

Probing the nuclear structure with relativistic heavy ion collisions

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第十五届QCD相变与重离子碰撞研讨会

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12/18/2023

Landscape of nuclear physics

degrees of freedom

**quarks
& gluons**



quarks, gluons

Energy
(MeV)

940
neutron mass



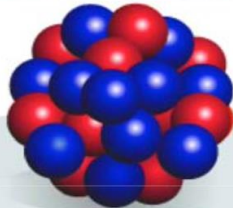
constituent quarks

**hadron
s**



baryons, mesons

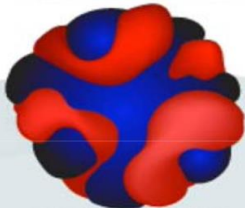
140
pion mass



protons, neutrons

8
proton separation
energy in lead

nuclei



nucleonic densities
and currents

1.32
vibrational
state in tin



collective coordinates

0.043
rotational
state in uranium

Landscape of nuclear physics

degrees of freedom

quarks & gluons



quarks, gluons

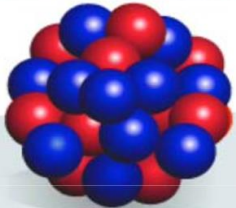


constituent quarks



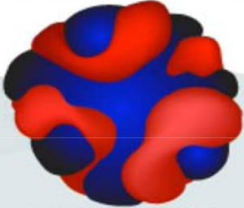
baryons, mesons

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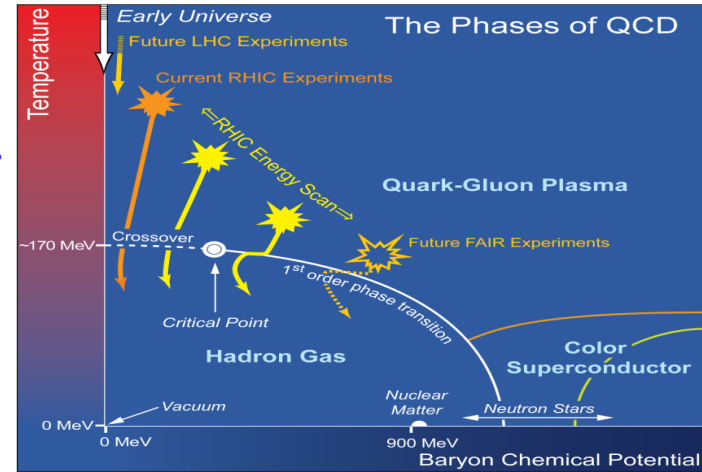
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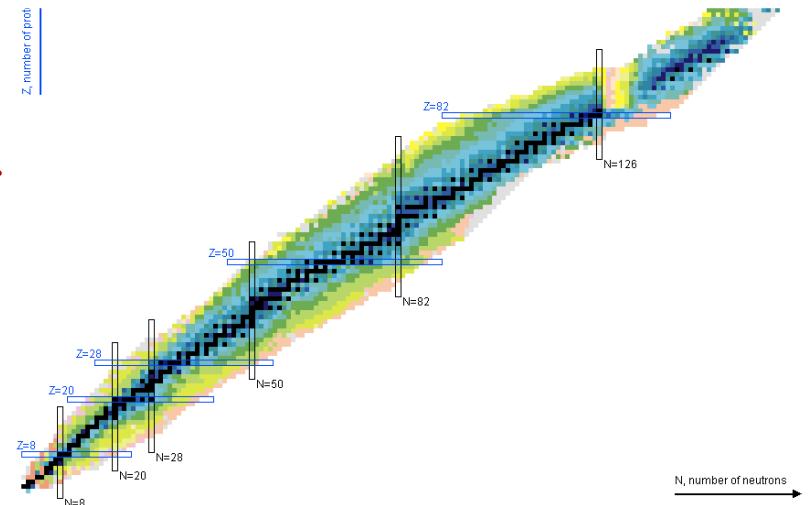
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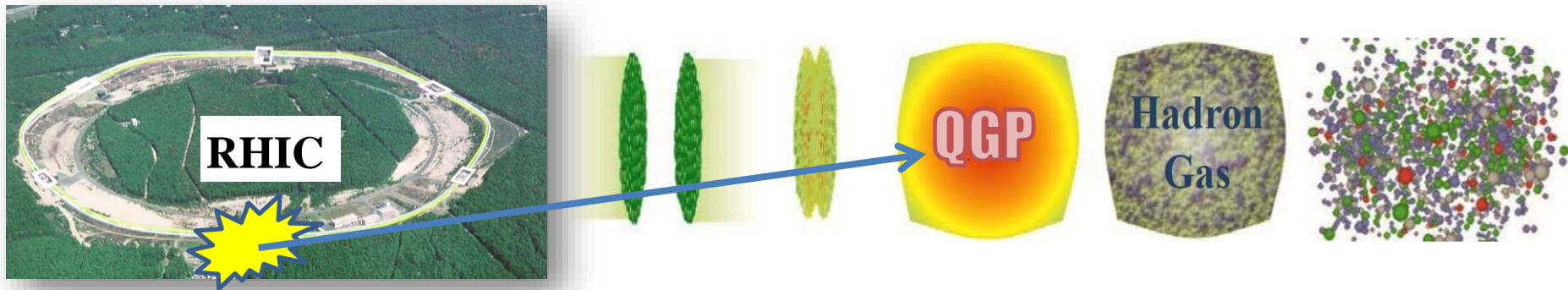
-intermediate and high energy nuclear physics



-nuclear structure

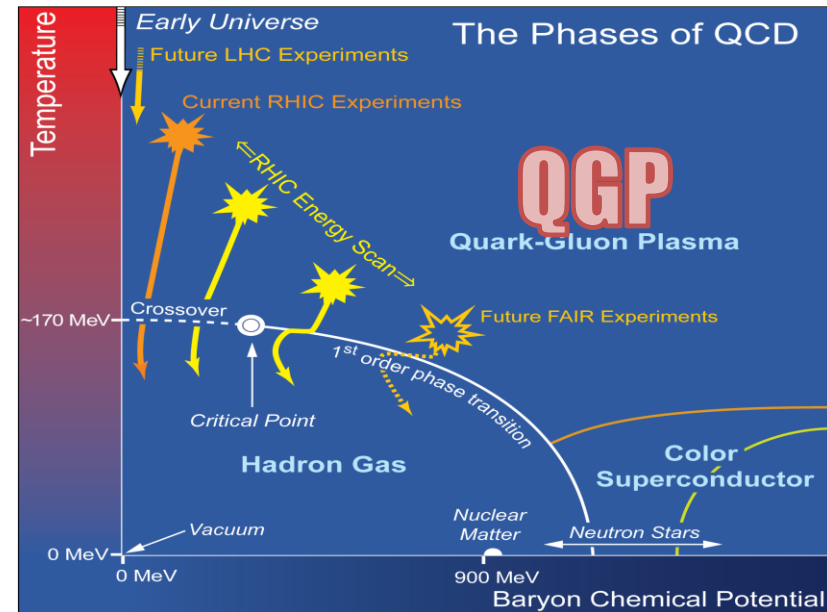


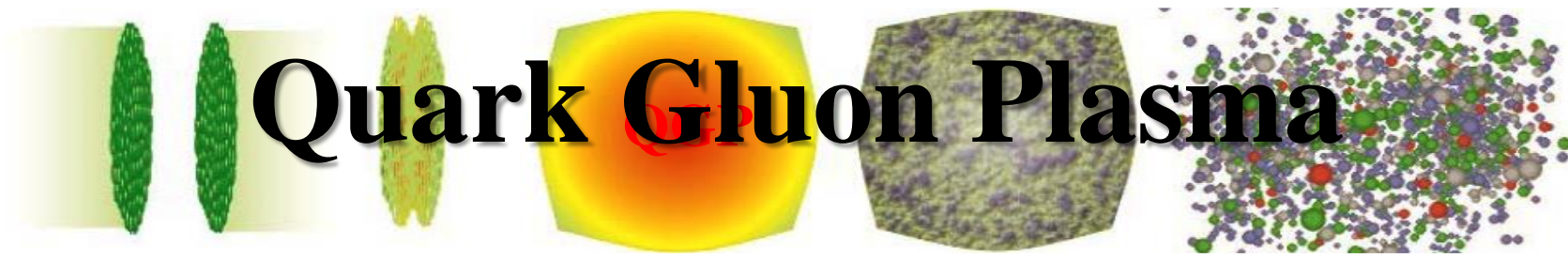
Relativistic Heavy Ion Collisions



Relativistic heavy ion collisions

- create and study QGP
- the QCD phase diagram
- the deconfinement & chiral phase transition
- the QCD vacuum





Quark Gluon Plasma

Hottest Matter on Earth

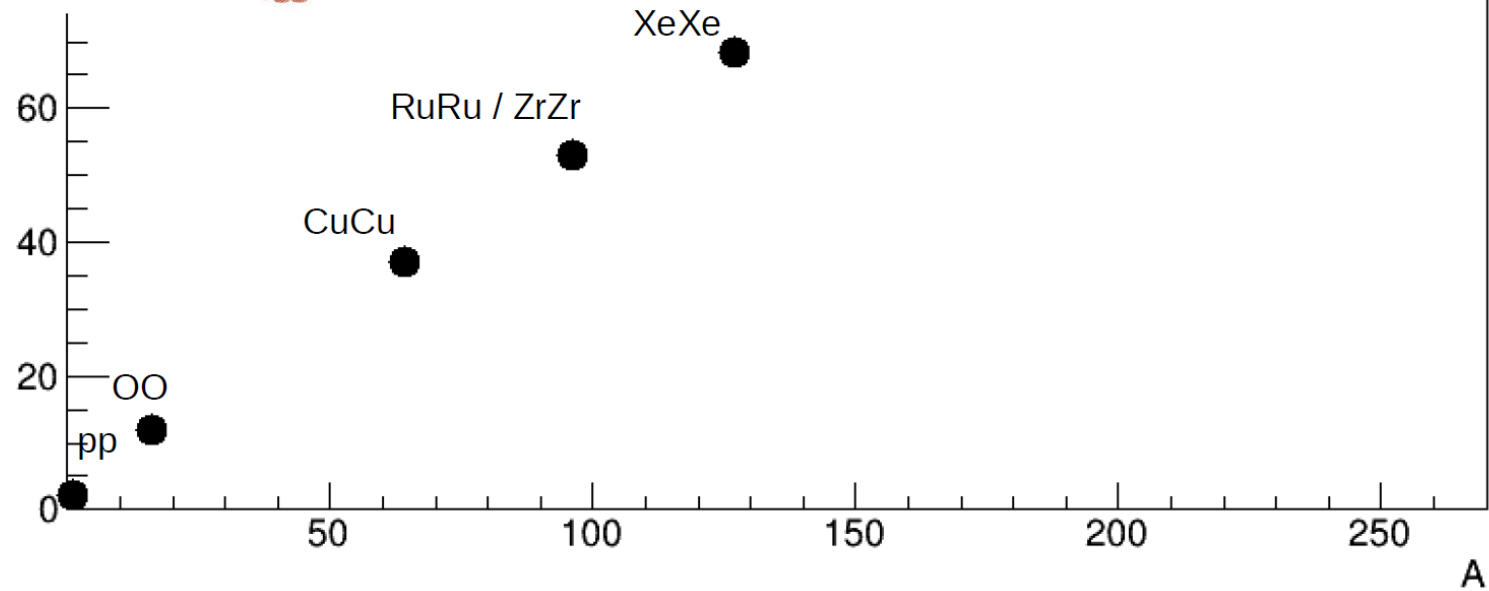
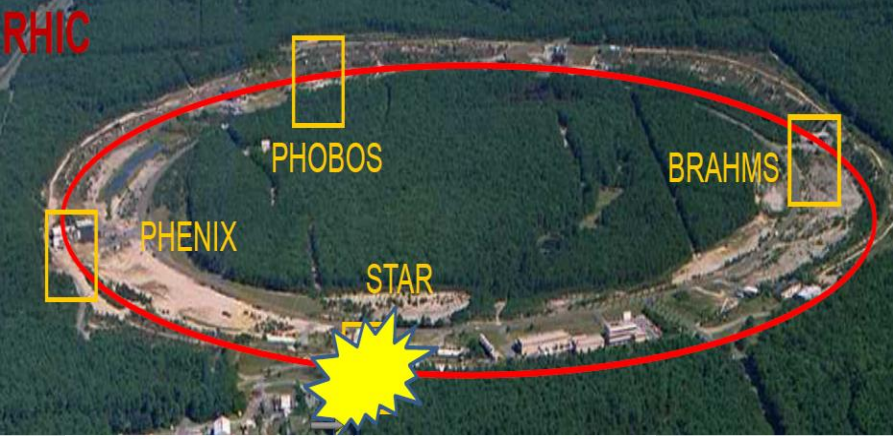


