



Nuclear structure/deformation from laser spectroscopy

Xiaofei Yang

SKLNPT, School of Physics, Peking University

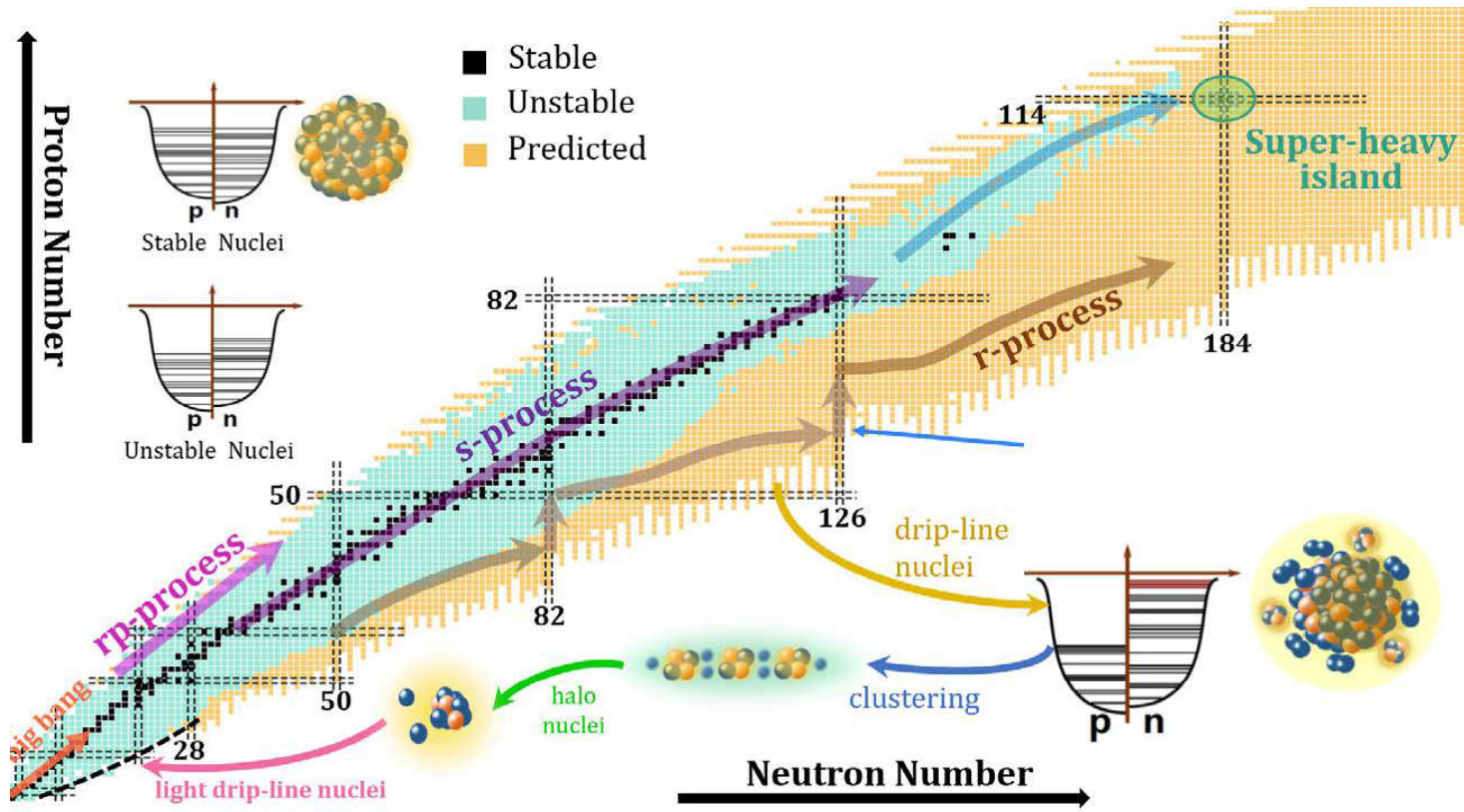
“Exploring Nuclear Physics across Energy Scales”, 15-27 April 2024, Beijing, China

Outline



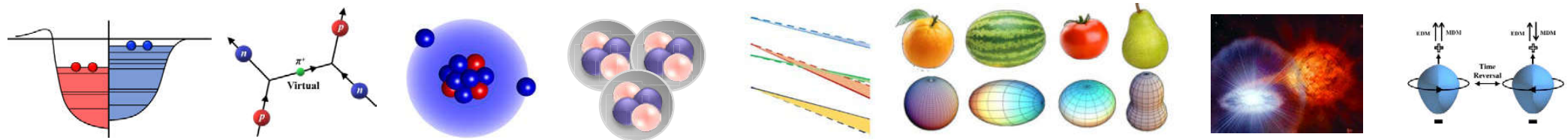
- **Nuclear structure and g.s. properties**
- **Hyperfine interaction and laser spectroscopy**
- **Nuclear structure studied from laser spectroscopy**
- **Laser spectroscopy development and near future work**

Nuclear structure of exotic nuclei



- ❑ Exotic structure
- ❑ Nuclear astrophysics
- ❑ Superheavy element
- ❑ Fundamental symmetry
- ❑ Applications

- Radioactive ion beam
- Experimental probing
- Theoretical development



Nuclear structure of exotic nuclei

K. Heyde, Basic ideas and concepts in nuclear physics

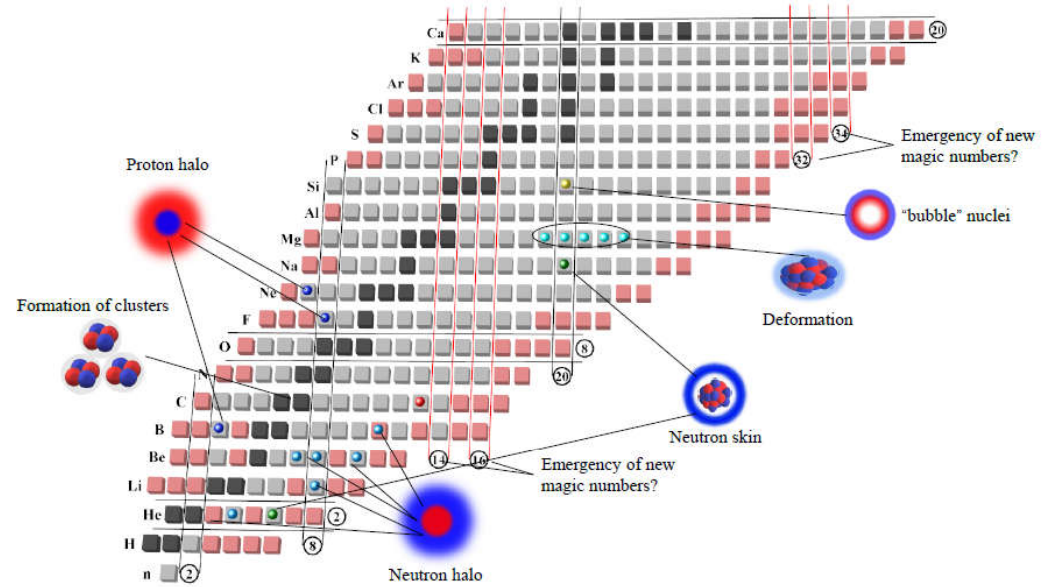
$$S \sim - \lambda - \Delta$$


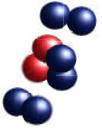
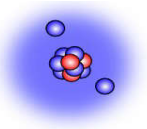
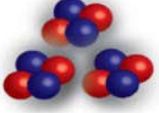
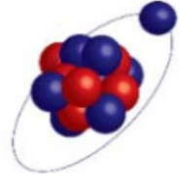
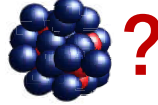
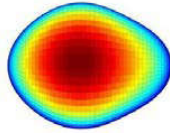
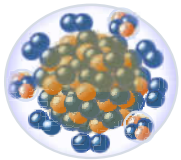
↓ ↑

λ : Mean Field
 Δ : Correlations

Y.L. Ye et al., Sci Sin-Phys Mech Astron, 50(2022)112003

- ❑ Strong coupling in the low density
- ❑ M-DOF structure
- ❑ New effective interactions
- ❑ Correlated reaction and decay

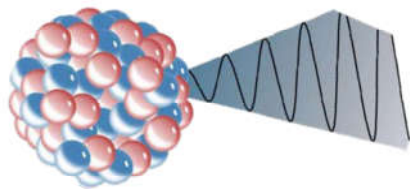
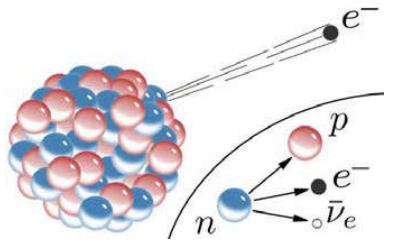


							
${}^2\text{H}$	${}^8\text{He}$	${}^{11}\text{Li}$	${}^{12}\text{C}$	${}^{23}\text{O}$	${}^{60}\text{Ca}$?	${}^{225}\text{Ra}$	AZ ?
Z=1, N=1 stable	Z=2, N=6 $T_{1/2}=119.1$ ms	Z=3, N=8 $T_{1/2}=8.75$ ms	Z=6, N=6 stable	Z=8, N=15 $T_{1/2}=97$ ms	Z=20, N=40 $T_{1/2}=?$	Z=88, N=137 $T_{1/2}=14.9$ d	Dripline nuclei in medium/heavy mass region

Nuclear structure of exotic nuclei (Experimental approaches)

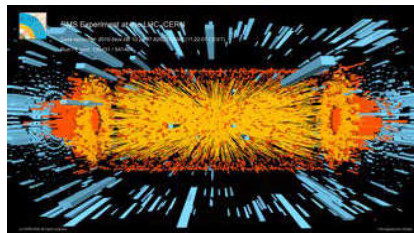
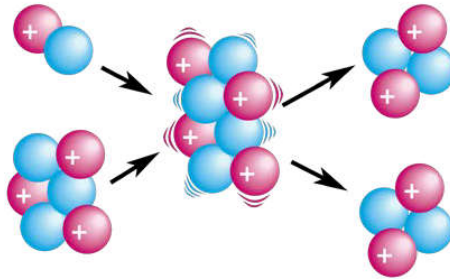
Nuclear decay

- α , β , γ , SF
- p-emitter
- n-emitter
-



Nuclear reaction

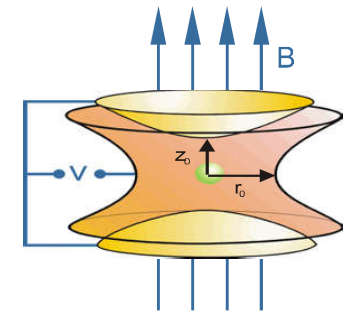
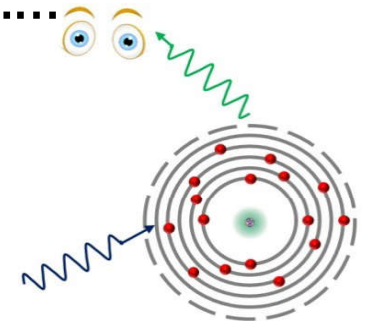
- Direct reaction
- Fusion reaction
- MNT reaction
-



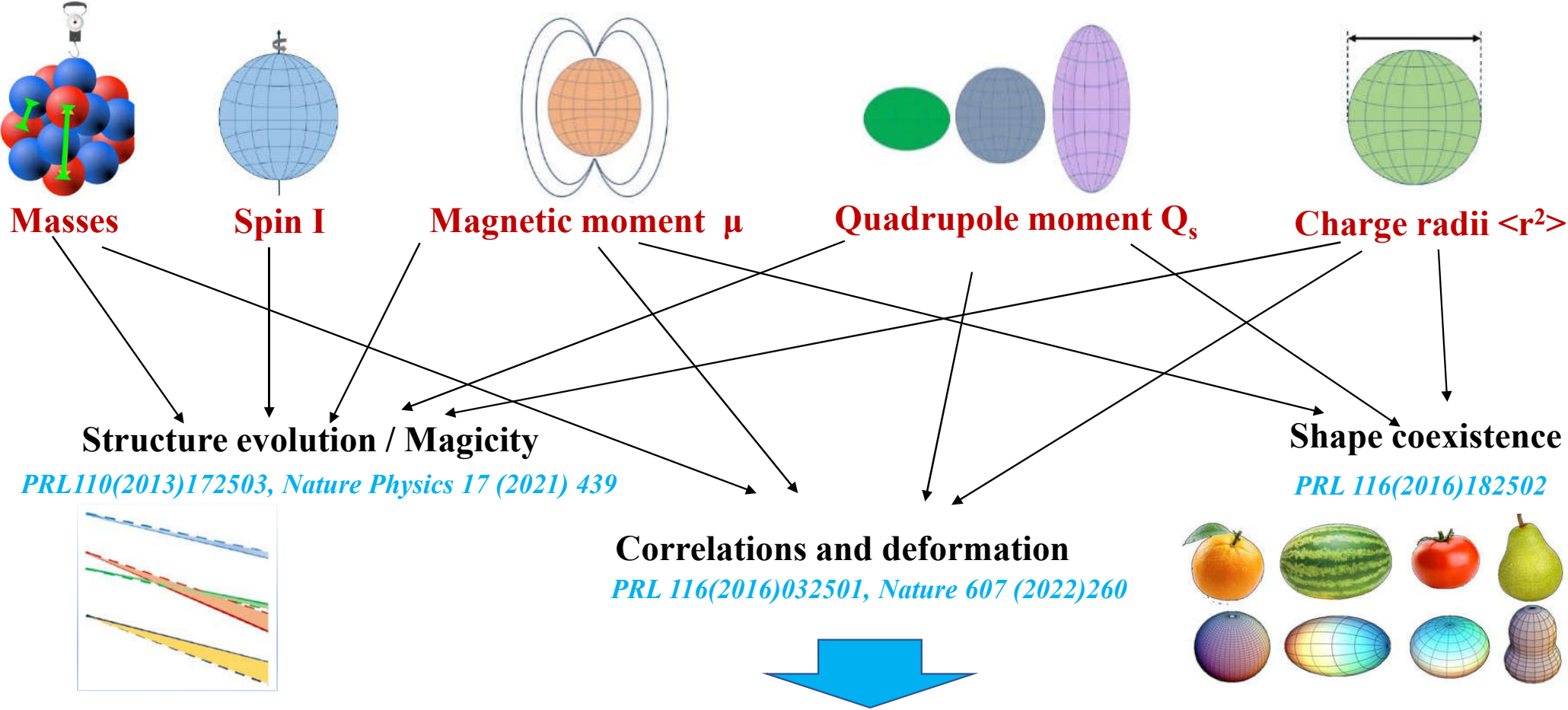
+Heavy ion collision

g.s. properties

- Ion trap/storage ring
- Laser spectroscopy
- β NMR/NQR
-



Ground state (g.s.) properties – Nuclear structure



Test of state-of-the-art nuclear theories
Nat. Phys. 12(2016)596, PRL 128 (2022) 022502

Ground state (g.s.) properties – Nuclear shapes

- general description of a shape:

$$R(\theta, \phi) = R_0 \left[1 + \sum_{\lambda=0}^{\infty} \sum_{\mu=-\lambda}^{\lambda} a_{\lambda, \mu} Y_{\lambda \mu}(\theta, \phi) \right]$$

- important nuclear shapes:

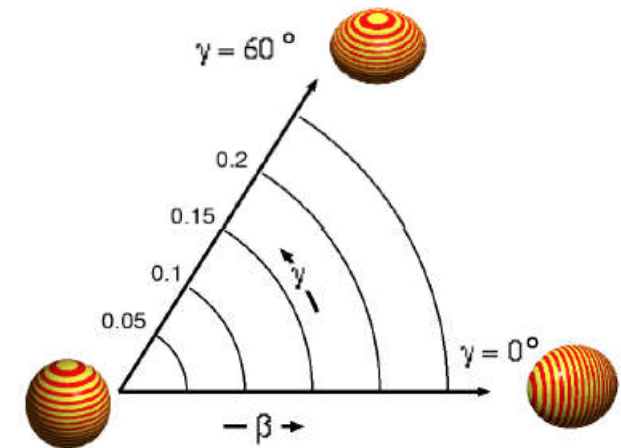
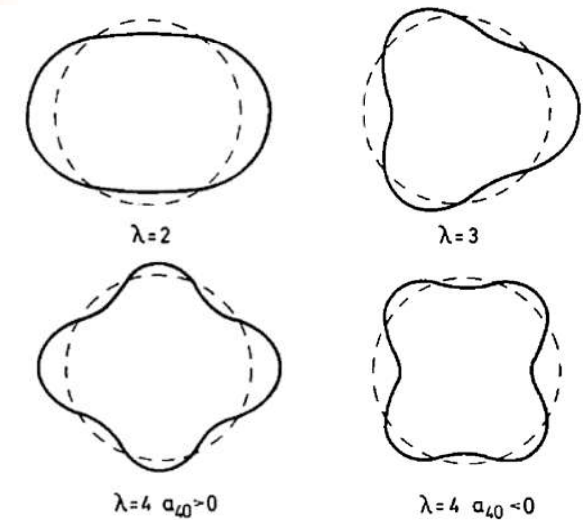
- $a_{2, \mu}$ quadrupole deformation (triaxial ellipsoid)
- $a_{3, \mu}$ octupole deformation (pear shape)

- in the principal axes frame $a_{2,1} = a_{2,-1} = 0$ and only two parameters are enough to describe all possible quadrupole shapes:

$$a_{2,0} = \beta \cos \gamma$$

$$a_{2,2} = a_{2,-2} = \frac{\beta \sin \gamma}{\sqrt{2}}$$

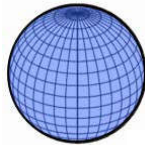
--from the talk of magdalena zielinska @Wednesday



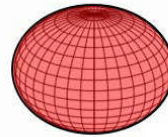
Ground state (g.s.) properties – Nuclear shapes

- Experimental observables for nuclear shapes

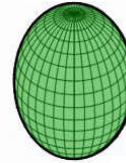
□ Quadrupole moment Q_s



$$Q_{intr.} = 0$$



$$Q_{intr.} < 0$$



$$Q_{intr.} > 0$$

$$Q_s = \frac{3K^2 - I(I + 1)}{(2I + 3)(I + 1)} Q_{intr.} \quad \rightarrow \quad Q_{intr.} = \frac{3}{\sqrt{5\pi}} ZR_0^2 \beta_2 (1 + 0.36 \beta_2)$$

□ Nuclear charge radii $R = \sqrt{\langle r^2 \rangle}$

$$\langle r^2 \rangle = \langle r^2 \rangle_0 \left(1 + \frac{5}{4\pi} \langle \beta_2^2 \rangle \right)$$

□ Transition probability for E2

$$B(E2; 0^+ \rightarrow 2^+) = \left(\frac{3}{4\pi} eZR_0^2 \right)^2 \beta_2^2$$

Laser spectroscopy
This talk

Coulomb-excitation exp.
 γ spectroscopy
Talk of magdalena zielinska

$$\langle \beta_2^2 \rangle = \langle \beta_2 \rangle^2 + (\langle \beta_2^2 \rangle - \langle \beta_2 \rangle^2) = \beta_{static}^2 + \beta_{dynamic}^2$$

J. Phys. G: Nucl. Part. Phys. 37 (2010) 113101

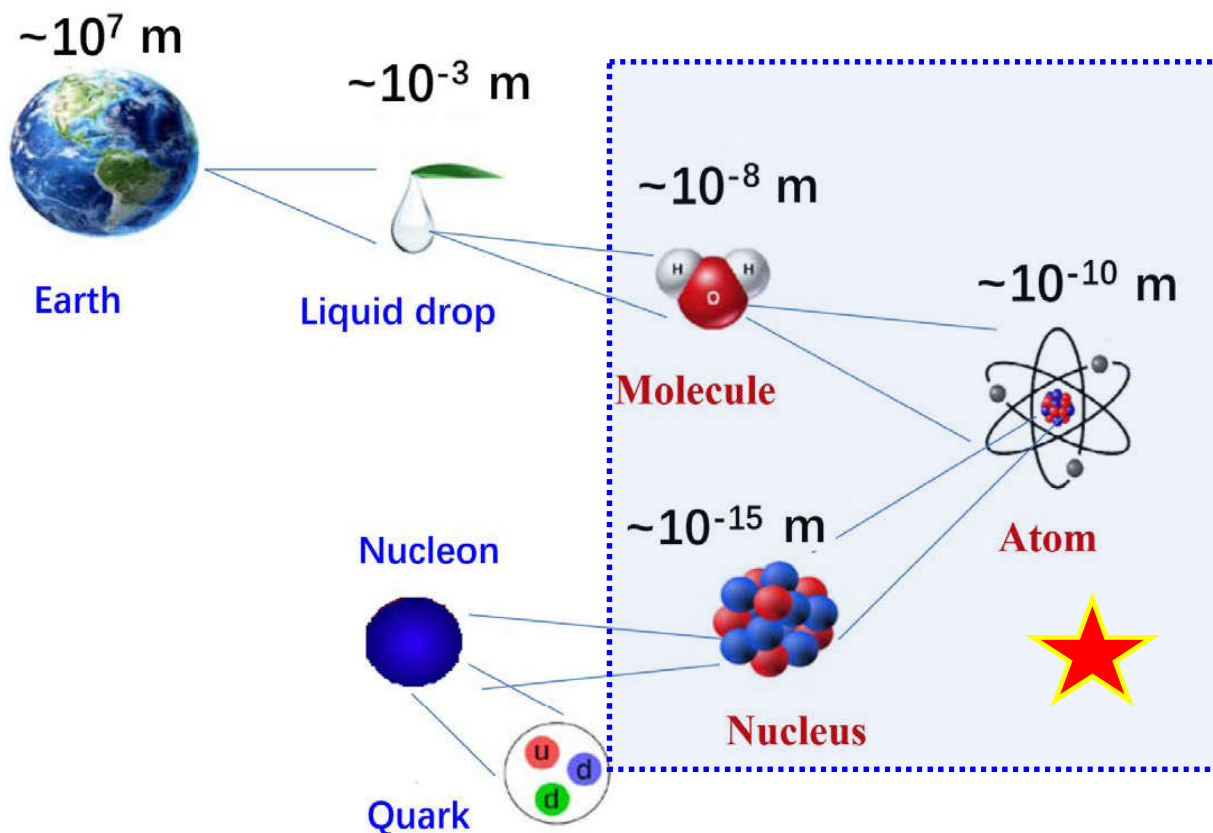
Outline



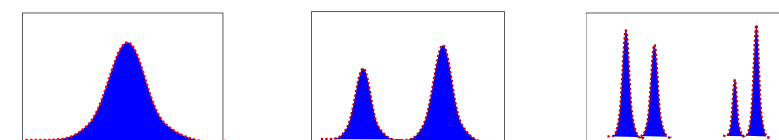
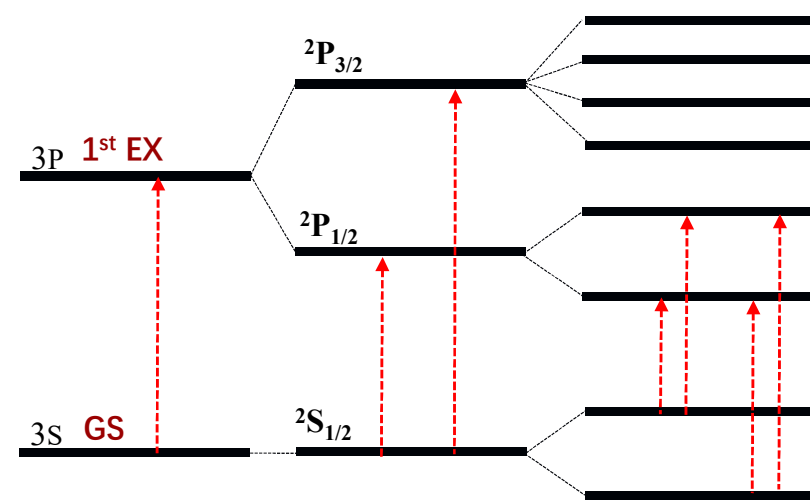
- Nuclear structure and g.s. properties
- **Hyperfine interaction and laser spectroscopy**
- **Nuclear structure studied from laser spectroscopy**
- **Laser spectroscopy development and near future work**

