

# EIC Physics

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# Outline:

- 3D imaging of proton
- Origin of proton mass and spin
- Small x physics

Partially overlapped with **Weiyao and Jinlong's talk**

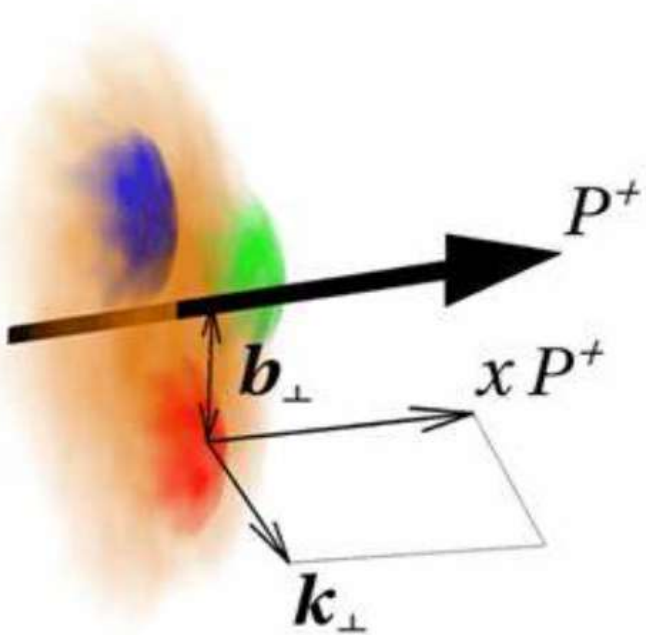
Disclaimer : Many interesting topics not covered: proton radius puzzle, Quasi PDFs...

A 3D visualization of a proton's internal structure. The proton is depicted as a large, glowing sphere with a complex internal structure. It is composed of several smaller, colored spheres (red, blue, green, orange, purple) representing quarks, connected by a network of yellow, coiled lines representing gluons. The entire structure is set against a dark blue background with a glowing, circular border. The text "3D imaging of proton" is overlaid at the bottom left.

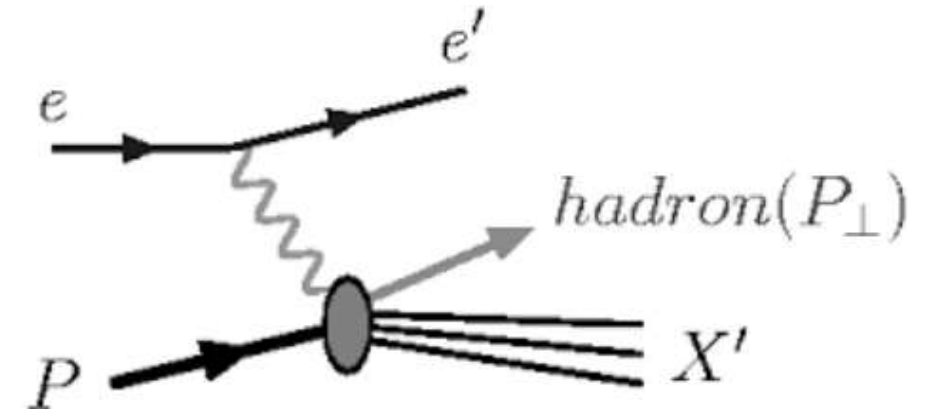
3D imaging of proton

# 3D imaging in momentum space: TMDs

- The “simplest” TMD is the unpolarized function  $f_1(x; k_\perp)$ , 8 leading power TMDs



SIDIS:



$$\int \frac{dy^- d^2y_\perp}{(2\pi)^3} e^{-ixP^+ \cdot y^- + i\vec{k}_\perp \cdot \vec{y}_\perp} \langle PS | \bar{\psi}_\beta(y^-, y_\perp) \mathcal{L}_v^\dagger(y^-, y_\perp) \mathcal{L}_v(0) \psi_\alpha(0) | PS \rangle$$

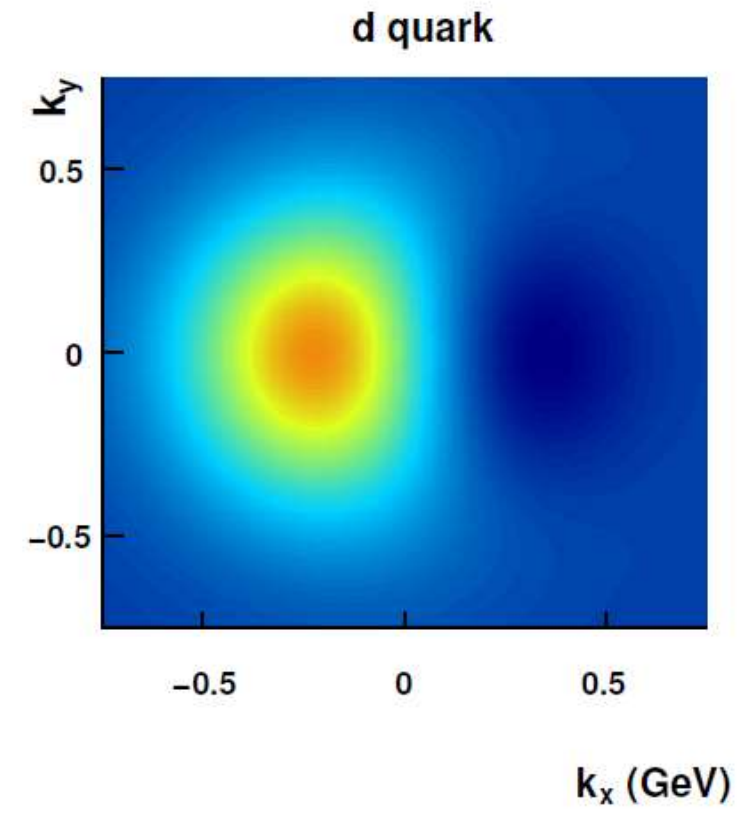
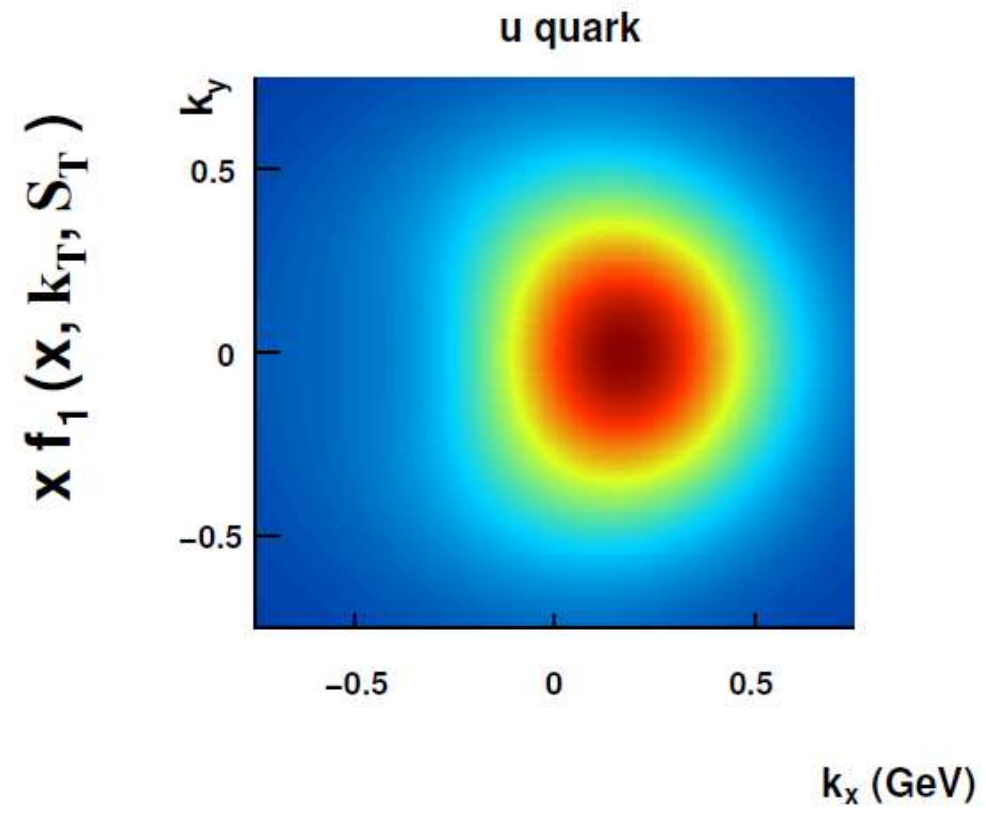
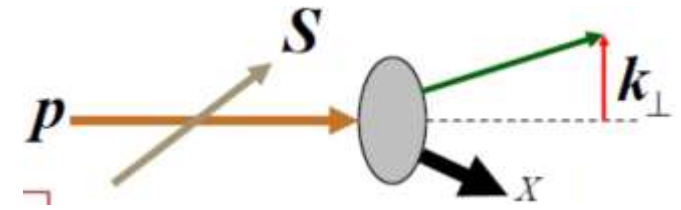
- ◆ TMD factorization: Collins-Soper 1981, Collins-Soper-Sterman 1985 ,  $kt \ll Q$

# Why TMDs?

- Phenomenological needs
- Confined motion of partons inside proton
- Access to orbital angular momentum
- Universality issue, QCD factorization

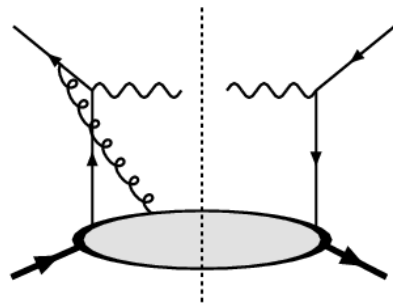
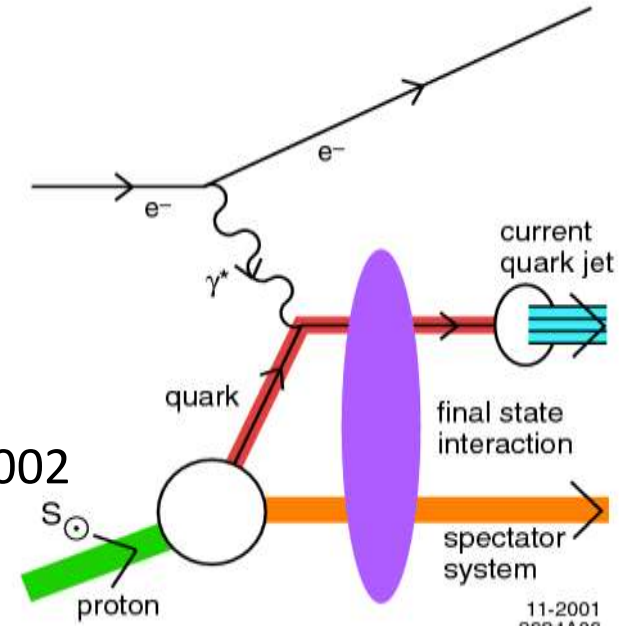
# The Sivers function

➤ The most interesting TMD: **Sivers function**:



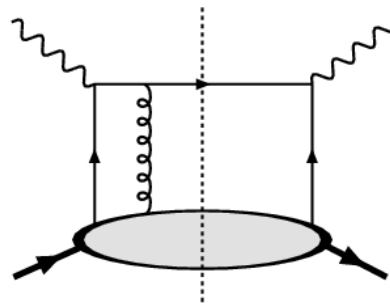
# The legend of the Sivers function

- The introduction of the Sivers function  
Sivers 1990
- Proof it is zero using time&parity invariance of QCD,  
Collins 1993
- Non-vanishing Sivers function in a model calculation,  
Brodsky-Hwang-Schmidt 2002
- Including gauge link contribution, prove :  
Collins 2002



