



中国科学院大学
University of Chinese Academy of Sciences



ICTP-AP
International Centre
for Theoretical Physics Asia-Pacific
国际理论物理中心-亚太地区

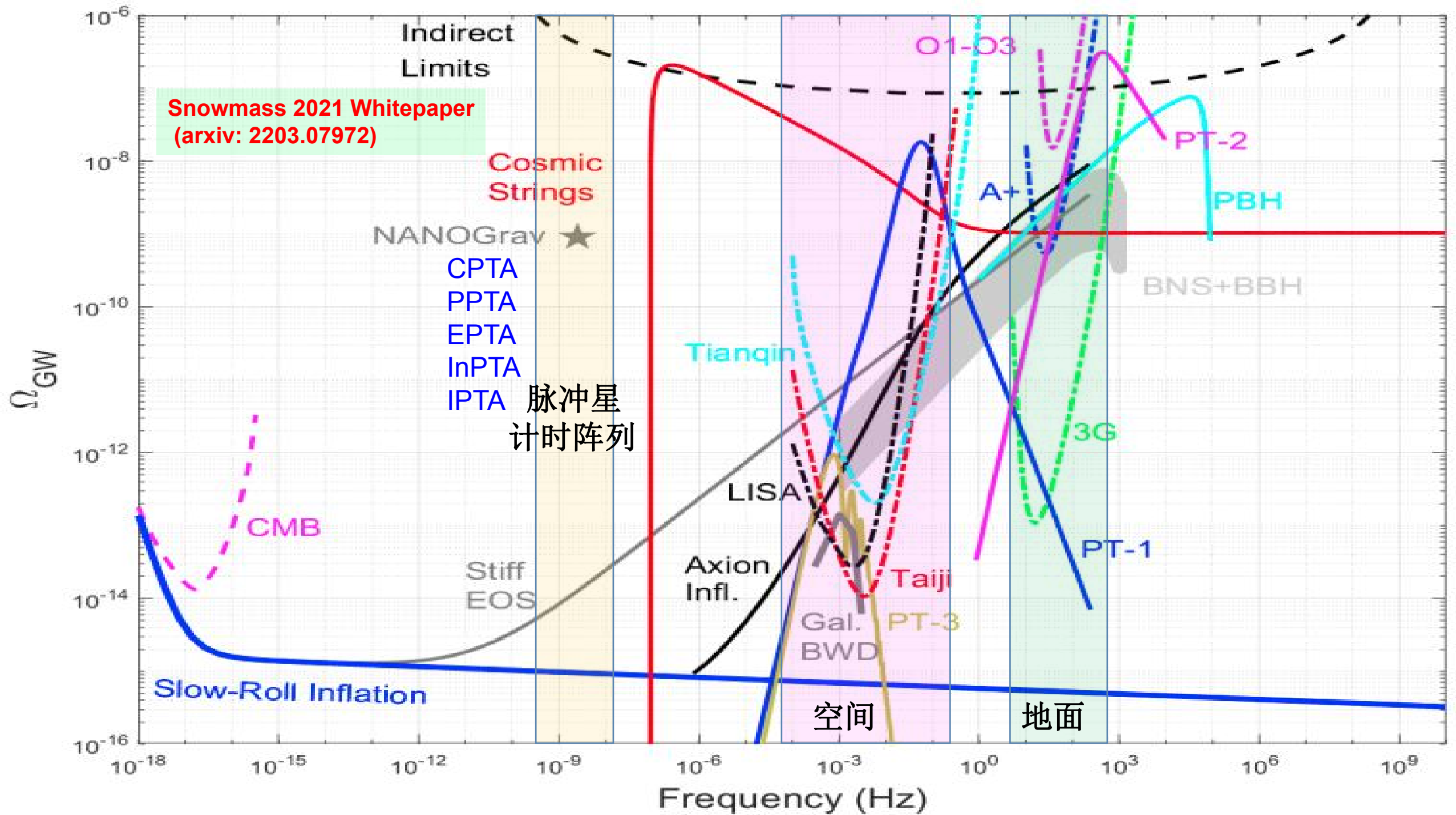
引力波与粒子物理

郭怀珂

UCAS (ICTP-AP)

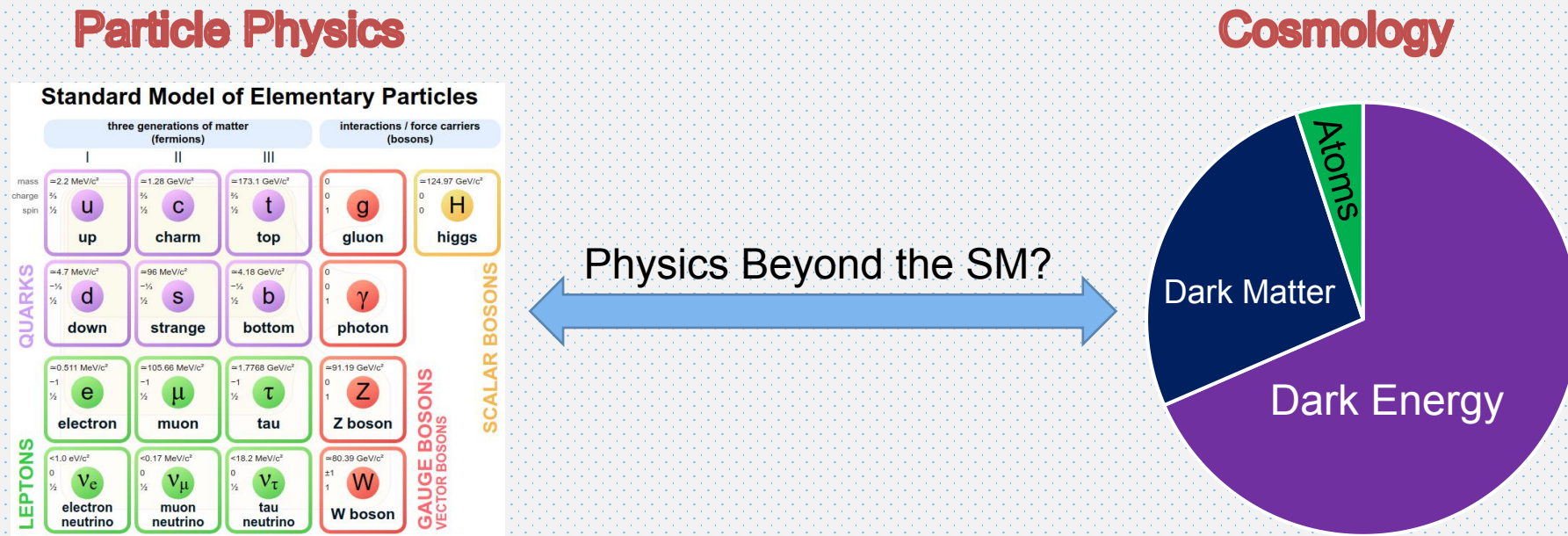
Sept. 26, 2023

第三届“江门中微子实验相关的理论与唯象学”研讨会
大统一专题



New Perspectives?

How can we reconcile the standard models of particle physics and cosmology?



Why more matter than anti-matter (baryogenesis, leptogenesis)? (phase transitions, solitons)

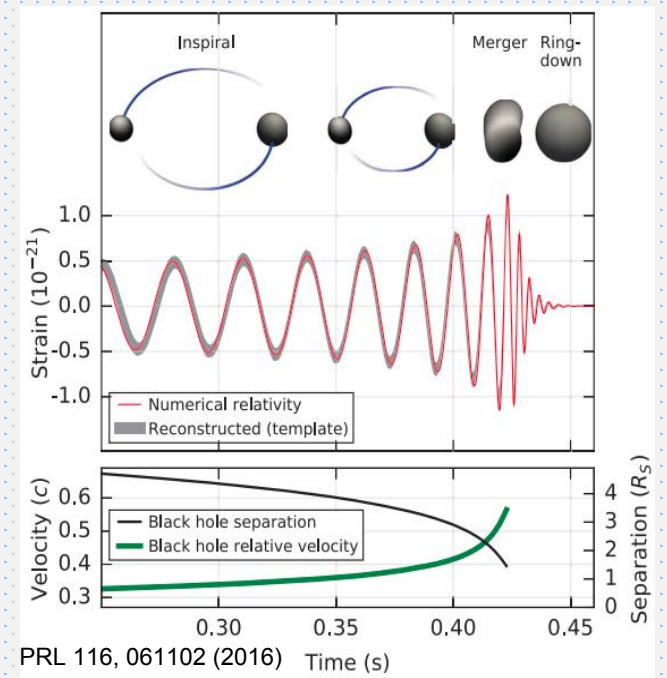
What is dark matter? (solitons, ultralight particles)

GWs from Particles?

GW generation requires **macroscopic mass/energy**

$$\square^2 h_{\mu\nu} = -16\pi G S_{\mu\nu} \rightarrow \text{matter}$$

$$h \sim 10^{-22} \frac{M/M_{\odot}}{r/100\text{Mpc}} \left(\frac{v}{c}\right)^2 \rightarrow \text{huge mass/energy}$$



How to study particle physics with GWs?

GWs from Particles

Here will focus only on a (limited) collection:

Extreme densities

disturbances in the early universe

As Macroscopic Objects

(non-) topological solitons

Environmental Effects

Faking GW signals (dark matter)

Not covered: neutrino damping of GWs, neutron star binary, ...

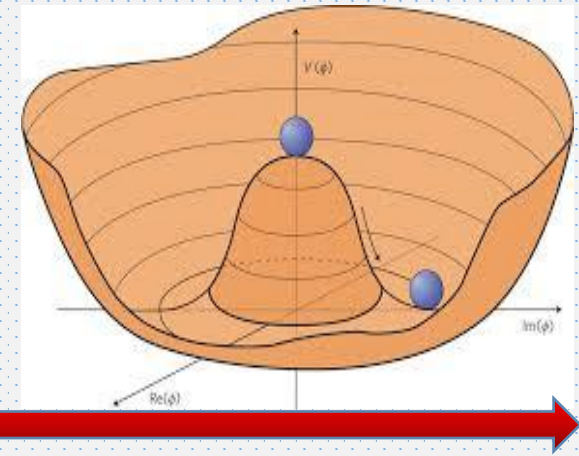
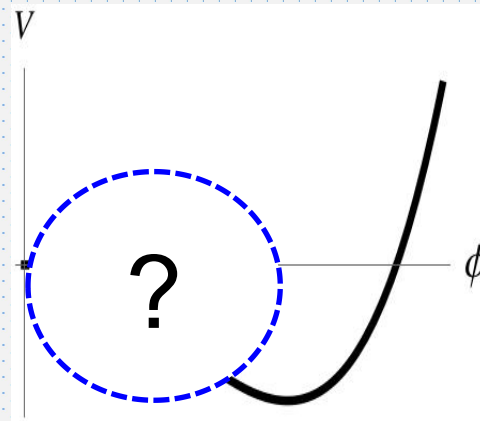
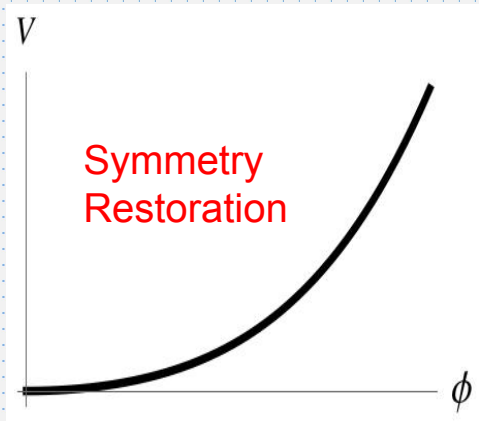
GWs from Particles

Extreme densities ✓
disturbances in the early universe

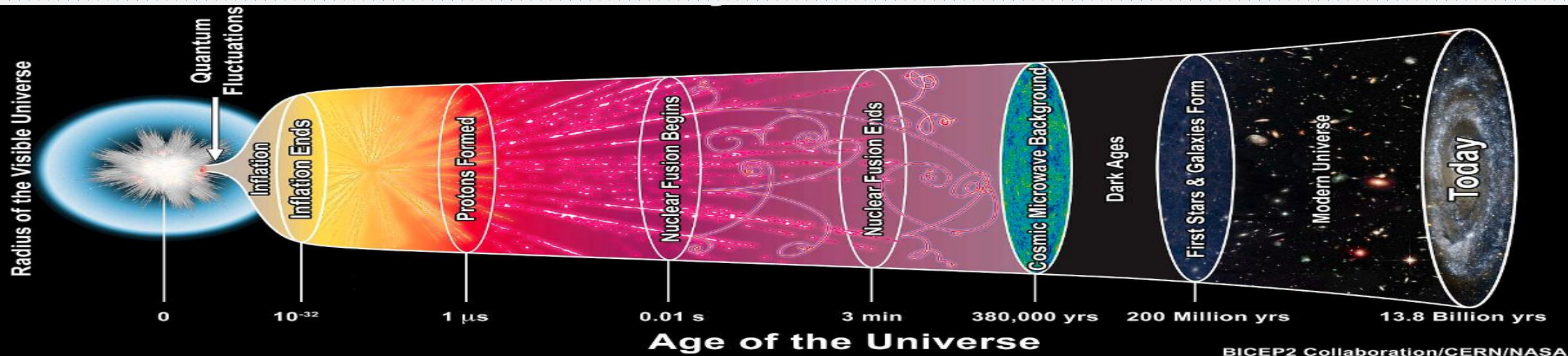
As Macroscopic Objects
(non-) topological solitons

Environmental Effects
Faking GW signals (dark matter)

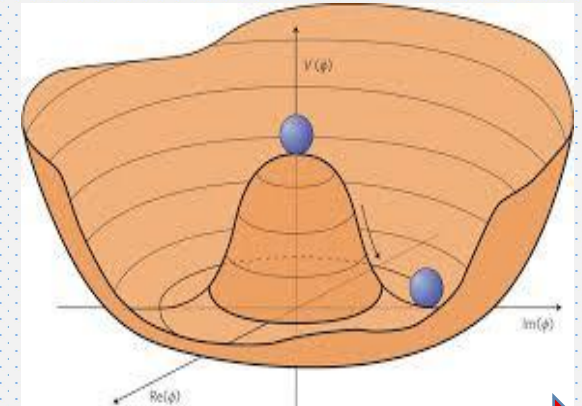
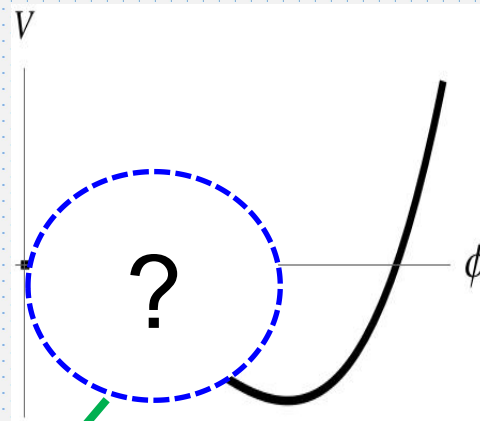
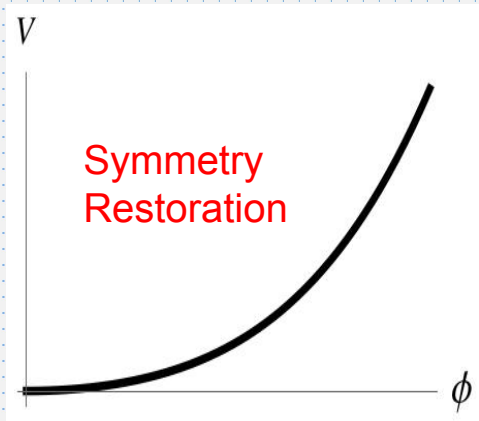
Electroweak Phase Transition



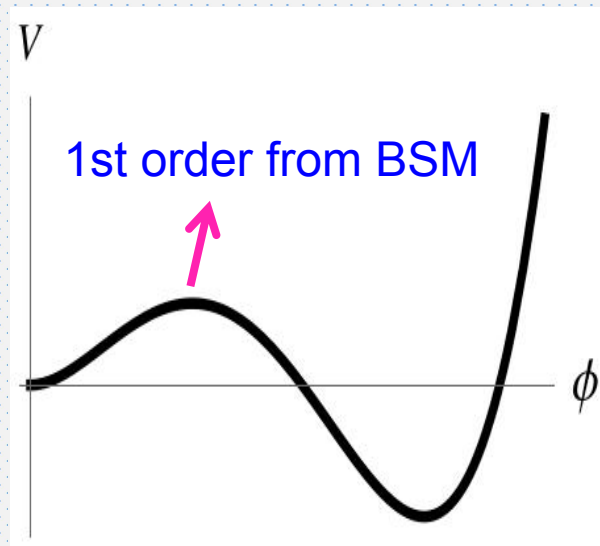
Temperature drops



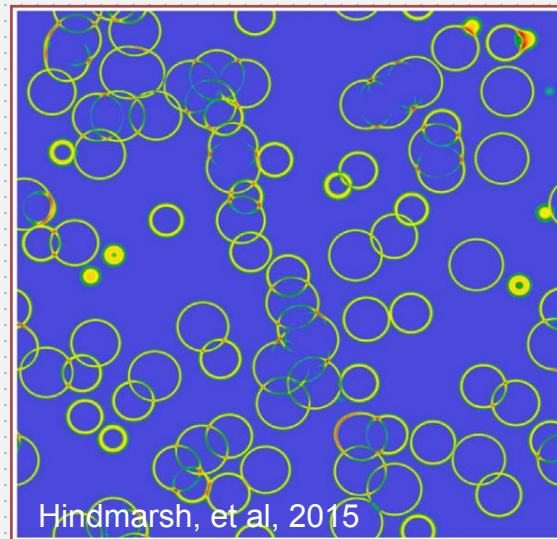
Electroweak Phase Transition



Temperature drops



bubbles, plasma, MHD

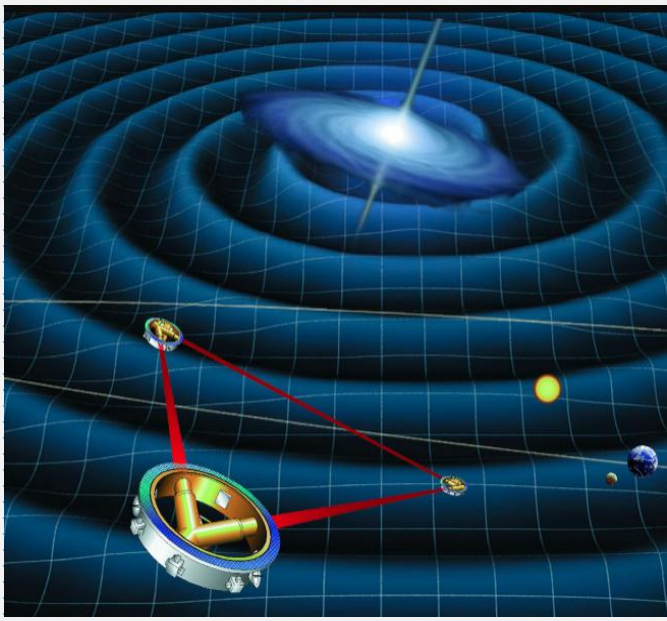


Electroweak Baryogenesis

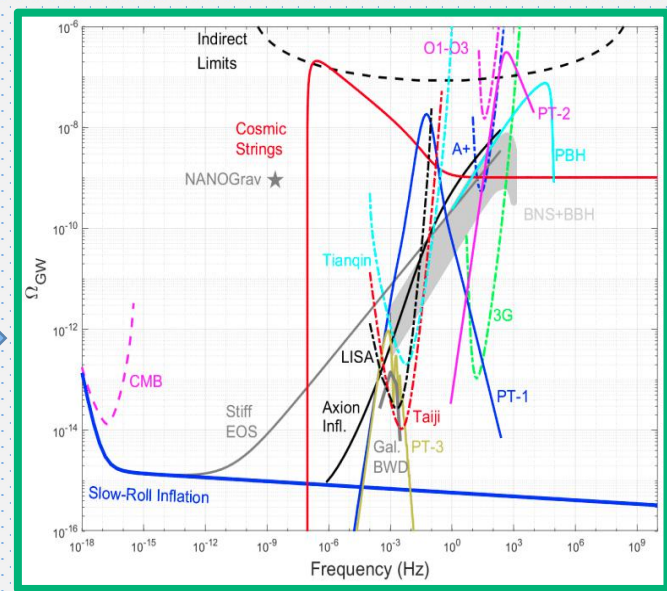
- Modified Higgs potential (Higgs physics, GW)
- Extra CP-violation (EDM, LHC)
- B-violation: Sphaleron process (LHC, GW)

Flow of Studies

theoretical calculation of gravitational wave spectrum and detector simulation



LIGO, LISA, Taiji, Tianqin...



Gravitational Wave Spectrum

α
 β
 v_w
 T_*
 g_s
...

