



中国科学院大学
University of Chinese Academy of Sciences



ICTP-AP
International Centre
for Theoretical Physics Asia-Pacific
国际理论物理中心-亚太地区

宇宙相变引力波理论和实验进展

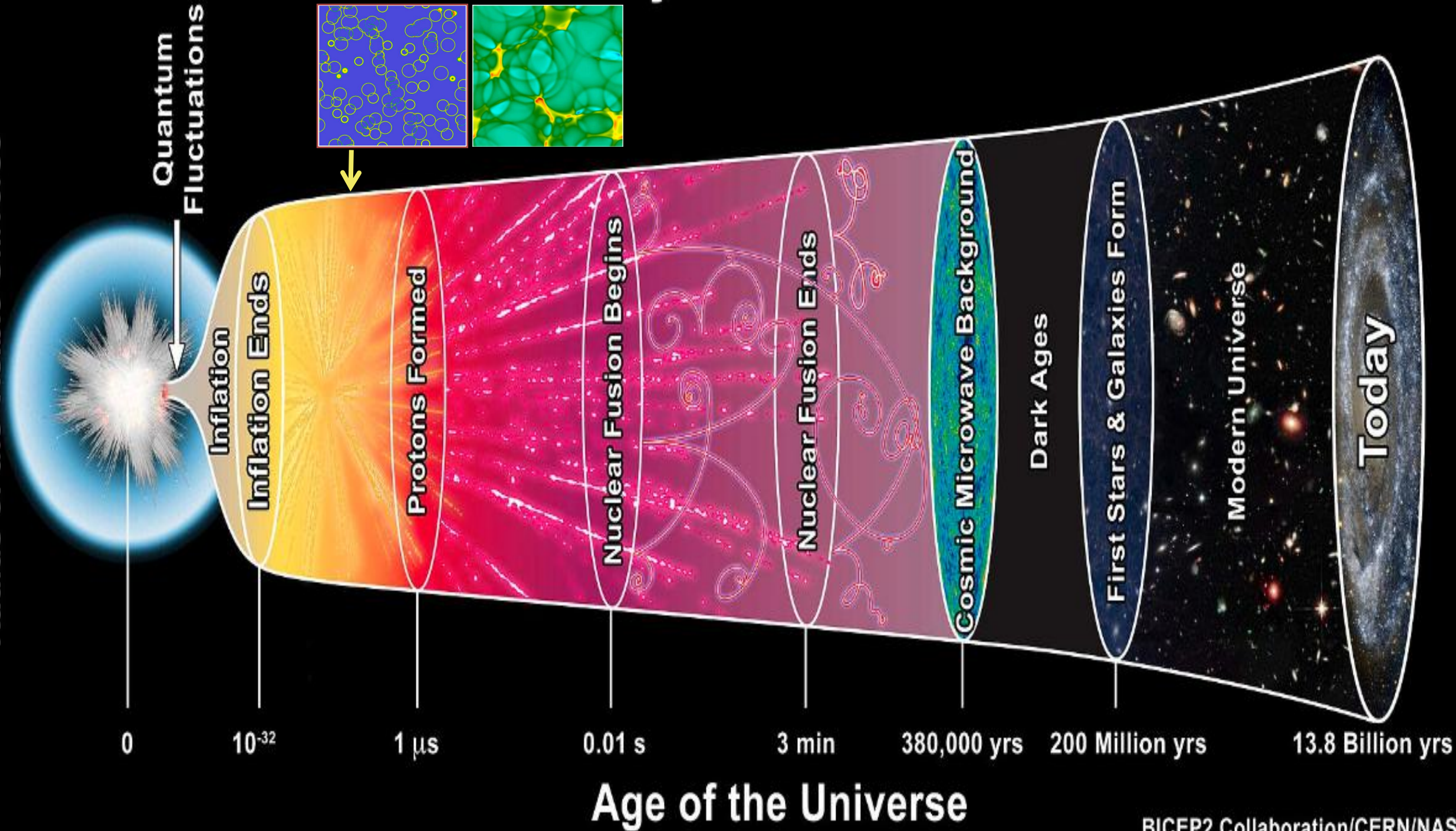
郭怀珂

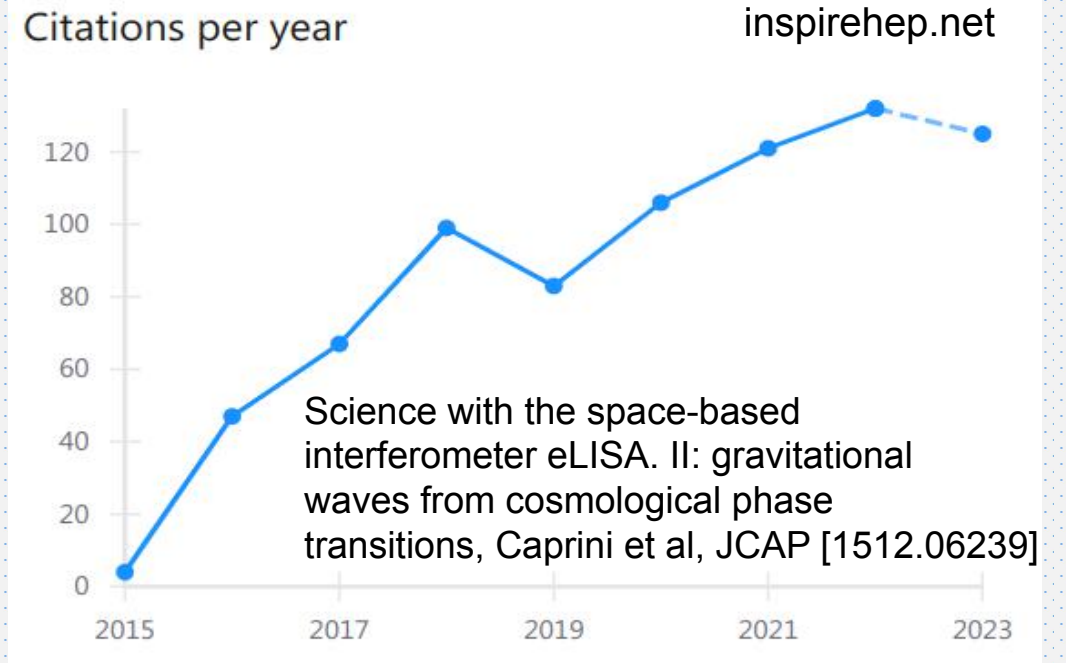
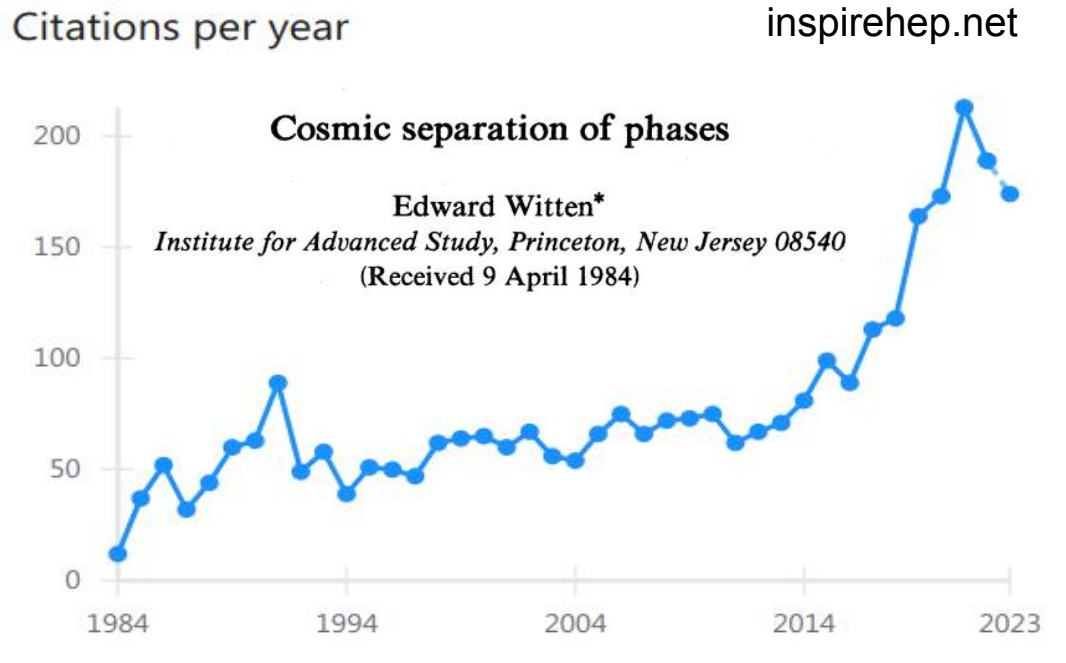
中国科学院大学
国际理论物理中心-亚太地区

2023-12-17

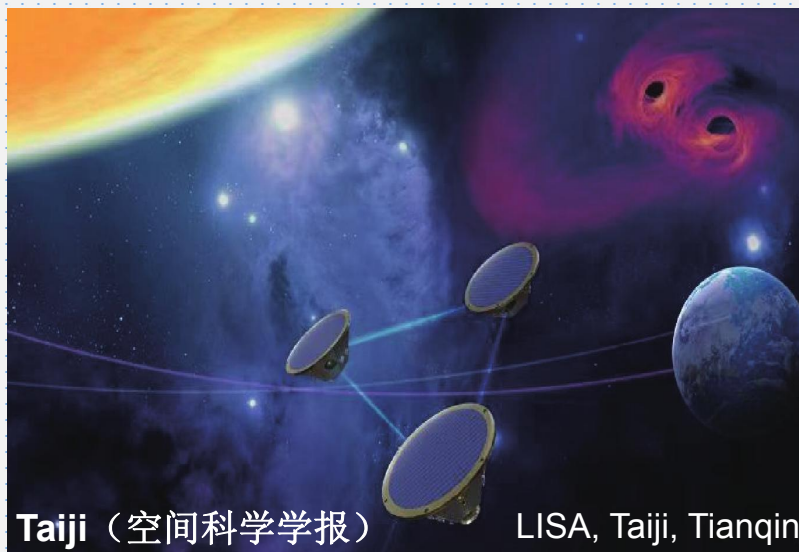
第十七届**TeV**工作组学术研讨会

Radius of the Visible Universe





中国脉冲星测时阵列 (CPTA)



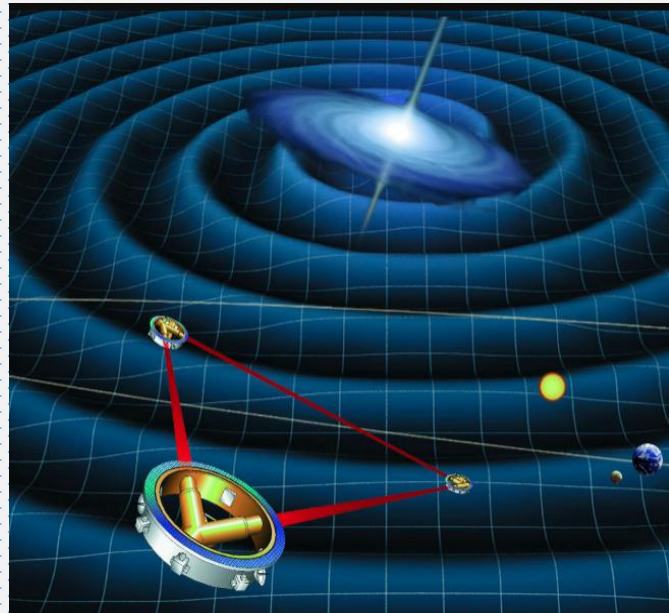
Taiji (空间科学学报) LISA, Taiji, Tianqin



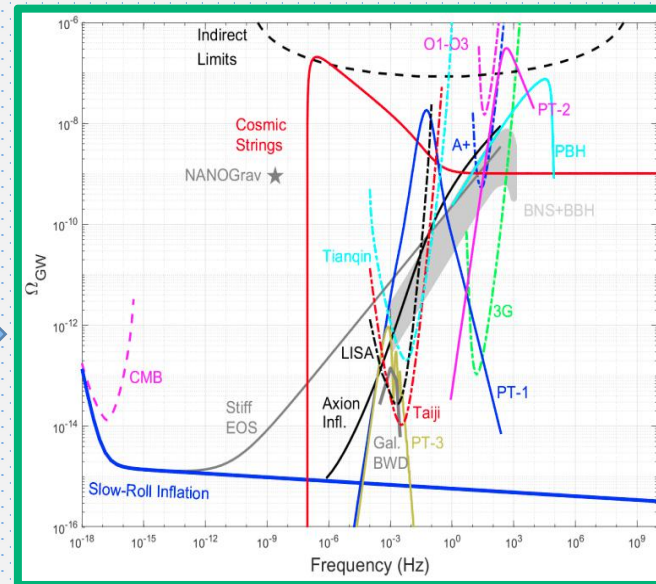
ligo.caltech.edu

From Theory to Experiment

theorist



LIGO, LISA/Taiji/Tianqin, PTA, ...



Gravitational Wave Spectrum

α
 β
 v_w
 T_*
 g_s
 ...

Phase Transition Parameters

Standard Model of Elementary Particles

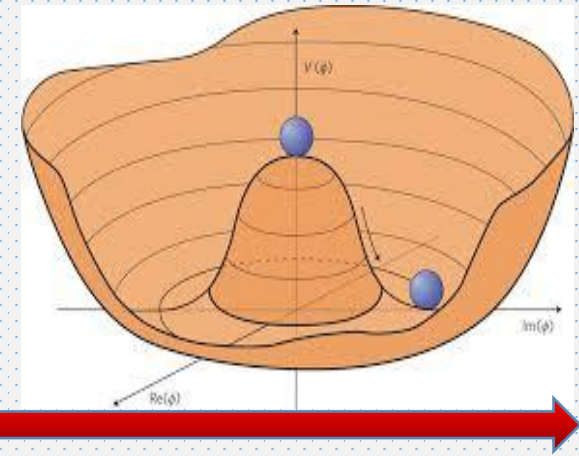
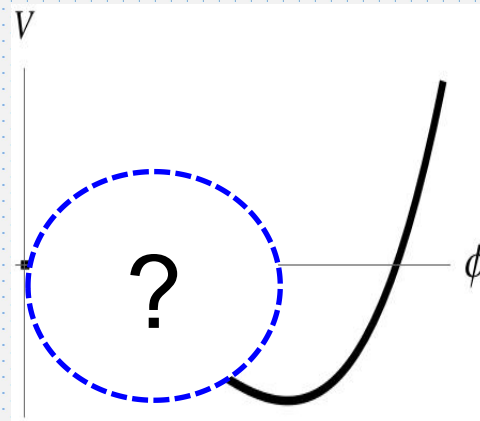
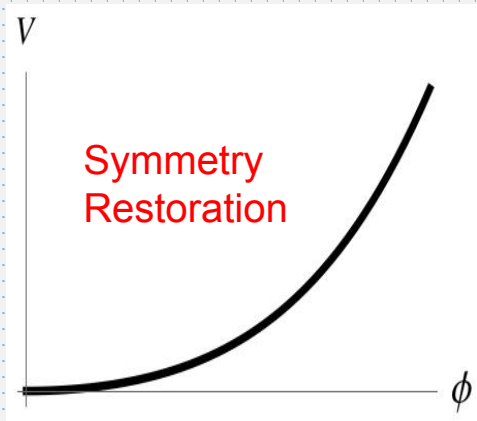
	three generations of matter (fermions)			interactions / force carriers (bosons)	
	I	II	III		
mass	$\approx 2.2 \text{ MeV}/c^2$	$\approx 1.28 \text{ GeV}/c^2$	$\approx 173.1 \text{ GeV}/c^2$	0	$\approx 124.97 \text{ GeV}/c^2$
charge	$\frac{2}{3}$	$\frac{2}{3}$	$\frac{2}{3}$	0	0
spin	$\frac{1}{2}$	$\frac{1}{2}$	$\frac{1}{2}$	1	0
	u up	c charm	t top	g gluon	H higgs
	d down	s strange	b bottom	γ photon	BSM
	e electron	μ muon	τ tau	Z Z boson	GAUGE BOSONS
	ν_e electron neutrino	ν_μ muon neutrino	ν_τ tau neutrino	W W boson	VECTOR BOSONS
					SCALAR BOSONS