**Drell-Yan**

ISI



FSI

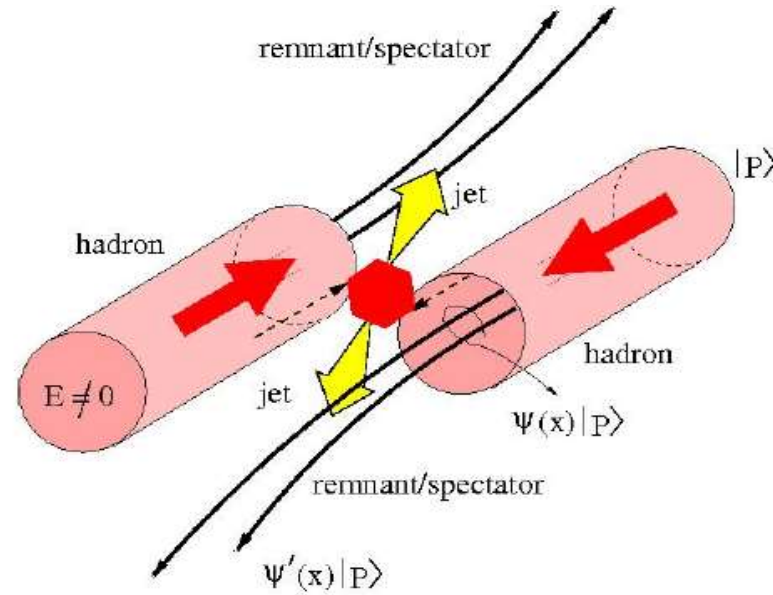
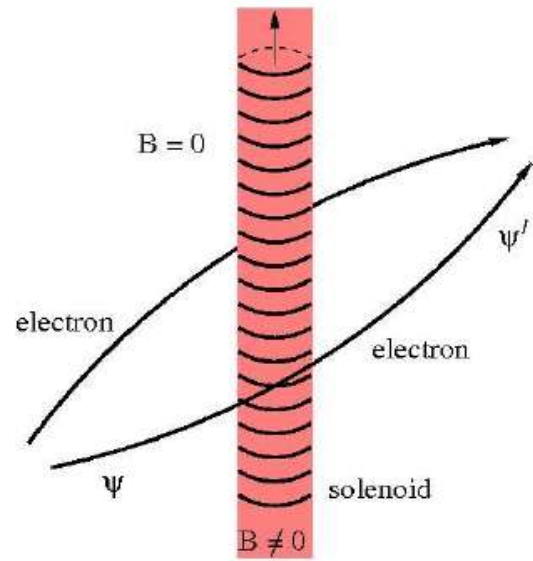
**DIS**



$$\text{Sivers}|_{\text{DY}} = -\text{Sivers}|_{\text{DIS}}$$



◆ QCD AB effect?



Gauge link (Wilson line), pure gauge gluon

$$\psi' = e^{ie \int ds \cdot A} \psi$$

$$\psi_i(x) |P\rangle = e^{-ig \int_x^{x'} ds_\mu A^\mu} \psi_i(x') |P\rangle$$

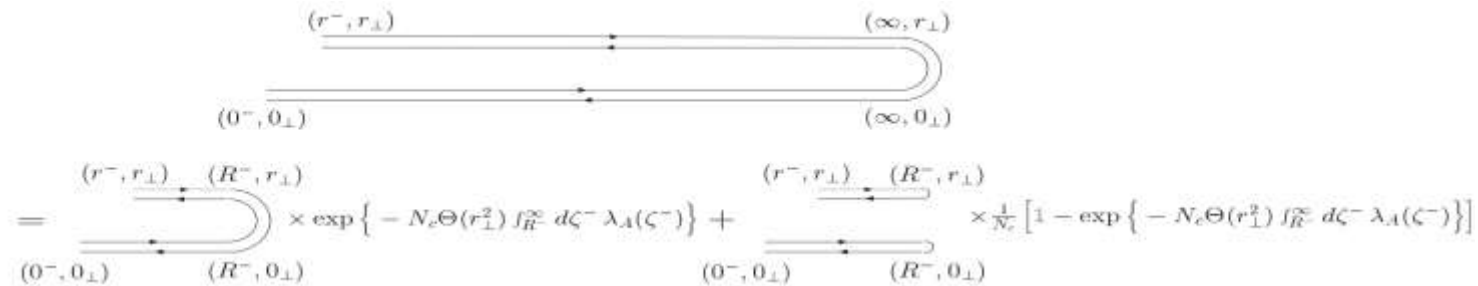
◆ S and P wave interference

Boris, Liang 1993  
Belitsky, Ji, Yuan, 2004

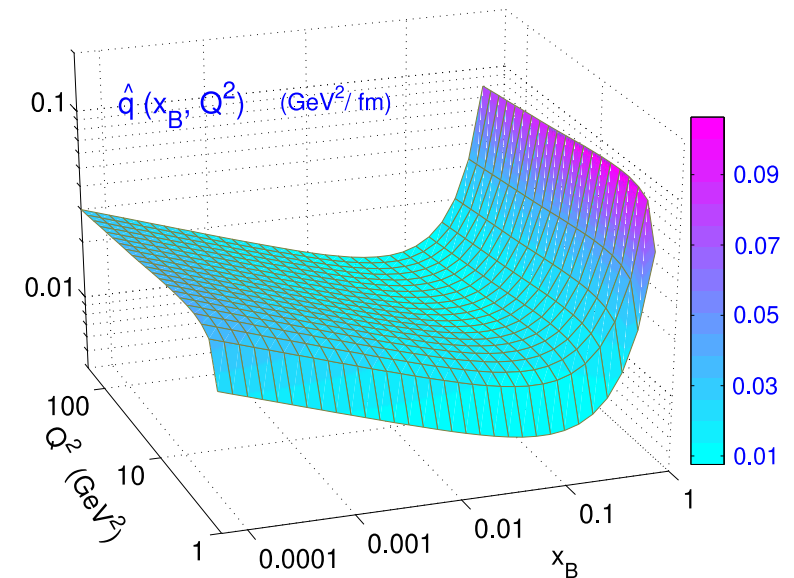
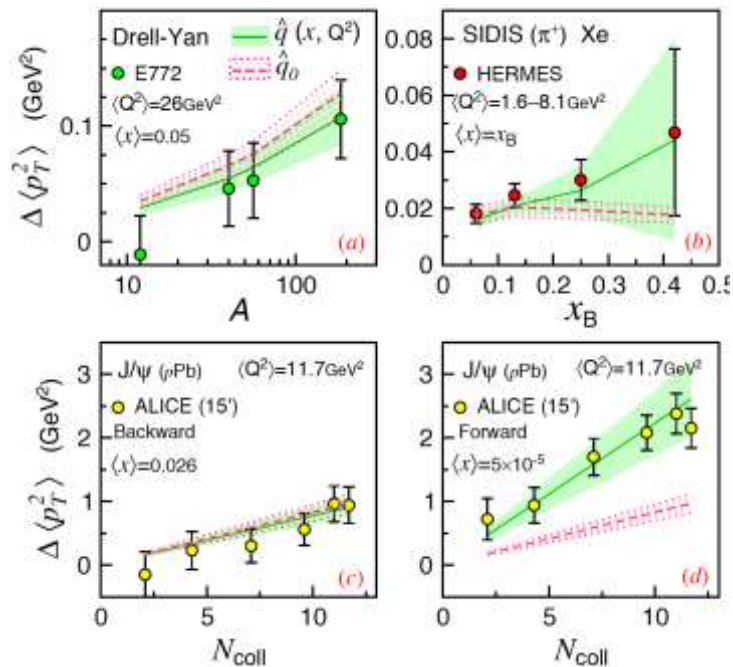


# TMDs of nucleus: Cold nuclear matter effect

- Gauge link contribution to nuclear TMDs, [Z.t. Liang, X.n. Wang, ZJ,2009](#); [A. Schafer, ZJ, 2013](#)



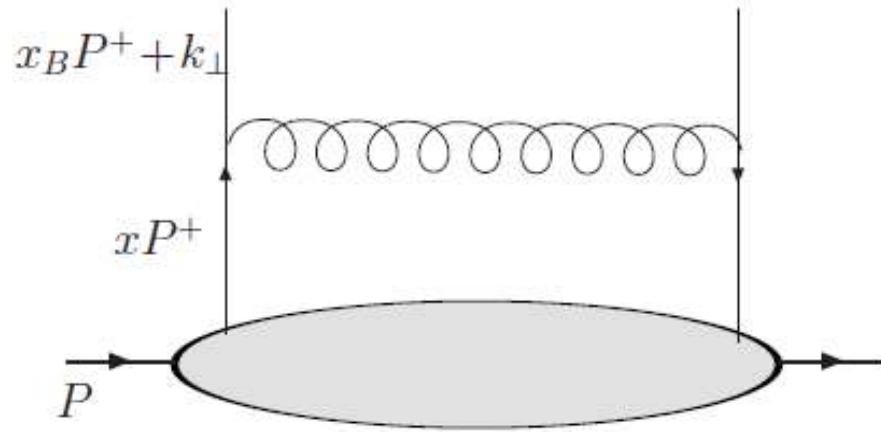
- Global fits based on the collinear twist-4 framework [Ru, Kang, Wang, Xing, Zhang, PRD\(L\), 2021](#)



# TMD: a PQCD playground

# TMD dynamics at large $kt$

- ◆ TMD distributions can be calculated within perturbative QCD at large  $kt$ ,



radiated gluon generate  
large transverse momentum,

$$f_1(x_B, k_\perp) = \frac{\alpha_s}{2\pi^2} \frac{1}{\vec{k}_\perp^2} C_F \int \frac{dx}{x} f_1(x) \left[ \frac{1 + \xi^2}{(1 - \xi)_+} + \delta(1 - \xi) \left( \ln \frac{x_B^2 \zeta^2}{\vec{k}_\perp^2} - 1 \right) \right]$$

TMD evolution: resum to all orders  
using the Collins-Soper equation

# kt-odd TMD distributions at large Kt at twsit-3

- Sivers and Boer-Mulders

$$f_{1T}^\perp|_{DY}(x_B, k_\perp) = \frac{\alpha_s}{\pi} \frac{M^2}{(\vec{k}_\perp^2)^2} \int \frac{dx}{x} \left[ A_{f_{1T}^\perp} + C_F T_F(x, x) \delta(1 - \xi) \left( \ln \frac{x_B^2 \zeta^2}{\vec{k}_\perp^2} - 1 \right) \right]$$

Ji, Qiu, Vogelsang, Yuan

$$h_{1T}^\perp|_{DY}(x_B, k_\perp) = \frac{\alpha_s}{\pi} \frac{M^2}{(\vec{k}_\perp^2)^2} \int \frac{dx}{x} \left[ A_{h_{1T}^\perp} + C_F T_F^{(\sigma)}(x, x) \delta(1 - \xi) \left( \ln \frac{x_B^2 \zeta^2}{\vec{k}_\perp^2} - 1 \right) \right]$$

ZJ, Yuan, Liang, 2009

- $g_{1T}$  and  $h_{1L}$

$$g_{1T}(x_B, k_\perp) = \frac{\alpha_s}{\pi^2} \frac{M^2}{(k_\perp^2)^2} \int \frac{dx}{x} \left\{ A_{g_{1T}} + C_F \tilde{g}(x) \delta(\xi - 1) \left( \ln \frac{x_B^2 \zeta^2}{k_\perp^2} - 1 \right) \right\}$$

$$h_{1L}(x_B, k_\perp) = \frac{\alpha_s}{\pi^2} \frac{M^2}{(k_\perp^2)^2} \int \frac{dx}{x} \left\{ A_{h_{1L}} + C_F \tilde{h}(x) \delta(\xi - 1) \left( \ln \frac{x_B^2 \zeta^2}{k_\perp^2} - 1 \right) \right\}$$

ZJ, Yuan, Liang, 2009

$$A_{f_{1T}^\perp} = -\frac{1}{2N_c} T_F(x, x) \frac{1 + \xi^2}{(1 - \xi)_+} + \frac{C_A}{2} T_F(x, x_B) \frac{1 + \xi}{(1 - \xi)_+} + \frac{C_A}{2} \tilde{T}_F(x_B, x)$$

$$A_{h_{1T}^\perp} = -\frac{1}{2N_c} T_F^{(\sigma)}(x, x) \frac{2\xi}{(1 - \xi)_+} + \frac{C_A}{2} T_F^{(\sigma)}(x, x_B) \frac{2}{(1 - \xi)_+}$$

$$A_{g_{1T}} = \int dx_1 \left\{ \frac{1}{2N_c} \tilde{g}(x) \frac{1 + \xi^2}{(1 - \xi)_+} \delta(x_1 - x) \right. \\ \left. + \left[ C_F \left( \frac{x_B^2}{x^2} + \frac{x_B}{x_1} - \frac{2x_B^2}{x_1 x} - \frac{x_B}{x} - 1 \right) + \frac{C_A (x_B^2 + x x_1) (2x_B - x - x_1)}{2 (x_B - x_1) (x - x_1) x_1} \right] \tilde{G}_D(x, x_1) \right. \\ \left. + \left[ C_F \left( \frac{x_B^2}{x^2} + \frac{x_B}{x_1} - \frac{x_B}{x} - 1 \right) + \frac{C_A (x_B^2 - x x_1)}{2 (x_1 - x_B) x_1} \right] G_D(x, x_1) \right\}$$

$$A_{h_{1L}} = \int dx_1 \left\{ \frac{1}{2N_c} \tilde{h}(x) \frac{2\xi}{(1 - \xi)_+} \delta(x_1 - x) \right. \\ \left. + \left[ C_F \frac{2(x - x_1 - x_B)}{x_1} + \frac{C_A 2x_B (x_B x + x_B x_1 - x^2 - x_1^2)}{2 (x_B - x_1) (x - x_1) x_1} \right] H_D(x, x_1) \right\}$$

