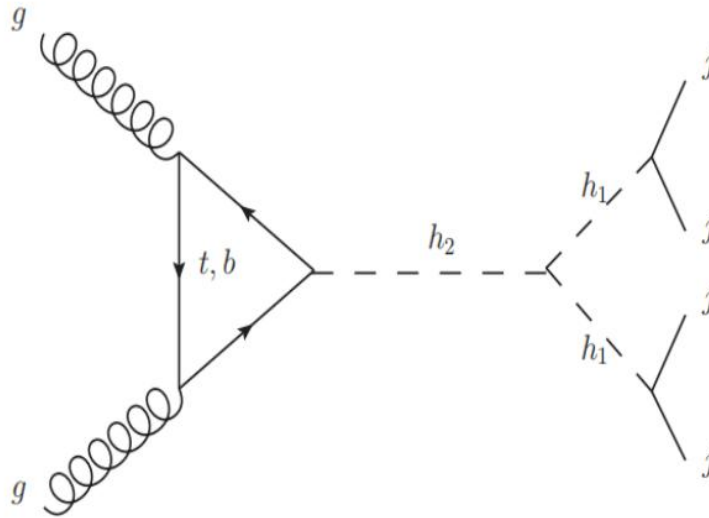
There are analytical bounds from two-step transition

$$a_2 \gtrsim \frac{m_{h_1}^2}{4v^2} \frac{\Delta}{1 - \Delta},$$
$$|b_3| > \sqrt{\frac{9}{4} b_4 (2m_{h_1}^2 - a_2 v^2 + 2T_{\text{EW}}^2 \beta)},$$
$$b_4 \gtrsim \frac{m_{h_1}^4 \Delta}{4\lambda v^4 (1 - \Delta)},$$

Production processes

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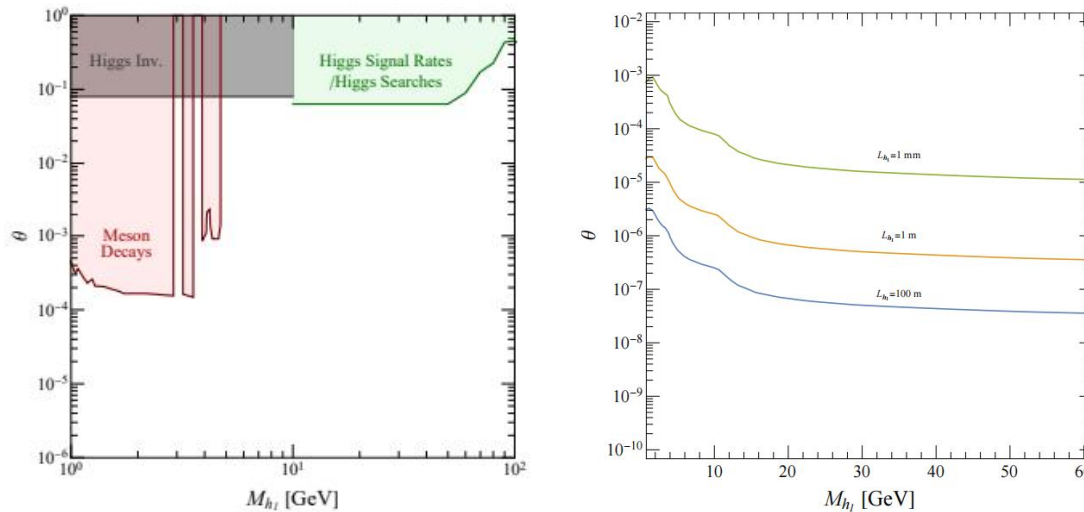
$$gg \rightarrow h_{2(SM)} \rightarrow h_1 h_1 \rightarrow 4j$$



1st-order EWPT leads to large $BR(h_2 \rightarrow h_1 h_1)$.
 h_1 decays into jets dominantly.

