

# Quantum Computing for High Energy Physics

Dec. 17, 2023@第十七届TeV工作组学术研讨会

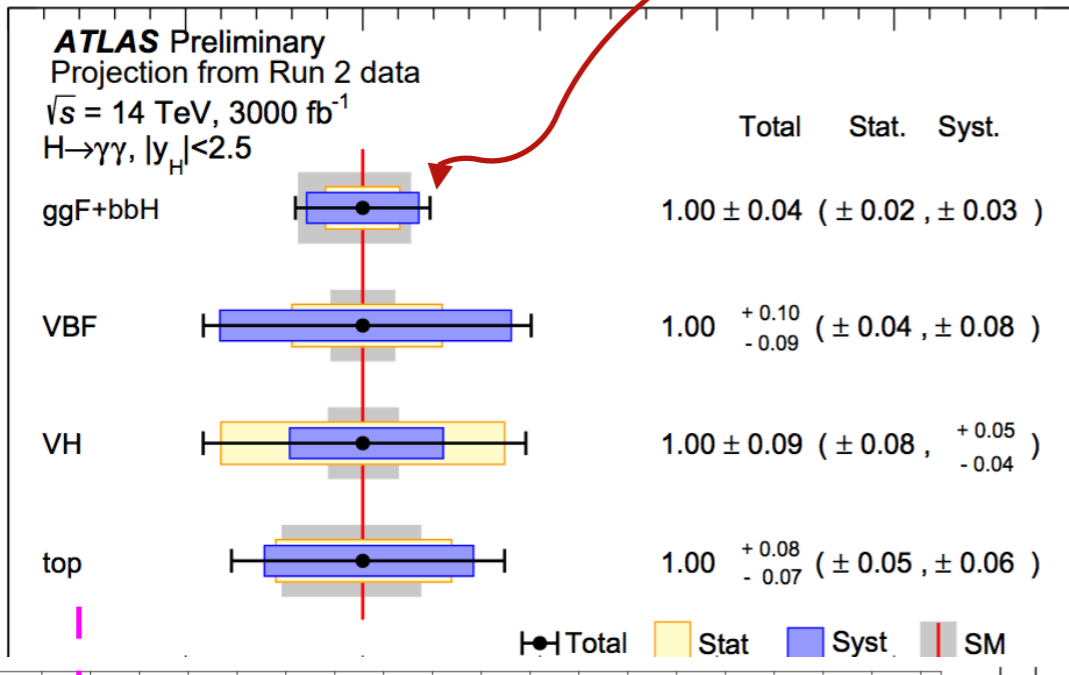
Theoretical inputs  
to colliders

theoretical uncertainties

real-time dynamics  $\langle \text{out} | e^{-iH[\psi]t} | \text{in} \rangle$

PDF

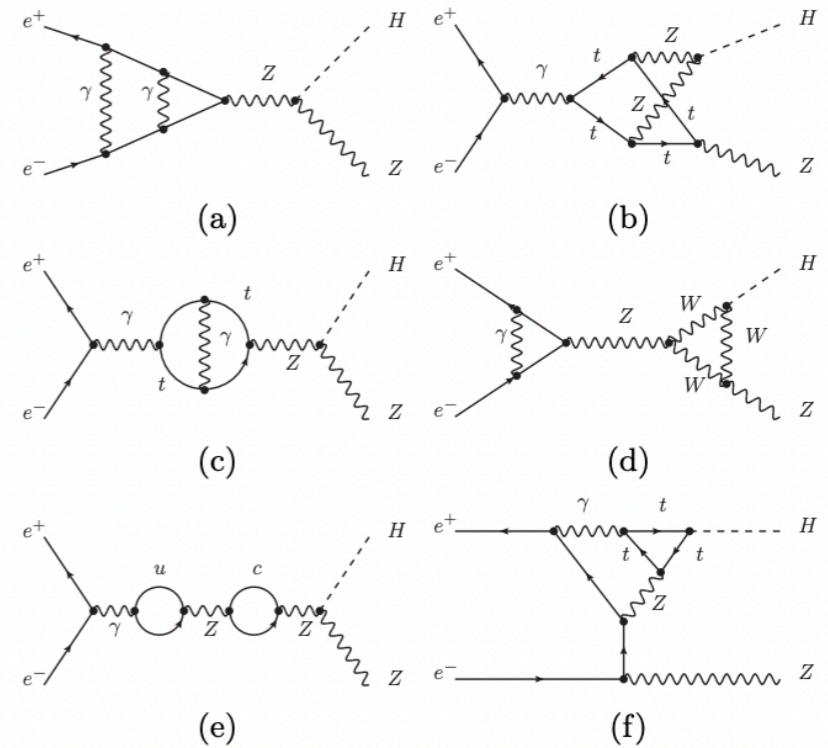
higher order corrections



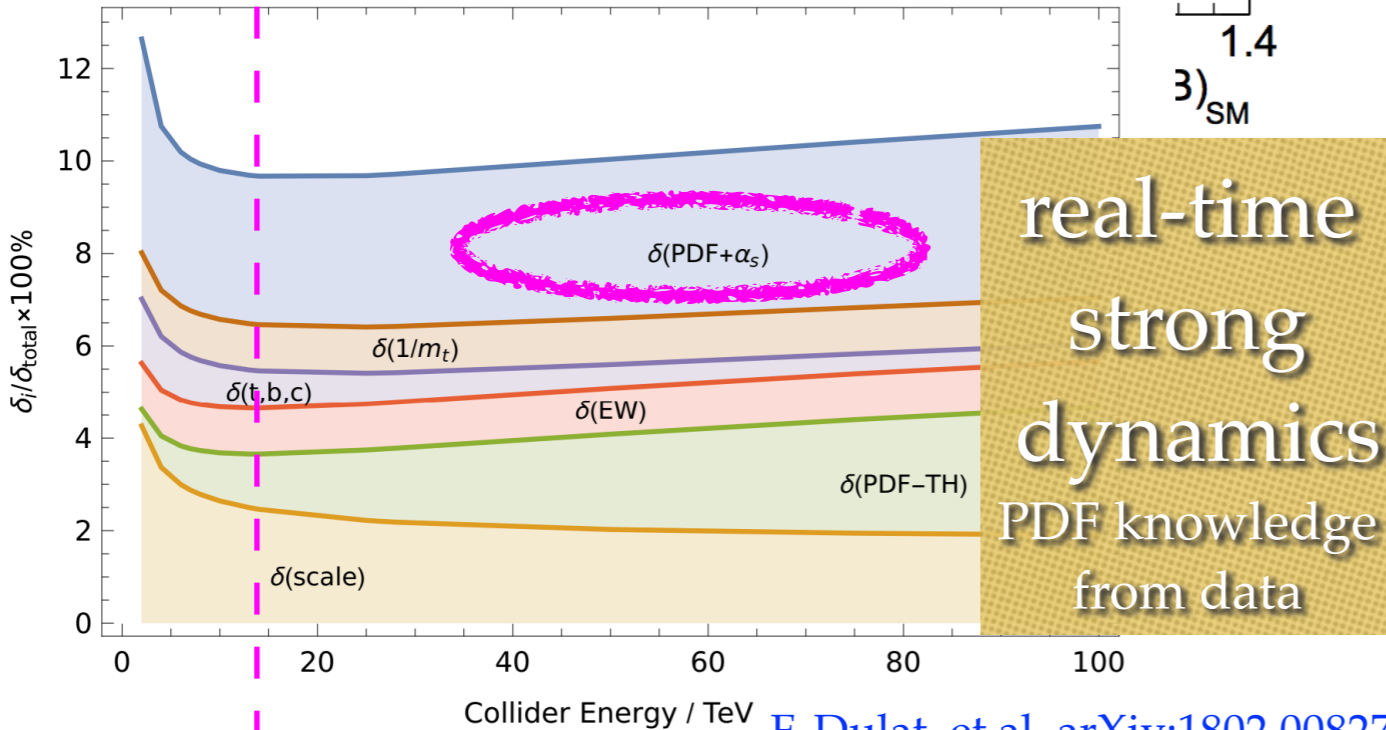
CEPC :  $\sigma(e^+e^- \rightarrow ZH), 0.51\%$

NLO EW  
NNLO EW-QCD 1%

complete two loop



F. An, et al, arXiv:1810.09037  
Y. Gong et al., Q. -F. Sun et al.,  
X. Chen et al., arXiv: 2209.14953



real-time  
strong  
dynamics  
PDF knowledge  
from data

F. Dulat, et al, arXiv:1802.00827  
M. Cepeda, et al, arXiv:1902.00134

# Why Quantum Computing

lattice non-perturbative  
calculations

$$\langle O \rangle = \frac{\sum_{\mathcal{C}} O(\mathcal{C}) W(\mathcal{C})}{\sum_{\mathcal{C}} W(\mathcal{C})}$$

Imaginary time problem :  $W(\mathcal{C}) \sim \exp(-S(\mathcal{C}))$

complex  $S(\mathcal{C})$  for non vanishing  $\theta$

real-time dynamics, finite density...

Sign Problem!!!

configuration space  $\mathcal{C}$  is  
exponentially large in system size

out-of-equilibrium,  
non-perturbative  
higher order processes,  
quantum interference  
cannot be solved classically  
due to theoretical or  
computational limitations:

**sign problem or rare events  
that has  
exponential-scaling of the  
complexity**

# Why Quantum Computing

lattice non-perturbative calculations

$$\langle O \rangle = \frac{\sum_{\mathcal{C}} O(\mathcal{C}) W(\mathcal{C})}{\sum_{\mathcal{C}} W(\mathcal{C})}$$

Imaginary time problem :  $W(\mathcal{C}) \sim \exp(-S(\mathcal{C}))$

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Sign Problem!!!

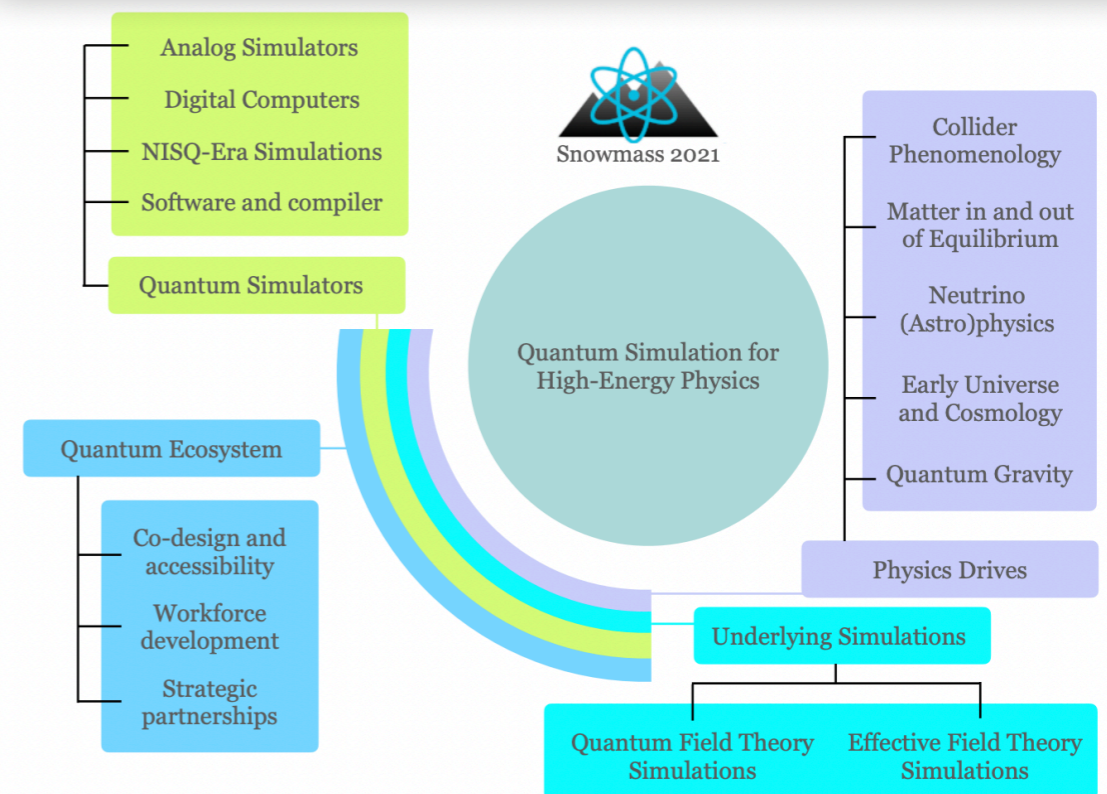
configuration space  $\mathcal{C}$  is exponentially large in system size

$$\langle x | e^{-iHt} | y \rangle = \int \mathcal{D}\phi e^{iS}$$

[PRX Quantum 4 (2023) 2, 027001]

## Quantum Simulation for High Energy Physics

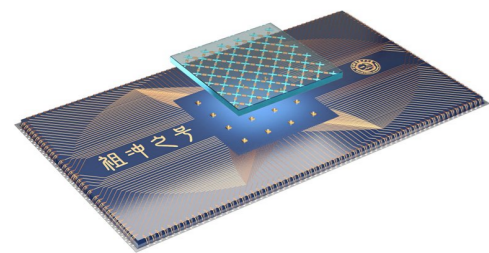
Christian W. Bauer,<sup>1, a</sup> Zohreh Davoudi,<sup>2, b</sup> A. Baha Balantekin,<sup>3</sup> Tanmoy Bhattacharya,<sup>4</sup>  
 Marcela Carena,<sup>5, 6, 7, 8</sup> Wibe A. de Jong,<sup>1</sup> Patrick Draper,<sup>9</sup> Aida El-Khadra,<sup>9</sup>  
 Nate Gemelke,<sup>10</sup> Masanori Hanada,<sup>11</sup> Dmitri Kharzeev,<sup>12, 13</sup> Henry Lamm,<sup>5</sup>  
 Ying-Ying Li,<sup>5</sup> Junyu Liu,<sup>14, 15</sup> Mikhail Lukin,<sup>16</sup> Yannick Meurice,<sup>17</sup>  
 Christopher Monroe,<sup>18, 19, 20, 21</sup> Benjamin Nachman,<sup>1</sup> Guido Pagano,<sup>22</sup> John Preskill,<sup>23</sup>  
 Enrico Rinaldi,<sup>24, 25, 26</sup> Alessandro Roggero,<sup>27, 28</sup> David I. Santiago,<sup>29, 30</sup>  
 Martin J. Savage,<sup>31</sup> Irfan Siddiqi,<sup>29, 30, 32</sup> George Siopsis,<sup>33</sup> David Van Zanten,<sup>5</sup>  
 Nathan Wiebe,<sup>34, 35</sup> Yukari Yamauchi,<sup>2</sup> Kübra Yeter-Aydeniz,<sup>36</sup> and Silvia Zorzetti<sup>5</sup>



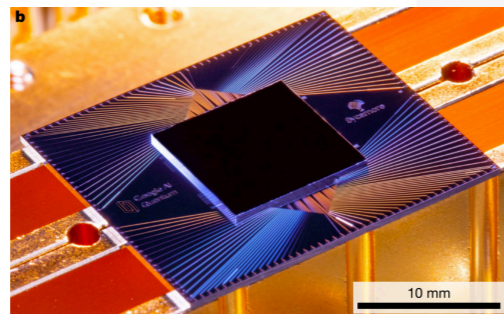
# Rapidly improving universal quantum computing hardware