Phase Transition Parameters

Standard Model of Elementary Particles

	three generations of matter (fermions)			interactions / force carriers (bosons)	
	I	II	III		
mass	$\approx 2.2 \text{ MeV}/c^2$	$\approx 1.28 \text{ GeV}/c^2$	$\approx 173.1 \text{ GeV}/c^2$	0	$\approx 124.97 \text{ GeV}/c^2$
charge	$\frac{2}{3}$	$\frac{2}{3}$	$\frac{2}{3}$	0	0
spin	$\frac{1}{2}$	$\frac{1}{2}$	$\frac{1}{2}$	1	0
	u up	c charm	t top	g gluon	H higgs
	d down	s strange	b bottom	γ photon	BSM
	e electron	μ muon	τ tau	Z Z boson	SCALAR BOSONS
	ν_e electron neutrino	ν_μ muon neutrino	ν_τ tau neutrino	W W boson	GAUGE BOSONS VECTOR BOSONS

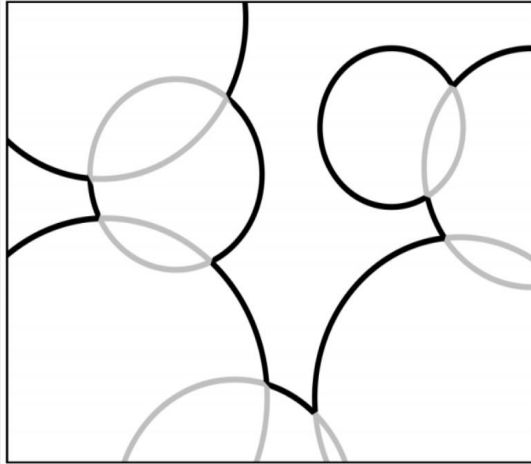
Particle Physics Model



data analysis, constraints or discovery(parameter estimation)

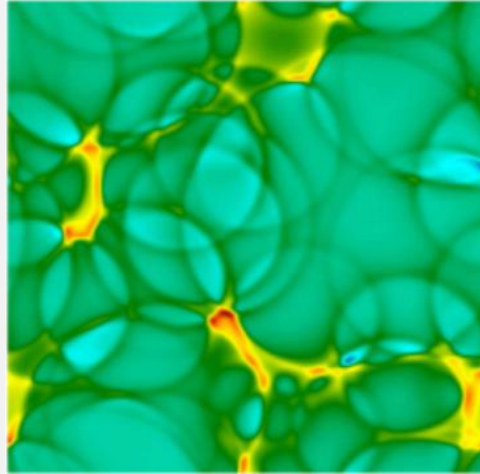
Gravitational Wave Sources

Bubble Collisions



energy concentrated at walls

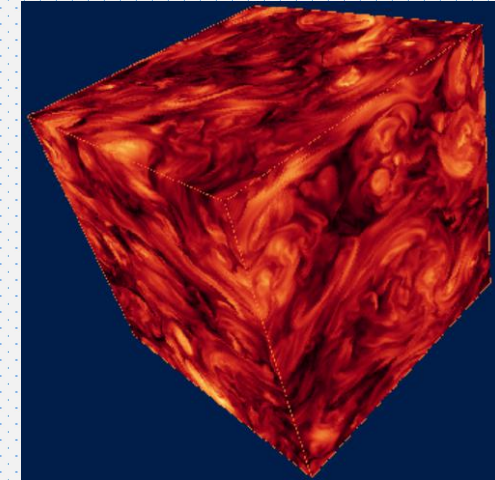
Sound Waves



Hindmarsh, et al, PRL 112, 041301 (2013)

acoustic production

MagnetoHydrodynamic Turbulence



<https://home.mpcdf.mpg.de>

turbulent motion

New observables: primordial magnetic field, scalar perturbations, anisotropy, primordial black hole...

Di, Wang, Zhou, Bian, Cai, Liu, PRL 126 (2021) 25, 251102

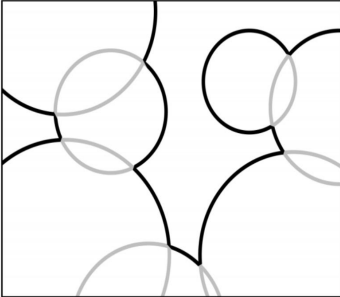
Jing, Bian, Cai, Guo, Wang, PRL 130 (2023) 051001

Li, Huang, Wang, Zhang, PRD 105 (2022) 083527

Huang, Xie, PRD 105 (2022) 11, 115033, JHEP 09 (2022) 052

The GW Observable

bubble collision

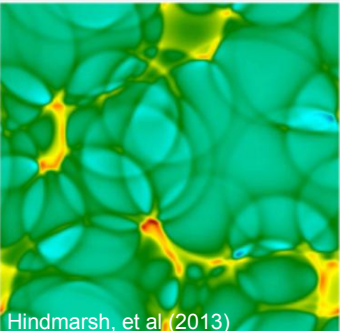


$$\Omega_{\text{coll}}(f)h^2 = 1.67 \times 10^{-5} \Delta \left(\frac{H_{\text{pt}}}{\beta} \right)^2 \left(\frac{\kappa_{\phi} \alpha}{1 + \alpha} \right)^2 \times \left(\frac{100}{g_*} \right)^{1/3} S_{\text{env}}(f),$$

Energy density Spectrum

$$\Omega_{\text{GW}}(f) = \frac{d\rho_{\text{GW}}}{\rho_c d \log f}$$

sound waves



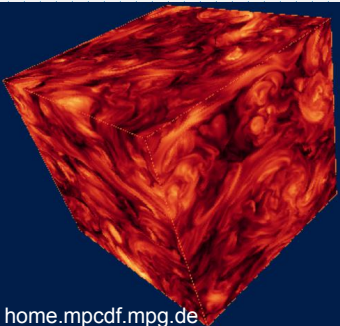
Hindmarsh, et al (2013)

$$\Omega_{\text{sw}}(f)h^2 = 2.65 \times 10^{-6} \left(\frac{H_{\text{pt}}}{\beta} \right) \left(\frac{\kappa_{\text{sw}} \alpha}{1 + \alpha} \right)^2 \left(\frac{100}{g_*} \right)^{1/3} \times v_w \left(\frac{f}{f_{\text{sw}}} \right)^3 \left(\frac{7}{4 + 3(f/f_{\text{sw}})^2} \right)^{7/2} \Upsilon(\tau_{\text{sw}}),$$

$$\Upsilon = 1 - (1 + 2\tau_{\text{sw}} H_{\text{pt}})^{-1/2} \quad (\text{RD})$$

HG, Sinha, Vagie, White, JCAP 01 (2021) 001

MHD

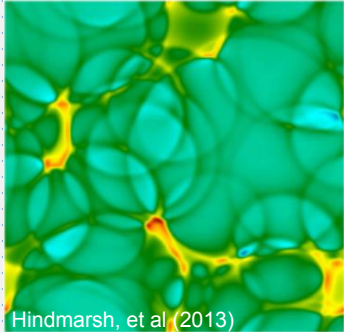


home.mpcdf.mpg.de

$$h^2 \Omega_{\text{turb}}(f) = 3.35 \times 10^{-4} \left(\frac{H_*}{\beta} \right) \left(\frac{\kappa_{\text{turb}} \alpha}{1 + \alpha} \right)^{\frac{3}{2}} \left(\frac{100}{g_*} \right)^{1/3} v_w S_{\text{turb}}(f)$$

Sound Waves

sound waves



Hindmarsh, et al (2013)

$$\Omega_{\text{sw}}(f)h^2 = 2.65 \times 10^{-6} \left(\frac{H_{\text{pt}}}{\beta}\right) \left(\frac{\kappa_{\text{sw}}\alpha}{1+\alpha}\right)^2 \left(\frac{100}{g_*}\right)^{1/3} \times v_w \left(\frac{f}{f_{\text{sw}}}\right)^3 \left(\frac{7}{4+3(f/f_{\text{sw}})^2}\right)^{7/2} \Upsilon(\tau_{\text{sw}})$$

Chiara Caprini et al JCAP04(2016)001

$$\Upsilon = 1 - (1 + 2\tau_{\text{sw}}H_{\text{pt}})^{-1/2} \quad (\text{RD})$$

HG, Sinha, Vagie, White, JCAP 01 (2021) 001

PHYSICAL REVIEW LETTERS 127, 251302 (2021)

Editors' Suggestion

Featured in Physics

Searching for Gravitational Waves from Cosmological Phase Transitions with the NANOGrav 12.5-Year Dataset

Zaven Arzoumanian,¹ Paul T. Baker,² Harsha Blumer,^{3,4} Bence Bécsy,⁵ Adam Brazier,^{6,7} Paul R. Brook,^{3,4} Sarah Burke-Spolaor,^{3,4,8} Maria Charisi,⁹ Shami Chatterjee,⁶ Siyuan Chen,^{10,11,12} James M. Cordes,⁶ Neil J. Cornish,⁵ Fronefield Crawford,¹³ H. Thankful Cromartie,⁶ Megan E. DeCesar,^{14,15*} Paul B. Demorest,¹⁶ Timothy Dolch,^{17,18} Justin A. Ellis,¹⁹ Elizabeth C. Ferrara,^{20,21,22} William Fiore,^{3,4} Emmanuel Fonseca,²³ Nathan Garver-Daniels,^{3,4} Peter A. Gentile,^{3,4} Deborah C. Good,²⁴ Jeffrey S. Hazboun,²⁵ A. Miguel Holgado,^{26,27} Kristina Iso,²⁸ Ross J. Jennings,⁶ Megan L. Jones,²⁸ Michael T. Larson,³⁴ Dustin R. Malmgren,³⁴ David J. Nice,¹⁴ Xavier Siemens,³⁰ Jerry P. Sun,³⁰ Nima Laal,³⁰ Yan S. Lynch,³⁶ Cherry Ng,³⁹ Shaphiro-Albert,^{3,4} Kevin Stovall,¹⁶ Leah J. Vigeland,²⁸

considered in this work. Because of the finite lifetime [54,55] of the sound waves, to derive Ω_{sw} Eq. (4) needs to be multiplied by a suppression factor $\Upsilon(\tau_{\text{sw}})$ given by [54]

$$\Upsilon(\tau_{\text{sw}}) = 1 - (1 + 2\tau_{\text{sw}}H_*)^{-1/2} \quad (6)$$

(NANOGrav Collaboration)

THE ASTROPHYSICAL JOURNAL LETTERS, 951:L11 (56pp), 2023 July 1

<https://doi.org/10.3847/2041-8213/acde91>

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The NANOGrav 15 yr Data Set: Search for Signals from New Physics

Adeela Afzal,^{1,2} Gabriella Agazie,³ Akash Anumarlapudi,³ Anne M. Archibald,⁴ Zaven Arzoumanian,⁵ Paul T. Baker,⁶ Bence Bécsy,⁷ Jose Juan Blanco-Pillado,^{8,9,10} Laura Blecha,¹¹ Kimberly K. Boddy,¹² Adam Brazier,^{13,14} Paul R. Brook,¹⁵ Sarah Burke-Spolaor,^{16,17} Rand Burnette,⁷ Robin Case,⁷ Maria Charisi,¹⁸ Shami Chatterjee,¹³ Katerina Chatziioannou,¹⁹ Belinda D. Cheeseboro,^{16,17} Siyuan Chen,²⁰ Tyler Cohen,²¹ James M. Cordes,¹³ Neil J. Cornish,²² Fronefield Crawford,²³ H. Thankful Cromartie,^{13,77} Kathryn Crowter,²⁴ Curt J. Cutler,^{19,25} Megan E. DeCesar,²⁶ Dallas DeGan,⁷ Paul B. Demorest,²⁷ Heling Deng,⁷ Timothy Dolch,^{28,29} Brendan Drachler,^{30,31} Richard von Eckardstein,¹ Elizabeth C. Ferrara,^{32,33,34} William Fiore,^{16,17} Emmanuel Fonseca,^{16,17} Gabriel E. Freedman,³ Nate Garver-Daniels,^{16,17} Peter A. Gentile,^{16,17} Kyle A. Gersbach,¹⁸ Joseph Glaser,^{16,17} Deborah C. Good,^{35,36} Lydia Guertin,³⁷ Kayhan Gültekin,³⁸ Jeffrey S. Hazboun,⁷ Sophie Hourihane,¹⁹ Kristina Iso,³ Ross J. Jennings,^{16,17,78} Aaron D. Johnson,^{3,19} Megan L. Jones,³ Andrew R. Kaiser,^{16,17} David L. Kaplan,³ Luke Zoltan Kelley,³⁹ Matthew Kerr,⁴⁰ Joey S. Key,⁴¹ Nima Laal,⁷ Michael T. Lam,^{30,31} William G. Lamb,¹⁸ T. Joseph W. Lazio,²⁵ Vincent S. H. Lee,¹⁹ Natalia Lewandowska,⁴² Rafael R. Lino dos Santos,^{1,43} Tyson B. Littenberg,⁴⁴ Tingting Liu,^{16,17} Alexander McEwen,⁴⁵ Patrick M. Meyers,⁴⁶ Cherry Ng,⁵⁶ Polina Petrov,¹⁸ Shashwat C. Levi Schult,¹⁸ Ingrid H. Stairs,²⁴ Joseph K. Swiggum,⁴⁷ Michele Va

time of matter–radiation equality. The production of GWs from sound waves stops after a period τ_{sw} , when the plasma motion turns turbulent (Ellis et al. 2019a, 2019b, 2020; Guo et al. 2021). In Equation (34), this effect is taken into account by the suppression factor

$$\Upsilon(\tau_{\text{sw}}) = 1 - (1 + 2\tau_{\text{sw}}H_*)^{-1/2}, \quad (36)$$

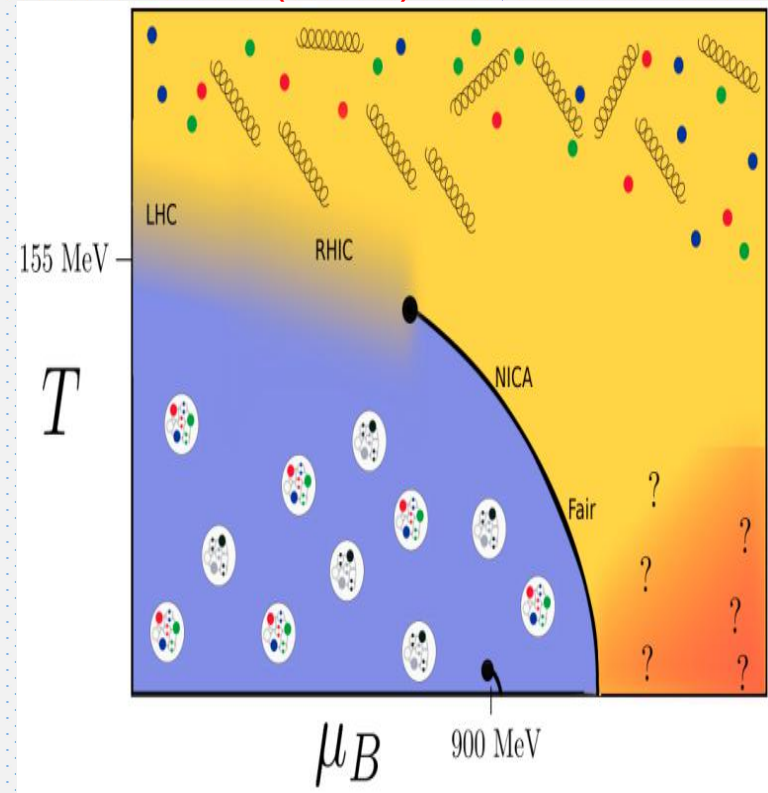
Caitlin A. Witt, David Wright, Onvia Young, Kathryn M. Zurek, and The NANOGrav Collaboration

Generic Features

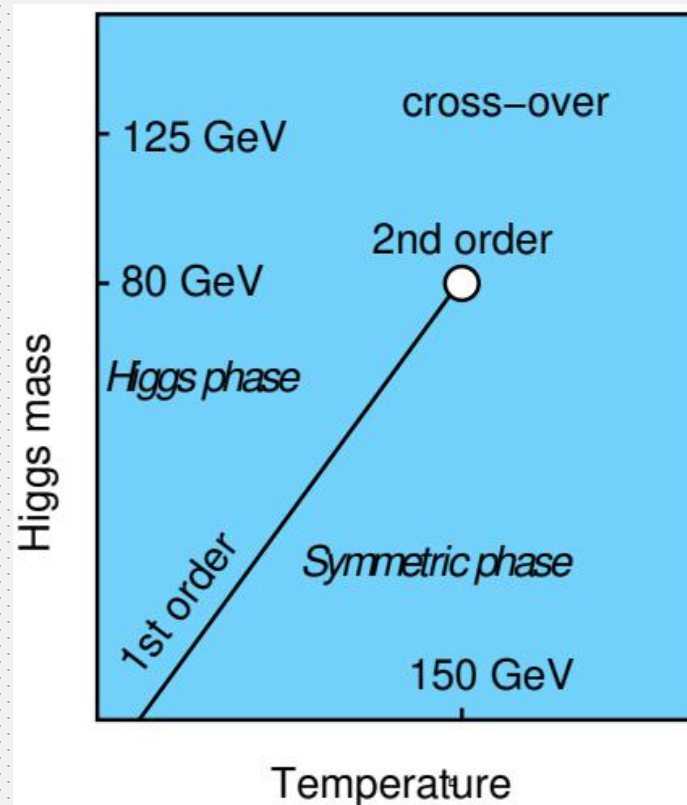
- LIGO (~100Hz) : (~PeV - EeV)
- LISA, Taiji, Tianqin: ~mHz : (~100GeV)
- PTA: nHz (~100MeV)

QCD (scale) PT ↓

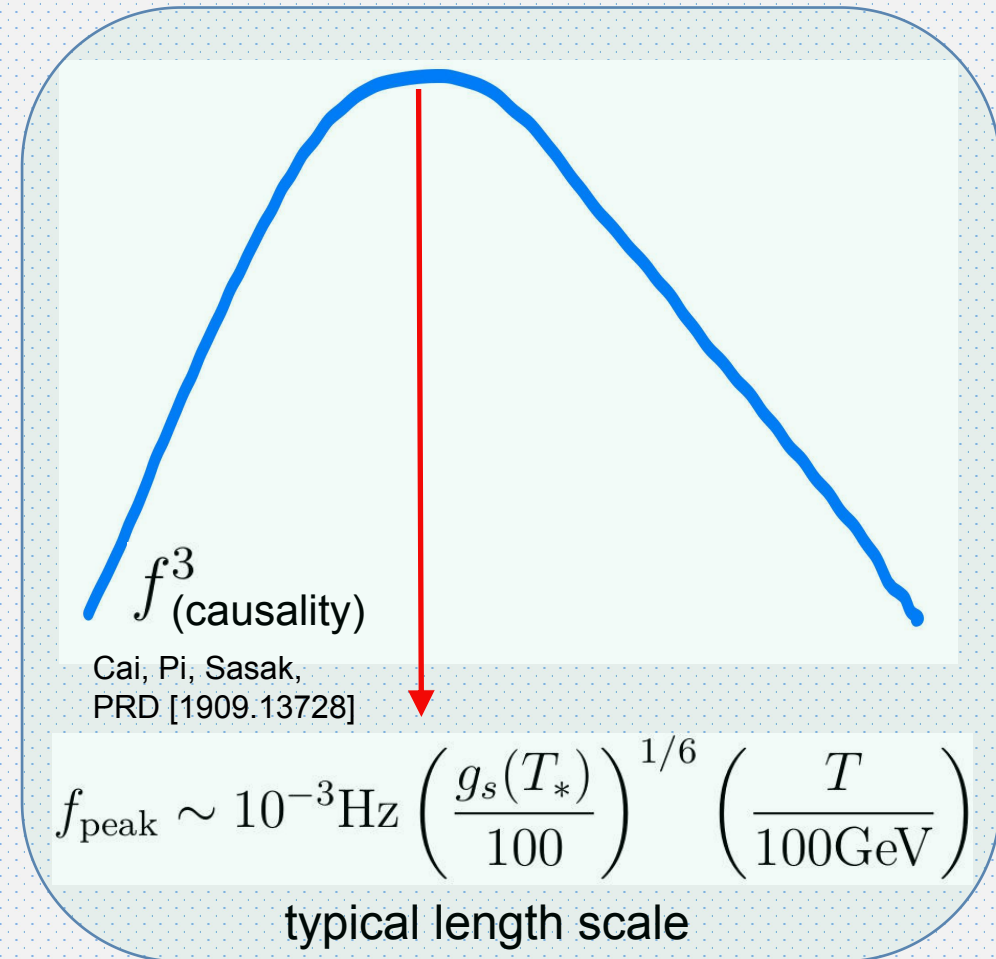
EWPT



Guenther [2010.15503]



Hindmarsh et al SciPost Phys.Lect.Notes [2008.09136]



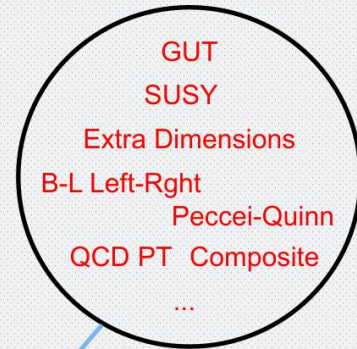
tells PT temperature
(symmetry breaking scale)

BSM studies

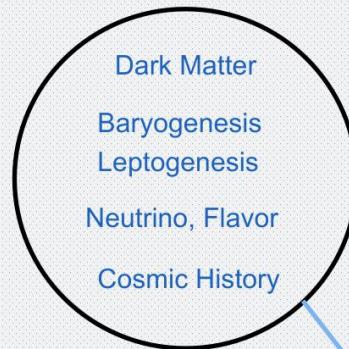
Chung, Long, Wang, PRD [1209.1819]

- Large cubic term from thermal corrections (loop level)
- Add new scalars (tree level)
- Including non-renormalizable operators

More general EFT approach: Cai, Hashino, Wang, Yu [2202.08295]



