

EFTs of Weakly-Interacting Light Particles and Their Phenomenology

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CEPC Flavor Physics/New Physics/Detector Technology Workshop

[HS, Sun, Yu \[2306.05999\]](#)

[HS, Sun, Yu \[2305.16770\]](#)

Kling, Li, [HS](#), Su, Su, JHEP [[2212.06186](#)]

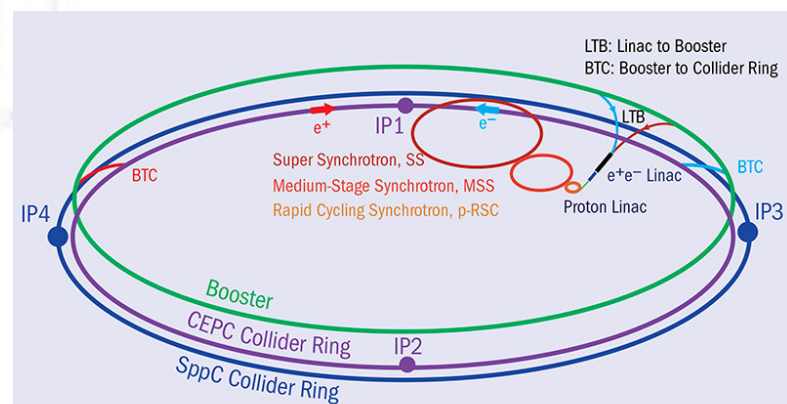
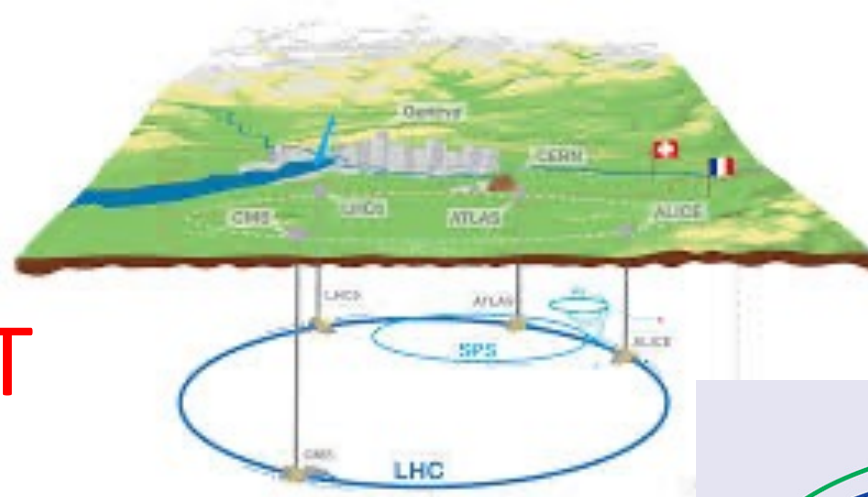
Aug 18, 2023

Search for New Physics

Status:

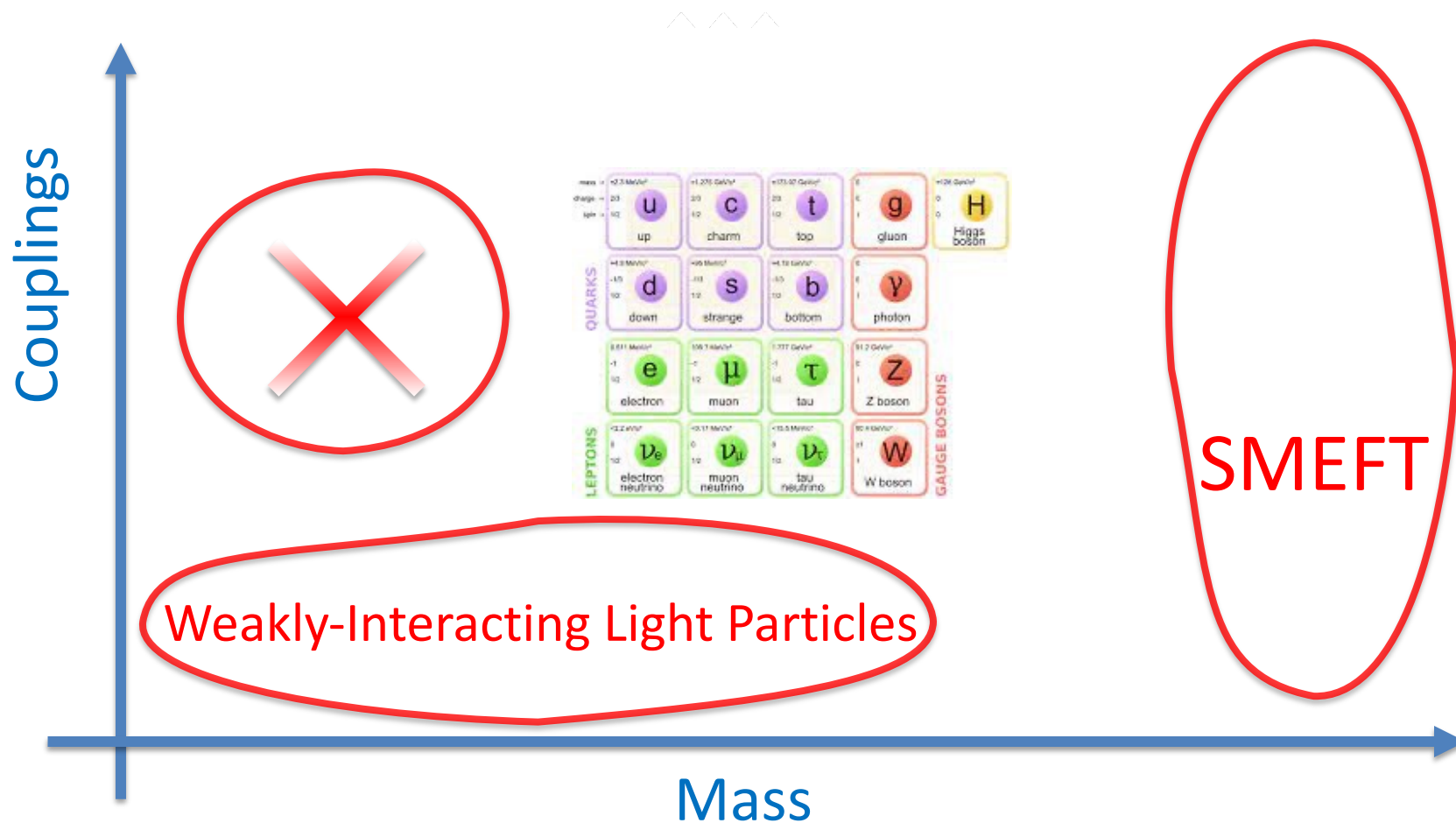
- No new particles are directly found with mass up to $\sim 1 \text{ TeV}$ and $\mathcal{O}(1)$ couplings
- Experiment anomalies and theoretical challenges need new physics

