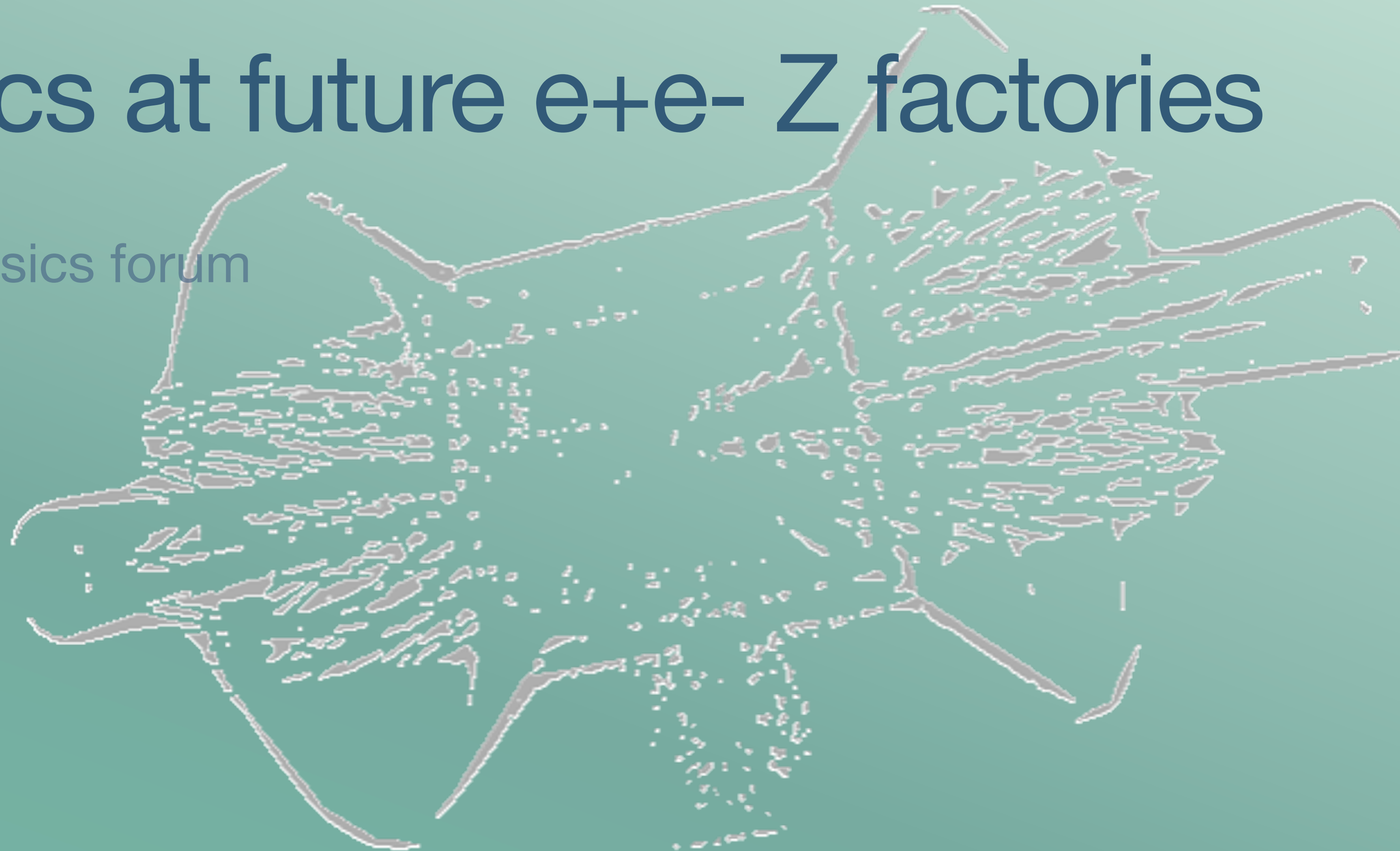


Flavor physics at future e^+e^- Z factories

September 06, 2023

SYSU-PKU collider physics forum

左训午 (KIT)



Outline



- Z factory dataset
- b physics program
 - $b \rightarrow q\ell\nu$
 - $b \rightarrow s\ell\ell$
 - $b \rightarrow s\nu\nu$
 - B^0/B_s^0 mixing
- Non-b physics program
 - Charm physics
 - Tau physics
 - Other opportunities

Z factories



	T ₀			+5				+10				+15				+20		...	+26
ILC	0.5/ab 250 GeV					1.5/ab 250 GeV					1.0/ab 500 GeV			0.2/ab 2m _{top}	3/ab 500 GeV				
CEPC	5.6/ab 240 GeV						16/ab M _Z	2.6 /ab 2M _W								SppC =>			
CHC	1.0/ab 380 GeV								2.5/ab 1.5 TeV							5.0/ab => until +28 3.0 TeV			
FCC	150/ab ee, M _Z		10/ab ee, 2M _W	5/ab ee, 240 GeV				1.7/ab ee, 2m _{top}										hh.eh =>	
LHeC	0.06/ab					0.2/ab				0.72/ab									
HE-LHC	10/ab per experiment in 20y																		
FCC eh/hh	20/ab per experiment in 25y																		

Trillions of Z bosons
— **factory!**

- Will use FCC-ee as the main example for the rest of this talk. All points are valid for CEPC

European Strategy 2020, 1910.11775
(Outdated, but enough for the purpose)

FCC-ee



- 91km ring near CERN
- Possibility for 4 experiment sites
- Operate at Z, WW, ZH, tt energies
- ~15 years of operation starting ~2045



FCC-ee dataset

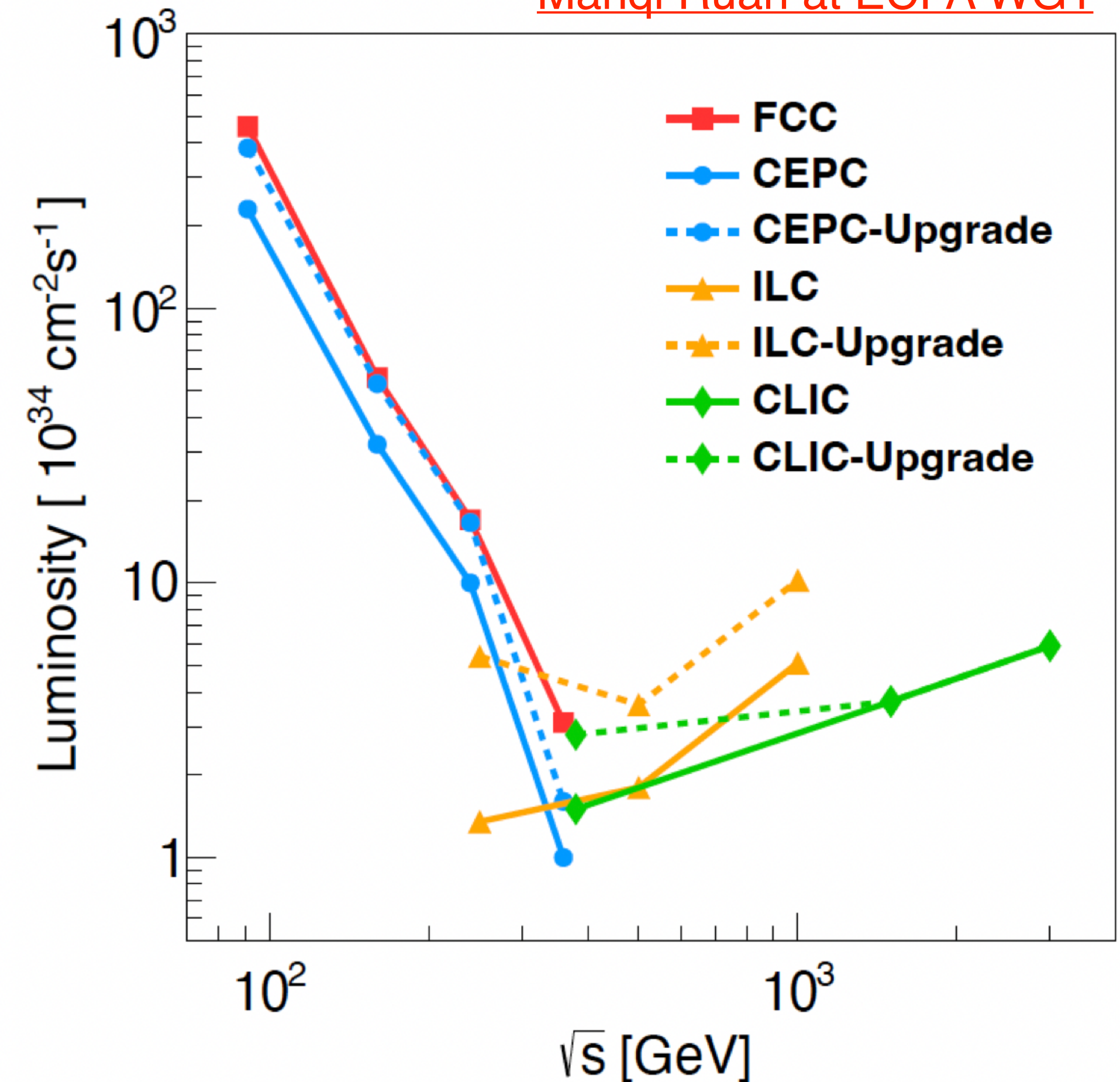


Manqi Ruan at ECFA WG1

Much more than just “H-factory”

- Splendid datasets expected with a plethora of physics opportunities
 - EW precision measurement (Z, W, H, t)
 - QCD precision measurement (α_s)
 - Flavor physics (b, c, τ)
 - BSM particles (ALPs, dark photons, LLPs)

Dataset	Operation	Int. lumi. (ab^{-1})	Events
Z	4 years	180	6×10^{12}
WW	2 years	12	2.4×10^8
ZH	3 years	7	1.5×10^6
tt	5 years	2.5	2×10^6



4 IPs assumed for FCC luminosity estimates, and the rest of the slides

FCC-ee as flavor factory



Best option for next-generation flavor machine

- FCC-ee expects to operate at Z-pole for 4 years, producing a total of 6×10^{12} Z bosons
- About 14x as many B^0/B^+ as at Belle II (50 ab^{-1})
- About 9x as many τ as Super tau-charm factory
- All species of b-hadrons are produced
- Decay products significantly boosted

Attribute	$\Upsilon(4S)$	pp	Z^0
All hadron species		✓	✓
High boost		✓	✓
Enormous production cross-section		✓	
Negligible trigger losses	✓		✓
Low backgrounds	✓		✓
Initial energy constraint	✓		(✓)

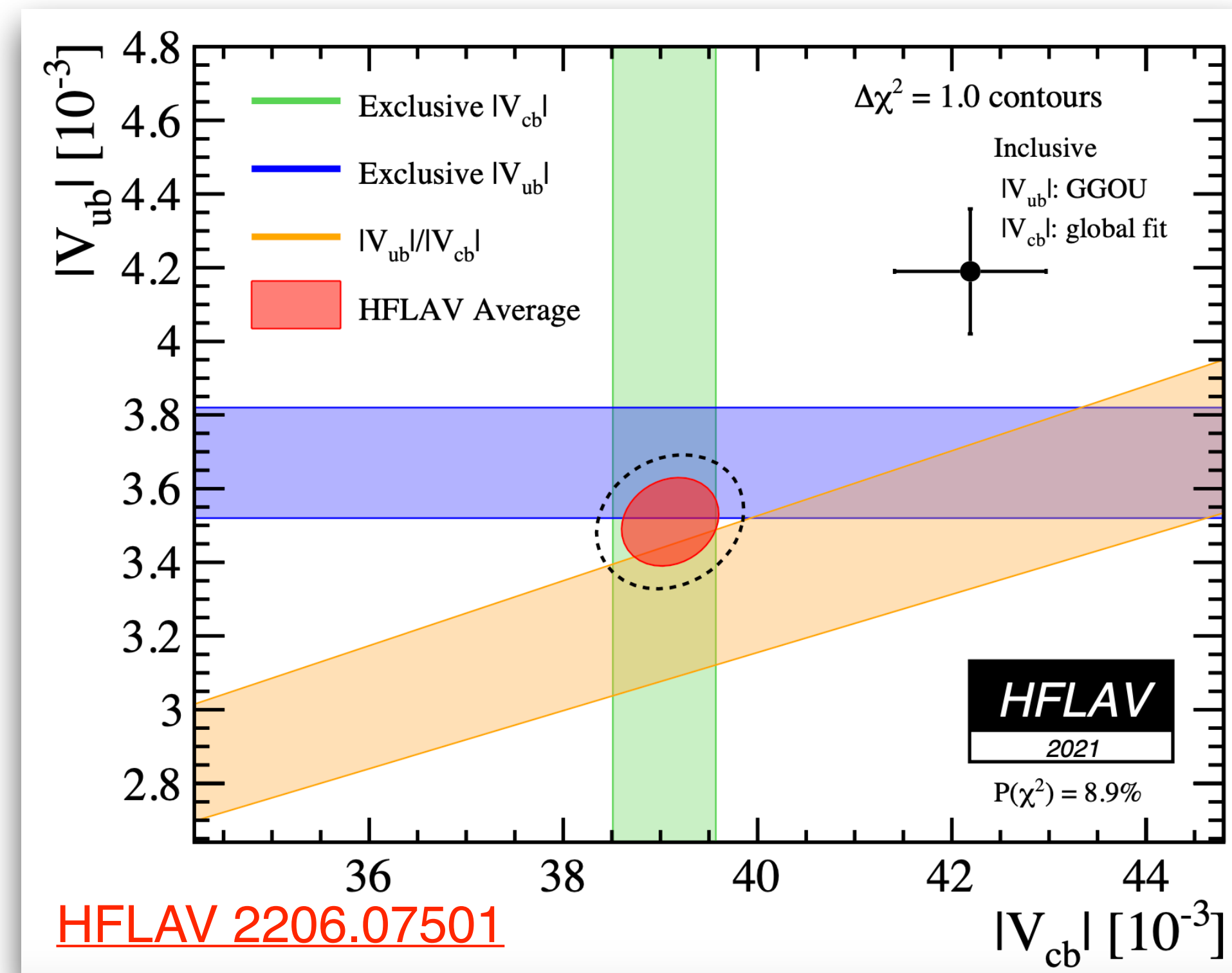
particle count ($\times 10^9$)	$B^0 (\bar{B}^0)$	$B^\pm$	$B_s (\bar{B}_s)$	$B_c^\pm$	$\Lambda_b (\bar{\Lambda}_b)$	$c (\bar{c})$	$\tau^\pm$
Belle II	55	55	0.6	N.A.	N.A.	130	90
FCC-ee	770	770	170	7	150	1400	400

b physics

- $b \rightarrow q\ell\nu$
- $b \rightarrow s\ell\ell$
- $b \rightarrow s\nu\nu$
- B^0/B_s^0 mixing

$b \rightarrow q\ell\nu$ transition

- Precise determination of CKM $|V_{ub}|$ and $|V_{cb}|$
 - Long-standing discrepancy between inclusive and exclusive extractions
 - Extreme precision at FCC-ee with exclusive decays
 - Independent clean probe via $B^+ \rightarrow \tau^+\nu_\tau$ ([Zuo et al. 2305.02998](#))
- Test of LFU with $H_b \rightarrow H_c\ell\nu$
 - $R(D)$ and $R(D^*)$ together present 3.3σ tension with SM
 - Opportunities for new $R(H_c)$ ([Ho et al. 2212.02433](#))
 - Possibility of differential test of LFU ([Ligeti et al. 2112.07685](#))
 - Independent probe of $b \rightarrow c\ell\nu$ through $B_c^+ \rightarrow \ell^+\nu_\ell$ ([Zheng et al. 2007.08234](#), [Zuo et al. 2305.02998](#))