Classification according to the symmetries



Classification according to the problems



Models	Strong 1 st order phase transition	GW signal	Cold DM	Dark Radiation and small scale structure
SM charged				
Triplet [20–22]	✓	✓	✓	✗
complex and real Triplet [23] (Georgi-Machacek model)	✓	✓	✓	✗
Multiplet [24]	✓	✓	✓	
2HDM [25–30]	✓	✓		✗
MLRSM [31]	✓	✓	✗	✗
NMSSM [32–36]	✓	✓	✓	✗
SM uncharged				
S_ν (xSM) [37–49]	✓	✓	✗	✗
2 S_ν 's [50]	✓	✓	✓	✗
S_c (cxSM) [49, 51–54]	✓	✓	✓	✗
$U(1)_D$ (no interaction with SM) [55]	✓	✓	✓	✗
$U(1)_D$ (Higgs Portal) [56]	✓	✓	✓	
$U(1)_D$ (Kinetic Mixing) [57]	✓	✓	✓	
Composite $SU(7)/SU(6)$ [58]	✓	✓	✓	
$U(1)_L$ [59]	✓	✓	✓	✗
$SU(2)_D \rightarrow$ global $SO(3)$ by a doublet [60–62]			✓	✗
$SU(2)_D \rightarrow U(1)_D$ by a triplet [63–65]			✓	✓
$SU(2)_D \rightarrow Z_2$ by two triplets [66]			✓	✗
$SU(2)_D \rightarrow Z_3$ by a quadruplet [67, 68]			✓	✗
$SU(2)_D \times U(1)_{B-L} \rightarrow Z_2 \times Z_2$ by a quintuplet and a S_c [69]			✓	✗
$SU(2)_D$ with two dark Higgs doublets [70]	✓	✓	✗	✗
$SU(3)_D \rightarrow Z_2 \times Z_2$ by two triplets [62, 71]			✓	✗
$SU(3)_D$ (dark QCD) (Higgs Portal) [72, 73]	✓	✓	✓	
$G_{SM} \times G_{D,SM} \times Z_2$ [74]	✓	✓	✓	
$G_{SM} \times G_{D,SM} \times G_{D,SM} \dots$ [75]	✓	✓	✓	
Current work				
$SU(2)_D \rightarrow U(1)_D$ (see the text)	✓	✓	✓	✓

Ghosh, HG, Han, Liu, JHEP [2012.09758]

Collider and Gravitational Wave Complementarity

- Collider and GW work towards a common goal
- Correlation and complementarity in their roles

Detection of early-universe gravitational-wave signatures and fundamental physics

[Robert Caldwell](#), [Yanou Cui](#), [Huai-Ke Guo](#) , [Vuk Mandic](#), [Alberto Mariotti](#), [Jose Miguel No](#), [Michael J. Ramsey-Musolf](#), [Mairi Sakellariadou](#) , [Kuver Sinha](#), [Lian-Tao Wang](#), [Graham White](#), [Yue Zhao](#), [Haipeng An](#), [Ligong Bian](#), [Chiara Caprini](#), [Sebastien Clesse](#), [James M. Cline](#), [Giulia Cusin](#), [Bartosz Fornal](#), [Ryusuke Jinno](#), [Benoit Laurent](#), [Noam Levi](#), [Kun-Feng Lyu](#), [Mario Martinez](#), [Andrew L. Miller](#), [Diego Redigolo](#), [Claudia Scarlata](#), [Alexander Sevrin](#), [Barmak Shams Es Haghi](#), [Jing Shu](#), [Xavier Siemens](#), [Danièle A. Steer](#), [Raman Sundrum](#), [Carlos Tamarit](#), [David J. Weir](#), [Ke-Pan Xie](#), [Feng-Wei Yang](#) & [Siyi Zhou](#) — Show fewer authors

General Relativity and Gravitation **54**, Article number: 156 (2022) | [Cite this article](#)

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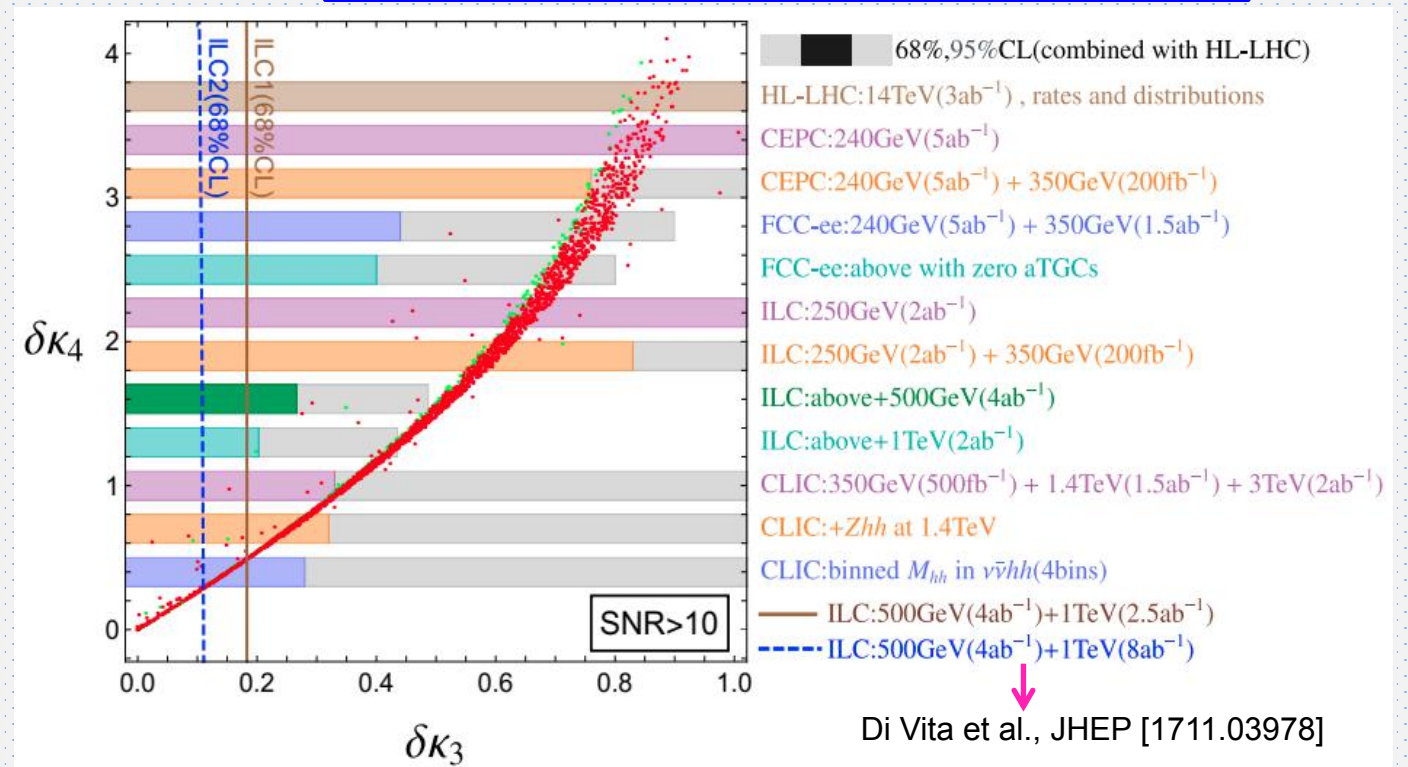
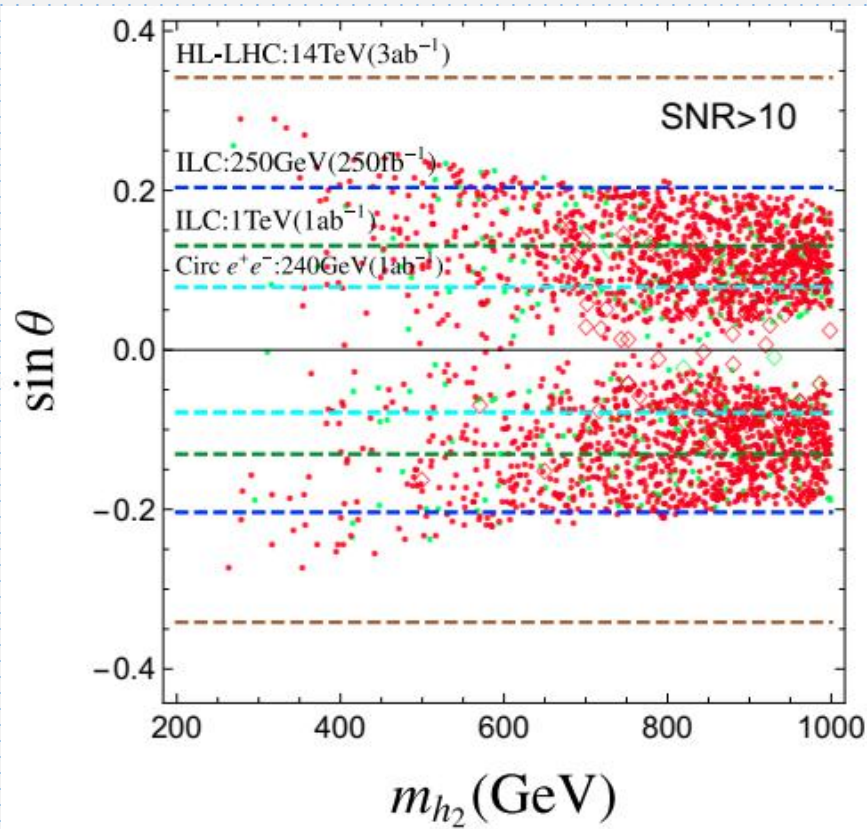
Session leads: Michael Ramsey-Musolf and Lian-Tao Wang

Higgs Precision Measurements

- First order EWPT achievable in simplest **SM+Singlet** model
- **Correlation** and **complementarity** between collider and GW probes

h1: the Higgs
h2: heavier scalar

$$\Delta\mathcal{L} = -\frac{1}{2} \frac{m_{h_1}^2}{v} (1 + \delta\kappa_3) h_1^3 - \frac{1}{8} \frac{m_{h_1}^2}{v^2} (1 + \delta\kappa_4) h_1^4$$

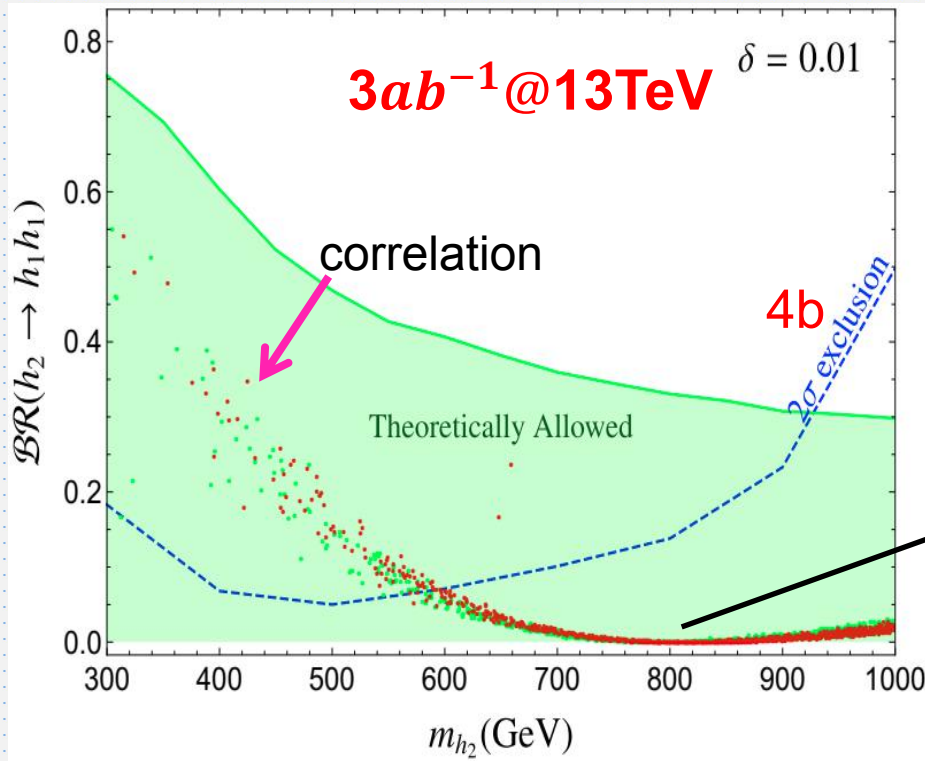
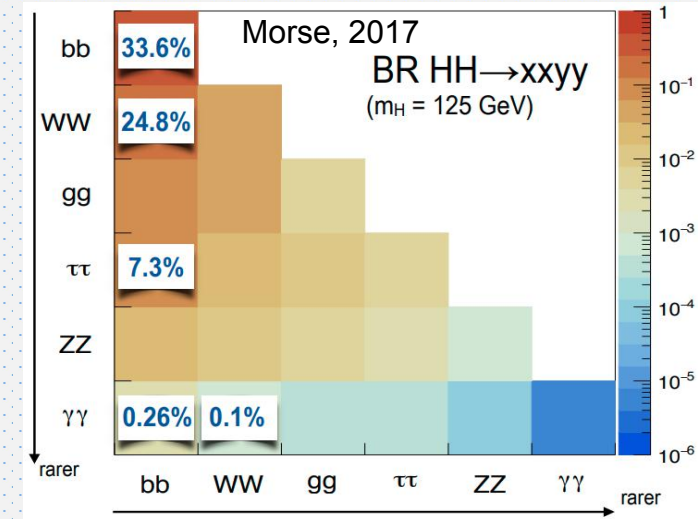
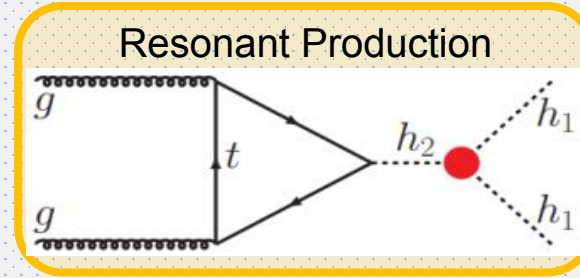


Di-Higgs Production

- Enhanced (resonant) di-Higgs production

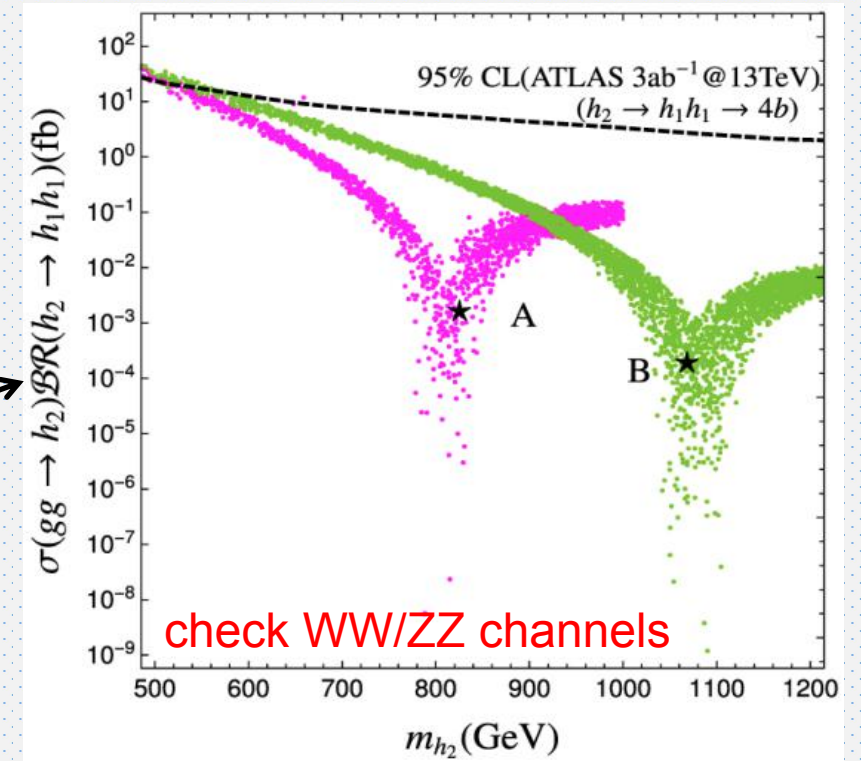
See also:

- No,Ramsey-Musolf, PRD [1310.6035]
- Li,Ramsey-Musolf,Willocq, JHEP [1906.05289]
- Huang,No,Pernie,Ramsey-Musolf,Safonov, PRD [1701.04442]
- Zhang,Li,Liu,Ramsey-Musolf,Zeng,Arunasalam [2303.03612]
- Liu,Xie,JHEP [2101.10469]
- and more...



Alves,Gonçaves,Ghosh,HG,Sinha, JHEP [1909.05268]

di-Higgs "blindspot"
complementarity



Alves,Gonçaves,Ghosh,HG,Sinha, PLB [2007.15654]

Detection at Space-based Detectors

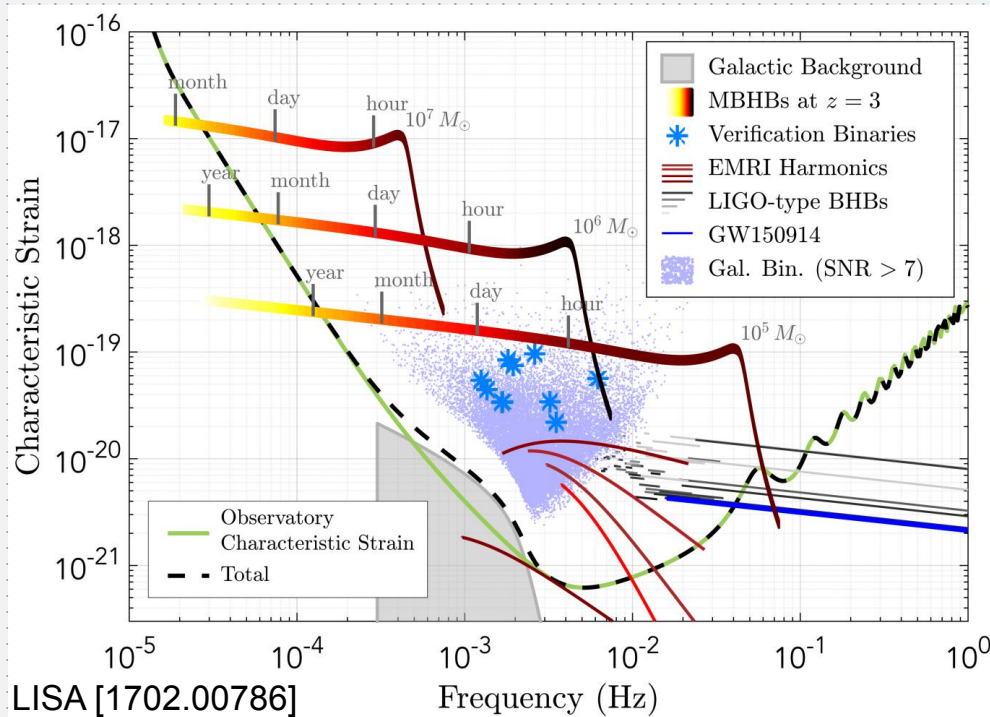
Detection with a single detector

- Complicated, and correlated noise
- Complications from time-delay interferometry
- Solution: null channel method, or with a network

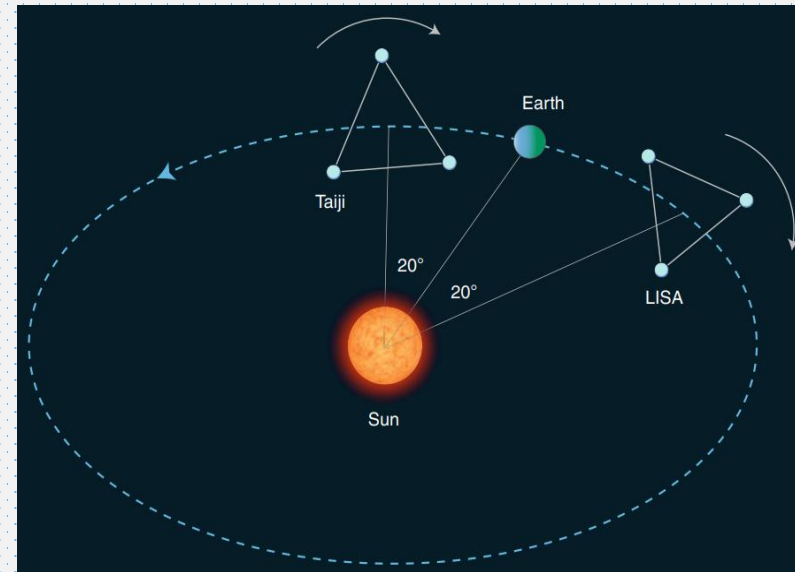
galactic foreground + astro background + cosmic background

SGWB detectable down to $\Omega_{GW} \sim \mathcal{O}(10^{-13})$

Boileau et al, MNRAS [2105.04283]



The LISA–Taiji network



Ruan, Liu, Guo, Wu, Cai, Nature Astron [2002.03603]