Most Perfect Liquid



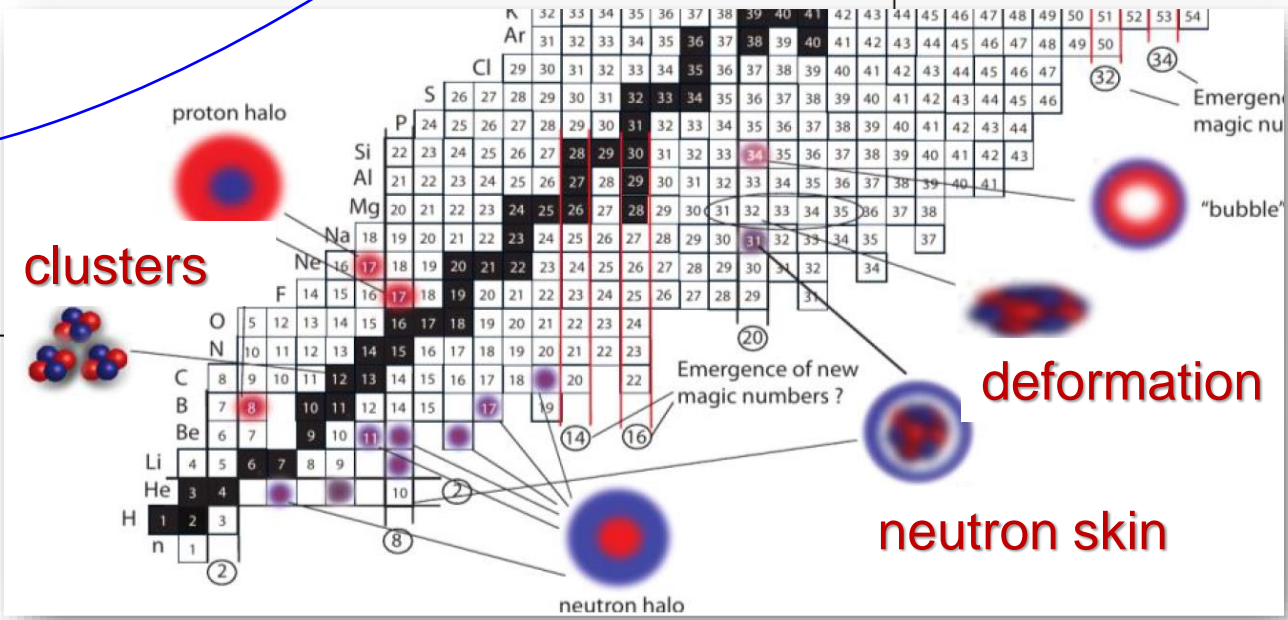
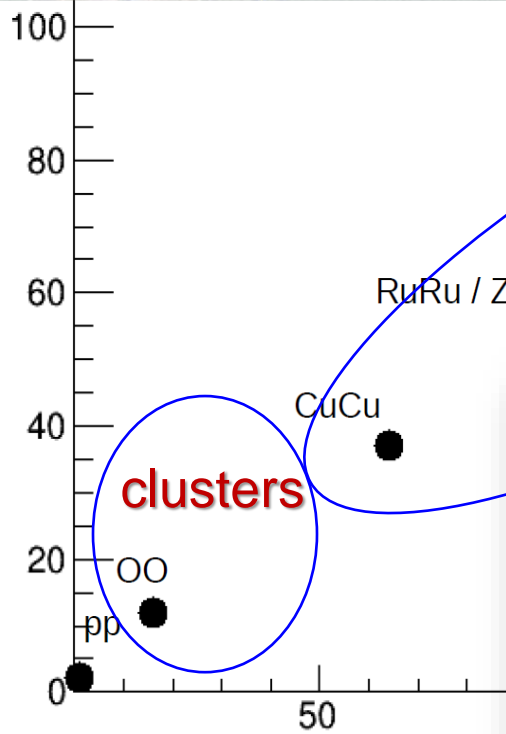
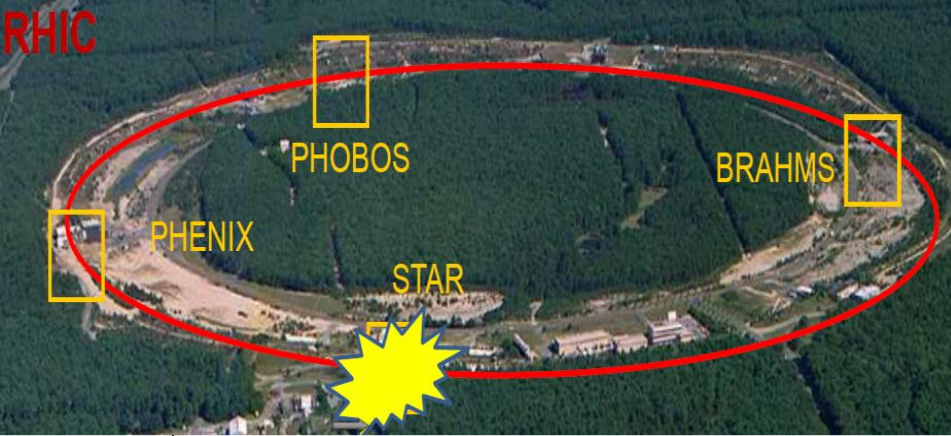
Most Vortical Fluid

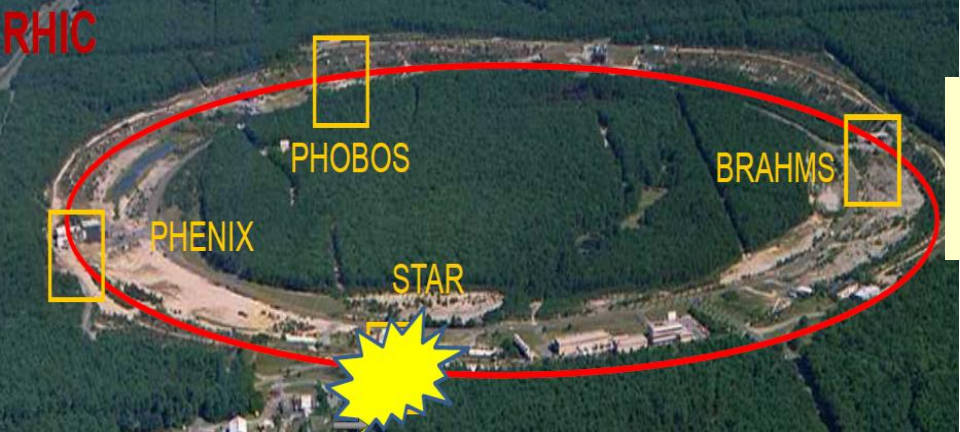
Rich A-A collisions at RHIC & the LHC



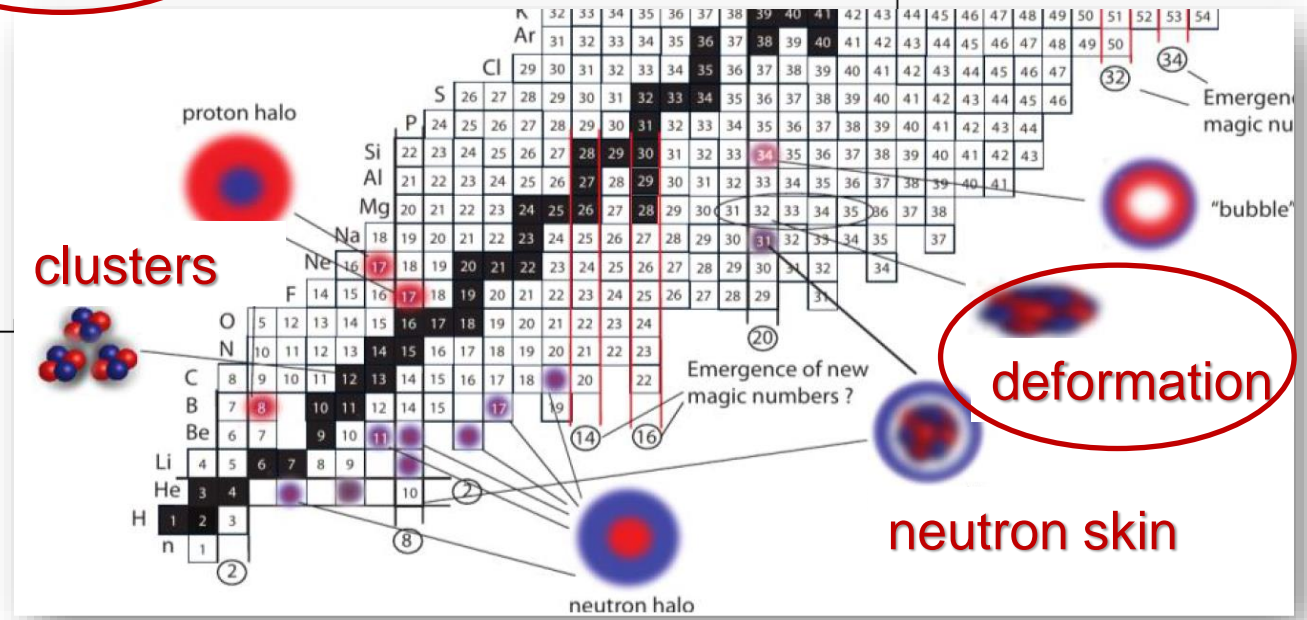
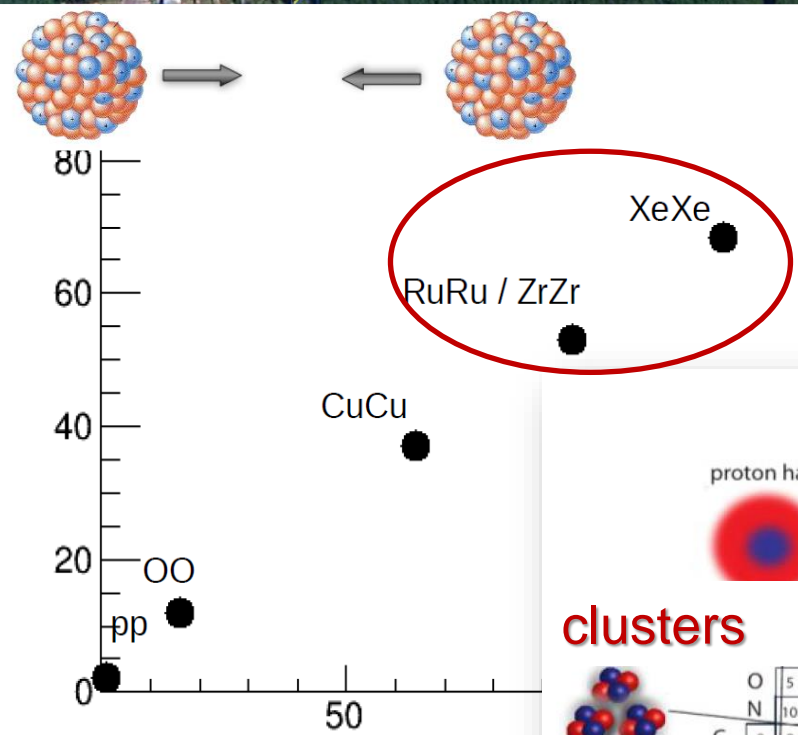
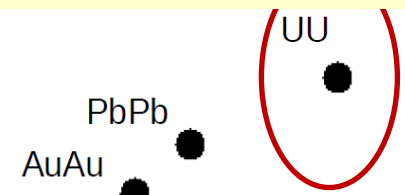
$^{197}\text{Au} + ^{197}\text{Au}$, $^{238}\text{U} + ^{238}\text{U}$, $^{208}\text{Pb} + ^{208}\text{Pb}$, $^{129}\text{Xe} + ^{129}\text{Xe}$, $^{96}\text{Zr} + ^{96}\text{Zr}$,
 $^{96}\text{Ru} + ^{96}\text{Ru}$, $^{64}\text{Cu} + ^{64}\text{Cu}$, $^{16}\text{O} + ^{16}\text{O}$, $p + ^{208}\text{Pb}$, $p + p$

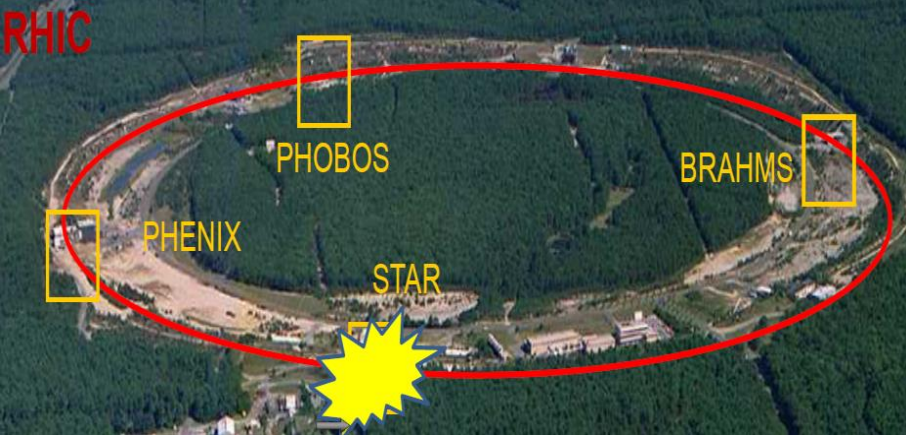
High energy nucleon nucleon collisions & nuclear structure





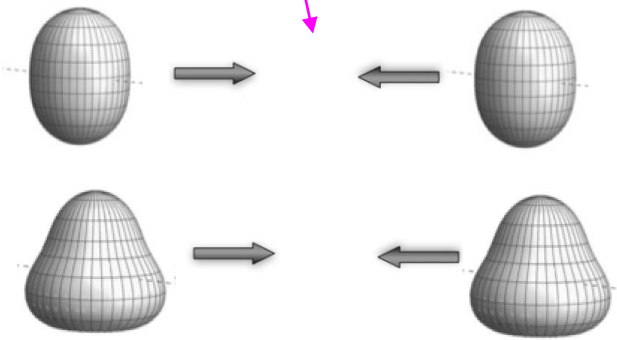
Probe the deformation of nuclei with relativistic heavy ion collisions



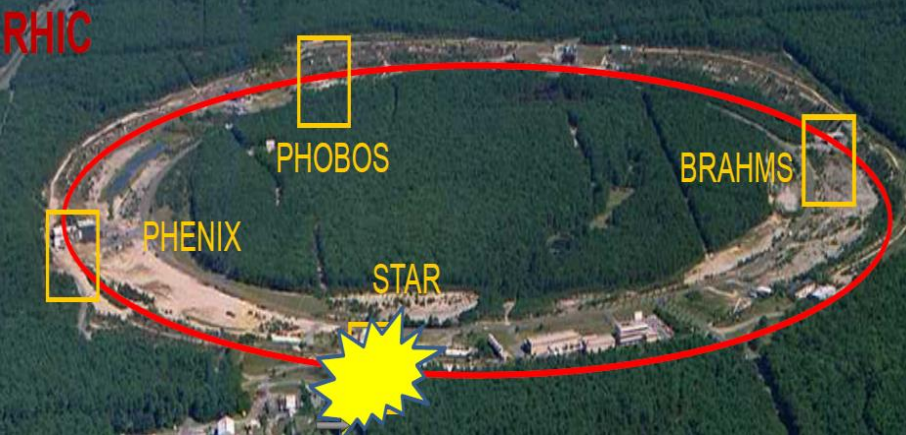


Probe the deformation of nuclei with relativistic heavy ion collisions

- Relativistic heavy collisions start from nuclei

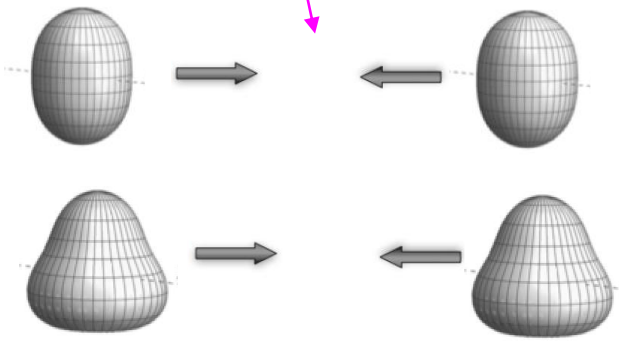


**initial conditions:
(with deformations)**

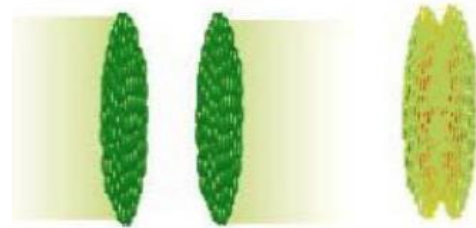


Probe the deformation of nuclei with relativistic heavy ion collisions

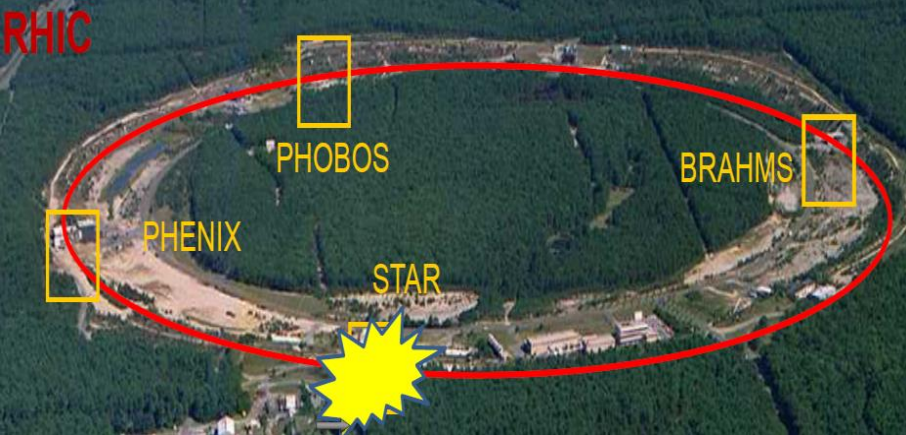
- Relativistic heavy collisions start from nuclei
- Collision time $< 10^{-24}$ s directly probe the ground state of nuclei



