

# Mass measurements with modern techniques

---- Mass/Q-value measurements with

JYFLTRAP at IGISOL

&MR-TOF at GSI-FAIR

&Rare-RI Ring/Bigrips-OEDO at RIBF



**Zhuang GE**

**Academy Fellowship (PI)**

**2023-11-08**

University of Jyväskylä/Finland

GSI/ Germany

[zhuang.z.ge@jyu.fi](mailto:zhuang.z.ge@jyu.fi); [z.ge@gsi.de](mailto:z.ge@gsi.de)



# Motivation: why do we measure nuclear masses?

Mass  $\rightarrow$  binding energy  $\rightarrow$  interaction



$$\begin{aligned}
 & \text{Nucleus} = N \times \text{neutron} + Z \times \text{proton} \\
 & \quad - \text{binding energy}
 \end{aligned}$$

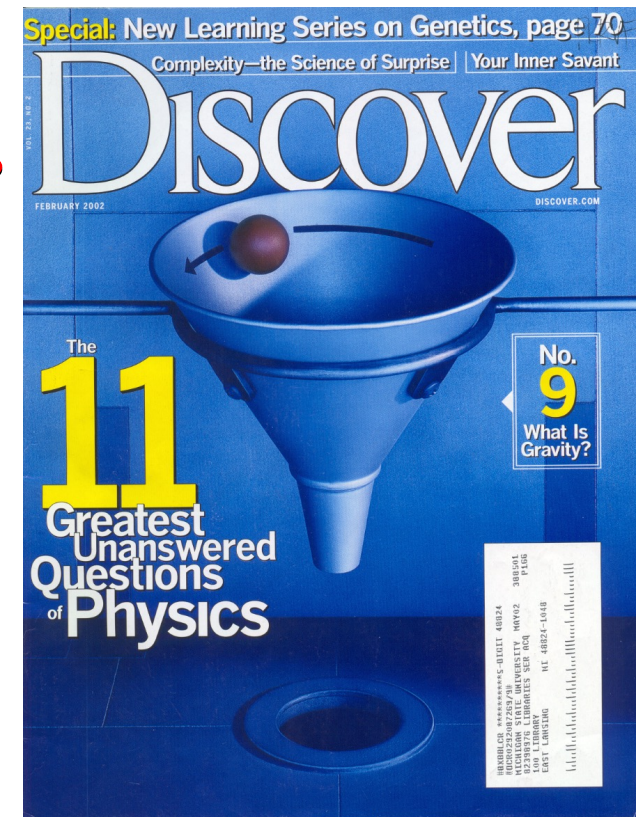
Exotic nuclei

Filed of application	Required uncertainty
Chemistry: identification of molecules	$10^{-5} - 10^{-6}$
Nuclear physics: shells, sub-shells, pairing	$10^{-6}$
Nuclear fine structure: deformation, halos	$10^{-7} - 10^{-8}$
Astrophysics: r-process, vp-, rp-process, waiting points	$10^{-7}$
Nuclear models and formulas: IMME	$10^{-7} - 10^{-8}$
Weak interaction studies: CVC hypothesis, CKM unitarity	$10^{-8}$
Atomic physics: binding energies, QED; neutrino physics	$10^{-9} - 10^{-11}$
Metrology: fundamental constants, CPT	$10^{-10}$

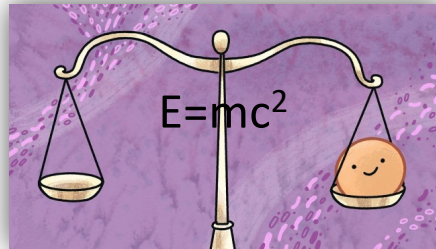


# Top 11 Greatest Unanswered Questions of Physics in this century

1. What is dark matter?
2. What is dark energy?
- 3. How were the heavy elements from iron to uranium made?**
4. Do neutrinos have mass?
5. Where do ultrahigh-energy particles come from?
6. New light and matter theory needed at ultra-high energies?
7. New states of matter at ultrahigh temperatures and densities?
8. Are protons unstable?
9. What is gravity?
10. Are there additional dimensions?
11. How did the universe begin?



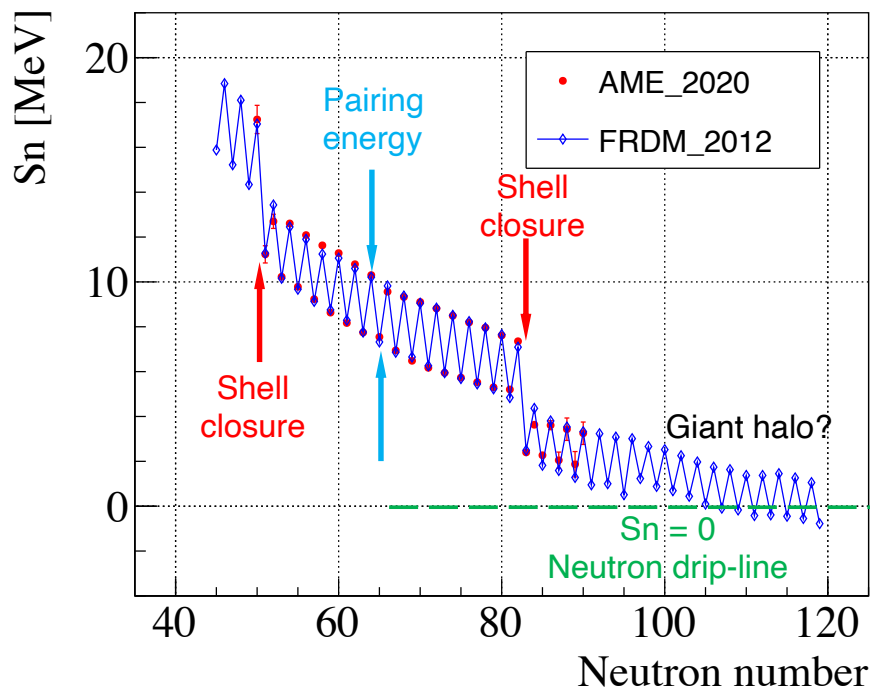
# Motivation for mass measurements



Nuclear structure

Nuclear astrophysics

tin ( $Z = 50$ ) one neutron separation energy



For example:  
rp process



**X-ray burst**

J. Grindlay et al., *Astrophys. J.* 205 (1976) L127.

time-scale  $\propto e^{(Q/kT)} / A(Q)$   
 isotope production  $\propto A(Q) \cdot e^{(Q/kT)}$   
 energy production  $\propto A(Q) \cdot Q \cdot e^{(Q/kT)}$   
**Common parameter: Q (mass difference)**

Nuclear mass  $\leftrightarrow$  nuclear binding energy:

$$M(N, Z) = Z \cdot m_p + N \cdot m_n - B(N, Z)/c^2$$

$$B(Z, N) = [NM_n + ZM_H - M_N(Z, N)]c^2$$

$$S_n(Z, N) = M(Z, N - 1) + M_n - M(Z, N) = BE(N, Z) - BE(N - 1, Z)$$



# Mass Measurement Techniques of Exotic/stable Nuclei

## Storage Rings



### Isochronous MS

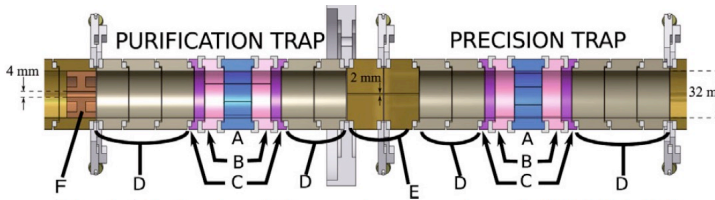
$t_{\text{meas}} \sim 100 \mu\text{s}$   
 $m/\Delta m = 2 \cdot 10^5$   
 $\delta m/m \sim 10^{-6}$   
 broadband  
 $\sim 10\text{-}200 \text{ keV}$

1. RIKEN/Rare RI Ring

## Penning Trap MS (TOF-ICR and PI-ICR-MS)

### TOF-ICR MS

$t_{\text{meas}} \sim 100\text{-}1000 \text{ ms}$   
 $m/\Delta m = 10^6\text{-}10^7$   
 $\delta m/m < 10^{-7}$   
 scanning



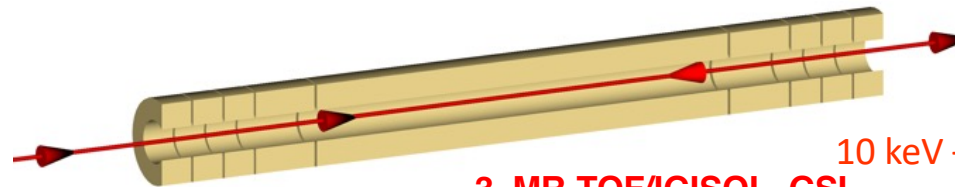
### PI-ICR MS

$t_{\text{meas}} \sim 100\text{-}1000 \text{ ms}$   
 $m/\Delta m \sim 10^7$   
 $\delta m/m < 10^{-8}$   
 broadband  
 $1 \text{ eV} - 10 \text{ keV}$

2. IGISOL/JYFLTRAP

## Multiple-Reflection Time-of-Flight MS (MR-TOF-MS)

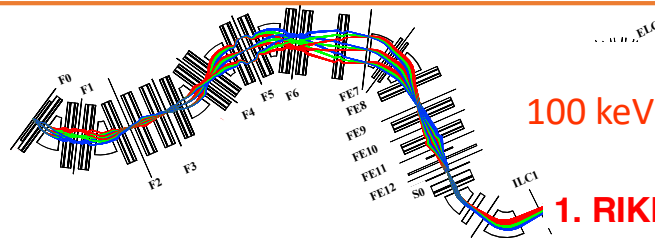
$t_{\text{meas}} \sim 10 \text{ ms}$   
 $m/\Delta m > 10^5$   
 $\delta m/m < 10^{-6}$   
 Broadband



10 keV – 100 keV  
 3. MR-TOF/IGISOL, GSI

## Magnetic-rigidity Time-of-Flight MS

$t_{\text{meas}} < 1 \mu\text{s}$   
 $m/\Delta m \sim 10^4$   
 $\delta m/m > 10^{-6}$   
 Broadband



100 keV – 1000 keV

1. RIKEN/BigRIPS-OEDO-SHARAQ

# Part 1

## Mass/Q-value measurements at JYFLTRAP

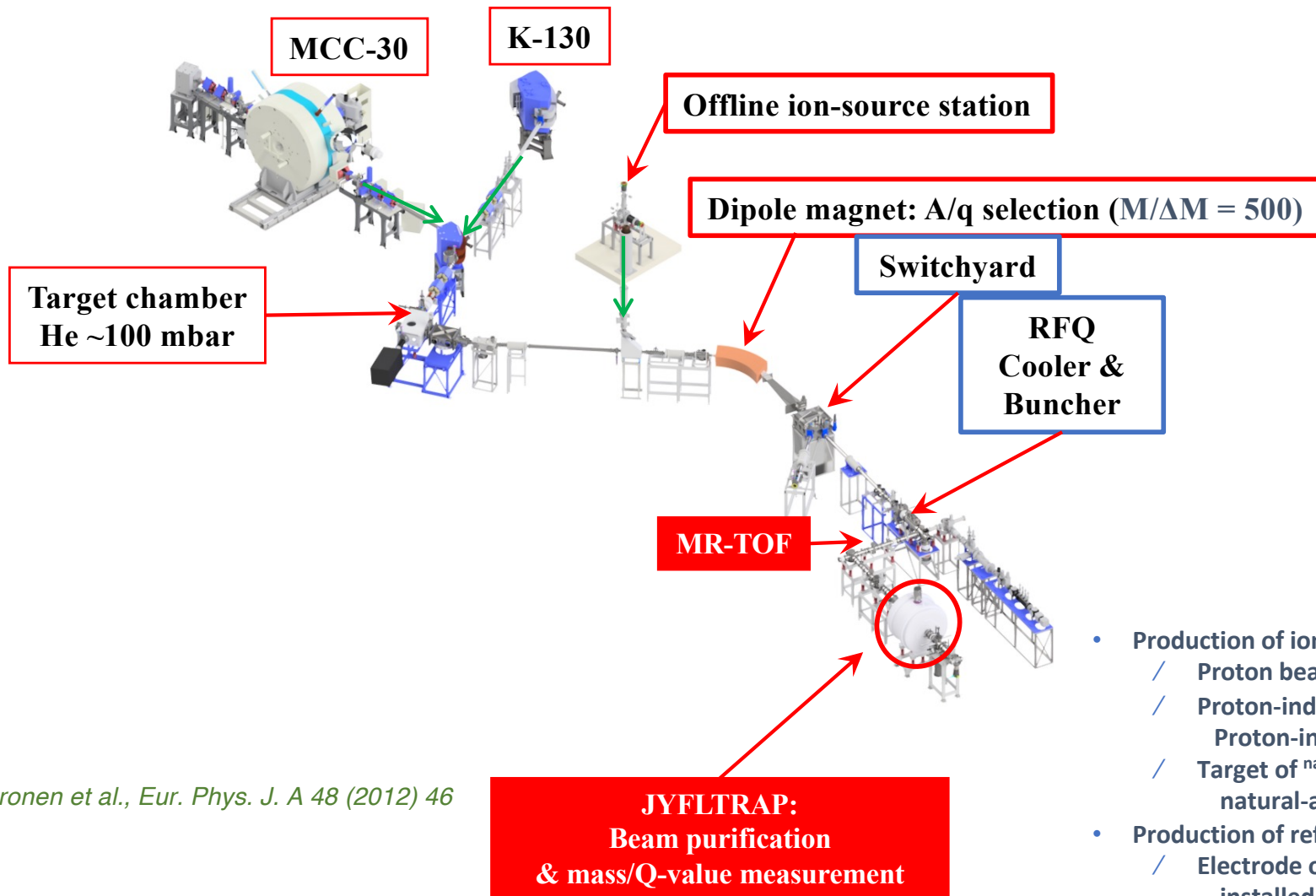




# The Ion Guide Isotope Separator On-Line facility (IGISOL)

J. Ärje, J. Äystö et al., PRL 54 (1985) 99

A fast and universal method to produce radioactive beams

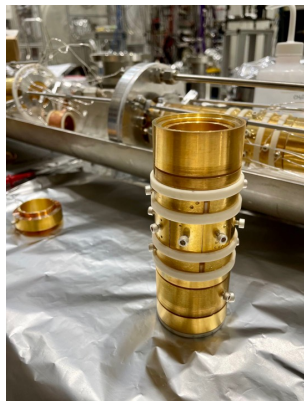
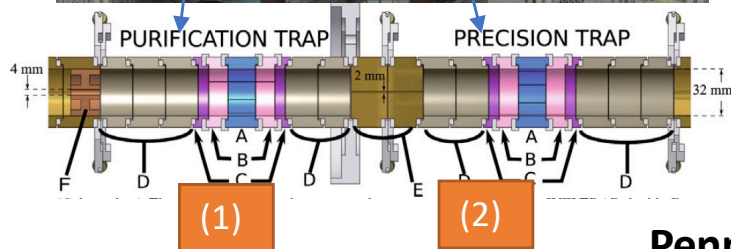
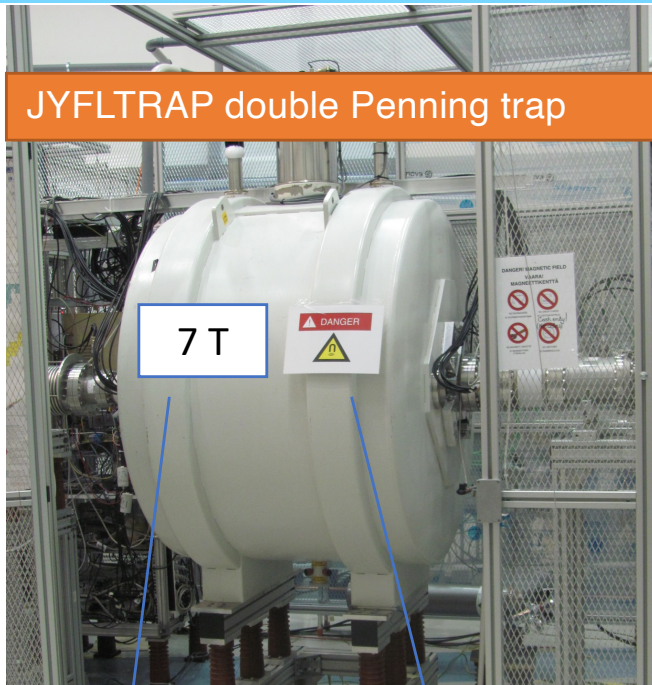


T. Eronen et al., Eur. Phys. J. A 48 (2012) 46

- Production of ions of interest:
  - / Proton beam of 5-65 MeV
  - / Proton-induced fission
  - Proton-induced fusion-evaporation
  - / Target of  $^{nat}\text{U}$ : 15mg/cm<sup>2</sup>
  - natural-abundance target ~2mg/cm<sup>2</sup>
- Production of reference nucleus:
  - / Electrode of reference material installed in the spark source

# JYFLTRAP double Penning trap

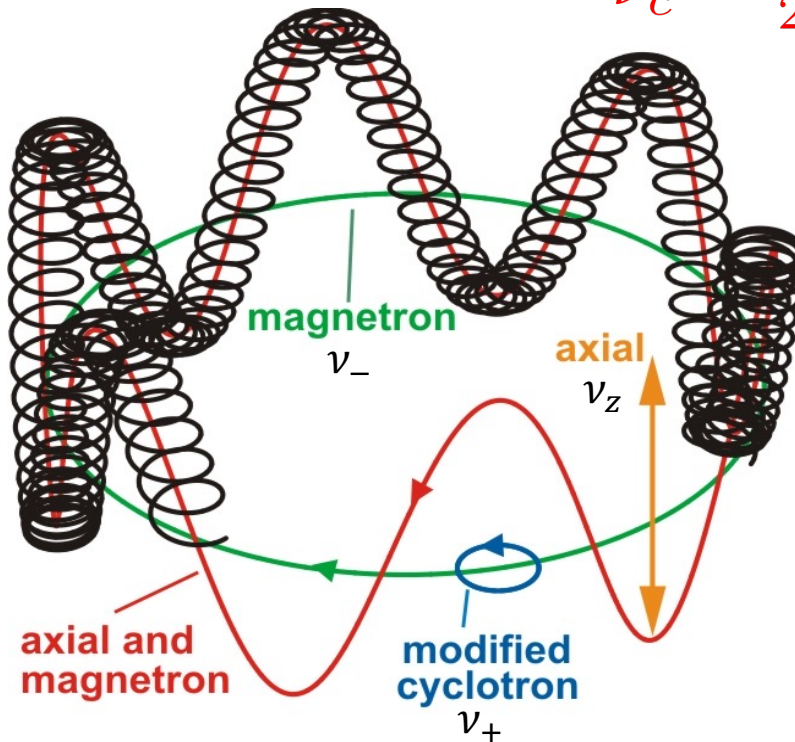
JYFLTRAP double Penning trap



Eronen et al., EPJA 48 (2012) 46

Cyclotron frequency

$$\nu_c = \frac{1}{2\pi} \frac{q}{m} B$$



Penning trap eigenfrequencies:

$$\nu_z = \frac{1}{2\pi} \sqrt{\frac{U_0}{d^2} \frac{q}{m}}$$

$$\nu_{\pm} = \frac{1}{2} \left( \nu_c \pm \sqrt{\nu_c^2 - 2\nu_z^2} \right)$$

Invariance theorem:

$$\nu_c^2 = \nu_-^2 + \nu_+^2 + \nu_z^2$$

# Q-value and mass measurements

- Cyclotron frequency:

$$\nu_c = \nu_+ + \nu_- = \frac{qB}{2\pi m}$$

- Frequency ratio  $r$ :

$$r = \frac{\nu_1}{\nu_2}$$



- $Q$ -value:

$$Q = M_2 - M_1 = (r - 1)(M_1 - m_e) + m_e$$

- Mass:

$$M_2 = r(M_1 - m_e) + m_e$$

*Eronen et al., EPJA 48 (2012) 46*

## 1. TOF-ICR

Time-of-Flight Ion-Cyclotron-Resonance (TOF-ICR) technique  
*Eronen et al., EPJA 48 (2012) 46*

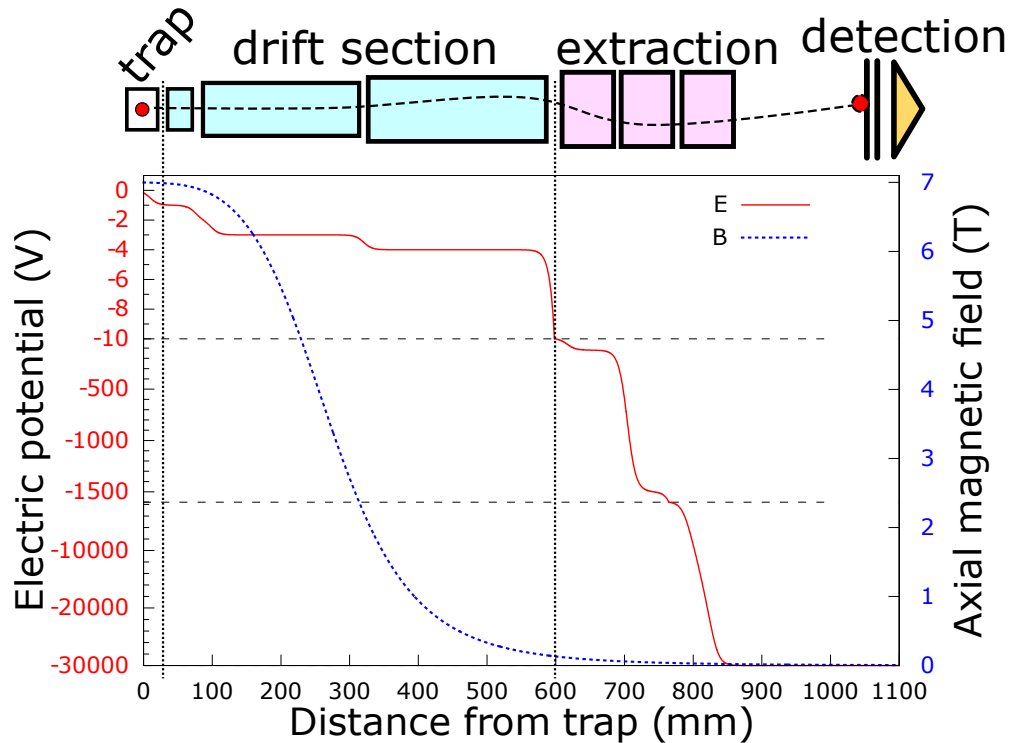
- Normal TOF-ICR
- Ramsey TOF-ICR

## 2. PI-ICR

Phase-imaging Ion Cyclotron Resonance (PI-ICR) technique  
*S. Eliseev et al., Phys. Rev. Lett. 110, 082501 (2013).*