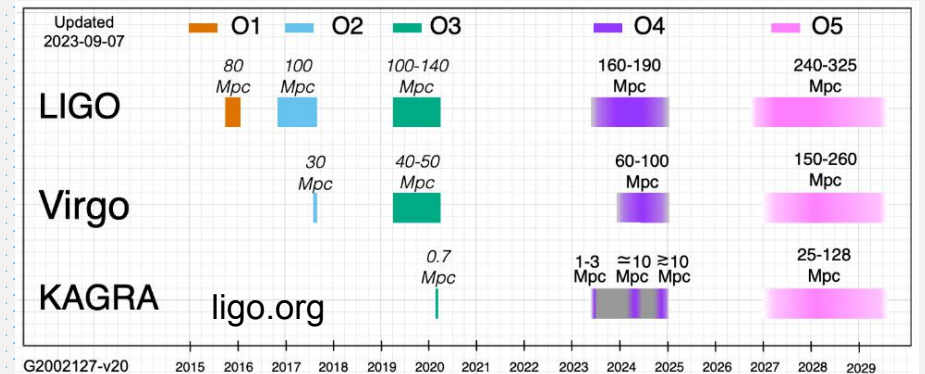
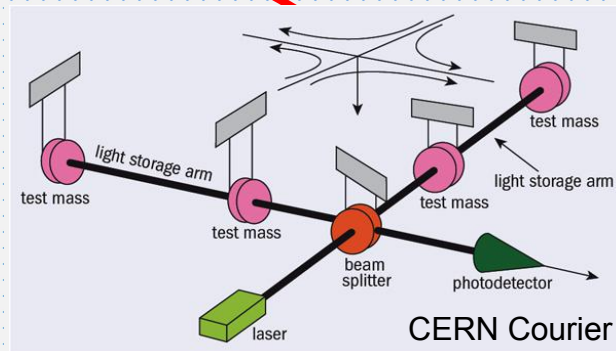
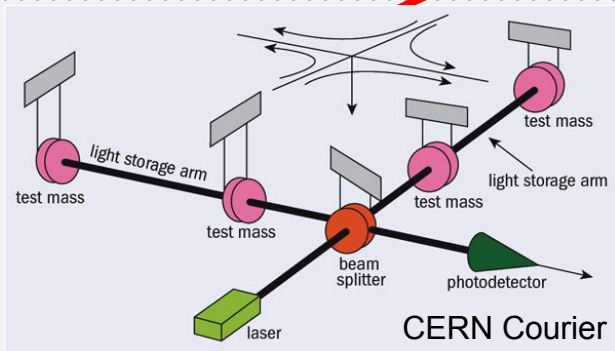
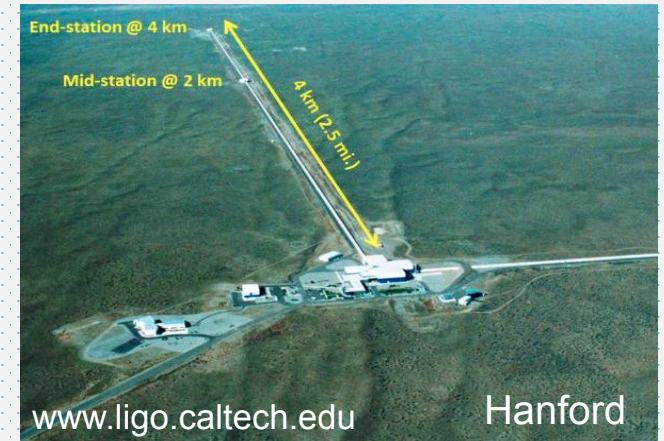
Cai et al [2305.04551]

Detection at LIGO

Using multiple interferometers (cross-correlation)

- So far, no discovery
- Constraints set on power laws, and relevant sources (PT etc)

LVK, PRD [2101.12130]



LIGO Search Result

O1+O2+O3@LIGO (H1, L1), Virgo

- No Evidence for Broken Power Law Signal
- No Evidence for Bubble Collision Domination Signal
- No Evidence for Sound Waves Domination Signal

Broken Power Law

95% CL UL (CBC+BPL)

$$\Omega_{\text{ref}} = 6.1 \times 10^{-9}$$

$$\Omega_* = 5.6 \times 10^{-7}$$

$$\Omega_{\text{BPL}}(25 \text{ Hz}) = 4.4 \times 10^{-9}$$

Bubble Collision

95% CL UL with fixed T_{pt} and β/H_{pt}

Phenomenological model (bubble collisions)

$\Omega_{\text{coll}}^{95\%}(25 \text{ Hz})$

$\beta/H_{\text{pt}} \backslash T_{\text{pt}}$	10^7 GeV	10^8 GeV	10^9 GeV	10^{10} GeV
0.1	9.2×10^{-9}	8.8×10^{-9}	1.0×10^{-8}	7.2×10^{-9}
1	1.0×10^{-8}	8.4×10^{-9}	5.0×10^{-9}	...
10	4.0×10^{-9}	6.3×10^{-9}

no sensitivity

Sound Waves

95% CL UL

$$\Omega_{\text{sw}}(25 \text{ Hz}) = 5.9 \times 10^{-9}$$

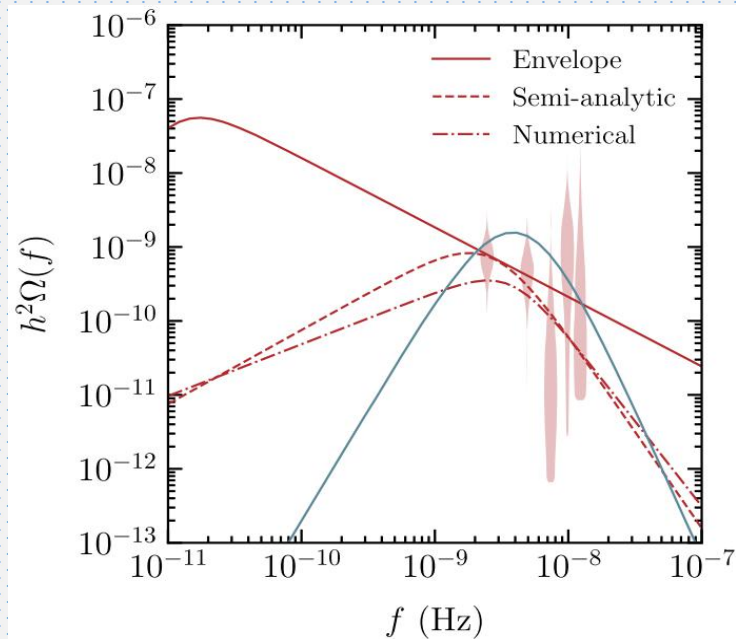
$$\beta/H_{\text{pt}} < 1 \text{ and } T_{\text{pt}} > 10^8 \text{ GeV}$$

Jiang, Huang, JCAP [2203.11781]

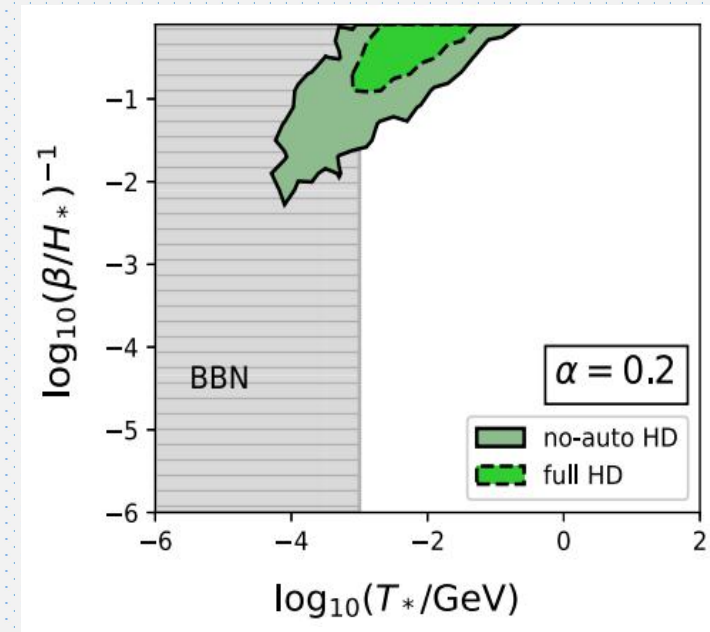
Yu, Wang, PRD [2211.13111]

PTA

- No evidence for GW, constraints set

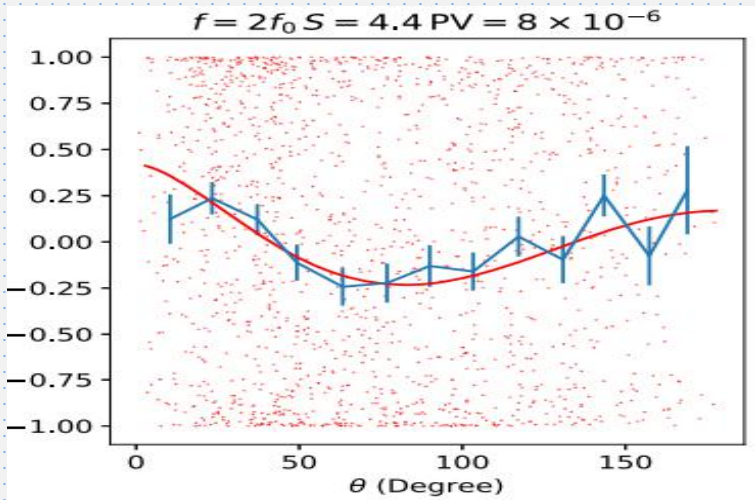


NANOGrav, PRL [2104.13930]

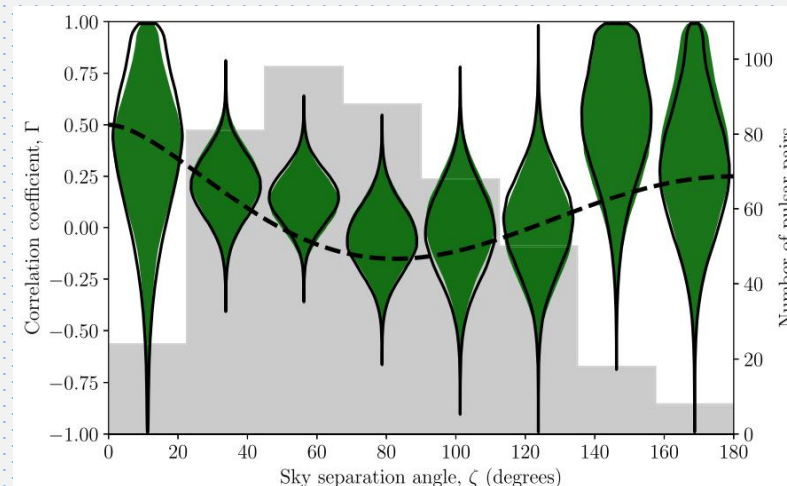


PPTA, Xue, et al, PRL [2110.03096]

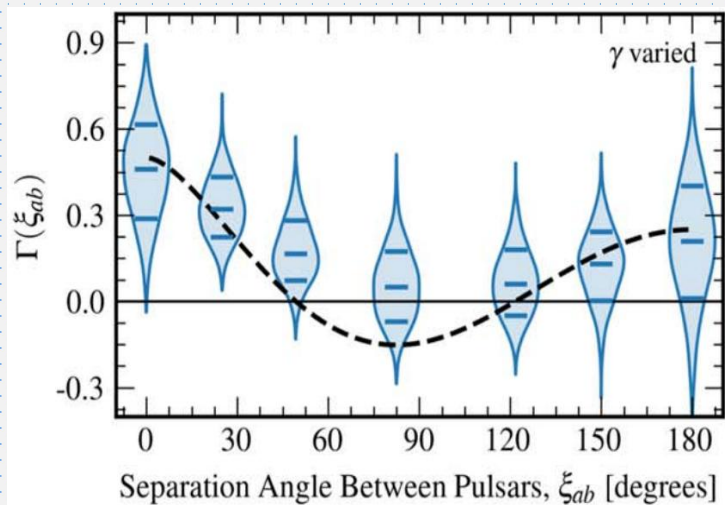
PTA: New Results with Evidence for GW



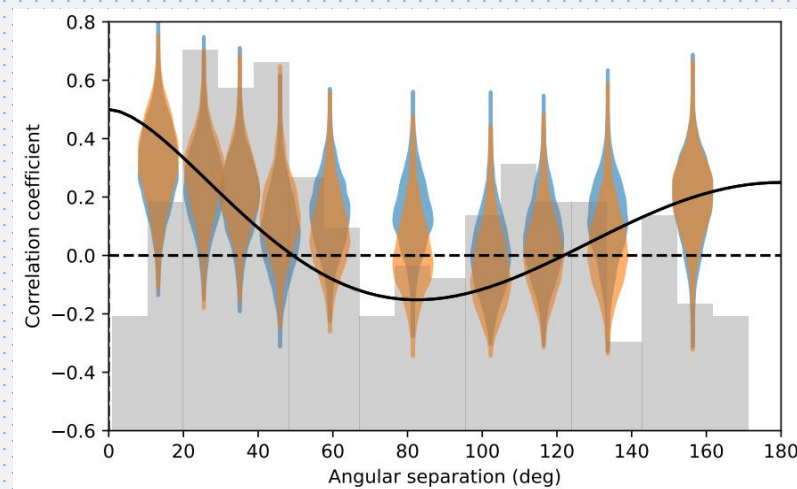
CPTA, RAA, [2306.16216]



PPTA, ApJL [2306.16215]



NANOGrav, ApJL [2306.16213]

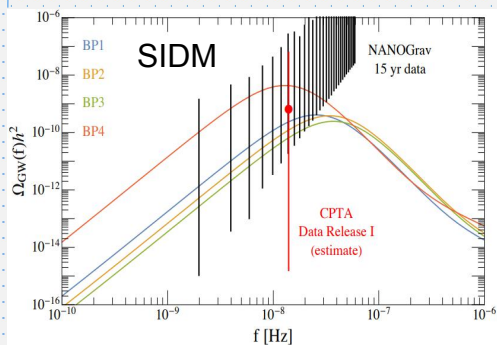
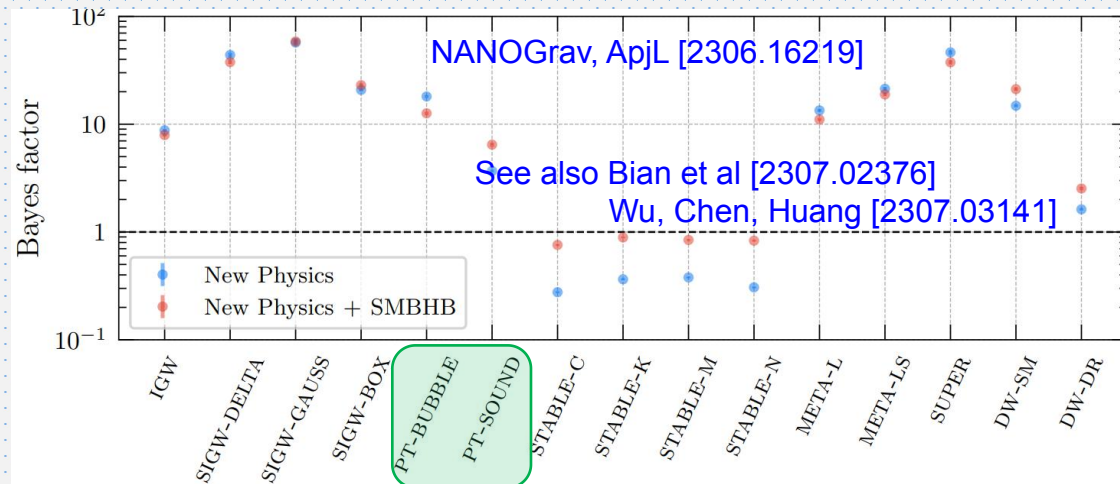


EPTA, A&A [2306.16214]

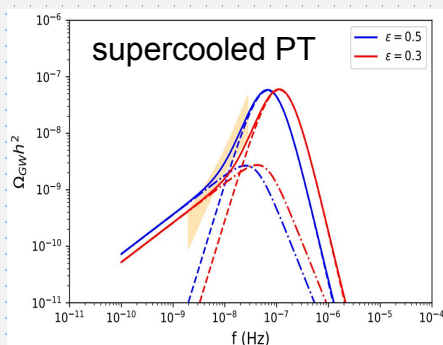
What possible PTA discovery implies?

- Once discovered, firstly needs to know its origin
- Can be the next “CMB” (spectral shape, anisotropy, etc)
- Can be from first order QCD-scale PT

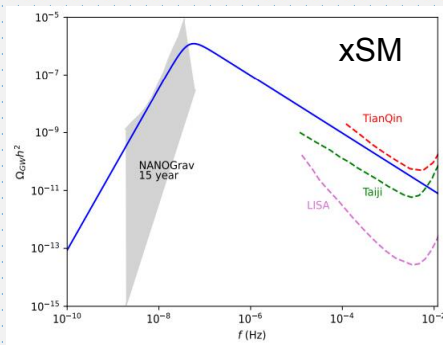
PPTA: Xue et al, PRL [2110.03096]
 NANOGrav (12.5-year): Arzoumanian et al, PRL [2104.13930]
 ...



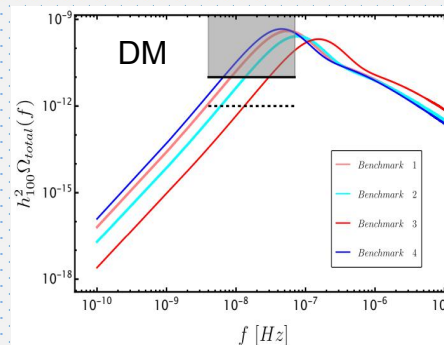
Han, Xie, Yang, Zhang [2306.16966]



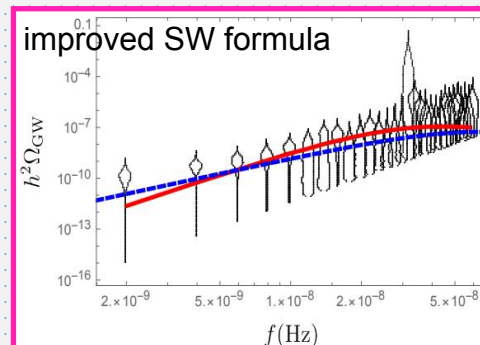
Zu, Zhang, Li, Gu, Tsai, Fan [2306.17239]



Xiao, Yang, Zhang [2307.01072]



Yang, Ma, Jiang, Huang [2306.17827]



Ghosh et al [2307.02259]

and more...

GWs from Particles

Extreme densities

disturbances in the early universe

As Macroscopic Objects

(non-) topological solitons



Environmental Effects

Faking GW signals (dark matter)

Solitons

- Localized
- Associated with nonlinear problem

Found in:

- ✓ Optics
- ✓ Hydrodynamics
- ✓ Condensed matter systems
- ✓ Quantum field theory

...



Solitons in Quantum Field Theory

- **Topological solitons:** symmetry breakings in the early universe (new physics, baryon asymmetry)
- **Non-Topological solitons:** as DM candidates (ultralight DM, macroscopic DM)

	Topological Solitons	Non-Topological Solitons
Definition	<p>Static Solution (Theory with Spontaneously Broken Symmetry)</p> <ul style="list-style-type: none"> ● Global symmetry (Skyrmion, Cosmic String) ● Discrete symmetry (Domain wall) ● Local symmetry (Monopole, Cosmic String or Vortex line...) ● Pure gauge theory (Instanton) 	<p>Bose-Einstein Condensate (of Ultralight particles)</p> <ul style="list-style-type: none"> ● Galactic scale (DM Halo) ● Stellar scale (Boson stars)
Boundary	Non-Trivial (needs degenerate vacuum states)	Trivial vacuum state
Stabilized by	Topology (boundary field values)	<p>Conserved Charge, and Balancing</p> <ul style="list-style-type: none"> ● quantum pressure ● gravity (or not, Q-balls etc) ● self-interactions (or not)

Topological Solitons in the Early Universe

- Firstly proposed to form in the early universe (Kibble, 1976)
(None observed)
- Later proposed to form in condensed matter systems (Zurek, 1985)
(already observed)

Name variant:
Topological Defects

The Cosmological Kibble Mechanism in the Laboratory: String Formation in Liquid Crystals
[Science, 263 \(1994\)](#)
Mark J. Bowick,* L. Chandar, E. A. Schiff, Ajit M. Srivastava

Can we detect the (cosmic) topological solitons?