# TMD evolution

Two scales problem(formulated in bt space):

$$\frac{d \ln \tilde{f}(x, b; \zeta, \mu)}{d \ln \sqrt{\zeta}} = \tilde{K}(b; \mu),$$

Collins Soper(CS)  
equation

$$\frac{d \ln \tilde{f}(x, b; \zeta, \mu)}{d \ln \mu} = \gamma_F(g(\mu); \zeta/\mu^2)$$

Renormalization group  
equation

J. Collins, D. Soper , 1982; J. Collins, D. Soper, G. Sterman 1985

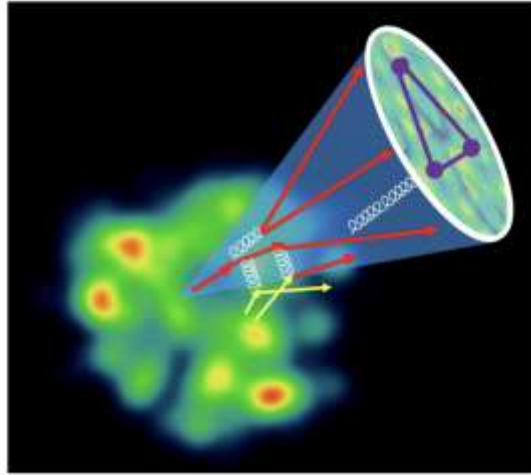
Recent developments:

- Joint small x & TMD resummation, ZJ 2016, Xiao, Yuan, ZJ 2017, ZJ 2019

$$xG^{(1)}(x, k_{\perp}, \zeta) = -\frac{2}{\alpha_S} \int \frac{d^2 x_{\perp} d^2 y_{\perp}}{(2\pi)^4} e^{ik_{\perp} \cdot r_{\perp}} \mathcal{H}^{WW}(\alpha_s(Q)) e^{-S_{sud}(Q^2, r_{\perp}^2)} \mathcal{F}_{Y=\ln 1/x}^{WW}(x_{\perp}, y_{\perp})$$

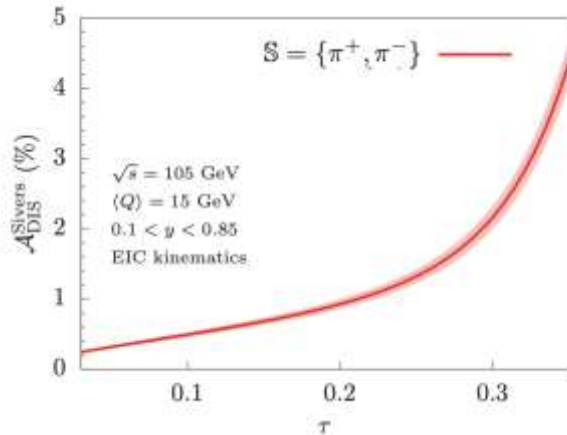
- Joint threshold & TMD resummation Kang, Lee, Shao, Zhao 2023

# Energy-Energy correlation



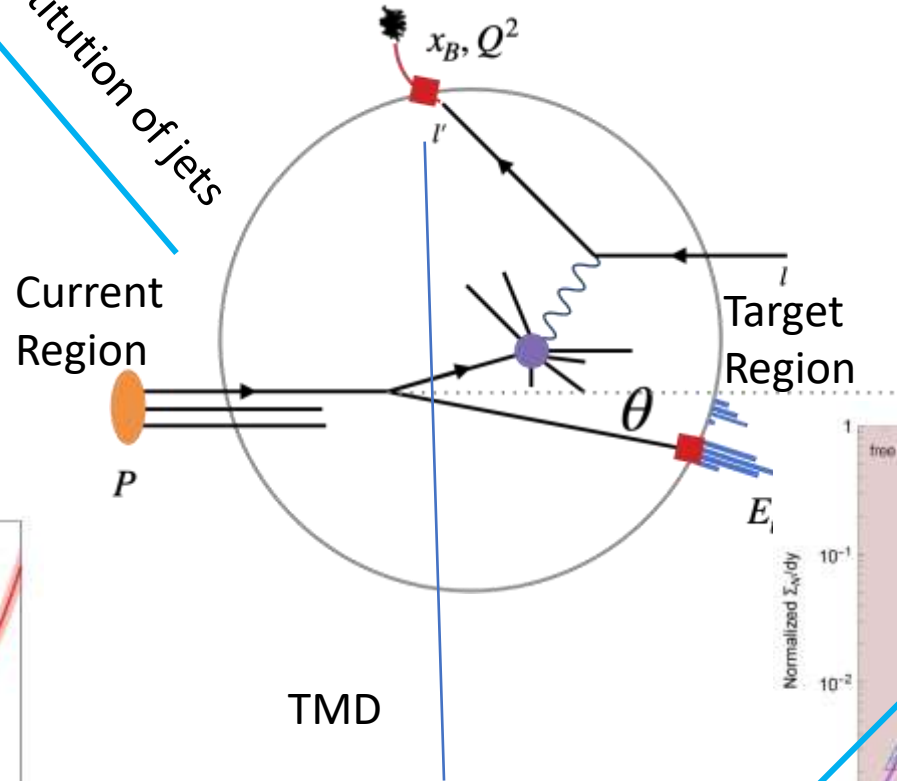
medium modification of **EEC**  
Enhanced at large angles  
Suppressed at small angles

Yang, He, Moutl, Wang, PRL 2023

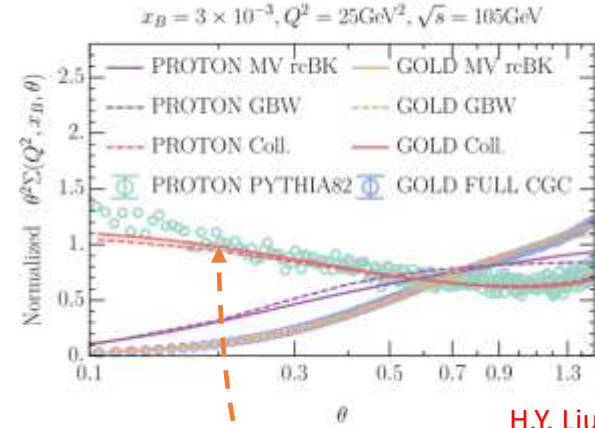


More EEC, Yayun's & Zhong's talk

substitution of jets



TMD

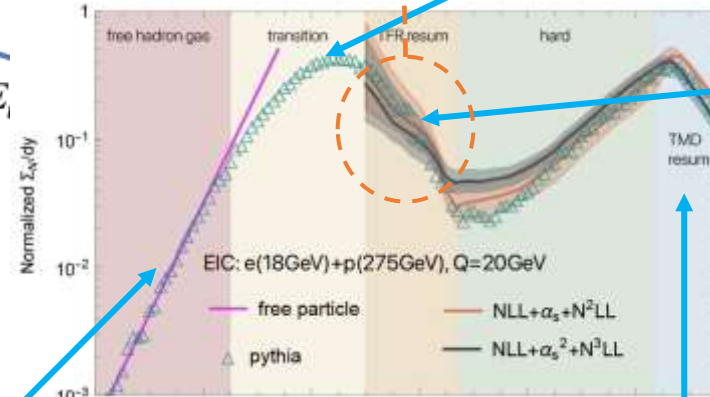


H.Y. Liu et al., PRL 2023

Probe the onset of gluon saturation

coll. predictions

Non-perturbative transition, probe **fEEC!**



Cao et al., to appear

Liu and Zhu., PRL 2023

TMD physics

Perturbative resummation + FO to high precision

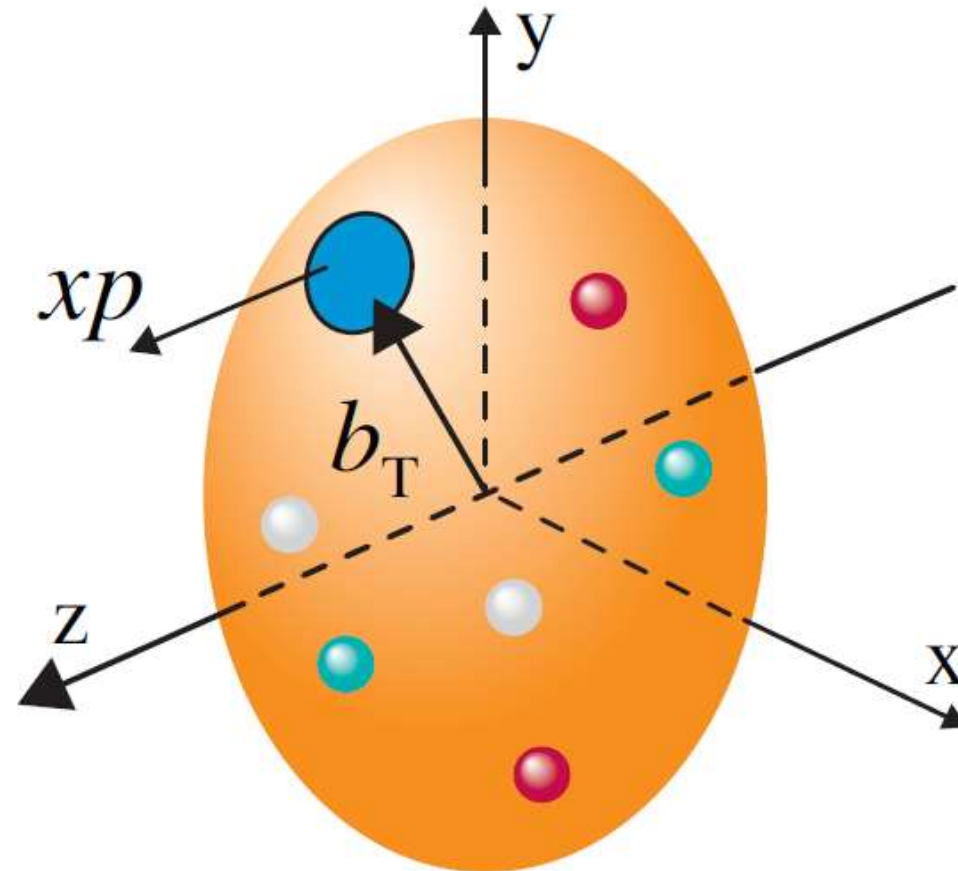
Free hadron gas, slope = 2

➤ Collins type EEC Kang, Lee, Shao, Zhao 2023

# Spatial imaging of Quarks and Gluons

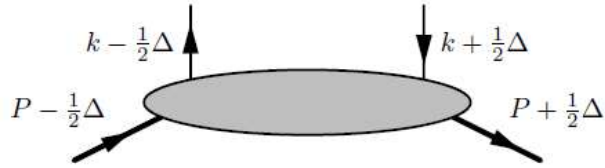
- Longitudinal momentum distribution + transverse spatial distribution:  $f(x, b_T)$

➤ Remark:  $f(x, b_T)$  and  $f(x, k_T)$  are not related to each other by a Fourier transform