EFT
SMEFT

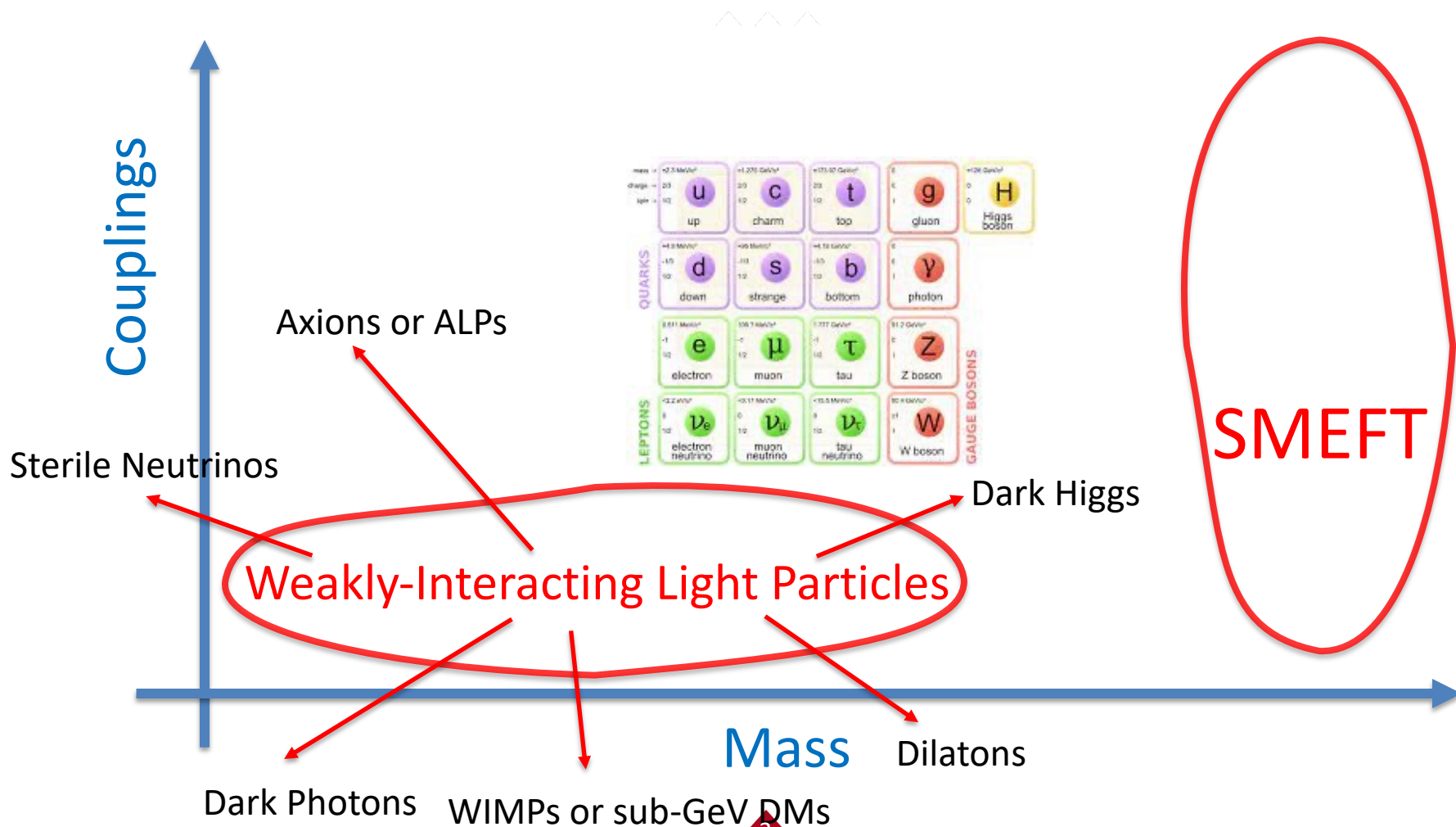


Search for New Physics

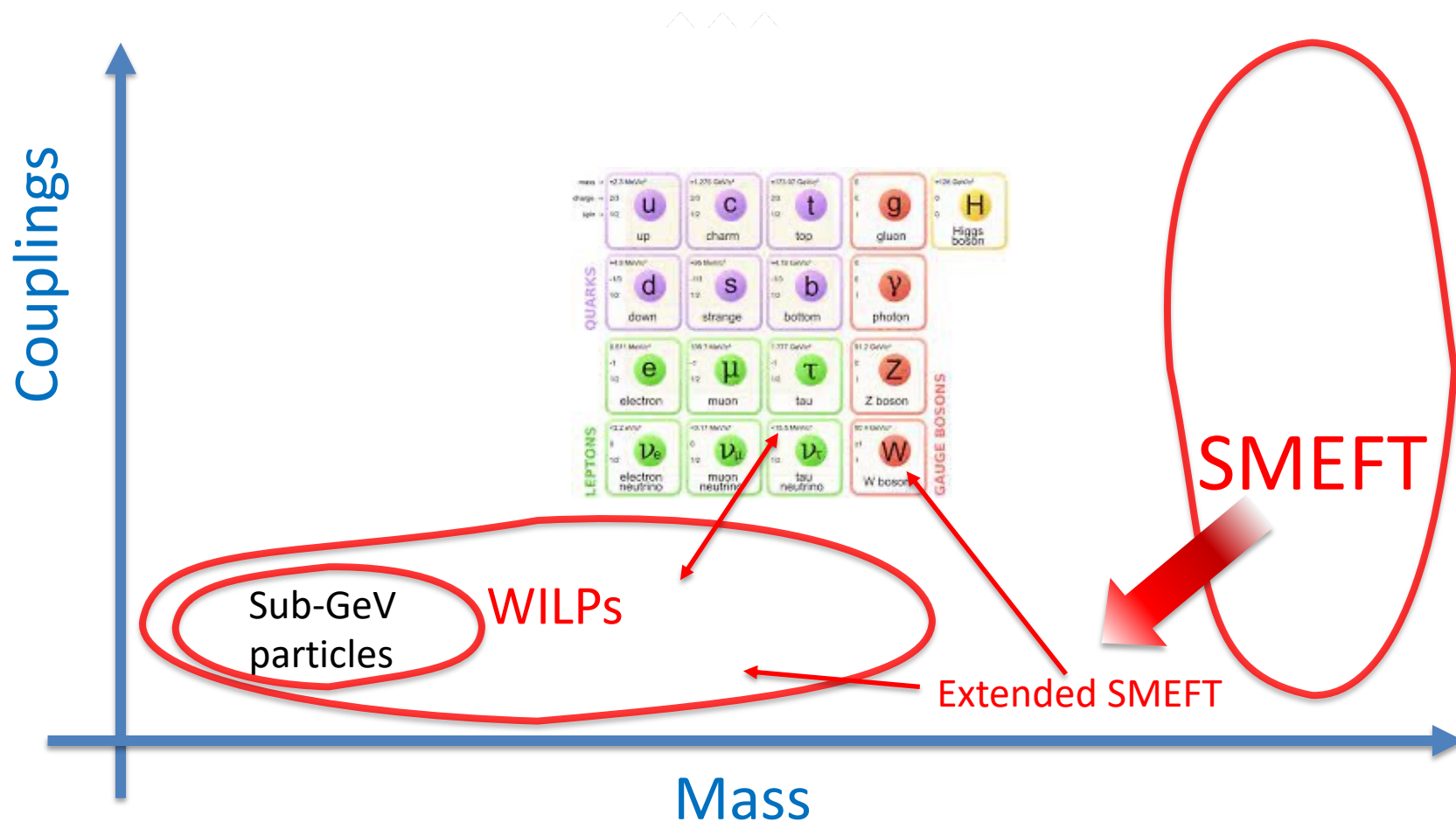
DoFs are correct or enough?



