

New channel to search for dark matter at Belle II

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2023年12月30-31日，南京师范大学

Outline

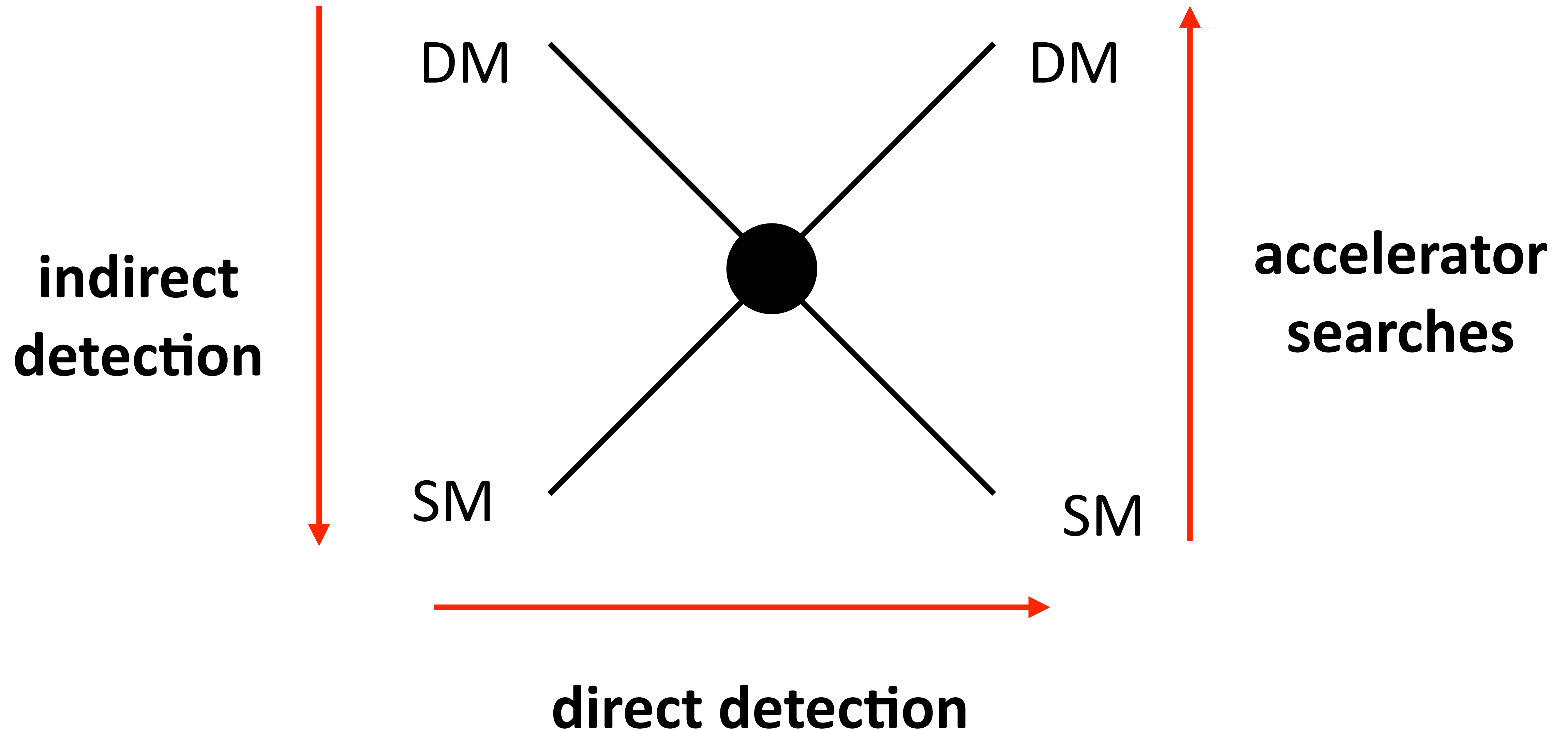
- 1 New dark matter channel @ Belle II
- 2 Standard model backgrounds
- 3 Sensitivity on invisible dark photon models

in collaboration with Jinhua Liang and Lan Yang [2212.04252]

1

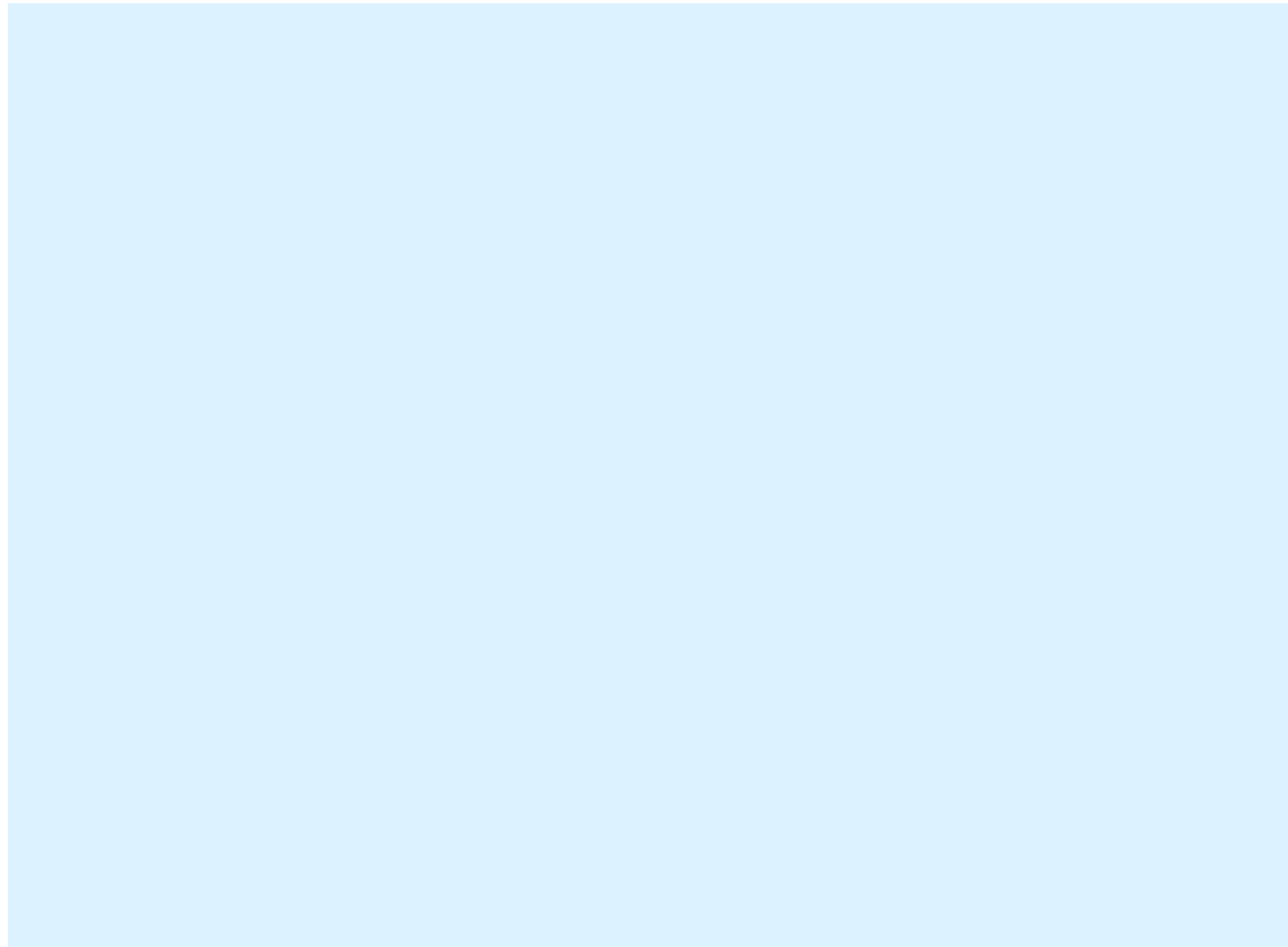
New dark matter channel @ Belle II

Searches for dark matter in particle physics experiments



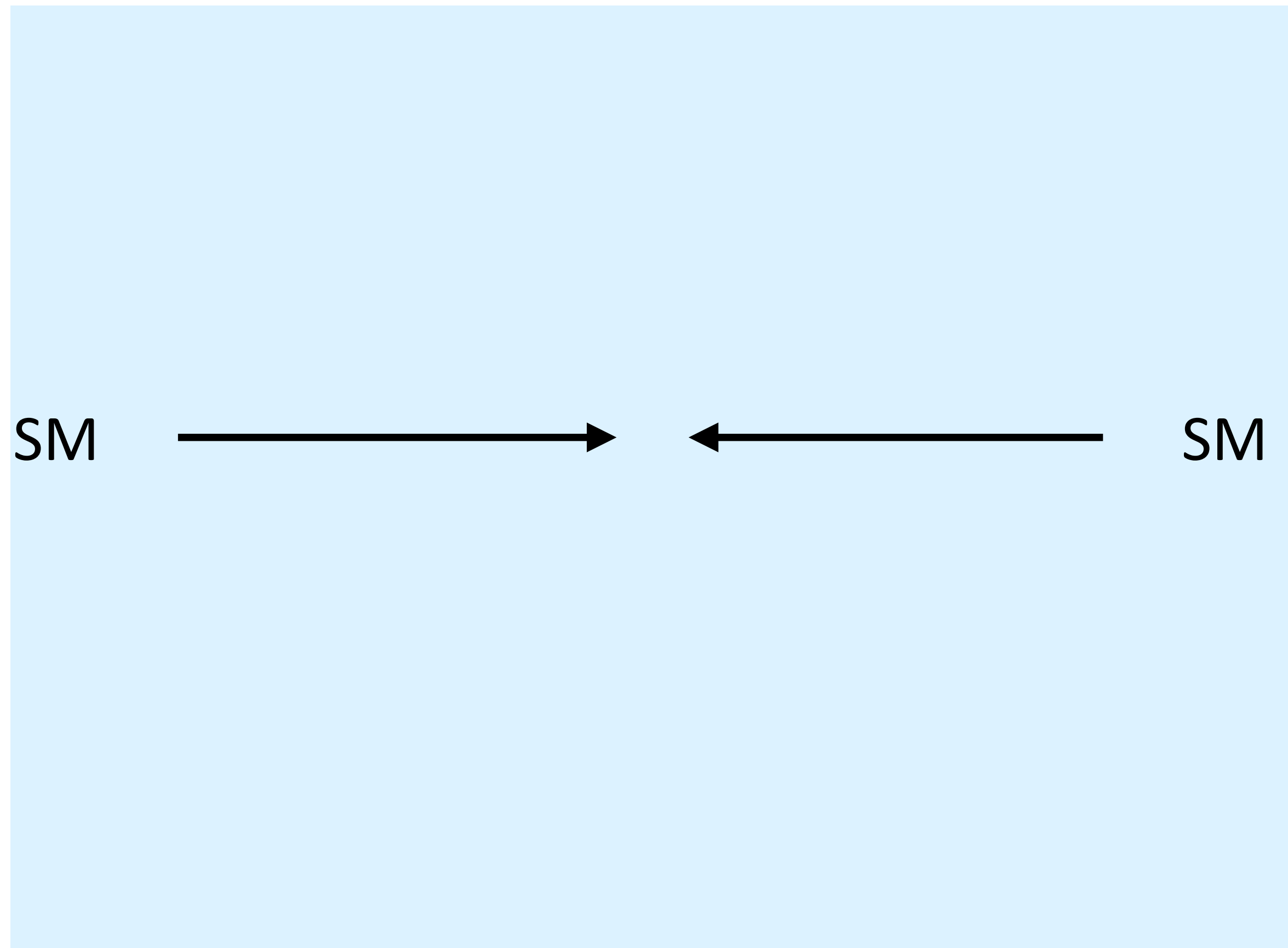
Previous dark matter detection channels at colliders

Most studies focus on mono-X channel with SM X produced at the primary vertex



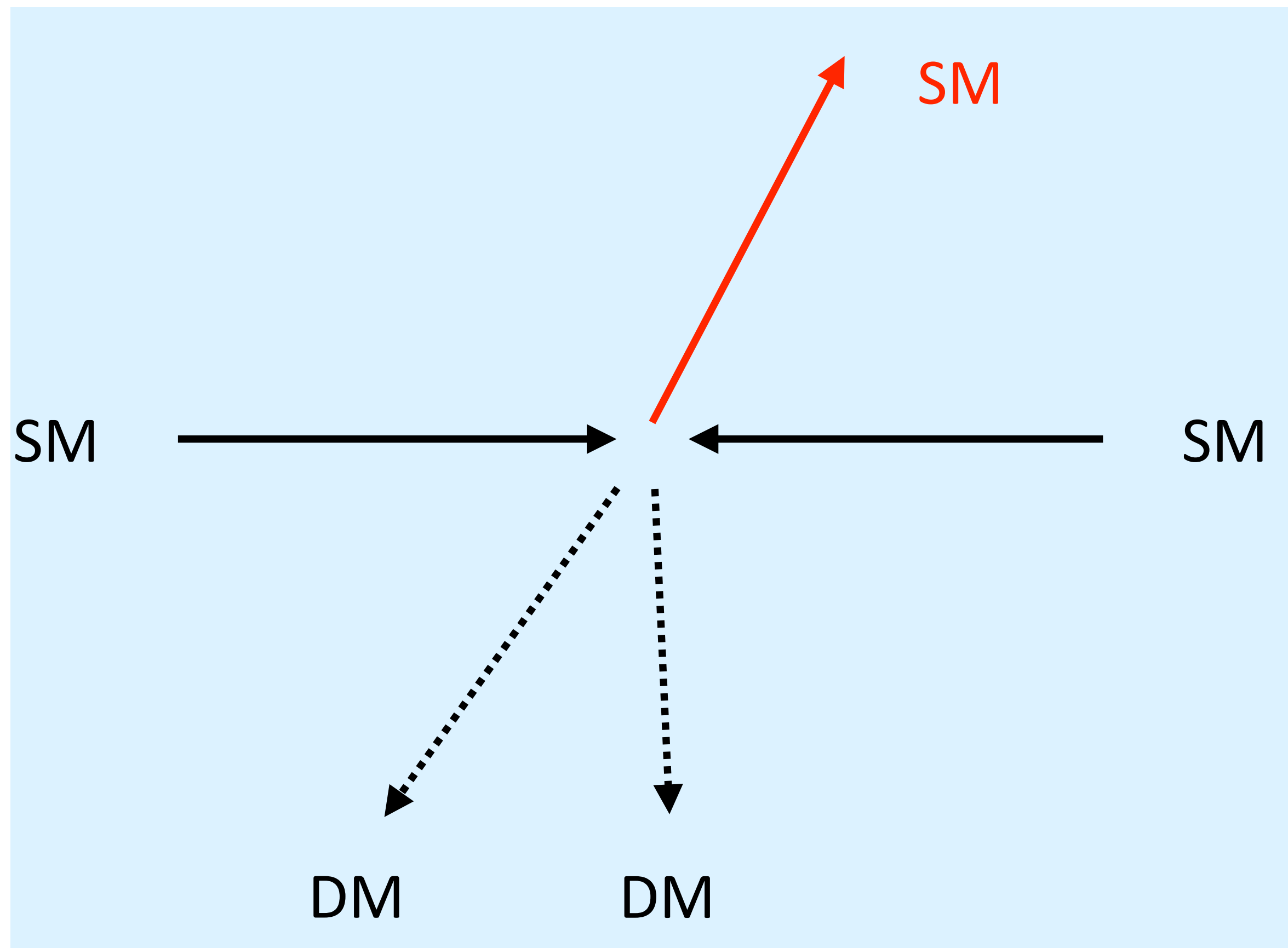
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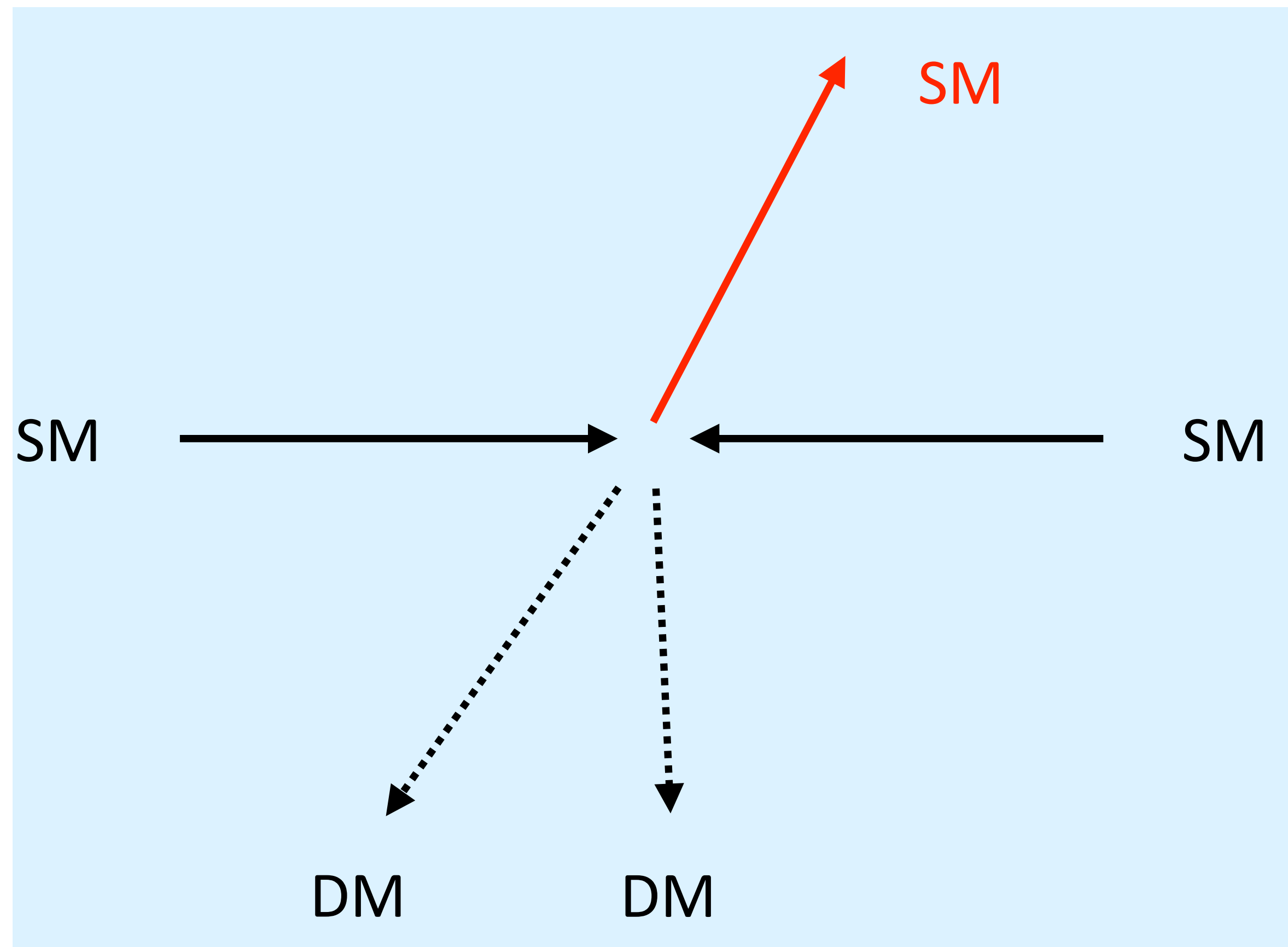
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Previous dark matter detection channels at colliders

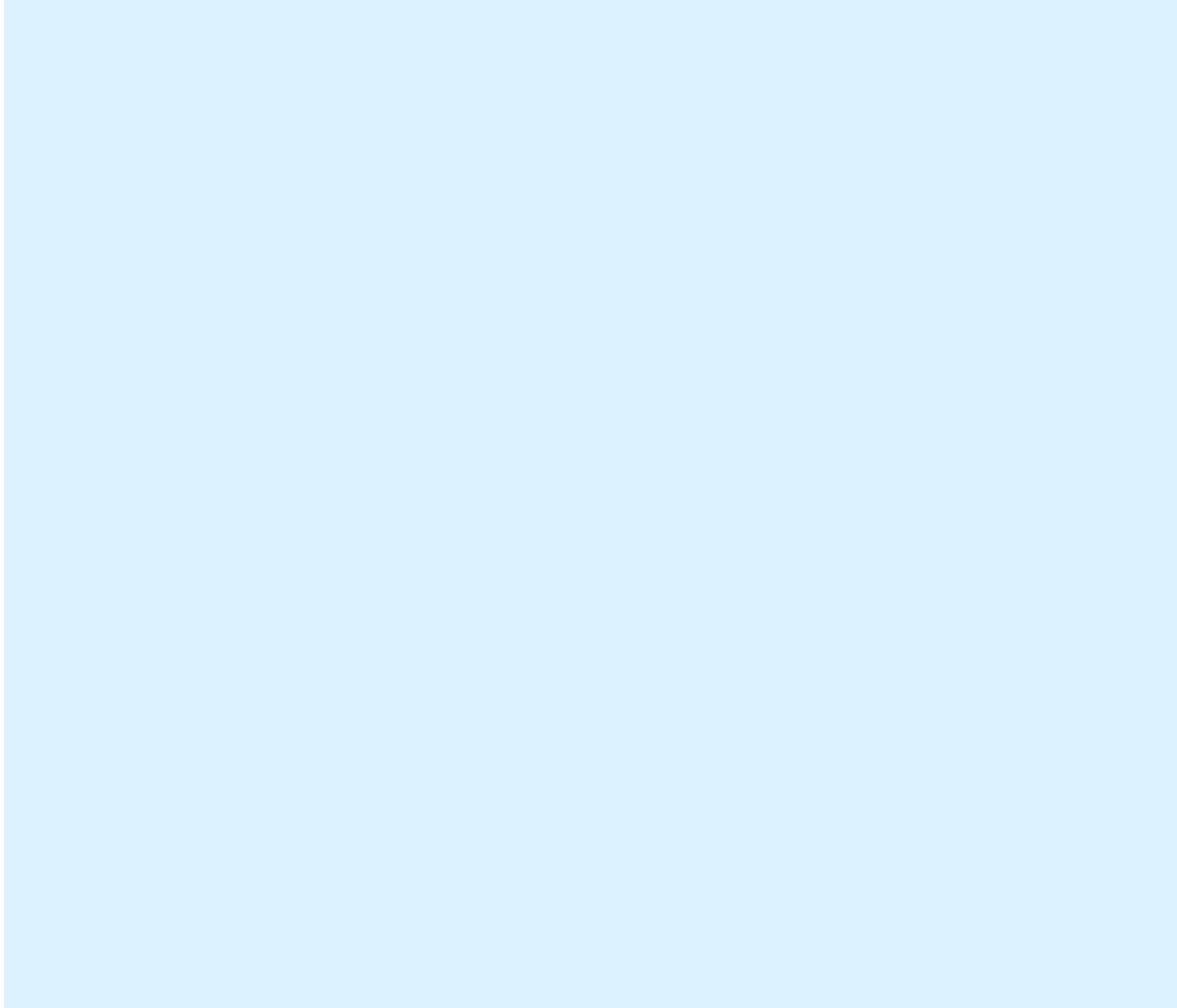
Most studies focus on mono-X channel with SM X produced at the primary vertex



