




中国散裂中子源  
Chinese Spallation Neutron Source

Presentation on MELODY 2023 Workshop  
Nov. 4~6, 2023, Dongguan, China

# Physical Design and Simulation Study of Searching for MuMubar on MELODY

A decorative graphic consisting of four grey chevron arrows pointing to the right, arranged in a horizontal row.

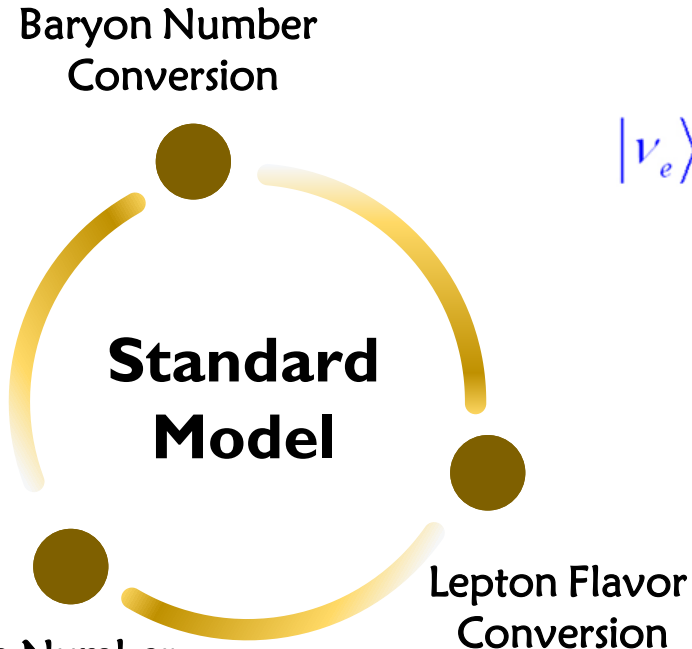
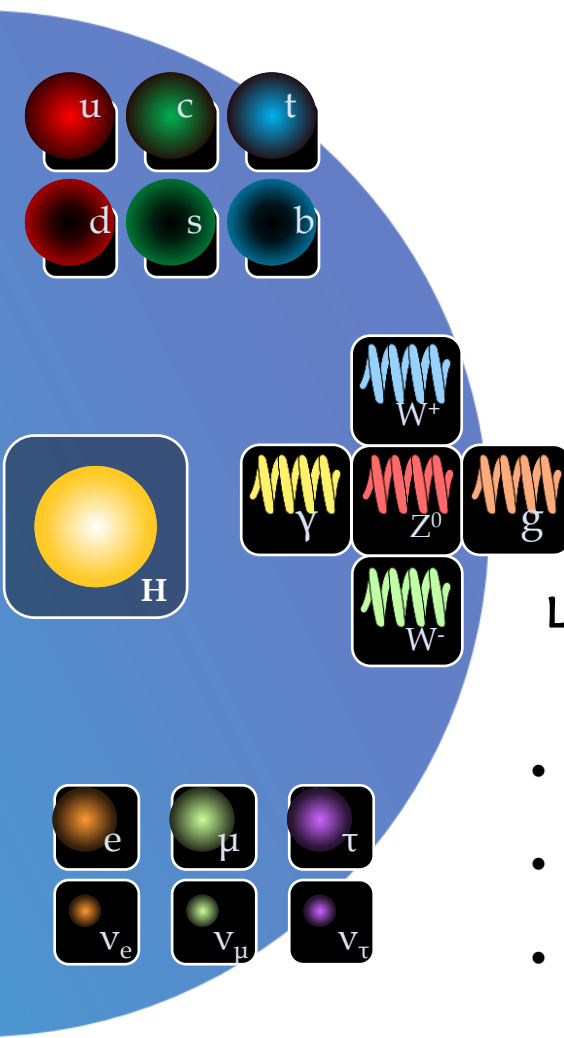
**Yuhang Guo, Yu Bao**  
**2023. 11. 06**

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2. The MACS and a Novel MuMubar Spectrometer
3. Simulation Study of Novel MuMubar Spectrometer
4. Sensitivity Analysis on Searching for MuMubar with MELODY
5. Discussion and Summary

# 1.1 The cLFV prediction



- $\mu^+ \rightarrow e^+ \nu_e \bar{\nu}_\mu$
- $\mu^+ \rightarrow e^+ \nu_e \bar{\nu}_\mu \gamma$
- $\mu^+ \rightarrow e^+ e^+ e^- \nu_e \bar{\nu}_\mu$

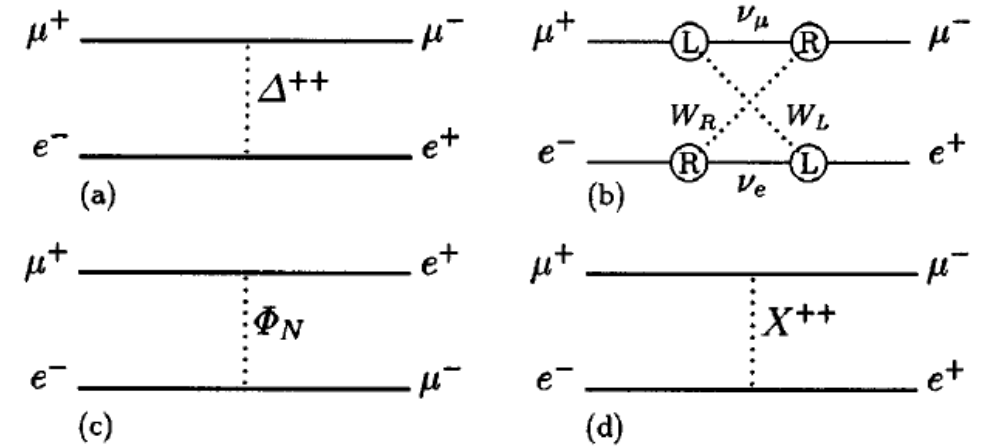
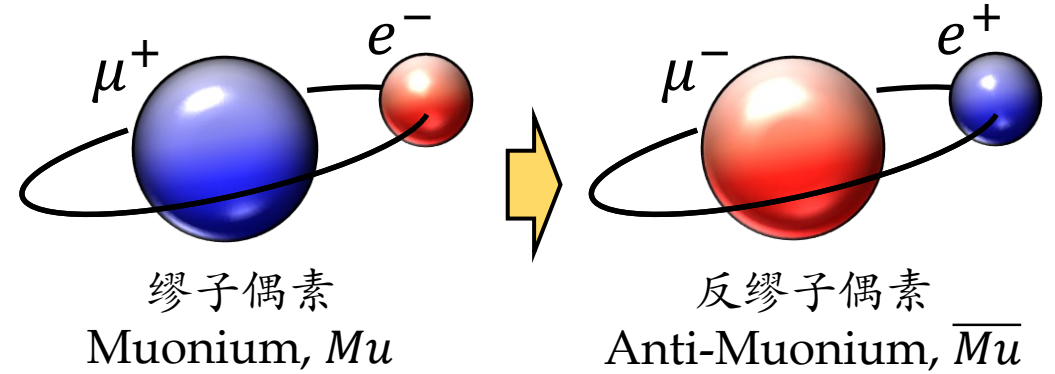
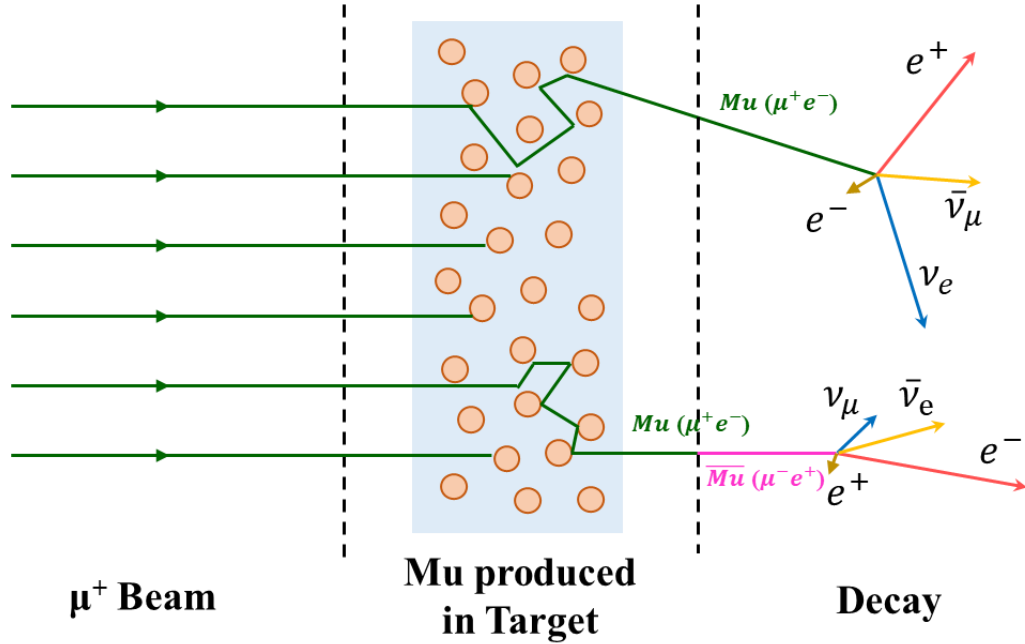
$$|\nu_e\rangle = \begin{matrix} \nu_1 \\ \nu_2 \\ \nu_3 \end{matrix} = c_1 |\nu_e\rangle + c_2 |\nu_\mu\rangle + c_3 |\nu_\tau\rangle$$

- Neutrino Oscillation indicated Neutral Lepton Flavor Violation.
- However, charged Lepton Flavor Violation (cLFV) is not observed so far.
- Searching for cLFV is an interesting topic.



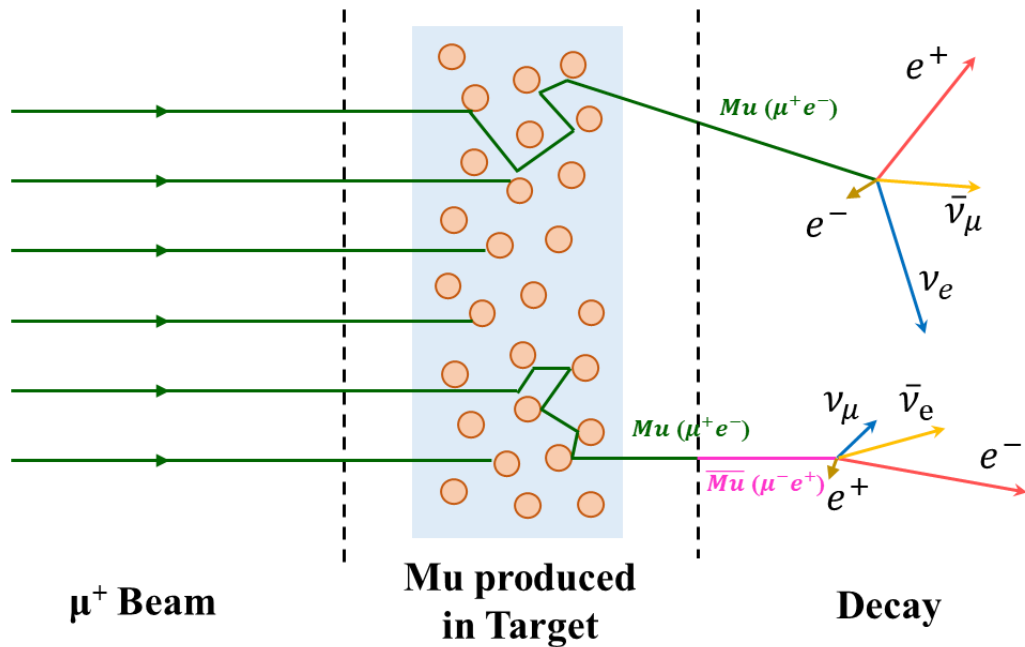
- $\mu^+ \rightarrow e^+ e^+ e^-$
- $\mu^+ \rightarrow e^+ \gamma$
- $\mu^- N \rightarrow e^- N$
- $\mu^+ e^- \rightarrow \mu^- e^+$

# 1.2 What is MuMubar?

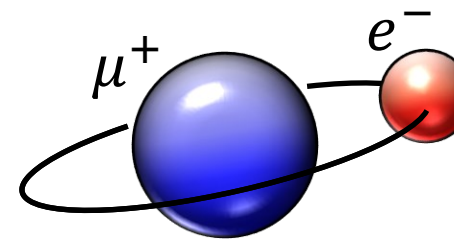


- MuMubar is one of possible way of cLFV.
- By capturing a  $e^-$ ,  $\mu^+$  would become to muonium.
- Muonium might become to Anti-muonium if muon and electron exchange charge.
- Lepton flavor doesn't conserve in this progress. 2 units of lepton flavor are violated.

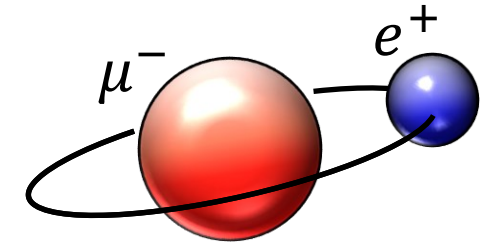
# 1.3 How to Search for MuMubar?



