

Imaging the Nucleon Interior

QCD Lagrangian

$$\mathcal{L} = \frac{1}{4g^2} G_{\mu\nu}^a G_{\mu\nu}^a + \sum_j \bar{q}_j (i\gamma_\mu D_\mu + m_j) q_j$$

where

$$G_{\mu\nu}^a \equiv \partial_\mu A_\nu^a - \partial_\nu A_\mu^a + if_{bc}^a A_\mu^b A_\nu^c$$

and

$$D_\mu \equiv \partial_\mu + i t^a A_\mu^a$$

That's all!

How does the spin-1/2 proton with mass 938 MeV/c² arise?



Strong QCD 2024 Strong QCD from Hadron Structure Experiments - VI

May 14-17

Administrators:
Zhu-Fang Cui, NJU, physics@nju.edu.cn
Meng-Ting He, NJU, mthe@nju.edu.cn

Organizing Committee:
Zhu-Fang Cui - NJU
Ralf Gothe - USC (co-chair)
Meng-Ting He - NJU
Victor Mokeev - JLab (co-chair)
Craig D. Roberts - NJU (chair)

This workshop will canvass the following themes:

- Emergence of mass origins and expressions
- Hadron structure: hadron elastic and transition form factors
- Hadron parton distributions: from 1-D to 3-D
- Mechanical properties of hadrons
- Searches for new states of hadron matter
- Hadron spectroscopy and structure using conventional and lattice methods
- Advances in quark models of hadron spectra and structure
- Emergence of atomic nuclei from strong QCD
- Reactor models and amplitude analyses
- Insights into strong QCD from experiments at modern facilities

Web pages: <https://indico.hep.ac.cn/event/20519/>

Context

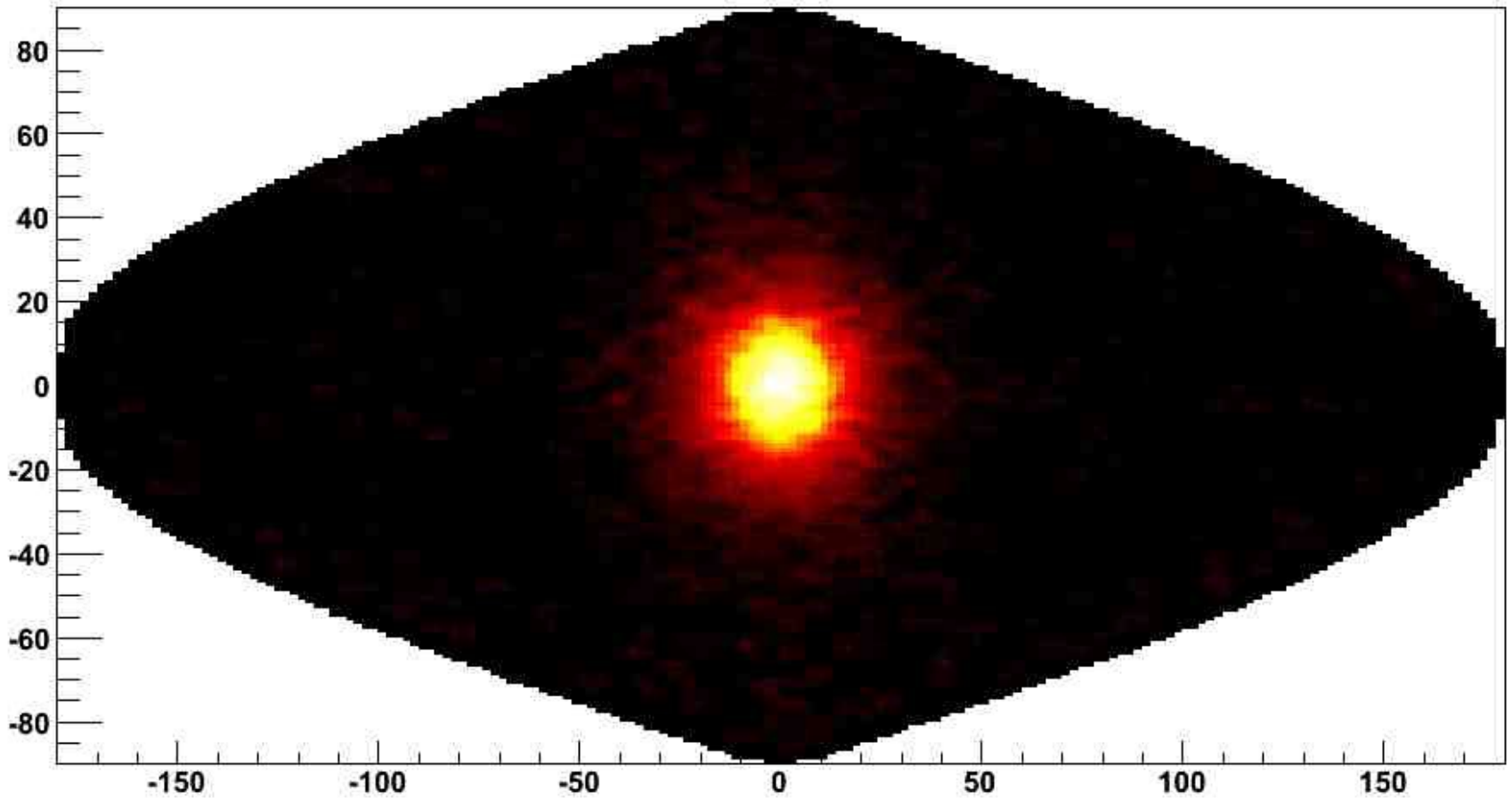
- Visualizations are a powerful means to describe and understand complicated phenomena in physics, *e.g.*
 - free body diagrams in Newtonian mechanics
 - field lines of Faraday in electricity and magnetism
 - Feynman diagrams in quantum field theory
- Physicists have developed the Standard Model which successfully explains the subatomic world.
- Current and planned large-scale facilities should provide a comprehensive set of measurements to inform our understanding of QCD.
- However, the quarks and gluons of QCD are not detectable and the important phenomena are emergent.
- Can this subatomic world be visualized so that the non-expert can begin to appreciate its unique structure?

Earth Rise from the Moon

Apollo 8
August 1968



The Sun as viewed by neutrino detection deep underground



Super-Kamiokande experiment in 4504 days of data taking

Crab Nebula



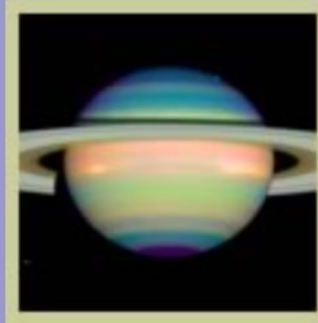
From the Hubble web page

Color as a Tool



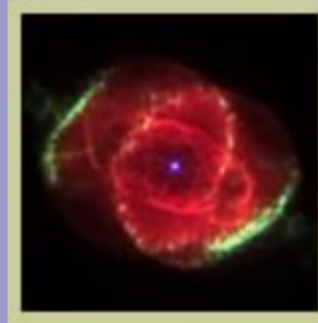
Natural Color

The colors in this image of a galaxy were chosen to simulate the colors that our eyes might see if we were able to visit it in a spacecraft.



Representative Color

Representative color helps scientists visualize what would otherwise be invisible, such as the appearance of an object in infrared light.



Enhanced Color

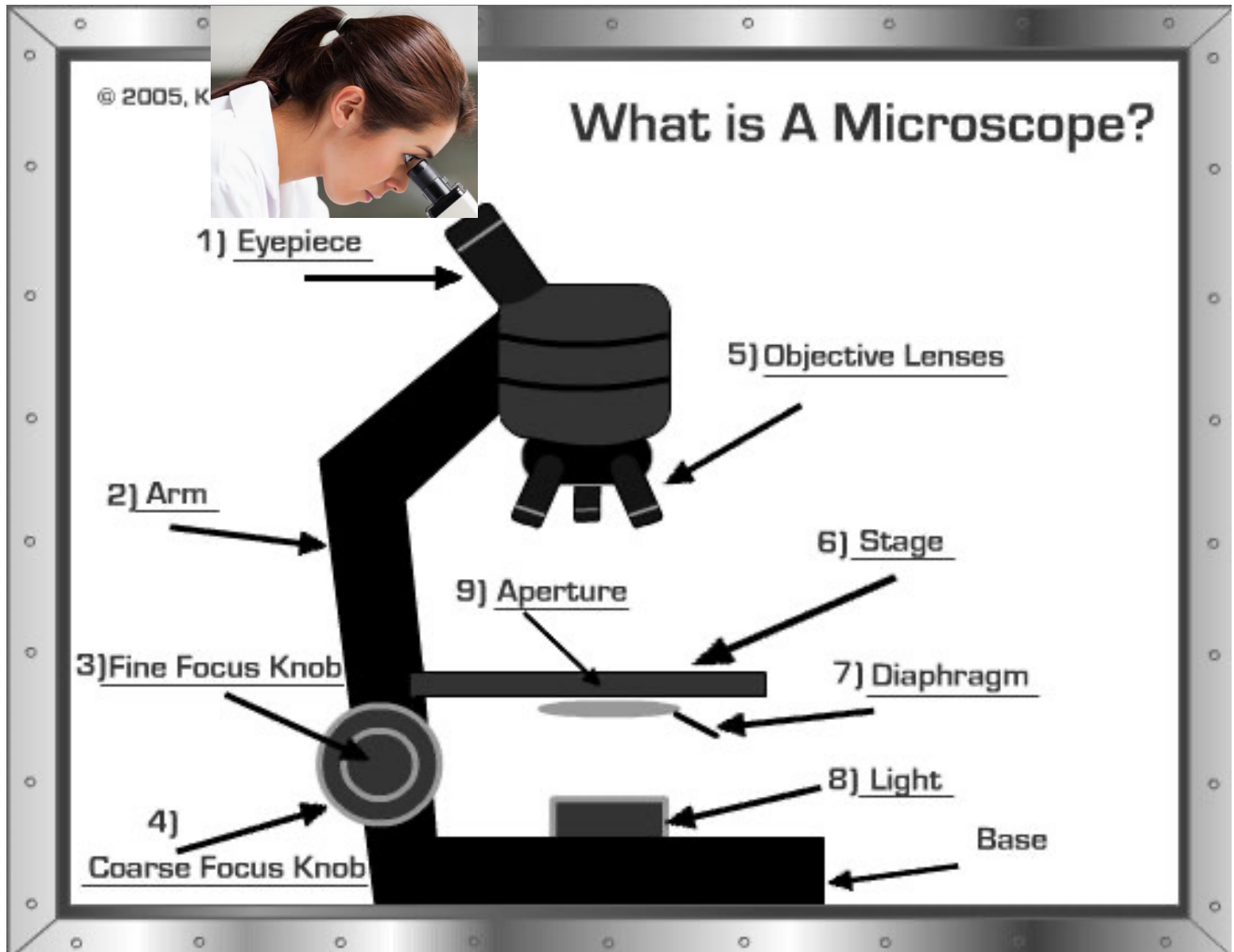
Enhancing the visible colors in an image often brings out an object's subtle structural detail.

Color in Hubble images is used to highlight interesting features of the celestial object being studied. It is added to the separate black-and-white exposures that are combined to make the final image.

