Exploring New Physics and Nuclear Structure through Coherent Elastic Neutrino-Nucleus Measurements



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Neutrino properties & neutrino as a probe

Neutrino interactions over a range of energies



Neutrino floor as ultimate background

Natural Neutrino Sources are the ultimate background in the Dark Matter Direct Detection experiment



However, it will become a future neutrino detector, very soon!

Part A: Some History

Discovery of NC Interactions in 1973

- Alternating neutral currents:
- Two neutrino experiments were running:
 (A) Gargamelle at the CERN Proton Synchrotron
 (B) HPWF (Harvard, Pennsylvania, Wisconsin, Fermilab) counter at Fermi
- > To measure the NC & CC Interactions with muon neutrinos:

Table 1		
	v-exposure	\bar{v} -exposure
No. of neutral-current candidates	102	64
No. of charged-current candidates	428	148

- The result from Fermi lab was published in 1974.
- W&Z at CERN were discovered in 1983.



Fig. 1. The Gargamelle heavy-liquid bubble chamber, installed into the magnet coils, at CERN in 1970.

First Prediction in 1974



PHYSICAL REVIEW D

VOLUME 9, NUMBER 5

1 MARCH 1974

Coherent effects of a weak neutral current

Daniel Z. Freedman[†] National Accelerator Laboratory, Batavia, Illinois 60510 and Institute for Theoretical Physics, State University of New York, Stony Brook, New York 11790

Our suggestion may be an act of hubris, because the inevitable constraints of interaction rate, resolution, and background pose grave experimental difficulties for elastic neutrino-nucleus scattering. We will discuss these problems at the end of this note, but first we wish to present the theoretical ideas relevant to the experiments.



In analogy to the coherent behavior of electron-nucleus scattering

First idea on the detection?

First idea on how to detect the neutrino coherent scattering process:

Superconducting-grain detector for (10-1000 eV) recoiled energies

PHYSICAL REVIEW D

VOLUME 30, NUMBER 11

1 DECEMBER 1984

Principles and applications of a neutral-current detector for neutrino physics and astronomy

A. Drukier and L. Stodolsky

Max-Planck-Institut für Physik und Astrophysik, Werner-Heisenberg-Institut für Physik, Munich, Federal Republic of Germany (Received 21 November 1983)

We study detection of MeV-range neutrinos through elastic scattering on nuclei and identification of the recoil energy. The very large value of the neutral-current cross section due to coherence indicates a detector would be relatively light and suggests the possibility of a true "neutrino observatory." The recoil energy which must be detected is very small $(10-10^3 \text{ eV})$, however. We examine a realization in terms of the superconducting-grain idea, which appears, in principle, to be feasible through extension and extrapolation of currently known techniques. Such a detector could permit determination of the neutrino energy spectrum and should be insensitive to neutrino oscillations since it detects all neutrino types. Various applications and tests are discussed, including spallation sources, reactors, supernovas, and solar and terrestrial neutrinos. A preliminary estimate of the most difficult backgrounds is attempted.

Direct detection of dark matter

PHYSICAL REVIEW D

VOLUME 31, NUMBER 12

15 JUNE 1985

Detectability of certain dark-matter candidates

Mark W. Goodman and Edward Witten Joseph Henry Laboratories, Princeton University, Princeton, New Jersey 08544 (Received 7 January 1985)

We consider the possibility that the neutral-current neutrino detector recently proposed by Drukier and Stodolsky could be used to detect some possible candidates for the dark matter in galac-

tic halos. This may be feasible if the galactic halos are made of particles with coherent weak interactions and masses $1-10^6$ GeV; particles with spin-dependent interactions of typical weak strength and masses $1-10^2$ GeV; or strongly interacting particles of masses $1-10^{13}$ GeV.

