

# Momentum and angular correlations in $Z/\gamma$ -hadron production in relativistic heavy-ion collisions

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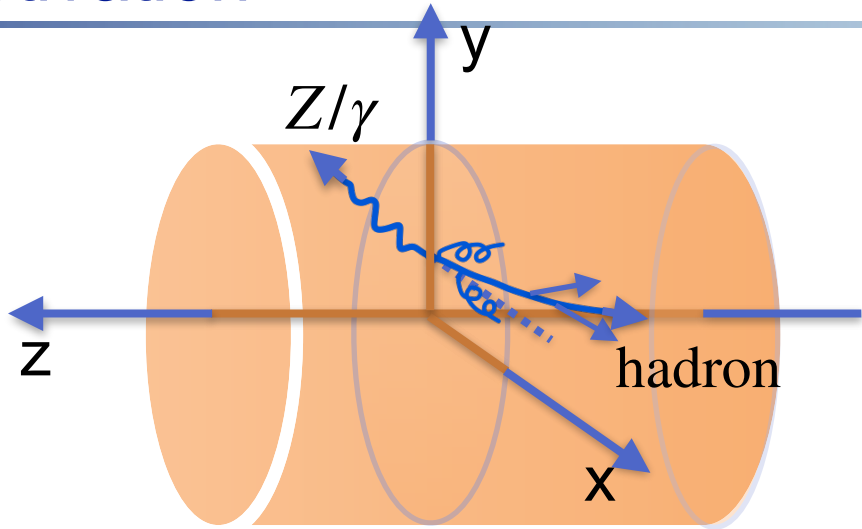
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# Outline

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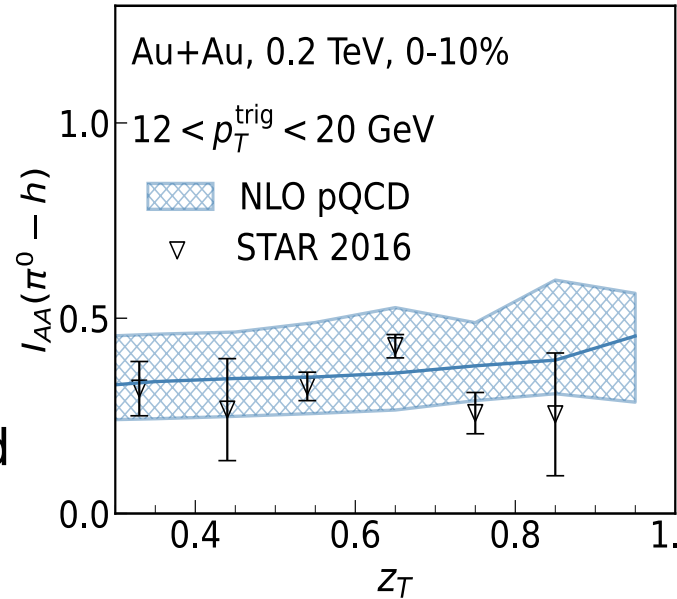
- ◎ Motivation
- ◎ Sudakov resummation improved pQCD parton model,  
HT  $\Delta E$  &  $\langle p_{\perp}^2 \rangle$ -broadening
- ◎ Numerical results
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  - Azimuthal angular correlations for  $Z/\gamma$ -hadron
  - RMS width of  $\Delta\phi$  distribution
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# Motivation

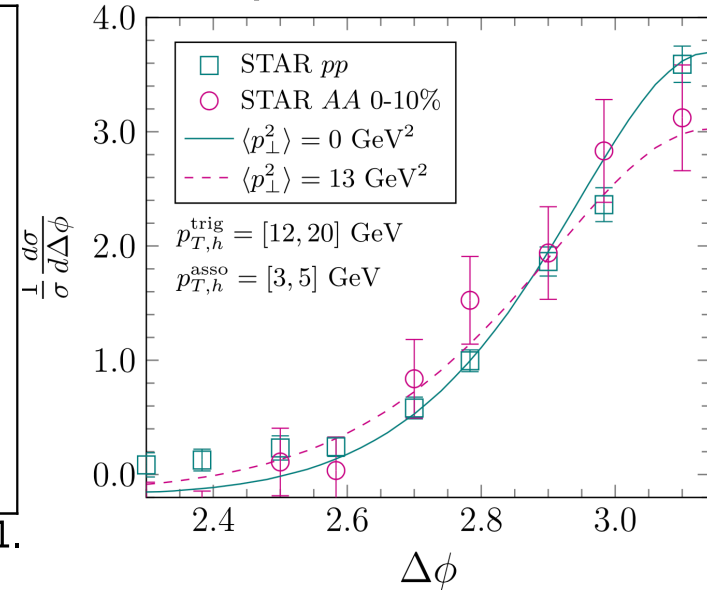


- Quark-gluon plasma (QGP) has been created in high-energy heavy-ion collisions.
- Jet quenching is an extremely useful tool to explore the transport properties of QGP. [X.-N. Wang and M. Gyulassy, PRL 68, 1480 (1992)]
- In jet trajectory, jets lose energy  $\Delta E$  and gain transverse momentum  $\langle p_{\perp}^2 \rangle$ , due to interaction with the medium by multiple scattering.

suppression...



$\Delta\phi$  de-correlation...



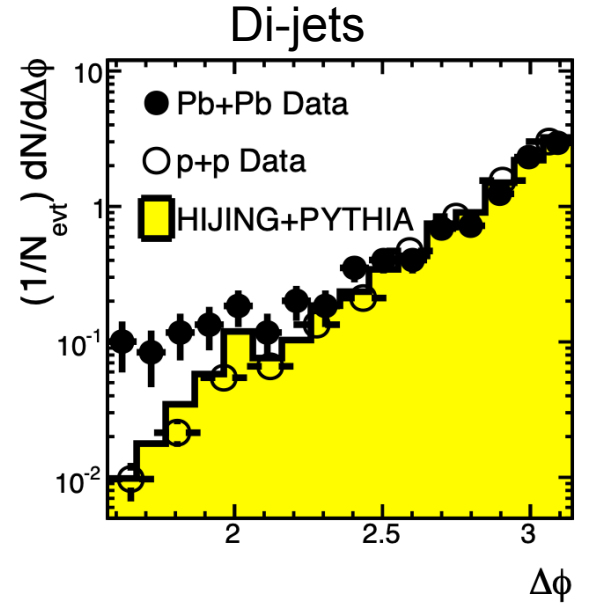
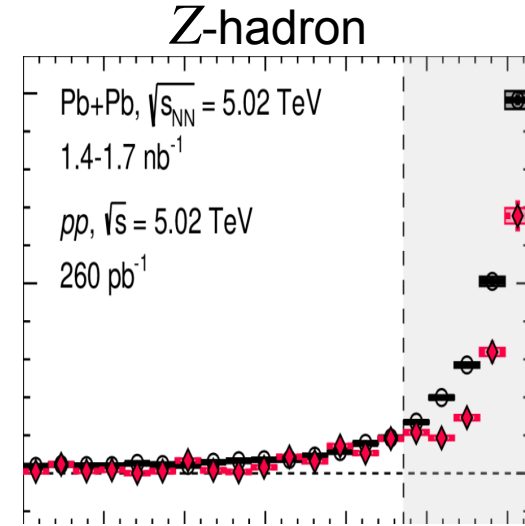
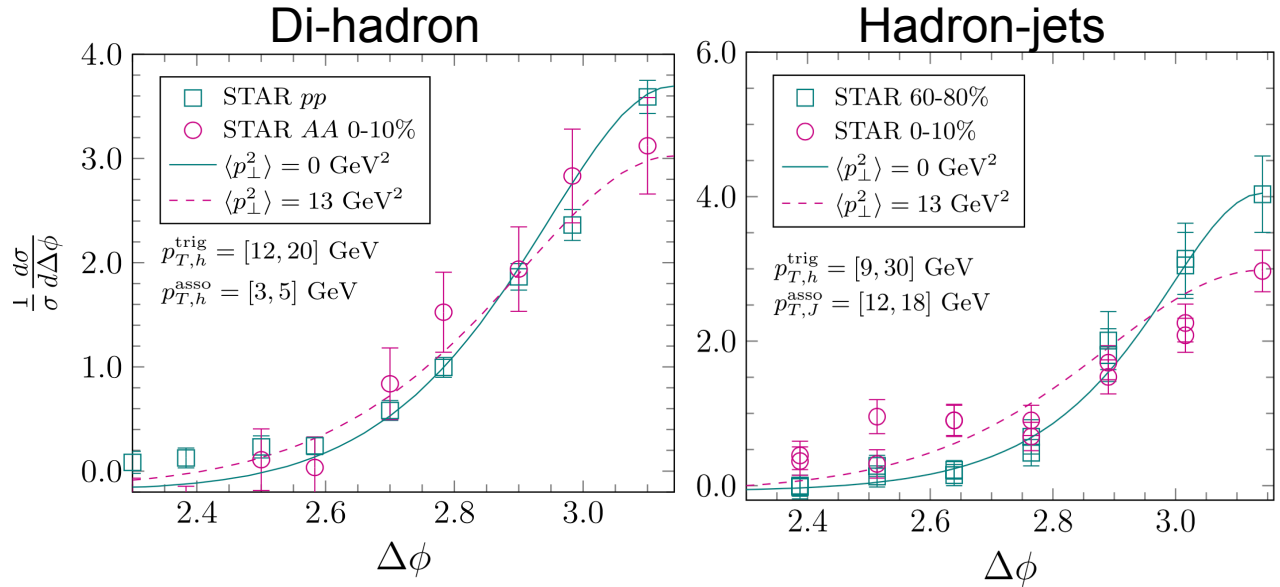
[M Xie, WY Ke, HZ Zhang, XN Wang, PRC 108 (2023) 1, L011901]  
 [L Chen, GY Qin, SY Wei, BW Xiao, HZ Zhang, PLB 773, 672 (2017)]

- Both of them are related to jet transport parameter

$$\hat{q} = \sum_{b,cd} \int dq_{\perp}^2 \frac{d\sigma_{ab \rightarrow cd}}{dq_{\perp}^2} \rho_b q_{\perp}^2.$$

[BDMPS, NPB 483, 291 (1997) & 484 265 (1997)]

# Motivation



- De-correlation caused by the  $\langle p_{\perp}^2 \rangle$ -broadening has been observed in di-hadron and hadron-jets correlations at RHIC.