# Generalized Parton Distributions(GPDs)



$$P = \frac{p + p'}{2} \quad \Delta = p' - p$$

$x, \zeta, t$

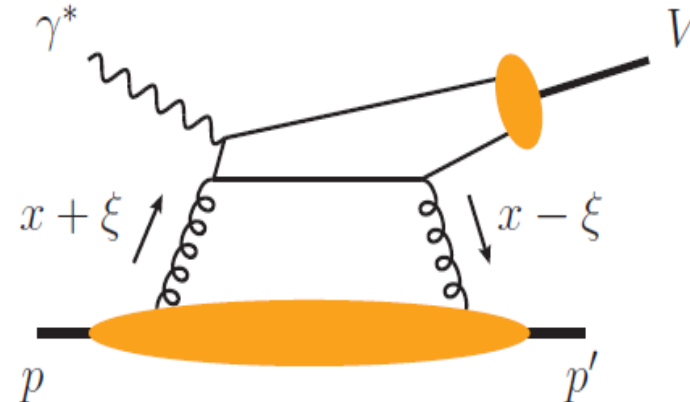
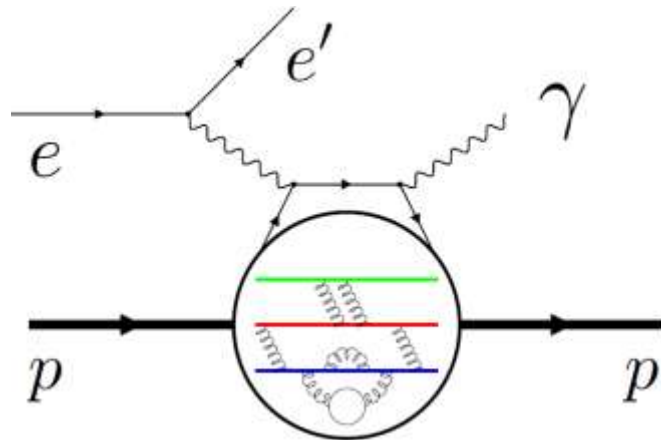
D. Muller, 94  
X. D. Ji, 97  
A. V. Radushkin, 97

$$\int \frac{d\lambda}{2\pi} e^{ix(Pz)} n_{-\alpha} n_{-\beta} \langle p' | G^{\alpha\mu} \left(-\frac{z}{2}\right) G_{\mu}^{\beta} \left(\frac{z}{2}\right) | p \rangle \Big|_{z=\lambda n_{-}} = \frac{1}{2} \left[ H^s \bar{u}(p') \not{n}_{-} u(p) + E^s \bar{u}(p') \frac{i\sigma^{\alpha\beta} n_{-\alpha} \Delta_{\beta}}{2m_N} u(p) \right]$$

➤ Transverse spatial distribution  $\mathcal{H}^q(x, \vec{b}_T^2) = \int \frac{d^2 \vec{\Delta}_T}{(2\pi)^2} e^{-i\vec{\Delta}_T \cdot \vec{b}_T} H^q(x, 0, -\vec{\Delta}_T^2)$

Soper 77 & Burkardt 2000

DVCS



# 5D imaging of proton

# Parton Wigner distributions

In quantum mechanics:

$$\widehat{W}^{[\Gamma]}(\vec{b}_\perp, \vec{k}_\perp, x) \equiv \frac{1}{2} \int \frac{dz^- d^2 z_\perp}{(2\pi)^3} e^{i(xp^+ z^- - \vec{k}_\perp \cdot \vec{z}_\perp)} \bar{\psi}(\vec{b}_\perp - \frac{z}{2}) \Gamma \mathcal{W} \psi(\vec{b}_\perp + \frac{z}{2}) \Big|_{z^+=0}$$

Operator definition:

$$\rho^{[\Gamma]}(\vec{b}_\perp, \vec{k}_\perp, x, \vec{S}) \equiv \int \frac{d^2 \Delta_\perp}{(2\pi)^2} \langle p^+, \frac{\vec{\Delta}_\perp}{2}, \vec{S} | \widehat{W}^{[\Gamma]}(\vec{b}_\perp, \vec{k}_\perp, x) | p^+, -\frac{\vec{\Delta}_\perp}{2}, \vec{S} \rangle.$$

A. Belitisky, X. D. Ji and F. Yuan, 2003

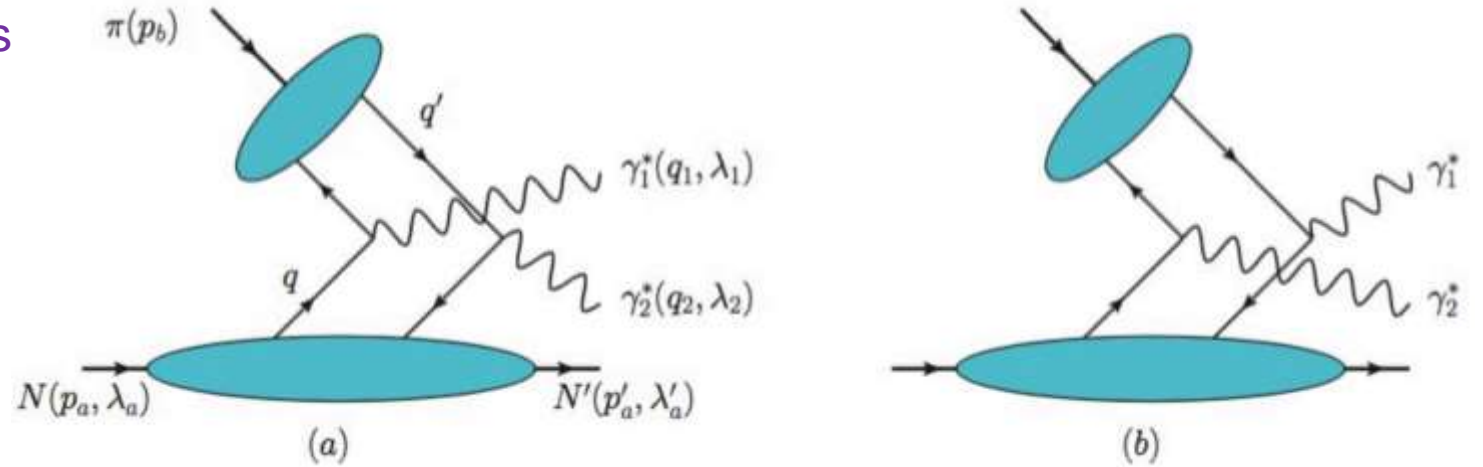
Motivations of studying parton Wigner distributions:

- tomography picture of nucleon
- encode information on parton OAM

Are they measurable?

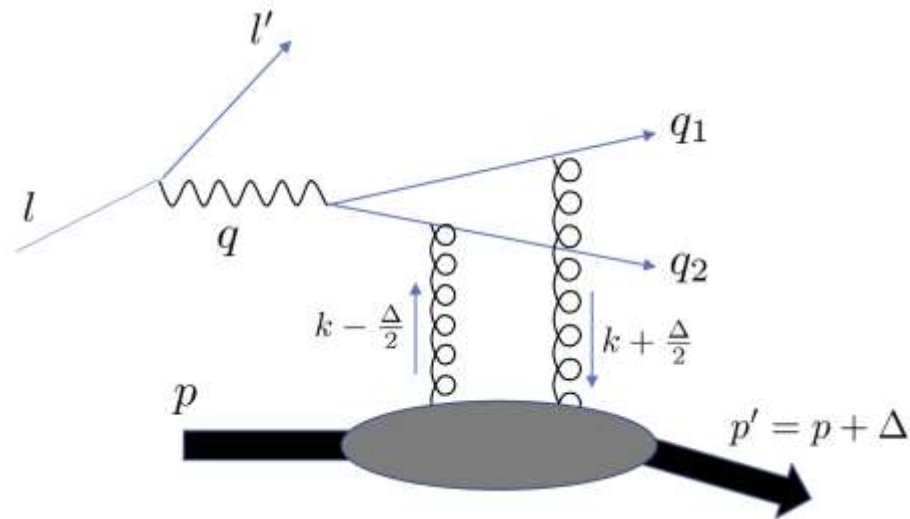
# Exclusive double Drell-Yan process

Quark case: exclusive double DY proces

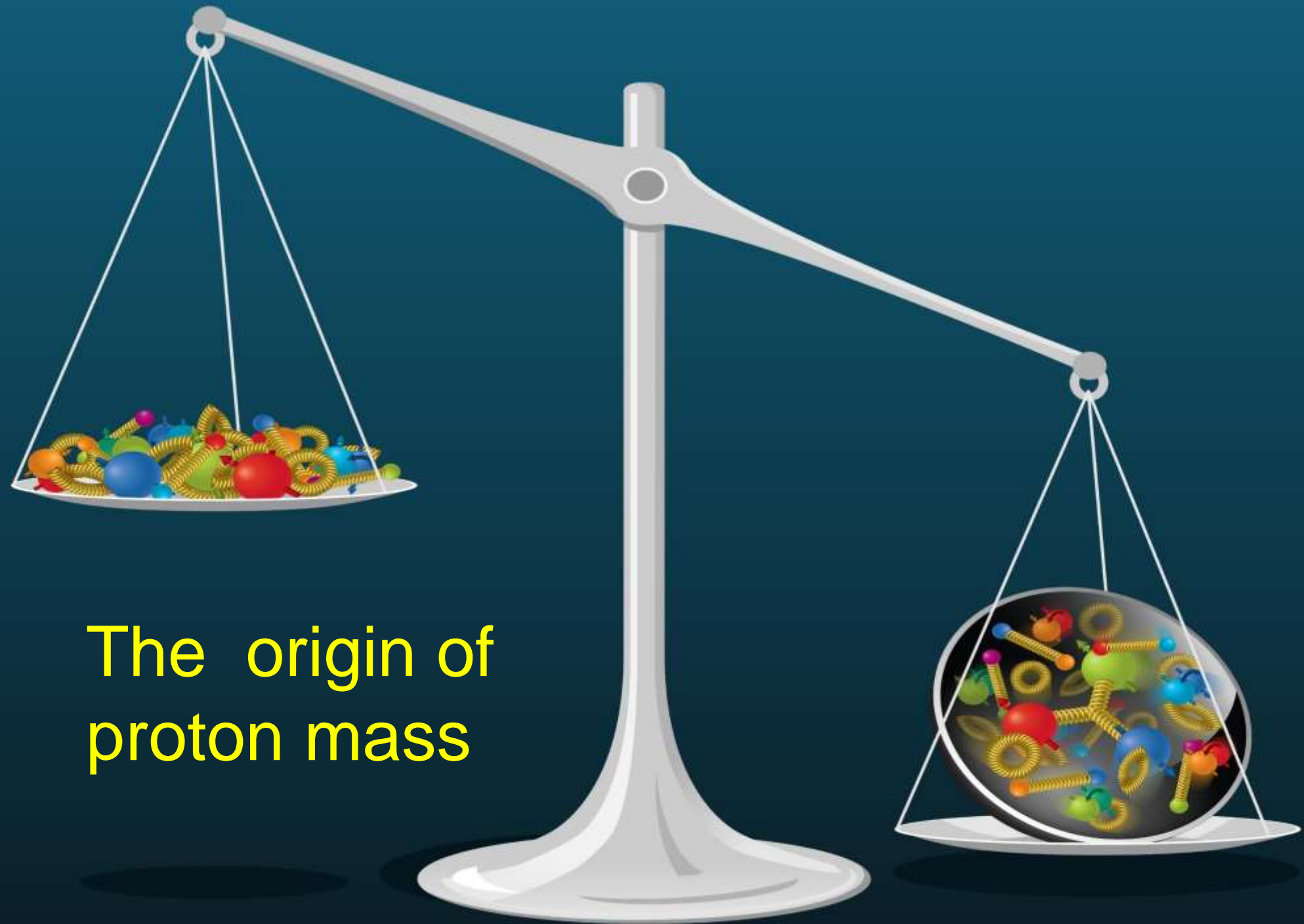


Bhattacharya, Metz, ZJ 2017

Glucion case: diffractive di-jet production

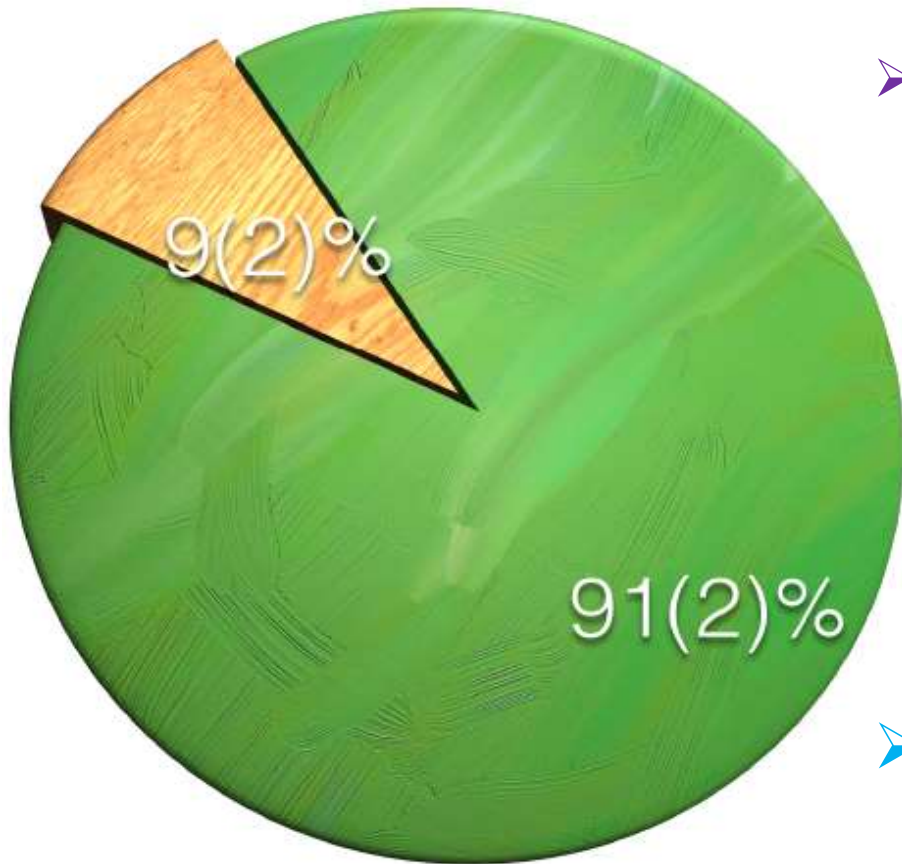


Hatta-Nakagawa-Yuan-Zhao-Xiao, 2017



The origin of  
proton mass

# Proton mass budget



Lattice result

- Mass from Quark and gluon kinetic energy accessible via PDF

$$\int_0^1 dx xq(x) \quad \int_0^1 dx xg(x)$$

◆ In the massless limit:  $m_q=0$ :

- Quark&Gluon kinetic energy make up  $\frac{3}{4}$  proton mass.
- Trace anomaly contributes to another  $\frac{1}{4}$  proton mass.