PHYSICAL REVIEW D

THIRD SERIES, VOLUME 33, NUMBER 8

15 APRIL 1986

Possibility of detecting heavy neutral fermions in the Galaxy

Ira Wasserman

Center for Radiophysics and Space Research, Cornell University, Ithaca, New York 14853 (Received 22 May 1985; revised manuscript received 31 October 1985)

It is shown that heavy neutral fermions in the galactic halo could produce numerous detectable low-energy events in a "thermal" neutrino detector if the heavy-fermion—nucleon vector coupling is comparable in strength to the vector weak interaction. The conditions under which a detectable event rate could arise for fermions with purely axial-vector couplings are also discussed. In a silicon detector heavy-fermion events would be concentrated at low energies, and could be distinguished

First direct detection in 2017

Observation of coherent elastic neutrino-nucleus scattering

D. Akimov^{1,2}, J. B. Albert³, P. An⁴, C. Awe^{4,5}, P. S. Barbeau^{4,5}, B. Becker⁶, V. Belov^{1,2}, A. Brown^{4,7}, A. Bolozdy...
 See all authors and affiliations

Science 03 Aug 2017: eaao0990 DOI: 10.1126/science.aao0990

Science

2017 BREAKTHROUGH OF THE YEAR

Cosmic convergence

RUNNERS-UP

Life at the atomic level A tiny detector for the shiest particles Deeper roots for *Homo sapiens* Pinpoint gene editing Biology preprints take off A cancer drug's broad swipe A new great ape species Earth's atmosphere 2.7 million years ago Gene therapy triumph

A tiny detector for the shiest particles





Peer Reviewed ← see details

Part B: Brief Introduction

Coherent Elastic Neutrino-Nucleus Scattering

- **CE** ν **NS**: pronounced "sevens"
- Weak Neutral-Current (NC) interaction:

 $\nu_{\alpha} + \mathcal{N}(A, Z) \rightarrow \nu_{\alpha} + \mathcal{N}(A, Z)$



The nucleus $\mathcal{N}(A, Z)$ recoils as a whole!

So what?



The CEvNS kinematics

$|\vec{q}| R \lesssim 1$

- Heavy target nucleus $\mathcal{N}(A, Z)$: $A \sim 100$ $M \sim 100$ GeV $R \approx 1.2 A^{1/3} \, \text{fm} \approx 5 \, \text{fm}$ \blacktriangleright CE ν NS for $|\vec{q}| \lesssim 40$ MeV
 - Non-Relativistic nuclear recoil:
 - $|\vec{q}| \simeq \sqrt{2 M T}$



Outgoing neutrino





Observable nuclear recoil kinetic energy:

$$T \simeq rac{|ec{q}|^2}{2M} \lesssim 10 \, \mathrm{keV} \; \leftarrow \; \mathrm{Very \; Small!}$$

The CEvNS Cross Section

Standard Model:
$$\frac{d\sigma_{CE\nu NS}}{dT}(E_{\nu}, T) = \frac{G_{F}^{2}M}{4\pi} \left(1 - \frac{MT}{2E_{\nu}^{2}}\right) \left[Q_{W}(Q^{2})\right]^{2}$$
Weak charge of the nucleus \mathcal{N} :

$$|\vec{q}| = \sqrt{2MT}$$

$$Q_{W}(Q^{2}) = g_{V}^{n} N F_{N}(|\vec{q}|) + g_{V}^{p} Z F_{Z}(|\vec{q}|)$$

$$g_{V}^{n} = -\frac{1}{2} \qquad g_{V}^{p} = \frac{1}{2} - 2\sin^{2}\vartheta_{W}(Q^{2} \simeq 0) = 0.0227 \pm 0.0002$$
The neutron contribution is dominant! $\implies \frac{d\sigma_{CE\nu NS}}{dT} \propto N^{2}$
[Freedman, PRD 9 (1974) 1389; Drukier, Stodolsky, PRD 30 (1984) 2295; Barranco, Miranda, Rashba, hep-ph/0508299]
The coherent nuclear recoil gives a big cross section enhancement for heavy nuclei: $\sigma_{NC}^{incoherent} \propto N \implies \sigma_{CE\nu NS}/\sigma_{NC}^{incoherent} \propto N$
The nuclear form factors $F_{N}(|\vec{q}|)$ and $F_{Z}(|\vec{q}|)$ describe the loss of coherence for $|\vec{q}|R \gtrsim 1$. [Patton et al, arXiv:1207.0693; Bednyakov, Naumov, arXiv:1806.08768; Papoulias

et al, arXiv:1903.03722; Ciuffoli et al, arXiv:1801.02166; Canas et al, arXiv:1911.09831; Van Dessel et al, arXiv:2007.03658]