Normal Progress



繆子偶素  
Muonium,  $Mu$



反繆子偶素  
Anti-Muonium,  $\bar{M}u$

MuMubar

Track Electron  $E_k = 13.5 \text{ eV}$

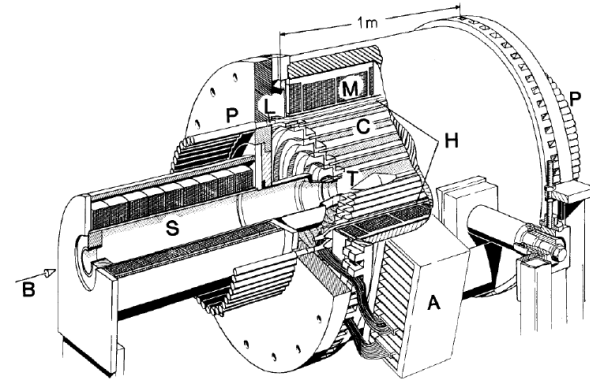
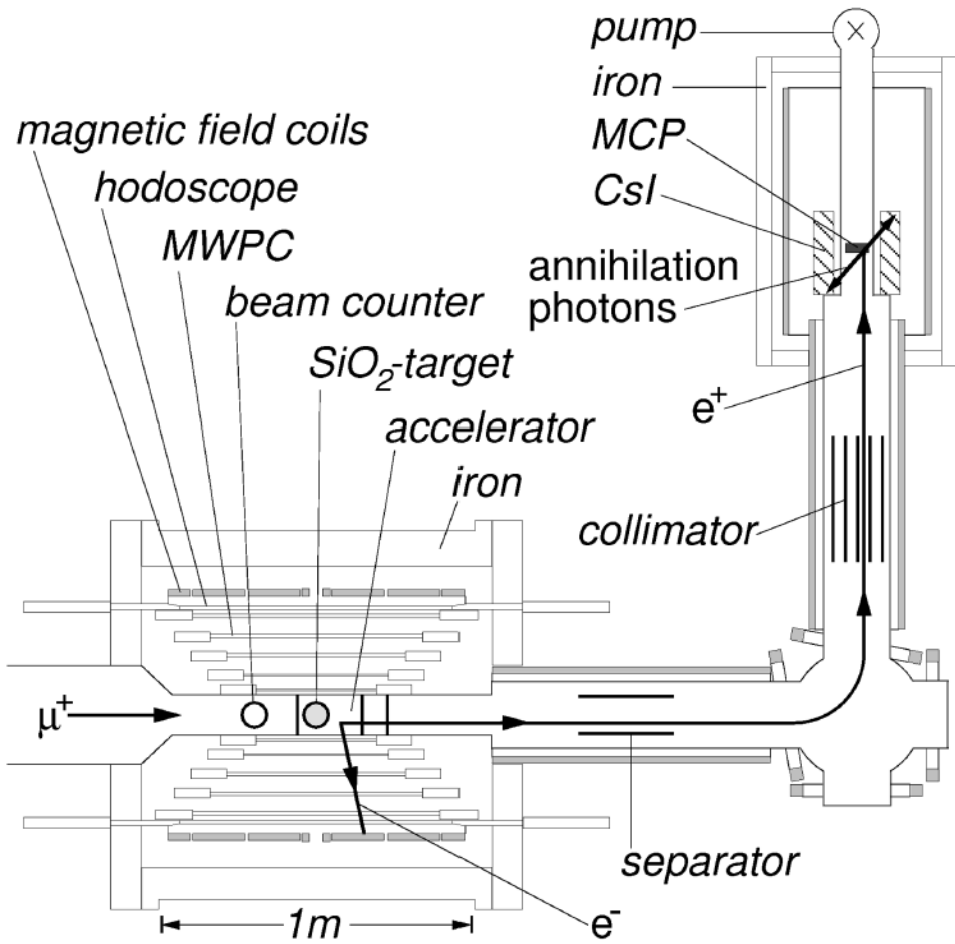


- $Mu$  and  $\bar{M}u$  are unstable and will decay.
- Their decay products owns opposite charges.
- Searching for MuMubar is searching for the decay products with  $\bar{M}u$  decay characteristics.

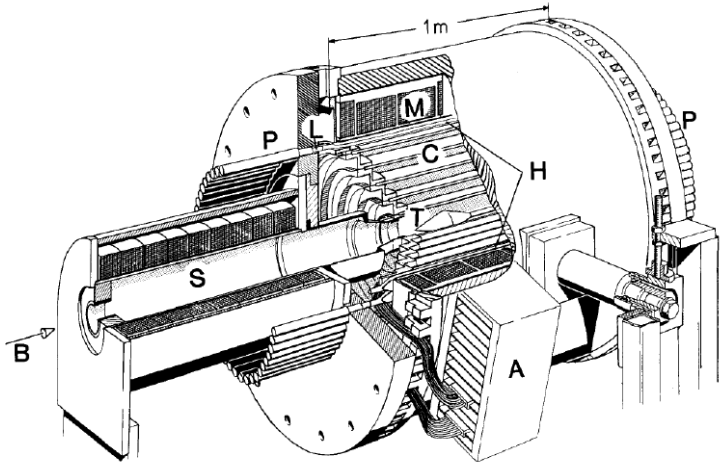
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  - 2.3 Physical Design of Novel MuMubar Spectrometer
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4. Sensitivity Analysis on Searching for MuMubar with MELODY
5. Discussion and Summary



- MACS, 1998, @PSI-πe5,  $8 \times 10^6 \mu/s$ , CM
- **Decay Electron Spectrometer (DES):**
  - MWPC + Scintillator + 0.1 T Mag Field
- **Track Electron Spectrometer (TES):**
  - MCP + Scintillator
- 0.1 T Mag Field guide track electron to TES
- $P < 8.3 \times 10^{-11}$  with 180 days observing.



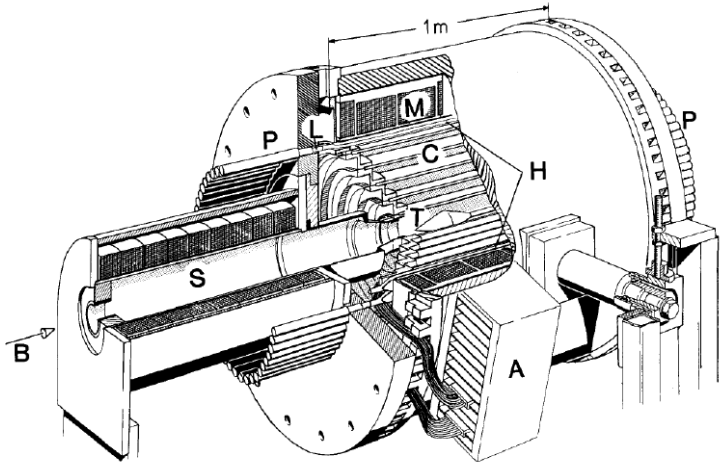
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### More Muon Exposure

- Longer observing time
  - 180 days to 3 years
- More intensive muon source
  - $8 \times 10^6 \mu/s$  to  $10^{10} \mu/s$



## 2.2 Ways to improve MACS – spectrometer



- MACS, 1998, @PSI-πe5,  $8 \times 10^6 \mu/s$ , CM
- Decay Electron Spectrometer (DES):
  - MWPC + Scintillator + 0.1 T Mag Field
- Track Electron Spectrometer (TES):
  - MCP + Scintillator
- 0.1 T Mag Field guide track electron to TES
- $P < 8.3 \times 10^{-11}$  with 180 days observing.

### More Muon Exposure

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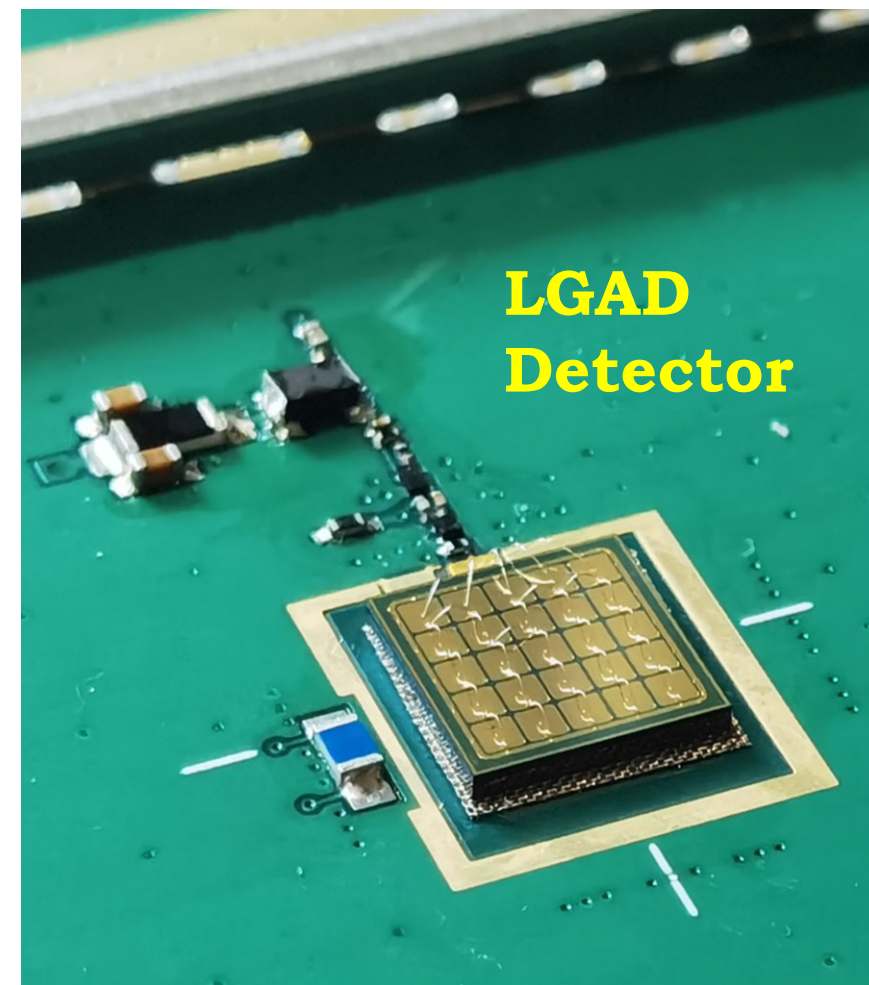
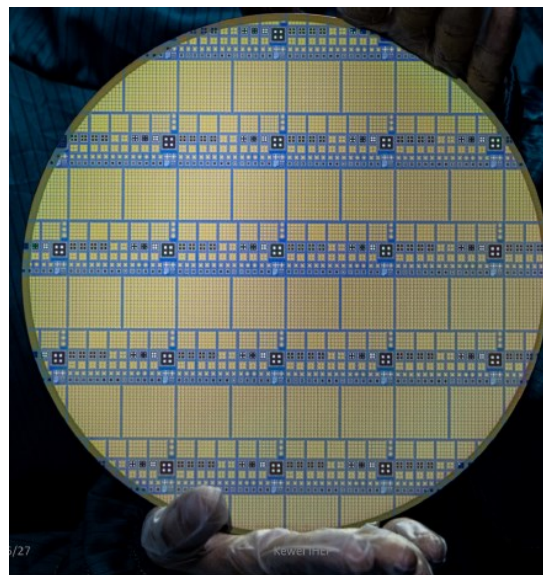
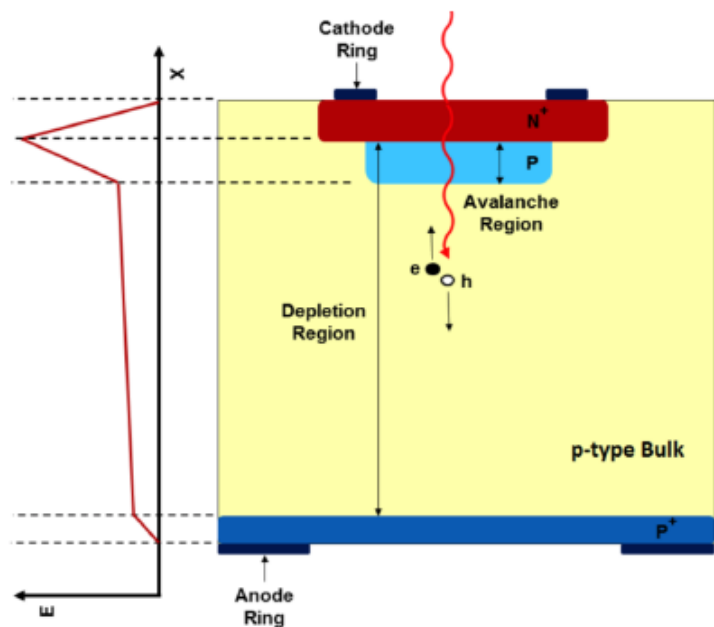
### More Sensitive Detector

- Need a detector with:
  - Excellent timing sensitivity.
  - Small mass budget.