**initial conditions:
(with deformations)**

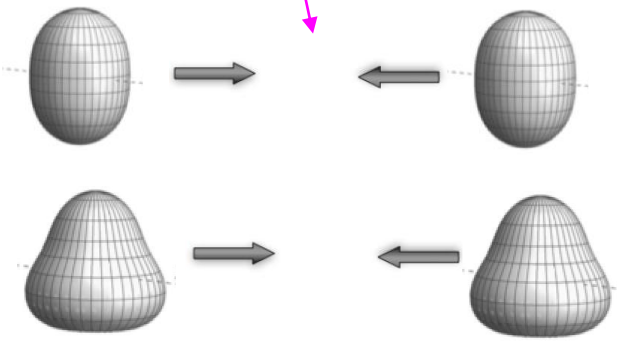


Collision time $< 10^{-24}$ s

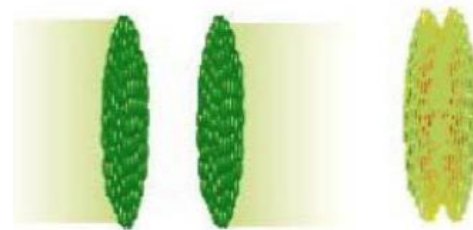


Probe the deformation of nuclei with relativistic heavy ion collisions

- Relativistic heavy collisions **start from nuclei**
- Collision time $< 10^{-24}$ s **directly probe the ground state of nuclei**

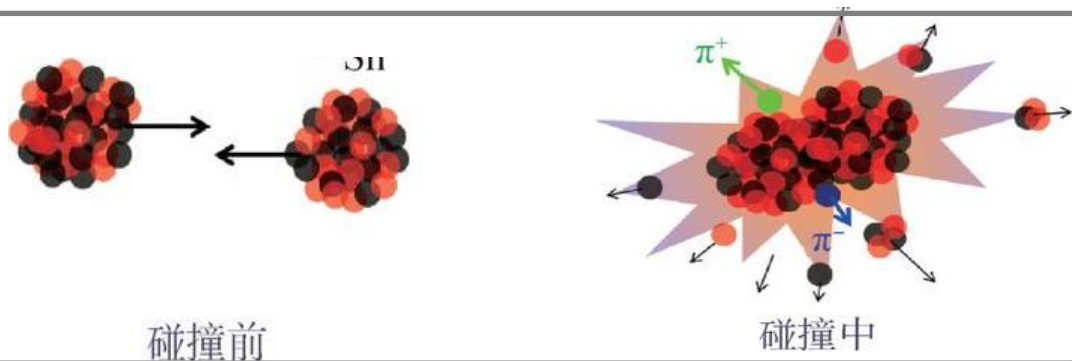


**initial conditions:
(with deformations)**



Collision time $< 10^{-24}$ s

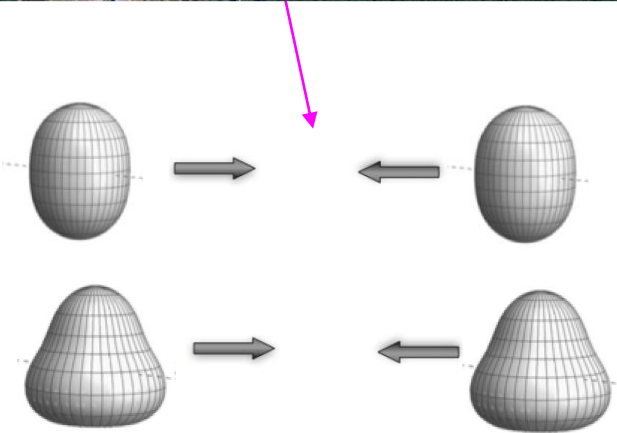
heavy ion collision at intermediate energies breaks up / excites nuclei during the collisions





Probe the deformation of nuclei with relativistic heavy ion collisions

- Relativistic heavy collisions **start from nuclei**
- Collision time $< 10^{-24}$ s directly **probe the ground state of nuclei**
- **Well calibrated calculations for QGP evolution**; to focus on the initial state



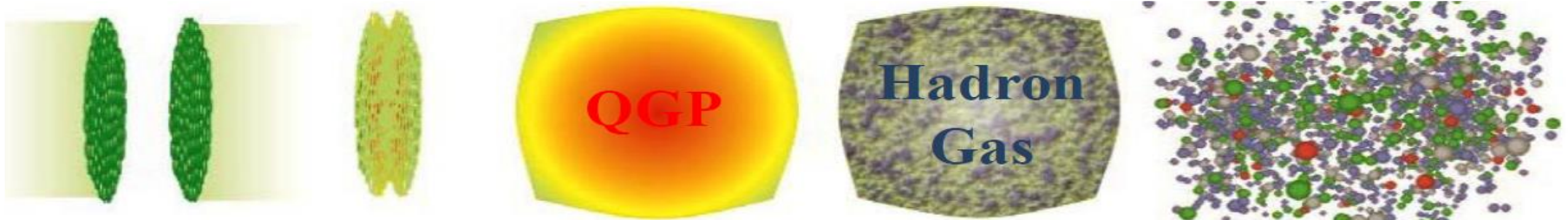
**initial conditions:
(with deformations)**

Well calibrated calculations

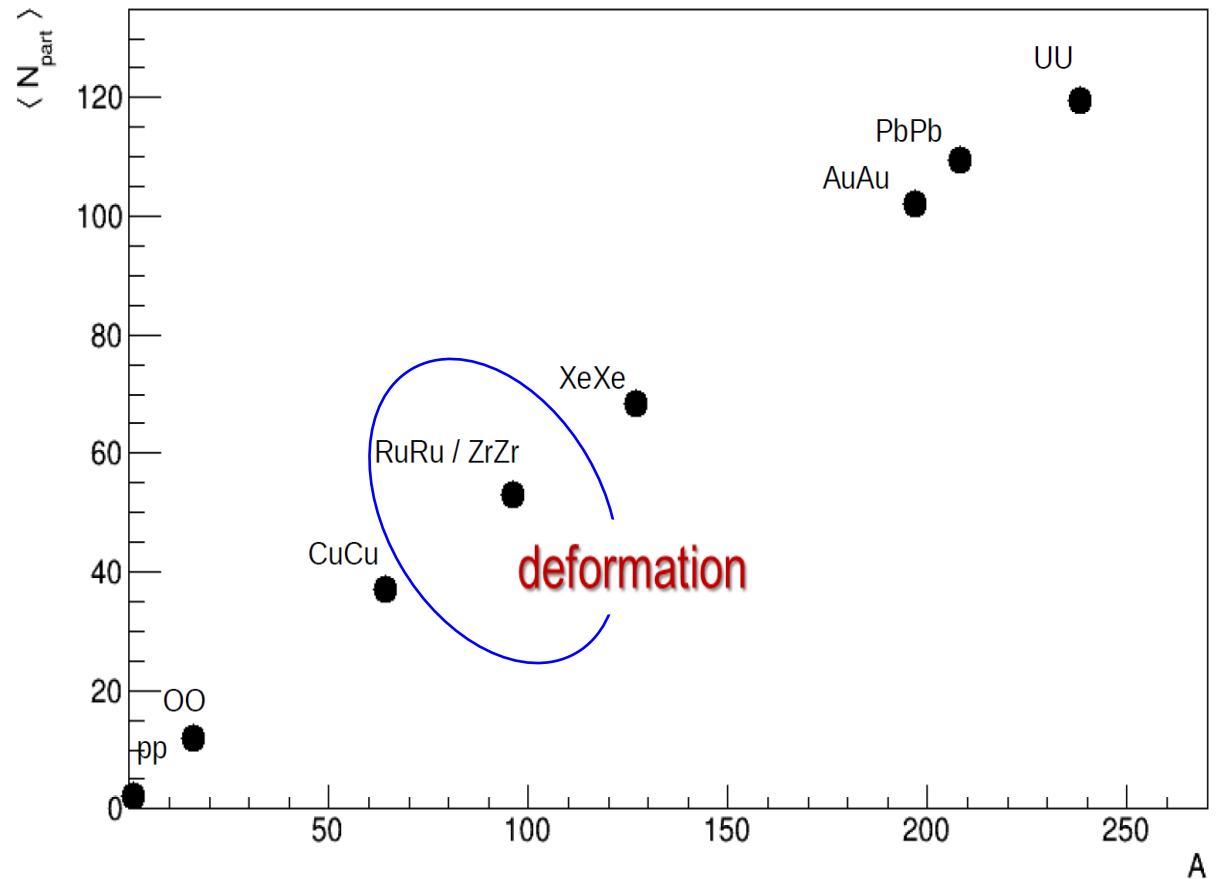
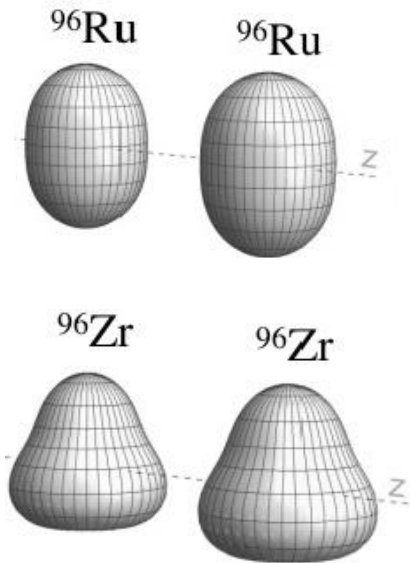
Initial conditions

viscous hydro

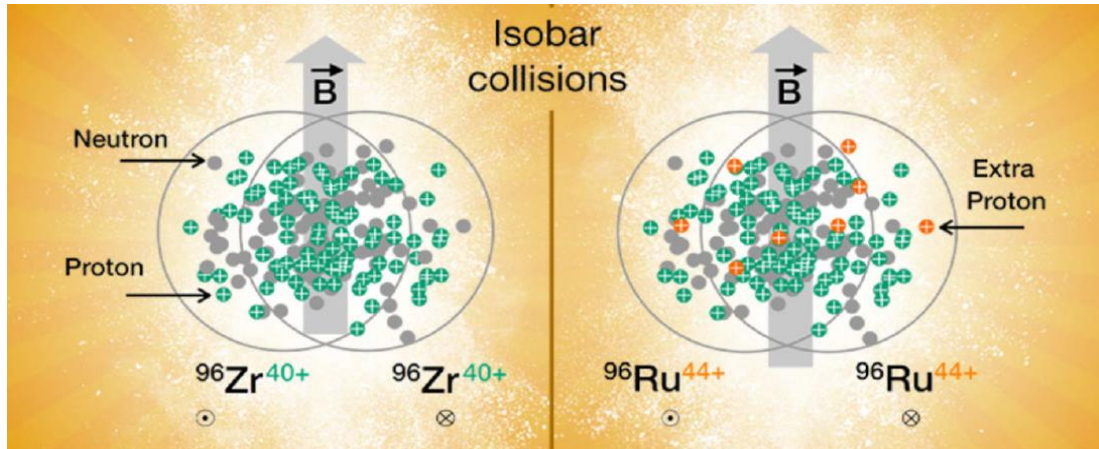
hadron cascade



Study the deformation of ^{96}Ru and ^{96}Zr at RHIC isobar run



$^{96}\text{Ru}+^{96}\text{Ru}$ and $^{96}\text{Zr}+^{96}\text{Zr}$ Collisions @ RHIC isobar run



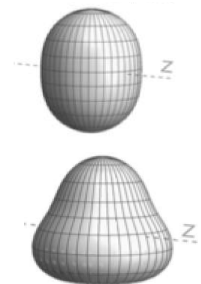
-to search the Chiral Magnetic Effect (CME)

-Obviously different early magnetic field for Ru+Ru and Zr+Zr collisions

Deformation of ^{96}Ru and ^{96}Zr

Conversion from $B(E_n)$ to β_n via: $\beta_2 = \frac{4\pi}{3ZR_2^2} \sqrt{\frac{B(E2)\uparrow}{e^2}}$, $\beta_3 = \frac{4\pi}{3ZR_0^3} \sqrt{\frac{B(E3)\uparrow}{e^2}}$

	β_2	$E_{2_1^+}$ (MeV)	β_3	$E_{3_1^-}$ (MeV)
^{96}Ru	0.154	0.83	-	3.08
^{96}Zr	0.062	1.75	0.202, 0.235, 0.27	1.90



ADNDT107,1 (2016) ADNDT80,35(2002)

Model calculation for Nuclear Deformation

General approach (DFT level)

Non-relativistic Schrodinger equation:
Skyrme and Gogny DFT

Relativistic Dirac equation:
covariant DFT (CDFT)

Range of interaction

Zero range - point coupling models
in CDFT (no mesons)
- Skyrme DFT

Finite range - meson exchange models
in CDFT
- Gogny DFT

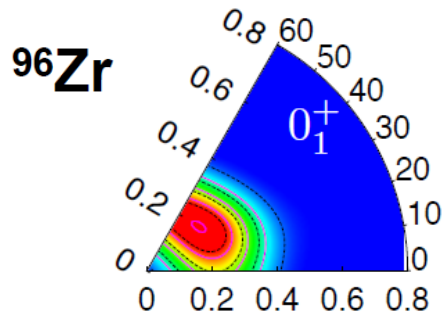
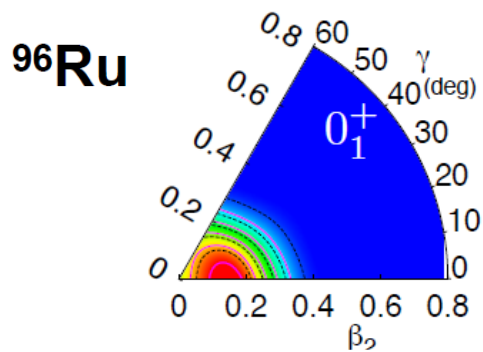
Effective density dependence

CDFT :