Topology of cosmic domains and strings

T W B Kibble

[J.Phys.A 9 \(1976\) 1387-1398](#)

Blackett Laboratory, Imperial College, Prince Consort Road, London

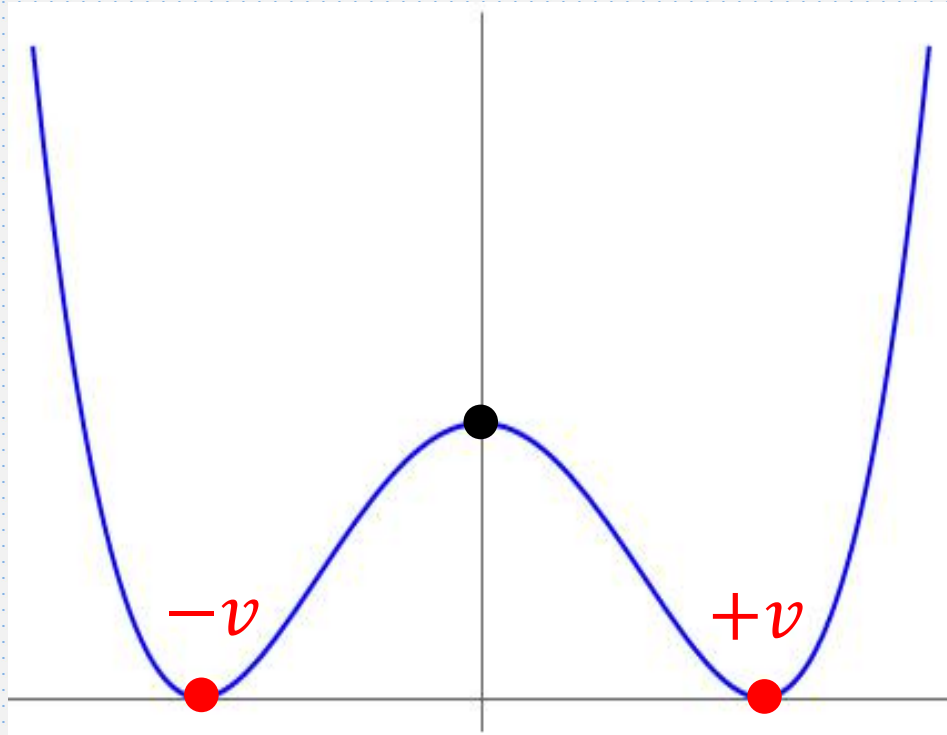
Received 11 March 1976

www.theguardian.com



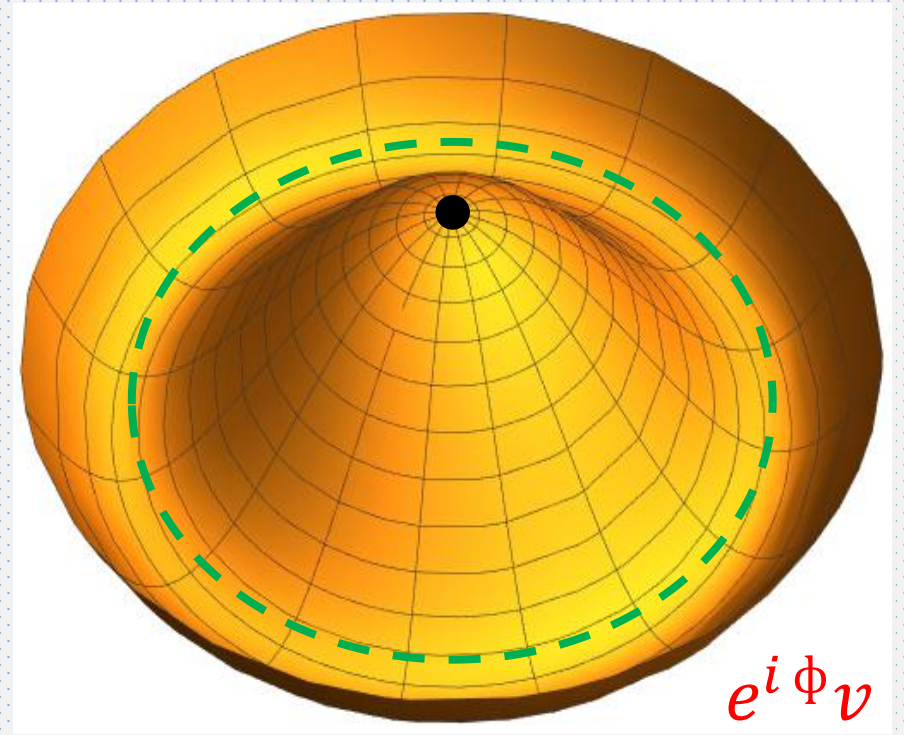
Degenerate Vacuum States

$$V(\phi) = \frac{1}{4}(\phi^2 - v^2)^2$$



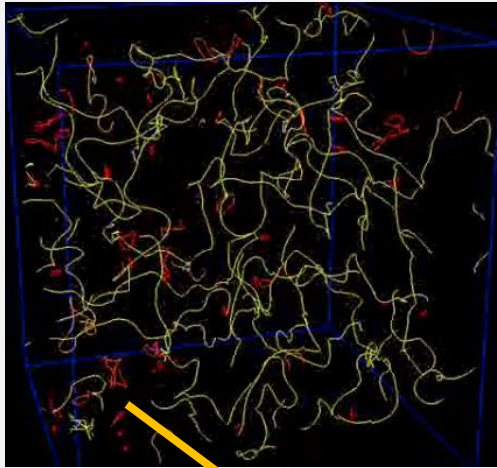
Domain wall

$$V(\Phi) = \frac{1}{4}(|\Phi|^2 - \eta^2)^2$$

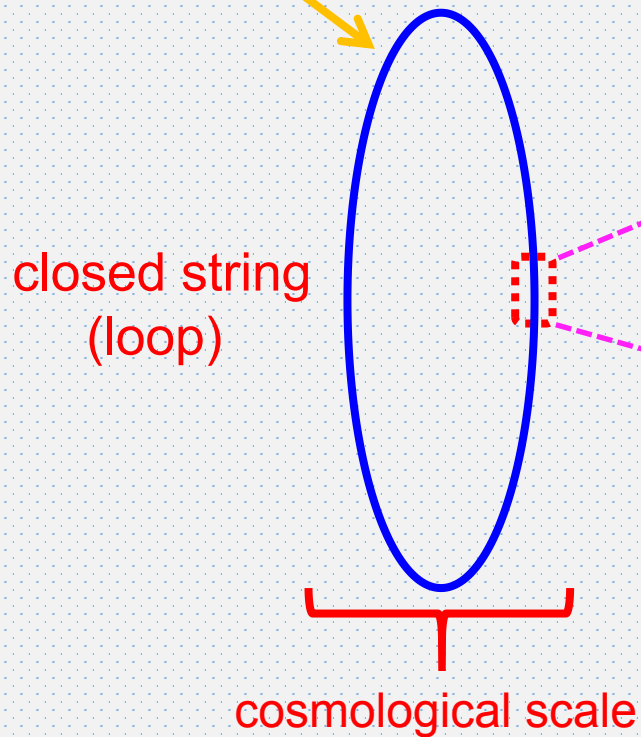


Cosmic String

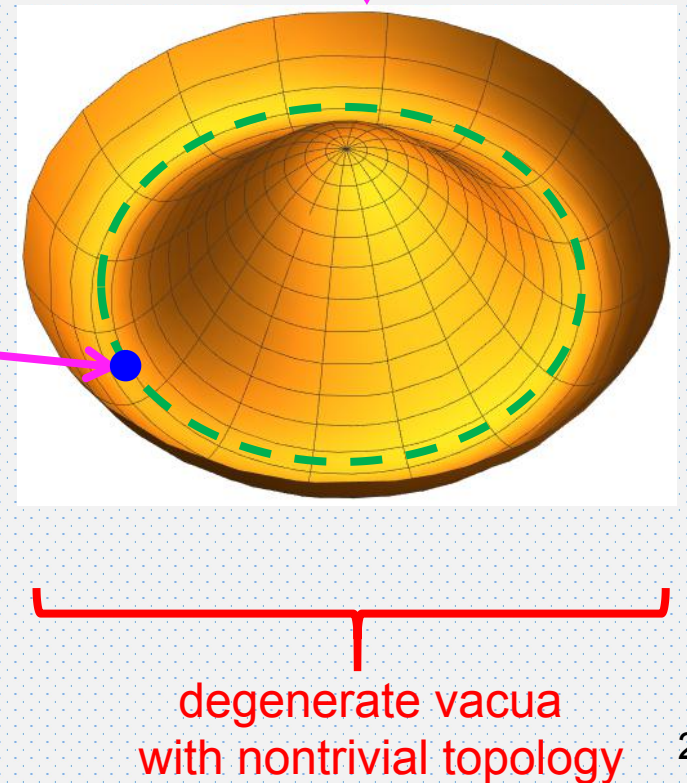
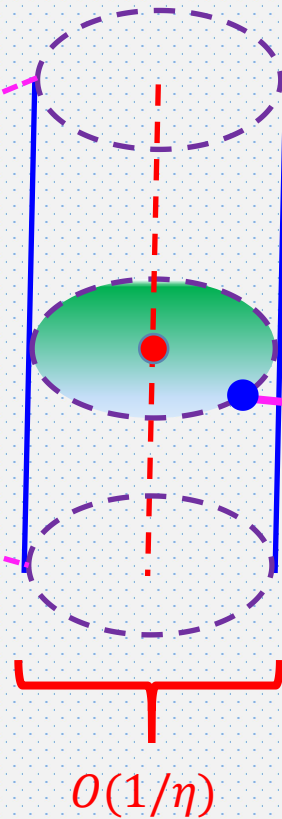
Cosmic String



Example: the Abelian Higgs Model

$$\mathcal{L} = |(\partial_\mu - igA_\mu)\Phi|^2 - \frac{1}{4}\lambda(|\Phi|^2 - \eta^2)^2 - \frac{1}{4}F_{\mu\nu}F^{\mu\nu}$$


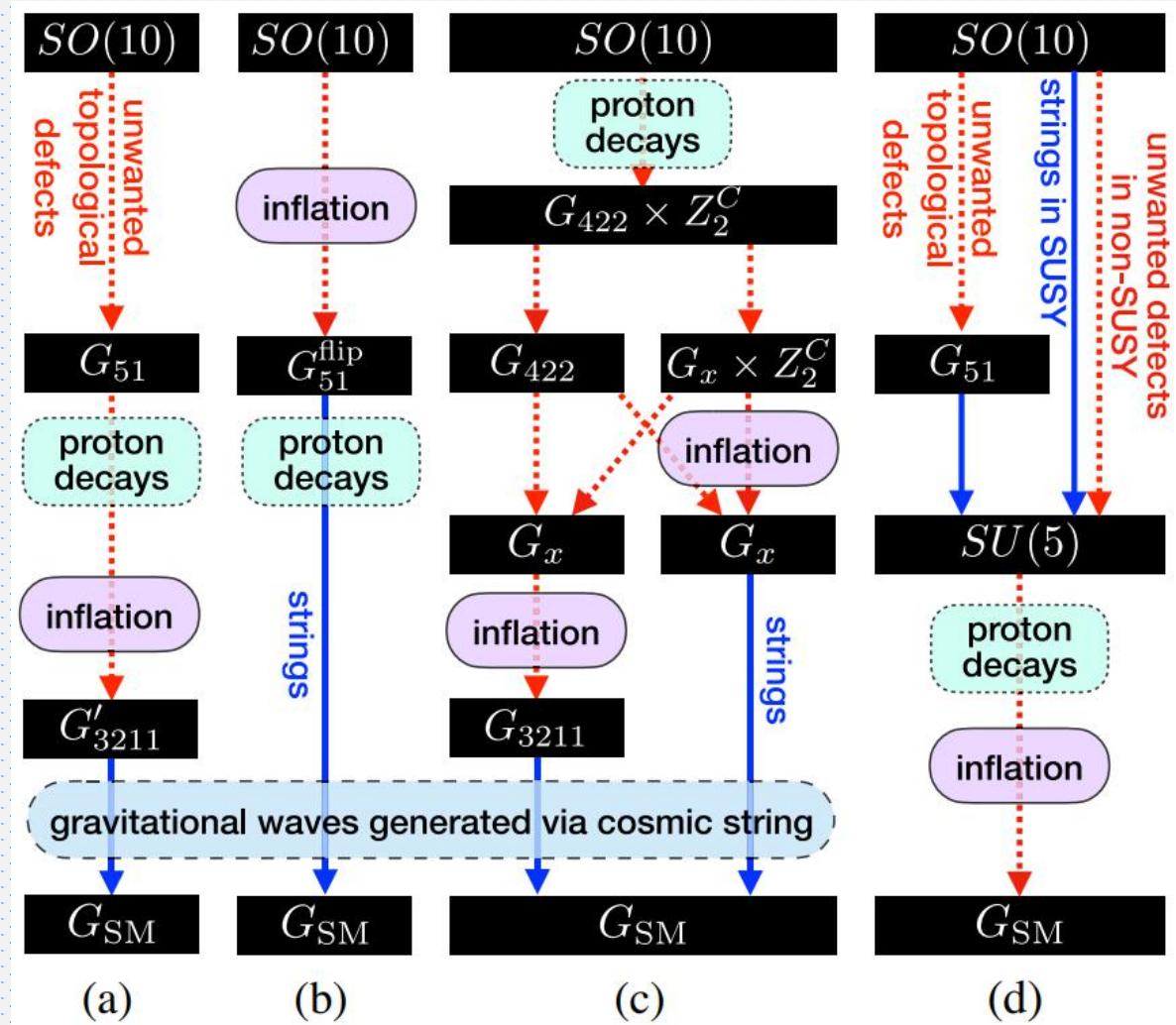
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GUT: Breaking Chains

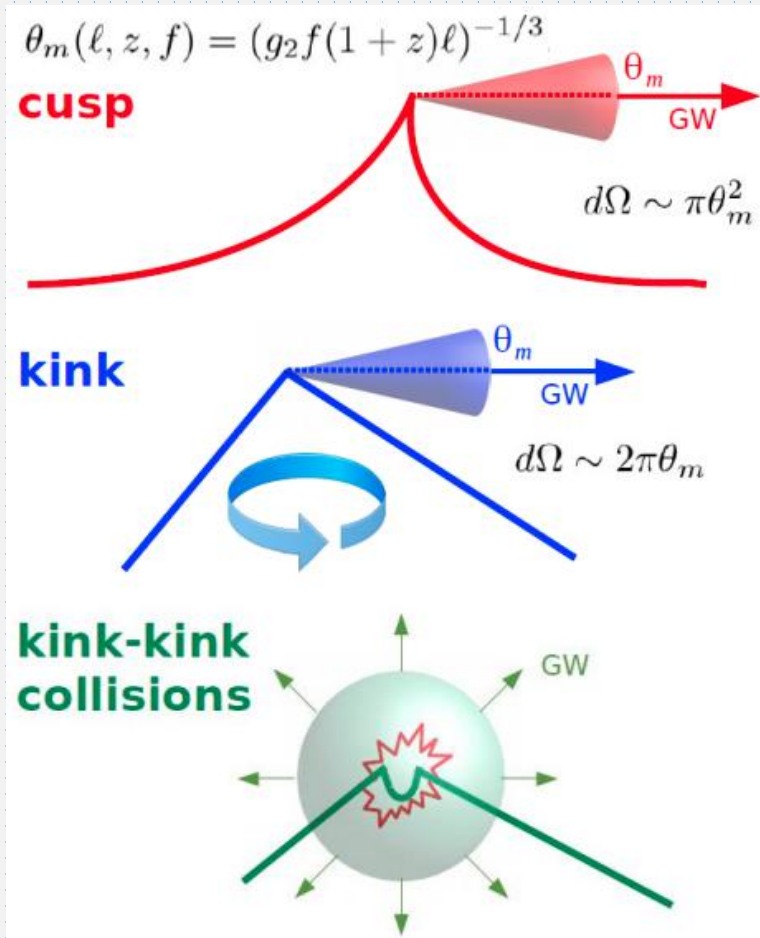
King, Pascoli, Turner, Zhou, PRL [2005.13549], JHEP [2106.15634]

$$\begin{aligned}
 G_{51} &= SU(5) \times U(1)_X, & G_{51}^{\text{flip}} &= SU(5)_{\text{flip}} \times U(1)_{\text{flip}}, \\
 G_{3221} &= SU(3)_C \times SU(2)_L \times SU(2)_R \times U(1)_{B-L}, \\
 G_{3211} &= SU(3)_C \times SU(2)_L \times U(1)_R \times U(1)_{B-L}, \\
 G'_{3211} &= SU(3)_C \times SU(2)_L \times U(1)_Y \times U(1)_X, \\
 G_{421} &= SU(4)_C \times SU(2)_L \times U(1)_Y, \\
 G_{422} &= SU(4)_C \times SU(2)_L \times SU(2)_R.
 \end{aligned}
 \tag{1}$$



Gravitational Wave Production

Burst types: **cusps**, **kinks** and **kink-kink collisions**
 (Damour, Vilenkin, PRL 85,3671, PRD 64, 064008).



simple waveforms in frequency domain

$$h_i(\ell, z, f) = A_i(\ell, z) f^{-q_i}$$

$$A_i(\ell, z) = g_{1,i} \frac{G\mu \ell^{2-q_i}}{(1+z)^{q_i-1} r(z)}$$

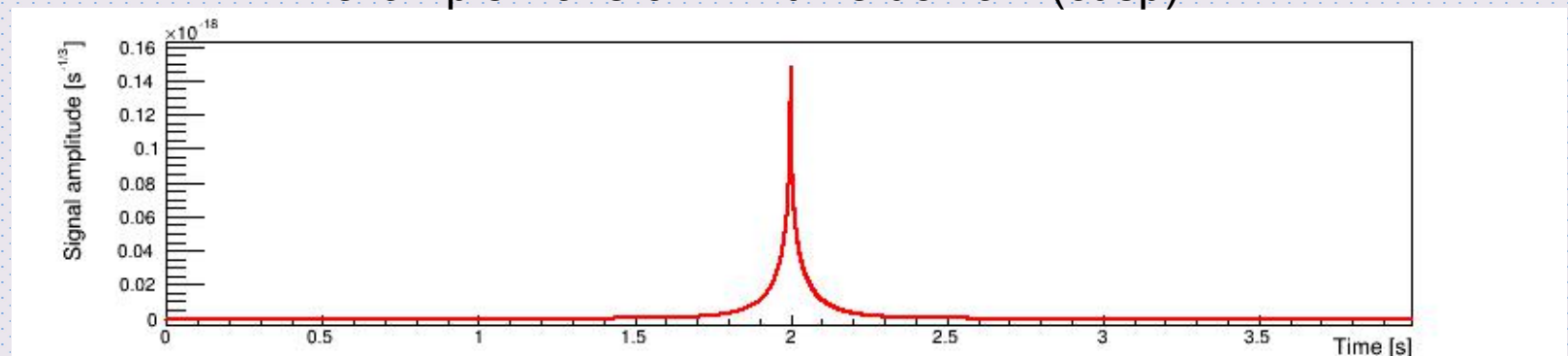
$q = 4/3, 5/3, 2$ for cusp, kink, and kk

scale

$$G\mu \sim (\eta/M_{\text{Pl}})^2$$

particle physics model dependence

example waveform in time domain (cusp)



<https://www.ligo.org/science/Publication-S5S6CosmicStrings>

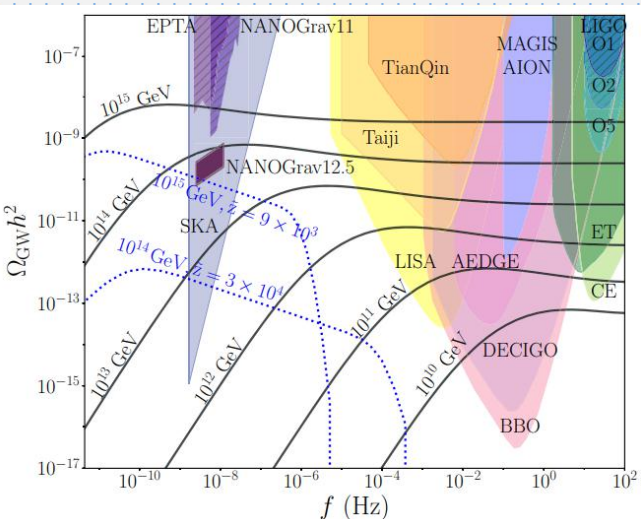
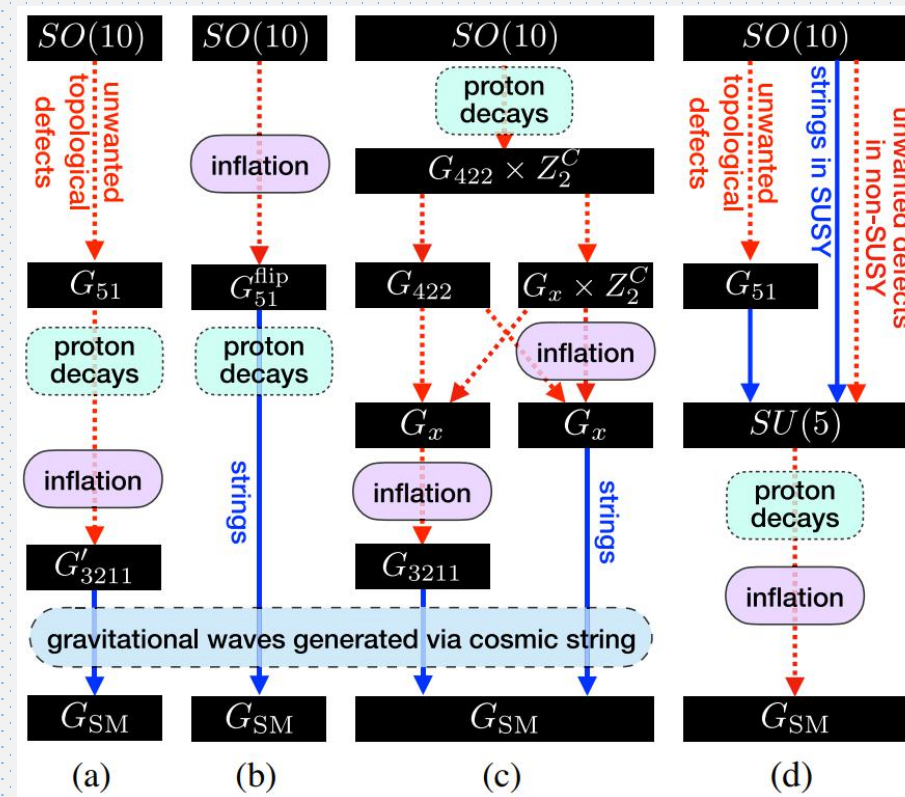
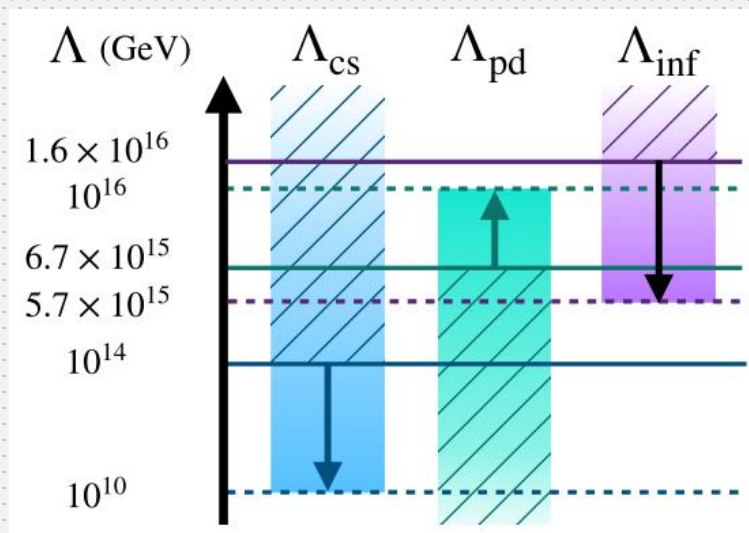
GUT: Proton Decay and GW Complementarity

King, Pascoli, Turner, Zhou, PRL [2005.13549], JHEP [2106.15634]

