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# Meson Structure Studies at EIC

May 14<sup>th</sup>, 2024

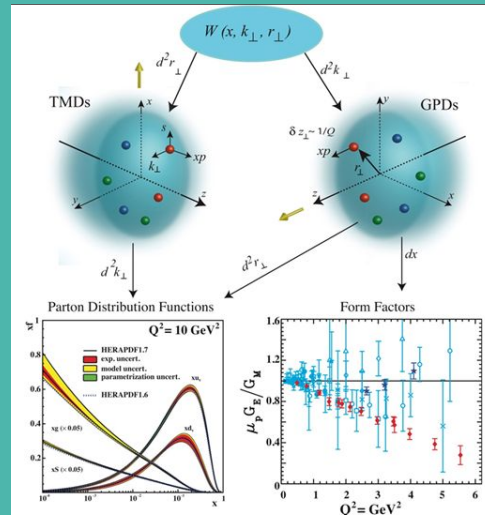
Richard L. Trotta



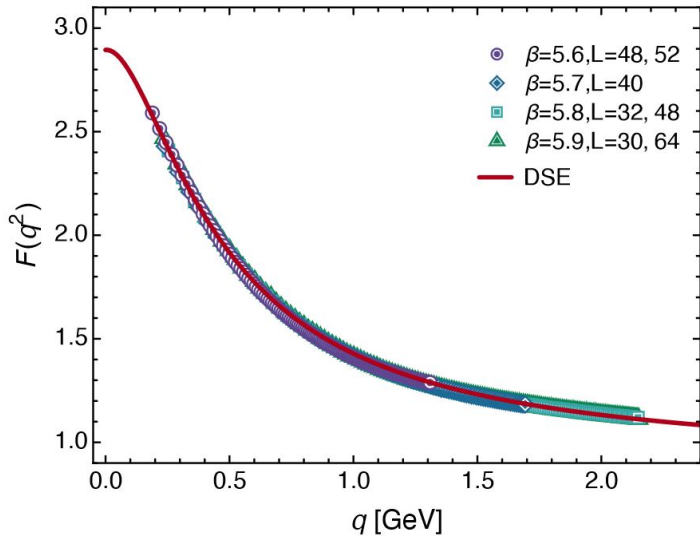
# Overview

1. Introduction
2.  $\pi^+$  Structure Functions at EIC
3.  $\pi^+$  Form Factors at EIC
4.  $K^+$  Structure at EIC

# Introduction



# Overview of Pion and Kaon Structure

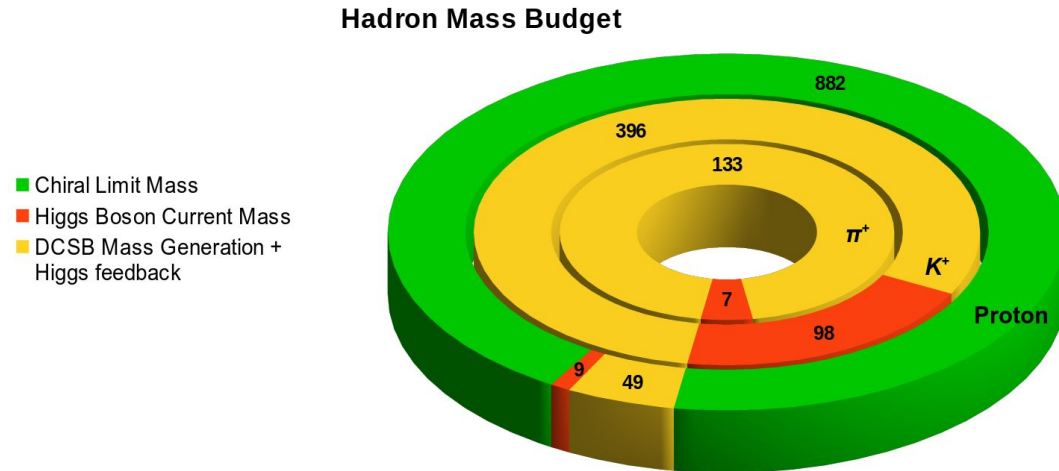


2203.00942 [hep-ph] Few Body Syst. 63 (2022) 2, 42

- The pion is both the lightest bound quark system with a valence  $\bar{q}q$  structure
- The kaon is the next simplest system containing strangeness
- Both are **Nambu-Goldstone bosons**
- There are exact statements from QCD in terms of current quark masses due to PCAC [Phys. Rep. 87 (1982) 77; Phys. Rev. C 56 (1997) 3369; Phys. Lett. B420 (1998) 267]
  - From this, it follows the mass of bound states increase as  $\sqrt{m}$  with the mass of the constituents
  - In both DSE and IQCD, the mass function of quarks is the same.

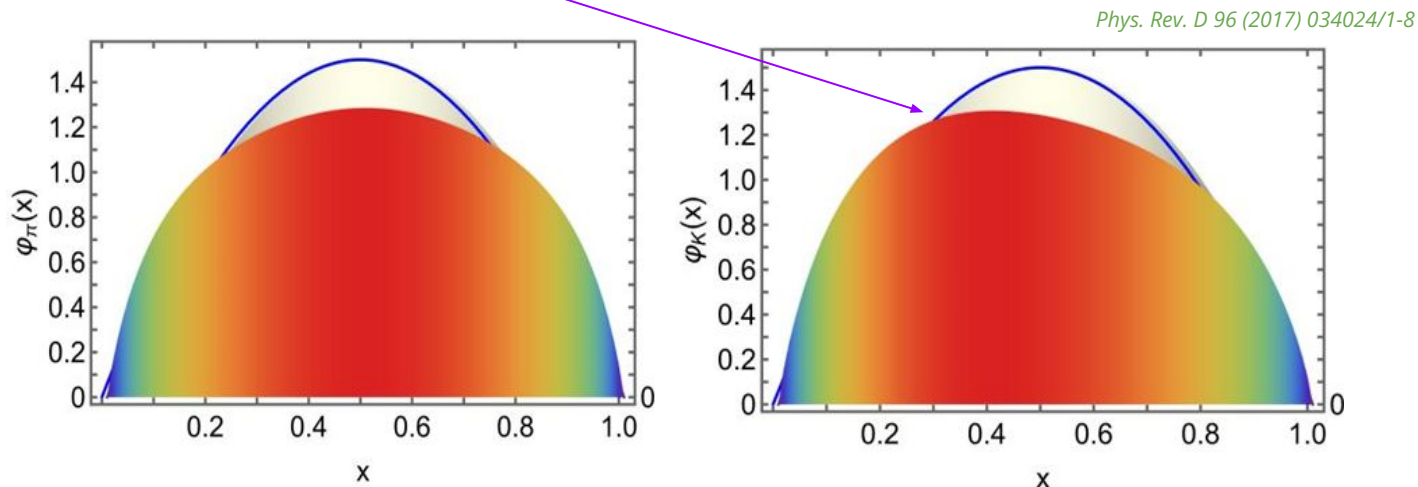
# Pion and Kaon Discrepancy

- The mass budgets for the lightest mesons,  $\pi$  and K, differ significantly from those of heavy nucleons and even from each other!
- By comparing distributions of light versus strange quarks within mesons...
  - We can measure signals of EHM



# Kaon Strangeness

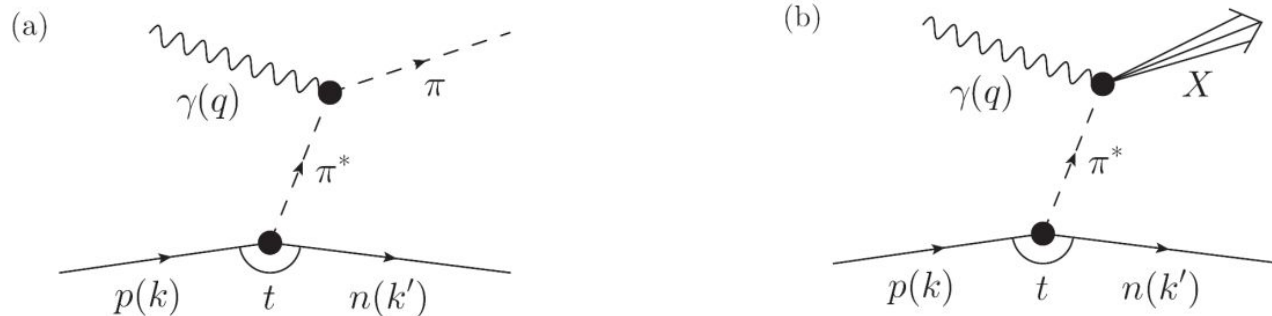
- Data suggests that **heavier flavor** quark mass is primarily generated through the **Higgs mechanism**
- The **kaon** sits in a unique position because its quark composition is both light and heavy ( $u\bar{s}$ )
  - **EHM** generates broadening in both  $\pi$  &  $K$
  - **EHM + Higgs interference** is responsible for skewing in kaon



Broadening can be verified, e.g., in  $\pi$  and  $K$  elastic form factor measurements at large  $Q^2$

# Accessing the Pion and Kaon Structure

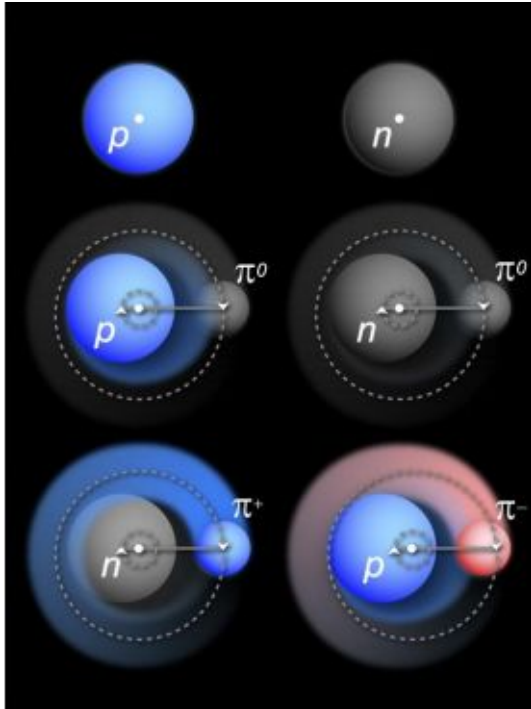
- At **low -t** values, the cross-section displays behavior characteristic of meson pole dominance
  - The **Sullivan process** can provide reliable access to a meson target in this region
- Experimental studies over the last decade have given confidence in the electroproduction method yielding the **physical pion form factor**



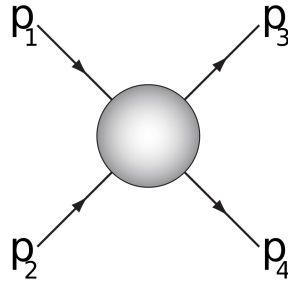
Pion cloud can access a) Elastic Form Factor b)