Superconducting Processor

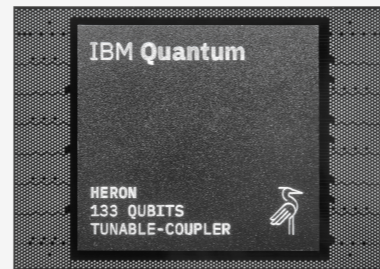
multi-chip quantum processor



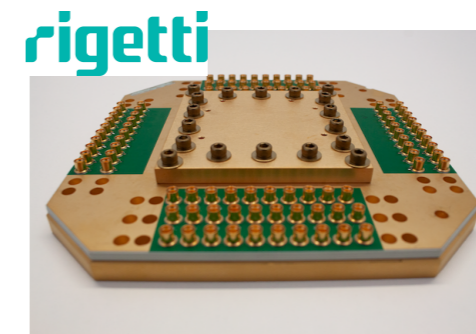
176 qubits



54 qubits

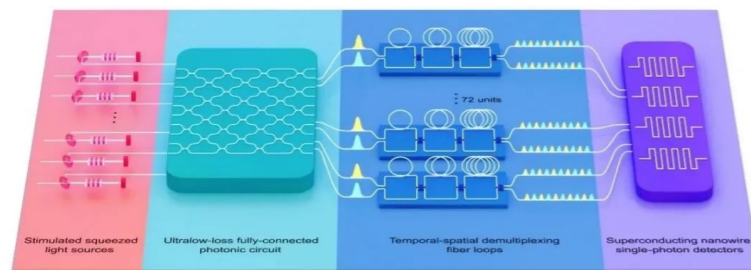


1121 qubits  
access to 133 qubits  
trapped ion qubits

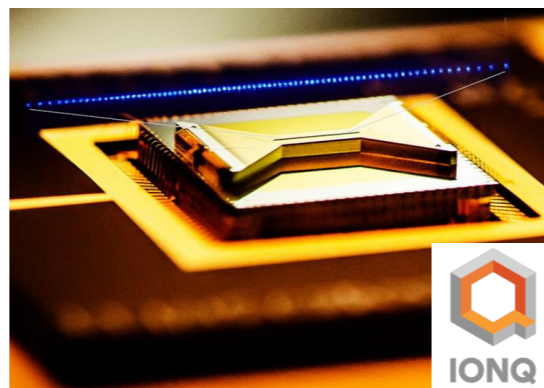


80 qubits

Photon qubits



九章三号 - 255 qubits



22 qubits

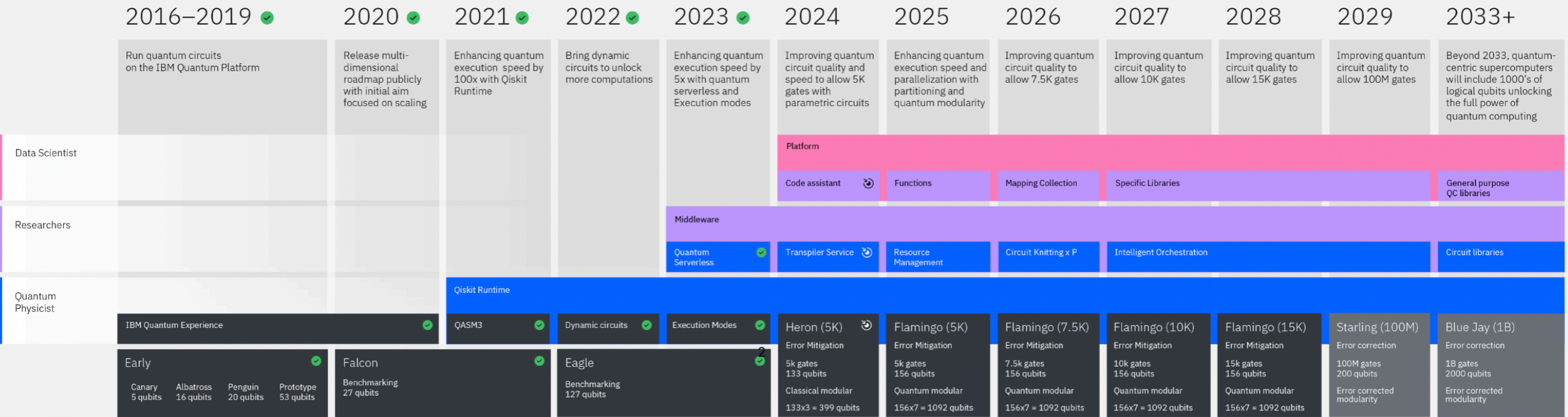
neutral atoms  
48 logical Qubits,  
hundreds of entangling logical operations



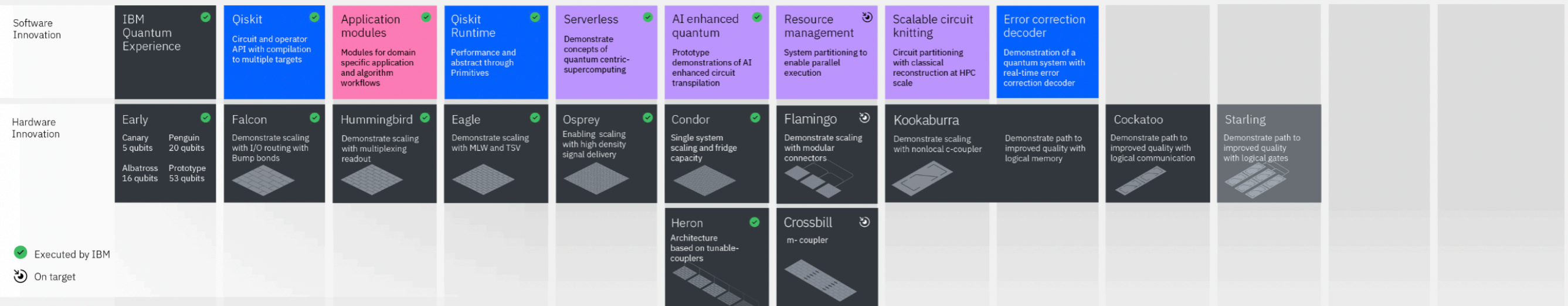
# Rapidly improving universal quantum computing hardware

## Development Roadmap

IBM Quantum



## Innovation Roadmap



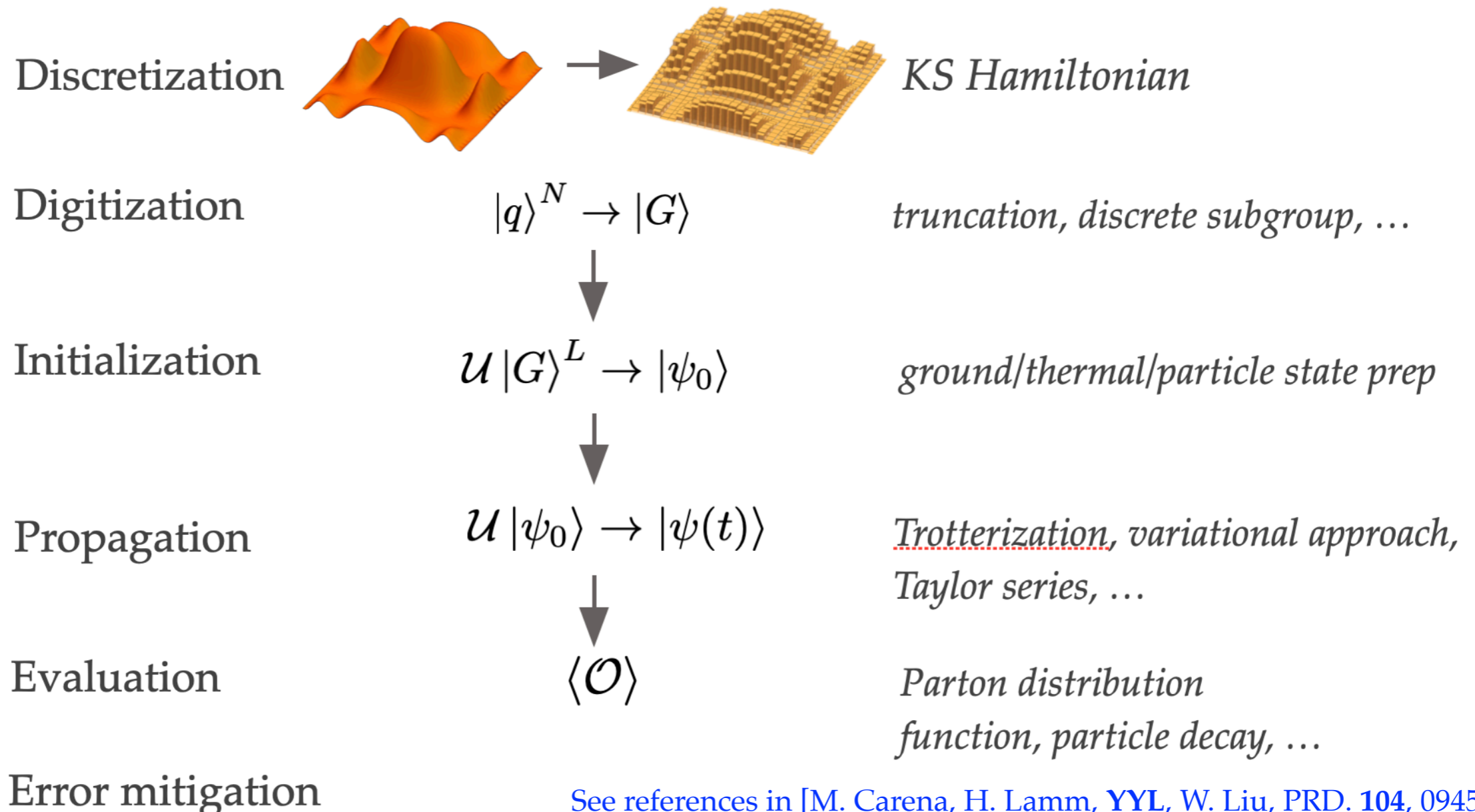
Executed by IBM  
On target

IBM Quantum / © 2023 IBM Corporation

# Quantum Simulation for Quantum Field Theory

Bosonic and fermionic DOF,  
Dynamical and coupled global and local (gauge) symmetries,  
Relativistic - particle number non-conservation,  
Nontrivial vacuum state in strongly interacting theories

## “Galactic Algorithms”



See references in [M. Carena, H. Lamm, YYL, W. Liu, PRD. 104, 094519]

Discretization

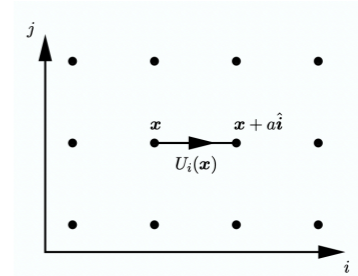


infinities in QFT

$$H = \int d^d x \text{Tr} (\mathbf{E}^2 + \mathbf{B}^2)$$

gauge invariance

$$U_{\square} = \exp \left\{ ig \oint_{\square} A \cdot dx \right\}$$



$$U_i(x) = e^{ig \int_a^0 dt A_i(x+t\hat{i})}$$

Kogut and Susskind formulation: [Phys. Rev. D **11**, 395 (1975)]

$$H = \underbrace{-t \sum_{\langle xy \rangle} s_{xy} (\psi_x^\dagger U_{xy} \psi_y + \psi_y^\dagger U_{xy}^\dagger \psi_x)}_{\text{fermion kinetic}} + \underbrace{m \sum_x s_x \psi_x^\dagger \psi_x}_{\text{fermion mass}} + \underbrace{\frac{g^2}{2} \sum_x \mathbf{E}(x)^2}_{\text{energy of electric field}} - \underbrace{\frac{1}{4g^2} \sum_{\square} \text{Tr} (U_{\square} + U_{\square}^\dagger)}_{\text{energy of magnetic field}}$$



Discretization



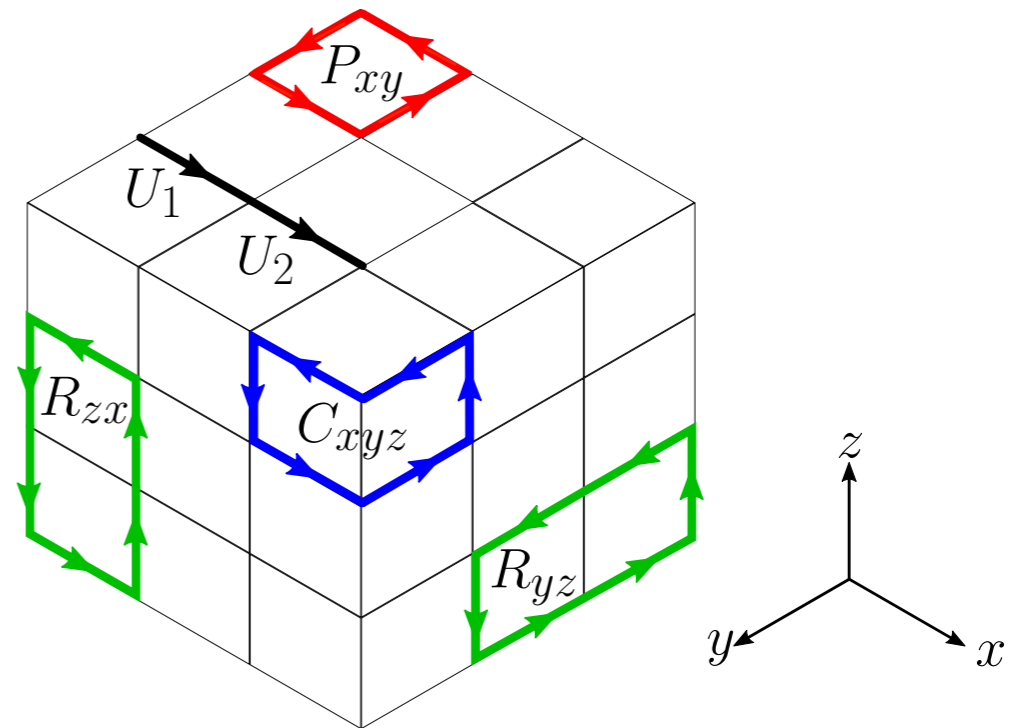
[J. Carlsson, et al, hep-lat/0105018]

$$P_{ij}(x) = 1 - \frac{1}{N} \text{ReTr} \exp \left\{ ig \oint_{\square} A \cdot dx \right\} \approx \frac{g^2 a^4}{2N} \text{Tr} \{ F_{ij}(x) F_{ij}(x) \} + \frac{g^2 a^6}{12N} \text{Tr} \{ F_{ij}(x) (D_i^2 + D_j^2) F_{ij}(x) \} + \dots$$

deviations from the continuum start from  $a^2$  error, classical computational resources proportional  $a^{-k}$  to for Wilson action

$$R_{ij}(x) = 1 - \frac{1}{N} \text{ReTr} \left\{ \begin{array}{c} \text{rectangle} \\ i \quad j \end{array} \right\} = \frac{4g^2 a^4}{2N} \text{Tr} \{ F_{ij}(x) F_{ij}(x) \} + \frac{4g^2 a^6}{24N} \text{Tr} \{ F_{ij}(x) (4D_i^2 + D_j^2) F_{ij}(x) \} + \dots$$

deviations from the continuum starts from  $a^2 g^2$  at quantum level



Discretization



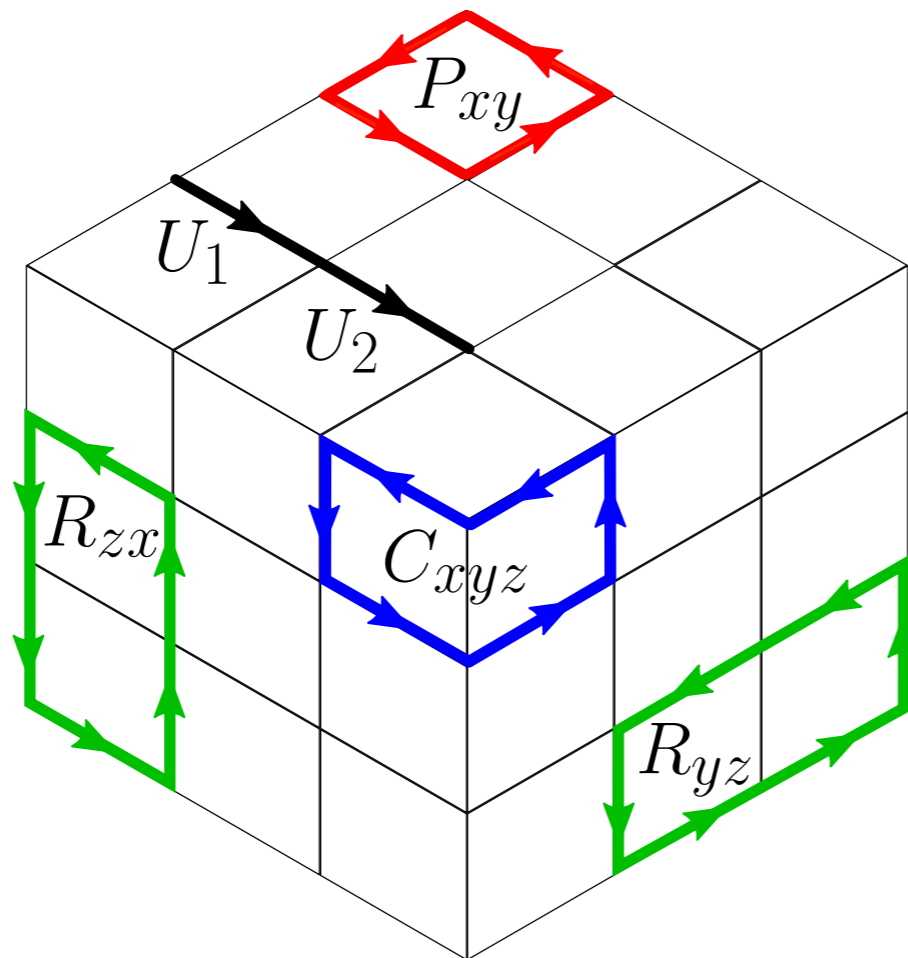
$$H_I = K_I + V_I$$

$$V_I = \beta_{V0} V_{KS} + \beta_{V1} V_{\text{rect}}$$

$$K_I = \beta_{K0} K_{KS} + \beta_{K1} K_{2L}$$

$$V_{\text{rect}} = \frac{2}{ag_s^2} \sum_{\mathbf{x}, i < j} \text{Re Tr} [R_{ij}(\mathbf{x}) + R_{ji}(\mathbf{x})]$$

$$\begin{aligned} K_{2L} &= \frac{g_t^2}{a} \sum_{\mathbf{x}, i} \text{Tr} [L_i(\mathbf{x}) U_i(\mathbf{x}) L_i(\mathbf{x} + a\mathbf{i}) U_i^\dagger(\mathbf{x})] \\ &= \frac{g_t^2}{a} \sum_{x, i} \text{Tr} [R_i(\mathbf{x}) L_i(\mathbf{x} + a\mathbf{i})] \end{aligned}$$