The CEvNS Cross Section

Big cross section enhancement for heavy nuclei $\mathcal{N}(A, Z)$ with many nucleons N_i :





Partial Coherence

In the COHERENT experiment the scattering is not completely coherent





Neutron Form Factor



▶ Partial coherency is described by the nuclear neutron form factor $F_N(|\vec{q}|)$

Fourier transform of the neutron distribution in the nucleus $\rho_N(r)$: $F_N(|\vec{q}|) = \int e^{-i\vec{q}\cdot\vec{r}} \rho_N(r) d^3r$

• Measurable parameter: the radius R_n of the nuclear neutron distribution

Neutron Form Factor

Helm form factor: $F_N^{\text{Helm}}(|\vec{q}|^2) = 3 \frac{j_1(|\vec{q}|R_0)}{|\vec{q}|R_0} e^{-|\vec{q}|^2 s^2/2}$ Spherical Bessel function of order one: $j_1(x) = \frac{\sin(x)}{x^2} - \frac{\cos(x)}{x}$ Obtained from the convolution of a sphere with constant density with radius R_0 and a gaussian density with standard deviation s Rms radius: $R^2 = \langle r^2 \rangle = \frac{3}{5} R_0^2 + 3s^2$ Surface thickness: $s \simeq 0.9 \, \text{fm}$ 0.0012 2 s = 0.9 fm 0.0010 R = 4 fm0.8 R = 5 fmR = 6 fm0.0008 0.6 $F^2(q^2)$ 0.0006 PC 0.4 R_0 0.0004 0.2 0.0002 R = 5 fms = 0.9 fm0.0000 0.0 R 0 20 60 80 100 40 2 6 8 10 4 [MeV] a [fm]

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Part C: Observation and Implications

The COHERENT experiment

- > 14.6 kg CsI scintillating crystal and 24 kg LAr detector.
- > Prompt monochromatic v_{μ} from stopped pion decays:

 $\pi^+ \rightarrow \mu^+ + \nu_\mu$

> Delayed $\bar{\nu}_{\mu}$ and ν_{e} from the subsequent muon decays:

 $\mu^+ \to e^+ + \bar{\nu}_{\mu} + \nu_e$

> The COHERENT energy and time information allow us to distinguish the interactions of v_e , v_μ and \bar{v}_μ





First observation of CEvNS at Csl (2017)





Akimov et al. *Science* Vol 357, Issue 6356 15 September 2017

- Data are beam coincident and anti-coincident residuals during SNS operation, "On", and during SNS shutdown periods, "Off".
- Excess in light yield and timing distributions only for Beam on.

 $^{133}_{55}Cs_{78}$ and $^{127}_{53}I_{74} \leftarrow$ Heavy nuclei well suited for $CE\nu NS$

Neutron Distributions of Cs & I

• Fit of the 2017 COHERENT CsI data to get $R_n(^{133}Cs) \simeq R_n(^{127}I)$:



First determination of R_n with neutrino-nucleus scattering:

$$R_n(Csl) = 5.5^{+0.9}_{-1.1} \, \text{fm}$$

[Cadeddu, Giunti, Li, Zhang, arXiv:1710.02730]

With new 2020 COHERENT Csl data:

[Pershey @ Magnificent CEvNS 2020]

 $R_n(CsI) = 5.55 \pm 0.44 \,\mathrm{fm}$

[Cadeddu et al, arXiv:2102.06153]

Neutron Distributions of Cs & I

- Neutron form factor is the Fourier transform of the neutron distribution
- First measurement of neutron radius with neutrinos, pure weak NC measurement!
- > neutron skin → the nuclear Equation of State (EOS) → neutron star radius

 $R_n(CsI) = 5.55 \pm 0.44 \,\mathrm{fm}$

- The uncertainty is large, but it can be improved in future.
- ▶ Predictions of nuclear models: $R_n(CsI) \approx 4.9 5.1 \text{ fm}$
- ► A large *R_n* has important implications for:
 - Nuclear physics: a larger pressure of neutrons
 - Astrophysics: a larger size of neutron stars