PDF

# Sullivan Process



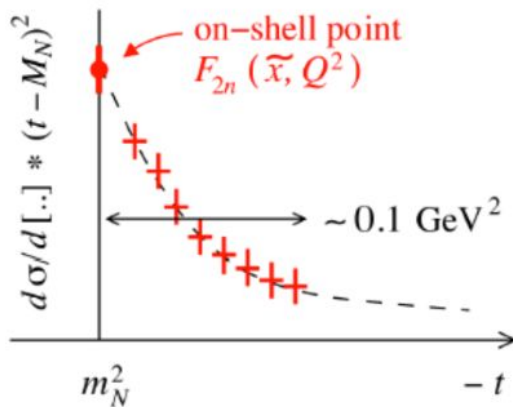
- Sullivan process is **probing the meson cloud** of the proton to study the structure of pions and kaons.
- At low  $t$ , the cross-section of the forward nucleon exhibits characteristics consistent with **meson pole dominance**.
- Meson pole dominance implies that the scattering behavior observed is primarily governed by the **exchange of mesons**
  - Leading to resonant enhancements in the scattering cross-sections



$$t = (p_1 - p_3)^2 = (p_4 - p_2)^2$$



# Off-Shell Considerations

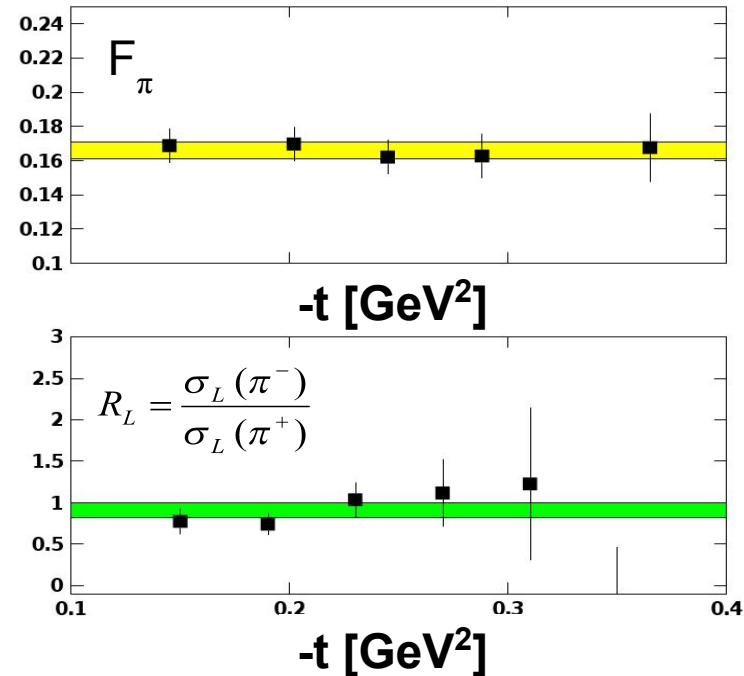


S-X Qin, C. Chen, C. Mezrag, C.D. Roberts, *Phys. Rev. C* 97 (2018) 015203

- A concern of using the Sullivan process is the off-shell considerations that arise from using a **virtual (off-shell) particle as a target**.
- Sullivan process can provide reliable access to a meson target as  $t$  becomes **space-like**
- If the pole associated with the **ground-state meson** remains the dominant feature of the process...
  - The structure of the related correlation **evolves slowly and smoothly** with virtuality
- A well-constrained experimental analysis should be reliable
  - For the **pion** when  $-t \leq 0.6 \text{ GeV}^2$
  - For the **kaon** when  $-t \leq 0.9 \text{ GeV}^2$

# Experimental Validation

- Data is taken covering a **range in t**
- Compare this data with phenomenological and theoretical expectations
  - $F_\pi$  values **do not** depend on  $-t$  which gives confidence in applicability of model to the kinematic regime of the data
- Verify that the pion pole diagram is the **dominant contribution** in the reaction mechanism
  - $R_L (= \sigma_L(\pi^-)/\sigma_L(\pi^+))$  approaches the **pion charge ratio**, consistent with pion pole dominance



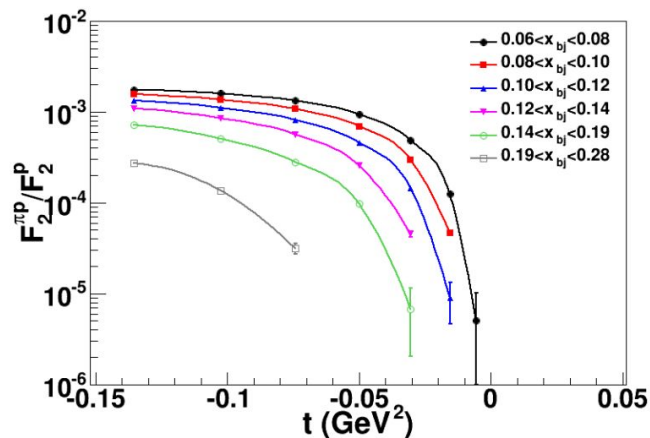
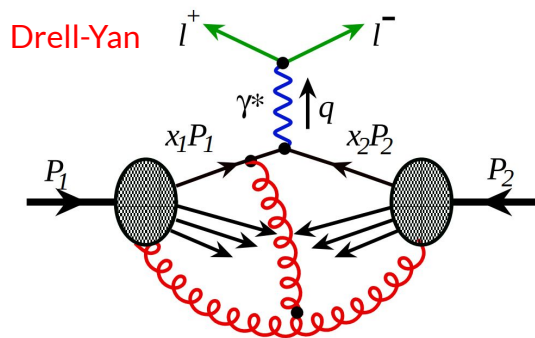
*T. Horn, C.D. Roberts, J. Phys. G43 (2016) no.7, 073001*

*G. Huber et al, PRL112 (2014)182501*

*R. J. Perry et al., arXiv:1811.09356 (2019)*

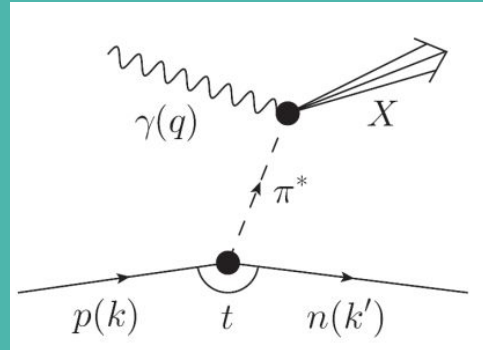
# EIC Capabilities

- $L_{\text{EIC}} = 10^{34}$  e-nucleons/cm<sup>2</sup>/s =  $1000 \times L_{\text{HERA}}$
- Fraction of proton wave function related to pion Sullivan process is roughly  $10^{-3}$  for a small  $-t$  bin (0.02)
  - Pion data at EIC should be comparable or better than the proton data at HERA, or the 3D nucleon structure data at COMPASS
- By mapping pion (kaon) structure for  $-t < 0.6$  (0.9) GeV<sup>2</sup>, we gain at least a decade as compared to HERA/COMPASS
- Consistency checks with complementary COMPASS++/AMBER Drell-Yan data can show process-independence of pion structure information



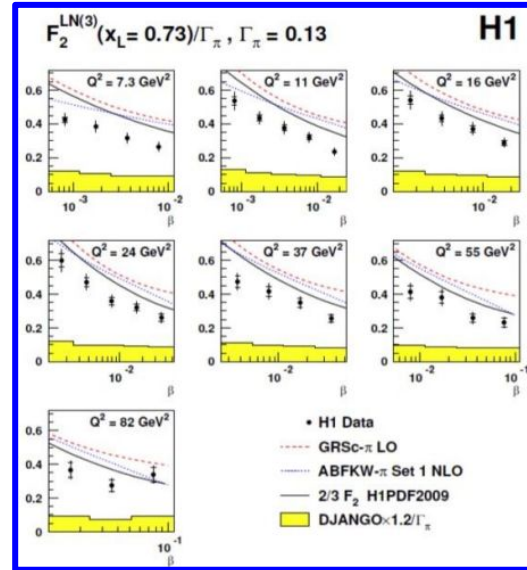
Jefferson Lab TDIS Collaboration, JLab Experiment C12-15-005  
Journal of Physics G (2021) arXiv:2102.11788

# $\pi^+$ Structure Functions at EIC

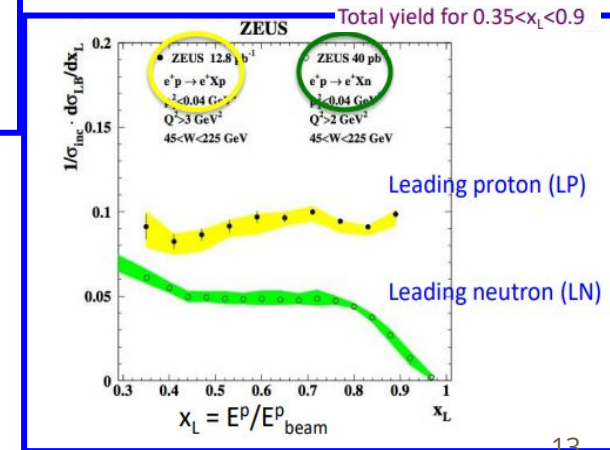
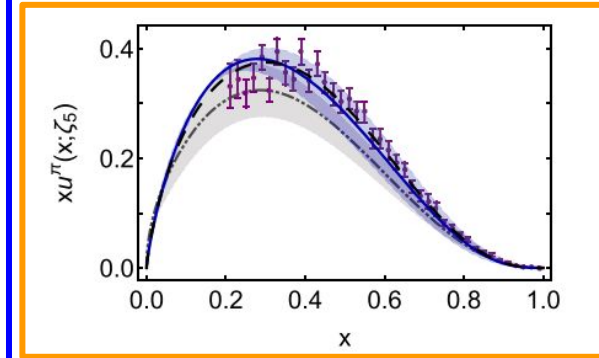


# Existing Meson Structure Function Measurements

- Knowledge of the pion structure function is very limited...
  - At low  $x$  - HERA TDIS data through Sullivan process
  - At large  $x$  - Pionic Drell-Yan from nucleons in nuclei
- One pion exchange is the dominant mechanism
  - Can extract pion structure function
  - In practice, use in-depth model and kinematic studies to include rescattering, absorption...

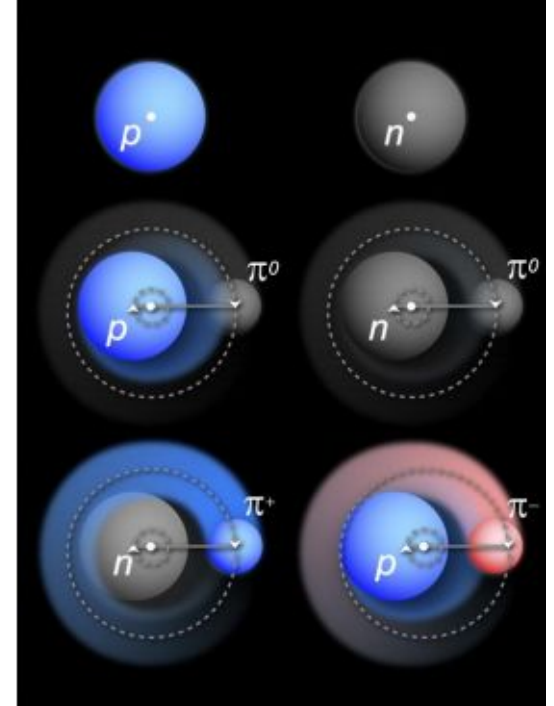
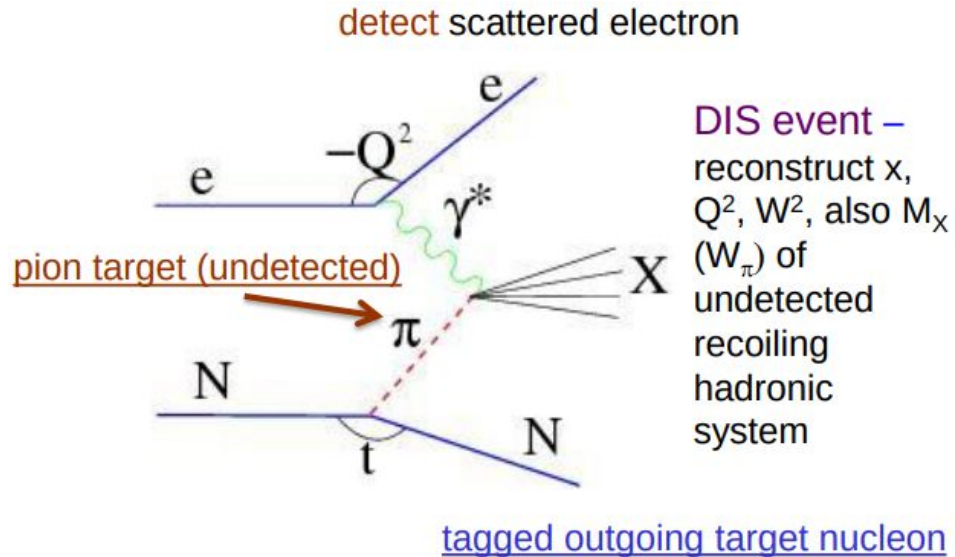