# TOF-ICR method



T. Eronen et al. / Progress in Particle and Nuclear Physics 91 (2016) 259–293

Flight-of-time (TOF) from trap to MCP detector:

$$T(\omega) = \int_0^{z'} \sqrt{\frac{m}{2(E_0 - qU(z) - \mu B(z))}} dz$$

$E_0$ : initial axial kinetic energy of the ion,

$U(z)$ : electrostatic potential,

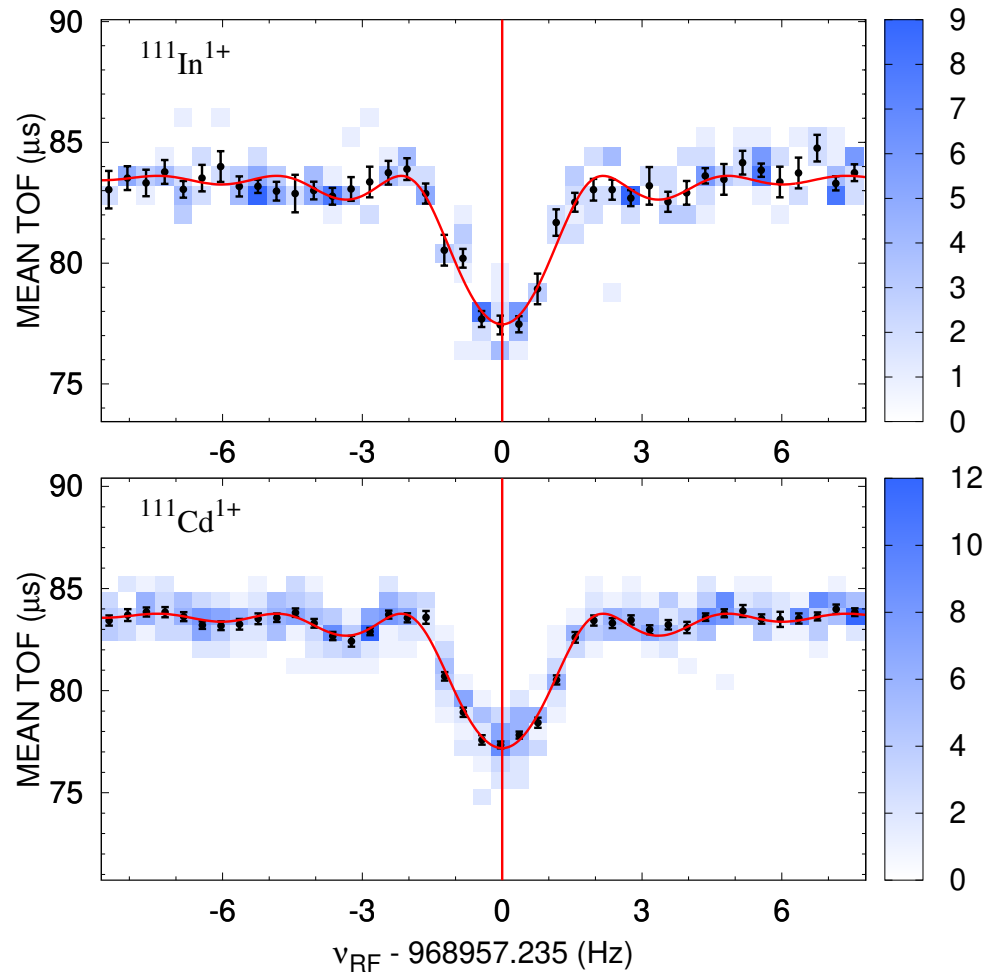
$B(z)$ : the magnetic field along the flight path

## Measurement procedure:

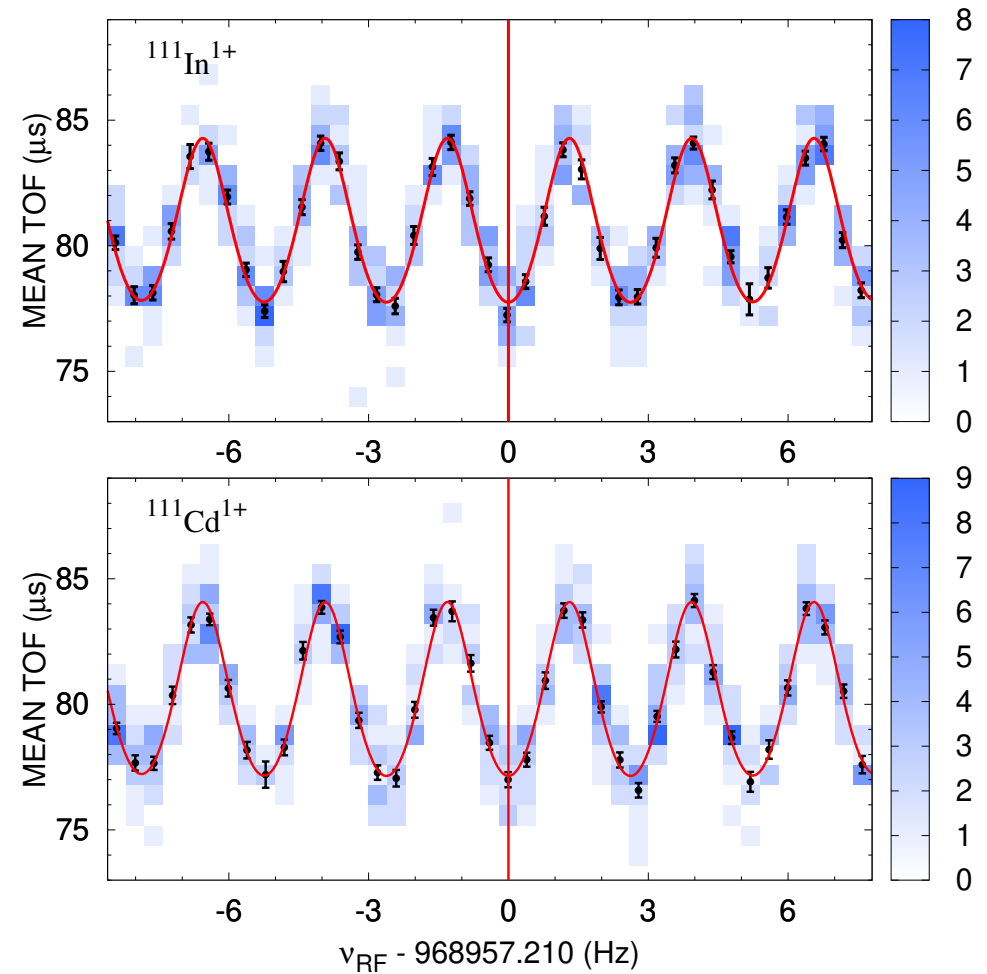
scanning the quadrupolar excitation frequency  $\nu_{RF}$  around the cyclotron frequency  $\nu_c$  and determining the frequency resulting in the shortest flight time from the trap to the MCP detector

# TOF-ICR method

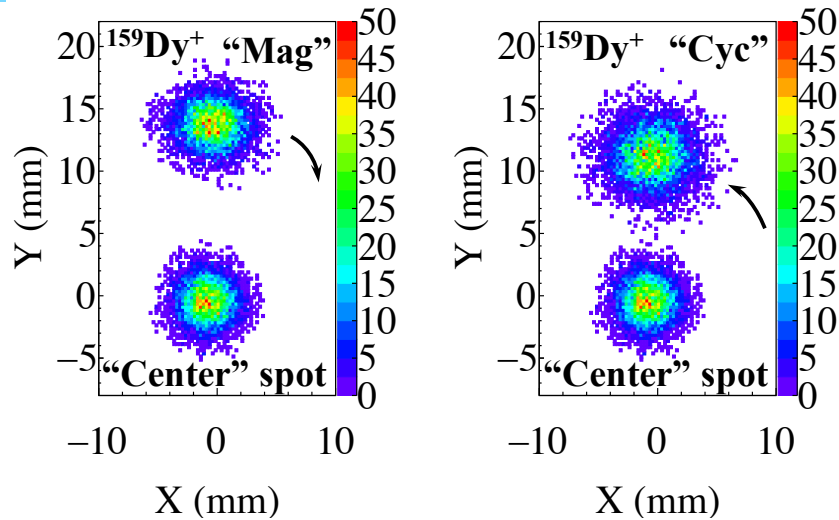
one-pulse radio-frequency (rf) field (400 ms)



two-pulse rf field (25-350-25 ms)



# Phase-imaging Ion-Cyclotron-Resonance (PI-ICR)

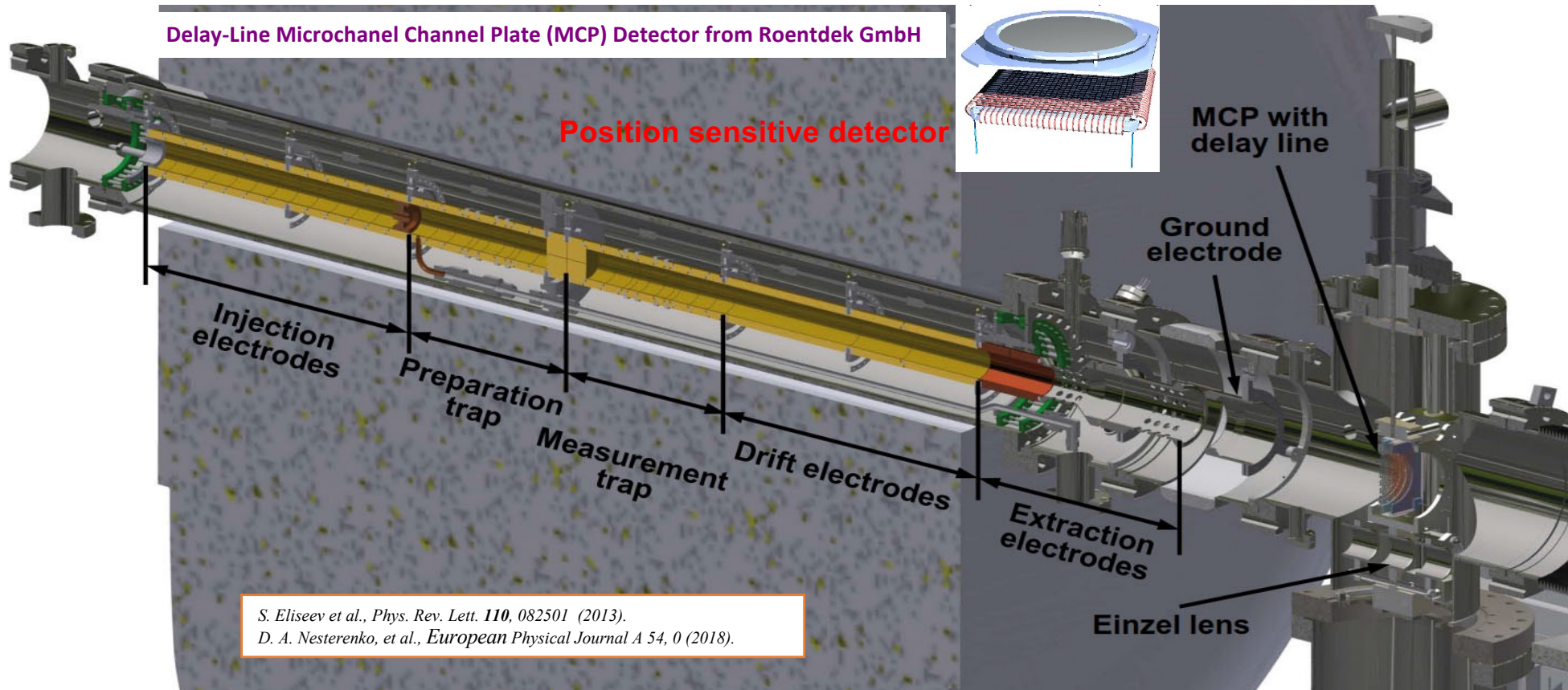


Angle between cyclotron and magnetron motion phases with respect to the center spot:

$$\alpha_c = \alpha_- + \alpha_+$$

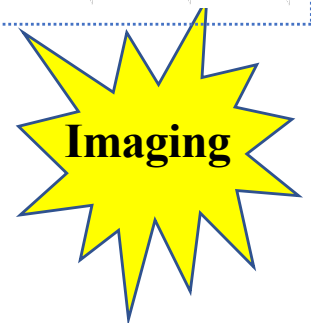
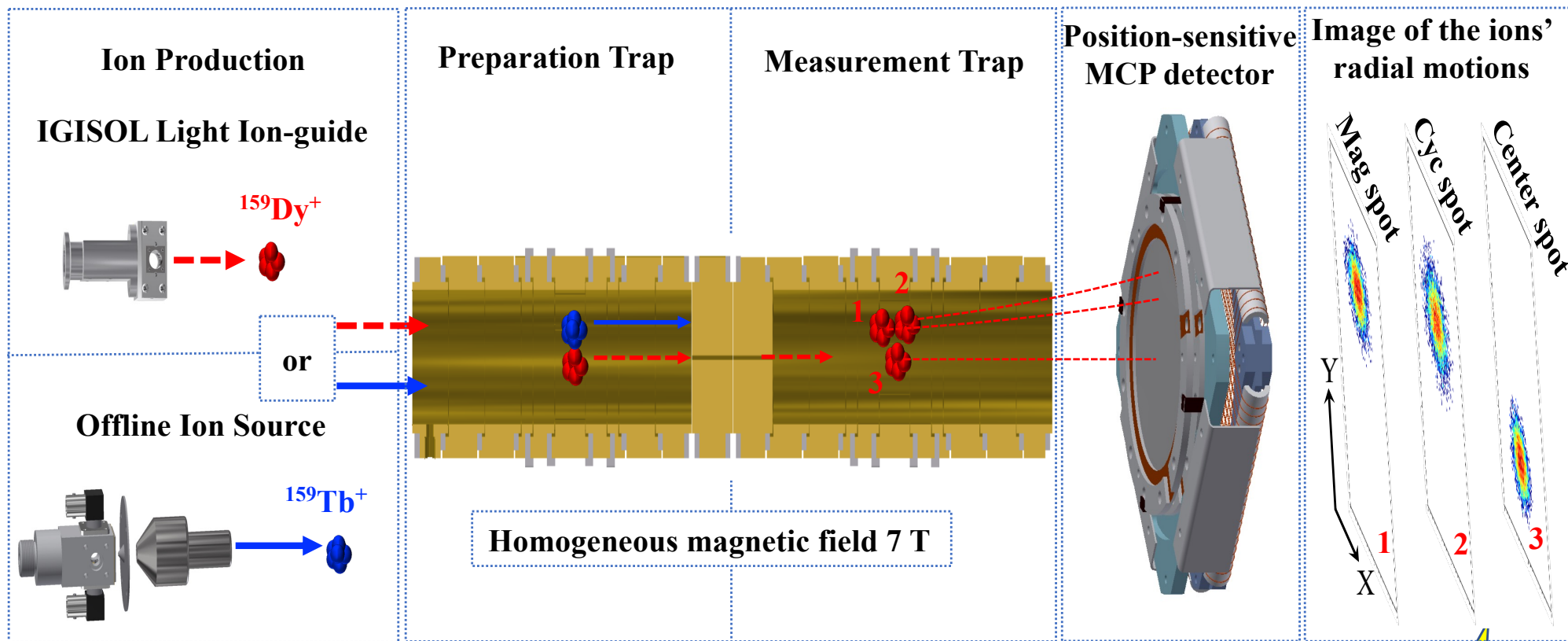
cyclotron frequency:

$$\nu_c = \nu_+ + \nu_- = \frac{\alpha_c + 2\pi n}{2\pi t}$$



S. Eliseev et al., *Phys. Rev. Lett.* **110**, 082501 (2013).  
 D. A. Nesterenko, et al., *European Physical Journal A* **54**, 0 (2018).

# Schematic of PI-ICR for $^{159}\text{Dy}$ - $^{159}\text{Tb}$ Q-value measurements



D. A. Nesterenko, T. Eronen, Z. Ge, et al., Eur. Phys. J. A 57, 302 (2021).

<https://doi.org/10.1140/epja/s10050-021-00608-3>;

M. Ramalho, Z. Ge, T. Eronen et al., Phys. Rev. C 00, 005500 (2022) DOI: [10.1103/PhysRevC.00.005500](https://doi.org/10.1103/PhysRevC.00.005500)

# Determination of neutrino mass from single $\beta^\pm/EC$ decay

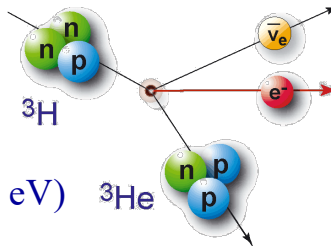
Current direct neutrino mass probes: Ground-state to ground-state (gs-to-gs) decays  
 ( $\beta^-$ : Tritium,  $^{187}\text{Re}$ ; EC:  $^{163}\text{Ho}$ )

- Lower Q-value, higher sensitivity to neutrino mass
- Model independent method

**Our Purpose: Search for low Q-value decays**

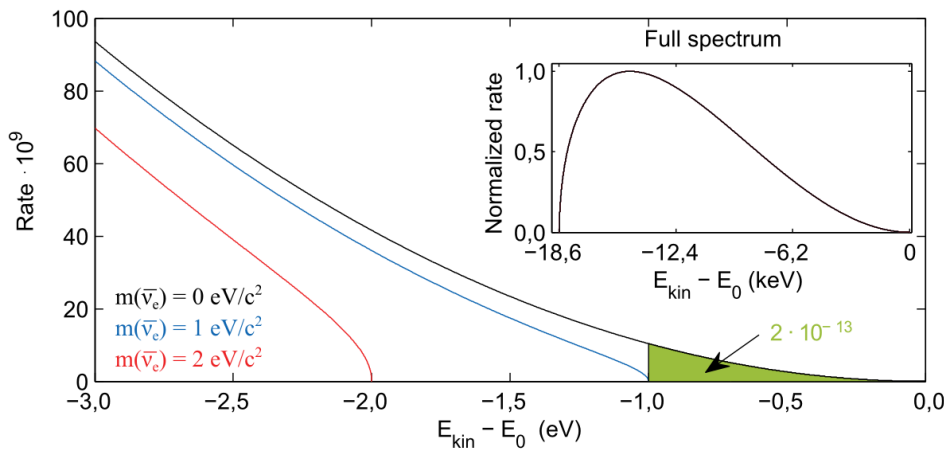
**$Q \rightarrow 0$ , and  $Q < 1$  keV (ultra-low)**

**Tritium ( $\beta^-$ -decay)**



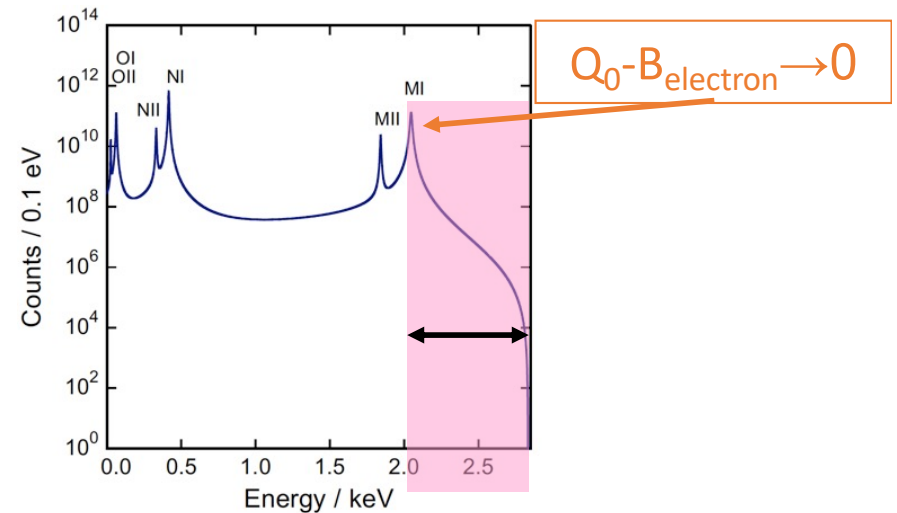
$E_0 = Q_0 - E_{\text{rec}}$  (recoil corrections: 1.72 eV)  $^3\text{He}$

Endpoint energy  $E_0 \sim 18.57$  keV



**$^{163}\text{Ho}$  (Electron Capture)**

$Q_0 \sim 2.83$  keV

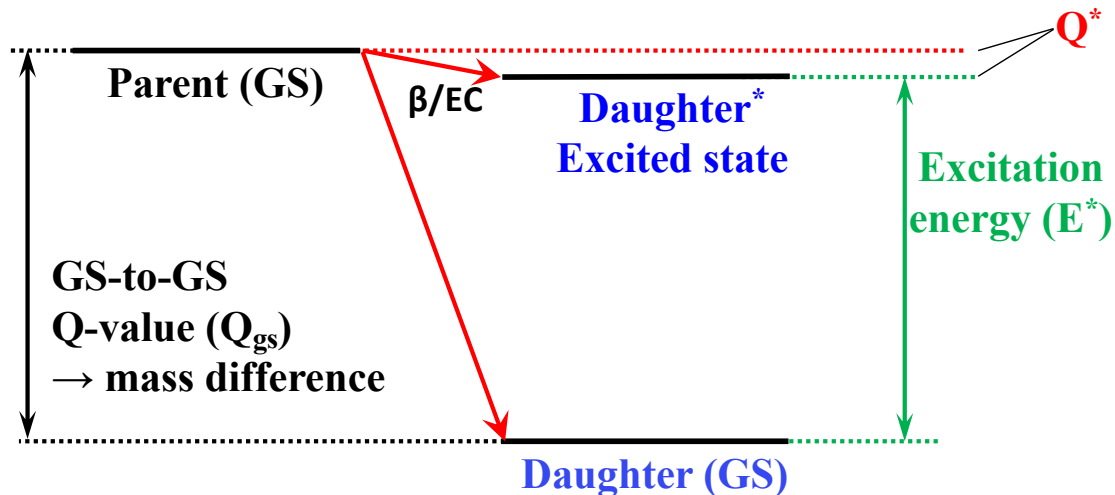




# Low Q-value decays for neutrino mass determination

We search for low Q-value ground state to nuclear excited state decays.

- Low Q-value ( $Q^*$ ):  $< 1$  keV



$$Q^* = Q_{gs} - E^*$$

$E^*$  From gamma spectroscopy

- Typical uncertainty  $\sim 100$  eV
- Potentially  $\sim 10$  eV

Our work:  $Q_{gs}$  measurements

- Penning trap mass spectrometry (JYFLTRAP)
- $Q_{gs}$  through  $E = mc^2$

Nuclear theory:

- Partial half-life based on  $Q^*$

1.  $\beta$ -decay of  $^{115}\text{In}(9/2^+) \rightarrow ^{115}\text{Sn}^*(9/2^+)$ :  $Q^*$ -value = 0.147(10) keV

$E^*$  improvement: V. A. Zheltonozhsky et al. 2018 EPL 121 12001

2.  $\beta$ -decay of  $^{135}\text{Cs}(7/2^-) \rightarrow ^{135}\text{Ba}^*(11/2^+)$ :  $Q^*$ -value = 0.44(31) keV

$Q_{gs}$  improvement: A. De Roubin, J. Kostensalo, T. Eronen et al., Phys. Rev. Lett., 124 (22), 222503.