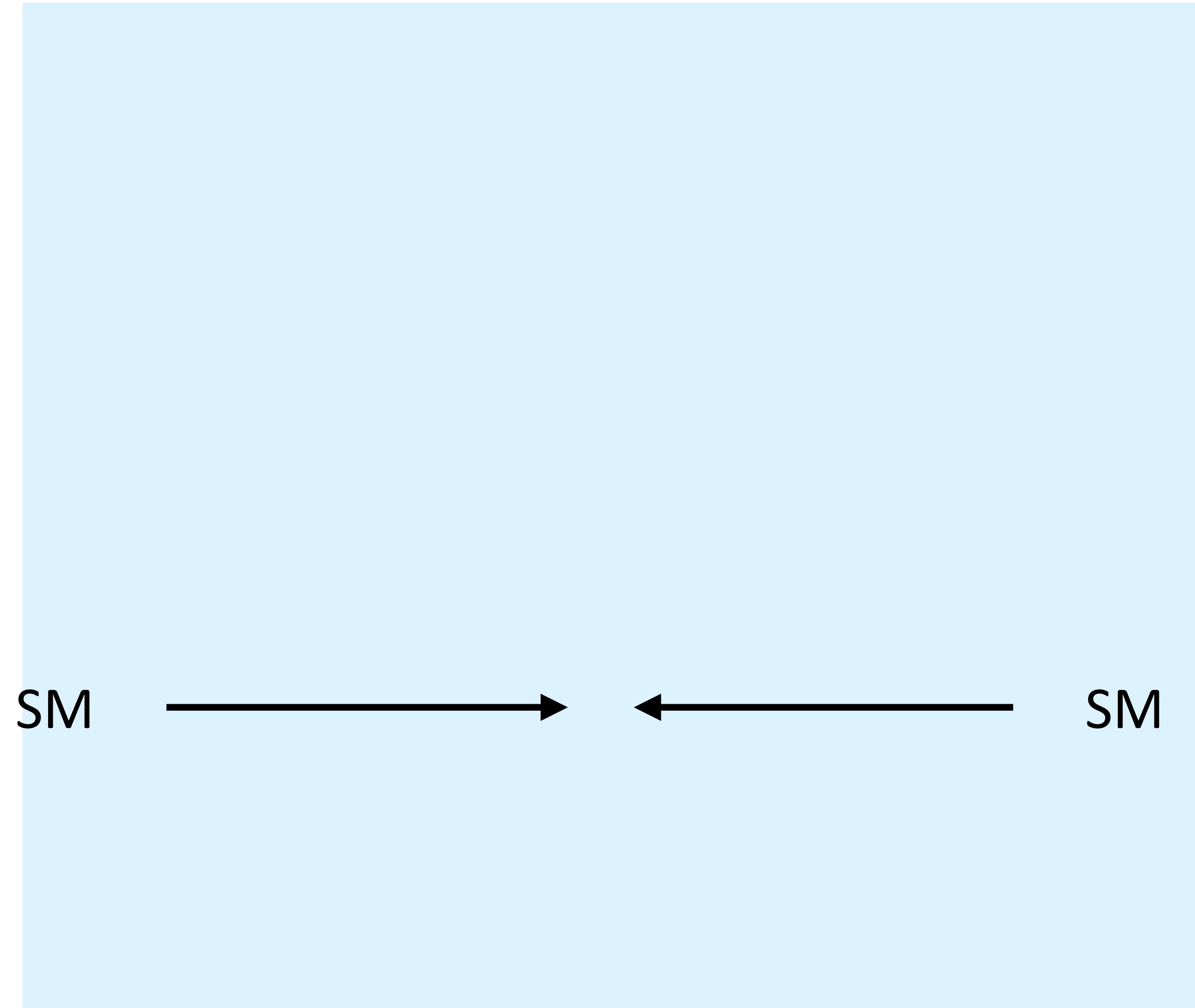
Different mono-X channels

- mono-photon
- mono-jet
- mono-Higgs
- mono-Z
- mono-top

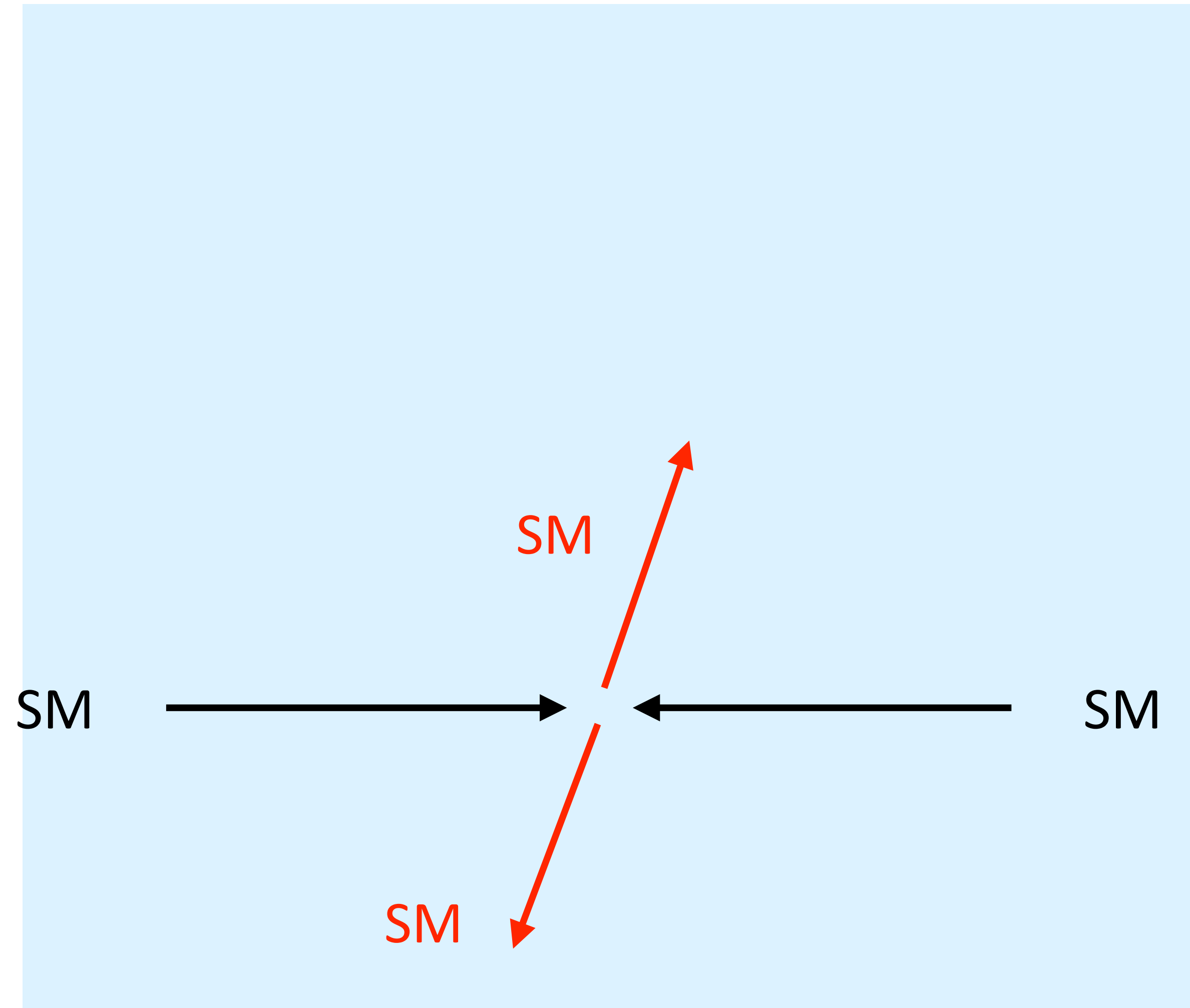
We propose a new dark matter channel at colliders



We propose a new dark matter channel at colliders

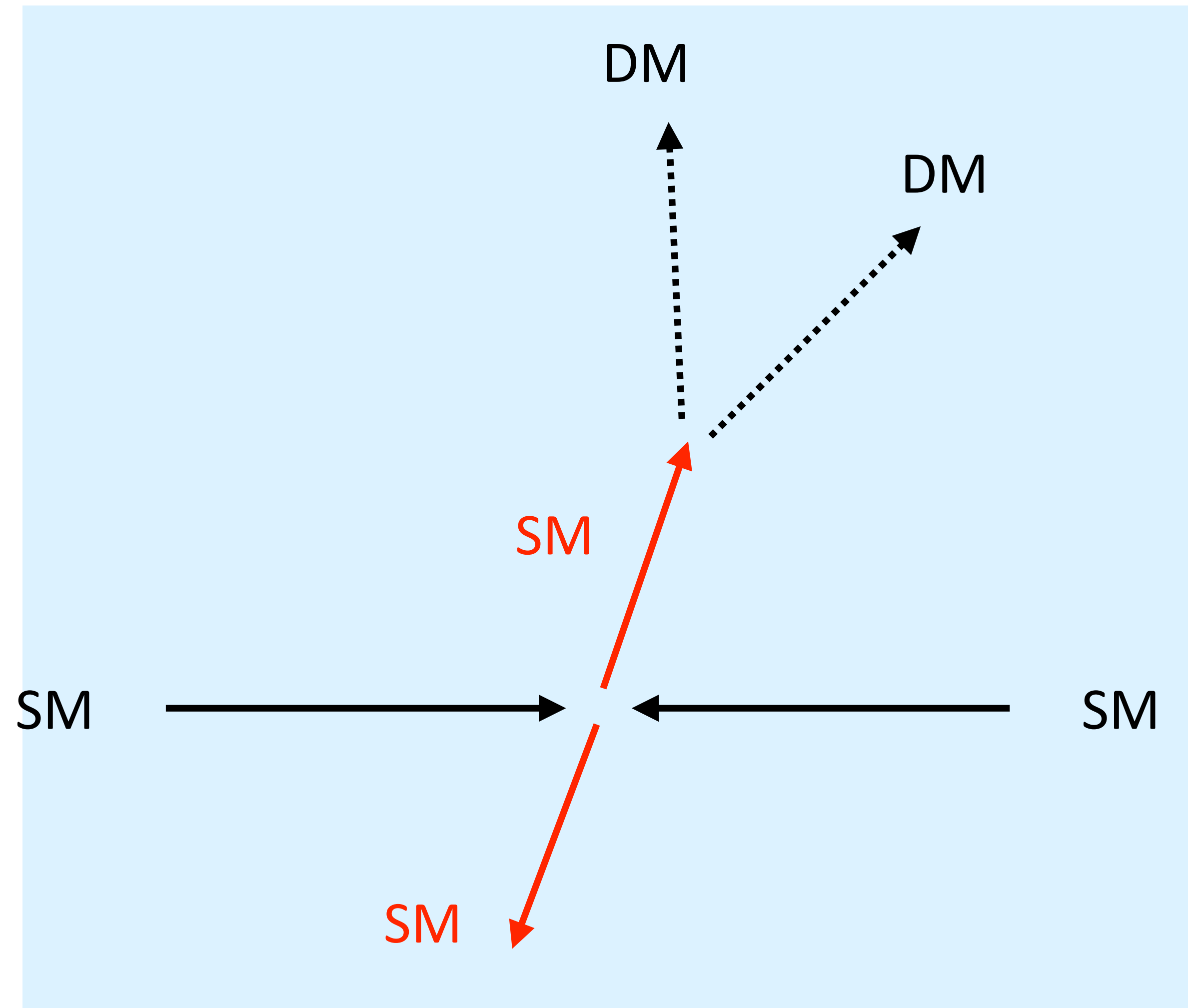


We propose a new dark matter channel at colliders



A pair of SM particles
produced at the primary vertex

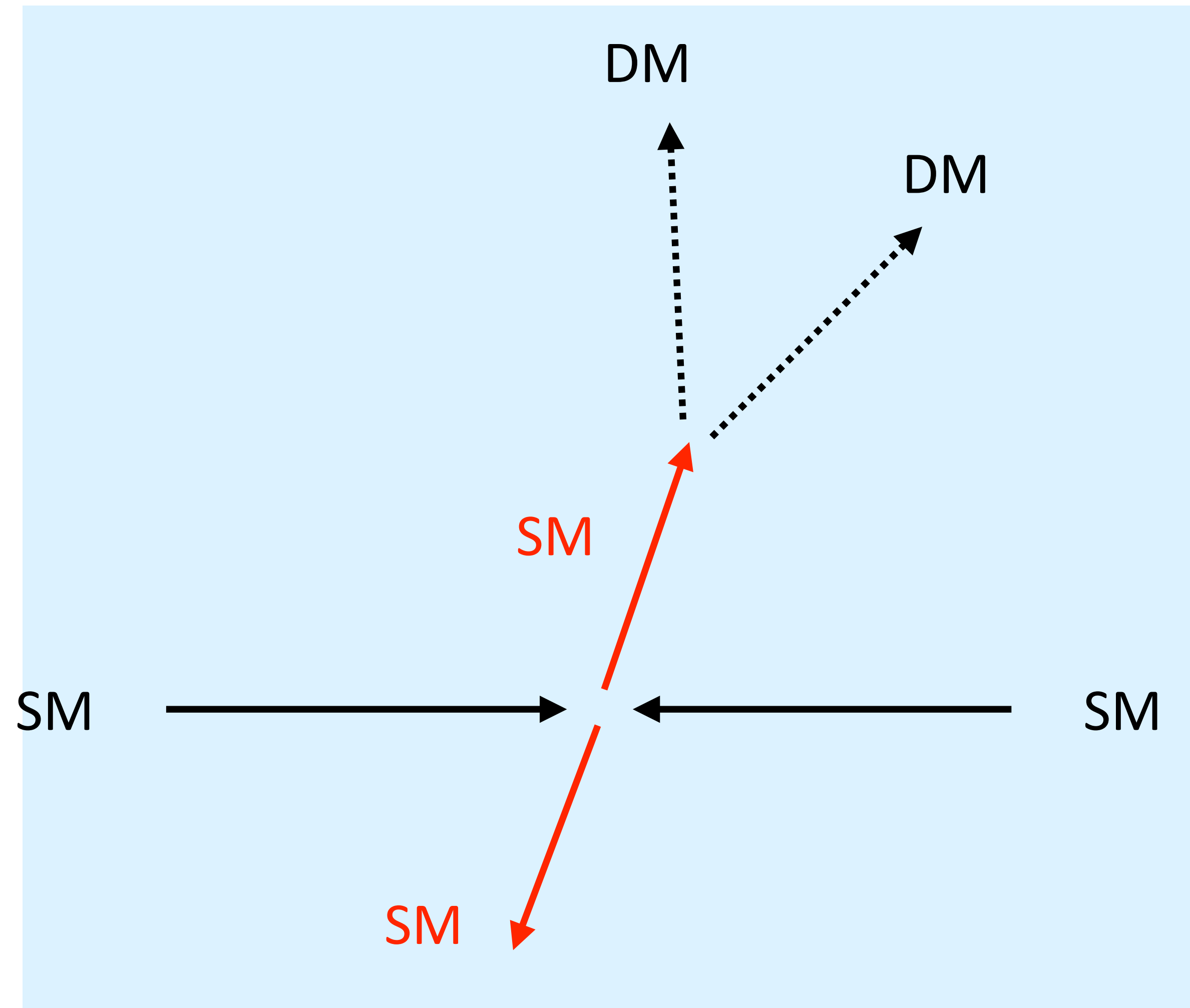
We propose a new dark matter channel at colliders



One SM particle interacts with the detector to produce a pair of DM particles

A pair of SM particles produced at the primary vertex

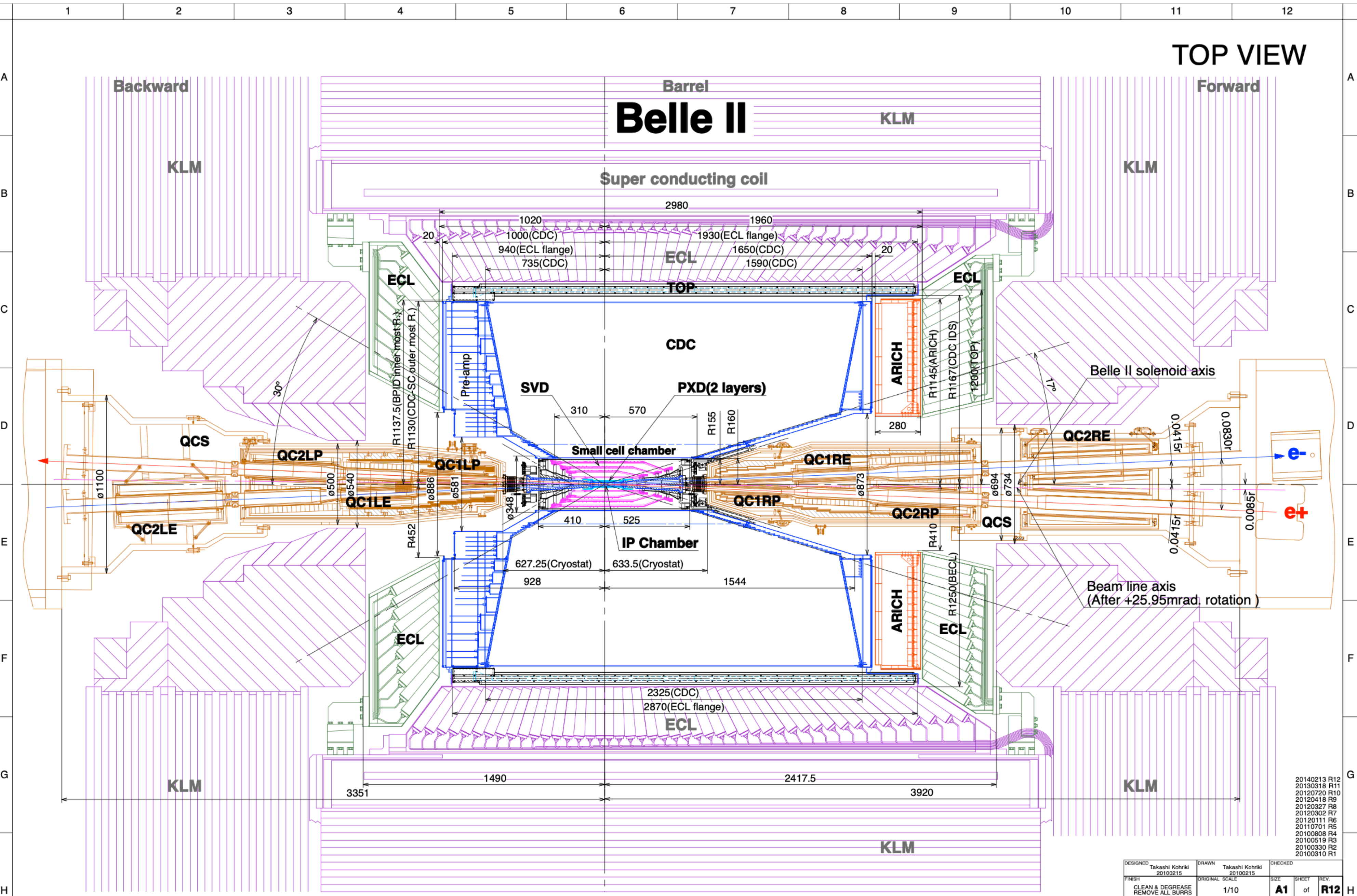
We propose a new dark matter channel at colliders



One SM particle interacts with the detector to produce a pair of DM particles

A pair of SM particles produced at the primary vertex

fixed target in collider



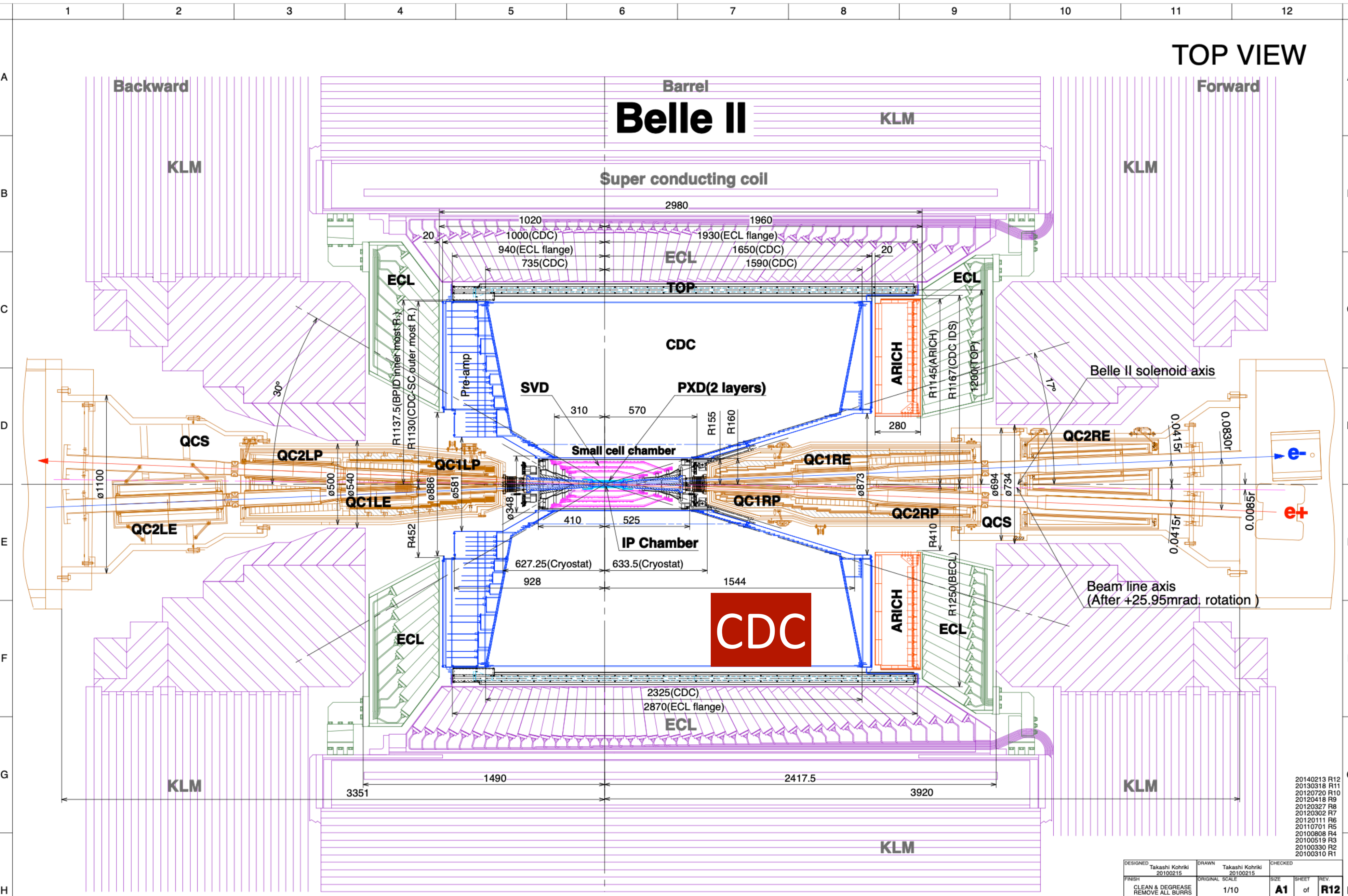
TOP VIEW

Belle II

- 20140213 R12
- 20130318 R11
- 20120720 R10
- 20120418 R9
- 20120327 R8
- 20120302 R7
- 20120111 R6
- 20110701 R5
- 20100808 R4
- 20100519 R3
- 20100330 R2
- 20100310 R1