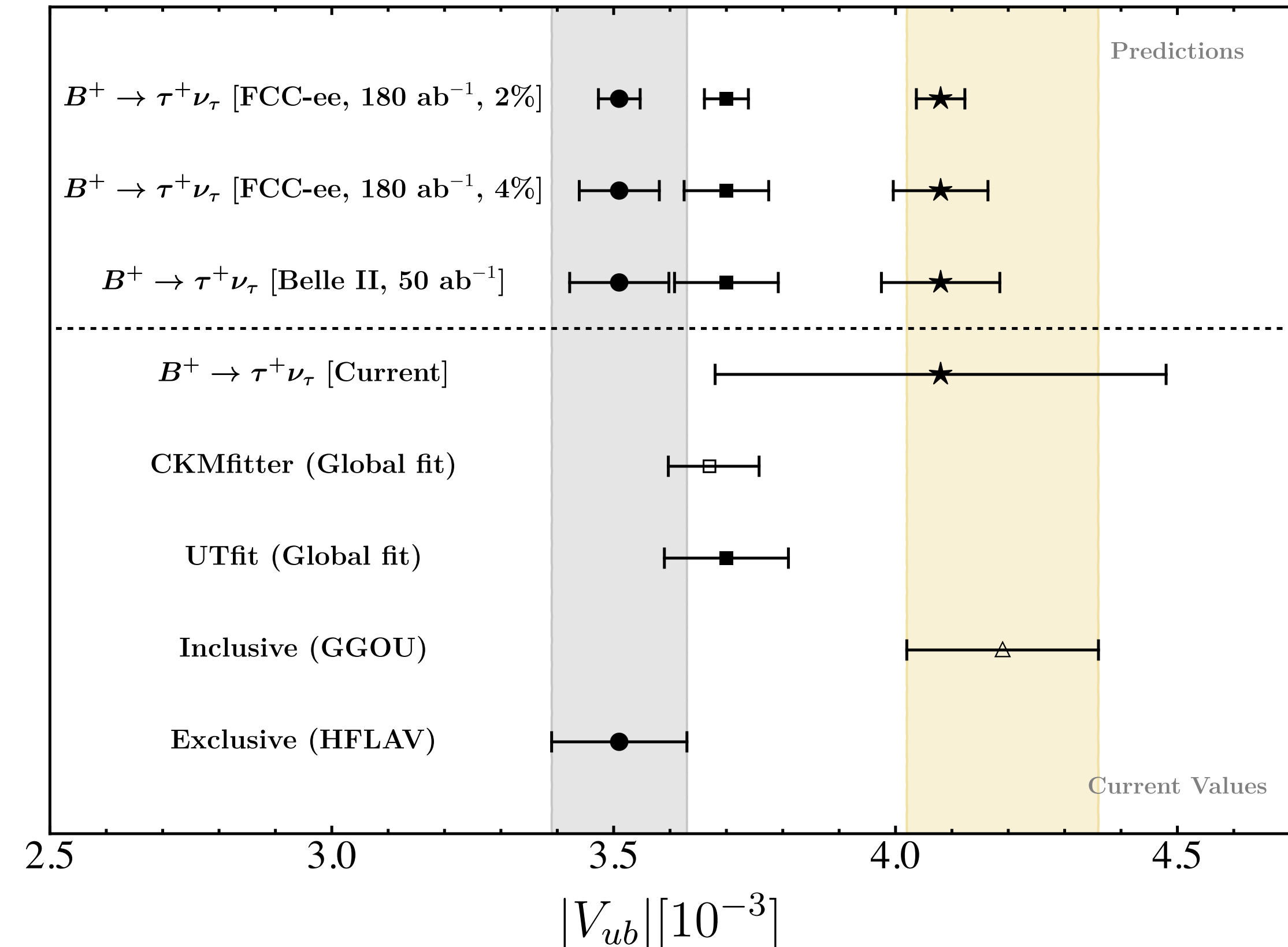
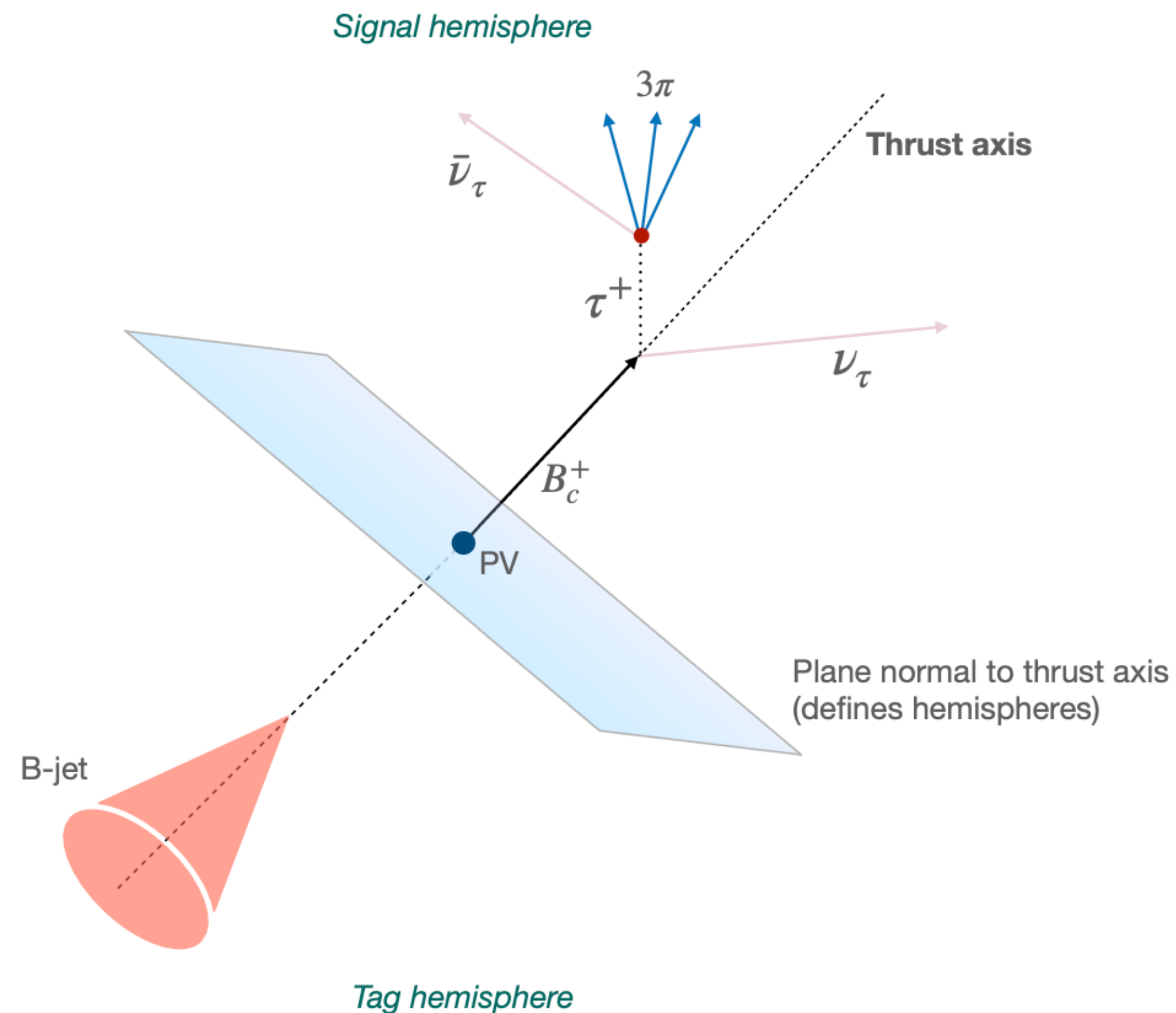
HFLAV Summer 2023	$R(D)$	$R(D^*)$
Meas. Ave.	0.357 ± 0.029	0.284 ± 0.012
Pred. Ave.	0.298 ± 0.004	0.254 ± 0.005

Case study - $B^+/B_c^+ \rightarrow \tau^+ \nu_\tau$

- Tag 3-prong hadronic decay of τ
- MVA analysis to separate B^+ , B_c^+ and backgrounds

- Measure $\mathcal{B}(B^+ \rightarrow \tau^+ \nu_\tau)$ and extract $|V_{ub}|$

$$\mathcal{B}(B_q^+ \rightarrow \tau^+ \nu_\tau)^{\text{SM}} = \tau_{B_q^+} \frac{G_F^2 |V_{qb}|^2 f_{B_q^+}^2 m_{B_q^+} m_\tau^2}{8\pi} \left(1 - \frac{m_\tau^2}{m_{B_q^+}^2}\right)^2, \quad q = u, c$$

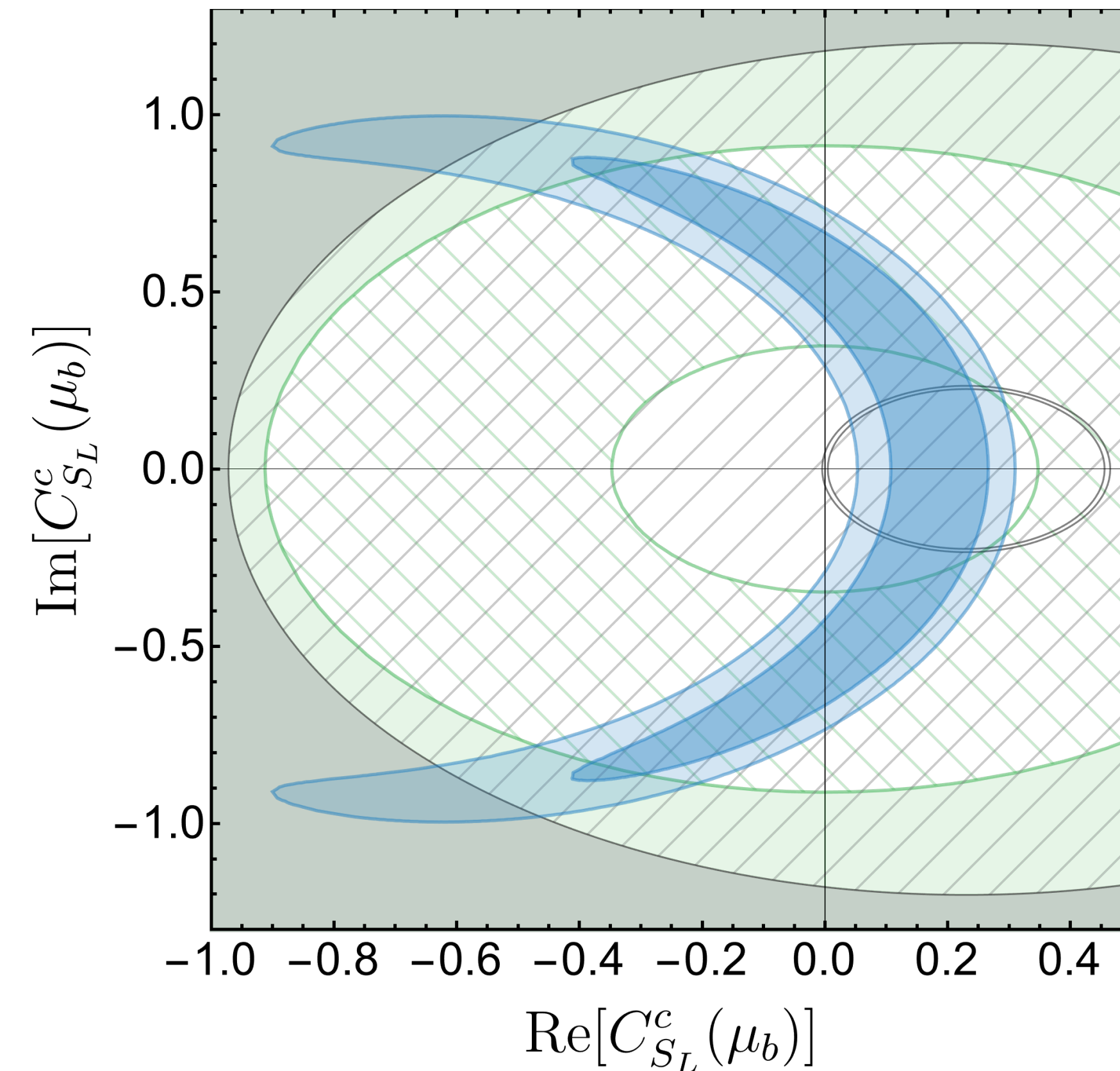
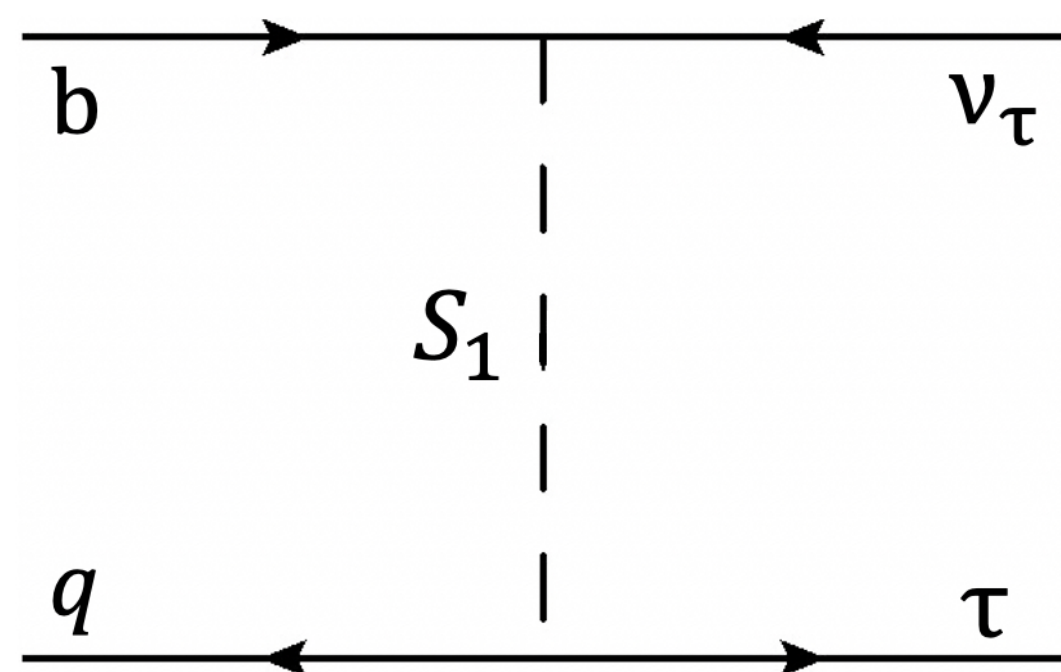


Case study - $B^+/B_c^+ \rightarrow \tau^+ \nu_\tau$

- Consider a generic EFT Hamiltonian that affects the $\mathcal{B}(B^+ \rightarrow \tau^+ \nu_\tau)$ and $\mathcal{B}(B_c^+ \rightarrow \tau^+ \nu_\tau)$