[L Chen, GY Qin, SY Wei, BW Xiao, HZ Zhang, PLB 773, 672 (2017)]

- However, the  $\langle p_{\perp}^2 \rangle$  effect is not yet clearly observed for di-jets,  $Z/\gamma$ -hadron/jets within the precision of current measurements at RHIC and the LHC.

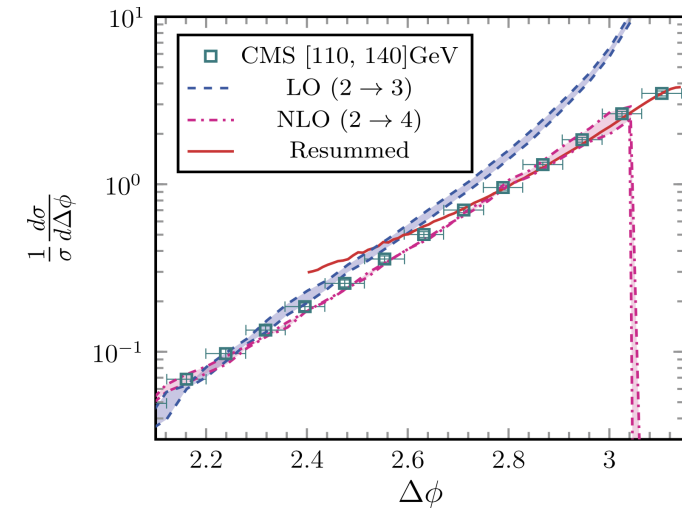
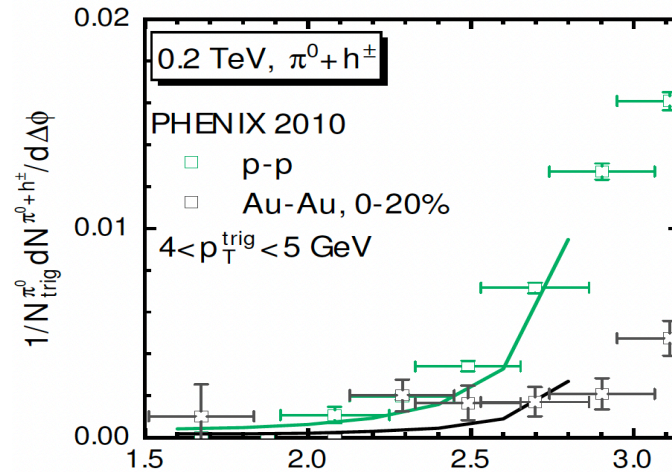
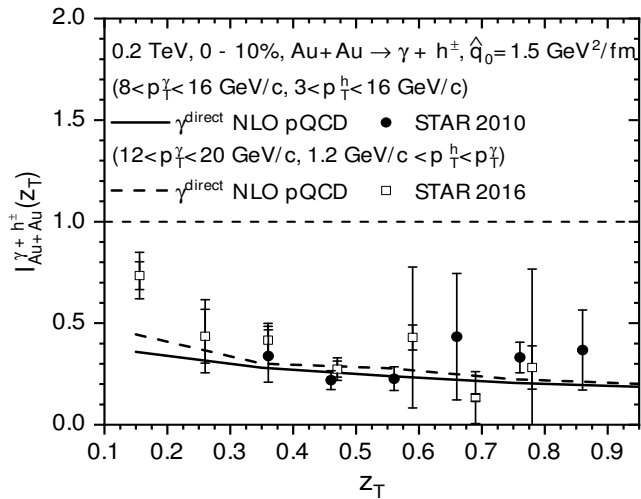
[ATLAS, PRL 105 (2010) 252303] [CMS, PRL 128, 122301 (2022)]

- Additional inclusion of the jet energy loss may also influence the angular correlation of two-particle.

$$q_{\perp AA}^{*2} \sim q_{\perp pp}^{*2} + \langle p_{\perp}^2 \rangle$$

# Motivation

With a pQCD parton model ( $\Delta E$ ) improved by the Sudakov resummation ( $\langle p_{\perp}^2 \rangle$ ) technique to study the medium modification on  $p_T$  and  $\Delta\phi$  correlations for  $Z/\gamma$ -hadron in HIC.



- NLO pQCD describes the  $p_T$  distribution well. However, its expansion fails to converge at  $\Delta\phi \sim \pi$ .

[M Xie, XN Wang, HZ Zhang, PRC 103, 034911 (2021)]  
 [J. F. Owens, PRD 65 (2002) 034011]

- The Sudakov resummation describes the data at  $\Delta\phi \sim \pi$  well.

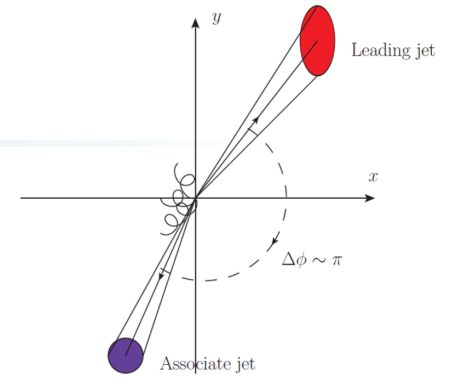
[L Chen, GY Qin, SY Wei, BW Xiao, HZ Zhang, PLB 782, 773 (2018), Mueller, Xiao, Yuan, PRL 110, 082301 (2013), & PRD 88, 114010 (2013), Sun, Yuan, Yuan, PRL 113, 232001 (2014)]

- $Z/\gamma$  Preserve the momentum information of the away-side jets before they get quenched.

# Sudakov resummation improved pQCD parton model

In  $p + p$  collisions:

$$\frac{d\sigma_{pp \rightarrow Vh}}{d\mathcal{P} \cdot \mathcal{S}} = \sum_{a,b,d} \int \frac{dz_d}{z_d^2} D_{h/d}(z_d, \mu^2) \frac{|\overline{\mathcal{M}}_{ab \rightarrow Vd}|^2}{16\pi^2 \hat{s}^2} x_a f_{a/p}(x_a, \mu^2) x_b f_{b/p}(x_b, \mu^2) \int \frac{d^2 \vec{b}_\perp}{(2\pi)^2} e^{-i\vec{q}_\perp \cdot \vec{b}_\perp} e^{-S_{\text{vac}}(Q, b_\perp)}$$



$$S_{\text{vac}}(Q, b_\perp) = S_{\text{pert}}^i(Q, b_\perp) + S_{\text{pert}}^f(Q, b_\perp) + S_{\text{NP}}(Q, b_\perp)$$

$$S_{\text{pert}}^i(Q, b_\perp) = \int_{\mu_b^2}^{Q^2} \frac{d\mu^2}{\mu^2} \left[ \left( A_i^{(1)} + A_i^{(2)} \right) \ln \frac{Q^2}{\mu^2} + B_i \right]$$

$$\sum_{k=0}^{\infty} (-1)^k \mathcal{O} \left( \left( \alpha_s \ln^2 \frac{P_\perp^2}{q_\perp^2} \right)^k \right)$$

[Mueller, Xiao, Yuan, PRL 110 (2013) 082301, PRD 88 (2013) 114010; Sun, Yuan, Yuan, PRL 113, 232001(2014); Sun, Isaacson, Yuan, Yuan, JMPA 33 (2018) no.11, 1841006]

In  $A + A$  collisions:

$$\frac{d\sigma_{AA \rightarrow Vh}}{d\mathcal{P} \cdot \mathcal{S}} = \int d^2 \vec{b} T_{AB}(\vec{b}) \int \frac{d\phi_d}{2\pi} \sum_{abd} \int \frac{dz_d}{z_d^2} \tilde{D}_{h/d}(z_d, \mu^2, \Delta E_d) \frac{|\overline{\mathcal{M}}_{ab \rightarrow Vd}|^2}{16\pi^2 \hat{s}^2} x_a \tilde{f}_{a/A} x_b \tilde{f}_{b/A} \int \frac{d^2 \vec{b}_\perp}{(2\pi)^2} e^{-i\vec{q}_\perp \cdot \vec{b}_\perp} e^{-S_{\text{med}}(Q, b_\perp)}$$