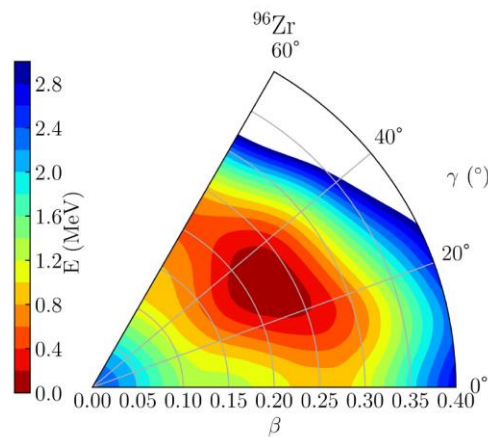
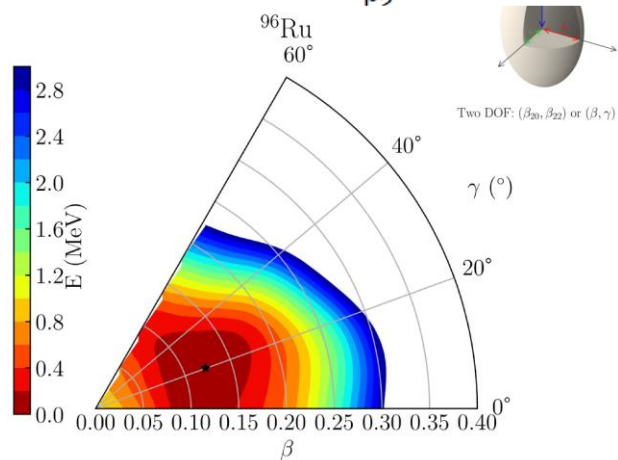
- explicit (DD-ME2, DD-PC1)
- non-linear (through the powers of mesons) (NL1, NL3*)

Skyrme and Gogny DFTs: different prescriptions for density dependence

Deformation of ^{96}Ru & ^{96}Zr – DFT calculations

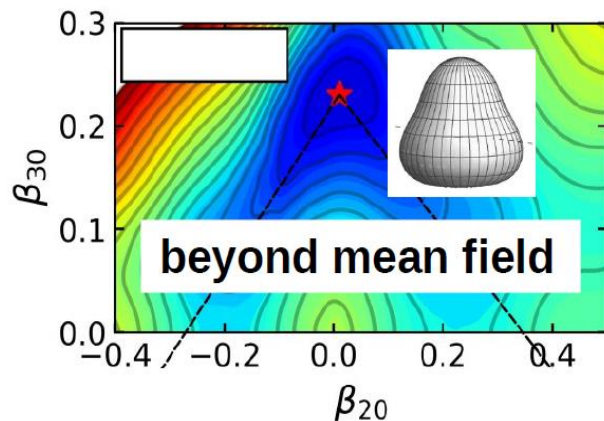
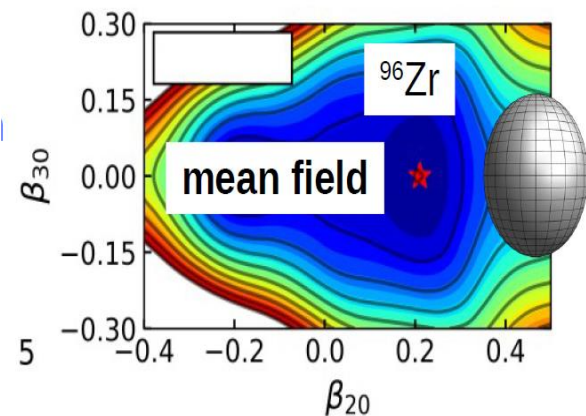


Gogny energy density functional |(Tiaxial) T R.
Rodríguez EMMI RRTF 2022



Skyrme EDF (with rotational correction)

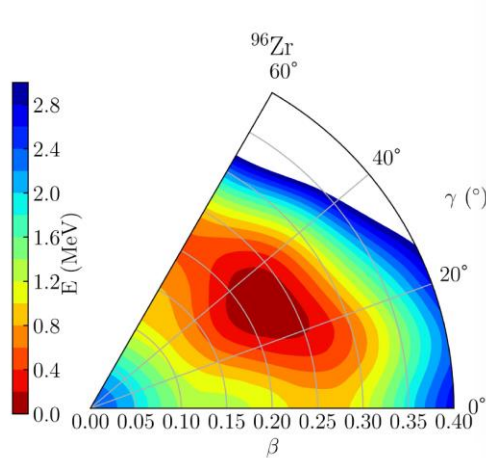
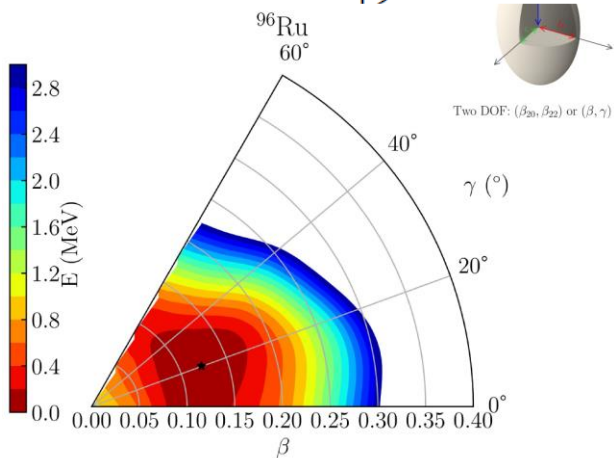
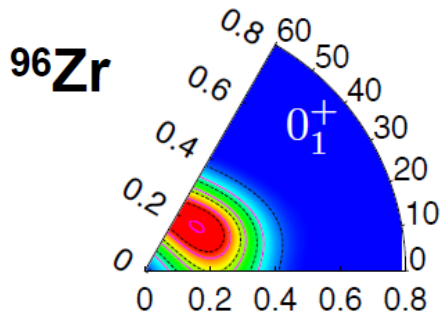
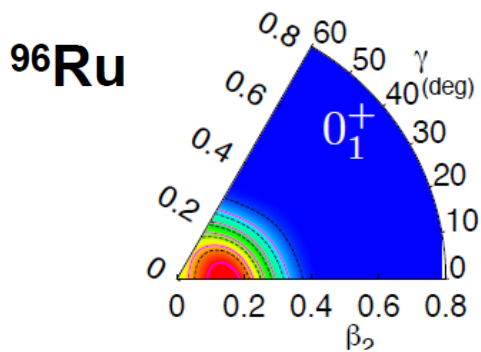
W Ryssens EMMI RRTF 2022



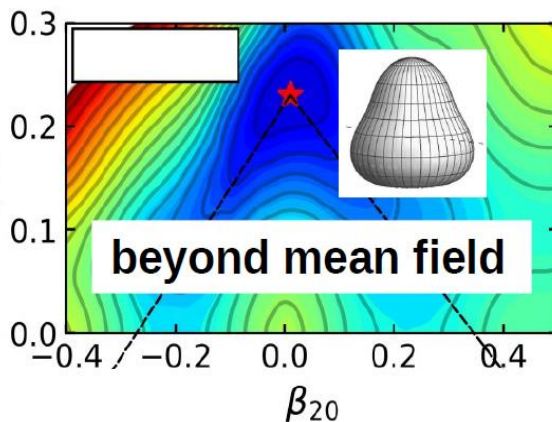
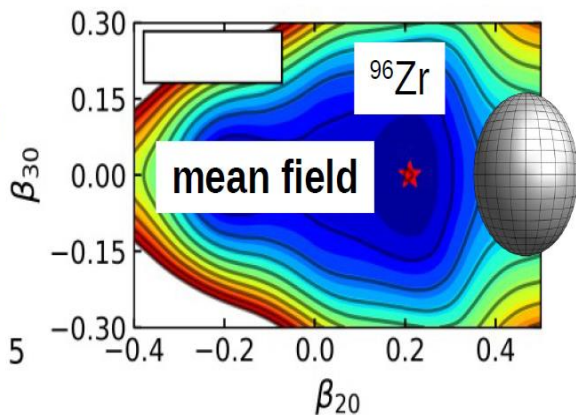
Beyond-mean-field correction is very important

Rong, Lu, arXiv:2201.02114

Deformation of ^{96}Ru & ^{96}Zr – personal comments

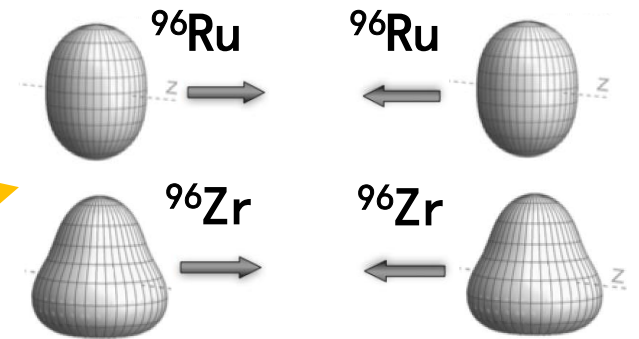
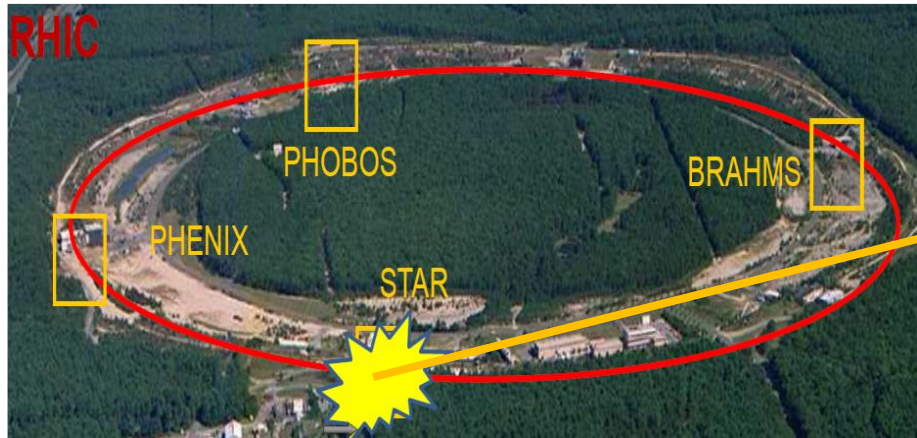


18^+	8205.7	15^-	6754.1
16^+	6441.6	14^+	5680.7
13^-	5750.2	12^+	4418.3
11^-	4798.7	10^+	3817.2
9^-	3951.1	8^+	2950.4
7^-	3291.5	6^+	2149.7
5^-	2588.4	4^+	1518.1
		2^+	832.6
		0^+	0.0



Nuclear structure physics obtain the deformation information from the spectrum with certain model calculations (not directly image the deformation in position space)

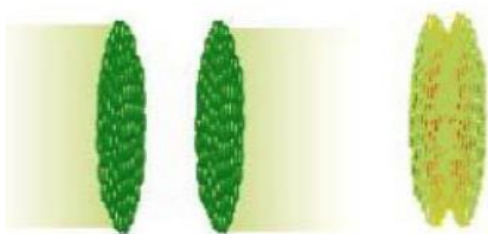
Probe the deformation (mass distributions) of ^{96}Ru & ^{96}Zr with isobar collisions



**initial conditions:
(deformation / mass distributions)**

Well calibrated calculations

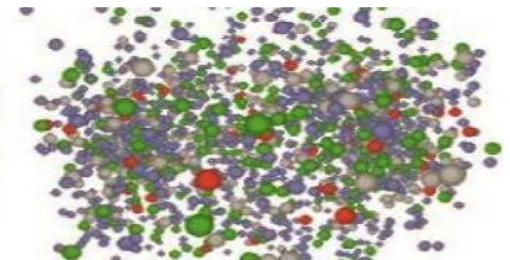
Initial conditions



viscous hydro



hadron cascade



Hydrodynamic calculation with initially deformed nuclei

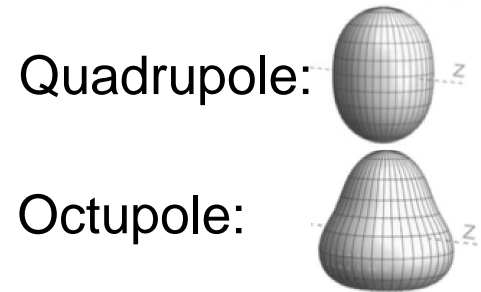
Initial conditions (TRENTO)

-Sample nucleon position in deformed nuclei with:

$$\rho(r, \theta, \phi) = \frac{\rho_0}{1 + e^{(r-R(\theta, \phi))/a_0}}$$

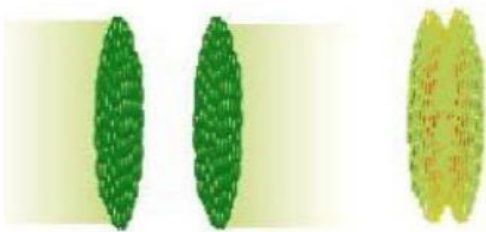
$$R(\theta, \phi) = R_0 \left(1 + \beta_2 [\cos \gamma Y_{2,0} + \sin \gamma Y_{2,2}] \right.$$

$$\left. + \beta_3 \sum_{m=-3}^3 \alpha_{3,m} Y_{3,m} + \beta_4 \sum_{m=-4}^4 \alpha_{4,m} Y_{4,m} \right)$$