# Summary of measured Q-values of potential candidates at JYFLTRAP

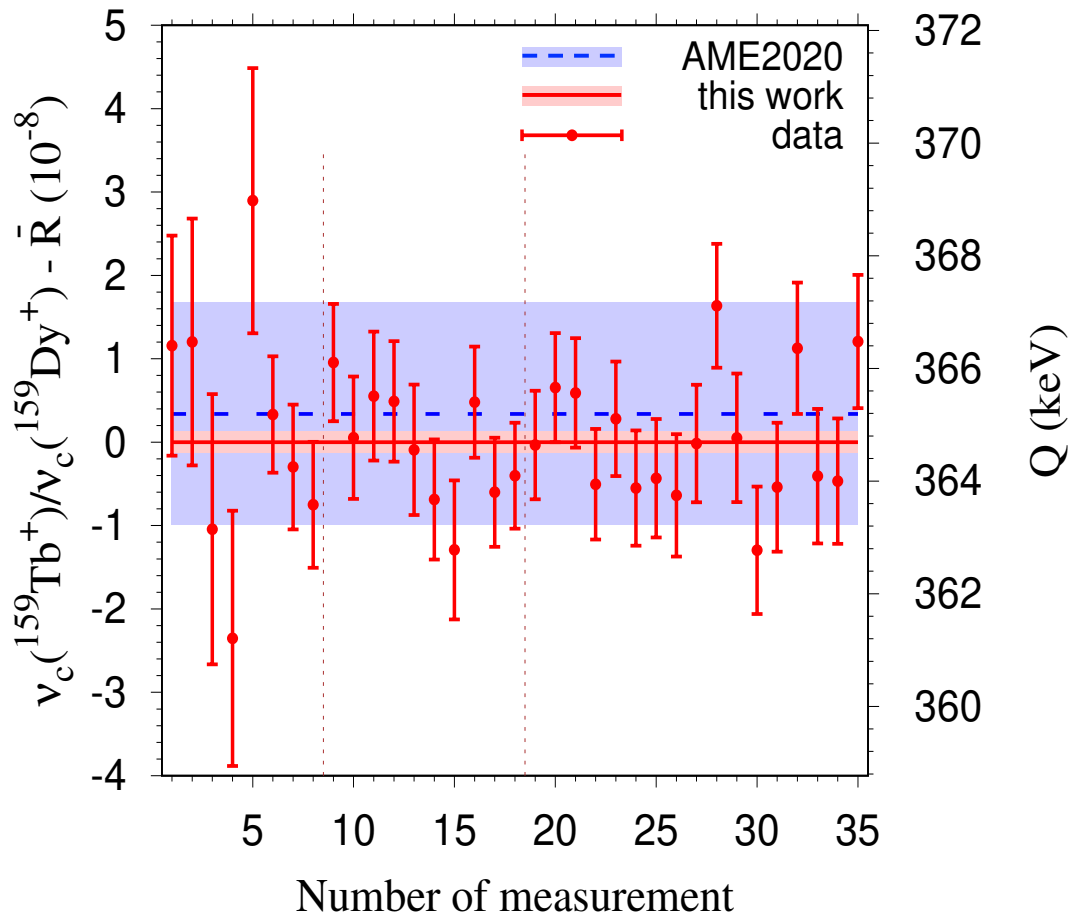
- List of measured promising low Q-value decay candidates for neutrino mass determination

Parent	T1/2	Daughter	E* (keV)	decay type	Q* (keV)	Decay	Q <sub>0</sub> (keV)	dQ <sub>0</sub> (keV)	
146Pm(3-)	5.53(5) y	146Nd(2+)	1470.63(6)	1st FNU	1.3(4.2)	EC	1472.000	4.000	
149Gd(7/2-)	9.28(10) dy	149Eu(5/2+)	1312(4)	1st FNU	2(6.4)	EC	1314.100	4.000	
<b>155Tb(3/2+)</b>	<b>5.32(6) dy</b>	155Gd{3/2+}	815.731(3)	Allowed{?}	4.2(10.1)	EC	820.000	10.000	
<i>Z. Ge, T. Eronen et al., PHYSICAL REVIEW Letter</i>	<b>159Dy(3/2-)</b>	<b>144.4(2) dy</b>	<b>159Tb(5/2-)</b>	<b>363.5449(14)</b>	<b>Allowed</b>	<b>1.7(1.2)</b>	<b>EC</b>	<b>365.200</b>	<b>1.200</b>
			<b>159Tb(11/2+)</b>	<b>362.050(40)</b>	<b>3rd FU</b>	<b>3.2(1.2)</b>	<b>EC</b>	<b>365.200</b>	<b>1.200</b>
	161Ho(5/2-)	18.479(4) hr	161Dy{7/2+}	858.502(7)	1st FNU	1.0(2.2)	EC	858.500	2.200
			161Dy{3/2-}	858.7919(18)	Allowed	-0.3(2.2)	EC	858.500	2.200
<i>Z. Ge, T. Eronen et al., PHYSICAL REVIEW C 103, 065502 (2021)</i>	72As(2-)	26.0(1)h	72Ge{1}	4358.7(3)	Allowed{?}	-2.8(4.0)	EC	4356.000	4.000
			72Ge(3-)	3325.01(3)	Allowed	8.9(4.0)	β+	4356.000	4.000
			72Ge(2+)	3327(3)	1st FNU	6.9(5.0)	β+	4356.000	4.000
			72Ge{1+}	3338.0(3)	1st FNU{?}	-4.1(4.0)	β+	4356.000	4.000
	72Ge{2-}	3341.76(4)	Allowed{?}	-7.9(4.0)	β+	4356.000	4.000		
159Gd(3/2-)	26.24(9) h	159Tb{1/2+}	971	1st FNU{?}	0.0(1.8)	β-	970.900	0.800	
<i>Z. Ge, T. Eronen, et al., PRC</i>	77As(3/2-)	38.79(5) h	77Se(5/2+)	680.1035(17)	1st FNU	3.1(1.7)	β-	683.200	1.700
	76As(2-)	26.24(9) h	76Se{2-}	2968.4(7)	Allowed{?}	-7.8(1.1)	β-	2960.600	0.900
<i>M. Ramalho, Z. Ge, T. Eronen et al., Phys. Rev. C</i>	153Tb(5/2+)	2.34(1)dy	153Gd(5/2-)	548.7645(18)	1st FNU	-1.2(4.0)	β+	1569.000	4.000
			153Gd{5/2}	551.092(19)	Allowed{?}	-3.5(4.0)	β+	1569.000	4.000
<i>Z. Ge, T. Eronen, et al., PLB</i>	111In(9/2+)	3dy	111Cd(3/2+)	864.8(3)	2nd FU	-6.6(3.0)	EC	860.2	3.4
			111Cd(3/2+)	864.8(3)	2nd FU	-4.6(3.0)	EC	860.2	3.4
			111Cd(3/2+)	855.6(1.0)	2nd FU	4.6(3.2)	EC	860.2	3.4
			111Cd(7/2+)	853.94(7)	Allowed	6.3(3.0)	EC	860.2	3.4
<i>T. Eronen, Z. Ge, et al., PLB</i>	131I(7/2+)	8dy	131Xe(9/2+)	971.22(13)	Allowed{?}	-0.42(0.61)	β-	970.80	0.60
			131Xe(7/2+)	973.11(14)	Allowed	-2.31(0.62)	β-	970.80	0.60
155Eu(5/2+)	5yr	155Gd(9/2-)	251.7056(10)	1st FU	0.1(1.8)	β-	252.00	2.40	

Q<sub>0</sub> from: *M. Wang et al., Chinese Physics C 45, 030003 (2021)*

E\* from: *National nuclear data center, Available at <https://www.nndc.bnl.gov>*

# Q-value measurement of $^{159}\text{Dy}$



## Gs-to-GS Q value ( $Q_{\text{EC}}^{\text{GS}}$ )

Obtained frequency ratio  $r$  with a precision of  $1.3 \times 10^{-9}$

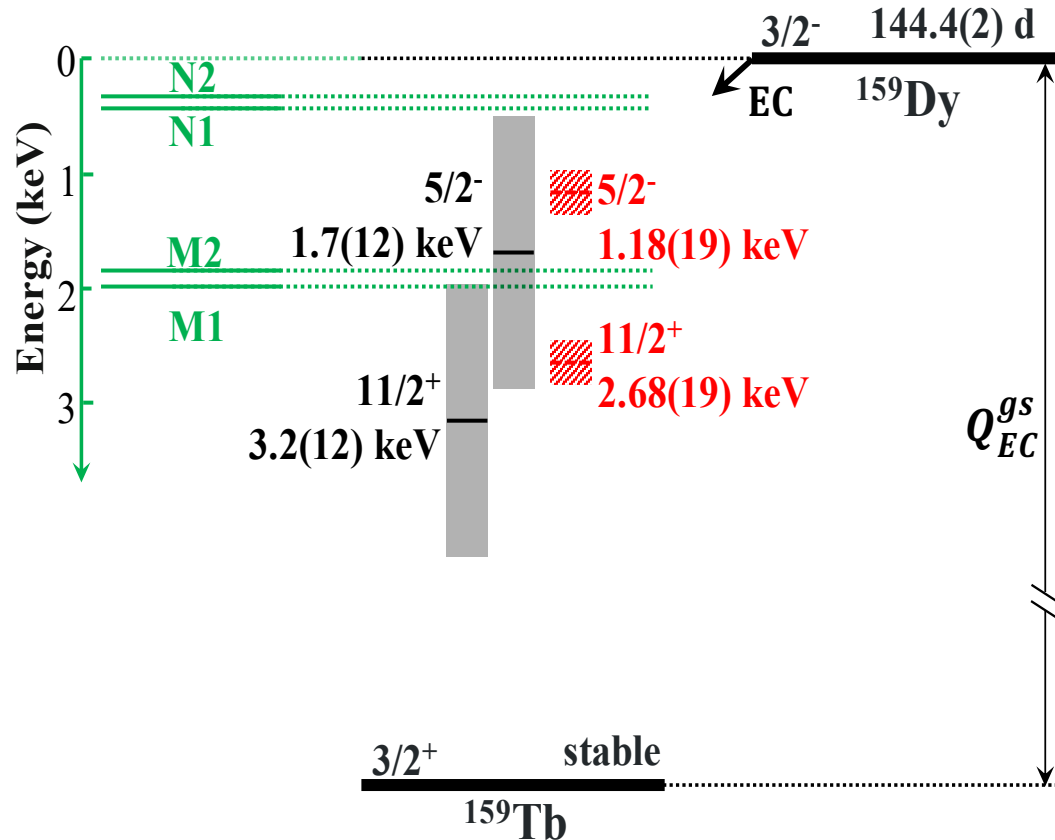


Q-value precision: **190 eV**

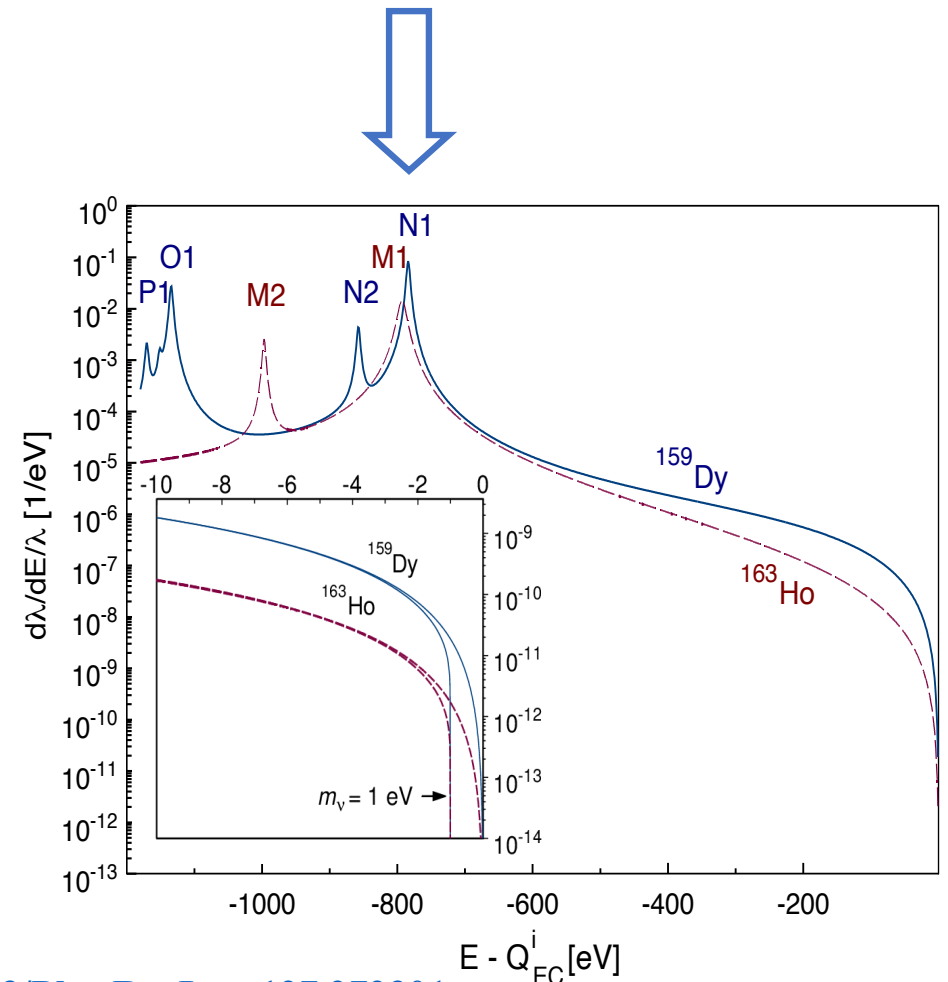
now **6.3 times** more precise and 0.47 keV smaller than literature value

[Z. Ge et al., Phys. Rev. Lett. 127, 272301 \(2021\) DOI: 10.1103/PhysRevLett.127.272301;](#)

# Level scheme of $^{159}\text{Dy}$ with refined Q-value



Gs-to-GS Q value ( $Q_{EC}^{GS}$ )	
$E_i^*$	Binding energy $e_x$ (allowed atomic shell x of the EC)
5/2- 363.5449(14)	+
11/2+ 362.050(40)	



Z. Ge et al., Phys. Rev. Lett. 127, 272301 (2021) DOI: 10.1103/PhysRevLett.127.272301;



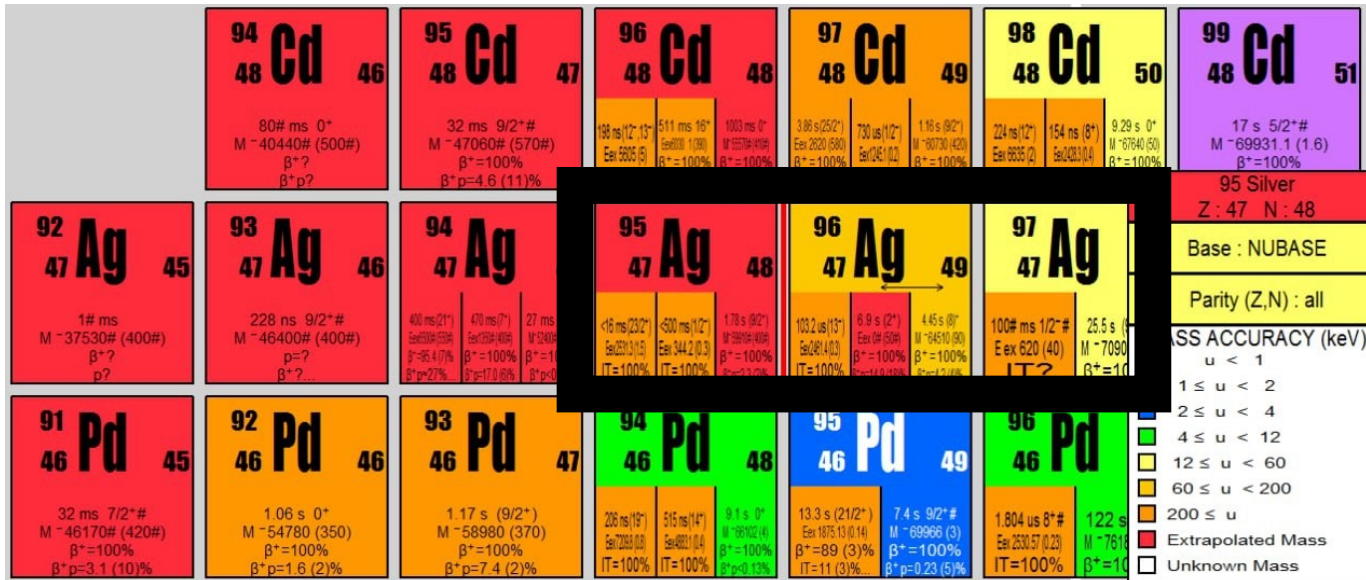
# Part 2

# Mass measurements at JYFLTRAP





# Mass measurements of $^{95-97}\text{Ag}$ mass data



Cyclotron frequency:

$$v_c = v_+ + v_- = \frac{qB}{2\pi m}$$

Frequency ratio  $r$ :

$$r = \frac{v_1}{v_2}$$

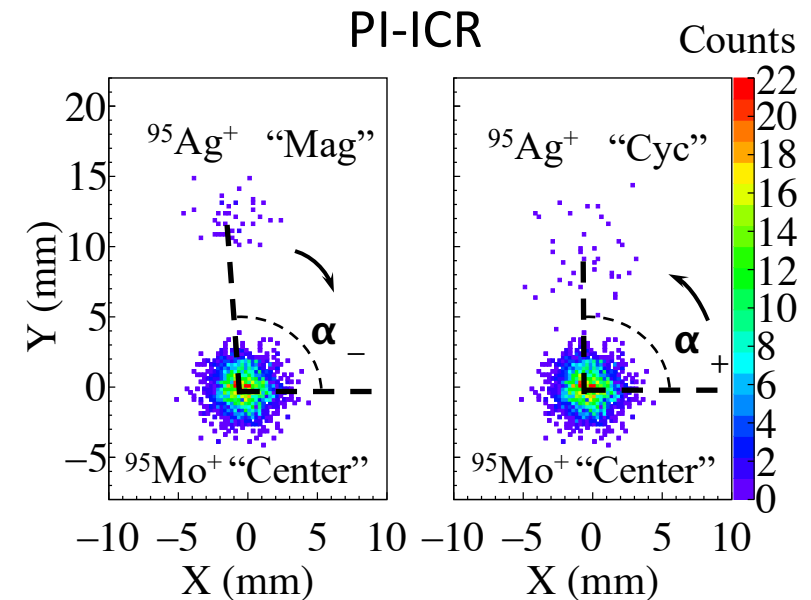
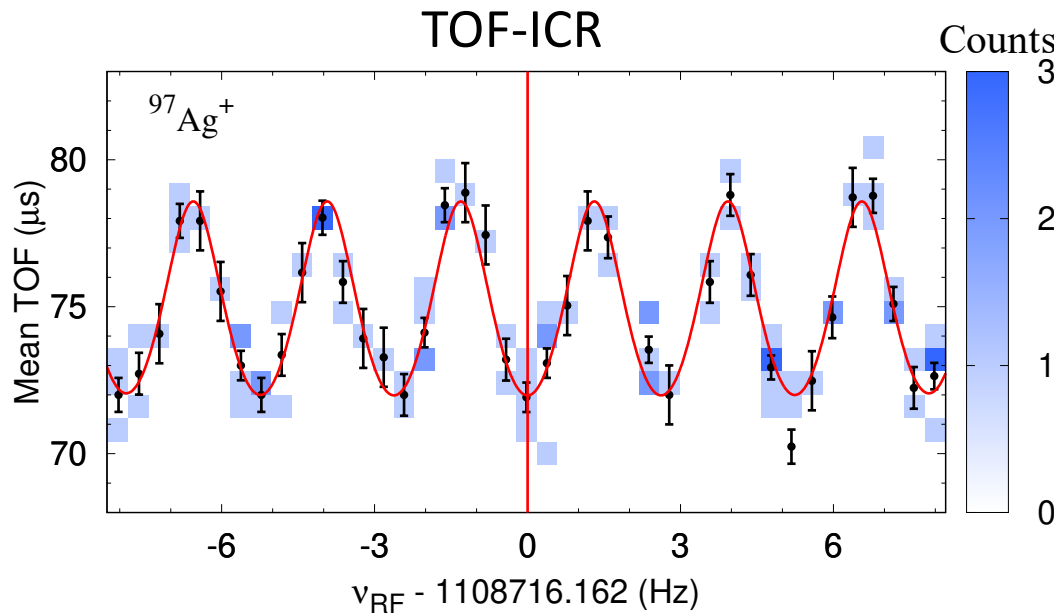
Q-value:

$$Q = M_2 - M_1 = (r - 1)(M_1 - m_e) + m_e$$

Mass:

$$M_2 = r(M_1 - m_e) + m_e$$

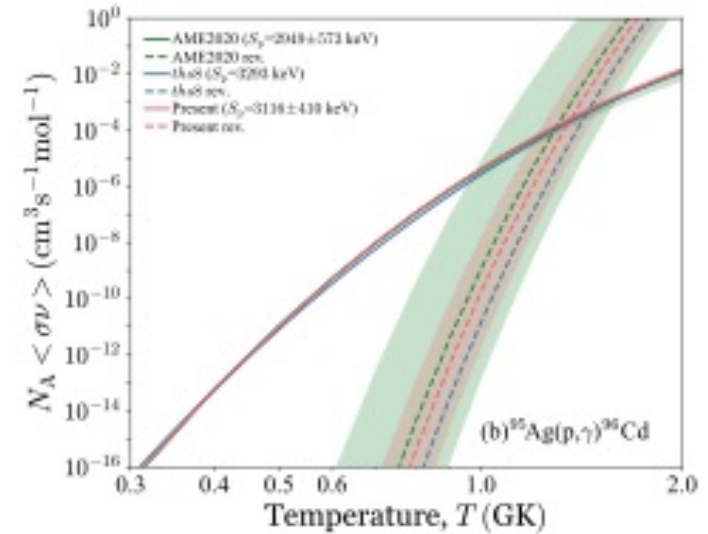
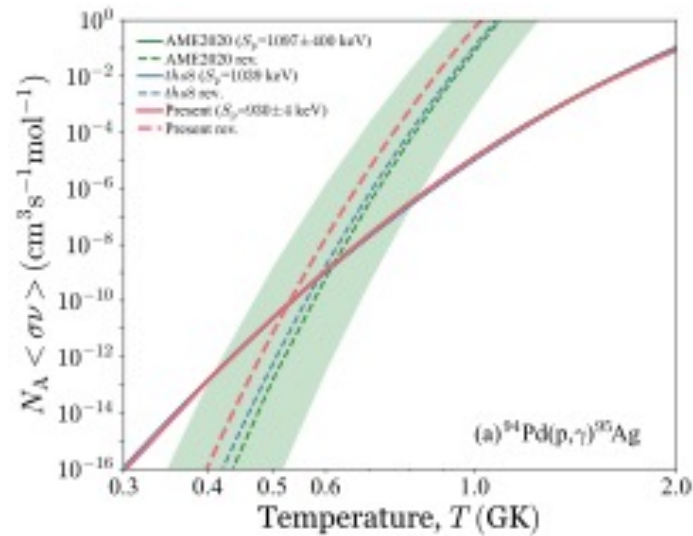
Z. Ge, M. Reponen, T. Eronen et al., in preparation (IGISOL collaboration)