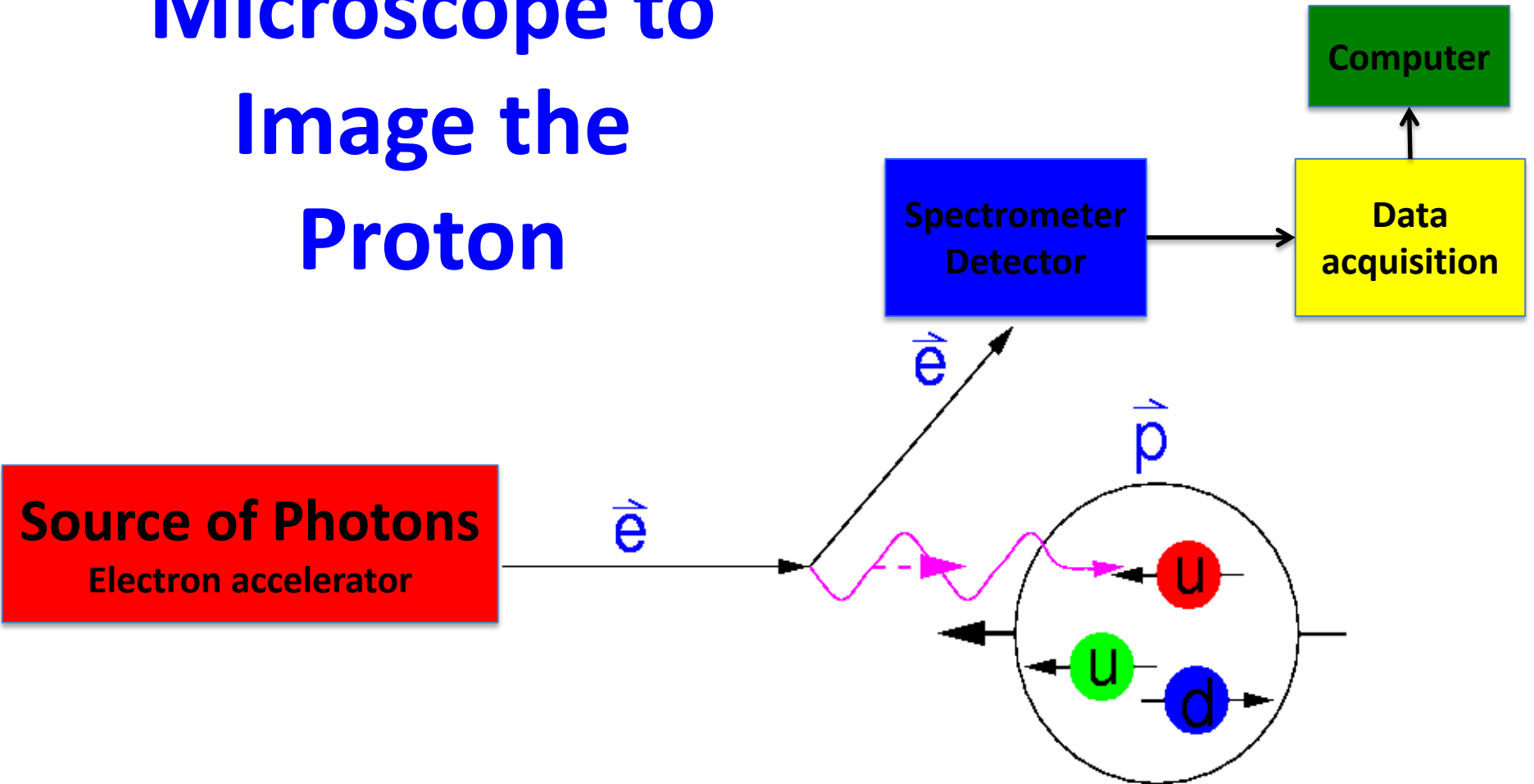
Creating color images out of the original black-and-white exposures is equal parts art and science.

We use color:

- To depict how an object might look to us if our eyes were as powerful as Hubble
- To visualize features of an object that would ordinarily be invisible to the human eye
- To bring out an object's subtle details.



An Electron Microscope to Image the Proton

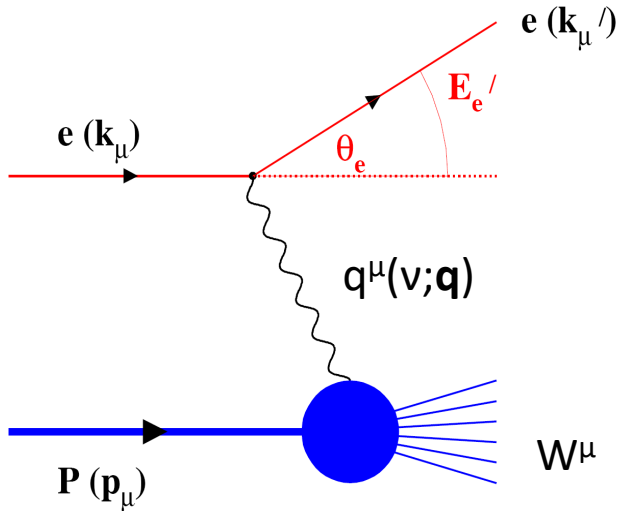


Jefferson Lab

Thomas Jefferson National Accelerator Facility



Imaging the Proton



- Scatter electron from the proton
- Exchange a virtual photon of mass $Q^2 = -q^\mu q_\mu$
- $1/Q$ determines the spatial resolution (pixel size) probed
- $W^2 = W^\mu W_\mu = M^2 + 2M\nu - Q^2$

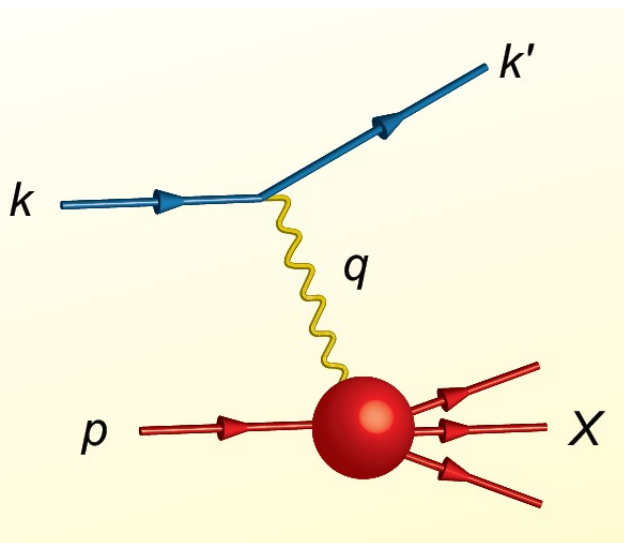
- **Elastic scattering:** $W^2 = M^2$ so $Q^2 = 2 M\nu$ *Hofstadter*
electromagnetic structure of proton described by two form-factors $G_E(Q^2)$ and $G_M(Q^2)$

- **High energy, deep inelastic scattering:** $W^2 > 4$, $Q^2 > 1$ *Friedman, Kendall, Taylor*
quark structure of proton described by structure functions $F_2(x, Q^2)$



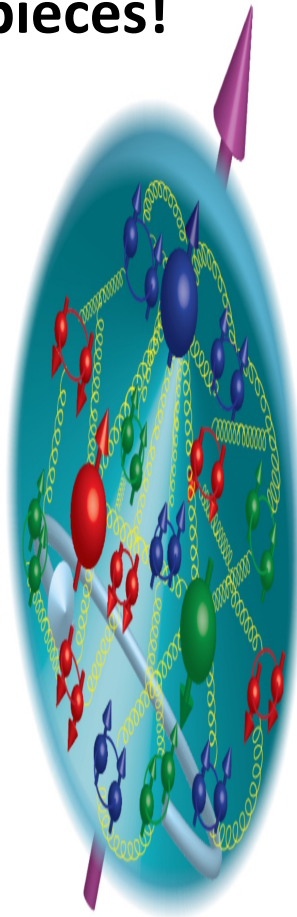
Proton Viewed in High Energy Electron Scattering: 1 Longitudinal Dimension

Proton is smashed into pieces!



Lorentz Invariants

- $E_{\text{CM}}^2 = (p+k)^2$
- $Q^2 = -(k-k')^2$
- $x = Q^2/(2p \cdot q)$



- Viewed from boosted frame, length contracted by

$$\gamma_{\text{Breit}} = \sqrt{1 + \frac{Q^2}{4M^2}}$$

- Internal motion of the proton's constituents is slowed down by time dilation – the instantaneous charge distribution of the proton is seen.
- In boosted frame x is understood as the longitudinal momentum fraction
valence quarks: $0.1 < x < 1$
sea quarks: $x < 0.1$

J. Bjorken, SLAC-PUB-0571
March 1969

Visualization

- The camera is a device to capture an image on a desired medium, e.g. CCD or film.
- Movie cameras capture a series of individual images in time to give the illusion of having captured motion.
- Essential elements of any camera are
 - the focus which uses a lens to gather light from a selected image => pixel size
 - the shutter which is a door that opens for a definite time to allow selected light to reach the medium.

Shutter speed



Richard Milner

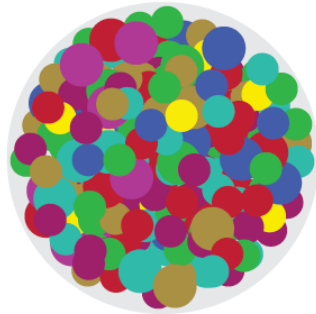
Strong QCD Conference, Nanjing.

May 14, 2024



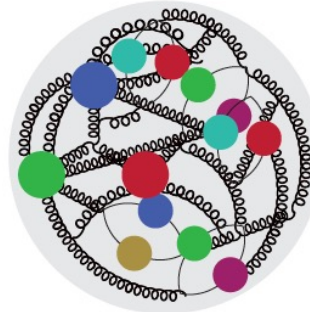
High Energy Electron Scattering

Snapshots where $0 < x < 1$ is the shutter exposure time



$x \approx 10^{-4}$

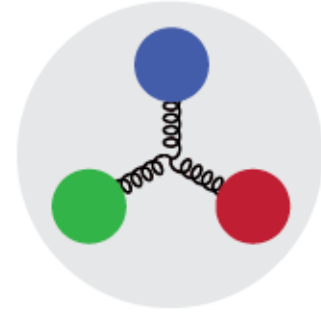
Probe non-linear dynamics
short exposure time