DESY 08-176 JHEP06 (2009) 74  
 Eur. Phys. J. C (2020) DOI:10.1140/epjc/s10052-020-08578-4



# Tagged Deep Inelastic Scattering (TDIS)

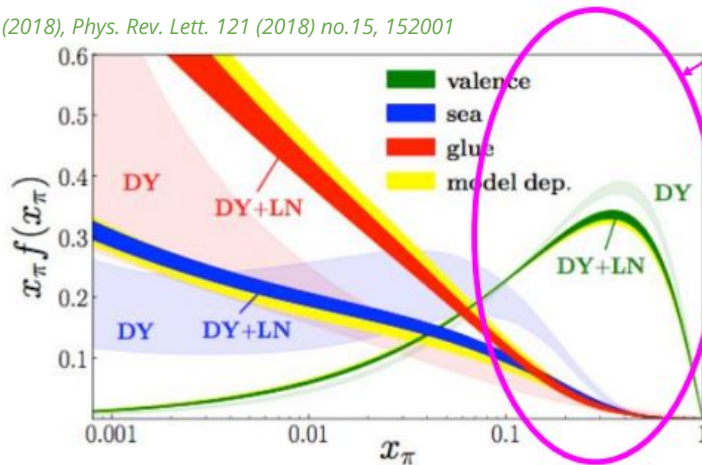
- Using the **Sullivan process** – scattering from nucleon-meson fluctuations



# Global Fits: Pion and Kaon Structure Functions

- First MC global QCD analysis of pion PDFs
  - Using Fermilab DY and HERA Leading Neutron data
  - Significant reduction of uncertainties on sea quark and gluon distributions in the pion with inclusion of HERA leading neutron data
  - Implications for “TDIS” (Tagged DIS) experiments at JLab

Barry, Sato, Melnitchouk, Ji (2018), *Phys. Rev. Lett.* 121 (2018) no.15, 152001



- JLab 12 GeV: Tagged Pion and Kaon TDIS
- Also prospects for kaon DY at COMPASS and pion and kaon LN at EIC

DY =  $\pi N$  Drell-Yan

LN = Leading Neutron

# $\pi^+$ Structure Functions ( $F_2^{\pi^+}$ )

- For projections, a Fast Monte Carlo that includes the Sullivan process is used

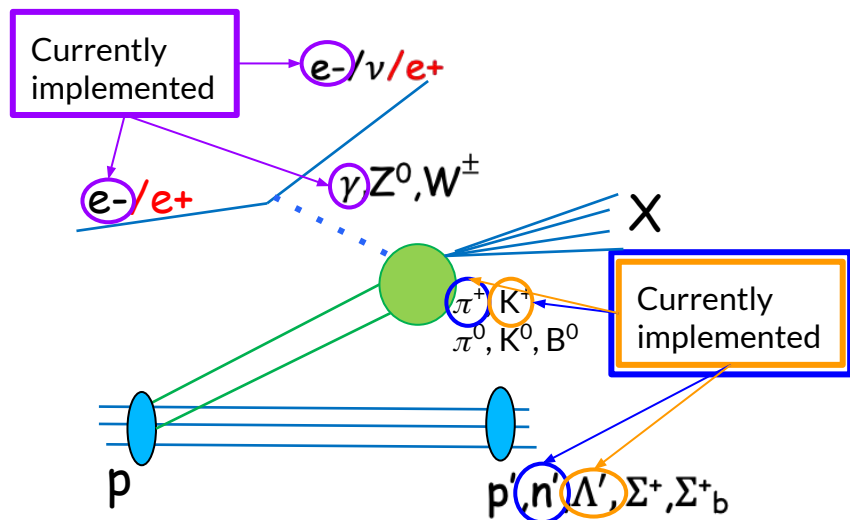
- PDFs, form factor, fragmentation function projections

- Progress made with generator documented in the following publications...

- Feasibility of structure function data [2019 EPJA article ([DOI:10.1140/epja/i2019-12885-0](https://doi.org/10.1140/epja/i2019-12885-0))]
  - Pion structure function projections [2021 JPhysG ([arXiv:2102.11788](https://arxiv.org/abs/2102.11788))]
  - **Detector proposals using ePIC configuration** [2023 NIM ([DOI:10.1016/j.nima.2023.168238](https://doi.org/10.1016/j.nima.2023.168238))]

- $\pi$  structure function: Measure DIS cross section with tagged neutron at small  $-t$

- Beam energies: 5 on 41, 5 on 100, 10 on 100, 10 on 135, 18 on 275

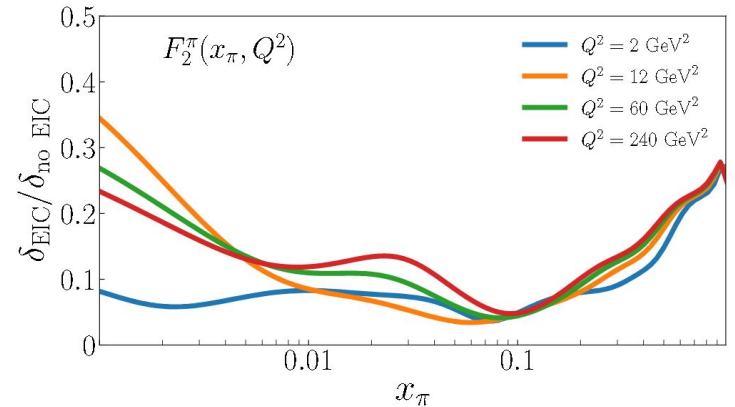
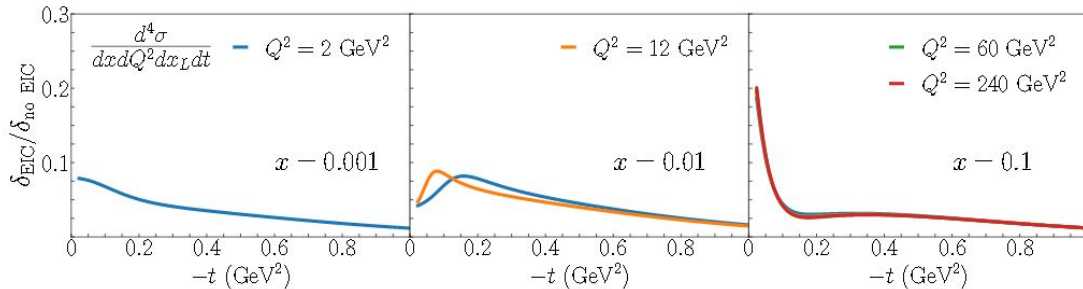
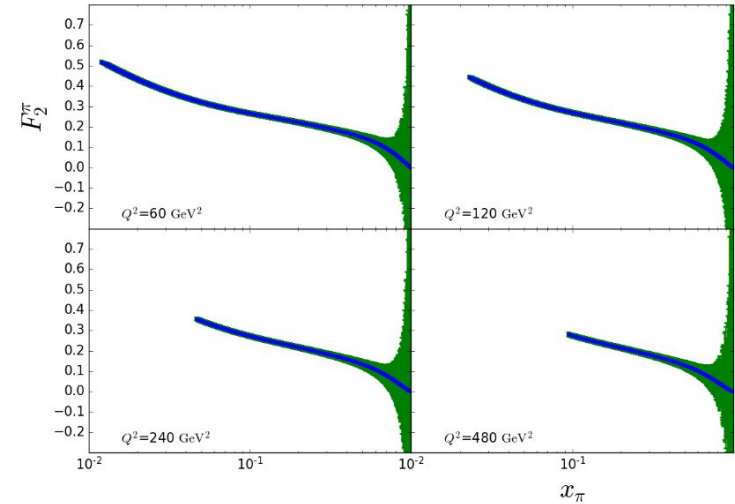




# $F_2^\pi$ Projections

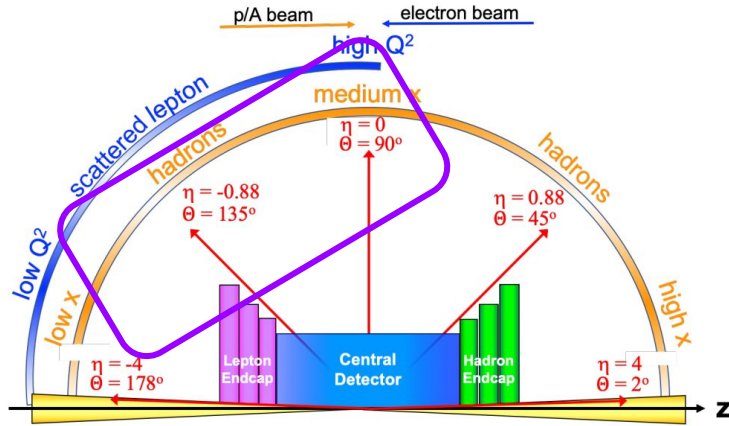
- Reasonable uncertainties in the mid-to-large  $x$  region but **increasing rapidly as  $x \rightarrow 1$** 
  - Even with these restrictions, the coverage in mid to high  $x$  is unprecedented
- Access to a significant range of  $Q^2$  and  $x$ , for appropriately small  $-t$ 
  - Allows for much-improved **insights in the gluonic content** of the pion

NLO through pion PDFs

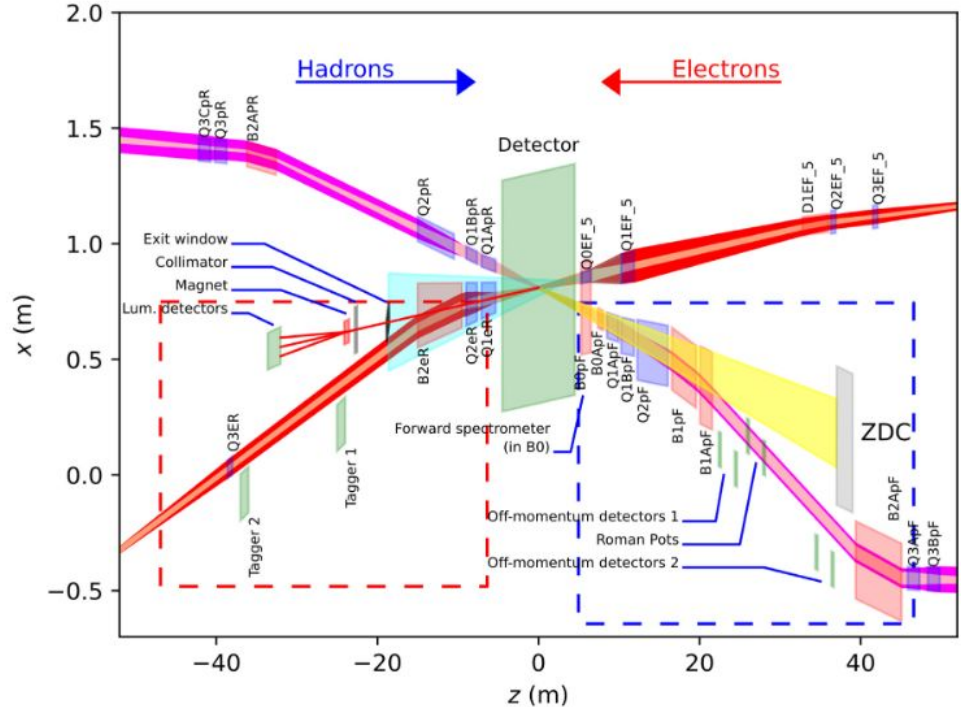
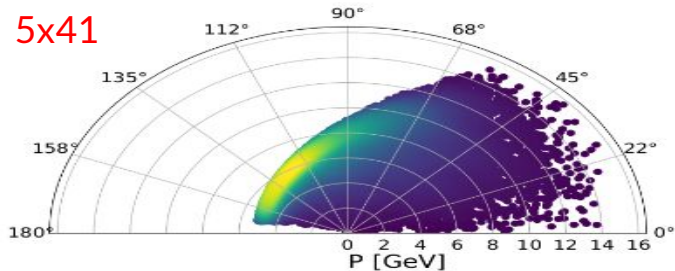


