

*FeynArts*绘制费曼图
以及*FeynCalc*计算振幅、截面

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一、 *FeynArts*、*FeynCalc*
二、 计算过程

目
录

$$e^- \gamma \rightarrow e^- \gamma$$

$$e^+ e^- \rightarrow \mu^+ \mu^-$$

$$e^+ e^- \rightarrow e^+ e^-$$

$$e^+ e^- \rightarrow c\bar{u}$$

FeynArts is a Mathematica package for the generation and visualization of Feynman diagrams and amplitudes.

FeynArts-3.11

FeynCalc is a Mathematica package for algebraic calculations in QFT and semi-automatic evaluation of Feynman diagrams.

FeynCalc-9.3.1

Quit[];

[退出内核]

SetDirectory[NotebookDirectory[]];

[设置目录 [当前笔记本的目录]

\$LoadFeynArts = True;

[真]

<< FeynCalc`;

F[1]

中微子

F[2]

轻子

F[3]

u c t

F[4]

d s b

V[1]

γ

V[2]

Z

V[3]

W^-

S[1]

H

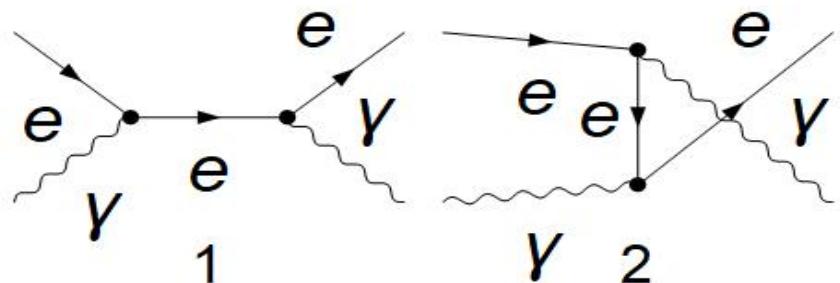
S[2]

G^0

S[3]

G^-

```
top = InsertFields[CreateTopologies[0, 2 → 2], {F[2, {1}], V[1]} → {F[2, {1}], V[1]},  
InsertionLevel → {Classes}, Model → "SM", Restrictions → QEDOnly];  
Paint[top, ColumnsXRows → {2, 1}, Numbering → Simple, SheetHeader → None,  
ImageSize → {400, 400}];  
[图像尺寸]
```

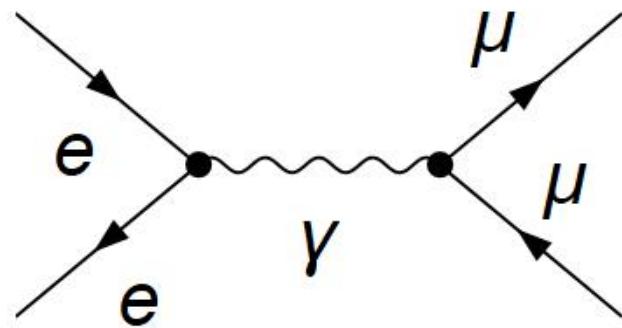


$$-\frac{e^2 (\varphi(\bar{p}', m_e)).(\bar{\gamma} \cdot \bar{\varepsilon}(k)).(\bar{\gamma} \cdot (\bar{p}' - \bar{k}) + m_e).(\bar{\gamma} \cdot \bar{\varepsilon}^*(k')).(\varphi(\bar{p}, m_e))}{(\bar{k} - \bar{p}')^2 - m_e^2} -$$
$$\frac{e^2 (\varphi(\bar{p}', m_e)).(\bar{\gamma} \cdot \bar{\varepsilon}^*(k')).(\bar{\gamma} \cdot (\bar{k}' + \bar{p}') + m_e).(\bar{\gamma} \cdot \bar{\varepsilon}(k)).(\varphi(\bar{p}, m_e))}{(-\bar{k}' - \bar{p}')^2 - m_e^2}$$

```
amp = FCFAConvert[CreateFeynAmp[top], IncomingMomenta → {p, k}, OutgoingMomenta → {p', k'},  
UndoChiralSplittings → True, ChangeDimension → 4, List → False, SMP → True] // Contract  
[真] [列表] [假] [真]
```

```
top = InsertFields[CreateTopologies[0, 2 → 2],  
{F[2, {1}], -F[2, {1}]} → {F[2, {2}], -F[2, {2}]}, InsertionLevel → {Classes},  
Model → "SM", Restrictions → QEDOnly];  
Paint[top, ColumnsXRows → {1, 1}, Numbering → Simple, SheetHeader → None,  
ImageSize → {200, 200}];
```

