Discovery and Discovery Potential of Doubly Heavy Hadrons 秦 溱 华中科技⼤学

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*Phys.Lett.B*782(2018)412, Ali,Parkhomenko,**QQ**,Wang *Phys.Lett.B*785(2018)605*,* Ali,**QQ**,Wang *Chin.Phys.C*45(2021)103106, **QQ**,Shen,Yu *Phys.Rev.D*104(2021)114009, Jin,Li,Liu,**QQ**,Si,Yu *Phys.Rev.D*105(2022)L031902, **QQ**,Shi,Wang,Yang,Yu,Zhu

Contents

• Why do we need doubly heavy hadrons?

• Discovery of T_{cc}

• Discovery potential of Ξ*bc*

The quark model

Murry Gell-Mann 1969 Nobel Prize for physics

- Old myth
- New life

Three new milestones

• Observation of tetraquarks

• Observation of pentaquarks

The *Physics World* 2015 "top-10 breakthroughs"

国家科技部"2017年度中国科学十大进展"

• Observation of a double-charm baryon Ξ_{cc}^{++} [LHCb, *Phys.Rev.Lett.* 119 (2017) 112001]

The *Physics* 2013 "Highlights of the Year" (rank 1st)

[LHCb, *Phys.Rev.Lett.* 115 (2015) 072001]

[BESIII, *Phys.Rev.Lett.* 110 (2013) 252001]

"Periodic table of the hadrons"

, X(6900): a new main group Ξ*cc*

 $\boldsymbol{Z_c,P_c:}$ a new period

Beyond stamp collecting

• Because of color confinement, properties of quarks are studied via

• New types of hadrons provide new visual angles into QCD and

hadrons

also electroweak dynamics

analogous to a heavy meson, but also different: bosonic, sizable heavy element

e.g., doubly heavy baryons have a unique structure, resembling a 'double star' with a 'planet' attached

e.g., the doubly heavy tetraquarks help us probe the nature of exotic hadronic states, cusps or true resonances

• More is better

Who is to be shot next?

Two targets after the Ξ_{cc}^{++} discovery.

: [**QQ**,Shi,Wang,Yang,Yu,Zhu,2108.06716] Ξ*bc* <u>"Inclusive approach for beauty-charmed baryon Ξ_{bc} search"</u>

: [**QQ**,Shen,Yu,2008.08026] *Tcc* "Discovery potential of double-charm tetraquarks"

One year later $-- T_{cc}$ discovery was reported by LHCb on 28 July 2021.

[LHCb,2109.01038;2109.01056]

Discovery of T_{cc}

Production Mechanism with (

• It was proposed for double-bottom hadron production these cut-o↵ parameters forces the two *b*-quarks to over-

> [Ali,Parkhomenko,QQ,Wang,1805.02535;Ali,QQ,Wang,1806.09288] the inclusive *Bc*-meson production in *Z*-boson decays. 9

mostly soft pions or kaons. Likewise, the *bb*-diquark

- Assuming T_{cc} a real tetraquark, the same mechanism applies $\lim_{\Delta} T$ a real tetraguerk the same mechanish $\boldsymbol{\mu}$, $\boldsymbol{\mu}$ and $\boldsymbol{\mu}$ and $\boldsymbol{\mu}$ and $\boldsymbol{\mu}$ and $\boldsymbol{\mu}$ in the right-hand frame $\boldsymbol{\mu}$
- Stay close enough? One parameter —
- 1. Two produced heavy quarks stay close enough to form a heavy diquark lap in the phase space space is the phase space of the form productu nitavy quarks <u>stay close chough</u> to form
- 1 2. The heavy diquark further fragments into doubly heavy hadrons

 $\Delta M \equiv M_{cc} - 2m_c \leq (2.0^{+0.5}_{-0.4})$ GeV $\Delta M - M$ Δm \angle (2 0 \pm 0.5) ΔM $\Delta w = w_{cc} - \Delta w_c \ge (\Delta v_{-0.4})$ dev

 Γ Determined by matching the B_c production rate to $\bar{b}b\bar{c}c$

-
-
-
-

• The cross section for all double-charm hadrons

 $\sigma(pp \to H_{cc} + X) = (310^{+10}_{-70}) \text{ nb};$ $\sigma(pp \to H_{cc} + X) = (310^{+170}_{-70})$ nb

- For double-charm baryons, e.g. $\sigma(\Xi_{cc}^{++}) = (103^{+56}_{-22})$ nb
- For double-charm tetraquarks, e.g.