20140213 R12
 -QCS20131203
 -CDC covers
 -B&FWD new pole pieces

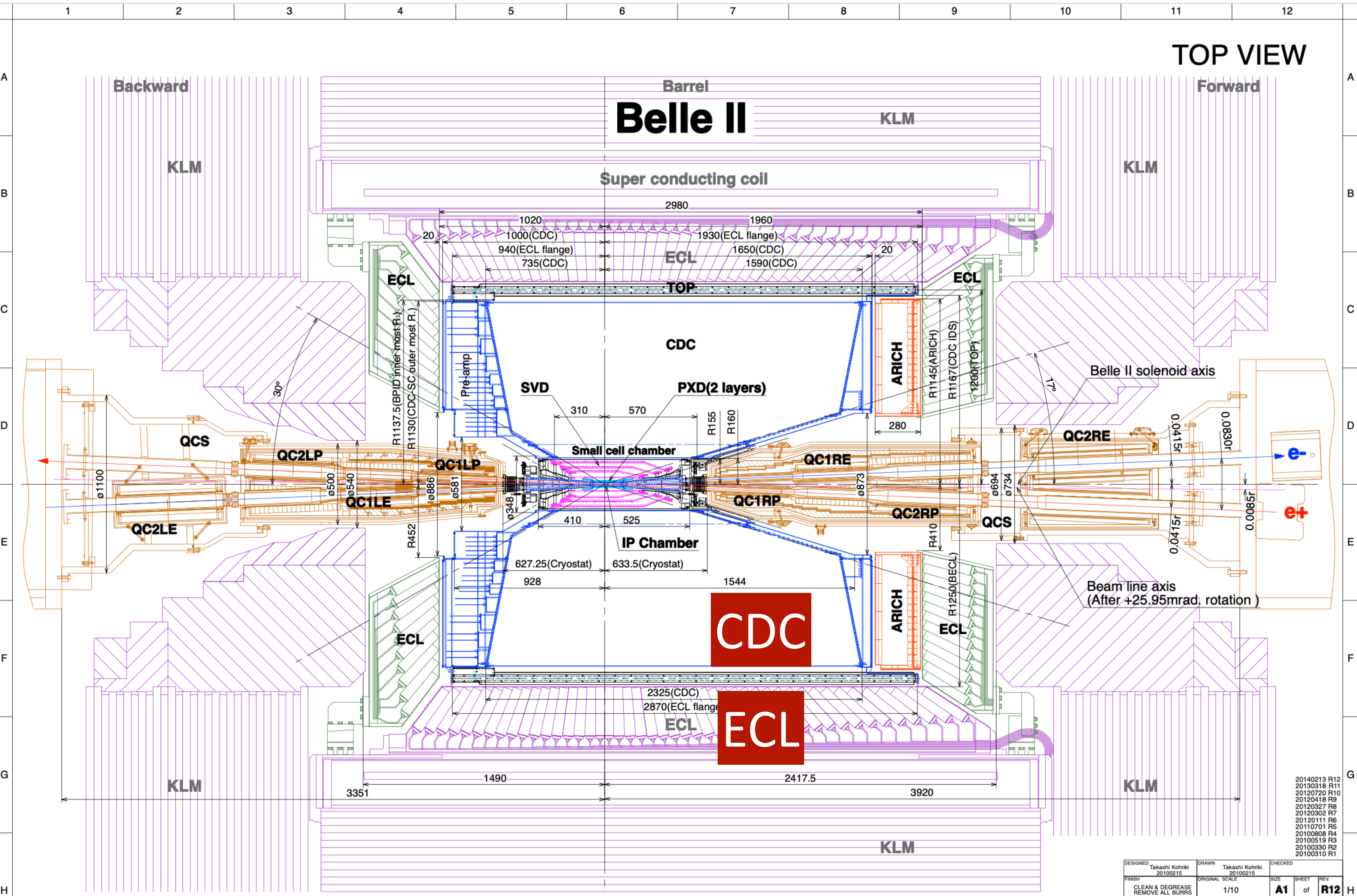
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| DESIGNED Takashi Kohriki 20100215 | DRAWN Takashi Kohriki 20100215 | CHECKED |
| FINISH CLEAN & DEGREASE REMOVE ALL BURRS | ORIGINAL SCALE 1/10 | SIZE SHEET REV. A1 of R12 |
| TITLE Belle-II(Nano beam) IR=±41.5 mrad.(Top view A) | | DRAWING NO. Belle-IITopview±41.5.vwx |
| PROJECT MECHANICAL ENGINEERING GROUP INSTITUTE FOR PARTICLE AND NUCLEAR STUDIES HIGH ENERGY ACCELERATOR RESEARCH ORGANIZATION 6HO 1-1, TSUKUBA, IBARAKI 305-0801, JAPAN | | PROJECTION Belle II |



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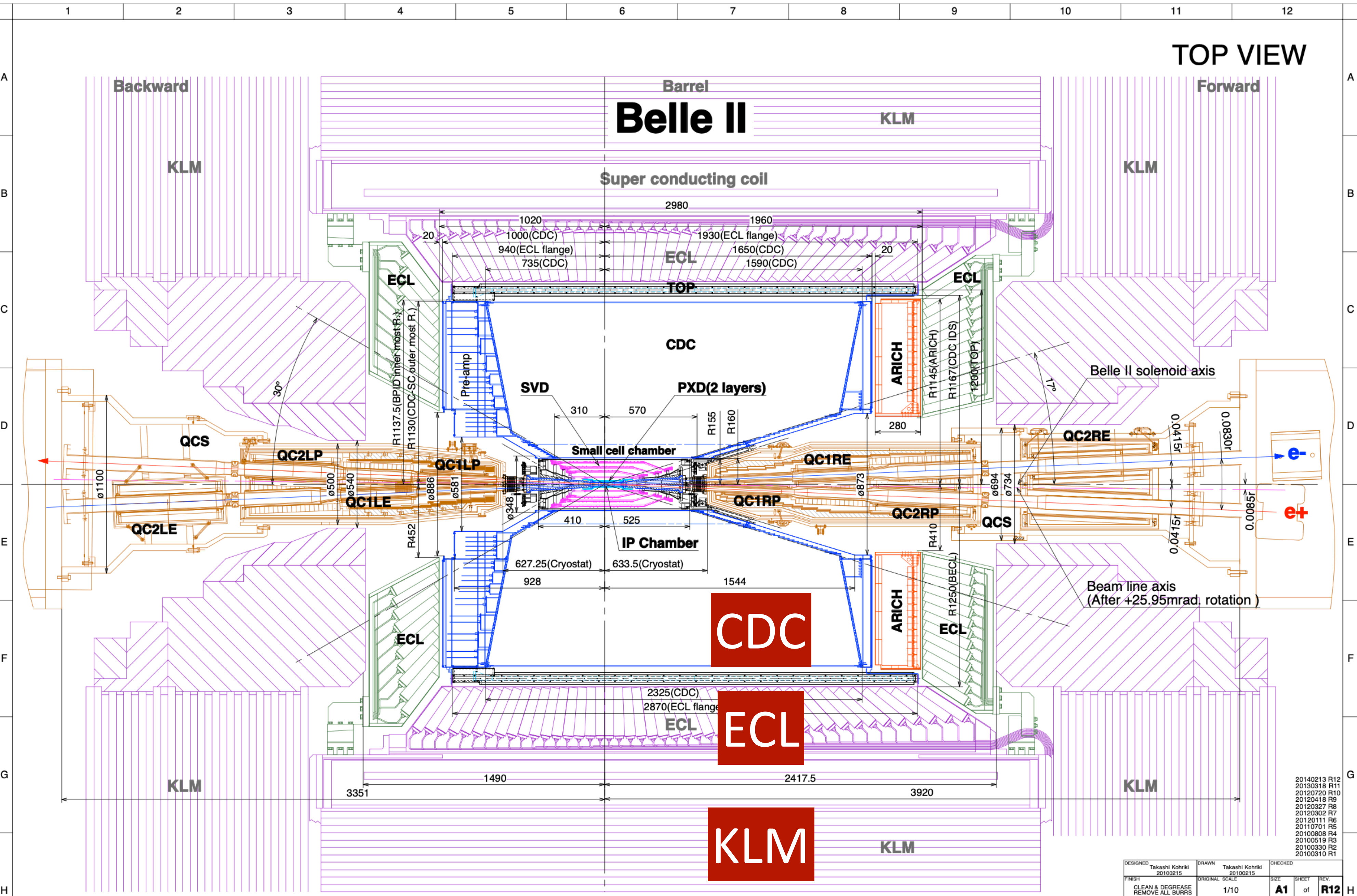
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TOP VIEW

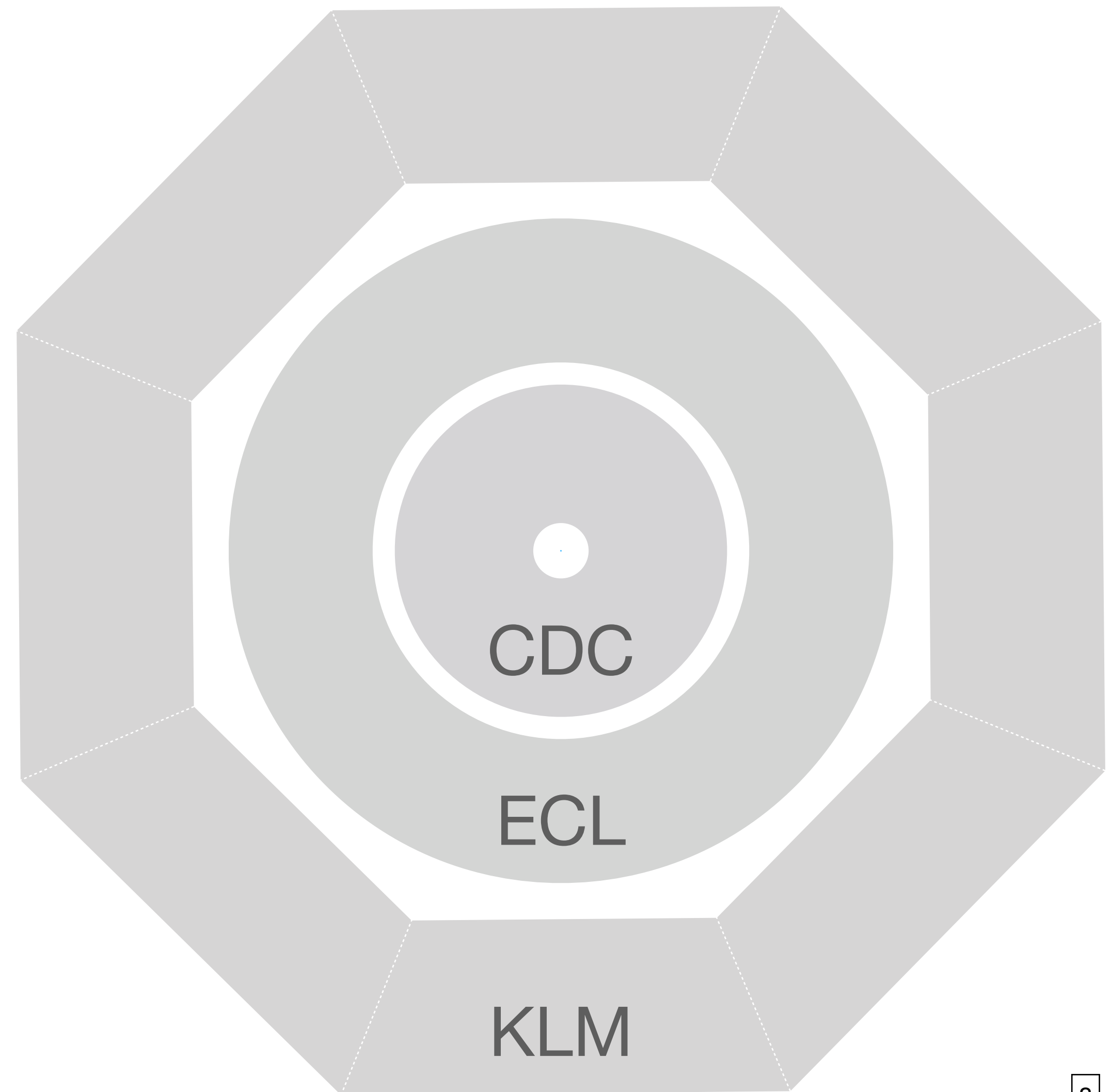
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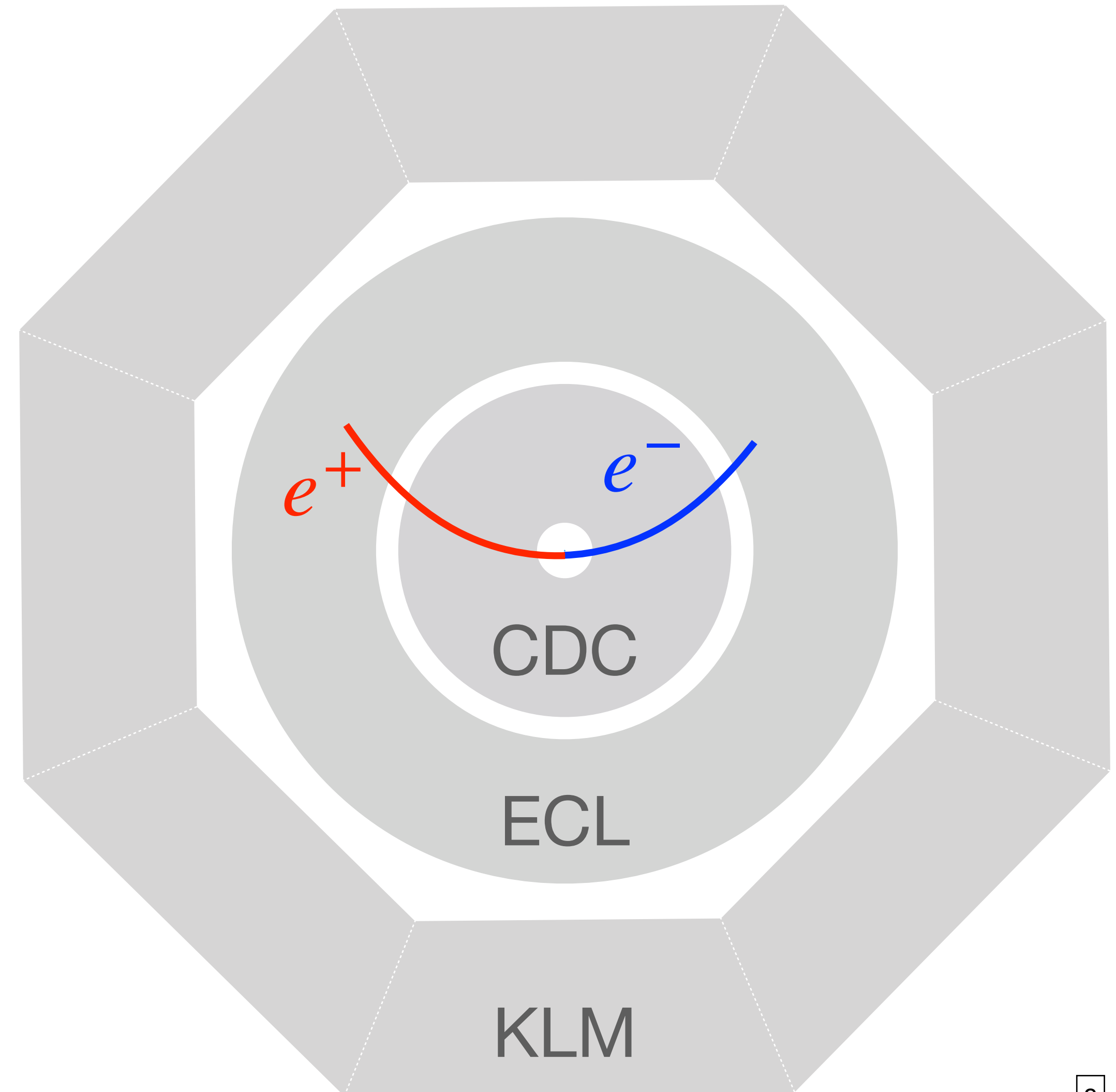
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New DM channel @ Belle II (x-y plane)



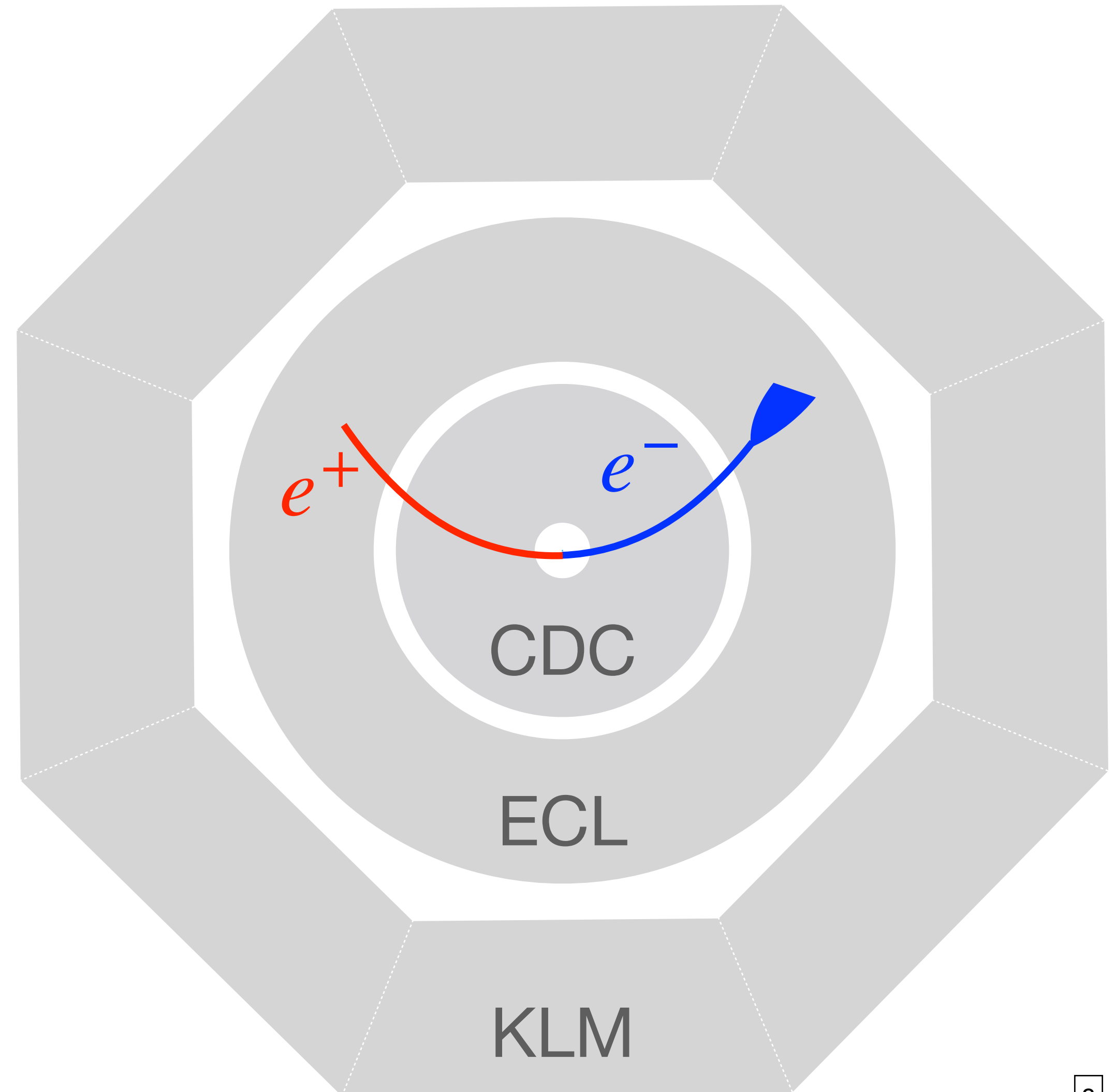
New DM channel @ Belle II (x-y plane)

- $e^+e^- \rightarrow e^+e^-$



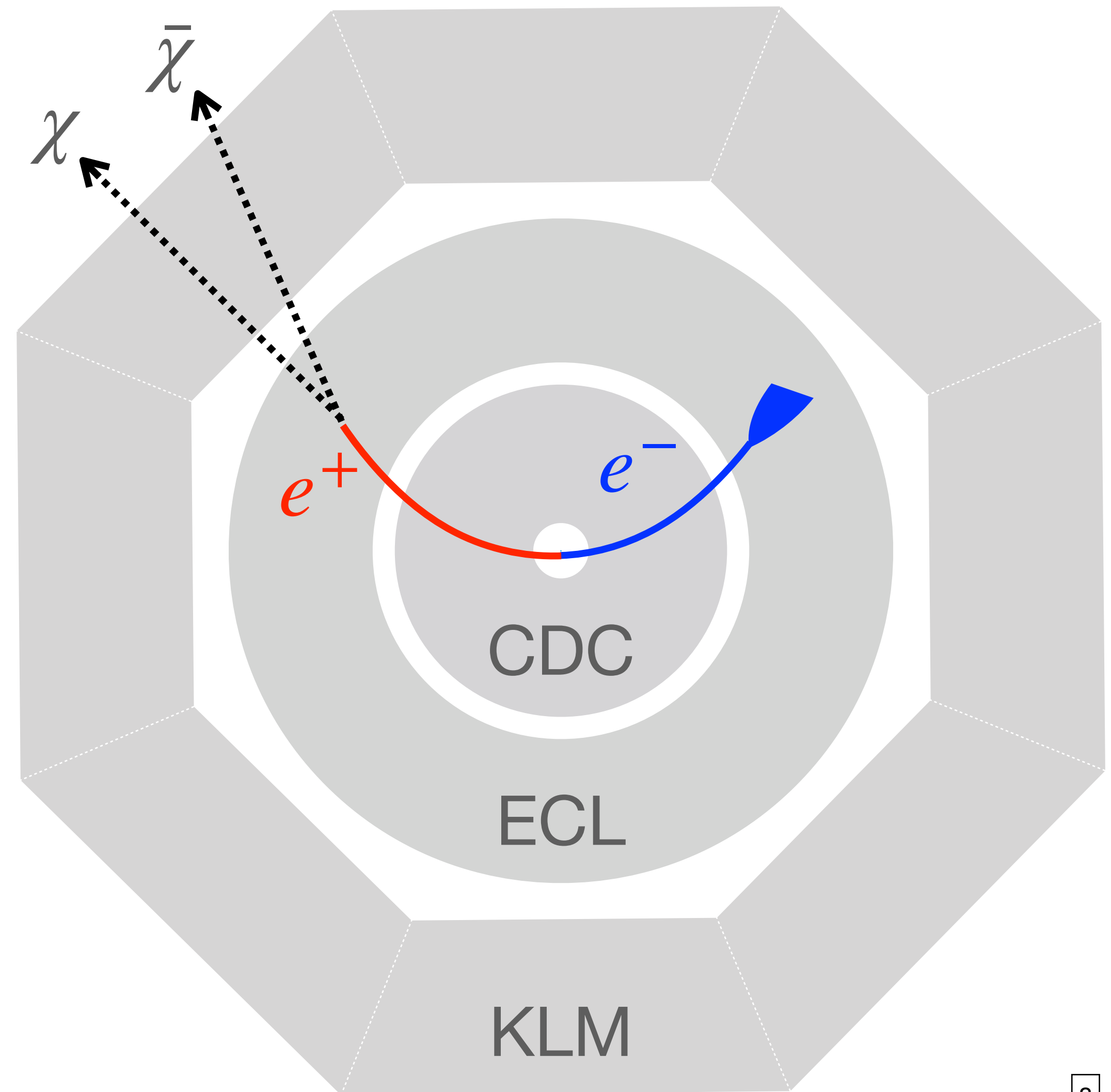
New DM channel @ Belle II (x-y plane)

- $e^+e^- \rightarrow e^+e^-$
- e^- deposit energy in ECL



New DM channel @ Belle II (x-y plane)