Antiparticles are denoted by a minus sign in front of the field.



$$-\frac{e^2 (\varphi(-\bar{p}', m_e)).\bar{\gamma}^{\text{Lor1}}.(\varphi(\bar{p}, m_e))(\varphi(\bar{k}, m_\mu)).\bar{\gamma}^{\text{Lor1}}.(\varphi(-\bar{k}', m_\mu))}{(\bar{k} + \bar{k}')^2}$$

```

amp = FCFAConvert[CreateFeynAmp[top], IncomingMomenta -> {p, p'},
  OutgoingMomenta -> {k, k'}, UndoChiralSplittings -> True, ChangeDimension -> 4,
  List -> False, SMP -> True] // Contract
| 真
| 假
| 真
    
```

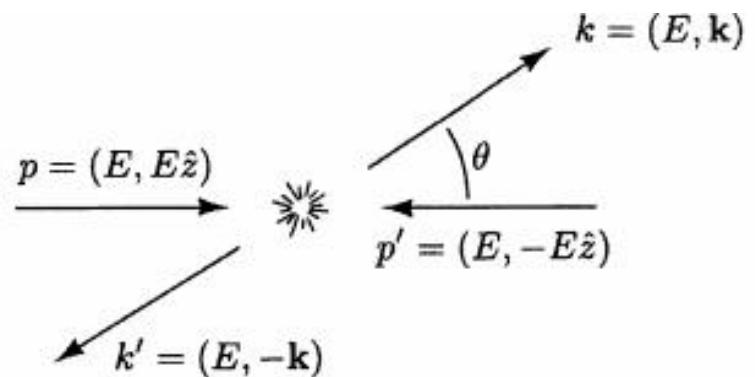
```
SetMandelstam[s, t, u, p, p', -k, -k', θ, θ, SMP["m_mu"], SMP["m_mu"]];  
sqAmp =  
(amp * (ComplexConjugate[amp] // FCRenameDummyIndices)) //  
PropagatorDenominatorExplicit // FermionSpinSum[#, ExtraFactor → 1 / 2^2] & //  
ReplaceAll[#, {SMP["m_e"] → 0, DiracTrace -> Tr}] & // Contract // Simplify  
[全部替换] [迹] [化简]
```

$$\frac{2 e^4 (2 m_\mu^4 + 2 m_\mu^2 (s - t - u) + t^2 + u^2)}{s^2}$$

$$s = (p + p')^2 = (k + k')^2$$

$$t = (k - p)^2 = (k' - p')^2$$

$$u = (k' - p)^2 = (k - p')^2$$



$$\frac{16 \pi^2 \alpha^2 (4 m_\mu^2 - 4 m_\mu^2 \cos^2(\theta) + s \cos^2(\theta) + s)}{s}$$

sqAmpθ =

Factor [sqAmp /. {t → $\text{SMP}["m_{\mu}"]^2 - (\text{s}/2 - \text{Sqrt}[\text{s}^2/4 - \text{SMP}["m_{\mu}"]^2 * \text{s}] * \text{Cos}[\theta])$ },
 |因式分解 |平方根 |余弦

u → $\text{SMP}["m_{\mu}"]^2 - (\text{s}/2 + \text{Sqrt}[\text{s}^2/4 - \text{SMP}["m_{\mu}"]^2 * \text{s}] * \text{Cos}[\theta])$,
 |平方根 |余弦

$\text{SMP}["e"]^4 \rightarrow (4 * \text{Pi} * \text{SMP}["\text{alpha_fs}"])^2 \}$

$$\left(\frac{d\sigma}{d\Omega} \right)_{\text{CM}} = \frac{1}{2E_A 2E_B |v_A - v_B|} \frac{|\mathbf{p}_1|}{(2\pi)^2 4E_{\text{cm}}} |\mathcal{M}(p_A, p_B \rightarrow p_1, p_2)|^2$$

```
prefac = Sqrt[s / 4 - SMP["m_mu"]^2] / (32 Pi^2 * s * Sqrt[s]);
[平方根] [圆周率] [平方根]
```

```
diffXSection0 = prefac * sqAmp0;
```

```
crossSectionTotal0 = 2 Pi * Integrate[diffXSection0 * Sin[th], {th, 0, Pi}]
```