[GLM, NPB 21 (1970) 135] [CT18A PRD 103(1), 014013 (2021)] [EPPS 21, EPJC 82 (2022) 5, 413] [S. Kretzer, PRD 62, 054001 (2000)]

$$\tilde{D}_{h/d}(z_d, \mu^2, \Delta E_d) = (1 - e^{-N_g}) \left[ \frac{z'_d}{z_d} D_{h/d}(z'_d, \mu^2) + N_g \frac{z'_g}{z_d} D_{h/g}(z'_g, \mu^2) \right] + e^{-N_g} D_{h/d}(z_d, \mu^2)$$

[XN Wang, PRC70 (2004) 031901], [HZ Zhang, JF Owens, EK Wang, XN Wang, PRL 98.212301 (2007); 103, 032302 (2009)]

$$S_{\text{med}}(Q, b_\perp) = S_{\text{vac}}(Q, b_\perp) + \frac{b_\perp^2}{4} \langle p_\perp^2 \rangle$$

[AH Mueller, B Wu, BW Xiao, Y Feng, PLB 763 (2016) 208-212], [J Yong J, BW Xiao, Y Feng, PRD 101, 094008 (2020)]

# $\Delta E$ and $\langle p_{\perp}^2 \rangle$

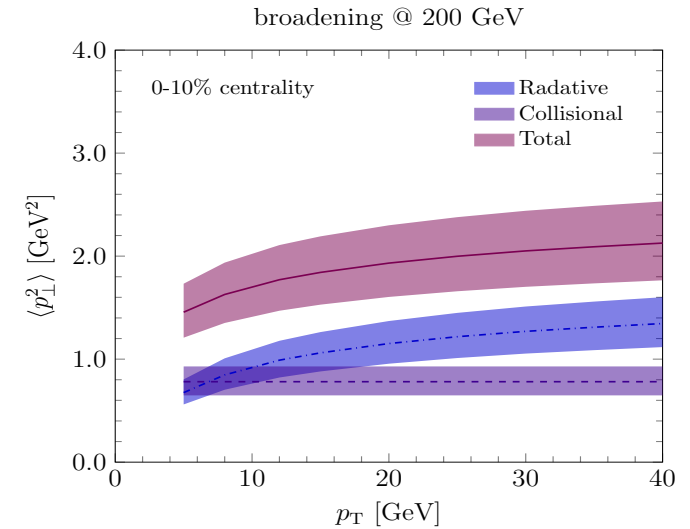
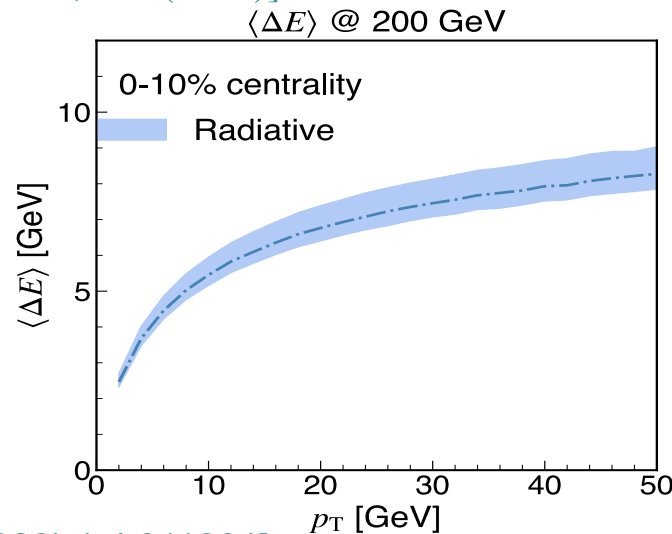
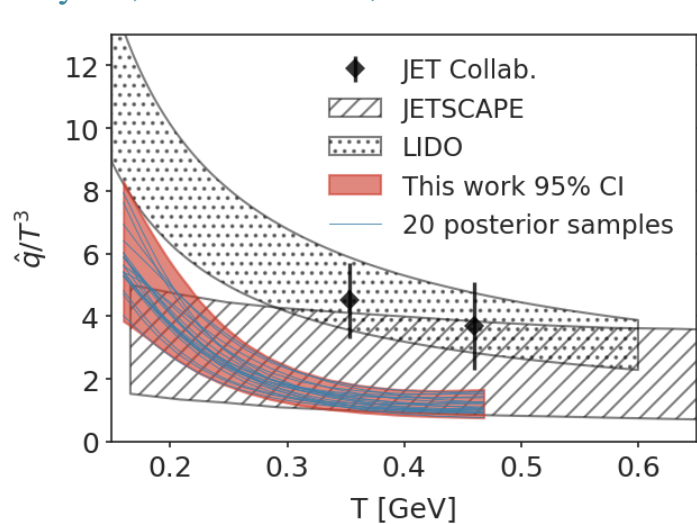
**High-Twist approach** [WT Deng, XN Wang, PRC 81, 024902(2010), E. Wang, XN Wang, PRL 87, 142301 (2001); 89, 162301 (2002), NB Chang, WT Deng, XN. Wang, PRC 89, 03491 (2014)]

$$\frac{dN_d^{\text{med}}}{dz dl_T^2 d\tau} = \frac{2C_A \alpha_s}{\pi l_T^4} \left[ \frac{1 + (1-z)^2}{z} \right] \hat{q}_d \left( \tau, \vec{r} + (\tau - \tau_0) \vec{n} \right) \sin^2 \left[ \frac{l_T^2 (\tau - \tau_0)}{4z(1-z)E} \right]$$

$$N_g^d = \int d\tau \int dl_T^2 \int dz \frac{dN_d^{\text{med}}}{dz dl_T^2 d\tau}, \quad \frac{\Delta E_d}{E} = \int d\tau \int dl_T^2 \int dz \left( z \frac{dN_d^{\text{med}}}{dz dl_T^2 d\tau} \right)$$

$$\langle p_{\perp}^2 \rangle_{\text{tot}} = \langle p_{\perp}^2 \rangle_{\text{el}} + \langle p_{\perp}^2 \rangle_{\text{rad}}, \quad \langle p_{\perp}^2 \rangle_{\text{el}} = \left\langle \int d\tau \hat{q}_d \left( \tau, \vec{r} + (\tau - \tau_0) \vec{n} \right) \right\rangle, \quad \langle p_{\perp}^2 \rangle_{\text{rad}} = \left\langle \int d\tau \int dl_T^2 \int dz \left( l_T^2 \frac{dN_d^{\text{med}}}{dz dl_T^2 d\tau} \right) \right\rangle$$

[A Majumder and B Muller, PRC 77, 054903 (2008), GY Qin, A Majumder, PRC 87, 024909 (2013), H. Clayton, M. D. Sievert, and W. A. Horowitz, EPJC 82, 437 (2022)]