- Proton decay measurement
- GW detection
- Dangerous defects

$$\frac{\epsilon_{\alpha\beta}}{\Lambda_1^2} [(\bar{u}_R^c \gamma^\mu Q_\alpha)(\bar{d}_R^c \gamma_\mu L_\beta) + (\bar{u}_R^c \gamma^\mu Q_\alpha)(\bar{e}_R^c \gamma_\mu Q_\beta)]$$

$$+ \frac{\epsilon_{\alpha\beta}}{\Lambda_2^2} [(\bar{d}_R^c \gamma^\mu Q_\alpha)(\bar{u}_R^c \gamma_\mu L_\beta) + (\bar{d}_R^c \gamma^\mu Q_\alpha)(\bar{\nu}_R^c \gamma_\mu Q_\beta)],$$



Observables		Proton decays
		$p \rightarrow \pi^0 e^+$ observed \Rightarrow non-SUSY contribution indicated
GWs	Observed	<ul style="list-style-type: none"> • types (a) and (c) favoured • types (b) and (d) excluded
	Marginal	<ul style="list-style-type: none"> • types (a) and (c) favoured • type (d) excluded • type (b) allowed if $p \rightarrow K^+ \bar{\nu}$ not observed and $\Lambda_{pd} \sim \Lambda_{cs}$

Leptogenesis

Dror, Hiramatsu, Kohri, Murayama, White, PRL [1908.03227]

	$H = G_{\text{SM}}$		$H = G_{\text{SM}} \times \mathbb{Z}_2$	
G	<i>Defects</i>	<i>Higgs</i>	<i>Defects</i>	<i>Higgs</i>
G_{disc}	Domainwall*	$B - L = 1$	Domainwall*	$B - L = 2$
G_{B-L}	Abelianstring*	$B - L = 1$	\mathbb{Z}_2 string [†]	$B - L = 2$
G_{LR}	Texture*	$(\mathbf{1}, \mathbf{1}, \mathbf{2}, \frac{1}{2})$	\mathbb{Z}_2 string	$(\mathbf{1}, \mathbf{1}, \mathbf{3}, \mathbf{1})$
G_{421}	None	$(\mathbf{10}, \mathbf{1}, \mathbf{2})$	\mathbb{Z}_2 string	$(\mathbf{15}, \mathbf{1}, \mathbf{2})$
G_{flip}	None	$(\mathbf{10}, \mathbf{1})$	\mathbb{Z}_2 string	$(\mathbf{50}, \mathbf{2})$

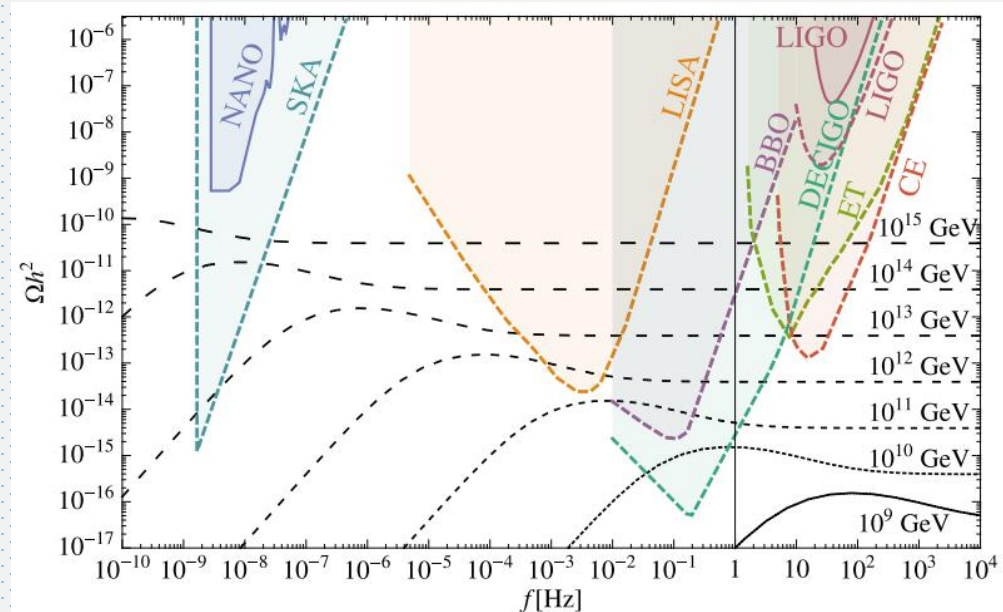
$$G_{\text{disc}} = G_{\text{SM}} \times \mathbb{Z}_N,$$

$$G_{B-L} = G_{\text{SM}} \times U(1)_{B-L},$$

$$G_{LR} = SU(3)_C \times SU(2)_L \times SU(2)_R \times U(1)_{B-L},$$

$$G_{421} = SU(4)_{\text{PS}} \times SU(2)_L \times U(1)_Y,$$

$$G_{\text{flip}} = SU(5) \times U(1).$$



Loop Distribution Function

3 models considered

- Model A: (Blanco-Pillado et al., PRD 89,023512) (simulations)
- Model B: Lorentz et al., JCAP 10 (2010) 003 (analytical modelling, matched onto simulation result)
- Model C: Auclair et al., JCAP 06 (2019) 015 (interpolation between above 2)

C-1 (C-2) reproduces LDF of Model A (B) in the radiation era and LDF of Model B (A) in the matter era

Large N_c or N_k does not necessarily lead to large signal (loops decays faster)

$$\gamma_d = \Gamma_d G \mu$$

$$\Gamma_d \equiv \frac{P_{\text{gw}}}{G\mu^2} = \sum_i \frac{P_{\text{gw},i}}{G\mu^2} \quad \text{dimensionless decay constant}$$

$$= N_c \frac{3\pi^2 g_{1,c}^2}{(2\delta)^{1/3} g_2^{2/3}} + N_k \frac{3\pi^2 g_{1,k}^2}{(2\delta)^{2/3} g_2^{1/3}} + N_{kk} 2\pi^2 g_{1,kk}^2$$

cusp

kink

kink-kink collision

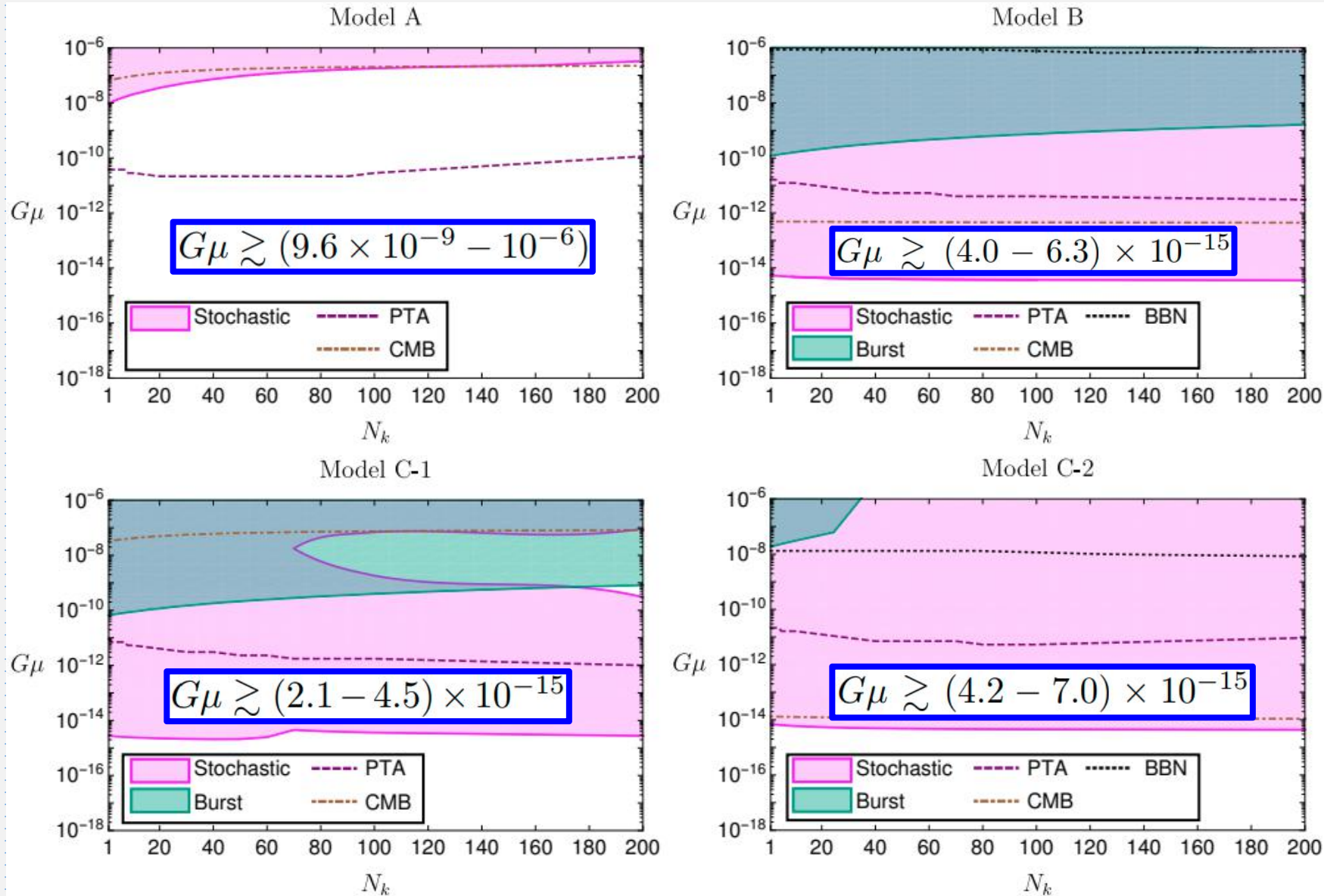
modelling loop distribution (F, dimensionless)

$$\frac{\partial}{\partial t} [a^3 F(l, t)] = a^3 \mathcal{P}(l, t) + a^3 \gamma_d \frac{\partial}{\partial t} F(l, t)$$

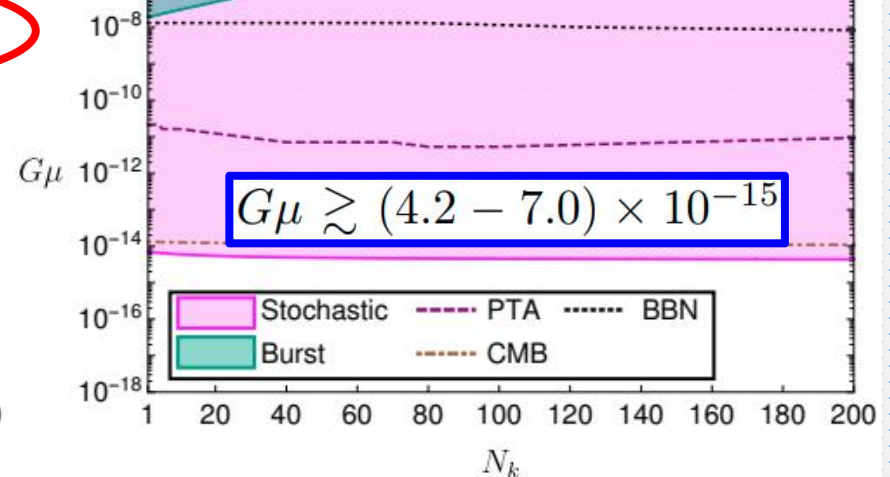
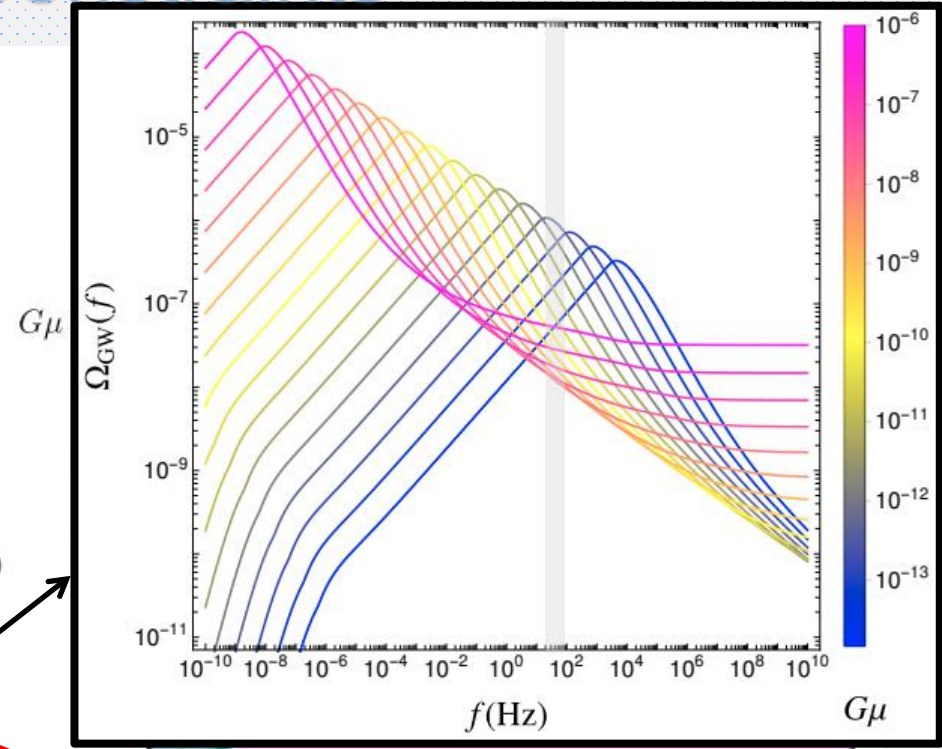
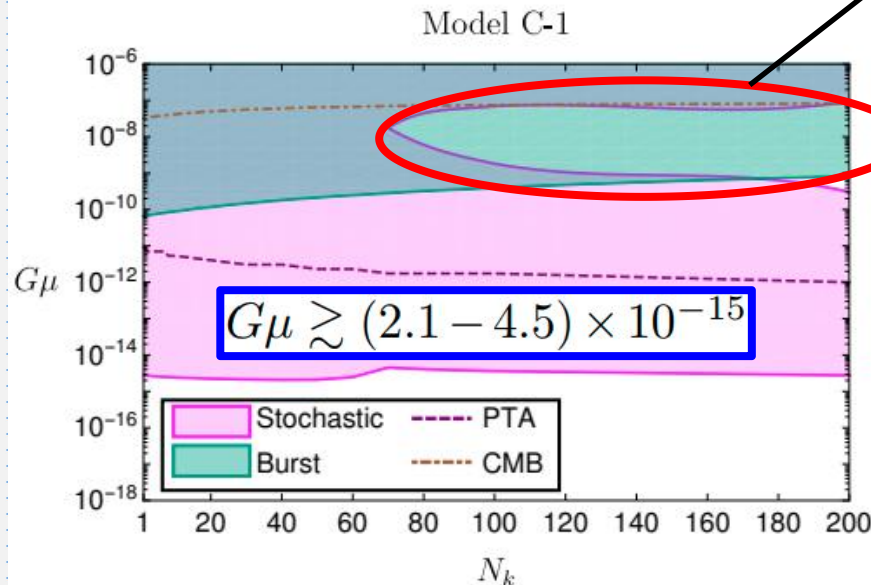
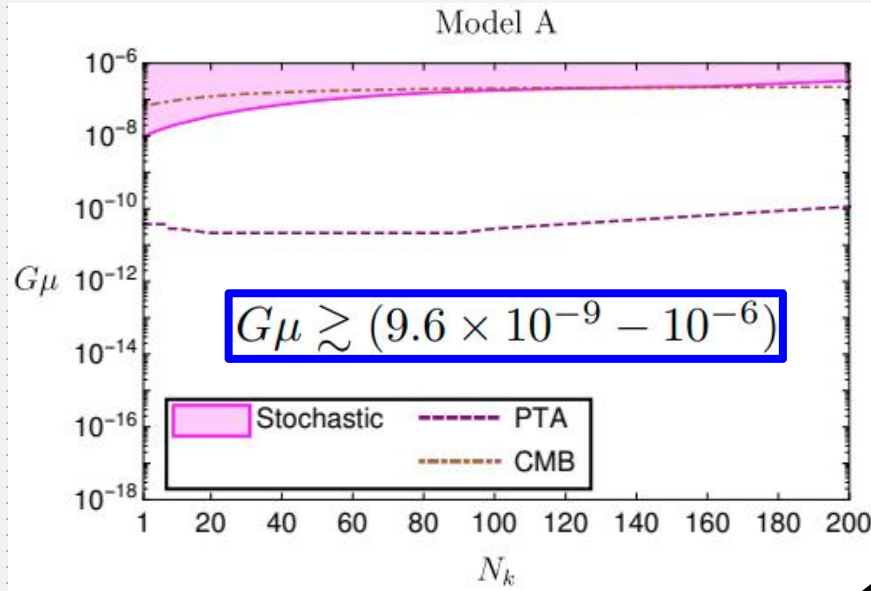
production from long strings

decay due to GW radiation

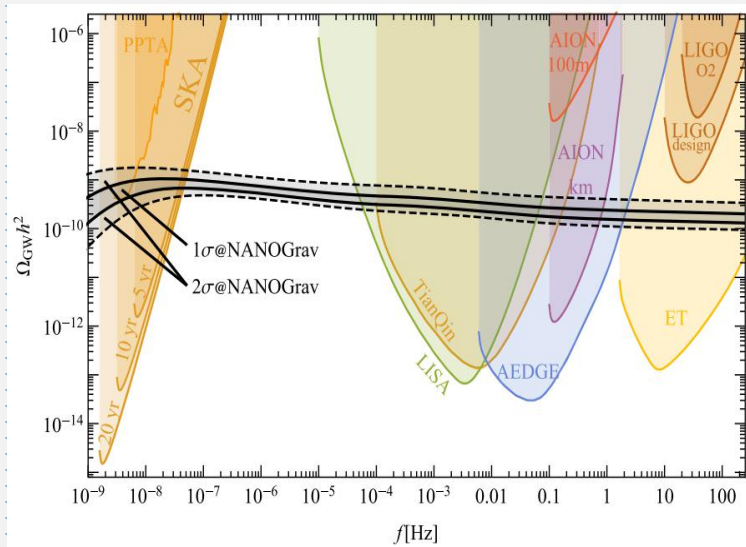
LIGO Constraints



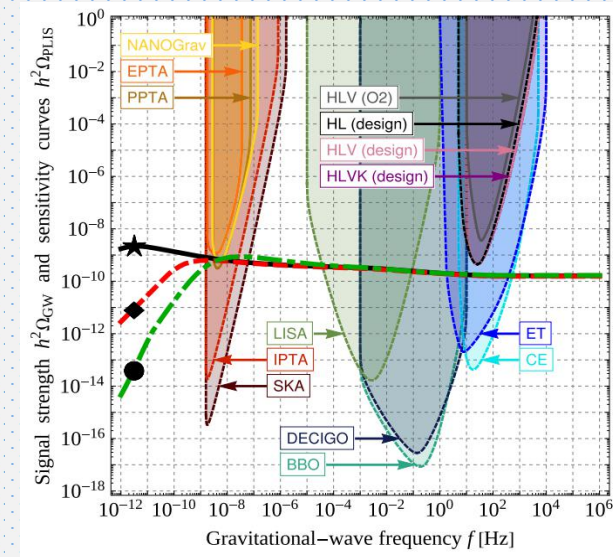
LIGO Constraints



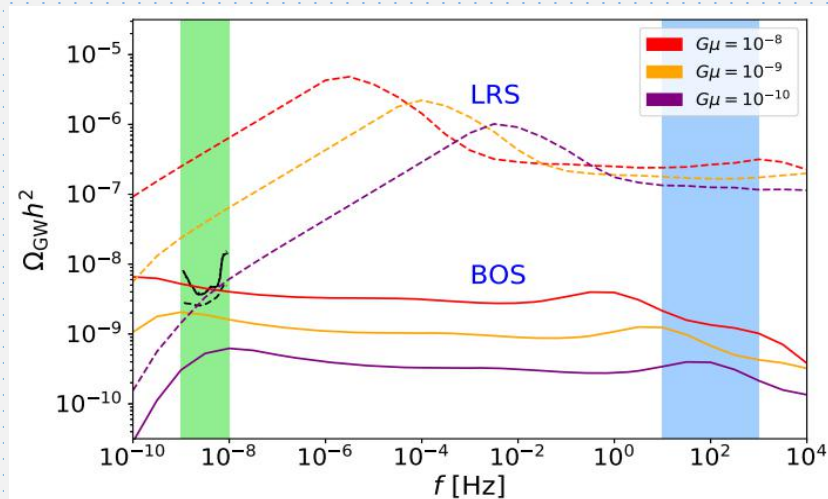
PTA



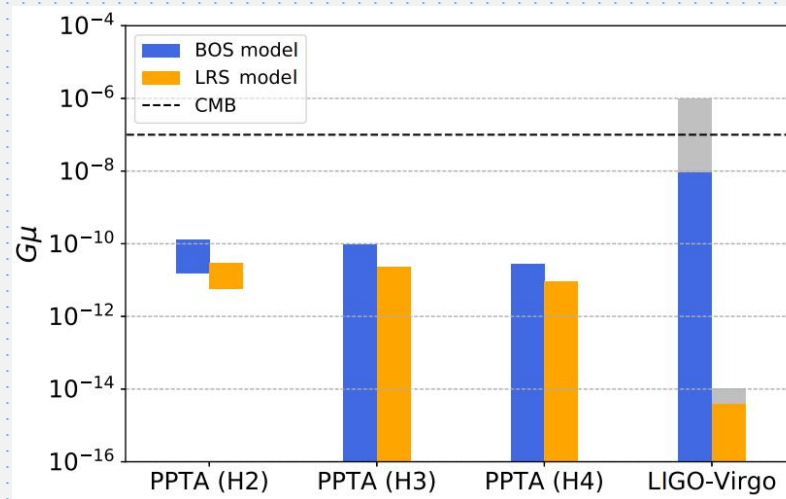
Ellis, Lewicki, PRL [2009.06555]