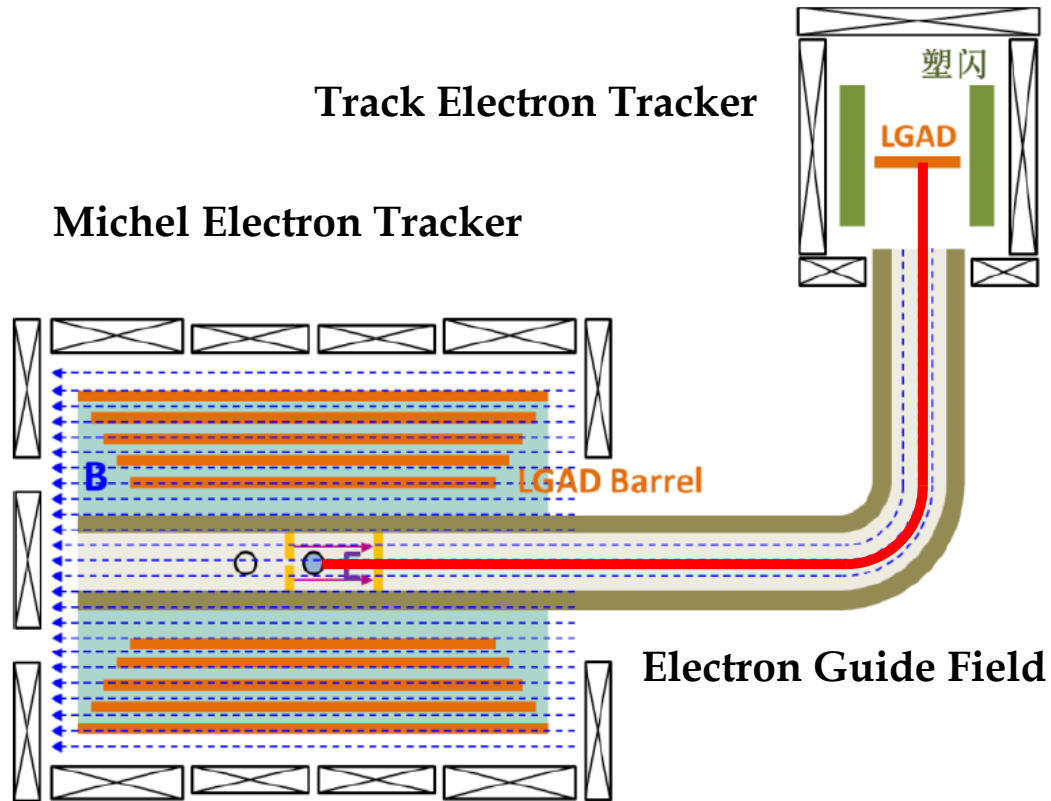
# 2.2 Ways to improve MACS – LGAD

- Low Gain Avalanche Diode (LGAD).
- Developed for ATLAS and CMS.

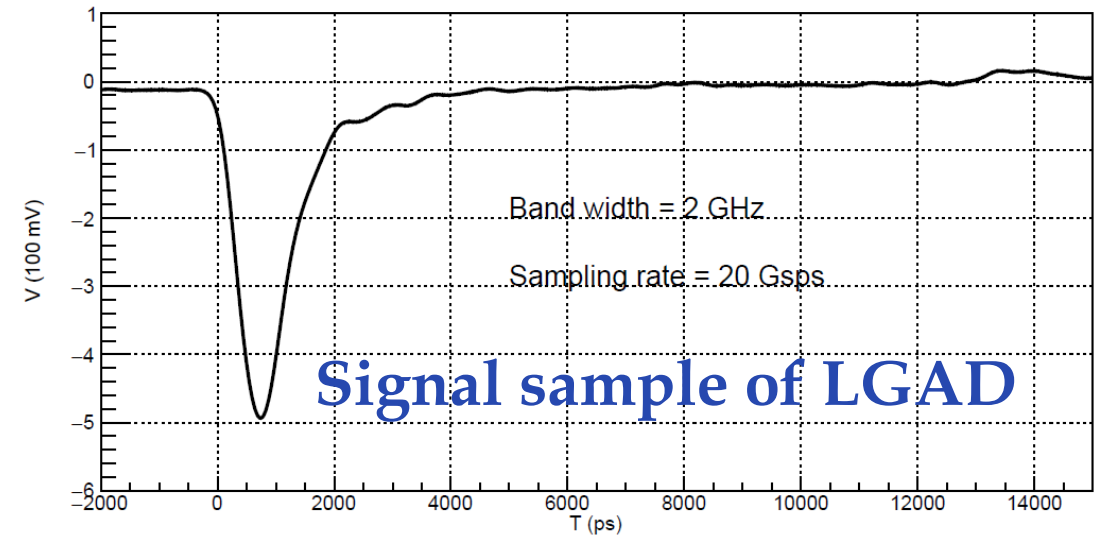
Depth	Signal Width	Temporal Res.	Seperation Size
50 $\mu$ m	2~3ns	30 ps	1.3 $\times$ 1.3 mm <sup>2</sup>



## 2.3 Physical Design of Novel MuMubar Spectrometer



Construction of Novel MuMubar Spectrometer  
(Not to scale)



- Replace the MWPC with LGAD as the Michel Electron Tracker (MET).
- The Advantages:
  - 2 order of magnitude better on temporal resolution.
  - High feasibility, no risk of strike.

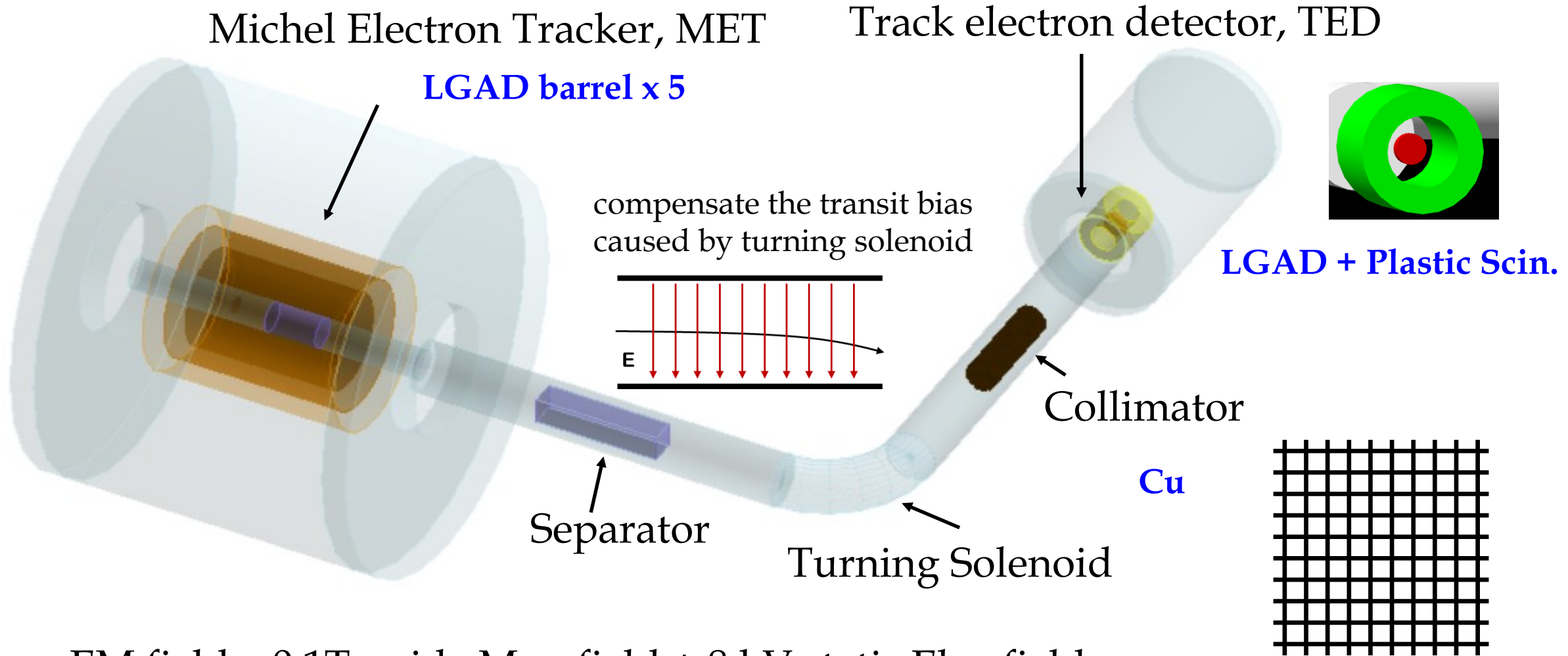
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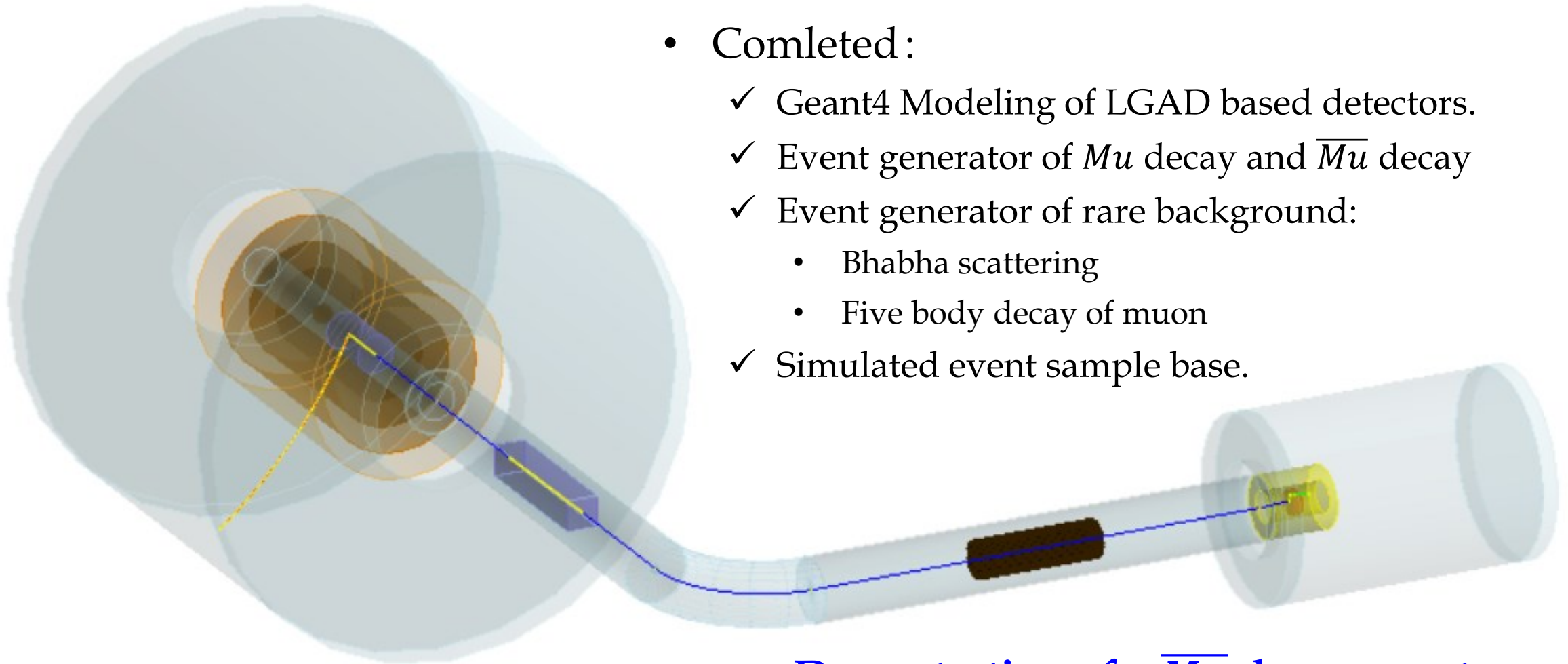
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  - 3.2 Event Reconstruction
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# 3.1.1 Geant4 Modeling