Weakly-Interacting Light Particles (WILPs)



Weakly-Interacting Light Particles (WILPs)



classification of Singlet Particles

We only consider SM singlet particles with spin up to 1.

$$\begin{aligned}
 h = 0 &: \phi \sim 1 && \wedge \wedge \wedge \wedge \\
 h = -\frac{1}{2} &: \psi \sim \lambda_\alpha \\
 h = \frac{1}{2} &: \psi^\dagger \sim \tilde{\lambda}^{\dot{\beta}} && p \sim \lambda_\alpha \tilde{\lambda}^{\dot{\beta}} \\
 h = -1 &: X_L \sim \lambda_\alpha \lambda_\beta \\
 h = 1 &: X_R \sim \tilde{\lambda}^{\dot{\alpha}} \tilde{\lambda}^{\dot{\beta}}
 \end{aligned}$$

The independent and complete effective operators can be constructed systematically via the Young tensor method.

Li et al. 20', 20', 22'

ABC4EFT

Building Blocks Summary

Sector	Building block	Lorentz group	$SU(3)_C$	$SU(2)_W$	$U(1)_Y$	$U(1)$
SM	$G_{L/R}$	$(1, 0)/(0, 1)$	8	1	0	0
	$W_{L/R}$	$(1, 0)/(0, 1)$	1	3	0	0
	$B_{L/R}$	$(1, 0)/(0, 1)$	1	1	0	0
	L/L^\dagger	$(\frac{1}{2}, 0)/(0, \frac{1}{2})$	1	2	$\mp\frac{1}{2}$	0
	e_c/e_c^\dagger	$(\frac{1}{2}, 0)/(0, \frac{1}{2})$	1	1	± 1	0
	Q/Q^\dagger	$(\frac{1}{2}, 0)/(0, \frac{1}{2})$	$3\bar{3}$	2	$\pm\frac{1}{6}$	0
	u_c/u_c^\dagger	$(\frac{1}{2}, 0)/(0, \frac{1}{2})$	$\bar{3}/3$	1	$\mp\frac{2}{3}$	0
	d_c/d_c^\dagger	$(\frac{1}{2}, 0)/(0, \frac{1}{2})$	$\bar{3}/3$	1	$\pm\frac{1}{3}$	0
	H/H^\dagger	$(0, 0)$	1	2	$\pm\frac{1}{2}$	0
Real scalar	s	$(0, 0)$	1	1	0	0
Complex Scalar	S/S^\dagger	$(0, 0)$	1	1	0	$\pm q_S$
Real Goldstone	$u_\mu = D_\mu s$	$(\frac{1}{2}, \frac{1}{2})$	1	1	0	0
Complex Goldstone	$u_\mu = D_\mu S$ $u_\mu^\dagger = D_\mu S^\dagger$	$(\frac{1}{2}, \frac{1}{2})$	1	1	0	$\pm q_u$
Majorana fermion	χ/χ^\dagger	$(\frac{1}{2}, 0)/(0, \frac{1}{2})$	1	1	0	$\pm q_M$
Dirac fermion	χ_L/χ_L^\dagger	$(\frac{1}{2}, 0)/(0, \frac{1}{2})$	1	1	0	$\pm q_D$
	$\chi_{Rc}/\chi_{Rc}^\dagger$	$(\frac{1}{2}, 0)/(0, \frac{1}{2})$	1	1	0	$\mp q_D$
Real Vector	X_L/X_R	$(1, 0)/(0, 1)$	1	1	0	0
Complex Vector	X_L/X_R	$(1, 0)/(0, 0)$	1	1	0	$+q_V$
	X_L^\dagger/X_R^\dagger	$(1, 0)/(0, 1)$	1	1	0	$-q_V$

Summary of SEFT

Singlet		$dim-4$	$dim-5$	$dim-6$	$dim-7$	$dim-8$	
ϕEFT Scalar	Real	w/o \mathbf{Z}_2	-	$9 + 6n_f^2$	$10 + n_f + 7n_f^2$	$30 + n_f + \frac{965}{12}n_f^2 + \frac{3}{2}n_f^3 + \frac{397}{12}n_f^4$	$\frac{1}{12}(516 + 36n_f + 1241n_f^2 + 42n_f^3 + 661n_f^4)$
		w/ \mathbf{Z}_2	-	-	$10 + 6n_f^2$	$n_f + n_f^2$	$\frac{1}{12}(516 + 1085n_f^2 + 18n_f^3 + 397n_f^4)$
	Complex	-	-	$12 + 11n_f^2$	$n_f + n_f^2$	$58 + \frac{1745}{12}n_f^2 + \frac{3}{2}n_f^3 + \frac{397}{12}n_f^4$	
χEFT Fermion	Majorana	w/o \mathbf{Z}_2	$2n_f$	2	$2 + 8n_f + 6n_f^2 + 13n_f^3$	$\frac{4}{3}(12 + 14n_f + 9n_f^2 + 25n_f^3)$	$18 + 68n_f + 56n_f^2 + 181n_f^3$
		w \mathbf{Z}_2	-	2	$2 + 5n_f^2$	$4(4 + 3n_f^2)$	$18 + 2n_f + 57n_f^2$
	Dirac	-	4	$7 + 10n_f^2$	$22 + 28n_f^2$	$43 + n_f + 113n_f^2$	
$VEFT$ Vector	Real	w/o \mathbf{Z}_2	$4 + 5n_f^2$	-	$37 + 71n_f^2$	$\frac{2}{3}(8n_f^2 + 7n_f^4)$	$\frac{1}{12}(4836 + 13529n_f^2 + 6n_f^3 + 4477n_f^4)$
		w/ \mathbf{Z}_2	2	-	$22 + 21n_f^2$	$n_f + n_f^2$	$\frac{1}{6}(1152 + 2503n_f^2 + 231n_f^4)$
	Complex	3	-	$51 + 42n_f^2$	n_f^2	$\frac{1}{3}(1617 + 2579n_f^2 + 3n_f^3 + 346n_f^4)$	