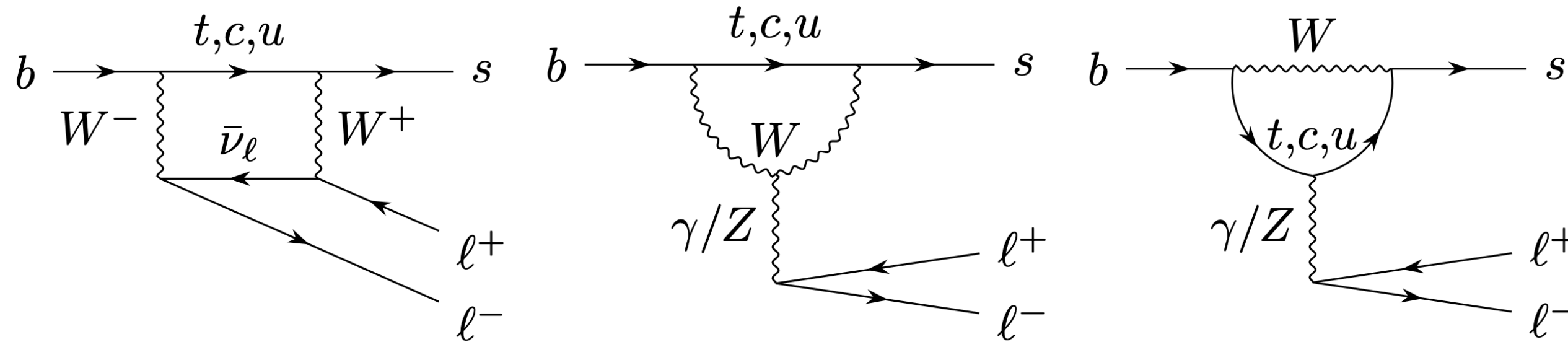
$$\mathcal{H}_{\text{eff}} = 2\sqrt{2}G_F \sum_{q=u,c} V_{qb} \left[(1 + C_{V_L}^q) (\bar{q}_L \gamma_\mu b_L) (\bar{\tau}_L \gamma^\mu \nu_L) + C_{V_R}^q (\bar{q}_R \gamma_\mu b_R) (\bar{\tau}_L \gamma^\mu \nu_L) \right. \\ \left. + C_{S_L}^q (\bar{q}_R b_L) (\bar{\tau}_R \nu_L) + C_{S_R}^q (\bar{q}_L b_R) (\bar{\tau}_R \nu_L) + C_T^q (\bar{q}_R \sigma_{\mu\nu} b_L) (\bar{\tau}_R \sigma^{\mu\nu} \nu_L) \right] + \text{h.c.},$$

- As an example, showing the interpretation of $B_c^+ \rightarrow \tau^+ \nu_\tau$ in the scalar leptoquark model

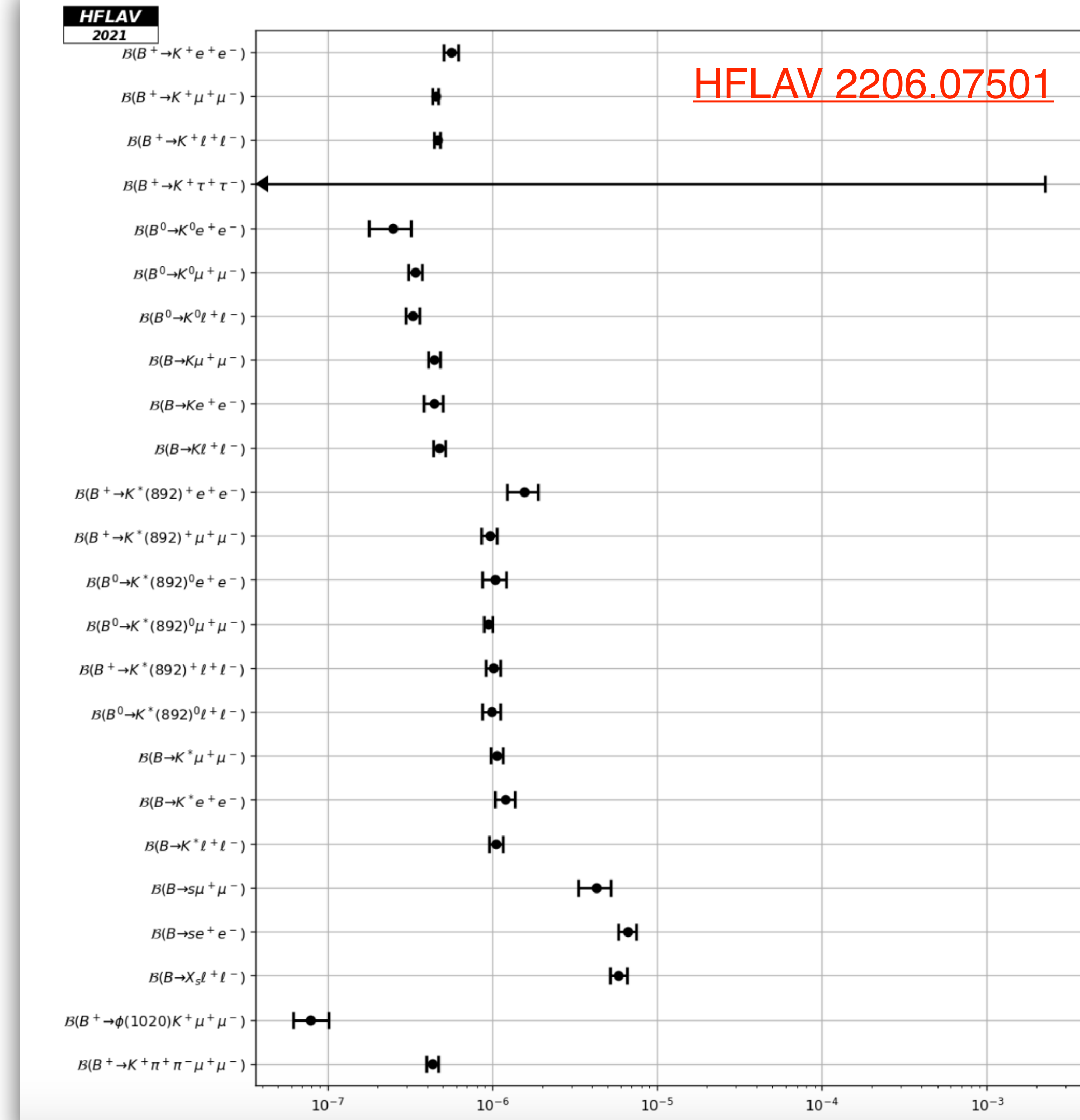


- Grey shade is the exclusion by current results
- Green hash is the exclusion expected for HL-LHC
- Grey hash is the exclusion by FCC-ee (the thin annulus survives)
- Blue shades are $1\sigma, 2\sigma, 3\sigma$ bands from current $b \rightarrow c$ anomalies

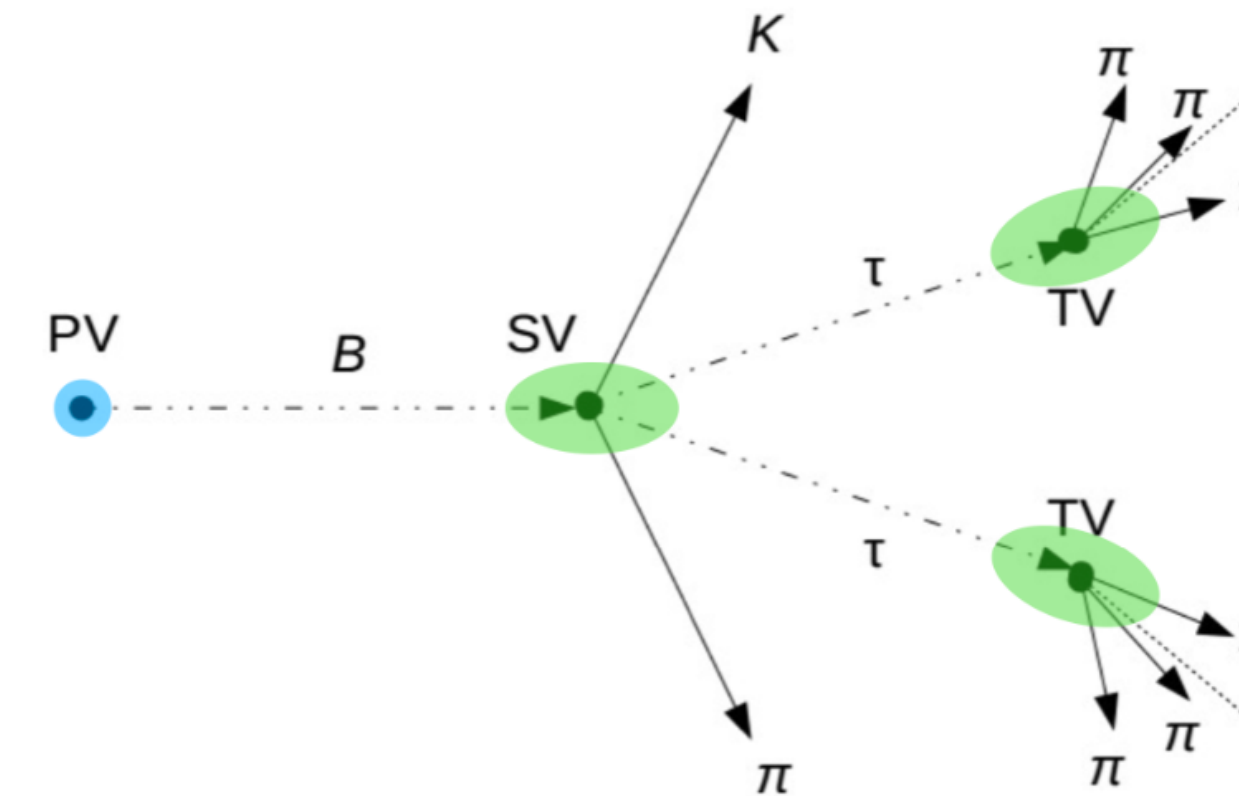
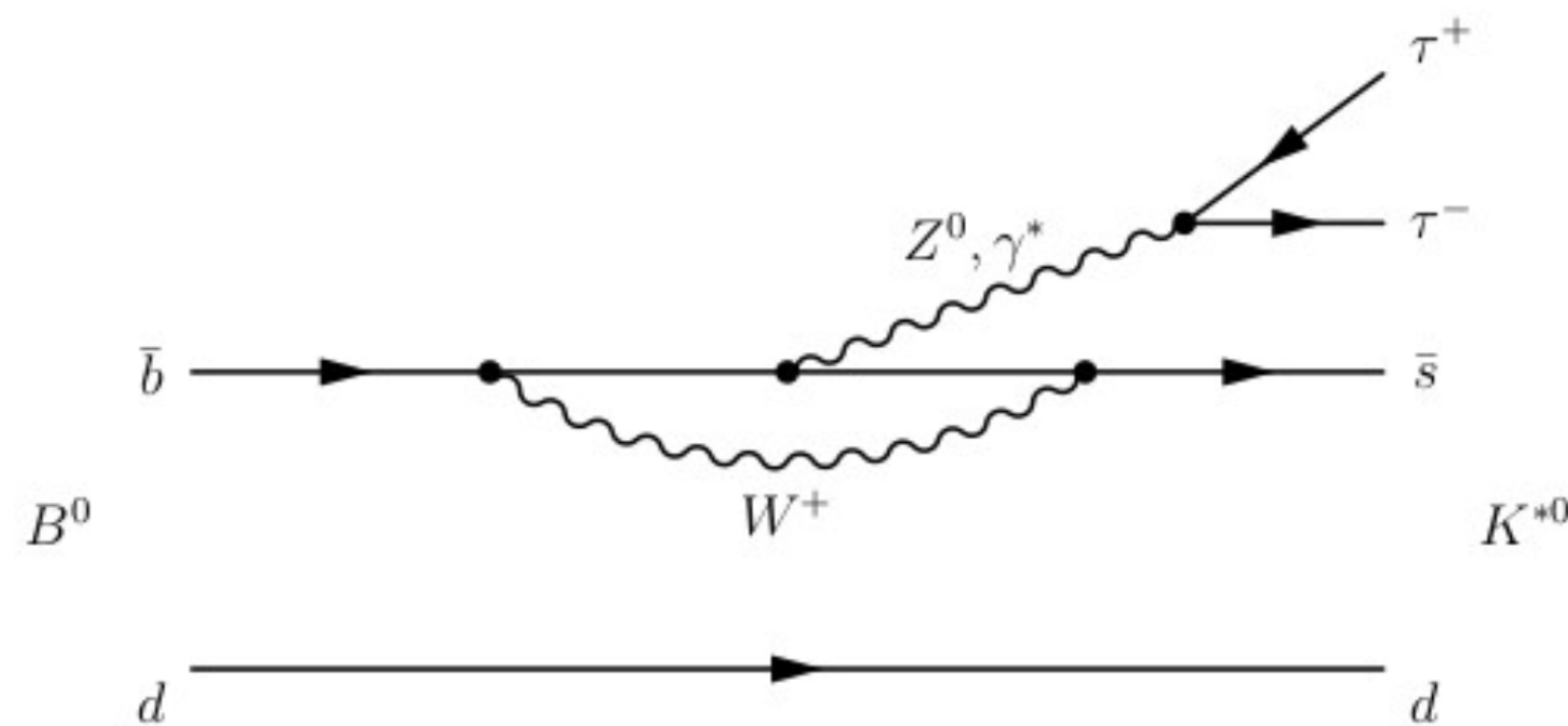
$b \rightarrow s \ell \ell$ transition



- Mediated by different diagrams in SM, with their relative importance varying with $q^2 = M_{\ell\ell}^2$
- Highly sensitive to BSM modification (also with large uncertainties due to non-perturbative QCD)
- R_K and R_{K^*} to be tested at higher precision
- $b \rightarrow s \ell \ell$ not yet established for τ
 - Expected $BR_{SM}(B \rightarrow K \tau \tau) \sim O(10^{-7})$