Well calibrated calculations

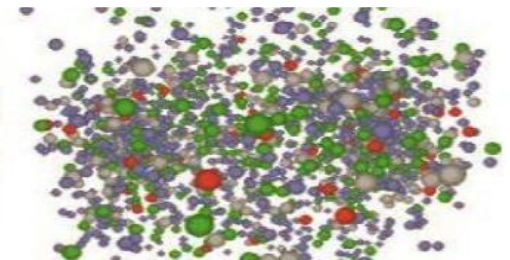
Initial conditions



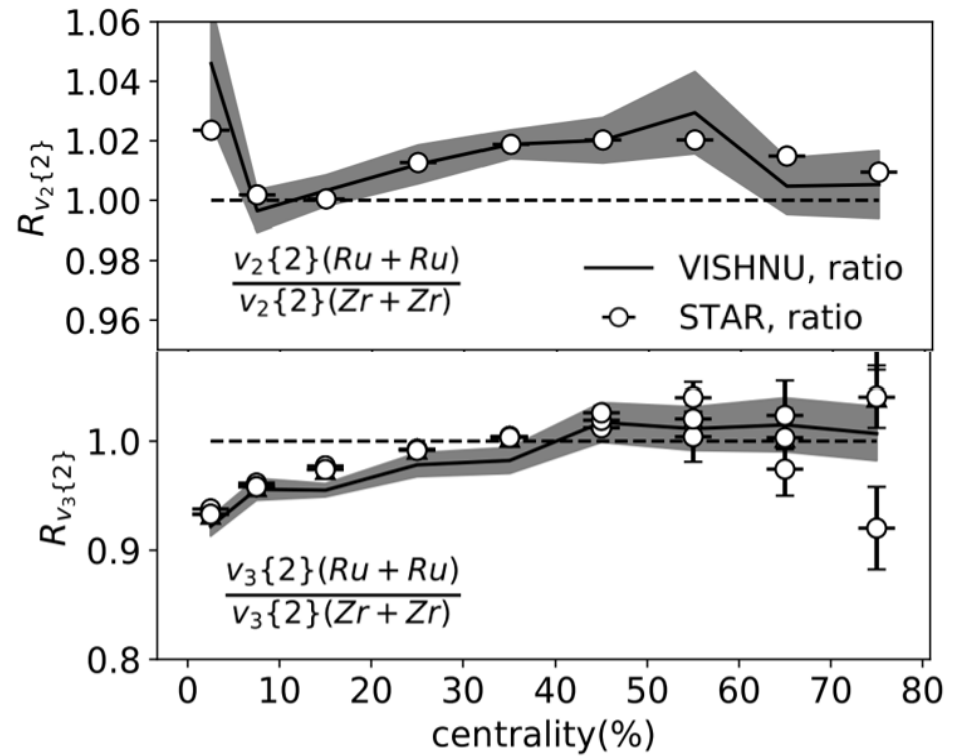
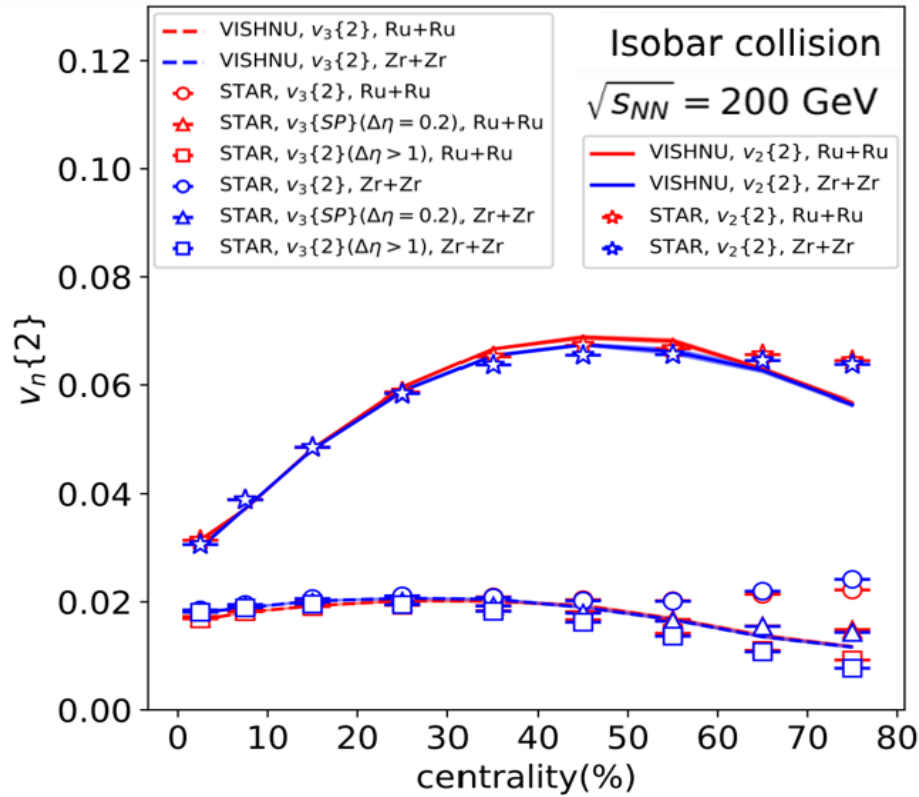
viscous hydro



hadron cascade



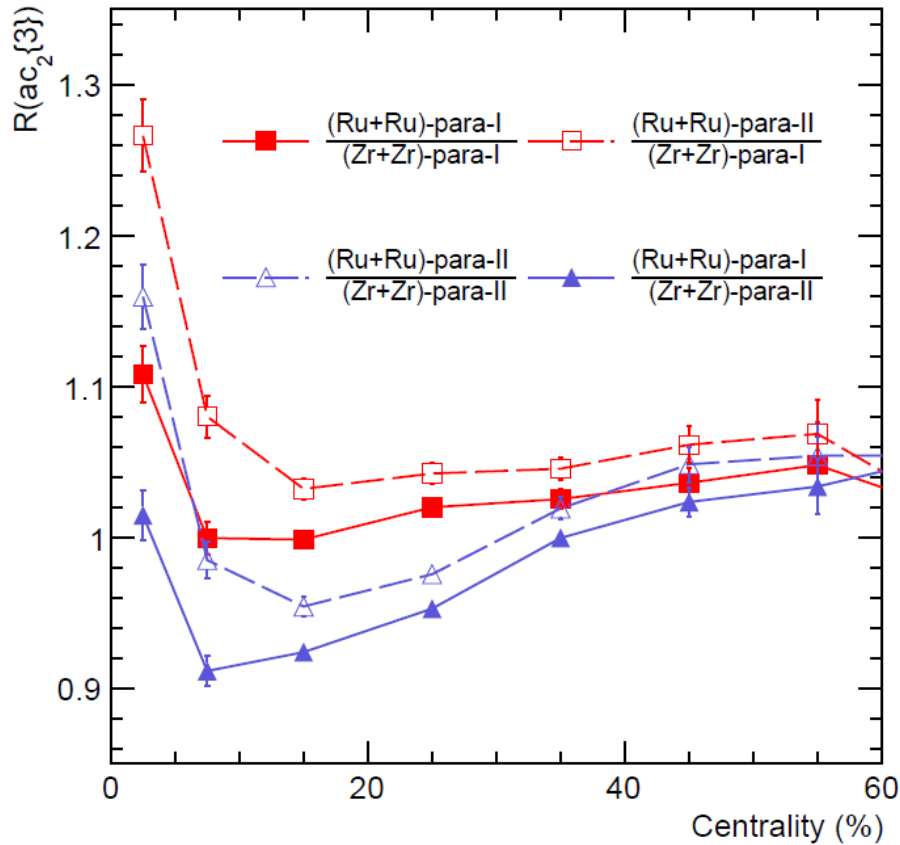
V_2 and V_3 for Ru+Ru and Zr+Zr collisions



- With fine tuning parameters, iEBE-VISHNU fits V_2 & V_3 for Ru+Ru collisions
- Using β_2 β_3 in table1, it “predicts” V_2 & V_3 for Zr+Zr collisions & the related ratio -- (the data are roughly described).

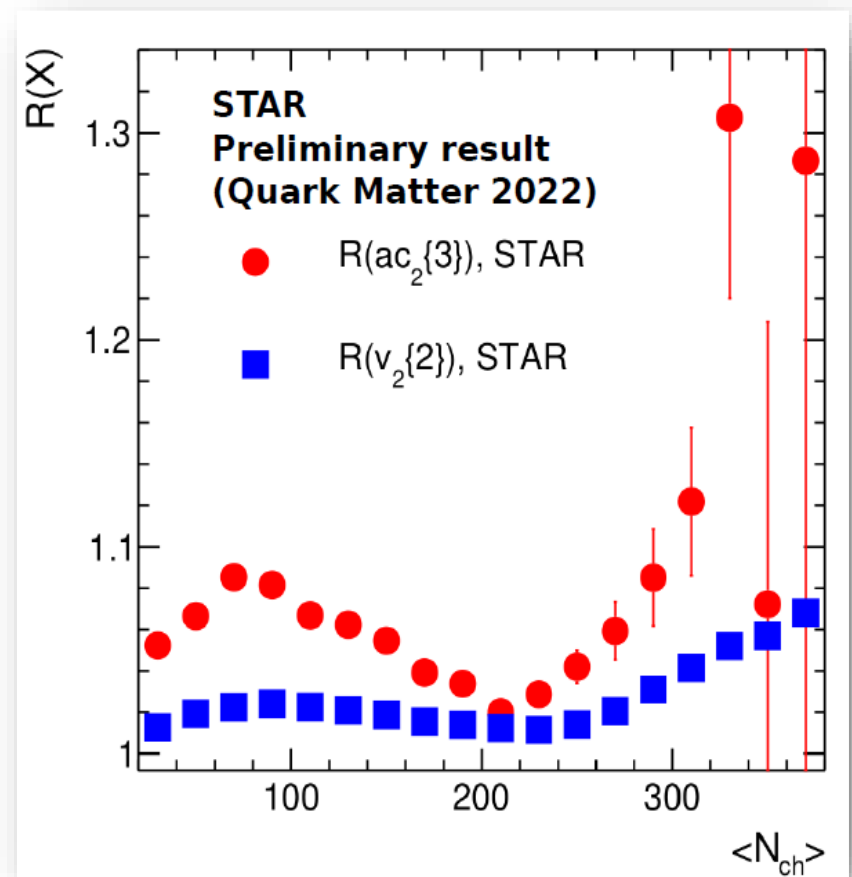
“standard”	Ru	Zr
a_0	0.46	0.52
β_2	0.162	0.060
β_3	0.00	0.200

ac_3 for Ru+Ru and Zr+Zr collisions



ac_3 is sensitive to quadrupole and octupole deformations

$$ac_2\{3\} = \langle v_2^2 v_4 \cos 4(\Phi_2 - \Phi_4) \rangle,$$



Probe the deformation of ^{96}Ru and ^{96}Zr

-- a short summary

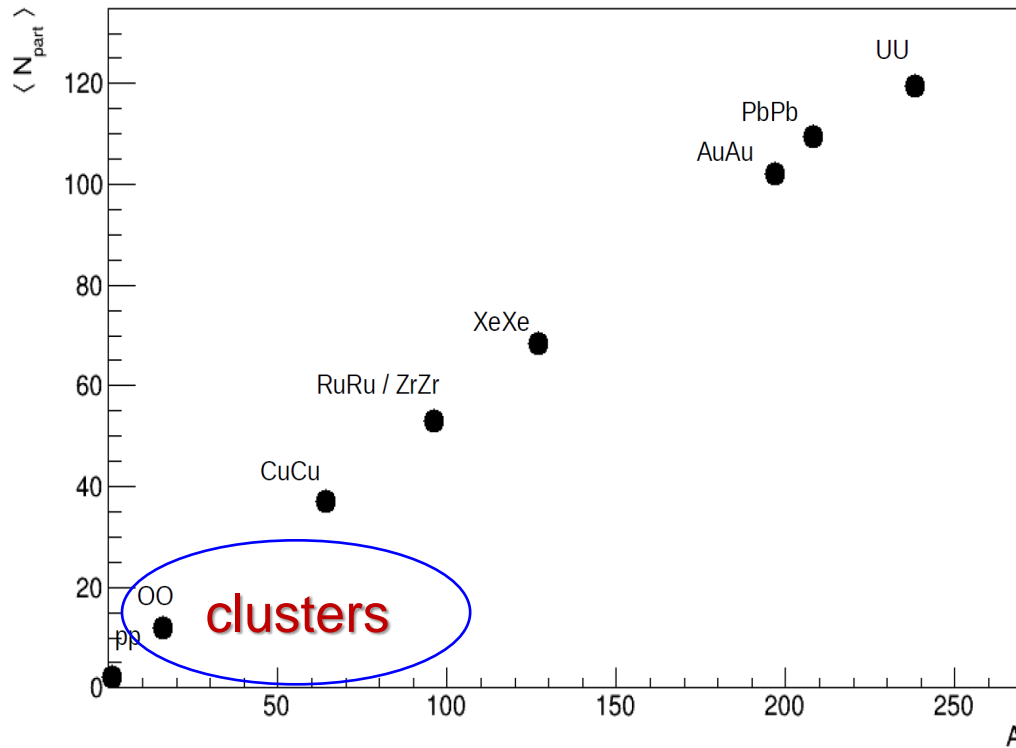


- ^{96}Ru and ^{96}Zr : two ideal nuclei for interdisciplinary research between relativistic heavy ion physics and nuclear structure

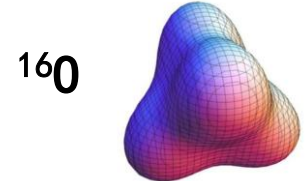
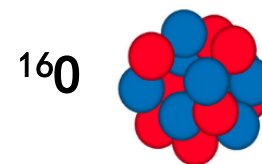
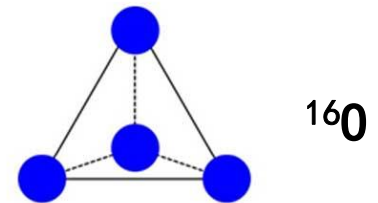
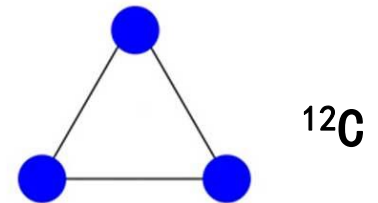
-isobar collisions provide rich and high statistical run data for various flow analysis, which could constrain the deformation of ^{96}Ru and ^{96}Zr from heavy ion physics side

-Need more efforts to study the deformation of ^{96}Ru & ^{96}Zr from both experimental and theoretical sides in nuclear structure

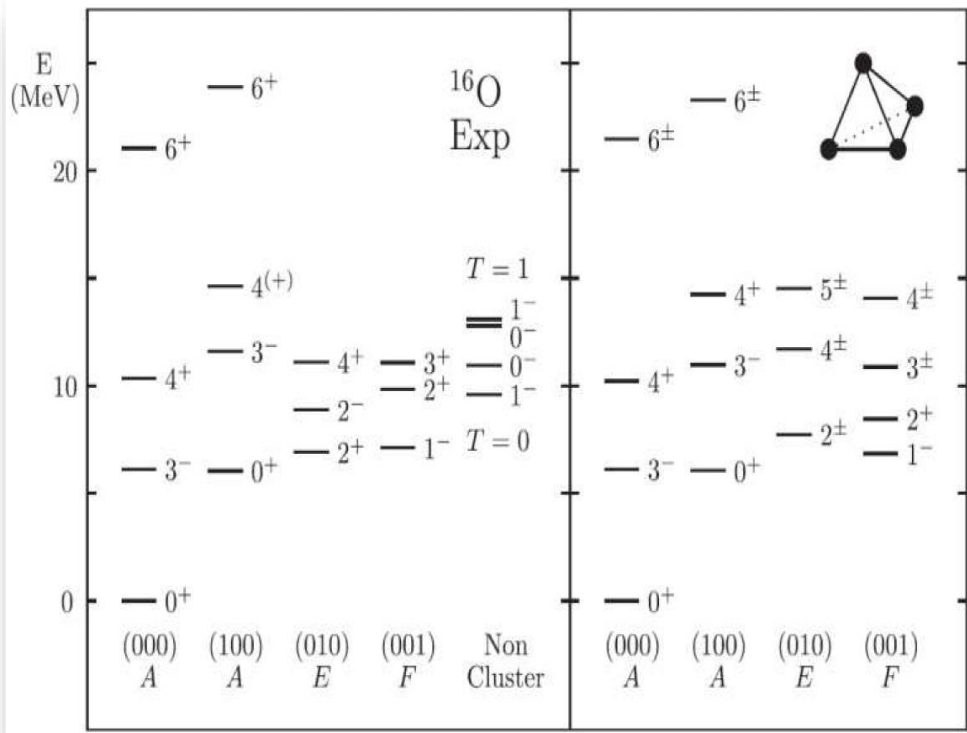
Probe the α -cluster of ^{16}O at RHIC and the LHC



$^{16}\text{O}+^{16}\text{O}$ collisions and $p+^{16}\text{O}$ collisions originally aim to study the possible formation of the QGP in small systems



α -cluster of ^{16}O from nuclear structure

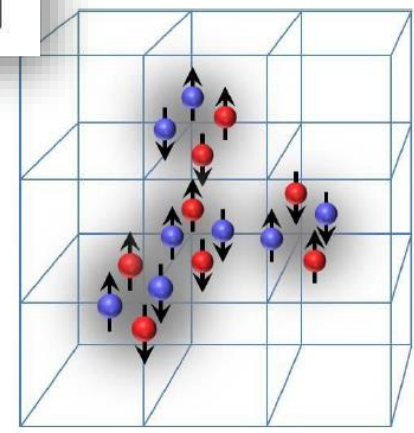


-ACM calculations show that the low-lying states of ^{16}O can be described as rotation-vibration of a 4α cluster with tetrahedral symmetry.