Particle Physics Model

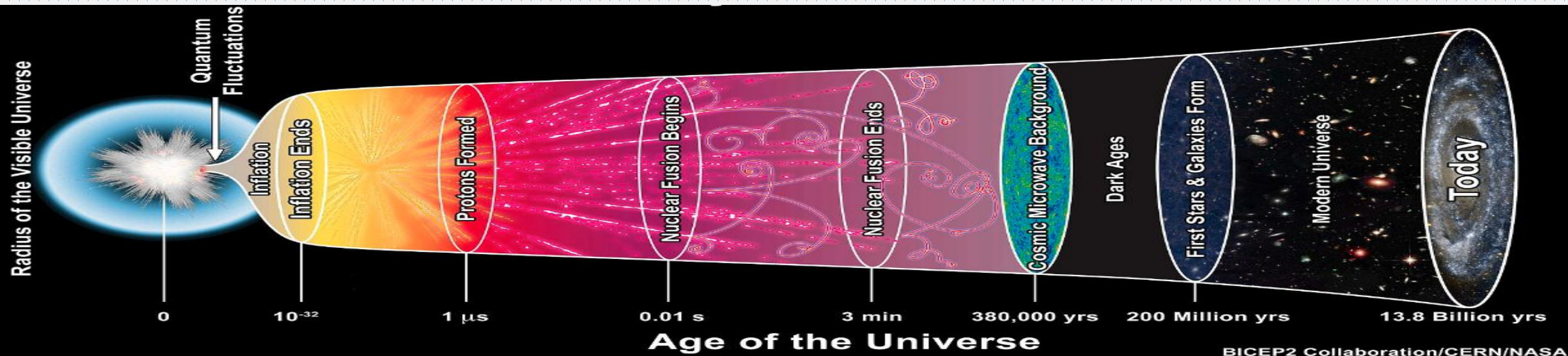


experimentalist

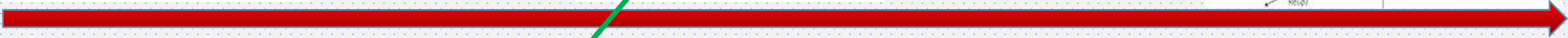
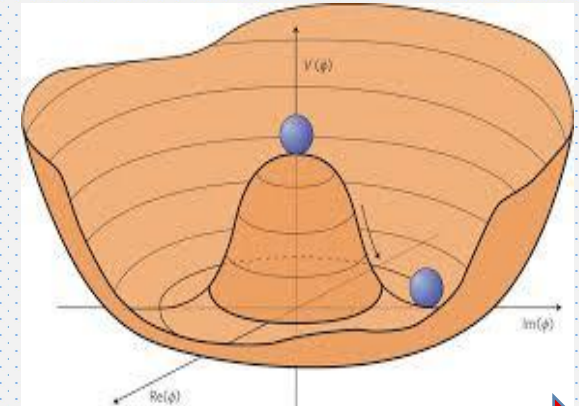
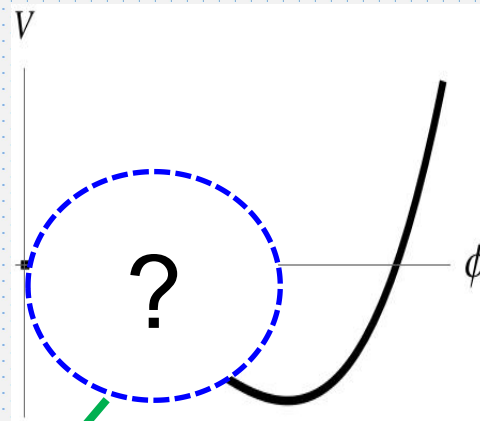
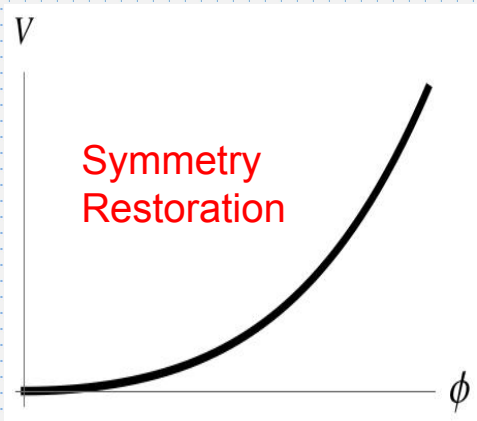
Electroweak Phase Transition



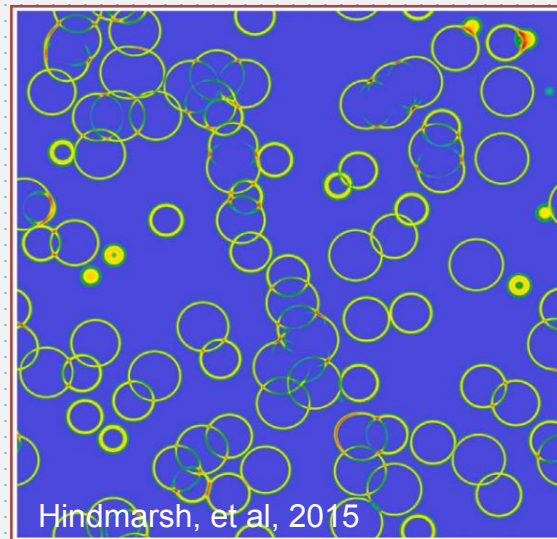
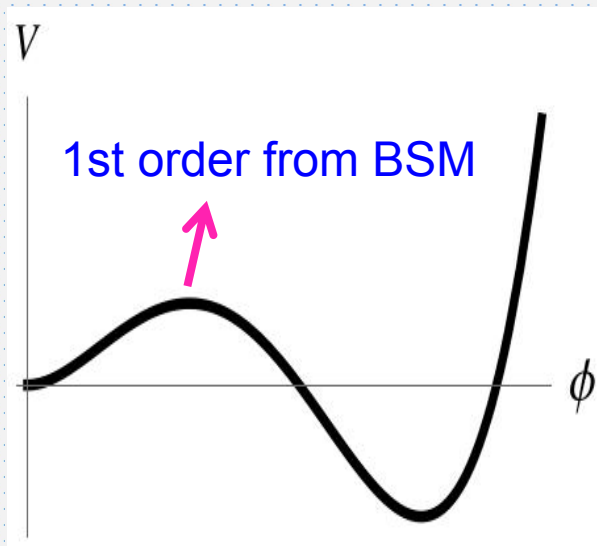
Temperature drops



Electroweak Phase Transition



Temperature drops





Electroweak Baryogenesis

- Modified Higgs potential (Higgs physics, GW)
- Extra CP-violation (EDM, LHC)
- New particles, symmetries (LHC, GW)

Trodden, Rev.Mod.Phys [9803479]

Phenomenological Studies

Detection of early-universe gravitational-wave signatures and fundamental physics

Robert Caldwell, Yanou Cui, Huai-Ke Guo , Vuk Mandic, Alberto Mariotti, Jose Miguel No, Michael J. Ramsey-Musolf, Mairi Sakellariadou , Kuver Sinha, Lian-Tao Wang, Graham White, Yue Zhao, Haipeng An, Ligong Bian, Chiara Caprini, Sebastien Clesse, James M. Cline, Giulia Cusin, Bartosz Fornal, Ryusuke Jinno, Benoit Laurent, Noam Levi, Kun-Feng Lyu, Mario Martinez, Andrew L. Miller, Diego Redigolo, Claudia Scarlata, Alexander Sevrin, Barmak Shams Es Haghi, Jing Shu, Xavier Siemens, Danièle A. Steer, Raman Sundrum, Carlos Tamarit, David J. Weir, Ke-Pan Xie, Feng-Wei Yang & Siyi Zhou — Show fewer authors

General Relativity and Gravitation **54**, Article number: 156 (2022) | [Cite this article](#)

Models	Strong 1 st order phase transition	GW signal	Cold DM	Dark Radiation and small scale structure
SM charged				
Triplet [20–22]	✓	✓	✓	✗
complex and real Triplet [23] (Georgi-Machacek model)	✓	✓	✓	✗
Multiplet [24]	✓	✓	✓	
2HDM [25–30]	✓	✓		✗
MLRSM [31]	✓	✓	✗	✗
NMSSM [32–36]	✓	✓	✓	✗
SM uncharged				
S_ν (xSM) [37–49]	✓	✓	✗	✗
2 S_ν 's [50]	✓	✓	✓	✗
S_c (cxSM) [49, 51–54]	✓	✓	✓	✗
$U(1)_D$ (no interaction with SM) [55]	✓	✓	✓	✗
$U(1)_D$ (Higgs Portal) [56]	✓	✓	✓	
$U(1)_D$ (Kinetic Mixing) [57]	✓	✓	✓	
Composite SU(7)/SU(6) [58]	✓	✓	✓	
$U(1)_L$ [59]	✓	✓	✓	✗
$SU(2)_D \rightarrow$ global $SO(3)$ by a doublet [60–62]			✓	✗
$SU(2)_D \rightarrow U(1)_D$ by a triplet [63–65]			✓	✓
$SU(2)_D \rightarrow Z_2$ by two triplets [66]			✓	✗
$SU(2)_D \rightarrow Z_3$ by a quadruplet [67, 68]			✓	✗
$SU(2)_D \times U(1)_{B-L} \rightarrow Z_2 \times Z_2$ by a quintuplet and a S_c [69]			✓	✗
$SU(2)_D$ with two dark Higgs doublets [70]	✓	✓	✗	✗
$SU(3)_D \rightarrow Z_2 \times Z_2$ by two triplets [62, 71]			✓	✗
$SU(3)_D$ (dark QCD) (Higgs Portal) [72, 73]	✓	✓	✓	
$G_{SM} \times G_{D,SM} \times Z_2$ [74]	✓	✓	✓	
$G_{SM} \times G_{D,SM} \times G_{D,SM} \dots$ [75]	✓	✓	✓	
Current work				
$SU(2)_D \rightarrow U(1)_D$ (see the text)	✓	✓	✓	✓

arXiv > hep-ph > arXiv:2203.08206

High Energy Physics - Phenomenology

[Submitted on 15 Mar 2022]

Probing the Electroweak Phase Transition with Exotic Higgs Decays

Marcela Carena, Jonathan Kozaczuk, Zhen Liu, Tong Ou, Michael J. Ramsey-Musolf, Jessie Shelton, Yikun Wang, Ke-Pan Xie

arXiv > hep-ph > arXiv:2203.10046

High Energy Physics - Phenomenology

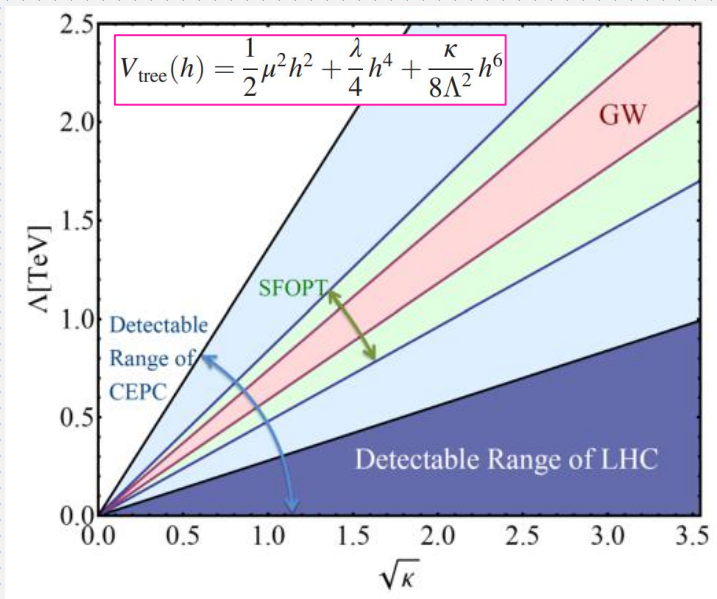
[Submitted on 18 Mar 2022]

Scalar-mediated dark matter model at colliders and gravitational wave detectors -- A White paper for Snowmass 2021

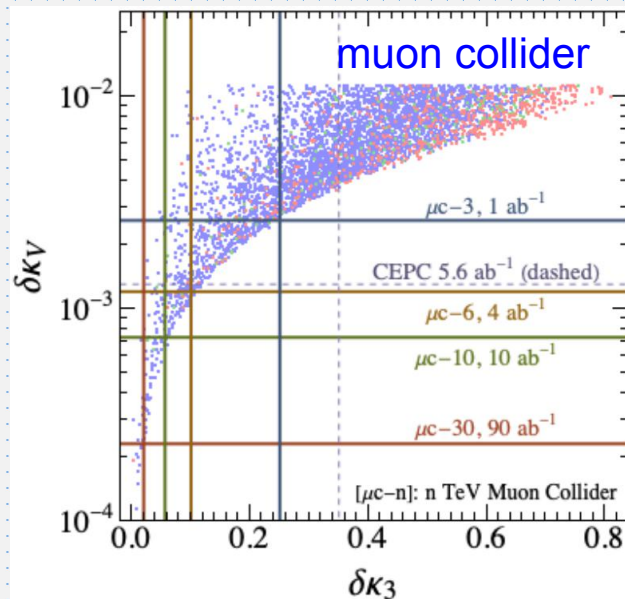
Jia Liu, Xiao-Ping Wang, Ke-Pan Xie

Snowmass 2021 White papers

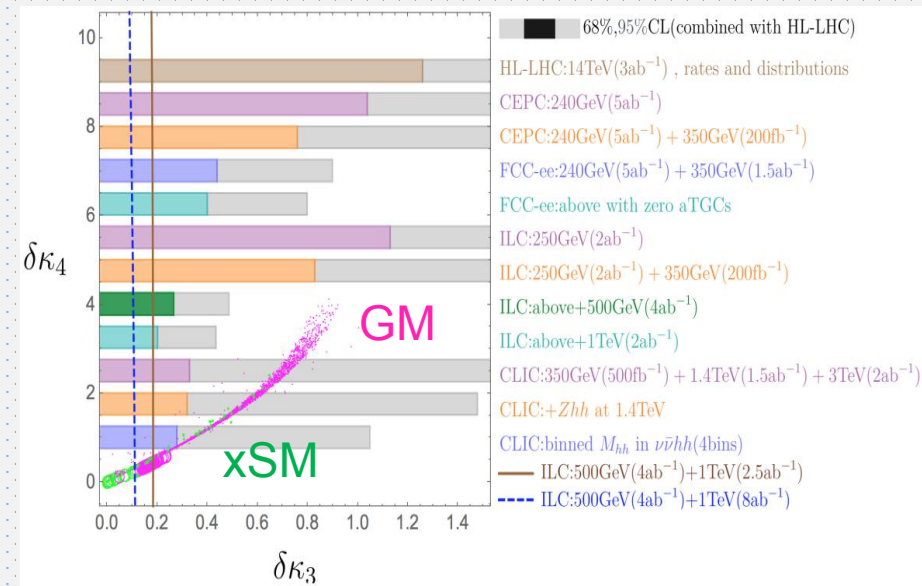
Ghosh, HG, Han, Liu, JHEP [2012.09758]