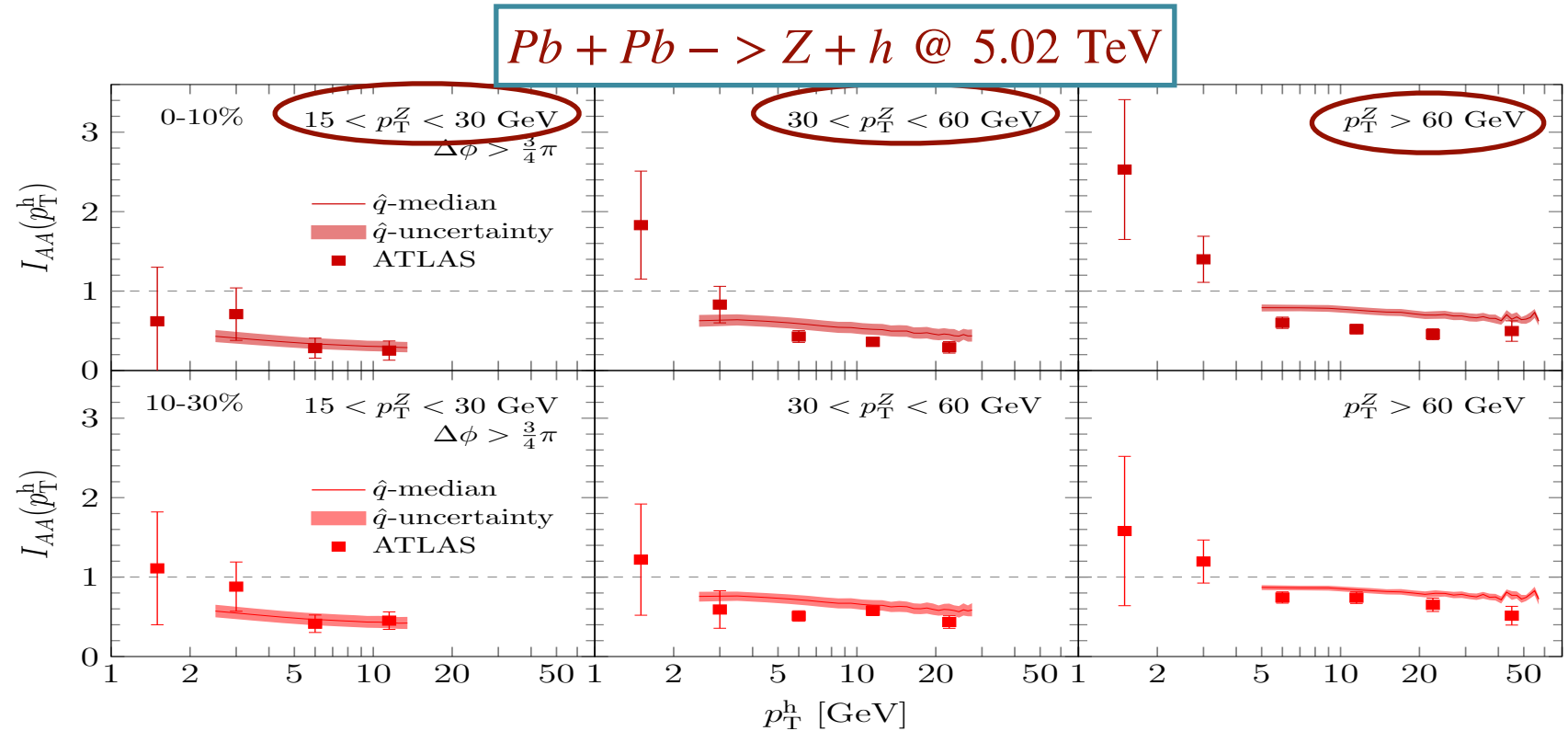
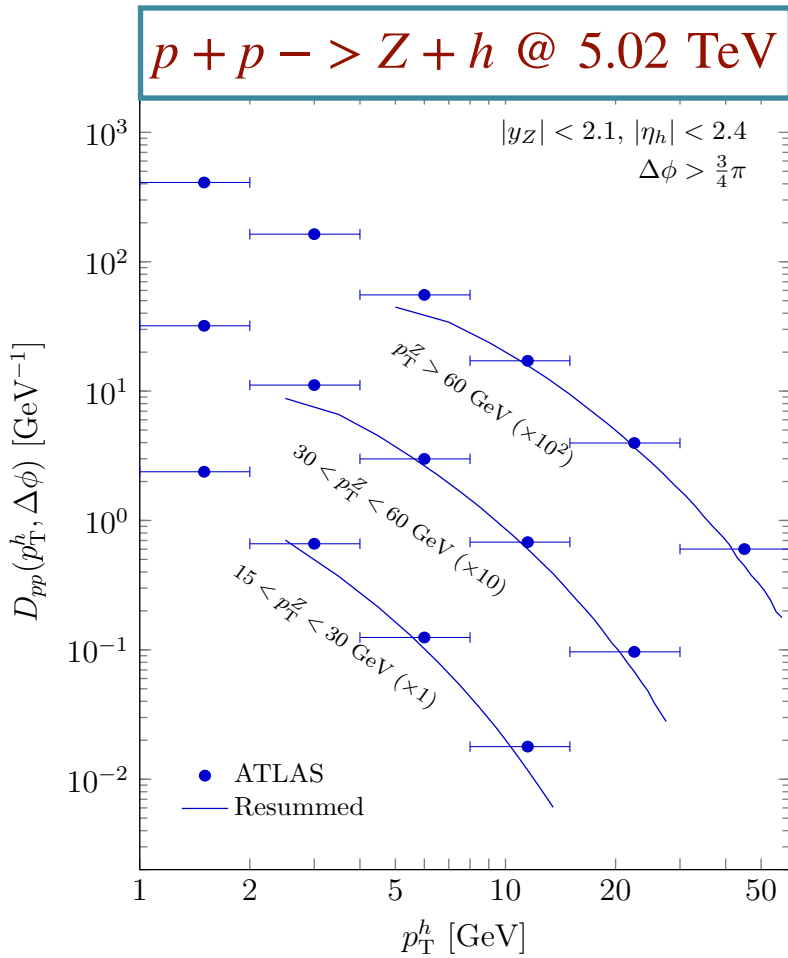


[M. Xie, WY Ke, HZ Zhang, XN Wang, PRC 108 (2023) 1, L011901]

# $p_T$ distribution for $Z$ -hadron

$$D_{pp}(p_T^h) = \frac{1}{N_V^{pp}} \frac{dN_{Vh}^{pp}}{dp_T^h} = \frac{\int d\Delta\phi dp_T^V (d^3\sigma_{Vh}^{pp} / dp_T^V dp_T^h d\Delta\phi)}{\int dp_T^V (d\sigma_V^{pp} / dp_T^V)}$$

$$I_{AA}(p_T^h) = D_{AA}(p_T^h) / D_{pp}(p_T^h)$$

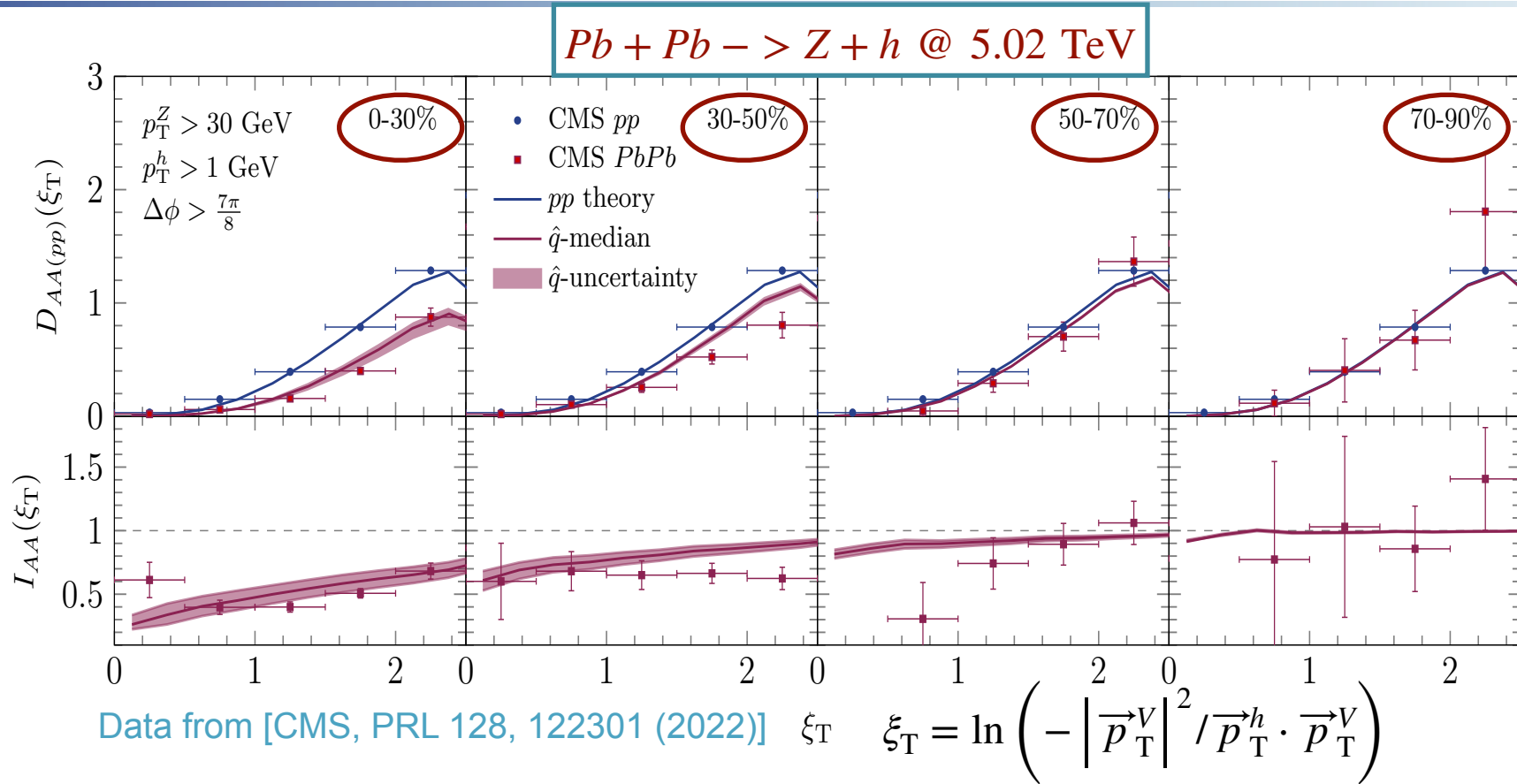


- Sudakov resummation improved pQCD parton model with  $\Delta E$  &  $\langle p_{\perp}^2 \rangle$  describes the  $p_T$  distribution of  $Z$ -hadron correlation well.
- As the  $p_T^Z$  increases, the suppression decreases.