# Meson SF – Scattered Electron

- Scattered electrons can be detected in the **central detector**

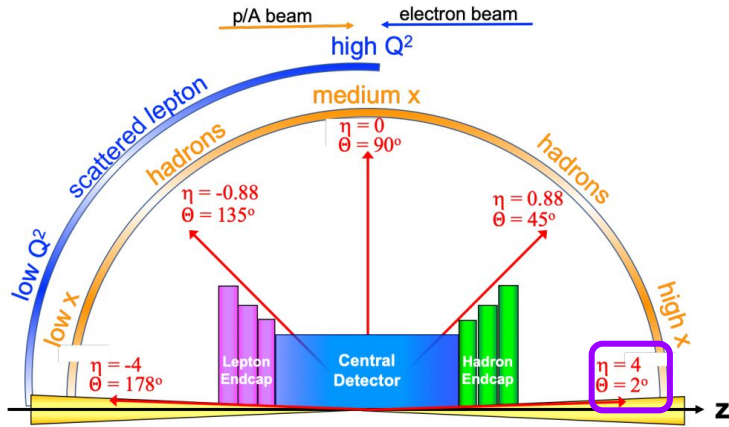


5x41

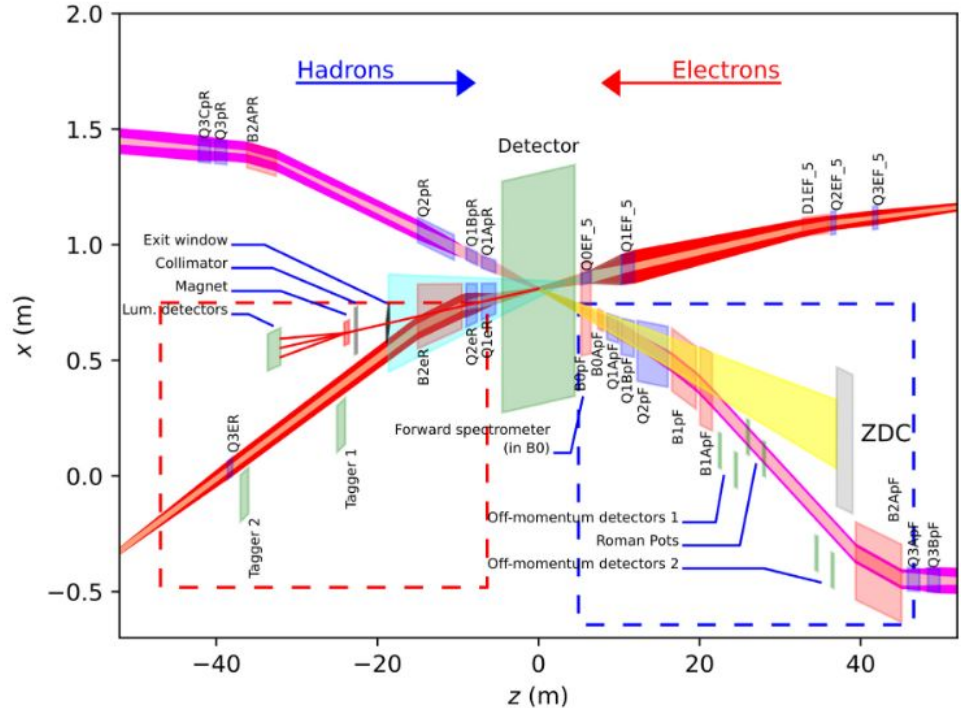
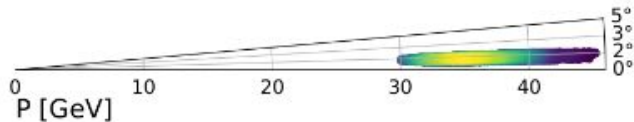


# Meson SF – Forward Baryon

- Baryon (neutron, lambda) at **very small forward angles** and **nearly the beam momentum**

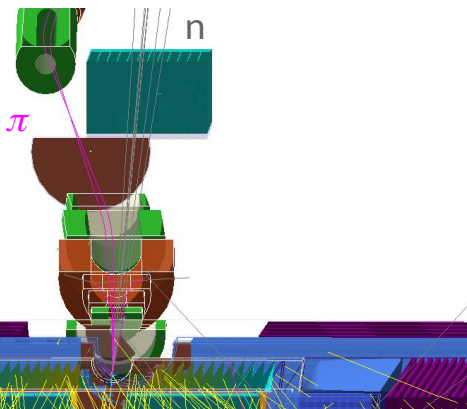
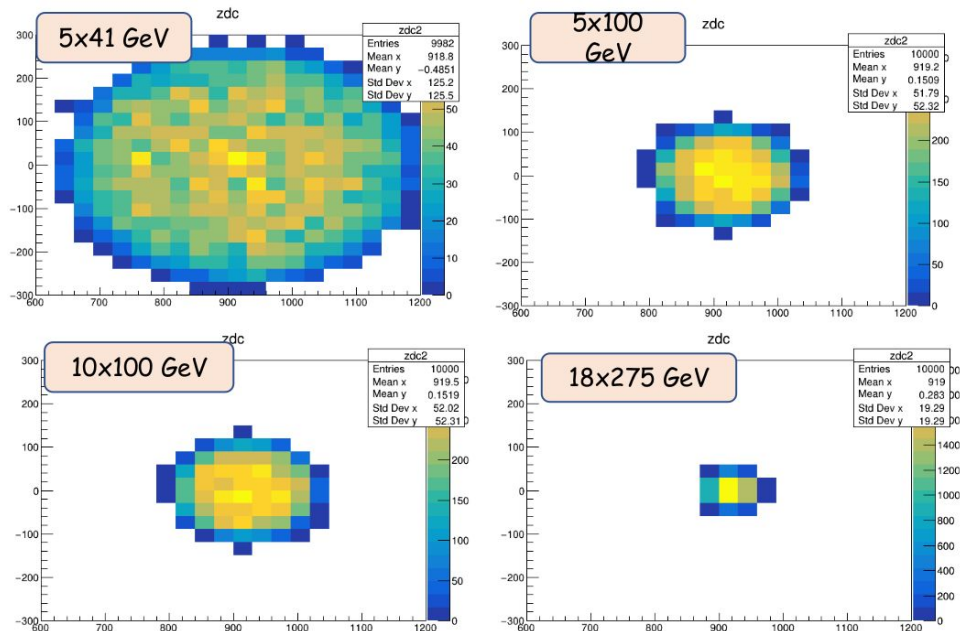


5x41



# $F_{\pi}^{\pi}$ Neutron Final State (1)

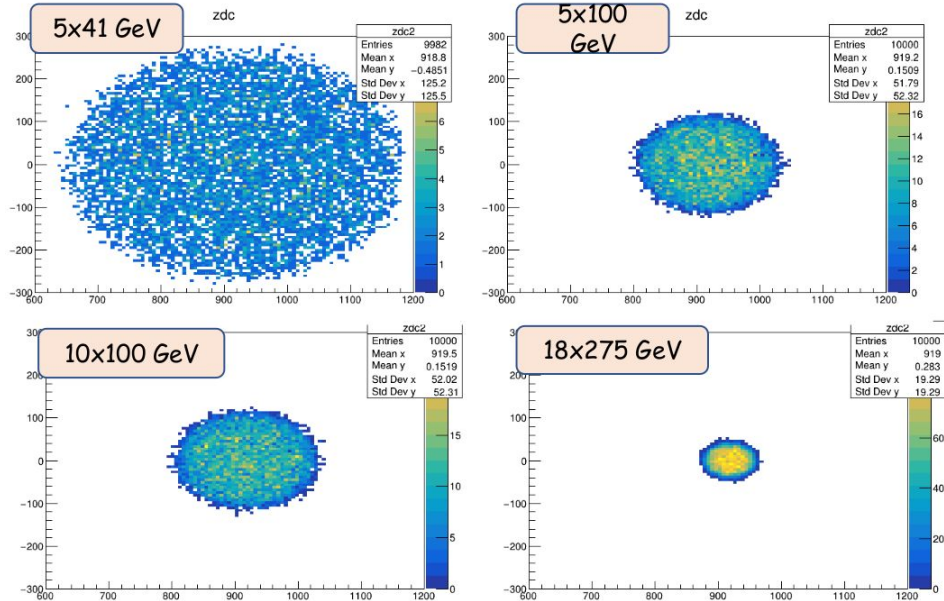
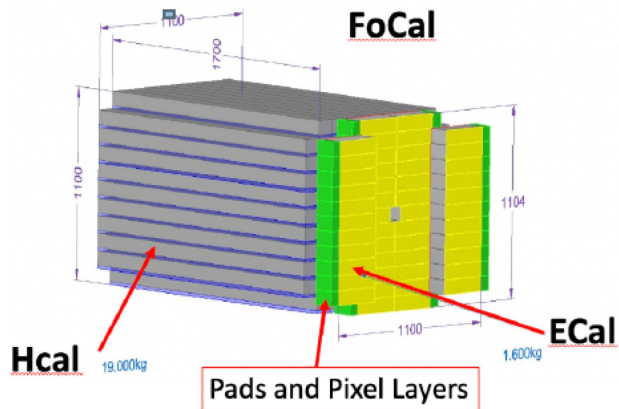
- For neutron final state use ZDC
  - detection fractions  $\sim 100\%$  for 60x60 cm ZDC size
  - Need good ZDC angular resolution for required  $t$  resolution



- ZDC: [ 60x60 cm, 20 bins  $\rightarrow$  3 cm towers ]
- The 60x60 cm ZDC allows for high detection efficiency for wide range of energies (K-A detection benefits from 5 on 41, 5 on 100)
  - Higher energies (10 on 100, 18 on 275) show too coarse of a distribution at this resolution

# F<sup>π</sup><sub>2</sub> Neutron Final State (2)

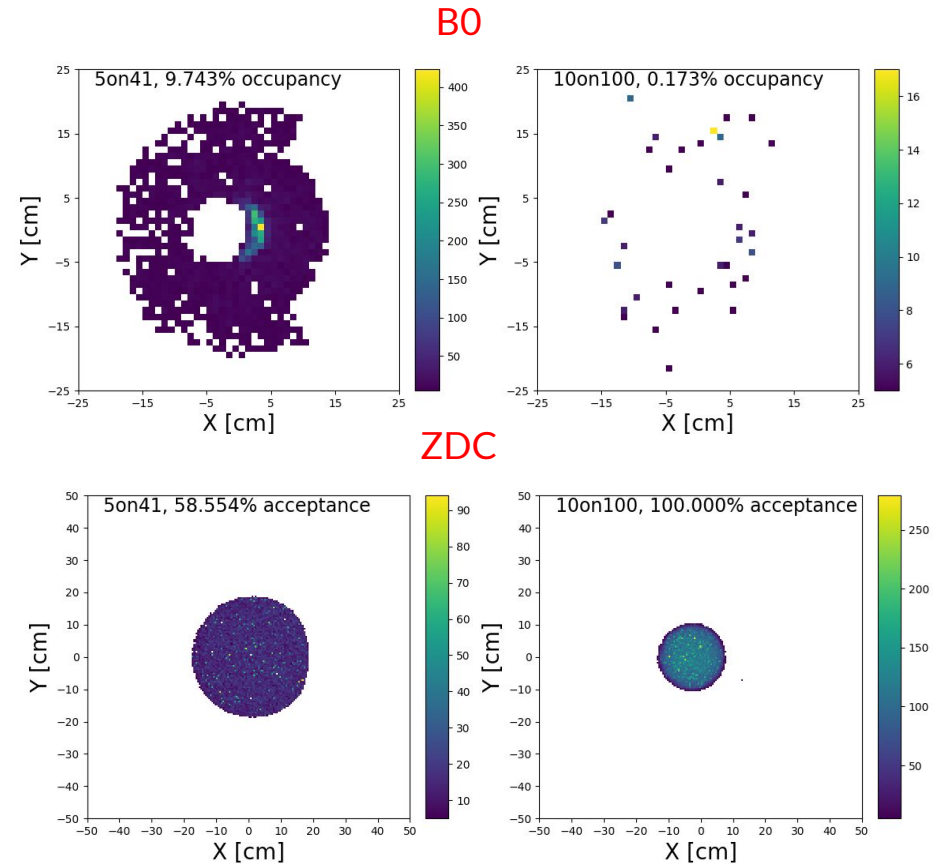
- For neutron final state use ZDC
  - detection fractions ~100% for 60x60 cm ZDC size
  - Need good ZDC angular resolution for required t resolution