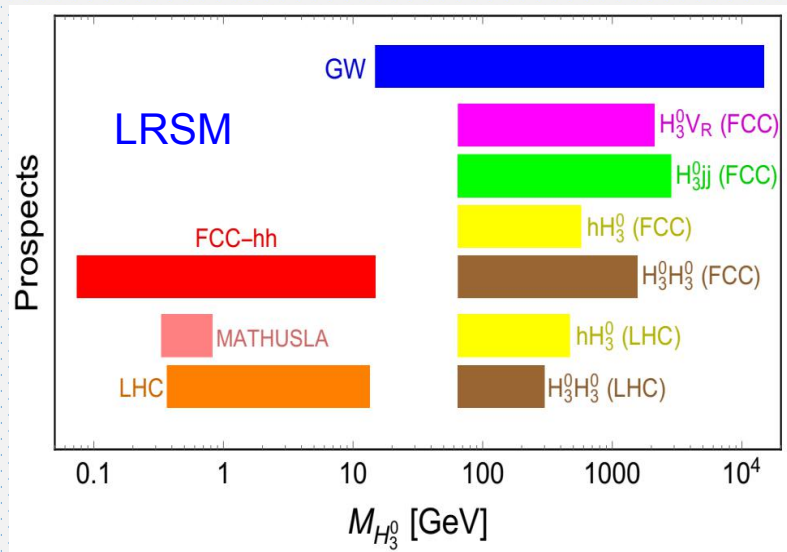
Fapeng Huang, Yi-Fu Cai, Xinmin Zhang, et al, PRD [1601.01640]



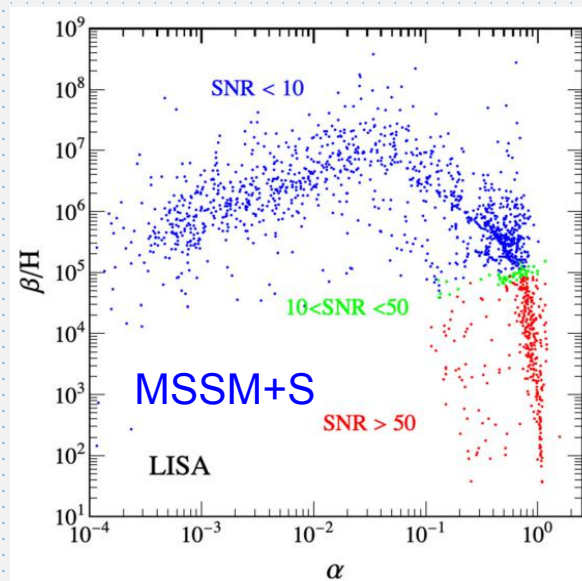
Wei Liu, Ke-Pan Xie, JHEP [2101.10469]



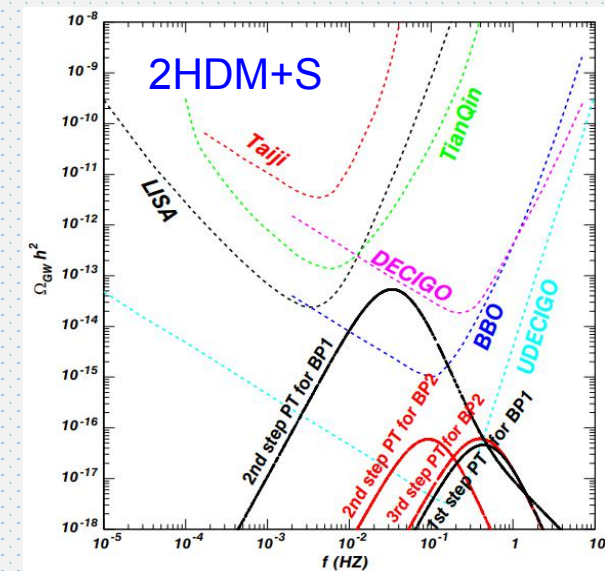
Ligong Bian, HG, Yongcheng Wu, Ruiyu Zhou, PRD [1906.11664]



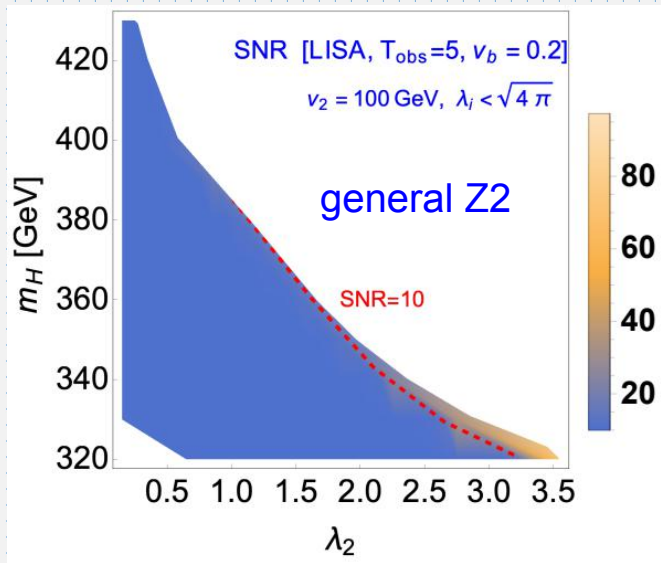
Mingqiu Li, Qi-Shu Yan, Yongchao Zhang, Zhijie Zhao, JHEP [2012.13686]



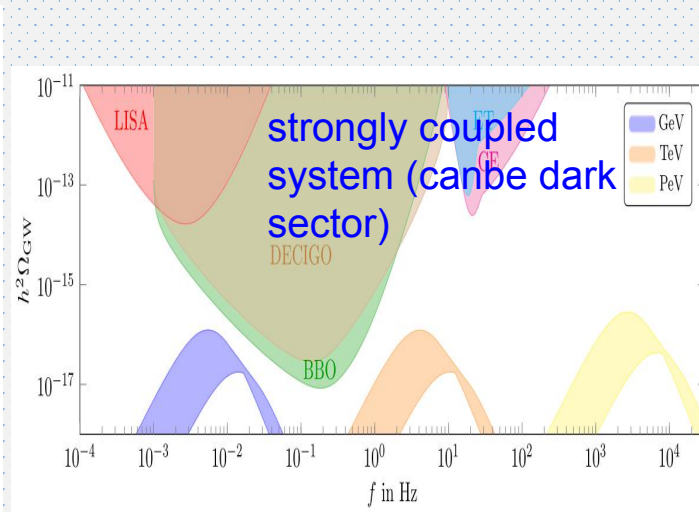
Wenyu Wang, Ke-Pan Xie, Wu-Long Xu, Jin Min Yang, EPJC [2204.01928]



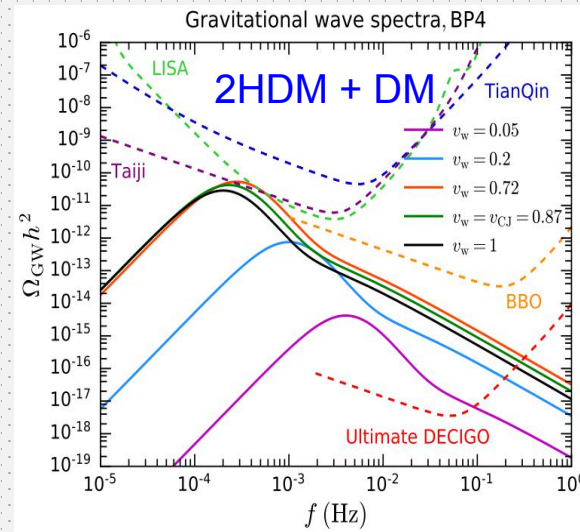
Songtao Liu, Lei Wang, PRD [2302.04639]



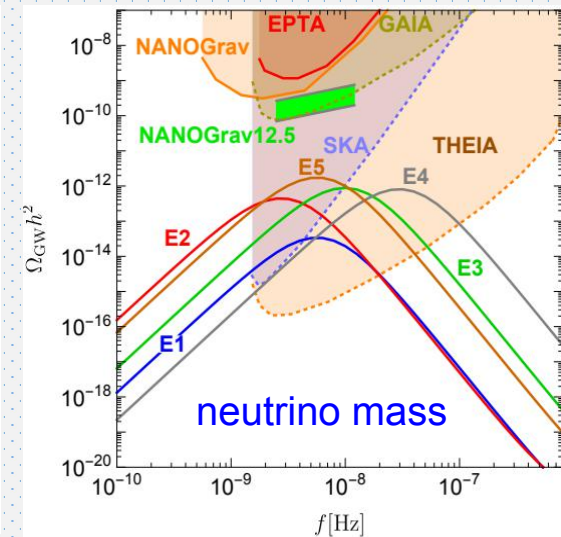
Qing-Hong Cao, Katsuya Hashino, Xu-Xiang Li, Jiang-Hao Yu [2212.07756]



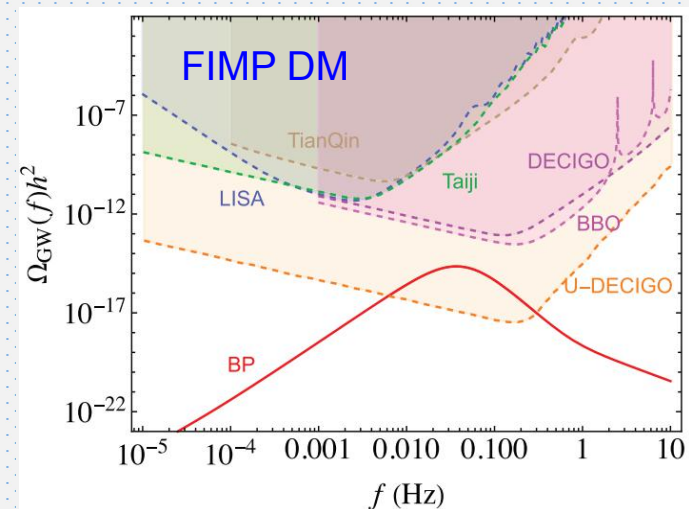
Zhi-Wei Wang, et al, PRD [2012.11614]



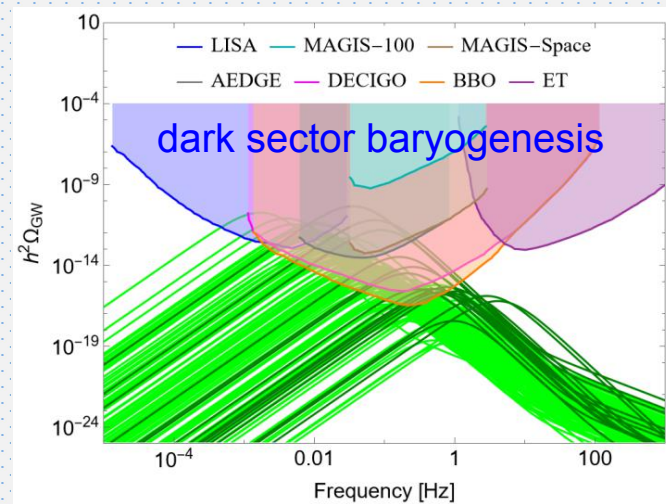
Zhao Zhang, Chengfeng Cai, Xue-Min Jiang, Yi-Lei Tang, Zhao-Huan Yu, and Hong-Hao Zhang, JHEP [2102.01588]



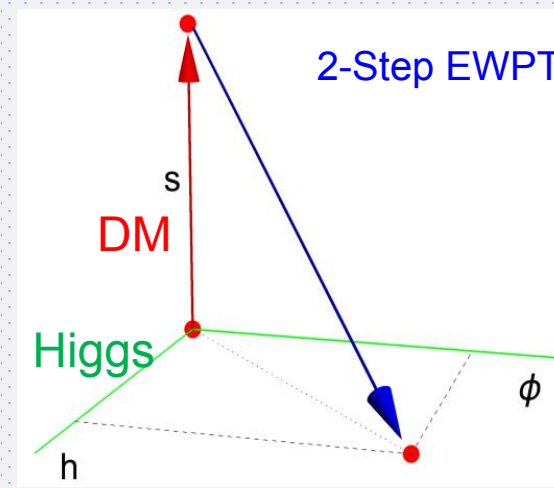
Pasquale Di Bari, Danny Marfatia, Ye-Ling Zhou, JHEP [2106.00025]



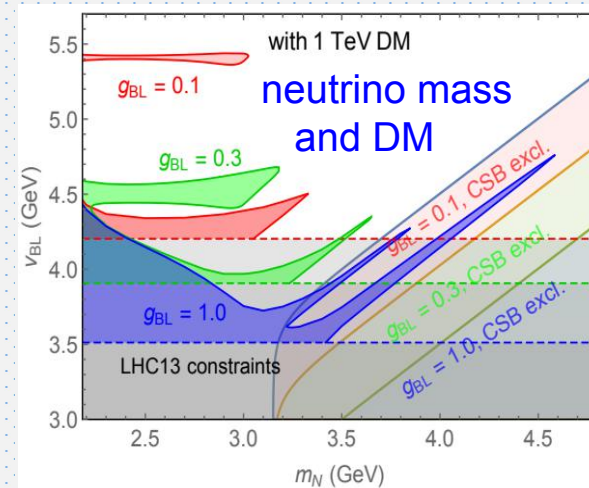
Xuewen Liu, Shu-Yuan Guo, Bin Zhu, Ying Li, Sci.Bull. [2022.06.011]



Marcela Carena, Ying-Ying Li, Tong Ou, Yikun Wang, JHEP [2210.14352]



Wei Chao, HG, Jing Shu, JCAP [1702.02698]



Ligong Bian, Wei Cheng, HG, Yongchao Zhang, CPC [1907.13589]

Collider and GW Complementarity

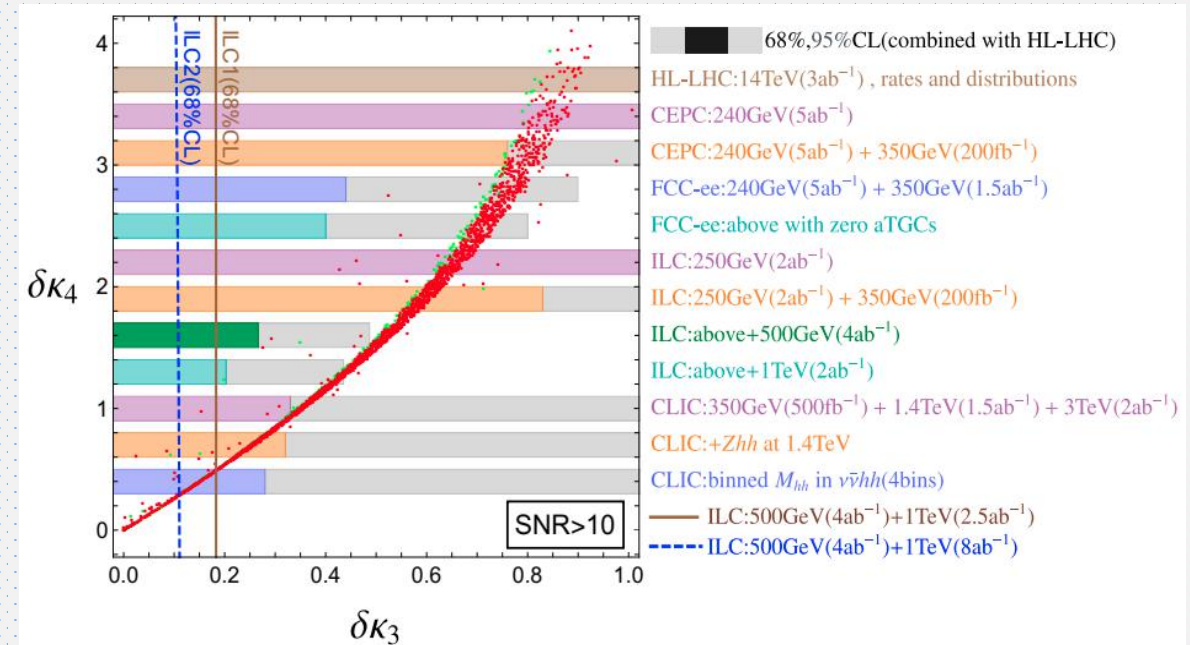
Contents

Snowmass 2021 Whitepaper, GRG [2203.07972]