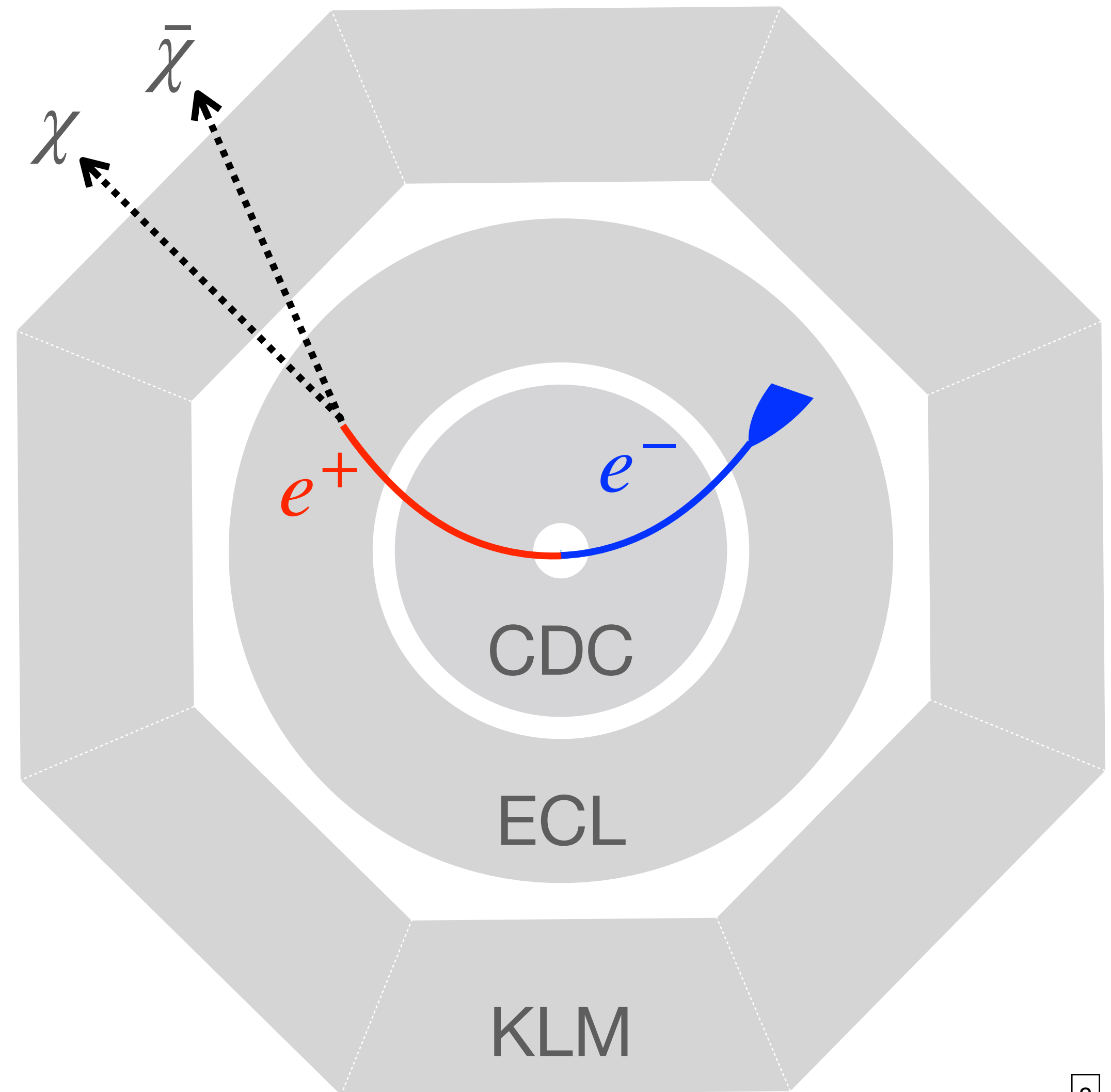
- $e^+e^- \rightarrow e^+e^-$
- e^- deposit energy in ECL
- e^+ interact with ECL to produce DM



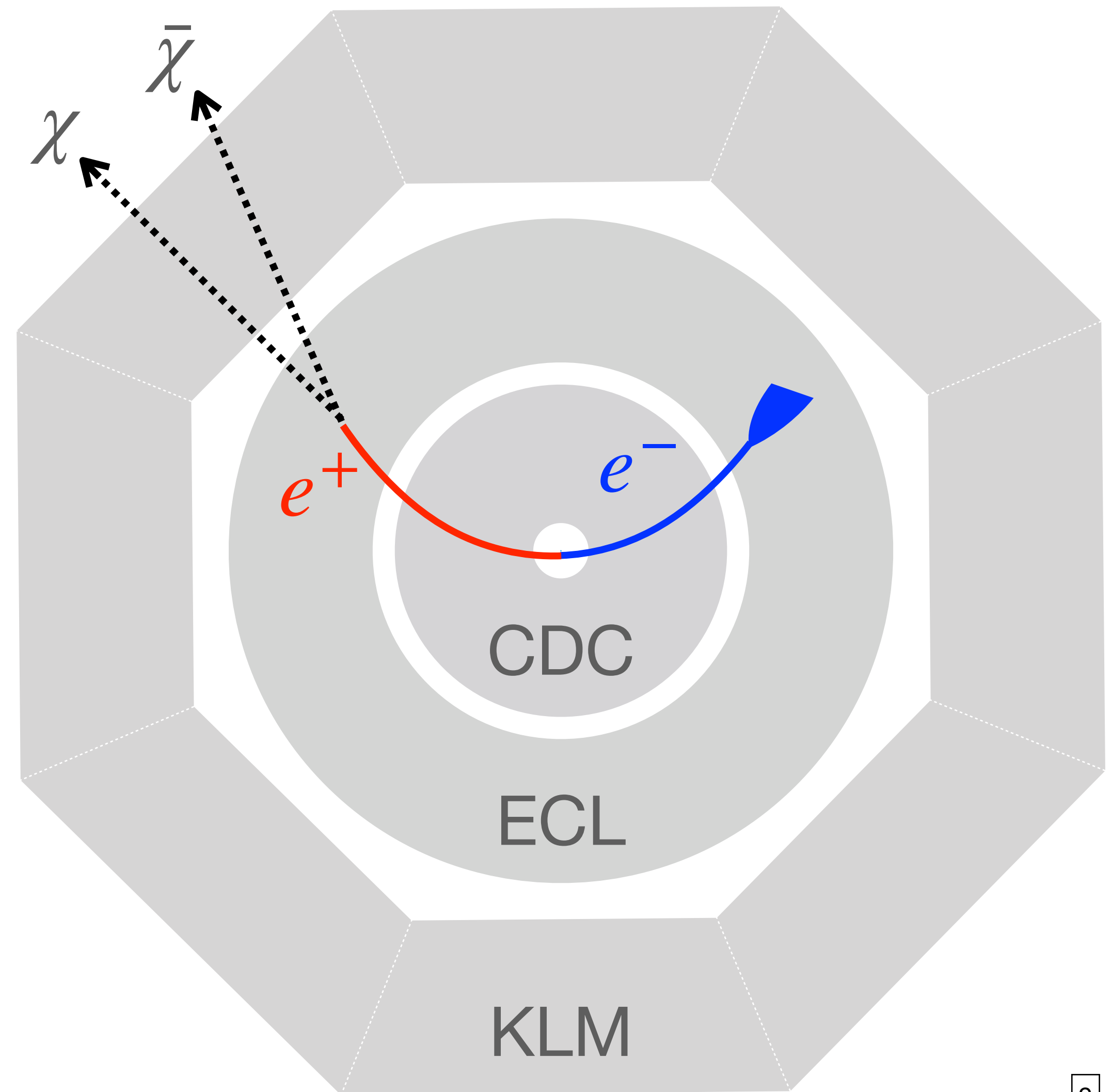
New DM channel @ Belle II (x-y plane)

- $e^+e^- \rightarrow e^+e^-$
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- e^+ interact with ECL to produce DM

disappearing positron track



“disappearing positron track” signature

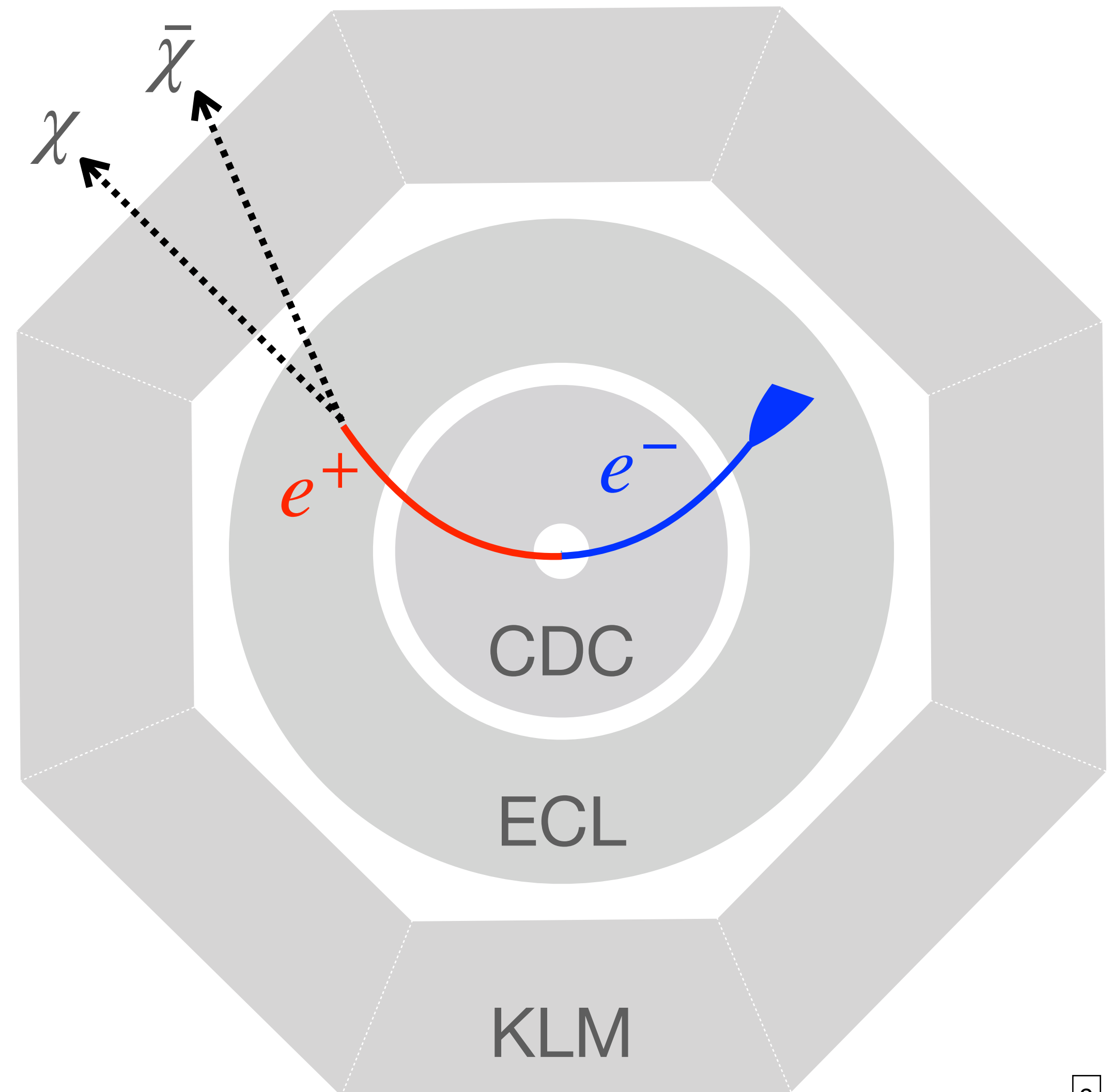


“disappearing positron track” signature

- CDC: e^- & e^+

$$\text{CDC: } \frac{\delta p_T}{p_T} \simeq 0.4 \% \text{ for } p_T \simeq 3 \text{ GeV}$$

Equal & opposite momenta
for e^- & e^+ in the CM frame



“disappearing positron track” signature

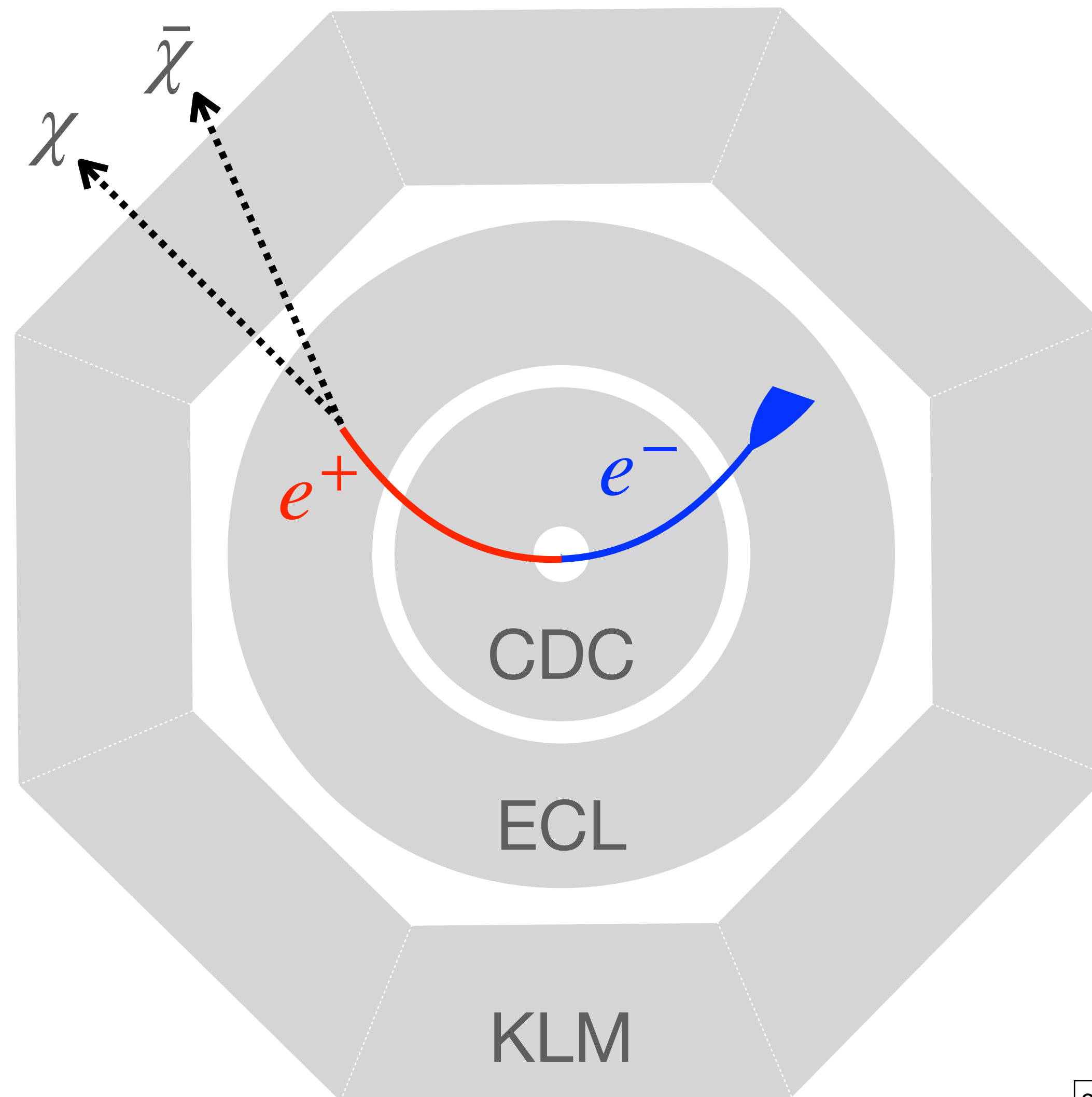
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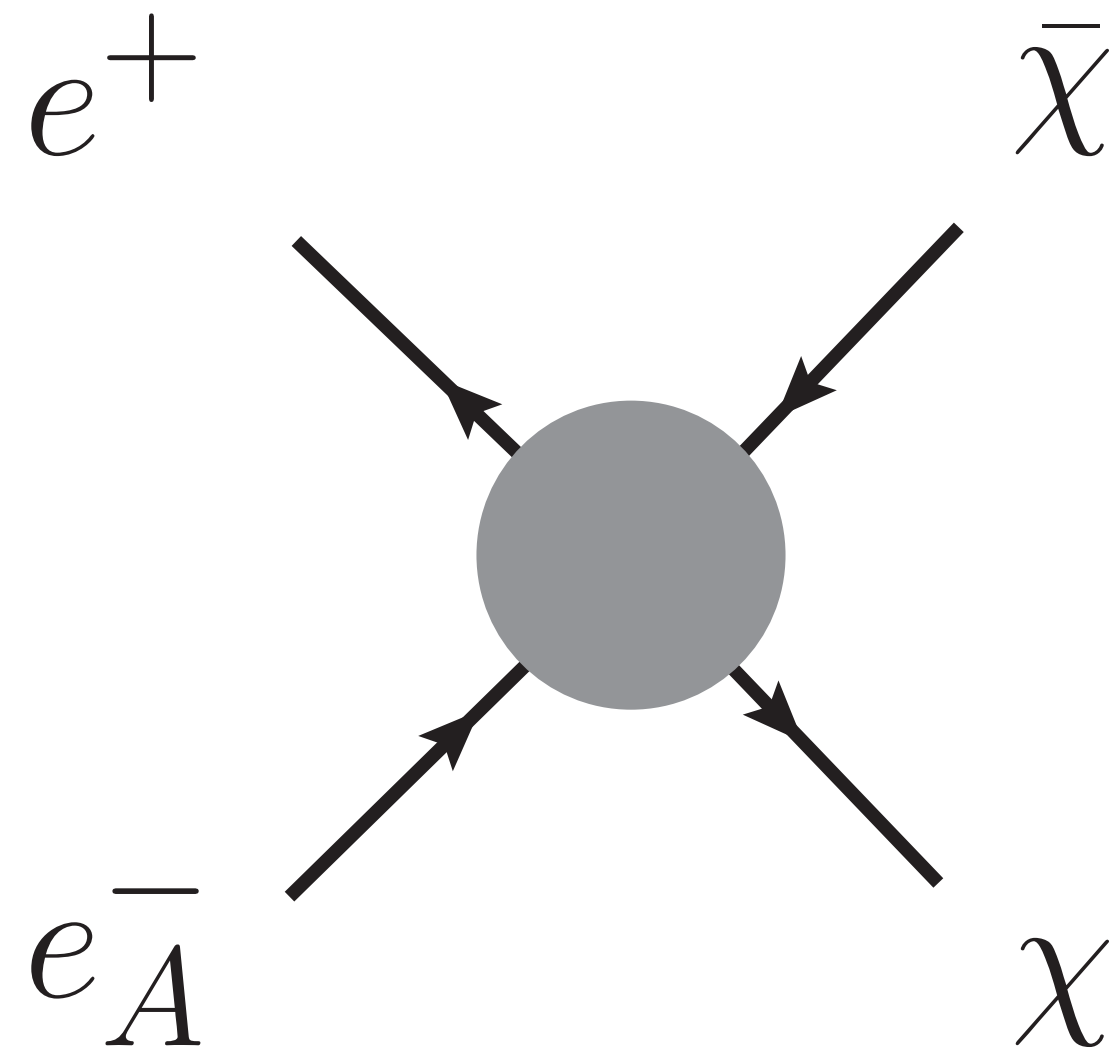
Equal & opposite momenta
for e^- & e^+ in the CM frame

- ECL: e^- & e^+

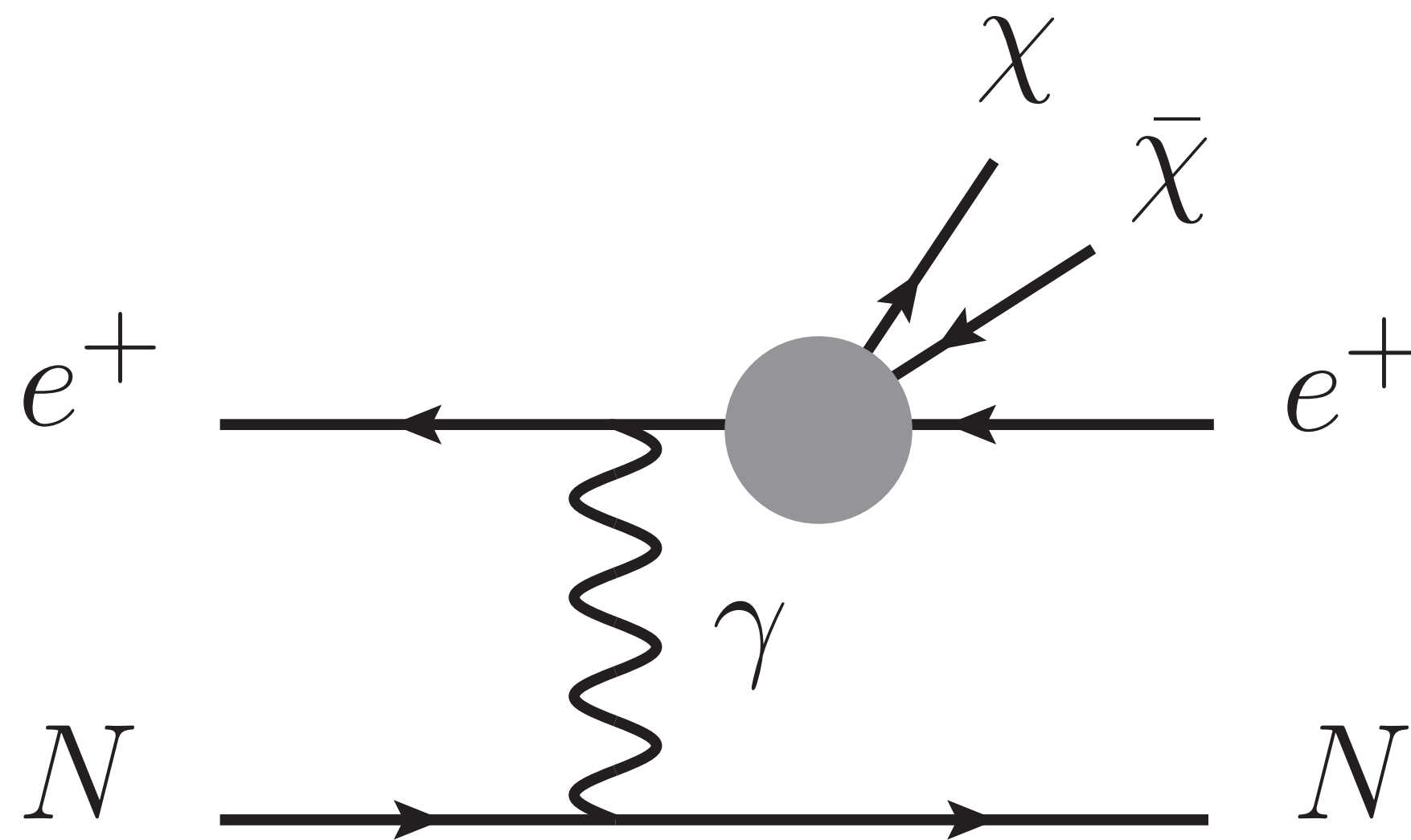
missing energy: $<5\%$ e^+ energy in ECL