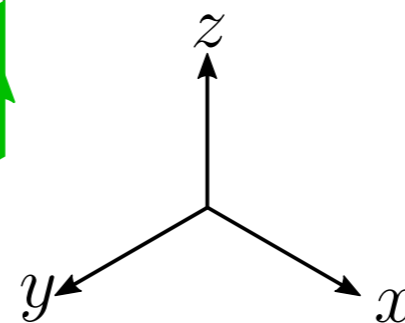


[M. Alford, et al, hep-lat/9507010, ...]

$$a \rightarrow 2a$$

$$N_q \sim \left(\frac{L}{a}\right)^d$$

[Demonstration with the improved Hamiltonian is still needed]



[M. Carena, H. Lamm, YYL, W. Liu, PRL. 129, 051601]

Digitization

$$|q\rangle^N \rightarrow |G\rangle$$

infinities in QFT

Kogut and Susskind formulation: [\[Phys. Rev. D 11, 395 \(1975\)\]](#)

$$H = -t \sum_{\langle xy \rangle} s_{xy} (\psi_x^\dagger U_{xy} \psi_y + \psi_y^\dagger U_{xy}^\dagger \psi_x) + m \sum_x s_x \psi_x^\dagger \psi_x + \frac{g^2}{2} \sum_x \mathbf{E}(x)^2 - \frac{1}{4g^2} \sum_{\square} \text{Tr} (U_{\square} + U_{\square}^\dagger)$$

continuous field variables

## infinities in QFT

Kogut and Susskind formulation: [Phys. Rev. D 11, 395 (1975)]

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continuous field variables

## rapid development with its own pros and cons

*rate of convergences to the infinite-dimensional theory, resource requirements,  
local and global gauge symmetry*

Casimir dynamics, Natalie et al

LSH formalism, Mathur et al, Anishetty et al

Group-element basis and discrete subgroups, Erez et al, Lamm et al, Carena et al

Magnetic or dual representations, Mathur et al, Bauer et al

Tensor renormalization group (character expansion, Fourier series), Meurice et al

Light-front quantization (light-cone instead of fixed time-slicing), Mannheim et al

Quantum link models / qubit regularization (critical point), Brower et al

Matrix models (dimension reduction), Shen et al

$$|q\rangle^N \rightarrow |G\rangle$$

infinities in QFT

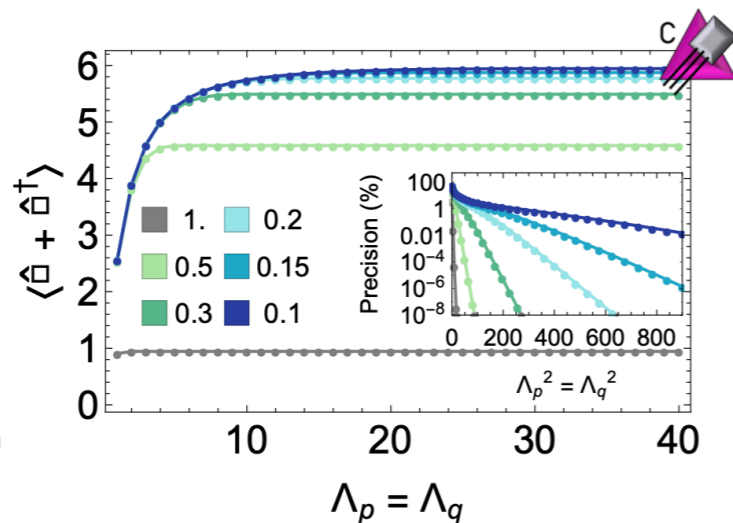
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$$H = -t \sum_{\langle xy \rangle} s_{xy} (\psi_x^\dagger U_{xy} \psi_y + \psi_y^\dagger U_{xy}^\dagger \psi_x) + m \sum_x s_x \psi_x^\dagger \psi_x + \frac{g^2}{2} \sum_x \mathbf{E}(x)^2 - \frac{1}{4g^2} \sum_{\square} \text{Tr} (U_{\square} + U_{\square}^\dagger)$$

continuous field variables

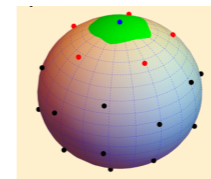
In angular momentum basis,  
truncated with cut-off  
 $SU(3)$  for one plaquette

$$\sum_b |\hat{\mathbf{E}}^{(b)}|^2 |p, q\rangle = \frac{p^2 + q^2 + pq + 3p + 3q}{3} |p, q\rangle$$



Ciavarella, Klco, and Savage,  
arXiv:2101.10227 [quant-ph]

group element basis -  
truncated with discrete subgroup



| $\xi_{1\text{-loop}}$ | $\xi$                       |
|-----------------------|-----------------------------|
|                       | $B\mathbb{I}$ $SU(2)$ [111] |
| 2.097                 | 2.099(1) ...                |
| 4.278                 | ... 4.35(19)                |
| 4.207                 | ... 4.22(11)                |
| 1.351                 | 1.369(19) ...               |
| 4.136                 | ... 4.08(9)                 |
| 1.351                 | 1.36(1) ...                 |

Carena, Gustafson, Lamm,  
YYL, Liu, PRD 106, 114504 (2022)

Digitization

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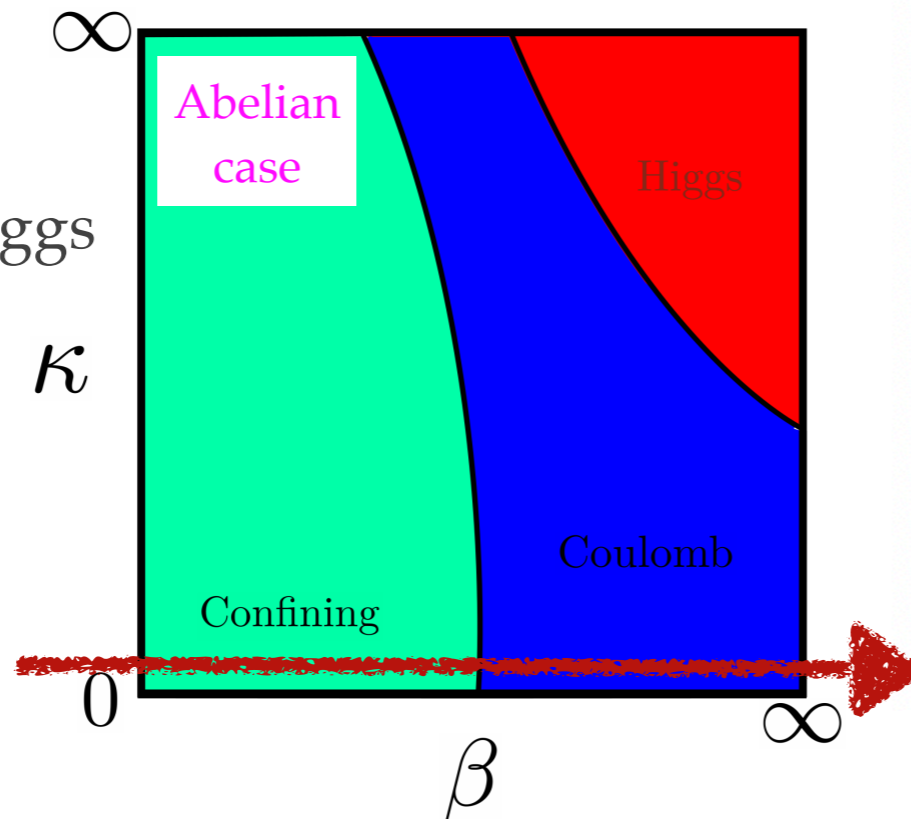
continuous field variables

Gauge field truncations with discrete group

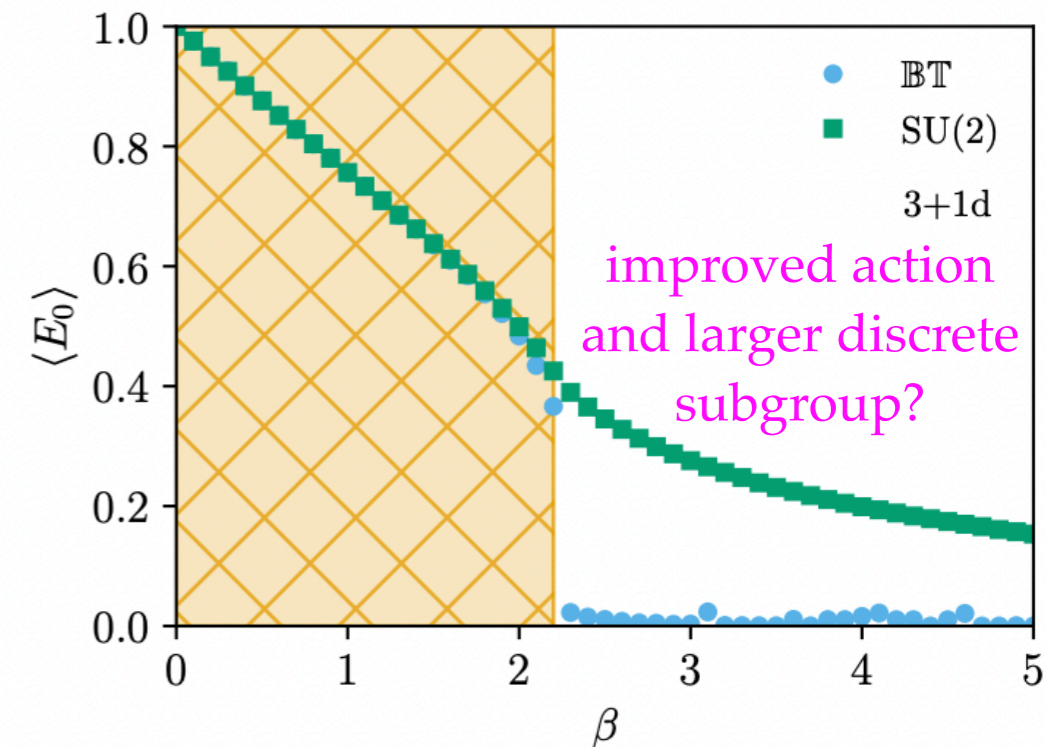
discrete group:

continuous group + Higgs

For non-Abelian  
gauge  
symmetry?



[Fradkin, Shenker, PRD. 19. 3682]



[Erik J. Gustafson et al., arXiv: 2208.12309]

Digitization

$$|q\rangle^N \rightarrow |G\rangle$$

infinities in QFT

Kogut and Susskind formulation: [\[Phys. Rev. D 11, 395 \(1975\)\]](#)

$$H = -t \sum_{\langle xy \rangle} s_{xy} (\psi_x^\dagger U_{xy} \psi_y + \psi_y^\dagger U_{xy}^\dagger \psi_x) + m \sum_x s_x \psi_x^\dagger \psi_x + \frac{g^2}{2} \sum_x \mathbf{E}(x)^2 - \frac{1}{4g^2} \sum_{\square} \text{Tr} (U_{\square} + U_{\square}^\dagger)$$

continuous field variables

Gauss's law operator

$$G^a(x) = -E_L^a(x) + E_R^a(x-1) + \psi^\dagger(x) T^a \psi(x)$$

$$G_x^a |P\rangle = 0$$

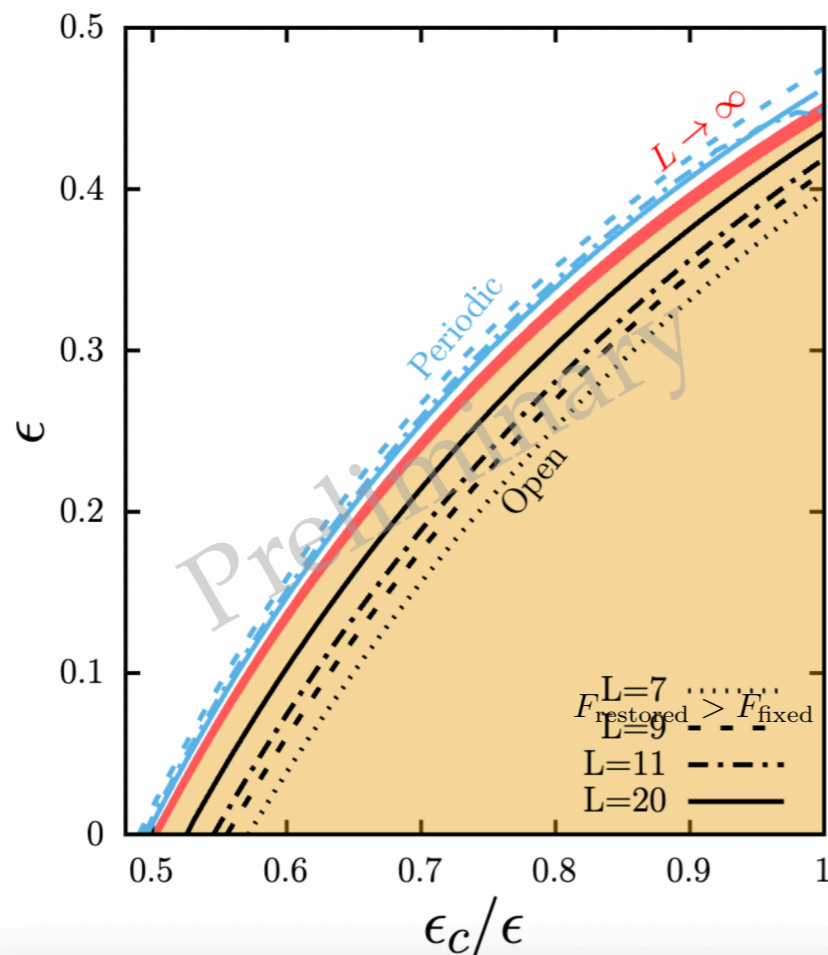
# Digitization

$$|q\rangle^N \rightarrow |G\rangle$$

Gauss's law operator  $G^a(x) = -E_L^a(x) + E_R^a(x-1) + \psi^\dagger(x)T^a\psi(x)$   $G_x^a |P\rangle = 0$

$\epsilon < \epsilon_{th}$  : redundancy makes the code more error-proof

$\epsilon > \epsilon_{th}$  : redundancy makes more errors than it can correct



gauge redundancy: resilience to quantum errors

[M. Carena, H. Lamm, YYL, W. Liu, in preparation]

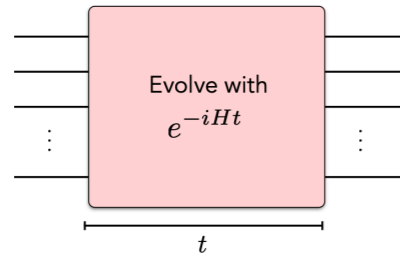
Gauge symmetry used for error corrections, see [Halimeh, et al.](#) [Lamm, et al.](#) ...