$x \approx 10^{-2}$

Probe rad. dominated
medium exposure time

Shutter speed



$x \approx 0.3$

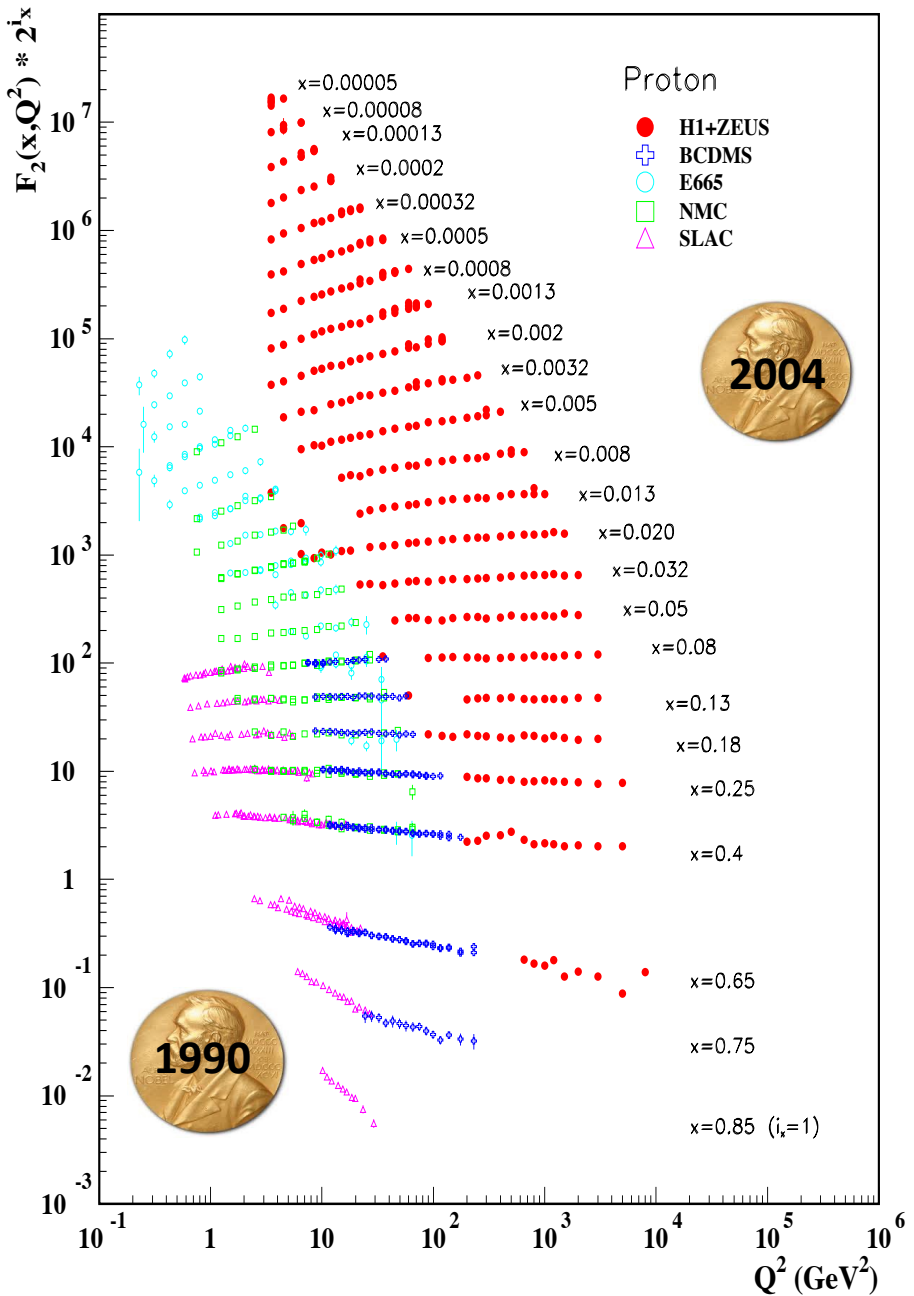
Probe valence quarks
long exposure time

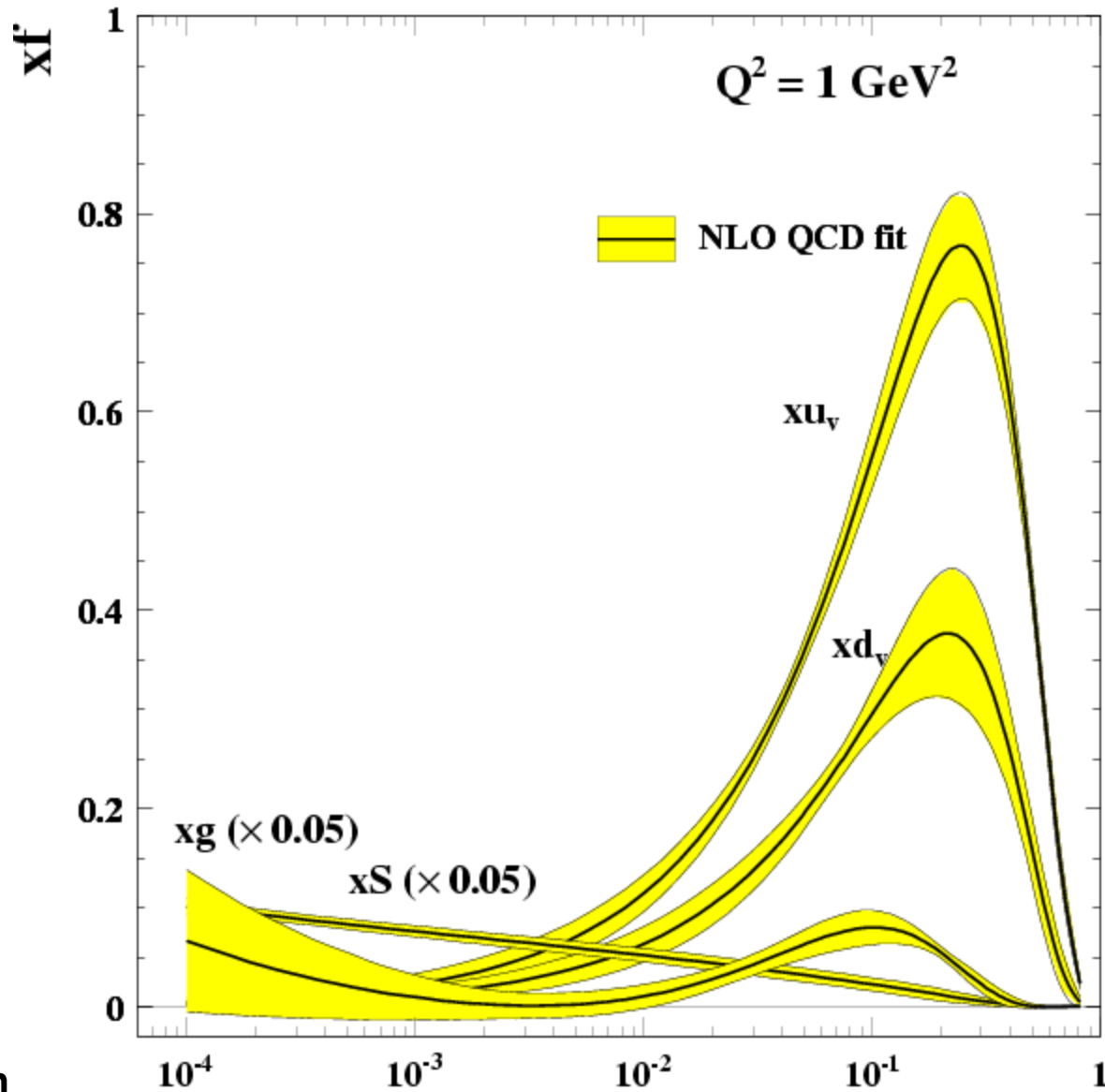
1/1000	1/500	1/250	1/125	1/60	1/30	1/15	1/8	1/4	1/2	1	2	4	8
Freeze action			Hand hold			Movement blurr - tripod needed							

Quark Structure of Proton from High-Energy Lepton Scattering

$e-p$ cross section $\approx \sigma_{\text{Mott}} \bullet F_2(x, Q^2)$

- Snap shots of the charged structure of the proton taken in the boosted frame
- $1/Q$ spatial resolution: pixel size
- x exposure time, $1/x$ shutter speed
- QCD prescribes evolution with Q^2 which connects quarks and gluons





R. Yoshida
C. Gwenlan

Charting the Inner Structure of the Proton

<https://www.youtube.com/watch?v=G-9I0buDi4s>

Christopher Boebel
Rolf Ent
James LaPlante
Joseph McMaster
Richard Milner

 Jefferson Lab

Richard Milner

**SPUTNIK
ANIMATION**

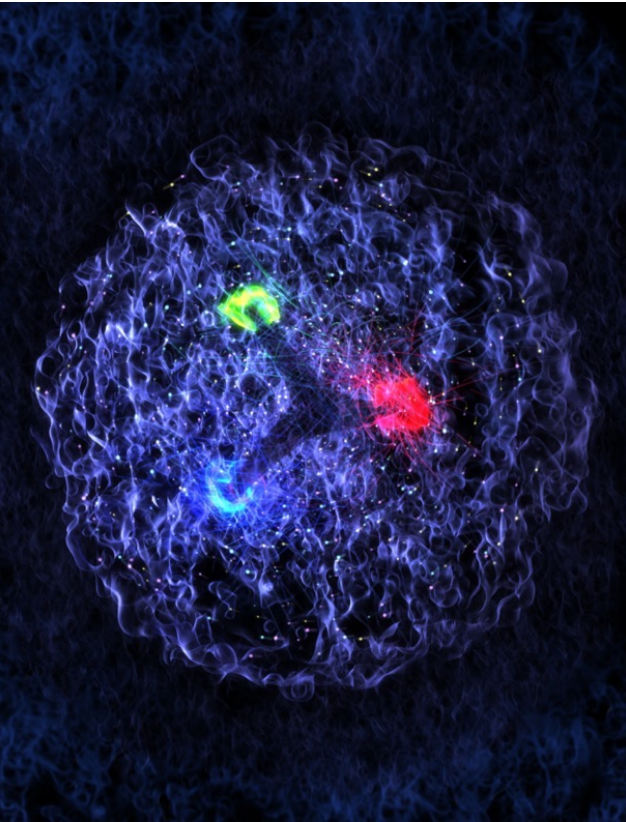
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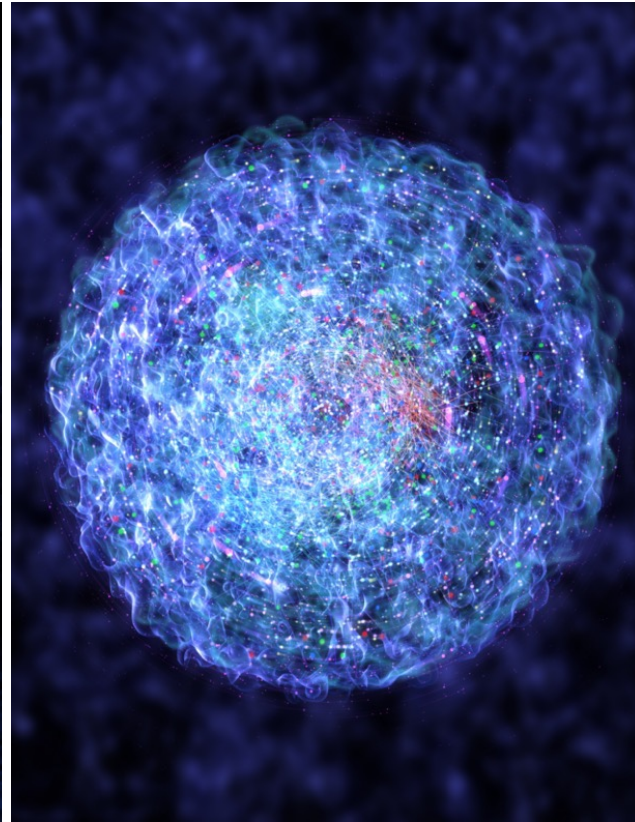
 ARTS
CENTER FOR ART,
SCIENCE & TECHNOLOGY
AT MIT

16

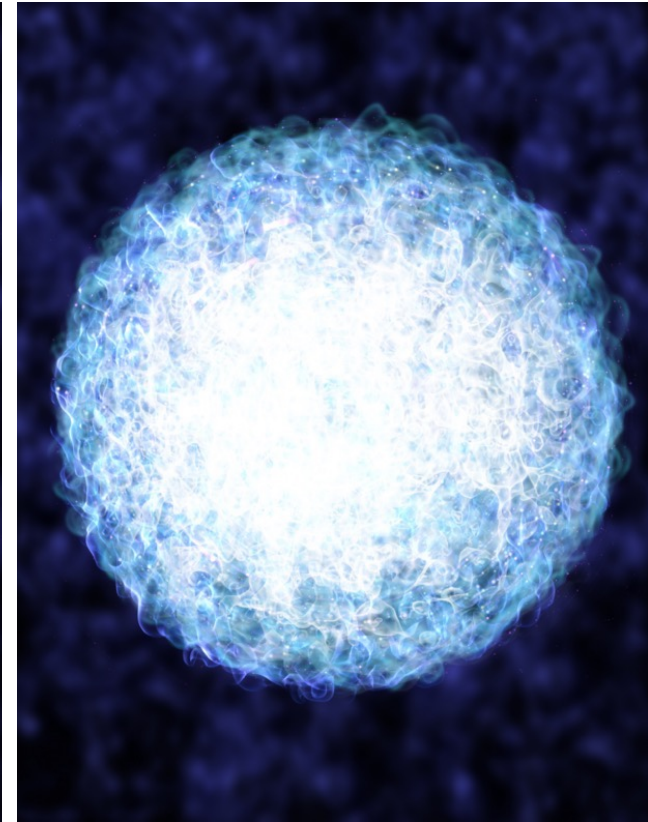
Quark and Gluon Dynamics Dominate Proton Structure