Positron interaction with ECL



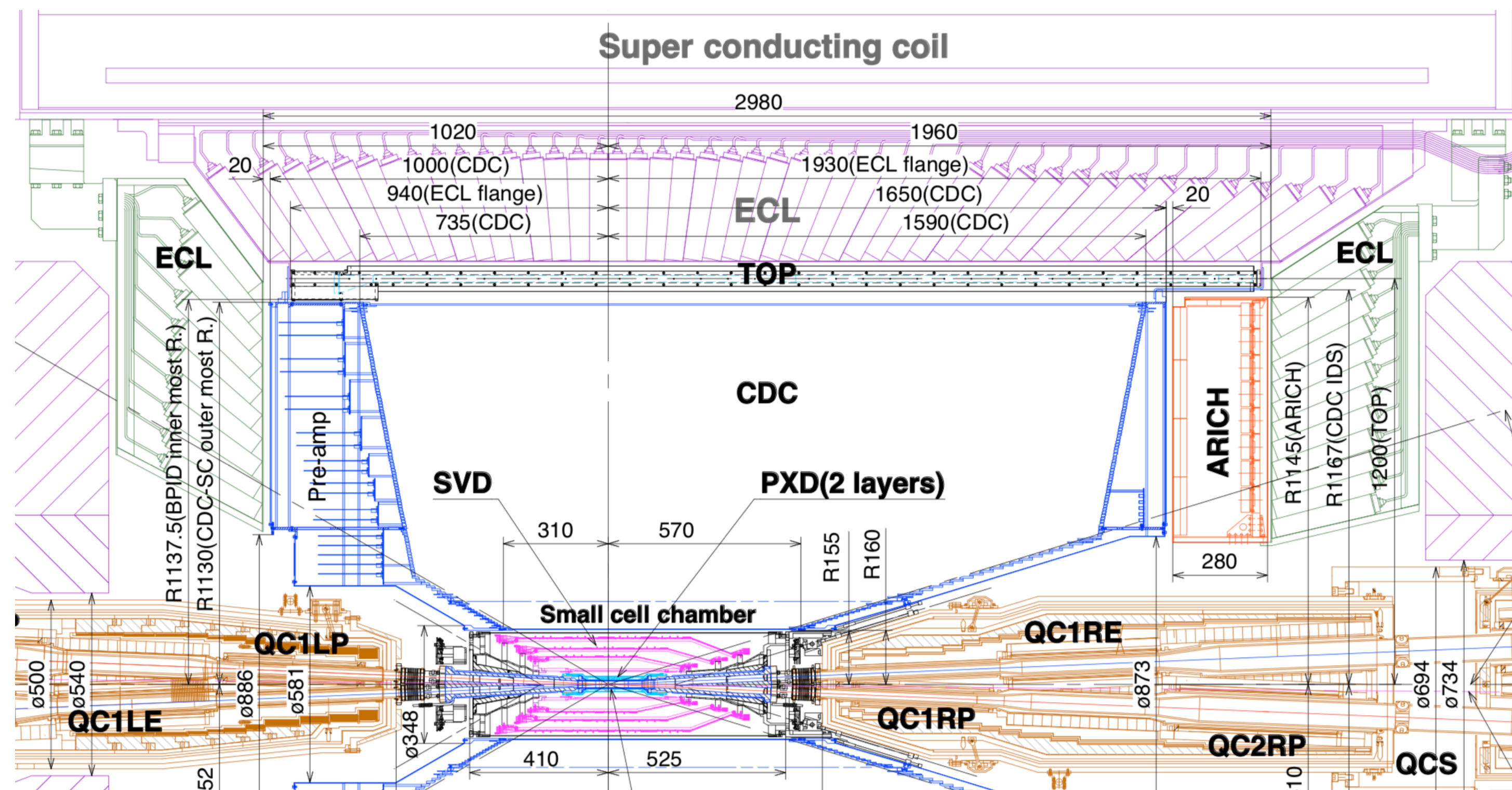
annihilation w/
atomic electrons



bremsstrahlung w/
target nucleus

Use the ECL barrel region as the fixed target

ECL barrel: $32.2^\circ < \theta < 128.7^\circ$

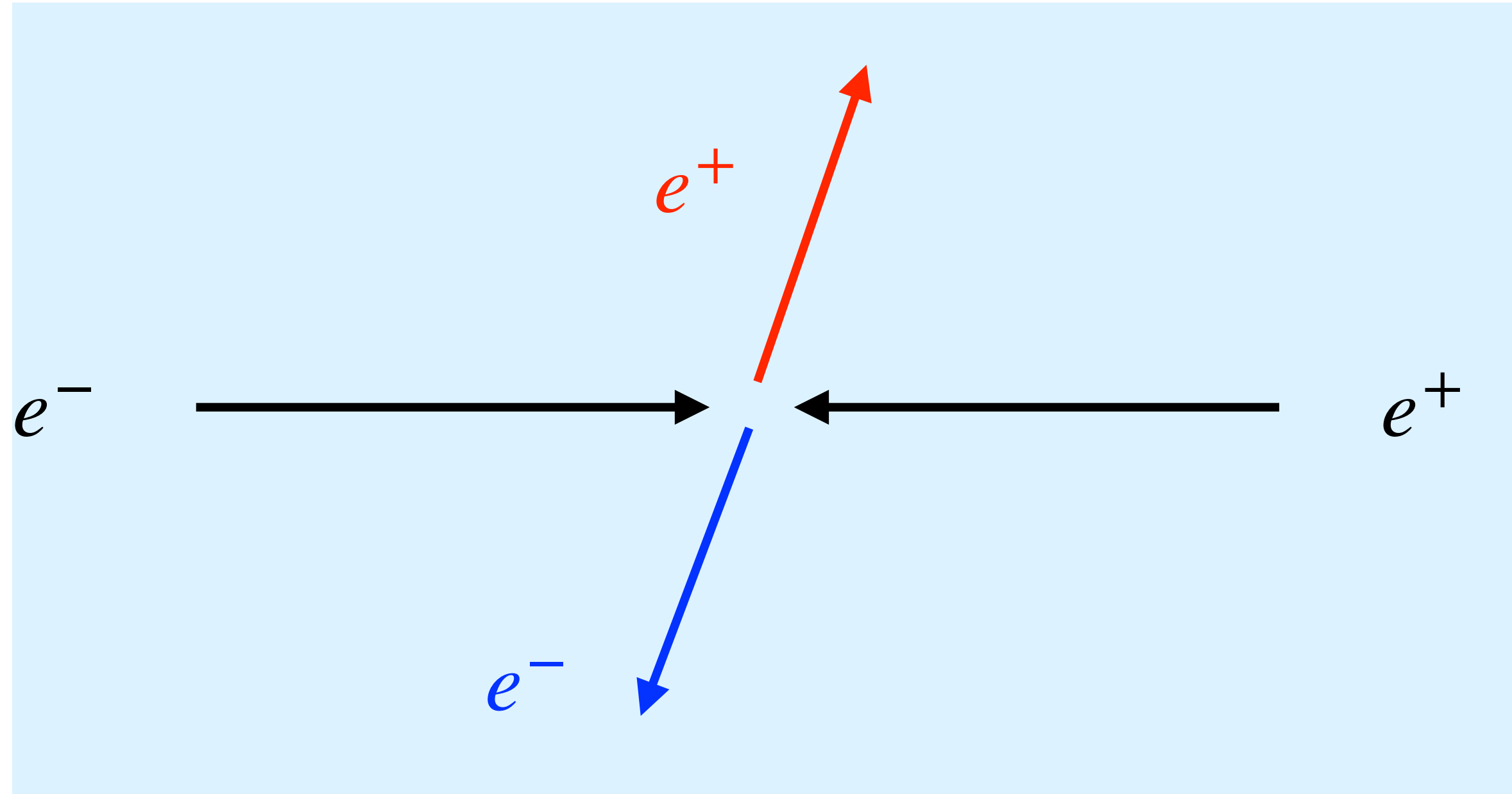


Better hermiticity
(non-projective gaps
between ECL crystals)

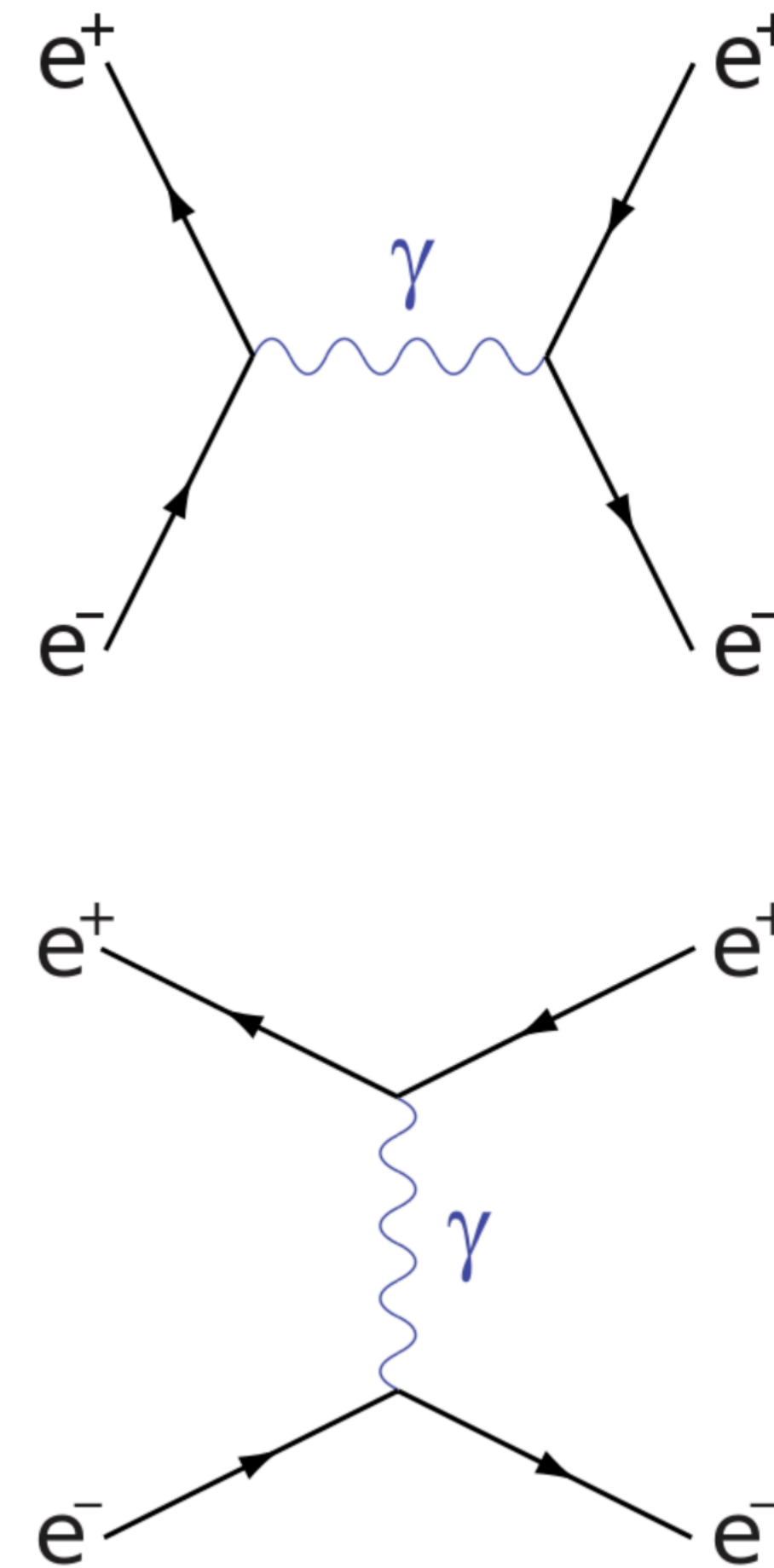
Less non-instrumented setups
(e.g., magnetic wires)
between ECL & KLM

More beam BG in Endcaps

Positrons in Bhabha scattering



$6 \times 10^{11} e^+e^-$ in the barrel region with 50/ab

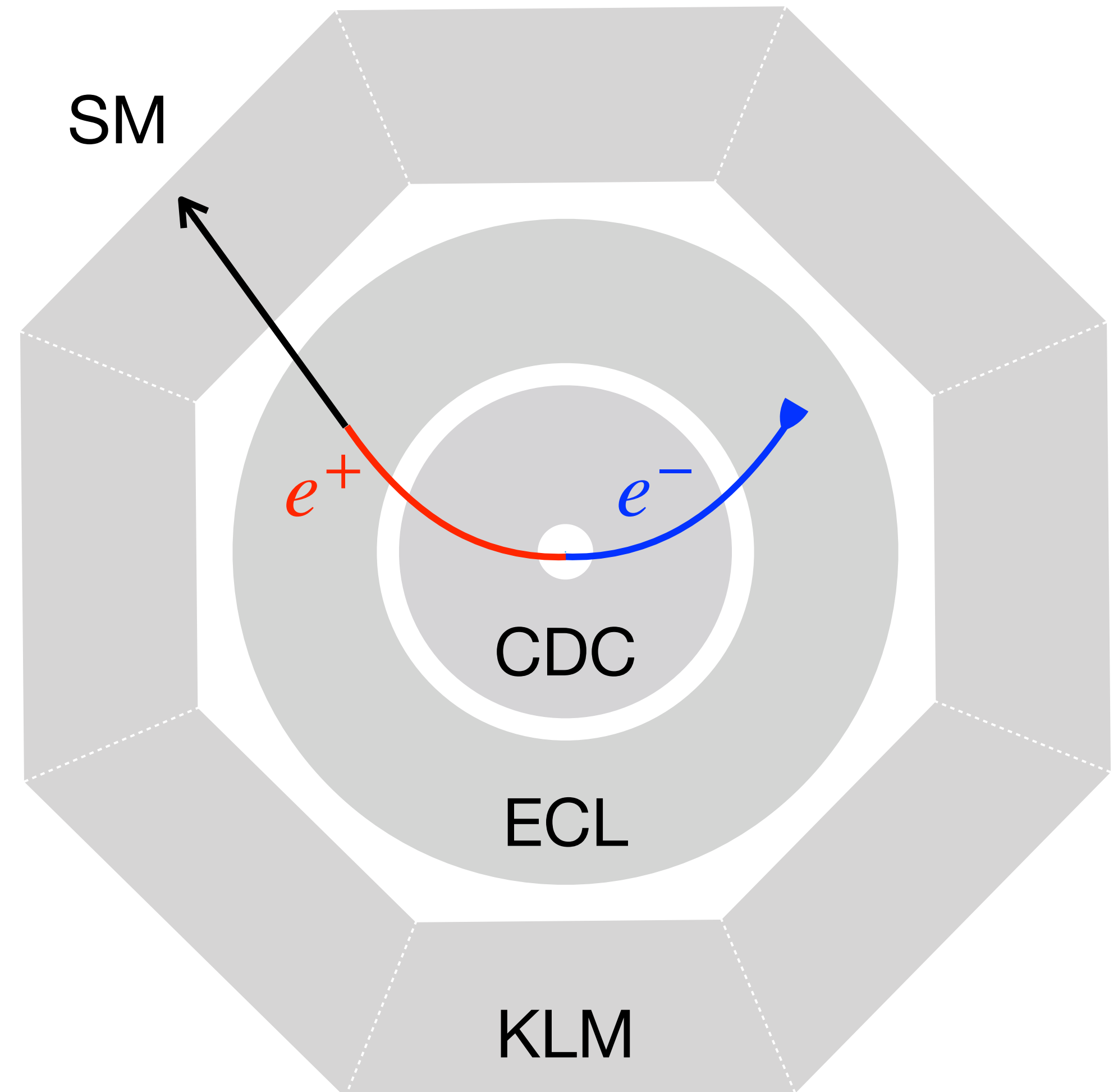


2

Standard model backgrounds

Standard model backgrounds

BG: $e^+ + \text{ECL} \rightarrow \text{SM}$
which then escape detection

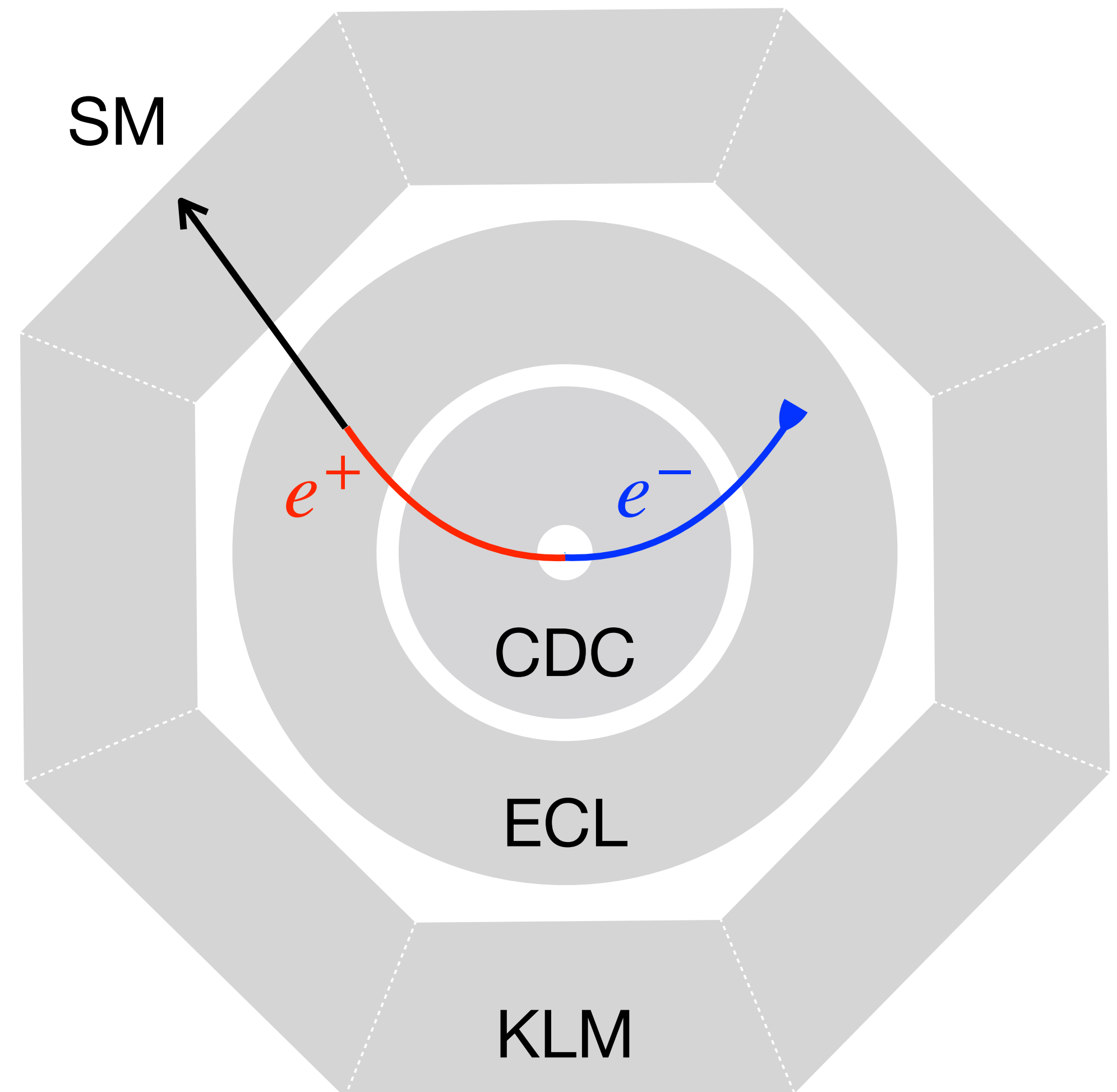


Standard model backgrounds

BG: $e^+ + \text{ECL} \rightarrow \text{SM}$

which then escape detection

- Charged particles (e, μ, π^\pm): likely detected by ECL and/or KLM
- Neutral particles (n, γ, ν): more difficult to detect



Standard model backgrounds

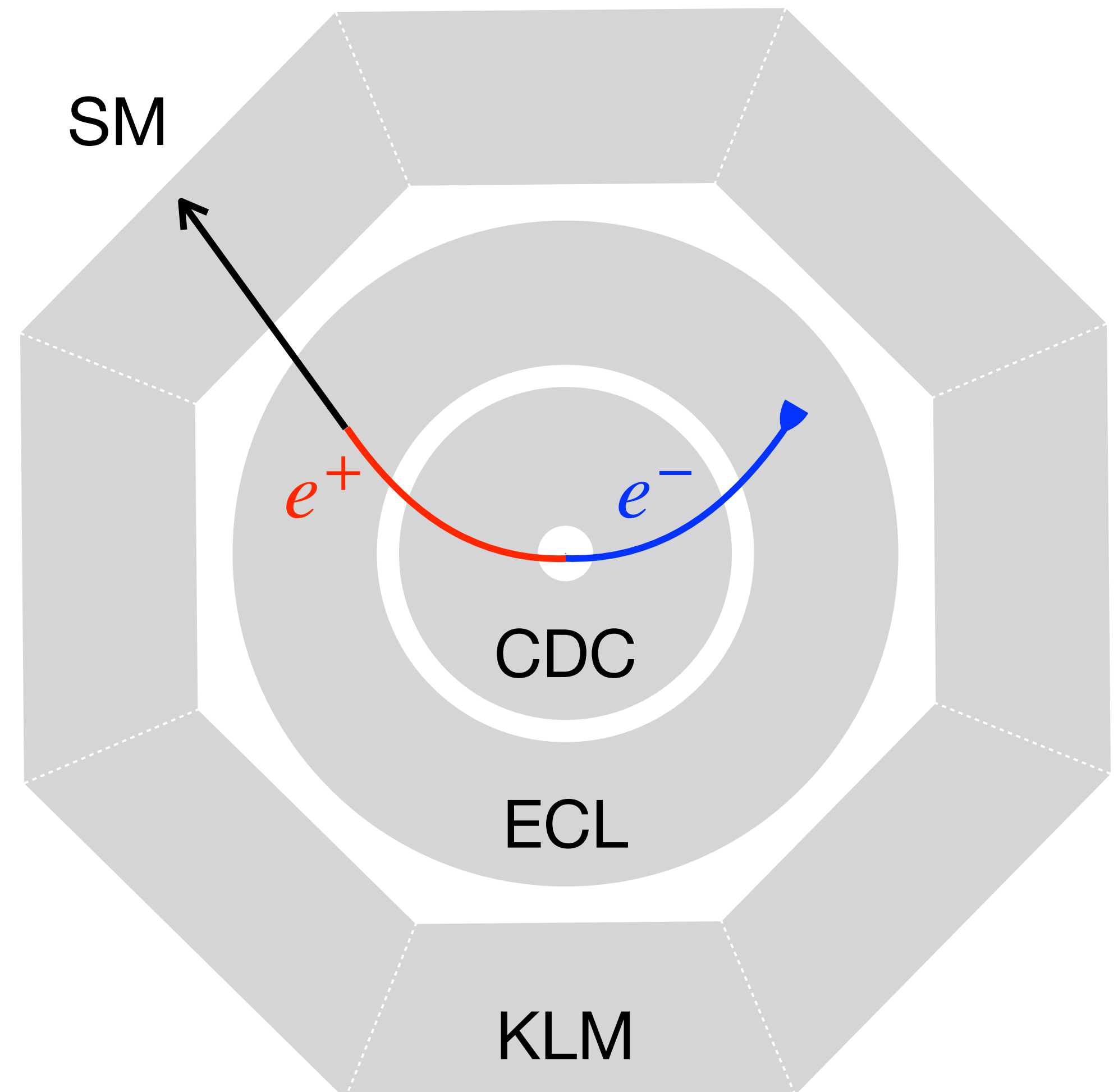
BG: $e^+ + \text{ECL} \rightarrow \text{SM}$

which then escape detection

- Charged particles (e, μ, π^\pm): likely detected by ECL and/or KLM
- Neutral particles (n, γ, ν): more difficult to detect

Neutrino BG is negligible (xsec is small)