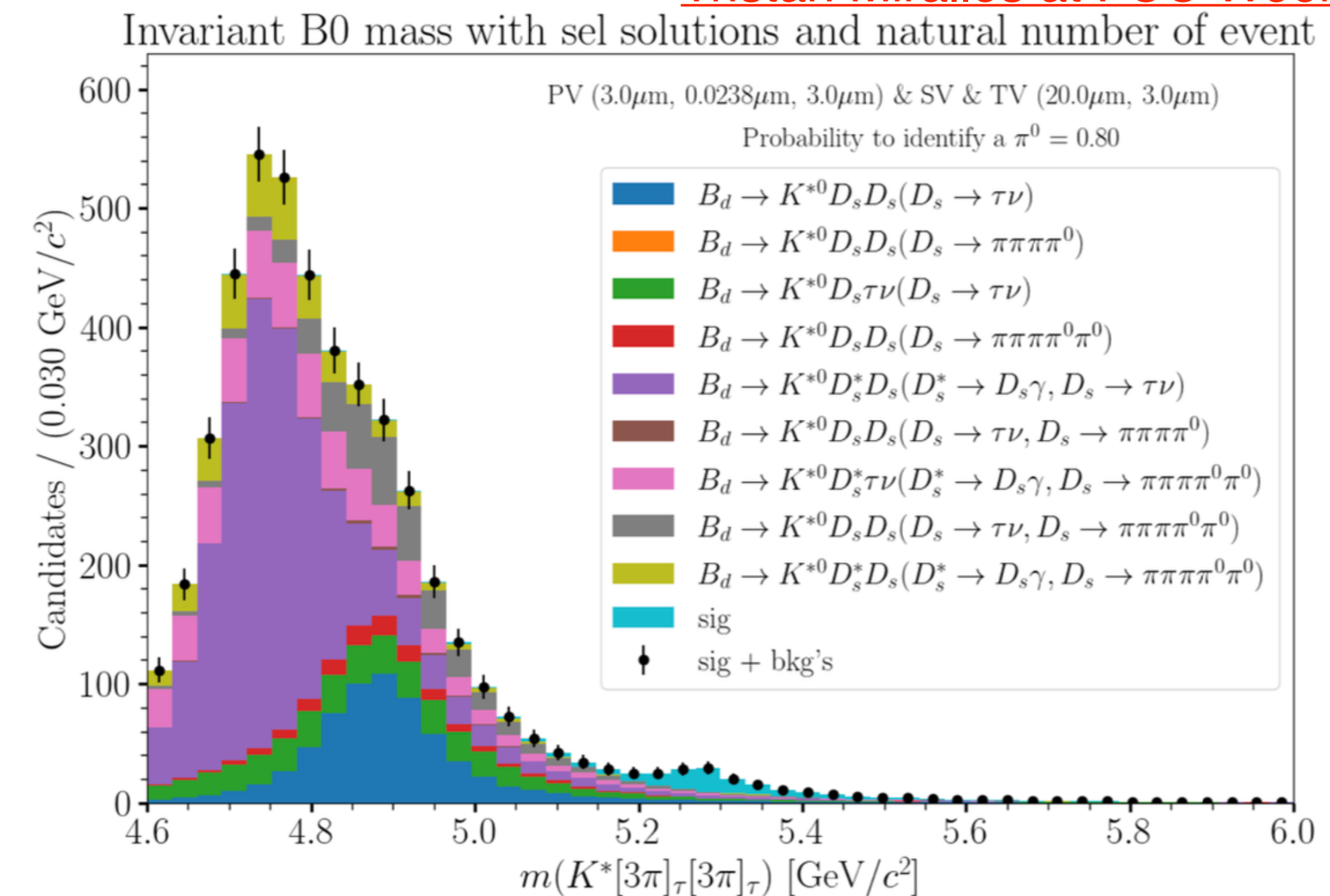


Case study - $B^0 \rightarrow K^{*0} \tau^+ \tau^-$



Tristan Miralles at FCC Week

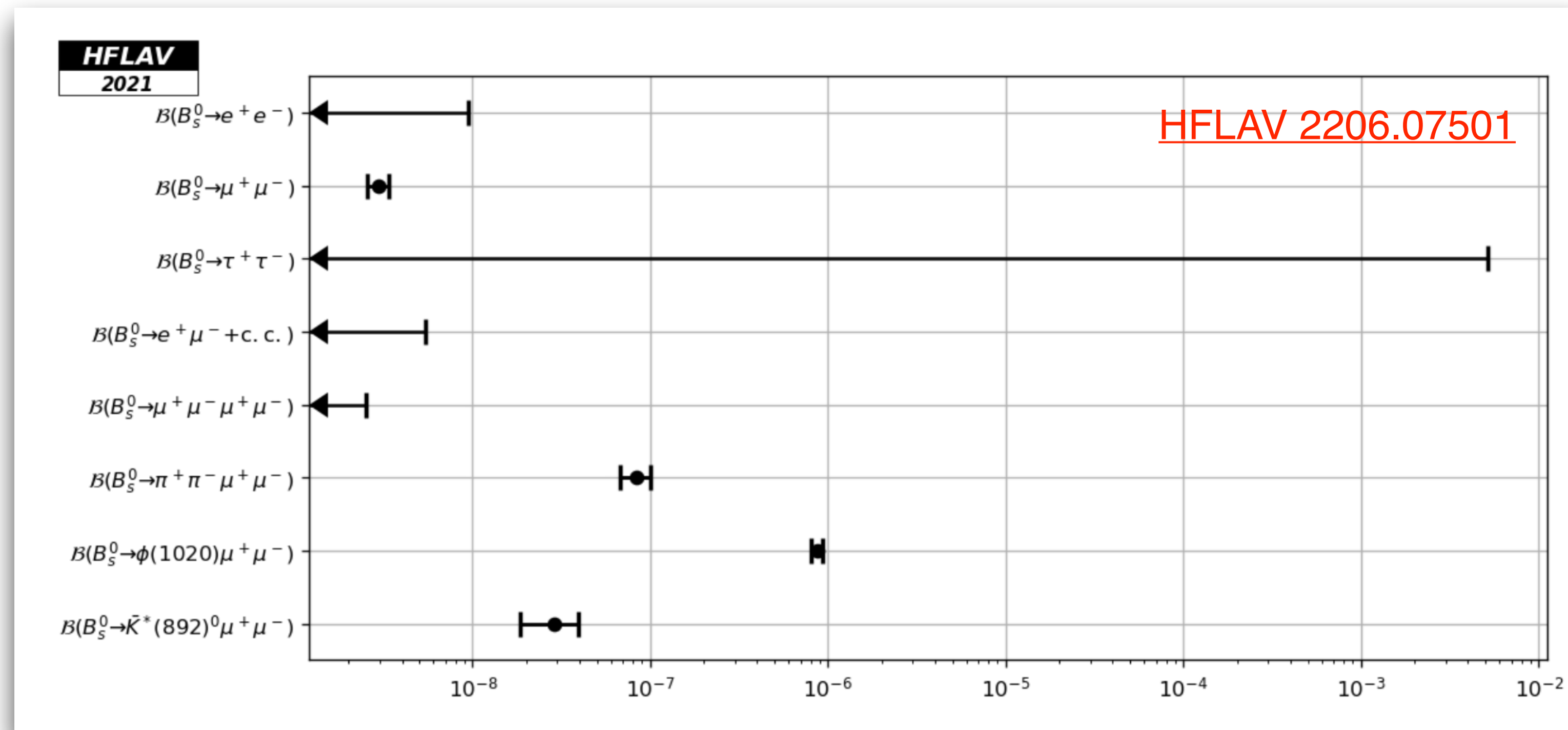
- Event kinematics fully reconstructable
- Background with the same final state can be separated by kinematic properties
 - More ongoing studies on comprehensive backgrounds toward a full analysis
- The goal is to understand the performance/requirements for vertex detectors (backup for π^0 ID)



$b \rightarrow s \ell \ell$ transition

- Purely leptonic $B_s \rightarrow \ell^+ \ell^-$ are clean probes for theory interpretations.
- SM expectation for $\mathcal{B}(B_s \rightarrow \tau^+ \tau^-) \approx 200 \times \mathcal{B}(B_s \rightarrow \mu^+ \mu^-)$
 - Difficult at LHCb and Belle II, well-identifiable at FCC-ee.
 - New probe of CP structure through τ polarization.

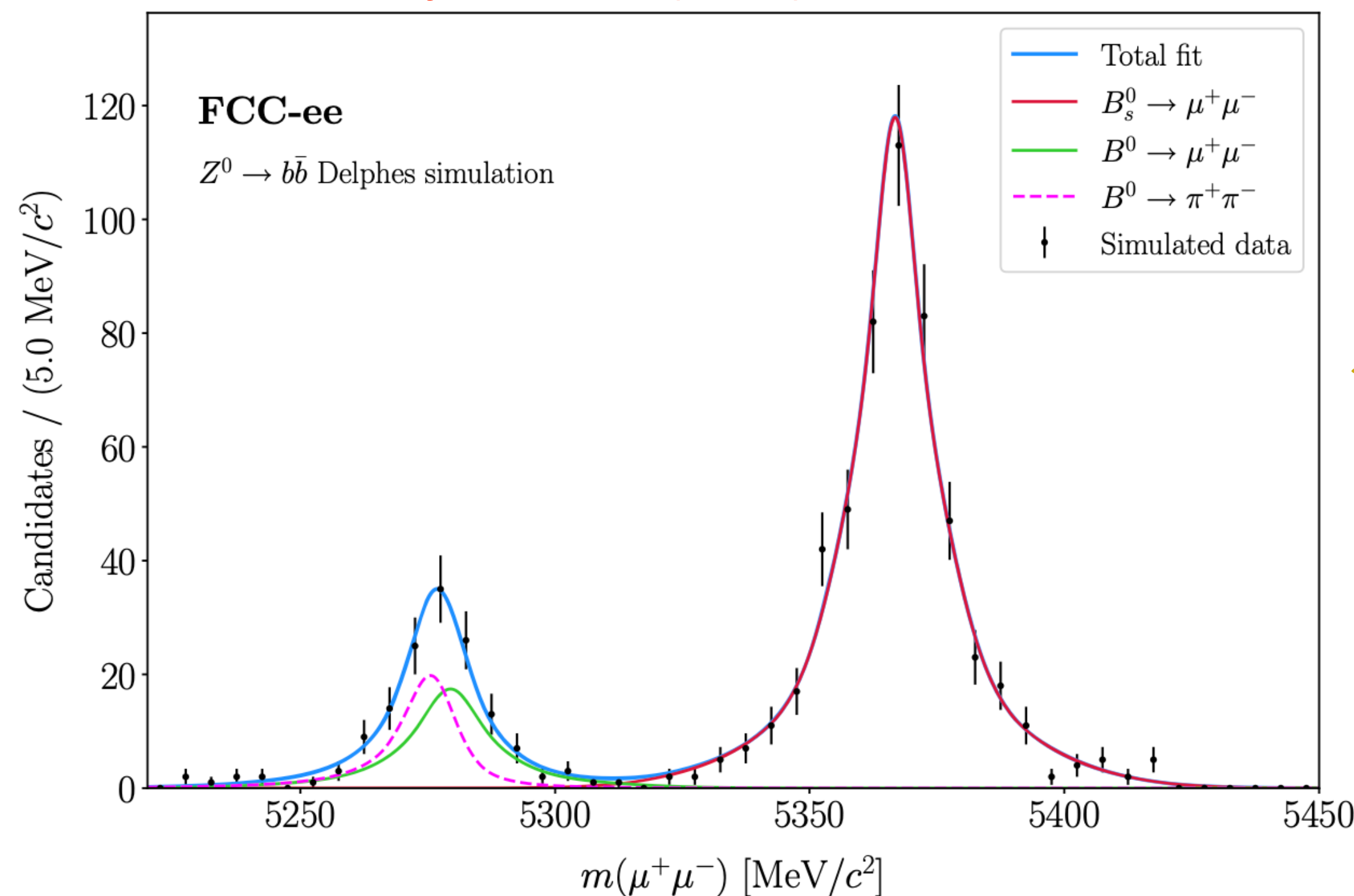
- Additional tests of CLFV decays of $B_s \rightarrow \tau \mu$ and $B_s \rightarrow \tau e$ at extreme precisions
 - Still room for large NP effects



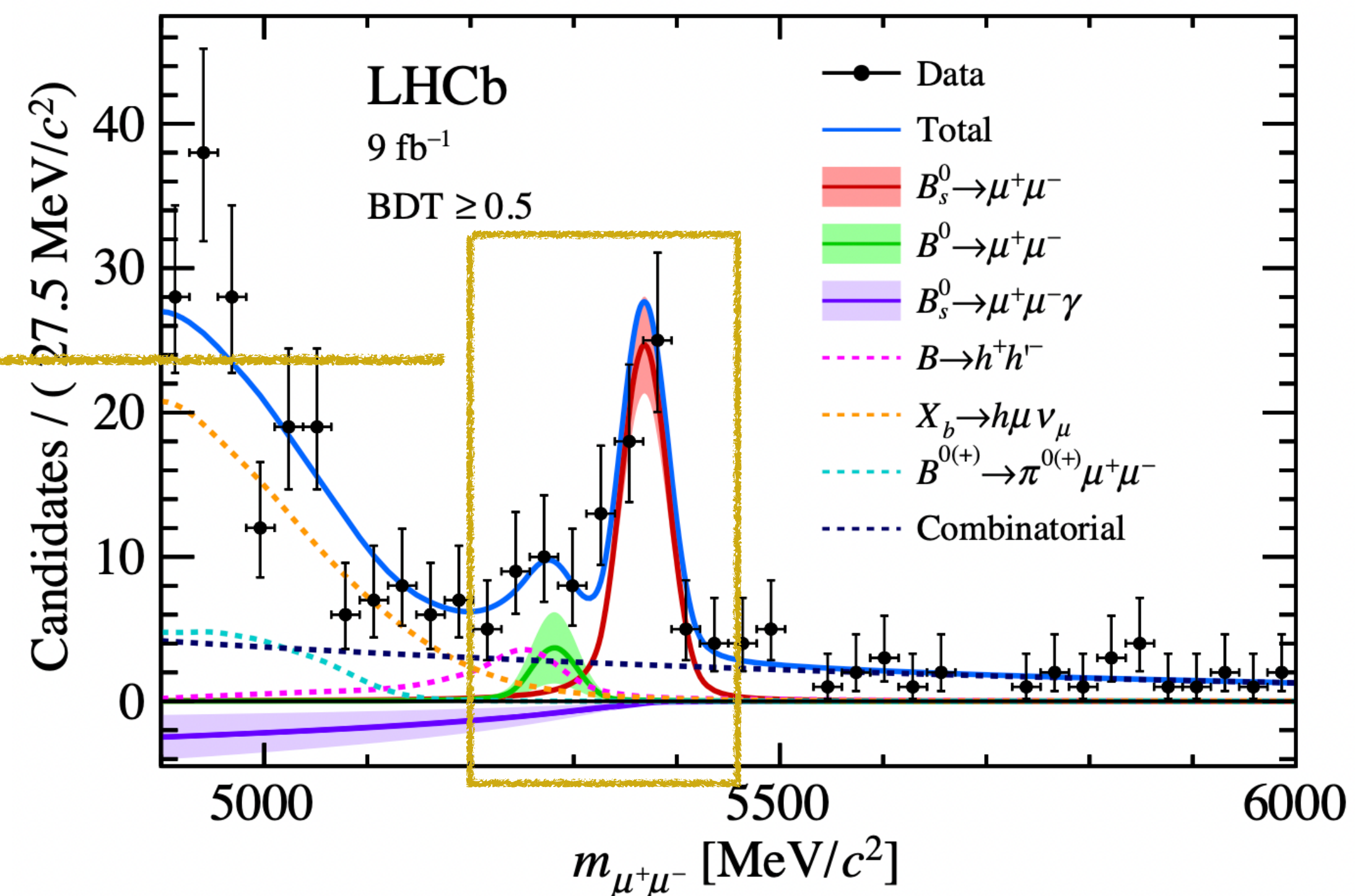
Case study - $B^0/B_s^0 \rightarrow \mu^+\mu^-$

- Measurements of ultra-rare $B \rightarrow \mu^+\mu^-$, some unique at FCC-ee
- High invariant-mass resolution expected from excellent tracking performance
- Controlling the misidentification of π^+ as μ^+ is an important consideration in detector design

[Eur. Phys. J. Plus \(2021\) 136:837](#)