[Chang,Qiao,Wang,Wu,0601032] their ground states, we do not need to multiply the *r^g* ratio for their production cross sections, which reads to be a section of the second section of the second section of the second section of the
Second sections, which reads to be a second sec

[LHCb,1910.11316] choosing the cuts 4 *< p*^T *<* 15 GeV and 2 *<* ⌘ *<* 4*.*5. From an LHCb measurement with passenger $\mathcal{L}_{\mathcal{A}}$, it can be extracted that ($\mathcal{L}_{\mathcal{A}}$

vs 62 nb (NRQCD) $\sqrt{}$ vs 62 nb (NRQCD) \mathcal{F} is the excited states of \mathcal{F} and \mathcal{F} and \mathcal{F} and \mathcal{F} into \mathcal{F} and \mathcal{F} into \mathcal{F} and \math

$$
\widehat{c(T_{cc}^+)} = (24^{+14}_{-7})^{\text{nb}}
$$

The cuts are $4 < p_T < 15$ GeV, $2 < \eta < 4.5$ @ 13 TeV LHCb

Production of double-charm hadrons \mathbf{P} . Provided production in \mathbf{P} *T{cc}* [¯*ud*¯] ⁺ *^X* at the LHC for ^p*^s* = 13 TeV with 2 *<* ⌘ *<* ⁴*.*5.

Comparison with theory (*pp* ! *^T{cc}* [¯*us*¯] ⁺ *^X*) = (*pp* ! *^T{cc}* [*d*¯*s*¯] ⁺ *^X*) = (6*.*0+3*.*⁵ 1*.*7) nb *.* (4)

The Comparison with experiment \sim \sim \sim *cc*) = (⌅⁺

1*.*5. To compare with this result, we reset the same cuts and find (⌅++ nb. Taking into account the large uncertainties, they agree with each other. In addition, vs [30, 130] nb accurate the With theory inputs)

> $\sigma(\Xi_{cc}^{++}) \times \mathcal{B}(\Xi_{cc}^{++} \to \Lambda_c^+ K^- \pi^+ \pi^+)$ $\sigma(\Lambda_c^+)$ $= (2.22 \pm 0.27 \pm 0.29) \times 10^{-4}$

[¯*ud*¯] ⁺ *^X*) = (24+14

⁷) nb *,*

(*pp* ! ⌦⁺

cc + *X*) = (26+14

⁶) nb *.* (5)

^c + ⇤

With partonic simulation by MadGraph & Pythia, we obtain

[**QQ**,Shen,Yu,2008.08026]

Propose the golden channel $T_{cc}^+ \rightarrow D^0 D^{*+} \rightarrow D^0 D^0 \pi^+$

- Big branching ratio
- Big detection efficiency (all charged particles)

Compared with
$$
\Xi_{cc}^{++} \to \Lambda_c^+ K^- \pi^+ \pi^+
$$

 $(4\%)^2$ 12

Production
$$
\sigma(\Xi_{cc}^{++}) = (103^{+56}_{-22}) \text{ nb}
$$

\n $\sigma(T_{cc}^{+}) = (24^{+14}_{-7}) \text{ nb}$

 (π^+) *Br*($D^0 \to K^- \pi^+$)²

$$
\begin{array}{ll}\n\text{Decay} & Br(\Xi_{cc}^{++} \to \Lambda_c^+ K^- \pi^+ \pi^+) \; Br(\Lambda_c^+ \to pl) \\
& 10\% & 6\% \\
\text{Br}(T_{cc} \to D^0 D^{*+}) \; Br(D^{*+} \to D^0 \pi^+) \\
& 1/2 & 2/3\n\end{array}
$$