Summary of *SEFT*

For a Goldstone singlet (*aEFT*), we find

dim-5: 6 (44)



dim-6: 1 (1)

Consistent with Grojean, et
al. [2307.08563](https://arxiv.org/abs/2307.08563)

dim-7: 44 (356)

dim-8: 32 (520)

All operators involving majoron with explicit shift symmetry start at *dim-8*

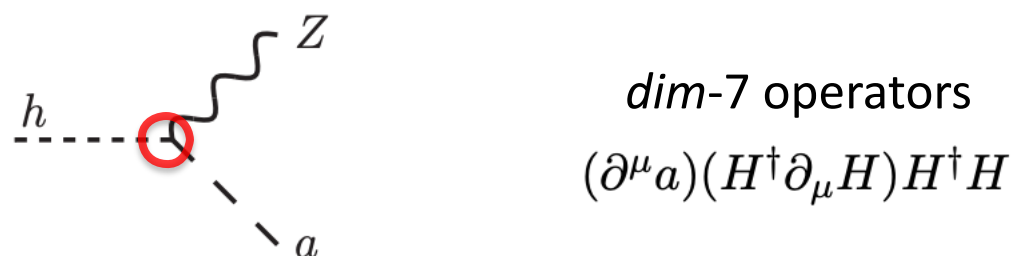
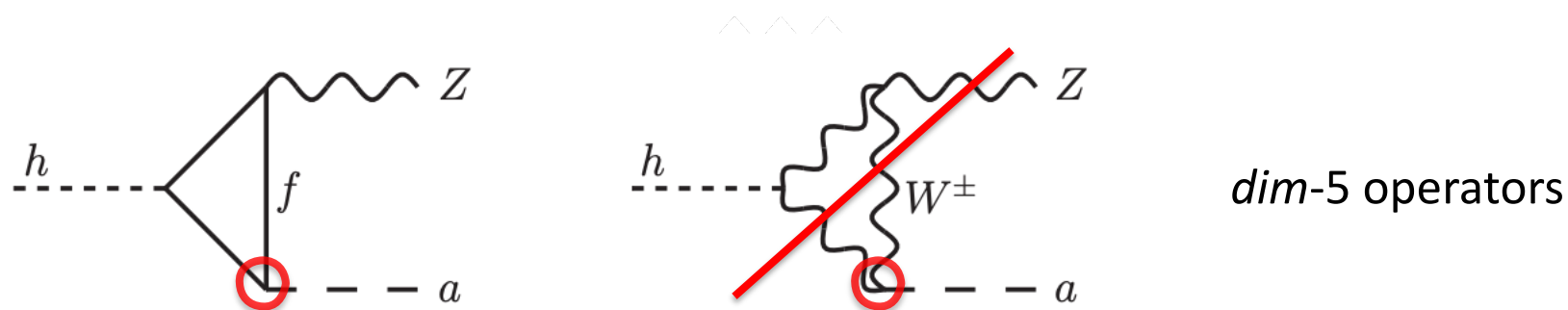
$$\epsilon^{ik}\epsilon^{jl}(D^\mu s)H_k(D_\mu H_l)(L_{pi}L_{rj}) \quad \epsilon^{ik}\epsilon^{jl}(D^\nu s)H_k(D^\mu H_l)(L_{pi}\sigma_{\mu\nu}L_{rj})$$

$$\epsilon^{ij}(D^\mu s)(d_{cp}^a L_{ri})(L_{sj}\sigma_\mu u_{cta}^\dagger) \quad \epsilon_{abc}(D^\mu s)(d_{cp}^a L_{si})(d_{cr}^b \sigma_\mu Q_t^{\dagger ci})$$

$$\epsilon_{abc}(D^\mu s)(d_{cp}^a d_{cr}^b)(d_{cs}^c \sigma_\mu e_{ct}^\dagger)$$

Phenomenology

Example 1: exotic decays of Higgs into ALPs

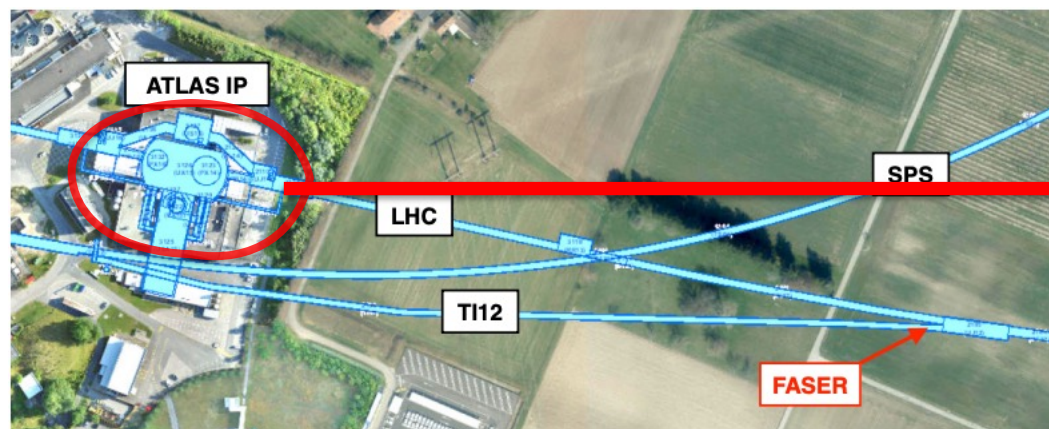


$$C_{Zh}^{\text{eff}} \approx \cancel{C_{Zh}^{(5)}} - 0.016 c_{tt} + 0.030 C_{Zh}^{(7)} \left[\frac{1 \text{ TeV}}{\Lambda} \right]^2$$

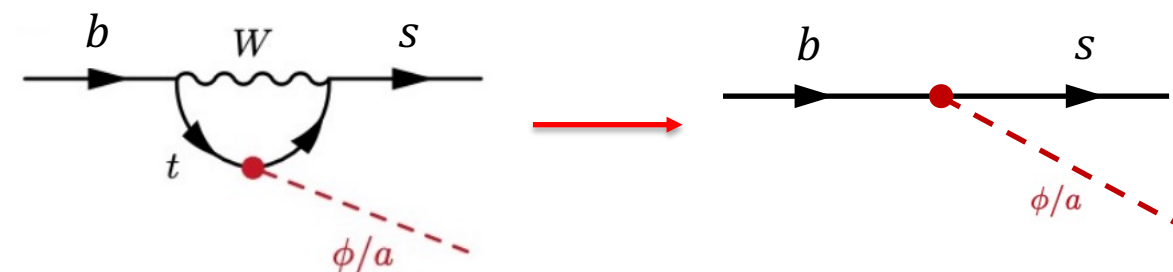
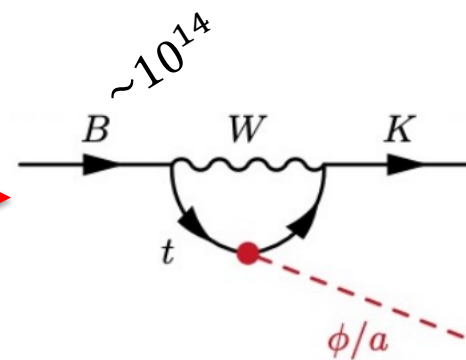
Bauer *et al.* 17'
 Bauer *et al.* 16'