High $x \sim 0.3$



Medium $x \sim 10^{-2}$



Low $x \sim 10^{-4}$

Quark and Gluon Dynamics Dominate Proton Structure



Quantum Connections in Sweden-11 Summer School

QCD 50th Anniversary

Jun 11 - 24, 2023 — Högberga Gård

High $x \sim 0.3$

Medium $x \sim 10^{-2}$

Low $x \sim 10^{-4}$

Quark and Gluon Dynamics Dominate Proton Structure

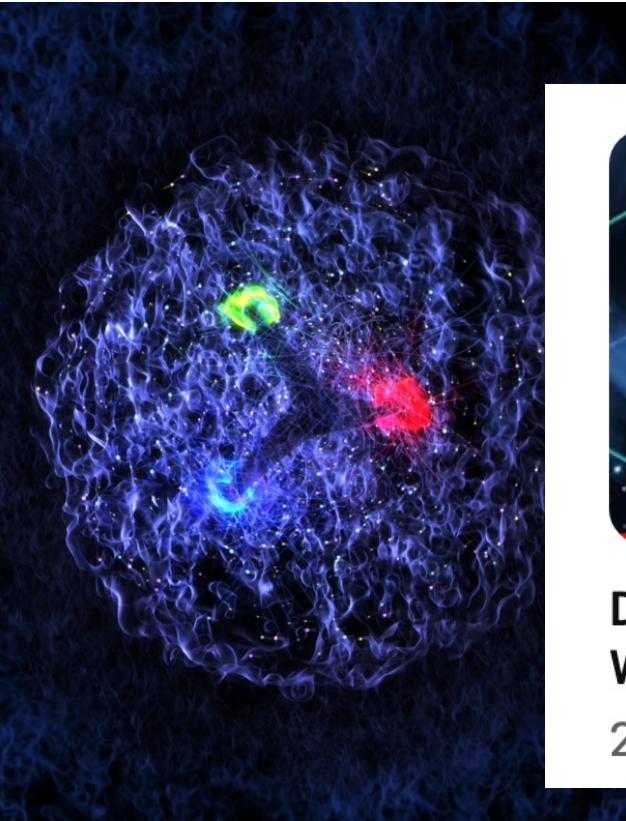


High $x \sim 0.3$

Medium $x \sim 10^{-2}$

Low $x \sim 10^{-4}$

Quark and Gluon Dynamics Dominate Proton Structure



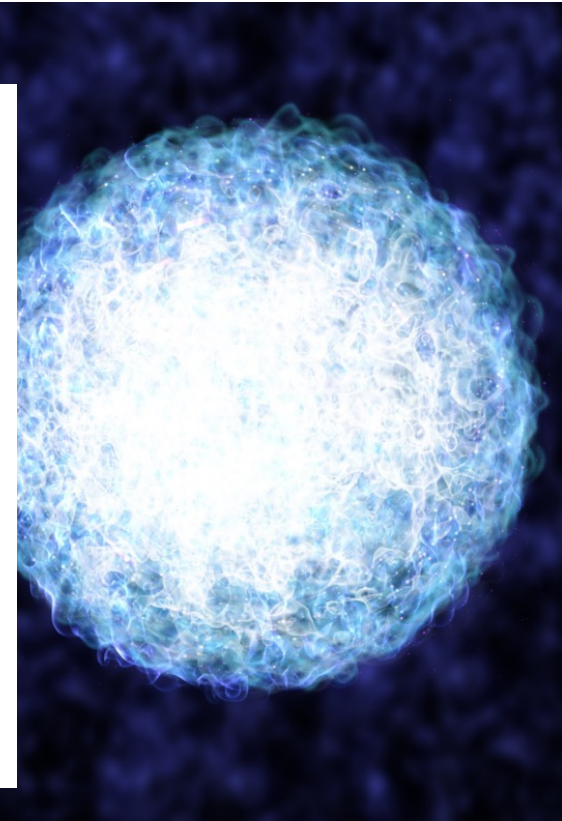
High $x \sim 0.3$



Did AI Prove Our Proton Model
WRONG?

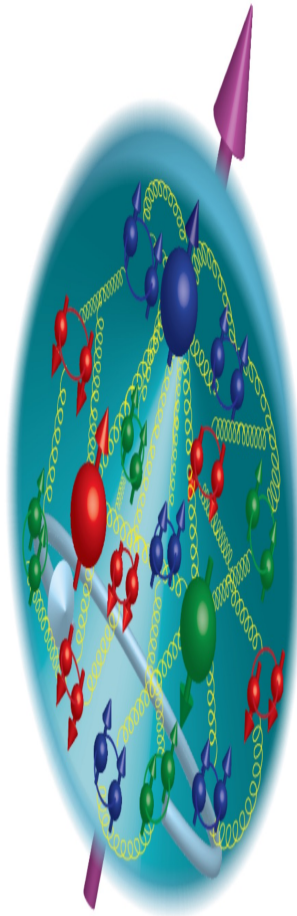
2M views • 9 months ago

Medium $x \sim 10^{-2}$



Low $x \sim 10^{-4}$

Proton Viewed in High Energy Electron Scattering: 1 Longitudinal Dimension

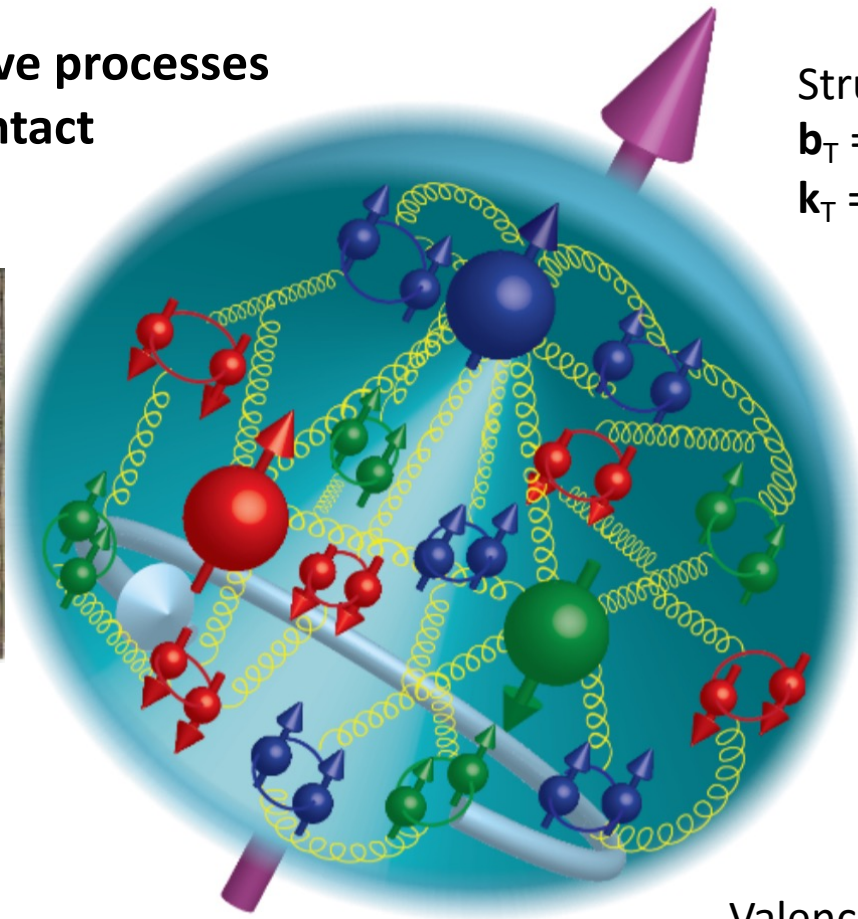


Proton Tomography: 2 New Dimensions Transverse to Longitudinal Momentum

Deeply virtual exclusive processes
where proton is left intact



Direction of longitudinal
momentum normal to
plane of slide



Structure mapped in terms of
 \mathbf{b}_T = transverse position
 \mathbf{k}_T = transverse momentum

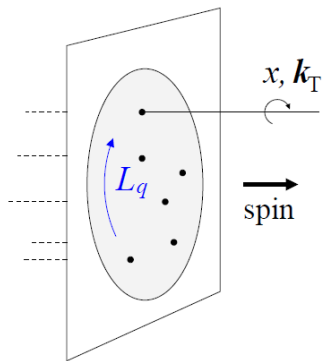
Nuclei!

**Goal:
Unprecedented
21st Century Imaging
of Hadronic Matter**

Valence Quarks: JLab 12 GeV
Sea Quarks and Gluons: EIC

3D Partonic Picture

Theorists have developed a powerful formalism for studying the 3D partonic picture of the nucleon and the nucleus. It is encoded in **Generalized Parton Distributions** and **Transverse Momentum Dependent Distributions**



Transverse
Momentum
Dependent
distributions

Wigner distribution

$$W(\mathbf{p}, \mathbf{x})$$

$$d^3 r$$

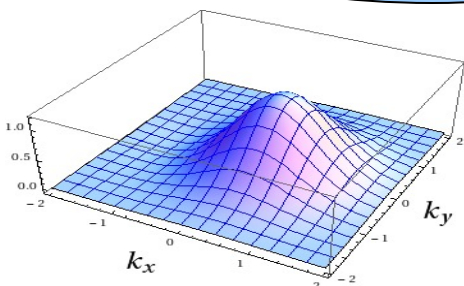
$$d^3 p$$

Generalized
Parton
Distributions

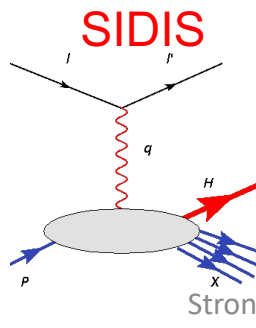
*Orbital motion
accessible!*

$$f(x, \mathbf{k}_\perp)$$

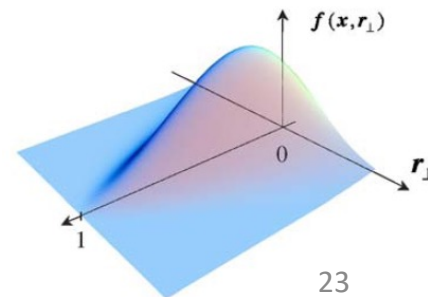
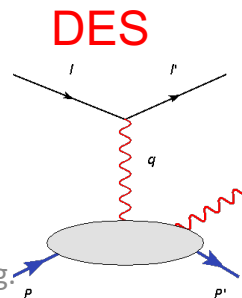
$$H(x, \xi, t)$$



Richard Milner

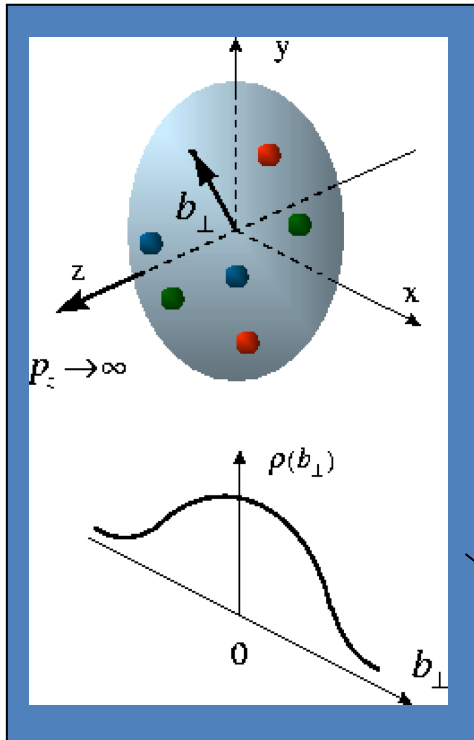


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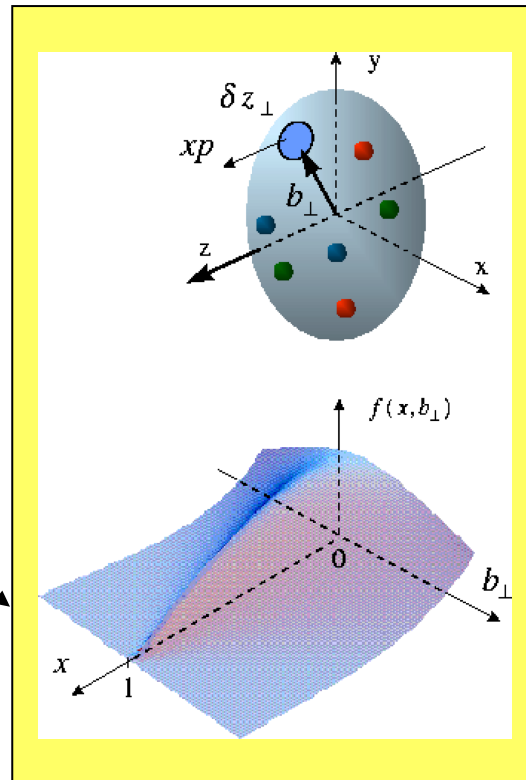
Generalized Parton Distributions

Last 60 years



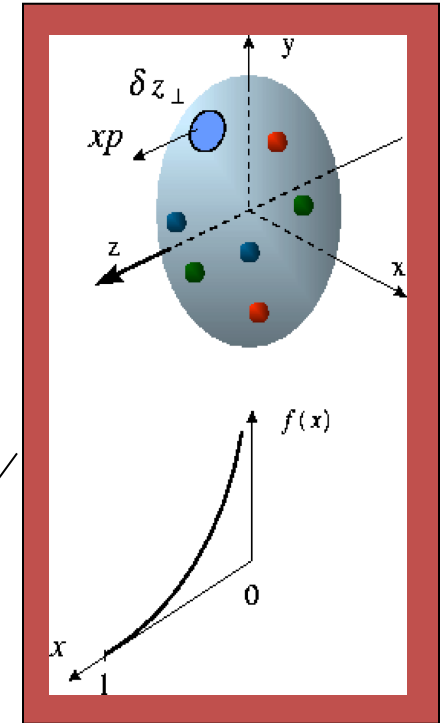
Elastic form factors \rightarrow
Transverse charge & current
 densities $F_1(t), F_2(t)$.