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Simplest model: xSM (SM + S)

$$\Delta\mathcal{L} = -\frac{1}{2} \frac{m_{h_1}^2}{v} (1 + \delta\kappa_3) h_1^3 - \frac{1}{8} \frac{m_{h_1}^2}{v^2} (1 + \delta\kappa_4) h_1^4$$



Alves, Ghosh, HG, Sinha, Vagie, JHEP [1812.09333]

Collider and Gravitational Wave Complementarity in Exploring the Singlet Extension of the Standard Model

#27

Alexandre Alves (Diadema, Sao Paulo Fed. U.), Tathagata Ghosh (Hawaii U.), Huai-Ke Guo (Oklahoma U.), Kuver Sinha (Oklahoma U.), Daniel Vagie (Oklahoma U.) (Dec 21, 2018)

Published in: JHEP 04 (2019) 052 • e-Print: 1812.09333 [hep-ph]

pdf DOI cite claim reference search 106 citations

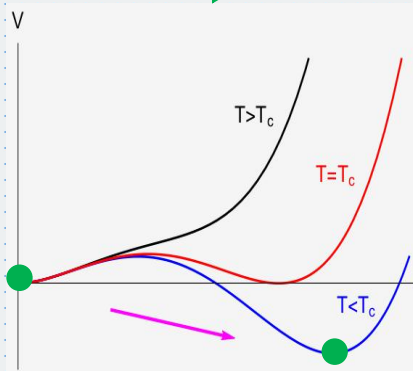
Nucleation Rate: Perturbative Method

The Usual Method

(Tree + Coleman-Weinberg + Daisy Resummation)

$$V_T = V_{\text{tree}} + V_{\text{CW}} + \frac{T^2}{24} \sum_i c_i M_i^2(\phi) - \frac{T}{12\pi} \sum_j d_j [M_j^2(\phi)]^{3/2}$$

$$V(\phi, T) = D(T^2 - T_0^2)\phi^2 - ET\phi^3 + \frac{\lambda}{4}\phi^4$$



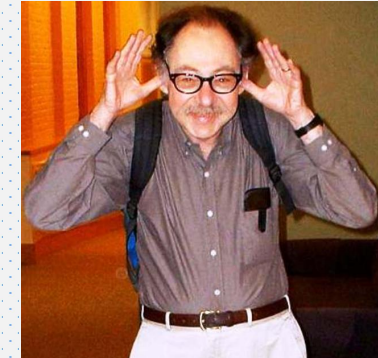
- Infrared problem (Linde, 1980)
- Gauge invariance (ok for high-T expansion) (Patel, Ramsey-Musolf, JHEP [1101.4665])

Nucleation rate

$$p = p_0 \exp \left[-\frac{S_{3,b}(T)}{T} \right]$$

fluctuations

critical bubble



Sidney Coleman



Andrei Linde

Gauge-invariant method proposed

Löfgren, Ramsey-Musolf, et al, PRL [2112.05472], JHEP [2112.08912]

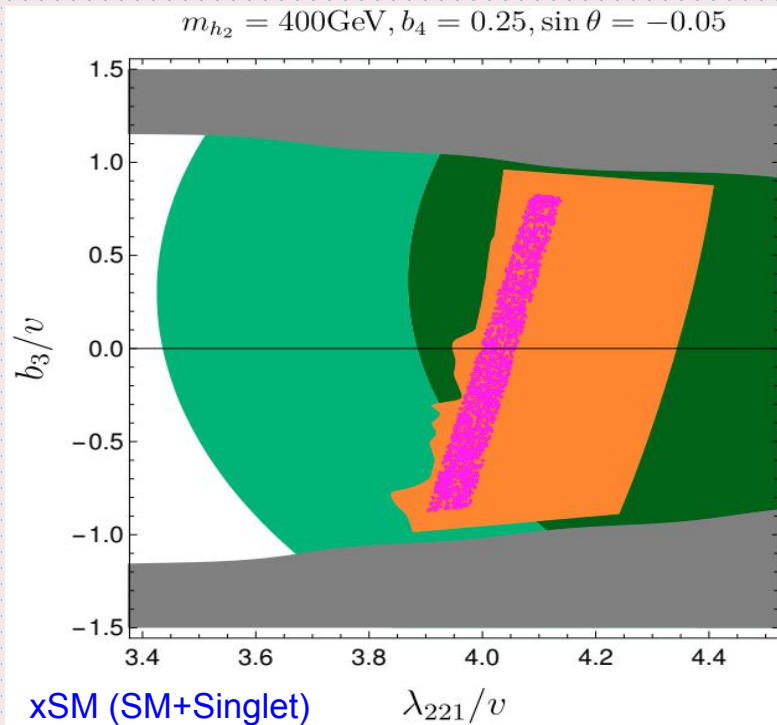
$$S_3 = a_0 g^{-3/2} + a_1 g^{-1/2} + \Delta$$

$$-\frac{1}{T} S_3[\phi_b] = -\frac{1}{T} \int d^3x \left[V_{\text{LO}}^{\text{eff}}(\phi_b) + V_{\text{NLO}}^{\text{eff}}(\phi_b) + \frac{1}{2} [1 + Z_{\text{NLO}}(\phi_b, T)] (\partial_i \phi_b)^2 + \dots \right]$$

Nucleation Rate: Non-Perturbative Method

- Non-perturbative method overcomes these problems
- But yet quite limited in BSM studies

perturbative vs non-perturbative

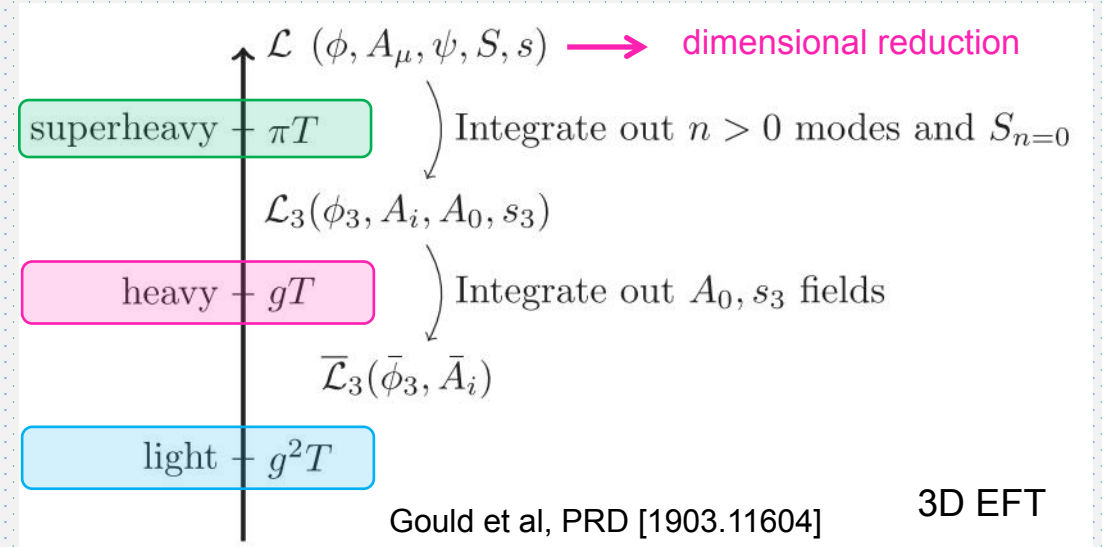


perturbative
(high-T, gauge independent)

non-perturbative
(high-dim operator needed)

perturbative (full one-loop)

Alves, Goncalves, Ghosh, HG, Sinha, JHEP [1909.05268]



Dimensional Reduction (Status)		
SM	✓	Farakos, Kajantie, Rummukainen, Shaposhnikov (1994)
MSSM	✓	Cline, Kainulainen (1996), Losada (1996), Laine (1996)
xSM (SM + Singlet)	✓	Brauner, Tenkanen, Tranberg, Vuorinen, Weir, JHEP [1609.06230]
Σ SM (SM + Triplet)	✓	Niemi, Patel, Ramsey-Musolf, Tenkanen, Weir, PRD [1802.10500]
2HDM	✓	Gorda, Helset, Niemi, Tenkanena, Weir, JHEP [1802.05056]

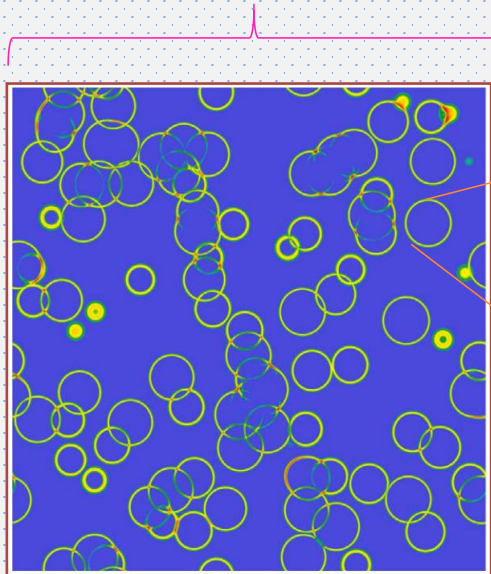
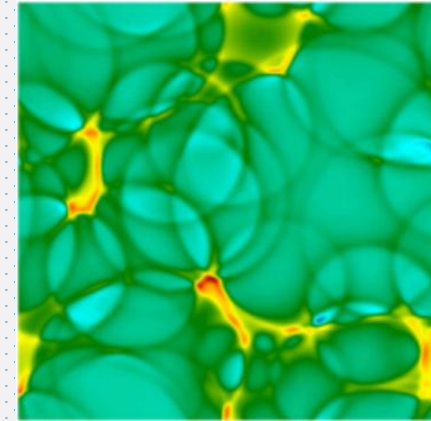
The Picture

Precise calculation of PT parameters:

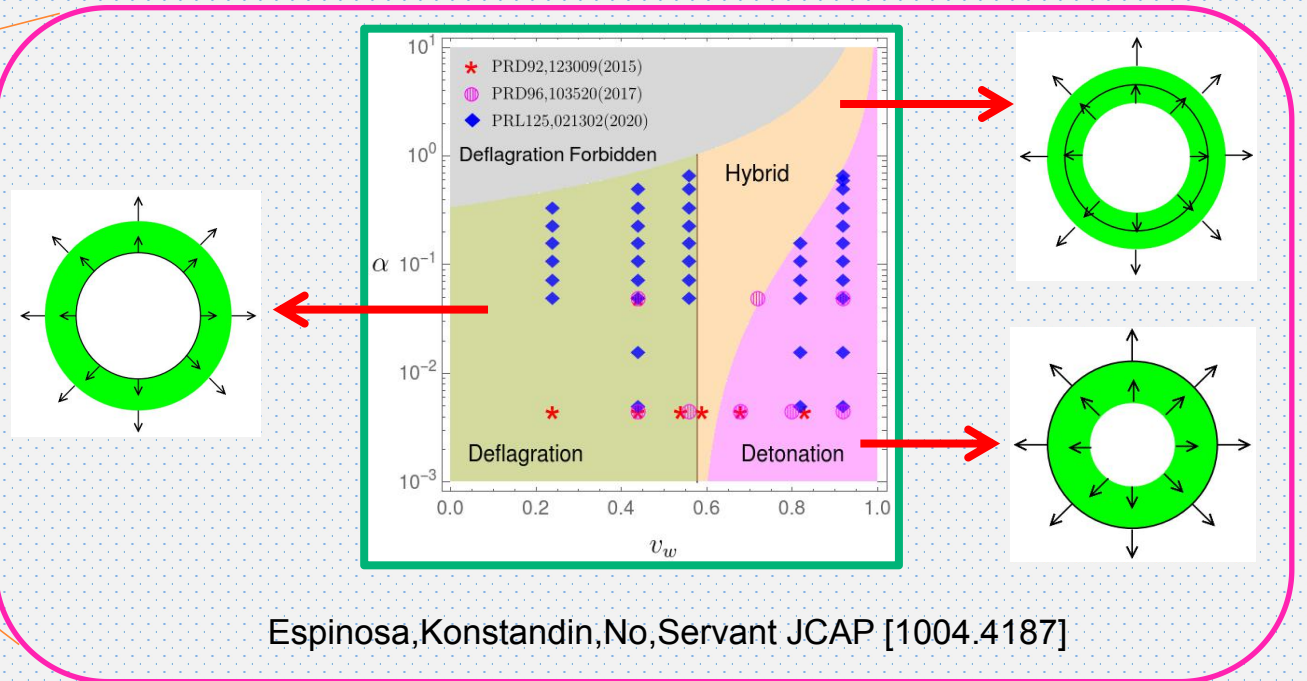
Minkowski spacetime: Hindmarsh, Hijazi, JCAP [1909.10040]

Expanding universe: HG, Sinha, Vagie, White, JCAP [2007.08537], JHEP [2103.06933]

- False Vacuum Fraction
- Unbroken Wall Area
- Bubble Lifetime Distribution
- Bubble Number Density



Hindmarsh et al, 2015



Espinosa, Konstandin, No, Servant JCAP [1004.4187]

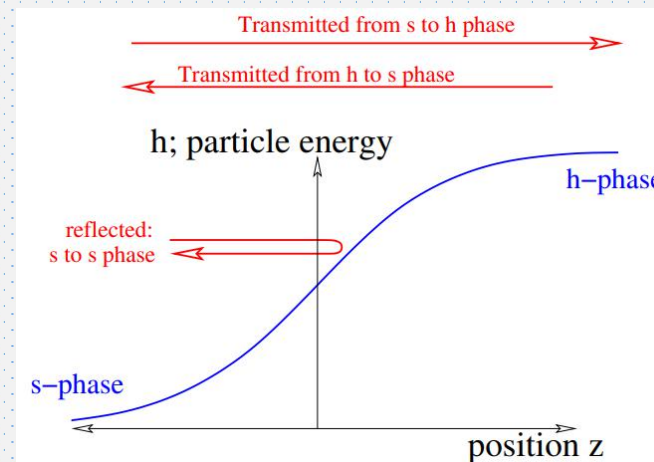
Wall Velocity: v_w

Usually chosen as fixed value in baryon asymmetry and GW studies

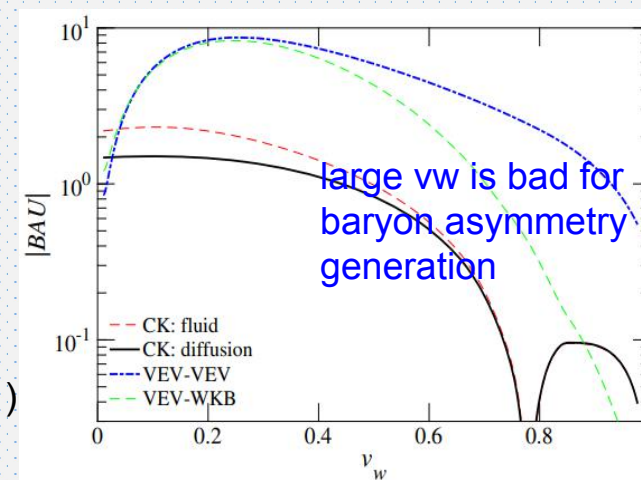
But, significant advances in recent years (driven by GW studies)

$$\square\phi + V'_T(\phi) + \sum \frac{dm^2}{d\phi} \int \frac{d^3 p}{(2\pi)^3 2E} \delta f(p, x) = 0$$