Phenomenology

Example 2: Light scalars @ FASER



Compared to CEPC
($10^{11} \sim 10^{12}$)



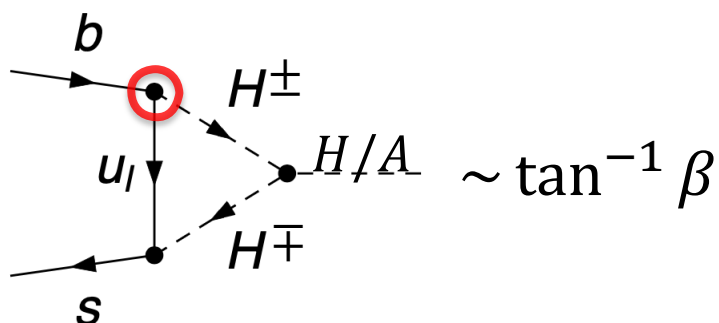
$$\mathcal{L}_{eff} = \frac{\phi}{v} \sum \xi_{\phi}^{ij} m_{f_j} \bar{f}_i P_R f_j + h.c.$$

$$s H^{\dagger i} (d_{cp}^a Q_{rai})$$

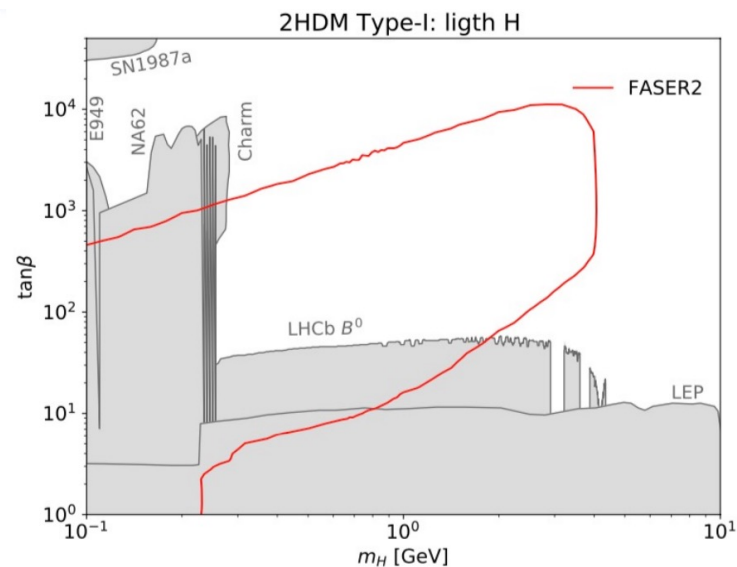
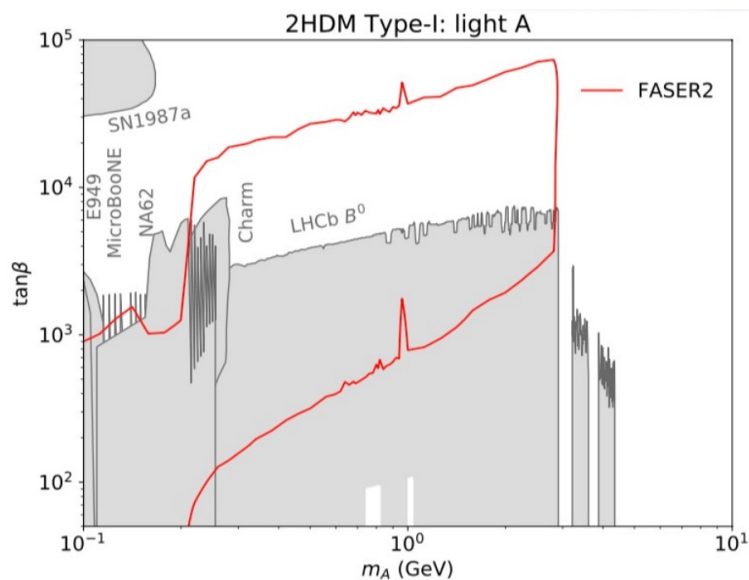
Phenomenology

Example 2: Light scalars @ FASER

Consider Type-I 2HDM as a UV model



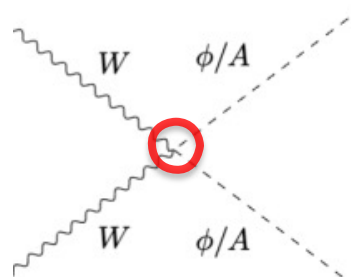
Similar to minimal model (Dark Higgs)



Phenomenology

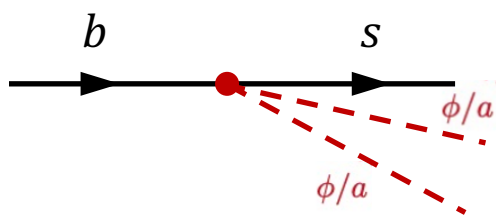
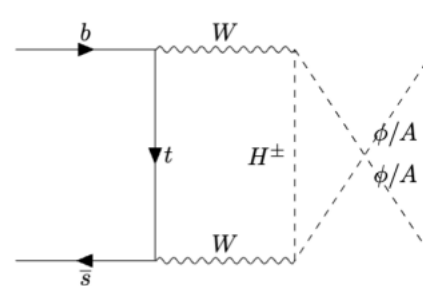
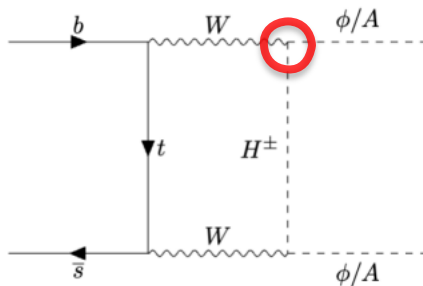
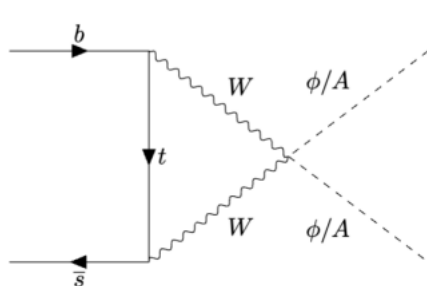
Example 2: Light scalars @ FASER