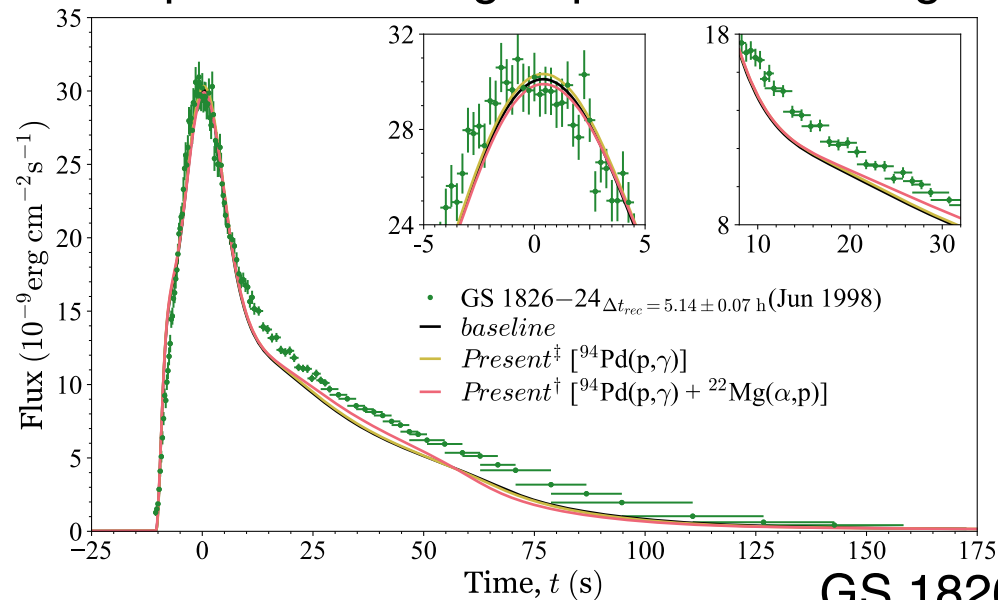
# Impact on nuclear astrophysics

*Influence on Forward and reverse  
thermonuclear reaction rates*

Y. Lam et al.,



Impact on averaged periodic burst light curves

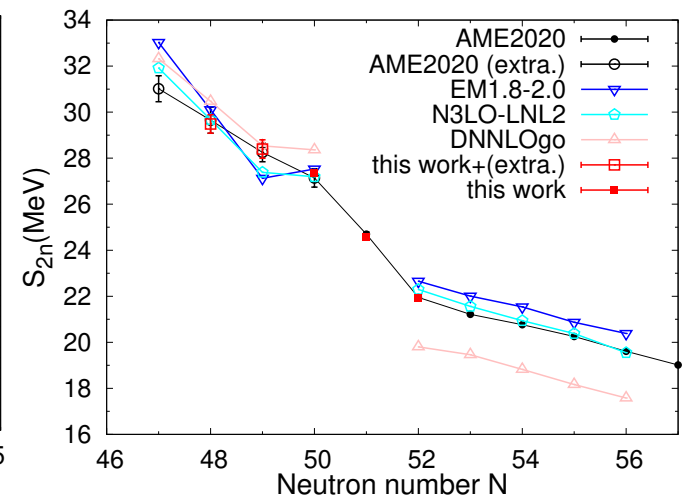
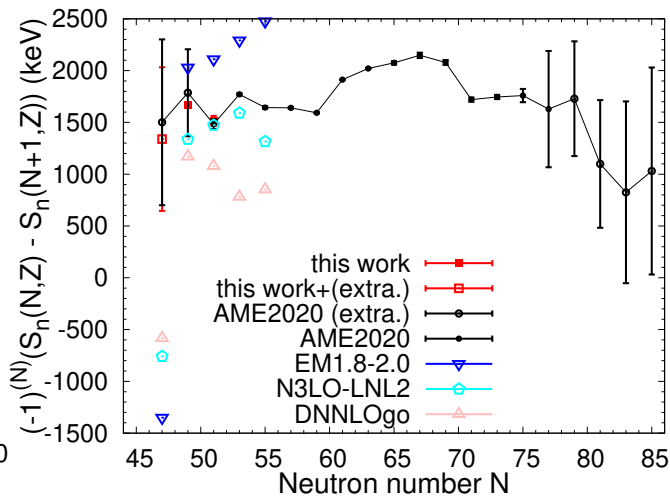
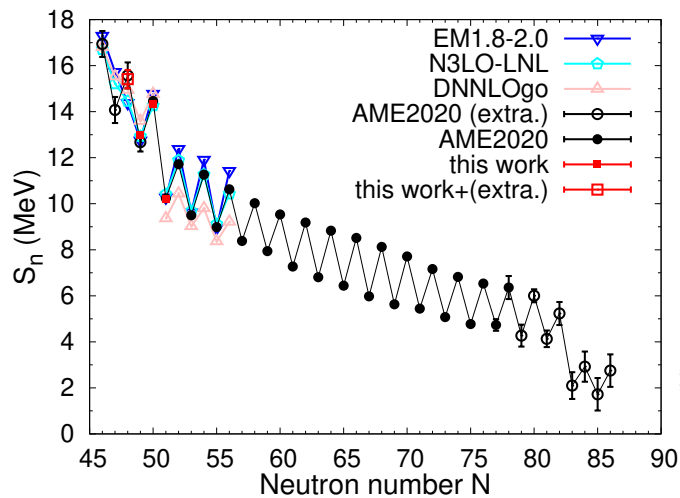
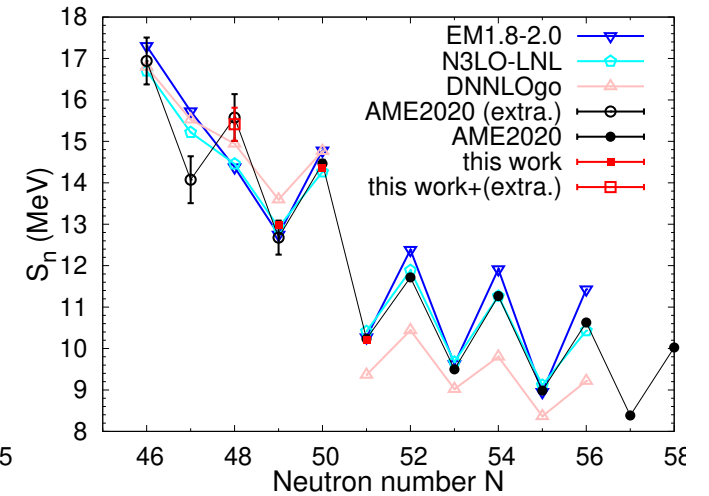
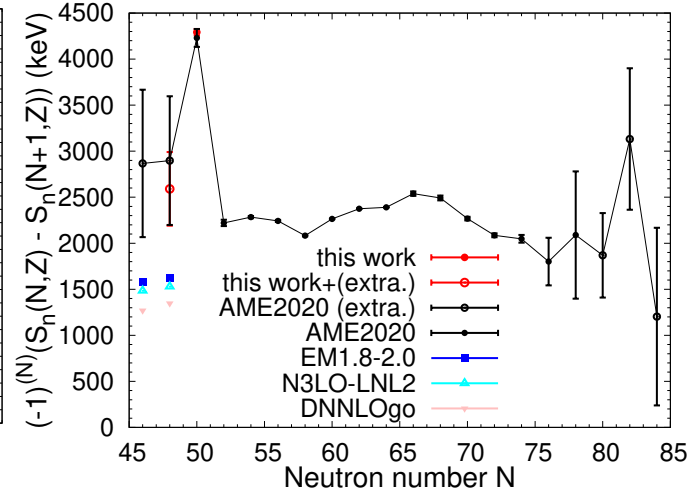
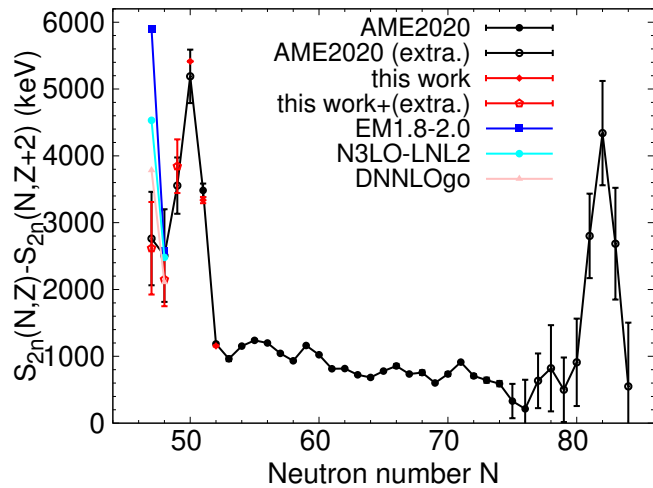


GS 1826–24 clocked burster

# Nuclear structure study

Ab-initio calculation compared to experimental data&extrapolation

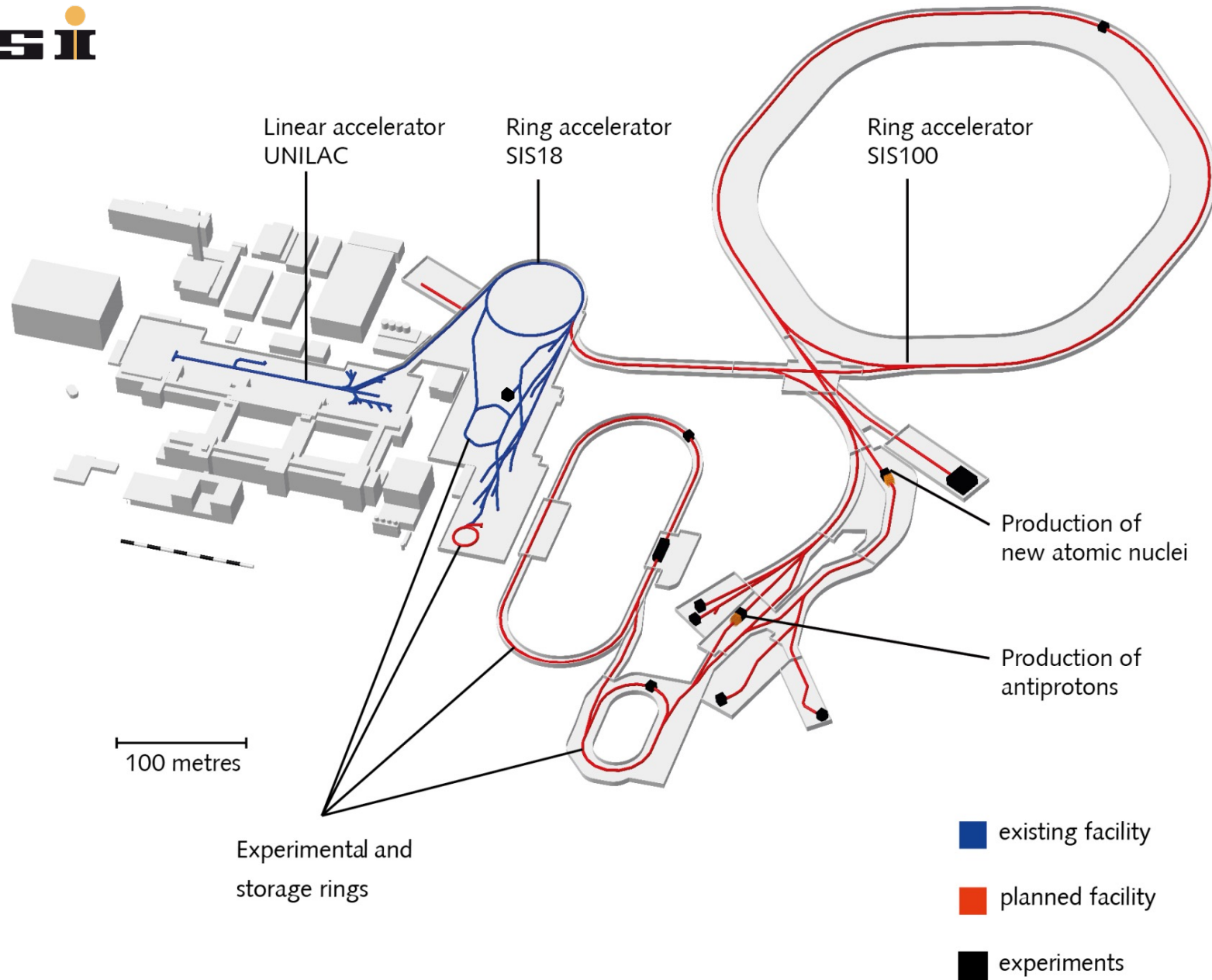
B, Hu, J Halt et al.



# Part 3

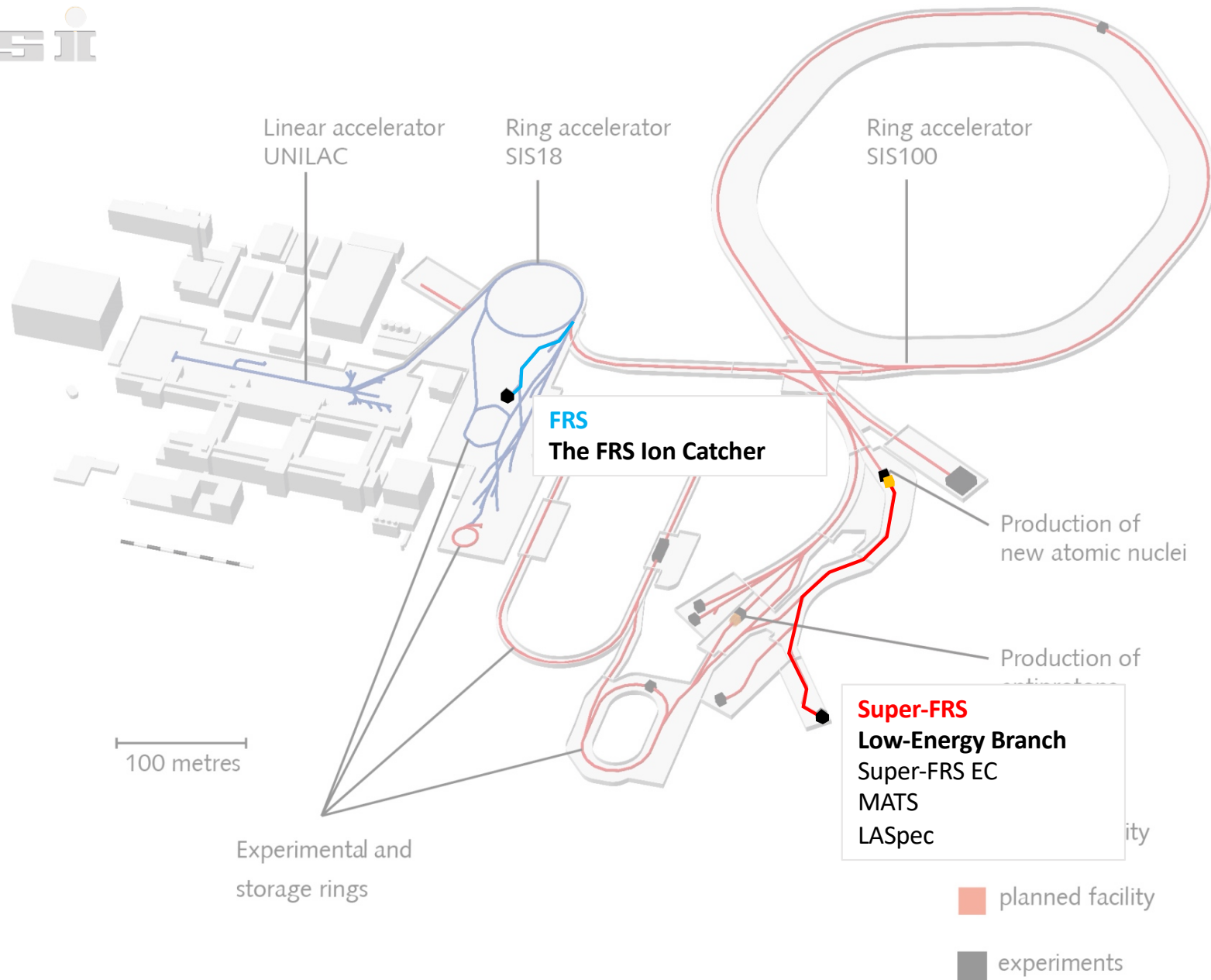
Mass measurements with  
the MR-TOF MS at  
FRS/FAIR after Ion-  
Catcher

# The FRS Ion Catcher at GSI/FAIR

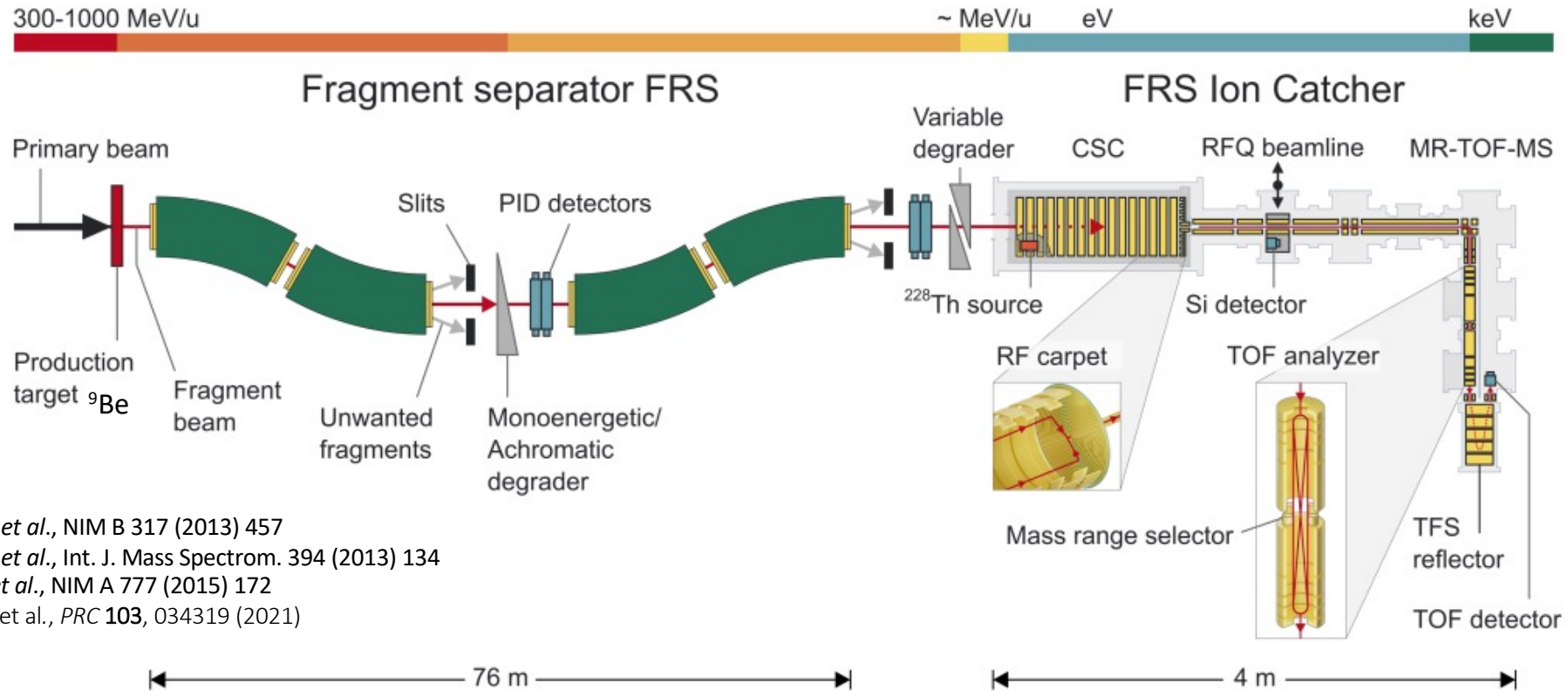




# The FRS Ion Catcher at GSI/FAIR



# The FRS Ion Catcher at GSI



W.R. Plaß *et al.*, NIM B 317 (2013) 457  
 W.R. Plaß *et al.*, Int. J. Mass Spectrom. 394 (2013) 134  
 T. Dickel *et al.*, NIM A 777 (2015) 172  
 I. Mardor *et al.*, PRC 103, 034319 (2021)

## ❖ Fragment separator FRS:

- Production & separation & PID of exotic nuclei via projectile fragmentation/fission

## ❖ Cryogenic Stopping cell (CSC):

- universal, fast, efficient stopping and extraction of cooled short-lived ( $T_{1/2} \sim \text{ms}$ ) exotic nuclei

## ❖ RF Quadrupole beamline:

- for low-energy ion transport
- Operate as a mass filter
- Background Suppression (molecular and ions)

## ❖ MR-TOF-MS

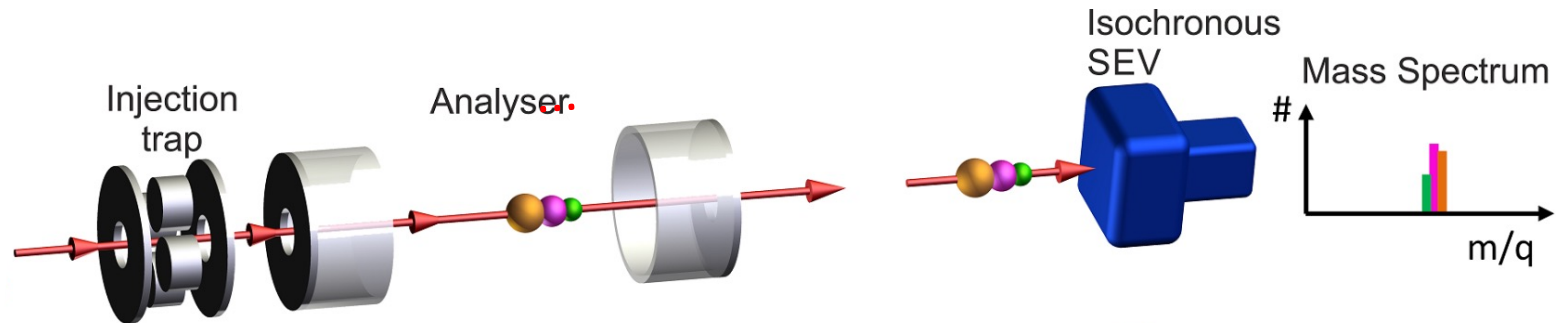
fast, sensitive, broadband and non-scanning

- Resolving power: up to 1,000,000
- resolve isomers (hundreds of keV)
- Best mass accuracy:  $1.7 \times 10^{-8}$
- Sensitivity: a few detected ions
- Rate capacity:  $10^6$  ions/s
- Cycle times: a few ms

# Concept: MR-TOF-MS

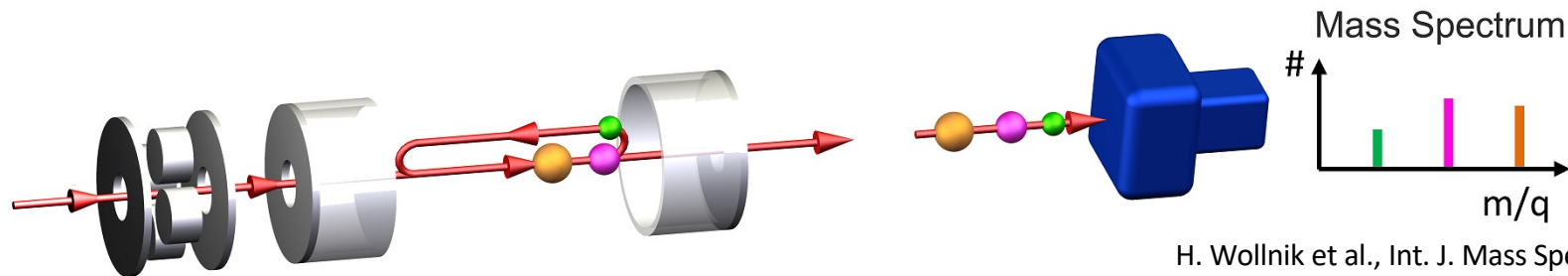
## Enables high performance

- Fast  $\rightarrow$  access to very short-lived ions ( $T_{1/2} \sim \text{ms}$ )
- Sensitive, broadband, non-scanning  $\rightarrow$  efficient, access to rare ions



To achieve high mass resolving power and accuracy:

## Multiple-reflection time-of-flight mass spectrometer (MR-TOF-MS)



H. Wollnik et al., Int. J. Mass Spectrom. Ion Processes 96 (1990) 267

## Applications

- Diagnostics measurements: monitor production, separation and low-energy beam preparation of exotic nuclei
- Direct mass measurements of exotic nuclei
- High-resolution mass separator

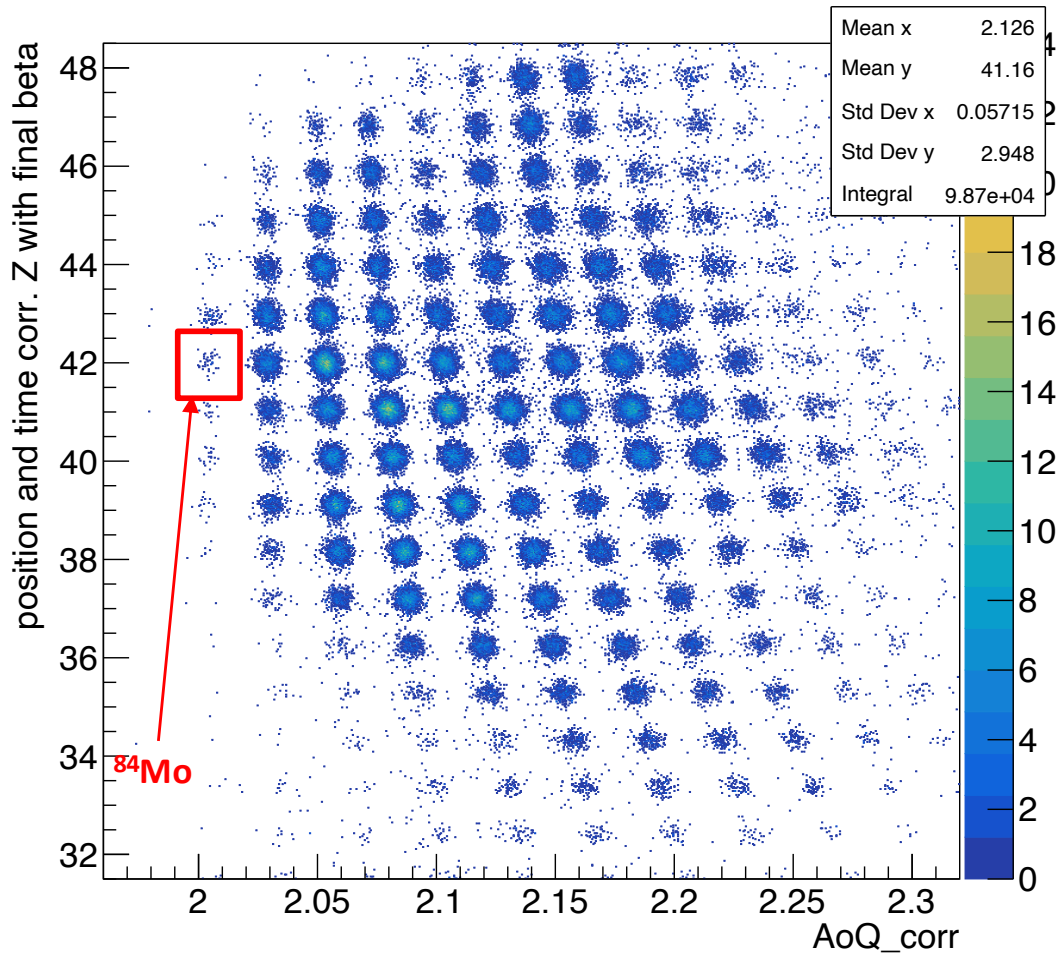
W.R. Plaß et al., Int. J. Mass Spectrom. 394 (2013) 134