BSM Neutrino Interactions in CEvNS



Neutrino Electromagnetic Interactions

k.i=1Effective electromagnetic vertex: $\nu_i(p_i)$ $\nu_f(p_f)$ $\langle \nu_f(p_f) | j^{(\nu)}_{\mu}(0) | \nu_i(p_i) \rangle = \overline{u_f}(p_f) \Lambda^{fi}_{\mu}(q) u_i(p_i)$ Λ $q = p_i - p_f$ $\gamma(q)$ Vertex function: $\Lambda_{\mu}(q) = \left(\gamma_{\mu} - q_{\mu} \phi/q^{2}\right) \left[F_{Q}(q^{2}) + F_{A}(q^{2})q^{2}\gamma_{5}\right] - i\sigma_{\mu\nu}q^{\nu} \left[F_{M}(q^{2}) + iF_{E}(q^{2})\gamma_{5}\right]$ Lorentz-invariant charge anapole magnetic electric form factors: $a^2 = 0 \implies$ helicity-conserving helicity-flipping

 $\mathcal{H}_{em}^{(\nu)}(x) = j_{\mu}^{(\nu)}(x)A^{\mu}(x) = \sum \overline{\nu_k}(x)\Lambda_{\mu}^{kj}\nu_j(x)A^{\mu}(x)$

Effective Hamiltonian:

Diagonal charge radii

Method	Experiment	Limit $[10^{-32} \text{ cm}^2]$	C.L.	Year
Poactor v o-	Krasnoyarsk	$ \langle r_{ u_e}^2 angle < 7.3$	90%	1992
Reactor $\nu_e e$	TEXONO	$-4.2 < \langle r^2_{ u_e} angle < 6.6^{a}$	90%	2009
Accelerator 11 0-	LAMPF	$-7.12 < \langle r^2_{ u_e} angle < 10.88^{a}$	90%	1992
Accelerator $\nu_e e$	LSND	$-5.94 < \langle r^2_{ u_e} angle < 8.28^{a}$	90%	2001
Accelerator y a	BNL-E734	$-5.7 < \langle r^2_{ u_\mu} angle < 1.1^{a,b}$	90%	1990
Accelerator ν_{μ} e	CHARM-II	$ \langle r^2_{ u_{\mu}} angle < 1.2^{a}$	90%	1994
CEvNS	COHERENT	$-7.1 < \langle r_{ u_e}^2 angle < 11.2$	00%	2022
[arXiv:2205.09484]	+ Dresden-II	$-8.1 < \langle r^2_{ u_\mu} angle < 4.3$	9070	2022

a Corrected by a factor of two due to a different convention.

b Corrected in Hirsch, Nardi, Restrepo, hep-ph/0210137.

[Previous CEvNS results: Papoulias et al, arXiv:1711.09773, arXiv:1907.11644, arXiv:2003.12050; Khan and Rodejohann, arXiv:1907.12444; Cadeddu et al, arXiv:1810.05606, arXiv:1908.06045, arXiv:2005.01645]

Magnetic dipole moment

Method	Experiment	Limit $[\mu_{B}]$	CL	Year
	Krasnoyarsk	$ \mu_{ u_e} < 2.4 imes 10^{-10}$	90%	1992
	Rovno	$ \mu_{ u_e} < 1.9 imes 10^{-10}$	95%	1993
Reactor ES $(ar{ u}_e e^-)$	MUNU	$ \mu_{ u_e} <$ 9 $ imes$ 10 $^{-11}$	90%	2005
	TEXONO	$ \mu_{ u_e} < 7.4 imes 10^{-11}$	90%	2006
	GEMMA	$ \mu_{ u_e} < 2.9 imes 10^{-11}$	90%	2012
Reactor CEvNS+ES	Dresden-II [Coloma et al, arXiv:2202.10829] [Atzori Corona et al, arXiv:2205.09484]	$ \mu_{ u_e} < 3.3 imes 10^{-10}$	90%	2022
	BNL-E734	$ \mu_{ u_{\mu}} < 8.5 imes 10^{-10}$	90%	1990
Accelerator ES $(u_{\mu} e^{-})$	LAMPF	$ \mu_{ u_{\mu}} <$ 7.4 $ imes$ 10 $^{-10}$	90%	1992
	LSND	$ \mu_{ u_{\mu}} < 6.8 imes 10^{-10}$	90%	2001
Accelerator CEvNS+ES	COHERENT [Coloma et al, arXiv:2202.10829] [Atzori Corona et al, arXiv:2205.09484]	$ \mu_{ u_\mu} < 2 imes 10^{-9}$	90%	2022