Last 20 years



Deeply exclusive processes \rightarrow GPD's
 and **3 D** images in transverse space
 and longitudinal momentum.
 4 GPDs **H, E, \tilde{H}, \tilde{E}** (x, ξ, t)

Last 45 years



DIS structure functions
 \rightarrow **Longitudinal** parton
 momentum & helicity
 densities, $F_2(x), g_1(x)$.

Generalized Parton Distributions

(Quantum phase-space quark distribution in the nucleon)

$$W_{\Gamma}(\mathbf{r}, k) = \frac{1}{2M_N} \int \frac{d^3\mathbf{q}}{(2\pi)^3} e^{-i\mathbf{q}\cdot\mathbf{r}} \left\langle \mathbf{q}/2 \left| \hat{W}_{\Gamma}(0, k) \right| -\mathbf{q}/2 \right\rangle ,$$

$$W_{\Gamma}(\mathbf{r}, \mathbf{k}) = \int \frac{dk^-}{(2\pi)^2} W_{\Gamma}(\mathbf{r}, k)$$

Integrate over
transverse
momentum space

GPDs H E \tilde{H} , \tilde{E}

Probe 3D structure 2D –
euclidean space and 1D –
momentum space.

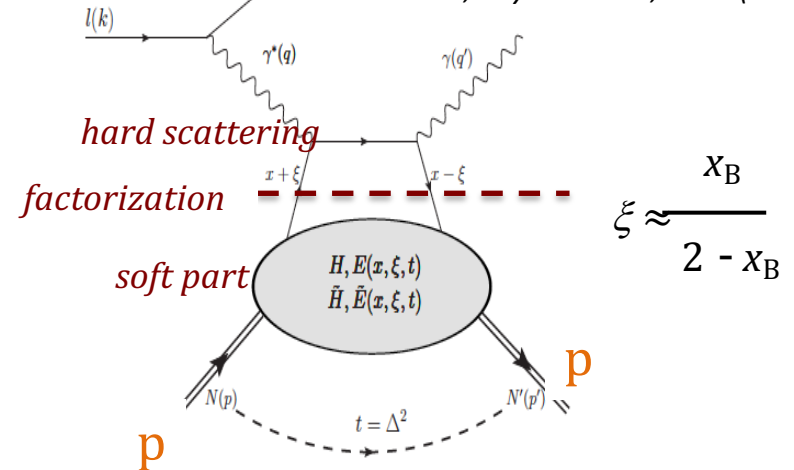
D. Müller et al., F. Phys. 42, 1994

X. Ji, PRL 78, 610, 1997

A. Radyushkin, PLB 380, 1996

Polarized DVCS probes GPDs.
JLab @ 12GeV has broad
DVCS program with
polarized beams and
polarized targets.

X. Ji, Phys.Rev.D55, 7114 (1997)



GPD H of special Importance
as it gives access to the
gravitational properties.

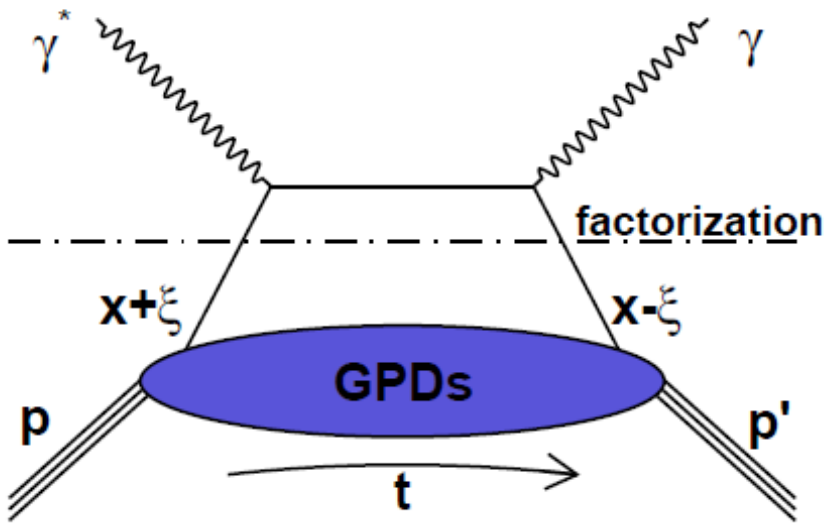
M. V. Polyakov, Physics Letters B 555 (2003) 57

I.V. Anikin and O.V. Teryaev, Phys.Rev.D76, 056007 (2007)

M. Diehl and D.Y. Ivanov, Eur. Phys. J. C52, 919, (2007)

Deeply Virtual Compton Scattering (DVCS) and GPDs

DVCS and Generalized Parton Distributions



$$\gamma^* p \rightarrow \gamma p'$$

Bjorken regime :
 $Q^2 \rightarrow \infty, x_B$ fixed

t fixed $\ll Q^2, \xi \rightarrow \frac{x_B}{2-x_B}$

$$\frac{p^+}{2\pi} \int dy^- e^{ixP^+y^-} \langle p' | \bar{\psi}_q(0) \gamma^+ (1 + \gamma^5) \psi(y) | p \rangle$$

$$= \bar{N}(p') \left[H^q(x, \xi, t) \gamma^+ + E^q(x, \xi, t) i\sigma^{+\nu} \frac{\Delta_\nu}{2M} \right. \\ \left. + \tilde{H}^q(x, \xi, t) \gamma^+ \gamma^5 + \tilde{E}^q(x, \xi, t) \gamma^5 \frac{\Delta^+}{2M} \right] N(p)$$

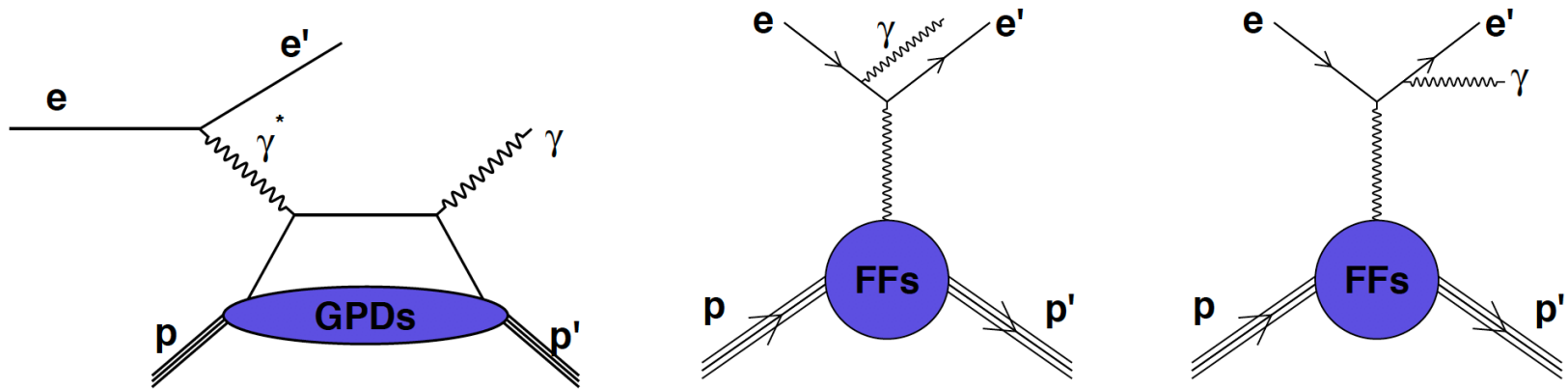
x : average fraction of quark longitudinal momentum

ξ fraction of longitudinal momentum transfer

$H, E, \tilde{H}, \tilde{E}$: Generalized Parton Distributions (GPDs)

3-D Imaging conjointly in transverse impact parameter and longitudinal momentum

Deeply Virtual Compton Scattering - Experiment



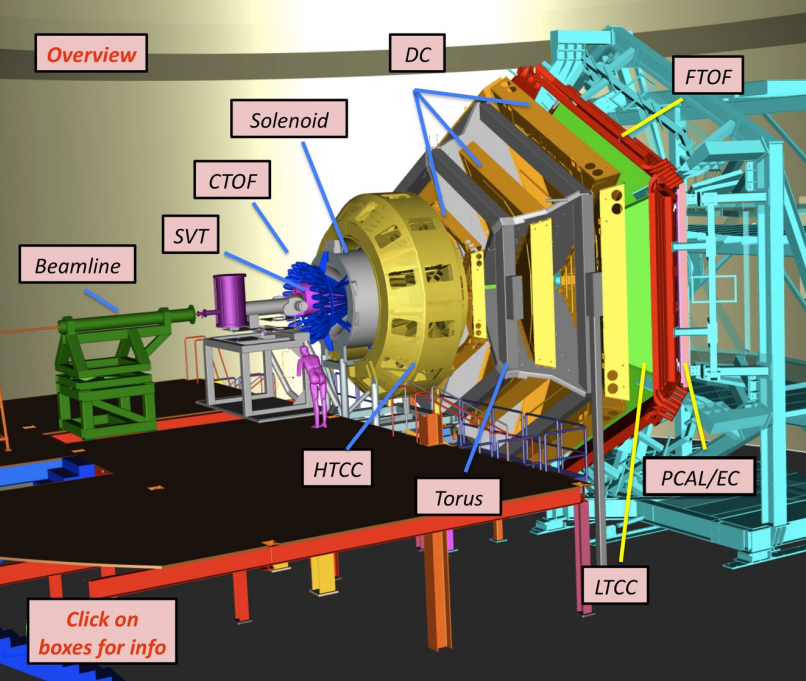
The Bethe-Heitler and DVCS processes interfere at the amplitude level :

$$|\mathcal{T}_{\text{BH}} + \mathcal{T}_{\text{DVCS}}|^2 = |\mathcal{T}_{\text{BH}}|^2 + |\mathcal{T}_{\text{DVCS}}|^2 + \mathcal{I}$$

The GPDs enter the DVCS amplitude through a complex integral. This integral is called a *Compton form factor* (CFF).

$$\mathcal{H}(\xi, t) = \int_{-1}^1 H(x, \xi, t) \left(\frac{1}{\xi - x - i\epsilon} - \frac{1}{\xi + x - i\epsilon} \right) dx$$

Measured both asymmetries and cross sections



CLAS12

Deeply Virtual Processes

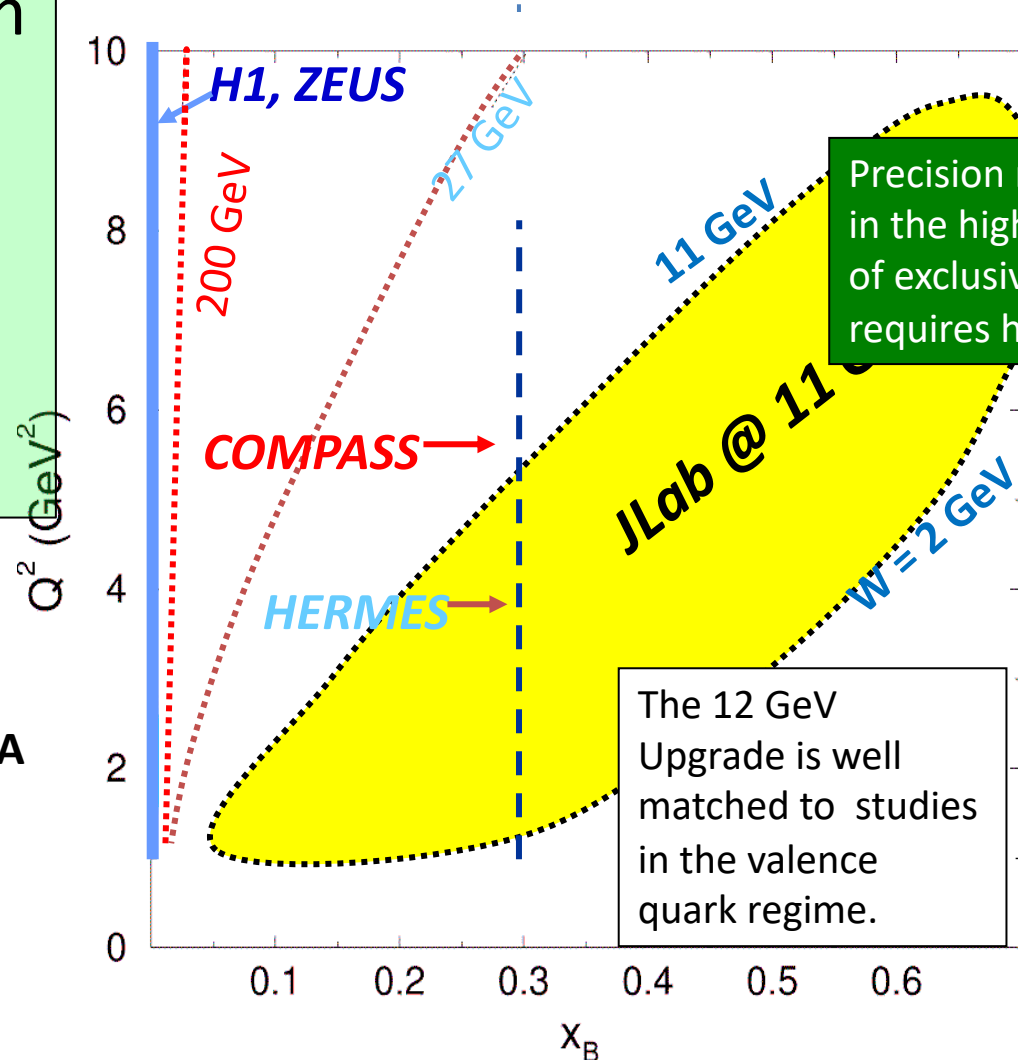
Access to new Generalized Parton Distributions