C. Scheidenberger et al., Hyperfine Interact. 132 (2001) 531

W.R. Plaß et al., NIM B 266 (2008) 4560

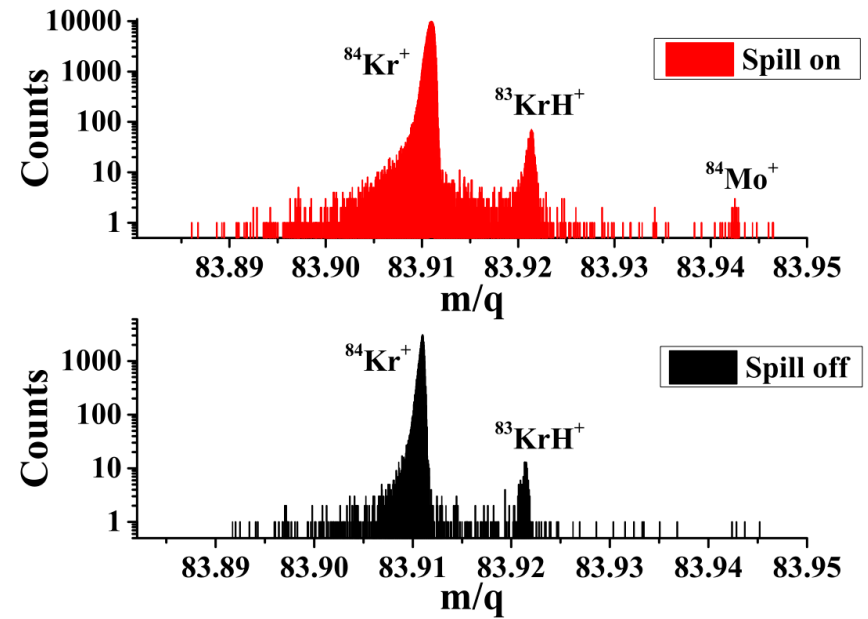
# Partical identification

ID\_Zbctcorr\_finalAoQ



AqQ-vs-Z spectrum

Z. Ge , in preparation



TOF spectrum

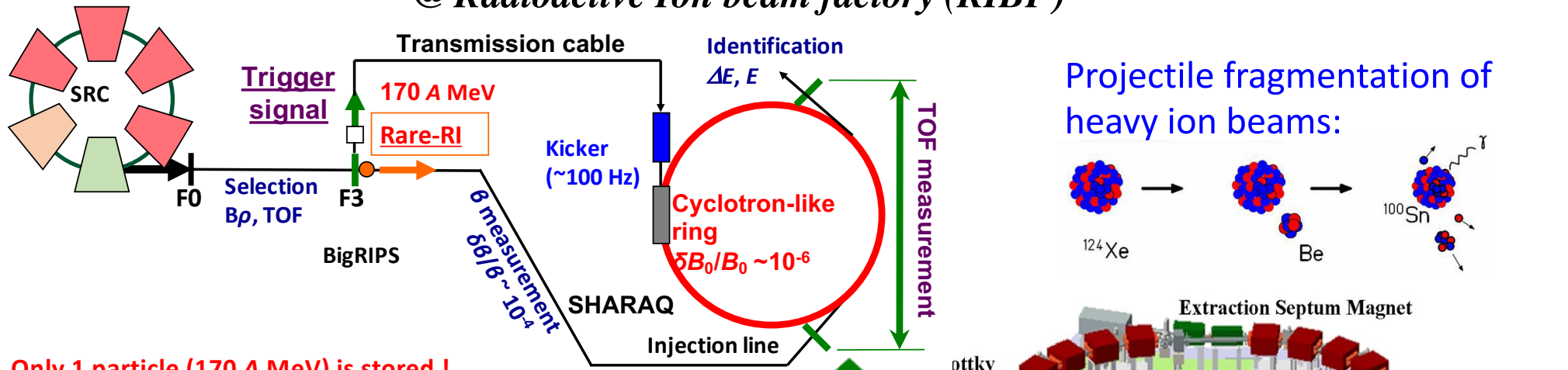
# Part 4

Mass measurements  
with the Rare-RI  
Ring at RIBF



# Scheme for Mass Measurement and location of Rare-RI Ring (R3)

@ Radioactive Ion beam factory (RIBF)



Only 1 particle (170 A MeV) is stored !

## Isochronous mass spectrometry

- Isochronous field  $\sim 10^{-6}$
- Beam-triggered individual injection

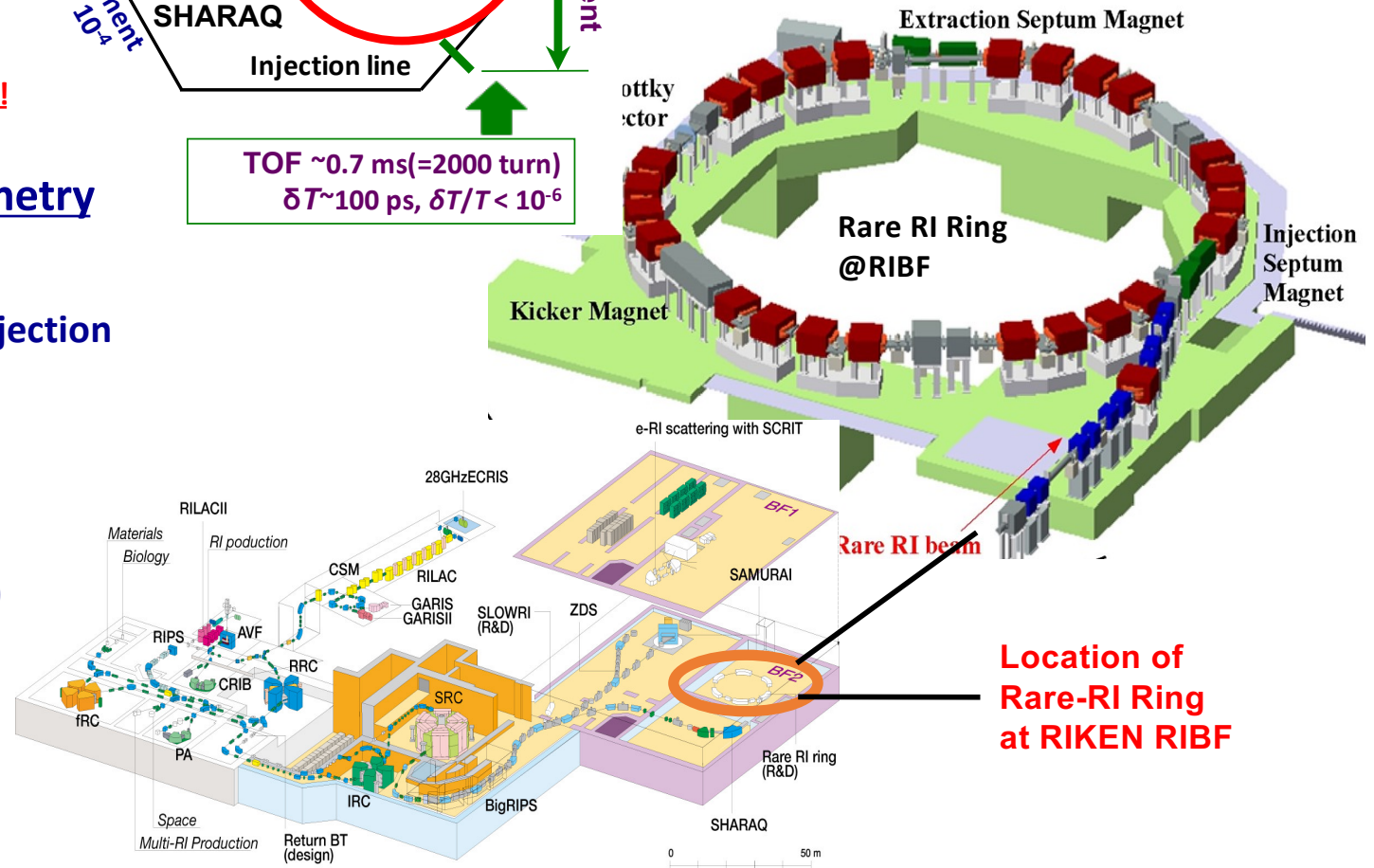


Short measurement time ( $< 1$  ms)

Good resolution ( $\sim 10^{-6}$ )

High efficiency ( $\sim 100\%$ )

TOF  $\sim 0.7$  ms (=2000 turn)  
 $\delta T \sim 100$  ps,  $\delta T/T < 10^{-6}$



# Detectors at beam-line

- Standard beam-line detectors at BigRIPS for TOF,  $B\rho$ ,  $\Delta E$  measurement for PID
- Clover-type Ge detectors for isomer measurement



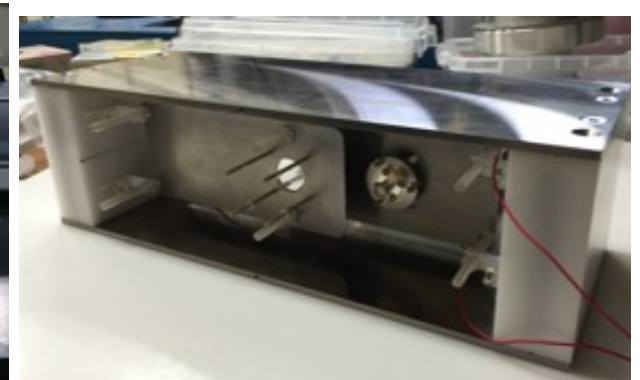
(1). Delay-line PPAC



(2). Plastic Scintillator



(3). Ionization Chamber



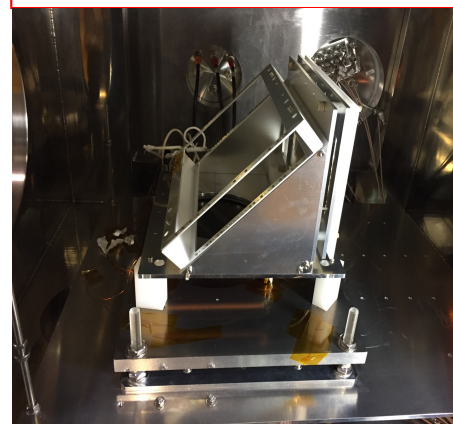
(4). BE-MCP



(5).  $\gamma$ -ray (Ge) detector



(6). Si detector



(7). E-MCP

## Function of detectors:

$\Delta E$ :

IC, Si

Isomer  $\gamma$ -ray:

Clover-Ge

TOF:

Scintillator, E-MCP,  
BE-MCP

Position:

DL-PPAC, CD-PPAC





# R3: Cyclotron-like Lattice Structure

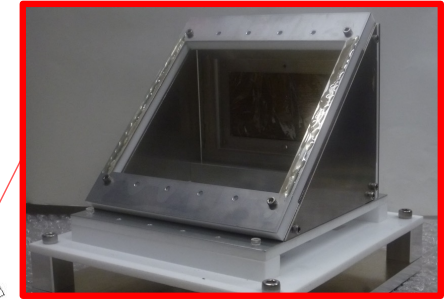
Injection septum magnets

(Start)

Injection beam line



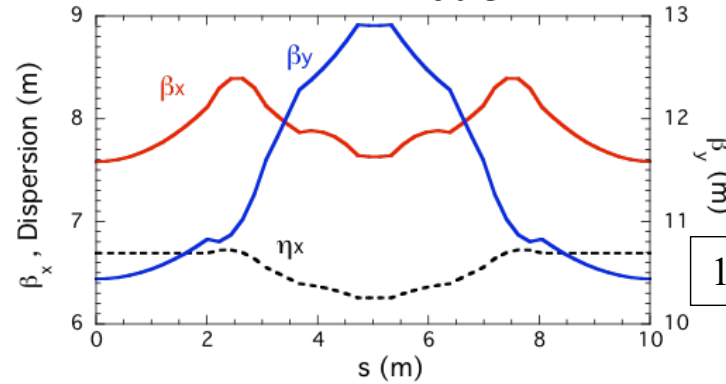
Sector magnets with 10 trim coils



C-Foil timing/2D-MCP detector

Hexagonal-Symmetry  
Weak-Focusing Lattice Structure

Circumference : 60.3m



1/6 Optics

Sector magnets

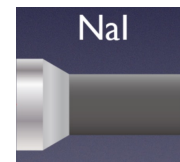
Extraction septum magnets



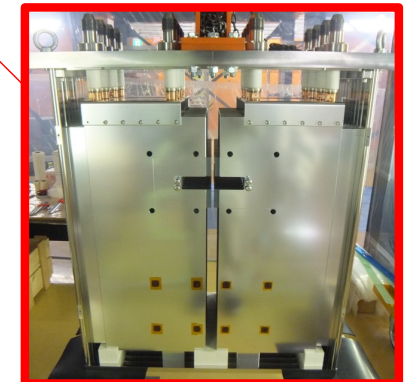
PID: Pla, IC and NaI

(Stop and PID)

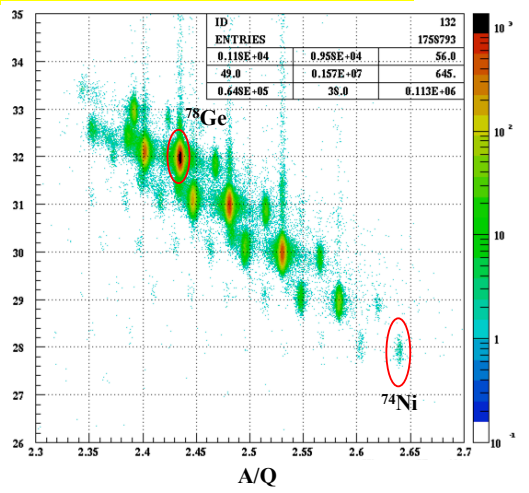
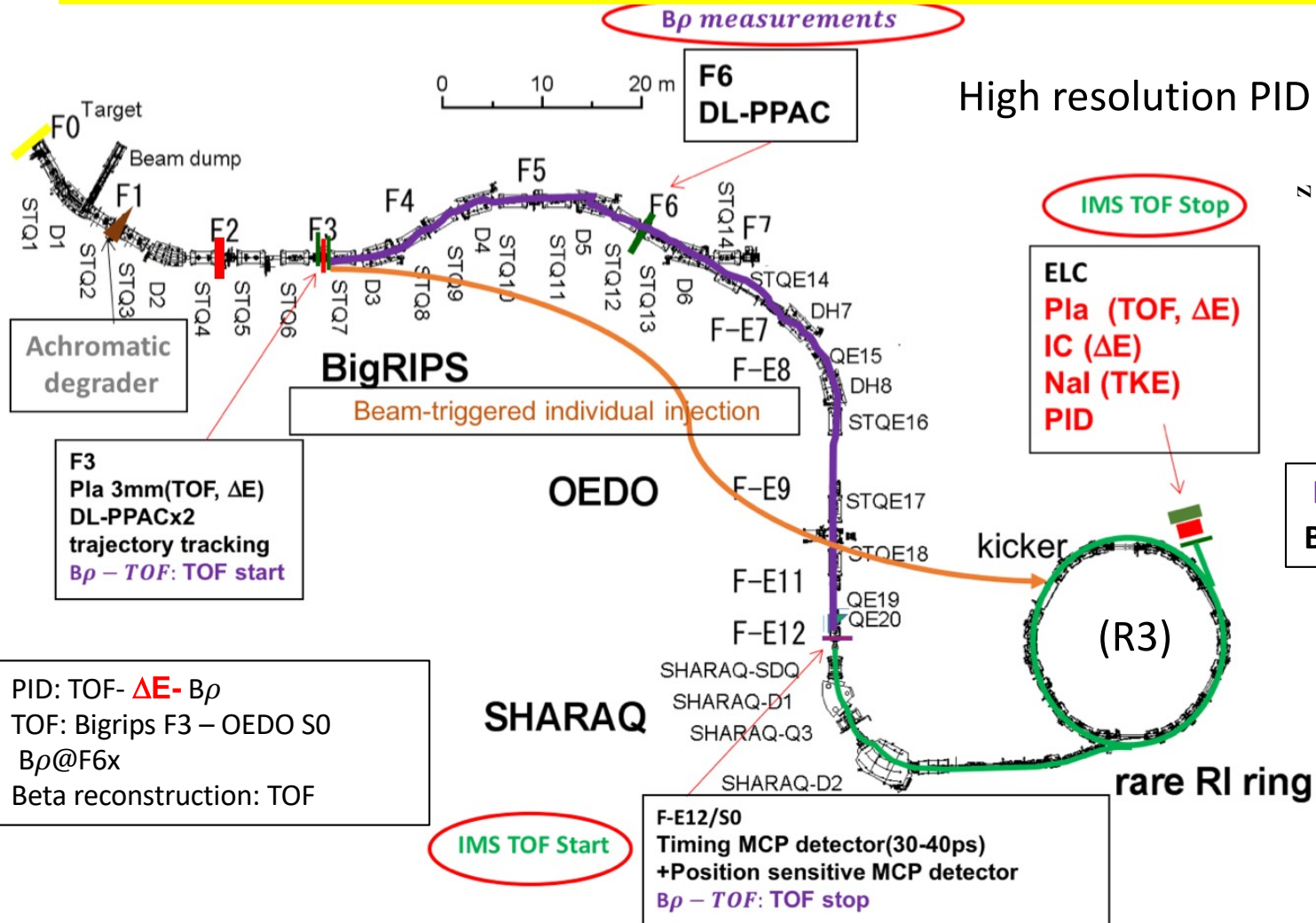
Cavity-type Schottky pickup



Fast-response Kicker magnets



# Setup for Mass measurements by $B\rho - TOF$ & $IMS$ (Isochronous mass spectrometry) @RIKEN



High resolution PID

IMS TOF Stop

- ELC
- Pla (TOF,  $\Delta E$ )
- IC ( $\Delta E$ )
- NaI (TKE)
- PID

$B\rho - TOF$  mass is  
By-product part of  $IMS$  runs

- F3-S0:  
Efficiency 70-90%
- Momentum acceptance  $\pm 0.5\%$
- Rare-RI Ring:  
Efficiency 1%
- Momentum acceptance  $\pm 0.3\%$

PID: TOF-  $\Delta E$ -  $B\rho$   
TOF: Bigrips F3 – OEDO S0  
 $B\rho$ @F6x  
Beta reconstruction: TOF

IMS TOF Start

F-E12/S0  
Timing MCP detector(30-40ps)  
+Position sensitive MCP detector  
 $B\rho - TOF$ : TOF stop

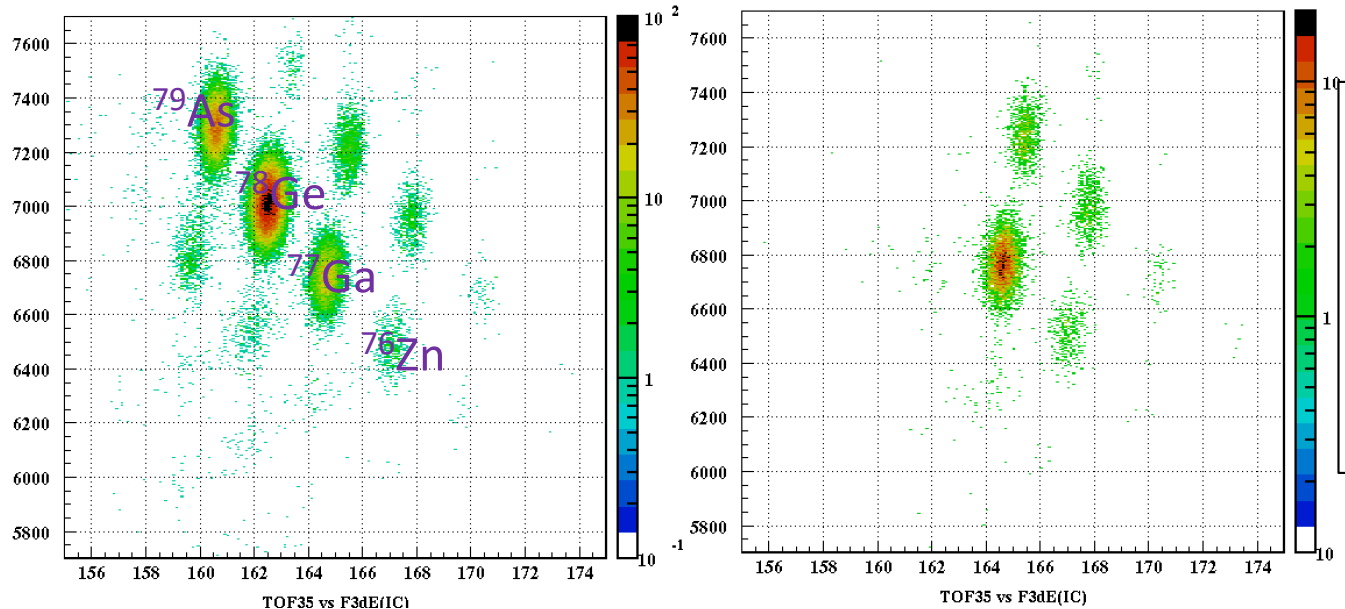
$IMS$  (Isochronous mass spectrometry) method.  
Revolution time Correction by beta/  $B\rho$  measurements:

Mass measurements by  $B\rho - TOF$ , TOF (F3-S0) and  $B\rho$  measurements at F6/F5:

$$\left(\frac{m}{q}\right)_1 = \left(\frac{m}{q}\right)_0 \frac{T_1 \gamma_0}{T_0 \gamma_1} = \left(\frac{m}{q}\right)_0 \frac{T_1}{T_0} \sqrt{\frac{1 - \beta_1^2}{1 - \left(\frac{T_1}{T_0} \beta_1\right)^2}}$$

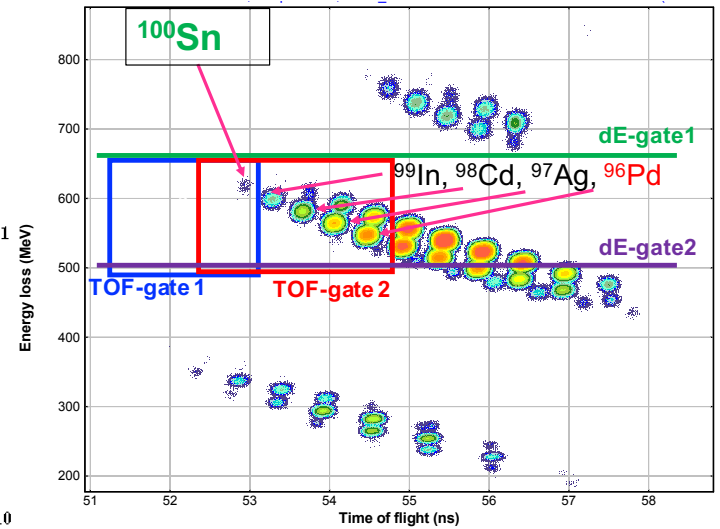
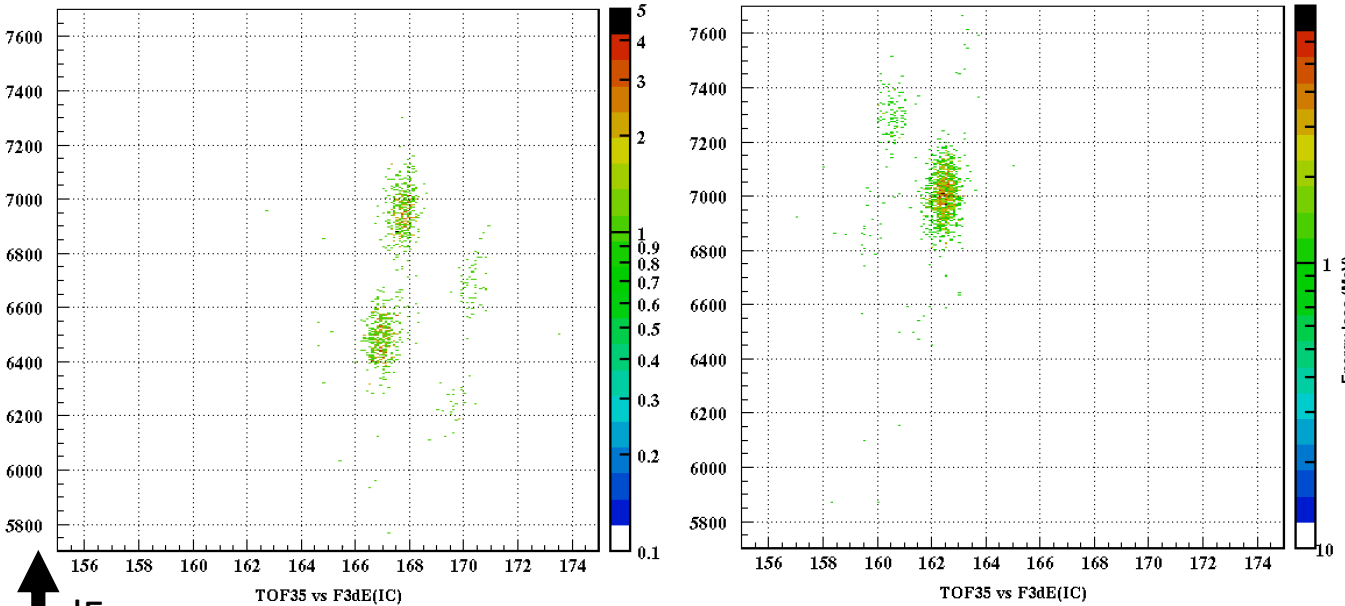
$$\frac{m_0}{q} = \frac{B\rho}{\gamma L/t} = B\rho \sqrt{\left(\frac{t}{L}\right)^2 - \left(\frac{1}{c}\right)^2}$$