[See also: Liao et al, arXiv:2202.10622; Aristizabal Sierra et al, arXiv:2203.02414; Khan, arXiv:2203.08892]

[Previous CEvNS results: Papoulias et al, arXiv:1711.09773, arXiv:1905.03750, arXiv:1907.11644, arXiv:2003.12050; Khan and Rodejohann, arXiv:1907.12444; Cadeddu et al, arXiv:1908.06045, arXiv:2005.01645; CONUS, arXiv:2201.12257]

[Future prospects: Miranda et al, arXiv:1905.03750]

Light mediators

Model	Q'_u	Q_d'	Q'_e	Q'_{μ}	Q'_{τ}
universal	1	1	1	1	1
B-L	1/3	1/3	-1	-1	-1
$B - 3L_e$	1/3	1/3	$\left -3\right $	0	0
$B - 3L_{\mu}$	1/3	1/3	0	-3	0
$B - 2L_e - L_\mu$	1/3	1/3	$\left -2\right $	-1	0
$B - L_e - 2L_\mu$	1/3	1/3	$\left -1\right $	-2	0
$B_y + L_\mu + L_\tau$	1/3	1/3	0	1	1
$L_e - L_\mu$	0	0	1	-1	0
$L_e - L_{\tau}$	0	0	1	0	$^{-1}$
$L_{\mu} - L_{\tau}$	0	0	0	1	-1

	Ar		CsI		CsI+Ar	
model	$g_{Z'}(\text{low } M_{Z'})$	$\frac{g_{Z'}}{M_{Z'}}$ (high $M_{Z'}$)	$g_{Z'}(\text{low } M_{Z'})$	$\frac{g_{Z'}}{M_{Z'}} (\text{high } M_{Z'})$	$g_{Z'}(\text{low } M_{Z'})$	$\frac{g_{Z'}}{M_{Z'}} (\text{high } M_{Z'})$
universal	3.91×10^{-5}	0.82×10^{-3}	2.36×10^{-5}	0.53×10^{-3}	2.07×10^{-5}	0.48×10^{-3}
B-L	5.35×10^{-5}	1.67×10^{-3}	5.27×10^{-5}	1.00×10^{-3}	4.42×10^{-5}	0.99×10^{-3}
$B_y + L_\mu + L_\tau$	10.4×10^{-5}	3.58×10^{-3}	4.97×10^{-5}	1.14×10^{-3}	4.47×10^{-5}	1.04×10^{-3}
$B - 3L_e$	4.91×10^{-5}	1.55×10^{-3}	5.16×10^{-5}	0.96×10^{-3}	4.34×10^{-5}	0.95×10^{-3}
$B - 3L_{\mu}$	3.45×10^{-5}	1.09×10^{-3}	3.21×10^{-5}	0.64×10^{-3}	2.76×10^{-5}	0.63×10^{-3}
$B - 2L_e - L_\mu$	4.62×10^{-5}	1.48×10^{-3}	4.79×10^{-5}	0.89×10^{-3}	3.95×10^{-5}	0.88×10^{-3}
$B - L_e - 2L_\mu$	3.97×10^{-5}	1.28×10^{-3}	3.86×10^{-5}	0.75×10^{-3}	3.26×10^{-5}	0.74×10^{-3}
$L_e - L_\mu$	161×10^{-5}	54.2×10^{-3}	166×10^{-5}	36.1×10^{-3}	137×10^{-5}	34.9×10^{-3}
$L_e - L_\tau$	204×10^{-5}	71.1×10^{-3}	140×10^{-5}	29.9×10^{-3}	125×10^{-5}	26.6×10^{-3}
$L_{\mu} - L_{\tau}$	234×10^{-5}	80.9×10^{-3}	116×10^{-5}	26.6×10^{-3}	103×10^{-5}	24.2×10^{-3}
	$\tilde{g}_{\phi}(\text{low } M_{\phi})$	$rac{ ilde{g}_{\phi}}{M_{\phi}}(ext{high } M_{\phi})$	$ ilde{g}_{\phi}(ext{low } M_{\phi})$	$rac{ ilde{g}_{\phi}}{M_{\phi}}(ext{high } M_{\phi})$	$\tilde{g}_{\phi}(\mathrm{low}\;M_{\phi})$	$rac{ ilde{g}_{\phi}}{M_{\phi}}(ext{high } M_{\phi})$
scalar	2.30×10^{-5}	0.58×10^{-3}	1.80×10^{-5}	0.31×10^{-3}	1.68×10^{-5}	0.30×10^{-3}