Propagation

$$\mathcal{U} |\psi_0\rangle \rightarrow |\psi(t)\rangle$$

ANALOG

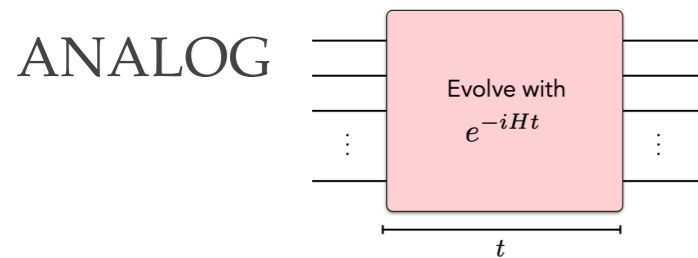


Cold neutral atoms, Trapped ions, Cavity quantum electrodynamics  
Superconducting circuits

...

# Propagation

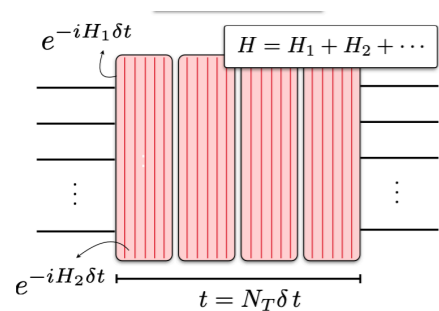
$$\mathcal{U} |\psi_0\rangle \rightarrow |\psi(t)\rangle$$



Cold neutral atoms, Trapped ions, Cavity quantum electrodynamics  
Superconducting circuits  
...

# DIGITAL

superconducting qubit/trapped-ion system



building blocks:  
one-qubit/two-qubit gate set

$$\|\mathcal{U} - e^{-iHt}\| < \epsilon$$

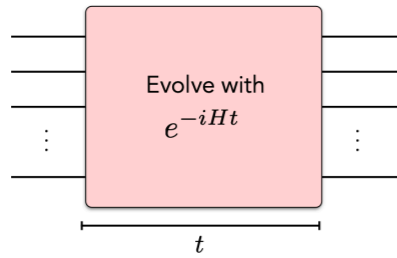
optimal asymptotically?  
overload of resources?  
easy implementation?

[Bauer et al, arXiv:2204.03381]

# Propagation

$$\mathcal{U} |\psi_0\rangle \rightarrow |\psi(t)\rangle$$

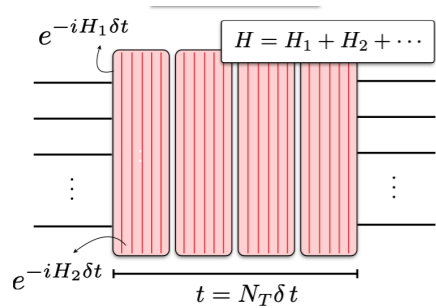
## ANALOG



Cold neutral atoms, Trapped ions, Cavity quantum electrodynamics  
Superconducting circuits  
...

## DIGITAL

superconducting qubit/trapped-ion system



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$$\|\mathcal{U} - e^{-iHt}\| < \epsilon$$

optimal asymptotically?  
overload of resources?  
easy implementation?

### Trotter-Suzuki decomposition

$$H = \sum_{l=1}^{\Gamma} H^{(l)}$$

$$\mathcal{U} = \left[ \prod_{l=1}^{\Gamma} e^{-itH^{(l)}/r} \right]^r$$

p-th order trotterization:  $\mathcal{O}\left(\left(\frac{t}{r}\right)^p\right)$

Errors depends on t and r  
No ancillary overhead  
Simpler implementation

### Taylor series expansion (LCU)

$$e^{-iHt} = (e^{-iHt/r})^r \equiv V^r$$

$$V \approx \tilde{V} = \sum_{k=0}^K \frac{1}{k!} \left(\frac{-iHt}{r}\right)^k$$

$$\mathcal{U} = \tilde{V}^r$$

$$\|\tilde{V} - V\| < \epsilon/r$$

K values depends on the aimed errors  
Ancillary qubits are needed  
Complex circuits implementation

### Quantum singular value transformation

$$e^{-iHt} = \cos(Ht) - i \sin(Ht)$$

$$e^{i\phi_0\sigma_z} \prod_{j=1}^k (W(x) e^{i\phi_j\sigma_z}) = \begin{bmatrix} P(x) & iQ(x)\sqrt{1-x^2} \\ iQ^*(x)\sqrt{1-x^2} & P^*(x) \end{bmatrix}$$

$$W(x) := \begin{bmatrix} x & i\sqrt{1-x^2} \\ i\sqrt{1-x^2} & x \end{bmatrix}$$

Jacobi-Anger expansion for cos and sin

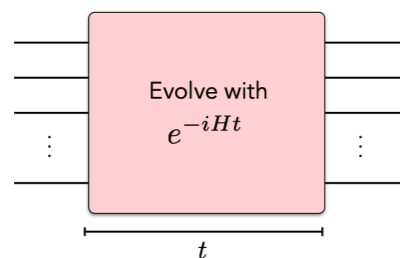
error: truncation order of the expansion  
Ancillary qubits are needed  
Complex circuits implementation

Quantum signal processing, blocking encoding, off-diagonal Hamiltonian expansion, etc... [PRX Quantum 4 \(2023\) 2, 027001](#)

# Propagation

$$\mathcal{U} |\psi_0\rangle \rightarrow |\psi(t)\rangle$$

ANALOG

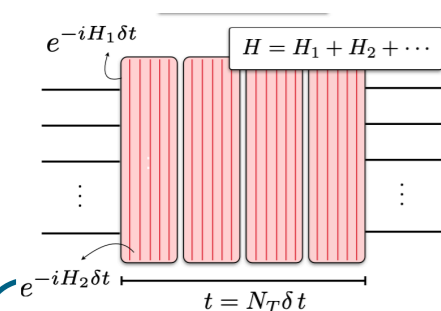


Cold neutral atoms, Trapped ions, Cavity quantum electrodynamics  
Superconducting circuits

...

DIGITAL

superconducting qubit/trapped-ion system



building blocks:  
one-qubit/two-qubit gate set

$$\|\mathcal{U} - e^{-iHt}\| < \epsilon$$

optimal asymptotically?  
overload of resources?  
easy implementation?

## HYBRID METHOD

Casanova et al (2011), Davoudi et al (2021) [trapped ion]

Harmalkar et al (2022) classical preprocessing

Zohar et al (2017), Bender et al (2018) effective interactions

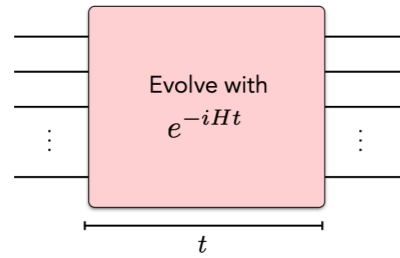
Klco et al (2018), Kokail et al (2019), Atas et al (2021) state preparations

Peruzzo et al (2014), Farhi et al (2014) optimization methods

# Propagation

$$\mathcal{U} |\psi_0\rangle \rightarrow |\psi(t)\rangle$$

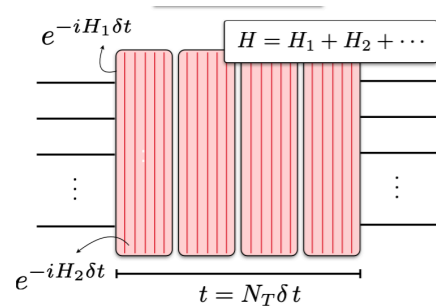
## ANALOG



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building blocks:

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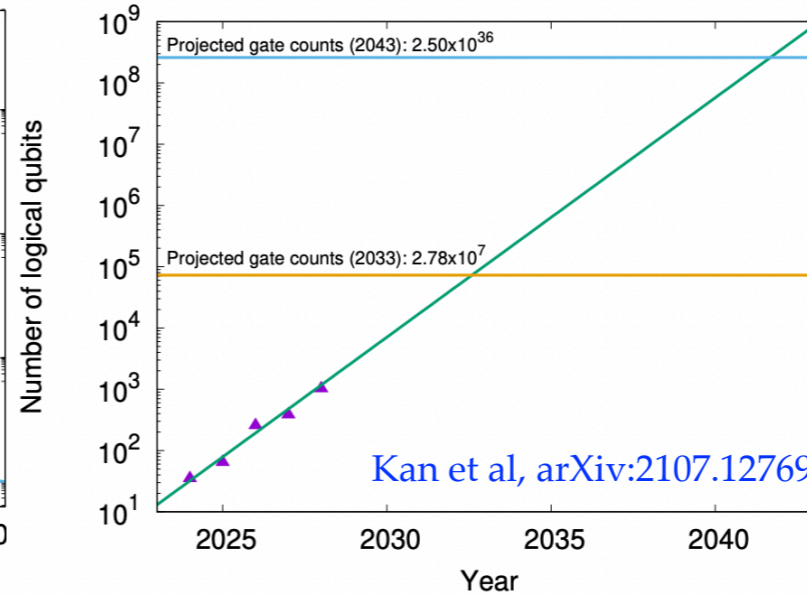
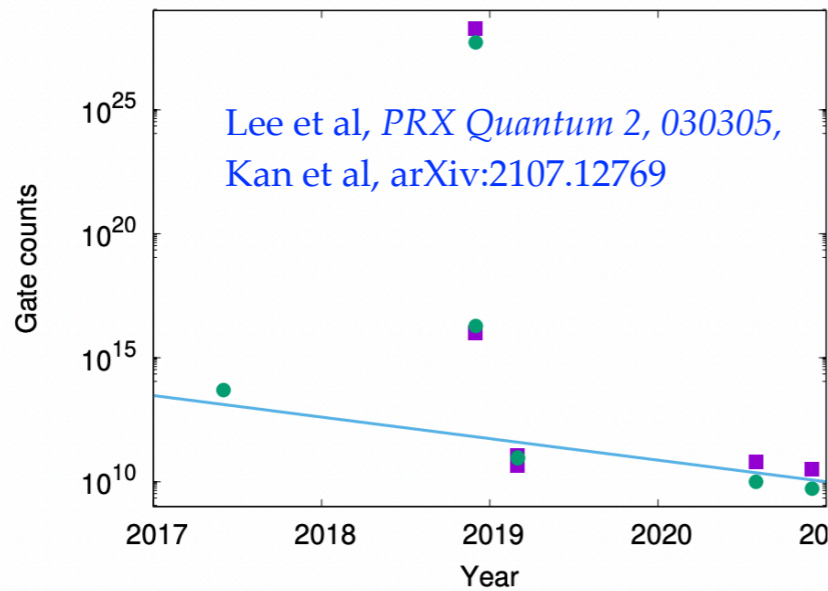
$$\|\mathcal{U} - e^{-iHt}\| < \epsilon$$

Trotter-Suzuki decomposition

$$H = \sum_{l=1}^{\Gamma} H^{(l)}$$

$$\mathcal{U} = \left[ \prod_{l=1}^{\Gamma} e^{-itH^{(l)}/r} \right]^r$$

### RESOURCE ESTIMATION AND CIRCUITS CONSTRUCTION IMPROVEMENT



heavy ion collision

Propagation

$$\mathcal{U} |\psi_0\rangle \rightarrow |\psi(t)\rangle$$

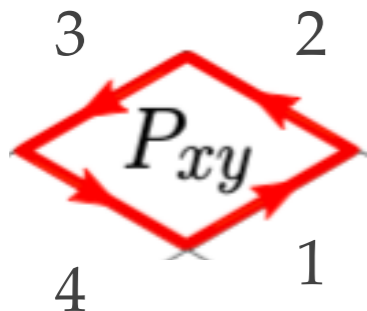
$$\mathcal{U}(t) = e^{-iH_{KS}t}$$

$$\approx \left[ e^{-i\delta t K_{KS}} e^{-i\delta t V_{KS}} \right]^{t/\delta t}$$

$$K_{KS} = \sum_{\mathbf{x}, i} \frac{g_t^2}{a} \text{Tr} L_i^2(\mathbf{x})$$

$$V_{KS} = - \sum_{\mathbf{x}, i < j} \frac{2}{g_s^2 a} \text{Re Tr} P_{ij}(\mathbf{x})$$

$$P_{ij}(x) = 1 - \frac{1}{N} \text{Re Tr} \left\{ \begin{array}{c} \text{square with arrows} \\ i \quad j \end{array} \right\}$$



$$\text{Tr} \{ U_1 U_2 U_3^\dagger U_4^\dagger \}$$

## General Method

[H. Lamm, et al, arXiv:1903.08807]

$G$ -register :  $|g\rangle$

$$\mathcal{U}_x |g\rangle |h\rangle = |g\rangle |gh\rangle$$

$$\mathcal{U}_{-1} |g\rangle = |g^{-1}\rangle$$

$$\mathcal{U}_{\text{Tr}}(\theta) |g\rangle = e^{i\theta \text{Re Tr} g} |g\rangle$$

$$\mathcal{U}_F \sum_{g \in G} f(g) |g\rangle = \sum_{\rho \in \hat{G}} \hat{f}(\rho)_{ij} |\rho, i, j\rangle$$

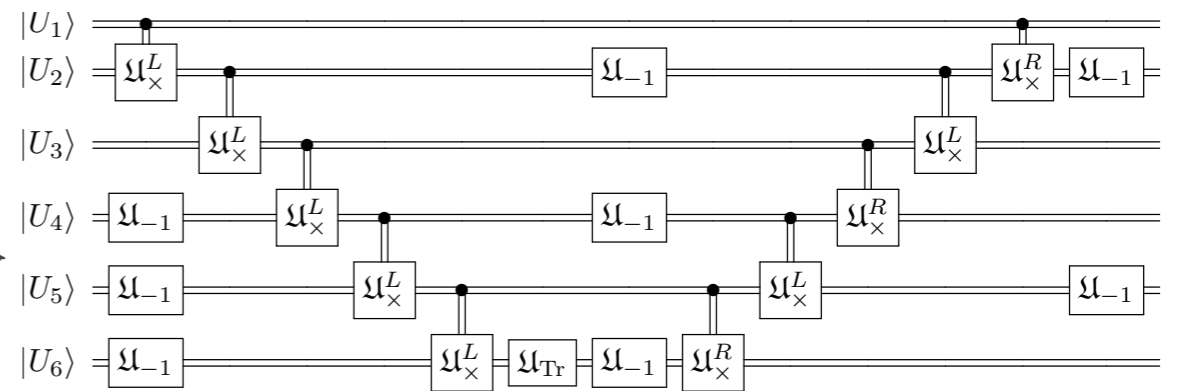
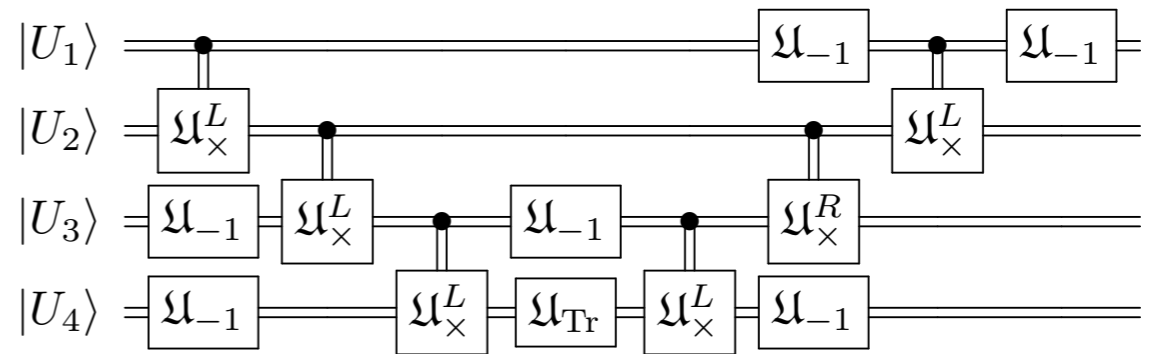
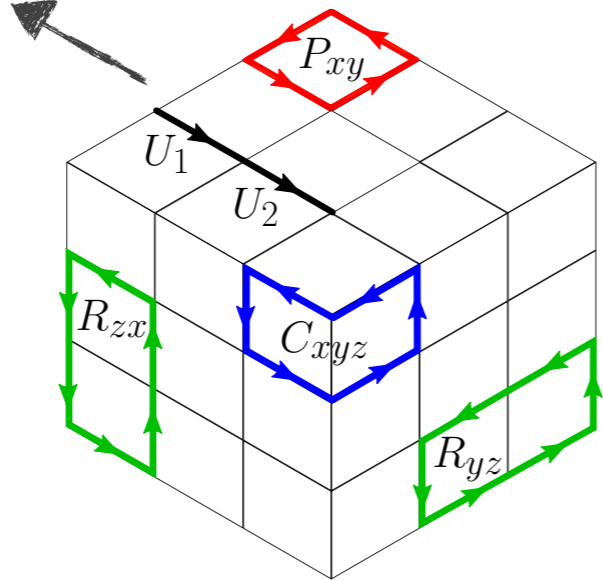
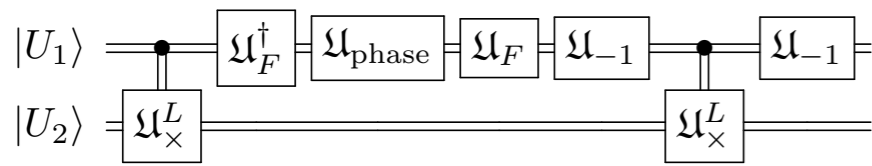
Propagation

$$\mathcal{U} |\psi_0\rangle \rightarrow |\psi(t)\rangle$$

$$H_I = K_I + V_I$$

$$V_I = \beta_{V0} V_{KS} + \beta_{V1} V_{\text{rect}}$$

$$K_I = \beta_{K0} K_{KS} + \beta_{K1} K_{2L}$$



[M. Carena, H. Lamm, YYL, W. Liu, PRL. 129, 051601]