Consider Type-I 2HDM as a UV model



$$\sim g^2$$

Governed by gauge symmetry and not suppressed



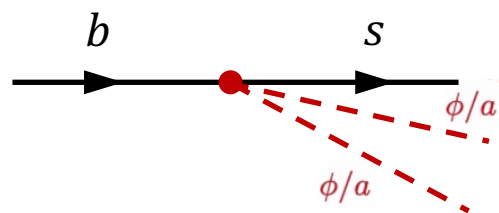
$$\mathcal{L} \supset \xi_{\phi\phi}^{ij} \frac{\phi^2}{v^2} m_j \bar{f}_i P_R f_j + \xi_{AA}^{ij} \frac{A^2}{v^2} m_j \bar{f}_i P_R f_j + h.c.$$

$$s^2 H^{\dagger i} (d_{cp}^a Q_{rai})$$

Phenomenology

Example 2: Light scalars @ FASER

Consider Type-I 2HDM as a UV $\hat{\Lambda}$ model



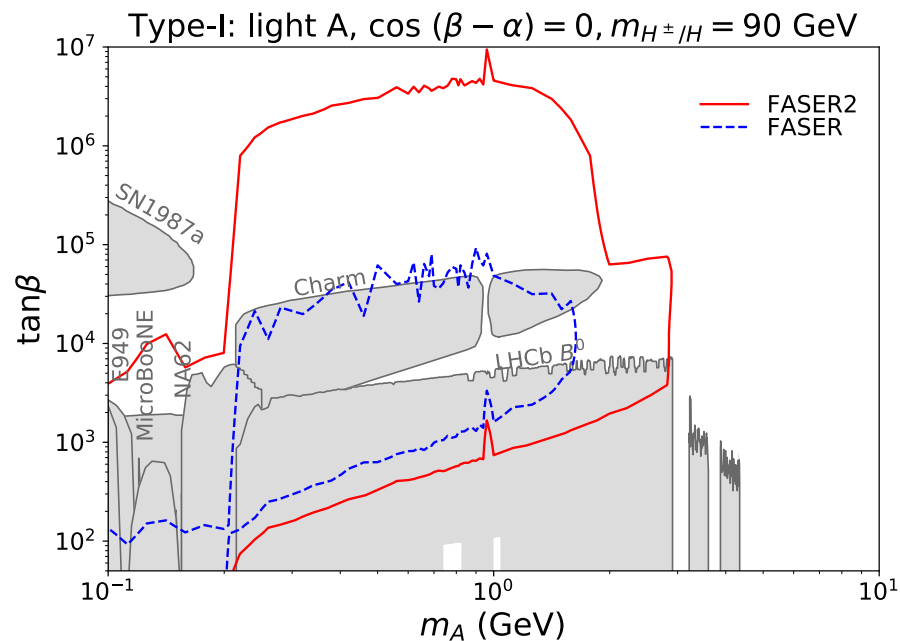
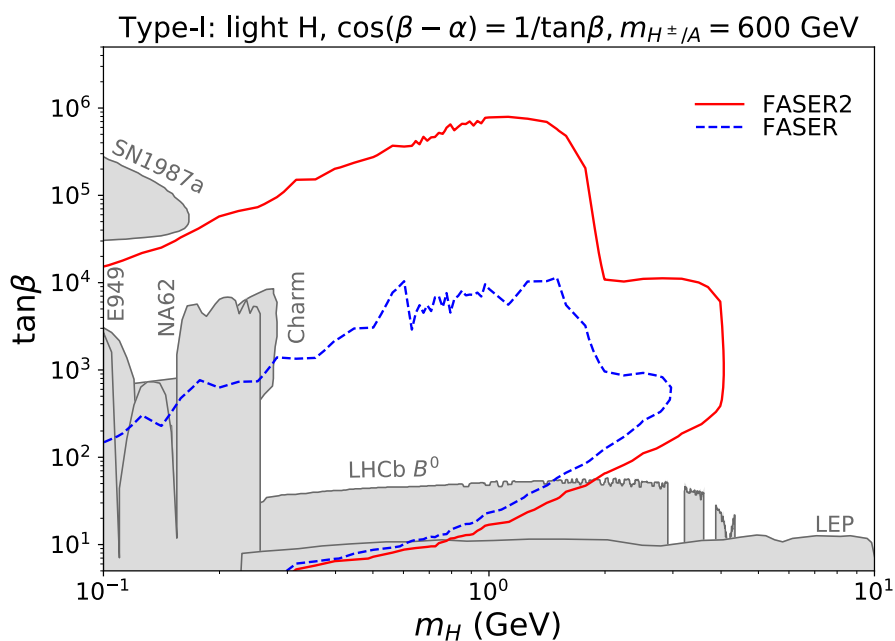
$$\mathcal{L} \supset \xi_{\phi\phi}^{ij} \frac{\phi^2}{v^2} m_j \bar{f}_i P_R f_j + \xi_{AA}^{ij} \frac{A^2}{v^2} m_j \bar{f}_i P_R f_j + h.c.$$

$$\xi_{\phi\phi}^{ij} \simeq \xi_{AA}^{ij} \simeq \frac{g^2}{64\pi^2} \sum_k V_{ki}^* [f_0(x_k, x_{H^\pm}) + f_1(x_k, x_{H^\pm}) \log x_k \\ + f_2(x_k, x_{H^\pm}) \log x_{H^\pm}] V_{kj} + \mathcal{O}(\cos(\beta - \alpha), 1/\tan \beta).$$

Phenomenology

Example 2: Light scalars @ FASER

Consider Type-I 2HDM as a UV model



LLPs from Flavor Physics @ CEPC

- New detectors: HErmetic CAvern TrackEr (HECATE)

Chrzęszcza *et al.* 20'

- Origins of the LLPs: two bottoms or charms, one of which can be tagged in the standard detector
- Identify the UV or the origin of the LLPs

prototype model: Dark Higgs $\mathcal{L}_{eff}^{Sqq} = \theta \frac{S}{v} \sum_{i,j} \xi_{ij} m_{Q_j} \bar{Q}_i P_R Q_j + h.c.$

most general case $\mathcal{L}_{eff} = \frac{\phi}{v} \sum \xi_{\phi}^{ij} m_{f_j} \bar{f}_i P_R f_j + h.c.$

@CEPC $10^{11} \sim 10^{12}$ D/B mesons

Summary and outlook

- Summary of results:
 1. EFTs for weakly-interacting light particles (ϕEFT , χEFT , $VEFT$) up to $dim-8$
 2. Light scalars at FASER, higher dim operators are phenomenological relevant in some model (Type-I 2HDM)
 3. CEPC provides more opportunities to study the productions of LLPs from flavor changing processes
- Matching & running between $sEFTs$ above EW scale and below EW scale
- Constraints on more general long-lived light scalars (pure EFT analysis and a2HDM, s2HDM & NMSSM)



Backup Slides

Goldstone Bosons

What makes Nambu-Goldstone bosons different from generic scalars?