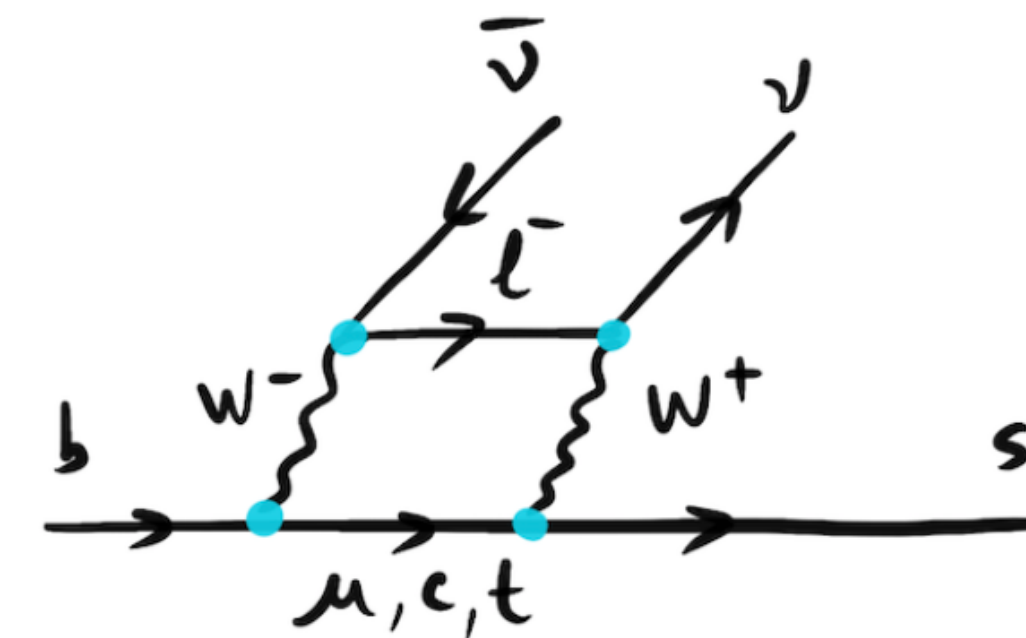
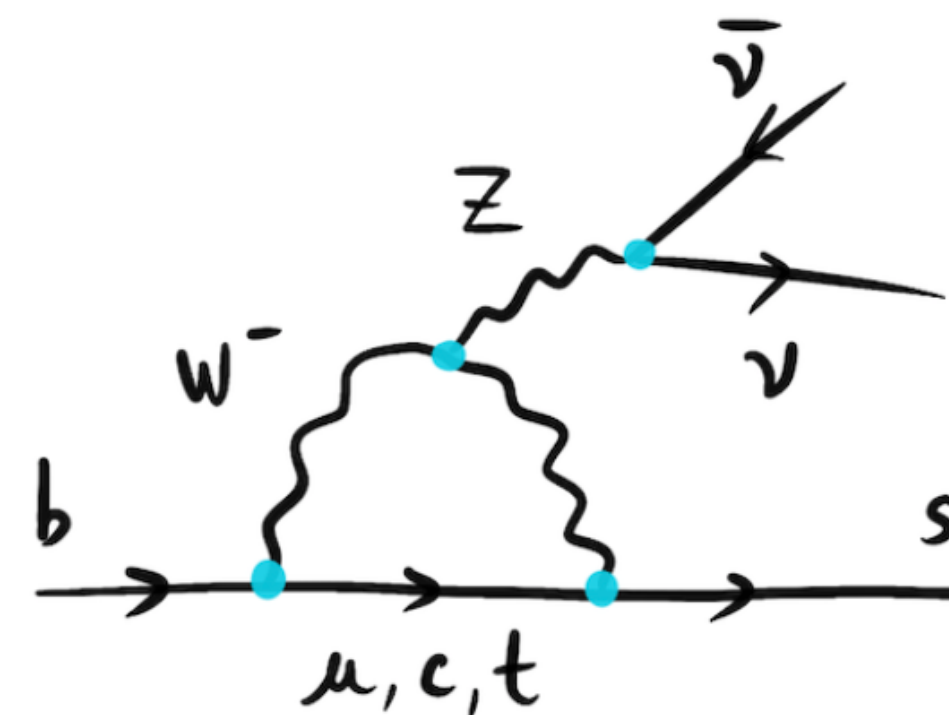


[Phys. Rev. Lett. 128, 041801](#)



$b \rightarrow s\nu\nu$ transition

- Probe of NP complementary to $b \rightarrow c\ell\nu$ and $b \rightarrow s\ell\ell$
- SM $\mathcal{B}(b \rightarrow s\nu\nu) \approx 10^{-5}$
 - First evidence of $B^+ \rightarrow K^+\nu\nu$ ([Eldar Ganiev at EPS2023](#))
 - Belle II expect 10% precision on $B \rightarrow K^{(*)}\nu\nu$ (projection to be updated)
 - Unique opportunities for $B_s \rightarrow \phi\nu\nu$, $\Lambda_b \rightarrow \Lambda\nu\nu$, and $B_c \rightarrow D_s\nu\nu$ at FCC-ee



- Low energy Hamiltonian written as
- in which SM corresponds to $C_L = -6.35$, $C_R = 0$

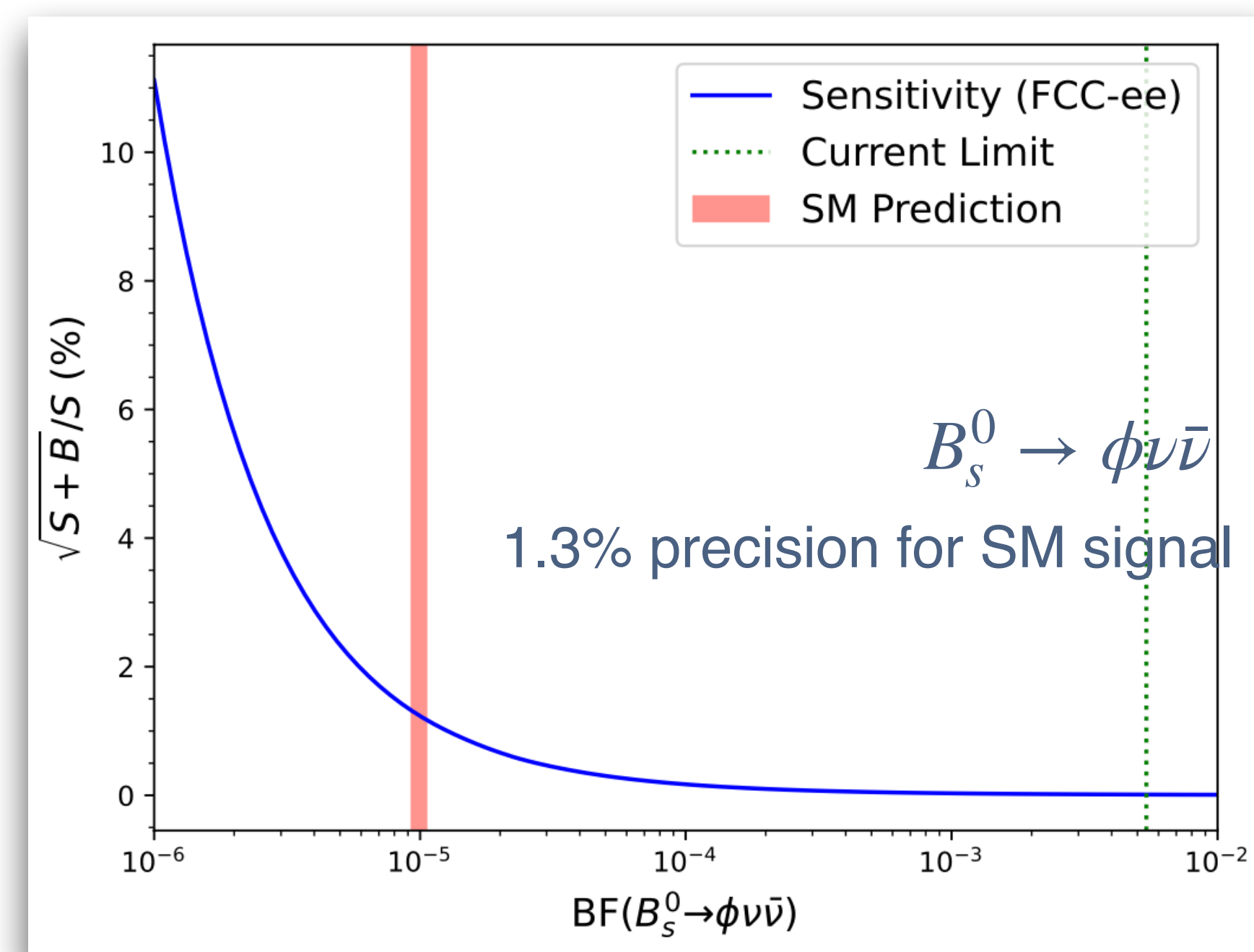
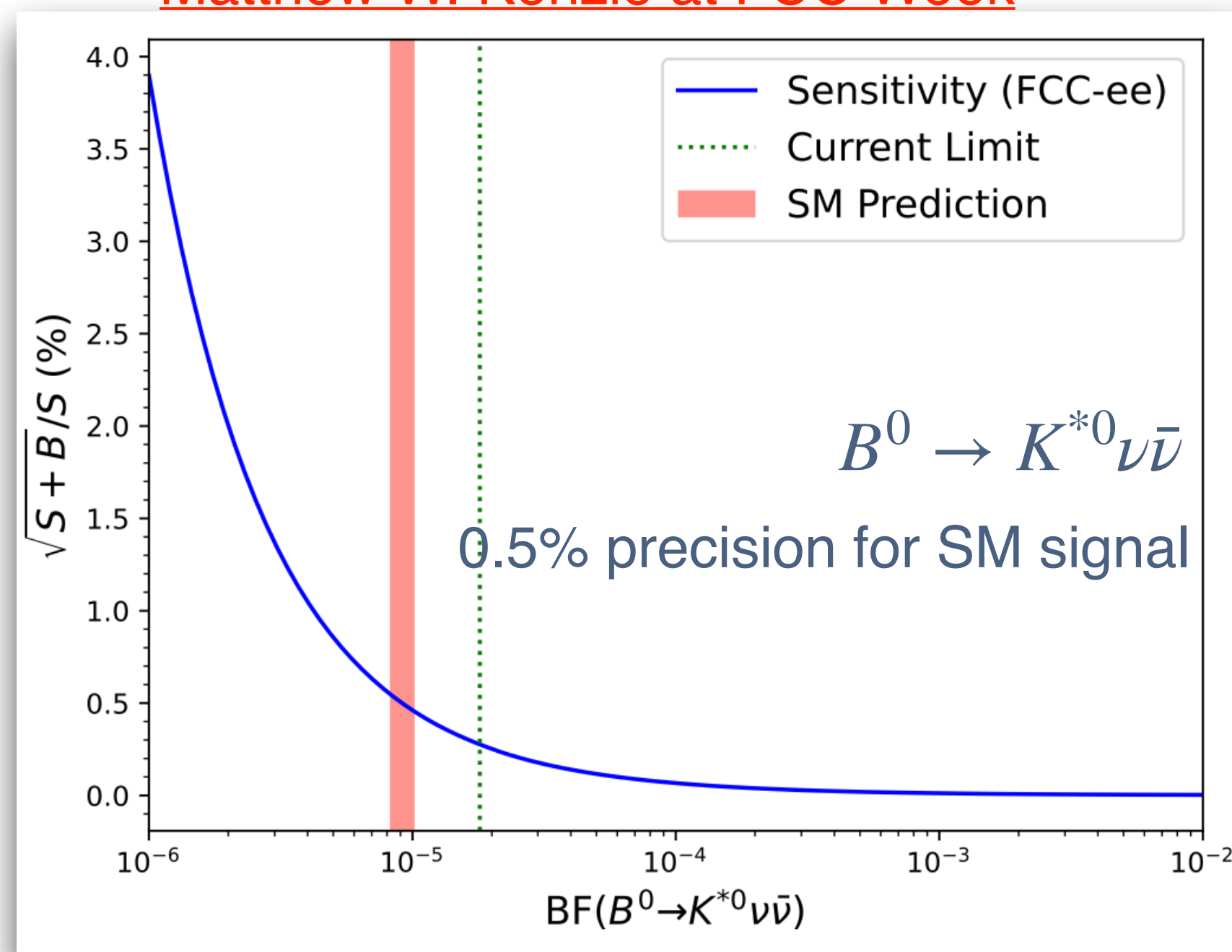
$$H_{\text{eff}} = -\frac{G_F}{\sqrt{2}} V_{tb} V_{ts}^* (C_L O_L + C_R O_R) + \text{h.c.}$$

$$O_{L(R)} = \frac{e^2}{2\pi^2} (\bar{s} \gamma^\mu P_{L(R)} b) (\bar{\nu}_l \gamma_\mu P_L \nu_l)$$

Case study - $b \rightarrow s\nu\nu$

- (Preliminary) expect O(1%) precision for $B^0 \rightarrow K^{*0}\nu\bar{\nu}$ and $B_s^0 \rightarrow \phi\nu\bar{\nu}$
 - Requires excellent vertex resolution and particle identification

Matthew W. Kenzie at FCC Week



- Study at CEPC with similar performance ([Li et al. 2201.07374](#))
- Proposal for studies of time-dependent CP asymmetry ([Descotes-Genon et al. 2208.10880](#))