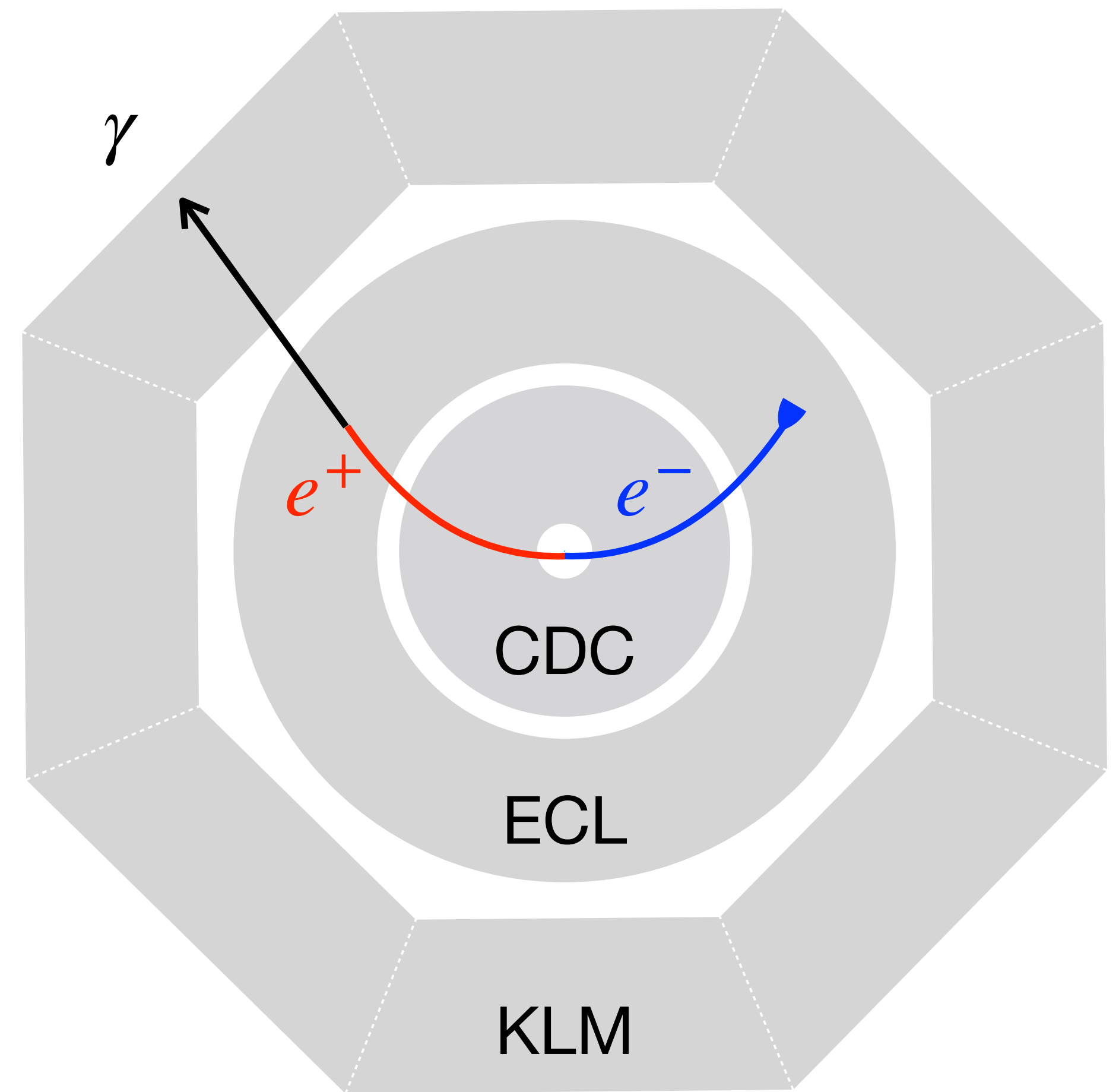
Main BG is due to n/γ



Photon-induced background

Photon energy measured in ECL

ECL = 16- X_0 CsI crystals, w/ $X_0 = 1.86$ cm



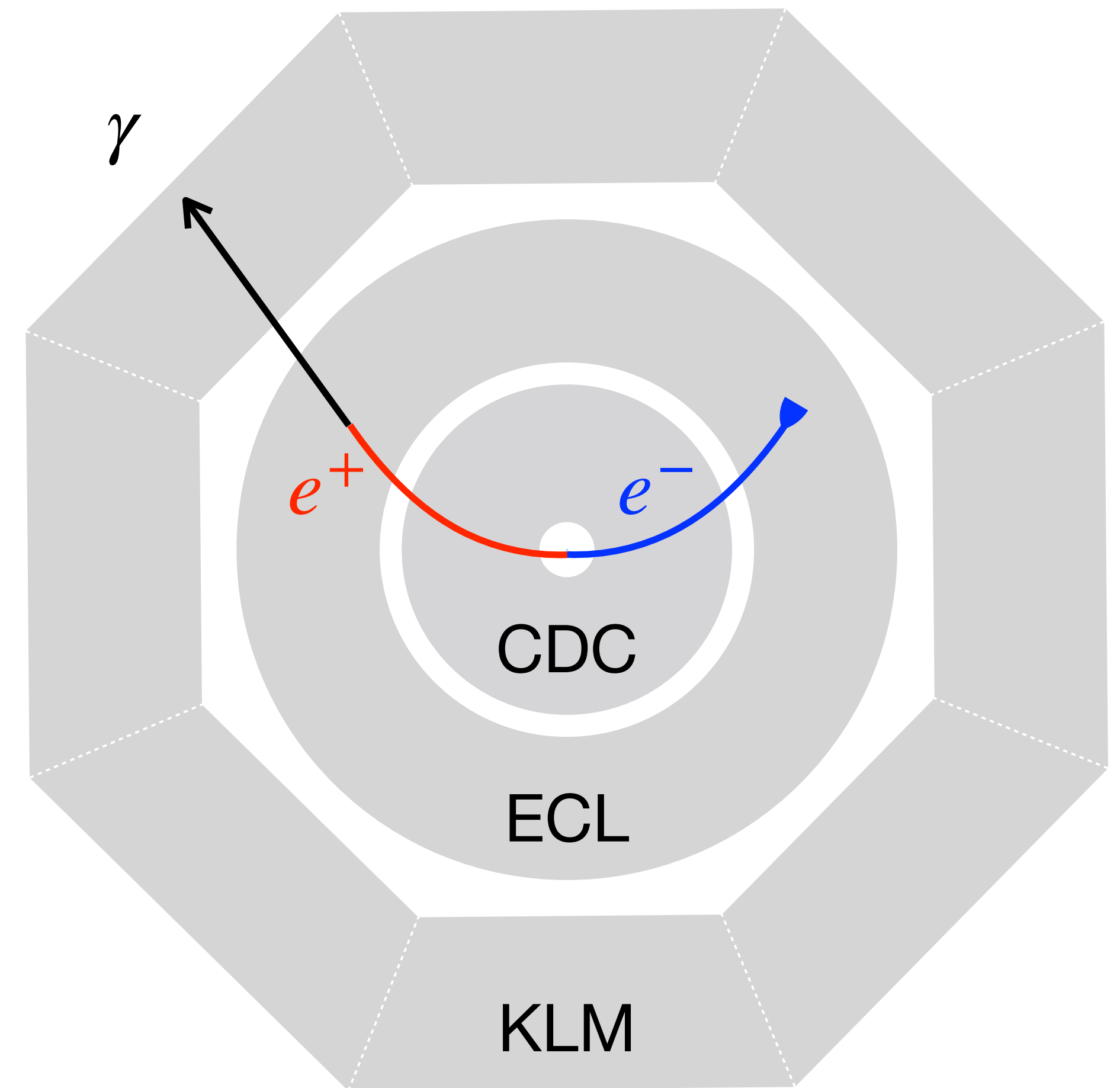
Photon-induced background

Photon energy measured in ECL

ECL = 16- X_0 CsI crystals, w/ $X_0 = 1.86$ cm

Photon can also be detected by KLM

KLM = alternating sandwich of 4.7-cm iron plates and active detectors



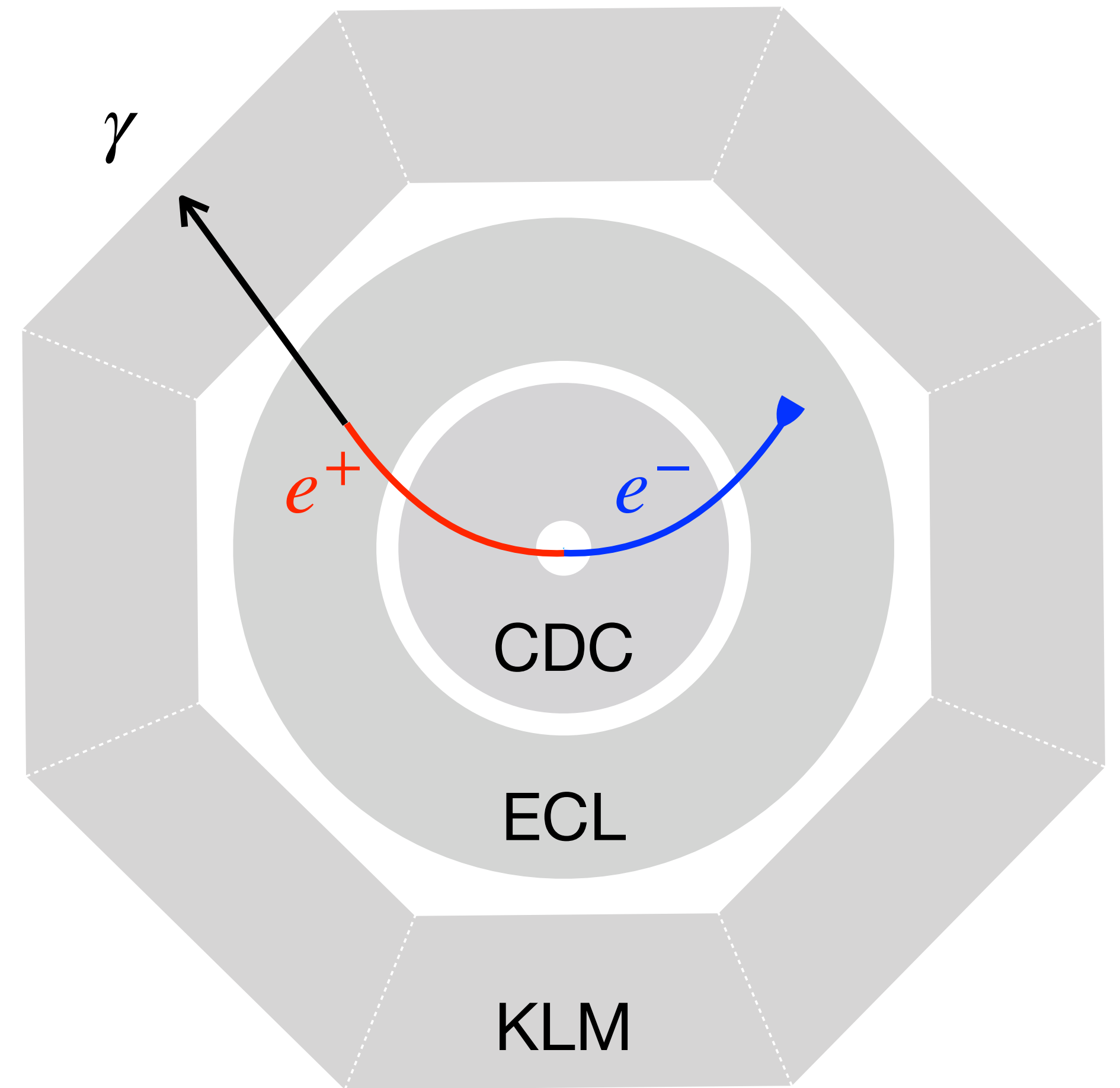
Photon escapes ECL

Photon energy spectrum due to e^+ collision with ECL

[Tsai & Whitis 1966]

$$\frac{dN_\gamma}{dx_\gamma}(t, x_\gamma) \simeq \frac{1}{x_\gamma} \frac{(1 - x_\gamma)^{(4/3)t} - e^{-(7/9)t}}{7/9 + (4/3)\ln(1 - x_\gamma)}$$

$$x_\gamma = E_\gamma / E_e \quad tX_0 \text{ is the distance}$$



Photon escapes ECL

Photon energy spectrum due to e^+ collision with ECL

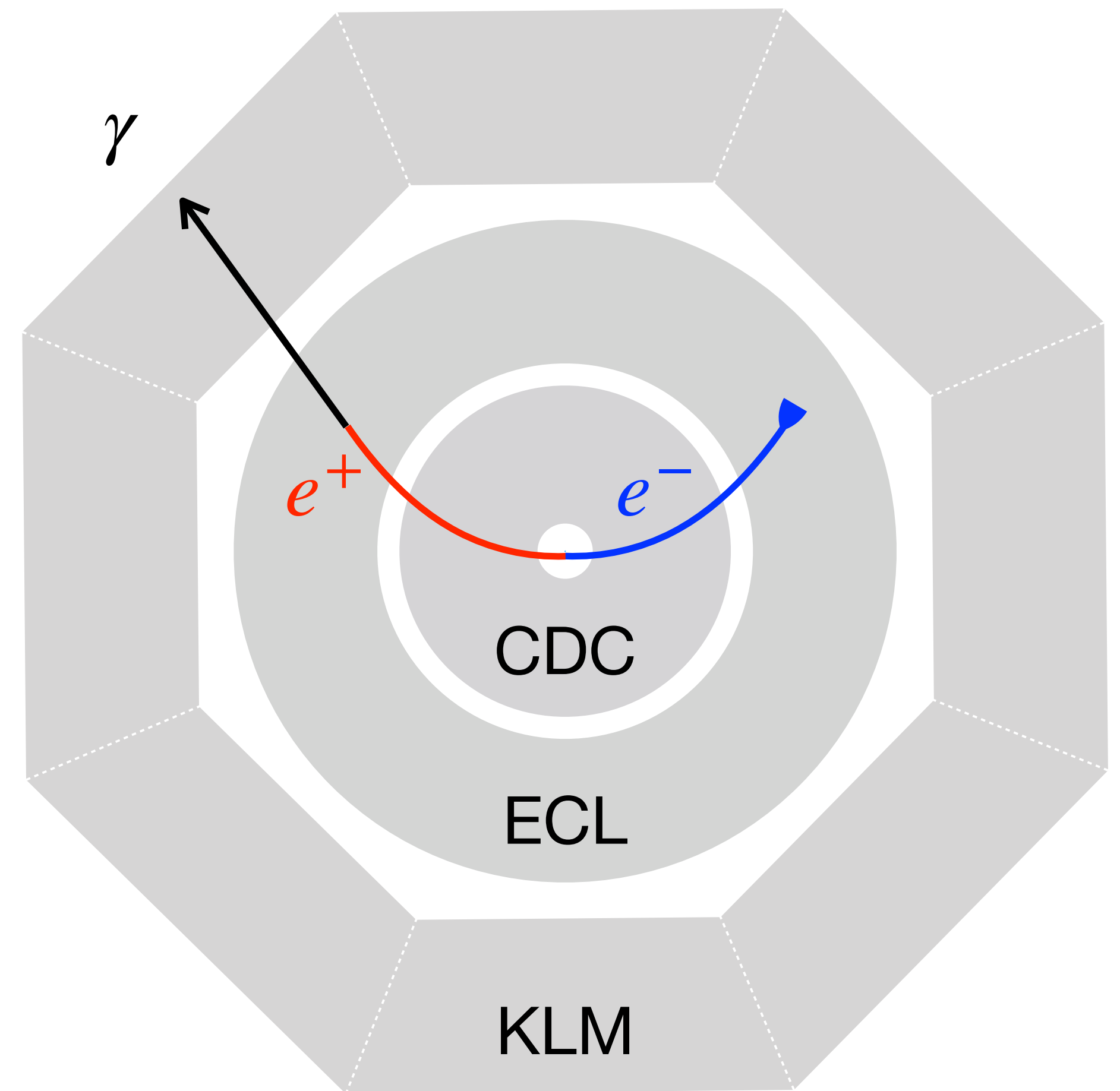
[Tsai & Whitis 1966]

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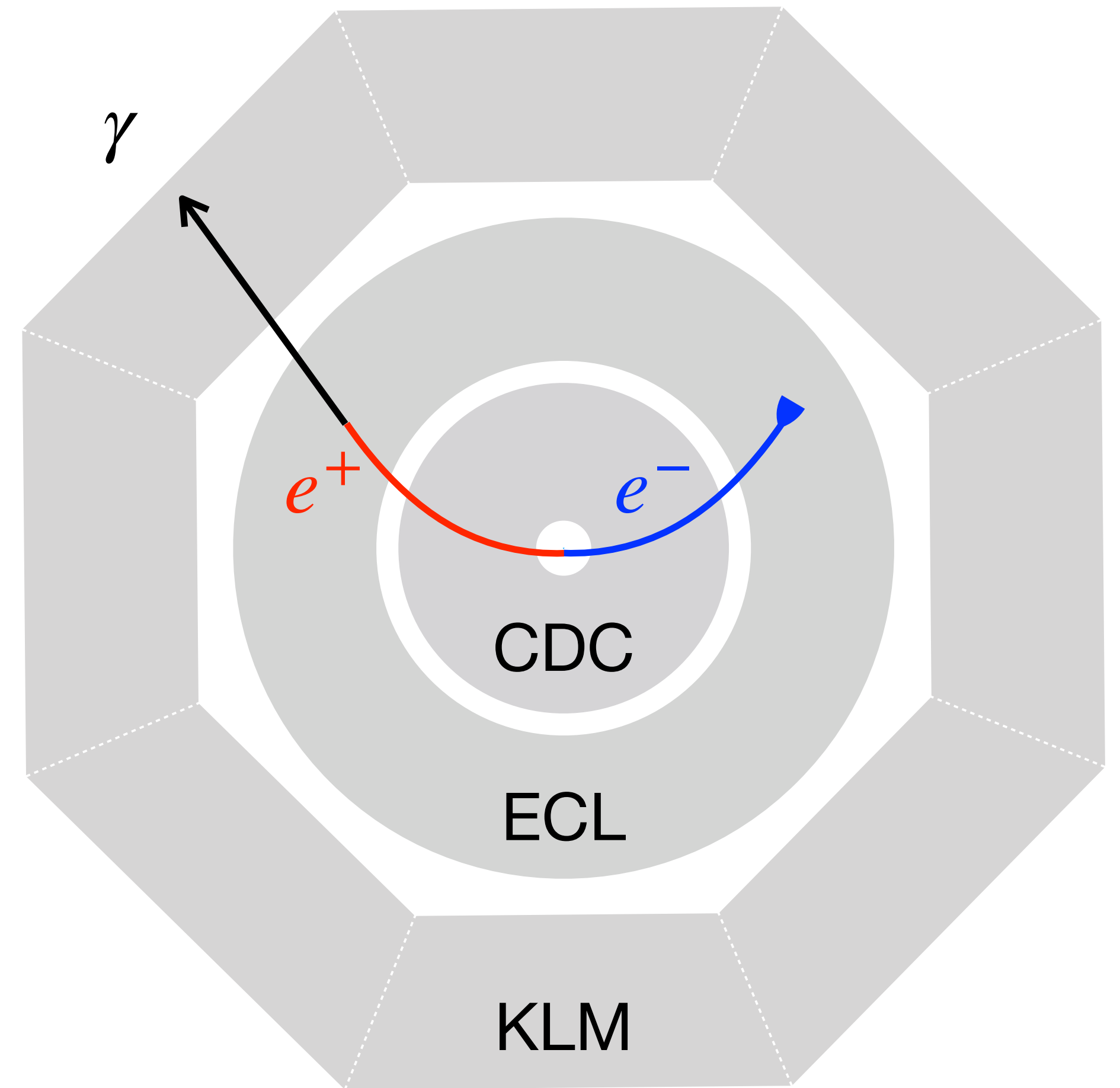
$$\int_{0.95}^1 dx_\gamma \frac{dN_\gamma}{dx_\gamma}(t = 16, x_\gamma) \simeq 4.7 \times 10^{-8}$$

$$\sim 2.8 \times 10^4 \gamma\text{-BG after ECL for } 6 \times 10^{11} e^+$$



KLM veto capability on photon

GeV γ is unlikely to penetrate the KLM

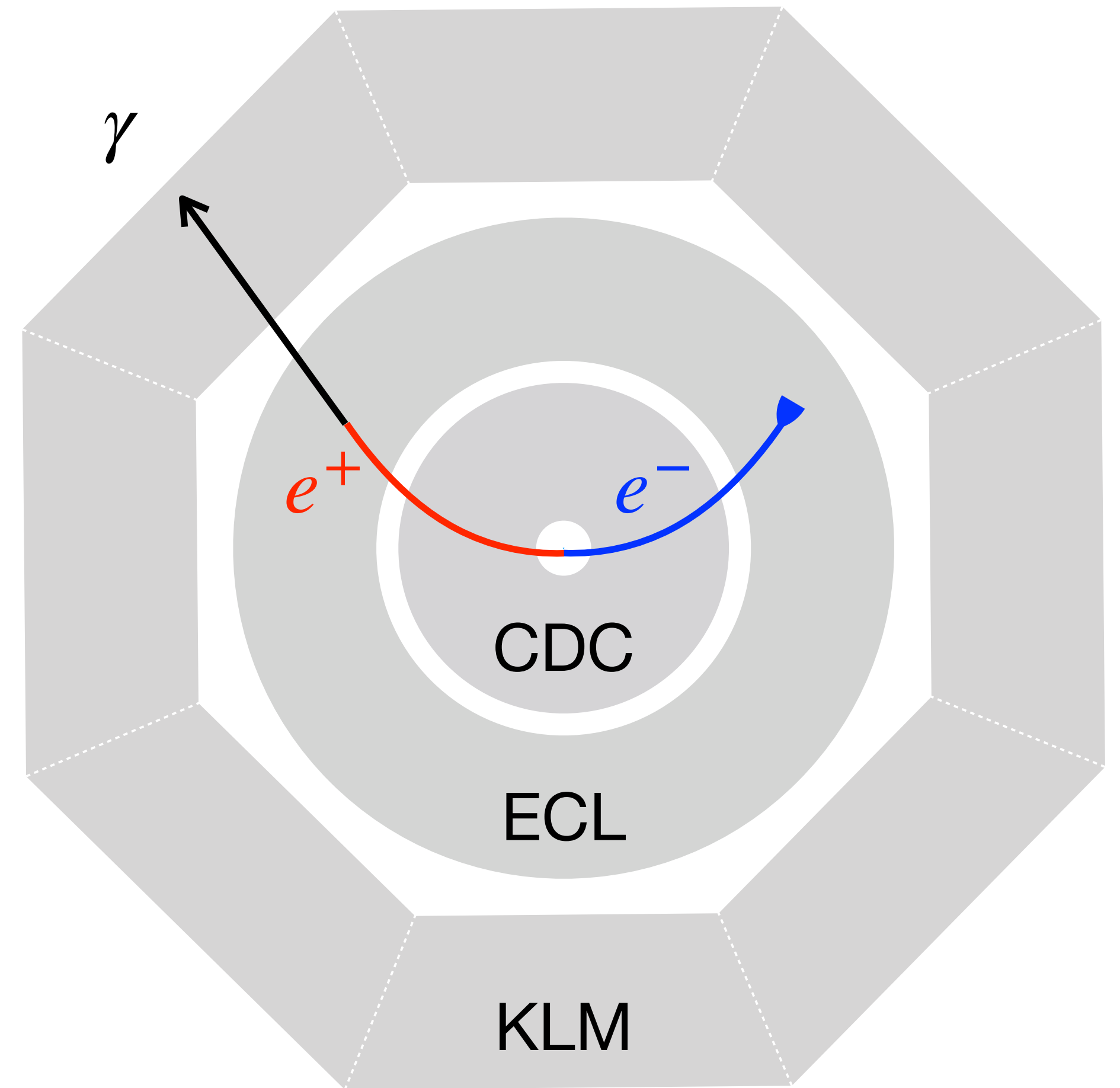


KLM veto capability on photon

GeV γ is unlikely to penetrate the KLM

However, γ can be absorbed by non-instrumented setups (e.g., magnet coil)