$$
T_{cc}^{\dagger} \cdot N_s \sim 100
$$

Detection of T_{cc}

$$
f_{T_{cc}}/f_{\Xi_{cc}} \sim 1/4
$$

$$
Br(T_{cc})/Br(\Xi_{cc}^{++}) \sim 1/4
$$

1500 events of $\Xi_{cc}^{++} \rightarrow \Lambda_c^+ K^- \pi^+ \pi^+$

[**QQ**,Shen,Yu, 2008.08026]

[LHCb,2109.01038;2109.01056]

Discovery potential of Ξ*bc*

Who is to be shot next?

$\sigma(\Xi_{bc}) = 37$ nb at 14 TeV LHCb

[X.G.Wu, et al 1101.1130]

Billions of Ξ_{bc} will be produced @ LHCb Run3.

Difficulties in experimental searches for Ξ*bc*

• Detection efficiency — — small exclusive branching ratios

[W. Wang, F.S. Yu, Z.X. Zhao, 1707.02834] [LHCb, 2104.04759]

• First experimental attempts (LHCb, 13 TeV, ~ 5 fb⁻¹)

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$$
\frac{\sigma(\Xi_{bc}^{0})\cancel{B}(\Xi_{bc}^{0}\rightarrow\Lambda_{c}^{+}\pi^{-})}{\sigma(\Lambda_{b}^{0})\cancel{B}(\Lambda_{b}^{0}\rightarrow\Lambda_{c}^{+}\pi^{-})}\n\leq [0.5,2.5]\times 10^{-4}
$$
\n
$$
\frac{\sigma(\Xi_{bc}^{0})}{\sigma(\Lambda_{b}^{0})}\frac{B(\Xi_{bc}^{0}\rightarrow\Xi_{c}^{+}\pi^{-})}{B(\Lambda_{b}^{0}\rightarrow\Xi_{c}^{+}\pi^{-})}\n\leq [1.4,6.9]\times 10^{-3}
$$

$$
\frac{\sigma(\Xi_{bc}^0)}{\sigma(\Lambda_b^0)} \frac{B(\Xi_{bc}^0 \to D^0 p K^-)}{B(\Lambda_b^0 \to D^0 p K^-)} < [1.7, 30] \%
$$

[LHCb, 2009.02481]

$$
(B(\Lambda_b^0 \to \Lambda_c^+ \pi^-) = 4.9 \times 10^{-3}, \sigma(\Lambda_b^0) \sim 10 \,\mu b, \sigma(\Xi_{bc}^0) \sim
$$

A novel approach —— inclusive Ξ*bc* **search**

• Generally, inclusive decays have (1) larger branching ratios but (2) lower detection efficiencies

• However, for $\Xi_{bc} \to \Xi_{cc}^{++} + X$, the efficiency can be large by making use of the inform of displaced vertex

Inspired by the proposal to search for Ξ_{bb} via $\Xi_{bb} \rightarrow B_c + X_c$ [Gershon,Poluektov,1810.06657]

- $\ \Xi_{bc}$ is (almost) the only source for displaced Ξ_{cc} 's
- The $B_c \rightarrow \Xi_{cc}^{++} + X$ decay is highly suppressed

 Ξ_{cc}^{++} \boldsymbol{p} IP

Basically impossible at hadron colliders

[**QQ**,Shi,Wang,Yang,Yu,Zhu,2108.06716]

Calculation of $E_{bc} \rightarrow E_{cc} + X$

- First important fact: $\Xi_{bc} \to \Xi_{cc} + X = \Xi_{bc} \to H_{cc} + X$ H_{cc} include excited states of E_{cc} , which still decay into E_{cc}
- Regarding the heavy diquarks χ_{bc} and χ_{cc} as point-like particles, the decay at the quark-diquark level is