- Our group is a member of the CLAS12 collaboration at Jefferson Lab, VA
- Have developed with MIT-LNS high performance computing group (computers located at Bates) the capability to run the CLAS12 Monte-Carlo code by collaborators worldwide
- Working on determination of the absolute cross sections for the following processes:
 - $p(e, e'\pi^0)p$ – sensitive to GPDs
 - $p(e, e'\gamma)p$ - Deeply Virtual Compton Scattering (DVCS)
 - $p(e, e'\varphi)p$ - sensitive to gluonic radius
- Seek new insights into the quark and gluon structure of the proton

Kinematic coverage for Imaging @ 11GeV

A flagship program of structure studies in deeply exclusive and semi-inclusive processes.

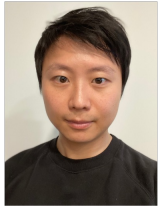
2018 data taking with RG-A
Liquid hydrogen target
Energy = 10.6 GeV



Precision measurements in the high x_B domain of exclusive processes requires high luminosity.

The 12 GeV Upgrade is well matched to studies in the valence quark regime.

DVCS Absolute Cross Section



Dr. Sangbaek Lee
(ANL)



Yijie Wang
(MIT)

- Analysis based on Fall 2018 data.
- Much more data already taken.
- Manuscript in preparation

0.600 GeV² < |t| < 0.800 GeV²
 + Experimental Data
 — Theory (BH)
 — Theory (KM15)

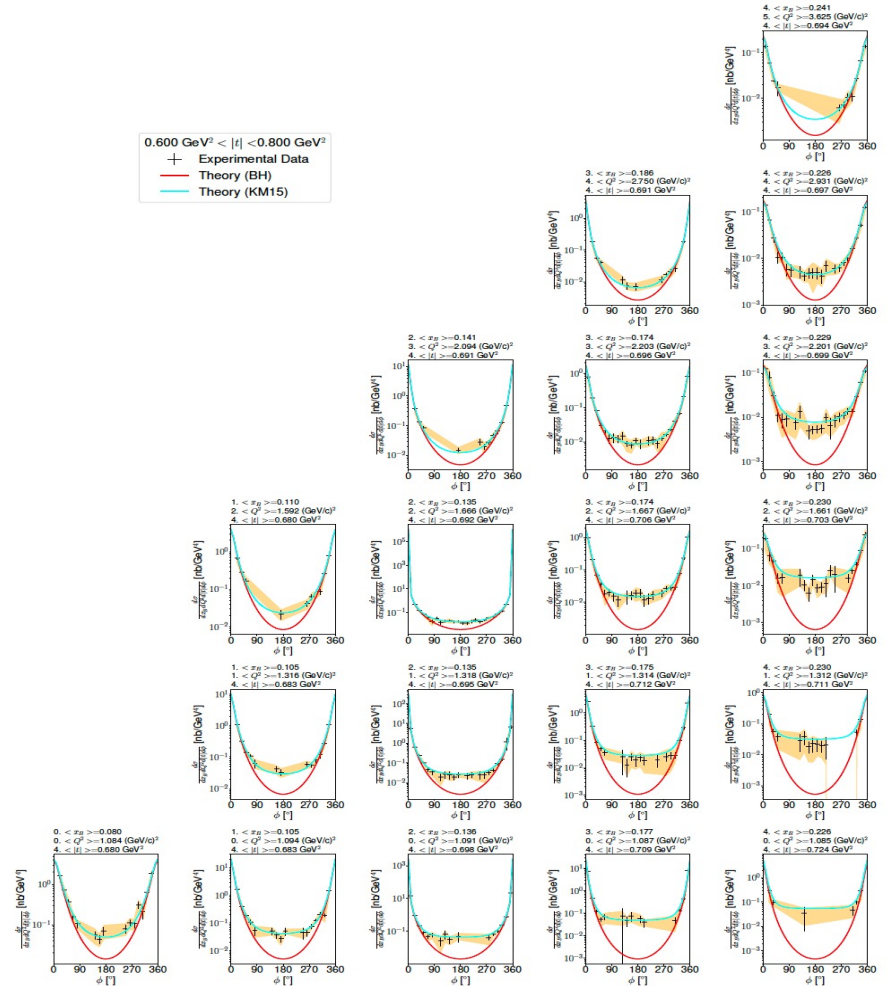


Figure 5-28: The unpolarized cross section in $x_B < 0.268$, $Q^2 < 4.326$ (GeV/c)², 0.600 GeV² < |t| < 0.800 GeV² bins.

DV π^0 absolute cross section



Dr. Robert Johnston



Dr. Igor Korover

- Analysis based on Fall 2018 data.
- Much more data already taken.
- Analysis note in preparation

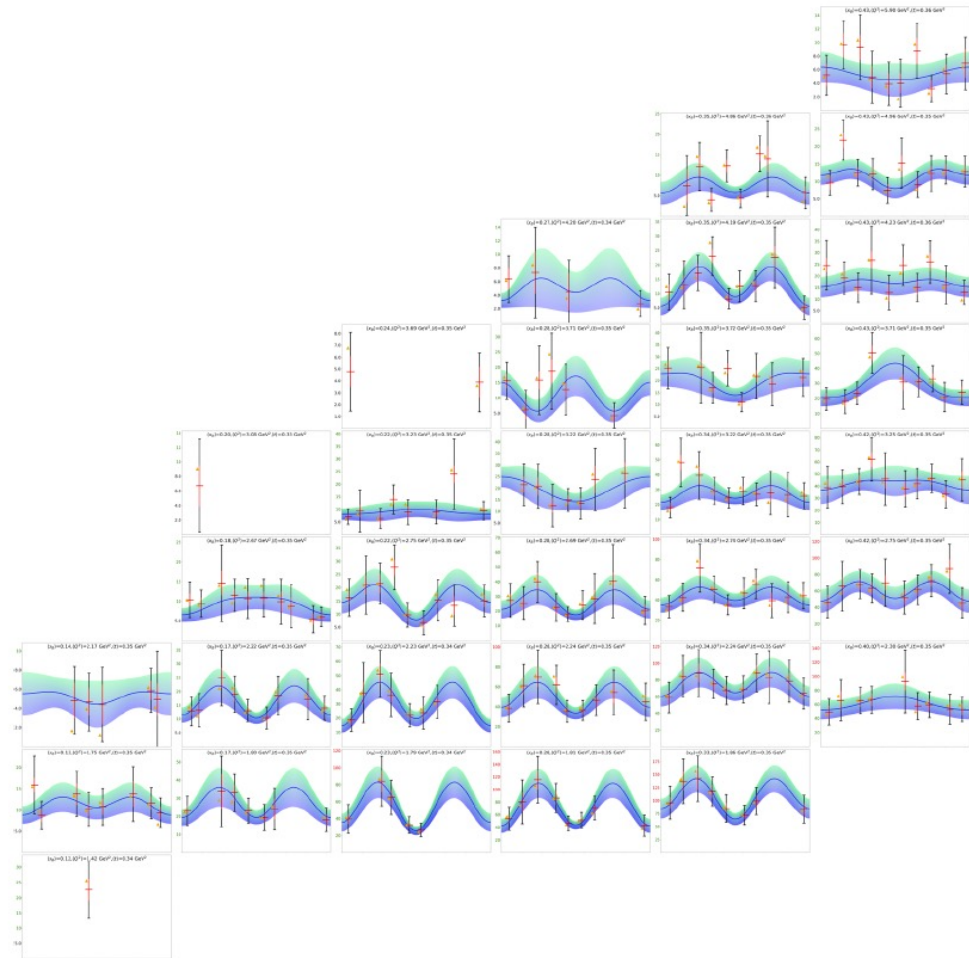


Figure 6-2: Reduced Cross Section for $0.3 \text{ GeV}^2 < t < 0.3 \text{ GeV}^2$ in bins of x_B (increasing left to right) and Q^2 (increasing vertically upwards).

DV $p(e,e'p)\Phi$ absolute cross section

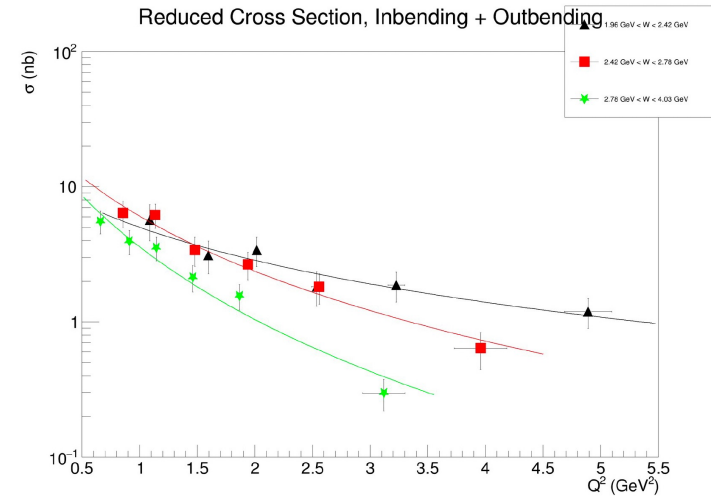


Dr. Patrick Moran
(College of Wm&Mary)

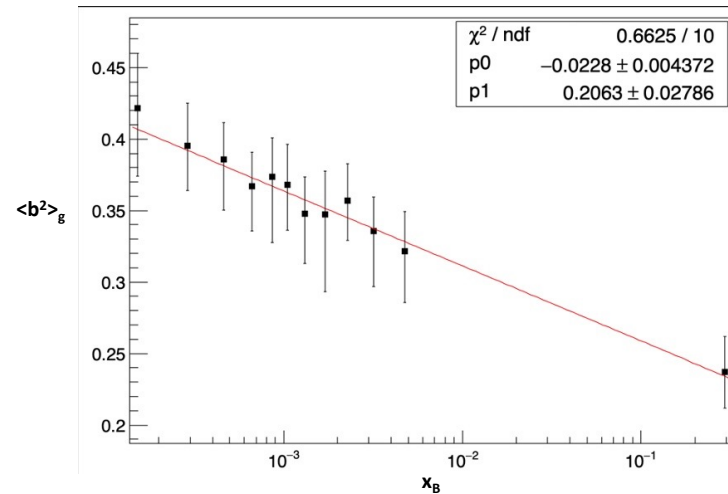


Dr. Igor Korover

- Preliminary analysis based on Fall 2018 data.
- Further analysis in progress by F.X. Girod (JLab)



Gluonic radius of proton



Transverse Momentum Structure of Nucleon – TMDs

(Quantum phase space quark distribution in the nucleon)