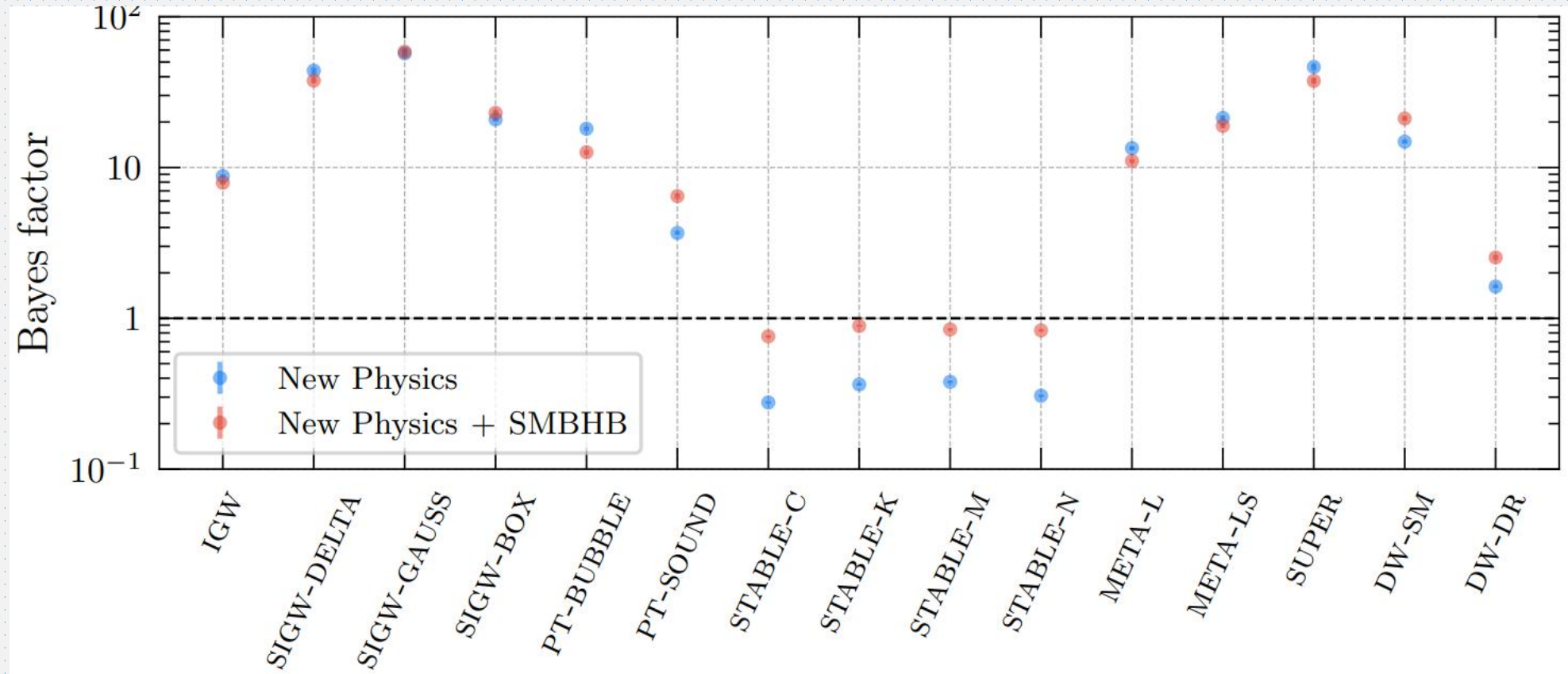
Blasi, Brdar, Schmitz, PRL [2009.06607]



Bian, Shu, Wang, Yuan, Zong, PRD Letter [2205.07293]



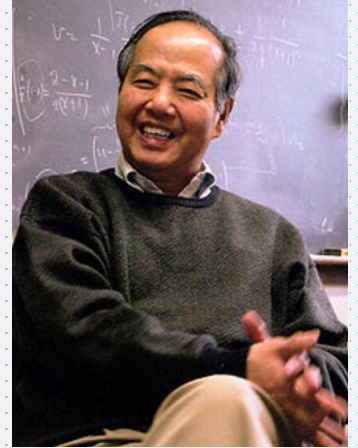
PTA: New



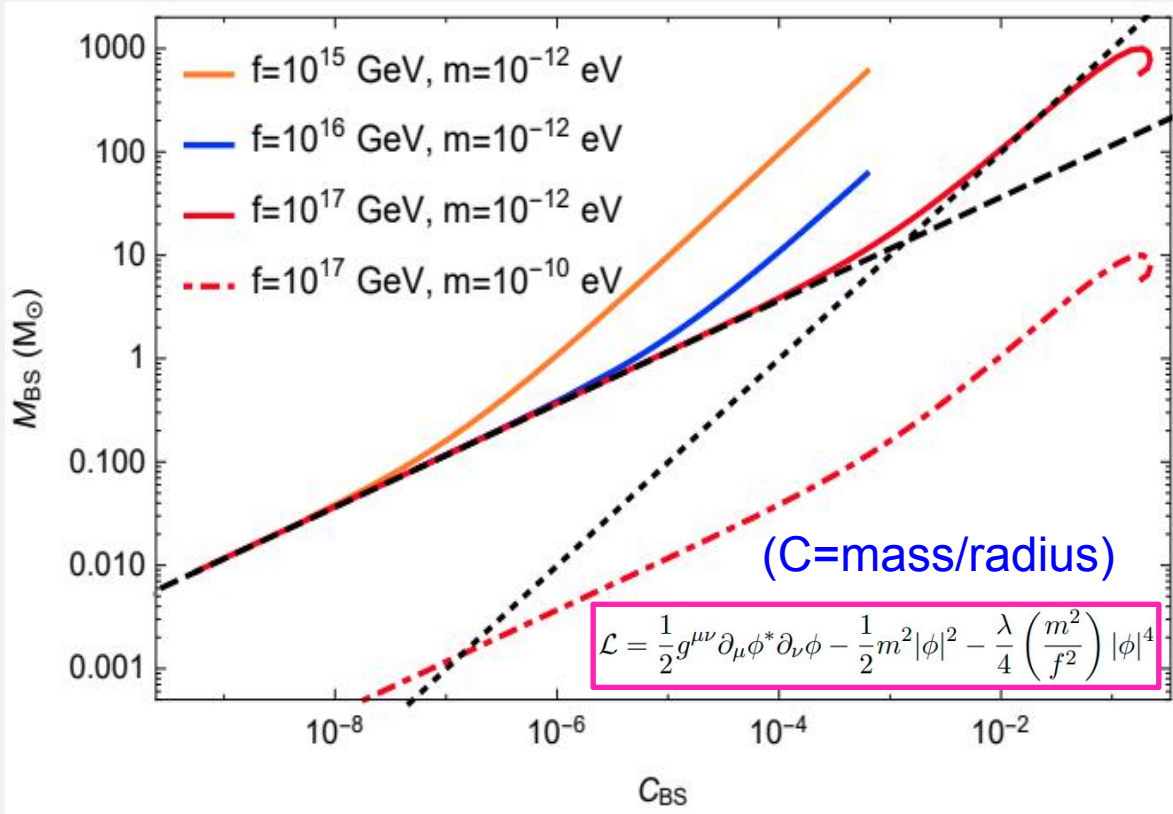
NANOGrav, ApjL [2306.16219]

See also Bian et al [2307.02376], Wu, Chen, Huang [2307.03141]

Non-Topological Solitons as Boson Stars



- Macroscopic Bose-Einstein condensate of ultralight particles
- Boson stars can be very massive and compact



HG, Sinha, Sun, JCAP 09 (2019) 032

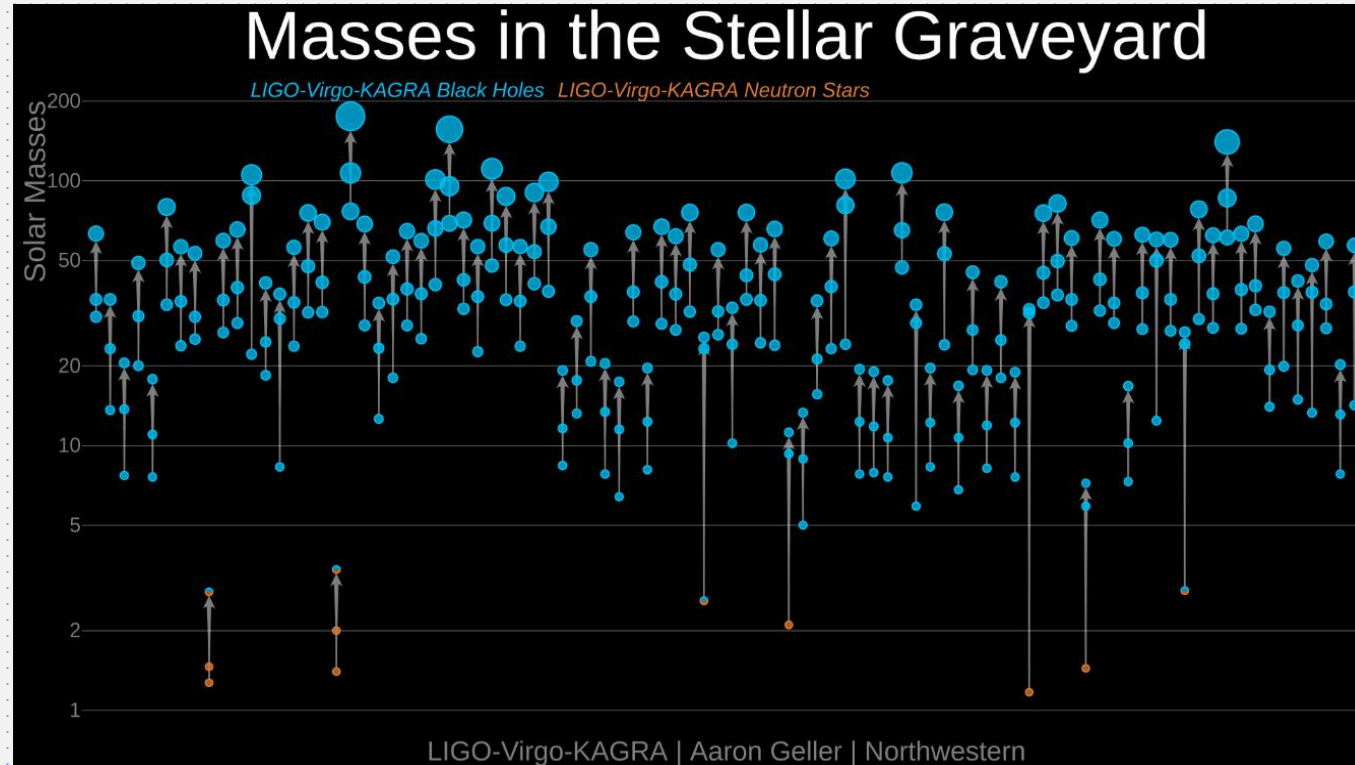
- ❖ Mini-Boson Star (without self-interaction)
- ❖ Solitonic Boson Star (specific potential)
- ❖ Oscillaton (real scalar field)
- ❖ Proca Star (massive complex vector)
- ❖ Axion Stars (dense, dilute)

See, e.g., Liebling, Palenzuela, Living Rev Relativ (2017) 20:5

Lee, Pang, Phys.Rept (1992)

Did LIGO detect Boson Stars?

- Difficult to distinguish
- Mass as discriminator
(SBH cannot be subsolar)



PRL 116, 201301 (2016)

PHYSICAL REVIEW LETTERS

week ending
20 MAY 2016

Did LIGO Detect Dark Matter?

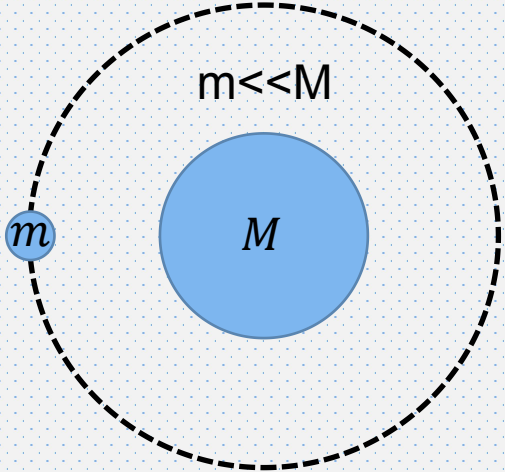
Simeon Bird,^{*} Ilias Cholis, Julian B. Muñoz, Yacine Ali-Haïmoud, Marc Kamionkowski,
Ely D. Kovetz, Alvise Raccanelli, and Adam G. Riess
*Department of Physics and Astronomy, Johns Hopkins University,
3400 North Charles Street, Baltimore, Maryland 21218, USA*
(Received 4 March 2016; published 19 May 2016)

GW190521 as a Merger of Proca Stars: A Potential New Vector
Boson of 8.7×10^{-13} eV

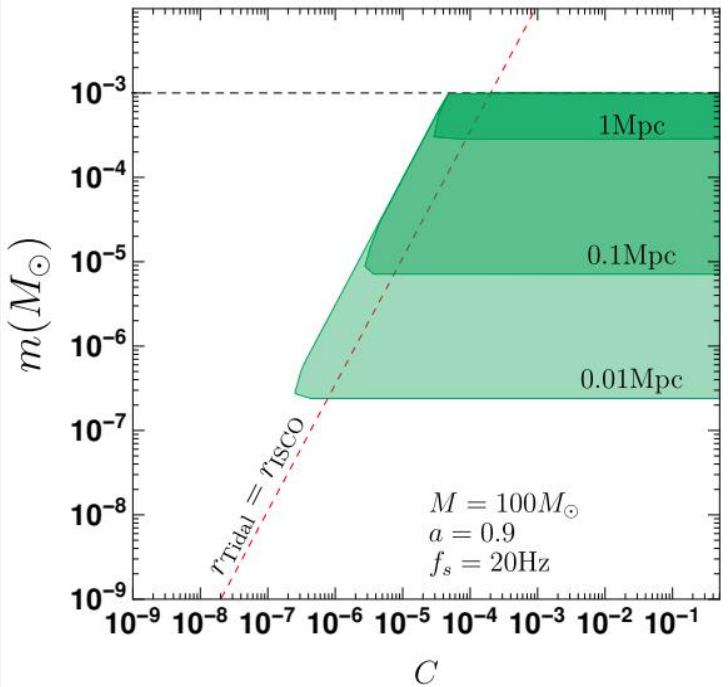
Juan Calderón Bustillo, Nicolas Sanchis-Gual, Alejandro Torres-Forné, José A. Font, Avi Vajpeyi, Rory Smith,
Carlos Herdeiro, Eugen Radu, and Samson H. W. Leong
Phys. Rev. Lett. **126**, 081101 – Published 24 February 2021

Detection with EMRI and mini-EMRI

- By making one object much heavier, one can probe much lighter companion object
- Ideal systems: extreme mass ratio inspirals (EMRIs), key target of Taiji, Tianqin, LISA.
- LIGO can detect mini-EMRIs (extreme mass ratio, but lighter objects)

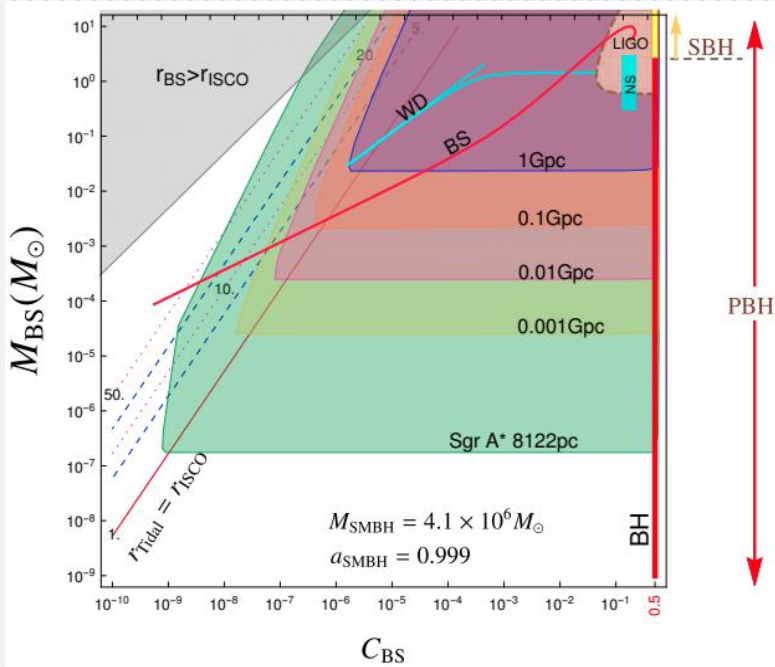


LIGO (“mini-EMRI”)



HG, A. Miller, arxiv:2205.10359

LISA, Taiji, Tianqin (EMRI)



HG, Sinha, Sun, JCAP 09 (2019) 032
 HG, Shu, Zhao, PRD 99 (2019) 023001

GWs from Particles

Extreme densities

disturbances in the early universe

As Macroscopic Objects

(non-) topological solitons

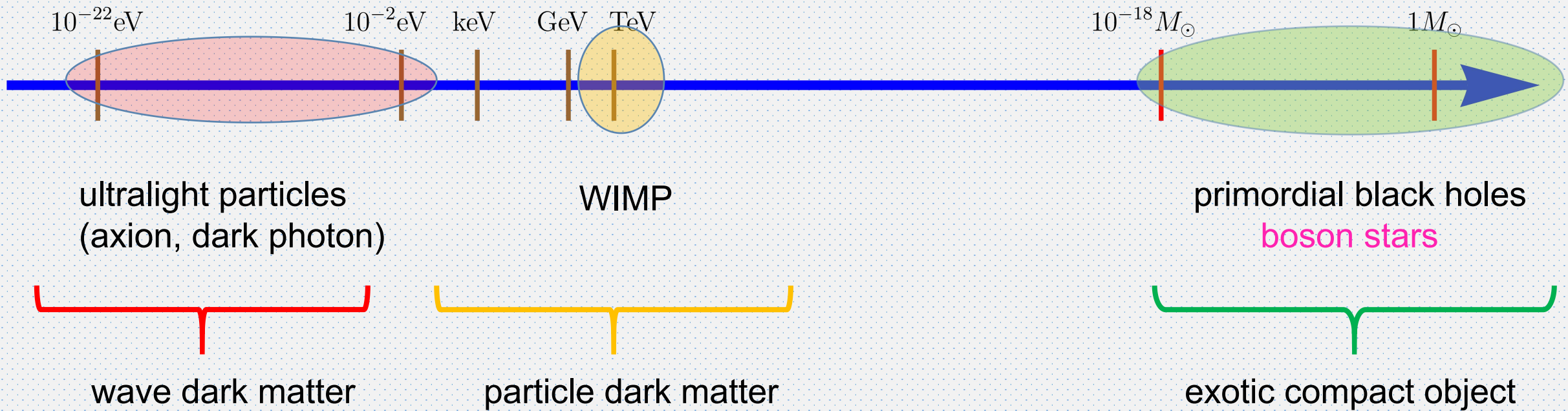
Environmental Effects

Faking GW signals (dark matter)



Ultralight Dark Matter

- Boson stars serve as macroscopic dark matter candidate
- So does the ultralight particle making up the boson stars



Dark Matter

Vector

$$\mathcal{L} = -\frac{1}{4}F^{\mu\nu}F_{\mu\nu} + \frac{1}{2}m^2 A^\mu A_\mu - \epsilon e J^\mu A_\mu$$

- Dark photon dark matter
- U(1) B or B-L
- Induces differential arm-length change for LIGO

Scalar

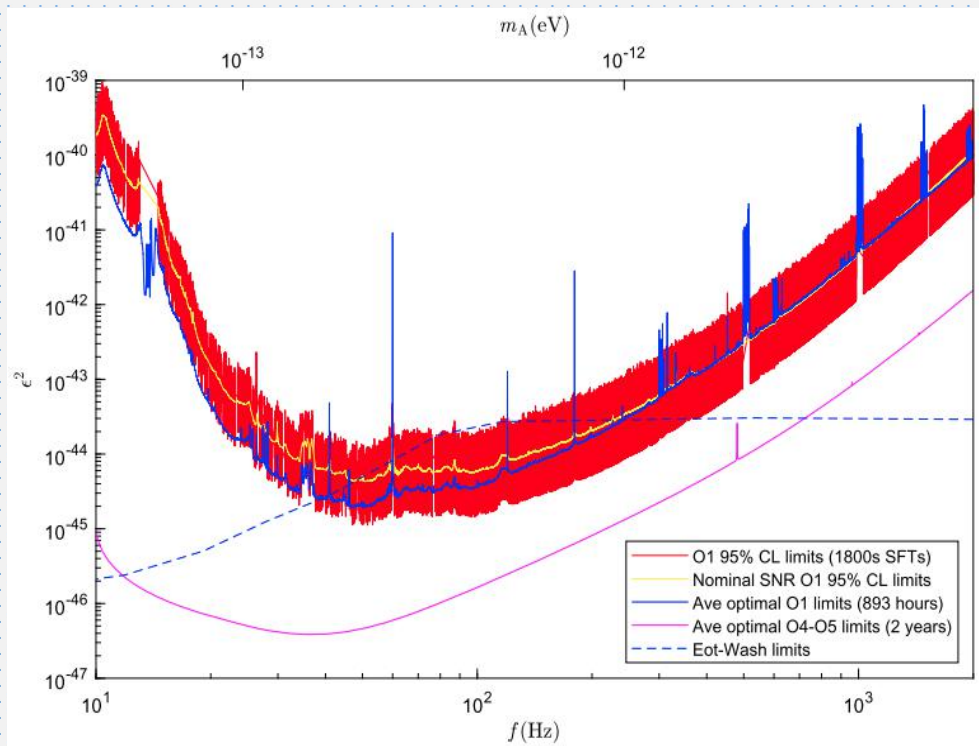
Damour, Donoghue, PRD [1007.2792]

$$\mathcal{L}_{\text{int}\phi} = \kappa\phi \left[+\frac{d_e}{4e^2}F_{\mu\nu}F^{\mu\nu} - \frac{d_g\beta_3}{2g_3}F_{\mu\nu}^A F^{A\mu\nu} - \sum_{i=e,u,d} (d_{m_i} + \gamma_{m_i}d_g)m_i\bar{\psi}_i\psi_i \right].$$