- In terms of operators: non-linearly realized symmetry on G/H

$$\pi_i^a \rightarrow \pi_i^a + \epsilon_i^a + \dots$$

G -invariant operators (e.g. $\text{tr}(u_\mu u^\mu)$) built from $u_\mu \sim D_\mu \pi$

- In terms of amplitudes: Adler's zero condition

$$\mathcal{M}(p_\pi) \rightarrow p_\pi \quad \text{for} \quad p_\pi \rightarrow 0$$

$$\lim_{p_\pi \rightarrow 0} \sum_{i=1}^D c_i \mathcal{B}^i = \sum_{i=1}^D c_i \lim_{p_\pi \rightarrow 0} \mathcal{B}^i = 0$$

Basis for scalars
 $\{\mathcal{B}^i | i = 1, 2, \dots, D\}$

\mathcal{B}'^i Basis for Goldstones

Goldstone Bosons (ALPs)

Axions or axion-like particles are pseudoscalars corresponding to some $U(1)$ symmetries breaking and possessing shift symmetry.

$$\mathcal{L} \supset \frac{1}{2} \partial_\mu a \partial^\mu a + c_{\tilde{B}} \frac{a}{f_a} B_{\mu\nu} \tilde{B}^{\mu\nu} + c_{\tilde{W}} \frac{a}{f_a} W_{\mu\nu}^a \tilde{W}^{a\mu\nu} + c_{\tilde{G}} \frac{a}{f_a} G_{\mu\nu}^\lambda \tilde{G}^{\lambda\mu\nu}$$

$$+ c_u \frac{\partial_\mu a}{f_a} (\bar{u}_R \gamma^\mu u_R) + c_d \frac{\partial_\mu a}{f_a} (\bar{d}_R \gamma^\mu d_R) + c_e \frac{\partial_\mu a}{f_a} (\bar{e}_R \gamma^\mu e_R)$$

$$+ c_Q \frac{\partial_\mu a}{f_a} (\bar{Q}_L \gamma^\mu Q_L)_{i,j \neq 1,1} + c_L \frac{\partial_\mu a}{f_a} (\bar{L}_L \gamma^\mu L_L)_{i \neq j}$$
54

Georgi et al. 86'

Chala et al. 20', Bauer et al. 20'

$$- \frac{a}{f_a} \left(c_{QH_u} \bar{Q}_L \tilde{H} u_R + c_{QH_d} \bar{Q}_L H d_R + c_{LH_e} \bar{L}_L H e_R + \text{h.c.} \right)$$
41

dim-6 $(D_\mu s)(D^\mu s) H_i H^{\dagger i}$

dim-8 $\epsilon^{ik} \epsilon^{jl} (D^\mu s) H_k (D_\mu H_l) (L_{p_i} L_{r_j}) \quad L = 2 \quad s \text{ is a majoron}$

Majorana & Dirac Fermions

For scalars, one can combine two real scalars into a complex one. An extra $U(1)$ symmetry should be imposed for the complex scalars in the operators.

One can perform similar thing in fermion case.

$$\mathcal{L} \supset -m\chi_1\chi_1 - m\chi_2\chi_2 + h.c. \quad \begin{pmatrix} \chi_1 \\ \chi_2 \end{pmatrix} \xrightarrow{SO(2)} \begin{pmatrix} \cos \phi & -\sin \phi \\ \sin \phi & \cos \phi \end{pmatrix} \begin{pmatrix} \chi_1 \\ \chi_2 \end{pmatrix}$$

$$\chi_L = \chi_1 + i\chi_2 \quad \chi_R = \chi_1 - i\chi_2 \longrightarrow \mathcal{L} \supset -m\bar{\chi}_L\chi_R + h.c.$$

$$U(1): \quad \chi_L \rightarrow e^{i\phi}\chi_L \quad \text{and} \quad \chi_R \rightarrow e^{-i\phi}\chi_R$$

Hence we construct EFT for $n_\chi = 2$ Majorana fermions and assign opposite $U(1)$ charges for them to obtain EFT for a Dirac fermion. (Double DoFs)

Massive vectors (Dark Photon)

How to describe a massive vector boson?

- Proca Lagrangian: $\mathcal{L} \supset -\frac{1}{4}X_{\mu\nu}X^{\mu\nu} + \frac{1}{2}m_X^2 X_\mu X^\mu - \epsilon B_{\mu\nu}X^{\mu\nu}$
breaks gauge symmetry, two building block $X_{\mu\nu}$ and X_μ (related by EoMs),
 $(X_\mu X^\mu)^2$? [M. Reece 1808.09966](#)

- Stueckelberg Lagrangian:

$$X_\mu \longrightarrow X_\mu + \partial_\mu \alpha(x)$$

$$\pi \longrightarrow \pi + m_X \alpha(x).$$

$$\mathcal{L}_{\text{Stueck}} = -\frac{1}{4}X_{\mu\nu}X^{\mu\nu} + \frac{1}{2}m_X^2 \left(X_\mu - \frac{1}{m_X}\partial_\mu \pi\right) \left(X^\mu - \frac{1}{m_X}\partial^\mu \pi\right)$$

$$-\frac{1}{2}(\partial^\mu X_\mu + m_X \pi)(\partial^\nu X_\nu + m_X \pi) \xrightarrow{\text{gauge-fixing}} -\frac{1}{2\xi}(\partial^\mu X_\mu + \xi m_X \pi)(\partial^\nu X_\nu + \xi m_X \pi)$$

$$U \equiv e^{i\frac{\pi}{m_X}}$$

$$\mathcal{L}'_{\text{Stueck}} = -\frac{1}{4}X_{\mu\nu}X^{\mu\nu} + \frac{m_X^2}{2}(D_\mu U)^\dagger D^\mu U - \frac{1}{2\xi}(\partial^\mu X_\mu - i\xi m_X^2 \ln U)^2$$

$$\begin{aligned} \xi &= \infty \\ U &= 1 \end{aligned}$$

$$m_X^2 X_\mu X^\mu / 2.$$

Massive vectors (Dark Photon)

Can EFT indeed includes $(X_\mu X^\mu)^2$?