Based on MACS



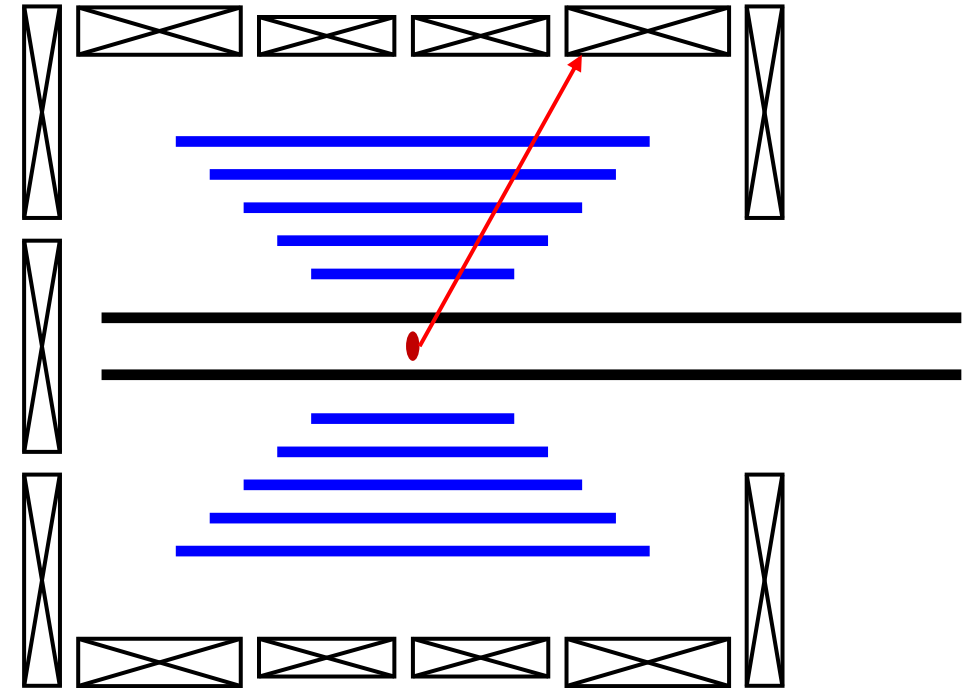
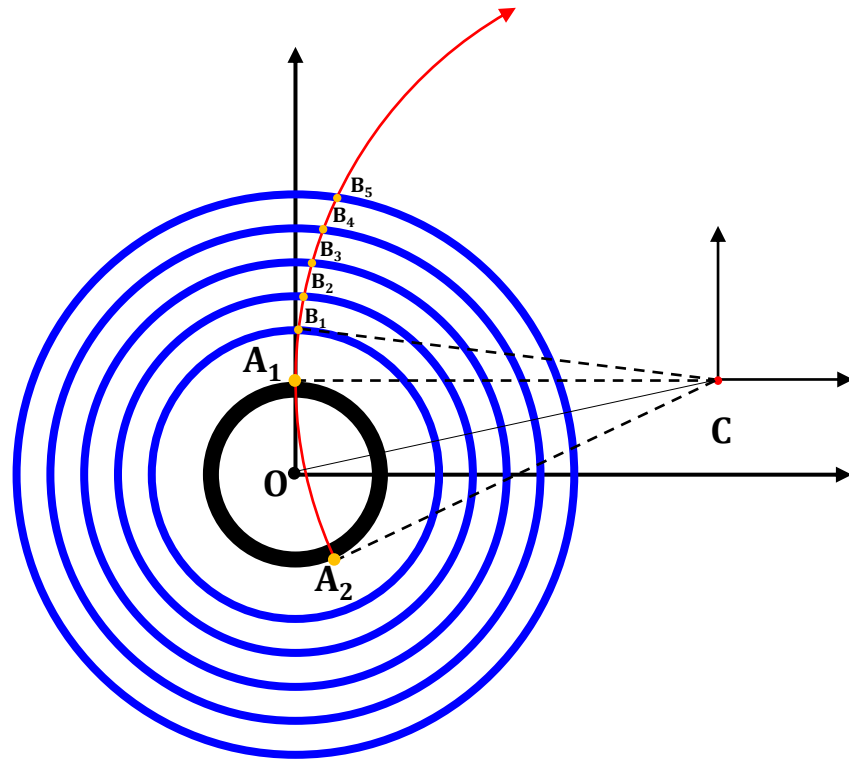
- EM field: 0.1T guide Mag-field + 8 kV static Elec-field



- Completed:
  - ✓ Geant4 Modeling of LGAD based detectors.
  - ✓ Event generator of  $Mu$  decay and  $\overline{Mu}$  decay
  - ✓ Event generator of rare background:
    - Bhabha scattering
    - Five body decay of muon
  - ✓ Simulated event sample base.

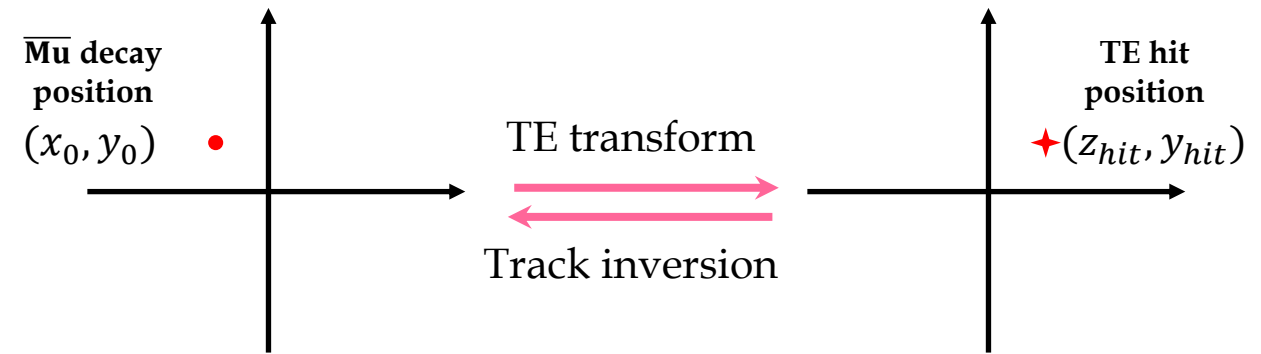
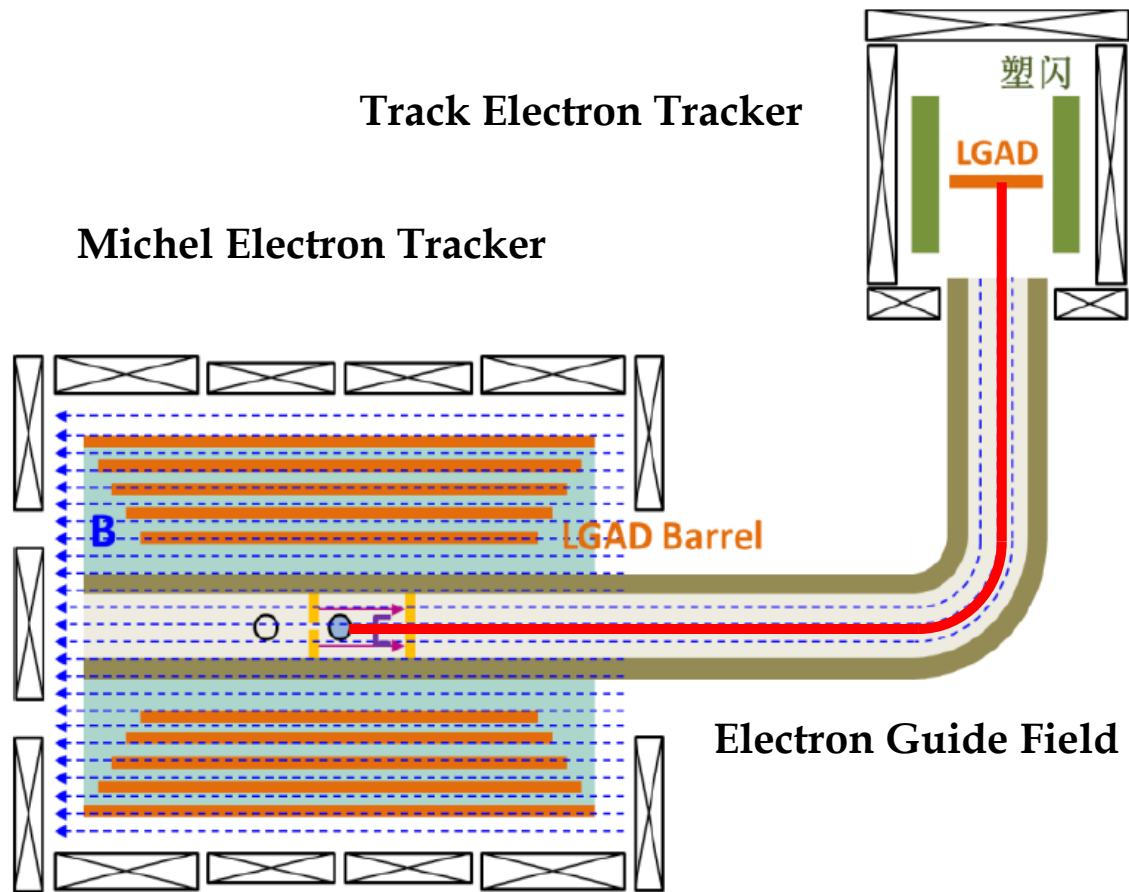
**Demostration of a  $\overline{Mu}$  decay event**

# 3.2.1 DE track reconstruction



The decay electron is reconstructed by the hits on MET barrels.

# 3.2.2 TE Track Reconstruction



The TE track is reconstructed by the inversion of hit on TE detector



# 3.3 Performance of the spectrometer



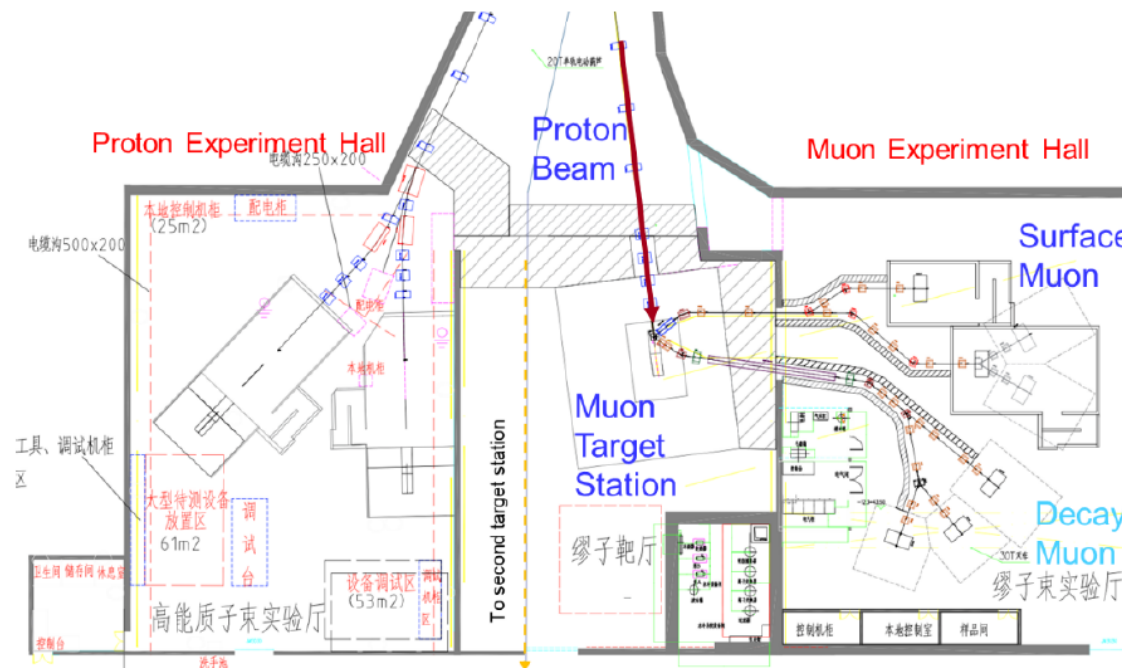
Items		Performance
<b>Michel Electron Tracker (MET)</b>	MET volume efficiency	~76%
	MET positioning resolution	1 mm
	MET hit time resolution	30 ps
<b>Track Electron Guide Tube</b>	Positron transformation efficiency	~80%
<b>Track Electron Detector (TED)</b>	TED detection efficiency	~70%
	TED positioning resolution	1 mm
	TED hit time resolution	30 ps
<b>Electrons vertex reconstruction</b>	Michel electron energy rec resolution	1.6 keV
	Track electron vertex rec resolution in XY	1.3 mm
	Track electron vertex rec resolution in Z	1.6 mm

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  - 4.2 The Piled-up Signals
  - 4.3 The Analysis Software and Algorithm
  - 4.4 Verification to the Reconstruction
  - 4.5 Selection Criteria and Preliminary Result
5. Discussion and Summary