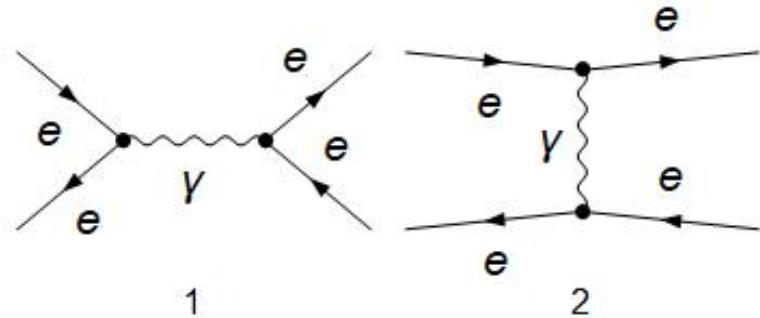
$$\frac{4\pi\alpha^2 \sqrt{s - 4m_\mu^2} (2m_\mu^2 + s)}{3s^{5/2}}$$

```
diffXSection1 = diffXSection0 /. SMP["m_mu"] -> 0 // Apart;
[分解分式]
```

```
crossSectionTotal1 = 2 Pi * Integrate[diffXSection1 * Sin[th], {th, 0, Pi}] 4\pi\alpha^2
[3s]
```

```
top = InsertFields[CreateTopologies[0, 2 → 2],  
{F[2, {1}], -F[2, {1}]] → {F[2, {1}], -F[2, {1}]}], InsertionLevel → {Classes},  
Model → "SM", Restrictions → QEDOnly];  
Paint[top, ColumnsXRows → {2, 1}, Numbering → Simple, SheetHeader → None,  
ImageSize → {200, 100}];
```

无

$e^+ e^- \rightarrow e^+ e^-$


$$\frac{e^2 (\varphi(\bar{k}, m_e)) \cdot \gamma^{\text{Lor}2} \cdot (\varphi(\bar{p}, m_e)) (\varphi(-\bar{p}', m_e)) \cdot \gamma^{\text{Lor}2} \cdot (\varphi(-\bar{k}', m_e))}{(\bar{k}' - \bar{p}')^2} -$$

$$\frac{e^2 (\varphi(\bar{k}, m_e)) \cdot \gamma^{\text{Lor}1} \cdot (\varphi(-\bar{k}', m_e)) (\varphi(-\bar{p}', m_e)) \cdot \gamma^{\text{Lor}1} \cdot (\varphi(\bar{p}, m_e))}{(\bar{k} + \bar{k}')^2}$$

```
amp = FCFAConvert [CreateFeynAmp[top], IncomingMomenta → {p, p'},
OutgoingMomenta → {k, k'}, UndoChiralSplittings → True, ChangeDimension → 4,
List → False, SMP → True] // Contract
```

[真]

```

SetMandelstam[s, t, u, p, p', -k, -k', SMP["m_e"], SMP["m_e"], SMP["m_e"], SMP["m_e"]];
sqAmp =
(amp * (ComplexConjugate[amp] // FCRenameDummyIndices)) // PropagatorDenominatorExplicit //
FermionSpinSum[#, ExtraFactor → 1 / 2^2] & // ReplaceAll[#, {DiracTrace -> Tr}] & //
 $\xrightarrow{\text{全部替换}}$                                           $\xrightarrow{\text{迹}}$ 
Contract // Simplify

```

$$\frac{2 e^4 \left(8 m_e^4 (s^2 + s t + t^2) - 4 m_e^2 (s^3 + s^2 (u - 2 t) + s t (3 u - 2 t) + t^2 (t + u)) + s^4 + s^2 u^2 + 2 s t u^2 + t^4 + t^2 u^2\right)}{s^2 t^2}$$

```

sqAmp0 = Factor[sqAmp /. {SMP["e"] ^4 → (4 * Pi * SMP["alpha_fs"]) ^2}];
 $\xrightarrow{\text{因式分解}}$                                           $\xrightarrow{\text{圆周率}}$ 
prefac = Sqrt[s / 4 - SMP["m_e"] ^2] / (32 Pi ^2 * s * Sqrt[s]);
 $\xrightarrow{\text{平方根}}$                                           $\xrightarrow{\text{圆周率}}$                                           $\xrightarrow{\text{平方根}}$ 
diffXSection0 = prefac * sqAmp0 /. SMP["m_e"] → 0