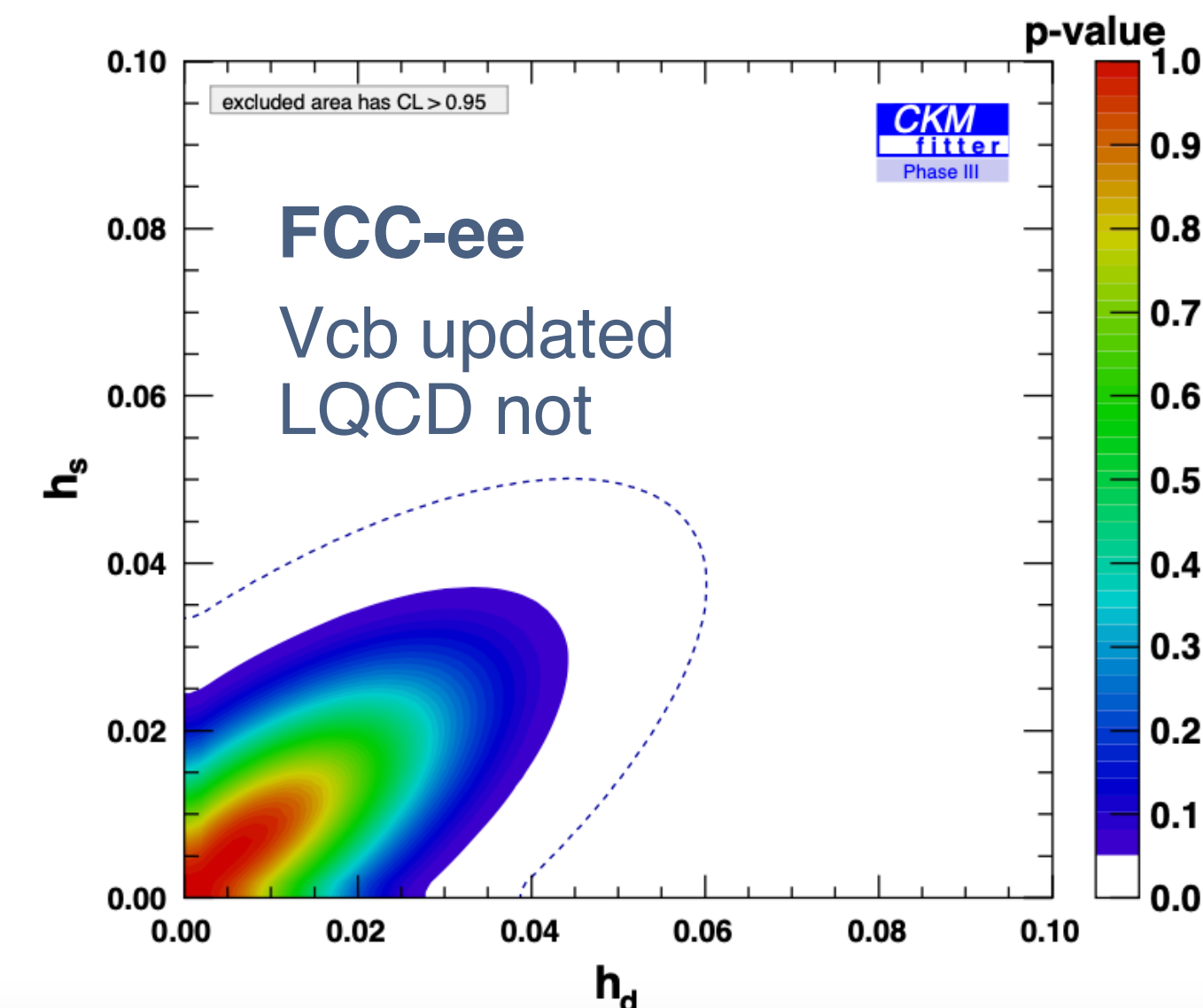
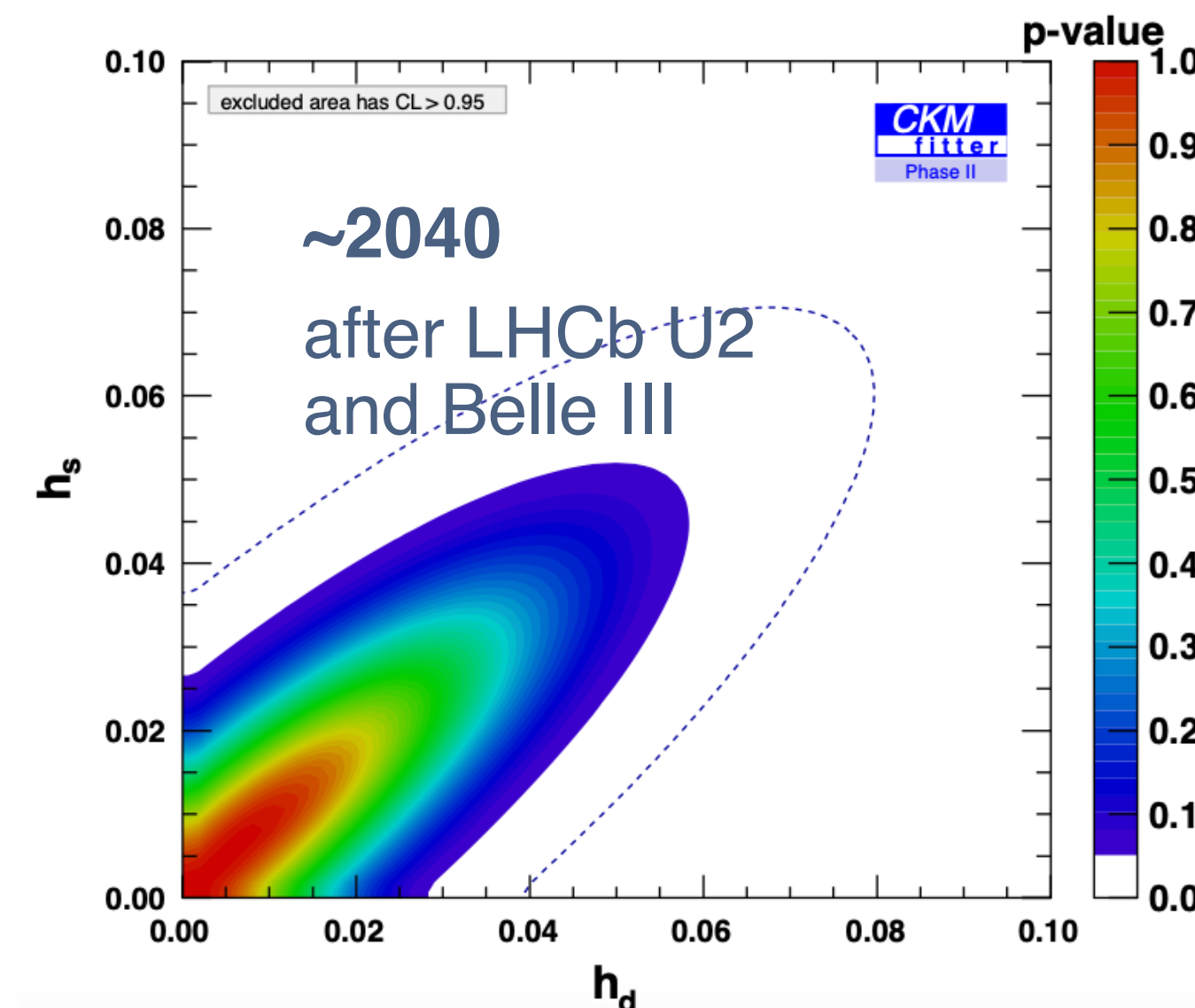
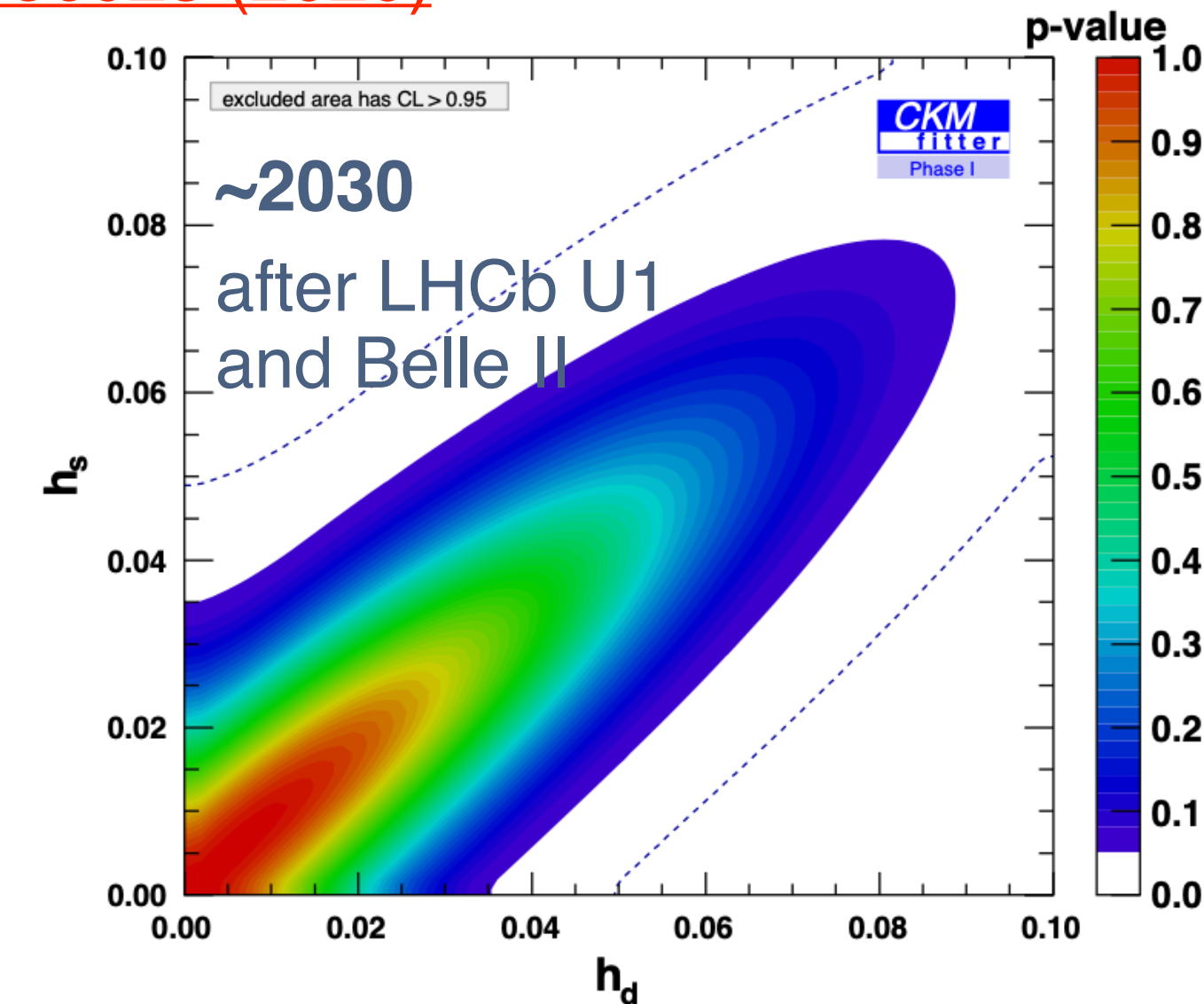
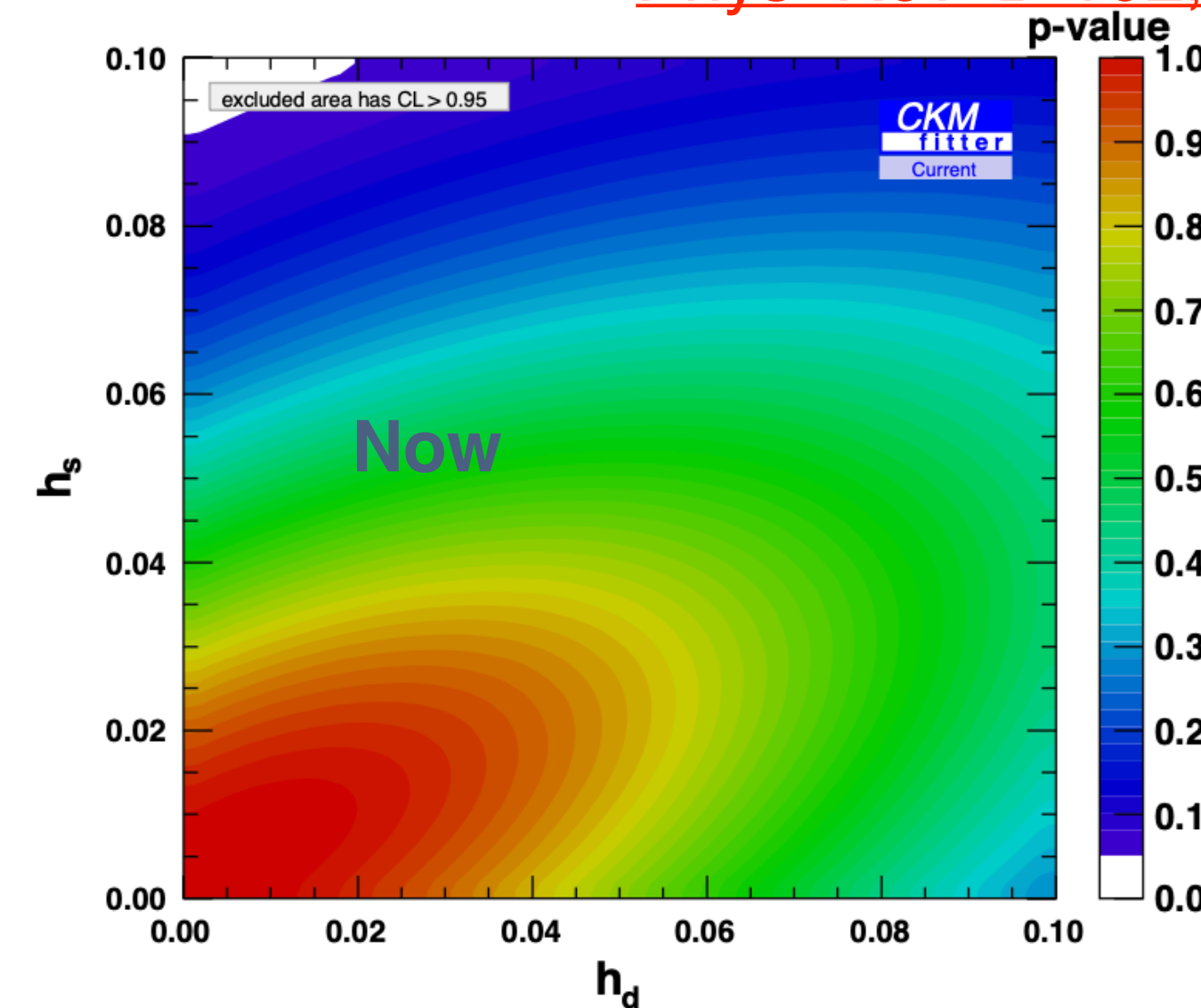
B^0/B_s^0 mixing

Phys. Rev. D 102, 056023 (2020)

- Model-independent search for CPV in the $B^0 - \bar{B}^0$ and $B_s^0 - \bar{B}_s^0$ mixings

$$M_{12} = M_{12}^{\text{SM}} \times (1 + h_{d,s} e^{2i\sigma_{d,s}})$$

- $|V_{cb}|$ precision and LQCD mixing parameters are main sources of uncertainty.
 - $|V_{cb}|$ will be greatly improved at FCC-ee with on-shell W decays