# dE-TOF gate Selection method

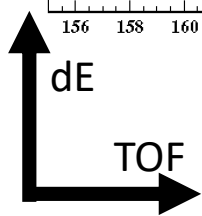


Setting TOF-gate1 and TOF-gate2 rates ratio to be 9:1

The two TOF gates set in 'or' logic (for example, 'N=Z and more exotic area' for TOF-gate 1 in 90 Hz and additional reference in TOF-gate 2 to be 10 Hz)



**Ion species of interest are selected as triggering ions for injection to R3**



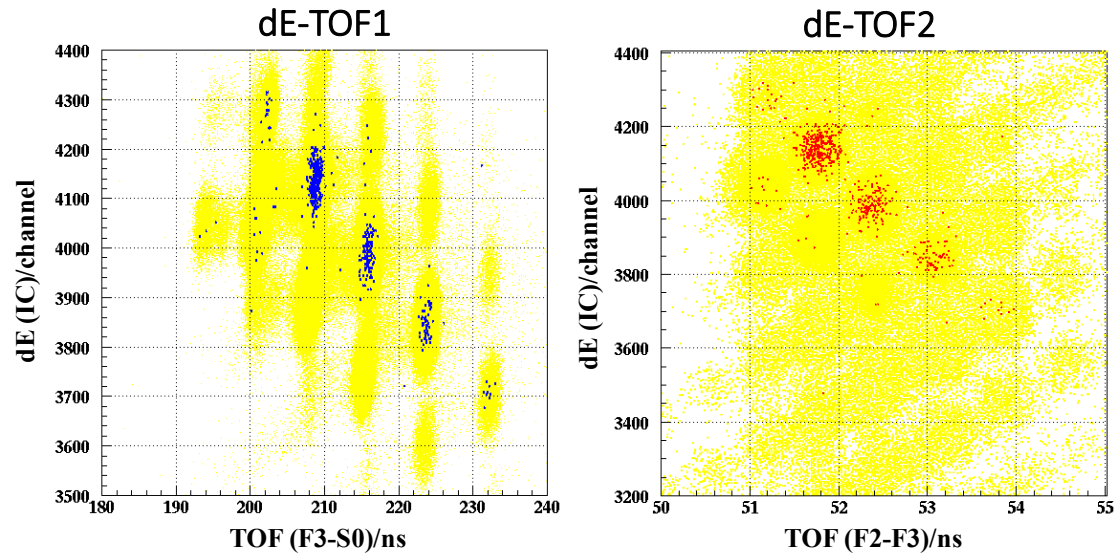


# Event-by-event PID with TOF(beamline)-B $\rho$ -dE-E-TOF(in-Ring)

Zhuang Ge, Tomohiro Uesaka et al., Hyperfine Interact (2019) 240: 92

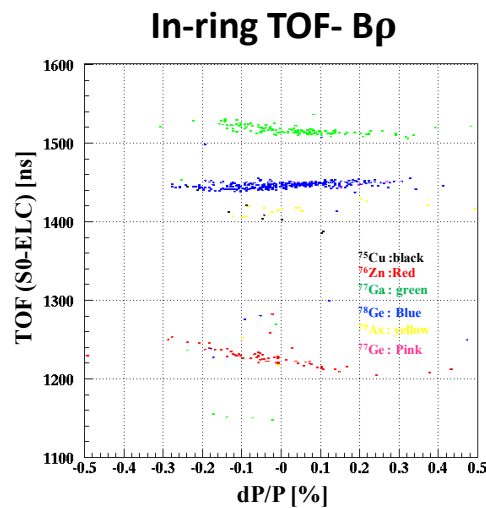
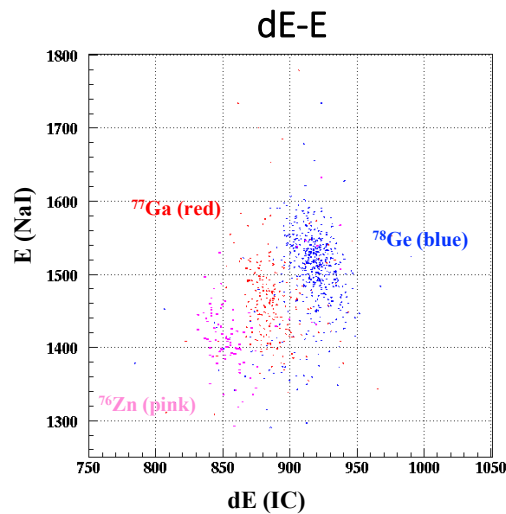
## Unambiguously identification with single ion sensitivity

TOF: beamline (F2-F3 and F3-S0), dE: beamline IC



Yellow: all ions detected at S0  
Blue: extracted from R3

Yellow: all ions detected at F3  
Blue: extracted from R3



dE: IC, E: ring-extraction NaI

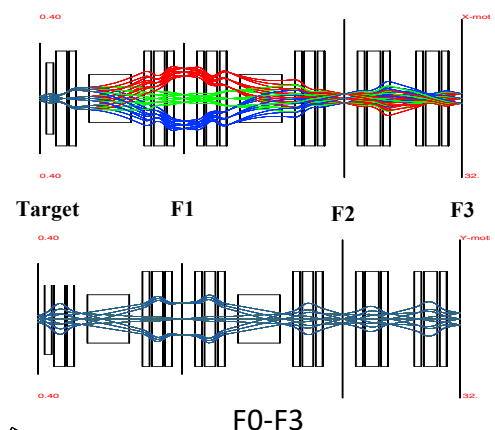
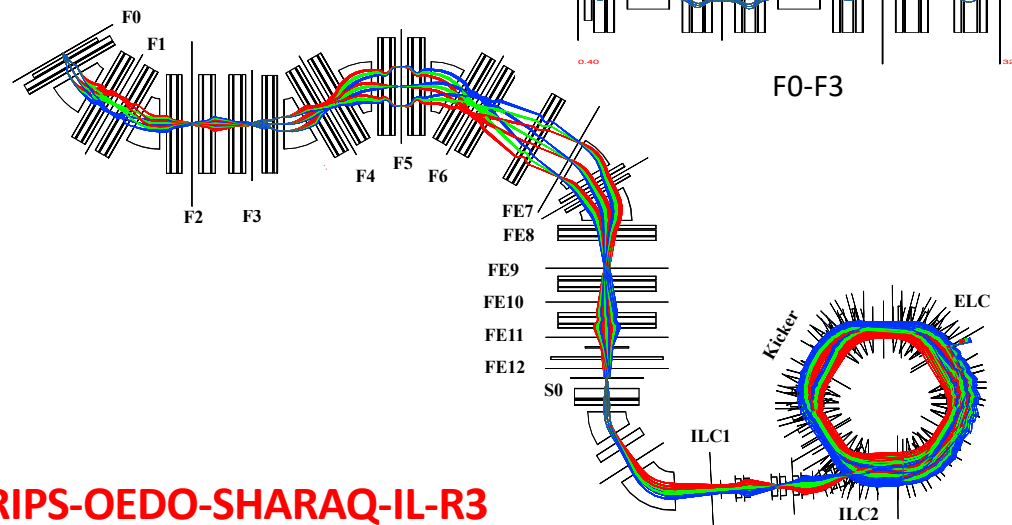
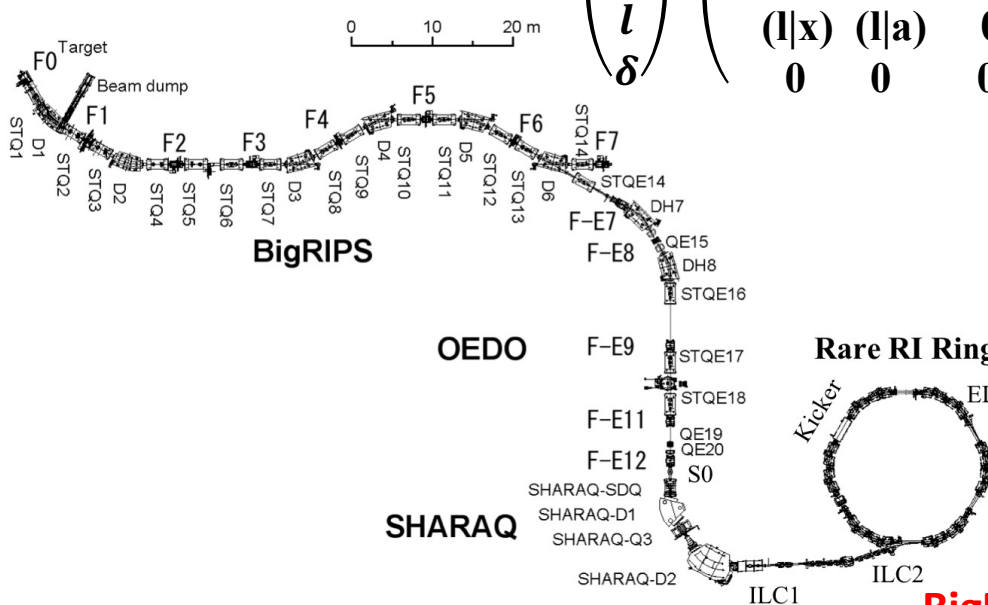
B $\rho$ : beamline, TOF: in ring

# Ion optics design (beam-line and storage ring)

	(x x)	(x a)	(a x)	(a a)	(y y)	(y b)	(b y)	(b b)	(x dp)	(a dp)	(l dp)	L dEk
<b>F3F4</b>	-0.966	0	0	-1.03	-3.88	0	-0.04	-0.26	-1.86	-1.89	4.04	2.187439
<b>F3F5</b>	-0.01	-9.6	0.1	0	1.298	0	-0.06	0.77	0.108	0.505	8.81	4.771546
<b>F3F6</b>	0.965	0	0	1.036	-3.88	0	0	-0.257	<b>7.54</b>	0.368	11.62	6.296793
<b>F3FE7</b>	-0.394	9.7	-0.1	0.016	1.17	-2.386	0.438	-0.039	0.316	-0.803	17.21	9.323857
<b>F3FE9</b>	-0.854	0	-0.14	-0.527	2.67	0	-0.55	0.373	0	0.297	26.94	14.59592
<b>F3S0</b>	2.18	0	0.58	0.46	-2.27	0	0	-0.44	0	0.258	36.09	19.54942
<b>F3ILC1</b>	1.38	-0.58	1.87	-0.06	3.34	0.02	0.76	0.304	-4.15	0.66	44.26	23.98
<b>F3ILC2</b>	-6.18	0	0.83	-0.16	-2.6	0.48	0.476	-0.465	-5.78	-0.66	54.08	29.2974
<b>F3KC</b>	-9.1	1.04	-0.3	-0.07	-2.53	3.71	-0.42	0.22	-7	0	58.43	31.65375

Transfer matrix :

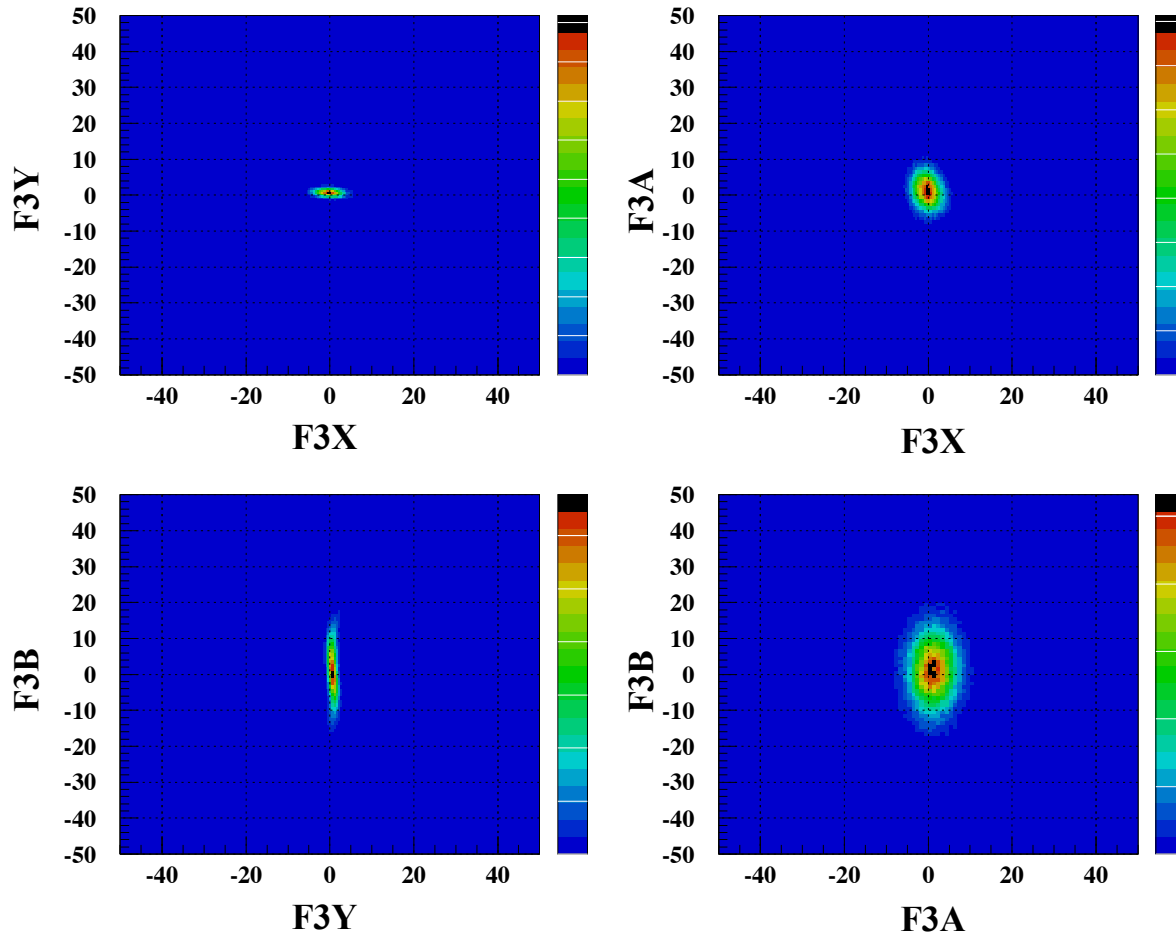
$$\begin{pmatrix} x \\ a \\ y \\ b \\ l \\ \delta \end{pmatrix} = \begin{pmatrix} (x|x) & (x|a) & 0 & 0 & 0 & (x|\delta) \\ (a|x) & (a|a) & 0 & 0 & 0 & (a|\delta) \\ 0 & 0 & (y|y) & (y|b) & 0 & 0 \\ 0 & 0 & (b|y) & (b|b) & 0 & 0 \\ (l|x) & (l|a) & 0 & 0 & 1 & (l|\delta) \\ 0 & 0 & 0 & 0 & 0 & 1 \end{pmatrix} = \begin{pmatrix} x_0 \\ a_0 \\ y_0 \\ b_0 \\ l_0 \\ \delta_0 \end{pmatrix}$$



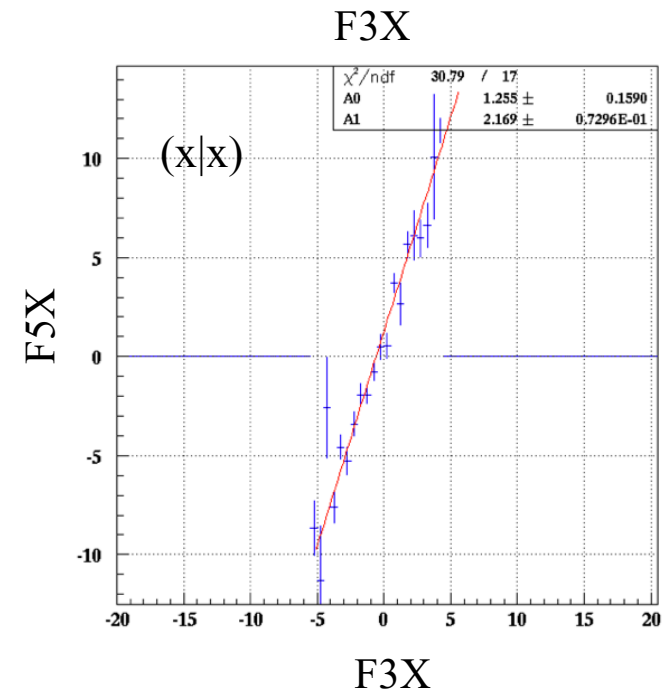
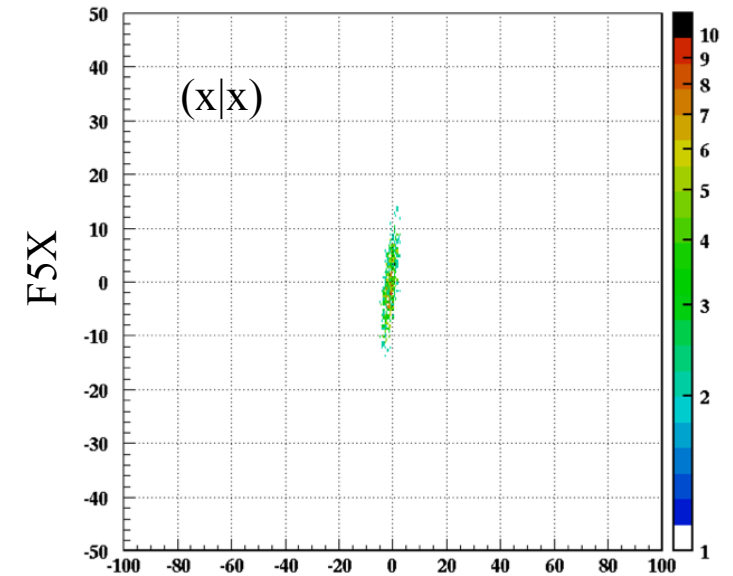
**BigRIPS-OEDO-SHARAQ-IL-R3**

# Optical matrix element reconstruction

## Emittance



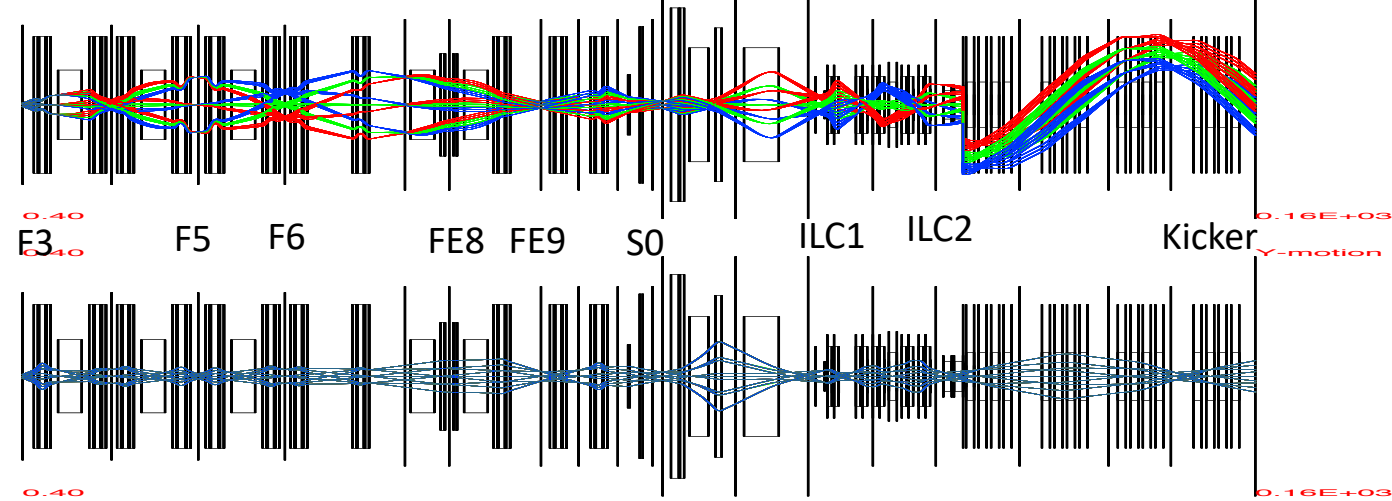
## F3-F5 (X|X) measurement



PPACs: position and angle

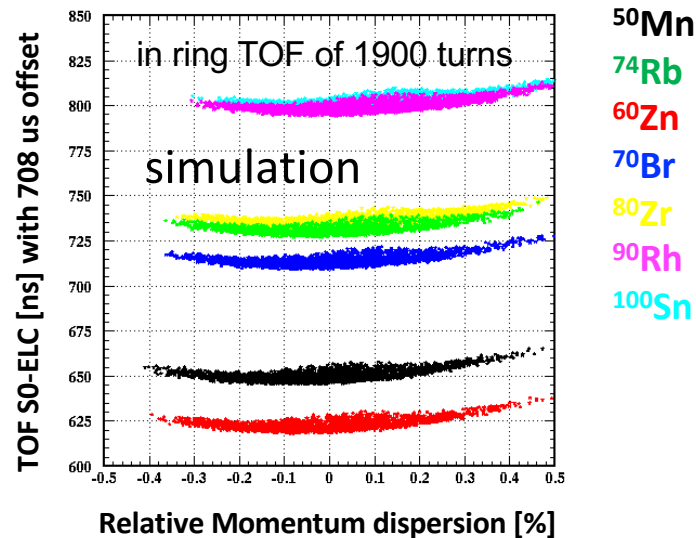
# Optics design with high momentum resolving power and ion transportation simulation

high-resolution achromatic (HA) mode: **Momentum resolving power  $R \sim 7800$**

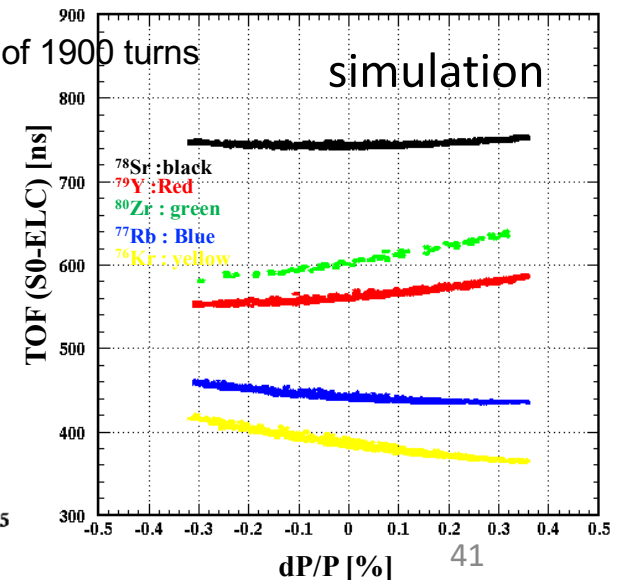
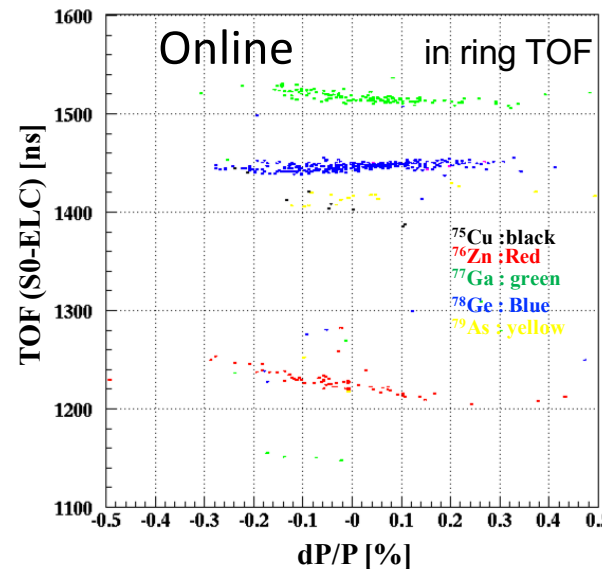