- Friction from out-of-equilibrium (Moore, Prokopec, PRL [9503296]; PRD [9506475])
- Transition radiation (Bodeker, Moore, JCAP [1703.08215])
- All orders resummation (Höche et al, JCAP [2007.10343])
- Lineared distribution or not (Laurent, Cline, PRD [2007.10935]; PRD [2204.13120])
- Singularity or not (Dorsch, Huber, Konstandin, JCAP [2112.12548], Laurent, Cline)
- Hydrodynamic (Cai, Wang, JCAP [2011.11451], Wang, Yuwen, PRD [2205.02492], 2310.07691)



Bodeker, Moore, JCAP [1703.08215]



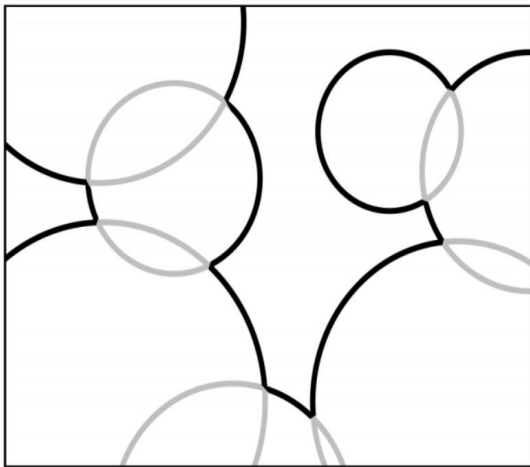
Cline, Kainulainen, PRD [2001.00568]

Gravitational Wave Sources

The current understanding:

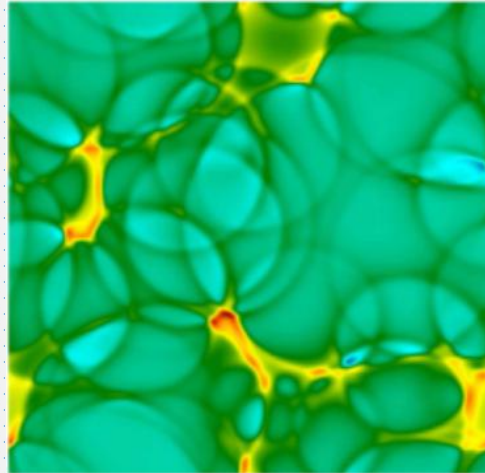
$$\square \bar{h}_{\mu\nu} = -\frac{16\pi G}{c^4} T_{\mu\nu}$$

energy near the wall



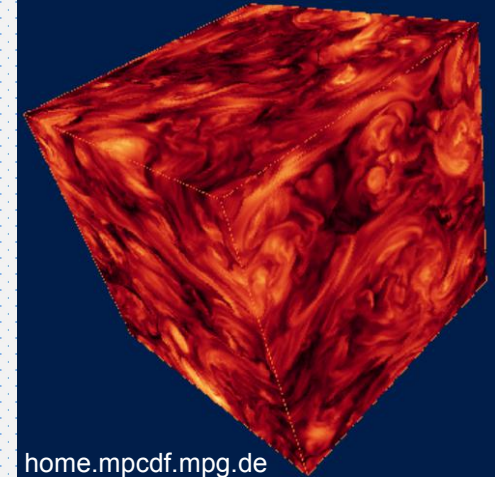
Bubble Collisions

fluid kinetic energy



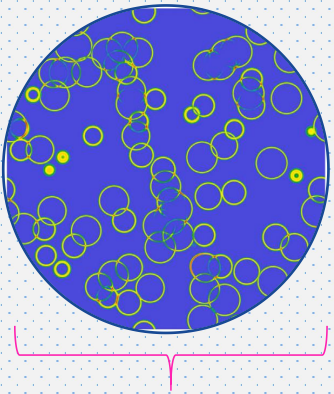
Sound Waves

turbulent fluid + magnetic field



Magnetohydrodynamic Turbulence

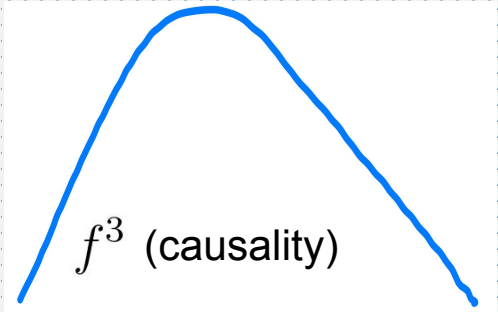
Basic Properties



Hubble size: $1/H^*$

$$f_{\text{now}} = 1.65 \times 10^{-5} \left(\frac{f_{\text{PT}}}{\beta} \right) \left(\frac{\beta}{H_*} \right) \left(\frac{T_*}{100\text{GeV}} \right) \left(\frac{g_*}{100} \right)^{1/6} \text{ Hz}$$

~100-1000



Cai, Pi, Sasak, PRD [1909.13728]

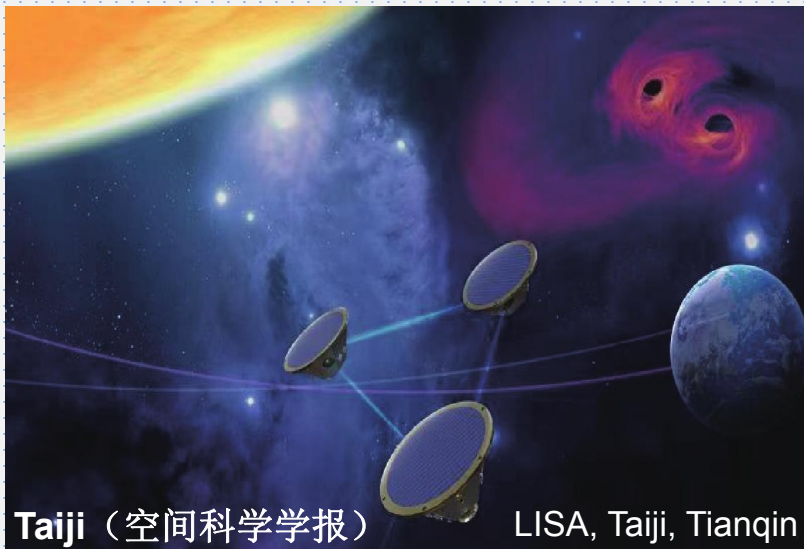
nHz (~100MeV) QCD scale

~mHz : (~100GeV) weak scale

~100Hz (~PeV - EeV) high scale

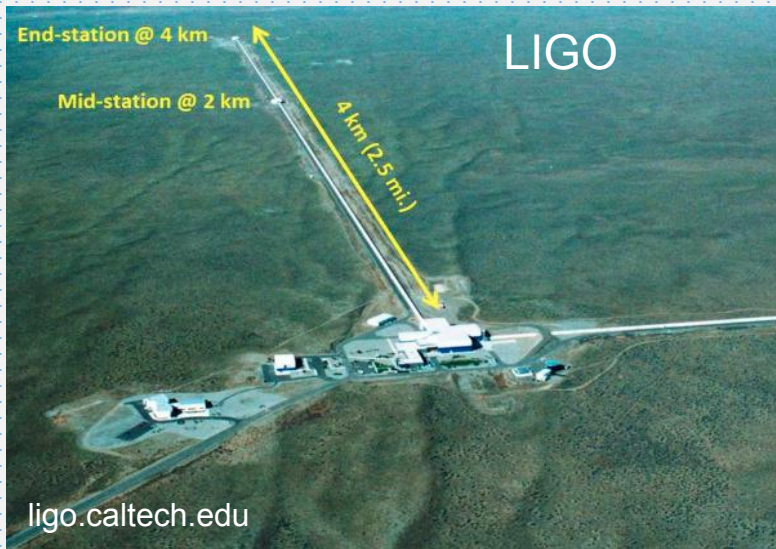


中国脉冲星测时阵列 (CPTA)



Taiji (空间科学学报)

LISA, Taiji, Tianqin



ligo.caltech.edu

Bubble Collisions

Envelope approximation:

Kosowsky, Turner, Watkins, Kamionkowski,
PRL69,2026(1992), PRD45,4514(1992), PRD47,4372(1993), PRD [9310044]

$$h^2 \Omega_{\text{BC}}(f) = 1.67 \times 10^{-5} \left(\frac{100}{g_*} \right)^{1/3} \Delta(v_w) \left(\frac{H_n}{\beta} \right)^2 \left(\frac{\kappa \phi \alpha}{1 + \alpha} \right)^2 S_{\text{env}}(f)$$

simulation

analytical

$$\Delta = \frac{0.11 v_w^3}{0.42 + v_w^2},$$

$$\frac{f_*}{\beta} = \frac{0.62}{1.8 - 0.1 v_w + v_w^2},$$

$$S_{\text{env}} = \left[\frac{3.8 (f/f_{\text{env}})^{2.8}}{1 + 2.8 (f/f_{\text{env}})^{3.8}} \right]$$

Huber, Konstandin, JCAP [0806.1828]

Chiara Caprini et al JCAP [1512.06239]

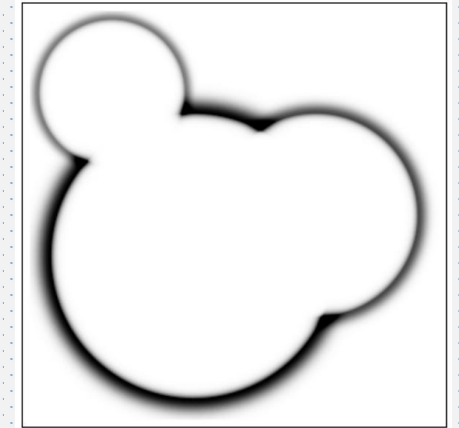
$$\Delta = \frac{0.48 v_w^3}{1 + 5.3 v_w^2 + 5 v_w^4},$$

$$\frac{f_*}{\beta} = \frac{0.35}{1 + 0.069 v_w + 0.69 v_w^4},$$

$$S_{\text{env}} = \left[c_l \left(\frac{f}{f_{\text{env}}} \right)^{-3} + (1 - c_l - c_h) \left(\frac{f}{f_{\text{env}}} \right)^{-1} + c_h \left(\frac{f}{f_{\text{env}}} \right) \right]^{-1}$$

$$(c_l = 0.064, \quad c_h = 0.48)$$

Jinno, Takimoto, PRD [1605.01403]



thin shell of uncollided walls

$$\Omega_{\text{BC}}(f \gtrsim f_{\text{peak}}) \propto f^{-1}$$

$$\Omega_{\text{BC}}(f \lesssim f_{\text{peak}}) \propto f^3$$

Bubble Collisions: Recent Development

- Wall thickness (probe effective potential)

Cutting et al, PRD [2005.13537], Gould et al, PRD [2107.05657], Mégevand, Membiela, JCAP [2302.13349]

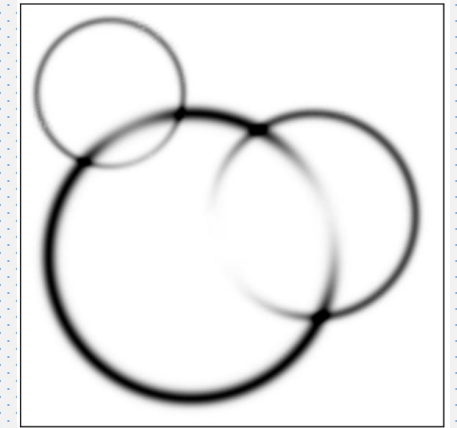
- Duration and Expanding Universe

Zhong, Gong, Qiu, JHEP [2107.01845]

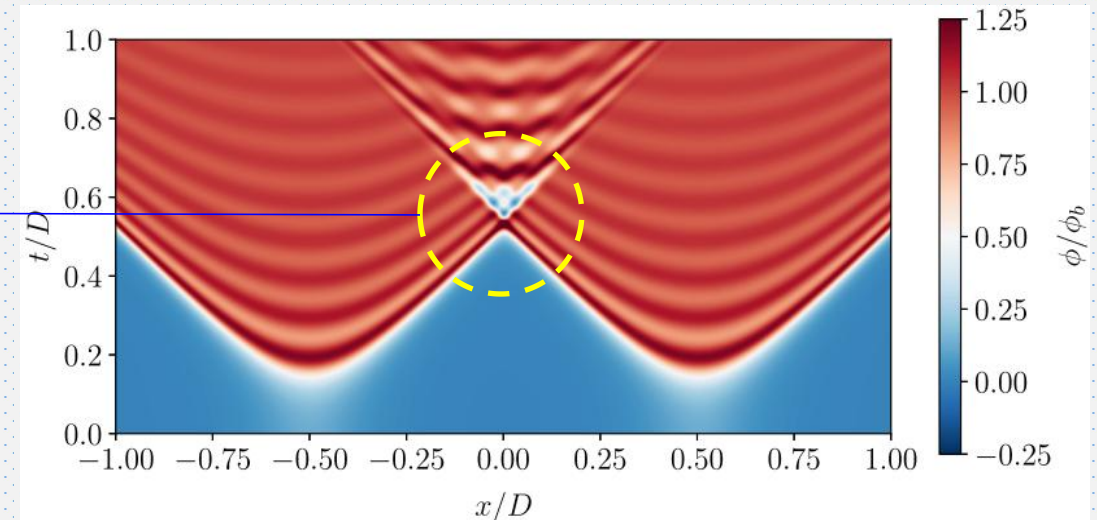
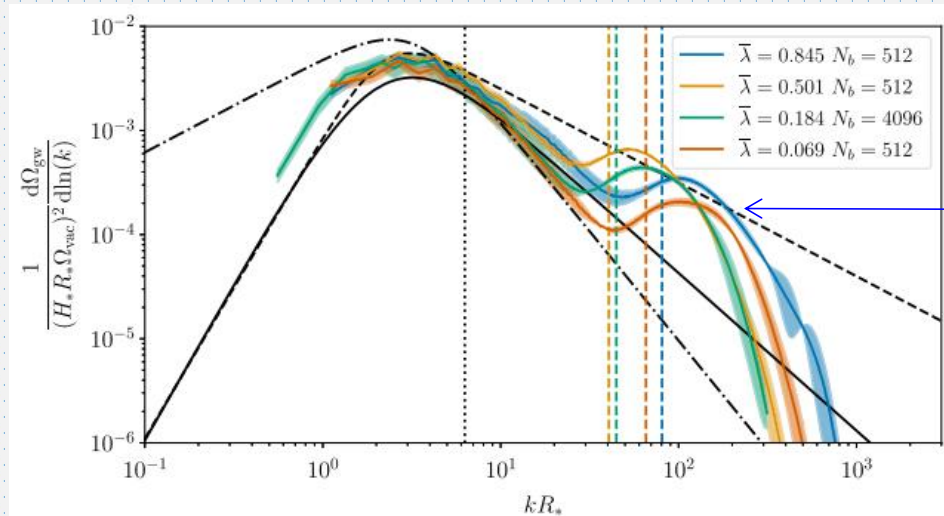
- Scalar + Gauge

Di, Wang, Zhou, Bian, Cai, Liu, PRL [2012.15625], Yang, Bian, PRD [2102.01398],
Lewicki, Vaskonen, EPJC [2007.04967]

Bulk flow model



Jinno, Takimoto, JCAP [1707.03111],
Konstandin, JCAP [1712.06869]