Propagation

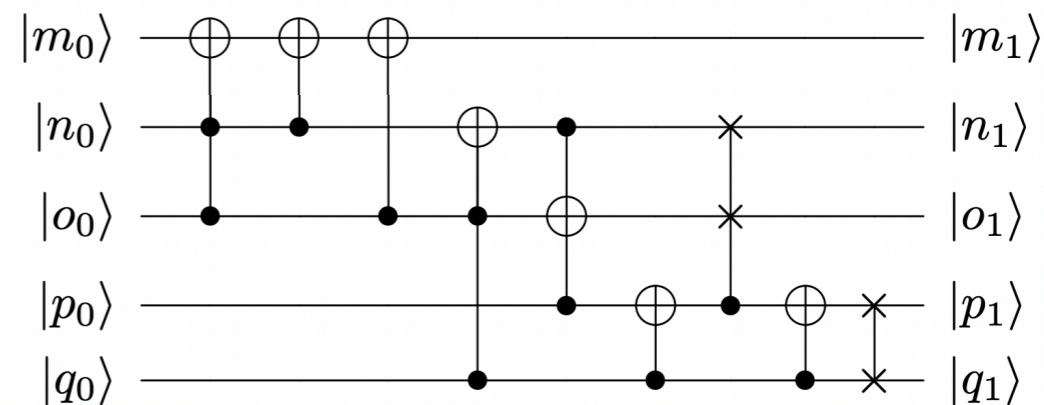
$$\mathcal{U} |\psi_0\rangle \rightarrow |\psi(t)\rangle$$

[Erik J. Gustafson et al., arXiv: 2208.12309]

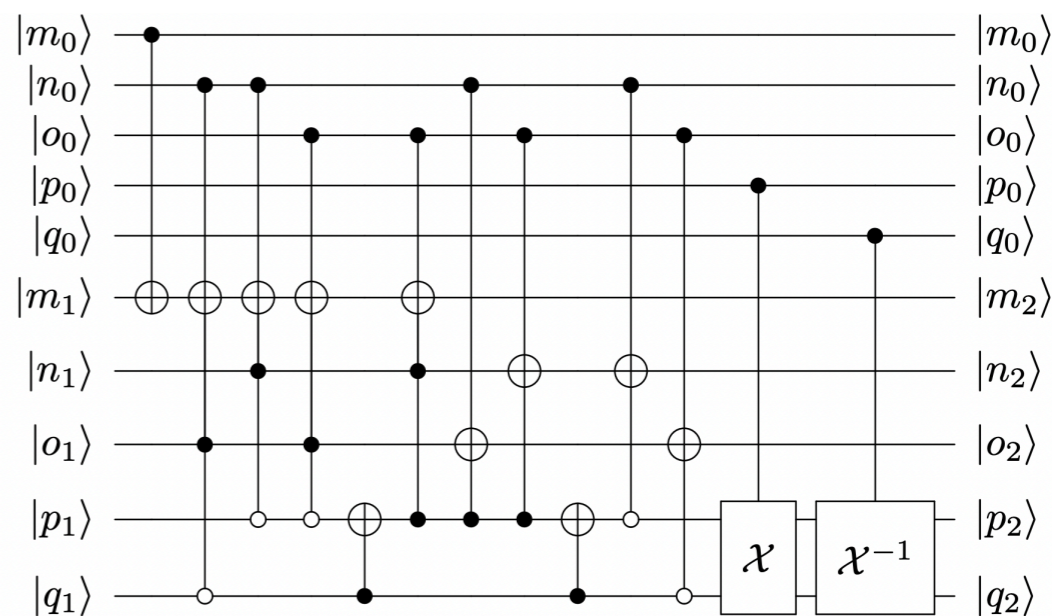
BT discrete group  
with 24 group elements

$$g = (-1)^m \mathbf{i}^n \mathbf{j}^o \mathbf{l}^{p+2q}$$

$$|qponm\rangle$$



$$\mathcal{U}_{-1} : U_0 \rightarrow U_0^\dagger$$



$$\mathcal{U}_x : U_3 U_0 \rightarrow U_3 U'_0$$

$\mathcal{U}_F : \sim 1000$  CNOT gates

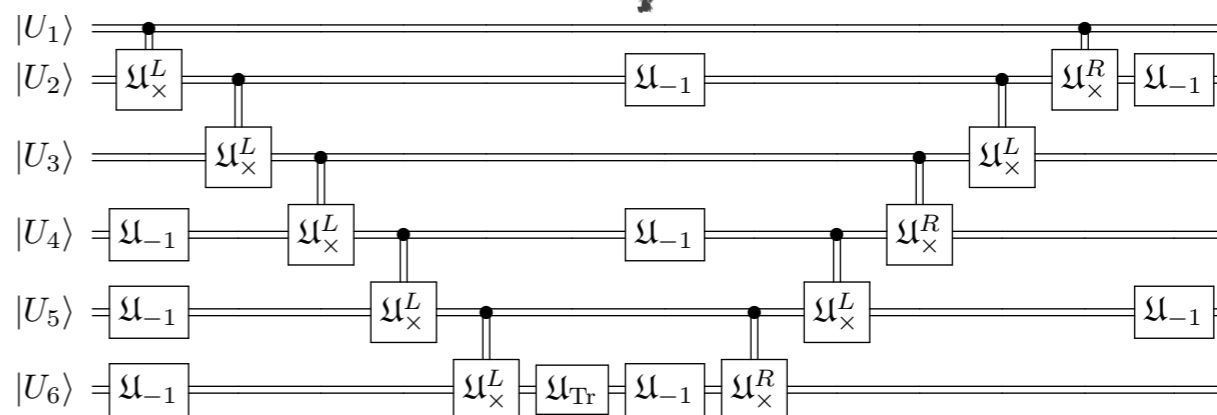
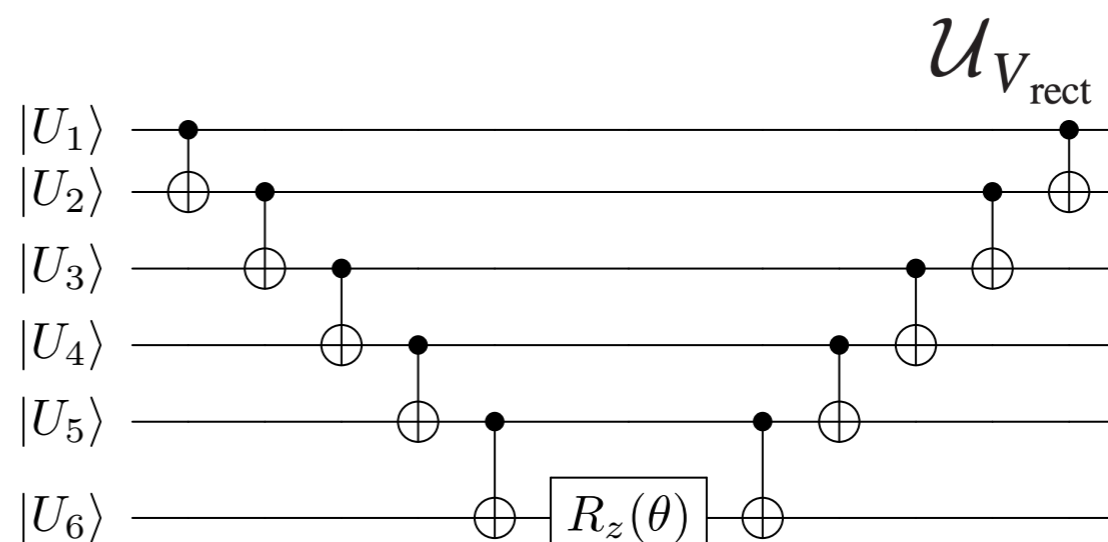
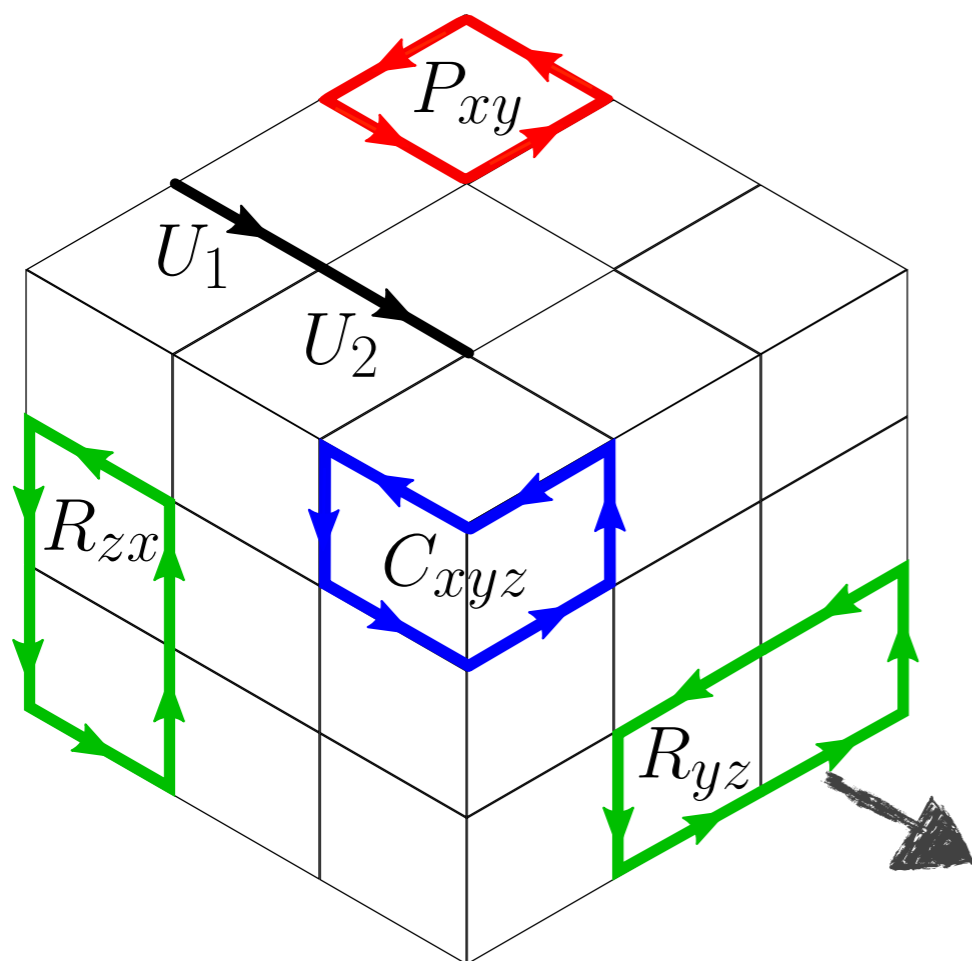


Propagation

$$\mathcal{U} |\psi_0\rangle \rightarrow |\psi(t)\rangle$$

$$\mathbb{Z}_2 \quad \begin{aligned} 1 &\rightarrow |0\rangle \\ -1 &\rightarrow |1\rangle \end{aligned}$$

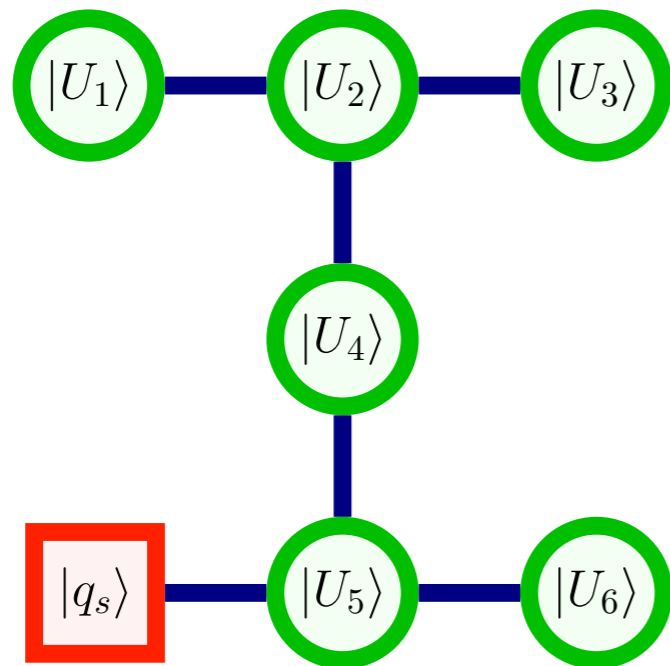
|                              |               |
|------------------------------|---------------|
| $\mathcal{U}_F$              | $H$           |
| $\mathcal{U}_{\text{phase}}$ | $R_z(\theta)$ |
| $\mathcal{U}_{\text{Tr}}$    | $R_z(\theta)$ |
| $\mathcal{U}_{-1}$           | $\mathbb{1}$  |
| $\mathcal{U}_\times$         | CNOT          |



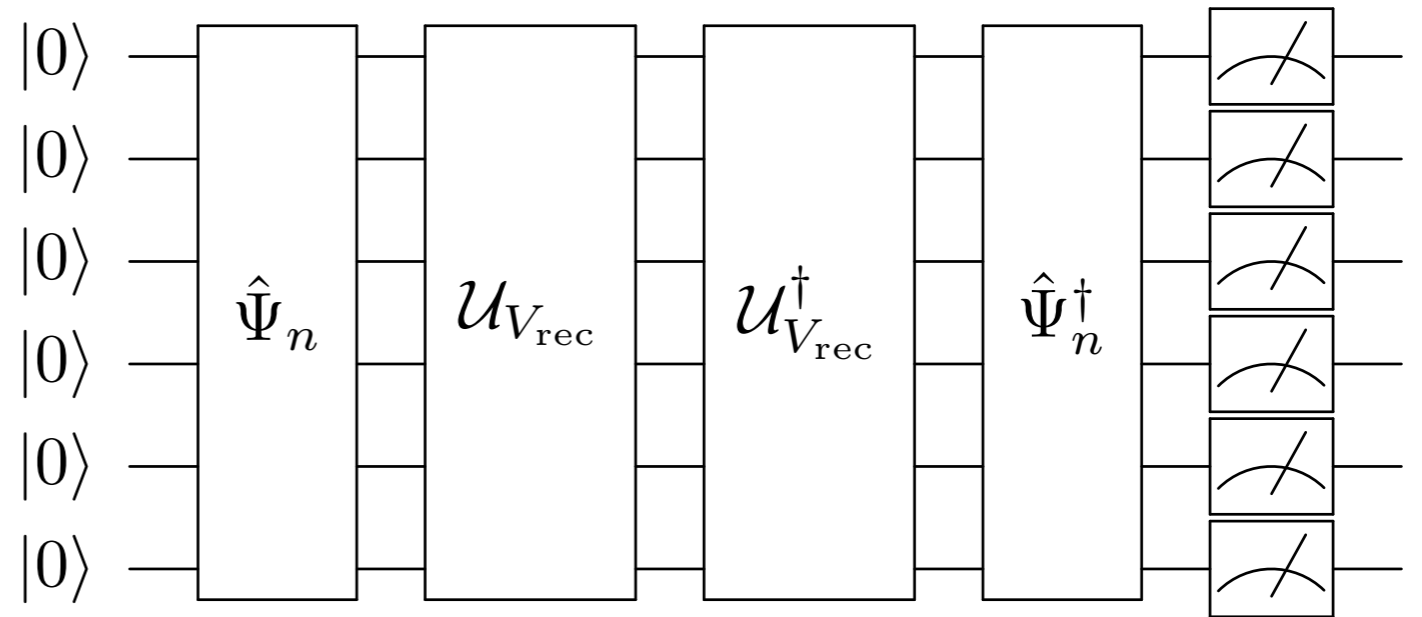
[M. Carena, H. Lamm, YYL, W. Liu, PRL. 129, 051601]