Zhuang Ge et al., Nuclear Physics Review, 2019, 36(3): 294-304 (2019)

## Advantage of N=Z nuclei for in-ring IMS



N=Z simulation (Z=25-50): all nuclei in isochronous  
In a same setting from F3 to R3, all with high resolving power

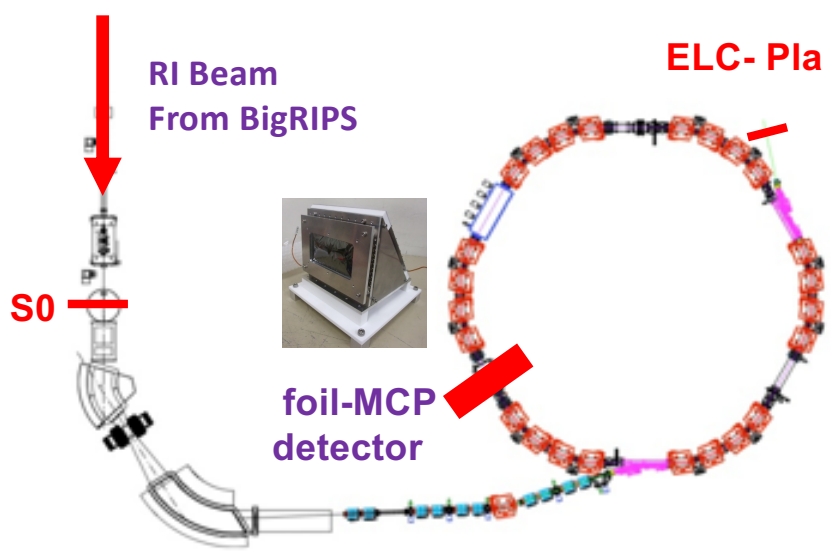


# Revolution time determination

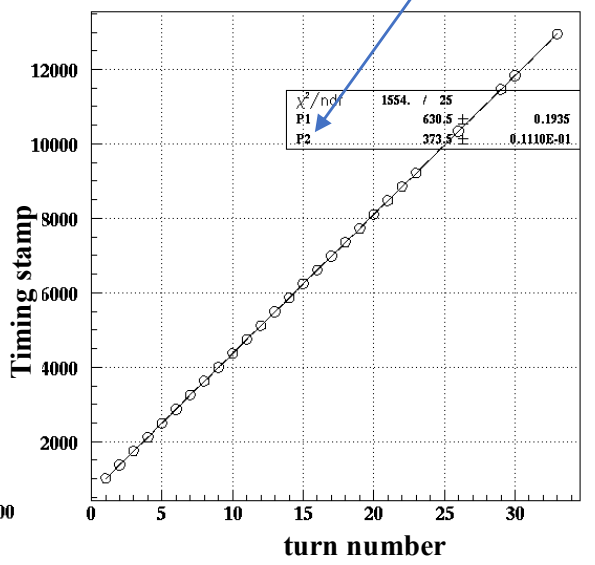
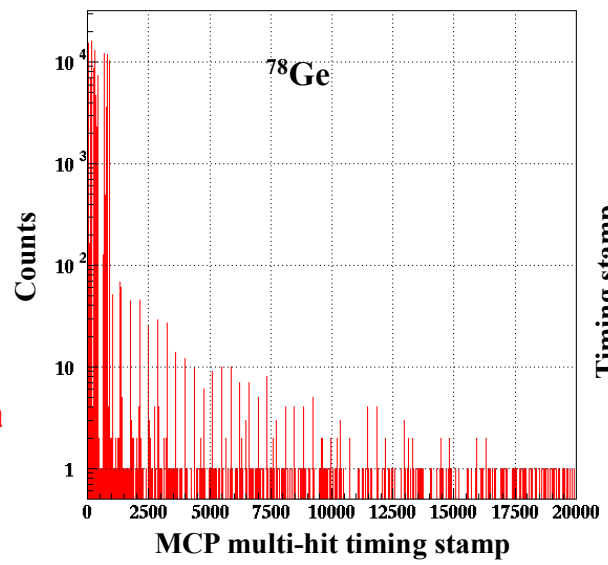
Circulation of turn number for each ion can be calculated from the Total TOF(S0->ELC) subtract the double kicker TOF over the MCP measured evolution time

$$N = \frac{TOF_{(S0 \rightarrow ELC)}^{total} - TOF_{(S0 \rightarrow ELC)}^{doublekicker}}{T}$$

To remove the non-isochronous TOF from S0 to kicker center and kicker center to ELC



Multi-hit *time stamp*:  $t = P2 * N + P1$   
 Revolution time:  $T = P2$

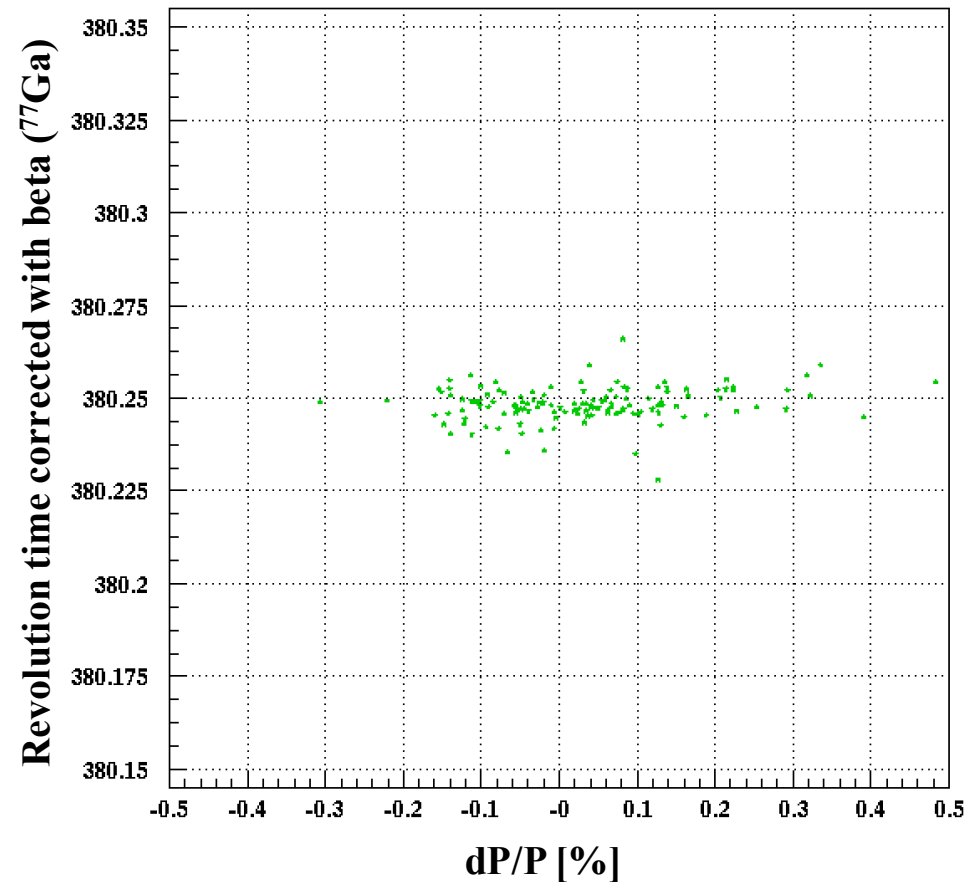
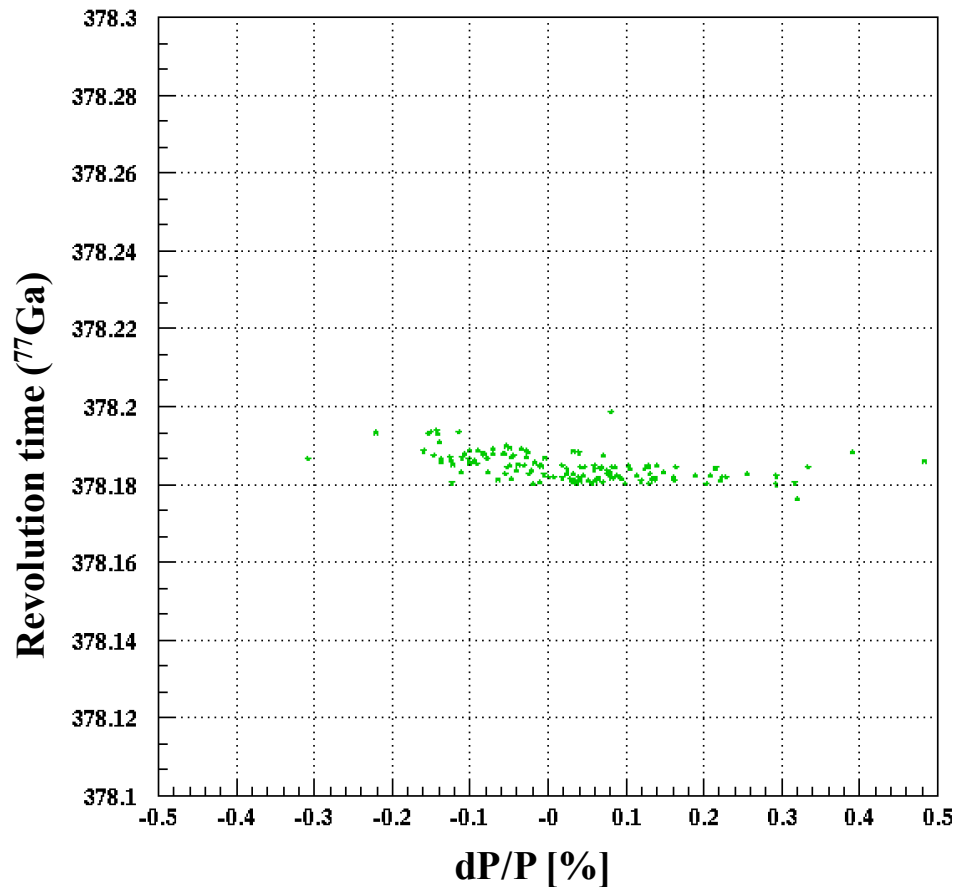


other particle's revolution time can be deduced from the relationship (assuming passing the same orbit):

$$\beta_0 T_0 = \beta_1 T_1$$



# Mass measurements by IMS method



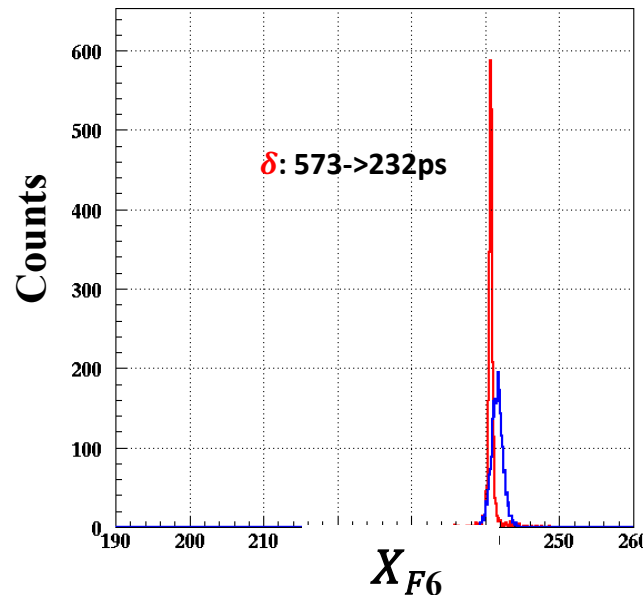
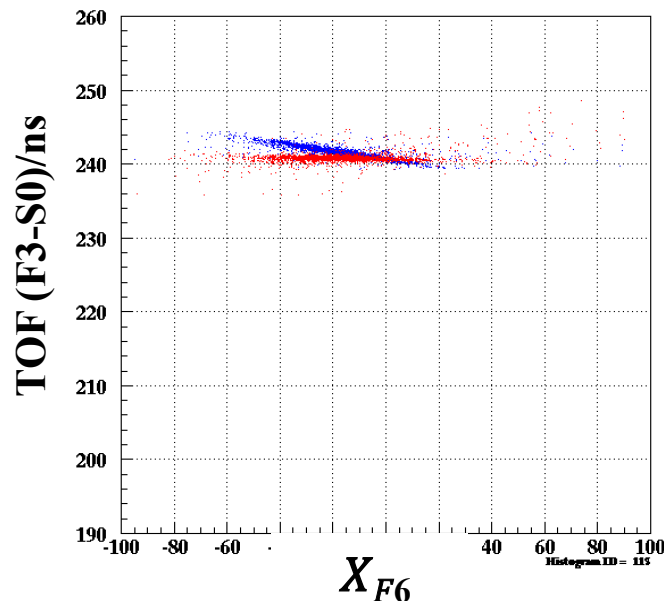
$$\left(\frac{m}{q}\right)_1 = \left(\frac{m}{q}\right)_0 \frac{T_1}{T_0} \frac{\gamma_0}{\gamma_1} = \left(\frac{m}{q}\right)_0 \frac{T_1}{T_0} \sqrt{\frac{1 - \beta_1^2}{1 - \left(\frac{T_1}{T_0} \beta_1\right)^2}}$$

**Mass accuracy:  $\sim 10^{-6}$**

**Revolution time Correction by velocity measurements,  
Velocity is deduced from TOF (F3-S0):**

# Mass measurements by $B\rho - TOF$ method

TOF determination with magnetic rigidity correction



Mass measurements by  $B\rho - TOF$  method:

$$\frac{m_0}{q} = \frac{B\rho}{\gamma L/t} = B\rho \sqrt{\left(\frac{t}{L}\right)^2 - \left(\frac{1}{c}\right)^2}$$

$$\frac{m_0}{\sigma_{m_0}} = 1 / \sqrt{\frac{\sigma_{(B\rho)}^2}{(B\rho)^2} + \frac{1}{k^2} \left( \frac{\sigma_t^2}{t^2} + \frac{\sigma_L^2}{L^2} \right)}$$

$$k = 1 - (L/(ct))^2$$

$X_{F6}$  : Proportional to momentum of ions

40ps MCP detector:

*Ge, Z.: the Rare-RI Ring Collaboration: RIKEN Accelerator Progress Report 51,152 (2018)*

$$\chi^2 = \sum_{\text{calibrants}} \frac{((m/q)_{\text{lit}} - f(\tau, z))^2}{(\sigma_{\text{lit}})_i^2 + (\sigma_{\text{stat}})_i^2 + \sigma_{\text{sys}}^2}$$

$$(\sigma_{\text{stat}})_i^2 = \left( \frac{\partial f(\tau, z)}{\partial \tau} \right)^2 \times \sigma_i^2(\tau)$$

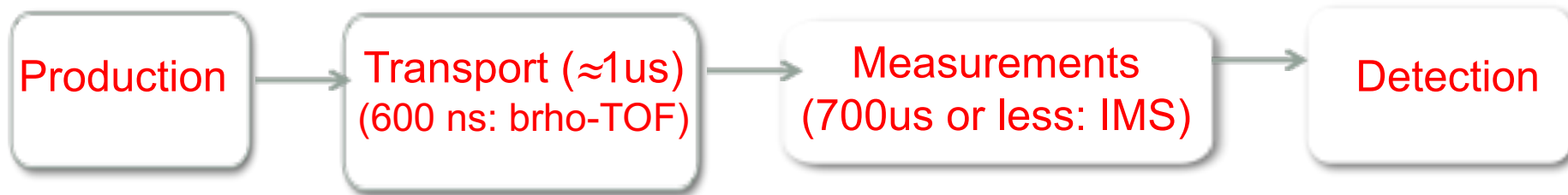
$m/q = f(T, A/Z, Z, A)$  :

Calibration function to deduce mass

Beam-line resolution:  $\sim 2 \times 10^{-4}$

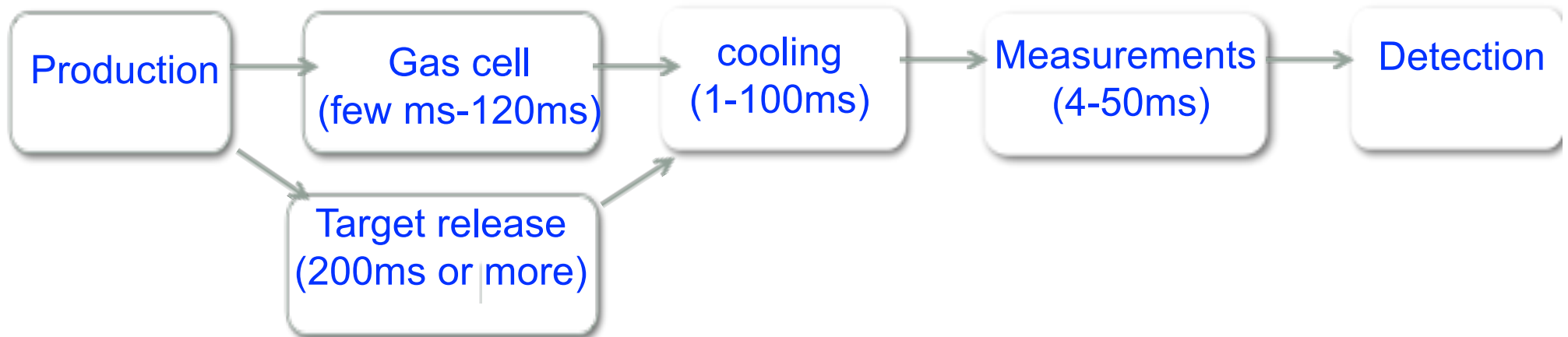
# Low energy beam VS accelerated beam

## BigRIPS&Rare-RI Ring @RIBF



- *background free and single ion sensitivity (event by event PID) of highly charged ions*

## MRTOF/Penning-trap @ In-flight/ISOL- facilities



*ISOL (chemical sensitivity)*

- *Cooled and bunched ion beam with backgrounds of molecules and adduct ions*

# Acknowledgements

## FRS Ion Catcher and IGISOL Collaborations

D. Amanbayev, B. Ashrafkhani, O. Aviv, S. Ayet San Andrés, J. Äystö, S. Bagchi, D. Balabanski, S. Beck, J. Bergmann, A. Blazhev, Z. Brencic, S. Cannarozzo, O. Charviakova, P. Constantin, D. Curien, D. Das, I. Dedes, M. Dehghan, T. Dickel, J. Dobaczewski, J. Dudek, T. Eronen, T. Fowler-Davis, Z. Gao, Z. Ge, H. Geissel, S. Glöckner, M. Górská, T. Grahn, F. Greiner, L. Gröf, M. Gupta, E. Haettner, O. Hall, M. Harakeh, B. S. Hu, C. Hornung, J.-P. Hukka, Y. Ito, A. Jokinen, B. Kaizer, N. Kalantar-Nayestanaki, A. Kankainen, A. Karpov, Y. Kehat, L. Kilmartin, D. Kostyleva, G. Kripkó-Koncz, D. Kumar, A. N. Kuzminchuk, Y. H. Lam, K. Mahajan, I. Mardor, A.A. Mehmandooost-Khajeh-Dad, N. Minkov, A. Mollaebrahimi, D. Morrissey, I. Moore, I. Mukha, G. Münzenberg, T. Murböck, M. Narang, D. Nichita, S. Nikas, D. A. Nesterenko, Z. Patyk, A. Perry, S. Pietri, A. Pikhteleev, W.R. Plaß, Pohjalainen, S. Pomp, S. Purushothaman, M.P. Reiter, M. Reponen, S. Rinta-Antila, H. Rösch, A. Rotaru, C. Scheidenberger, T. Schellhaas, P. Schury, A. Shrayar, S.K. Singh, A. Solders, A. Spataru, A. State, Y. Tanaka, P. Thirolf, N. Tortorelli, E.Vardaci, L. Varga, M. Vencelj, V. Virtanen, M. Wada, M. Wasserheß, H. Weick, M. Wieser, M. Will, H. Wilsenach, O. Yaghi, M.I. Yavor, X. Yang, J. Yu, A. Zadvornaya, J. Zhao



THE UNIVERSITY of EDINBURGH



**Fundings:** Academy of Finland under the Finnish Centre of Excellence Programme 2012-2017 (Nuclear and Accelerator Based Physics Research at JYFL) and projects No. 306980, 312544, 275389, 284516, 295207, 314733, 315179, 327629, 320062 and 345869. The support by the EU Horizon 2020 research and innovation programme under grant No. 771036 (ERC CoG MAIDEN) is acknowledged. This project has received funding from the European Union's Horizon 2020 research and innovation programme under grant agreement No. 861198-LISA-H2020-MSCA-ITN-2019.