 $\chi_{bc} \rightarrow \chi_{cc} + \ell^- \bar{\nu}, \chi_{cc} + \bar{q}q'$

It is reasonable because $r_{OO'} \sim 1/(m_O v) \ll 1/\Lambda_{\rm QCD}$ [e.g.,Brodsky,Guo,Hanhart,Meissner,1101.1983]

• By making use of OPE, the inclusive decay rate is expanded by powers of $1/M_{QQ'}$ within the Heavy Diquark Effective Theory

$$
{bc} \rightarrow H{cc} + X
$$

[Y.J.Shi, W.Wang, Z.X.Zhao,Meissner,2002.02785]

3 body \rightarrow 2 body

Heavy diquark effective theory

• Integrating out the degrees of freedom above $\Lambda_{\rm QCD}$, the two heavy quark system can be regarded as a point-like heavy diquark, scalar or axial-vector

- As HEQT for a heavy-light system (heavy meson), the big momentum $M_{X,S}$ v of a heavy diquark inside a doubly-heavy baryon can be integrated out by
- Then only the $\Lambda_{\rm QCD}$ degrees of freedom are left, the expansion $(\Lambda_{\rm QCD}/M_{X,S})^n$ for inclusive decays can be performed. At the leading power,

$$
B(\Xi_{bc} \to \Xi_{cc} + X) = B(\chi_{bc} -
$$

 $X^{\mu} = e^{-im_X v \cdot x} (X^{\mu}_{\nu} + Y^{\mu}_{\nu})$

[Y.J.Shi, W.Wang, Z.X.Zhao,Meissner,2002.02785]

 $B(\Xi_{bc} \to \Xi_{cc} + X) = B(\chi_{bc} \to \chi_{cc} + \ell^- \bar{\nu}, \chi_{cc} + \bar{q}q') + O(1/M_{QQ'})$

$$
\mathcal{L}_{S} = \frac{1}{2} (D_{\mu} S^{i})^{\dagger} (D^{\mu} S^{i}) - \frac{1}{2} m_{X}^{2} S^{i \dagger} S^{i}
$$

$$
\mathcal{L}_{X} = -\frac{1}{2} [(D_{\mu} X_{\nu}^{i})^{\dagger} (D^{\mu} X^{i \nu}) - (D_{\mu} X_{\nu}^{i})^{\dagger} (D^{\nu} X^{i \mu})] + \frac{1}{2} m_{X}^{2} X_{\mu}^{i \dagger} X^{i \mu}
$$

Hadron ⇒ **Diquark**

• The key issue is the 2-diquark-2-fermion interaction vertex, i.e. the $\chi_{bc} \to \chi_{cc}$ diquark current

 $\langle \chi_{cc}(v,\epsilon) | \bar{c} \gamma^{\mu} b | \chi_{bc}(v',\epsilon') \rangle \propto - a_0 \epsilon^* \cdot \epsilon' v'^{\mu} - a_1 \epsilon^* \cdot \epsilon' v^{\mu} + a_2 \epsilon^* \cdot v' \epsilon'^{\mu} + a_3 v \cdot \epsilon' \epsilon^* \mu$

 $\langle \chi_{cc}(v,\epsilon) | \bar{c} \gamma^{\mu} \gamma_5 b | \chi_{bc}(v',\epsilon') \rangle \propto -ib_0 \epsilon^{\epsilon' \epsilon^* v' \mu} - ib_1 \epsilon^{\epsilon' \epsilon^* v \mu}$

double lines denote the heavy quark while the triple lines [QQ,Shi,Wang,Yang,Yu,Zhu,2108.06716]

• Matching the $b \to c$ current to the $\chi_{bc} \to \chi_{cc}$ diquark current (analogous to a transition form factor)

- The matching is performed differently for different kinematic regions, because of different dynamics
- 1. Small recoil region (large q^2)
- 2. Large recoil region (small q^2)