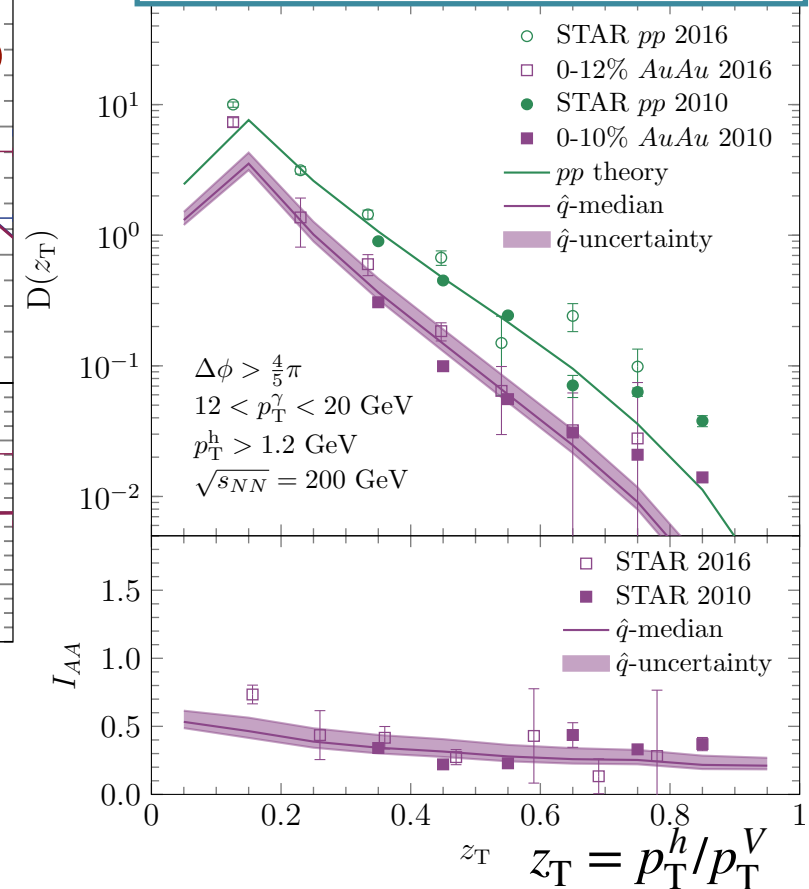


# $p_T$ distribution for $Z/\gamma$ -hadron

Data from [STAR, PRC 82, 034909 (2010)]



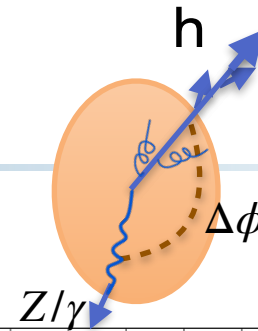
## $Au + Au \rightarrow \gamma + h @ 200 \text{ GeV}$



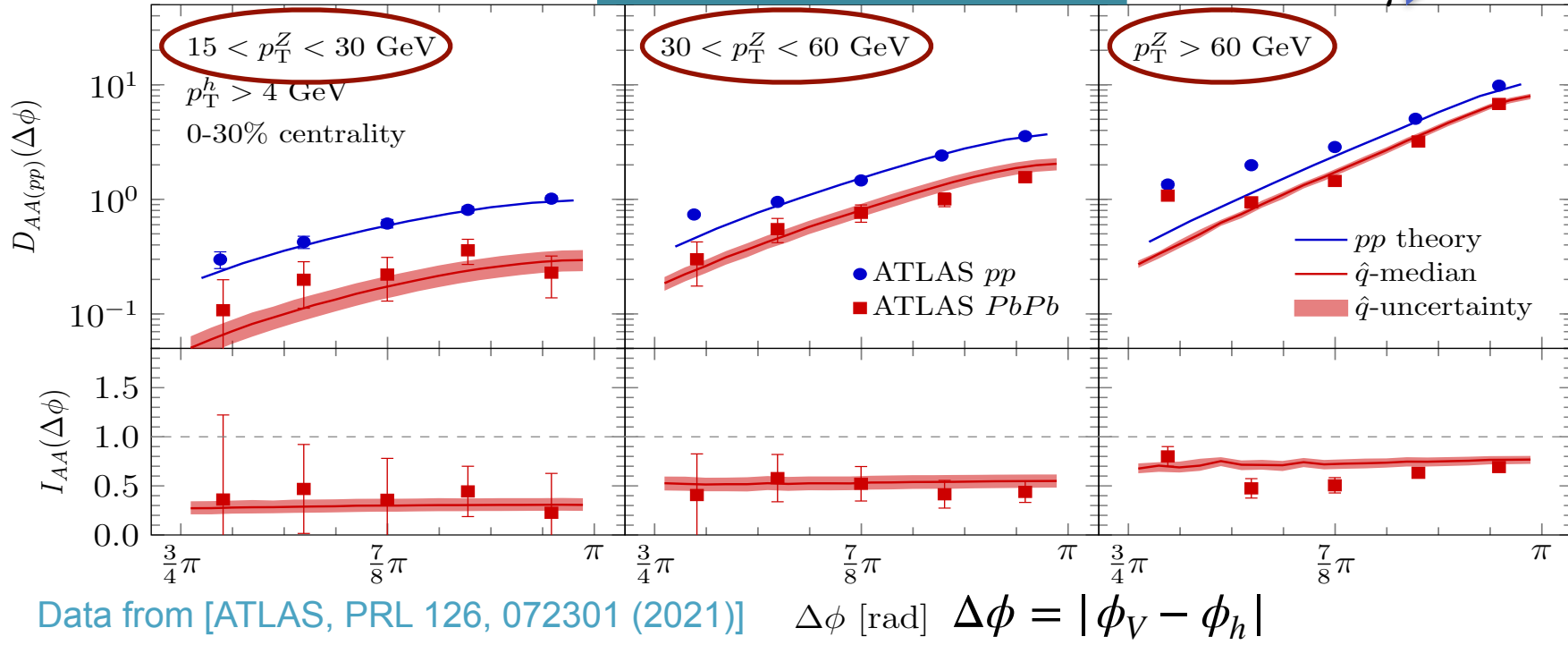
- The uncertainty is mainly from  $\Delta E$ .
- $\langle p_\perp^2 \rangle$  mainly affects the azimuthal angular and hardly affects the yield.
- Sudakov resummation improved pQCD describes the medium modification on  $p_T$  distribution for  $Z/\gamma$ -hadron correlations well, including the  $p_T^V$  and centrality dependence at both RHIC and LHC.

# $\Delta\phi$ distribution for $Z/\gamma$ -hadron

Data from [STAR, PLB 760, 689 (2016)]



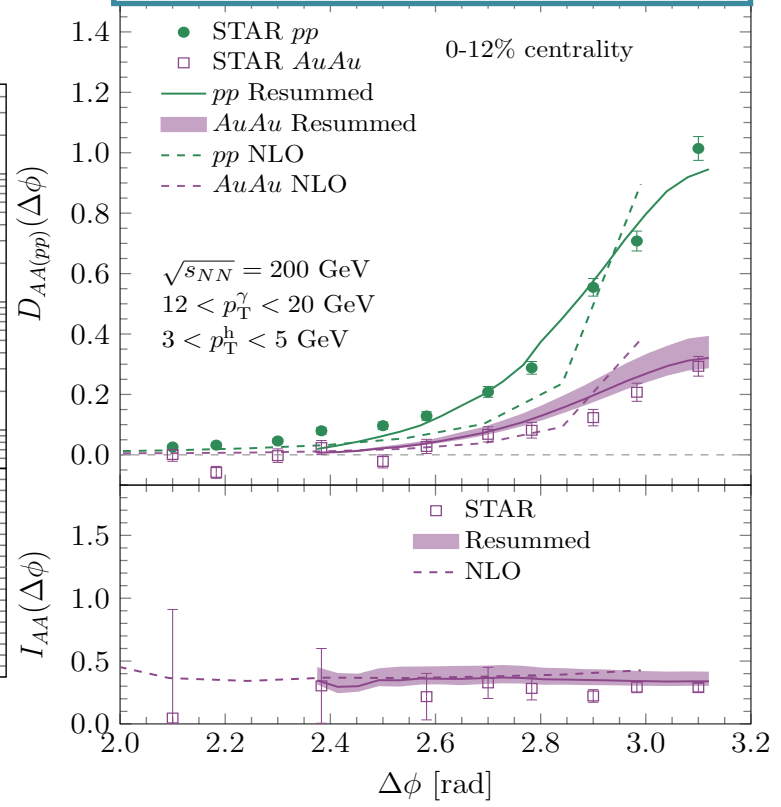
$Pb + Pb \rightarrow Z + h @ 5.02 \text{ TeV}$



Data from [ATLAS, PRL 126, 072301 (2021)]