```

$$\frac{\alpha^2 (s^4 + s^2 u^2 + 2 s t u^2 + t^4 + t^2 u^2)}{2 s^3 t^2}$$

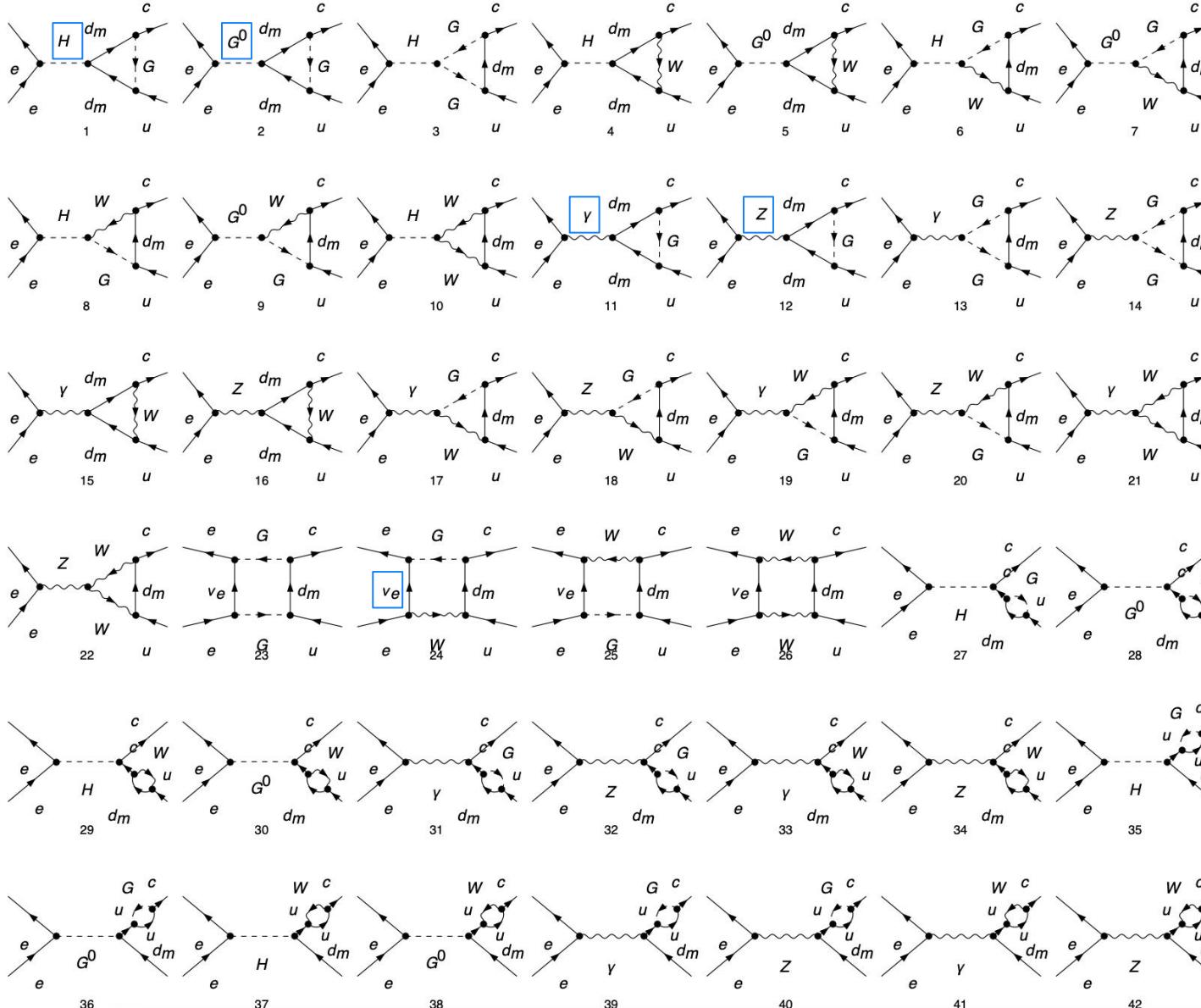
\$CKM = True;

[真]

top = InsertFields[CreateTopologies[1, 2 → 2],
{-F[2, {1}], F[2, {1}]} → {F[3, {2}], -F[3, {1}]}, InsertionLevel → {Classes}
(* , GenericModel → "Lorentz" *), Model → "SM"];

Paint[top, ColumnsXRows → {7, 6}, Numbering → Simple, SheetHeader → None,
[无]

ImageSize → {310, 270}];



`InsertFields[]`

`ExcludeParticles -> {S[1], S[2], F[1]}`

γ, Z

`ExcludeParticles -> {S[1], S[2], V[2], F[1]}`

γ

恳请各位老师同学
批评指正