Long-lived Particles

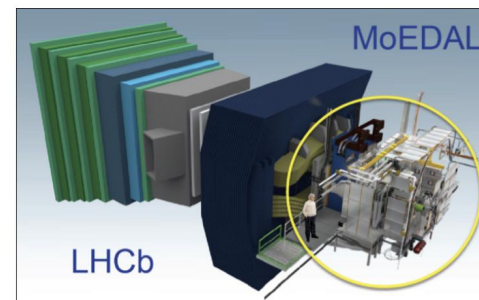
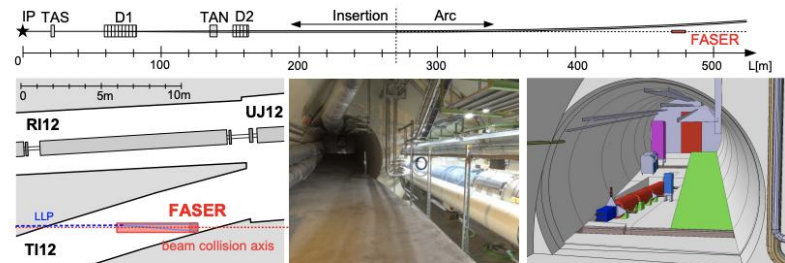
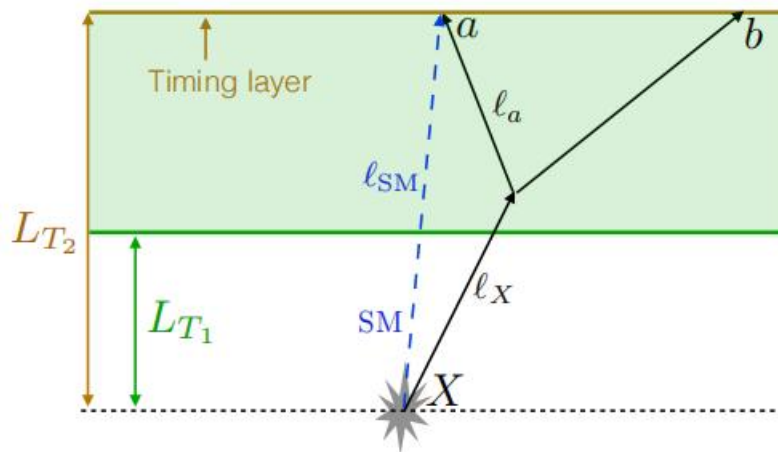
The current limits on (M_{h_1}, θ)



For $M_{h_1} < 10$ GeV, the current limits from rare meson decays at the LHCb, leads to h_1 as a long-lived particle (LLP).

Detectors for LLPs

CMS-Timing, FASER, MoEDAL-MAPP are to be operated at Run 3.



Many others, e.g. MATHUSLA and CODEX-b are in discussions.

CMS-Timing detector using the **time-delayed leptons/jets** as signals, while the other detectors using displaced vertex.

Connects to 1st-order EWPT

Link between the number of events and 1st-order EWPT

$$\begin{aligned} N_{\text{signal}} &= \sigma_{pp \rightarrow h_2} \times L \times BR_{h_2 \rightarrow h_1 h_1}(\mathbf{a}_2, \mathbf{M}_{h_1}) \\ &\times BR_{h_1 \rightarrow jj}^2(\mathbf{M}_{h_1}) \times \epsilon_{\text{kin}}(\mathbf{M}_{h_1}) \times \epsilon_{\text{geo}}(\mathbf{M}_{h_1}, \boldsymbol{\theta}) \end{aligned}$$