Propagation

$$\mathcal{U} |\psi_0\rangle \rightarrow |\psi(t)\rangle$$



ibm\_perth device



$$\hat{\Psi}_n = \prod_{m \leq n} H_m^\otimes$$

$$\left[ \prod_i (\sigma_i^{b_i})^\otimes \right] \text{CNOT} \otimes \mathbb{1}_4 \left[ \prod_i (\sigma_i^{a_i})^\otimes \right] = \text{CNOT} \otimes \mathbb{1}_4$$

$$\mathcal{F}_{\text{rect}} = 0.550 \quad \mathcal{F}_\delta \approx 0.25$$

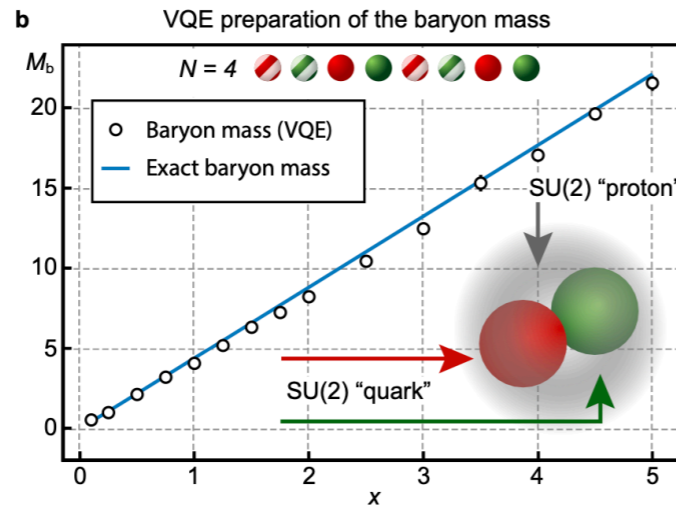
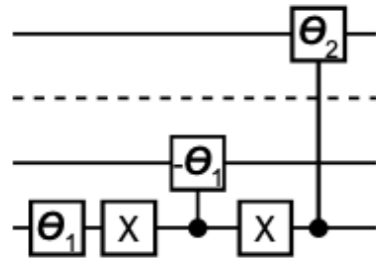
demonstration of improved Hamiltonian is allowed in the near future

# To reach the observables — How to do ...

## INITIAL STATE PREP

hadronic state, topological vacuum state, thermal state, etc

Hybrid methods with VQE protocols

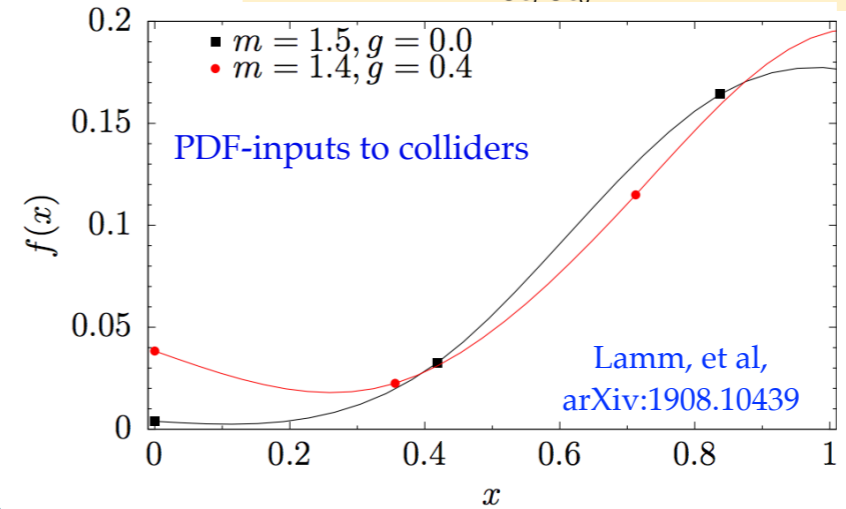


Atas et al, Nat Commun 12, 6499 (2021)

## MEASUREMENTS

time-separated correlators, exponentially suppressed process, entanglement, etc

$$\langle \Psi | \mathcal{O}(t) \mathcal{O}(0) | \Psi \rangle = \frac{\partial}{\partial \epsilon_t} \frac{\partial}{\partial \epsilon_0} \langle \Psi | e^{-iHt} e^{-i\mathcal{O}\epsilon_t} e^{iHt} e^{i\mathcal{O}\epsilon_0} | \Psi \rangle$$



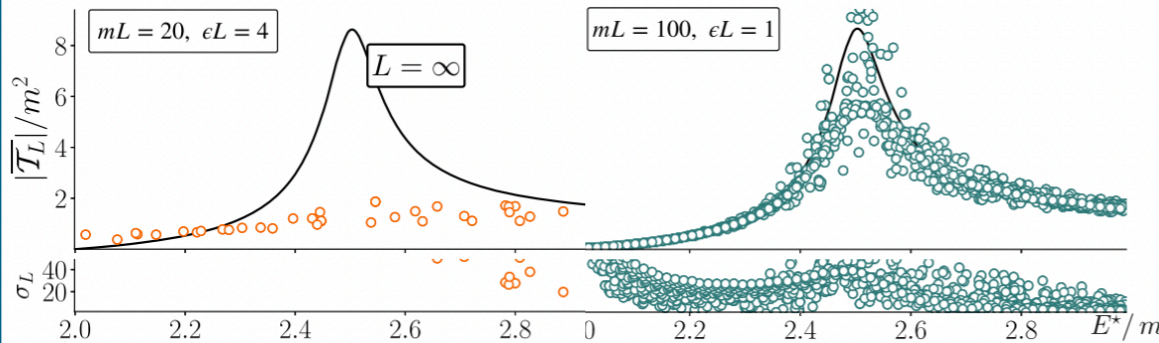
Lamm, et al, arXiv:1908.10439

T. Li, et al, arXiv:2207.13258

## SYSTEMATIC UNCERTAINTIES

finite volume effects, truncation errors, convergence rate

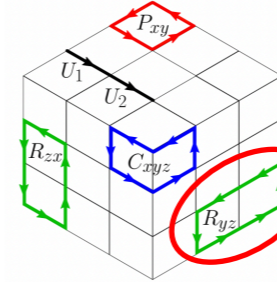
$$iT = \text{diagram with } q, p_f, p_i, p_f + q - p_i$$



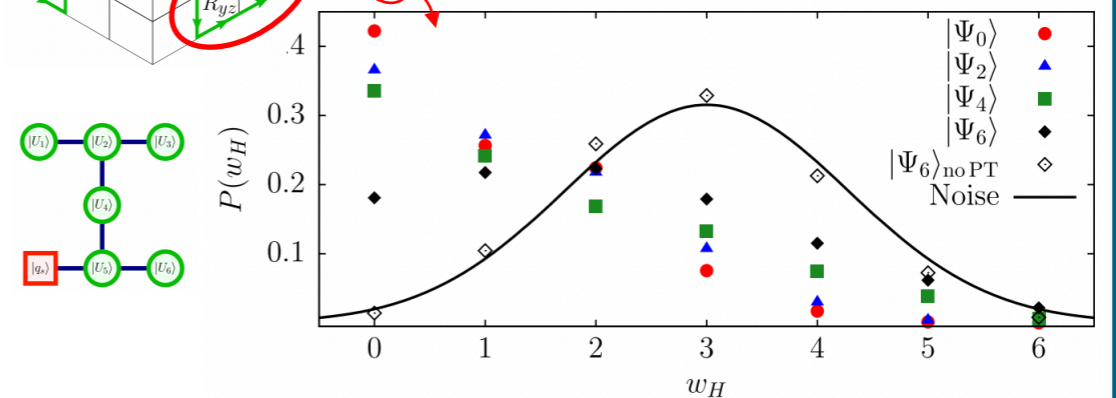
Briceno, PRD 103, 014506 (2021)

## ERROR CORRECTIONS

gate error - stochastic and coherent errors  
readout errors



$$Z_2 \left[ \prod_i (\sigma_i^{b_i})^{\otimes} \right] \text{CNOT} \otimes 1_4 \left[ \prod_i (\sigma_i^{a_i})^{\otimes} \right] = \text{CNOT} \otimes 1_4$$

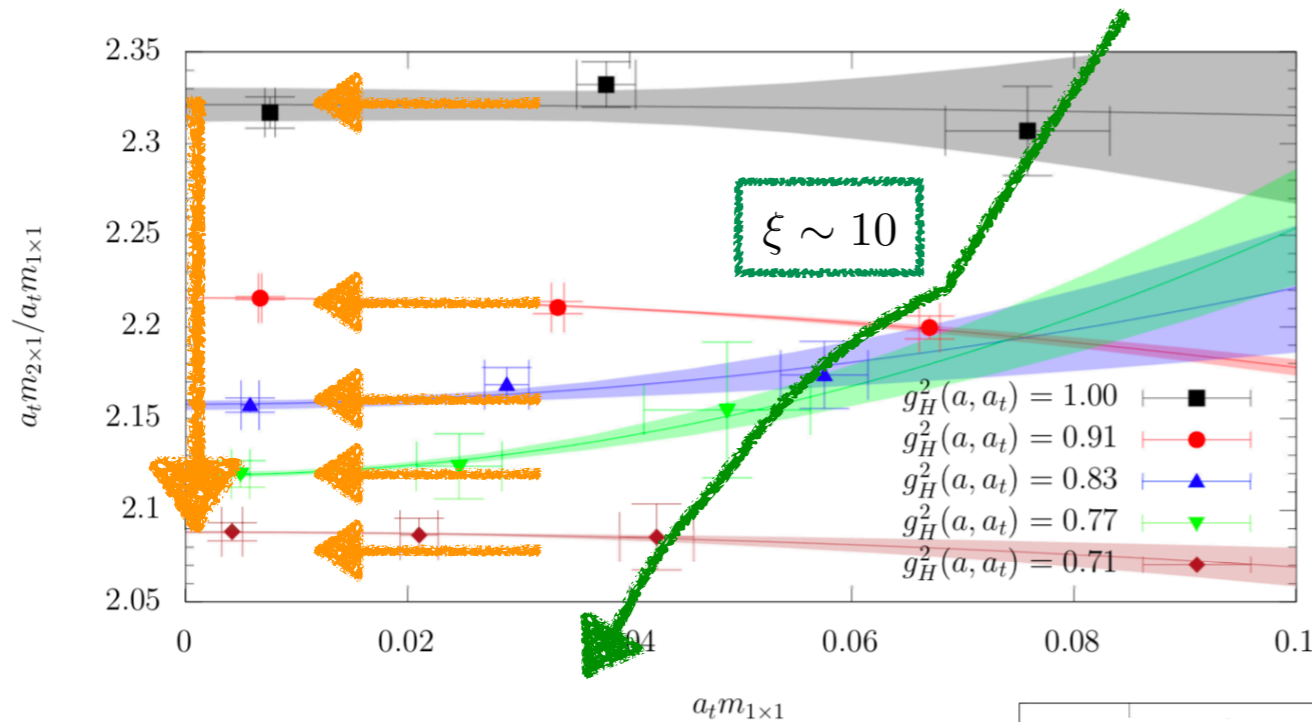


Carena, Lamm, YYL, Liu, PRL. 129, 051601

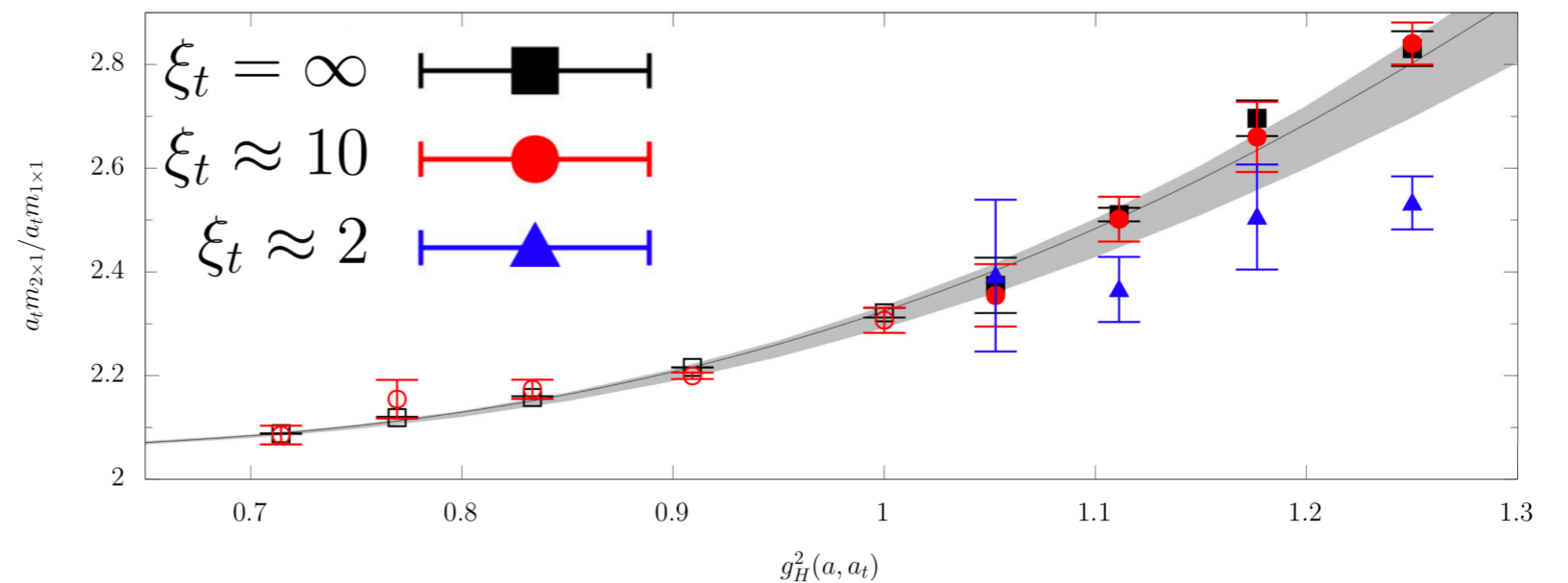
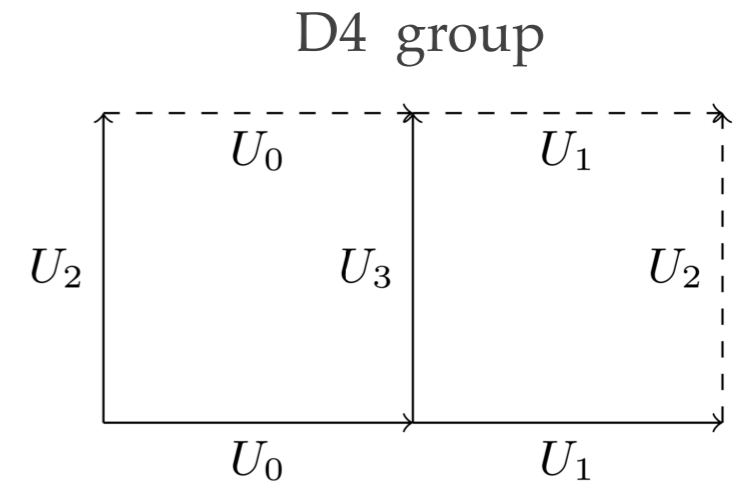
# To reach observables in the continuum limit