**Fundings:** German Federal Ministry for Education and Research (05P19RGFN1, 05P21RGFN1), Hessian Ministry for Science and Art (LOEWE Center HICforFAIR), HGS-HIRe, JLU Giessen and GSI (JLU-GSI strategic Helmholtz partnership agreement), German Research Foundation (SCHE 1969/2-1), Polish National Science Centre (2016/21/B/ST2/01227), European Union's Horizon 2020 research and innovation programme (654002 via the JRA SAT-NURSE), Israel Ministry of Energy (220-11-052), Israel Science Foundation (2575/21), Romanian Government and European Union (ELI-NP Phase II) (European Regional Development Fund – 1/07.07.2016, COP, ID 1334), IAEA (CRP F42007, 24000)





# 招收博士后，联合培养学生

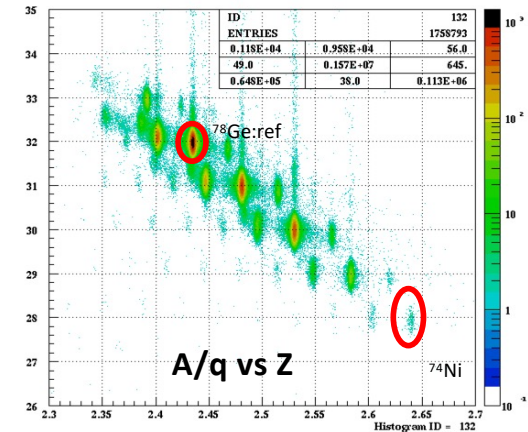
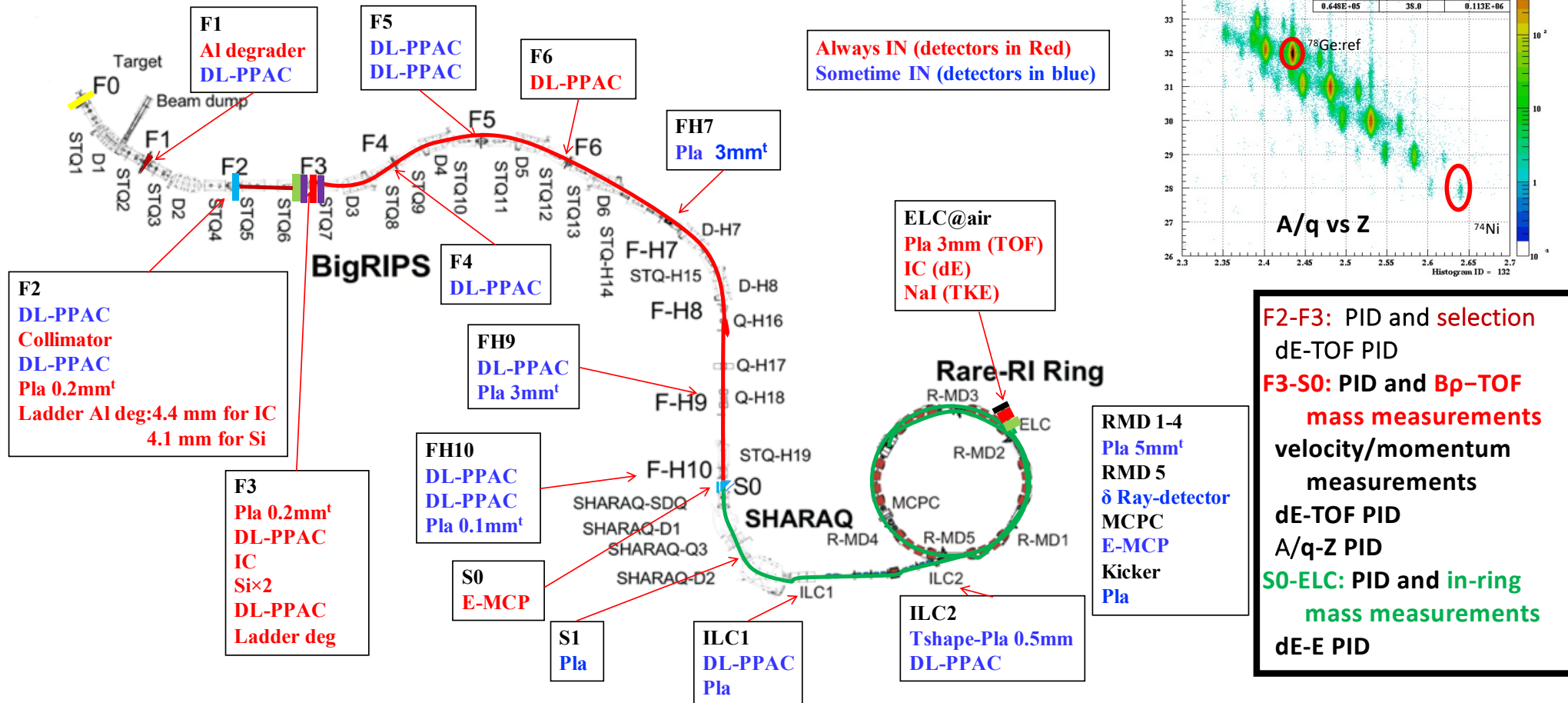
[zhuang.z.ge@jyu.fi](mailto:zhuang.z.ge@jyu.fi); [z.ge@gsi.de](mailto:z.ge@gsi.de) ; [zhuang@ribf.riken.jp](mailto:zhuang@ribf.riken.jp)

*Thank you  
for your attention*

# Experimental setup

In four years' time, to conduct the experiment.

$$B\rho = P/q = mv\gamma/q = A c\mu\gamma\beta/(qe)$$



$$\Delta E \propto E \propto (Z/v)^2$$

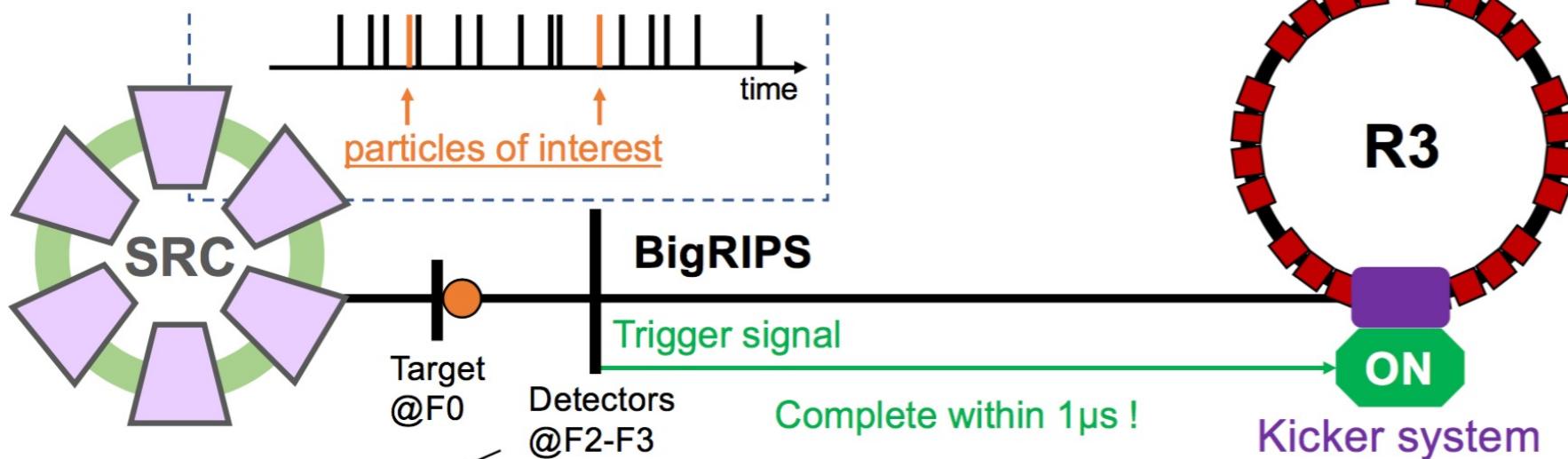
# Self-triggered injection method

Cyclotron



Storage Ring

I. Meshkov  
W. Mittig et. al.,  
NIMA523(2004)262



## Isotope selection

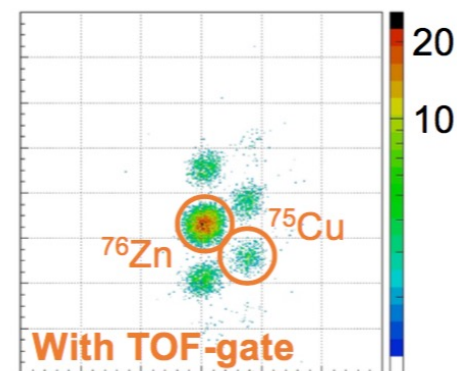
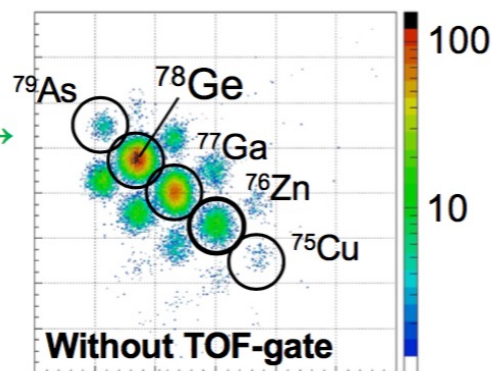
for trigger signal generation using "TOF-gate".

(TOF-gate: veto signal using reference RF-signal)

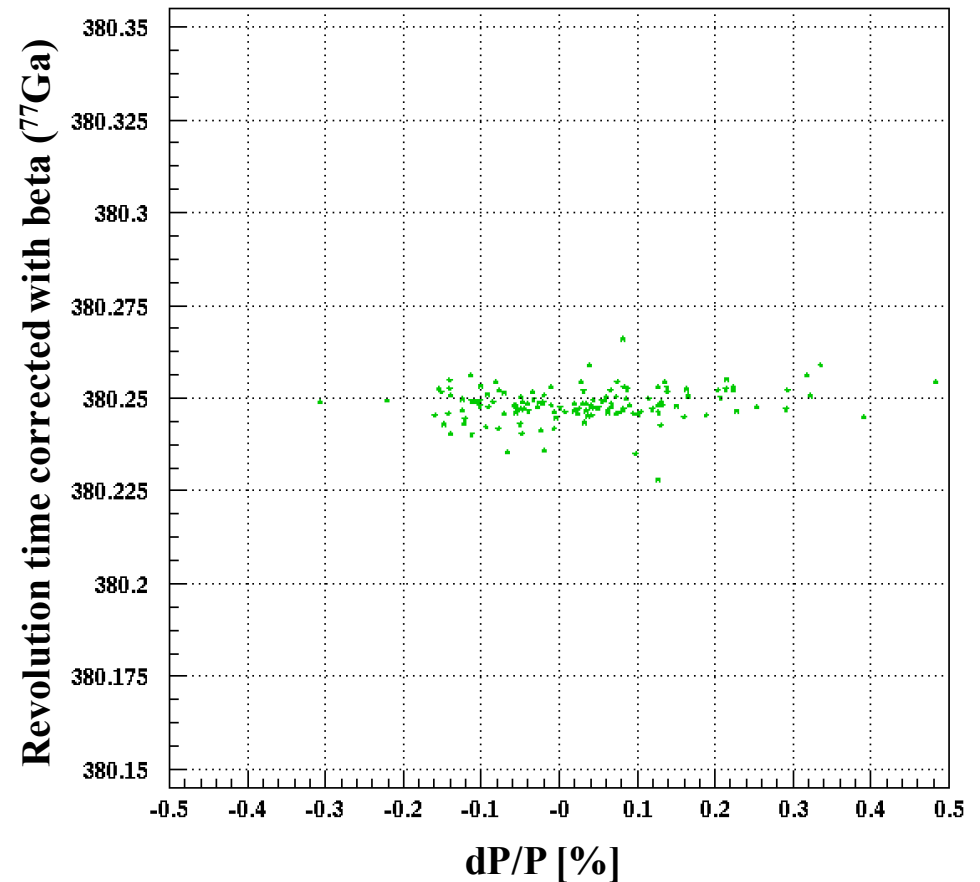
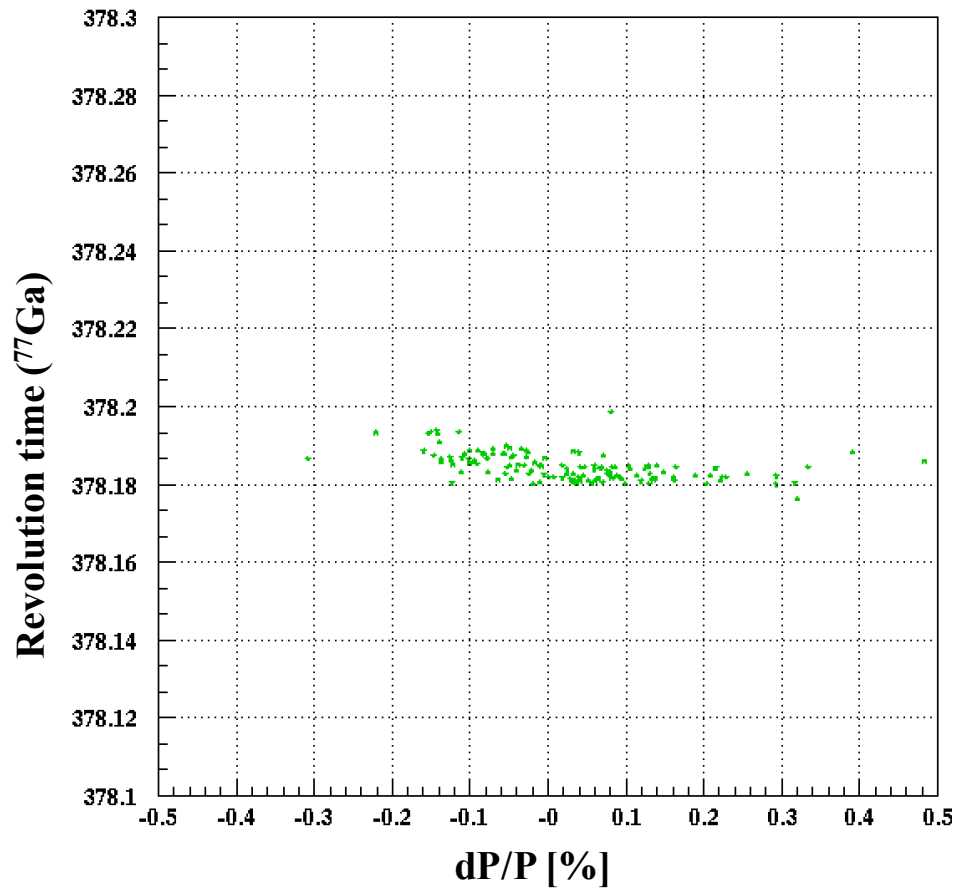
Trigger events  $\rightarrow$

$\Delta E$

TOF(F2-F3)



# Mass measurements by IMS method



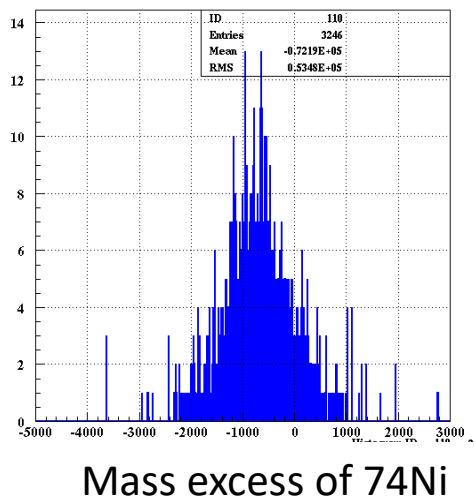
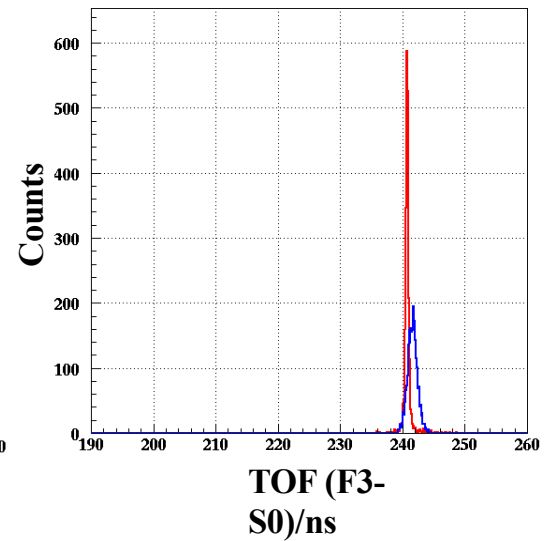
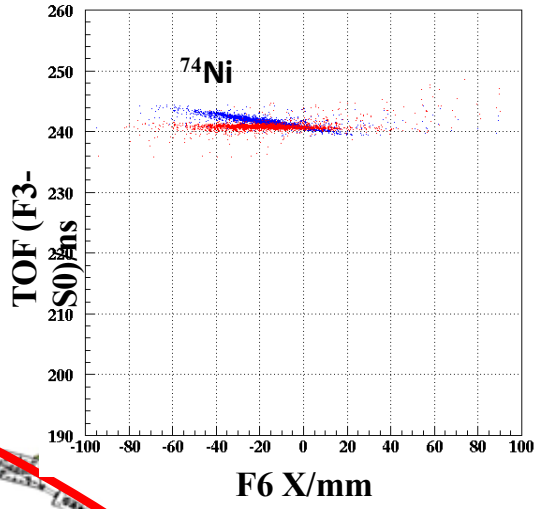
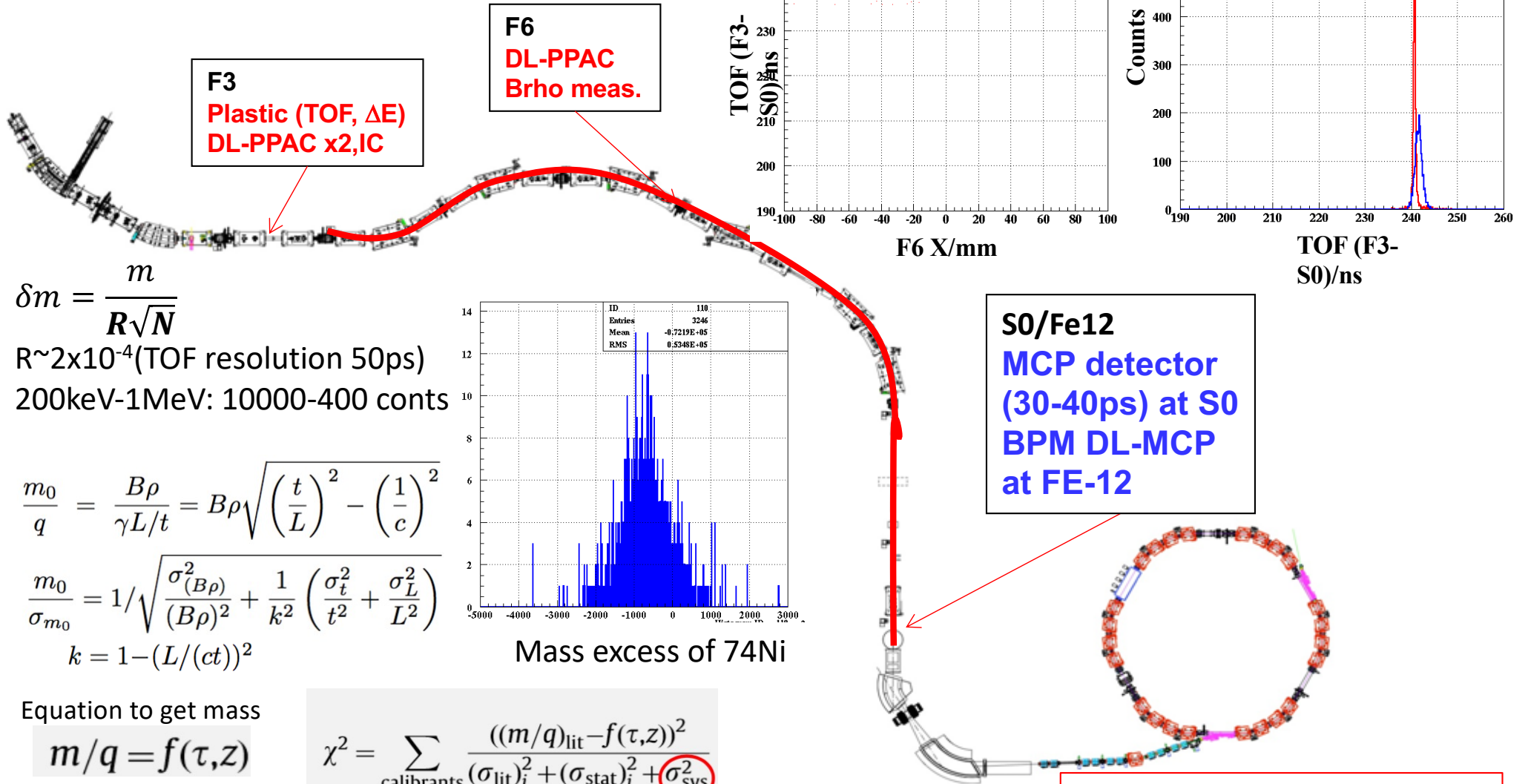
$$\left(\frac{m}{q}\right)_1 = \left(\frac{m}{q}\right)_0 \frac{T_1}{T_0} \frac{\gamma_0}{\gamma_1} = \left(\frac{m}{q}\right)_0 \frac{T_1}{T_0} \sqrt{\frac{1 - \beta_1^2}{1 - \left(\frac{T_1}{T_0} \beta_1\right)^2}}$$

Mass accuracy:  $\sim 10^{-6}$

Revolution time Correction by velocity measurements,  
Velocity is deduced from TOF (F3-S0):

# Brho(@F6 or F5)-TOF (f3-S0) mass measurements

MS03 machine study



$$\delta m = \frac{m}{R\sqrt{N}}$$

$$R \sim 2 \times 10^{-4} \text{ (TOF resolution 50ps)}$$

$$200\text{keV}-1\text{MeV}: 10000-400 \text{ conts}$$

$$\frac{m_0}{q} = \frac{B\rho}{\gamma L/t} = B\rho \sqrt{\left(\frac{t}{L}\right)^2 - \left(\frac{1}{c}\right)^2}$$

$$\frac{m_0}{\sigma_{m_0}} = 1 / \sqrt{\frac{\sigma_{(B\rho)}^2}{(B\rho)^2} + \frac{1}{k^2} \left( \frac{\sigma_t^2}{t^2} + \frac{\sigma_L^2}{L^2} \right)}$$

$$k = 1 - (L/(ct))^2$$

Equation to get mass

$$m/q = f(\tau, z)$$

$$\chi^2 = \sum_{\text{calibrants}} \frac{((m/q)_{\text{lit}} - f(\tau, z))^2}{(\sigma_{\text{lit}})_i^2 + (\sigma_{\text{stat}})_i^2 + \sigma_{\text{sys}}^2}$$

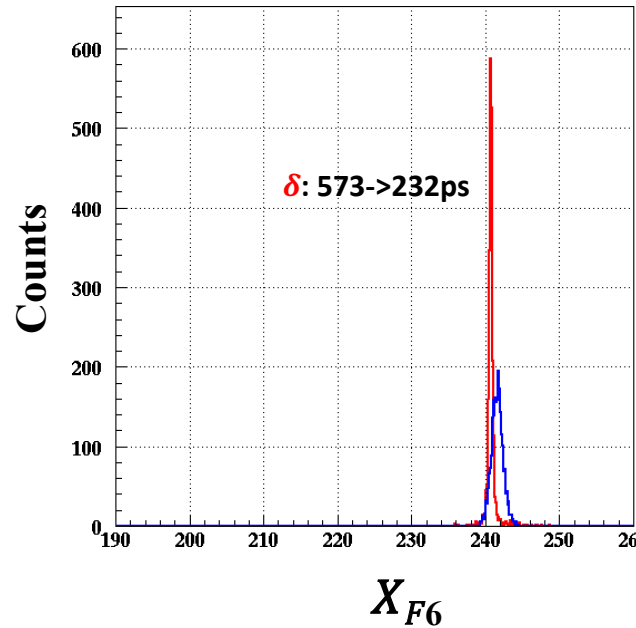
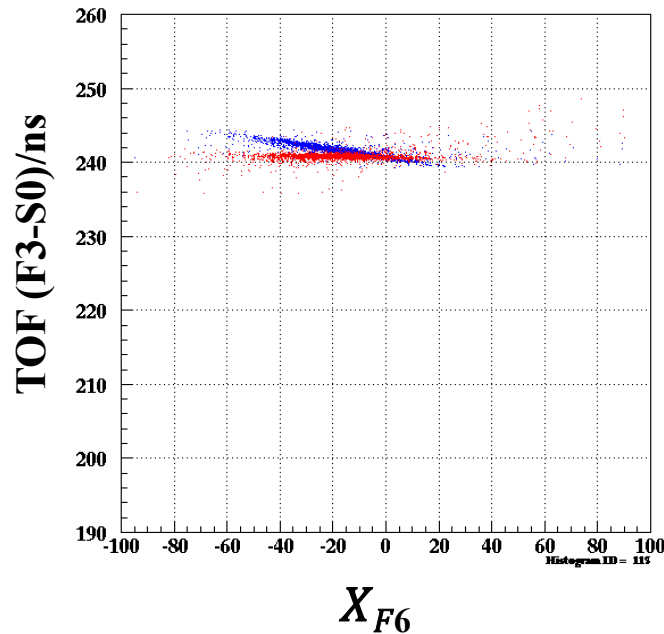
$$(\sigma_{\text{stat}})_i^2 = \left( \frac{\partial f(\tau, z)}{\partial \tau} \right)^2 \times \sigma_i^2(\tau)$$

**S0/Fe12**  
**MCP detector**  
**(30-40ps) at S0**  
**BPM DL-MCP**  
**at FE-12**

Momentum resolving  
 power(MS03):  $\sim 7500/0.9 \sim 8333$   
 $\delta B\rho/B\rho = 0.007\%$



# Mass measurements by $B\rho - TOF$ method



Mass measurements by  $B\rho - TOF$  method:

$$\frac{m_0}{q} = \frac{B\rho}{\gamma L/t} = B\rho \sqrt{\left(\frac{t}{L}\right)^2 - \left(\frac{1}{c}\right)^2}$$

$$\frac{m_0}{\sigma_{m_0}} = 1 / \sqrt{\frac{\sigma_{(B\rho)}^2}{(B\rho)^2} + \frac{1}{k^2} \left( \frac{\sigma_t^2}{t^2} + \frac{\sigma_L^2}{L^2} \right)}$$

$$k = 1 - (L/(ct))^2$$

$X_{F6}$  : Proportional to momentum of ions

TOF determination with magnetic rigidity correction

$$\chi^2 = \sum_{\text{calibrants}} \frac{((m/q)_{\text{lit}} - f(\tau, Z))^2}{(\sigma_{\text{lit}})_i^2 + (\sigma_{\text{stat}})_i^2 + \sigma_{\text{sys}}^2}$$

$$(\sigma_{\text{stat}})_i^2 = \left( \frac{\partial f(\tau, Z)}{\partial \tau} \right)^2 \times \sigma_i^2(\tau)$$

$m/q = f(T, A/Z, Z, A)$  :

Calibration function to deduce mass

Beam-line resolution:  $\sim 2 \times 10^{-4}$