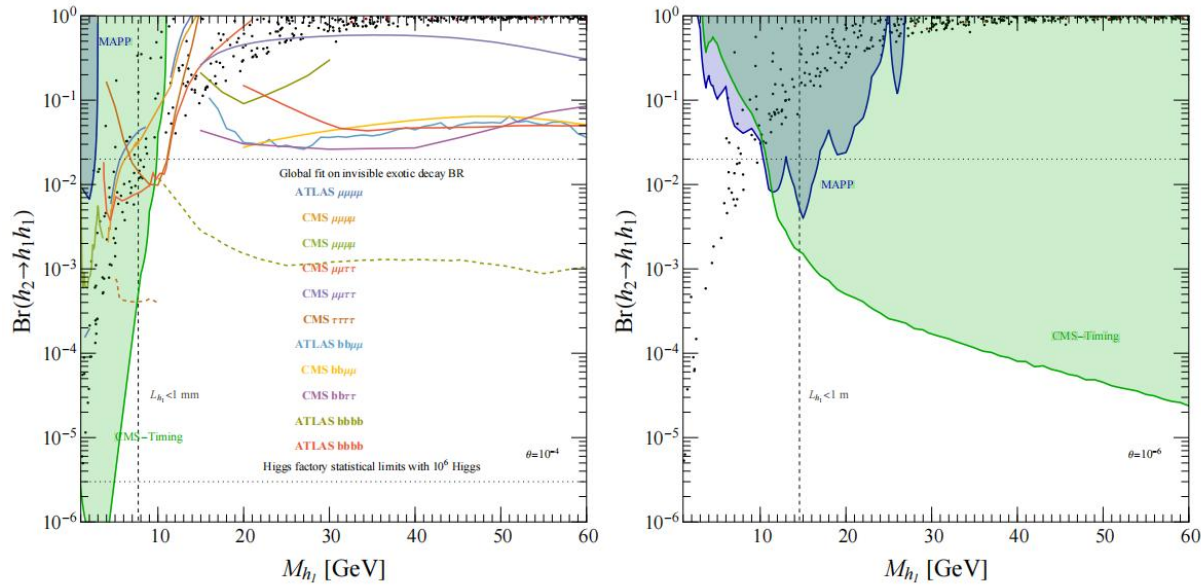
$$BR_{h_2 \rightarrow h_1 h_1}(\mathbf{a}_2, \mathbf{M}_{h_1}) = \frac{\Gamma_{h_2 \rightarrow h_1 h_1}}{\Gamma_{h_2}^{\text{SM}} + \Gamma_{h_2 \rightarrow h_1 h_1}}$$

$$\Gamma_{h_2 \rightarrow h_1 h_1} \propto (\mathbf{a}_2 \mathbf{v})^2$$

LLP events are sensitive to $|H|^2 S^2$ couplings.

Sensitivity

Fixed $\theta = 10^{-4}$ (left), 10^{-6} (right).



No FASER sensitivity, too forward

CMS-Timing can probe large parameter space where the searches for promptly exotic Higgs decays can not reach.

MAPP can only probe small parameter space, while none for FASER.

Conclusion

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1st-order EW phase transition is interesting:

- Theoretically, it is the essential ingredient of EW baryogenesis, and can trigger very rich dark matter mechanisms;
- Experimentally, it yields detectable gravitational waves.

We propose strategies to probe **1st-order EWPT** from LLP signatures at the HL-LHC, and at a high-energy **muon collider**.

For heavy, strongly coupled scalar corresponding to **1st-order EWPT**, it can lead to **direct and indirect signals at the muon colliders, and complementary GW signals**.

For light, weakly coupled scalar corresponding to **1st-order EWPT**, it can lead to **LLP signatures, but no detectable gravitational waves**.

LLP search is **complementary** to the searches for promptly exotic Higgs decays!

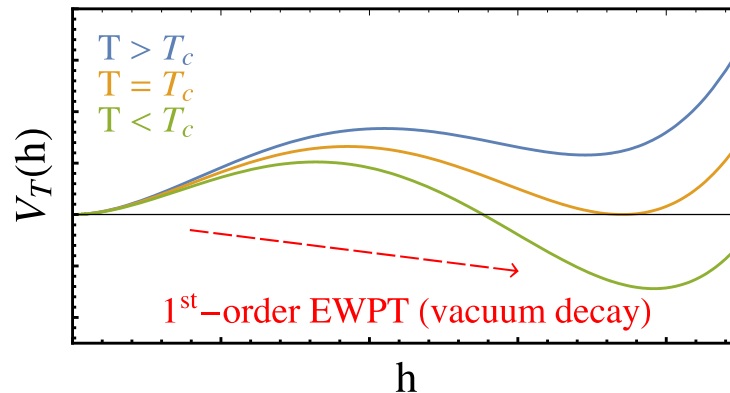
1st-order EWPT in the xSM

At finite temperature:

$$V = -(\mu^2 - c_H T^2)|H|^2 + \lambda|H|^4 + \frac{a_1}{2}|H|^2 S + \frac{a_2}{2}|H|^2 S^2 + (b_1 + m_1 T^2)S + \frac{b_2 + c_S T^2}{2}S^2 + \frac{b_3}{3}S^3 + \frac{b_4}{4}S^4$$

$$c_H = \frac{3g^2 + g'^2}{16} + \frac{y_t^2}{4} + \frac{\lambda}{2} + \frac{a_2}{24}, \quad c_S = \frac{a_2}{6} + \frac{b_4}{4}, \quad m_1 = \frac{a_1 + b_3}{12}$$

An Illustration --



Question:

Can collider experiments probe the 1st-order EWPT parameter space?

Muon collider: direct search

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Main background:

✓ Vector Boson Scattering $ZZ \rightarrow bbbb$ (IIII) and $h_1 h_1 \rightarrow bbbb$.

Kinematic Cuts:

Cut I: $p_T > 30 \text{ GeV}$, $|\eta| < 2.43$, $M_{recoil} > 200 \text{ GeV}$, (Cut I)

Cut II: minimizing $\chi^2 = (M_{12} - M_h)^2 + (M_{34} - M_h)^2$

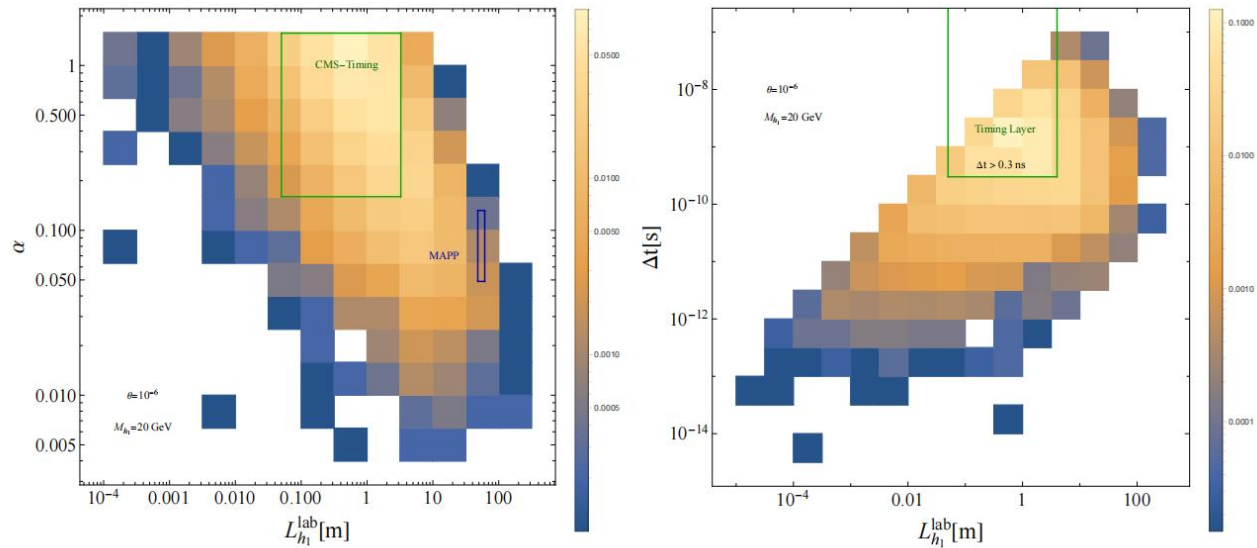
$|M_{12} - M_h| < 15(10) \text{ GeV}$, $|M_{34} - M_h| < 15(10) \text{ GeV}$