## TRAJECTORY TO THE CONTINUUM LIMIT

**continuum limit:** extrapolation to the continuum at  $\xi = a/a_t$



[M. Carena, H. Lamm, YYL, W. Liu, PRD. 104, 094519]

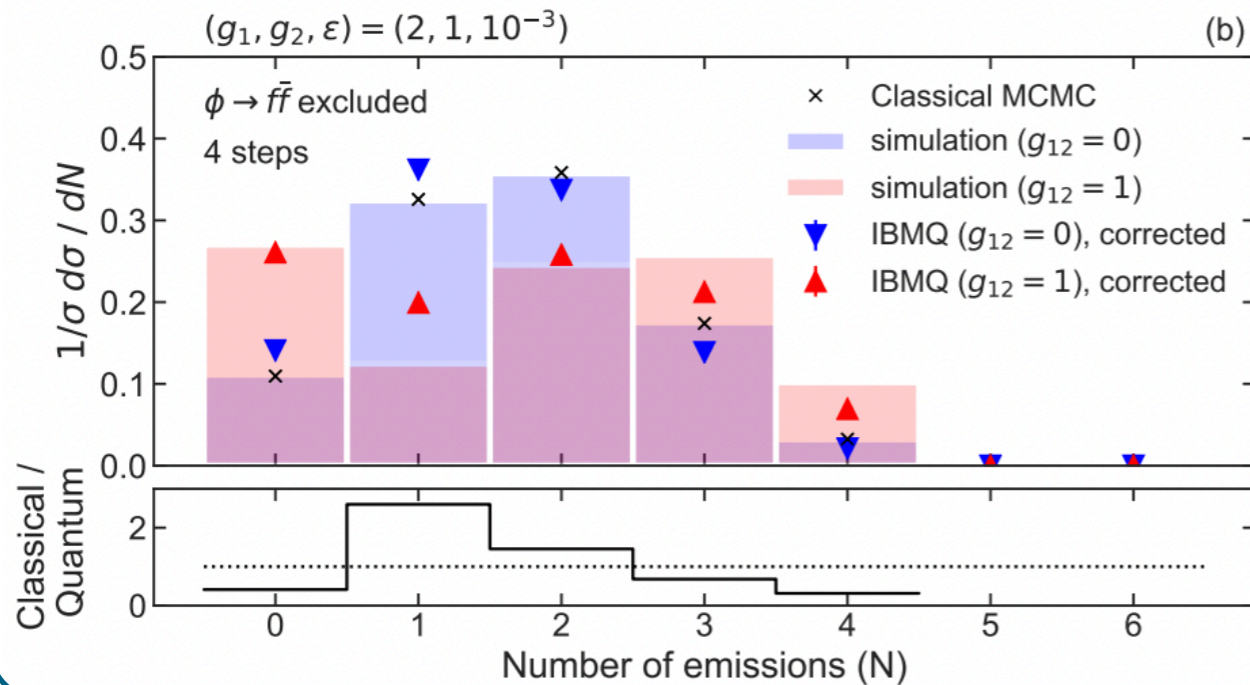
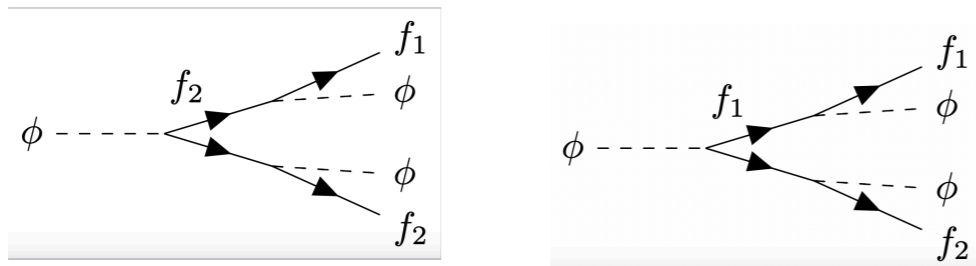


$$g_H^2 \propto 1/\log(a) \rightarrow 0$$

# Benchmarks

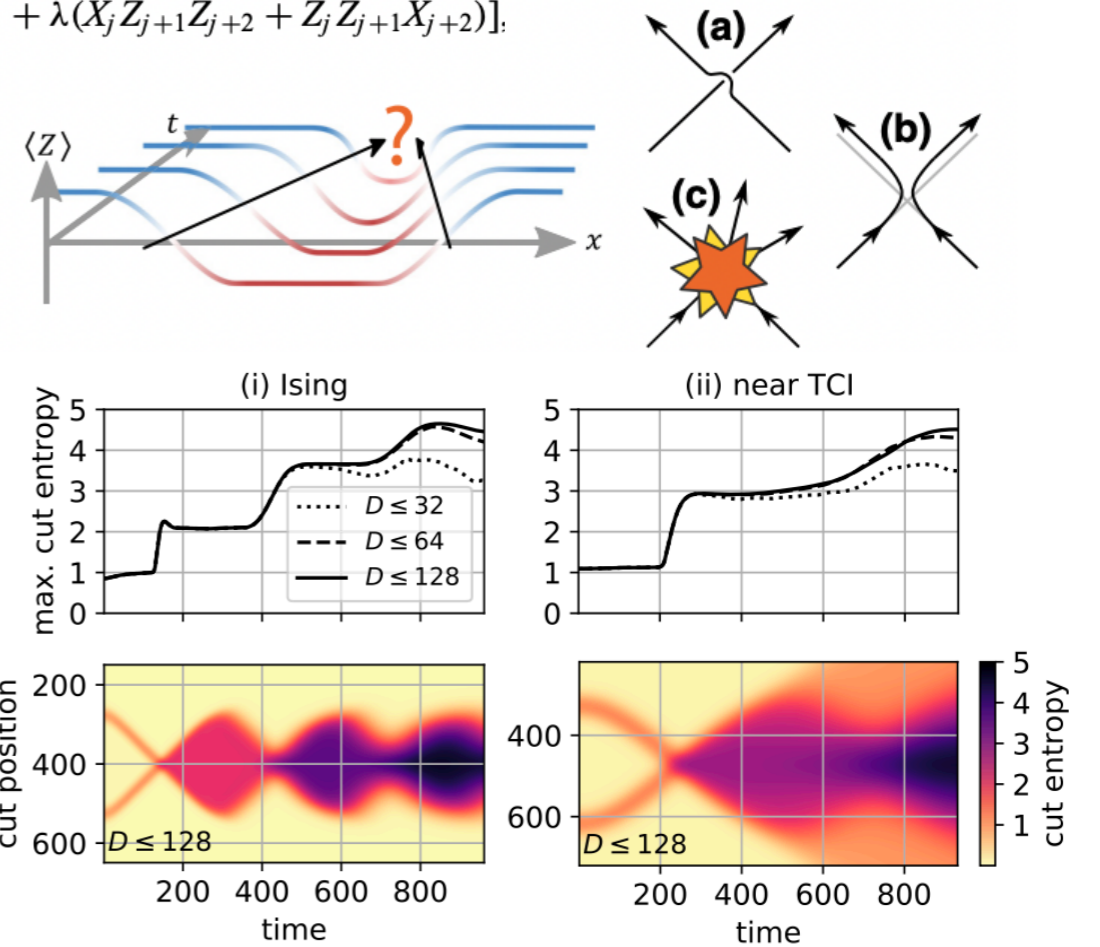
## PARTON SHOWERING [arXiv:2102.05044, PRD 103, 076020, PRD 106, 056002,...]

$$\mathcal{L} = \bar{f}_1(i\partial + m_1)f_1 + \bar{f}_2(i\partial + m_2)f_2 + (\partial_\mu\phi)^2 + g_1\bar{f}_1f_1\phi + g_2\bar{f}_2f_2\phi + g_{12}[\bar{f}_1f_2 + \bar{f}_2f_1]\phi$$



## BUBBLE COLLISION

$$H = \sum_{j=1}^N [-Z_j Z_{j+1} - gX_j - hZ_j + \lambda(X_j Z_{j+1} Z_{j+2} + Z_j Z_{j+1} X_{j+2})]$$



the maximum cut entropy at  $D \leq 128$  very likely not converged after  $t \approx 700$

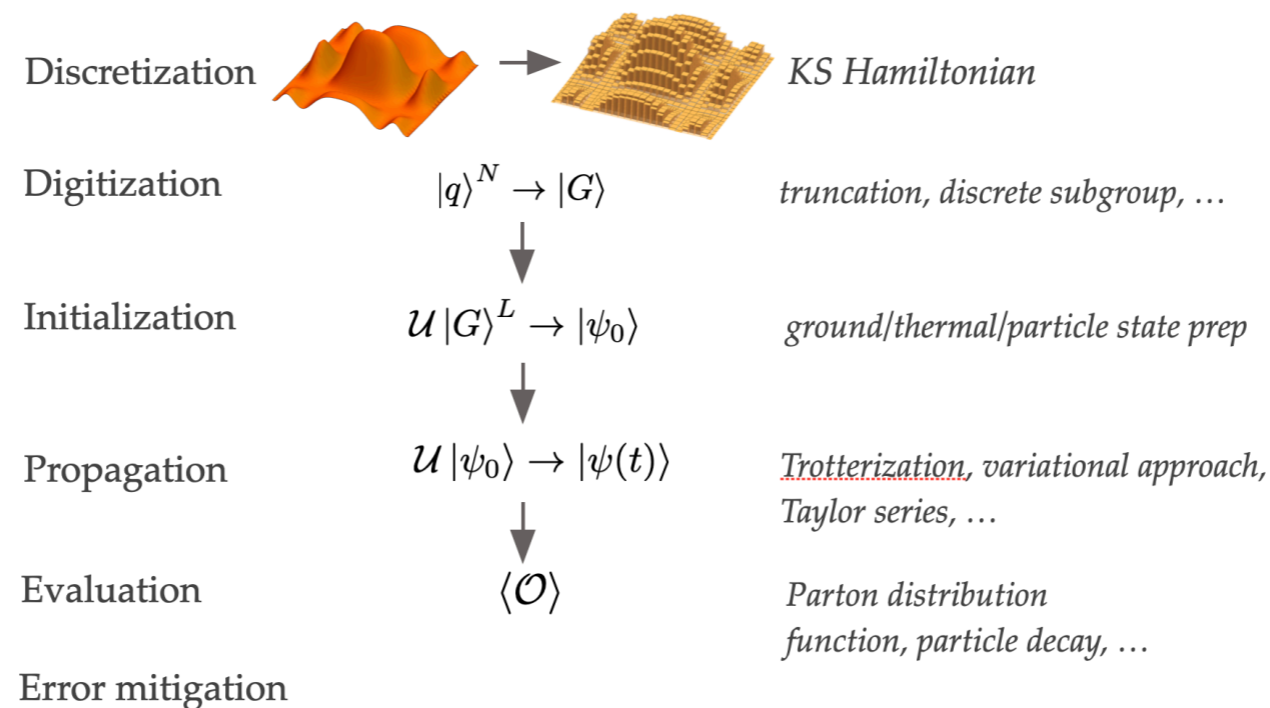
[Milsted, et al, PRXQuantum.3.020316]

# “It is time to go”

## SUMMARY and OUTLOOK

Quantum computing can access to quantities in high energy physics which are intractable with classical methods

So many things to do, ... and lots should be done to before scalable noise-resilient ones are available.



Theory investigations, algorithmic developments, benchmark study, hardware co-design,...

Thank you

BACK UP



# -1973: Standard Model

| 三代物质粒子 (费米子) |                                   |  |  |                                  |
|--------------|-----------------------------------|--|--|----------------------------------|
|              | I                                 | II                                       | III  |                                  |
| 质量           | $\approx 2.2 \text{ MeV}/c^2$     | $\approx 1.28 \text{ GeV}/c^2$           | $\approx 173.1 \text{ GeV}/c^2$            | 0                                |
| 电荷           | $2/3$                             | $2/3$                                    | $2/3$                                      | 0                                |
| 自旋           | $1/2$                             | $1/2$                                    | $1/2$                                      | $1$                              |
|              | <b>u</b><br>上                     | <b>c</b><br>粲                            | <b>t</b><br>顶                              | <b>g</b><br>胶子                   |
|              | <b>d</b><br>下                     | <b>s</b><br>奇                            | <b>b</b><br>底                              | <b>H</b><br>希格斯玻色子               |
|              | <b>e</b><br>电子                    | <b><math>\mu</math></b><br>$\mu$ 子       | <b><math>\tau</math></b><br>$\tau$ 子       | <b><math>\gamma</math></b><br>光子 |
|              | <b><math>\nu_e</math></b><br>电中微子 | <b><math>\nu_\mu</math></b><br>$\mu$ 中微子 | <b><math>\nu_\tau</math></b><br>$\tau$ 中微子 | <b>Z</b><br>Z玻色子                 |
|              |                                   |  |  | <b>W</b><br>W玻色子                 |

夸克

轻子

标量玻色子

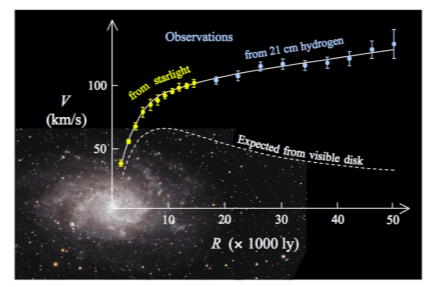
规范玻色子

1897-2012:

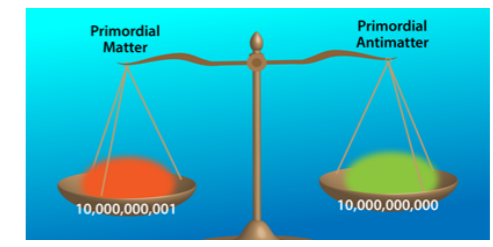
electron, muon, tau lepton, gluon, W and Z boson, top quark, tau neutrino, Higgs boson

# Puzzles we Encountered

1933-Now  
dark matter

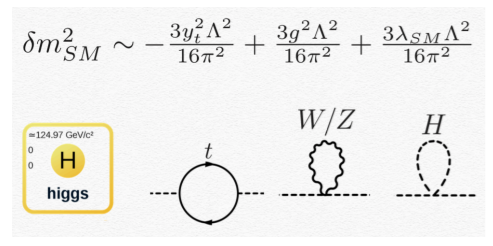


1940s-Now  
baryon  
asymmetry



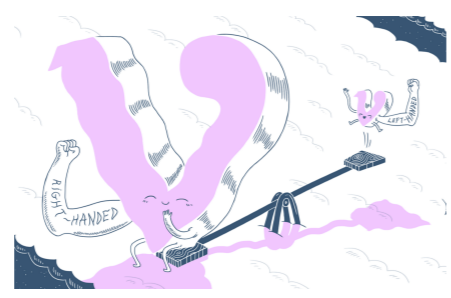
out of equilibrium

1967-Now  
naturalness  
problem



strong dynamics

1960s-Now  
neutrino mass



1960s-Now  
Strong CP problem

$$\mathcal{L} \supset -\frac{1}{4} G^2 + \frac{\theta g_s^2}{32\pi^2} G\tilde{G}$$

$$\bar{\theta} \lesssim 10^{-10}$$

CP-violating phase in the CKM matrix is about  $\pi/3$

complex action

grand unified theory?