non-b flavor physics

- Charm physics
- tau physics
- Other flavor physics with Z , W , H , t

Appealing opportunities. Experimental performance to be studied

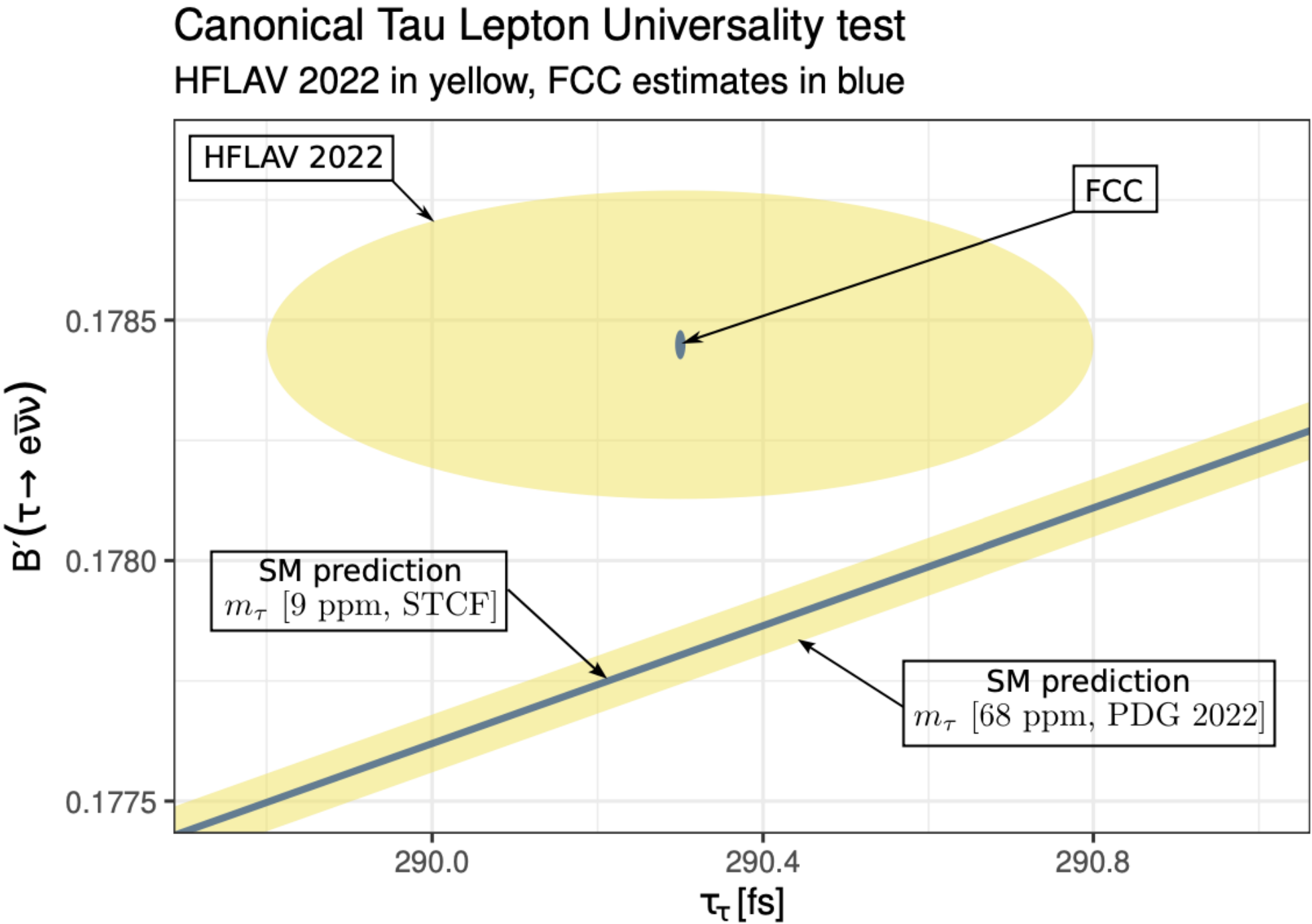
- FCNC $c \rightarrow u\nu\nu$ decay
[Phys. Rev. D 103, 015033](#)
 - $D \rightarrow \pi\nu\nu$, $D_s \rightarrow K\nu\nu$, $\Lambda_c^+ \rightarrow p\nu\nu$, etc.
 - Complementary to $c \rightarrow ull$ channels
 - Clean null tests of SM, only exp result to date $\mathcal{B}(D \rightarrow \pi\nu\nu) < 2.1 \times 10^{-4} @ 90\% \text{ CL}$ ([Phys. Rev. D 105, L071102](#))
 - BR can be probed down to 10^{-6} level at FCC-ee
- Pure leptonic $D^0 \rightarrow l^+l^-$ decay
[Belle II physics book](#)
 - Very little SM contribution
 - NP that contributes to $c \rightarrow ull$ would also have effect on $D^0 \rightarrow l^+l^-$
- CP asymmetry in $D^+ \rightarrow \pi^+\pi^0$ and $D^0 \rightarrow K_s^0K_s^0$ decays
 - CP violation for $D^0 \rightarrow K_s^0K_s^0$ may be $\sim 1\%$ in SM, could become the first evidence of CP violation in charm sector
 - CP violation for $D^+ \rightarrow \pi^+\pi^0$ is 0 in SM, good null test
[Phys. Rev. D 92, 054036](#)

tau properties

- High precision on tau properties (complementary to STCF)
 - Lifetime measurement benefits from high boost in $Z \rightarrow \tau\tau$ decays
 - LFU test of $\mathcal{B}(\tau \rightarrow e\nu\nu)/\mathcal{B}(\tau \rightarrow \mu\nu\nu)$
 - Need m_τ input from future τ -factories
 - Systematic uncertainties to be studied and improved

Observable	Measurement	Current precision	FCC-ee stat.	Possible syst.	Challenge
m_τ [MeV]	Threshold / inv. mass endpoint	1776.86 ± 0.12	0.005	0.12	Mass scale
τ_τ [fs]	Flight distance	290.3 ± 0.5 fs	0.005	< 0.040	Vertex detector alignment
$\mathcal{B}(\tau \rightarrow e\nu\nu)$ [%]	Selection of $\tau^+\tau^-$, identification of final state	17.82 ± 0.05	0.0001	No estimate; possibly 0.003	Efficiency, bkg, Particle ID
$\mathcal{B}(\tau \rightarrow \mu\nu\nu)$ [%]		17.39 ± 0.05			

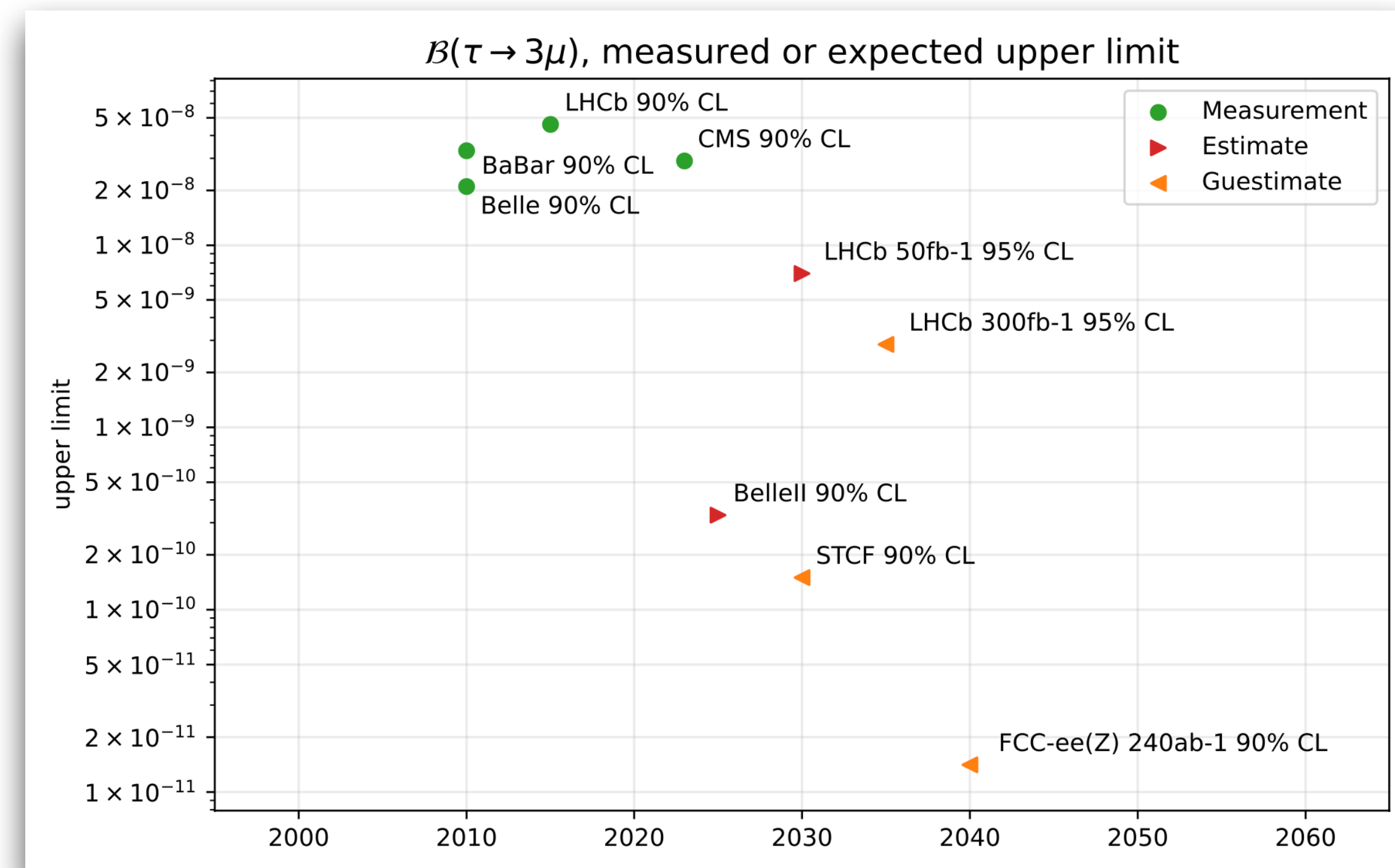
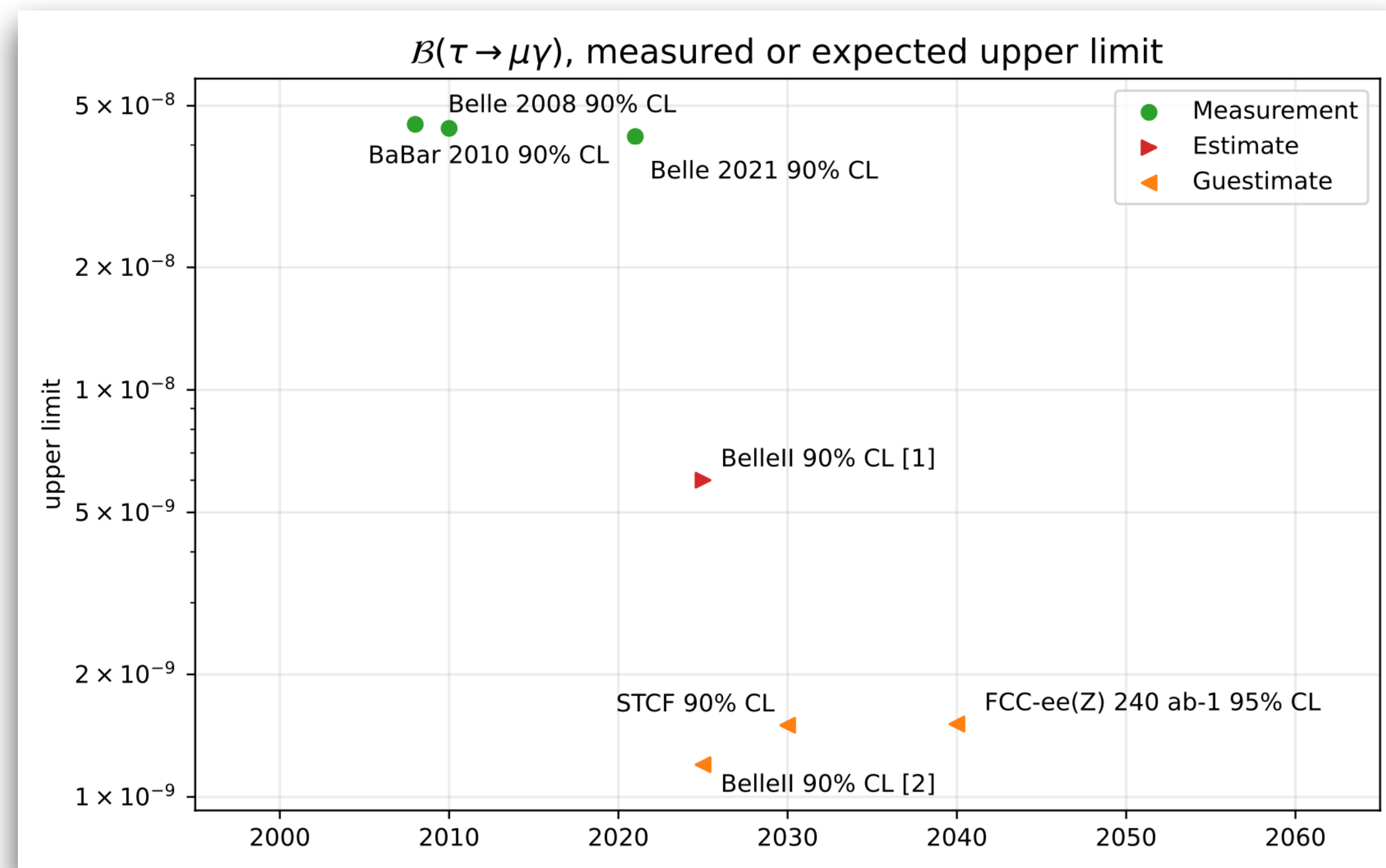
Mogens Dam at WS TAU



Alberto Lusiani at CLFV2023

CLFV tau decays

- All NP introducing $\mu \leftrightarrow e$ also call for $\tau \leftrightarrow \mu/e$
 - Usually more pronounced from m_τ/m_μ
 - Potential indirect constraint on $\mu \leftrightarrow e$ through $\mu \rightarrow \tau^* \times \tau^* \rightarrow e$ ([Ardu et al. 2202.09246](#))
- Precision at FCC-ee benefit from high efficiency and copious events

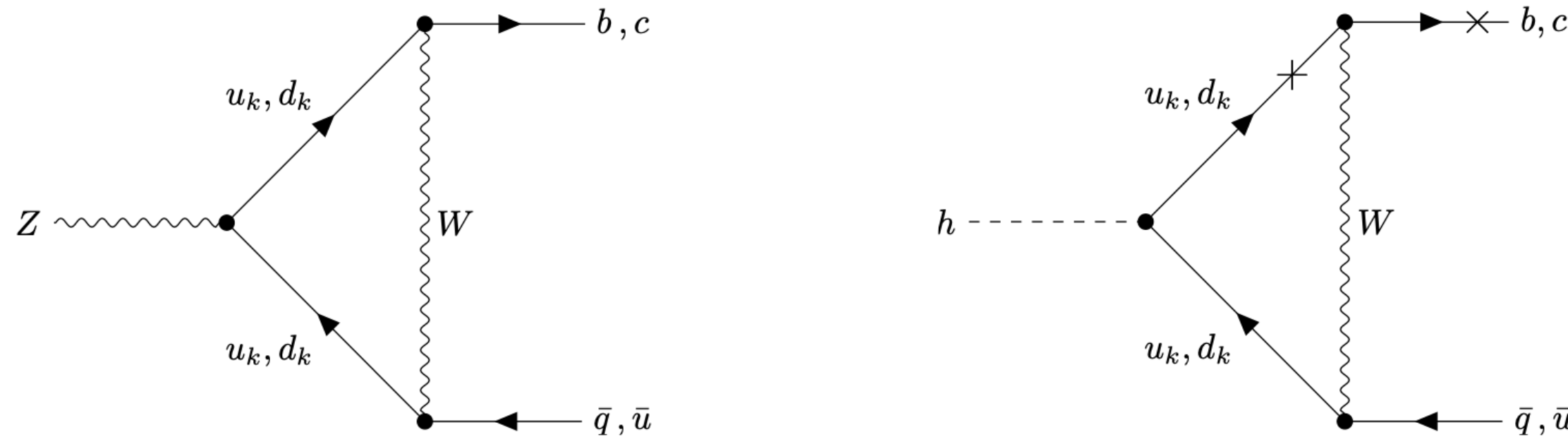


[Alberto Lusiani at CLFV2023](#)

Other opportunities

- Flavor changing decays of Z and H non-vanishing in SM

- $\mathcal{B}(Z \rightarrow bs)^{\text{SM}} = (4.2 \pm 0.7) \times 10^{-8}$
- $\mathcal{B}(H \rightarrow bs)^{\text{SM}} = (8.9 \pm 1.5) \times 10^{-8}$