$\Delta\phi$  [rad]  $\Delta\phi = |\phi_V - \phi_h|$

$Au + Au \rightarrow \gamma + h @ 200 \text{ GeV}$



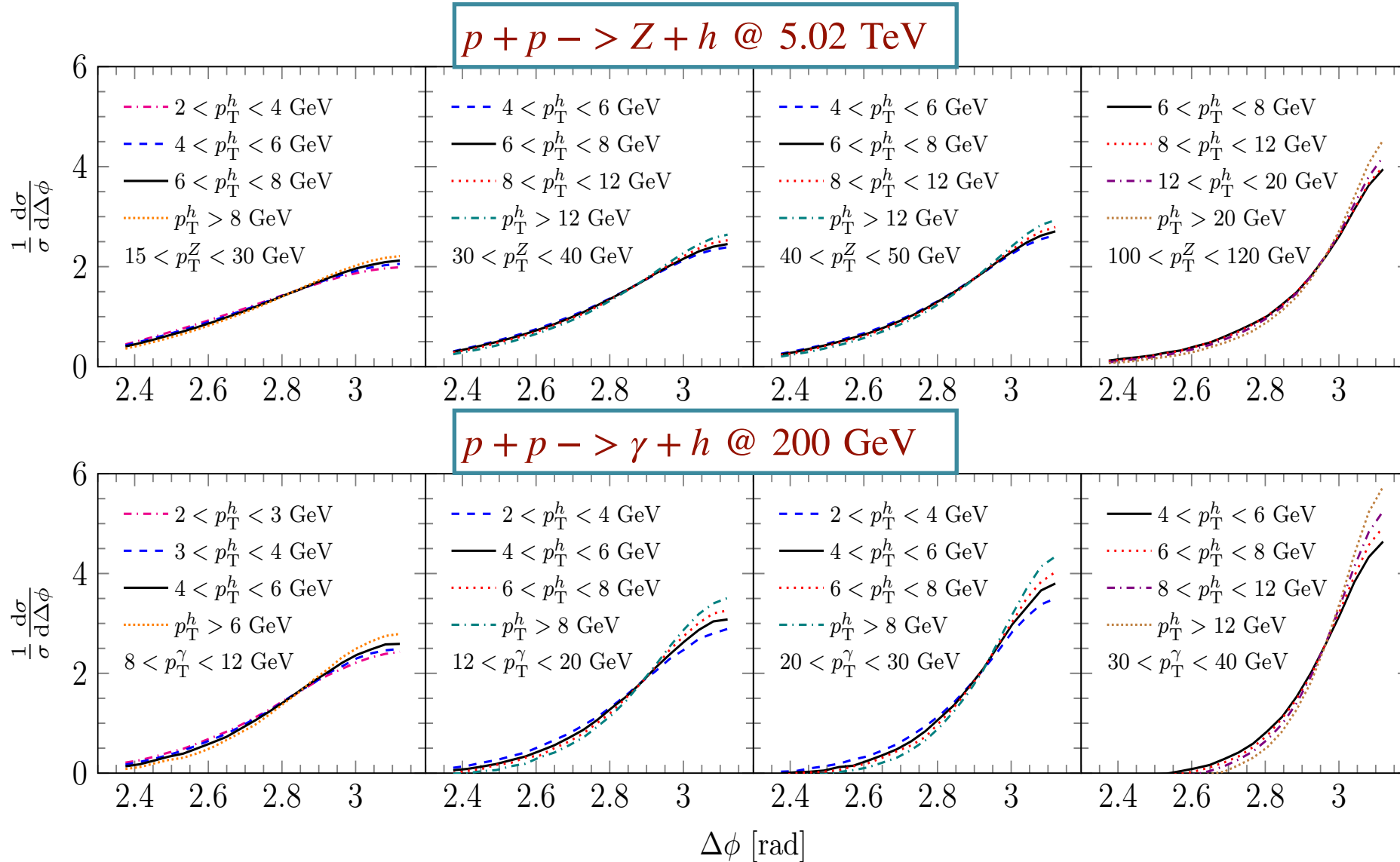
- NLO pQCD can fit the data away from  $\pi$ ; Sudakov resummation can fit the data near  $\pi$ .

[P Sun, CP Yuan, F Yuan PRL 113, 232001 (2014)] [C Lin, HZ Zhang, et al., PLB 782 (2018) 773–778]

- Sudakov resummation improved pQCD describes the medium modification on  $p_T$  &  $\Delta\phi$  distribution for  $Z/\gamma$ -hadron well, including the  $p_T^V$  and centrality dependence at both RHIC and LHC.

# Normalized $\Delta\phi$ distribution for $pp$ collisions

- Normalized the  $\Delta\phi$  distribution to unity to manifest the difference of  $\Delta\phi$  correlation between  $AA$  and  $pp$ .



$$\frac{1}{\sigma} \frac{d\sigma}{d\phi}$$

- With different  $p_T^V$  ranges
- With different  $p_T^h$  ranges

# RMS analysis to the width of $\Delta\phi$ distribution

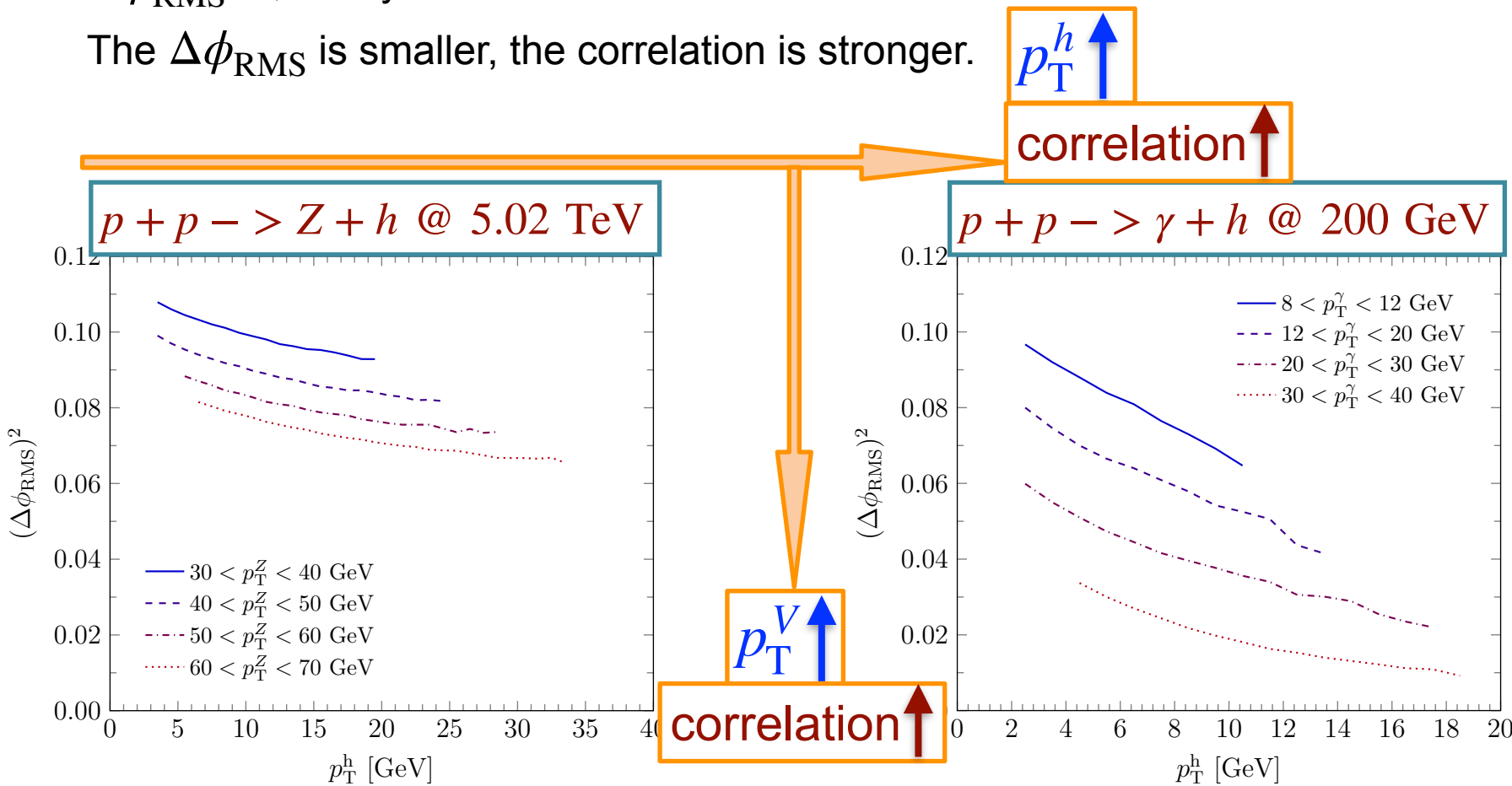
- To quantify the angular correlation strength by the RMS width:  $\Delta\phi_{\text{RMS}} =$

[JY Jia, SY Wei, BW Xiao, F Yuan, PRD 101, 094008 (2020)]

$\Delta\phi_{\text{RMS}}=0$ , totally back-to-back.