Bubble Collisions during Inflation

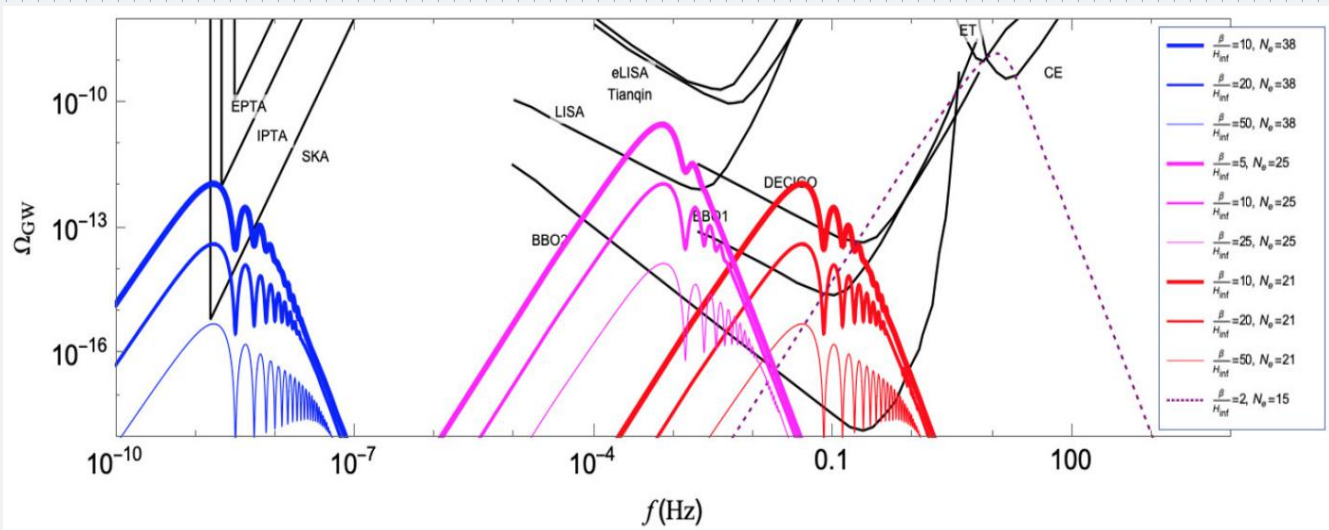
PT in the spectator field (σ), with negligible energy density

$$\mathcal{L} = -\frac{1}{2}g^{\mu\nu}\partial_\mu\phi\partial_\nu\phi - \frac{1}{2}g^{\mu\nu}\partial_\mu\sigma\partial_\nu\sigma - V(\phi, \sigma)$$

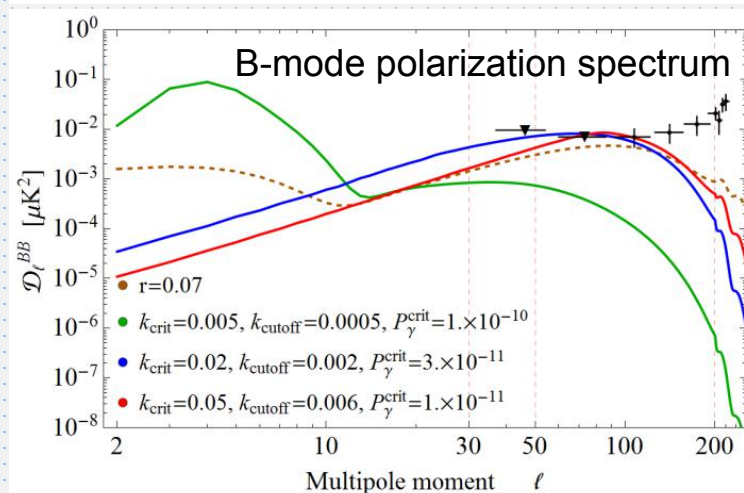
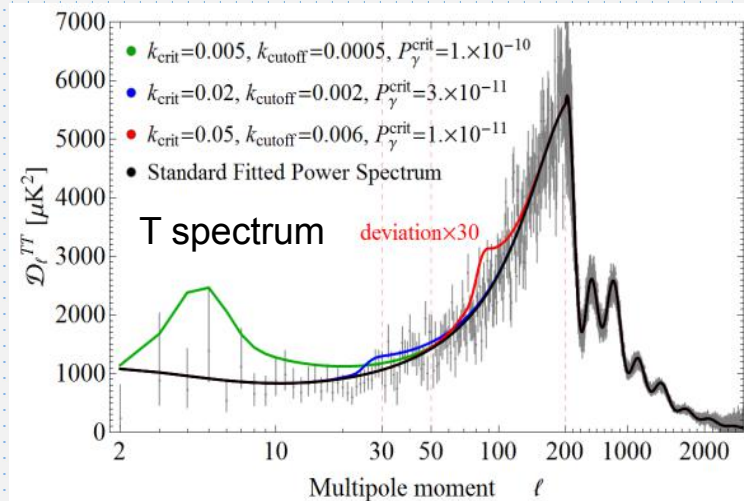
An, Lyu, Wang, Zhou, CPC [2009.12381], JHEP [2201.05171]

An, Tong, Zhou, [2208.14857]

An, Yang, [2304.02361]



Jiang, Liu, Sun, Wang, PLB [1512.07538]



Sound Waves

Hindmarsh, Huber, Rummukainen, Weir, PRL [1304.2433]

$$T^{ij} \propto (p + e)v^i v^j$$

$$h^2 \Omega_{\text{sw}}(f) = 2.65 \times 10^{-6} \left(\frac{100}{g_*} \right)^{\frac{1}{3}} \left(\frac{H_*}{\beta} \right) \left(\frac{\kappa_{\text{sw}} \alpha}{1 + \alpha} \right)^2 v_w S_{\text{sw}}(f) \Upsilon(\tau_{\text{sw}})$$

$$S_{\text{sw}}(f) = \left(\frac{f}{f_{\text{sw}}} \right)^3 \left[\frac{7}{4 + 3(f/f_{\text{sw}})^2} \right]^{7/2} \quad f_* = \frac{2\beta}{\sqrt{3}v_w} \approx \frac{3.4}{R_*}$$

Hindmarsh, Huber, Rummukainen, Weir, PRD [1504.03291]

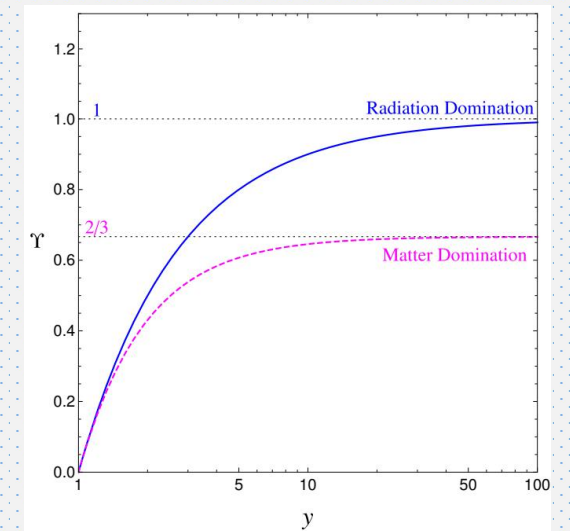
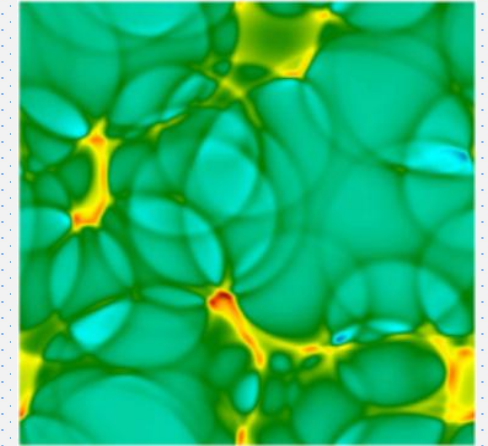
$$\Omega_{\text{sw}}(f \gtrsim f_{\text{peak}}) \propto f^{-4}$$

$$\Omega_{\text{sw}}(f \lesssim f_{\text{peak}}) \propto f^3$$

Slight different fit obtained by the same group, PRD [1704.05871]

$$\Upsilon = 1 - (1 + 2\tau_{\text{sw}} H_{\text{pt}})^{-1/2} \quad (\text{radiation domination})$$

HG, Sinha, Vagie, White, JCAP [2007.08537]



Sound Waves: Recent Development

$$\Upsilon = 1 - (1 + 2\tau_{\text{sw}}H_{\text{pt}})^{-1/2} \quad (\text{RD})$$

HG, Sinha, Vagie, White, JCAP [2007.08537]

Phase Transitions in an Expanding Universe: Stochastic Gravitational Waves in Standard and Non-Standard Histories

#1

Huai-Ke Guo (Oklahoma U.), Kuver Sinha (Oklahoma U.), Daniel Vagie (Oklahoma U.), Graham White (TRIUMF) (Jul 16, 2020)

Published in: *JCAP* 01 (2021) 001 • e-Print: 2007.08537 [hep-ph]

pdf DOI cite claim reference search 166 citations

PHYSICAL REVIEW LETTERS 127, 251302 (2021)

Editors' Suggestion

Featured in Physics

Searching for Gravitational Waves from Cosmological Phase Transitions with the NANOGrav 12.5-Year Dataset

Zaven Arzoumanian,¹ Paul T. Baker,² Harsha Blumer,^{3,4} Bence Bécsey,⁵ Adam Brazier,^{6,7} Paul R. Brook,^{3,4} Sarah Burke-Spolaor,^{3,4,8} Maria Charisi,⁹ Shami Chatterjee,⁶ Siyuan Chen,^{10,11,12} James M. Cordes,⁶ Neil J. Cornish,⁵ Fronefield Crawford,¹³ H. Thankful Cromartie,⁶ Megan E. DeCesar,^{14,15*} Paul B. Demorest,¹⁶ Timothy Dolch,^{17,18} Justin A. Ellis,¹⁹ Elizabeth C. Ferrara,^{20,21,22} William Fiore,^{3,4} Emmanuel Fonseca,²³ Nathan Garver-Daniels,^{3,4} Peter A. Gentile,^{3,4} Deborah C. Good,²⁴ Jeffrey S. Hazboun,²⁵ A. Miguel Holgado,^{26,27} Kristina Islo,²⁸ Ross J. Jennings,⁶ Megan L. Jones,²⁸ Nima Laal,³⁰ Michael T. Lam,²⁸ Ivan S. Lynch,³⁶ Dustin R. M. Malmgren,²⁸ Cherry Ng,³⁹ David J. Nice,¹⁴ Shaphiro-Albert,^{3,4} Xavier Siemens,¹⁶ Kevin Stovall,¹⁶ Jerry P. Sun,³⁰ Leah J. Vigeland,²⁸

considered in this work. Because of the finite lifetime [54,55] of the sound waves, to derive Ω_{SW} Eq. (4) needs to be multiplied by a suppression factor $\Upsilon(\tau_{\text{SW}})$ given by [54]

$$\Upsilon(\tau_{\text{SW}}) = 1 - (1 + 2\tau_{\text{SW}}H_*)^{-1/2} \quad (6)$$

(NANOGrav Collaboration)

THE ASTROPHYSICAL JOURNAL LETTERS, 951:L11 (56pp), 2023 July 1
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<https://doi.org/10.3847/2041-8213/acde91>

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CrossMark

The NANOGrav 15 yr Data Set: Search for Signals from New Physics

Adeela Afzal,^{1,2} Gabriella Agazie,³ Akash Anumarlapudi,³ Anne M. Archibald,⁴ Zaven Arzoumanian,⁵ Paul T. Baker,⁶ Bence Bécsey,⁷ Jose Juan Blanco-Pillado,^{8,9,10} Laura Blecha,¹¹ Kimberly K. Boddy,¹² Adam Brazier,^{13,14} Paul R. Brook,¹⁵ Sarah Burke-Spolaor,^{16,17} Rand Burnette,⁷ Robin Case,⁷ Maria Charisi,¹⁸ Shami Chatterjee,¹³ Katerina Chatziioannou,¹⁹ Belinda D. Cheeseboro,^{16,17} Siyuan Chen,²⁰ Tyler Cohen,²¹ James M. Cordes,¹³ Neil J. Cornish,²² Fronefield Crawford,²³ H. Thankful Cromartie,^{13,77} Kathryn Crowter,²⁴ Curt J. Cutler,^{19,25} Megan E. DeCesar,²⁶ Dallas DeGan,⁷ Paul B. Demorest,²⁷ Heling Deng,⁷ Timothy Dolch,^{28,29} Brendan Drachler,^{30,31} Richard von Eckardstein,¹ Elizabeth C. Ferrara,^{32,33,34} William Fiore,^{16,17} Emmanuel Fonseca,^{16,17} Gabriel E. Freedman,³ Nate Garver-Daniels,^{16,17} Peter A. Gentile,^{16,17} Kyle A. Gersbach,¹⁸ Joseph Glaser,^{16,17} Deborah C. Good,^{35,36} Lydia Guertin,³⁷ Kayhan Gültekin,³⁸ Jeffrey S. Hazboun,⁷ Sophie Hourihane,¹⁹ Kristina Islo,³ Ross J. Jennings,^{16,17,78} Aaron D. Johnson,^{3,19} Megan L. Jones,³ Andrew R. Kaiser,^{16,17} David L. Kaplan,³ Luke Zoltan Kelley,³⁹ Matthew Kerr,⁴⁰ Joey S. Key,⁴¹ Nima Laal,⁷ Michael T. Lam,^{30,31} William G. Lamb,¹⁸ T. Joseph W. Lazio,²⁵ Vincent S. H. Lee,¹⁹ Natalia Lewandowska,⁴² Rafael R. Lino dos Santos,^{1,43} Tyson B. Littenberg,⁴⁴ Tingting Liu,^{16,17} Alexander McEwen,⁴⁵ Patrick M. Meyers,⁴⁶ Cherry Ng,⁵⁶ David J. Nice,¹⁴ Polina Petrov,¹⁸ Shashwat C. Levi,¹⁸ Shult,¹⁸ Ingrid H. Stairs,²⁴ Joseph K. Swiggum,⁴⁷ Michele Va

time of matter–radiation equality. The production of GWs from sound waves stops after a period τ_{sw} , when the plasma motion turns turbulent (Ellis et al. 2019a, 2019b, 2020; Guo et al. 2021). In Equation (34), this effect is taken into account by the suppression factor

$$\Upsilon(\tau_{\text{sw}}) = 1 - (1 + 2\tau_{\text{sw}}H_*)^{-1/2}, \quad (36)$$

Caitlin A. Witt,⁴⁸ David Wright,⁴⁹ Onvia Young,⁵⁰ Kathryn M. Zurek,⁵¹ and The NANOGrav Collaboration

Sound Waves: Recent Development

Analytical Modelling

- Refine the sound shell model
- Synergy with simulations

Sound Shell Model

Hindmarsh, PRL [1608.04735]

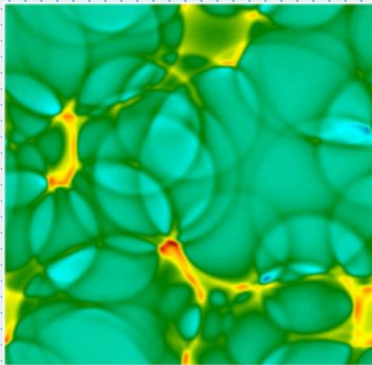
Hindmarsh, Hijazi, JCAP [1909.10040]

HG, Sinha, Vagie, White, JCAP [2007.08537]

Cai, Wang, Yuwen, PRD Letter [2305.00074]

Pol, Procacci, Caprini [2308.12943]