CONUS

Analysis of RUN-1 (2018) & RUN-2 (2019/2020) data → best UL on CEvNS with Ge !



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CONNIE



Dresden-II: Suggestive evidence

PHYSICAL REVIEW LETTERS 129, 211802 (2022)

Measurement of Coherent Elastic Neutrino-Nucleus Scattering from Reactor Antineutrinos

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Part D: Concluding Remarks

Summary of CEvNS experimental searches

Summary of CEvNS Results



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Exp. Program worldwide

Proliferation of experimental efforts worldwide !



Implications: What can we do with CEvNS?



EXTRAS

Natural sources of low-energy neutrinos



Artificial sources of low-energy neutrinos



New observation with Csl (2020)

Expected CEvNS in Csl





Implemented many analysis improvements since first observation – see talk by A. Konovalov

- Developed blind analysis to avoid biasing
- Perform 2D likelihood fit in PE and t_{rec}
- Beam-unrelated steady-state background measured in-situ with beam out-of-time data

Beam-related neutron backgrounds small

Expected events

Pershey@@Mag7s(2020)

Steady-state background	1286
Beam-related neutrons	18
Neutrino-induced neutrons	6
CEvNS	333

New observation with Csl (2020)

- Continued data collection up to June 2019 → increased statistics by a factor > 2
- Refinements in the SSB characterization and beam power determination
- Big work on re-measuring and understanding the QF

 \rightarrow Unc. reduced to 3.6% in the new analysis !

Updated measurement of CEvNS on Csl with new unc. budget !



No-CEvNS rejection	11.6 σ
SM CEvNS prediction	$333 \pm 11(\text{th}) \pm 42(\text{ex})$
Fit CEvNS events	306 ± 20
Fit χ^2/dof	82.4/98
CEvNS cross section	$169^{+30}_{-26}\times10^{-40}~{\rm cm^2}$
SM cross section	$189\pm6\times10^{-40}~{\rm cm^2}$



+ various searches of BSM physics...

See D. Pershey's talk

From M. Vivier summary talk @Mag7s(2020)

Single-Phase Liquid Argon

Single-Phase Liquid Argon

- ~24 kg active mass 2 x Hamamatsu 5912-02-MOD 8" PMTs
 - 8" borosilicate glass window
 - 14 dynodes
- QE: 18%@ 400 nm Wavelength shifter: TPB-coated Teflon walls and PMTs
- Cryomech cryocooler 90 Wt
 - PT90 single-state pulse-tube cold head





Detector from FNAL, previously built (J. Yoo et al.) for CENNS@BNB (S. Brice, Phys.Rev. D89 (2014) no.7, 072004)

COHERENT 2020: Argon (Ar)



Electromagnetic Vertex Function



- Hermitian form factors: $F_Q = F_Q^{\dagger}$, $F_A = F_A^{\dagger}$, $F_M = F_M^{\dagger}$, $F_E = F_E^{\dagger}$
- ► Majorana neutrinos: $F_Q = -F_Q^T$, $F_A = F_A^T$, $F_M = -F_M^T$, $F_E = -F_E^T$ no diagonal charges and electric and magnetic moments in the mass basis
- For left-handed ultrarelativistic neutrinos γ₅→ − 1 ⇒ The phenomenology of the charge and anapole are similar and the phenomenology of the magnetic and electric moments are similar.
- For ultrarelativistic neutrinos the charge and anapole terms conserve helicity, whereas the magnetic and electric terms invert helicity.