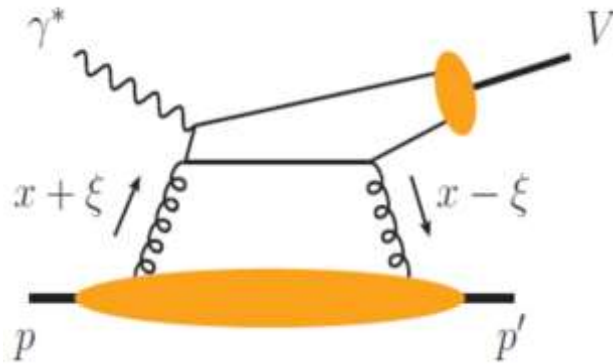
# How to measure trace anomaly

➤ Twist-4 operator:

$$\langle P' | F^{\mu\nu} F_{\mu\nu} | P \rangle$$

● Threshold J/psi production

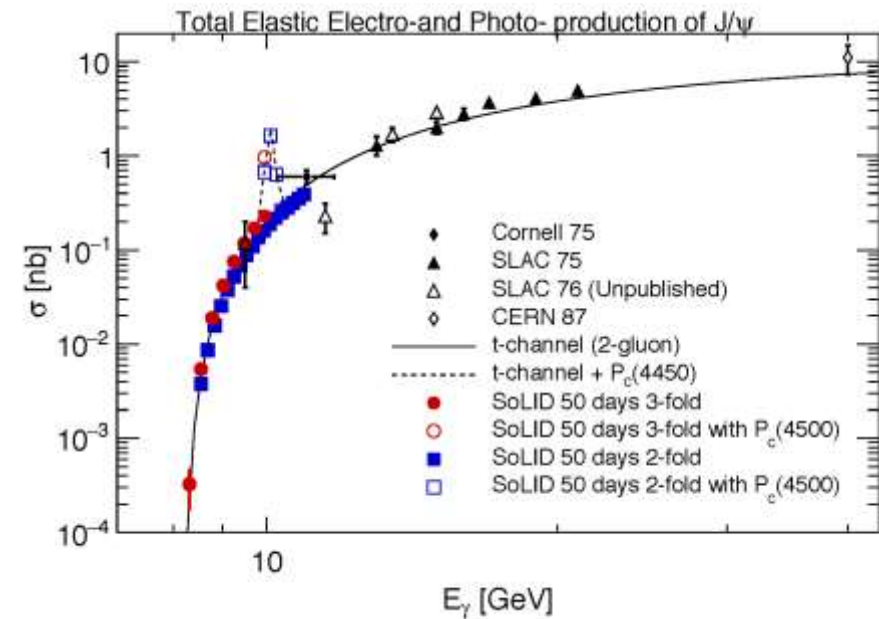
Kharzeev, Satz, Syamtomov, 1998



● Extractions: Xu-Xie-Wang-Chen, 2020  
Wang-Bu-Zeng, 2022

● Intense debates:

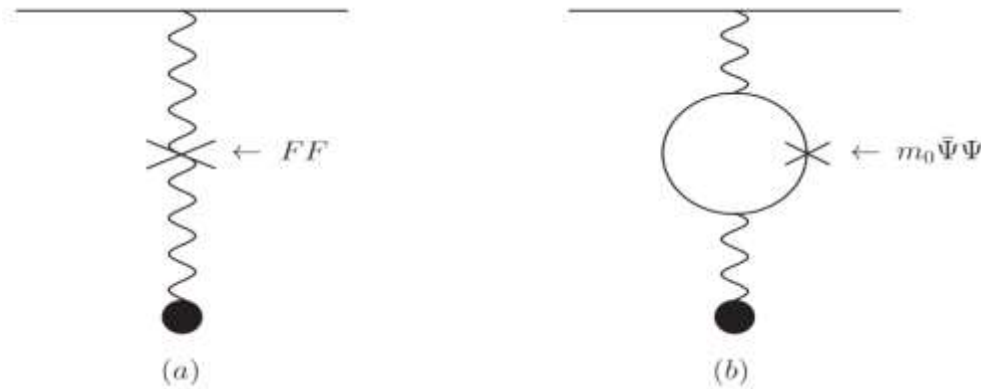
Hatta, Ji, Ma, Sun, Tong, Yuan.....





# Perturbative calculation of trace anomaly

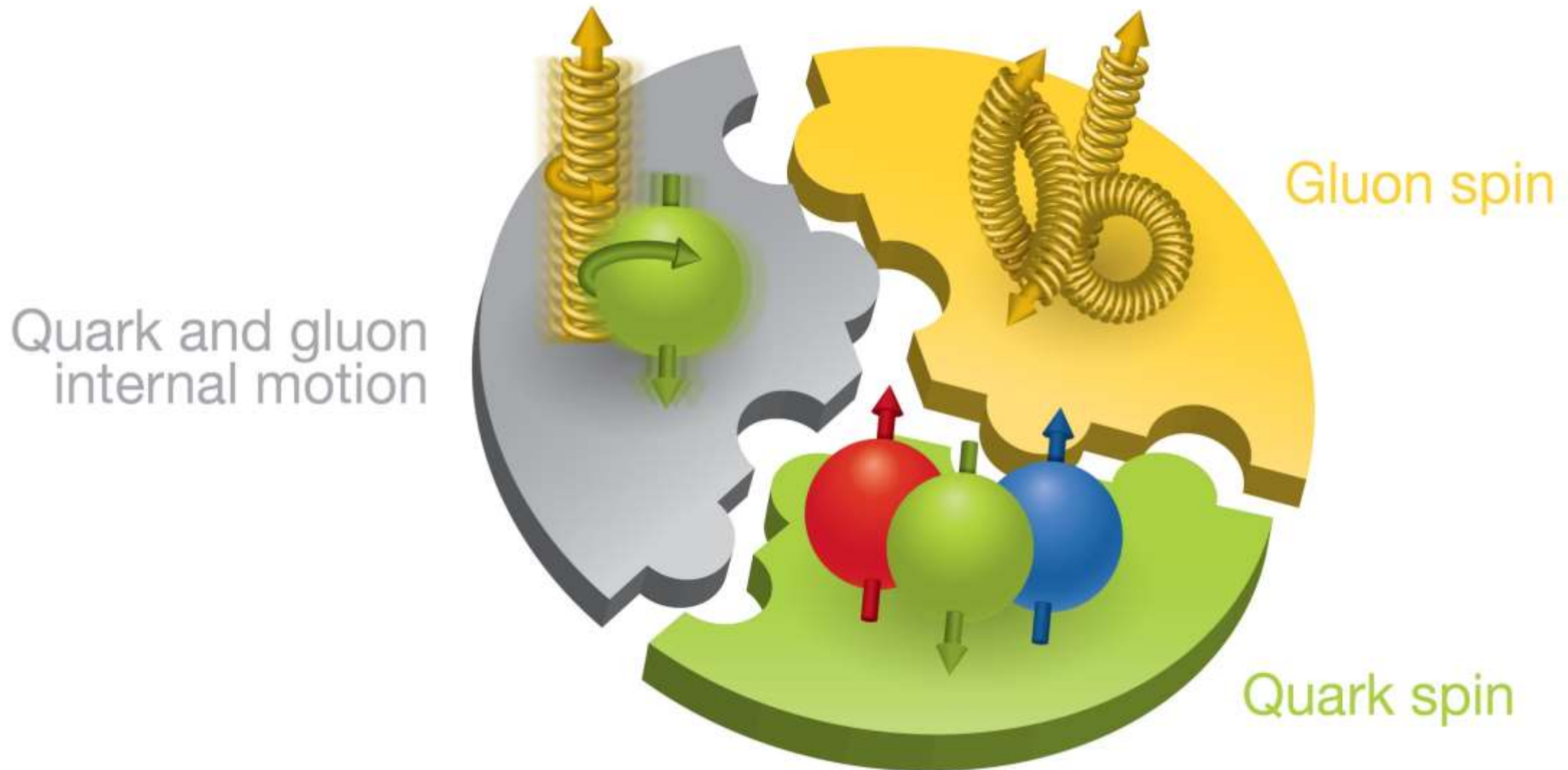
- Trace anomaly contribution to hydrogen atom mass



$$\delta\alpha_{em}^2 \int d^3y \int \frac{d^3q}{(2\pi)^3} e^{i\vec{q}\cdot\vec{y}} \int_0^1 da \frac{a^2(1-a)^2}{m^2} \varphi_0^\dagger(y) \varphi_0(y) = \frac{-4\alpha_{em}^2}{15m^2} \varphi_0^\dagger(0) \varphi_0(0)$$

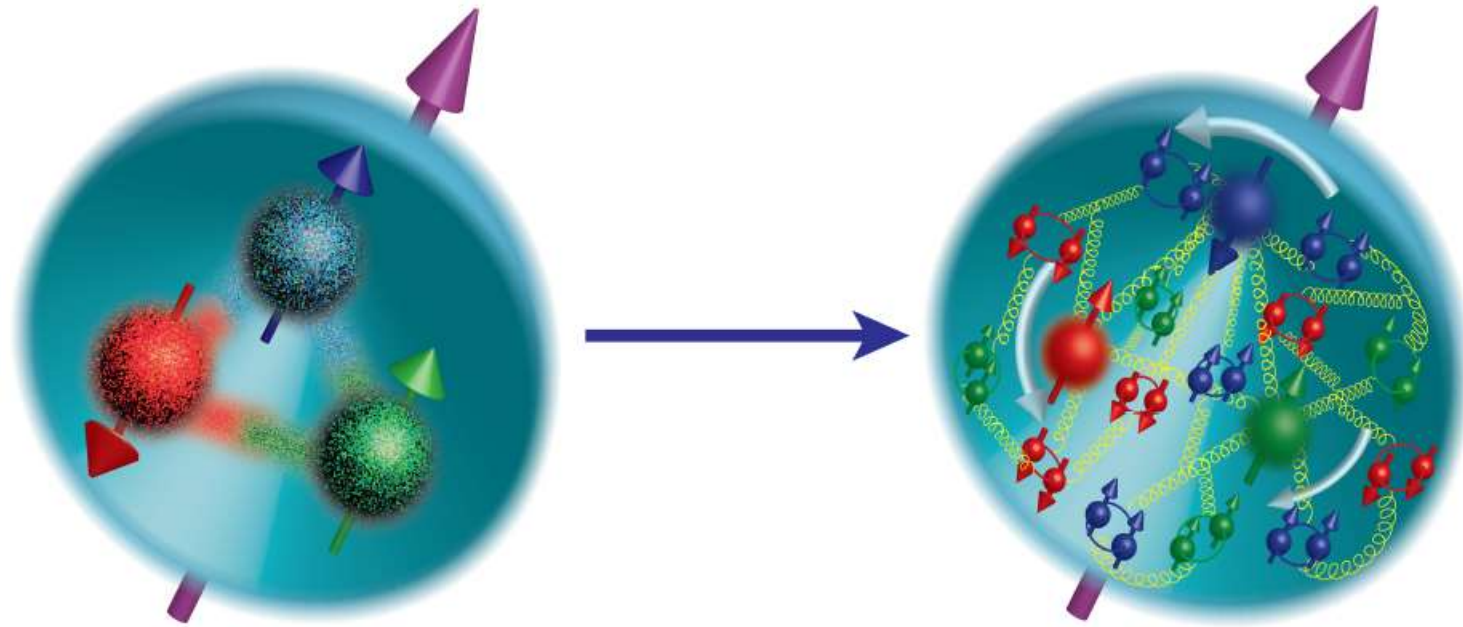
◆ Related to the **Lamb shift**. Sun-Sun-ZJ, 2020