precision measurement

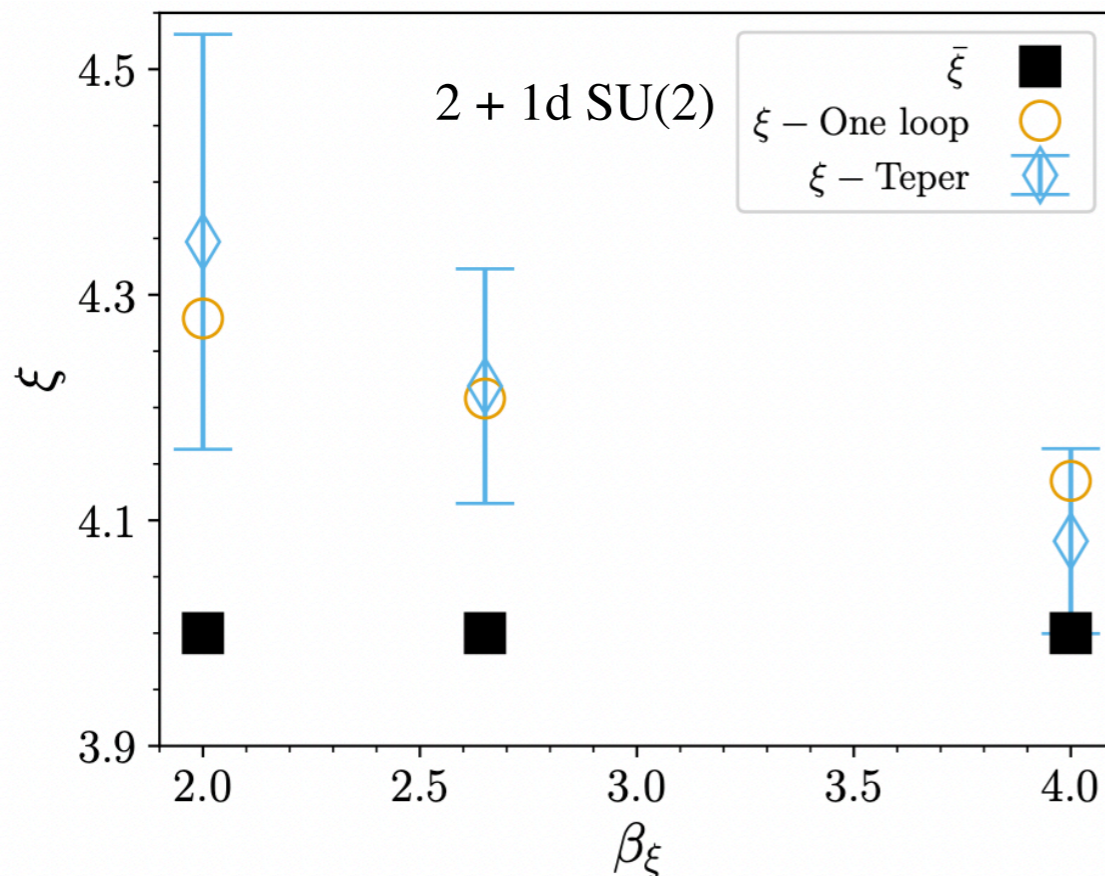
rare events  
theoretical inputs to colliders

Propagation

$$\mathcal{U} |\psi_0\rangle \rightarrow |\psi(t)\rangle$$

## Anisotropic Parameter $\xi = a/a_t$ Renormalization

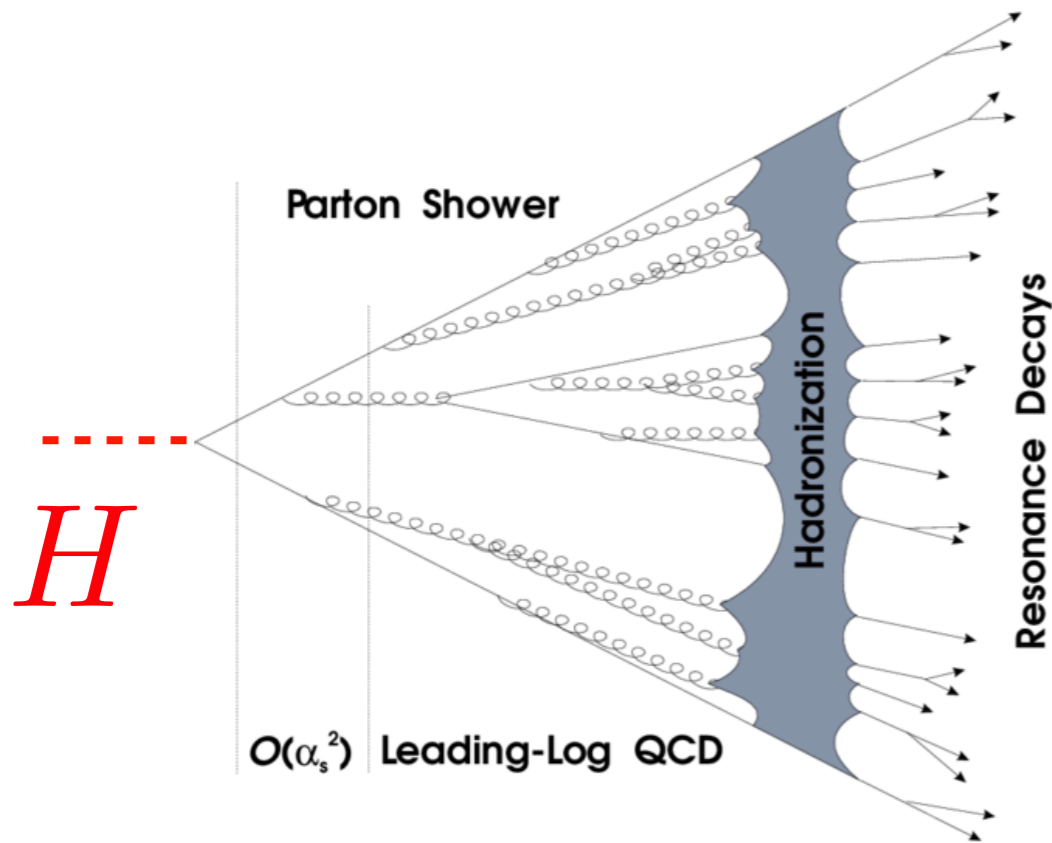
- numerical results is pretty tedious—saving measurement on the Euclidean side
- Preferred for analytical continuation
- Determine the fixed anisotropic trajectory
- Continuous group agrees quite well with their discrete subgroups



| $\beta_\xi$ | $N_s$           | $N_t$           | $\bar{\xi}$ | $\xi_{1\text{-loop}}$ | $\xi$       |
|-------------|-----------------|-----------------|-------------|-----------------------|-------------|
|             |                 |                 |             |                       | BI          |
|             |                 |                 |             |                       | SU(2) [111] |
| $D = 3$     |                 |                 |             |                       |             |
| 2.00        | 36              | 72              | 2.00        | 2.097                 | 2.099(1)    |
| 2.00        | 12 <sup>a</sup> | 60 <sup>a</sup> | 4.00        | 4.278                 | ...         |
| 2.65        | 16 <sup>a</sup> | 64 <sup>a</sup> | 4.00        | 4.207                 | ...         |
| 3.00        | 36              | 72              | 1.33        | 1.351                 | 1.369(19)   |
| 4.00        | 24 <sup>a</sup> | 96 <sup>a</sup> | 4.00        | 4.136                 | ...         |
| $D = 4$     |                 |                 |             |                       |             |
| 3.0         | 36              | 72              | 1.33        | 1.351                 | 1.36(1)     |

[M. Carena, E. Gustafson, H. Lamm, YYL, W. Liu, PRD 106 11, 114504]

# Theoretical inputs to colliders



## Parton Shower

Long-distance dynamics - dominated by massless modes, high multiplicity final states

$$\sigma = H \otimes J_1 \otimes \cdots \otimes J_n \otimes S$$

collinear

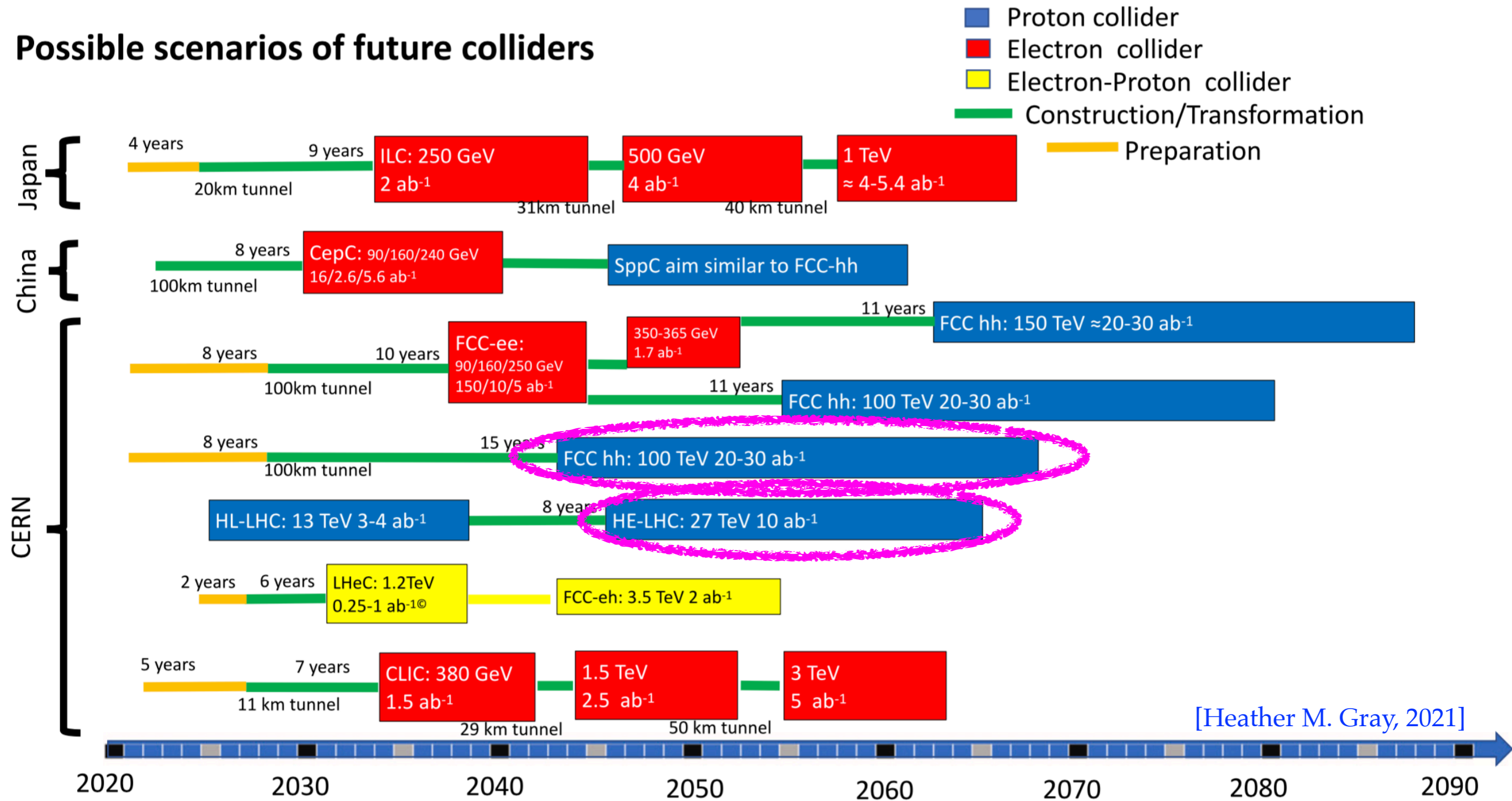
soft

**Lattice:** in principle, sign problem  
**State-of-art tech (MCMC):**  
 probability level—interference  
 not properly included

[arXiv:2102.05044, arXiv: 1904.03196,  
 PRD 103, 076020, PRD 106, 056002,...]

# -Now-: precision measurement

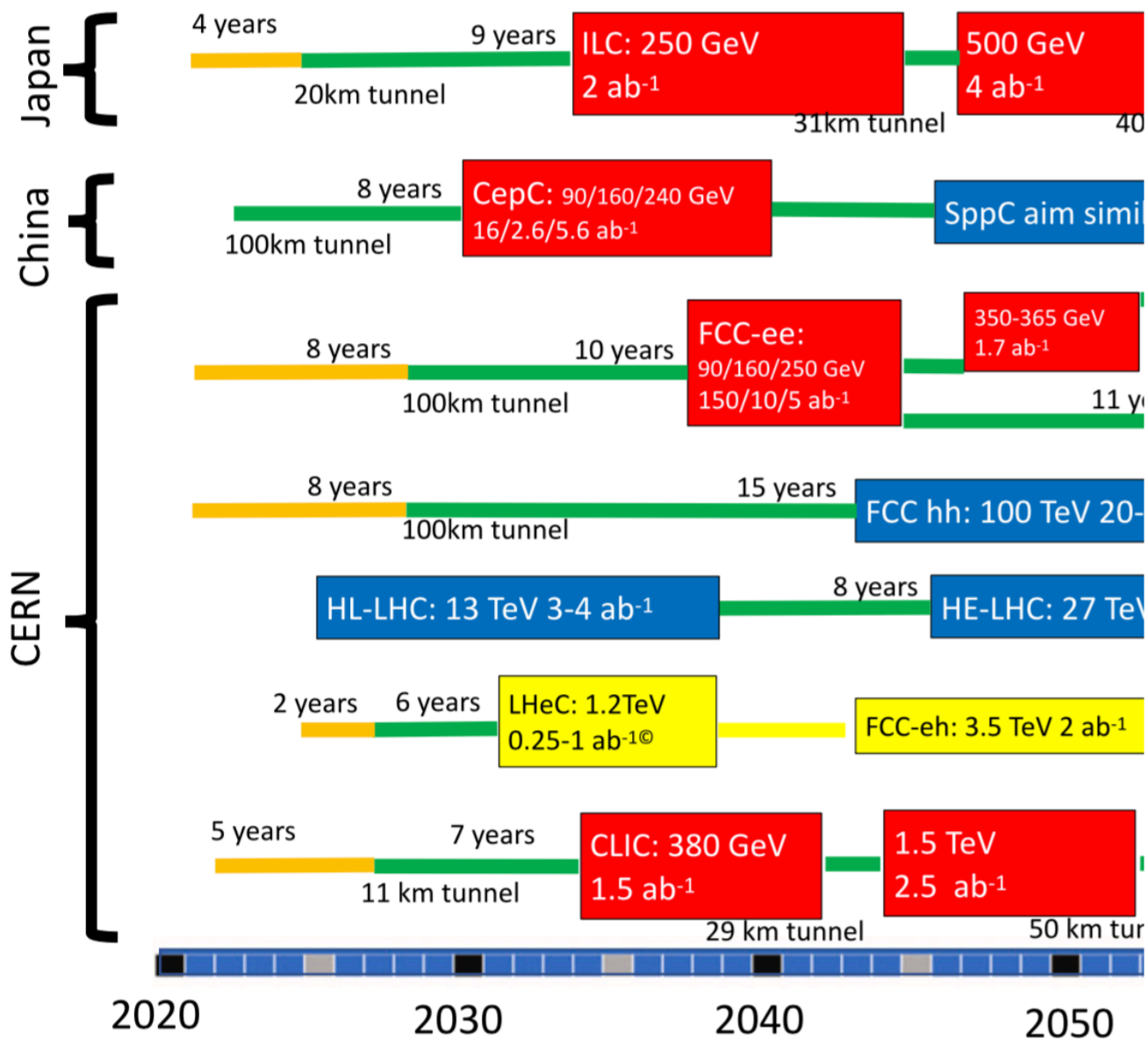
## Possible scenarios of future colliders



# -Now-: precision measurement

[Jorge de Blas, et al, arXiv:1907.04311]

## Possible scenarios of future colliders



| $\mu$ (%)                 | Future Circular Colliders |         |         |
|---------------------------|---------------------------|---------|---------|
|                           | CEPC                      | FCC-ee  |         |
|                           | 240 GeV                   | 240 GeV | 365 GeV |
|                           | unpolarized               |         |         |
| $\sigma_{Zh}$             | 0.005                     | 0.005   | 0.009   |
| $\mu_{Zh}^{bb}$           | 0.21 <sup>†</sup>         | 0.20    | 0.50    |
| $\mu_{Zh}^{cc}$           |                           |         | 0.50    |
| $\mu_{Zh}^{\tau\tau}$     |                           |         | 0.80    |
| $\mu_{Zh}^{\mu\mu}$       | 17.1                      | 19.0    | 40.0    |
| $\mu_{Zh}^{WW}$           | 0.98 <sup>†</sup>         | 1.20    | 2.60    |
| $\mu_{Zh}^{ZZ}$           | 5.09 <sup>†</sup>         | 4.40    | 12.0    |
| $\mu_{Zh}^{Z\gamma}$      | 15.0                      | 15.9    | —       |
| $\mu_{Zh}^{\gamma\gamma}$ | 6.84                      | 9.00    | 18.0    |
| $\mu_{Zh}^{gg}$           | 1.27 <sup>†</sup>         | 1.90    | 3.50    |

**New physics up to 100 TeV can be probed**