Wigner Function

$$W_{\Gamma}(\mathbf{r}, k) = \frac{1}{2M_N} \int \frac{d^3\mathbf{q}}{(2\pi)^3} e^{-i\mathbf{q}\cdot\mathbf{r}} \langle \mathbf{q}/2 | \hat{\mathcal{W}}_{\Gamma}(0, k) | -\mathbf{q}/2 \rangle$$

$$W_{\Gamma}(\mathbf{r}, \mathbf{k}) = \int \frac{dk^-}{(2\pi)^2} W_{\Gamma}(\mathbf{r}, k)$$

Integrate over *spatial* dimensions

Transverse Momentum-dependent Distributions (TMD)

3D imaging of the nucleon in momentum space

Quark spin polarization

N \ q		Quark spin polarization		
		U	L	T
Nucleon polarization	U	f_1		h_1^{\perp}
	L		g_1	h_{1L}^{\perp}
	T	f_{1T}^{\perp}	g_{1T}	h_1, h_{1T}^{\perp}

JLab has planned a complete SIDIS program with π/K to access quark TMDs

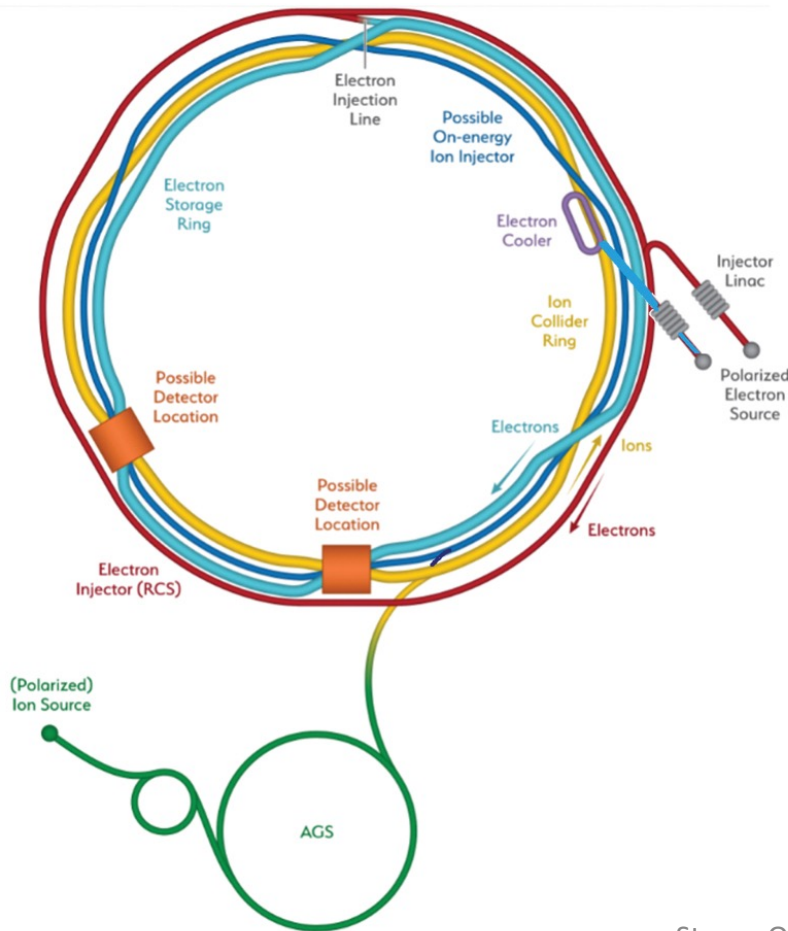
TMD Handbook

A modern introduction to the physics of
Transverse Momentum Dependent distributions



13 chapters
4 appendices

Electron-Ion Collider: add counter-circulating electron storage ring in existing RHIC tunnel



- 275 GeV/nucleon max. on 18 GeV e-beam
- High luminosity: 10^{34} e-nucleon $\text{cm}^{-2}\text{s}^{-1}$
- 70% polarized electron, nucleon beams
- Full range of ions: p to U
- Two collider detectors
- Actively considered since about 2000
- EIC highest priority for new facility construction by NP since 2015
- Blessed by NAS committee 2018
- Project officially launched by US DOE in January 2020
- Present schedule: accelerator turn-on 2031
- Project cost: \$ 2 billion approx.

Large Reach of EIC in x and Q^2

with greatly increased luminosity
inclusive, semi-inclusive, exclusive

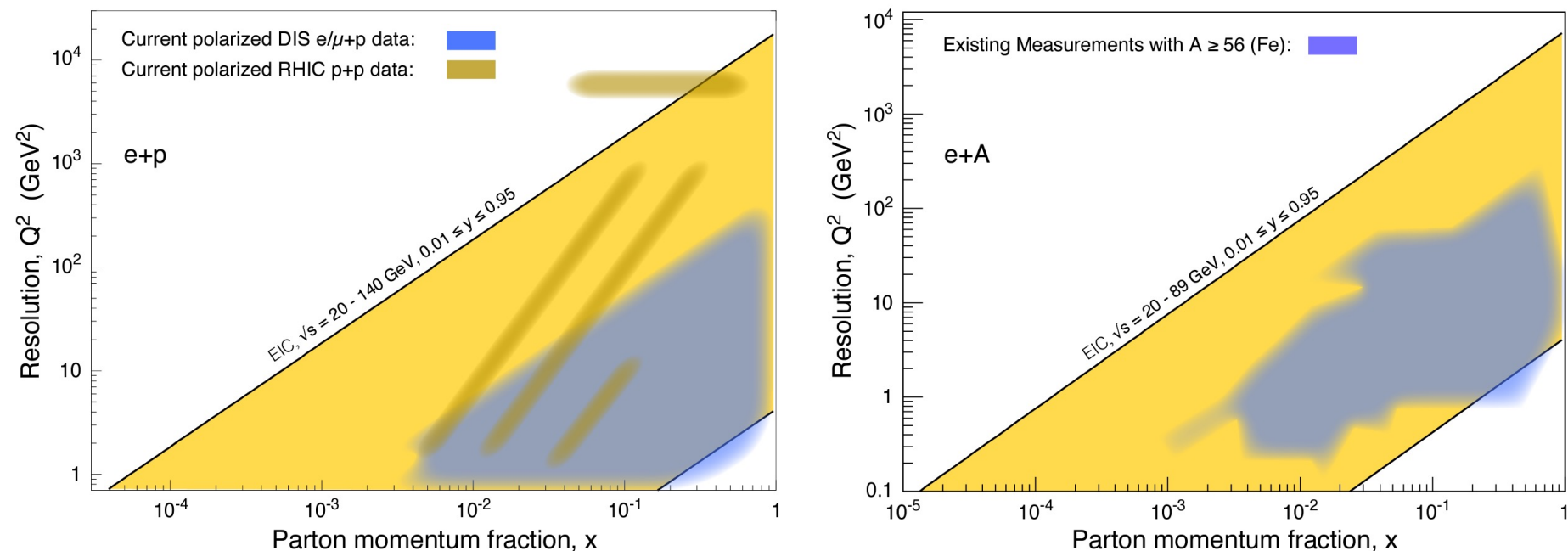
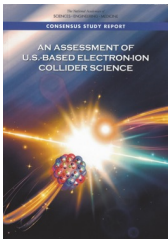
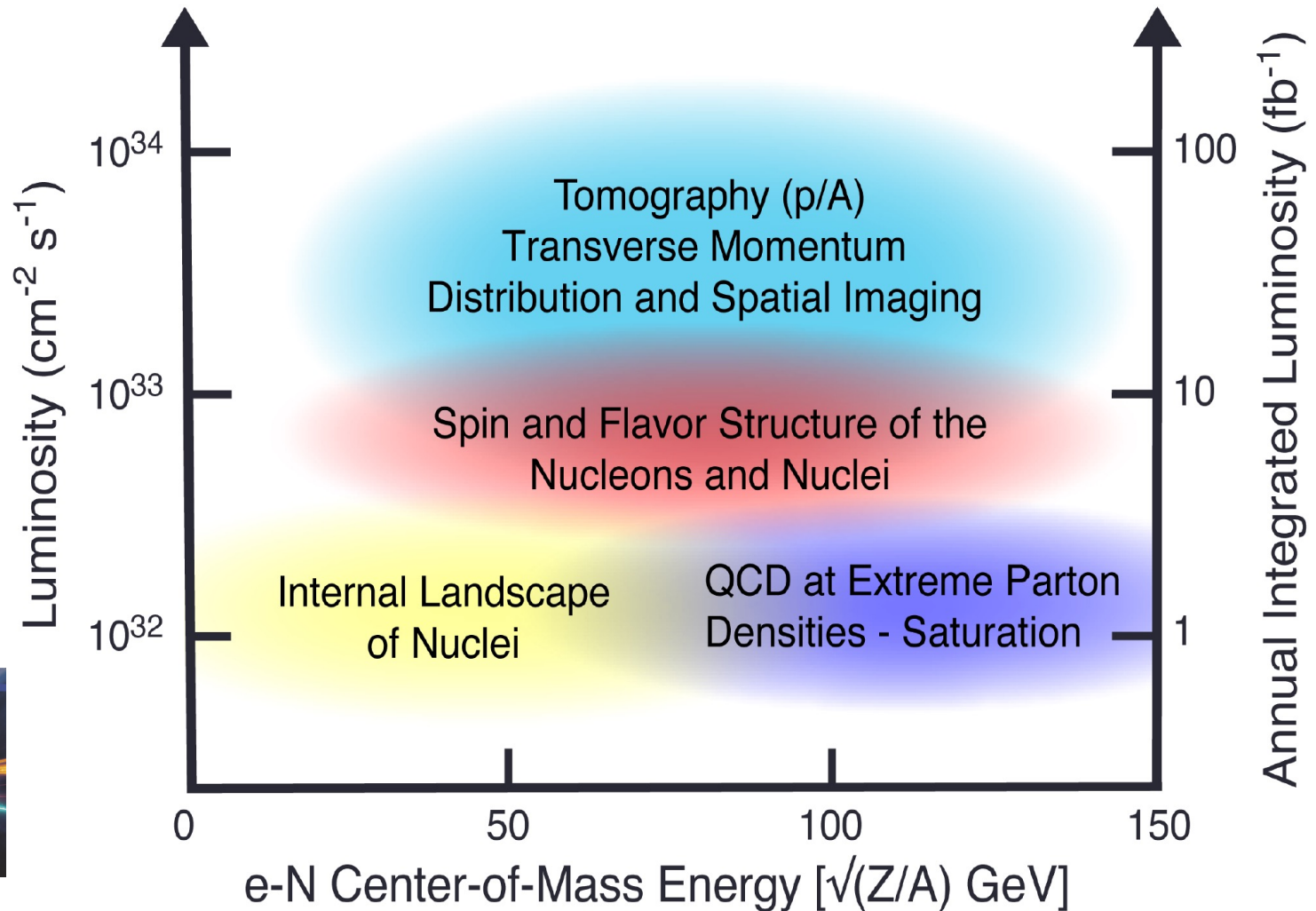


Figure 2.1: Left: The x - Q^2 range covered by the EIC (yellow) in comparison with past and existing polarized $e/\mu+p$ experiments at CERN, DESY, JLab and SLAC, and $p+p$ experiments at RHIC. Right: The x - Q^2 range for $e+A$ collisions for ions larger than iron (yellow) compared to existing world data.