# Proton spin decomposition



# Proton spin sum rule

$$J = \frac{1}{2}\Delta\Sigma(Q^2) + L_q(Q^2) + \Delta G(Q^2) + L_g(Q^2) = \frac{1}{2}$$



# Parton orbital angular momentum

➤ The total angular momentum is related to the GPD:

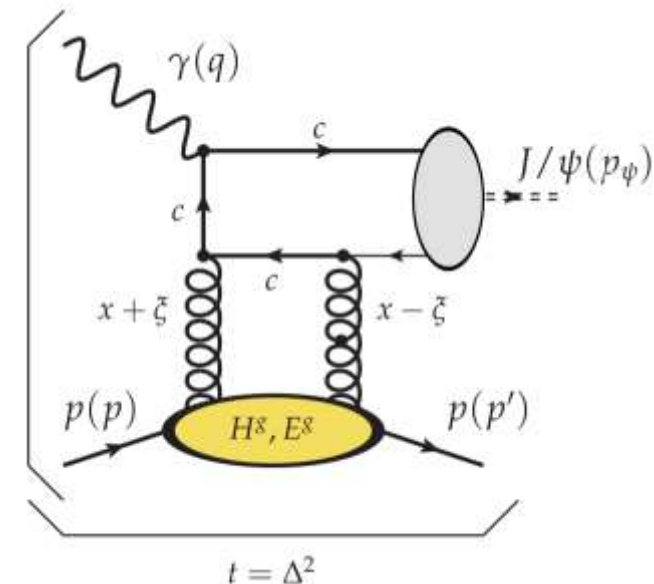
$$J_q = \lim_{t \rightarrow 0} \frac{1}{2} \int_0^1 dx x [H_q(x, t, \xi) + E_q(x, t, \xi)]$$

Ji, 1997

◆ SSA in exclusive process

$$A_N^\gamma = \frac{\frac{1}{2m_N} (1 + \xi) |\Delta_T| \sin(\phi_\Delta) \Im(\mathcal{H}^g \mathcal{E}^{g*})}{(1 - \xi^2) |\mathcal{H}^g|^2 + \frac{\xi^4}{1 - \xi^2} |\mathcal{E}^g|^2 - 2\xi^2 \Re(\mathcal{H}^g \mathcal{E}^{g*})}$$

Koempel, Kroll, Metz, ZJ, 2012



# Small x asymptotic behavior of gluon OAM

- Never can reach  $x=0$  at any experiment, **how to extrapolate down to  $x=0$**
- Small x evolution equation for  $Eg(x)$

$$\partial_Y \mathcal{E}(k_\perp) = \frac{\bar{\alpha}_s}{\pi} \int \frac{d^2 k'_\perp}{(k_\perp - k'_\perp)^2} \left[ \mathcal{E}(k'_\perp) - \frac{k_\perp^2}{2k'_\perp{}^2} \mathcal{E}(k_\perp) \right] - 4\pi^2 \alpha_s^2 \bar{\mathcal{F}}_{1,1}(k_\perp) \mathcal{E}(k_\perp)$$

**Hatta, ZJ, 2022**

**Conclusion:**  $Eg(x)$  rises as rapidly as the normal unpolarized gluon distribution!

$$x^{-0.3}$$





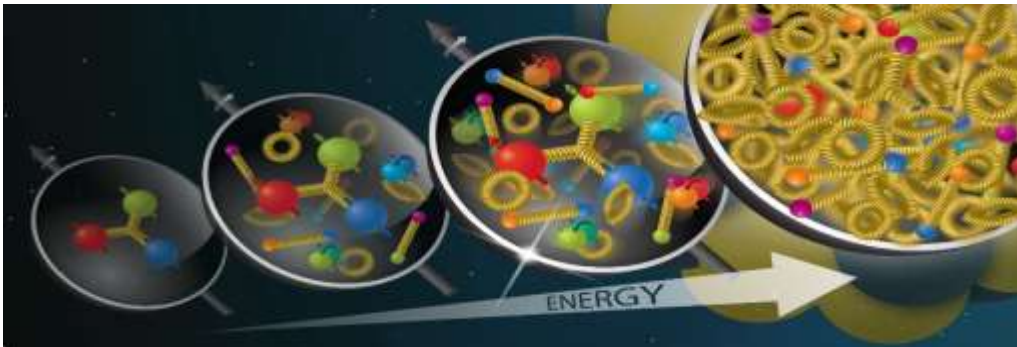
# Small x physics



# Glouns at small x

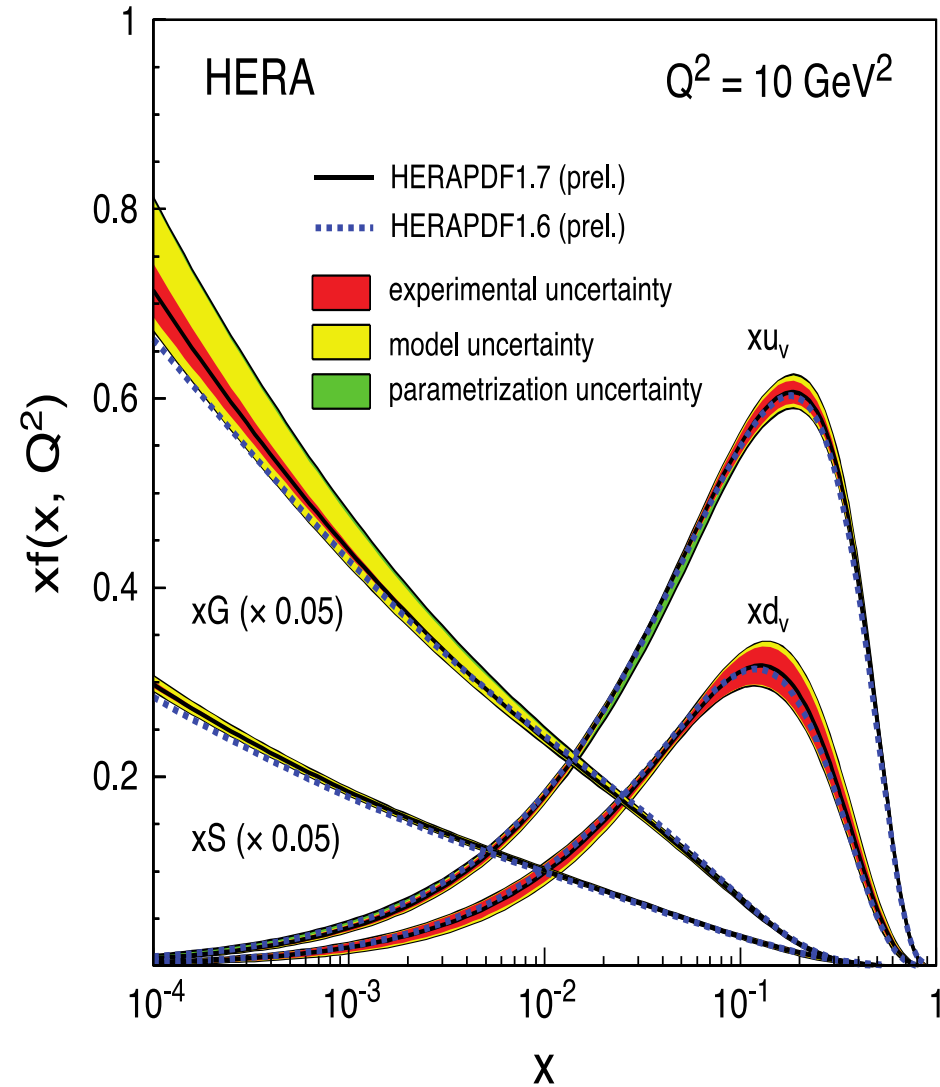
➤ DGLAP splitting function

$$P_{gg}(x) \sim \frac{1}{x} \text{ for } x \rightarrow 0$$



➤ Balitsky-Kovchegov(BK) equation:

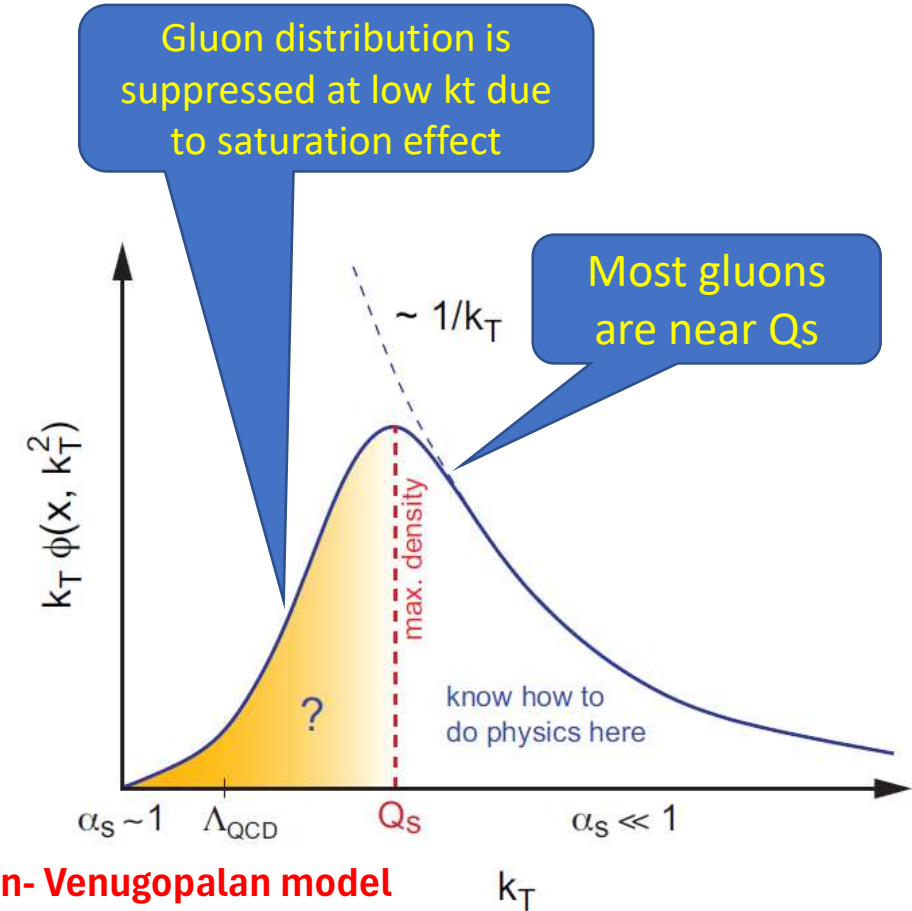
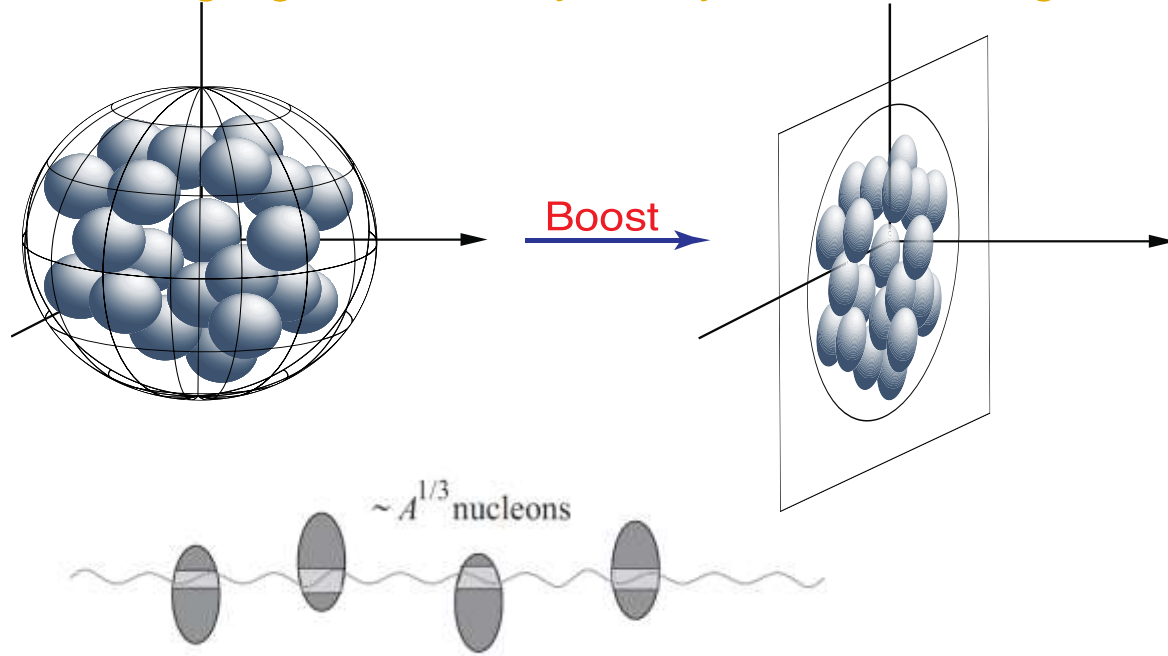
Balitsky, 1996  
Kovchegov, 1997