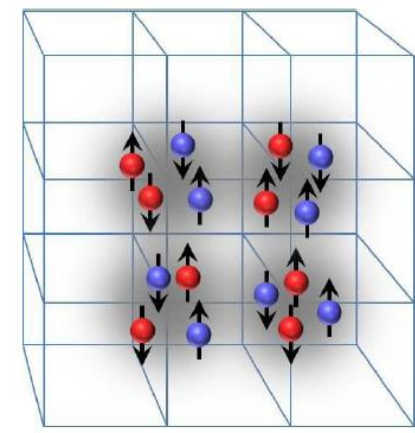
R.Bijker and F.Iachello, Phys. Rev. Lett. 112, no.15, 152501 (2014)

-ab initio lattice calculations demonstrate the nucleons are arranged in a tetrahedral alpha clusters in the ground state

E.~Epelbaum, et al Phys. Rev. Lett.112, no.10, 102501 (2014)



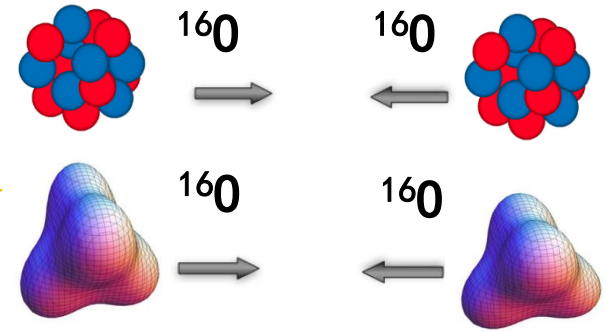
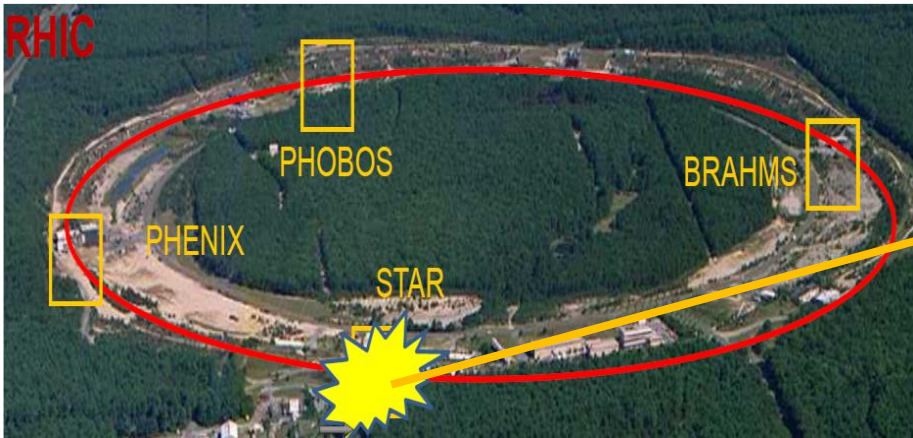
(a) Initial state "A", 8 equivalent orientations.



(b) Initial states "B" and "C", 3 equivalent orientations.

Nuclear structure physics infer the α -cluster configuration of ^{16}O from the measured spectrum

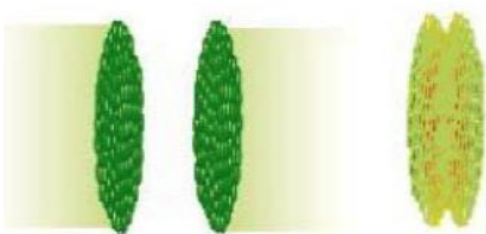
Relativistic heavy ion collision to probe the structure of ^{16}O



initial conditions:
(with or without α -
cluster)

Well calibrated calculations

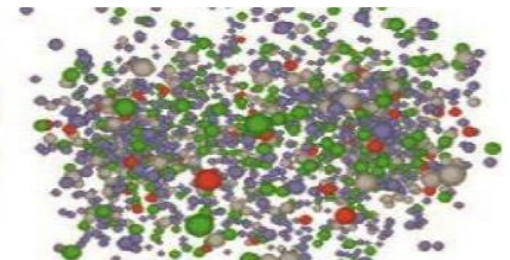
Initial conditions



viscous hydro



hadron cascade

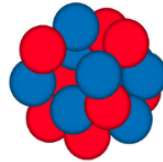


Hydrodynamic calculation w/wo clustering

Initial conditions (TRENTO)

-Woods-Saxon:

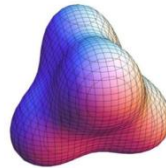
$$\rho(r, \theta, \phi) = \frac{\rho_0}{1 + e^{(r-R(\theta, \phi))/a_0}}$$



Spherical shape

-Alpha-Cluster:

$$f_i(\mathbf{r}) = A \exp \left[-\frac{3(\mathbf{r} - \mathbf{r}_i)^2}{2r_\alpha^2} \right]$$

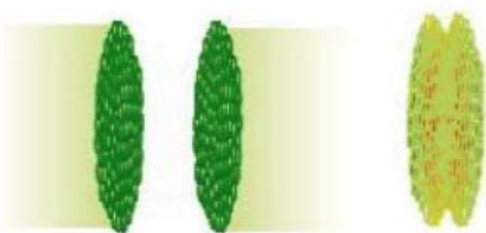


tetrahedral alpha clusters

	distribution	l	r_α
I	Woods-Saxon		
II	alpha cluster	2.8	2.0
III	alpha cluster	3.2	1.1
IV	alpha cluster	3.42	1.1

Well calibrated calculations

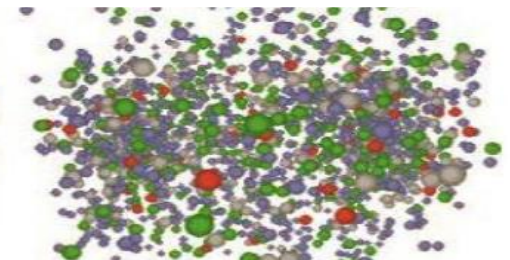
Initial conditions



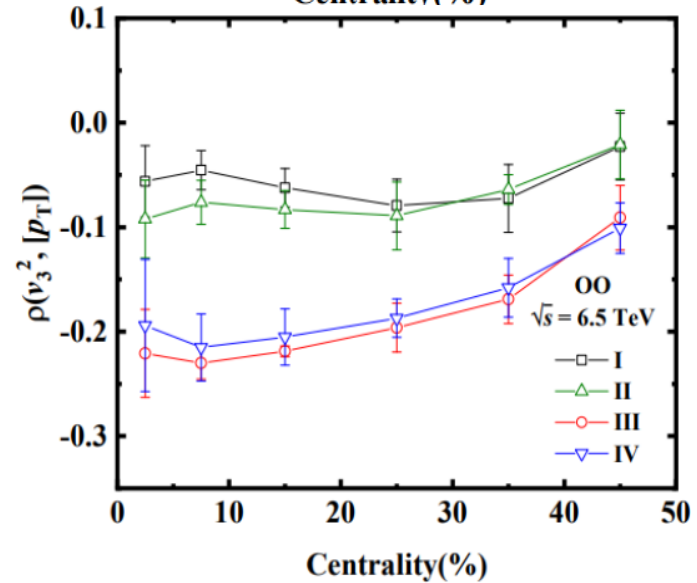
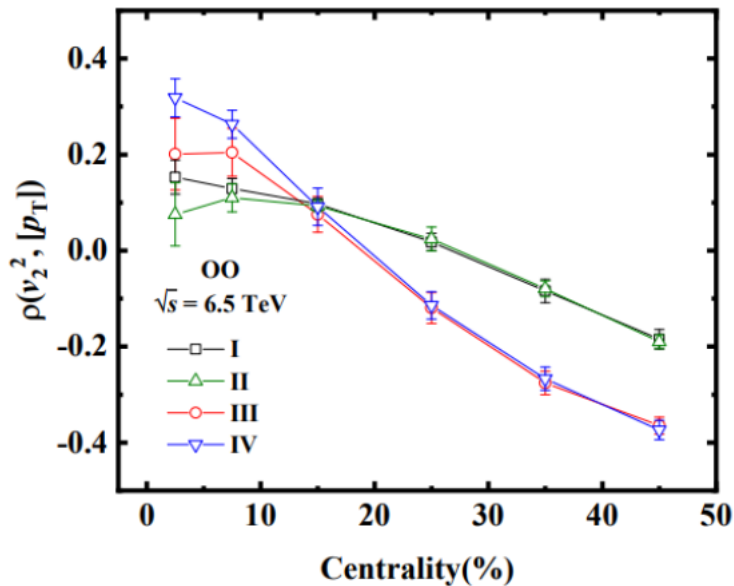
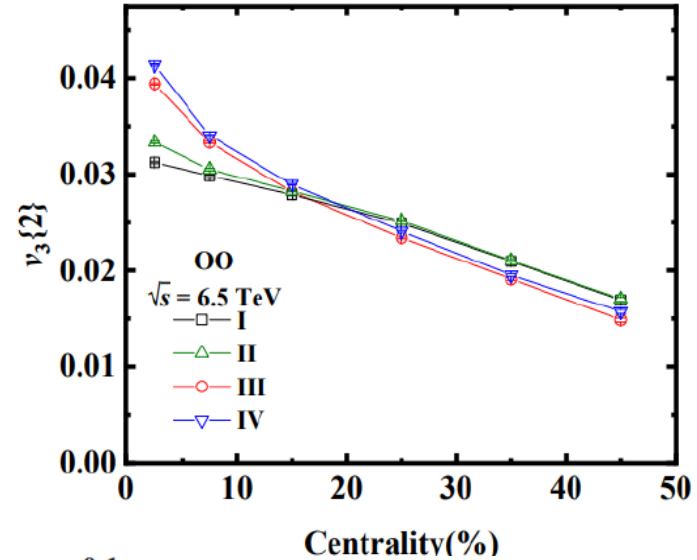
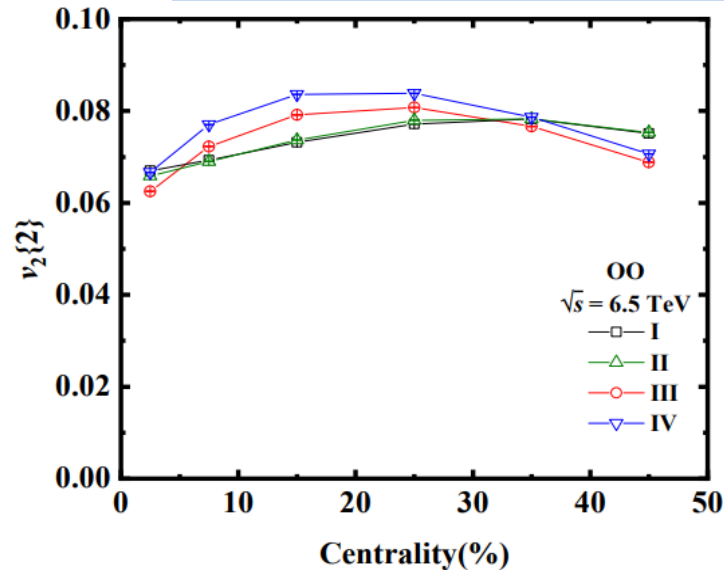
viscous hydro