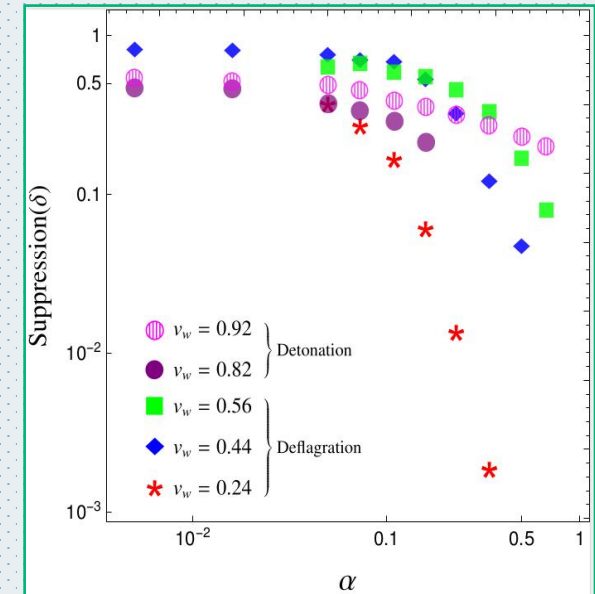
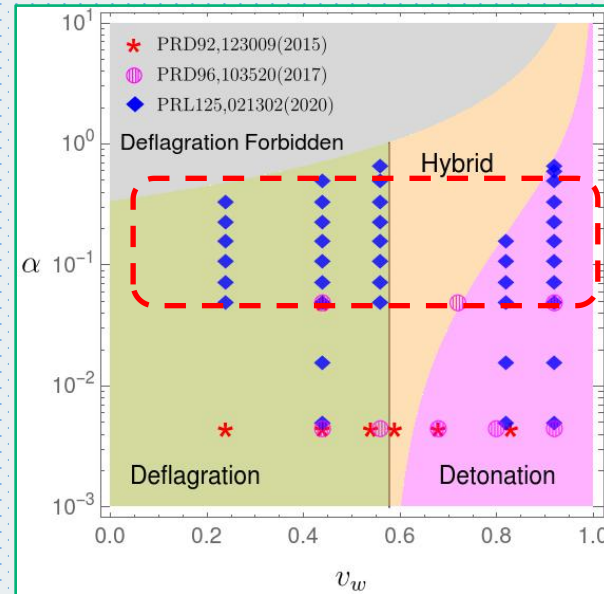
$$v_{\mathbf{q}}^i = \sum_{n=1}^{N_b} v_{\mathbf{q}}^{i(n)}$$



Numerical Simulation

- Suppression found for strong transitions with small v_w
- Need to cover more parameter space (very strong PT)

$$h^2 \Omega_{\text{sw}}(f) = 2.65 \times 10^{-6} \left(\frac{100}{g_*} \right)^{\frac{1}{3}} \left(\frac{H_*}{\beta} \right) \left(\frac{\kappa_{\text{sw}} \alpha}{1 + \alpha} \right)^2 v_w S_{\text{sw}}(f) \Upsilon(\tau_{\text{sw}})$$



Cutting, Hindmarsh, Weir, PRL [1906.00480]

Magnetohydrodynamic Turbulence

Earlier studies based on Kolmogorov spectrum:

Kamionkowski, Kosowsky, Turner, PRD [9310044]

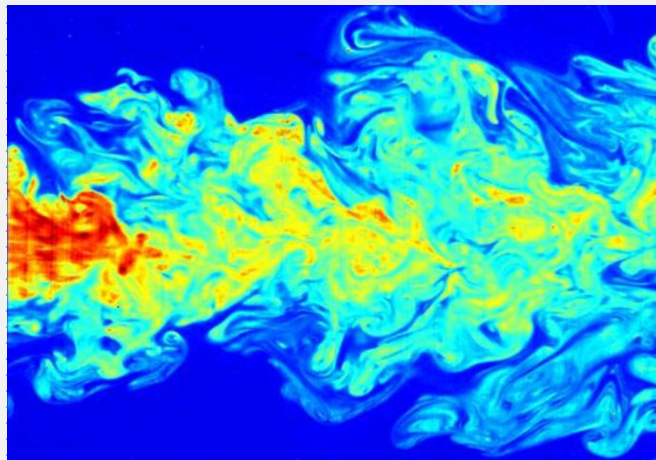
Kosowsky, Mack, Kahniashvili, PRD [0111483]

Gogoberidze, Kahniashvili, Kosowsky, PRD [0705.1733]

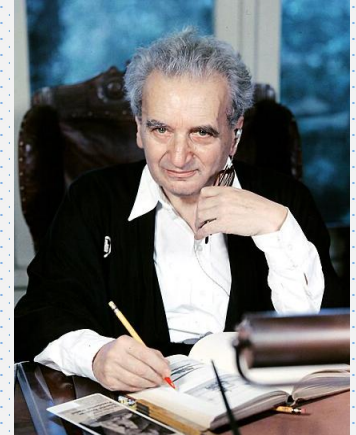
$$T^{ij} \sim (p + e)v^i v^j - B_i B_j$$

$$h^2 \Omega_{\text{turb}}(f) = 3.35 \times 10^{-4} \left(\frac{H_*}{\beta} \right) \left(\frac{\kappa_{\text{turb}} \alpha}{1 + \alpha} \right)^{\frac{3}{2}} \left(\frac{100}{g_*} \right)^{1/3} v_w S_{\text{turb}}(f)$$

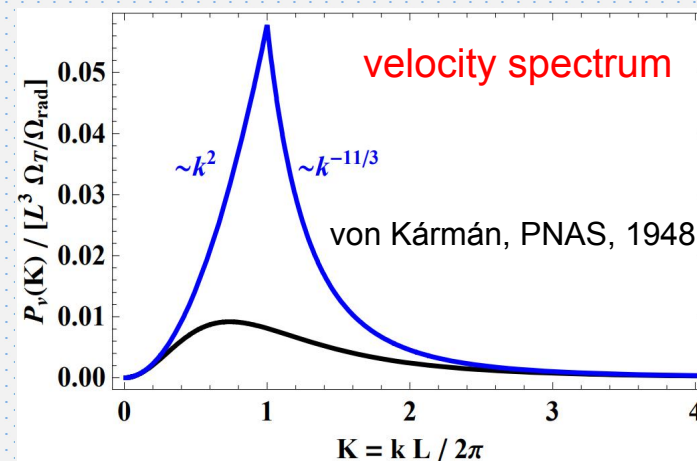
Caprini, Durrer, Servant, JCAP [0909.0622] (used von Kármán's spectrum)



Andrey Nikolaevich Kolmogorov



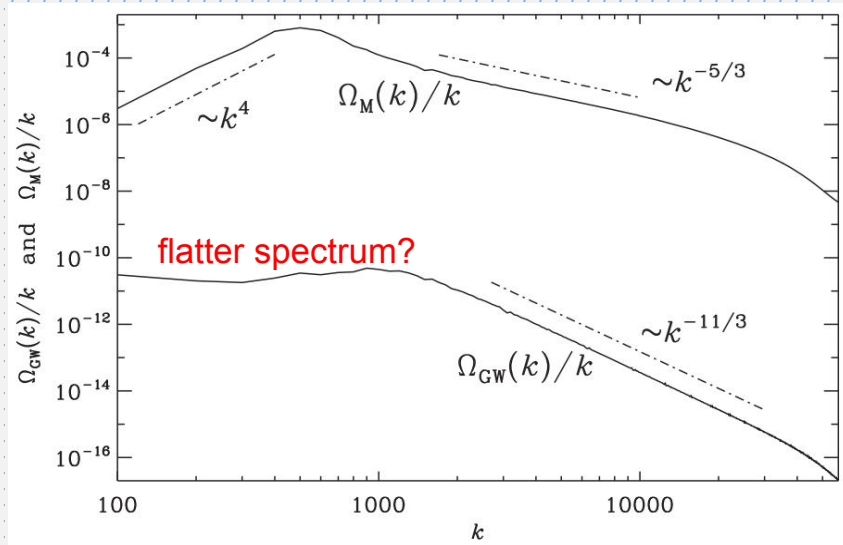
Theodore von Kármán



Magnetohydrodynamic Turbulence: Recent Development

Progress on **numerical** simulations, and **analytical** modellings

- Strong dependence on initial conditions
- Flatter spectrum at low frequency (violate causality?)

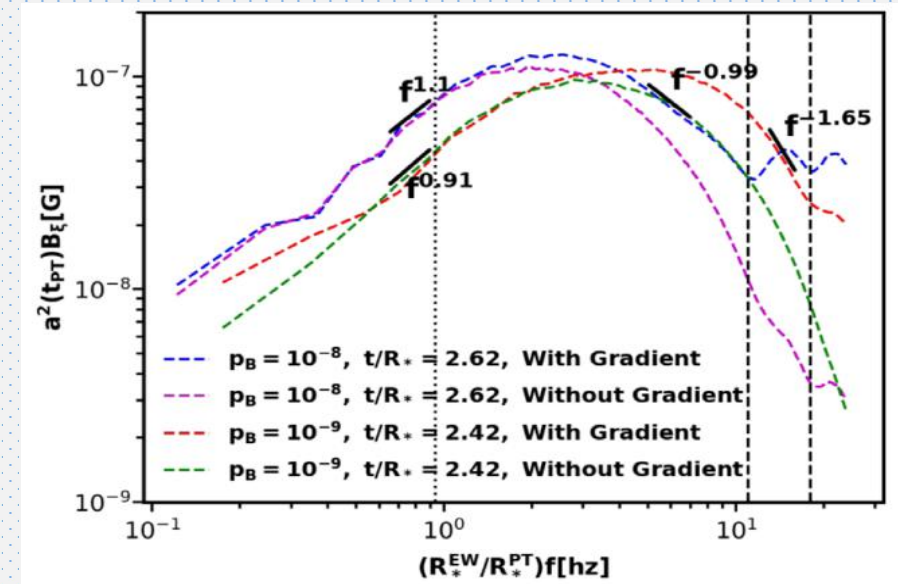


Pol et al, PRD [1903.08585]

- Modelling: Sharma, Brandenburg, PRD [2206.00055]
- Time decorrelation: Auclair et al, JCAP [2205.02588]
- Decay, viscosity: Dahl et al, PRD [2112.12013]
- Polarization: Pol et al, JCAP [2107.05356]

← as initial conditions?

Magnetic Field Generation (simulation)



Di, Wang, Zhou, Bian, Cai, PRL [2012.15625]
Yang, Bian, PRD [2102.01398]

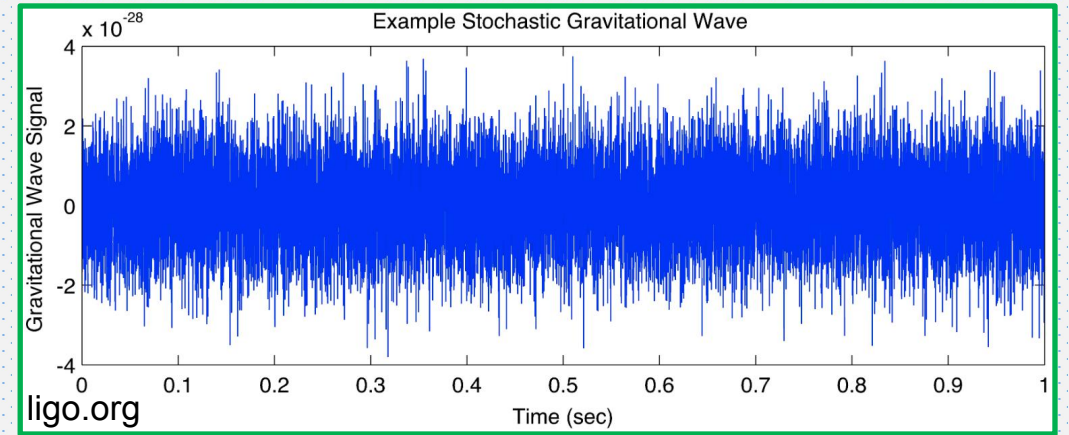
Detection at LIGO

Romero, Martinovic, Callister, HG, Martínez, Sakellariadou, Yang, Zhao, PRL [2102.01714]

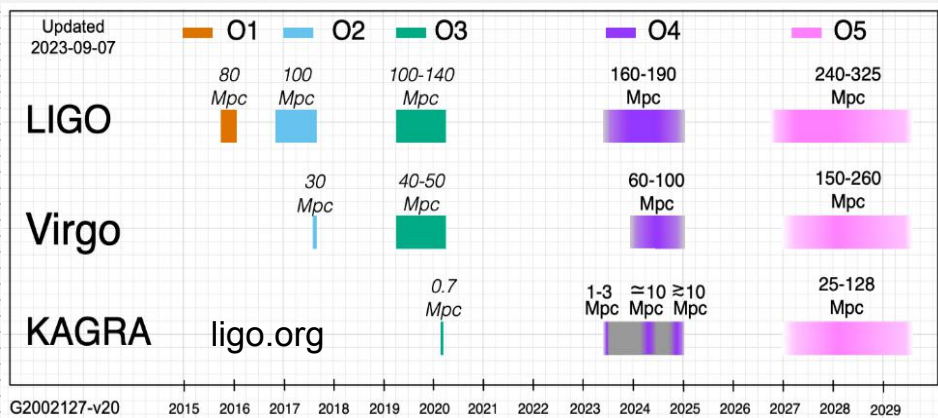
- No Evidence for Broken Power Law Signal
- No Evidence for Bubble Collision Domination Signal
- No Evidence for Sound Waves Domination Signal

See also: Jiang, Huang, JCAP [2203.11781], Yu, Wang, PRD [2211.13111]