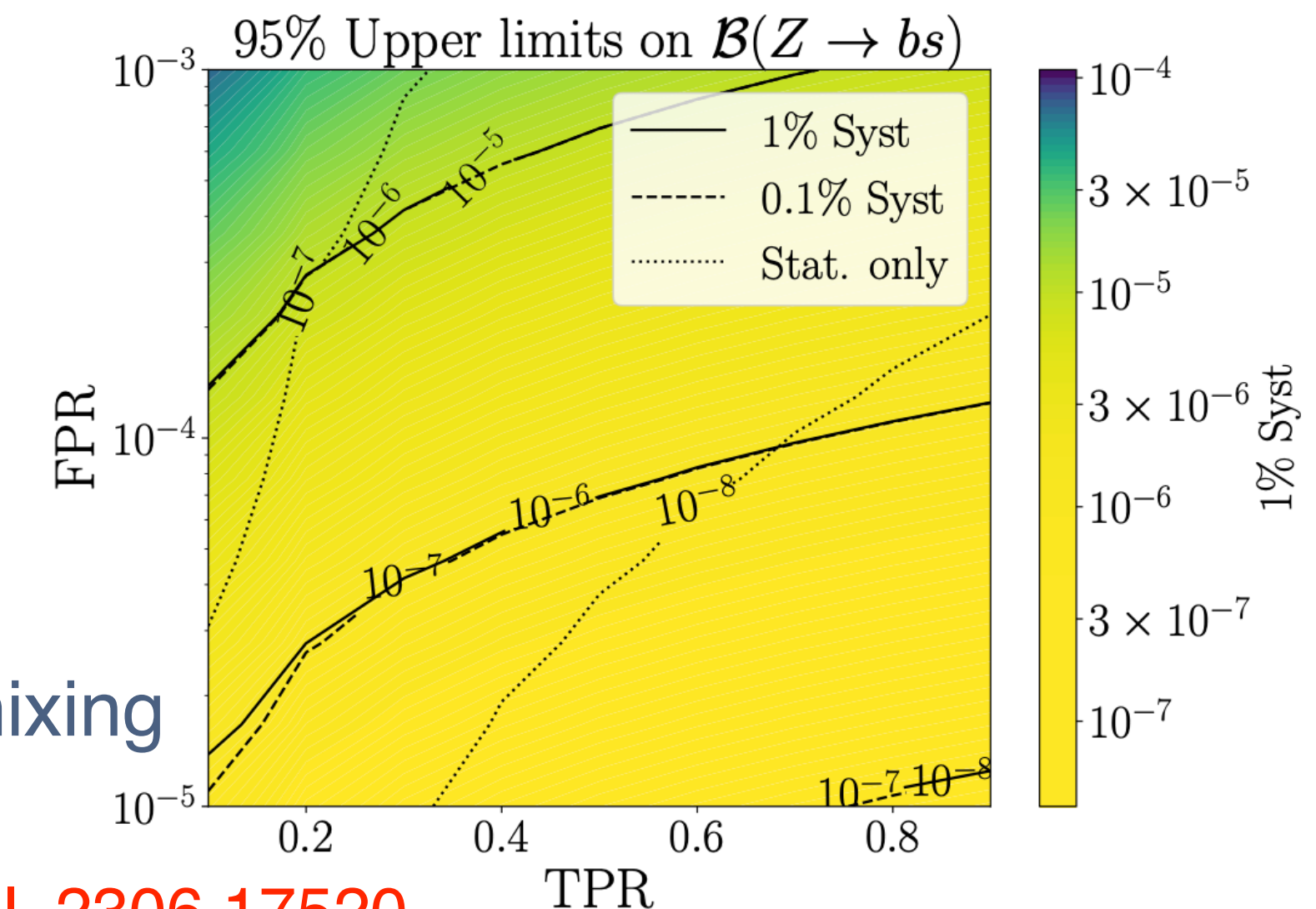
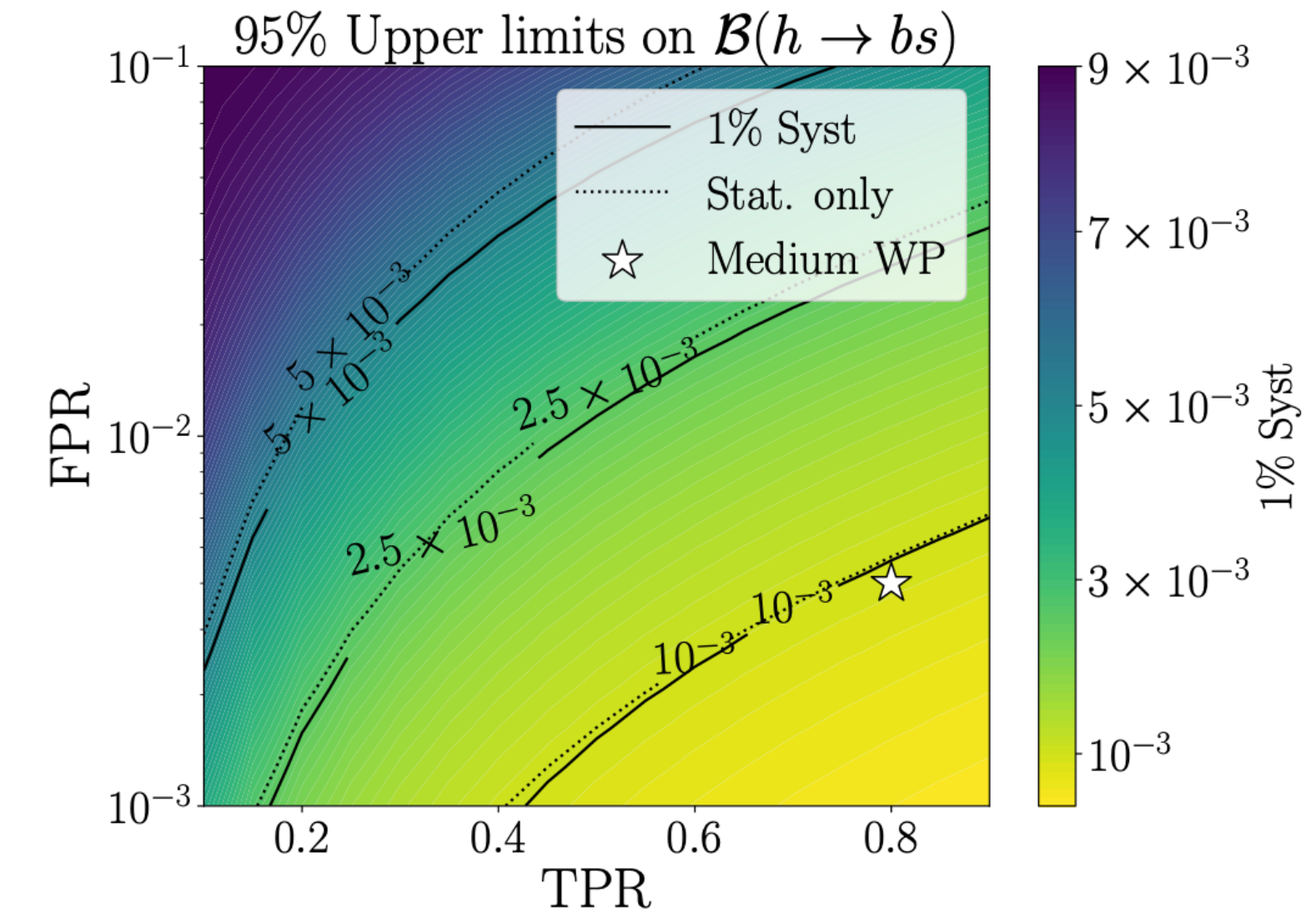
- With BSM modification

- $\mathcal{L} \supset g_{sb}^L (\bar{s}_L \gamma_\mu b_L) Z^\mu + g_{sb}^R (\bar{s}_R \gamma_\mu b_R) Z^\mu + y_{sb} (\bar{s}_L b_R) h + y_{bs} (\bar{b}_L s_R) h + \text{h.c.}$

- Requires excellent flavor tagging efficiency and fake rate

- Potential to probe Z-FCNC at SM level

- $H \rightarrow qq'$ complementary to indirect constraints from $B_s^0 - \bar{B}_s^0$ or $D - \bar{D}$ mixing



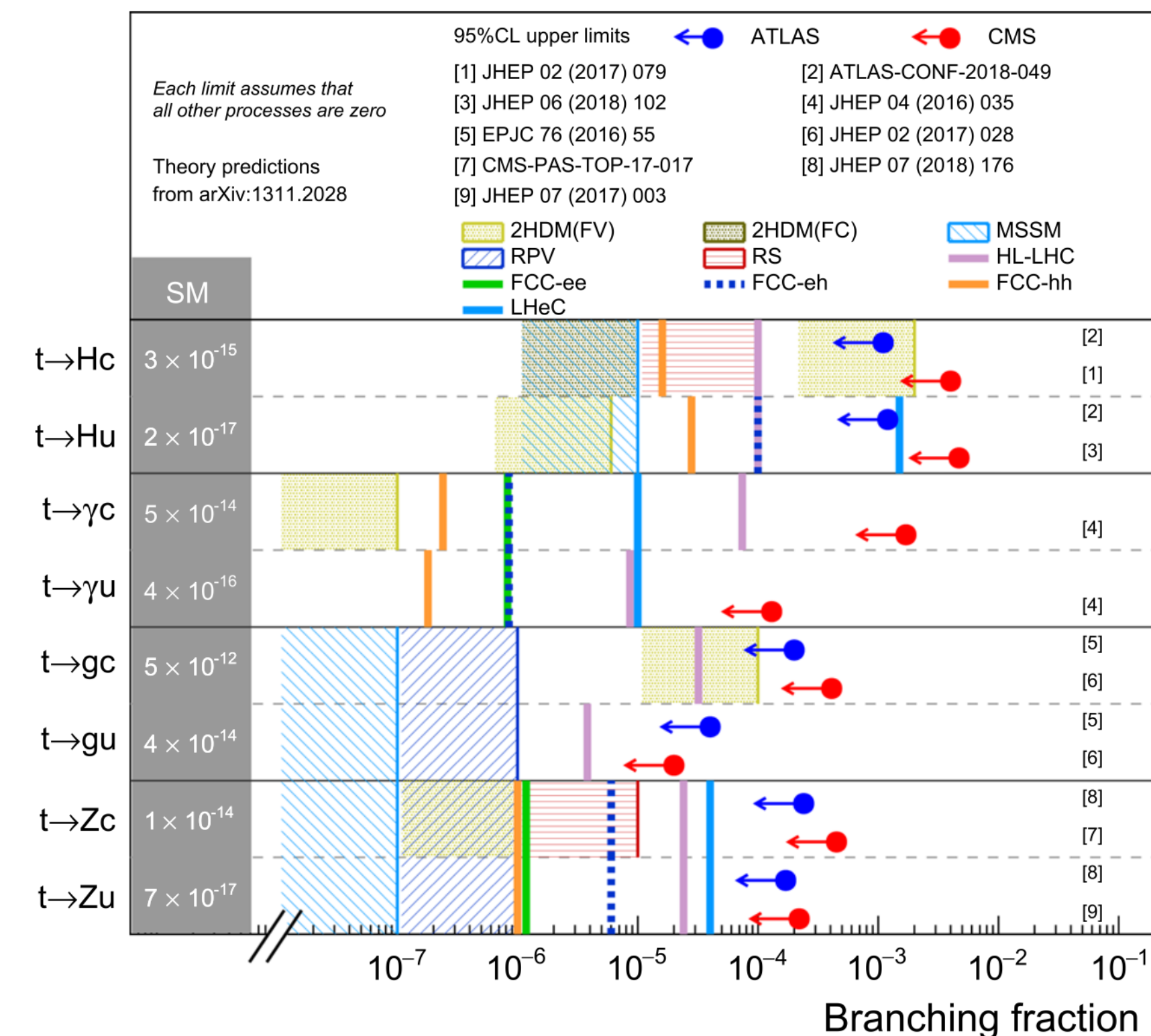
[J. F. Kamenik et al. 2306.17520](#)

Other opportunities



- Test CLFV in $Z \rightarrow \tau\mu$, $Z \rightarrow \tau e$ decays and $H \rightarrow ll'$ decays
 - Probe BR down to $10^{-8} - 10^{-10}$ ([SciPost Phys. Proc. 1, 041 \(2019\)](#))
- FCNC in top quark decays
 - Advantage in $t \rightarrow \gamma q$ and $t \rightarrow Zq$ at FCC-ee
 - distinguish c from u
- Measure CKM elements with on-shell $W \rightarrow bc$, $W \rightarrow cs$ decays
 - Expect excellent vertexing and flavor tagging efficiencies
 - Direct (theory-free) determination.
 - (Preliminary) expect $|V_{cb}|$ precision at 0.4%

FCC CDR



Summary



FCC-ee/CEPC is THE awesome next-generation flavor machine!



Backup

Phys. Rev. D 102, 056023 (2020)

	Central values	Uncertainties				Reference Phases I–III
		Current [28]	Phase I	Phase II	Phase III	
$ V_{ud} $	0.97437	± 0.00021	id	id	id	[28]
$ V_{us} f_+^{K \rightarrow \pi}(0)$	0.2177	± 0.0004	id	id	id	[28]
$ V_{cd} $	0.2248	± 0.0043	± 0.003	id	id	[40,41]
$ V_{cs} $	0.9735	± 0.0094	id	id	id	[28,40,41]
Δm_d [ps ⁻¹]	0.5065	± 0.0019	id	id	id	[17]
Δm_s [ps ⁻¹]	17.757	± 0.021	id	id	id	[17]
$ V_{cb} _{\text{SL}} \times 10^3$	42.26	± 0.58	± 0.60	± 0.44	id	[29]
$ V_{cb} _{W \rightarrow cb} \times 10^3$		...	...	...	± 0.17	[34–36]
$ V_{ub} _{\text{SL}} \times 10^3$	3.56	± 0.22	± 0.042	± 0.032	id	[29]
$ V_{ub}/V_{cb} $ (from Λ_b)	0.0842	± 0.0050	± 0.0025	± 0.0008	id	[30]
$\mathcal{B}(B \rightarrow \tau \nu) \times 10^4$	0.83	± 0.24	± 0.04	± 0.02	± 0.009	[29,34]
$\mathcal{B}(B \rightarrow \mu \nu) \times 10^6$	0.37	...	± 0.03	± 0.02	id	[29]
$\sin 2\beta$	0.680	± 0.017	± 0.005	± 0.002	± 0.0008	[29,30,34]
α [°] (mod 180°)	91.9	± 4.4	± 0.6	id	id	[29]
γ [°] (mod 180°)	66.7	± 5.6	± 1	± 0.25	± 0.20	[29,30,34]
β_s [rad]	-0.035	± 0.021	± 0.014	± 0.004	± 0.002	[30,34]
$A_{\text{SL}}^d \times 10^4$	-6	± 19	± 5	± 2	± 0.25	[14,17,34,37]
$A_{\text{SL}}^s \times 10^5$	3	± 300	± 70	± 30	± 2.5	[14,17,34,37]
$\bar{m}_t$ [GeV]	165.30	± 0.32	id	id	± 0.020	[28,34]
$\alpha_s(m_Z)$	0.1185	± 0.0011	id	id	± 0.00003	[28,34]
$f_+^{K \rightarrow \pi}(0)$	0.9681	± 0.0026	± 0.0012	id	id	[30]
f_K [GeV]	0.1552	± 0.0006	± 0.0005	id	id	[30]
f_{B_s} [GeV]	0.2315	± 0.0020	± 0.0011	id	id	[30]
B_{B_s}	1.219	± 0.034	± 0.010	± 0.007	id	[30]
f_{B_s}/f_{B_d}	1.204	± 0.007	± 0.005	id	id	[30]
B_{B_s}/B_{B_d}	1.054	± 0.019	± 0.005	± 0.003	id	[30]
$\tilde{B}_{B_s}/\tilde{B}_{B_d}$	1.02	± 0.05	± 0.013	id	id	[30,42,43]
$\tilde{B}_{B_s}$	0.98	± 0.12	± 0.035	id	id	[30,42,43]
η_B	0.5522	± 0.0022	id	id	id	[44]

π^0 identification

- Need exquisite EM calorimetry for π^0 identification
 - $3\% / \sqrt{E}$ expected

JINST 15 P11005