hadron cascade

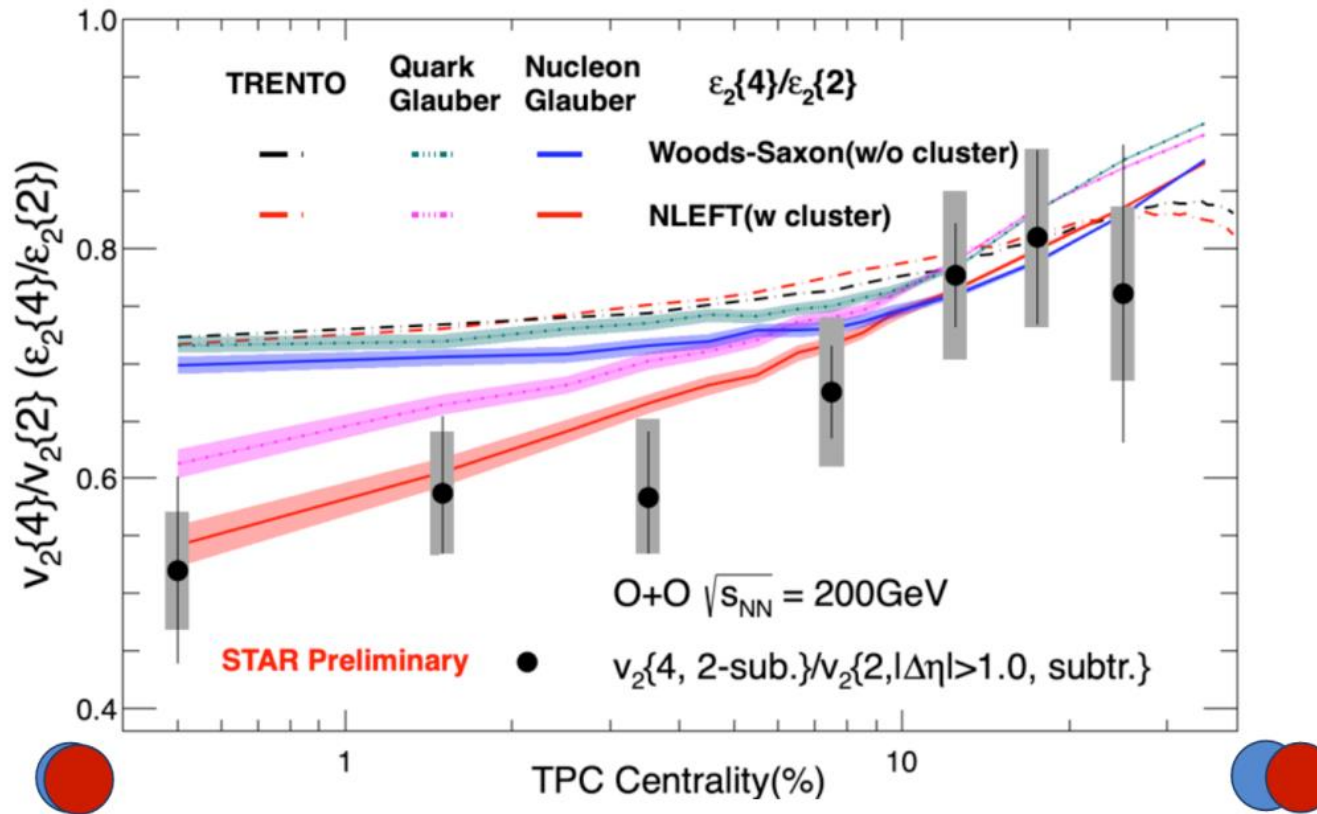


Sensitive observables for α -clustering



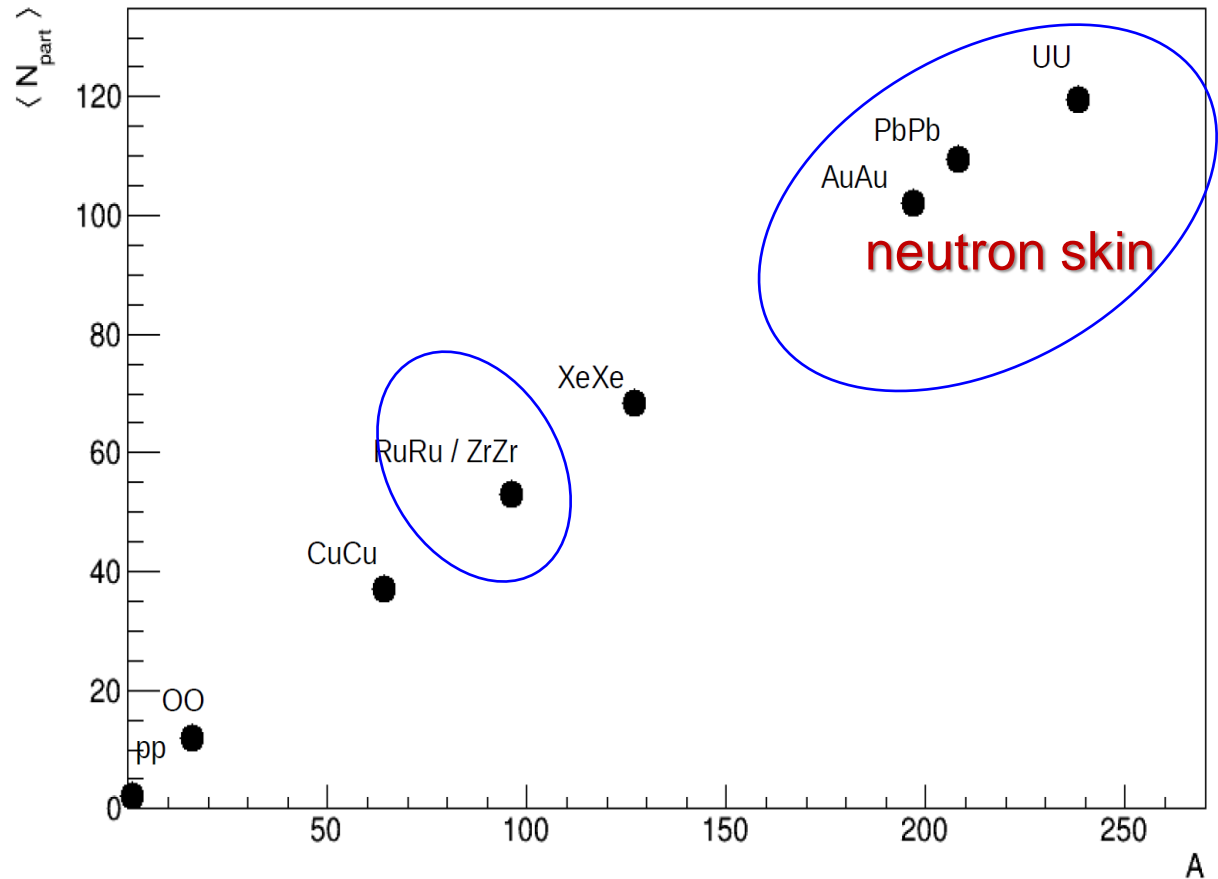
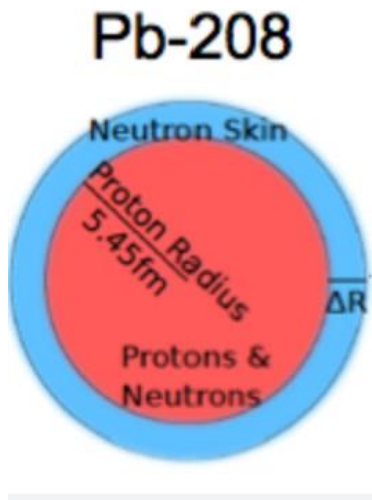
Y. Wang, S. Zhao, B. Cao, H. Xu and H. Song. Paper in preparation.
Please also refer to the work from Y G Ma's groups

Measurement from $^{16}\text{O}+^{16}\text{O}$ collisions



$-v_2\{4\}/v_2\{2\}$: enhanced fluctuations in ultra-central collisions
 heavy ion collision data hint alpha-clustering in ^{16}O

Probe neutron skin at RHIC and the LHC



Neutron Skin & neutron star

EOS of nuclear matter

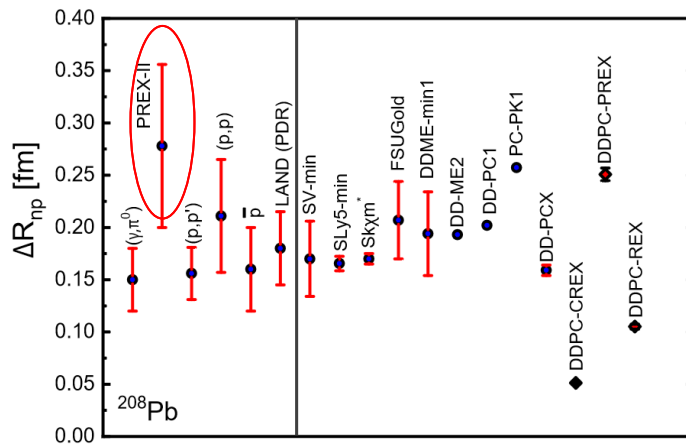
$$\epsilon(\rho, \alpha) = [\epsilon_{SNM}(\rho_0) + S(\rho_0)\alpha^2] + \alpha^2 L \frac{\rho - \rho_0}{3\rho_0} + \frac{1}{2}(K_0 + \alpha^2 K_{sym}) \left(\frac{\rho - \rho_0}{3\rho_0}\right)^2$$

L : the first order term in EOS; symmetry energy; Large L thick neutron skin

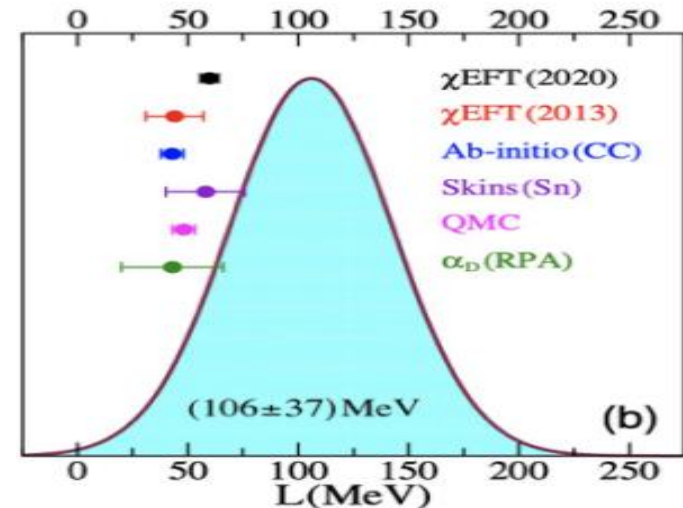
Probe the Neutron Skin at low energy nuclear physics

Parity-Violating Electron Scattering in Jefferson Lab

$$R_{skin}^{208} = 0.278_{-0.078}^{+0.078} fm \quad \text{Phys. Rev. Lett. 126, 172502, (2021)}$$

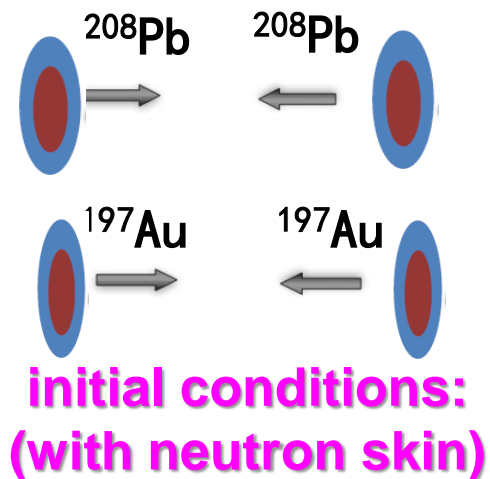
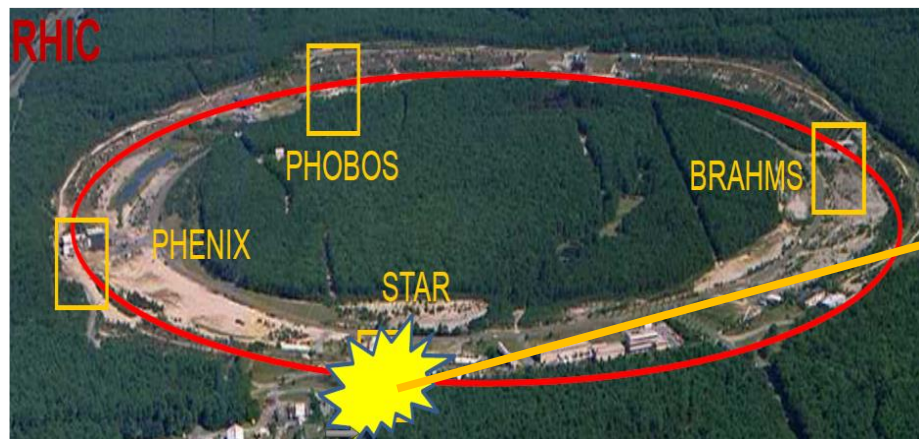


arXiv:2206.06527 Esra Yüksel and Nils Paar



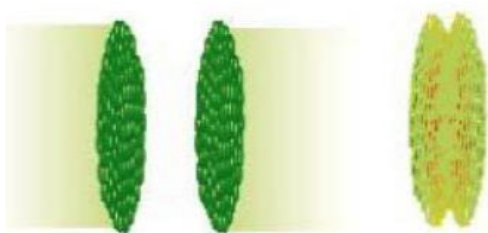
Phys. Rev. Lett. 126, 172502 D. Adhikari et al

Relativistic heavy ion collision to probe the neutron skin



Well calibrated calculations

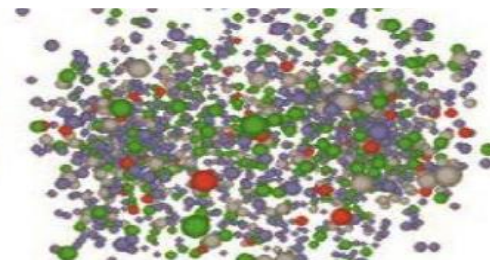
Initial conditions



viscous hydro

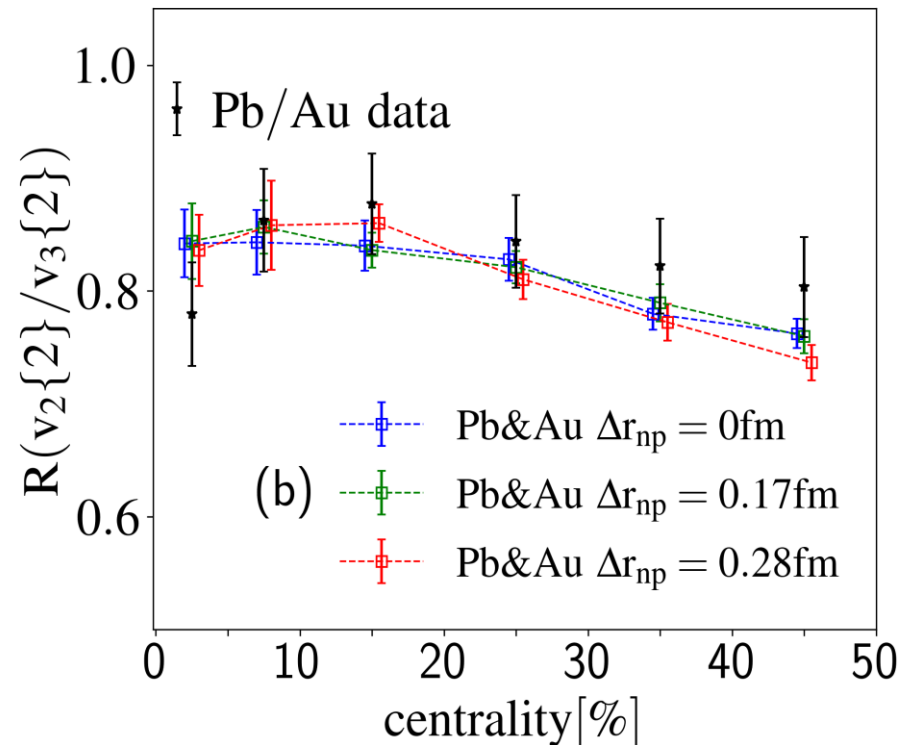
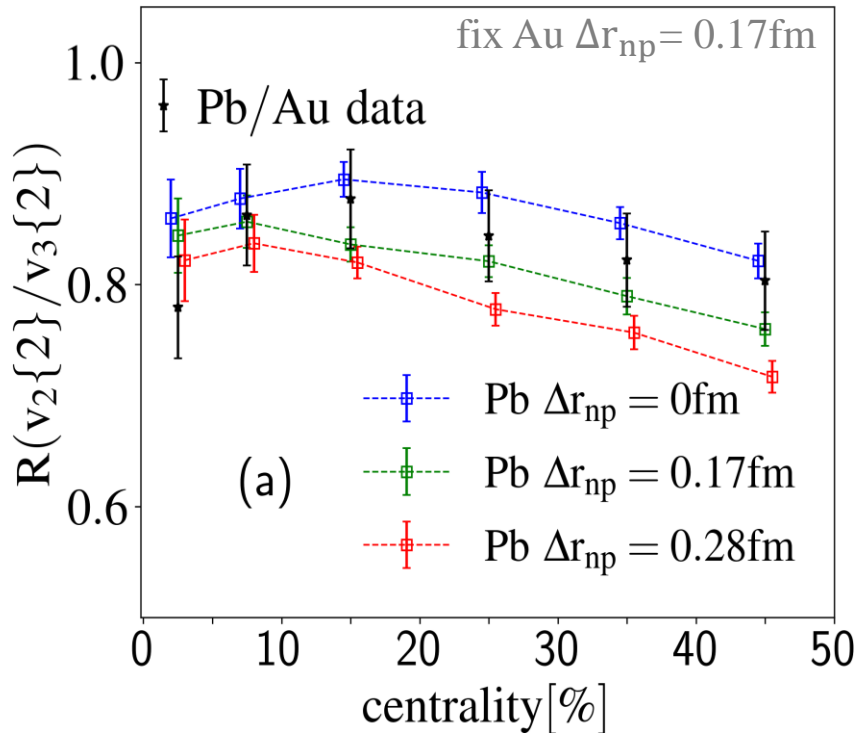