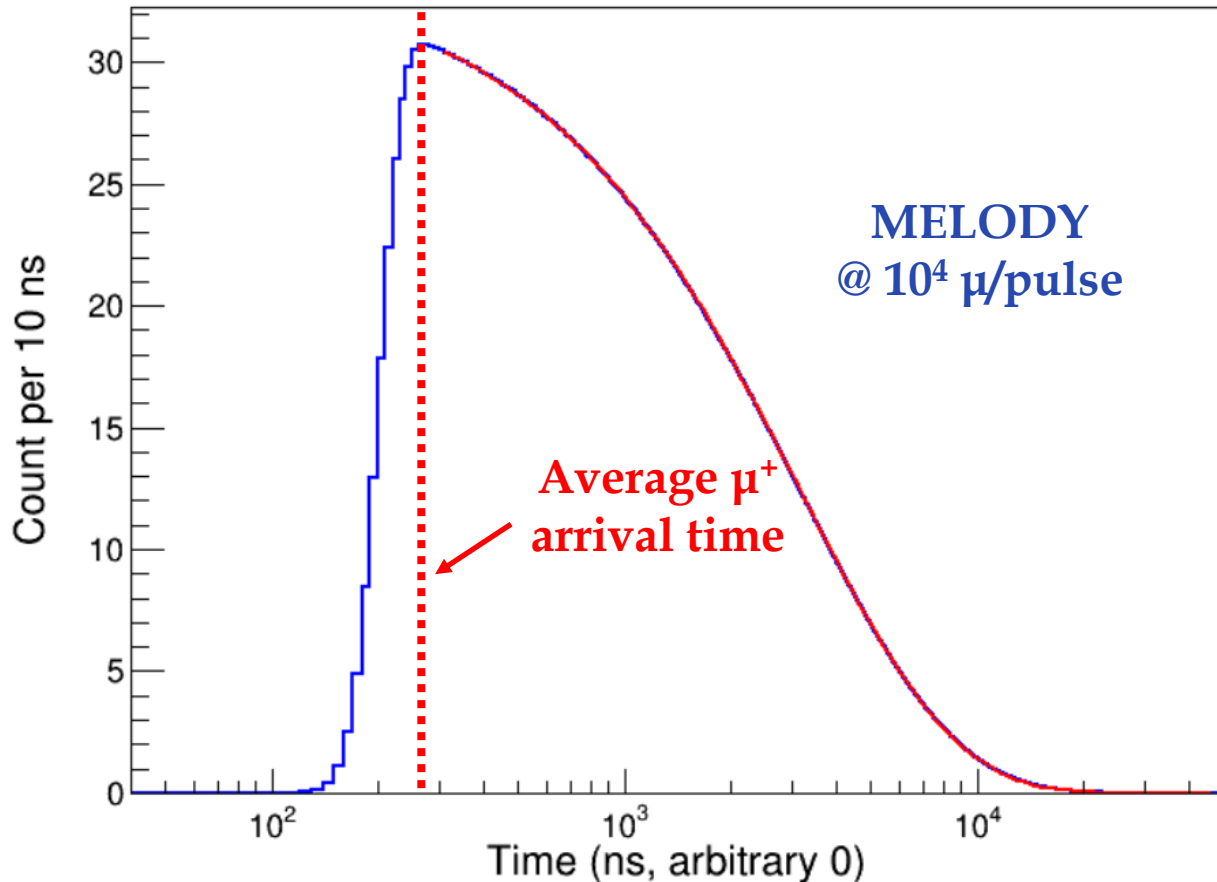
# 4.1 The MELODY



Parameters	Values
Pulse Frequency	1Hz
$\mu$ rate in single pulse	$10^5 \sim 10^7$ , adjustable
Full width of single pulse	150 ns

- One of the test beam to be built in CSNS-II project.
- Pulsed surface muon source, 1Hz.
- We hope to test and tune our spectrometer on MELODY.
- Deal with the pile-up signals applying intensive  $\mu$  source.

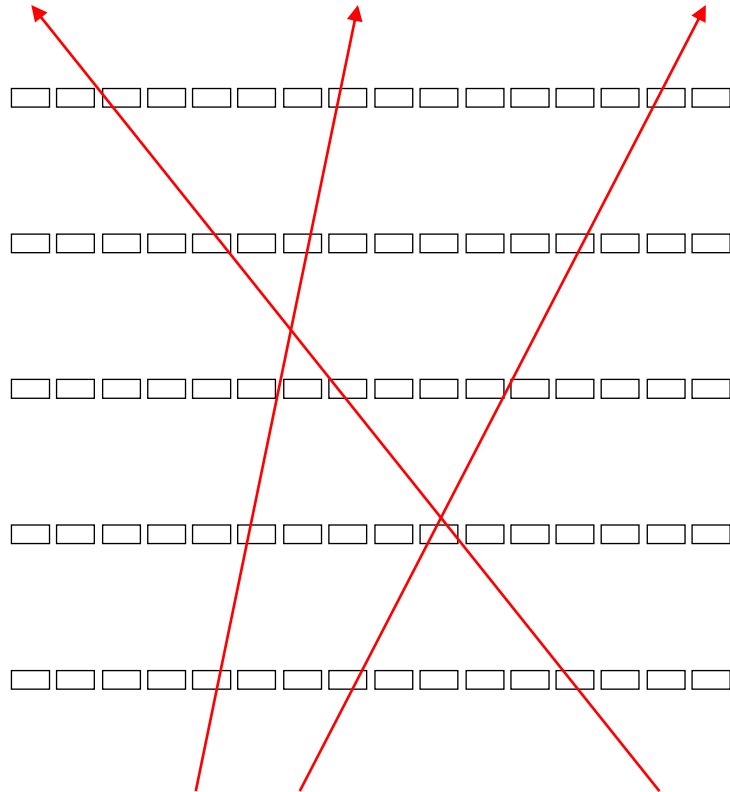
## Time of Michel Electron Produced



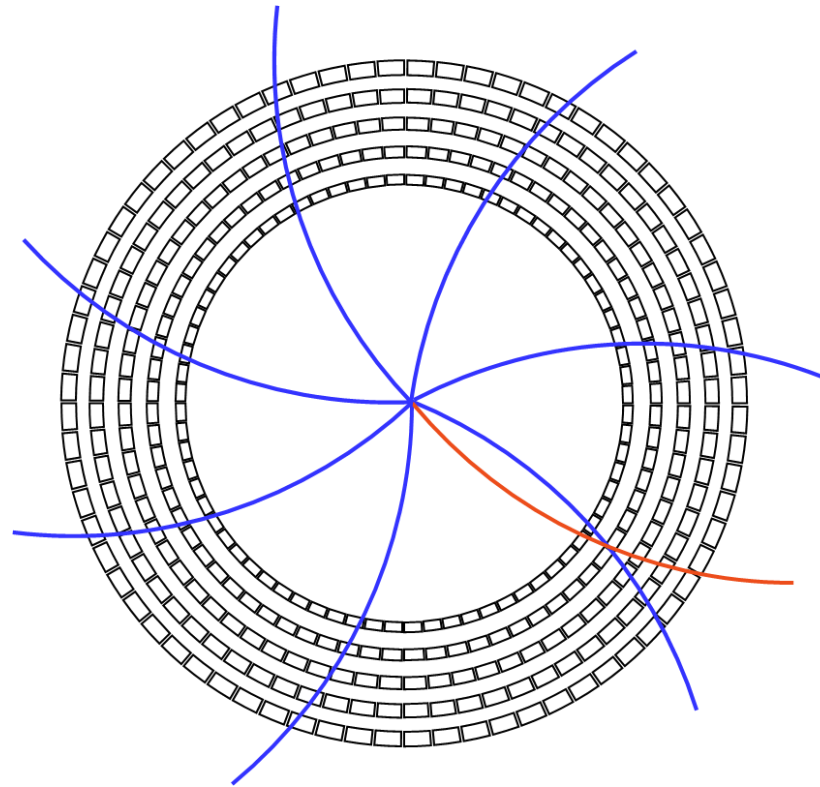
- Signals of Michel electron are too intensive, and pile up on the MET.
- Have to find the  $e^-$  from the massive  $e^+$  signals.
- The gaseous detectors will be blind in this condition.
- The LGAD can provide high temporal resolution measurement, which is necessary to discriminate the massive piling up signals.
- **This is an important issue in this study.**