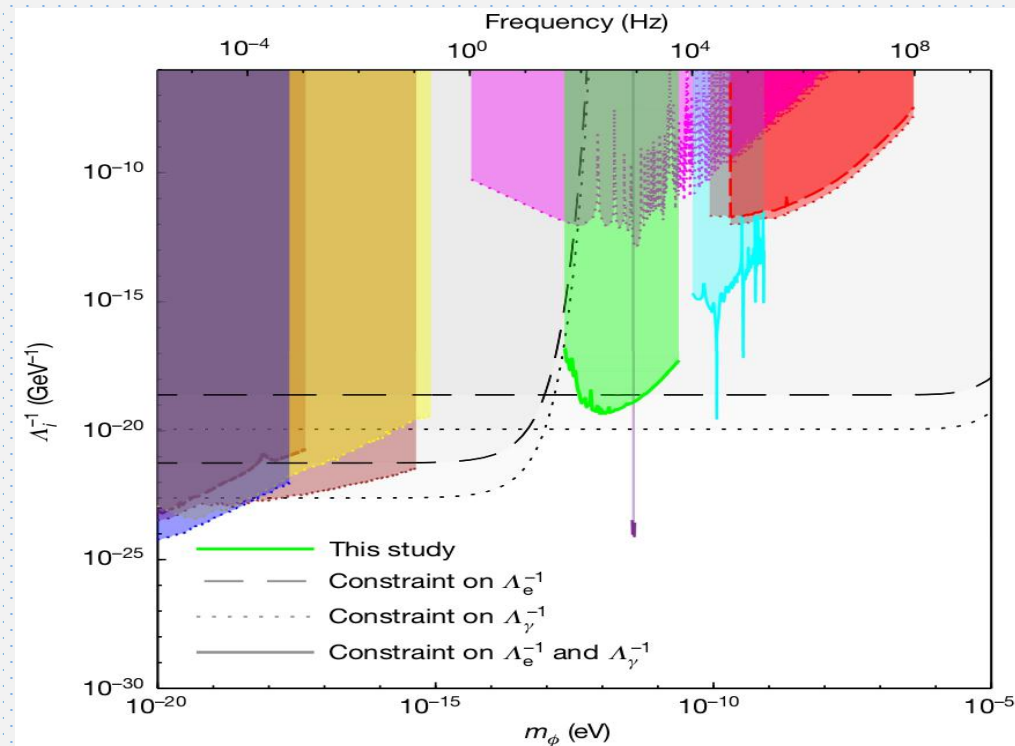
- Dilaton
- Cause variation in fundamental constants
- Changes mirror size and refractive index for LIGO

Ground-based GW Detectors

- Ground-based GW detector: LIGO-Virgo-KAGRA, GEO600
- LIGO O1 data first analyzed in 2019

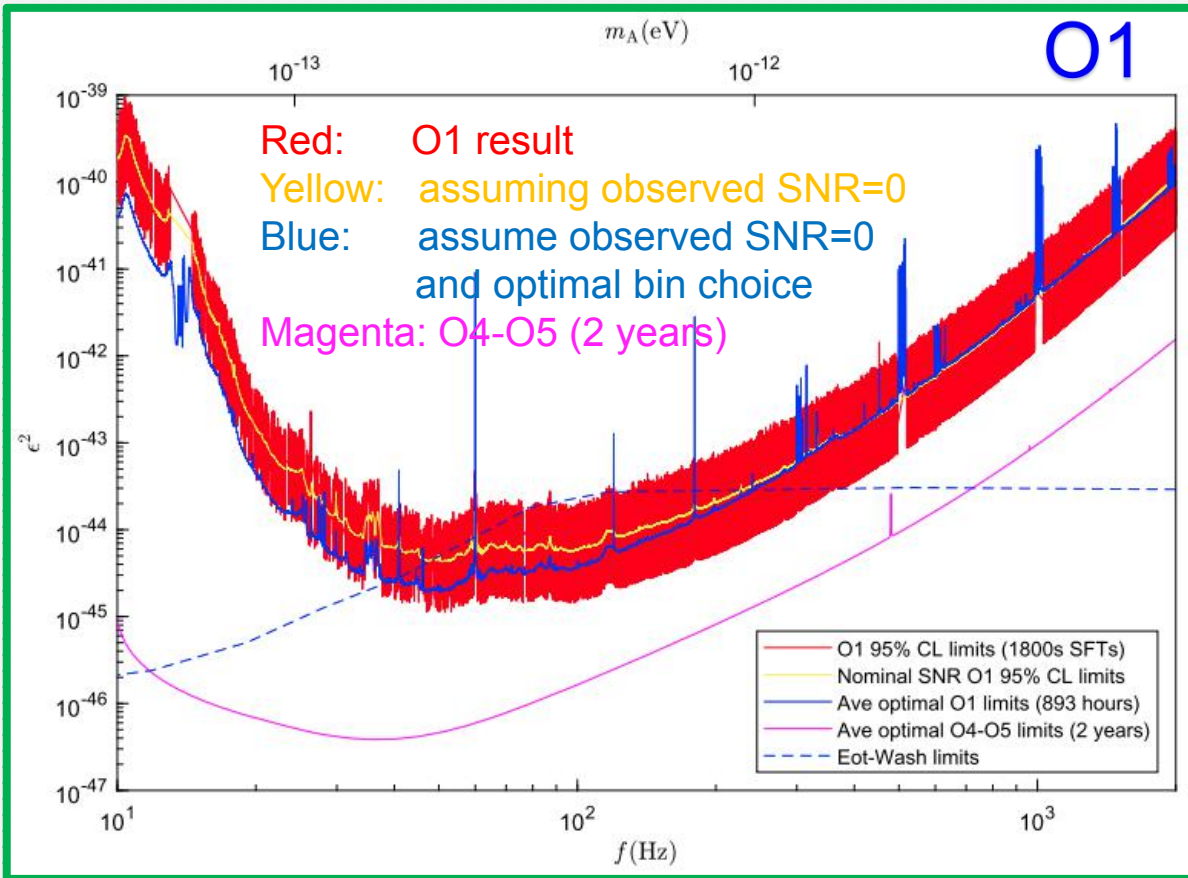


HG, Riles, Yang, Zhao, Communications Physics [1905.04316]

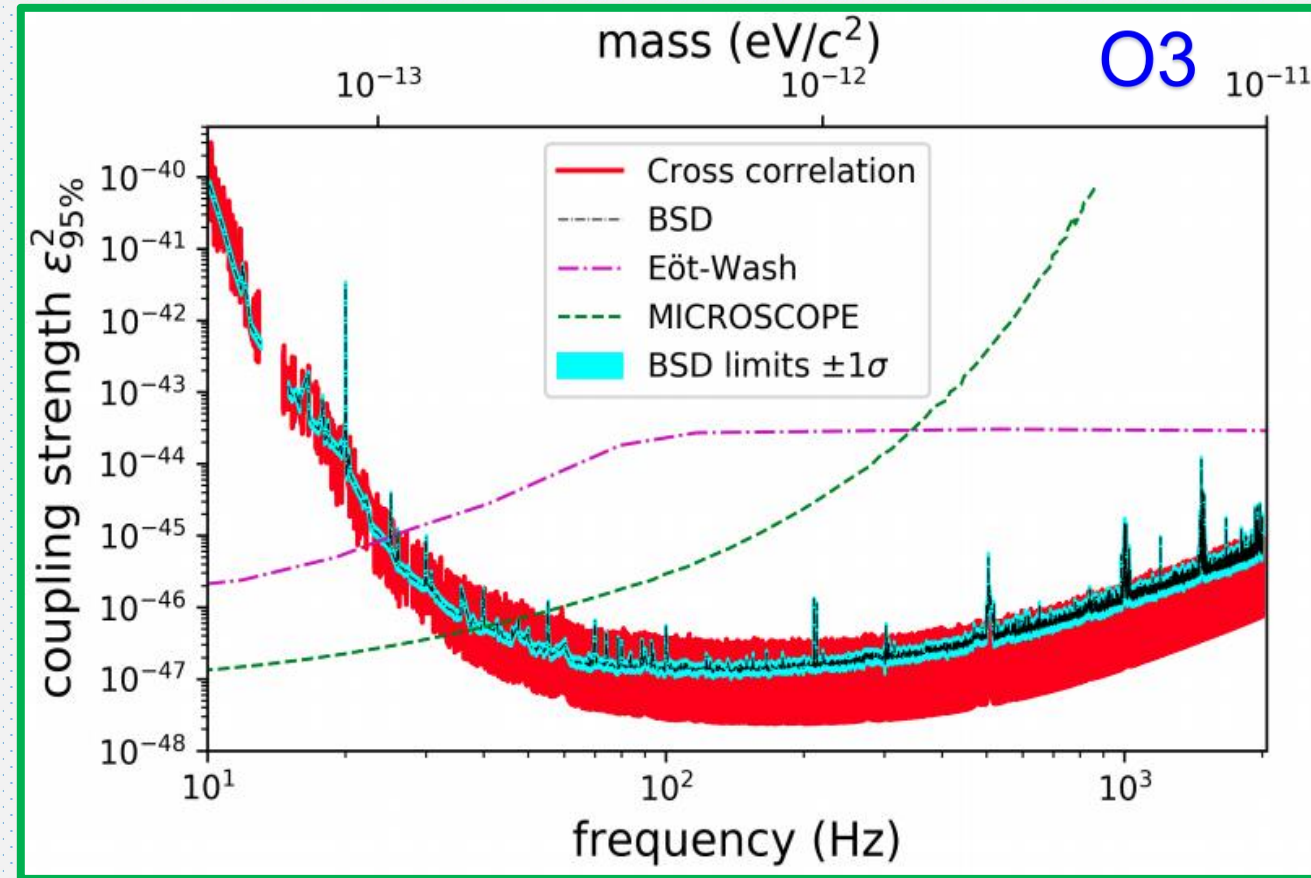


Vermeulen, et al, Nature [2103.03783]

LIGO Search Results



(Nature) Commun.Phys. 2 (2019) 155, [HG](#), Riles, Yang, Zhao



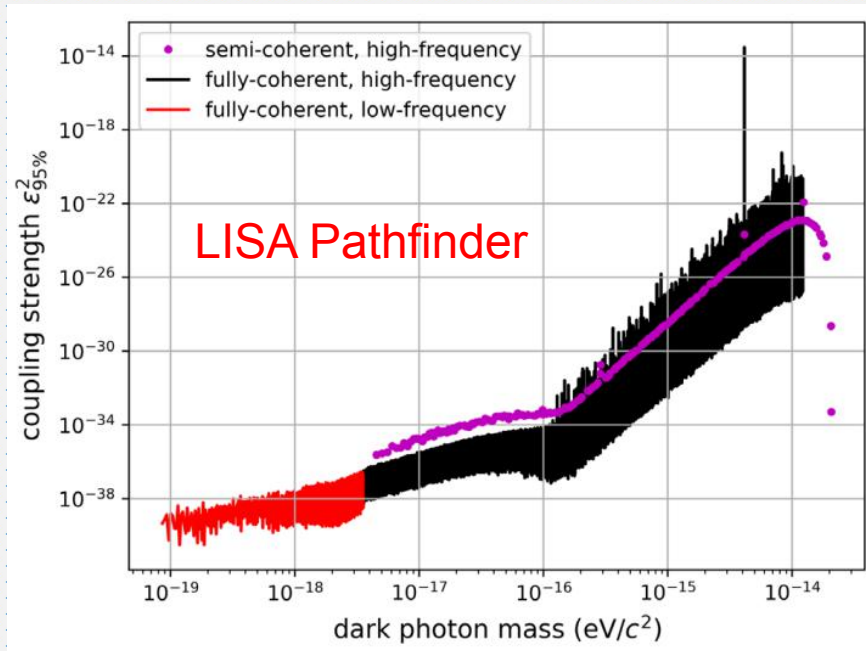
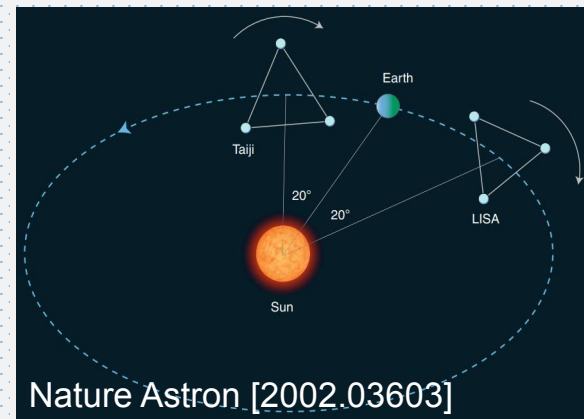
Phys.Rev.D 105 (2022) 6, LIGO-Virgo-KAGRA Collaborations

New in O3 search:

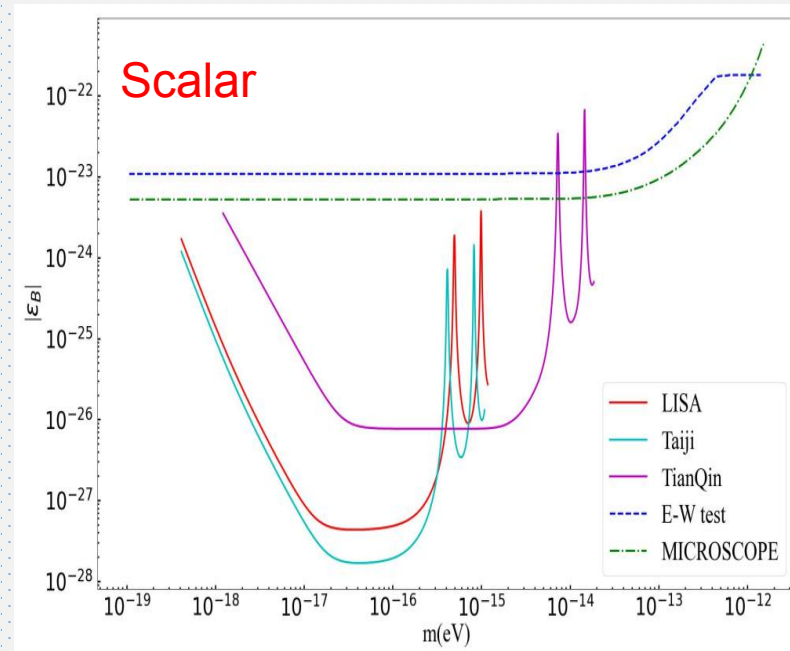
1. Another search performed by the continuous wave group with a different method
2. An improvement factor included from finite light travel time (PRD.103.L051702, Morisaki, et al)

Space-based GW Detectors

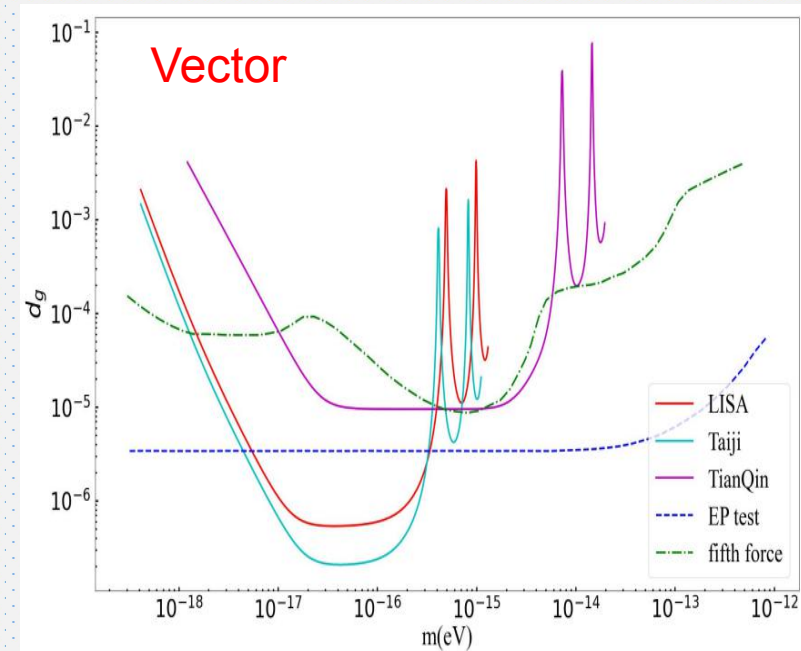
- Space-based GW detector: LISA, Taiji, Tianqin
- Lower frequency \rightarrow Lower mass
- Time delay interferometry: non-trivial detector response



Miller, Mendes, PRD [2301.08736]

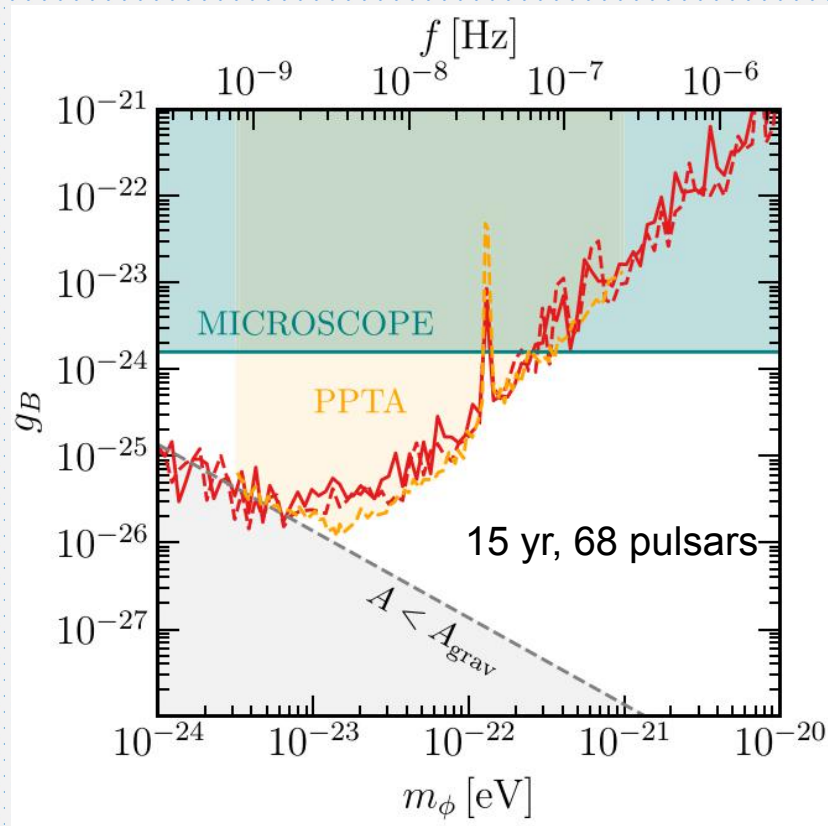


Yu, Yao, Tang, Wu [2307.09197]

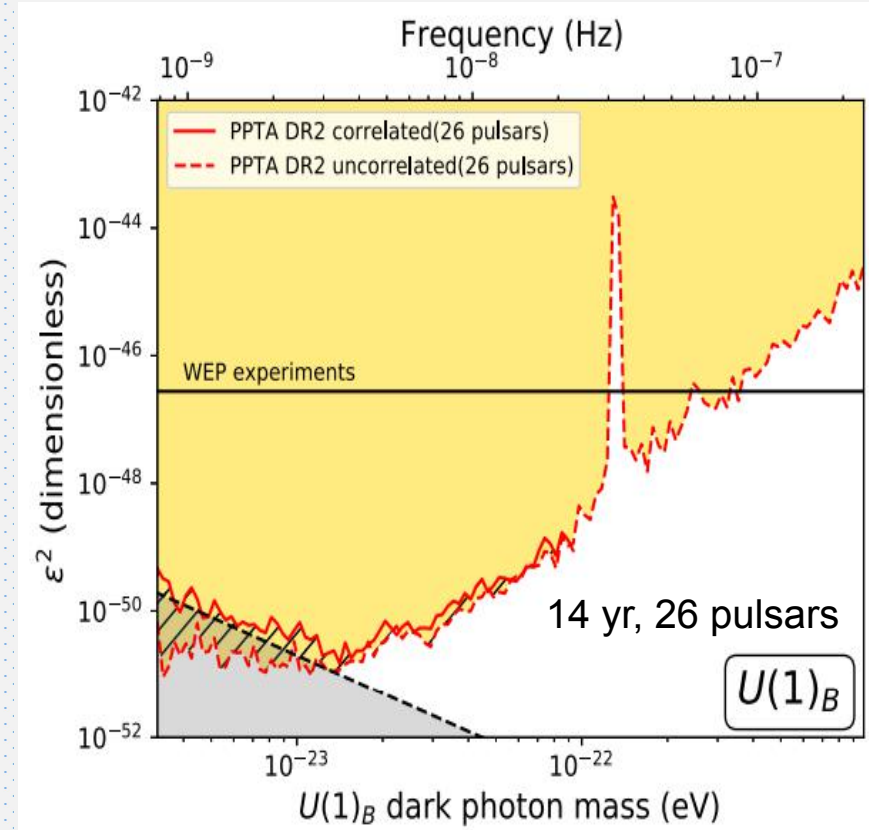


PTA Limits

- Even lower frequency -> even lower mass



NANOGrav, ApjL [2306.16219]



PPTA, Xue, et al, PRR [2112.07687]

Summary

GW is a new tool in particle physics studies

- Early universe symmetry breakings (phase transitions)
- Macroscopic solitons (topological and nontopological)
- Dark matter direct detection (environmental effects)

Thanks!