Hyperfine interaction and laser spectroscopy

Hyperfine interaction: EM interaction between atomic nucleus and the surrounding electrons



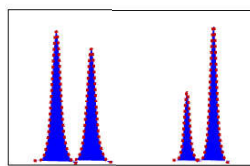
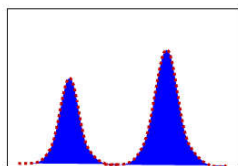
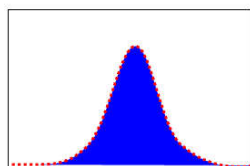
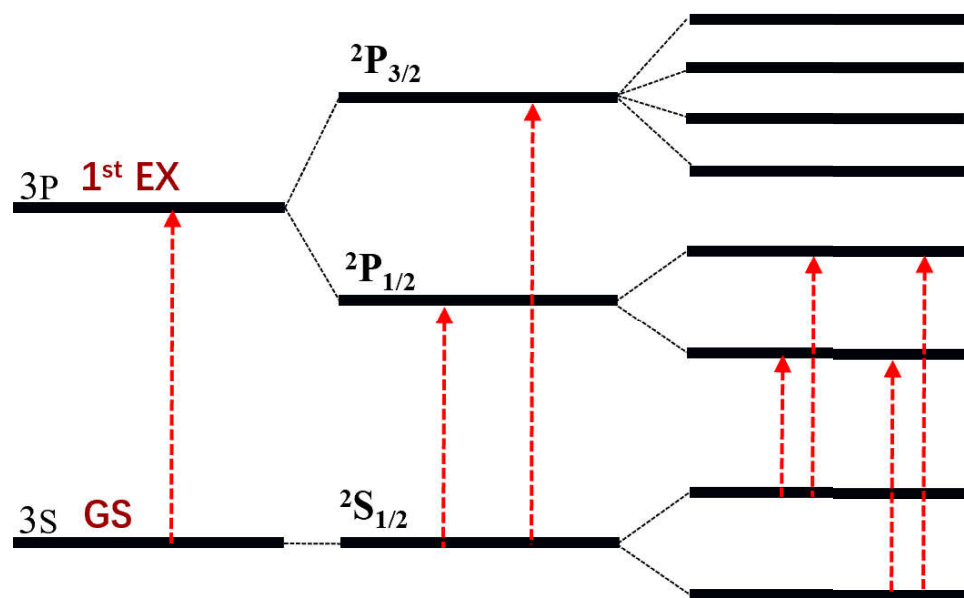
****Hyperfine structure/Isotope shift****



Hyperfine structure (HFS) spectrum

Hyperfine interaction and laser spectroscopy

Optical HFS spectrum



X.F. Yang et al., Prog. Part. Nucl. Phys. 129 104005 (2023)

$$H_{\text{hf}} = \sum_k \hat{T}_{\text{N}}^k \cdot \hat{T}_{\text{e}}^k$$

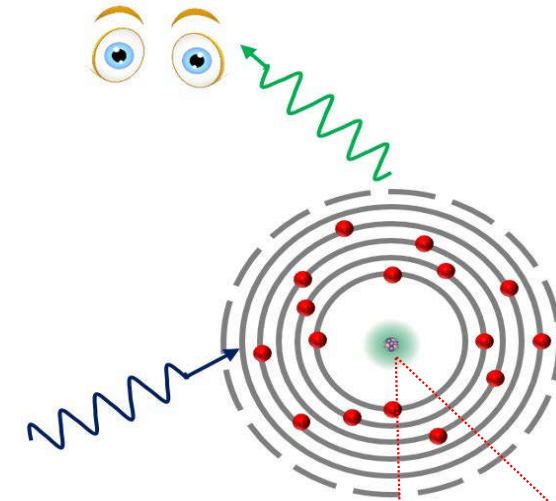
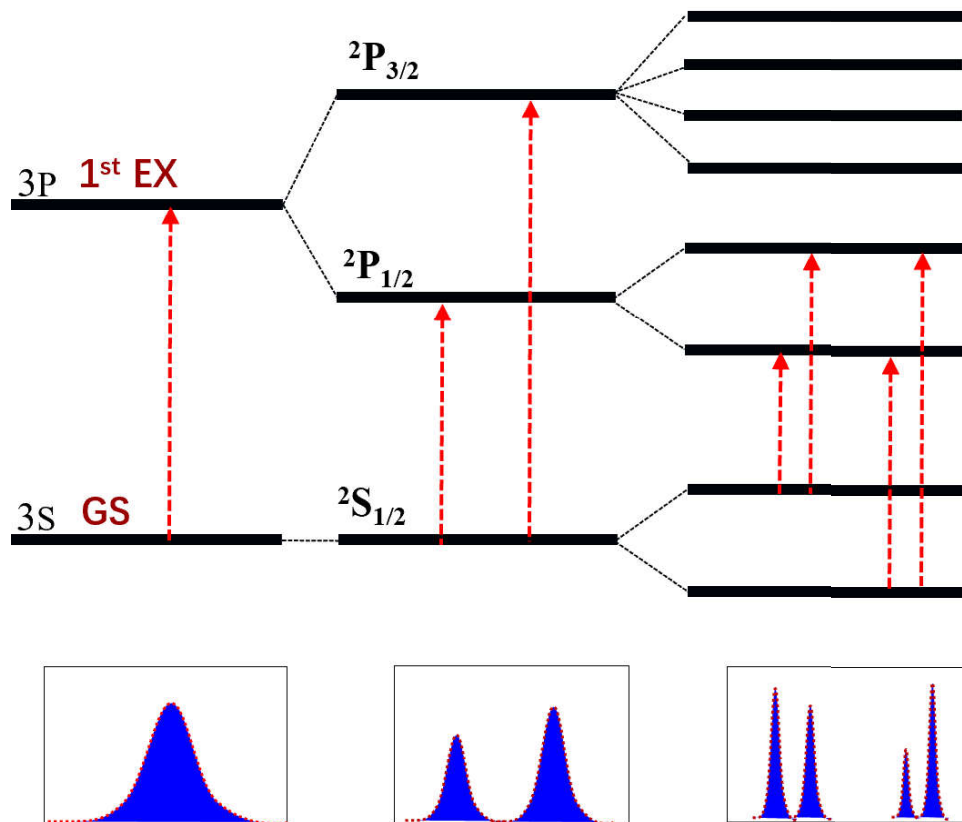
- K=0 electric monopole interaction
 - K=1 magnetic dipole interaction
 - K=2 electric quadrupole interaction
 - K=3 magnetic octupole interaction
 -
- } Dominate part

EDM? P, T violating
MQM?

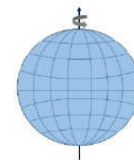
M.S. Safronova et al., RMP 90, 025008(2018)
 T.E. Chupp et al., RMP 91,015001(2019)

Hyperfine interaction and laser spectroscopy **Atoms or ions**

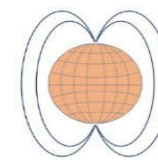
Optical HFS spectrum



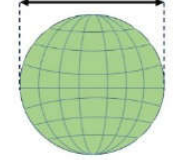
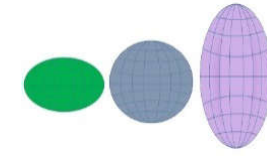
Nuclear properties



Spin I



Magnetic and quadrupole moments



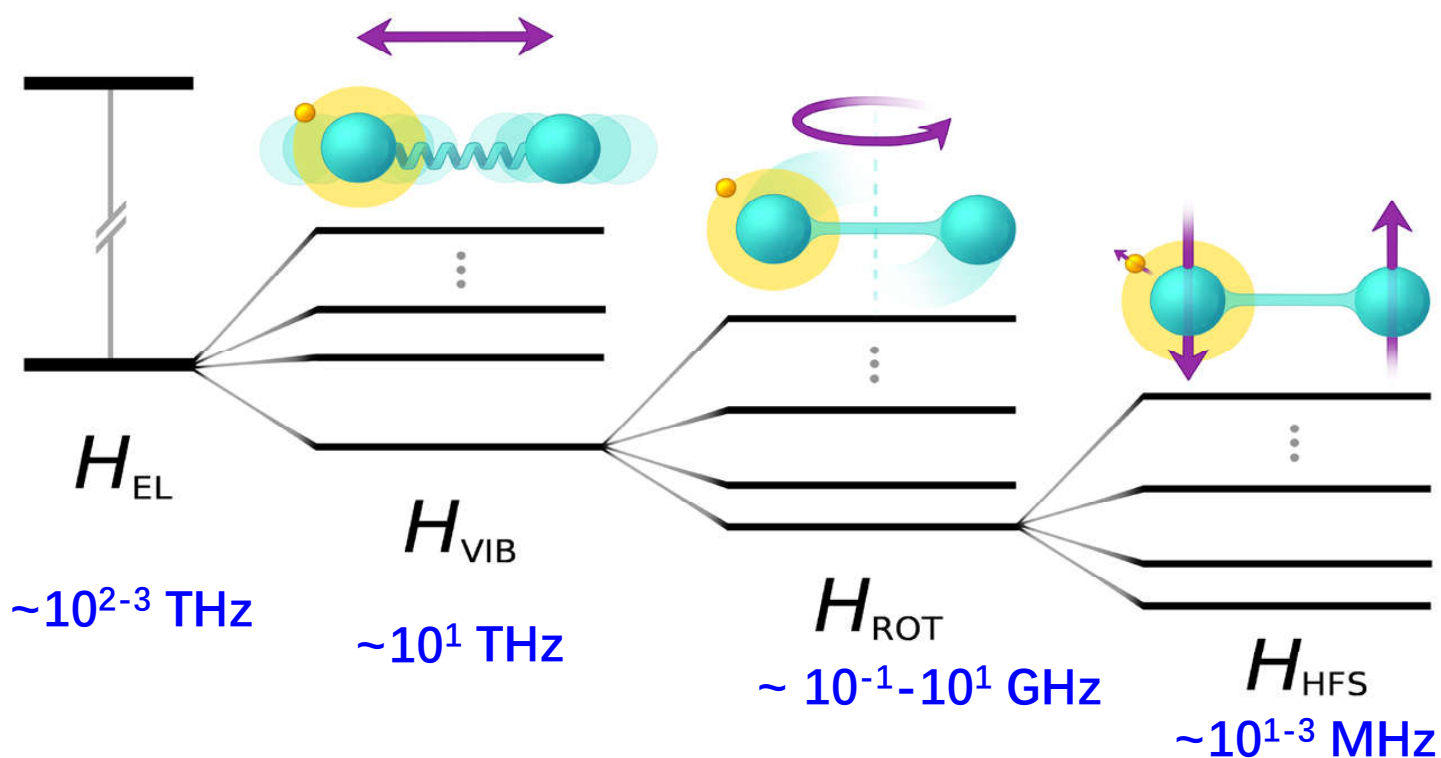
Radii $\langle r_c^2 \rangle$

In a nuclear-model independent manner

X.F. Yang et al., Prog. Part. Nucl. Phys. 129 104005 (2023)

Hyperfine interaction and laser spectroscopy Radioactive molecules

$$H_{\text{Mol.}} = H_{el} + H_{\text{vib.}} + H_{\text{rot.}} + \boxed{H_{\text{hfs}}} + \boxed{H_{\text{PV}} + H_{\text{PTV}}}$$



Nuclear Structure

- Moments
- Radii

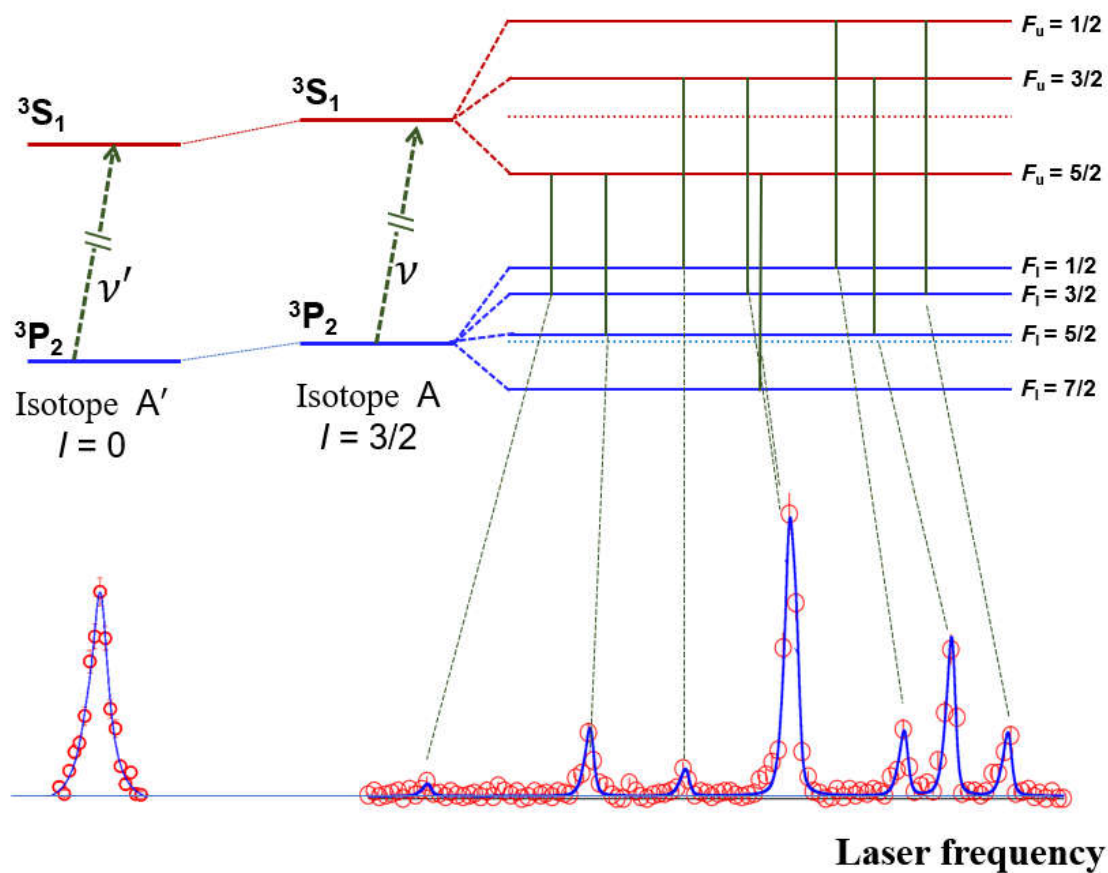
Symmetry violating

EDM, MQM

Opportunities for Fundamental Physics Research with Radioactive Molecules. Rep Prog Phys. 2024
 doi: 10.1088/1361-6633/ad1e39

Hyperfine interaction and laser spectroscopy

$$\Delta E = A \cdot K/2 + B \cdot \{3K(K+1)/4 - I(I+1)J(J+1)\} / \{2(2I-1)(2J-1)IJ\}, \quad K = F(F+1) - I(I+1) - J(J+1)$$



Atomic parameters

- Magnetic dipole HF parameter

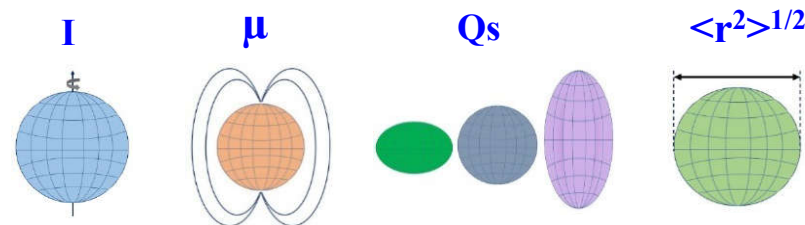
$$A = \frac{\mu_l B_J}{IJ} \quad I, \mu$$

- Electric quadrupole HF parameter

$$B = eQV_{zz} \quad Qs$$

- Centroid $\nu_0 \Rightarrow$ Isotopes shift

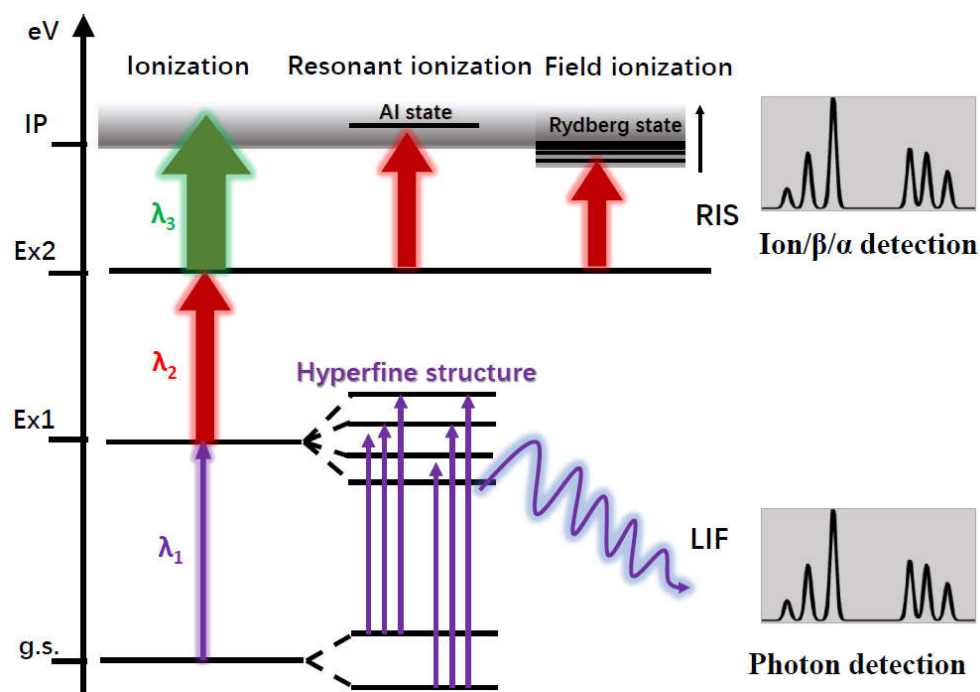
$$\delta\nu^{AA'} = M \frac{A' - A}{AA'} + F \delta \langle r^2 \rangle^{AA'}$$



X.F. Yang et al., "Laser Spectroscopy for the Study of Exotic Nuclei", *Prog. Part. Nucl. Phys.* 129, 104005(2023)

Hyperfine interaction and laser spectroscopy

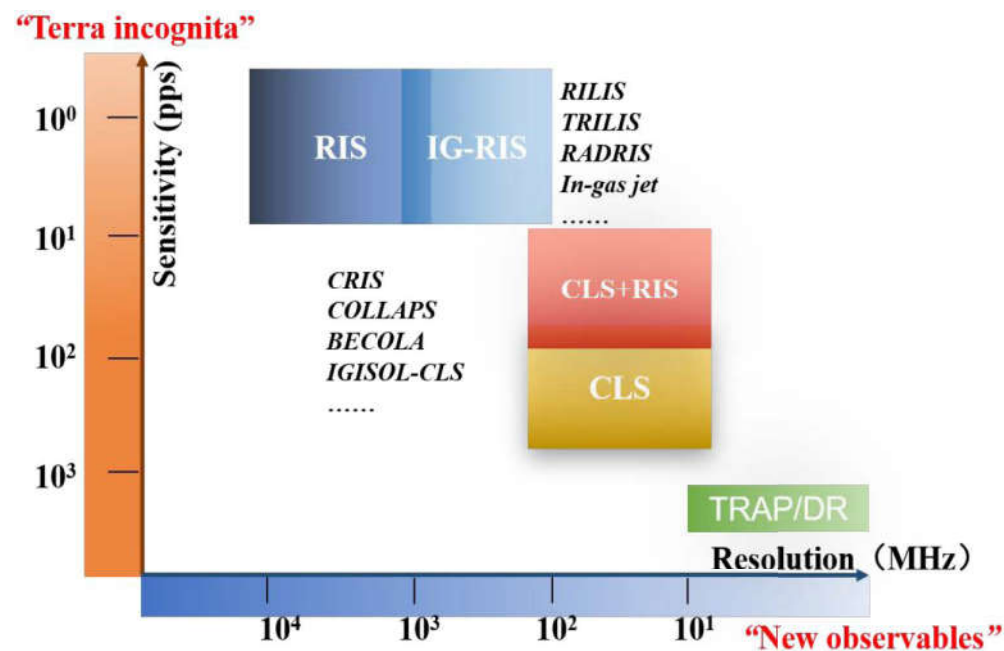
Approaches used to measure the HFS spectrum