# 4.3.1 Steps to Resolve the Piled-up Signals

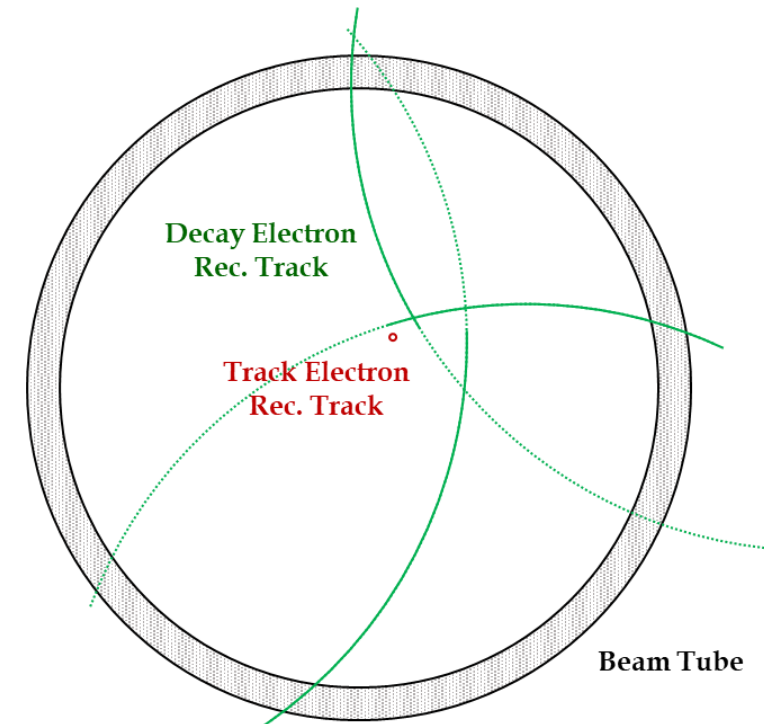
## Track Separation



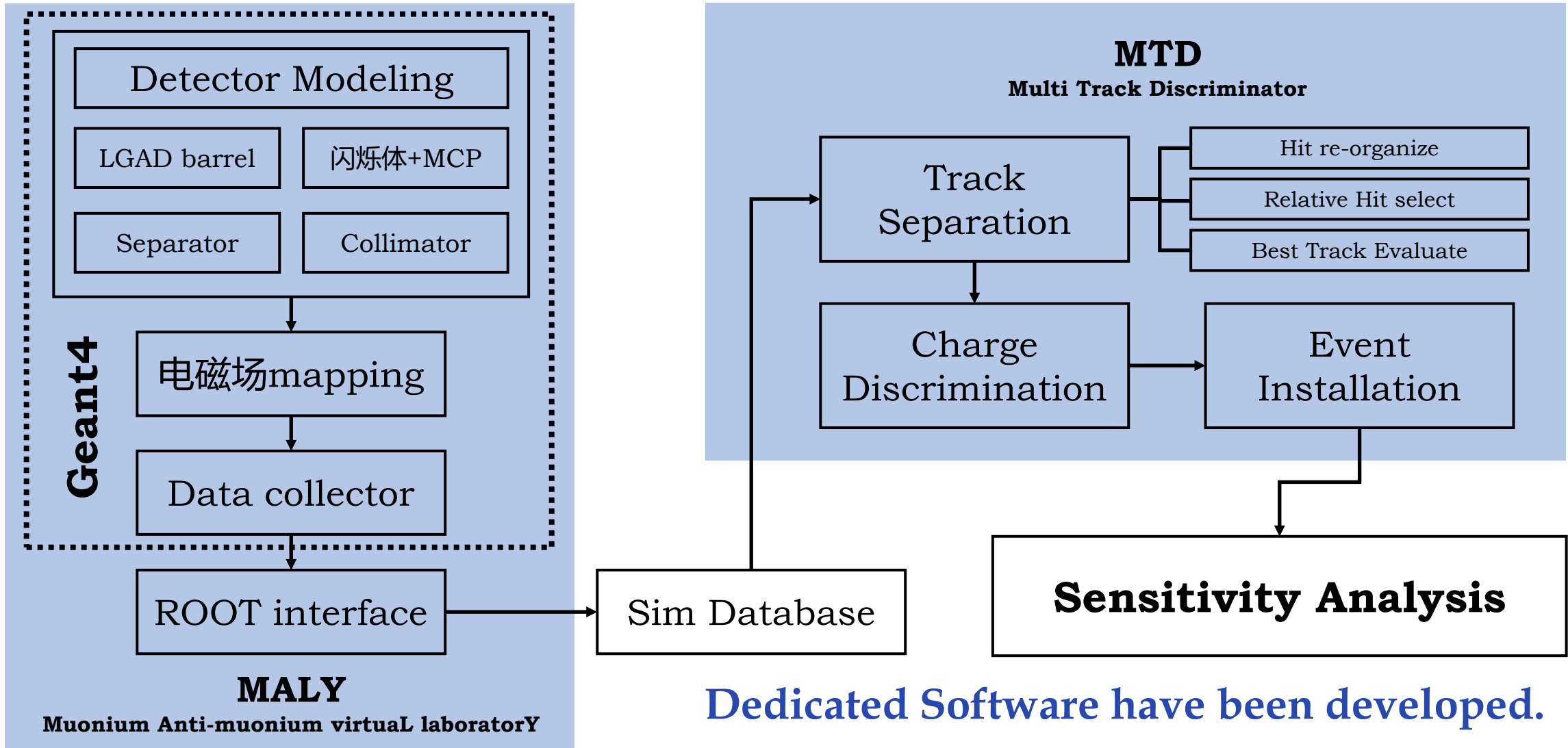
## Charge Discrimination



## Event Installation

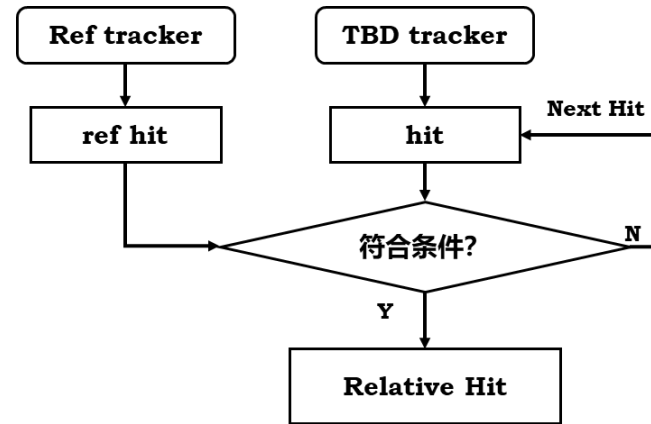
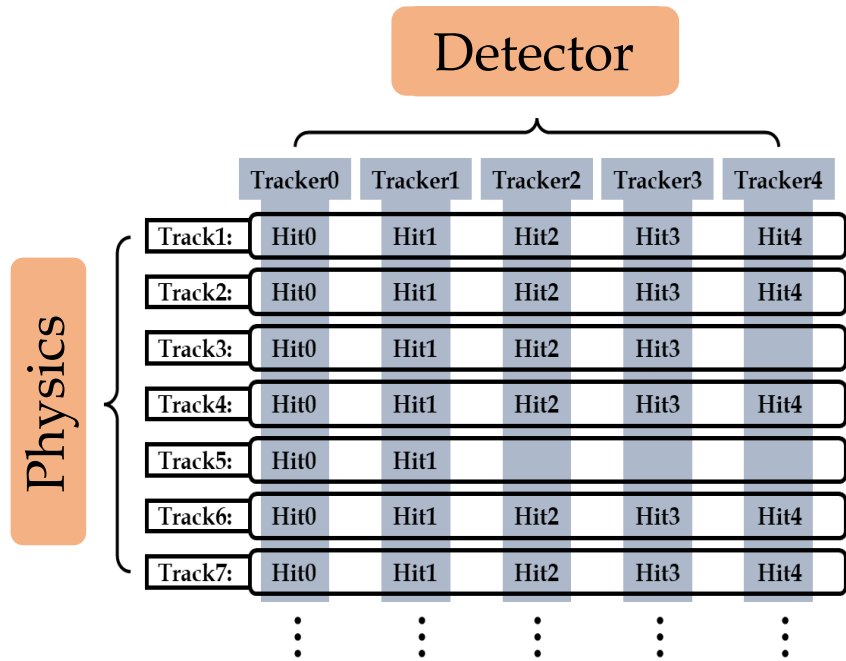


# 4.3.2 The Analysis Software

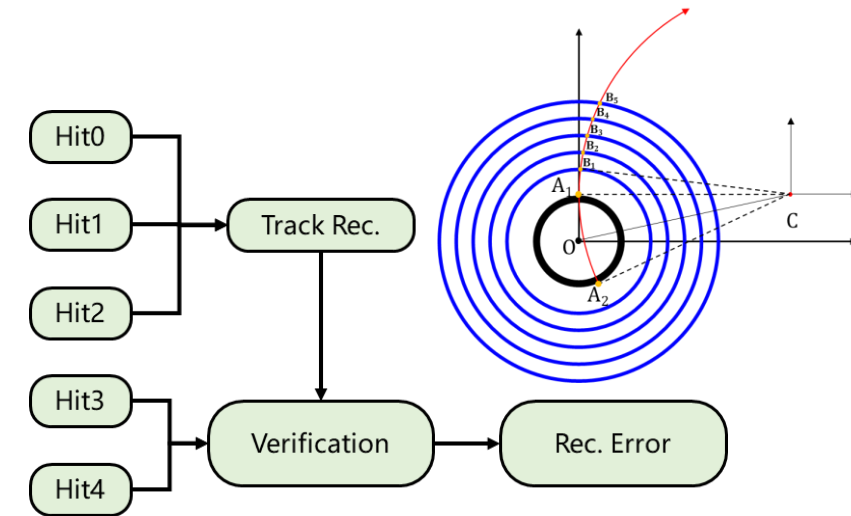


Dedicated Software have been developed.

# 4.3.3 The Analysis Algorithm



- $0 < \text{hitT} - \text{refT} < 1.5 \text{ ns}$
- $-15 \text{ deg} < \text{hit}\phi - \text{ref}\phi < 15 \text{ deg}$



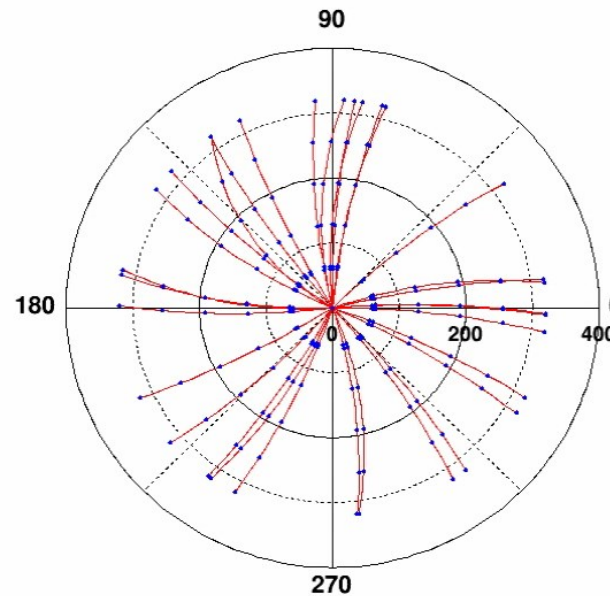
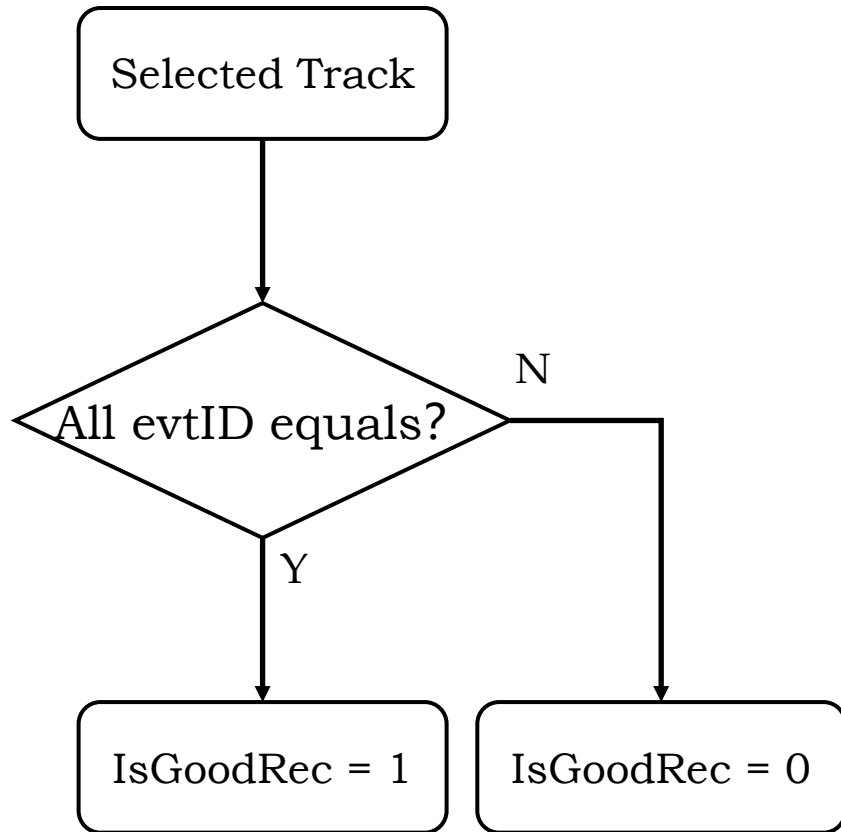
$$FOM_{rec} = \sqrt{\sum_{i=0}^{nHit} \frac{(Dist_i - R)^2}{nHit} + \sum_{i=0}^{nHit-1} \frac{(Z_i - Z_{trk})^2}{nHit - 1}}$$

Transform MC to DET data

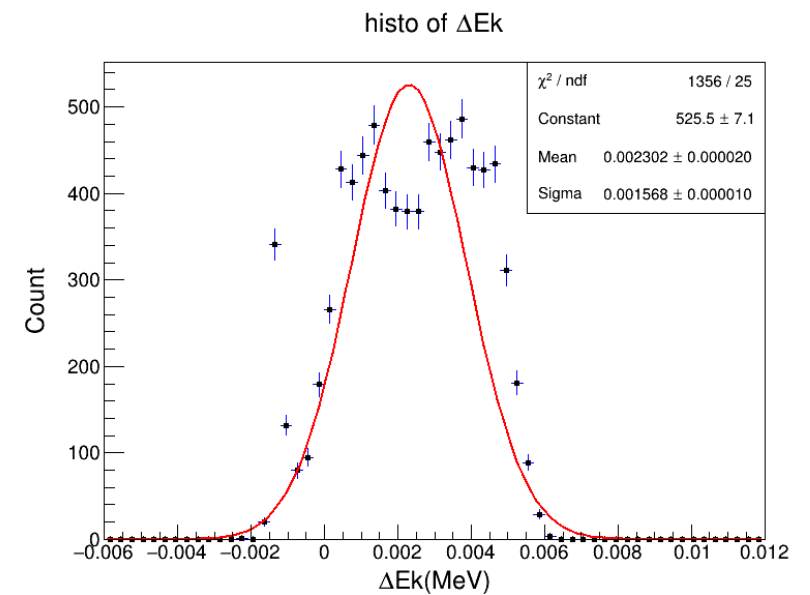
Find the correlated hits

Select the best Rec. track

- The selected best rec. tracks are verified by event ID (MC truth).



The Michel electron tracks are 100% well reconstructed

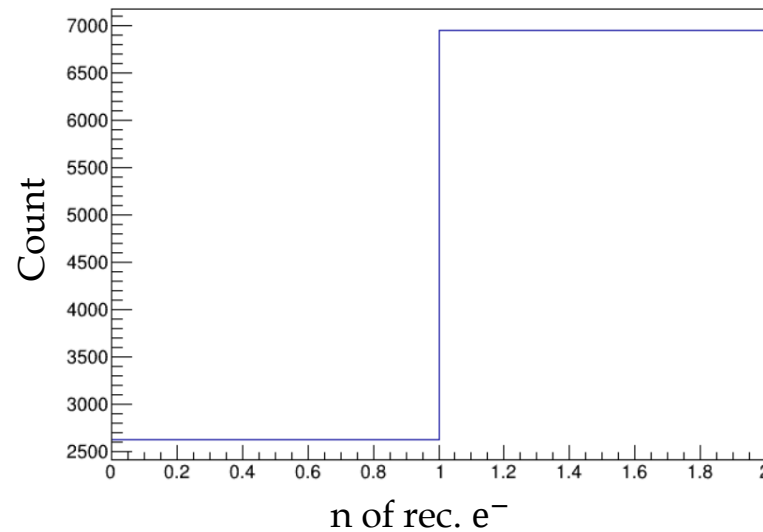
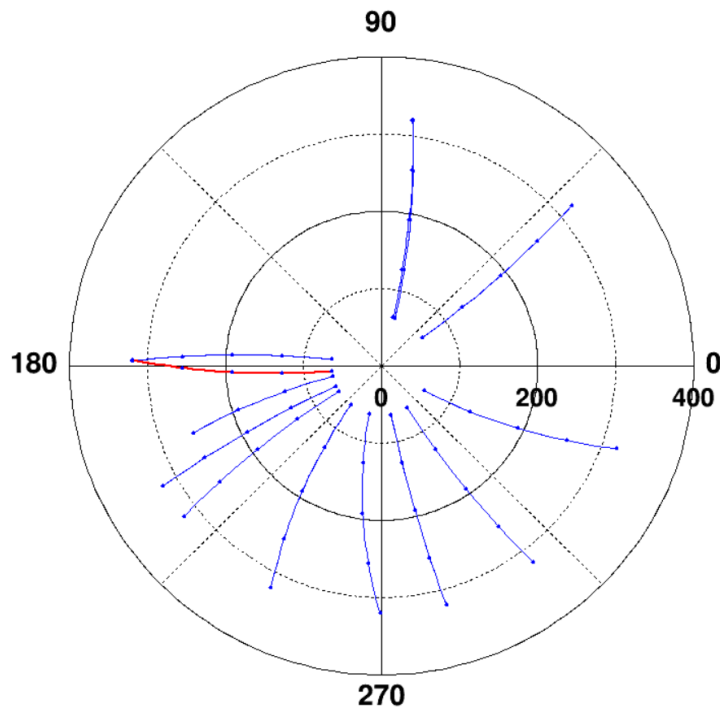


Rec. Michel electron  $E_k$   
Bias: 2.3 keV, Res. 1.6 keV

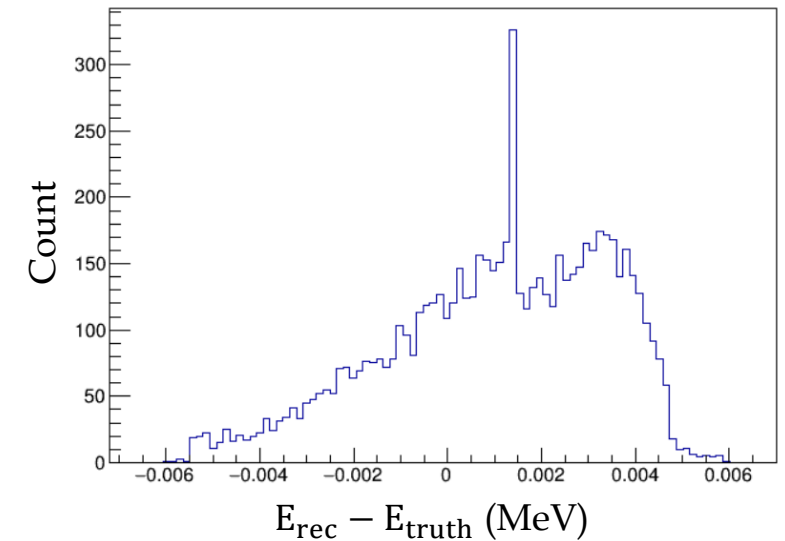


# 4.4 Verification to the Reconstruction

- (One  $\overline{Mu}$  decay + 10000  $Mu$  Decay)  $\times$  9576 pulse.
- Totally 6945 in 7289  $e^-$  tracks are successfully reconstructed. Eff = 95%.