Collider Specifications from Science



New Tools

Development of a Polarized He-3 Ion Source

Brookhaven National Laboratory

Gregor Atoian, Edward Beebe, Sergey Kondrashev, Deepak Raparia, John Ritter

Massachusetts Institute of Technology

Noah Wuerfel and Richard Milner

since 2012

and a

Polarized He-3 Target

Jefferson Laboratory

James Brock, Chris Keith, James Maxwell

Massachusetts Institute of Technology

Pushpa Pandey and Richard Milner

University of Tennessee

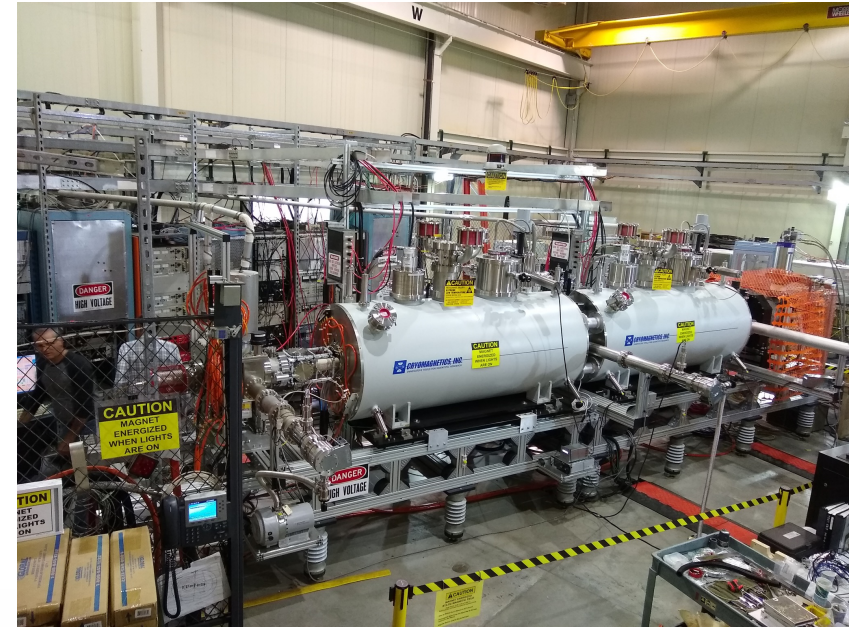
Dien Nguyen

since 2021

Using High-Field Optical Pumping

BNL-MIT Development of MEOP in High Magnetic Field

- Allows polarization of gas directly in EBIS.
- Direct transfer of polarized gas to EBIS vacuum system.
- Motivated development of tandem EBIS configuration which also benefits other ions.
- Polarized ^3He ion source for the EIC at RHIC at Brookhaven National Lab



Extraction and measurement of He-3 nuclear polarization anticipated in 2025.

A. Zelenski *et al.*, Nucl. Instr. and Meth. A 1055, 168494 (2023)

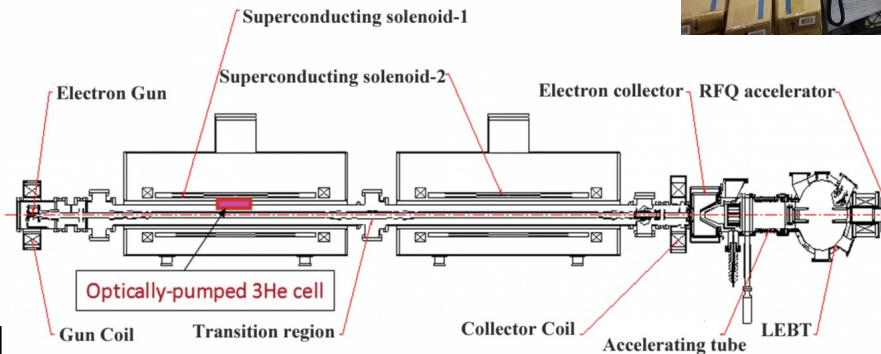


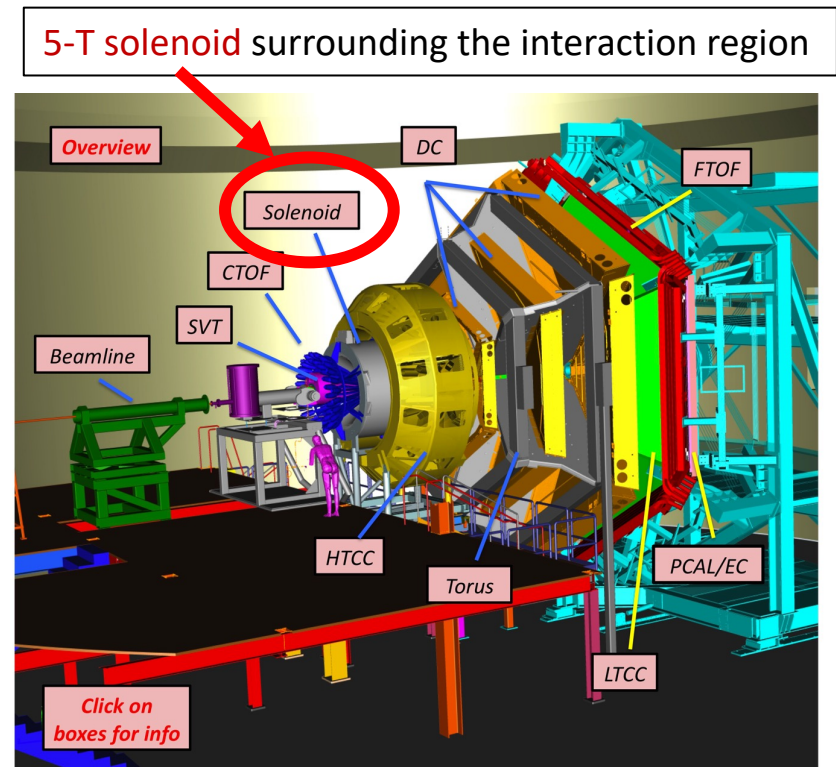
Figure 1: Schematic diagram of the extended EBIS. The polarized ^3He gas is injected into the drift tube of the new “injector” EBIS section. Here, RFQ means Radio Frequency Quadrupole and LEBT is the Low Energy Beam Transport.



Dr. Noah Wuerfel

Proposed Experiment Using Polarized ^3He at CLAS12 JLab

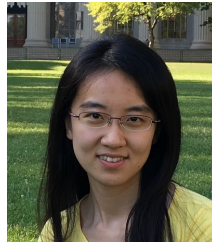
- CLAS12: CEBAF Large Acceptance Spectrometer for operation at 12 GeV
 - High luminosity electron scattering
 - Multi-particle final-state response
- PR12-20-002: A program of spin-dependent electron scattering using a polarized ^3He target at CLAS12
 - Spokespeople: H. Avakian, J. Maxwell, R. Milner, and D. Nguyen.
 - Approved with A- rating conditionally on the high-field MEOP target development
- Novel target design to accommodate to the standard CLAS12 configuration



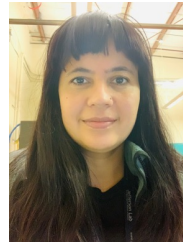
Target Development Status



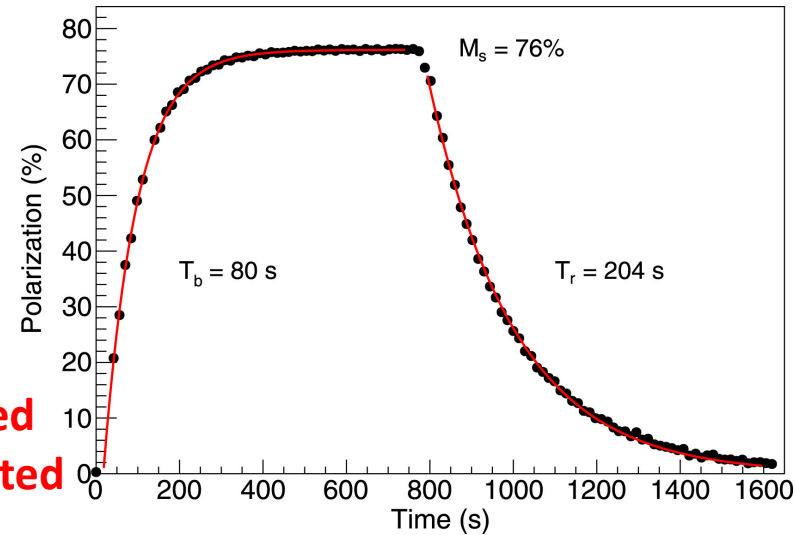
Nuclear Instruments and Methods in
Physics Research Section A:
Accelerators, Spectrometers,
Detectors and Associated Equipment
Volume 1057, December 2023, 168792



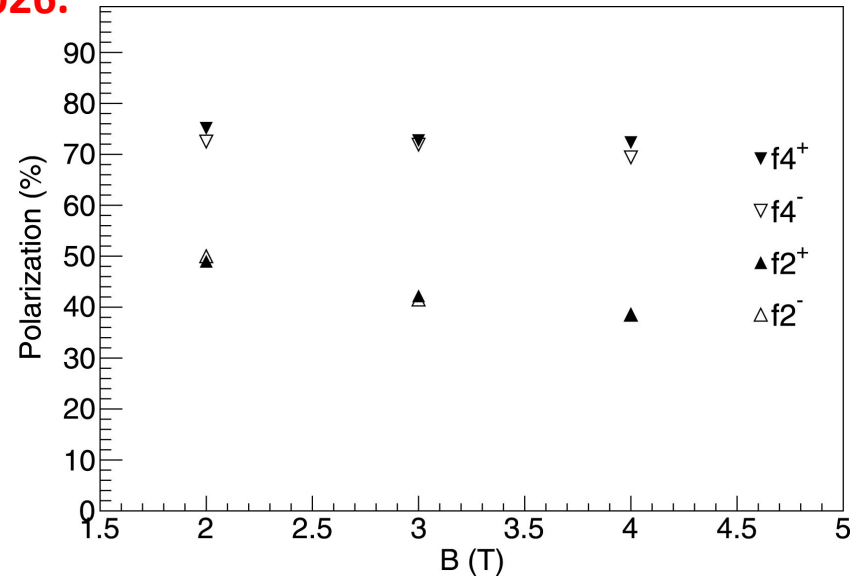
Dr. Xiqing Li
2021-2023



Dr. Pushpa
Pandey



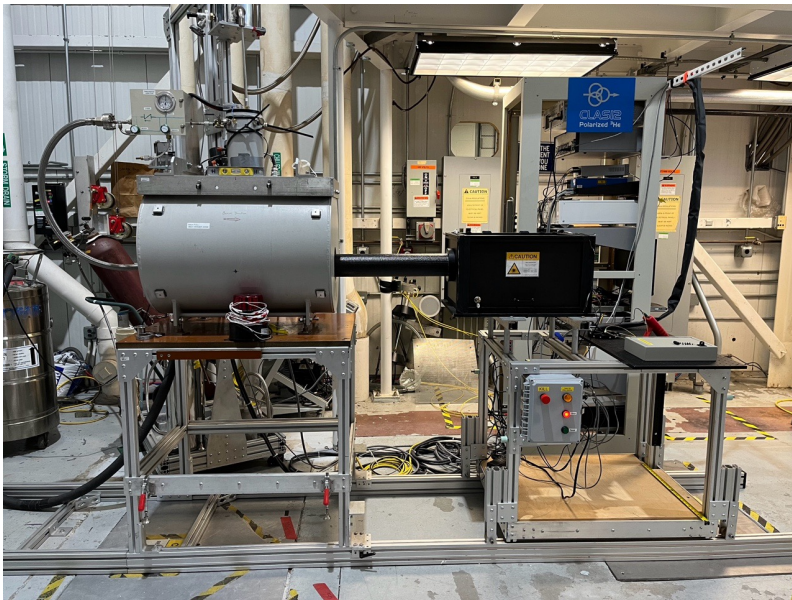
**Beam test
with polarized
target anticipated
in 2026.**



Full Length Article

Metastability exchange optical
pumping of ^3He at low pressure
and high magnetic field

X. Li^a, J.D. Maxwell^b, D. Nguyen^b, J. Brock^b, C.D. Keith^b,
R.G. Milner^a, X. Wei^b



Opportunity for China to Build a World Class QCD Machine in the Next Decade

- Need lepton scattering to access DIS and DVEP
 - 10 GeV on fixed target provides access to valence quarks
- Both transversely and longitudinally polarized targets of proton, deuteron and ^3He
 - Determine GPDs and TMDs
- Desire positron as well as electron beam
 - beam charge asymmetry for DVEP
 - test QED expansion
- Desire complementarity to Jefferson Lab as well as synergy with EIC-China

Realization

- 10 GeV electron/positron storage ring with 200 mA of circulating current
 - Is an existing ring available?
- Self polarization of stored e^+/e^- using the Sokolov-Ternov effect
- Polarized gas targets of H, D, ^3He and unpolarized gas targets
- Dedicated magnetic spectrometer with state-of-the-art particle identification
- Technically unique and complementary to Jefferson Lab
 - polarized targets: undiluted, longitudinal and transverse poln.
 - high intensity polarized positron beams
- Should come online in about a decade

Summary

- One of the central goals of twenty first century physics is to fully understand QCD.
- Lepton scattering over a broad kinematic range will be the principal experimental tool.
- Theory and simulation will be equal partners to experiment in this ambitious endeavor.
- The U.S. is a major player with the Jefferson Lab world class capability and the EIC anticipated at BNL in about a decade.
- China is building its community and making plans.
- Together we can make enormous progress.