KLM veto power is limited



KLM veto capability on photon

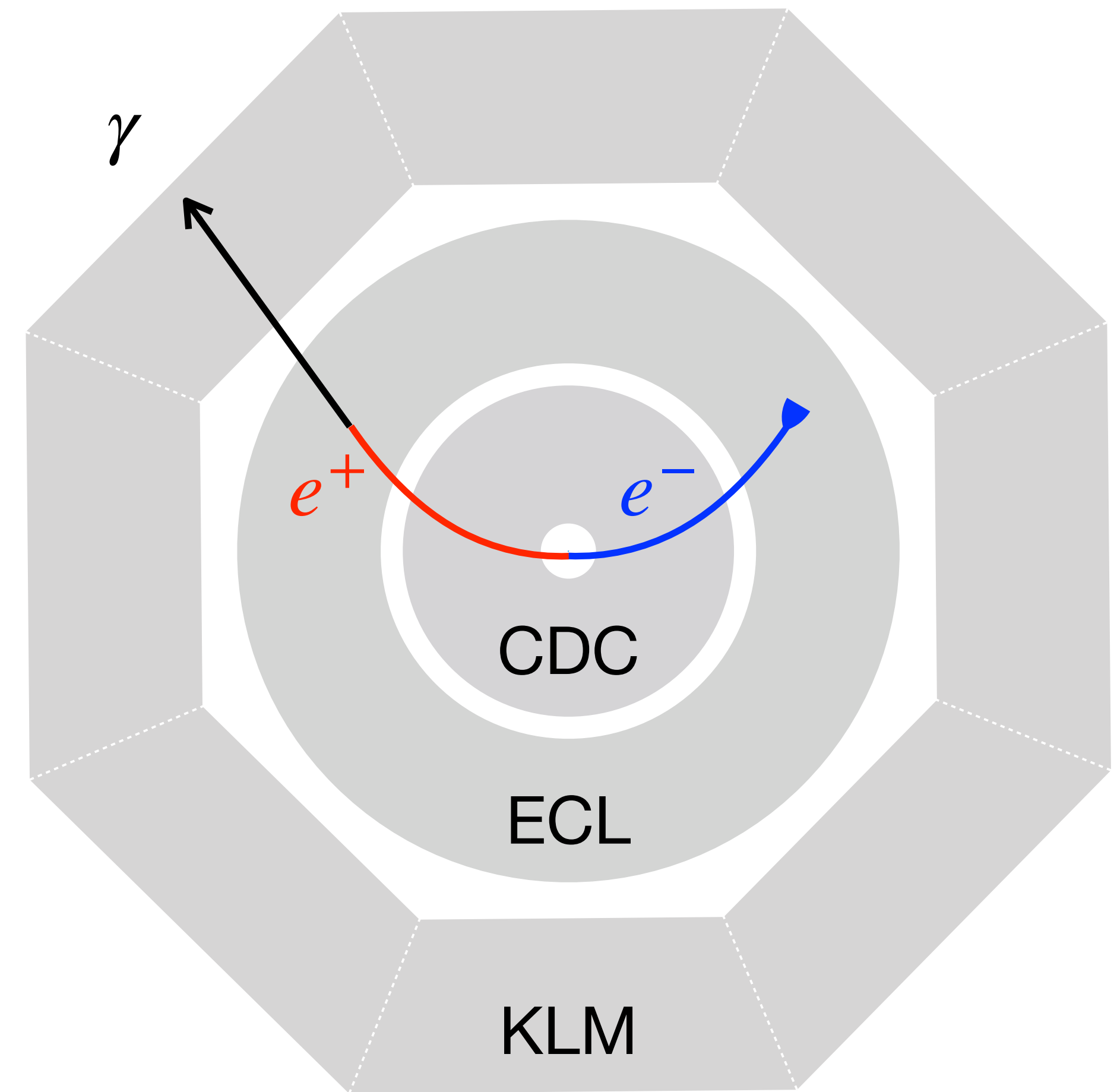
GeV γ is unlikely to penetrate the KLM

However, γ can be absorbed by non-instrumented setups (e.g., magnet coil)

KLM veto power is limited

IFR @ BaBar, veto eff = 4.5×10^{-4}

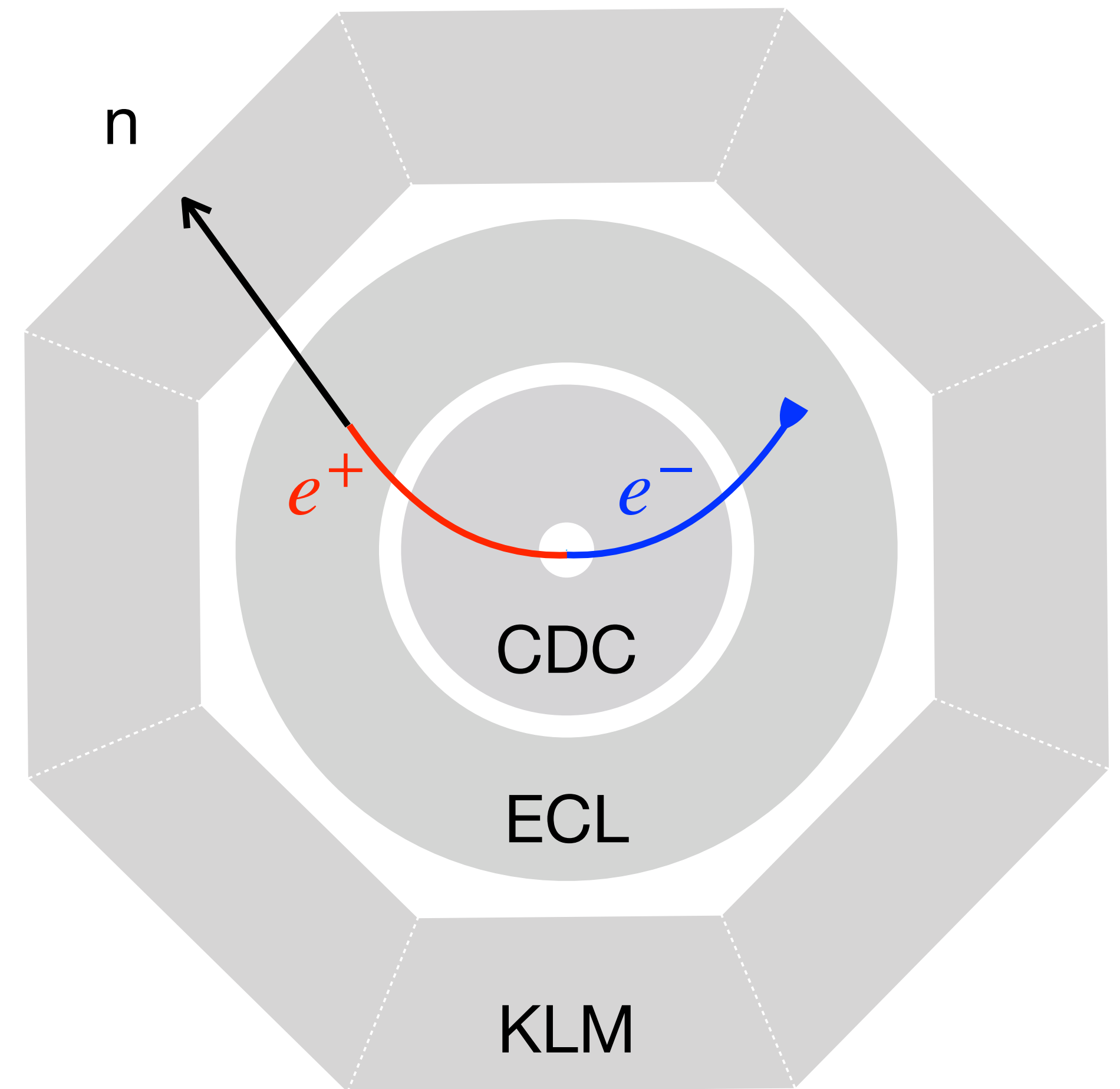
13 photon BG (conservative)



Neutron-induced backgrounds: GEANT4 simulations

GEANT4 simulation of $10^9 e^+$ with 4.35 GeV onto a CsI target with $1 X_0$

- Full simulation with $16 X_0$ is time-consuming
- Neutrons with significant energy are likely to be produced in the $1st X_0$ (confirmed in simulations with $2-X_0$)



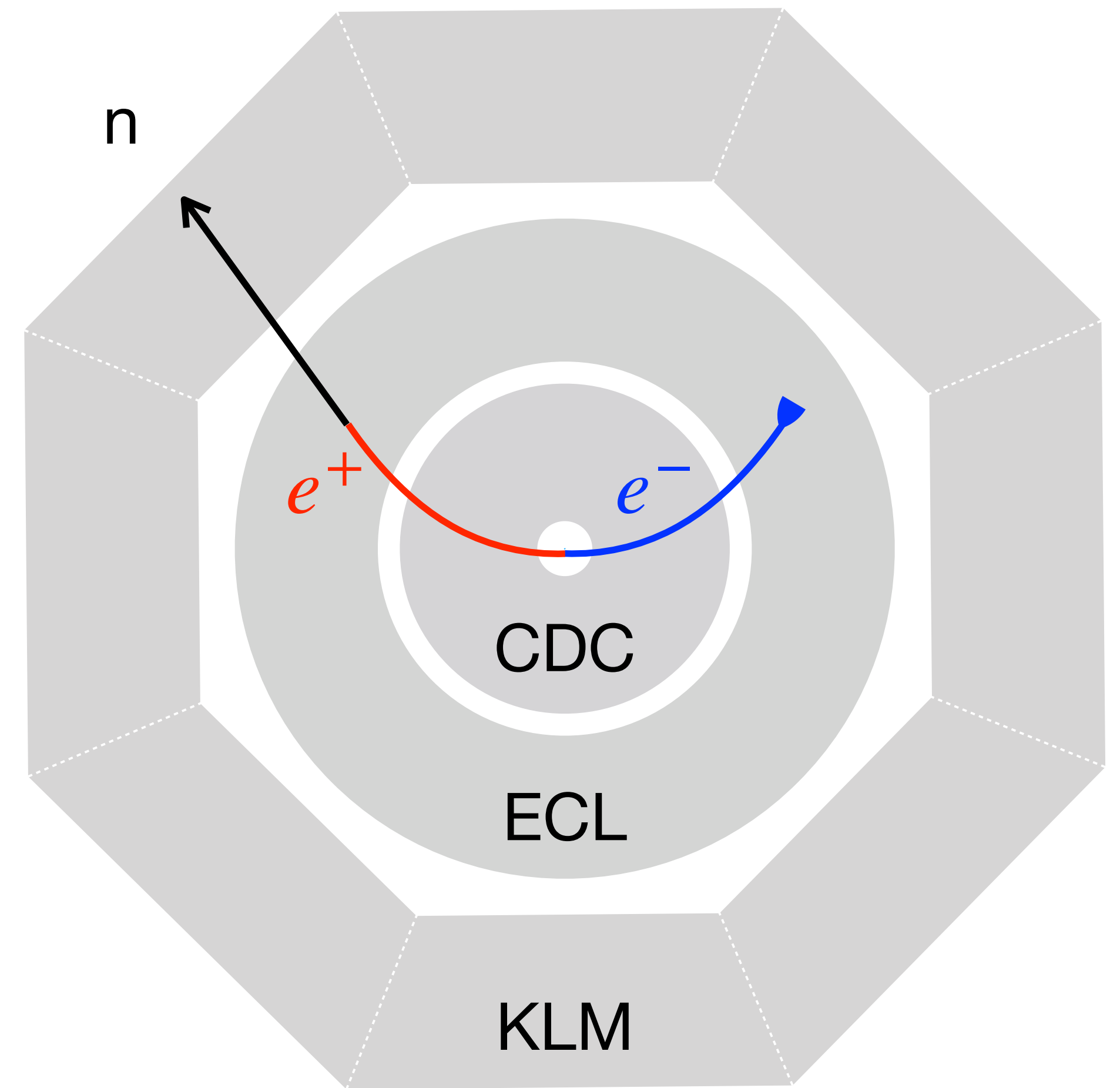
Selection in GEANT4 simulations

At least 1 neutron with energy > 3 GeV

Energy deposition in ECL $< 5\%$

Veto p/π^\pm with momentum > 0.6 GeV (either deposit energy in ECL or produce tracks in KLM)

Count # of neutrons with K.E. > 280 MeV
(hadronic shower threshold)



Probability for a neutron to penetrate ECL & KLM

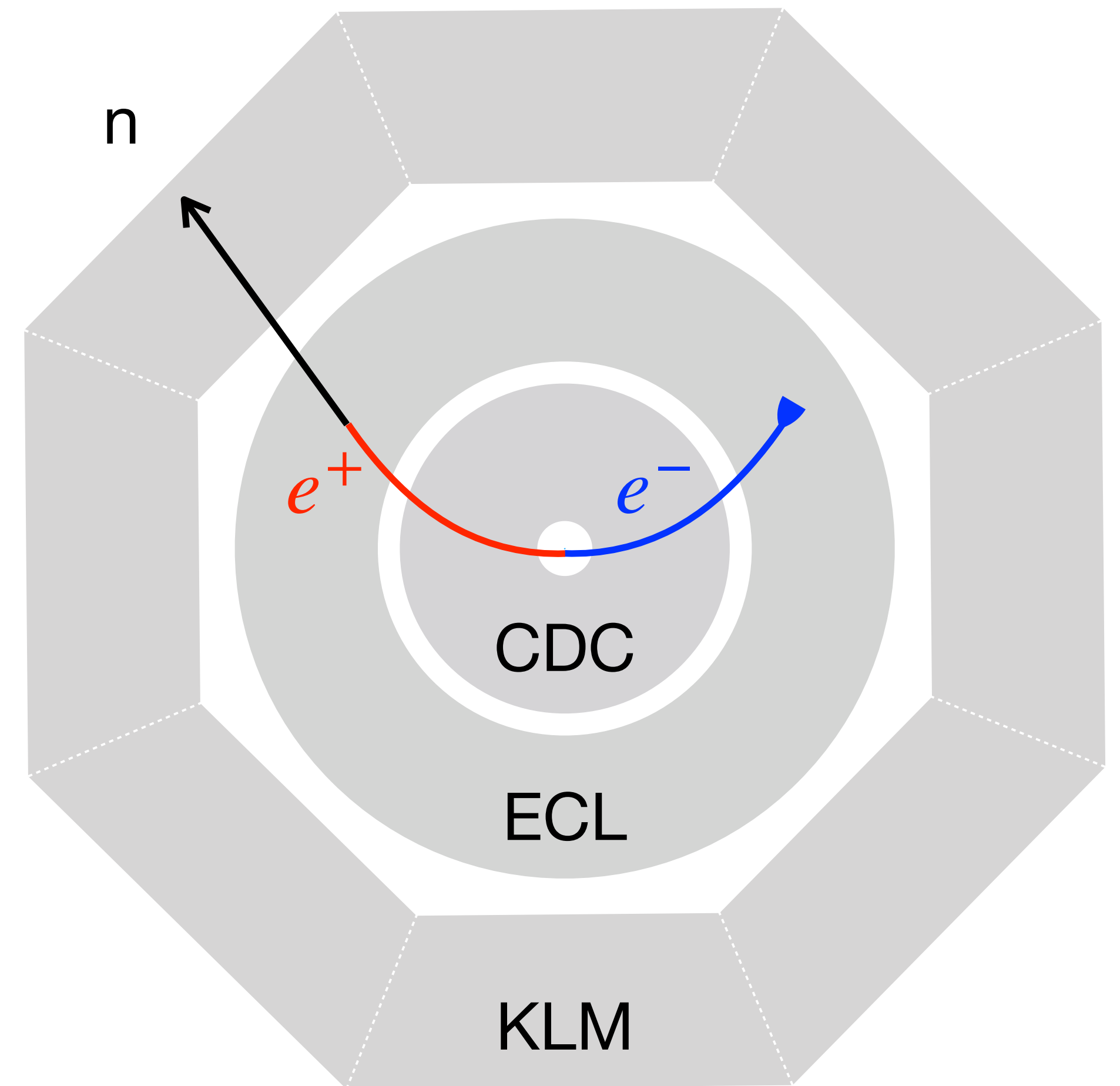
Prob to penetrate a target with length L

$$P = \exp(-L/\lambda_0)$$

λ_0 = hadronic interaction length

KLM has $\sim 3.9 \lambda_0$

ECL has $\sim 0.8 \lambda_0$



Probability for a neutron to penetrate ECL & KLM

Prob to penetrate a target with length L

$$P = \exp(-L/\lambda_0)$$

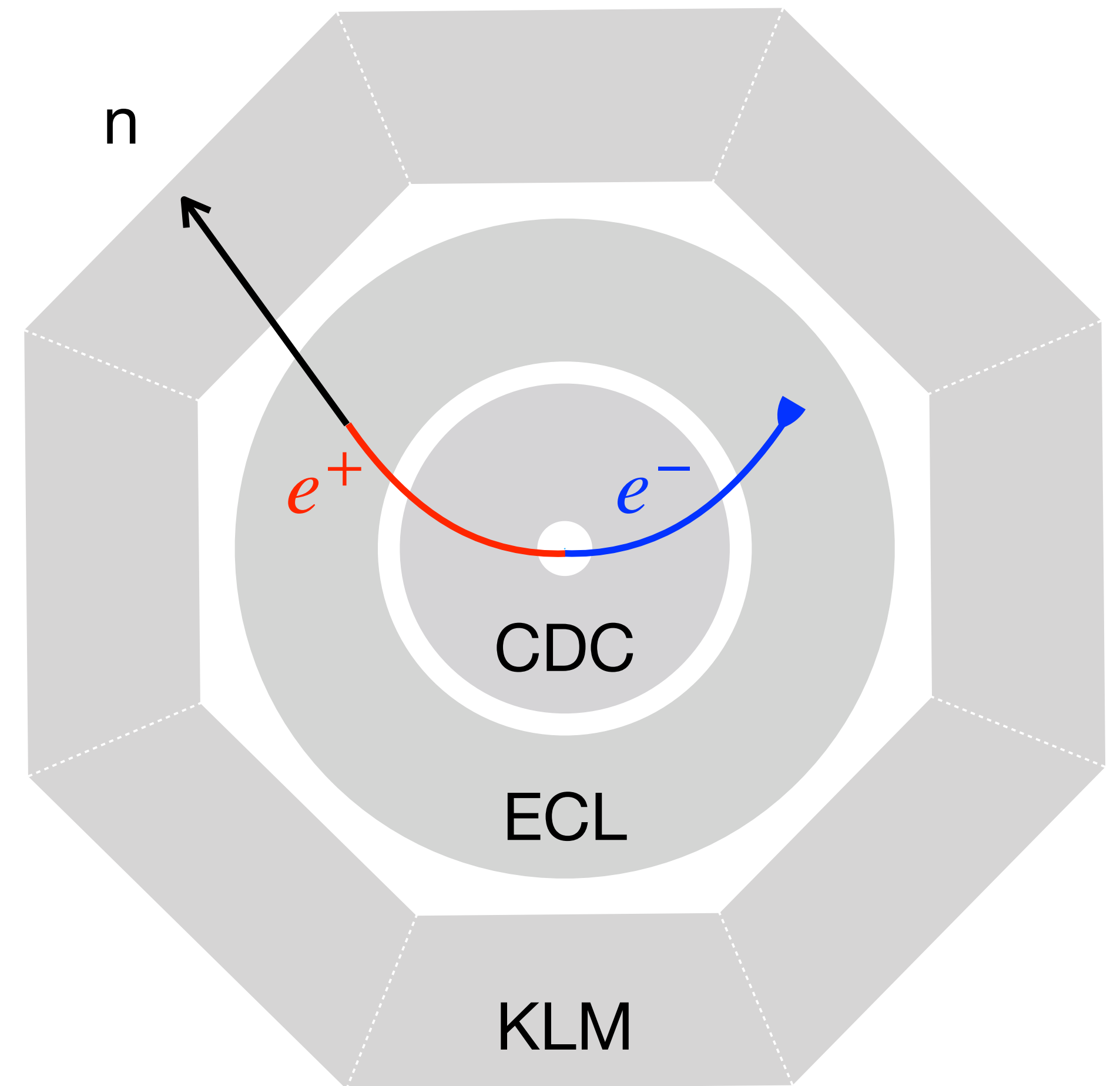
λ_0 = hadronic interaction length

KLM has $\sim 3.9 \lambda_0$

ECL has $\sim 0.8 \lambda_0$

Prob to penetrate ECL & KLM is about 1%

about 81 neutron background in total



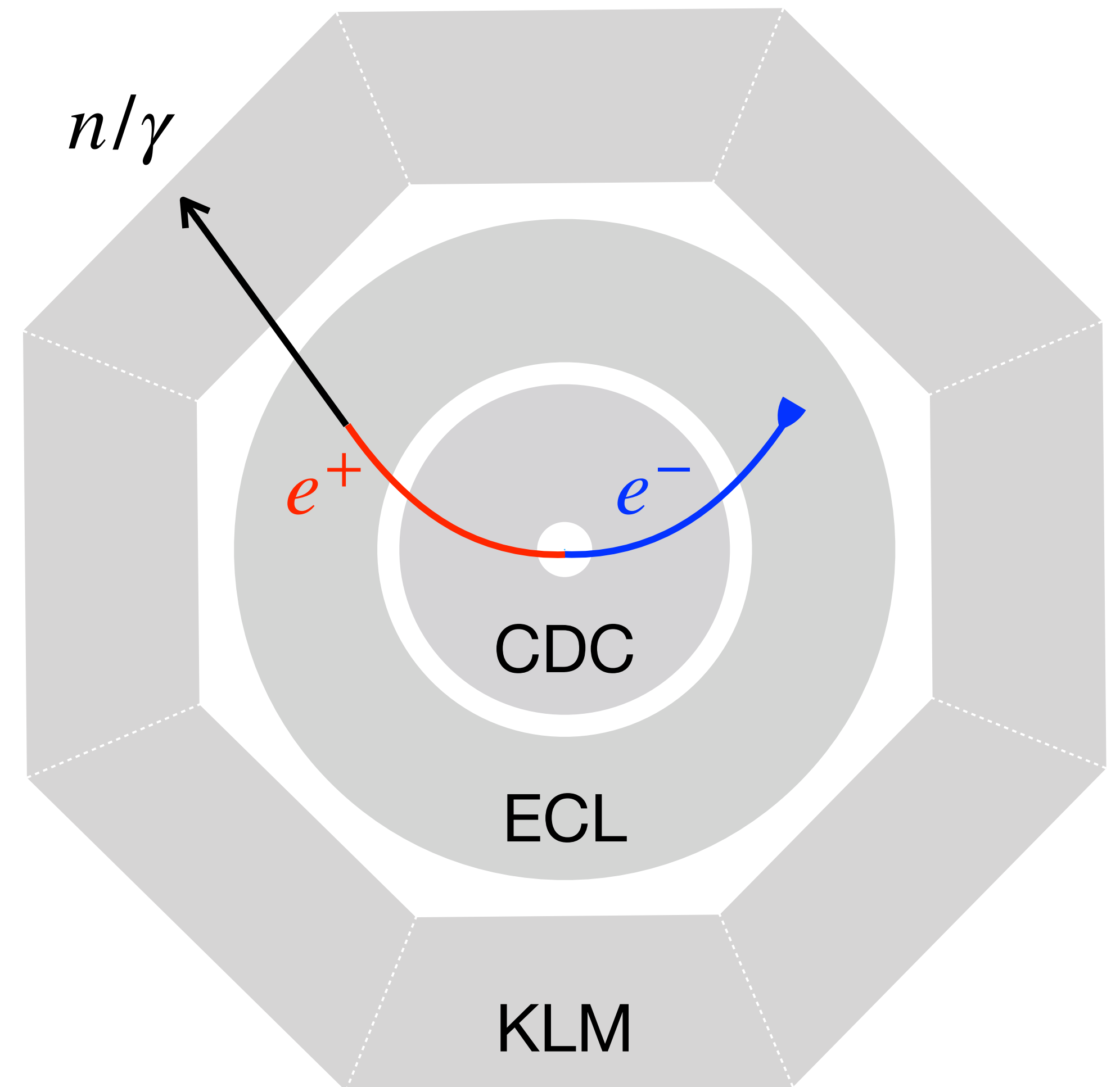
Summary on background estimation

BG: $e^+ + \text{ECL} \rightarrow \gamma/n$ which escape detection

Use KLM to veto such BG

- photon BG events: ~ 13
- neutron BG events: ~ 81

[Liang, ZL, Yang, 2212.04252]