# Saturation scale

□ To reach high gluon density: very small  $x$  & large nucleus

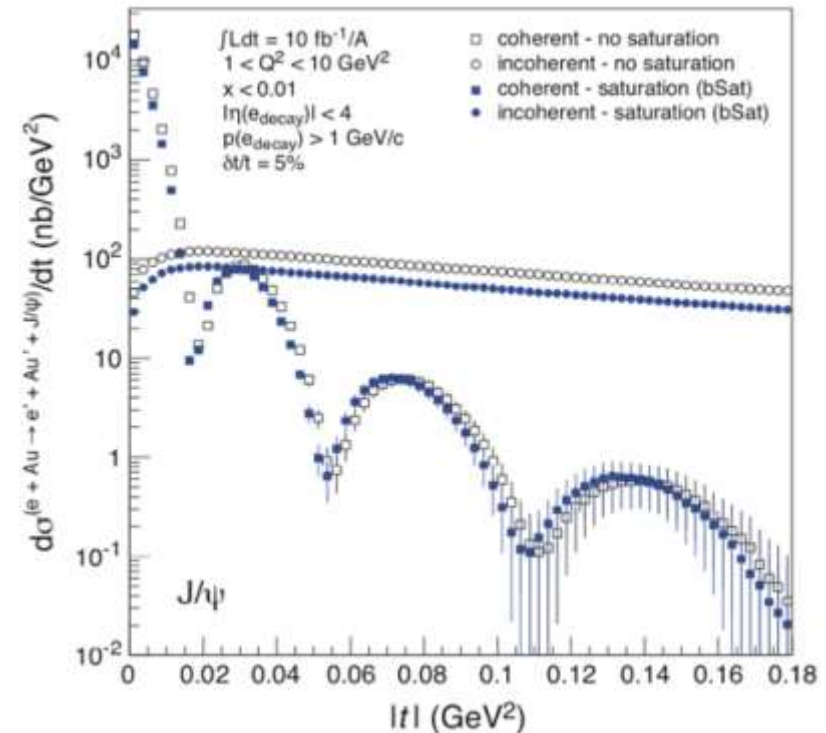
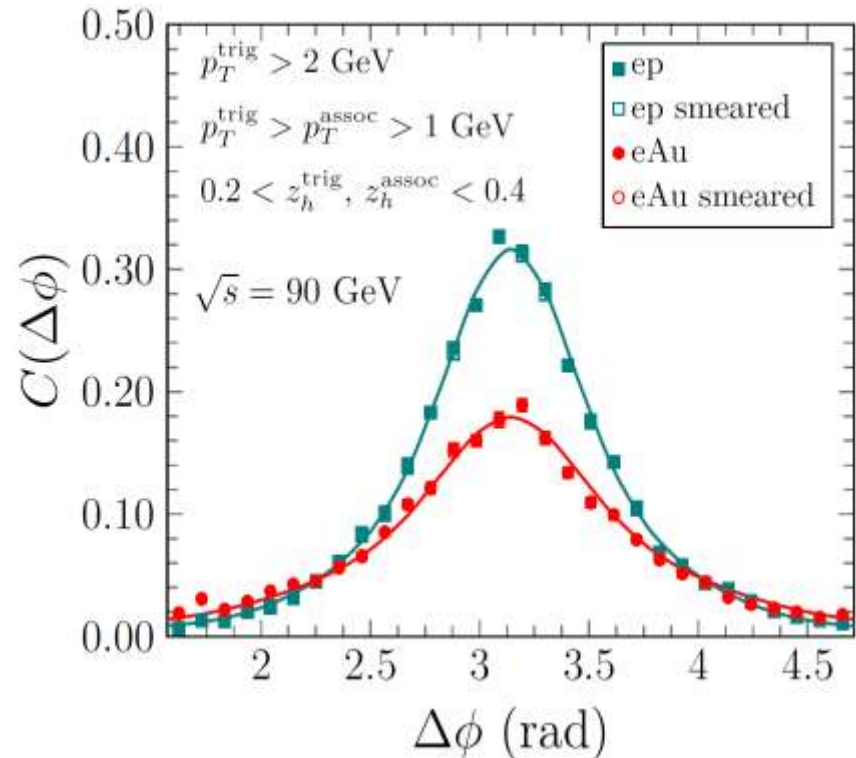


◆ Small  $x$  gluons (with long wave length) from different nucleons overlap with each other!

→  $Q_s^2(x) \sim \left(\frac{A}{x}\right)^{1/3}$  rcBK

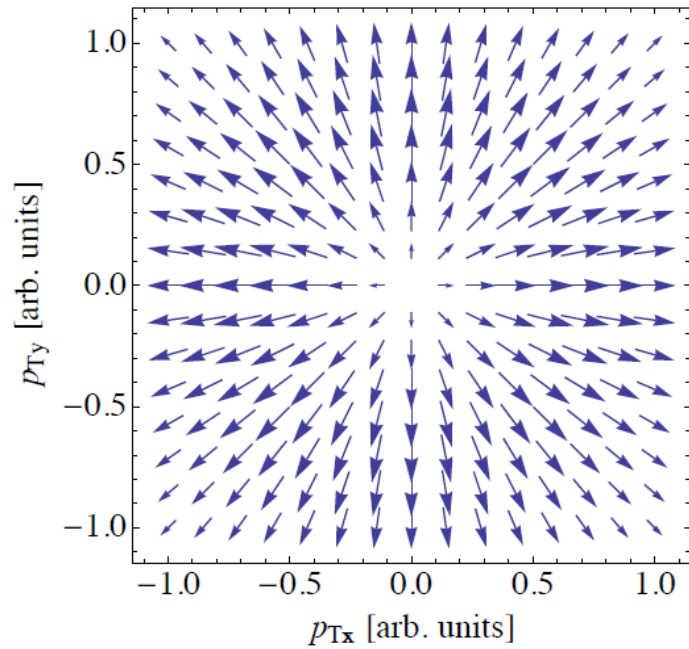
# The probe of saturation effect at EIC

- Semi-inclusive di-jet production in eA collisions
- Exclusive vector meson production in eA collisions

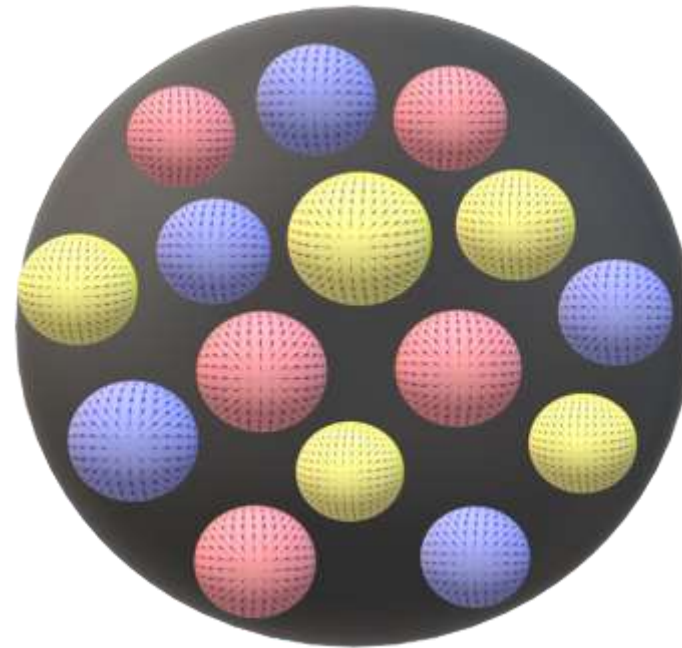


# Linearly polarized gluons at small x

Transverse momentum space



Transverse coordinate space

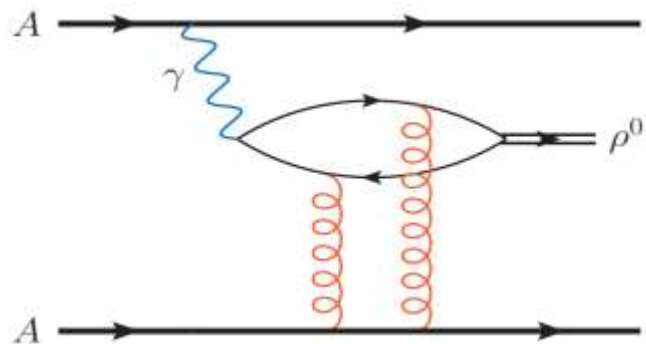


A. Metz, ZJ; 2011

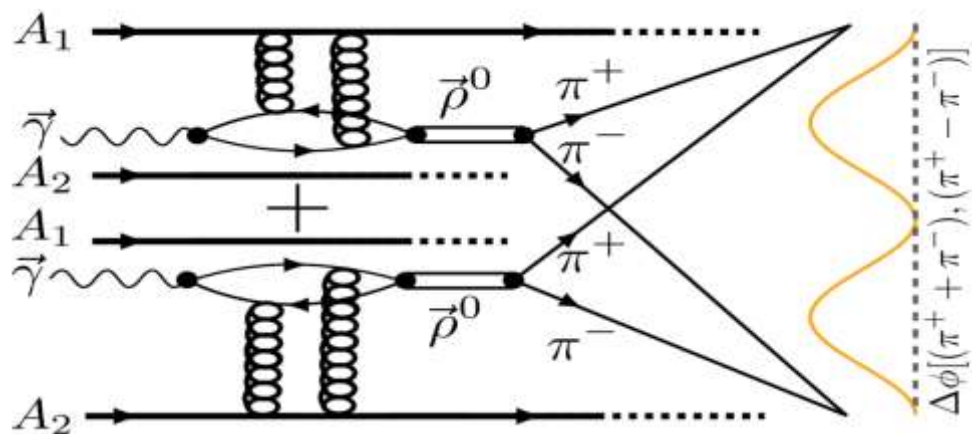
# UPC: a portal to small x physics

More UPC physics, see [Zebo's talk](#)