LIF: laser-induced fluorescence

RIS: laser resonance ionization spectroscopy

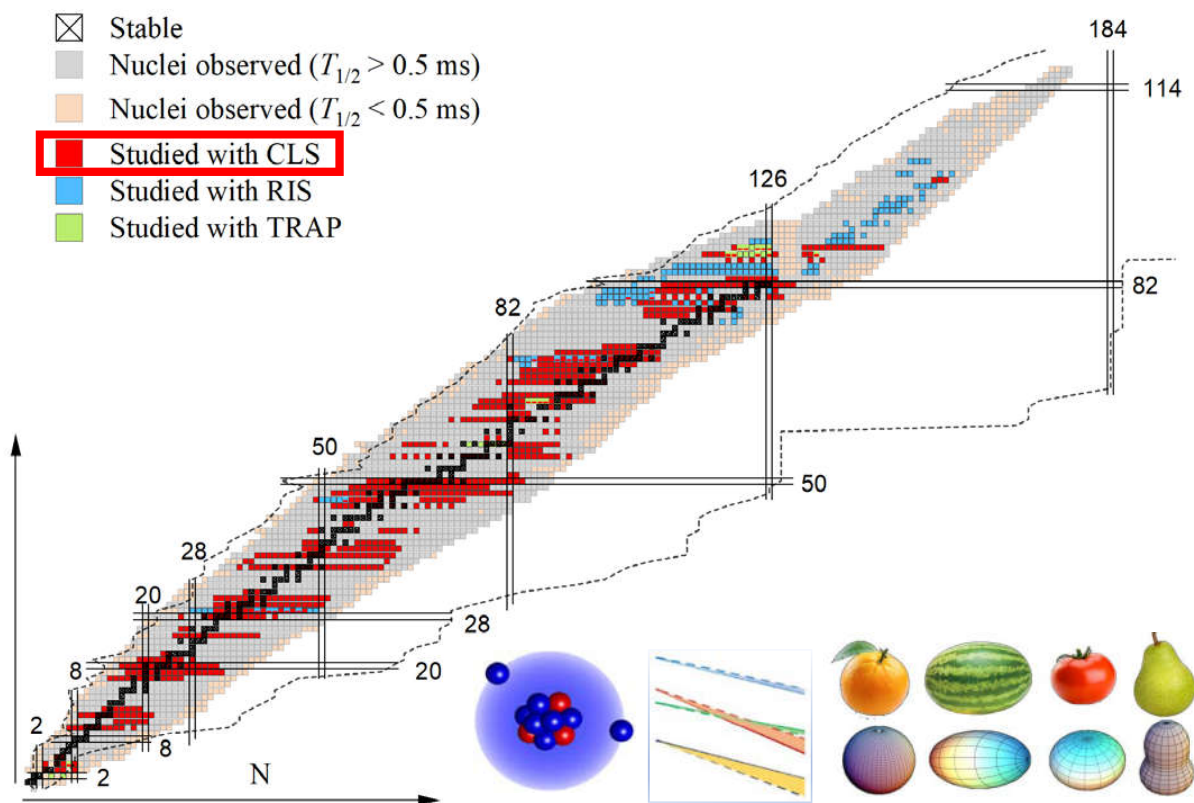
Three main categories of laser spectroscopy



- Collinear laser spectroscopy
- In-source laser spectroscopy
- Trap-assisted laser spectroscopy.

X.F. Yang et al., "Laser Spectroscopy for the Study of Exotic Nuclei", *Prog. Part. Nucl. Phys.* 129, 104005(2023)

Hyperfine interaction and laser spectroscopy



X.F. Yang et al., "Laser Spectroscopy for the Study of Exotic Nuclei", *Prog. Part. Nucl. Phys.* 129, 104005(2023)

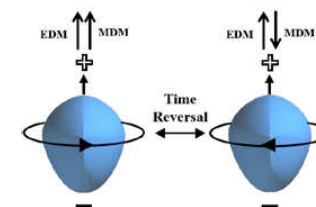
About 1000 nuclei was investigated

-contribute significantly to the study of nuclear structure and NN interaction

- *Nature* 607, 260-265 (2022)
- *Nat. Phys.* 17,439 (2021)

First laser spectroscopy of RaF (radioactive molecule)

-offer new opportunity for the study of fundamental symmetry

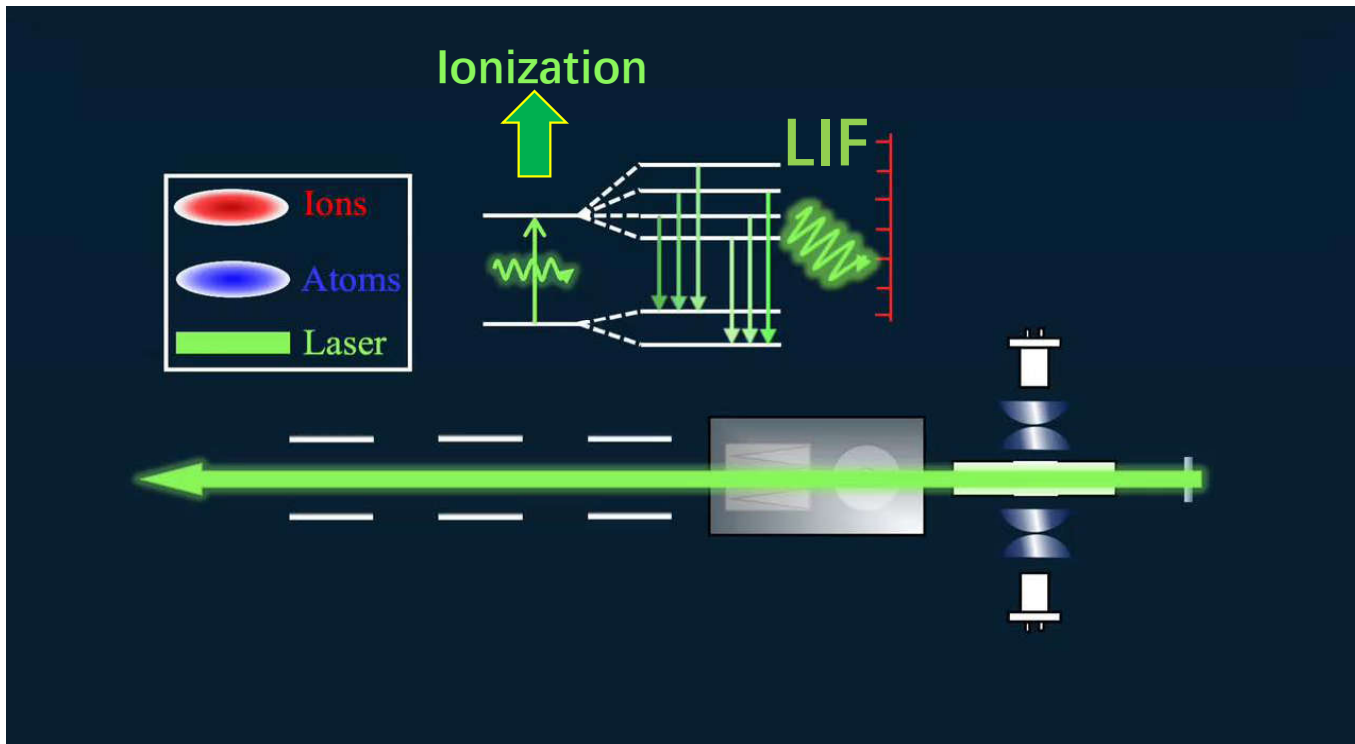


- *Nature* 581, 396 (2020)
- *Nat. Phys.* 20,202(2024)

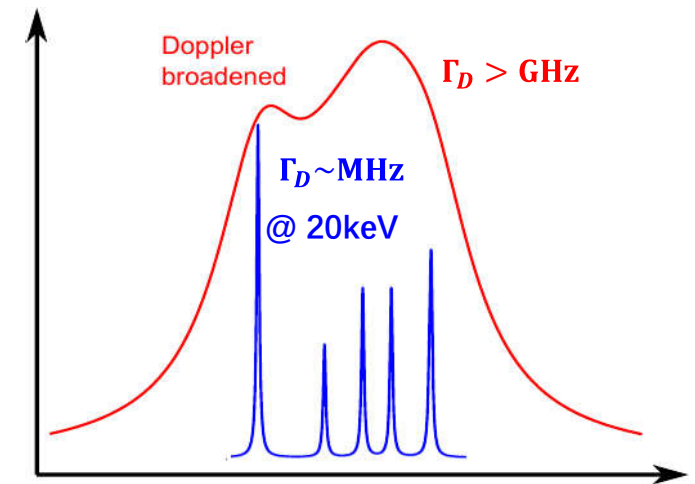
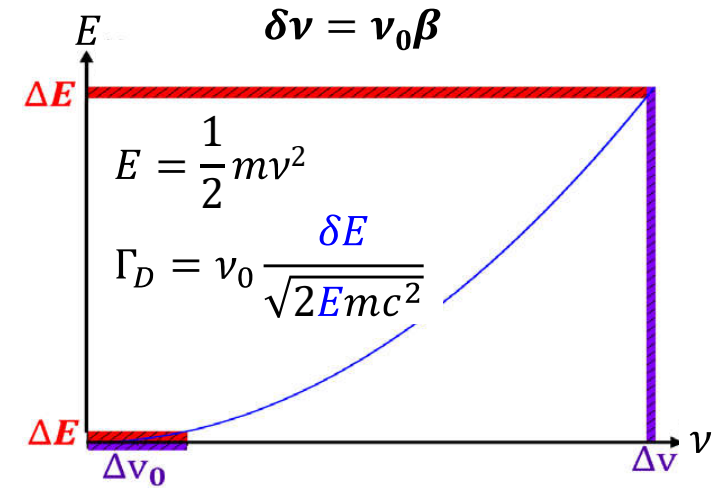
"New field"

Hyperfine interaction and laser spectroscopy (e.g. CLS)

CLS: Collinear laser spectroscopy

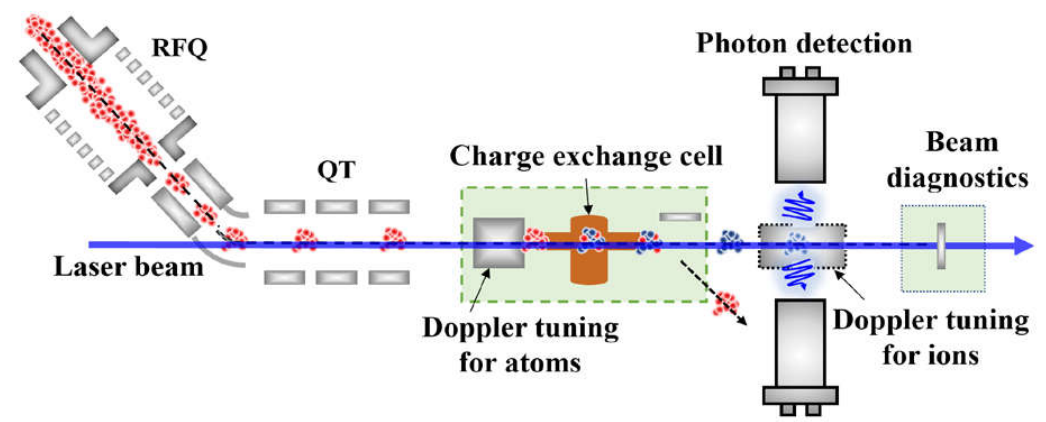
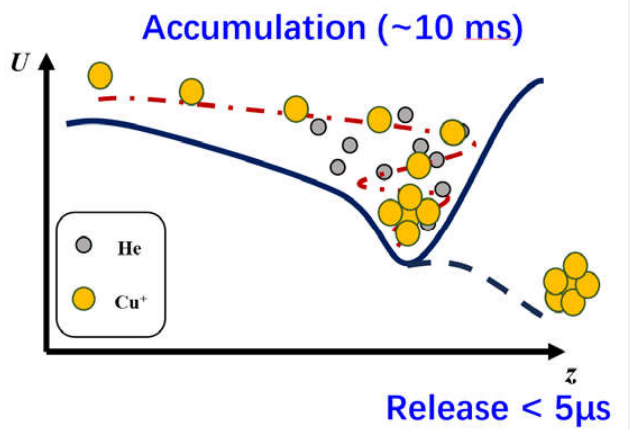
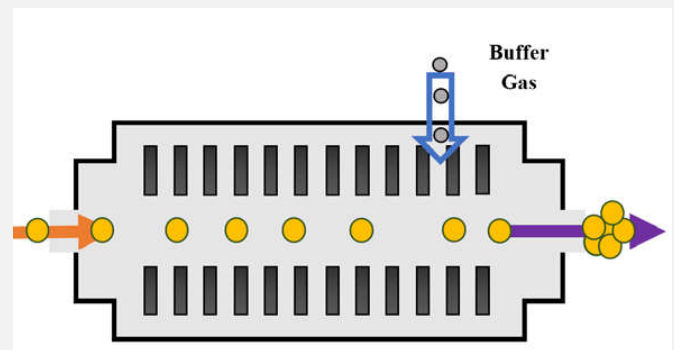


RI beam is overlapped with laser in a collinear/ant-collinear geometry

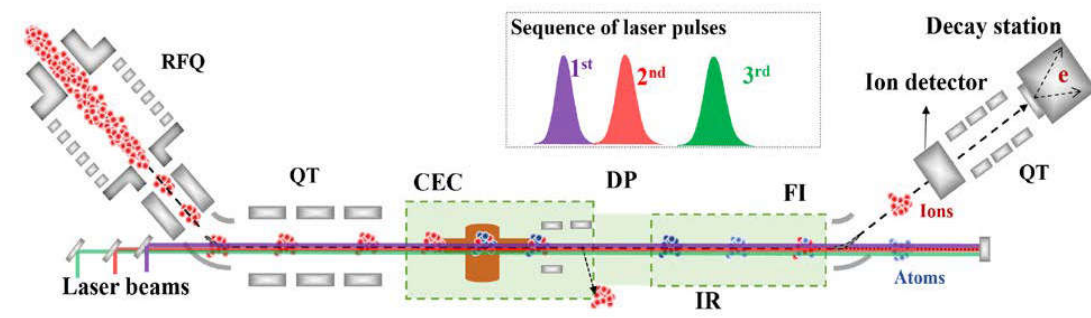
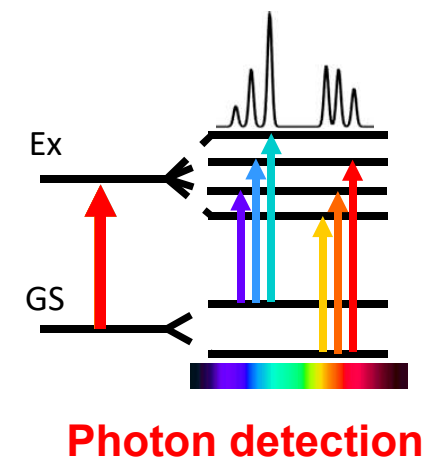


Hyperfine interaction and laser spectroscopy (e.g. CLS)

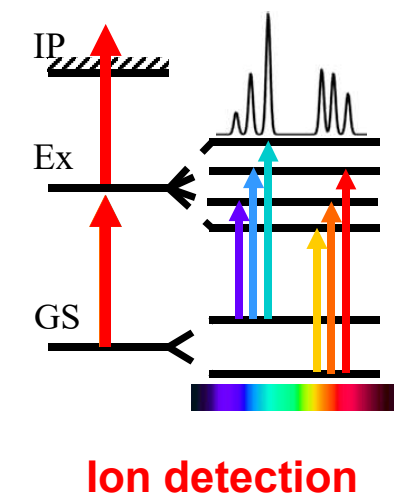
CW beam to bunched beam



Resolution < 100 MHz, Sensitivity 10^3 pps



Resolution < 100 MHz, Sensitivity 10^{1-2} pps

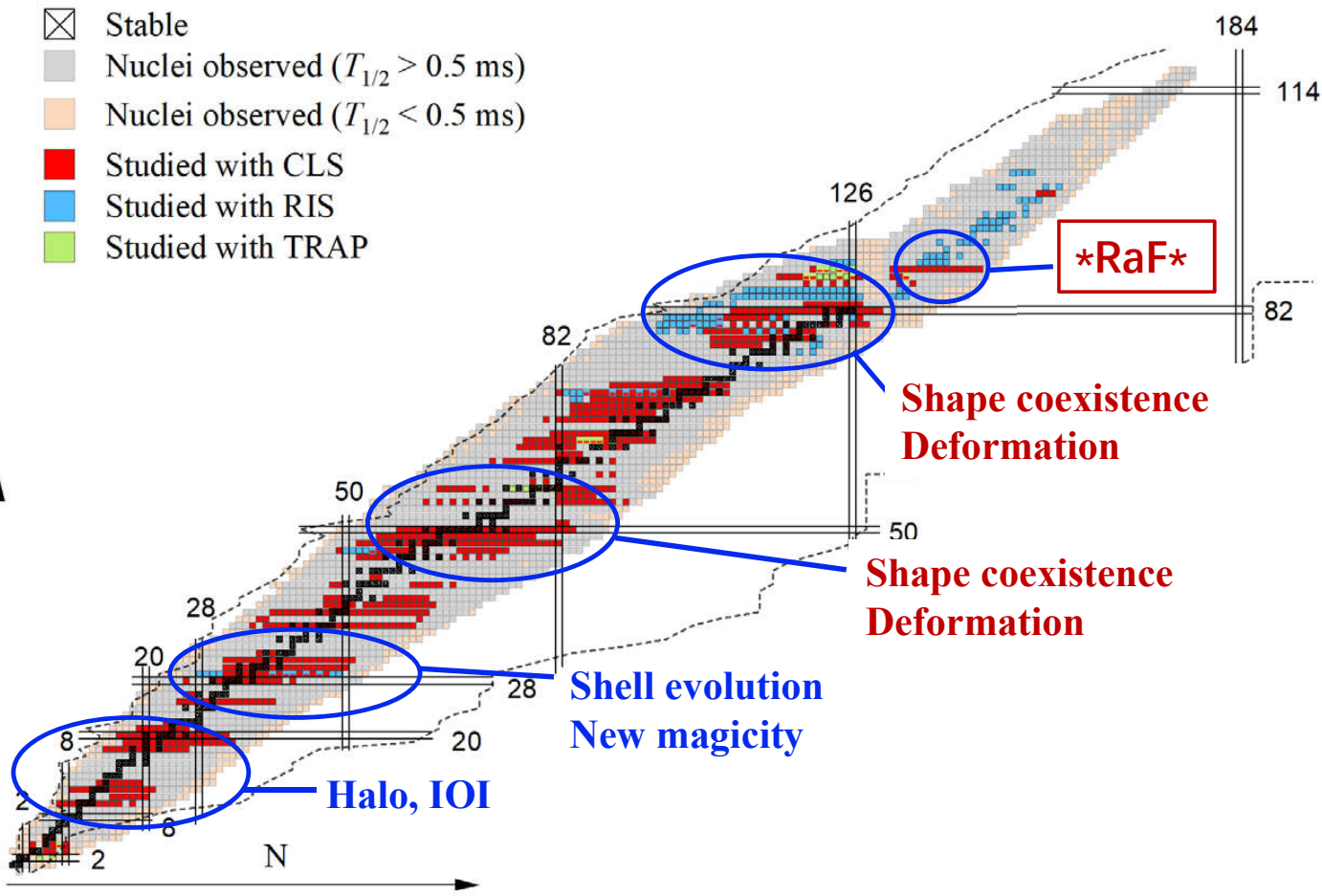


Outline



- Nuclear structure and g.s. properties
- Hyperfine interaction and laser spectroscopy
- **Nuclear structure studied from laser spectroscopy**
 - e.g. Nuclear shapes in neutron rich nickel region
 - e.g. Nuclear shapes in neutron deficient lead region
 - e.g. Nuclear information from radioactive molecules
- **Laser spectroscopy development and near future work**

Unstable nuclei probed by laser spectroscopy



X.F. Yang et al., "Laser Spectroscopy for the Study of Exotic Nuclei", Prog. Part. Nucl. Phys. 129, 104005(2023)

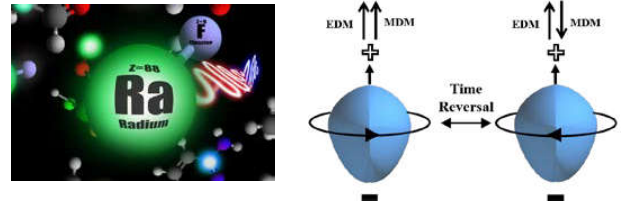
~1000 nuclei was investigated

-contribute significantly to the study of structure and NN interaction

- *Nature* 607, 260-265 (2022)
- *Nat. Phys.* (2024)

First laser spectroscopy of RaF (radioactive molecule)