3

Sensitivity on invisible dark photon

Invisible dark photon

[Holdom 1986]

$$\mathcal{L}_{\text{int}} = A'_\mu (e Q_f \epsilon \bar{f} \gamma^\mu f + g_\chi \bar{\chi} \gamma^\mu \chi)$$

[Foot & He 1991]

[Kors & Nath 2004]

dark photon A'_μ

[Feldman, ZL, Nath, [hep-ph/0702123](#), 373 cites]

suppressed coupling ϵ to SM fermion

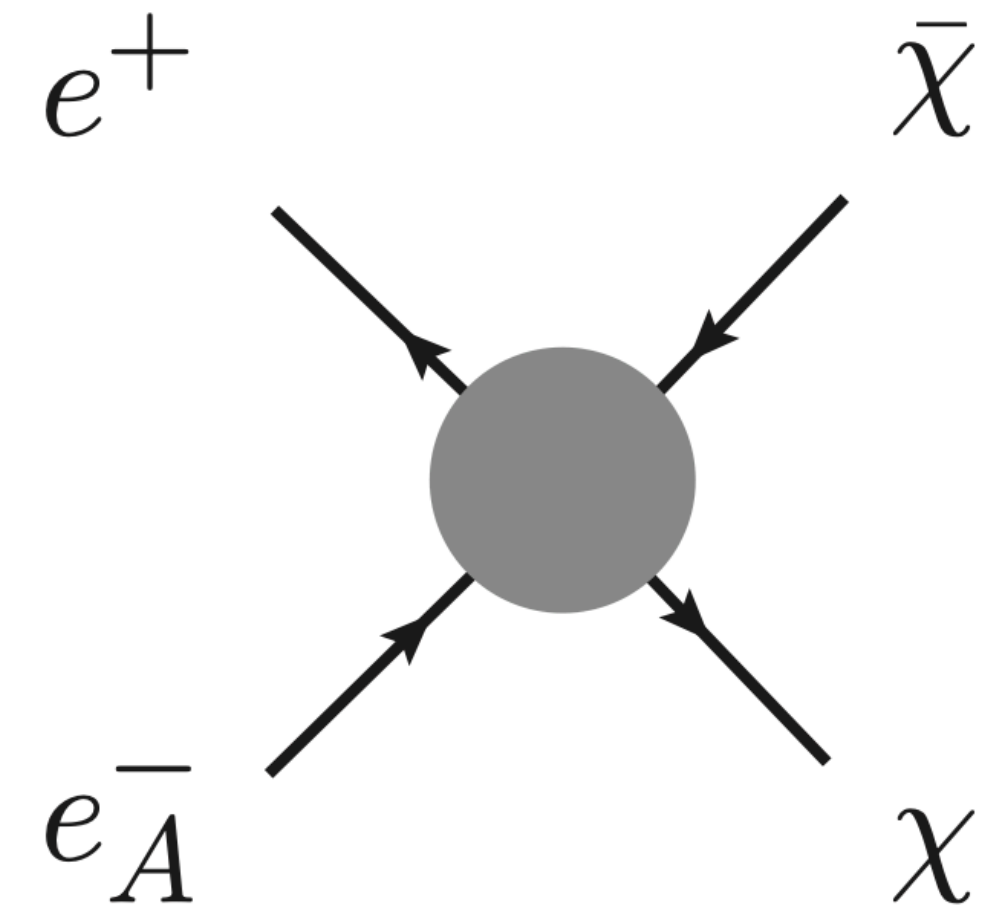
gauge coupling to hidden fermion χ : $g_\chi \gg e\epsilon$

$$m_{A'} = 3m_\chi$$

Annihilation with atomic electrons

annihilation process: $e^+ e_A^- \rightarrow A' \rightarrow \chi \bar{\chi}$

$$\sigma_{\text{ann}}(\sqrt{s}) = \frac{e^2 \epsilon^2 \alpha_D}{3} \frac{s + 2m_\chi^2}{(s - m_{A'}^2)^2 + \Gamma_{A'}^2 m_{A'}^2} \sqrt{1 - \frac{4m_\chi^2}{s}}$$
$$\alpha_D = g_\chi^2 / 4\pi \quad s = 2m_e E' + 2m_e^2 = 2m_e E_{A'}$$



Annihilation with atomic electrons (continued)

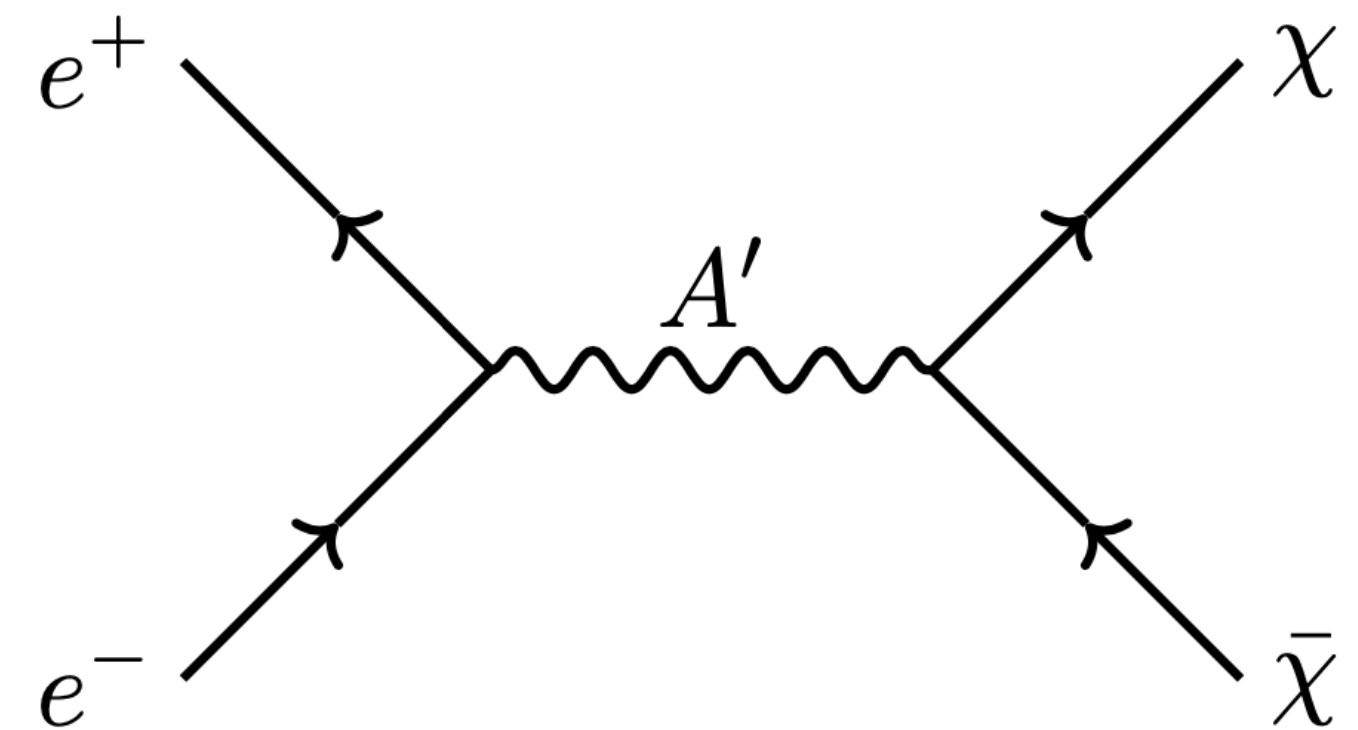
$$N_{\text{ann}} = \mathcal{L} \int_{E_{\text{min}}}^{E_{\text{max}}} dE \frac{d\sigma_B}{dE} \int_{0.95E}^{E+m_e} dE_{A'} n_e T_e(E' = E_{A'} - m_e, E, L_T) \sigma_{\text{ann}}(E_{A'})$$

$\frac{d\sigma_B}{dE}$ is the Bhabha xsec

n_e is the electron # density

$T_e(E', E, L_T)$ is the e^+ differential track length

[Tsai & Whitis 1966] [Bjorken et al, 1988]



Bremsstrahlung with target nucleus

dominated by on-shell A' production

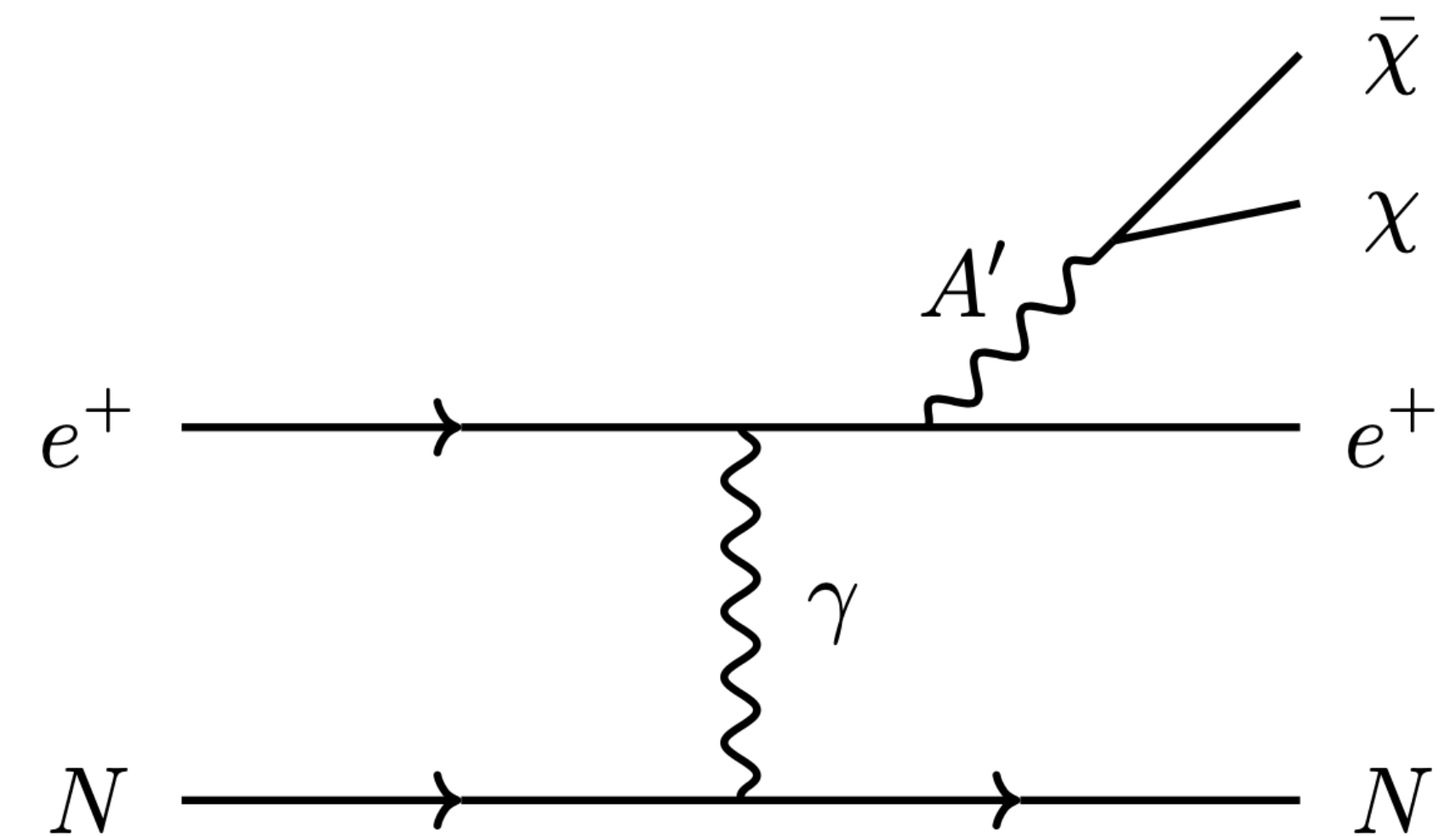
$$N_{\text{bre}} = \mathcal{L} \int_{E_{\text{min}}}^{E_{\text{max}}} dE \frac{d\sigma_B}{dE} \int_{0.95E}^{E-m_e} dE_{A'} n_N T_e(E', E, X_0) \frac{d\sigma_{\text{bre}}}{dE_{A'}}$$

$$\frac{d\sigma_{\text{bre}}}{dE_{A'}} = \text{xsec of on-shell produced } A'$$

[Bjorken et al, 0906.0580]

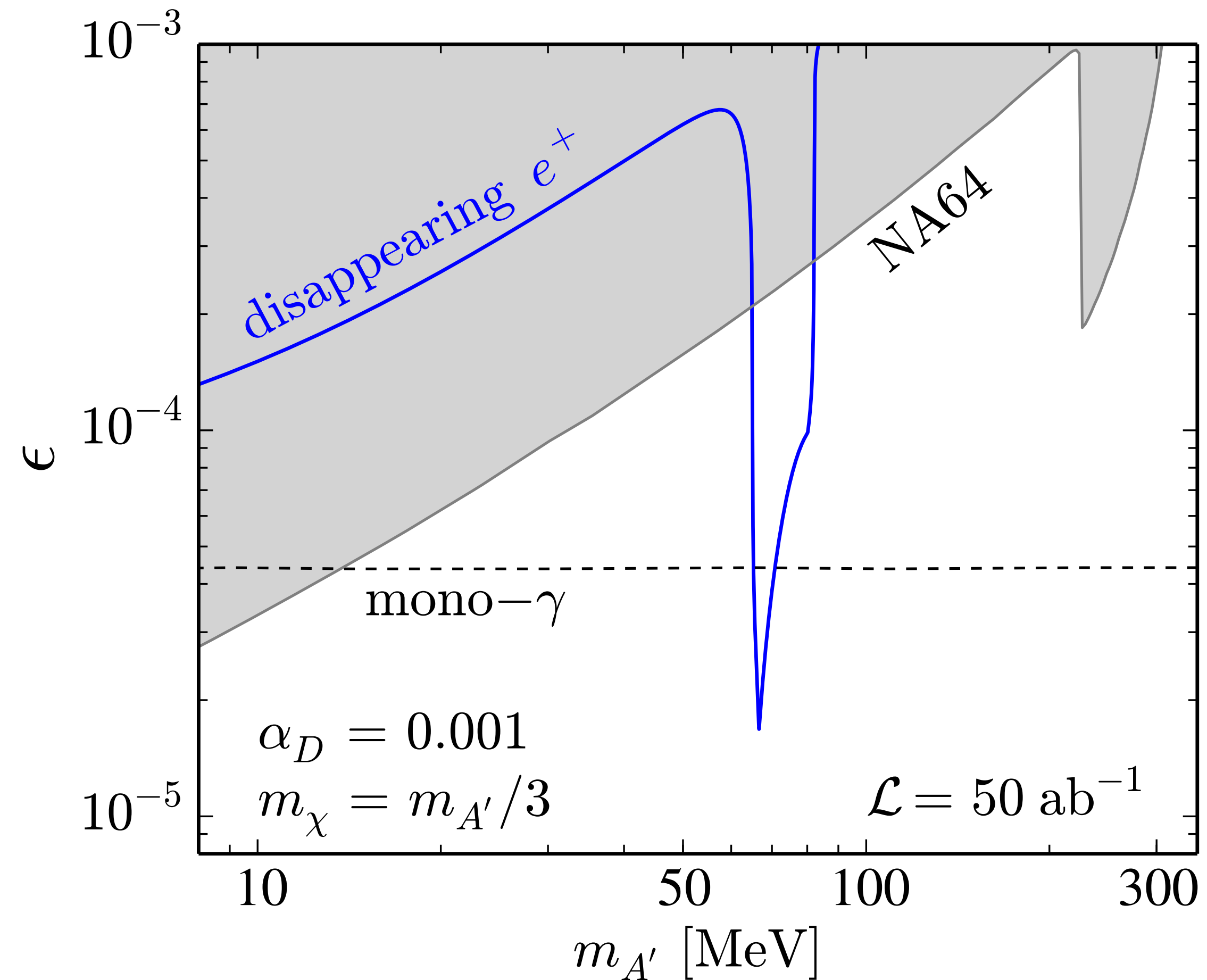
[Gninenko et al, 171205706]

[Liu & Miller, 1705.01633]



Belle II sensitivity on invisible dark photon

[Liang, ZL, Yang, 2212.04252]



Summary

We propose a new dark matter channel at colliders, where one SM particle interacts with the detector to produce DM particles

The main background at Belle II are due to photon and neutron events that escape detection

We find that this new DM channel at Belle II can probe new parameter space of invisible dark photon, surpassing both the mono-photon channel at Belle II and the missing momentum search at NA64

backup slides

Track length

For positrons with initial energy E to enter a target with thickness L_T , the differential track-length distribution as a function of the positron energy E' can be computed by [1, 2]

$$T_e(E', E, L_T) = X_0 \int_0^{L_T/X_0} I_e(E', E, t) dt, \quad (1)$$

where X_0 is the radiation length of the target. Here $I_e(E', E, t)$ is the energy distribution of E' at the depth tX_0 , which can be computed iteratively such that $I_e = \sum_i I_e^{(i)}$ where $I_e^{(i)}$ denotes the i -th generation positrons [3]. We adopt the analytical model of Ref. [3] up to second-generation positrons, which are found to be in good agreement with simulations in Ref. [1]. The contributions from the first two generations are [3]

$$I_e^{(1)}(E', E, t) = \frac{1}{E} \frac{(\ln(1/v))^{b_1 t - 1}}{\Gamma(b_1 t)}, \quad (2)$$

$$I_e^{(2)}(E', E, t) = \frac{2}{E} \int_v^1 \frac{dx}{x^2} \frac{1}{b_2 + b_1 \ln(1-x)} \left[\frac{(1-x)^{b_1 t} - (1-v/x)^{b_1 t}}{b_1 \ln[(x-x^2)/(x-v)]} + \frac{e^{-b_2 t} - (1-v/x)^{b_1 t}}{b_2 + b_1 \ln(1-v/x)} \right], \quad (3)$$

where $b_1 = 4/3$, $b_2 = 7/9$, $v = E'/E$.

[1] 1802.03794

[2] 1807.05884

[3] Tsai & Whitis 1966

xsec of on-shell dark photon

where n_N is the number density of I (or Cs). Here $d\sigma_{\text{bre}}/dE_{A'}$ is the differential cross section of the on-shell produced A' [71–73],

$$\frac{d\sigma_{\text{bre}}}{dE_{A'}} = (\phi_I + \phi_{\text{Cs}}) \frac{4\alpha^3 \epsilon^2}{E'} \frac{x(1-x+x^2/3)}{m_{A'}^2(1-x) + m_e^2 x^2}, \quad (13)$$

where $x \equiv E_{A'}/E'$, and ϕ_N denotes the effective flux of photons from nucleus N [71]:

$$\phi_N = \int_{t_{\min}}^{t_{\max}} dt \frac{t - t_{\min}}{t^2} \left[\frac{Za^2 t}{(1 + a^2 t)(1 + t/d)} \right]^2, \quad (14)$$

with $t_{\min} = (m_{A'}^2/2E')^2$, $t_{\max} = m_{A'}^2 + m_e^2$, $a = 111m_e^{-1}Z^{-1/3}$, and $d = 0.164A^{-2/3} \text{ GeV}^2$. We use $Z = 53$ (55) and $A = 127$ (133) for I (Cs). Here we only consider the dominant elastic form factor.

[71] Bjorken et al, 0906.0580

[72] Gninenko et al, 171205706

[73] Liu & Miller, 1705.01633

Hypercharge portal models \implies dark photon

$$SU(3)_c \times SU(2)_L \times U(1)_Y$$

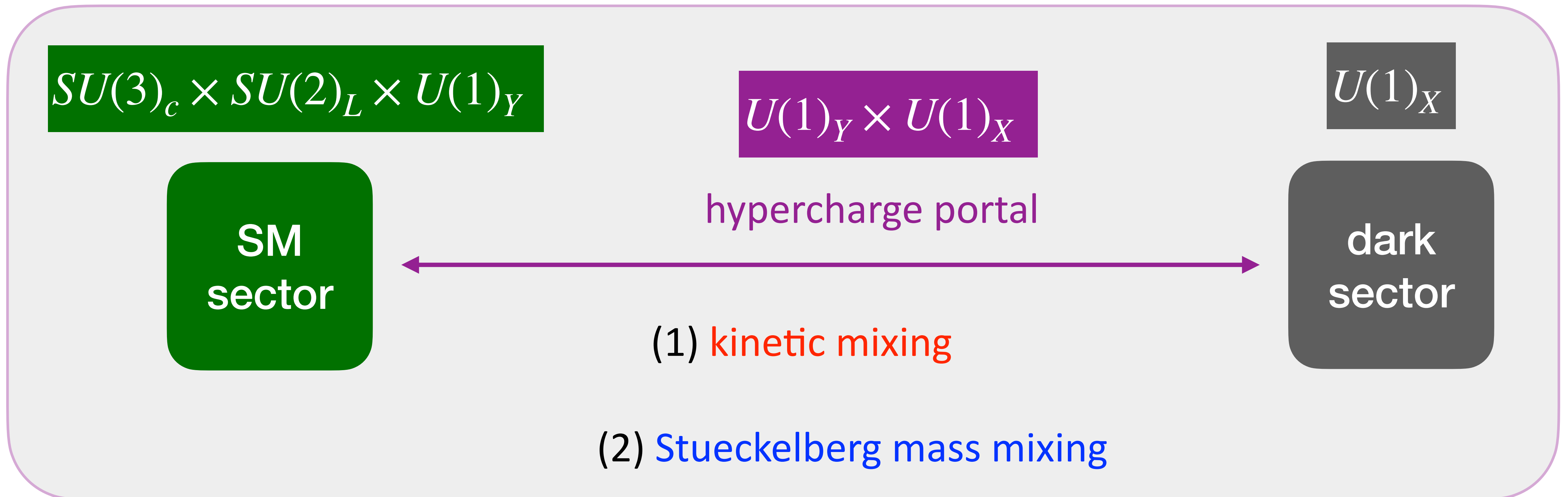
SM
sector

$$U(1)_X$$

dark
sector

[Holdom 1986] [Foot & He 1991] [Kors & Nath 2004] [Feldman, ZL, Nath, [hep-ph/0702123](https://arxiv.org/abs/hep-ph/0702123), 373 cites]

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Kinetic mixing & mass mixing

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$$\mathcal{L} = -\frac{1}{4}B_{\mu\nu}B^{\mu\nu} -\frac{1}{4}X_{\mu\nu}X^{\mu\nu} + g_D X_\mu \bar{\chi} \gamma^\mu \chi - \frac{\tilde{\delta}}{2} B_{\mu\nu} X^{\mu\nu} - \frac{M_1^2}{2} (\partial_\mu \sigma + X_\mu + \tilde{\epsilon} B_\mu)^2$$

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kinetic mixing $\tilde{\delta}$ & mass mixing $\tilde{\epsilon}$ are **degenerate** (w/o χ): only $\epsilon \sim (\tilde{\epsilon} - \tilde{\delta})$ is physical

dark photon & millicharged particles

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[see also Fabbrichesi+, 2005.01515, Dark Photon Review]

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- $X_\mu \implies A'_\mu$ (dark photon), if $M_1 \ll M_Z$

$$\epsilon e Q_f A'_\mu \bar{f} \gamma^\mu f \text{ (SM sector) and } g_D A'_\mu \bar{\chi} \gamma^\mu \chi \text{ (dark sector)}$$

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If A'_μ or Z'_μ is massive, χ is millicharged ($\epsilon e A'_\mu \bar{\chi} \gamma^\mu \chi$) only when $\tilde{\epsilon} \neq 0$

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