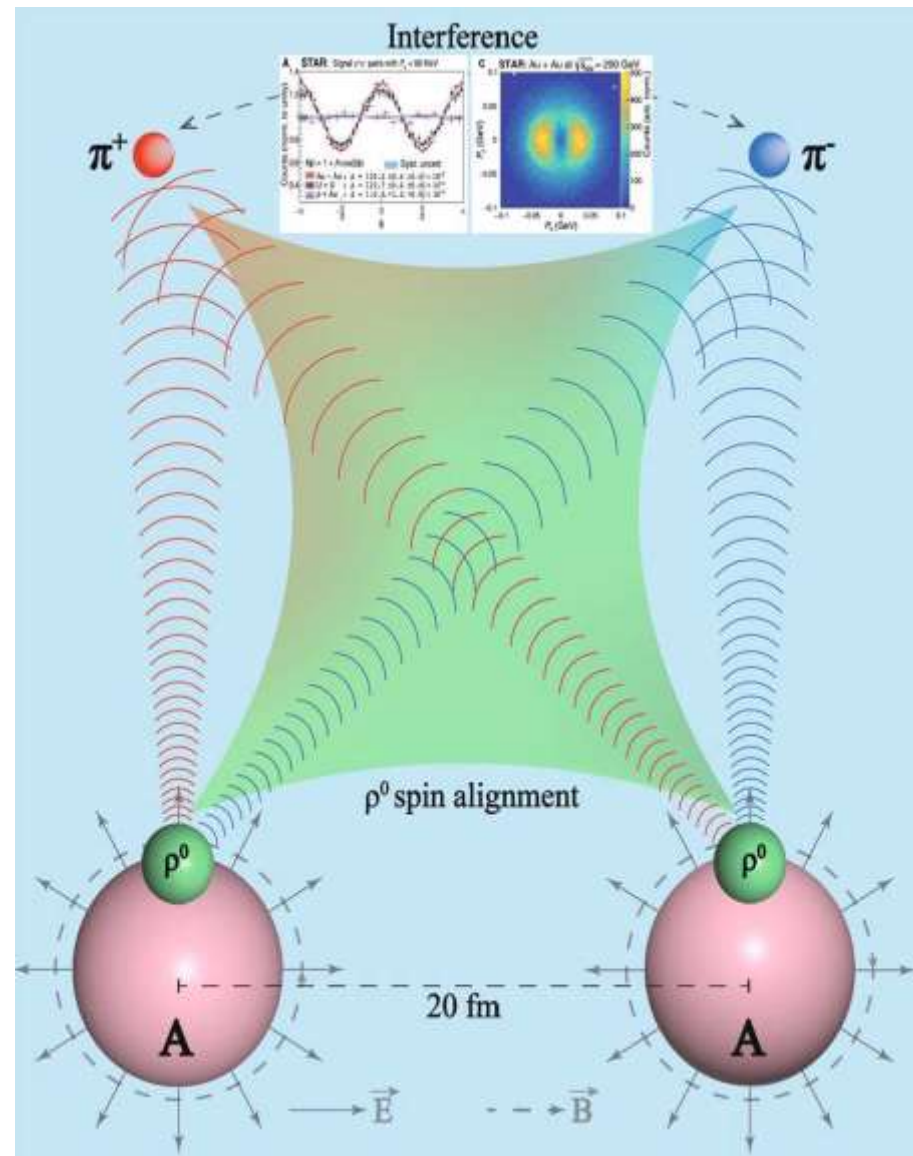
➤ Diffractive vector meson production



➤ double-slit experiment in UPCs



Klein-Nystrand, 1999



Taken from Prof. Ma's review paper

## Joint $\tilde{b}_\perp$ & $q_\perp$ dependent cross section III

➤ Full cross section:  $k_\perp + \Delta_\perp = k'_\perp + \Delta'_\perp$

$$\begin{aligned}
 \frac{d\sigma}{d^2q_\perp dY d^2\tilde{b}_\perp} &= \frac{1}{(2\pi)^4} \int d^2\Delta_\perp d^2k_\perp d^2k'_\perp \delta^2(k_\perp + \Delta_\perp - q_\perp) (\epsilon_\perp^{V*} \cdot \hat{k}_\perp) (\epsilon_\perp^V \cdot \hat{k}'_\perp) \left\{ \int d^2b_\perp \right. \\
 &\times e^{i\tilde{b}_\perp \cdot (k'_\perp - k_\perp)} [T_A(b_\perp) \mathcal{A}_{in}(Y, \Delta_\perp) \mathcal{A}_{in}^*(Y, \Delta'_\perp) \mathcal{F}(Y, k_\perp) \mathcal{F}(Y, k'_\perp) + (A \leftrightarrow B)] \\
 &+ \left[ e^{i\tilde{b}_\perp \cdot (k'_\perp - k_\perp)} \mathcal{A}_{co}(Y, \Delta_\perp) \mathcal{A}_{co}^*(Y, \Delta'_\perp) \mathcal{F}(Y, k_\perp) \mathcal{F}(Y, k'_\perp) \right] \\
 &+ \left[ e^{i\tilde{b}_\perp \cdot (\Delta'_\perp - \Delta_\perp)} \mathcal{A}_{co}(-Y, \Delta_\perp) \mathcal{A}_{co}^*(-Y, \Delta'_\perp) \mathcal{F}(-Y, k_\perp) \mathcal{F}(-Y, k'_\perp) \right] \\
 &+ \left[ e^{i\tilde{b}_\perp \cdot (\Delta'_\perp - k_\perp)} \mathcal{A}_{co}(Y, \Delta_\perp) \mathcal{A}_{co}^*(-Y, \Delta'_\perp) \mathcal{F}(Y, k_\perp) \mathcal{F}(-Y, k'_\perp) \right] \\
 &+ \left. \left[ e^{i\tilde{b}_\perp \cdot (k'_\perp - \Delta_\perp)} \mathcal{A}_{co}(-Y, \Delta_\perp) \mathcal{A}_{co}^*(Y, \Delta'_\perp) \mathcal{F}(-Y, k_\perp) \mathcal{F}(Y, k'_\perp) \right] \right\}, \quad (2.14)
 \end{aligned}$$

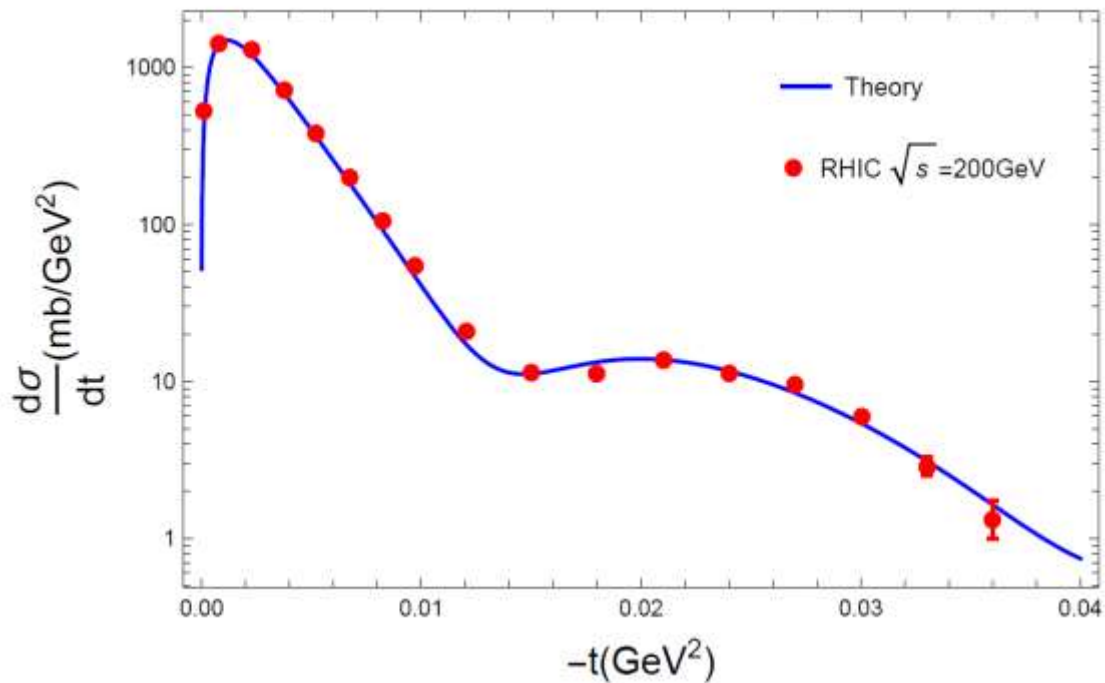
H.X. Xing, Z. Zhang, ZJ, Y.J. Zhou, 2020

➤ EM potential:  $\mathcal{F}(Y, k_\perp) = \frac{Z\sqrt{\alpha_e}}{\pi} |k_\perp| \frac{F(k_\perp^2 + x^2 M_p^2)}{(k_\perp^2 + x^2 M_p^2)}$

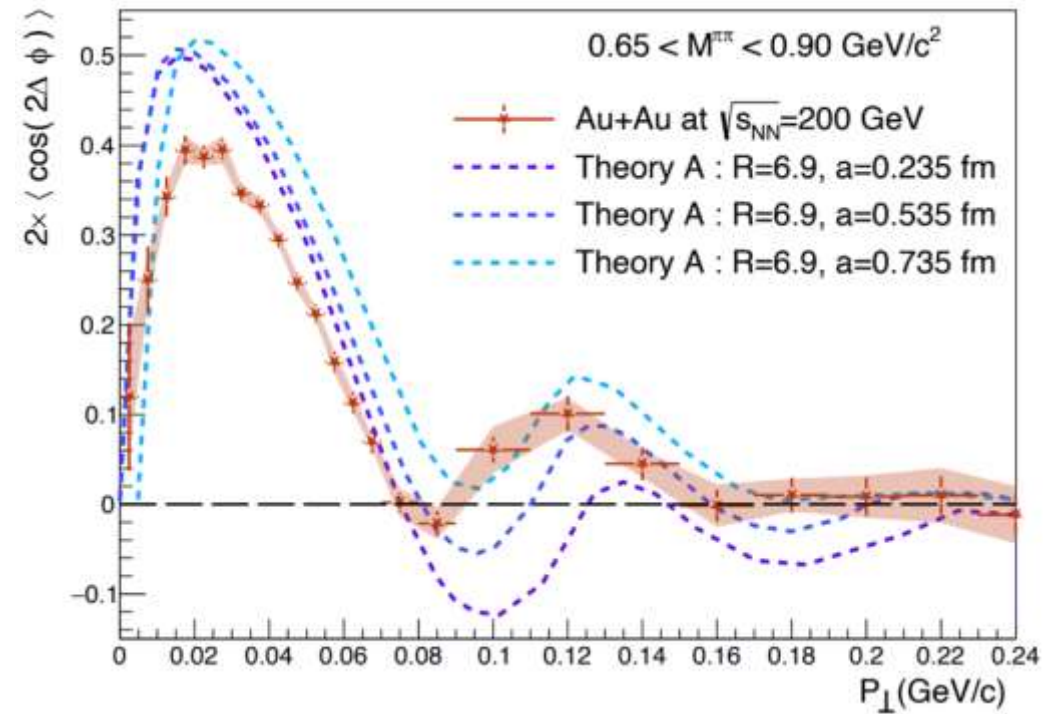


# $\rho^0$ production in UPCs

Azimuthal averaged cross section



Cos2 $\phi$  azimuthal asymmetry



Xing, Zhang, ZJ, Zhou 2020, Zha, Brandenburg, Ruan, Tang, 2021

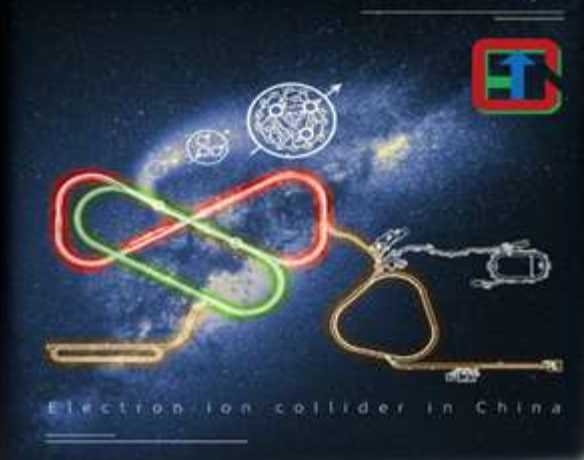


# The Scope of EIC/EicC physics

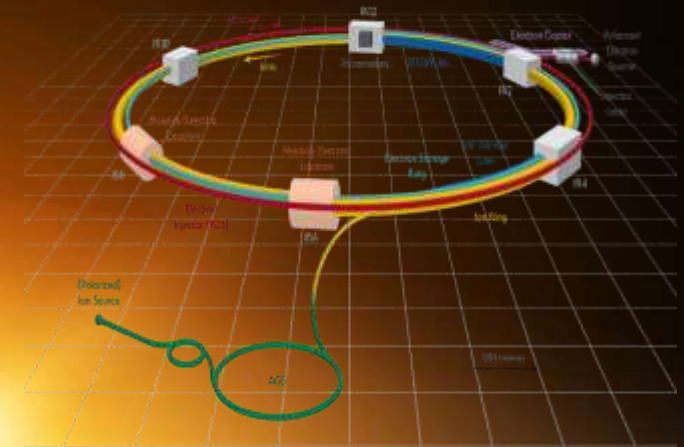
- 3D imaging of proton
  - Origin of proton mass and spin
  - Small x physics
- 
- The global properties of proton:  
proton radius, EM form factors, axial/tensor charge
  - Fragmentation processes
  - Double parton distributions
  - Jet physics
  - The lattice study, Quasi-PDFs, form factors...
  - Exotic hadronic states
  - Short range correlations
  - Beyond standard model physics: axion, dark photon.
  - .....

# The dawn of EIC era

EicC(17GeV), sea quark region



EIC(140GeV), gluonic matter



Thank you for your attention!