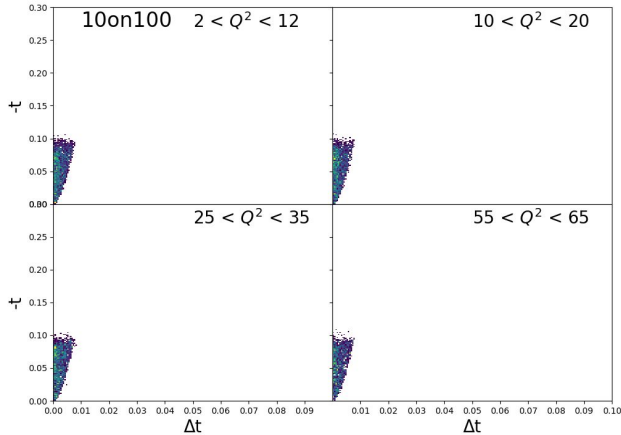
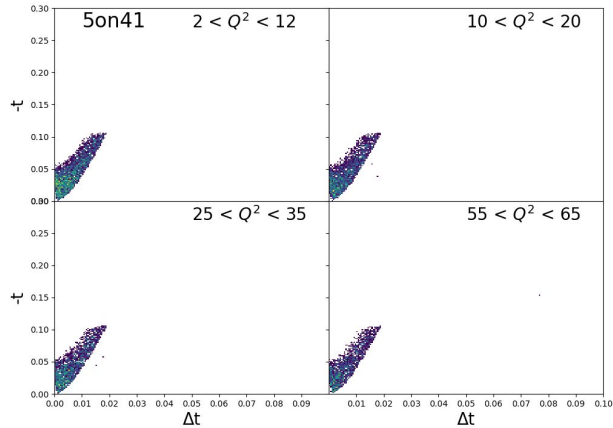
- ZDC: [ 60x60 cm, 100 bins → 0.6 cm towers ]
- If we want energies over 100 GeV, we will need resolution of ~1 cm or better

# $F^{\pi}_2$ Neutron Final State (3)

- Neutron final state uses Zero Degree Calorimeter (ZDC)
- Constraining neutron energy around  $50\%/\sqrt{E}$  will assure an achievable resolution in x
- The ZDC must reconstruct the energy and position well enough to constrain both scattering kinematics and 4-momentum of pion
- Acceptance  $\sim 100\%$  for energies  $>5\text{on}41$  with the  $60\times 60$  cm ZDC size
- B0 occupancy shows significant amount of leading neutrons hitting the detector for  $5\text{on}41$  corresponding to a significant drop in ZDC acceptance

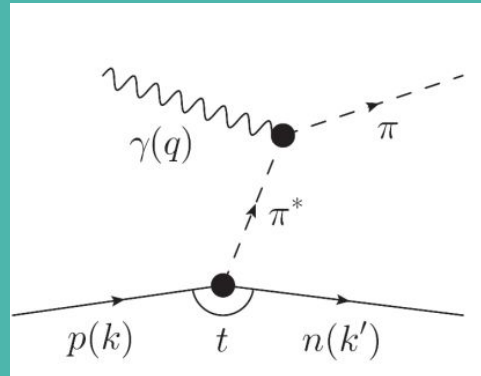


# $F_2^\pi$ -t reconstruction



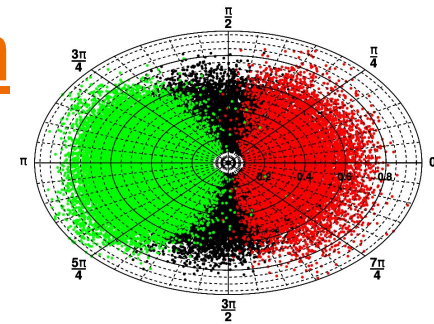
- A good ZDC angular resolution is required for a sufficient  $-t$  resolution
- The deviation of  $t$  from its detected value,  $\Delta t = t - t_{\text{Truth}}$ , is much greater for 5on41
- This provides a consistent picture between ZDC acceptance and  $-t$  resolution for the energy ranges
- Access to a significant range of  $Q^2$  and  $x$ , for appropriately small  $-t$ , will allow for much improved insights in the gluonic content of the pion

# $\pi^+$ Form Factors at EIC

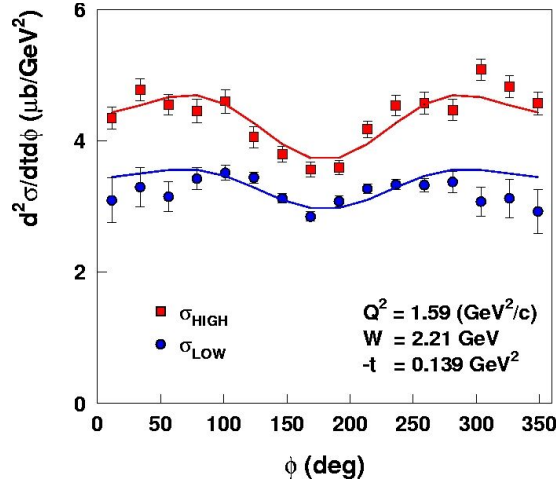




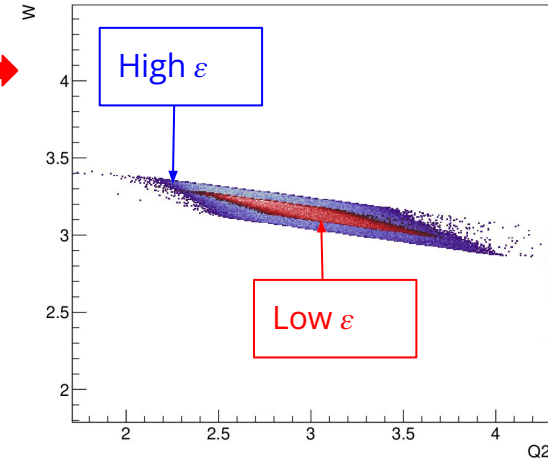
# Experimental considerations for FF extraction



- $\sigma_L$  is isolated using the [Rosenbluth separation technique](#)
- Measure the cross section at two beam energies and fixed  $W$ ,  $Q^2$ ,  $-t$



1. [Phase space matching](#) to constrain the kinematic region for the two differing beam energies  $\rightarrow$
  2. Extract cross section in  $-t$  and  $\phi$  bins
- $$\left( \frac{d\sigma_{exp}^2}{dt d\phi} \right) \Big|_{Q^2=\bar{Q}^2, t=\bar{t}} = \frac{Y_{exp}}{Y_{SIMC}} \left( \frac{d\sigma_{model}^2}{dt d\phi} \right) \Big|_{Q^2=\bar{Q}^2, t=\bar{t}}$$
3. This allows for the [simultaneous extraction](#) of  $L$ ,  $T$ ,  $LT$ , and  $TT$



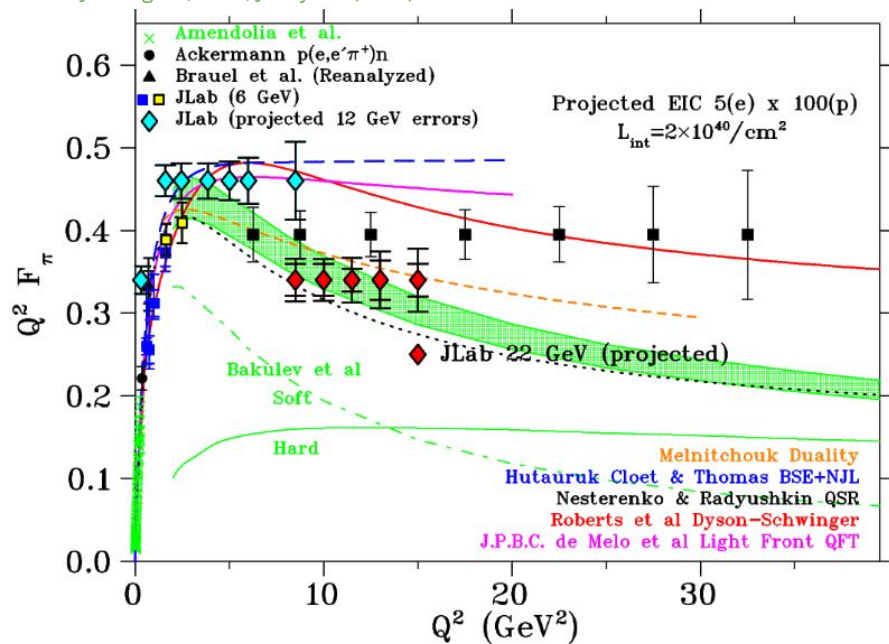
T. Horn et al., *PhysRevC* **97**(2006)192001

$$2\pi \frac{d^2\sigma}{dt d\phi} = \varepsilon \frac{d\sigma_L}{dt} + \frac{d\sigma_T}{dt} + \sqrt{2\varepsilon(\varepsilon+1)} \frac{d\sigma_{LT}}{dt} \cos \phi + \varepsilon \frac{d\sigma_{TT}}{dt} \cos 2\phi$$

# Existing Charged Meson Form Factor Measurements

- $\pi^+$  and  $K^+$  form factors are of special interest in hadron structure studies
- **Clearest case for studying transition from non-perturbative to perturbative regions**
- $\pi^+$  form factor has data covering a wide range of  $Q^2$  (up to  $8.5 \text{ GeV}^2$ )
  - $F_{\pi 1}/F_{\pi 2}$ : 2006, 2008
  - **PionLT**: E12-09-011 which covers KaonLT data plus Summer 2019
  - **PionLT**: E12-19-006 ran Fall 2021, Winter 2022, Summer 2022 and Fall 2022

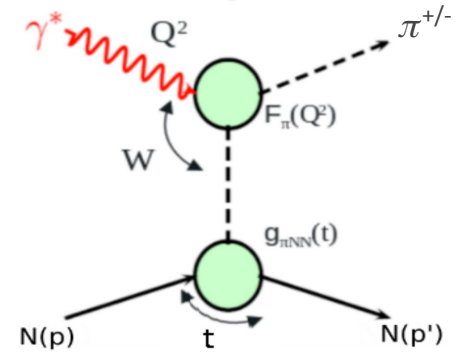
J Arrington, et al., J. Phys. G (2021) arXiv:2102.11788



- Meanwhile, the  $K^+$  form factor data is **very limited**
  - Before the JLab 12 GeV upgrade, there was a lack of facilities with capabilities required