stochastic GWs: noise-like



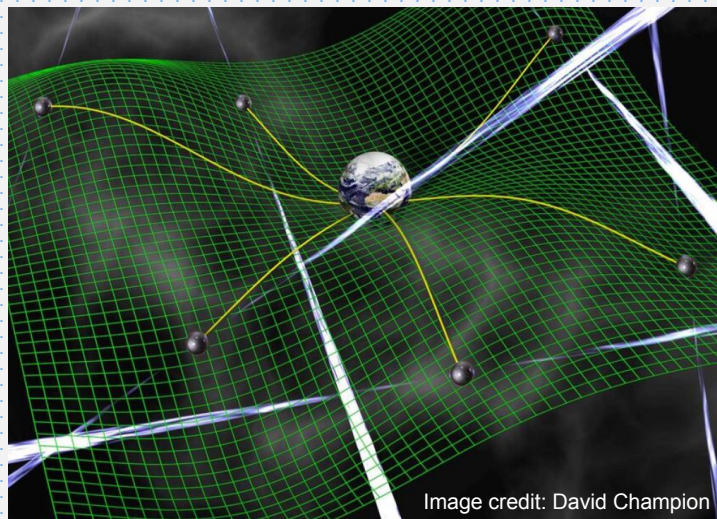
O1+O2+O3@LIGO (H1, L1), Virgo



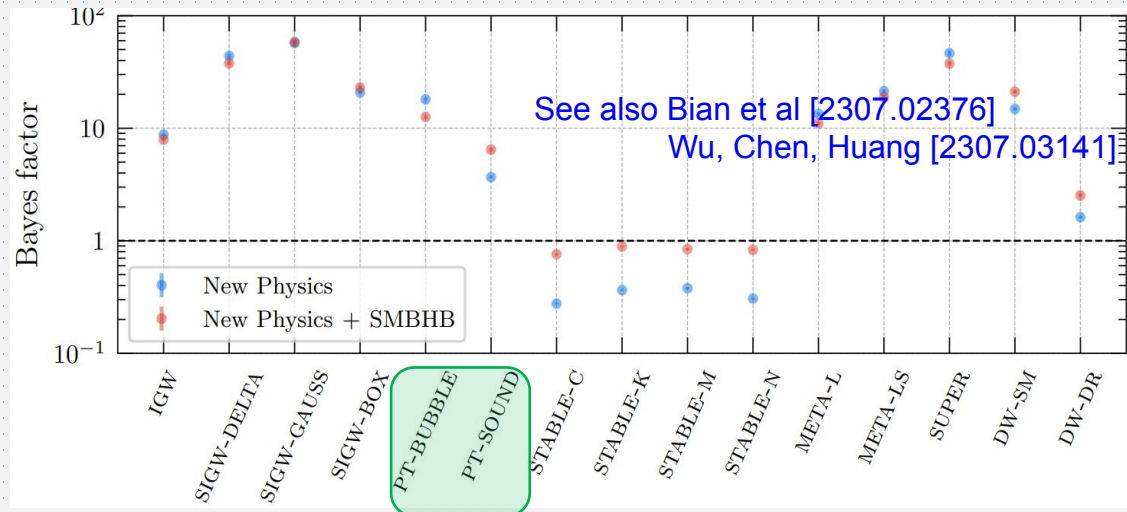
solution:
cross-correlation



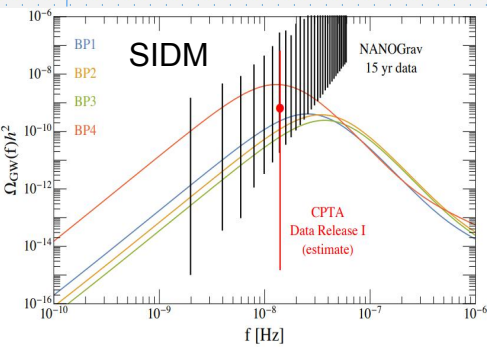
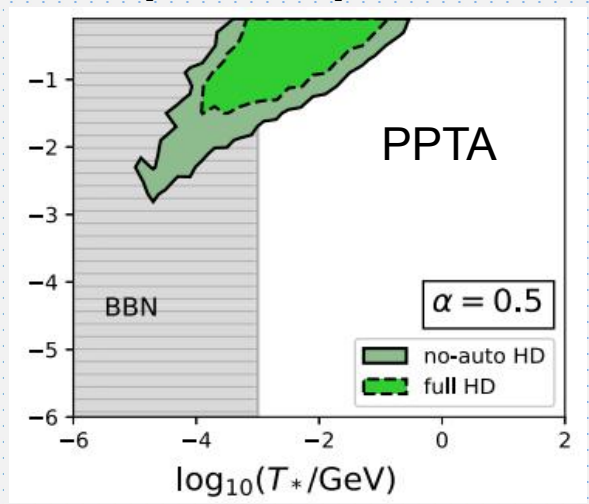
PTA



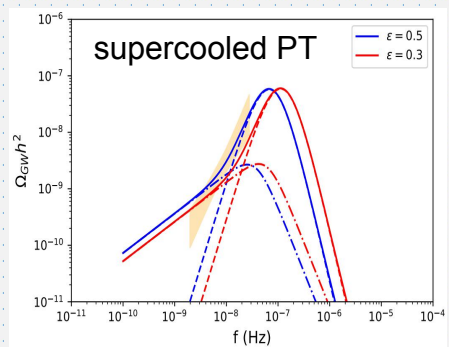
NANOGrav, ApJL [2306.16219]



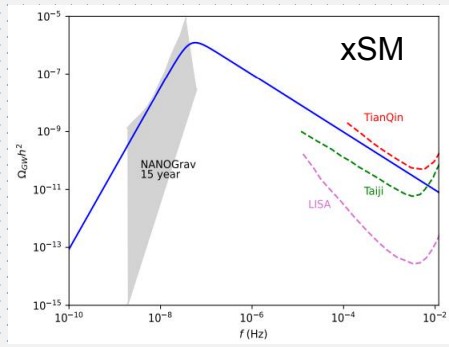
Xue, Bian, Shu, Yuan, Zhu, et al, PRL [2110.03096]



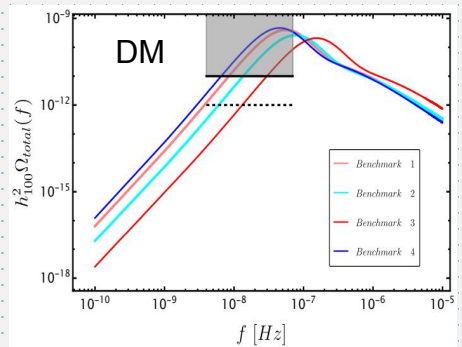
Han, Xie, Yang, Zhang [2306.16966]



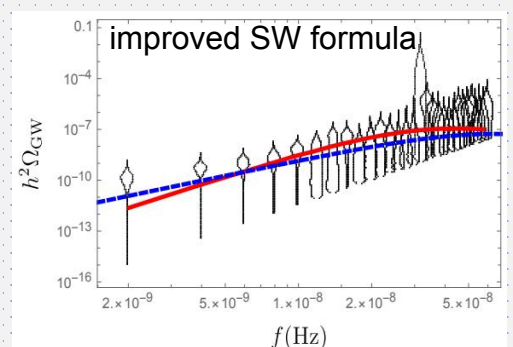
Zu, Zhang, Li, Gu, Tsai, Fan [2306.17239]



Xiao, Yang, Zhang [2307.01072]



Yang, Ma, Jiang, Huang [2306.17827]



Ghosh, Ghoshal, HG, ... [2307.02259]

and many more...

Uncertainties

- Finite T effective potential calculations
- Phase transition parameter calculations (vw)
- GW spectra calculations (simulations, modellings)

$\Delta\Omega_{\text{GW}}/\Omega_{\text{GW}}$	4d approach	3d approach
RG scale dependence	$\mathcal{O}(10^2 - 10^3)$	$\mathcal{O}(10^0 - 10^1)$
Gauge dependence	$\mathcal{O}(10^1)$	$\mathcal{O}(10^{-3})$
High- T approximation	$\mathcal{O}(10^{-1} - 10^0)$	$\mathcal{O}(10^0 - 10^2)$
Higher loop orders	unknown	$\mathcal{O}(10^0 - 10^1)$
Nucleation corrections	unknown	$\mathcal{O}(10^{-1} - 10^0)$
Nonperturbative corrections	unknown	unknown

Croon, Gould, Schicho, Tenkanen, White, JHEP [2009.10080]

Uncertainty	pre-factor1	pre-factor2	pre-factor3
T_p	0.003%	0.003%	0.002%
βR^*	8.1%	7.9%	5.9%
N_{tot}	11.4%	11.0%	9.8%
$f_{\beta R^*}^{\text{peak}}$	11.8%	12.0%	14.1%
$\Omega_{\text{GW}} h_{\beta R^*}^2$	37.6%	36.5%	28.9%
$f_{\text{sim}}^{\text{peak}}$	36.4%	36.4%	35.1%
$\Omega_{\text{GW}} h_{\text{sim}}^2$	334.0%	330.8%	336.7%

HG, Xiao, Yang, Zhang [2310.04654]

Effect (fixed wall velocity)	Range of error (medium)	Range of error (low)	Type of error
Transition temperature	$\mathcal{O}(10^{-4} - 10^1)$	$\mathcal{O}(10^{-1} - 10^0)$	Random
Mean bubble separation	$\mathcal{O}(0 - 10^{-1})$	$\mathcal{O}(10^{-1} - 10^0)$	Suppression
Fluid velocity	$\mathcal{O}(10^{-2} - 10^0)$	$\mathcal{O}(10^{-2} - 10^0)$	Random
Finite lifetime	$\mathcal{O}(10^{-3} - 10^{-1})$	$\mathcal{O}(10^1 - 10^3)$	Enhancement
Vorticity effects	$\mathcal{O}(10^{-1} - 10^0)$	—	Random

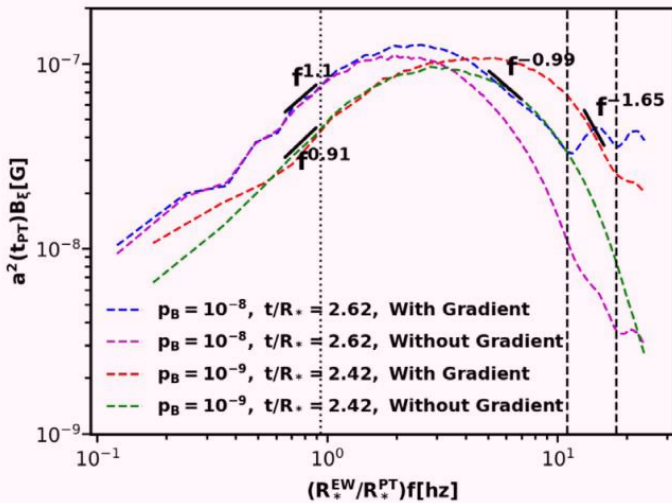
HG, Sinha, Vagie, White, JHEP [2103.06933]

Sound speed: Wang, Huang, Li, PRD [2112.14650], etc

See also: Athron, Balazs, Fowlie, Morris, White, Yang Zhang, JHEP [2208.01319]

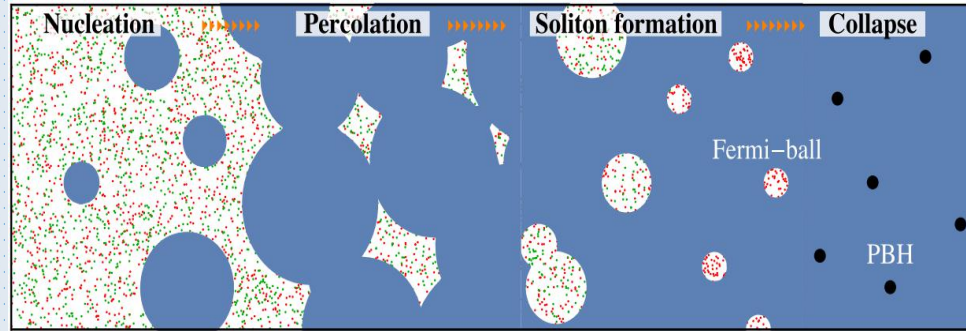
New Observables

Primordial magnetic field



Di, Wang, Zhou, Bian, Cai, PRL [2012.15625]
 Yang, Bian, PRD [2102.01398], ...

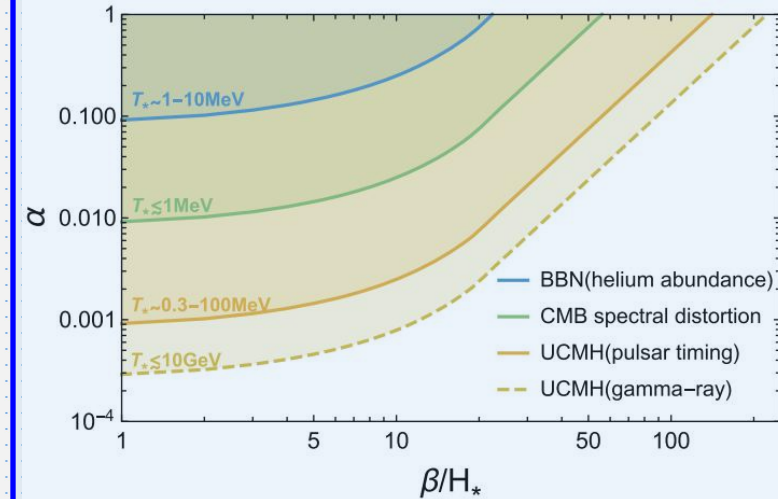
Primordial black holes and Solitons



Hong, Jung, Xie, PRD [2008.04430]
 Kawana, Xie, PLB [2106.00111]
 Lu, Kawana, Xie, PRD [2202.03439]
 Liu, Bian, Cai, Guo, Wang, PRD [2106.05637]

and more...

Curvature perturbations



Liu, Bian, Cai, Guo, Wang, PRL [2208.14086]
 Jiang, Liu, Sun, Wang, PLB [1512.07538]

GW Anisotropy: Geller, Hook, Sundrum, Yuhsin Tsai, PRL [1803.10780]
 Li, Huang, Wang, Zhang, PRD [2112.01409]
 Li, Yan, Huang, PRD [2211.03368]

Dissipative Effects as New Observables

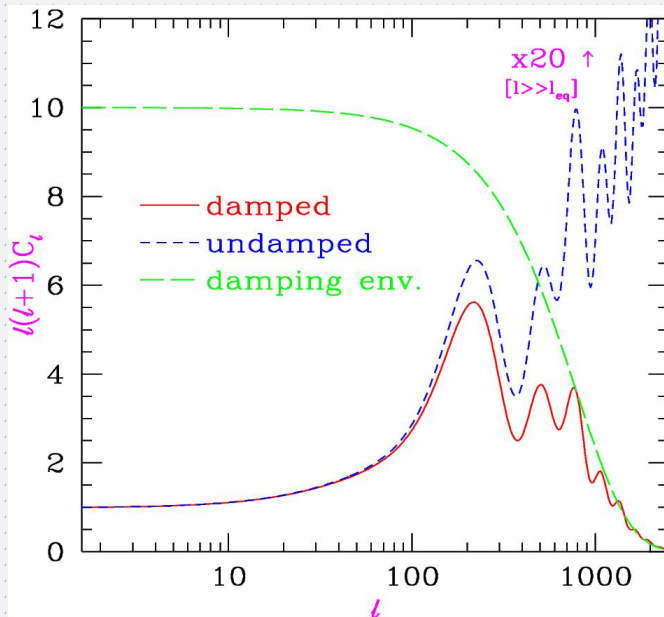
- Going beyond the perfect fluid approximation (viscosity, heat conduction)
- Particle physics origin of dissipations (very weak interactions)
- Can be searched for at LIGO, PTA, LISA/Taiji/Tianqin ...

Weinberg, ApJ, 1971

$$\Delta T^{ij} = -\eta \left(\frac{\partial U_i}{\partial x^j} + \frac{\partial U_j}{\partial x^i} - \frac{2}{3} \delta_{ij} \nabla \cdot \mathbf{U} \right) - \zeta \delta_{ij} \nabla \cdot \mathbf{U},$$

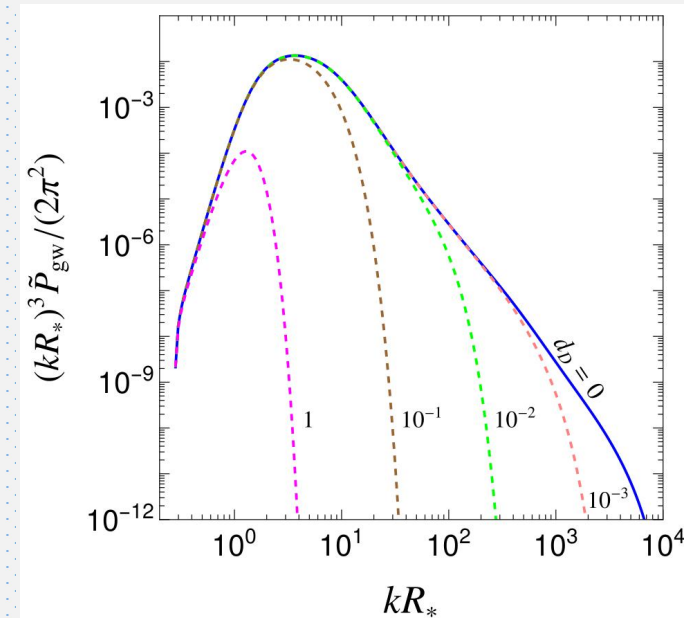
$$\Delta T^{i0} = -\chi \left(\frac{\partial T}{\partial x^i} + T \dot{U}_i \right). \quad (1)$$

Silk damping of CMB Anisotropy



Hu, White, ApJ [9609079]

damping of GW



HG [2310.10927]

Summary

- Significant advances in phenomenological studies
- Significant advances in PT and GW calculations
- Significant advances in experimental detections (LIGO, PTA, etc)
- More work to be done to probe better particle physics

Thanks!