Diquark ⇒ **Quark**

- **Small recoil region:** in the heavy quark limit, the two heavy quarks in the heavy diquark are relatively static $--$ sharing the same velocity ν
- Heavy diquarks can be represented by a Lorentz bilinear field

$$
D_{\nu}^{QQ'}(x) = \frac{1 + \nu \cdot \gamma}{2} [\gamma^{\mu} A_{\mu}(x) + i\gamma_5 S(x)]C
$$

Axial-vector Scalar

- Its Lorentz transformation $D_v^{\phantom i}(x)\to D_v'(x')=\Lambda_{1/2}^{\phantom i}D_v^{\phantom i}(\Lambda^{-1}x)\Lambda_{1/2}^{\rm T}$
-

• Then the matching comes to $\bar{c}\Gamma b=$ tr $\left|L^{\mathsf{T}}\,\bar{D}^{cQ}_{v'}\,\Gamma D^{bQ}_v\,\right|$, with $\ L=L_0+L_1v\cdot\gamma+L_2v'\cdot\gamma+L_3(v\cdot\gamma)(v'\cdot\gamma)$

$$
\xi(w = 1) = 1 \qquad a_{0,1,2,3}(q_{\text{max}}^2) = b_{0,1}(q_{\text{max}}^2) = 1
$$

- **.** Calculating the trace $\bar{c}\Gamma b$ = tr $\left| L^{\mathsf{T}}\ \bar{D}_{\nu'}^{c\mathcal{Q}}\ \Gamma D_{\nu}^{b\mathcal{Q}}\ \right|$ for $\Gamma=\gamma_{\mu},\gamma_{\mu}\gamma_5$, using $(\nu\cdot\gamma)D_{\nu}=D_{\nu}$
- It simplifies into

$$
\frac{1}{\sqrt{2M_{bc}M_{cc}}}\langle \chi_{cc}(v,\epsilon)|\bar{c}\gamma^{\mu}b|\chi_{bc}(v',\epsilon')\rangle = \xi(w)\Big[-\epsilon^* \cdot \epsilon'v^{\mu} - \epsilon^* \cdot \epsilon'v^{\mu} + \epsilon^* \cdot v'\epsilon^{\mu} + v \cdot \epsilon'\epsilon^{*\mu}\Big]
$$
\n
$$
\frac{1}{\sqrt{2M_{bc}M_{cc}}}\langle \chi_{cc}(v,\epsilon)|\bar{c}\gamma^{\mu}\gamma_5b|\chi_{bc}(v',\epsilon')\rangle = \xi(w)\Big[-i\epsilon^{\epsilon'\epsilon^*\nu'\mu} - i\epsilon^{\epsilon'\epsilon^*\nu\mu}\Big]
$$

Only one function $\xi(w)$ with $w = v \cdot v'$ to be determined, similar to the famous Isgur-Wise function.

• Making use of the state normalization we can fix ξ

[**QQ**,Shi,Wang,Yang,Yu,Zhu,2108.06716]

- **Large recoil region:** at least one hard gluon is to be exchanged, and is thus perturbatively calculable
- The calculation via NRQCD gives

$$
a_{2,3}(q^2) = \frac{\alpha_s}{2(1-w)^2 \sqrt{w}} \frac{N_c + 1}{N_c} \frac{1}{m_c^3} R_{bc}(q^2)
$$

$$
a_0(q^2) = b_0(q^2) = \bar{\xi}_2 a_{2,3}(q^2), \ a_1(q^2) = b_1(q^2)
$$

• At last, we connect the two regions by making a numerical fit accepting the z-series expansion formula

$$
f(q^2) = \frac{f(0)}{1 - q^2/m_{B_c}^2} \left[1 + b\zeta(q^2) + c\zeta^2(q^2)\right]
$$

[**QQ**,Shi,Wang,Yang,Yu,Zhu,2108.06716]