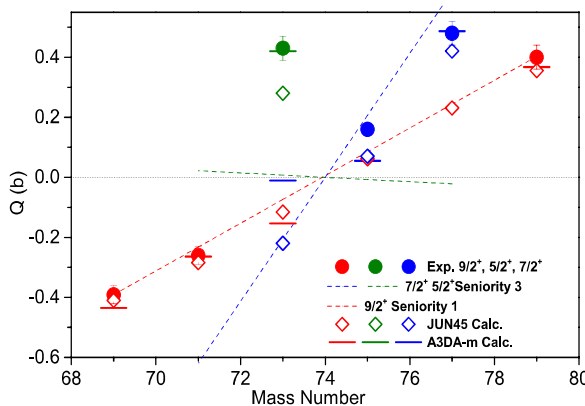
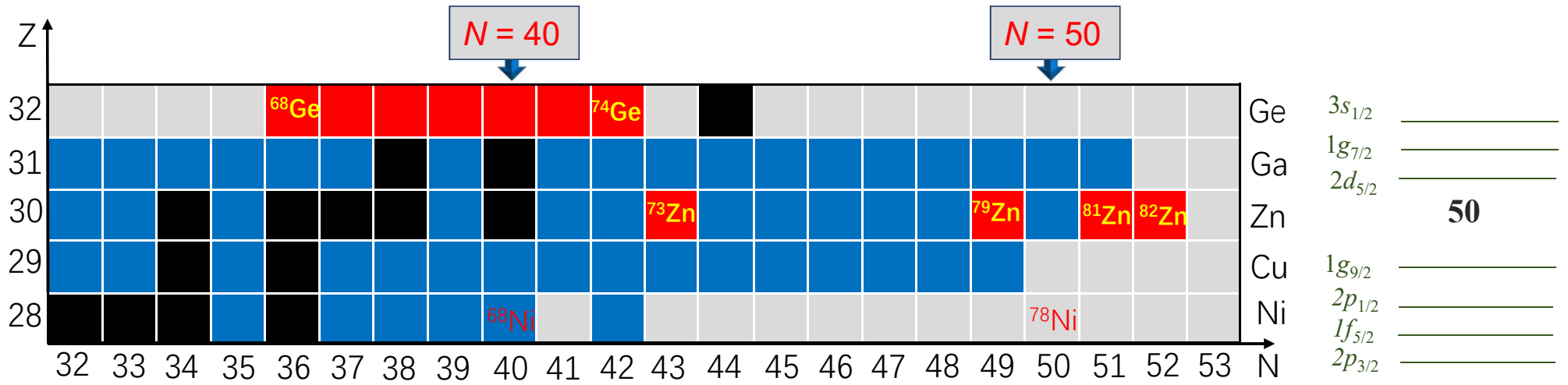
-offer new opportunity for the study of fundamental symmetry



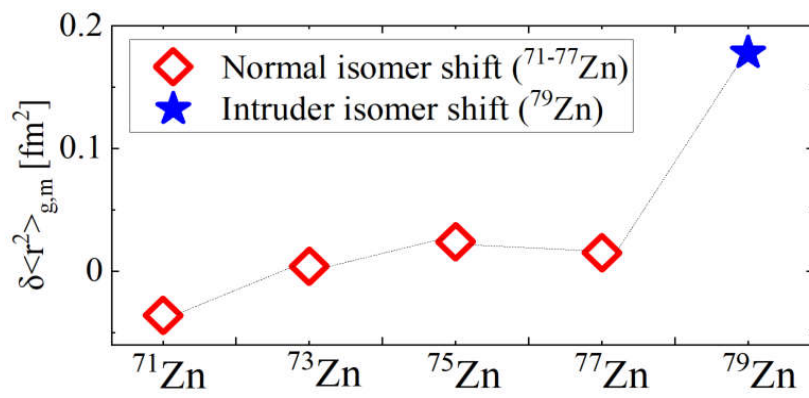
- *Nature* 581, 396 (2020)
- *Nat. Phys.* 20,202(2024)

"New field"

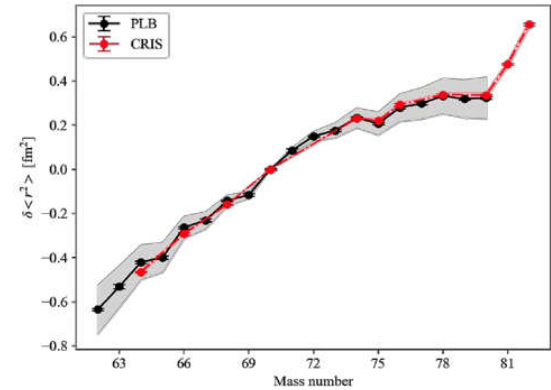
e.g. Nuclear shapes in neutron-rich Ni region



Triaxial deformation in ^{73}Zn

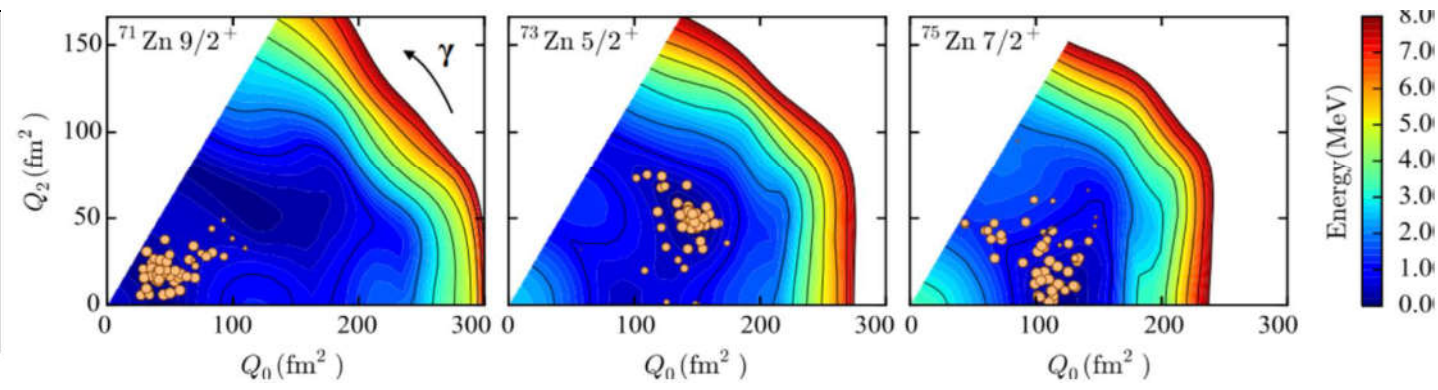
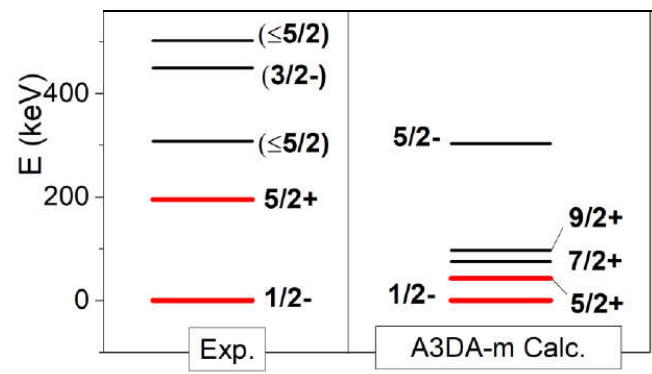
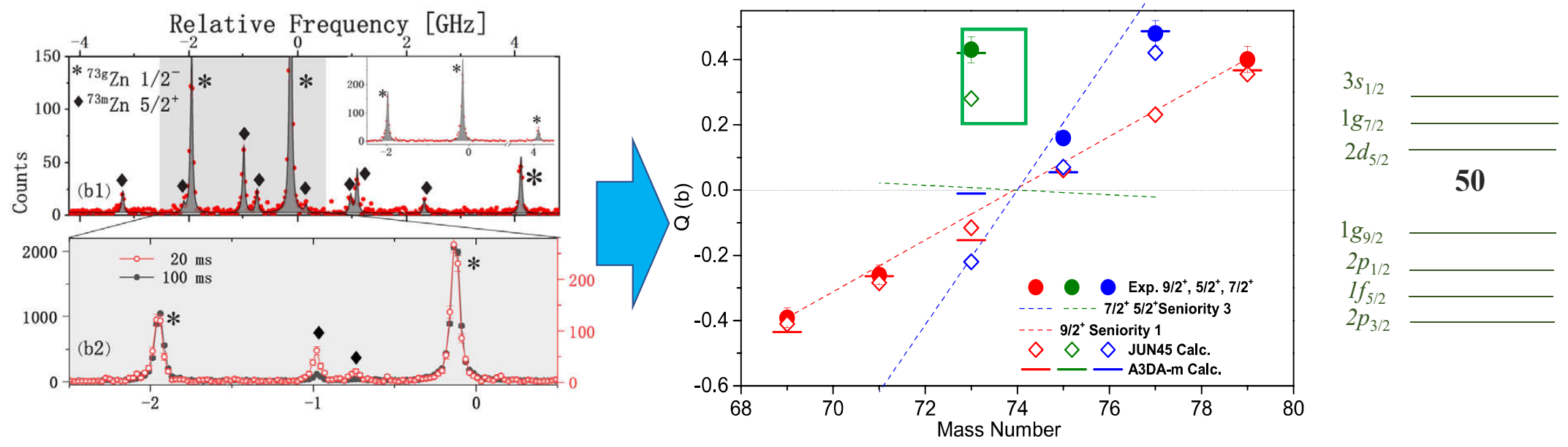


Shape coexistence in ^{79}Zn



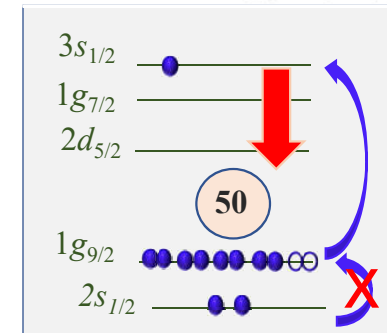
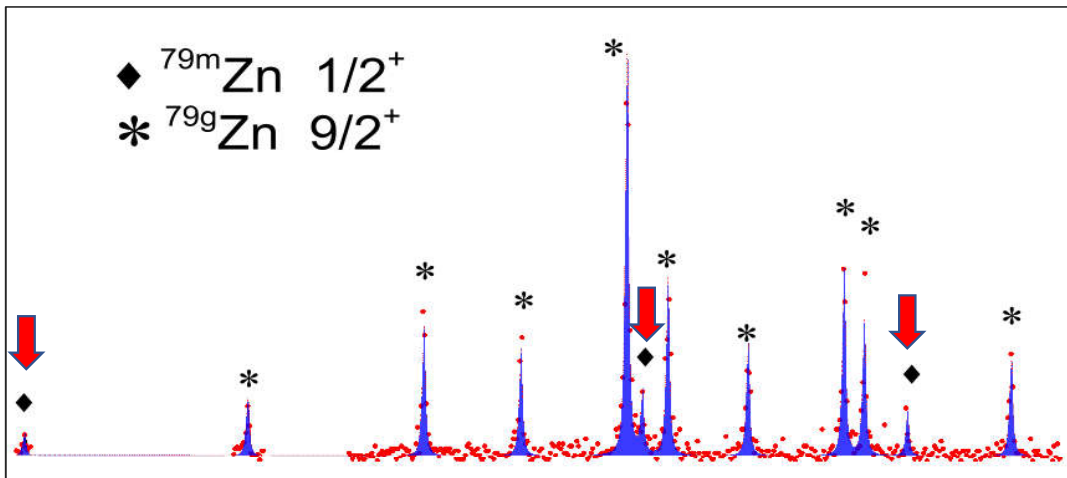
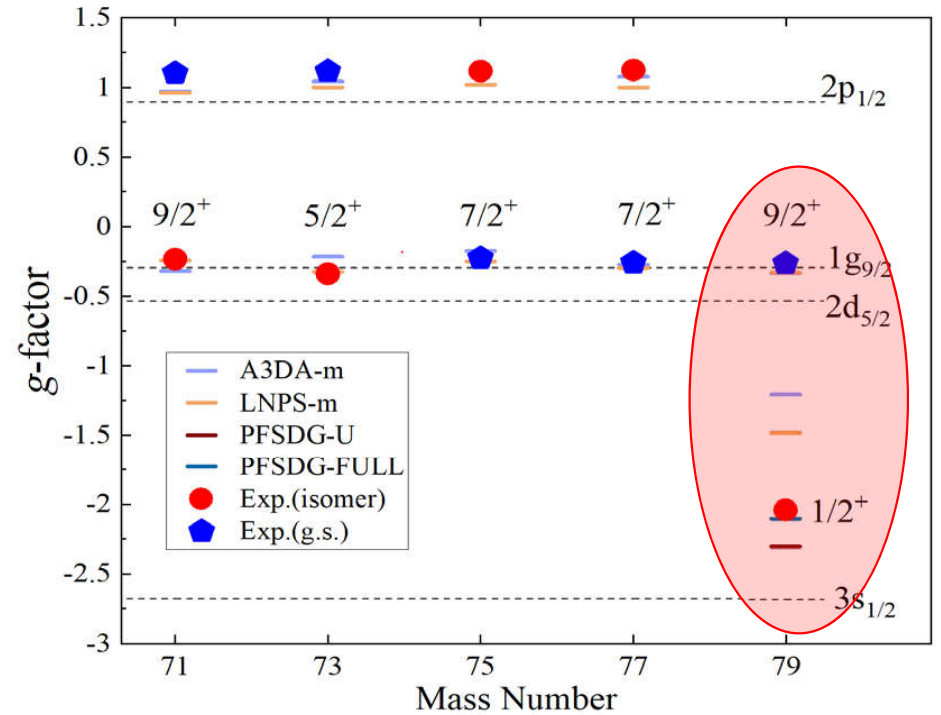
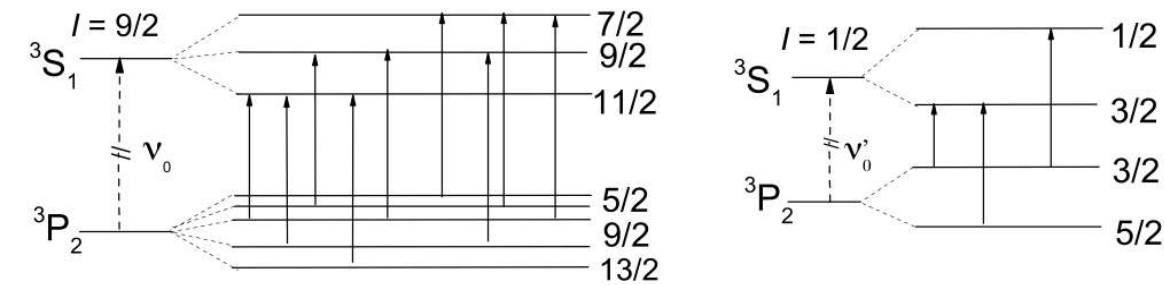
Defromation in $^{81-82}\text{Zn}$?

e.g. Nuclear shapes in neutron-rich Ni region (triaxiality in ^{73m}Zn)



[X. F. Yang et al., PRC 97, 044324 \(2018\)](#)

e.g. Nuclear shapes in neutron-rich Ni region (shape coexistence in ^{79}Zn)

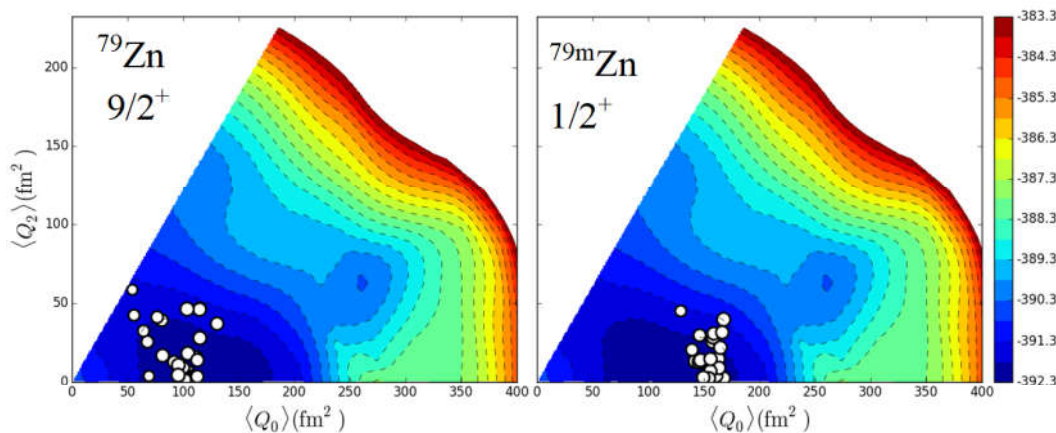
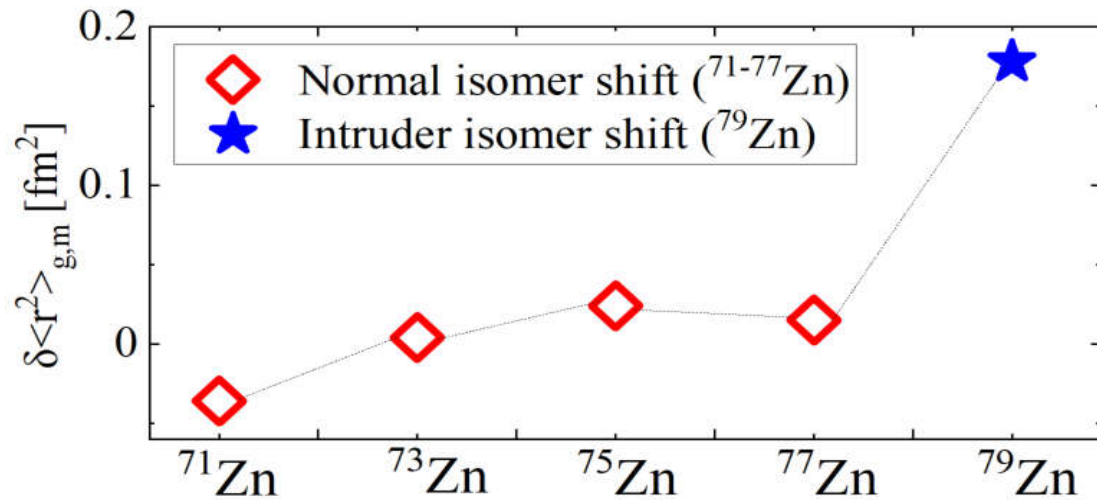


Intruder nature of $1/2^+$ state

Identification of a long-lived isomeric state in ^{79}Zn

[X.F Yang* et al PRL 116\(2016\)182502](#), [L.Xie. X.F. Yang et al., PLB797 \(2019\) 134805](#)

e.g. Nuclear shapes in neutron-rich Ni region (shape coexistence in ^{79}Zn)



- Quadrupole moment of $9/2^+$ g.s.
=>near spherical shape

$$Q_{\text{intr.}} = \frac{3}{\sqrt{5\pi}} Z R_0^2 \beta_2 (1 + 0.36\beta_2)$$

$$\beta_2 = 0.15(2)$$

- Larger isomer shift of the $1/2^+$ state
=>a larger deformation

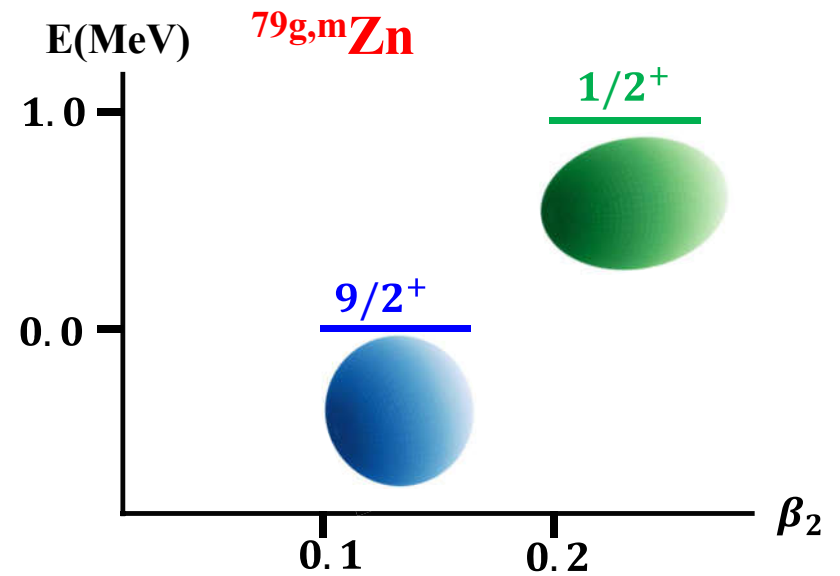
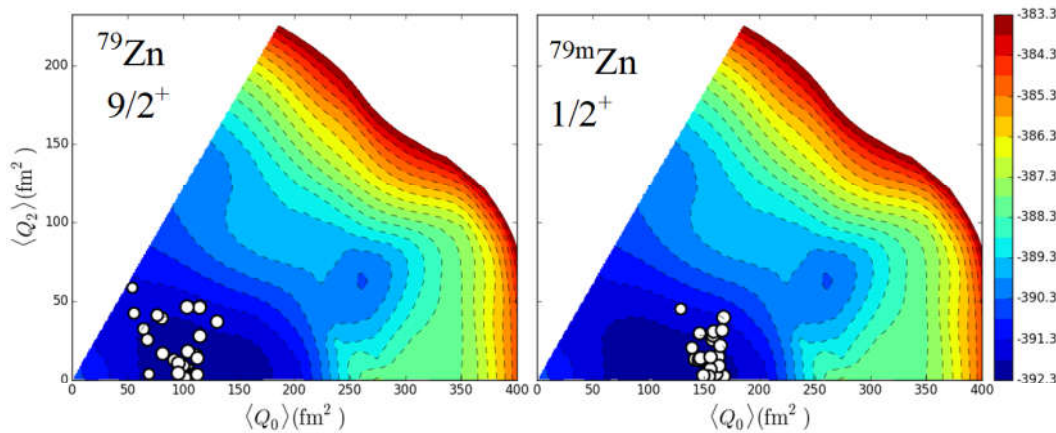
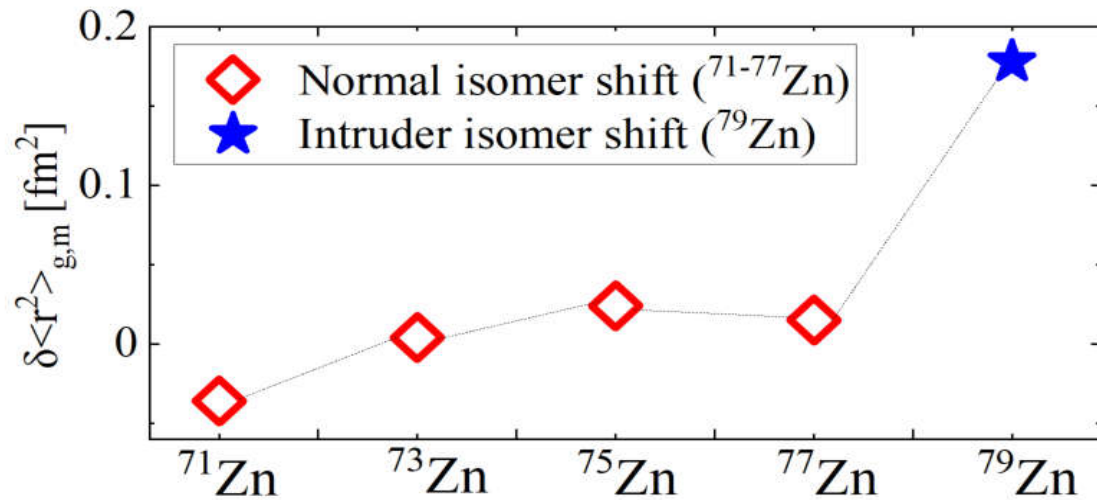
$$\langle r^2 \rangle = \langle r^2 \rangle_0 \left(1 + \frac{5}{4\pi} \langle \beta_2^2 \rangle \right)$$

$$\delta \langle r^2 \rangle^{A,A'} = \delta \langle r^2 \rangle_0^{A,A'} + \langle r^2 \rangle_0 \cdot \frac{5}{4\pi} \delta \langle \beta_2^2 \rangle^{A,A'}$$

$$\langle \beta_2^2 \rangle^{1/2} \sim 0.22$$

Deformation of the $1/2^+$ state

e.g. Nuclear shapes in neutron-rich Ni region (shape coexistence in ^{79}Zn)