The  $\Delta\phi_{\text{RMS}}$  is smaller, the correlation is stronger.

$$\Delta\phi_{\text{RMS}} = \sqrt{\frac{\int d\Delta\phi (\Delta\phi - \pi)^2 \frac{d\sigma}{d\Delta\phi}}{\int d\Delta\phi \frac{d\sigma}{d\Delta\phi}}}$$



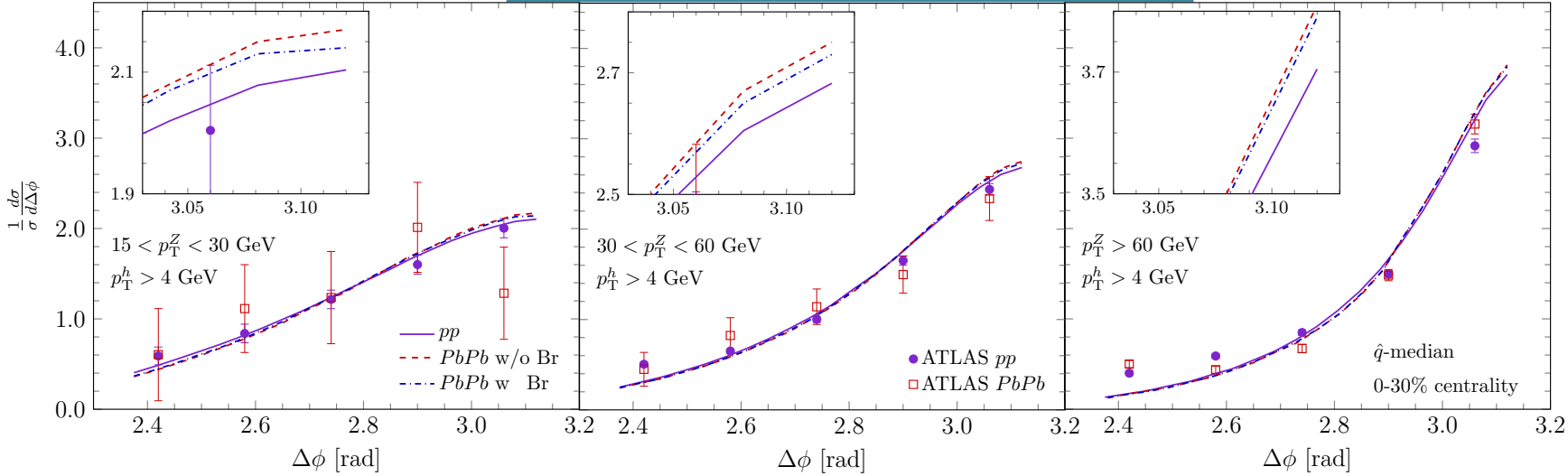
- Correlation is stronger both with the  $p_T^h$  &  $p_T^V$  increasing;
- Correlation is weaker at LHC than at RHIC;
- At LHC, as the  $Q^2$  increases, the Sudakov effect enhances.

$$S_{\text{pert}}^i(Q, b_\perp) =$$

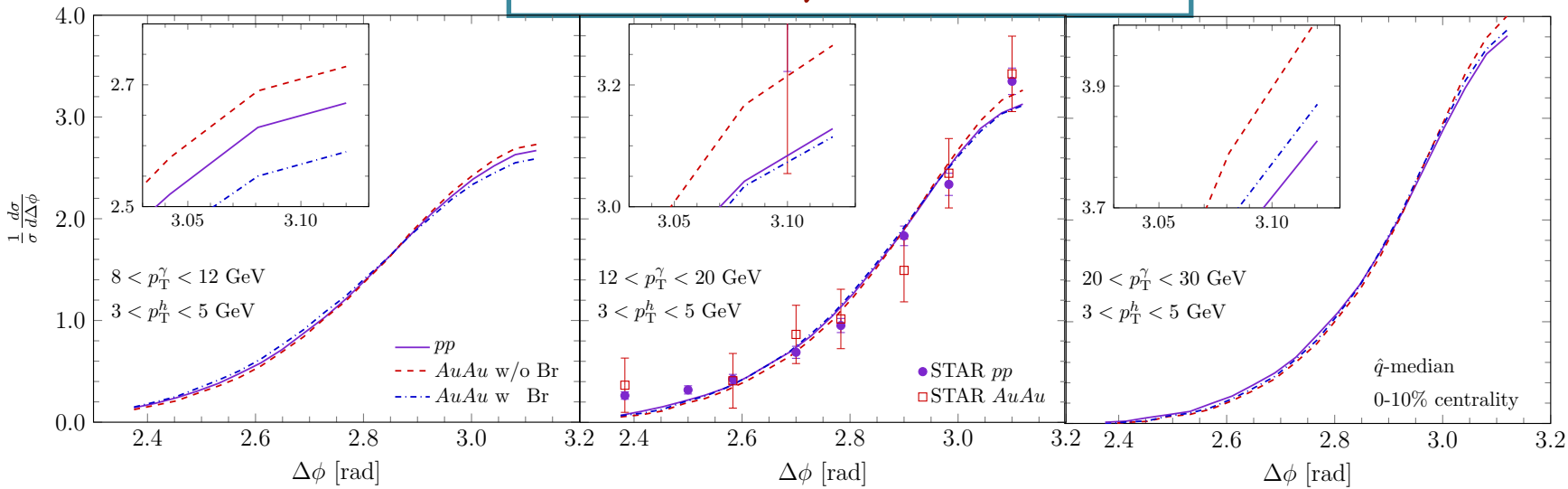
$$\int_{\mu_b^2}^{Q^2} \frac{d\mu^2}{\mu^2} \left[ \left( A_i^{(1)} + A_i^{(2)} \right) \ln \frac{Q^2}{\mu^2} + B_i \right]$$

# Normalized $\Delta\phi$ distribution for AA collisions

## $Pb + Pb \rightarrow Z + h @ 5.02 \text{ TeV}$



## $Au + Au \rightarrow \gamma + h @ 200 \text{ GeV}$



$$\tilde{D}_{h/d}(z_d, \mu^2, \Delta E_d)$$

$$S_{\text{med}}(Q, b_\perp) = S_{\text{vac}}(Q, b_\perp) + \frac{b_\perp^2}{4} \langle p_\perp^2 \rangle$$

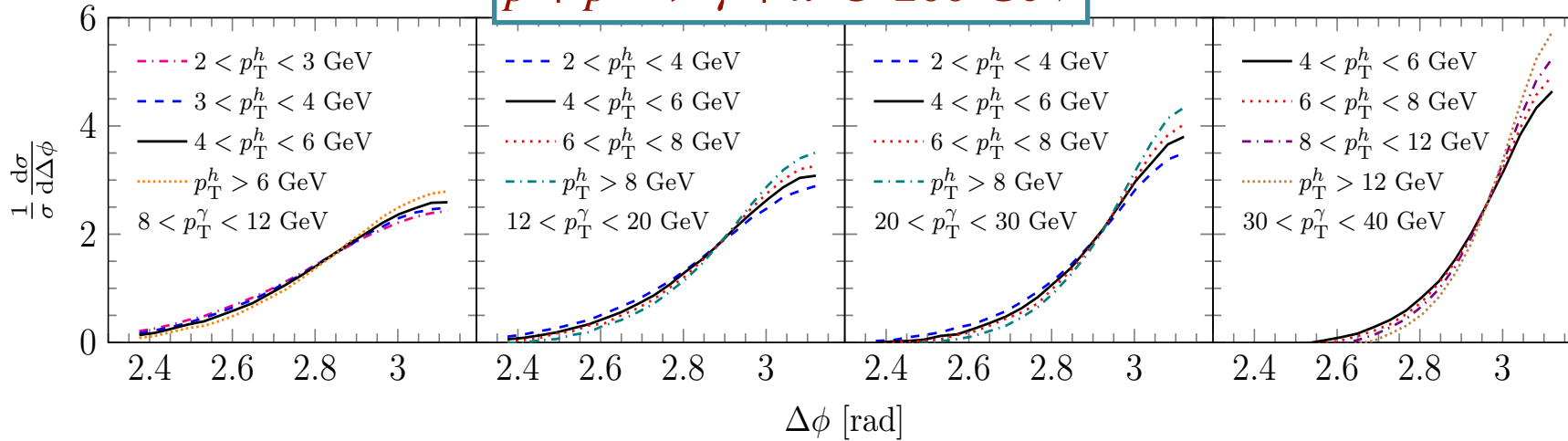
- $\Delta E$  makes the correlation stronger.
- $\langle p_\perp^2 \rangle$  makes the de-correlation stronger.

At the LHC:

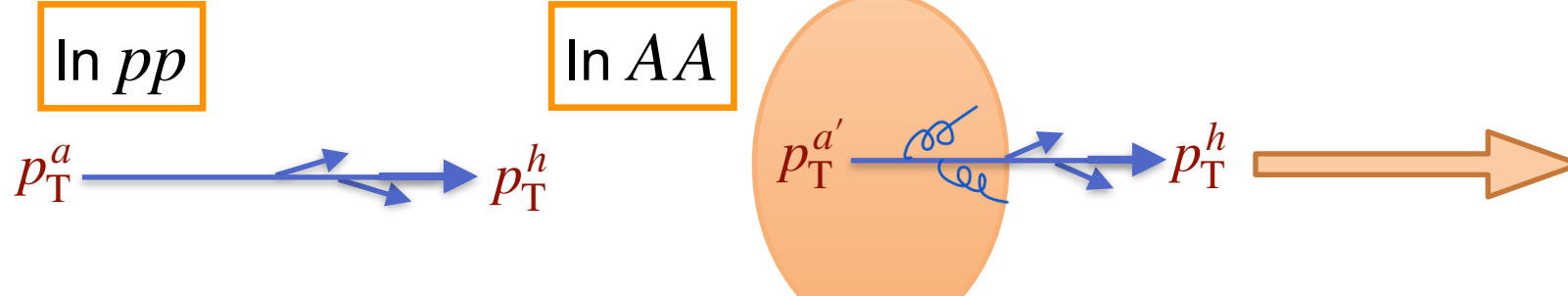
- $\langle p_\perp^2 \rangle$  effect is barely visible.
- $S_{\text{vac}}$  dominates.