Cut III: $|M_{1234} - M_{h_2}| < 30(20) \text{ GeV}$,

$\Delta E/E = 10\%$, $\epsilon_{b\text{-tag}} = 70\%$

Detector efficiency

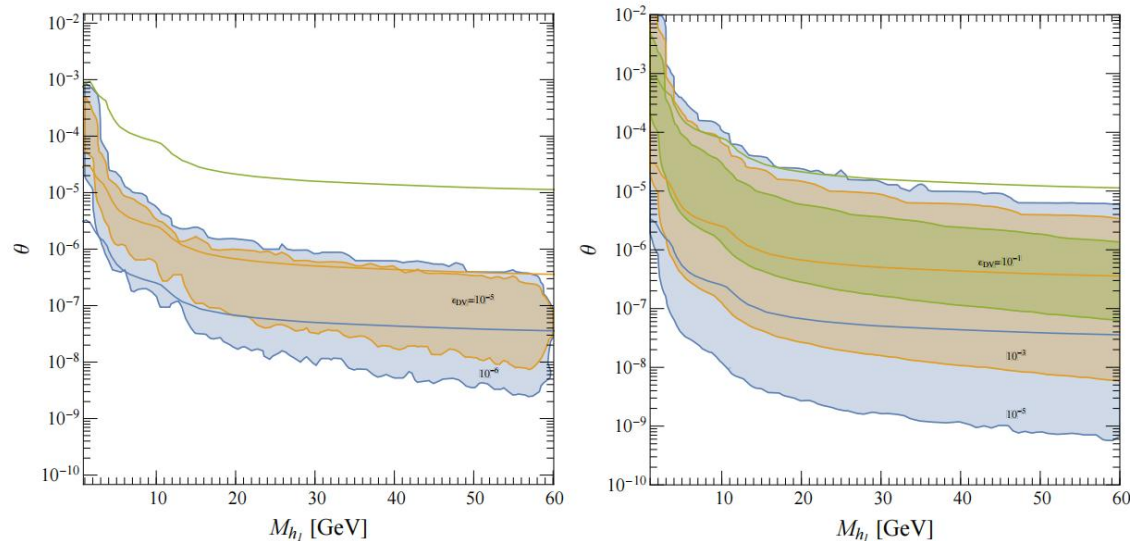
Detector efficiency is a function of geometrical coverage,



and resolution in time for timing detector.
CMS-Timing has large coverage, and good resolution.
MAPP has small coverage,
while negligible for FASER.

Detector efficiency

Detector efficiency is a function of geometrical coverage,



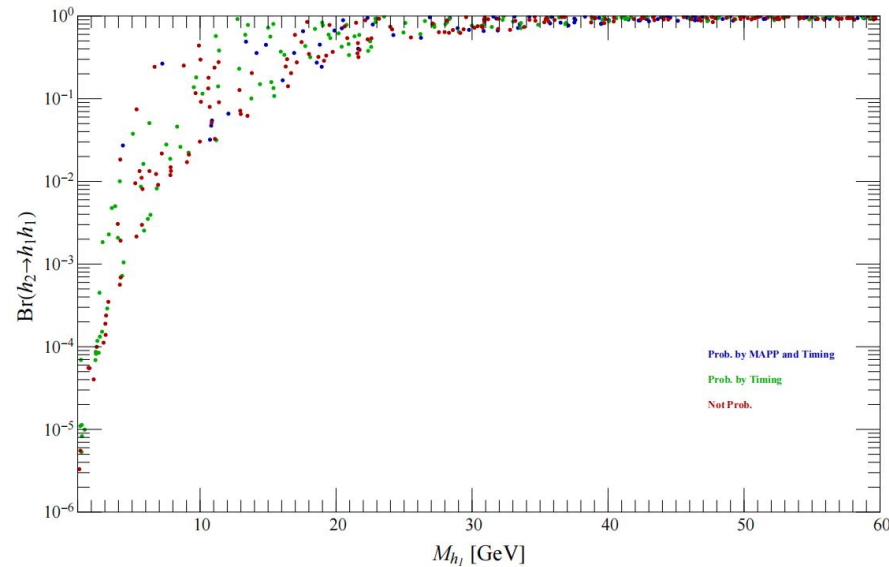
CMS-Timing has efficiency up to 10^{-1} .

MAPP has 10^{-4} ,

while negligible for FASER.

Signatures at Colliders

Running θ



Green points are probed by CMS-Timing, but not by MAPP. CMS-Timing can probe **a lot more** 1st-order EWPT points. There are still appreciable points not probed by any of LLP detectors.