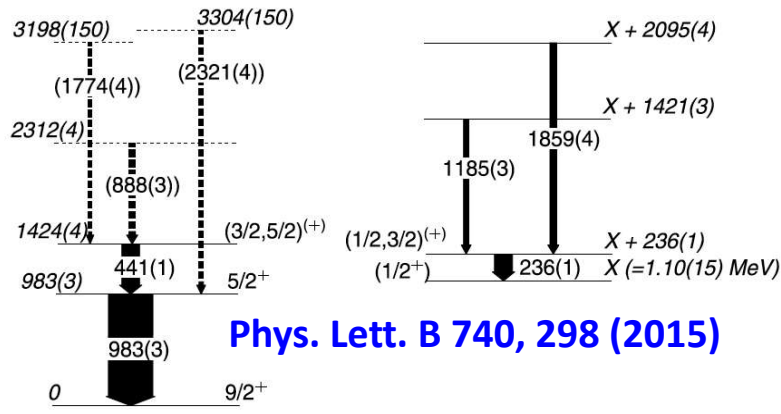


=> Experimental evidence for shape coexistence in ^{79}Zn

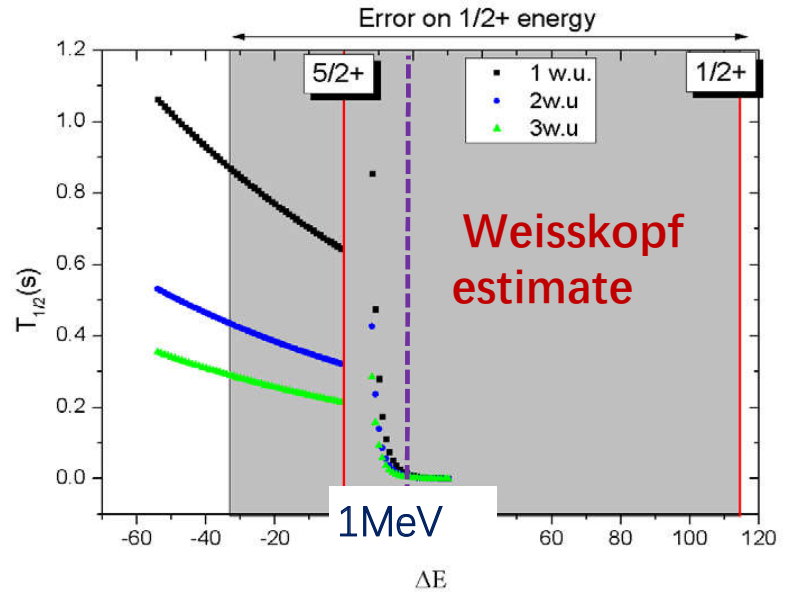
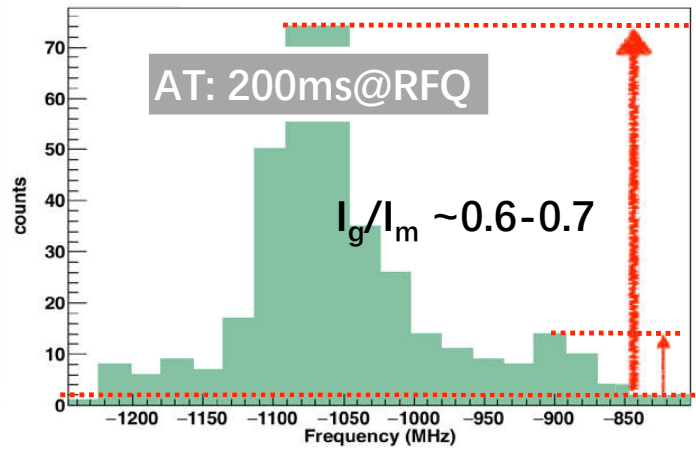
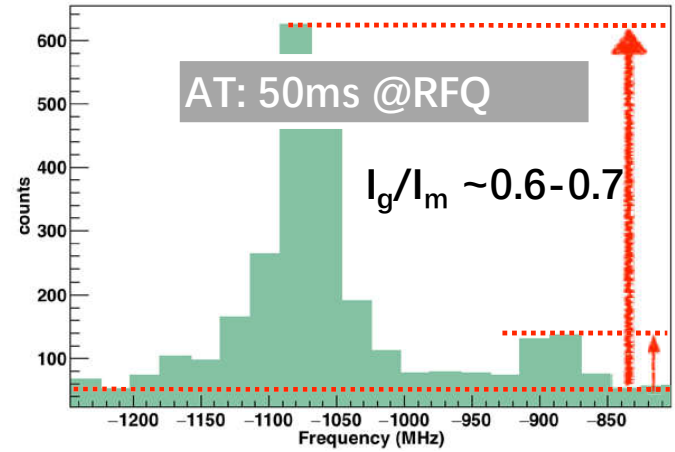
[X.F Yang* et al PRL 116(2016)182502, L.Xie. X.F. Yang et al., PLB797 (2019) 134805]

e.g. Nuclear shapes in neutron-rich Ni region (shape coexistence in ^{79}Zn)

◆ ^{79m}Zn $1/2^+$
* ^{79g}Zn $9/2^+$



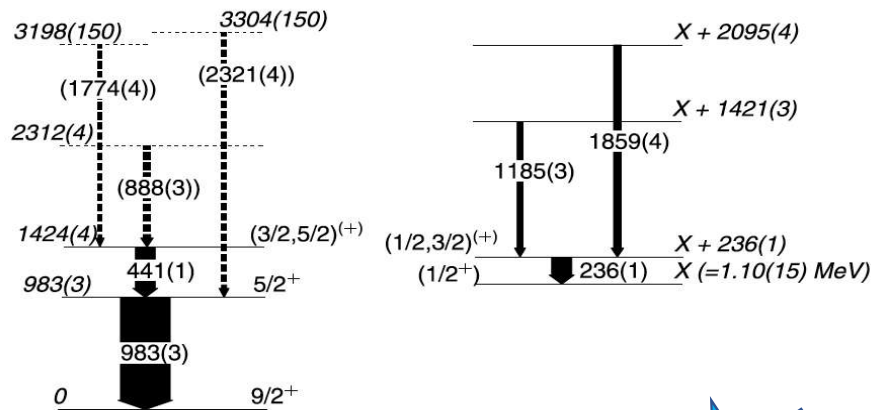
Phys. Lett. B 740, 298 (2015)



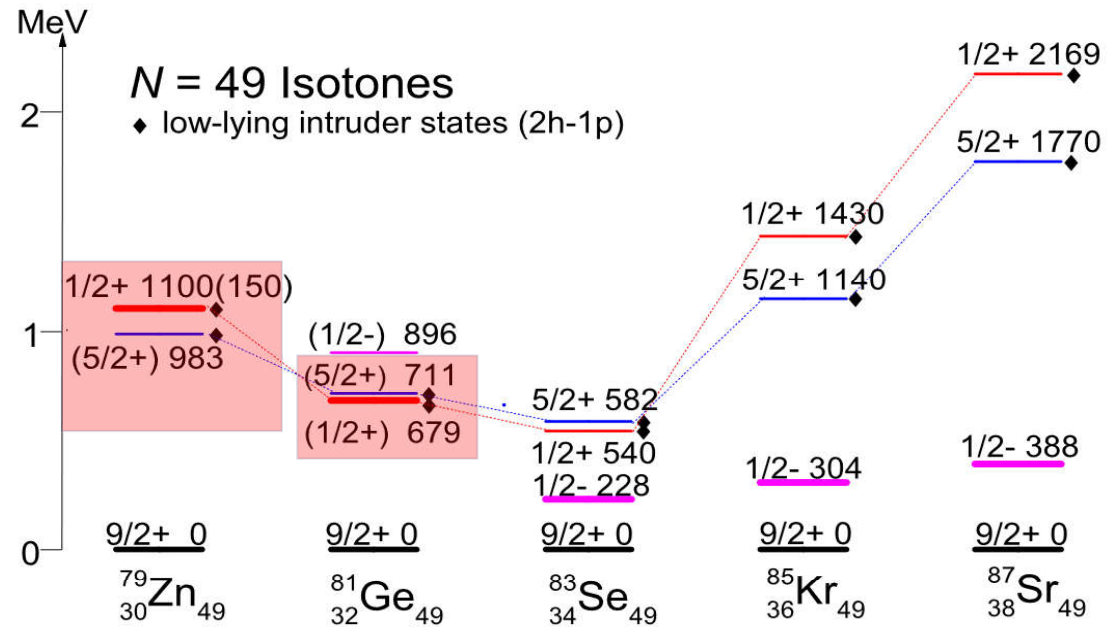
Conclusion:

1. Few hundreds ms half life for ^{79m}Zn as I_g/I_m stay no change using 50, 100, 200ms accumulation time in the RFQ
2. The energy of the $1/2^+$ isomer is lower than 1 MeV

e.g. Nuclear shapes in neutron-rich Ni region (shape coexistence in ^{79}Zn)



- $T_{1/2} > 200$ ms ?
E4 or E2?
- Mass (E) of $1/2+$?



L. Nies *et al.* Phys. Rev. Lett. 131, 222503 (2023) \Rightarrow $1/2+$ is the 1st excitation state of ^{79}Zn
 $E(1/2+) = 943$ keV

- The long-lived $1/2+$ state has been known in ^{81}Ge for 40 years *Nucl. Phys. A368, 210 (1981).*
- To confirm the shape coexistence in ^{81}Ge , high-resolution laser spectroscopy is needed.

M. L. Bissell, X. F. Yang et al., CERN-INTC-2016-036 ; INTC-I-170.

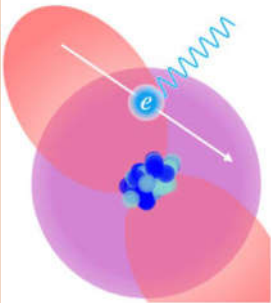
e.g. Nuclear shapes in neutron-rich Ni region (shape coexistence in ^{79}Zn)

EDITORS' SUGGESTION

Shape Coexistence Near ^{78}Ni 2016

Two different experiments observe nuclei with excited nuclear state that differ in shape from their ground states, so called shape coexistence. These nuclei lie close to the neutron-rich doubly-magic ^{78}Ni region of the nuclear chart.

X.F. Yang *et al.* A. Gottardo *et al.*
 PRL 116(2016)182502; PRL116(2016)182501


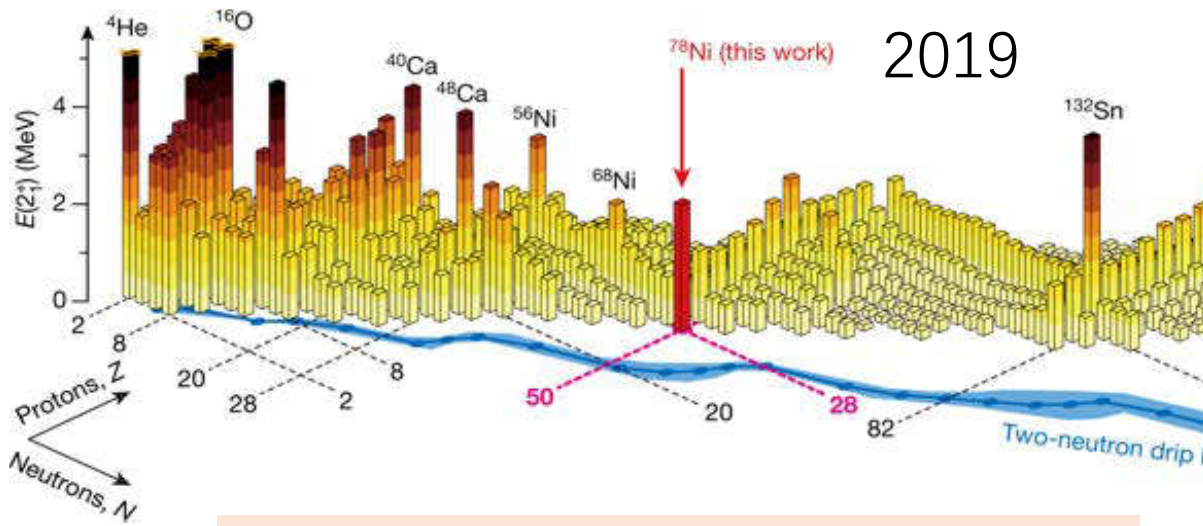


Physics Viewpoint: Doubly Magic Nickel

2017

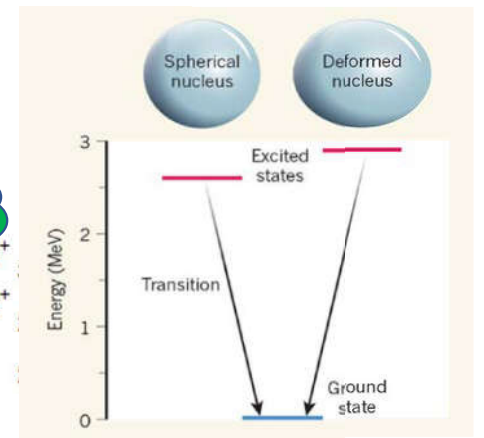
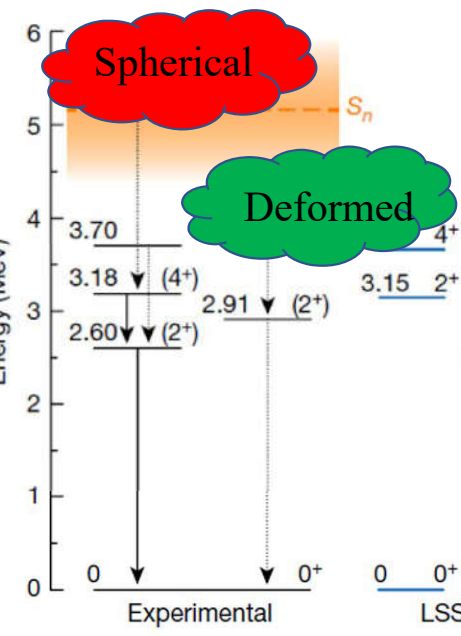
Two independent experiments on the isotope copper-79 confirm that its nuclear neighbor nickel-78 is indeed a doubly magic nucleus.

A. Welker *et al.* L. Olivier *et al.*
 PRL119(2017)192502; PRL119(2017)192501

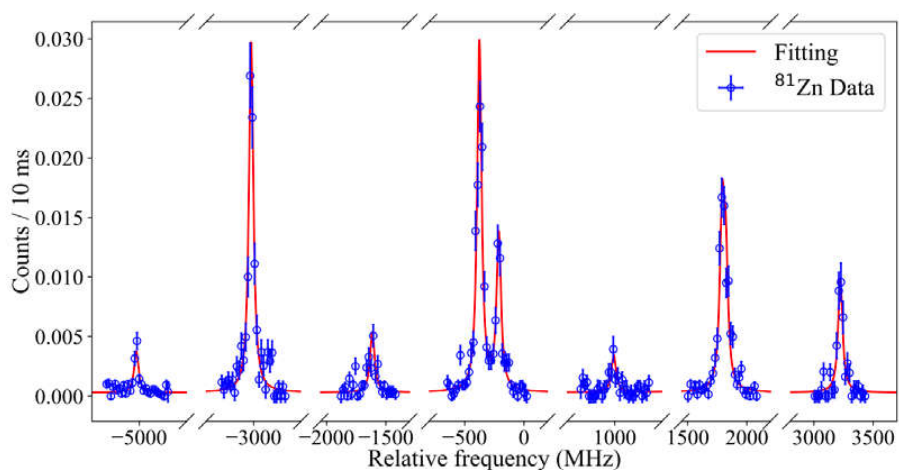



Deformed g.s. for more exotic nickel isotopes ($N > 50$) are suggested! !

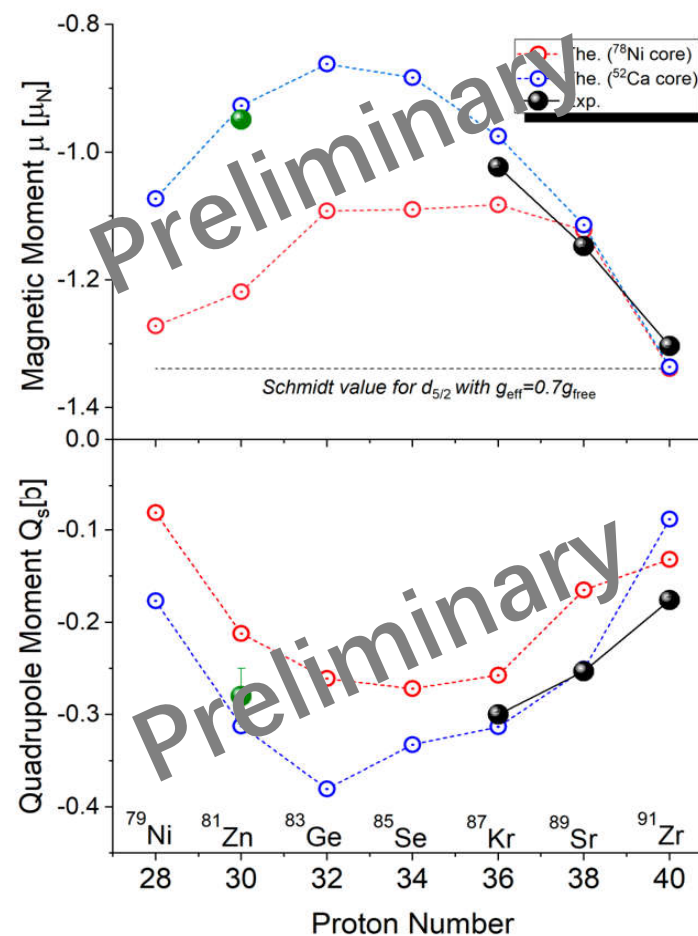
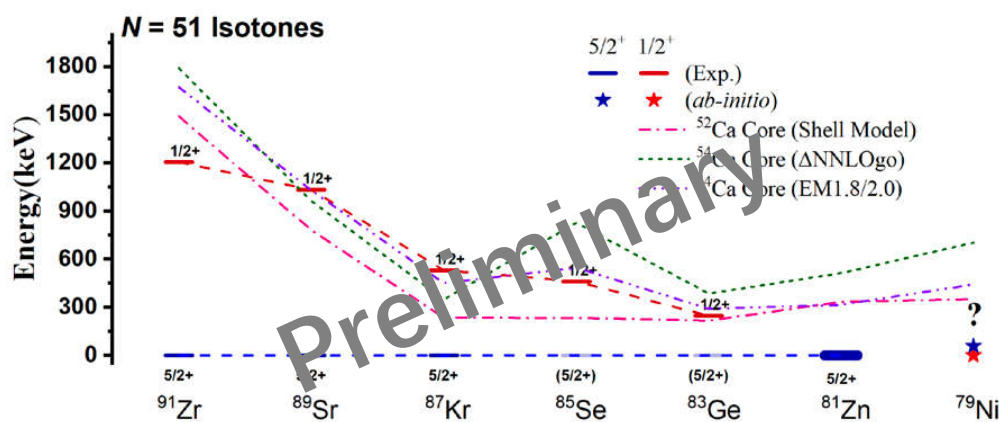
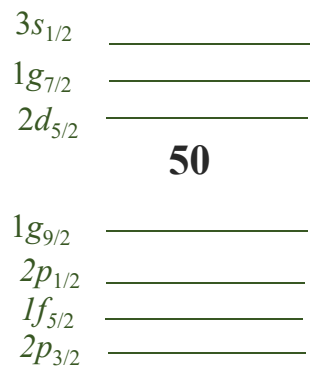
R. Taniuchi, et al. Nature 569 (2019) 53



e.g. Nuclear shapes in neutron-rich Ni region (deformation in $^{81,82}\text{Zn}$?)