Calculation of $E_{bc} \rightarrow E_{cc} + X$

• Numerical result for the decay width

$$
\Gamma(\Xi_{bc} \to \Xi_{cc} + X) = (1.9 \pm 0.
$$

• The branching ratio is

$$
93 \text{fs} < \tau(\Xi_{bc}^0) < 108 \text{ fs}, \, 409 \text{ fs} < \tau(\Xi_{bc}^+) < 607 \text{ fs}
$$

• Lifetime [H.Y.Cheng, F.R.Xu, 1903.08148]

$$
B(\Xi_{bc}^{+} \to \Xi_{cc} + X) \approx 14\,\%, \quad B(\Xi_{b}^{0})
$$

• Ξ_{cc}^{++} fragmentation suffers a factor of $1/2$

$$
B(\Xi_{bc}^{0}\to\Xi_{cc}+X)\approx3\,\%
$$

$$
\overline{2}
$$

$$
\underbrace{\sqrt{B(E_{bc}^{+}}\rightarrow E_{cc}^{++}+X)}_{24}\approx 7\,\%
$$
 $B(E_{bc}^{0}\rightarrow E_{cc}^{++}+X)\approx 1.5\,\%$

$(1 \pm 0.3 \pm 0.4) \times 10^{-13}$ GeV

Uncertainties from quark mass, wave function at origin, scale dependence

• Estimation of signal yield

Three ingredients:

1. Number of signals of Ξ_{cc}^{++} : 10000 for 23 ${\rm fb}^{-1}$ (Run III, by 2024)

$$
N(\Xi_{bc}^{+} \to \Xi_{cc}^{++} + X) = N_p(\Xi_{bc}^{+}) \cdot B(\Xi_{bc}^{+} \to \Xi_{cc}^{++} + X) \cdot \epsilon(\Xi_{cc}^{++})
$$

$$
= N_d(\Xi_{cc}^{++}) \cdot \frac{\sigma(\Xi_{bc})}{\sigma(\Xi_{cc})} \cdot B(\Xi_{bc}^{+} \to \Xi_{cc}^{++} + X)
$$

2. Production ratio $\sigma(\Xi_{bc})/\sigma(\Xi_{cc}) \approx 40\,\%$ [X.G.Wu et al, 1101.1130]

3. Branching fraction of inclusive ded

(The detection efficiency is identical to that of Ξ_{cc}^{++} **)**

$$
cay \text{ of } \Xi_{bc}^{+} \to \Xi_{cc}^{++} + X
$$

Search for
$$
\Xi_{bc}^{+} \rightarrow \Xi_{cc}^{++} + X
$$
 with displaced Ξ_{cc}^{++}

Search for $\Xi_{bc} \to \Xi_{cc}^{++} + X$ **with displaced** Ξ_{cc}^{++}

• Final number of estimated signal events @ LHCb Run3

$$
N(\Xi_{bc}^{+} \to \Xi_{cc}^{++} + X) = N(\Xi_{cc}^{++}) \cdot \frac{d}{d}
$$

$$
\approx 10^{4} \times 40\%
$$

$$
\approx 280
$$

• With possible efficiency lost, it should still be detectable @ LHCb Run3

$\sigma(\Xi_{bc}^{+})$ $\sigma(\Xi_{cc})$ \cdot $B(\Xi_{bc}^{+})$ *bc* $\rightarrow \Xi_{cc}^{++} + X$

 $\% \times 7\%$

[**QQ**,Shi,Wang,Yang,Yu,Zhu,2108.06716]

Conclusion

• **More is better**: we want more new hadrons.

 T_{cc}^+ discovery at the LHCb.

 Ξ_{cc}^{++} , with about 280 signal events to be observed @ LHCb Run 3.

• We predicted the correct discovery channel and the correct signal yield for the

• We propose to search for Ξ_{bc} via inclusive $\Xi_{bc}^+ \to \Xi_{cc}^{++} + X$ with a displaced $\rightarrow \Xi_{cc}^{++} + X$

Thank you!