hadron cascade



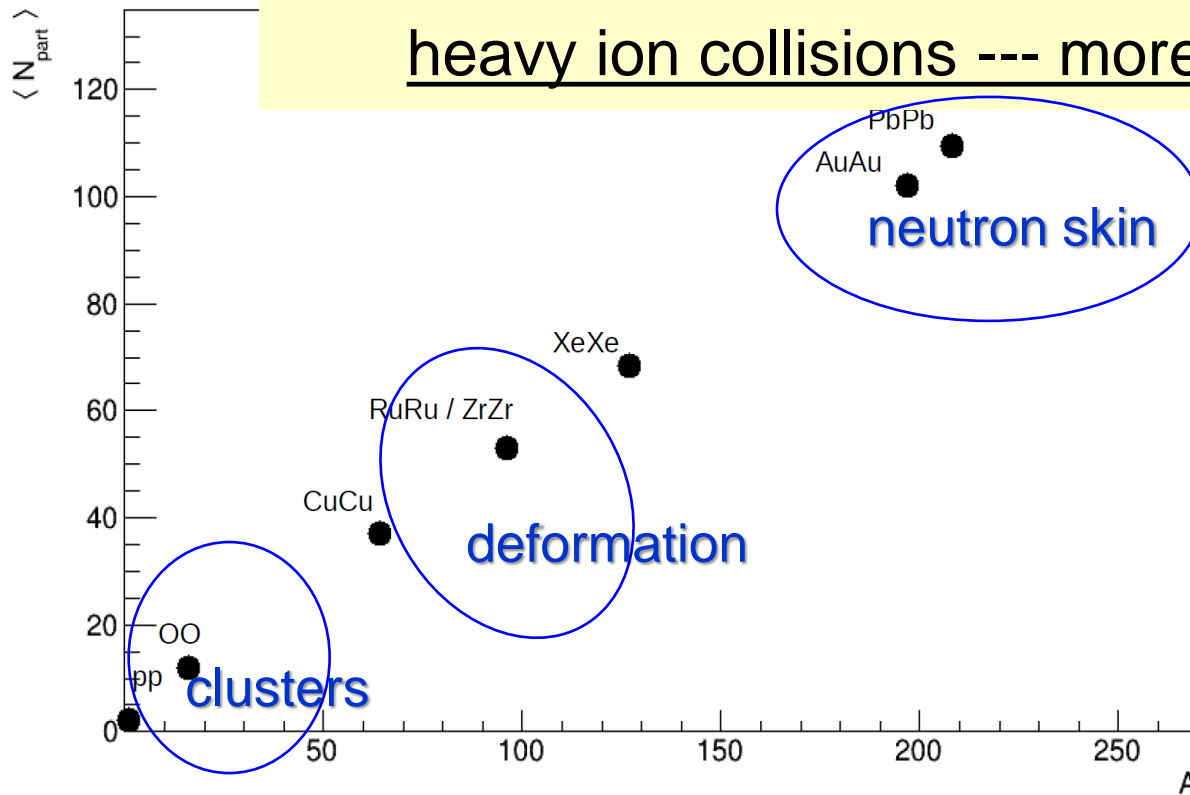
Probing the neutron skin of ^{197}Au and ^{208}Pb

semi-isobaric double ratio

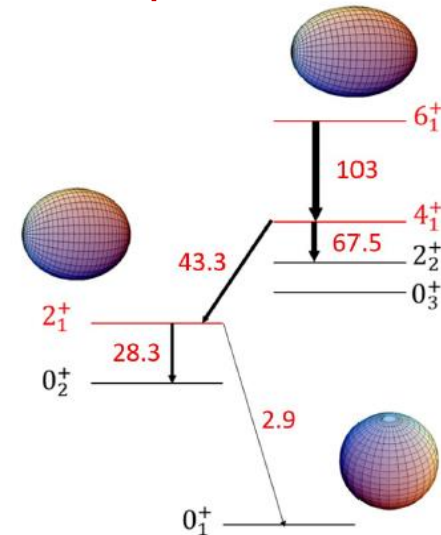


A scaling behavior was found in double ratio of $v_2\{2\}/v_3\{2\}$ when Au and Pb have the neutron skins of the same size,
The measured flow harmonics at various centrality suggest Au and Pb have similar neutron skin

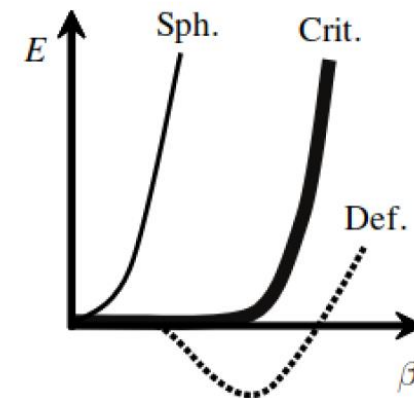
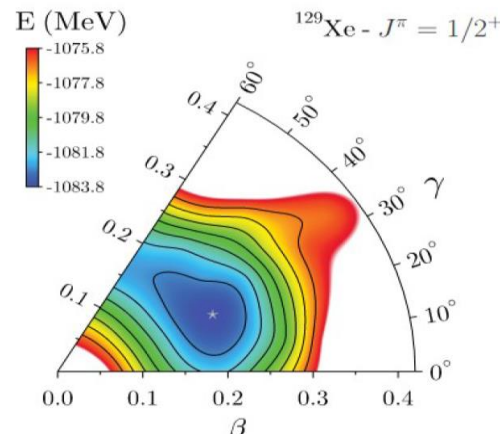
Probing the nuclear structure with relativistic heavy ion collisions --- more to explore



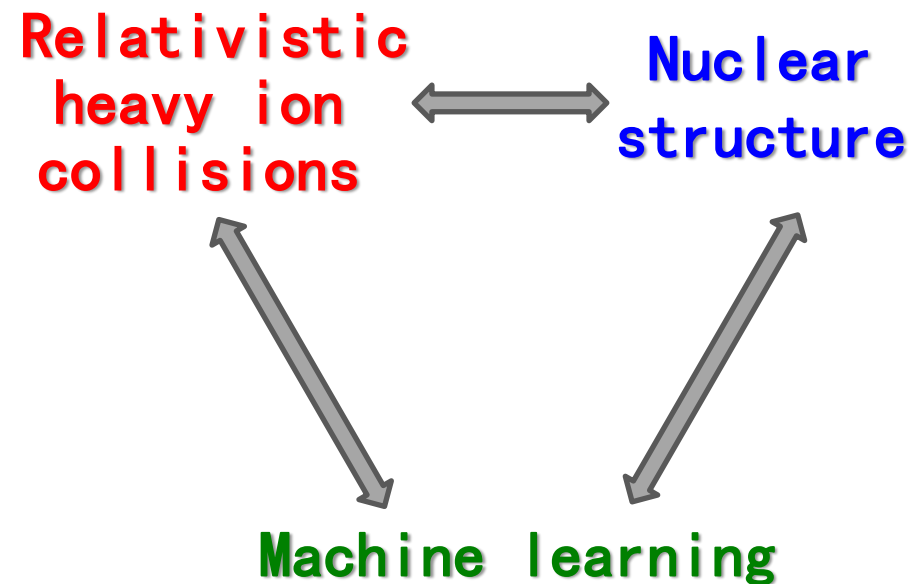
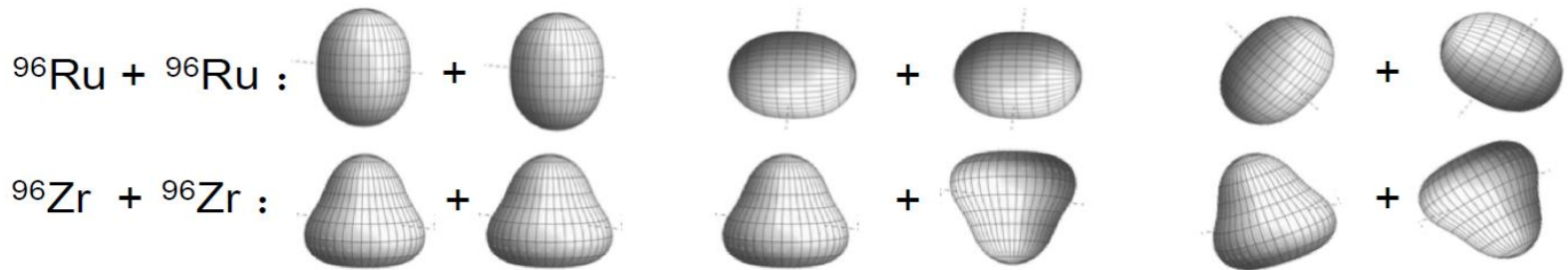
^{96}Zr : shape coexistence



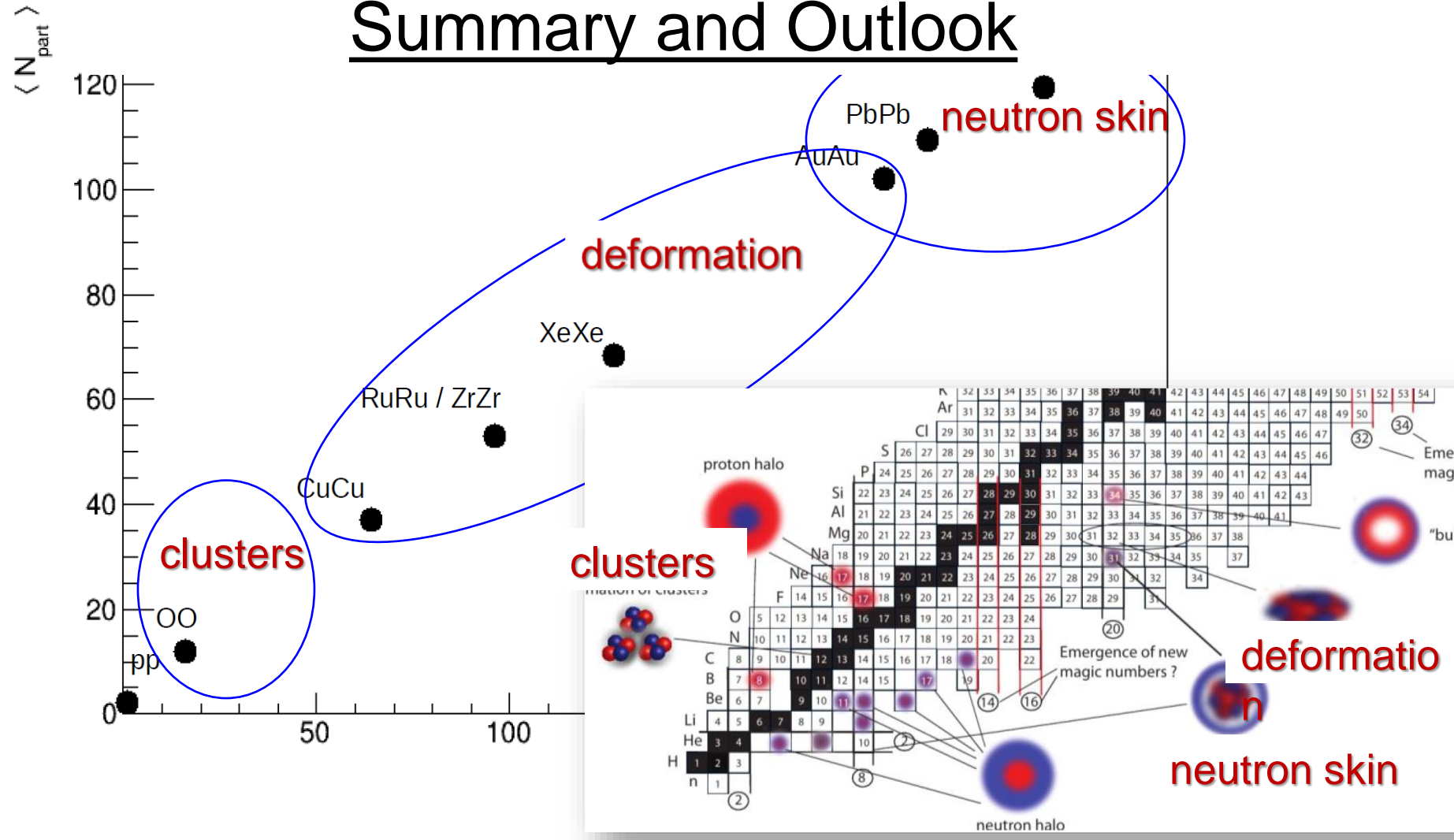
^{129}Xe : γ soft shape phase transition



- Nuclear structure: deformation, cluster, neutron skin; shape coexistence, γ -soft (shape phase transition)
- Rich configurations for QGP initial conditions

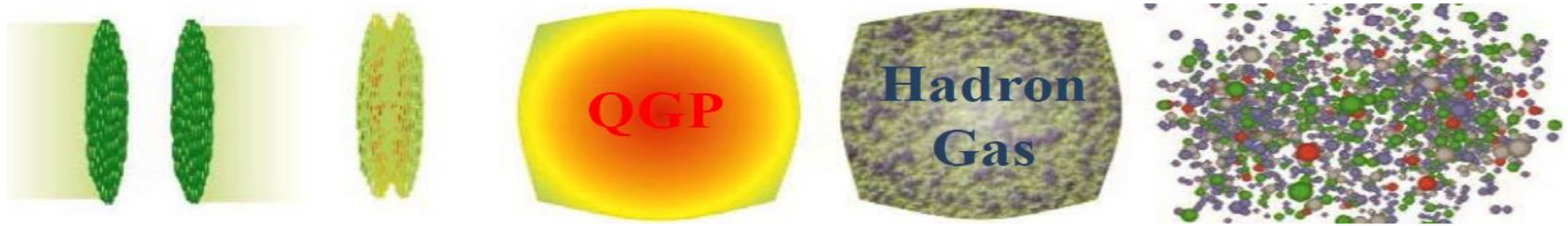


Summary and Outlook



Relativistic heavy ion collisions have already provide rich collision systems to study various aspects in nuclear structure. Even we focus on these several colliding nuclei, there are lots of things to explore !

Summary and Outlook



Initial conditions

viscous hydro

hadron cascade

- Over the past 40 years
 - the concept of QGP was proposed
 - the accelerators was built
 - the QGP was discovered
 - the properties of the QGP are being explored
- Put more efforts on initial conditions ([nuclear structure aspects](#))
 - high energy nuclear physics: necessary for a precisely study QGP
 - low energy nuclear physics: new insights for nuclear structure

The future is bright !

Exploring nuclear physics across energy scales

Program + workshop Beijing April 15-28 2024

Program: CCAST April 15-18, 23-28, 2024

seminars + discussions each day

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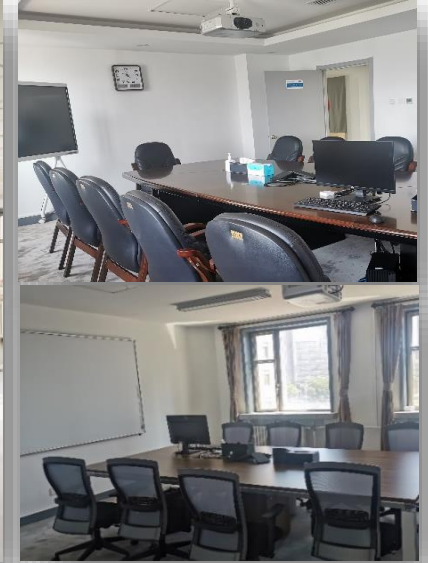
Sectaries:

Lviv (Peking U)
Ke-qian Hu (Peking U)
Chunxia Zhao(ITP,CAS)
Email: lviv@pku.edu.cn

CCAST Building



Discussion area



Meeting room



Visitor offices



Exploring nuclear physics across energy scales Program + workshop Beijing April 15-28 2024

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Welcome to Beijing in coming April next year!