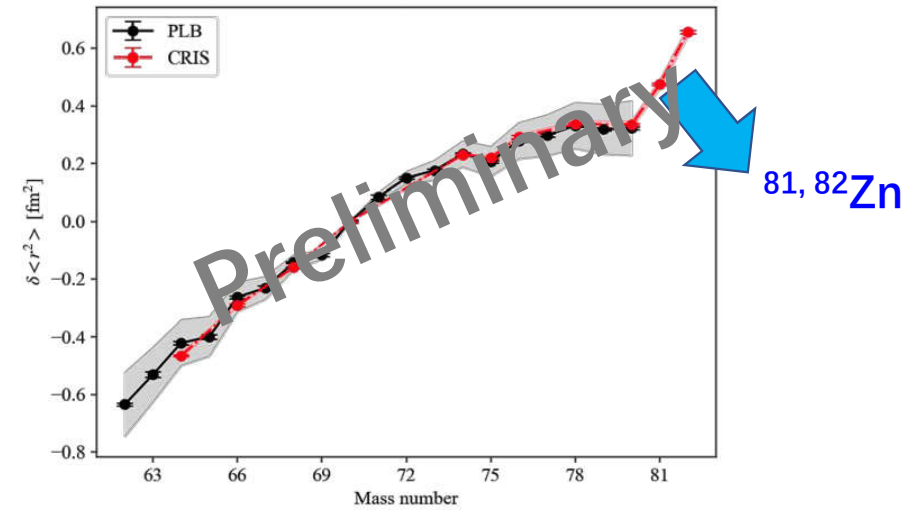
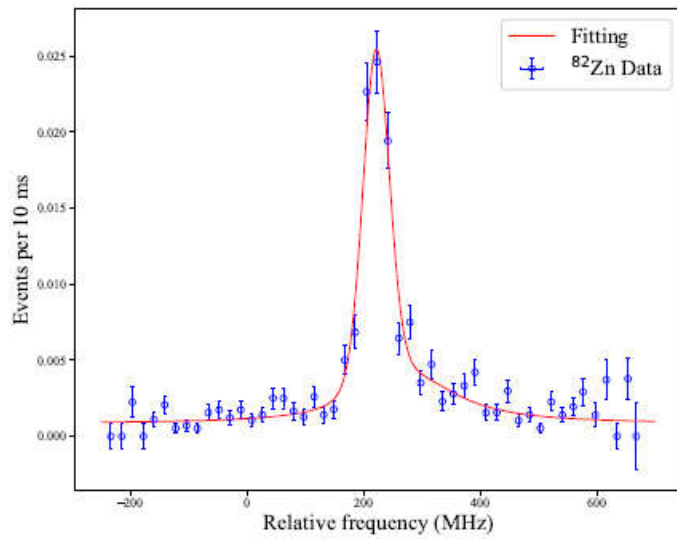
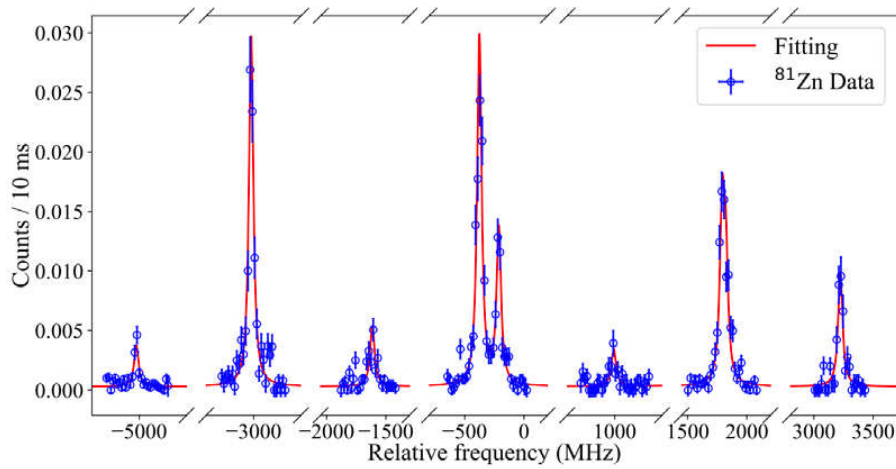


Spin $I = 5/2^+$

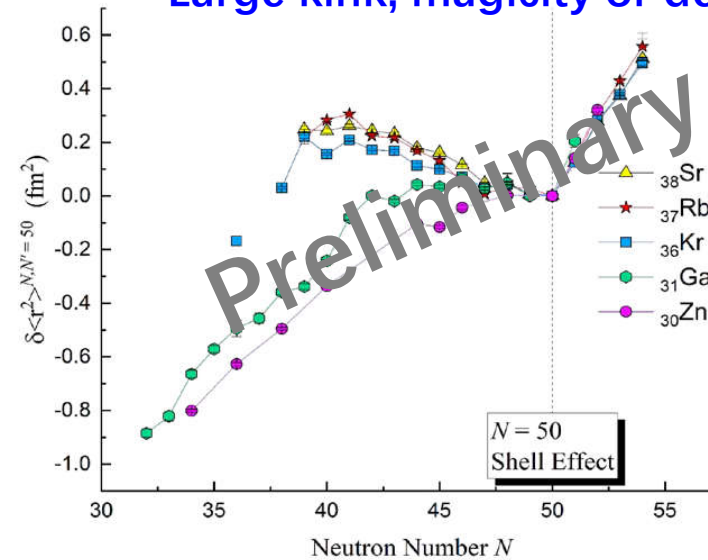


Cross-core excitations of ^{78}Ni is needed to reproduce ^{81}Zn moments

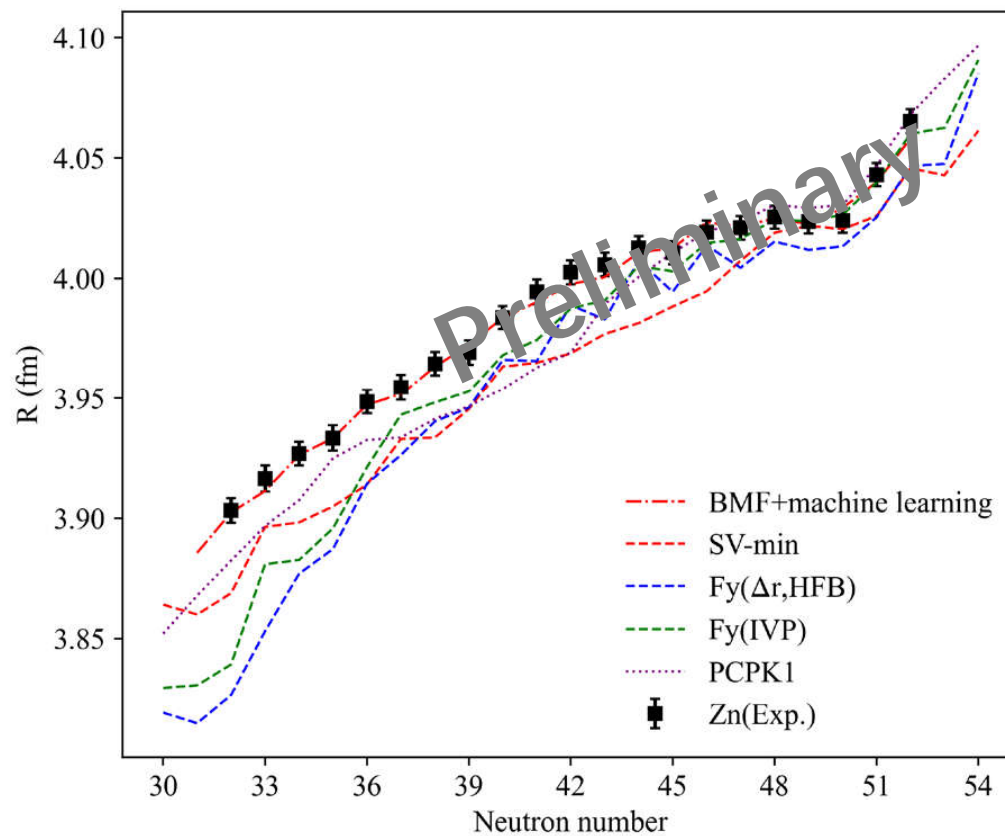
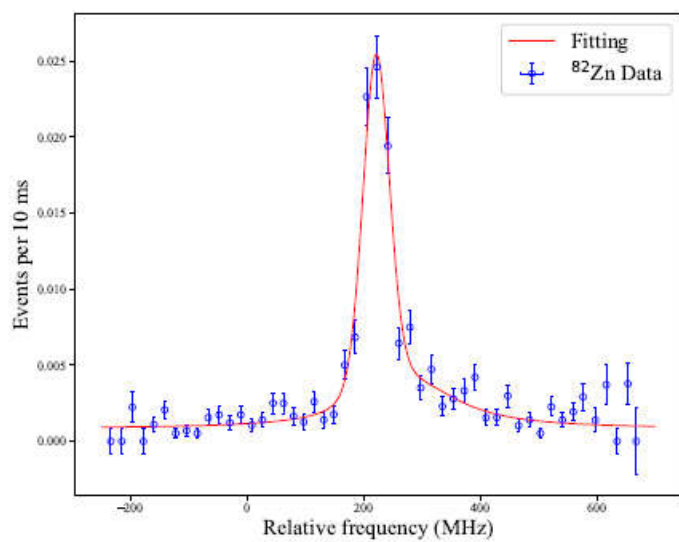
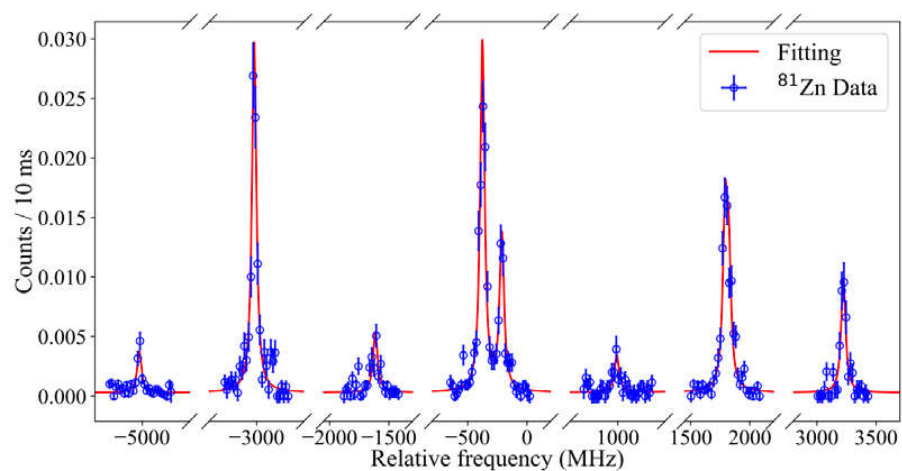
e.g. Nuclear shapes in neutron-rich Ni region (deformation in $^{81,82}\text{Zn}$)



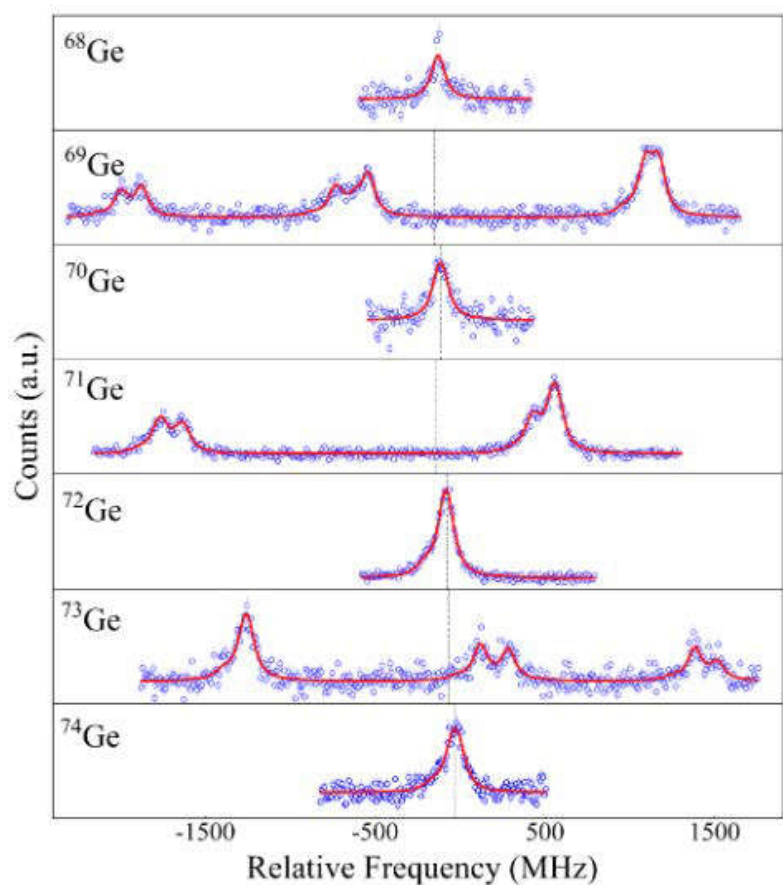
Large kink, magicity or deformation?



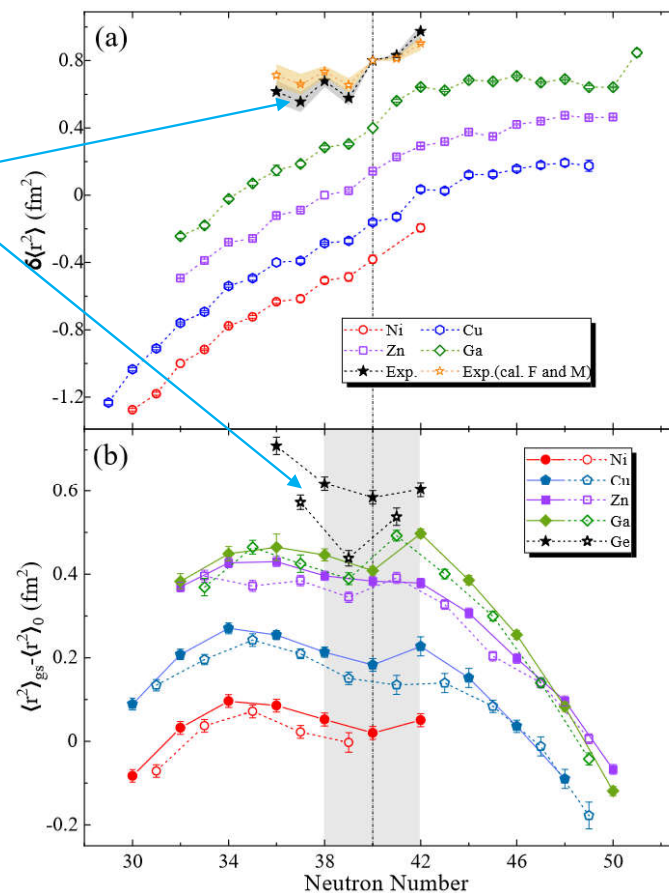
e.g. Nuclear shapes in neutron-rich Ni region (deformation in $^{81,82}\text{Zn}$?)



e.g. Nuclear shapes in neutron-rich Ni region (deformation in Ge around $N = 40$)



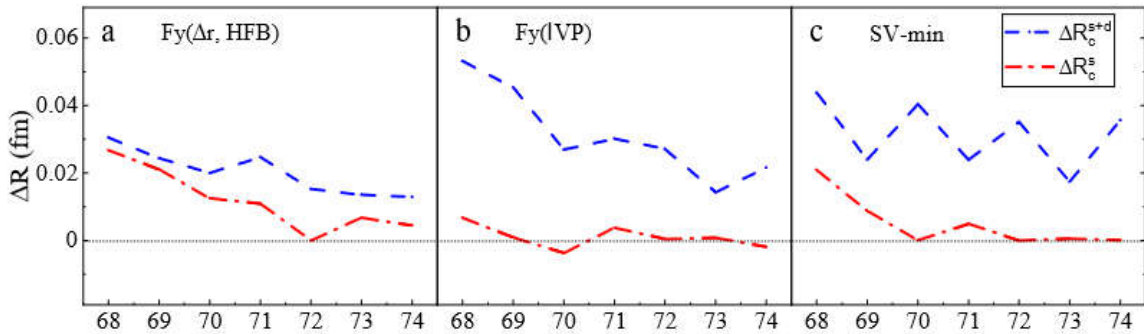
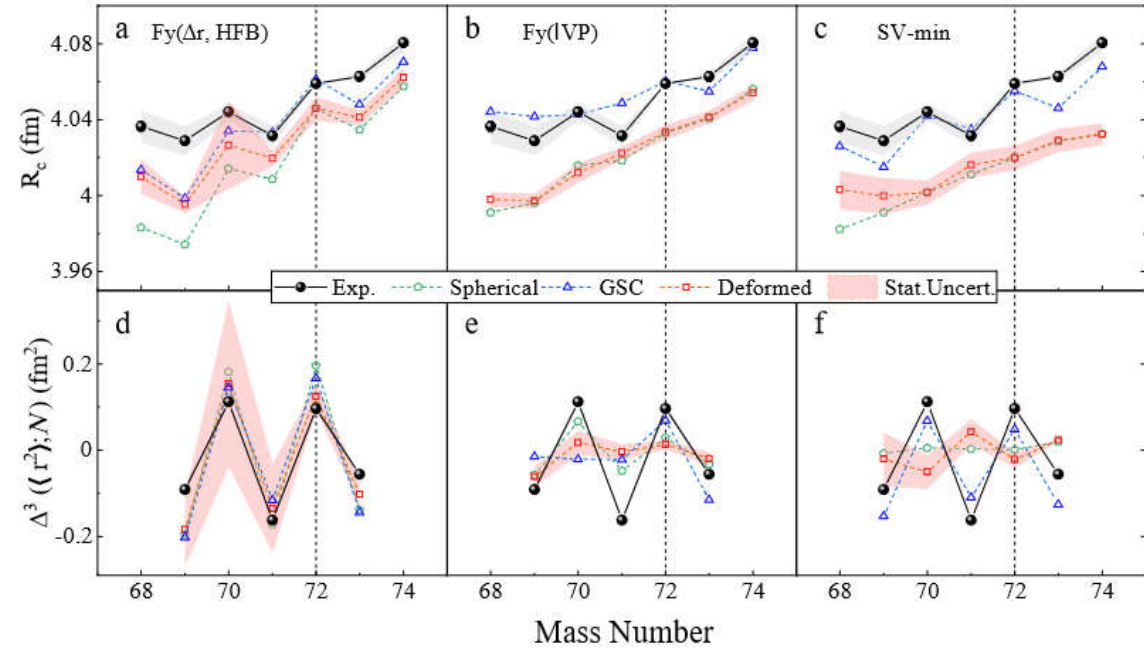
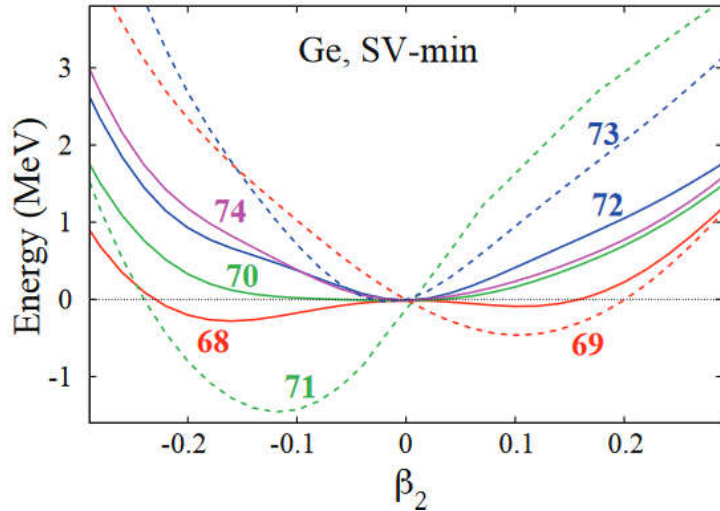
Ge radii



Enhanced even-odd staggering (OES) is observed in the charge radii of Ge isotopes around $N = 40$