# $\pi^+$ Form Factor: An alternate technique

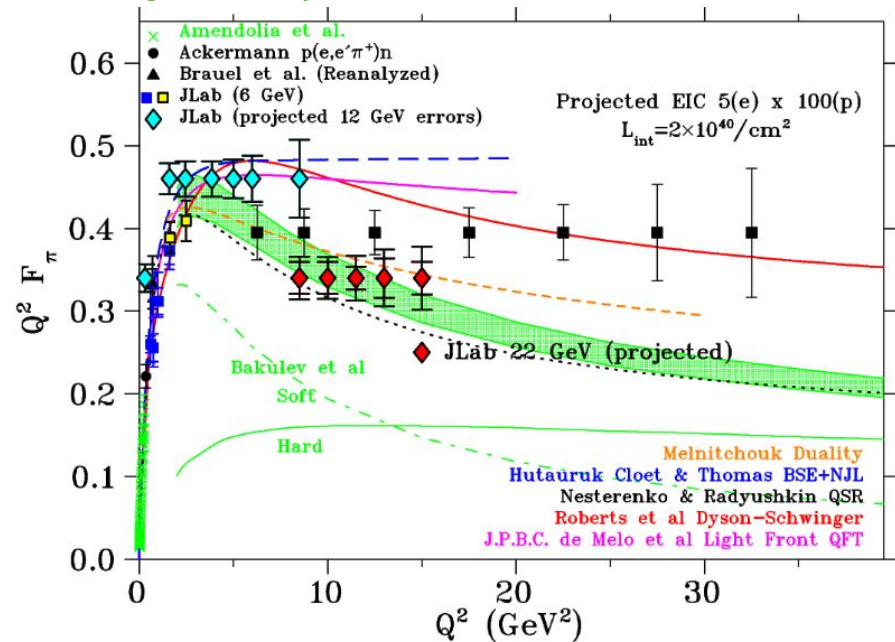
- An alternate technique is available to access  $\sigma_L$  via a model validated with **exclusive  $\pi^-/\pi^+$  ratios** from deuterium.
- After evaluating  $d\sigma_L/dt$  across the  $-t$  range from  $-t_{\min}$  to **approximately  $-t = 0.6 \text{ GeV}^2$**  (i.e., pion pole region)
  - $F_\pi(Q^2)$  is derived by comparing observed  $dL/dt$  values with the most accurate electroproduction model available
- This model considers off-shell pion and recoil nucleon effects
- The acquired  $F_\pi$  values theoretically rely on the employed model
  - However, it's expected that **this reliance diminishes as  $-t$  decreases**
  - Conducting measurements across various  $-t$  values is crucial for validating the model.



$$R = \frac{\sigma[n(e, e'\pi^-p)]}{\sigma[p(e, e'\pi^+n)]} = \frac{|A_V - A_S|^2}{|A_V + A_S|^2}$$

# $\pi^+$ Form Factors ( $F_\pi$ )

- Measurements of the  $p(e, e'\pi^+)n$  reaction at the EIC can potentially extend the  $Q^2$  reach of  $F_\pi$  measurements even further
- **Exclusive** reactions are of interest
  - $p(e, e'\pi^+)n$  exclusive reaction particular with  $p(e, e'\pi^+)X$  SIDIS events as the background
  - A clean sample of  $p(e, e'\pi^+)n$  events needs to be isolated by detecting the neutron
- A challenging measurement however
  - Need good identification of  $p(e, e'\pi^+)n$  triple coincidences
  - Conventional L-T separations are not feasible due to the inability to reach low enough  $\varepsilon$  values, which are essential for accurate separation.
  - Need to use a model to isolate  $d\sigma_L/dt$  from  $d\sigma_{\text{uns}}/dt$

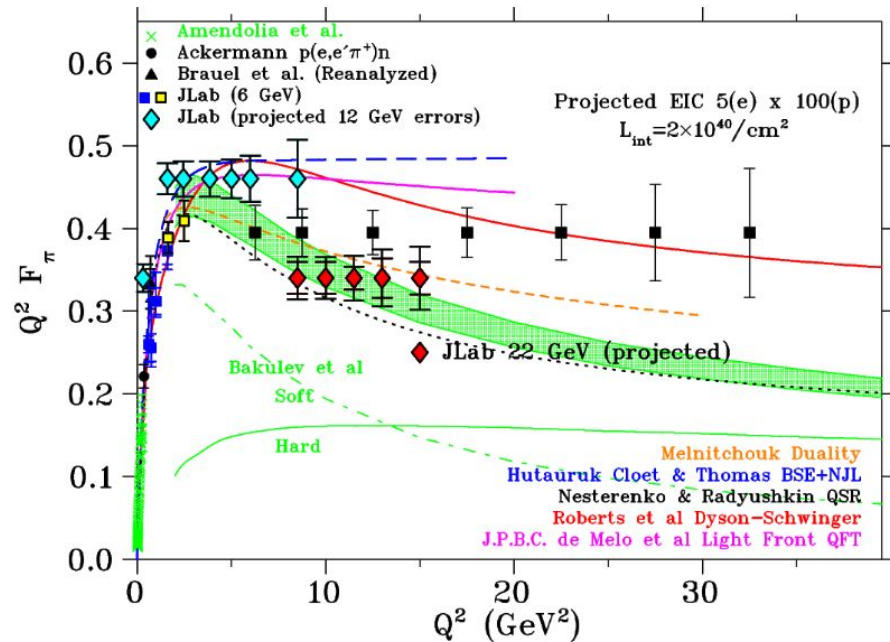


- Major updates have been made to the [Deep Exclusive Meson Production event generator \(DEMPgen\)](#) to enhance the reliability of feasibility studies
- Updated DEMPgen is used to generate new files for both pion and kaon reactions, which will then undergo the latest ePIC simulations

# $F_\pi$ Projections

- ePIC appears to be capable of measuring  $F_\pi$  to  $Q^2 \sim 32.5 \text{ GeV}^2$
- Error bars represent real projected error bars
  - 2.5% point-to-point
  - 12% scale
  - $\delta R = R$ ,  $R = \sigma_L / \sigma_T$
  - $R = 0.013 - 0.14$  at lowest  $-t$  from VR model
- **Uncertainties dominated by  $R$  at low  $Q^2$**
- Statistical uncertainties dominate at high  $Q^2$
- Results look promising, need to test  $\pi^-$  too
- **More details in...**
  - 2024 DEMPgen (arXiv: 2403.060 [hep-ph])
  - 2023 A. Bylinkin et al. (NIM A 1052 (2023) 168238 1-40)

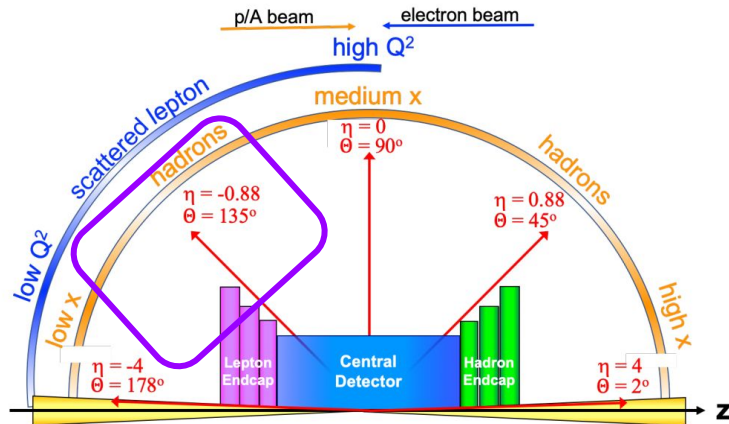
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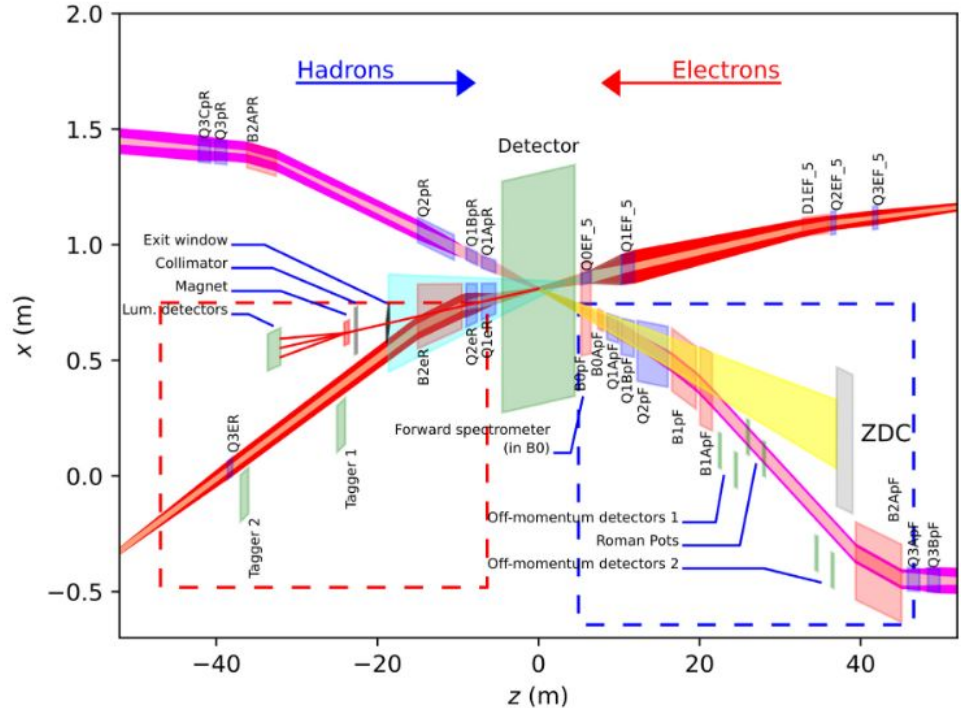
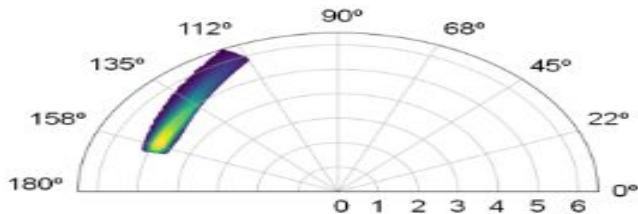
Analysis by Stephen Kay and Garth Huber

# $\pi^+$ Form Factor – Scattered Electron

- The **exclusive** electron are stuck to a tight band

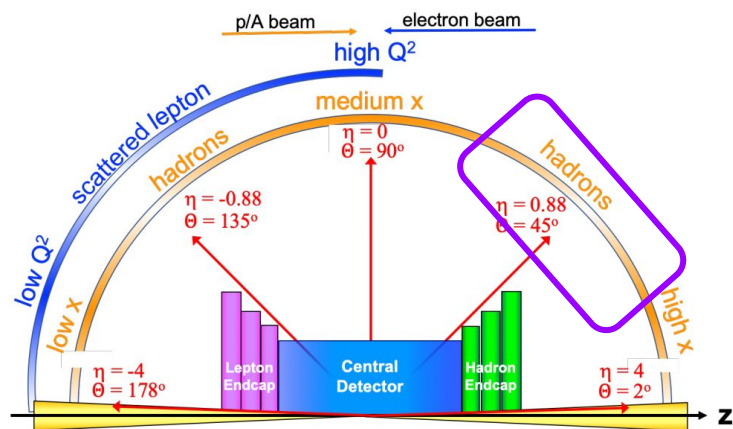


5x41

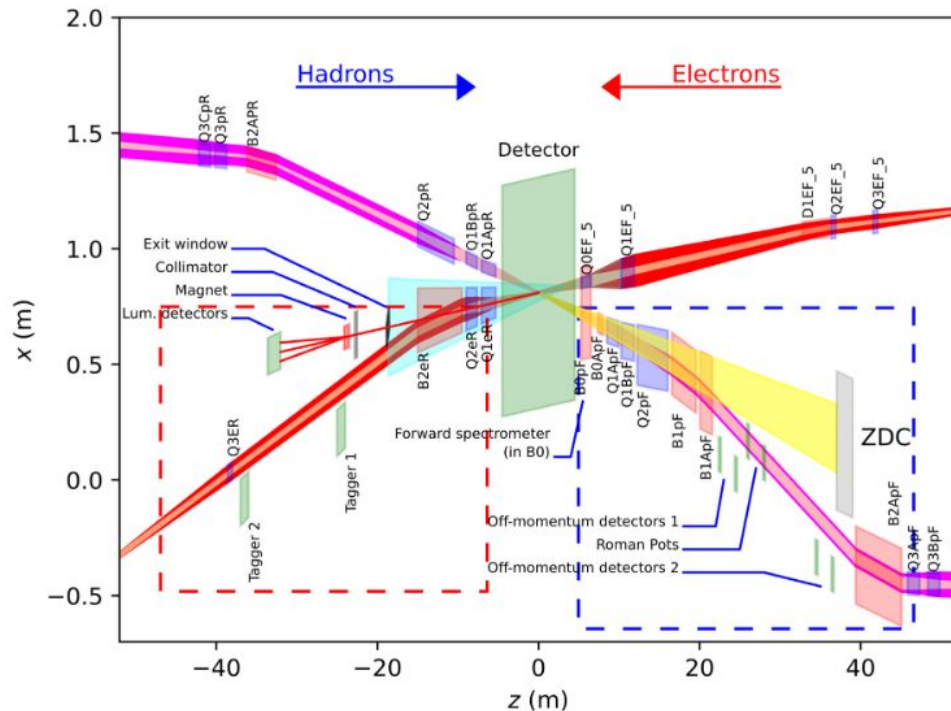
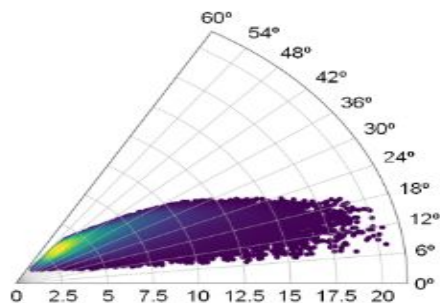