**Negative M.E.**  
**Rec. eff. = 95%**



**Negative M.E.**  
**Ek Rec. res. = 2.1 keV**

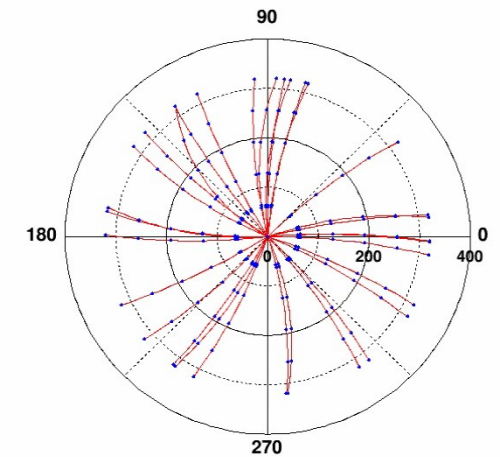
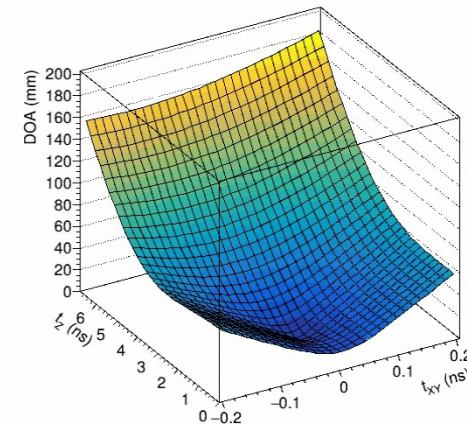
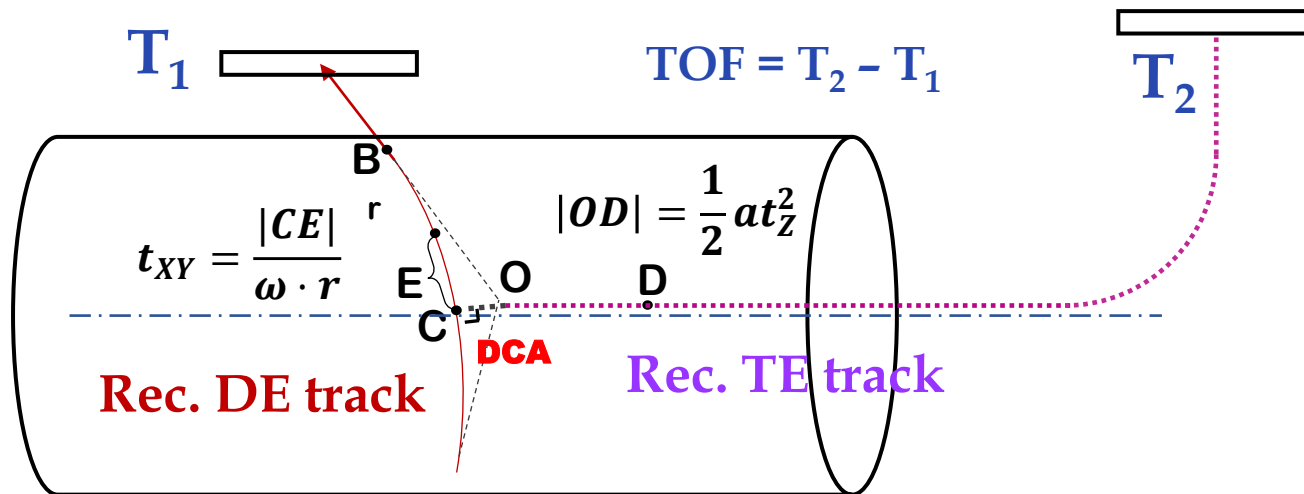
# 4.5.1 Selection Criteria

• Two Key criteria to suppress background :

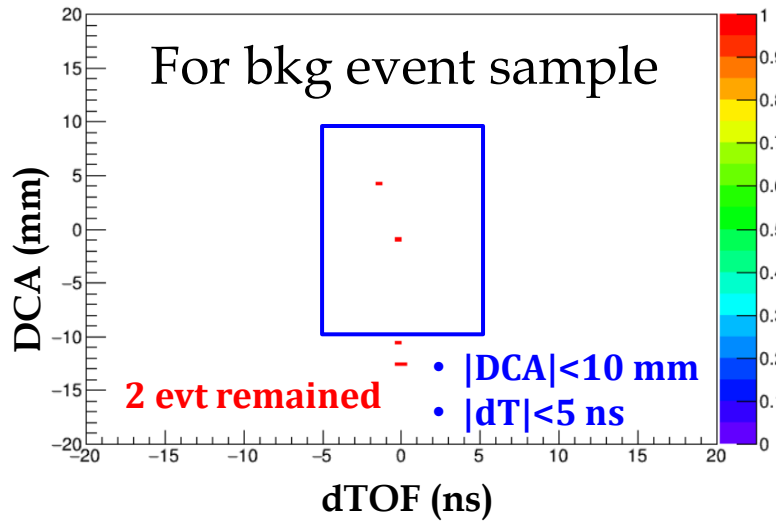
- Distance of Closest Approach (DCA)
- Time of TE flight (TOF)

1. Bhabha Scattering

2. Five Body Decay of Muon

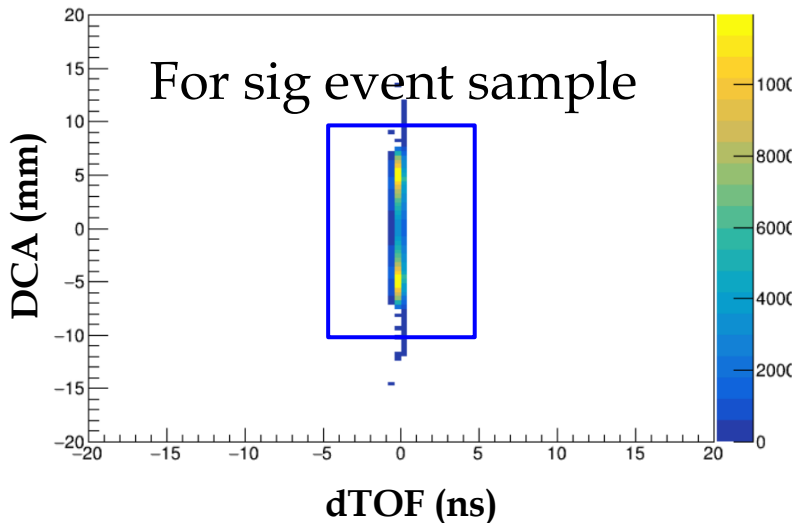


# 4.5.2 Preliminary Result of Analysis



## Criteria:

- nMWPCHit==5
- nMCPHit==1
- 1<=nCsIHit<=2
- CsIHitT<200
- CsIHitT-MCPHitT>0
- CsIHitT-MCPHitT<6
- CsIHitEk>0.4
- CsIHitEk<0.6



$$S = \frac{N_{90}}{N \cdot \varepsilon}$$

Parameters	Value
Detection Efficiency	39%
5-body bkg remained	2
Bhabha bkg remained	0
Equivalent observing time (year)	147 for 5-body bkg; 20 for Bhabha bkg;
Equivalent Bkg. Level	0.014

## • Sensitivity by Feldman-Cousins Approach:

- $N_{90}$ , 90% C.L. upper limit (0 obs).
- $N$ , total count of Mu decay event.
- $\varepsilon$ , the detection efficiency.

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- What sensitivity can we get on MELODY?
- Assumptions:
  - $1 \times 10^4$   $\mu$ /pulse, 1Hz repetition.
  - 3 years data taking,  $2 \times 10^7$  s per year.
  - Spectrometer running stably.
  - 5% free muonium producing efficiency.

**$2.1 \times 10^{-10}$  in 90% C.L.**  
**( $8.3 \times 10^{-11}$  of MACS)**

I ( $\mu$ /s)	Time	Free Mu Exposure	Detection Efficiency	Background Level	Sensitivity (90% C.L.)
$1 \times 10^4$	$6 \times 10^7$ s	$3 \times 10^{10}$	~39%	0.02	$2.1 \times 10^{-10}$
$1 \times 10^5$	$6 \times 10^7$ s	$3 \times 10^{11}$	~39%	If 0	$2.1 \times 10^{-11}$

# 5.1 Discussion



- Could it perform better if a larger repetition muon source is applied?
- Assumptions:
  - $1 \times 10^4$   $\mu$ /pulse, **1 kHz repetition**.
  - 3 years data taking,  $2 \times 10^7$  s per year.
  - Spectrometer running stably.
  - 5% free muonium producing efficiency.
- The intensity will reach  $1E7$   $\mu$ /s. Need more strict criteria to suppress the bkg level to  $\sim 0$ . Detection eff. will surely decrease.

I ( $\mu$ /s)	Time	Free Mu Exposure	Detection Efficiency	Background Level	Sensitivity (90% C.L.)
$1 \times 10^7$	$6 \times 10^7$ s	$3 \times 10^{13}$	If $\sim 25\%$	If $\sim 0$	$3.3 \times 10^{-13}$
$1 \times 10^7$	$6 \times 10^7$ s	$3 \times 10^{13}$	If $\sim 25\%$	If $\sim 1$	$4.1 \times 10^{-13}$
$1 \times 10^7$	$6 \times 10^7$ s	$3 \times 10^{13}$	If $\sim 25\%$	If $\sim 2$	$5.2 \times 10^{-13}$

- A preliminary design of novel MuMubar spectrometer has been proposed based on LGAD detector.
- The design has been studied by Geant4 simulation. Reconstruction Algorithms have been setup and tested:
  - Decay electron (DE) and Track electron (TE) track reconstruction.
  - Piled up Michel Electron track separation and reconstruction.
  - DE-TE installation under intensive muon source
- The detection efficiency is 39% and the background level is 0.014.
- For 3 years ( $2 \times 10^7$  s/y) observing on MELODY, the sensitivity is estimated to reach  $2.1 \times 10^{-10}$  (in 90% C.L.).
- This MuMubar spectrometer design ought to be potential for the future MuMubar experiment with intensive muon source.