[S.J. Wang, A. Kanellakopoulos, X.F. Yang et al., Submitted to PLB \(2024\), arXiv preprint arXiv:2404.06046](#)

e.g. Nuclear shapes in neutron-rich Ni region (deformation in Ge around $N = 40$)



$$\Delta R_c^s \equiv R_c^{\text{Deformed}} - R_c^{\text{Spherical}}$$

- from the static deformation

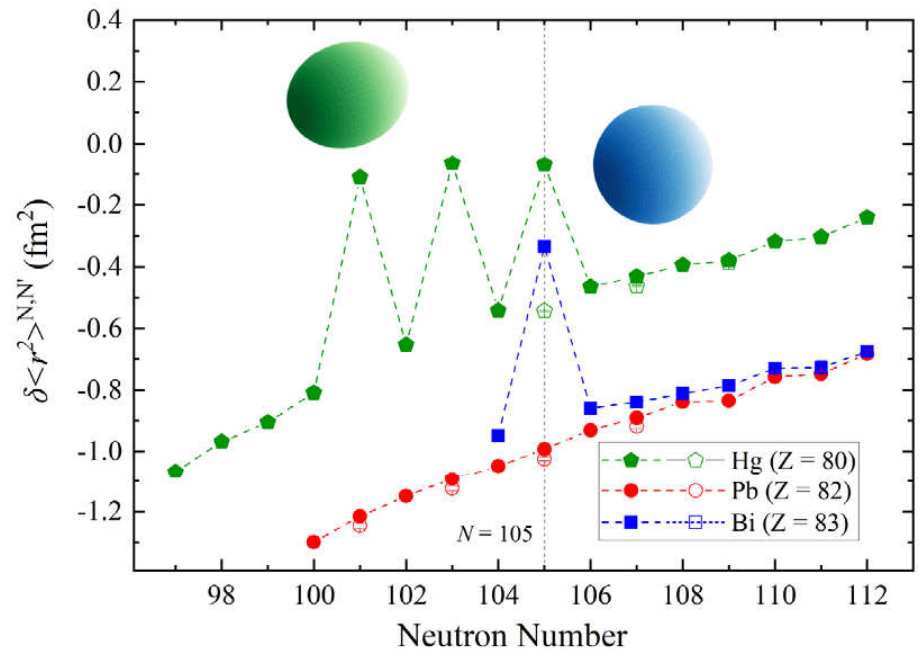
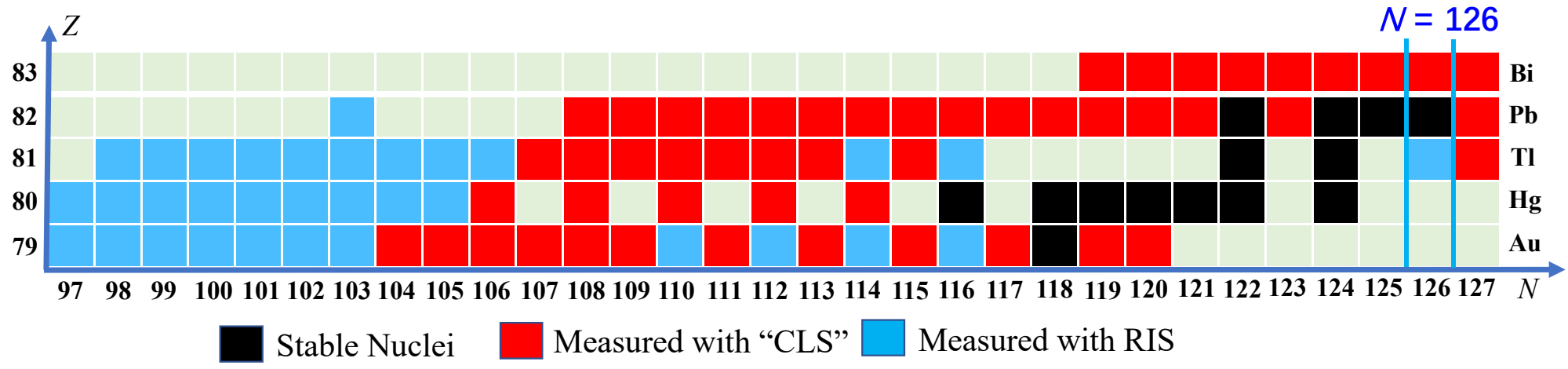
$$\Delta R_c^{s+d} \equiv R_c^{\text{GSC}} - R_c^{\text{Spherical}}$$

- from the static deformation
+dynamic fluctuations

Both pairing and deformation contribute to the enhanced OES in the Ge charge radii around $N = 40$

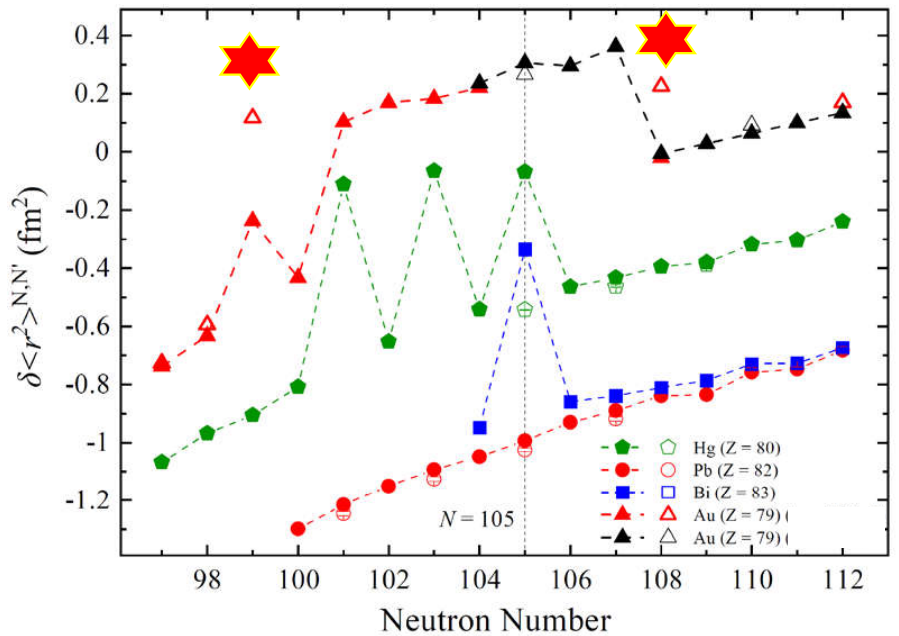
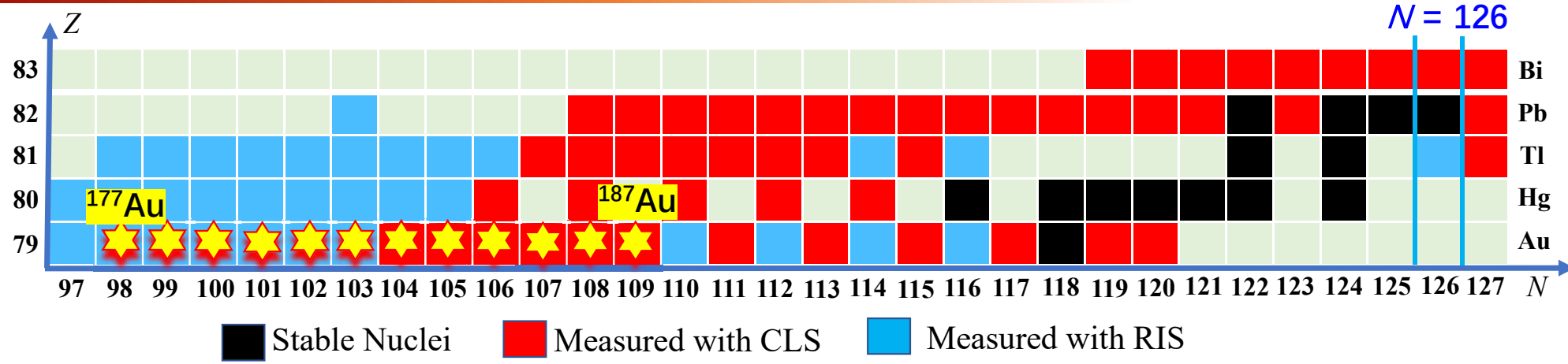
S.J. Wang, A. Kanellakopoulos, X.F. Yang et al., Submitted to PLB (2024), arXiv preprint arXiv:2404.06046

e.g. Nuclear shapes in neutron-deficient lead region



- Large shape staggering in Hg from $N = 105$ to 100**
 MCSM: interplay between monopole and quadrupole interactions driving a quantum phase transition
B. A. Marsh, et al. Nat. Phys. 14, 1163-1167(2018)
- Same phenomenon in Bi isotopes around $N = 105$**
A. Barzakh, et al. Phys. Rev. Lett. 127, 192501(2021)
- Pb isotopes remain spherical down to $N = 101$**
H. De. Witte et al., Phys. Rev. Lett., 98, 112502 (2007)

e.g. Nuclear shapes in neutron-deficient lead region (Island of deformation in Au?)

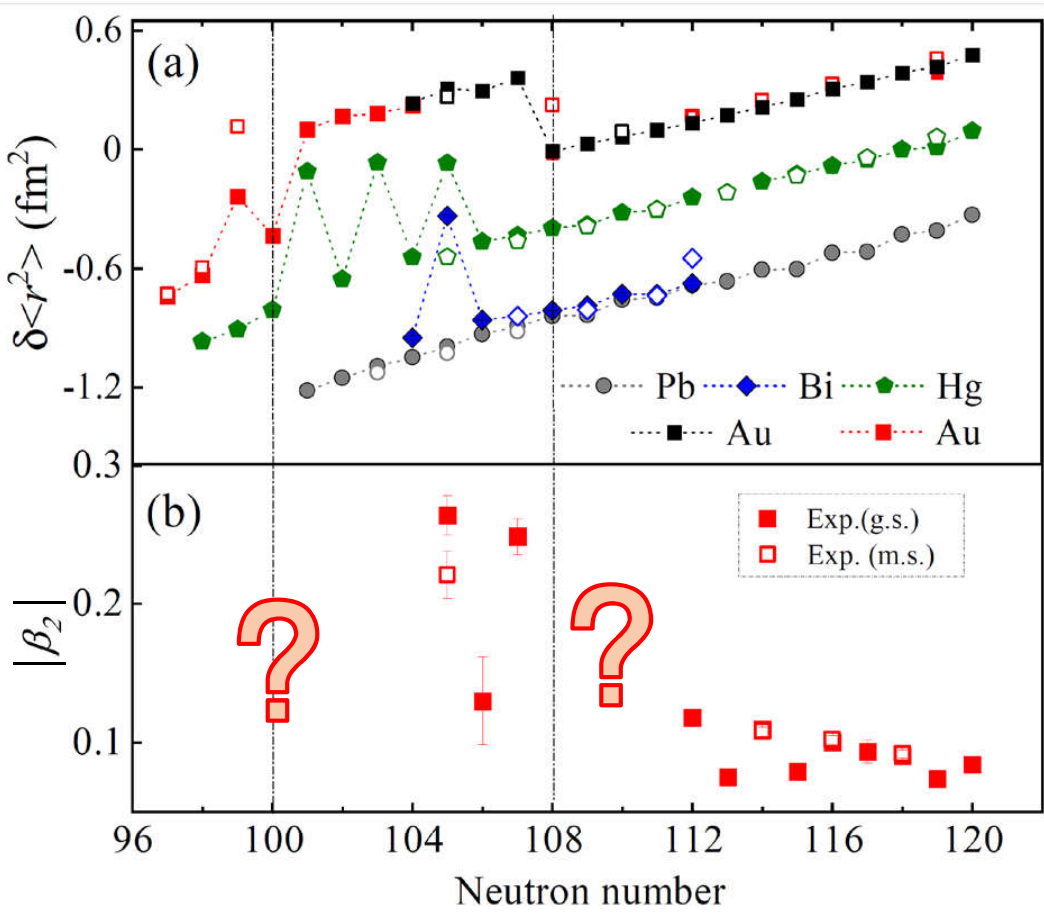


The scenario is very different in Au (Z = 79)

- A sudden onset of strong deformation with at N = 107
K. Wallmeroth et al., Nuclear Physics A 493, 224 (1989)
- Deformation remains constantly large down to N = 101
- Deformation ends at N ~100?
J. G. Cubiss et al. Phys. Rev. Lett. 131, 202501 (2023)
- Large isomer shifts found in ^{178,187}Au

A region called “island of deformation”

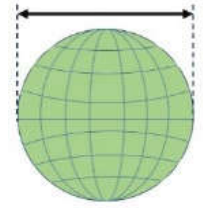
e.g. Nuclear shapes in neutron-deficient lead region (Island of deformation in Au?)



$$\langle \beta_2^2 \rangle = \langle \beta_2 \rangle^2 + (\langle \beta_2^2 \rangle - \langle \beta_2 \rangle^2) = \beta_{\text{static}}^2 + \beta_{\text{dynamic}}^2$$

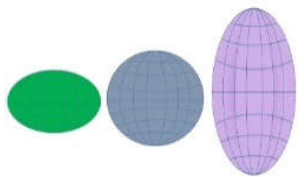
$$\langle r^2 \rangle = \langle r^2 \rangle_0 \left(1 + \frac{5}{4\pi} \langle \beta_2^2 \rangle \right)$$

Nuclear Charge radii
 => static deformation
 +dynamic fluctuations



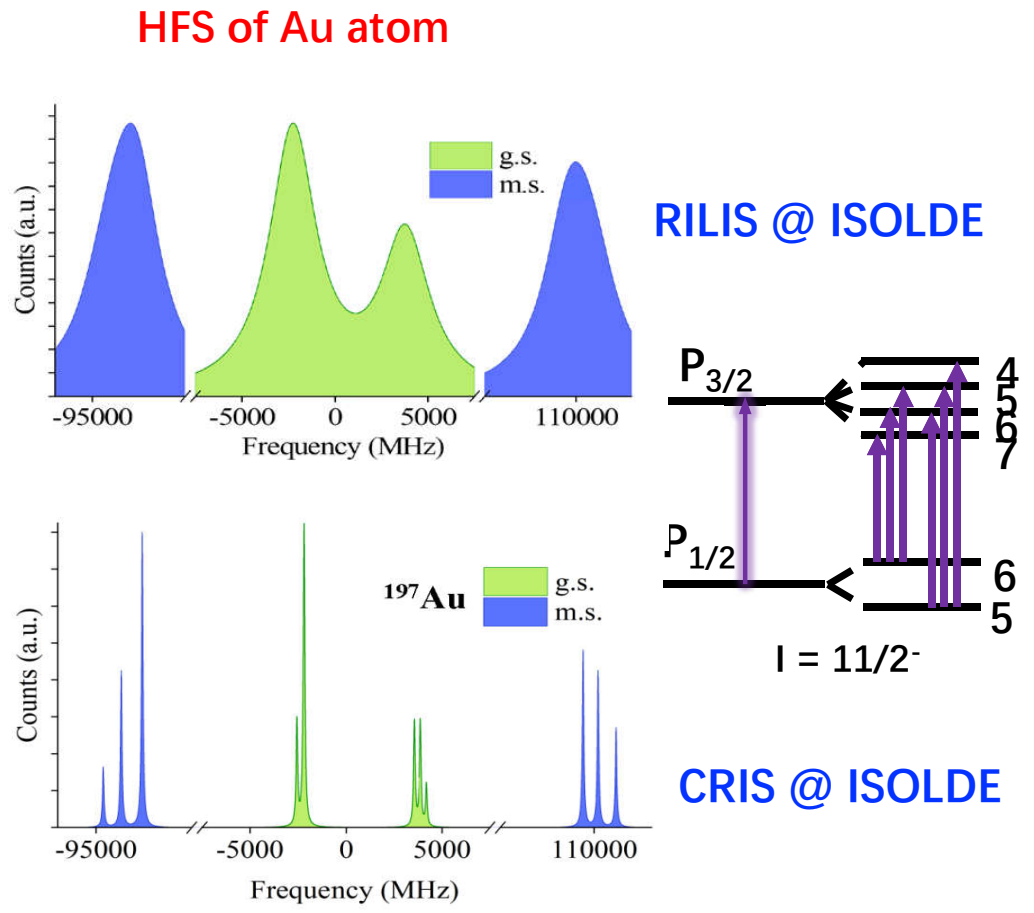
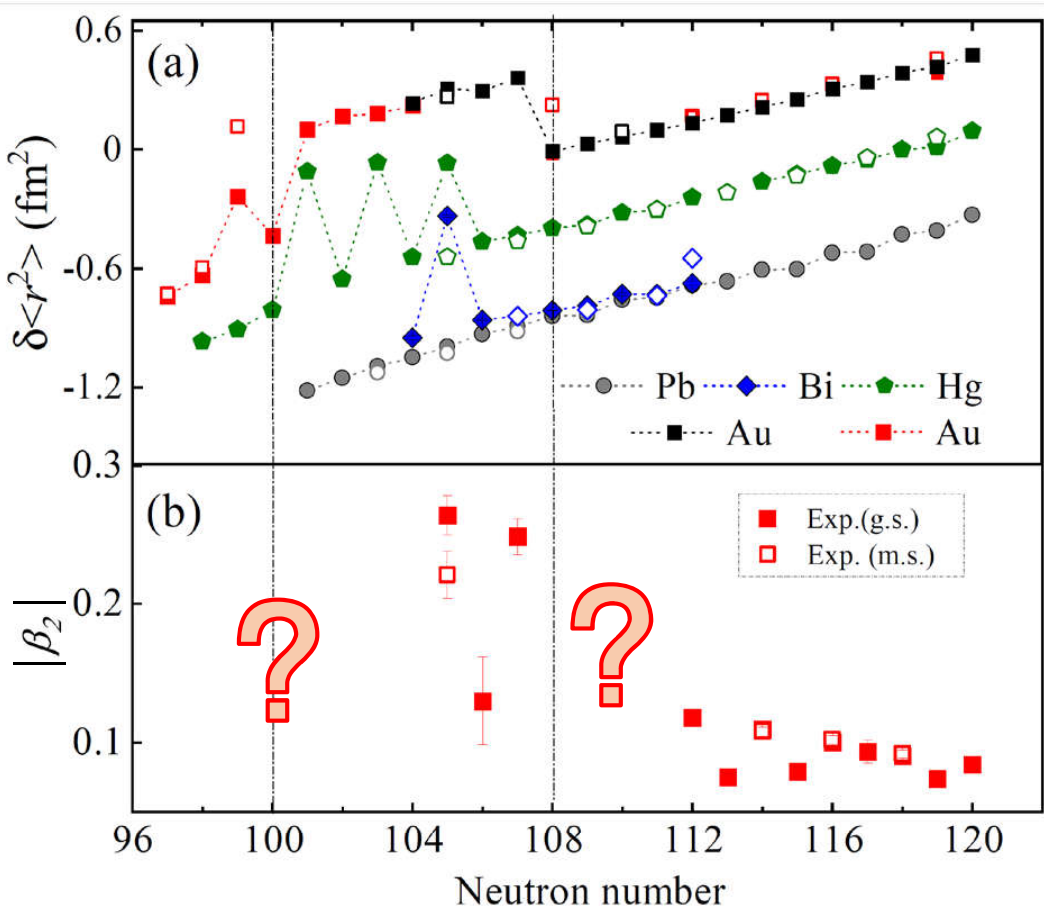
$$Q_{\text{intr.}} = \frac{3}{\sqrt{5\pi}} Z R_0^2 \beta_2 (1 + 0.36 \beta_2)$$

Quadrupole moment
 => static deformation



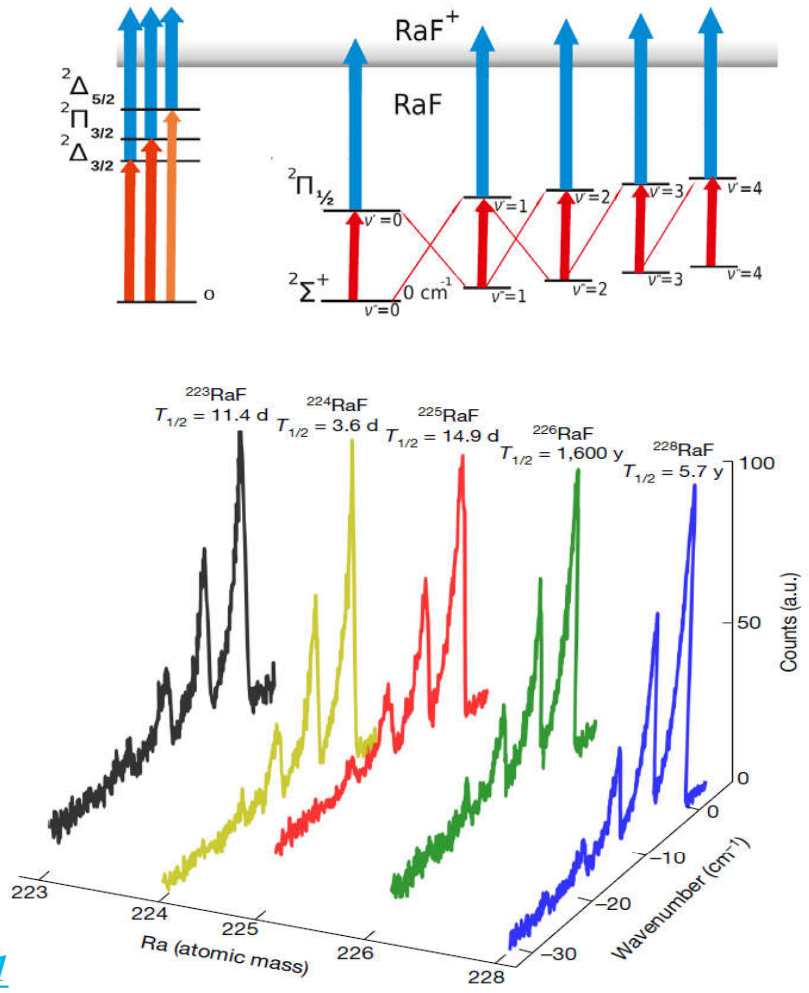
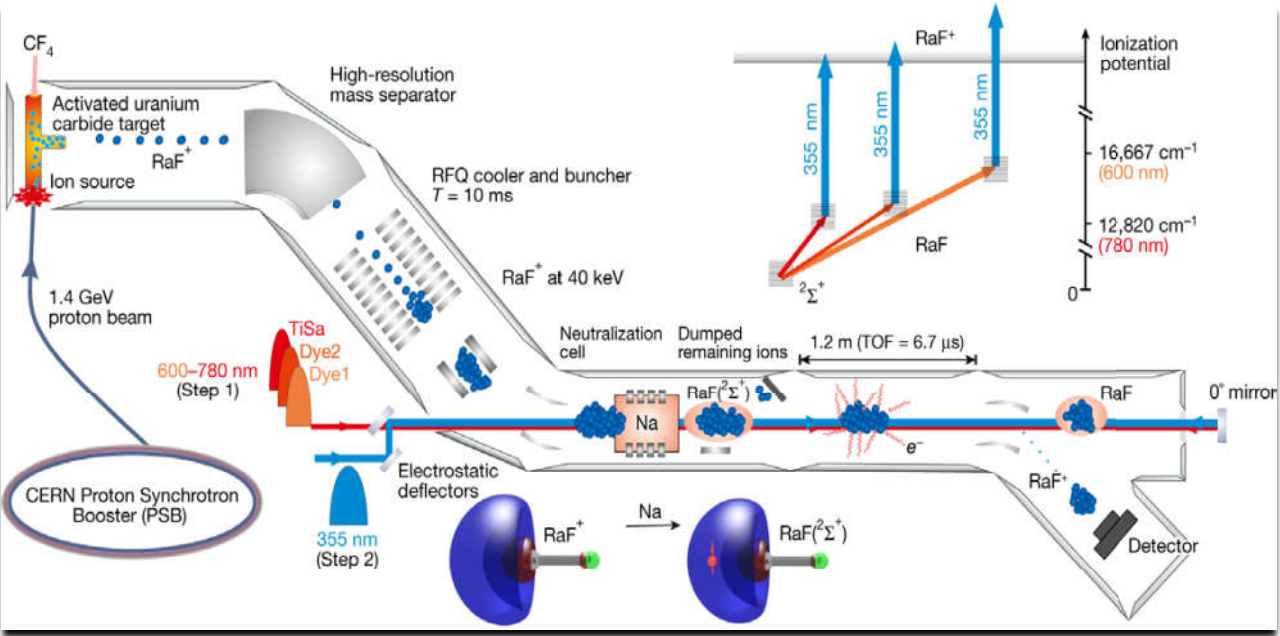
X.F. Yang et al., CERN-INTC-2023-044 ; INTC-P-667(2023)

e.g. Nuclear shapes in neutron-deficient lead region (Island of deformation in Au?)