# $\pi^+$ Form Factor – Scattered $\pi^+$

- Baryon (neutron, lambda) at **very small forward angles** and **nearly the beam momentum**

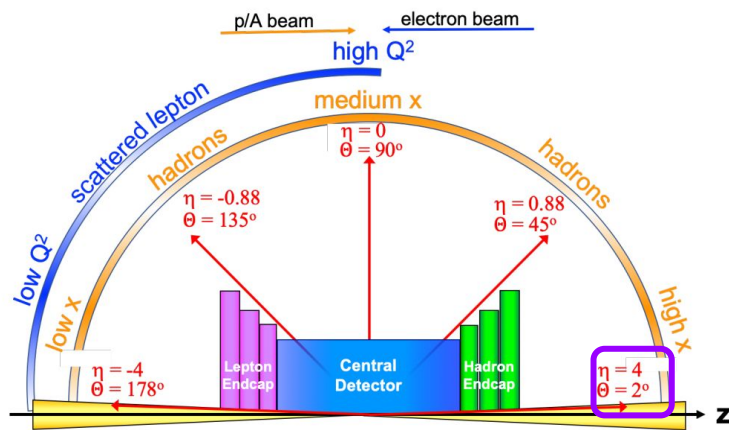


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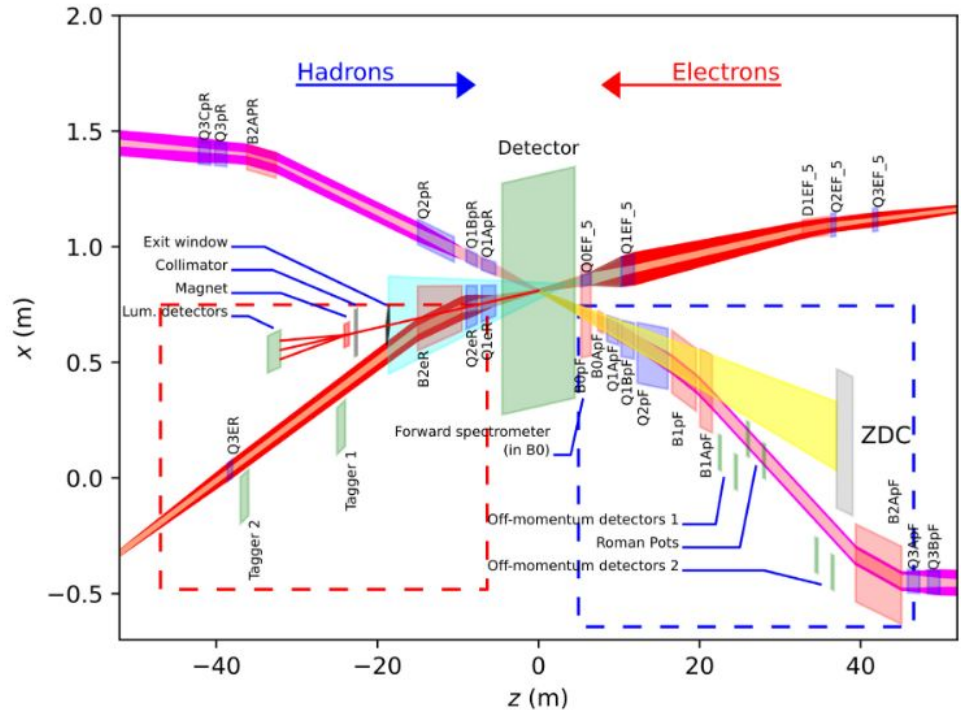
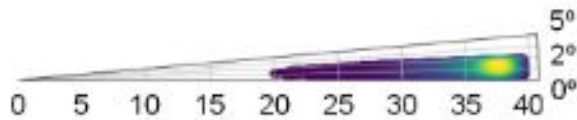


# $\pi^+$ Form Factor – Forward Baryon

- Neutron carries  $\sim 80\%$  of the momentum within  $0.2^\circ$  of outgoing proton



5x41





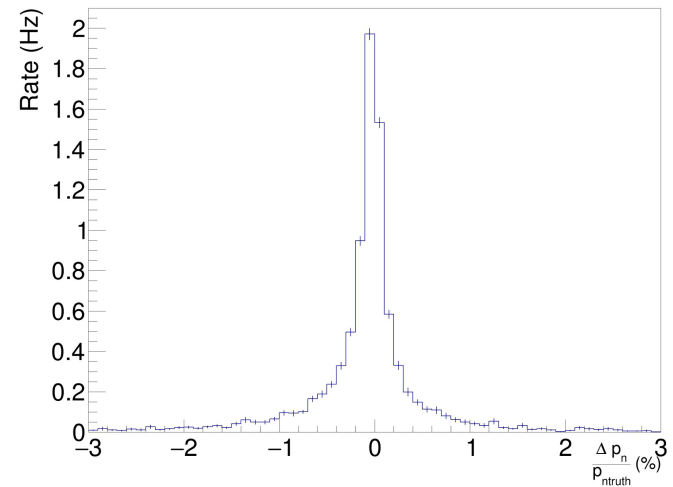
# F<sub>π</sub> Neutron Reconstruction

- High energy ZDC hit requirement used as a veto
  - ZDC neutron ERes is relatively poor though
- However, position resolution is excellent, ~ 1.5 mm
- **Combine ZDC position info with missing momentum track to reconstruct the neutron track**

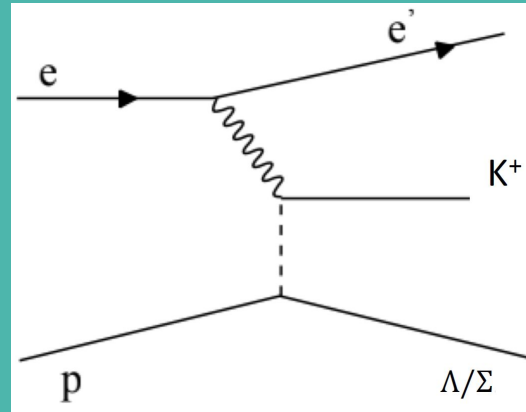
$$p_{miss} = |\vec{p}_e + \vec{p}_p - \vec{p}_{e'} - \vec{p}_{\pi^+}|$$

- Use ZDC angles,  $\theta_{ZDC}$  and  $\varphi_{ZDC}$  rather than the missing momentum angles,  $\theta_{pMiss}$  and  $\varphi_{pMiss}$
- Adjust  $E_{Miss}$  to reproduce  $m_n$
- After adjustments, reconstructed neutron track matches “truth” momentum closely

$$\frac{35\%}{\sqrt{E}} \oplus 2\%$$

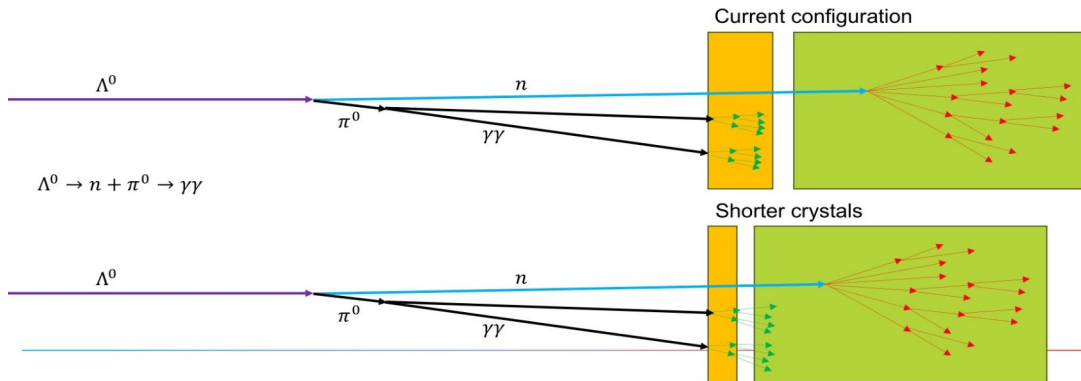
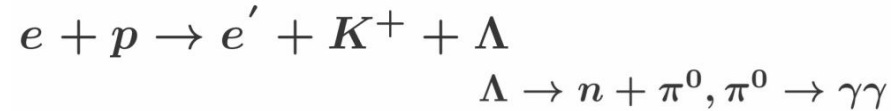
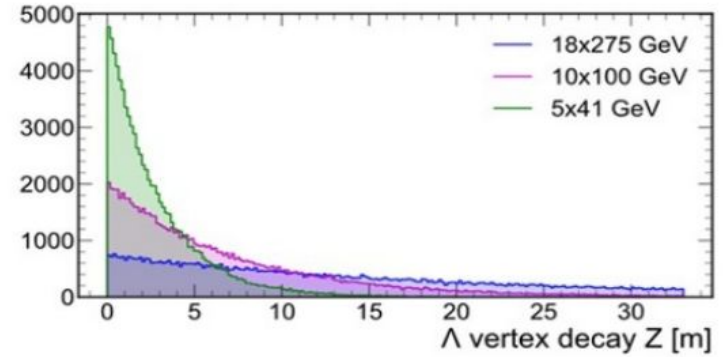


# $K^+$ Structure at EIC



# Plans for $F_K$ projections

- Track photons and neutrons from  $\Lambda$  in the ZDC – EMCAL and ZDC – HCAL
  - Will help to investigate ZDC – EMCAL thickness.
  - Impact on the  $\Lambda$  reconstruction from photons and neutrons.
- Reconstruction is considerably challenging, **uncertain about the achievable extent at present**

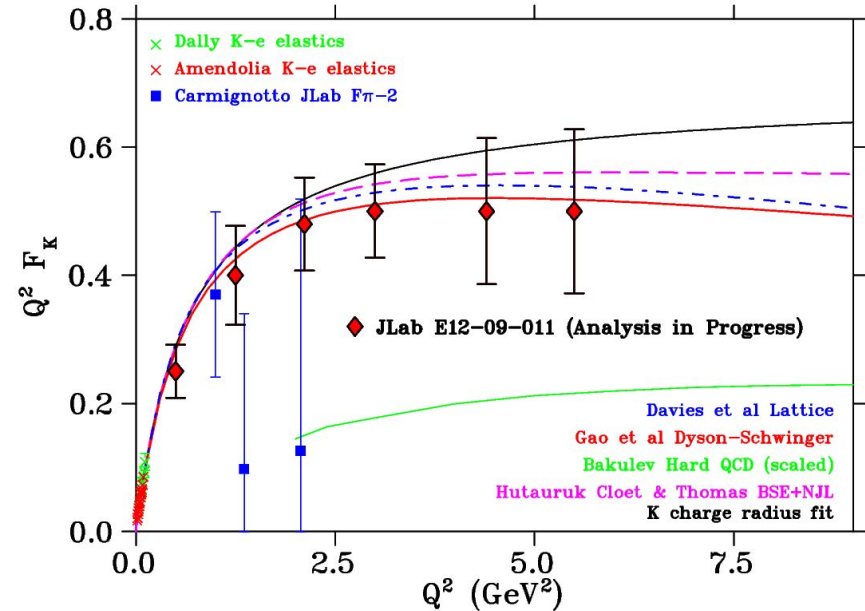


- Will perform tests on  $\Lambda$  reconstruction, focusing on efficiency, acceptance and resolution
- Aim to determine the  $F_K(Q^2)$  projections in the long term
- Analysis by Stephen Kay, Garth Huber and Love Preet**