Higgs mechanism

$$\mathcal{L}_{\text{Dark } \gamma + \text{Dark Higgs}} = -\frac{1}{4}X_{\mu\nu}X^{\mu\nu} + D_\mu S^\dagger D^\mu S + \mu^2 S^\dagger S - \lambda (S^\dagger S)^2$$

$$S = \frac{1}{\sqrt{2}}(v_S + \sigma) e^{-i\frac{\pi}{v_S}}$$

$$\begin{aligned} \mathcal{L}_{\text{Dark } \gamma + \text{Dark Higgs}} = & -\frac{1}{4}X_{\mu\nu}X^{\mu\nu} + \frac{1}{2}g^2v_S^2 \left(X_\mu - \frac{1}{gv_S}\partial_\mu\pi \right) \left(X^\mu - \frac{1}{gv_S}\partial^\mu\pi \right) \\ & + \frac{1}{2}\partial_\mu\sigma\partial^\mu\sigma - \frac{1}{2}2\lambda v_S^2\sigma^2 - \lambda v\sigma^3 - \frac{1}{4}\lambda\sigma^4 \\ & + \left(\frac{\sigma}{v} + \frac{\sigma^2}{2v^2} \right) (gvX_\mu - \partial_\mu\pi) (gvX^\mu - \partial^\mu\pi) \end{aligned}$$

Integrate out σ

$$\begin{aligned} \mathcal{L}_{\text{Dark } \gamma + \text{Dark Higgs} - \sigma}^{\text{EFT}} = & -\frac{1}{4}X_{\mu\nu}X^{\mu\nu} + \frac{1}{2}g^2v_S^2 \left(X_\mu - \frac{1}{gv_S}\partial_\mu\pi \right) \left(X^\mu - \frac{1}{gv_S}\partial^\mu\pi \right) \\ & + \frac{g^4v_S^2}{2m_\sigma^2} \left[\left(X_\mu - \frac{1}{gv_S}\partial_\mu\pi \right) \left(X^\mu - \frac{1}{gv_S}\partial^\mu\pi \right) \right]^2 + \dots \end{aligned}$$

MASSIVE VECTORS

How to build EFTs for massive vectors

- Building blocks: u_μ and $X_{\mu\nu}$
- Power counting: u_μ has dimension 1 (chiral dimension)

HEFT

<i>dim-4 operators</i>				
Class	Type	Stueckelberg	Unitary	F
F_L^2	$X_L B_L$	$B_{L\mu\nu} X_L^{\mu\nu}$	✓	
$u\psi\bar{\psi}$	$ue_c e_c^\dagger$	$(e_{cp} \sigma^\mu e_{cr}^\dagger) u_\mu$	$(e_{cp} \sigma^\mu e_{cr}^\dagger) X_\mu$	
	uLL^\dagger	$(L_{pi} \sigma^\mu L_r^\dagger)^i u_\mu$	$(L_{pi} \sigma^\mu L_r^\dagger)^i X_\mu$	
	uQQ^\dagger	$(Q_{pai} \sigma^\mu Q_r^\dagger)^{ai} u_\mu$	$(Q_{pai} \sigma^\mu Q_r^\dagger)^{ai} X_\mu$	
	$ud_c d_c^\dagger$	$(d_{cp}^a \sigma^\mu d_{cra}^\dagger) u_\mu$	$(d_{cp}^a \sigma^\mu d_{cra}^\dagger) X_\mu$	
	$uu_c u_c^\dagger$	$(u_{cp}^a \sigma^\mu u_{cra}^\dagger) u_\mu$	$(u_{cp}^a \sigma^\mu u_{cra}^\dagger) X_\mu$	
$u^2 \phi^2$	$u^2 H H^\dagger$	$H_i H^\dagger{}^i u_\mu u^\mu$	$H_i H^\dagger{}^i X_\mu X^\mu$	
u^4	u^4	$u_\mu u^\mu u_\nu u^\nu$	$X_\mu X^\mu X_\nu X^\nu$	

<i>dim-4 operators</i>							
Class	Type	Real	→	Complex	F	Z ₂	
F_L^2	$X_L B_L$	$B_{L\mu\nu} X_L^{\mu\nu}$	Double DoFs				
	$ue_c e_c^\dagger$	$(e_{cp} \sigma^\mu e_{cr}^\dagger) X_\mu$					
	uLL^\dagger	$(L_{pi} \sigma^\mu L_r^\dagger)^i X_\mu$					
	$u\psi\bar{\psi}$	uQQ^\dagger	$(Q_{pai} \sigma^\mu Q_r^\dagger)^{ai} X_\mu$				
		$ud_c d_c^\dagger$	$(d_{cp}^a \sigma^\mu d_{cra}^\dagger) X_\mu$				
$u^2 \phi^2$	$uu^\dagger H H^\dagger$			$H_i H^\dagger{}^i X_\mu X^\mu$		✓	
				$X_\mu^\dagger X^\mu X_\nu^\dagger X^\nu$		✓	
u^4	$u^2 u^\dagger{}^2$			$X_\mu^\dagger X^\dagger{}^\mu X_\nu X^\nu$		✓	
				$X_\mu^\dagger X^\dagger{}^\mu X_\nu^\dagger X^\nu$		✓	

Production channels of Light Scalars

- Semi-leptonic Pion and Kaon Decay $\pi/K \rightarrow \ell\nu\phi$

Kaon Decays

- Meson Decays
 - D-meson Decays $K/D/B \rightarrow X\phi$
 - B-meson decays

- Eta Decays

$$\eta \rightarrow \pi\phi, \eta' \rightarrow \eta\phi$$

- Bottomonium Decays

$$\Upsilon \rightarrow \gamma\phi$$

- Scalar Bremsstrahlung

- Weak Decays

$$h \rightarrow \phi\phi, Z \rightarrow H A, W \rightarrow H H^\pm$$

Explore Beyond the (Type-1) 2HDM

- We build a code that is able to handle
 - ❖ Both CP-even and CP-odd light scalar decays and **productions**
 - ❖ All kinds of scalar couplings: four types of 2HDMs, dark (pseudo)scalar, general scalar models with extra particles
 - ❖ Full low mass regime with the state of the art for calculations

CP-even

$$\begin{aligned} \mathcal{L}_\phi = & -\frac{1}{2}m_\phi^2\phi^2 - \sum_f \xi_\phi^f \frac{m_f}{v} \phi \bar{f}f - \xi_\phi^W \frac{2m_W^2}{v} \phi W^{\mu+} W_\mu^- \\ & - \xi_\phi^Z \frac{m_Z^2}{v} \phi Z^\mu Z_\mu + \xi_\phi^g \frac{\alpha_s}{12\pi} \frac{\phi}{v} G_{\mu\nu}^a G^{a\mu\nu} + \xi_\phi^\gamma \frac{\alpha}{4\pi} \frac{\phi}{v} F_{\mu\nu} F^{\mu\nu} \\ & + \sum_S \lambda_{\phi SS} \phi S^+ S^-. \end{aligned}$$

CP-odd

$$\begin{aligned} \mathcal{L}_A = & -\frac{1}{2}m_A^2 A^2 + \sum_{f=u,d,e} \frac{im_f}{v} \xi_A^f \bar{f} \gamma_5 f A \\ & + \xi_A^g \frac{\alpha_s}{4\pi} \frac{A}{v} G_{\mu\nu,a} \tilde{G}^{\mu\nu,a} + \xi_A^\gamma \frac{\alpha}{4\pi} \frac{A}{v} F_{\mu\nu} \tilde{F}^{\mu\nu}. \end{aligned}$$

- We will make the code public for further studies on long-lived light scalars at other experiments. https://github.com/shiggs90/Light_scalar_decay.git.