*Preliminary*

# 致谢

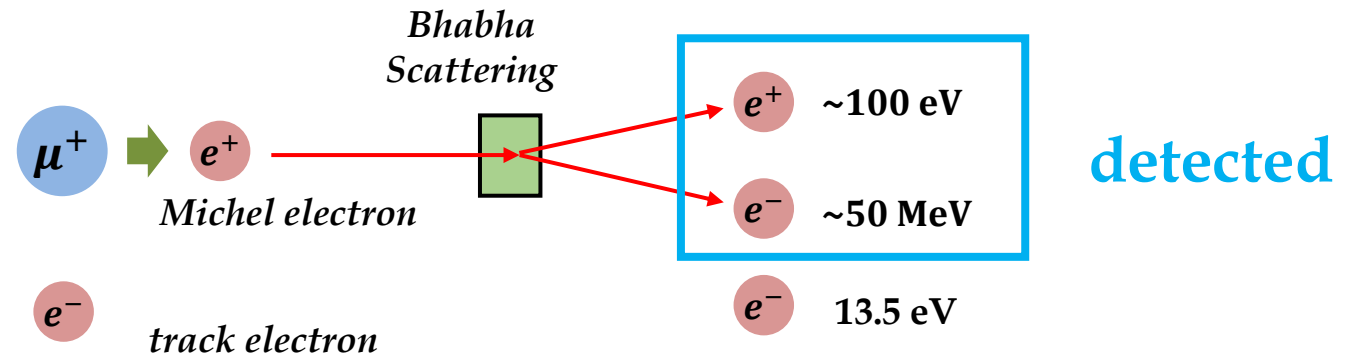
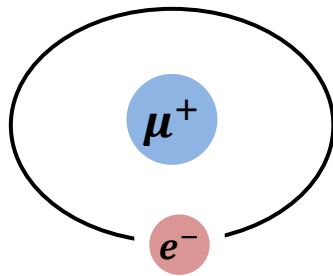


承蒙厚爱  
感谢倾听  
**Thanks!**

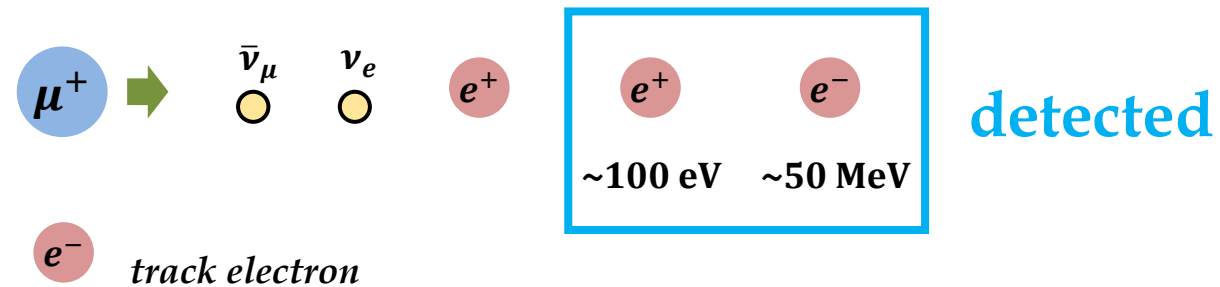
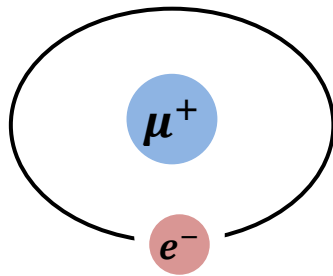


The MuMubar Searching is bothered by two types of Background:

## 1. Bhabha Scattering



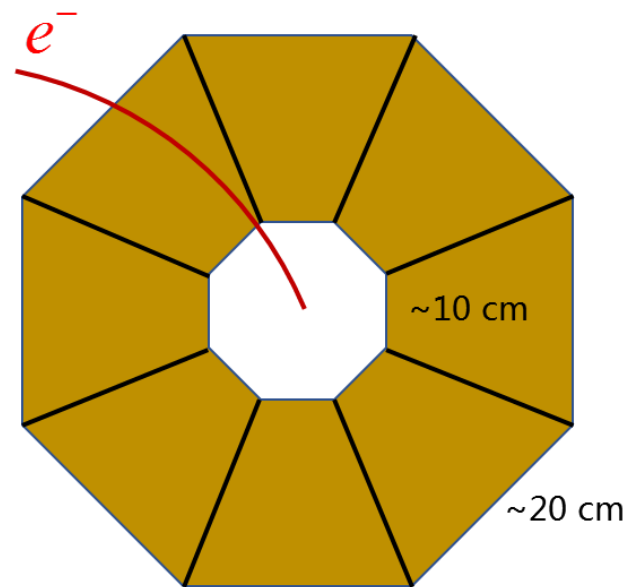
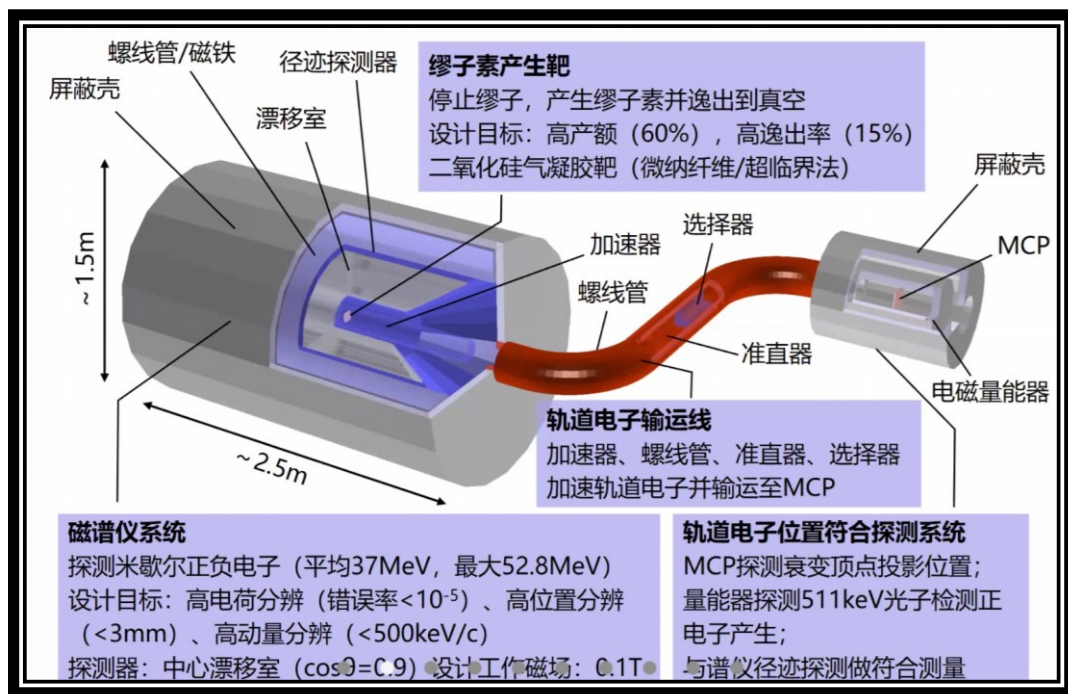
## 2. Five Body Decay of Muon



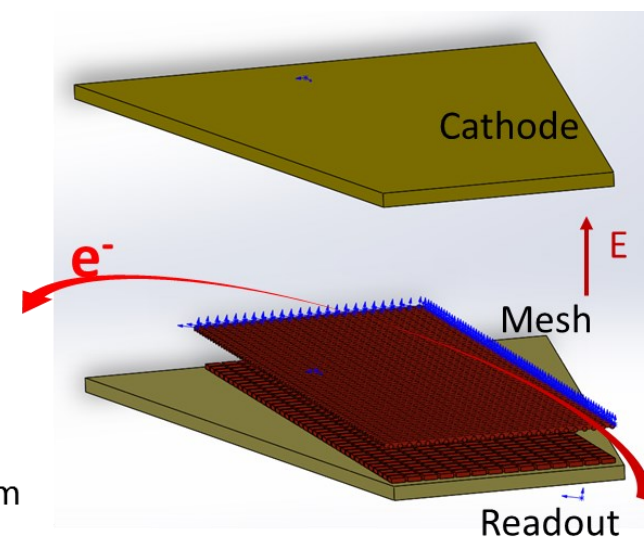
# More Intensive Muon Source

参数	COMET-I	COMET-II	Mu2e
Institute	J-PARC		FNL
Proton pulse width	100 ns	100 ns	700 ns
Proton per pulse	2.9E6	5.12E7	1.02E7
Muon generation efficiency	4.7E-4	4.7E-4	1.9E-3
<b>Muon generation per pulse</b>	<b>1375 <math>\mu</math>/pulse</b>	<b>24570 <math>\mu</math>/pulse</b>	<b>19380 <math>\mu</math>/pulse</b>
Muon Intensity	1.18E9 $\mu$ /s	2.1E10 $\mu$ /s	1.14E10 $\mu$ /s
Time to observe	~150 day	~180 day	~690 day
Total Muon to be observe	1.5E16	1.1E18	6.7E17
CLFV Sensitivity	7E-15	2.6E-17	2.3E-17

## 使用更灵敏的探测装置



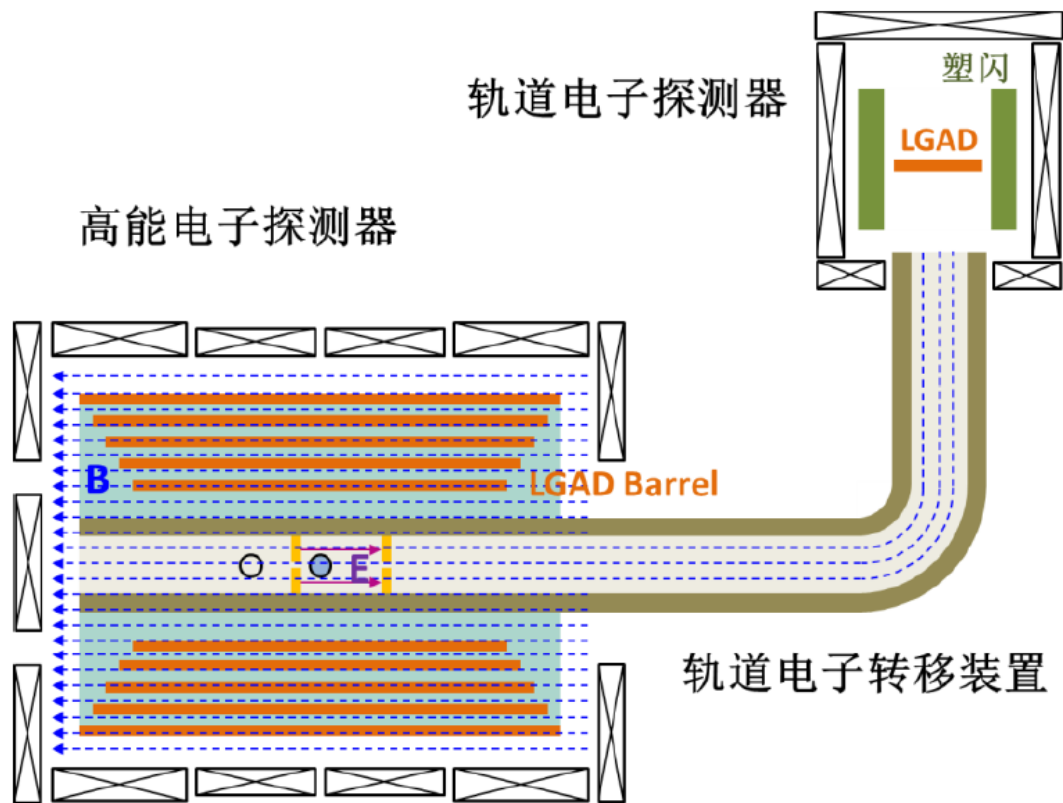
TPC探测器结构



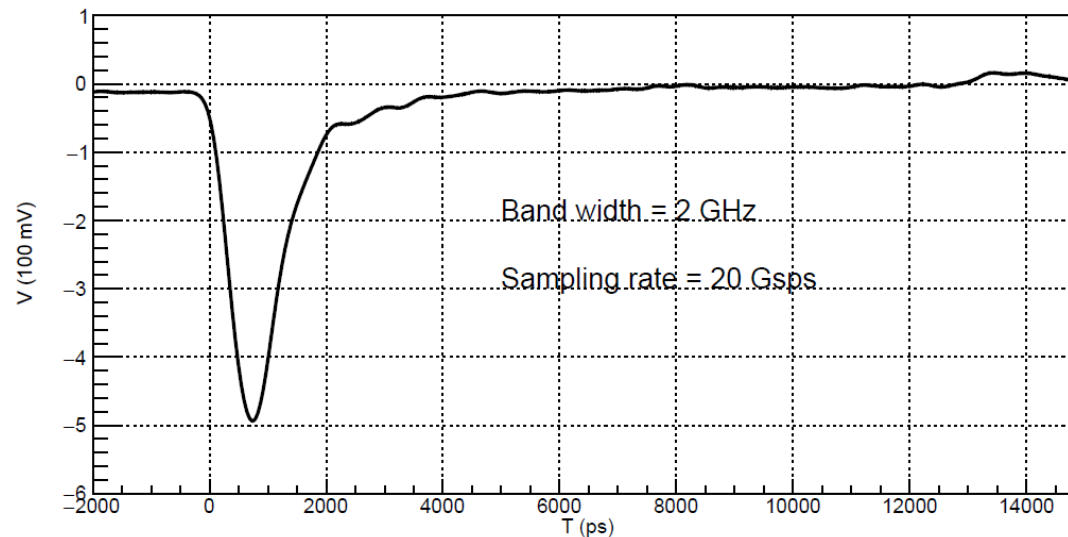
探测器扇形模块

中山大学/唐健团队/MACE实验

高能所/鲍煜团队



新型MuMubar谱仪结构  
(Not to scale)



- LGAD优势：
  - 时间分辨率比气体探测器好2个数量级。
  - 安全可靠，不存在打火的风险。
- LGAD劣势：
  - 位置分辨率约1mm，比气体探测器稍差。
  - 然而MuMubar实验径迹探测对位置分辨要求不高。

预计该方案所能使用的 $\mu$ 子源强度比气体方案高两个数量级