# $F_K$ from KaonLT at Jefferson Lab

- JLab 12 GeV KaonLT (E12-09-011) experiment will provide much needed data in a wide range of  $Q^2$ ,  $W$ ,  $t$
- Data taken...
  - Fall and Winter 2018
  - Spring 2019
- **Results coming soon!**

E (GeV)	$Q^2$ (GeV <sup>2</sup> )	W (GeV)	x	$\epsilon_{\text{high}}/\epsilon_{\text{low}}$	$\Delta\epsilon$
10.6/8.2	5.5	3.02	0.40	0.53/0.18	0.35
10.6/8.2	4.4	2.74	0.40	0.72/0.48	0.24
10.6/6.2	3.0	2.32	0.40	0.88/0.57	0.31
10.6/8.2	3.0	3.14	0.25	0.67/0.39	0.28
10.6/6.2	2.115	2.95	0.21	0.79/0.25	0.54
4.9/3.8	0.5	2.40	0.09	0.70/0.45	0.25



# Plans for $F_2^K$ projections

- Goal is to extend to **tagged kaon structure function**
- Very limited data on  $F_2^K$ 
  - Exploratory data on kaon SF are planned to come from TDIS JLab experiment (C12-15-006A) in the next few years.
- Kaon projected structure function data will be of **similar quality** as the projected pion structure function data for the small-t geometric forward particle detection acceptances at EIC - studies in progress
- Currently investigating **splitting functions** as way to gain insights

$$F_2^T = \kappa f F_2 \rightarrow f_{KY}^{(rbw)}(y) = \frac{C_{KY}^2 \bar{M}^2}{(4\pi f_\phi)^2} [f_Y^{(on)}(y) + f_K^{(\delta)}(y)] \rightarrow f_Y^{(on)}(y) = y \int dk_\perp^2 \frac{k_\perp^2 + (M_Y + \Delta)^2}{(1-y)^2 D_{KY}^2} F^{(on)}$$

# Summary

- Produced initial physics deliverables, physics objects, and kinematic plots/coverage
  - Physics deliverables:  $\pi$ /K structure function plots,  $\pi$  form factor plot
  - Physics objects:
    - scattered electron
    - Measure  $\pi$  and tagged neutron ( $\pi$  form factor)
    - Measure "X" and tagged neutron ( $\pi$  structure function)
    - Measure K and tagged  $\Lambda$  (K form factor)
    - Measure "X" and tagged  $\Lambda$  (K structure function)
- Next steps are to...
  - Simulate  $K\Lambda$  and  $K\Sigma$  events
  - Extend  $\pi$  to K structure function and form factor
    - Splitting functions
    - Track photons and neutrons from  $\Lambda$  in the ZDC – EMCAL and ZDC – HCAL
  - Continue far-forward analysis and extend to the 2nd IR (ie IP8)

# Meson structure working group members

Daniele Binosi , Huey-Wen Lin, Timothy Hobbs, Arun Tadepalli, Rachel Montgomery, Paul Reimer, David Richards, Rik Yoshida, Craig Roberts, Garth Huber, Thia Keppel, John Arrington, Lei Chang, Stephen Kay, Ian L. Pegg, Love Preet, Jorge Segovia, Carlos Ayerbe Gayoso, Bill Li, Yulia Furletova, Dmitry Romanov, Markus Diefenthaler, **Richard L. Trotta**, Tanja Horn, Rolf Ent, Tobias Frederico, Ali Usman



**Thank You for Your Time!**

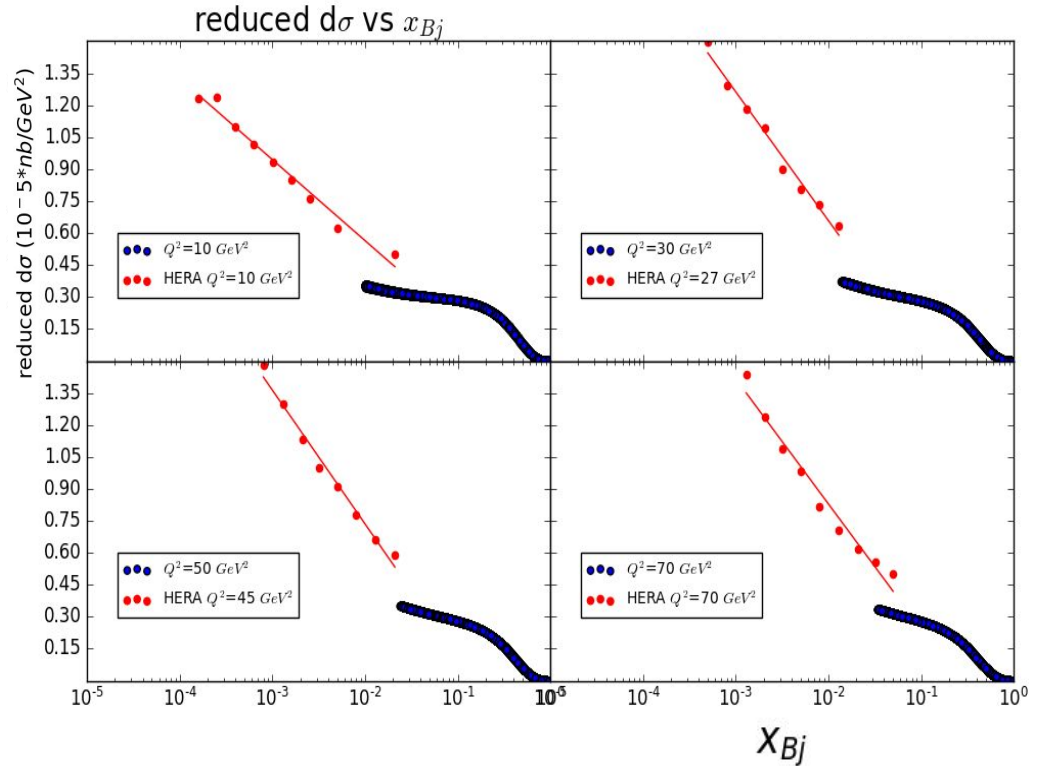


# Extra

# Validation: Reduced cross-section compared with HERA

- HERA data from *ZEUS collab, Eur. Phys. J. C 21 (2001)*  
*DOI:10.1007/s100520100749*
- Proton beam = 100 GeV/c
- Electron beam = 5 GeV/c
- $x_{Bj}=(0.01-1.0)$
- $Q^2=(10-100)$

$$\tilde{\sigma}^{e^+p} = \left[ \frac{2\pi\alpha^2}{xQ^4} Y_+ \right]^{-1} \frac{d^2\sigma_{\text{Born}}^{e^+p}}{dx dQ^2}$$



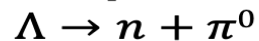
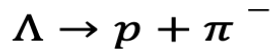
# Geometric particle detection fractions

- For the pion structure function, the final state neutron moves with an energy near that of the initial proton beam
  - The Zero Degree Calorimeter (ZDC) must reconstruct the energy and position well enough to constrain both scattering kinematics and 4-momentum of pion
  - Constraining neutron energy around  $35\%/\sqrt{E}$  will assure an achievable resolution in  $x$
- For the kaon structure function, the decay products of the  $\Lambda$  must be tracked through the very forward spectrometer
  - Distinguishing decay products is crucial

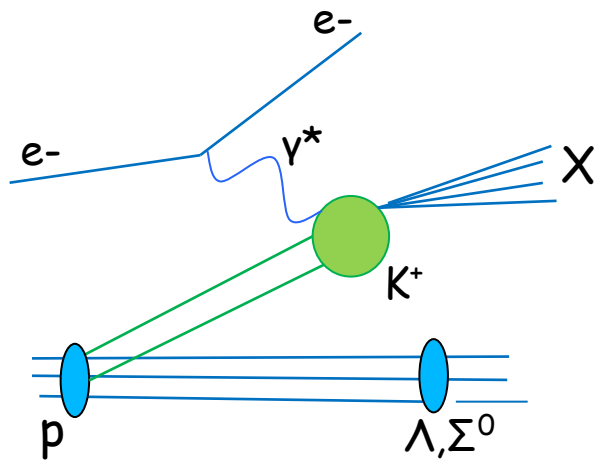
Process	Forward Particle	Geometric Detection Efficiency (at small $-t$ )
${}^1\text{H}(e, e' \pi^+) n$	$n$	$>20\%$
${}^1\text{H}(e, e' K^+) \Lambda$	$\Lambda$	50%
${}^1\text{H}(e, e' K^+) \Sigma$	$\Sigma$	17%

# $K^+$ Structure Functions ( $F_2^K$ )

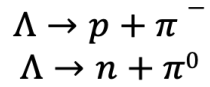
- $\Lambda$  has two primary decay modes...



- Optimizing the detection efficiency of these decay products is critical for kaon studies
- The decay length of  $\Lambda$  is dependent on the initial proton beam energy
  - Proper choice of this beam energy is a must since decay lengths can reach past the forward spectrometer at higher energies



# Lambda Final State

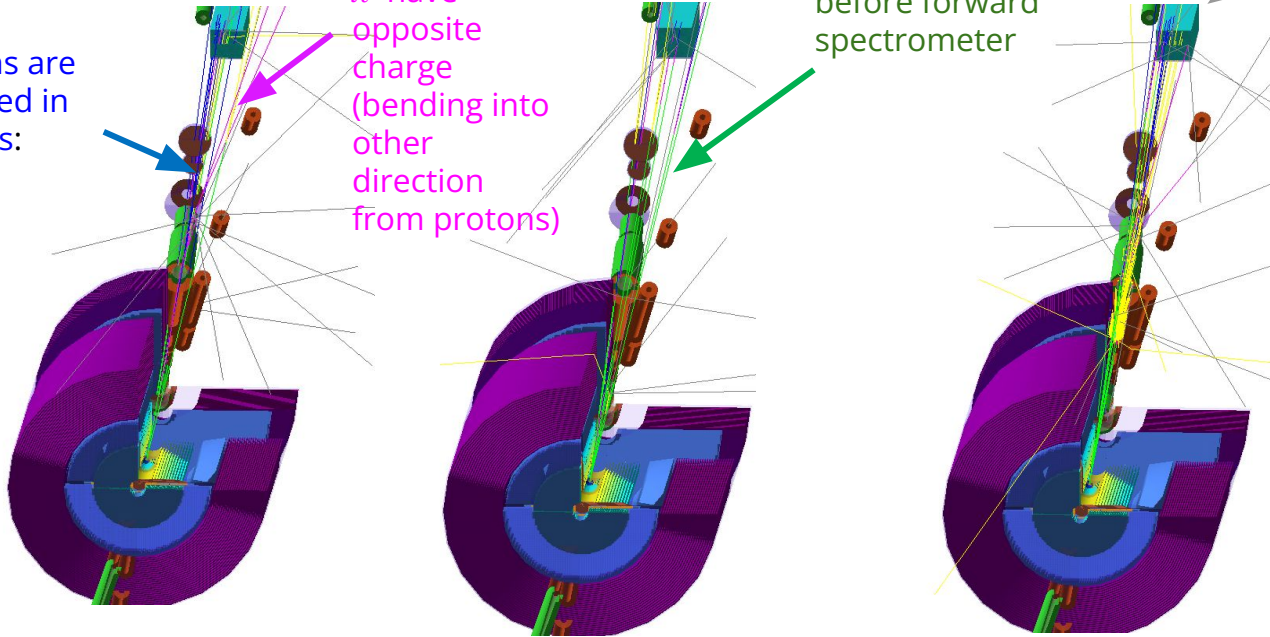


Protons are detected in the RPs:

$\pi^-$  have opposite charge (bending into other direction from protons)

30% of  $\Lambda$  at high energy does not decay before forward spectrometer

Neutrons and a fraction of  $\pi^0$  goes into ZDC



18 x 275

# Decay Length

- There are some advantages for lower proton energy for K- $\Lambda$  detection
- Possible advantage of the second IR