# Normalized $\Delta\phi$ distribution for AA collisions

$p + p \rightarrow \gamma + h @ 200 \text{ GeV}$



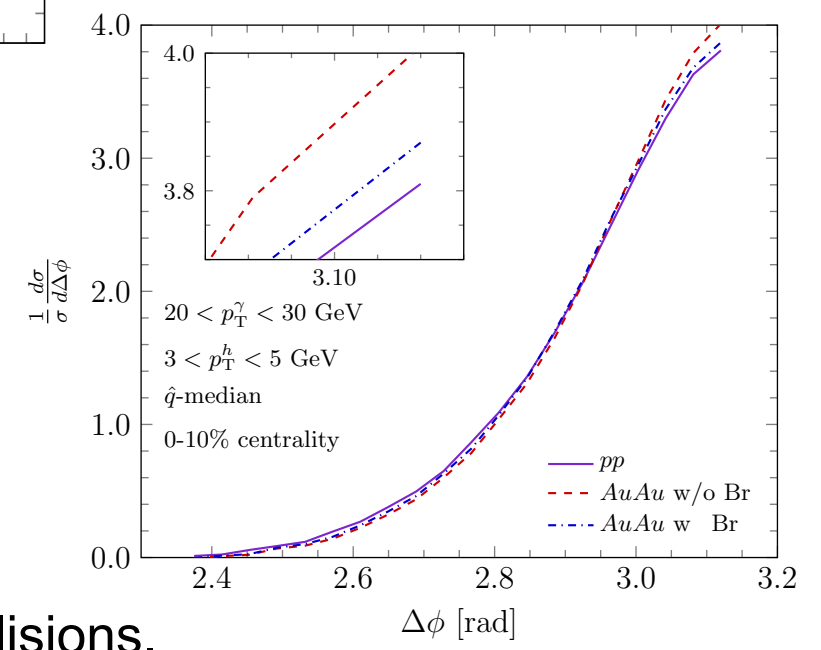
- The more larger the  $p_T$  is, the more stronger the angular correlation is from the Sudakov effects.



$p_T^a$  (weaker correlation)  $<$   $p_T^{a'}$  (stronger correlation)

Due to the bias of the same kinematics cuts between  $AA$  and  $pp$  collisions.

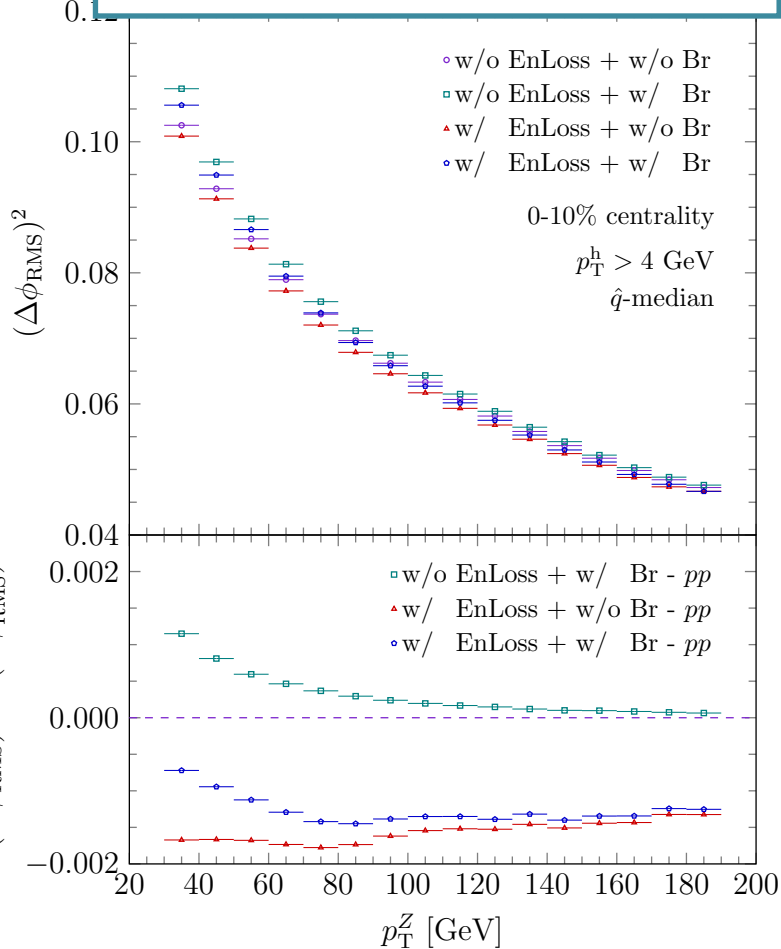
- $\Delta E$  makes the correlation stronger: Anti-broadening effect.
- $\langle p_\perp^2 \rangle$  makes a de-correlation stronger: Broadening effect.



# RMS width of $\Delta\phi$ distribution

- With or without  $\Delta E$
- With or without  $\langle p_{\perp}^2 \rangle$

*Pb + Pb -> Z + h @ 5.02 TeV*



- $\langle p_{\perp}^2 \rangle$ : broadening +
- $\Delta E$ : anti-broadening -

Competition results:

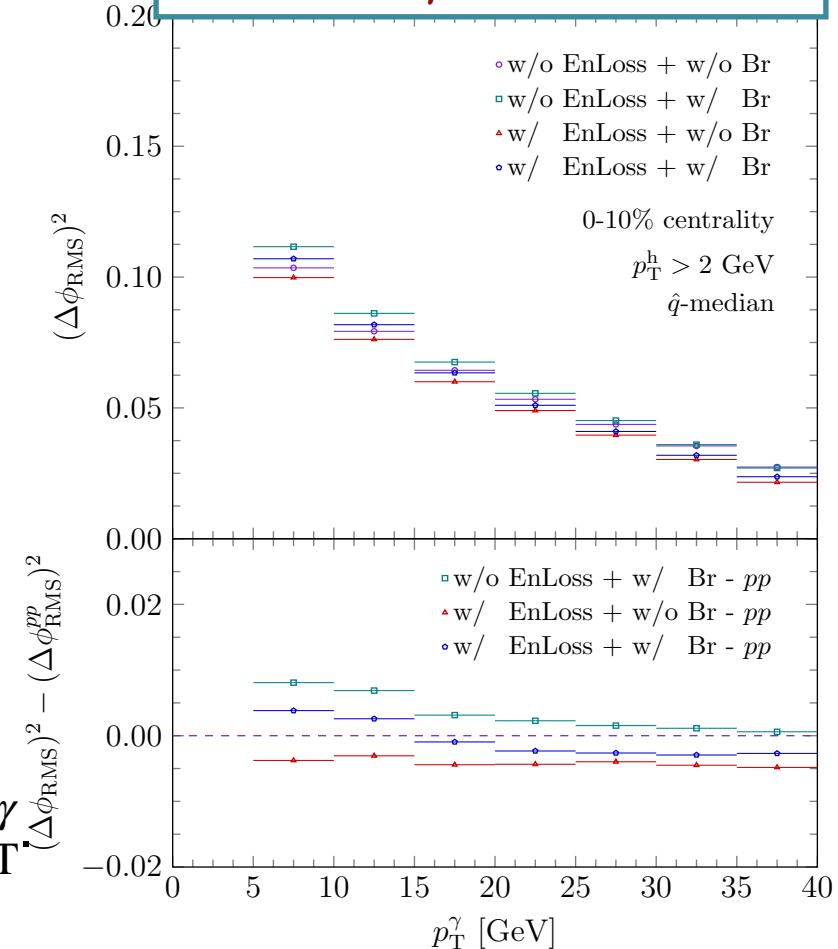
At the LHC

- “-”: correlation stronger;
- almost invisible.

At RHIC

- “+”: de-correlation for small  $p_T^{\gamma}$ ;
- “-”: correlation stronger for large  $p_T^{\gamma}$

*Au + Au -> γ + h @ 200 GeV*



At LHC, the negative effect of jet energy loss overwhelms the positive effect of the medium-induced broadening effect; therefore, the decorrelation of two-particle was not be observed;

At RHIC, their competition result precisely manifests the decorrelation of dihadron and hadron-jets.

# Summary

- ◉ We study the  $Z/\gamma$ -hadron production on  $p_T$  &  $\Delta\phi$  correlation using the Sudakov resummation improved pQCD parton model, including the HT  $\Delta E$  and medium-induced  $\langle p_{\perp}^2 \rangle$ -broadening effect.
- ◉ Our model can reproduce the  $Z/\gamma$ -hadron data on  $p_T$  &  $\Delta\phi$  distribution to a good degree.
- ◉  $\Delta E$  has an opposing anti-broadening effect compared to the  $\langle p_{\perp}^2 \rangle$ -broadening effect in the  $\Delta\phi$  distribution.
- ◉ At LHC, the negative effect of jet energy loss overwhelms the positive effect of the medium-induced broadening effect; therefore, the decorrelation of the two-particle was not observed. At RHIC, their competition result precisely manifests the decorrelation of dihadron and hadron-jets.

*Thanks for your attention!*