X.F. Yang et al., CERN-INTC-2023-044 ; INTC-P-667(2023)

e.g. Nuclear information from radioactive molecules



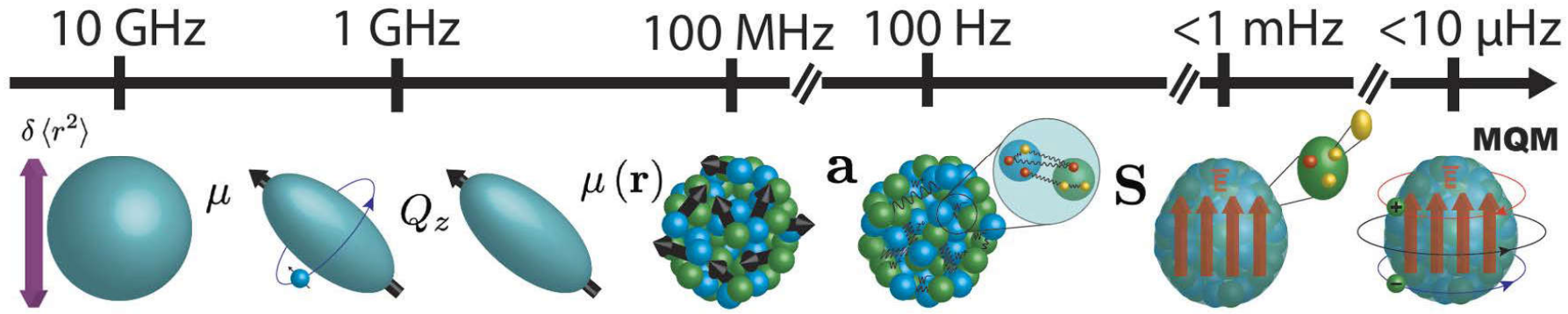
$$H_{\text{Mol.}} = H_{el} + H_{\text{vib.}} + H_{\text{rot.}} + H_{\text{hfs}}$$

☑
☑
☑
☑

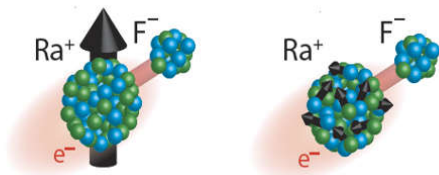
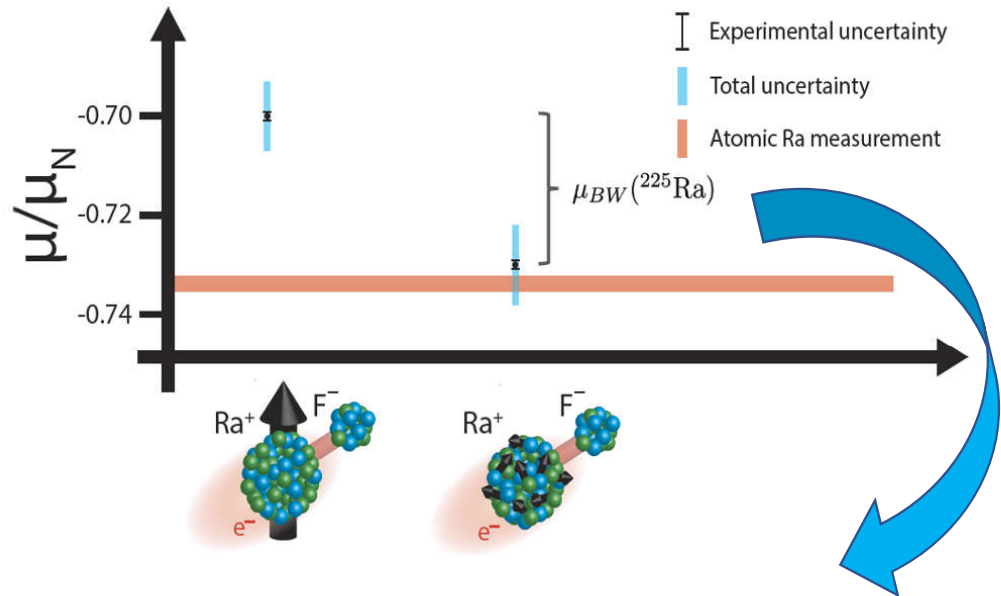
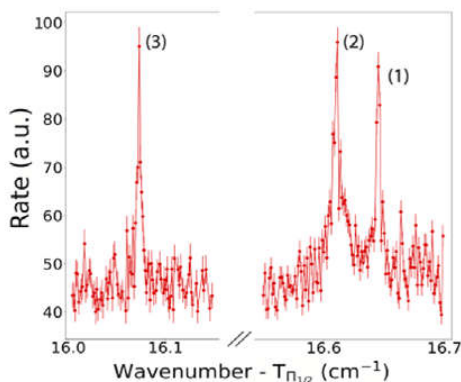
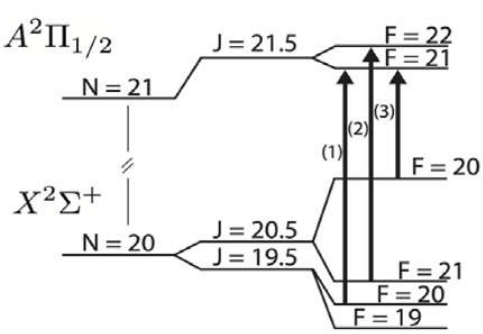
[Nature 581, 396 \(2020\)](#) ; [PRL 127,033001\(2021\)](#)
[Nat. Phys. 20, 202 \(2024\)](#) ; [Science, under review \(2023\)](#) [arXiv.2311.04121](#)

<https://isolde-cris.web.cern.ch/>

e.g. Nuclear information from radioactive molecules



$^{225}\text{Ra}^{19}\text{F}$, $Z = 88$



<https://doi.org/10.48550/arXiv.2311.04121>

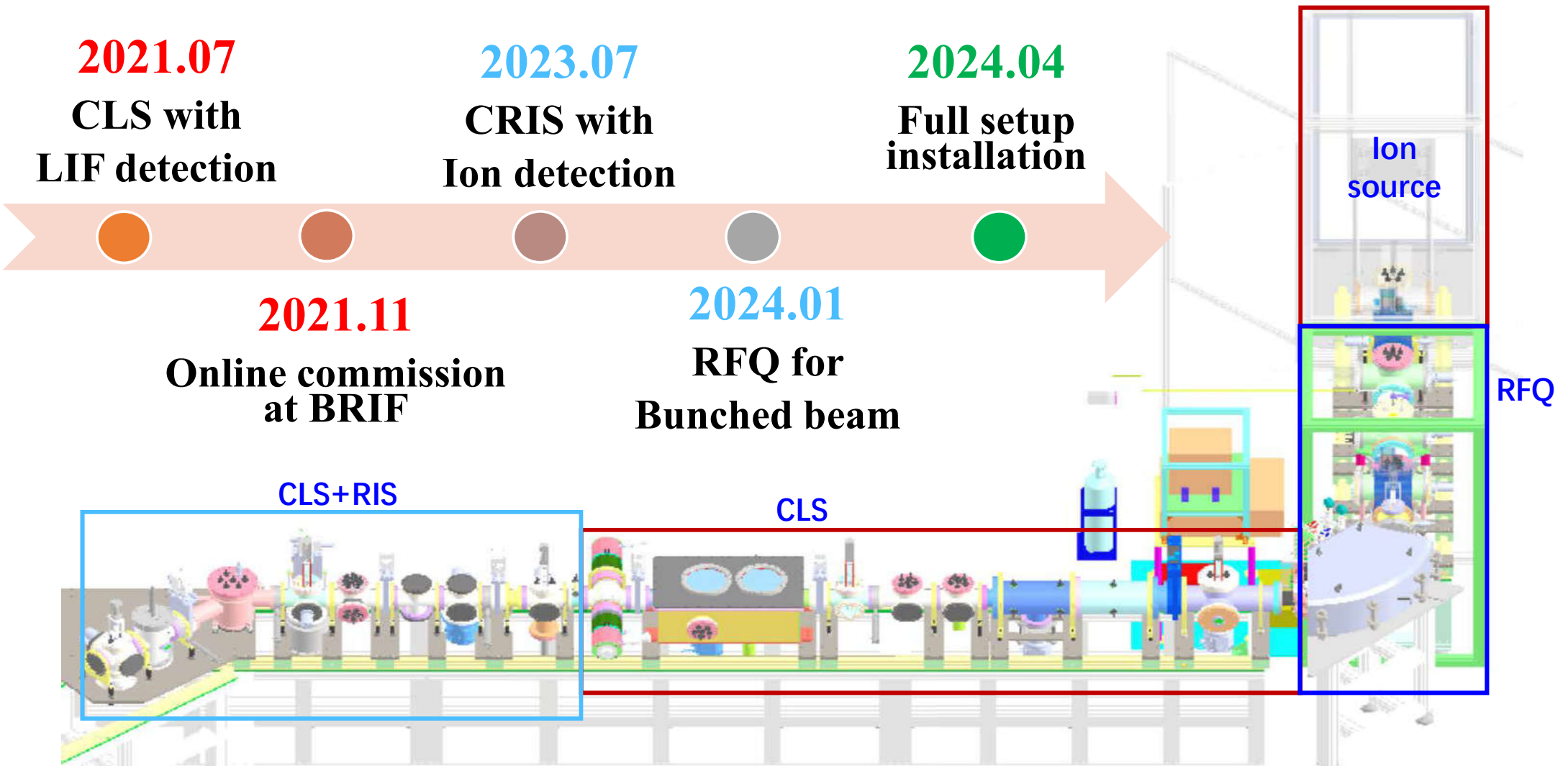
Bohr-Weisskopf effect (BW) arising from the non-uniform distribution of magnetization over the nucleus

Outline



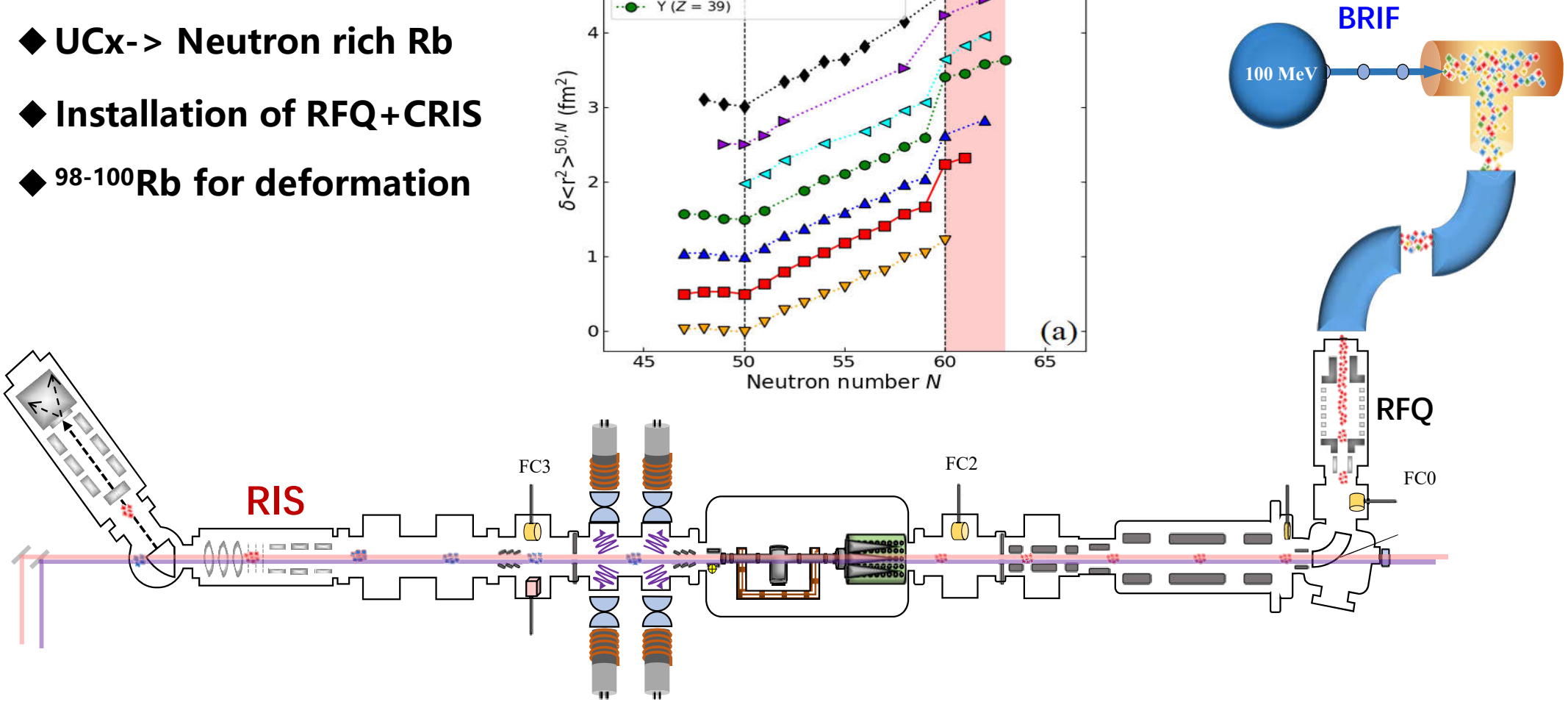
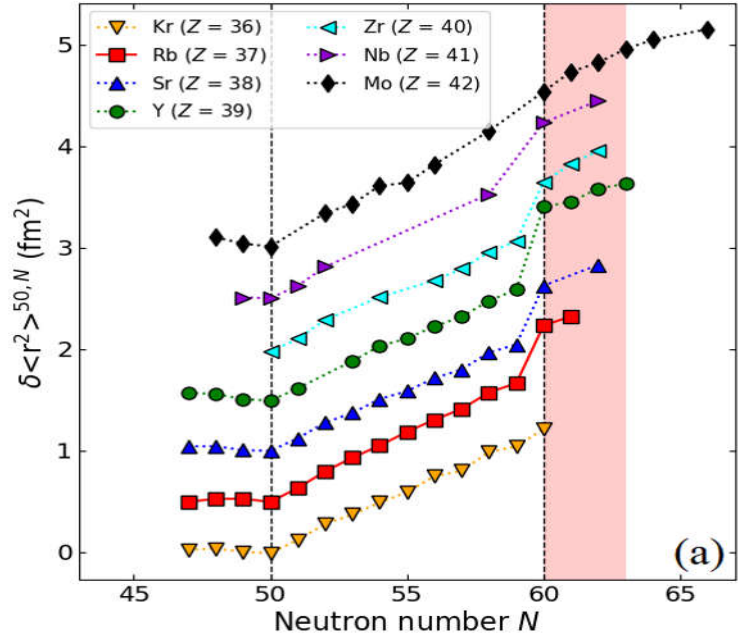
- Nuclear structure and g.s. properties
- Hyperfine interaction and laser spectroscopy
- Nuclear structure studied from laser spectroscopy
- **Laser spectroscopy development and near future work**

Laser spectroscopy development in China (PKU, CIAE, IMP, LZU)

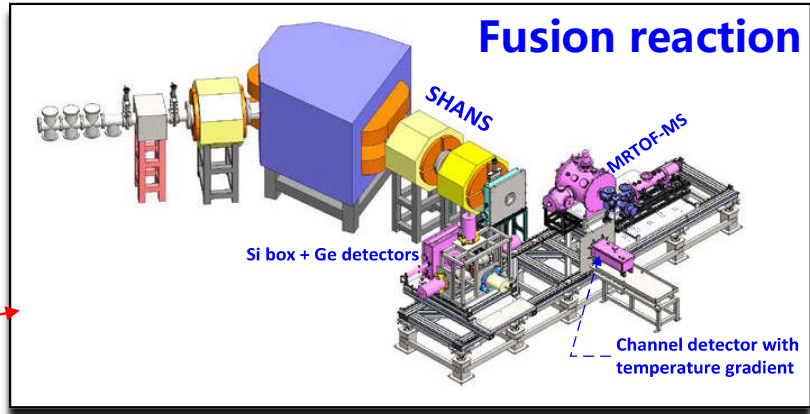
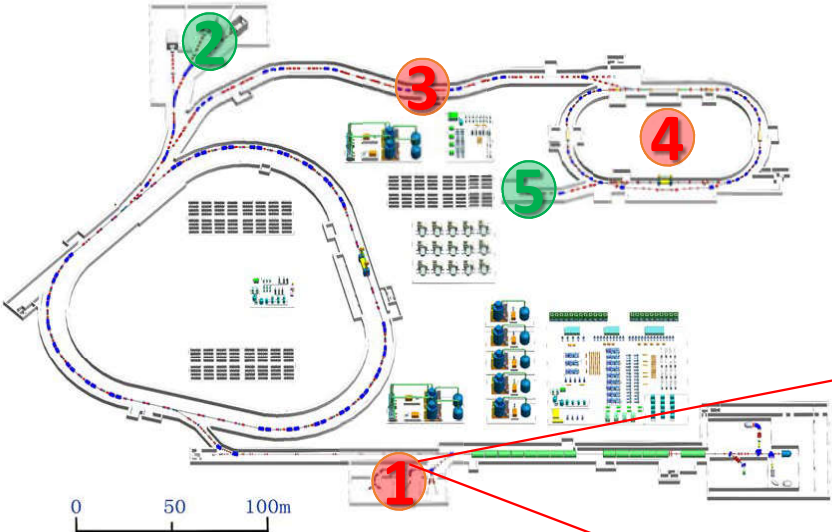


Near future work: CRIS @BRIF-CIAE

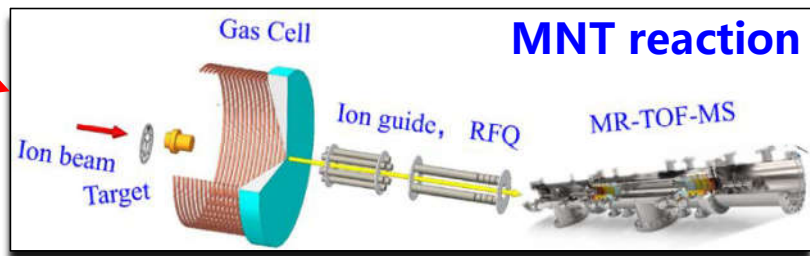
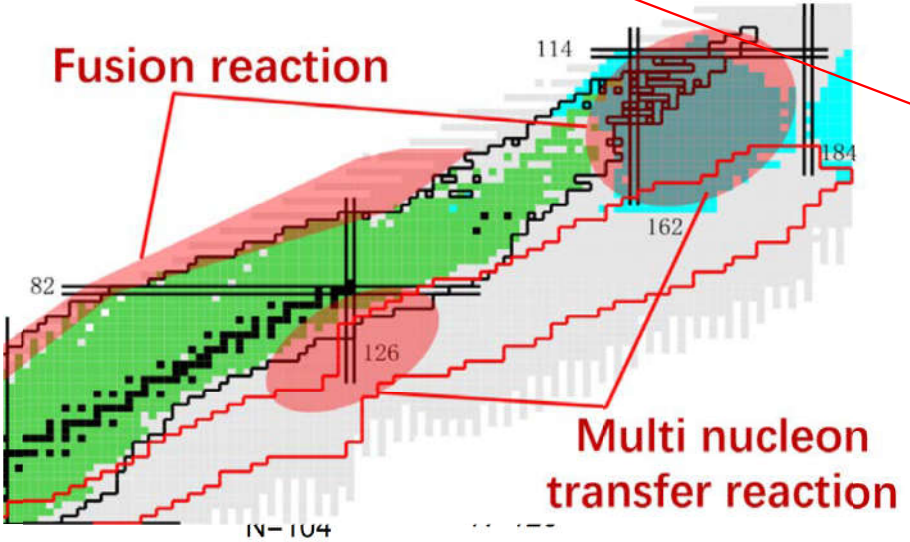
- ◆ UCx-> Neutron rich Rb
- ◆ Installation of RFQ+CRIS
- ◆ ⁹⁸⁻¹⁰⁰Rb for deformation



Near future work: CRIS @HIAF-IMP



- MR-TOF
 - Decay spectroscopy
 - Collinear laser spectroscopy
-

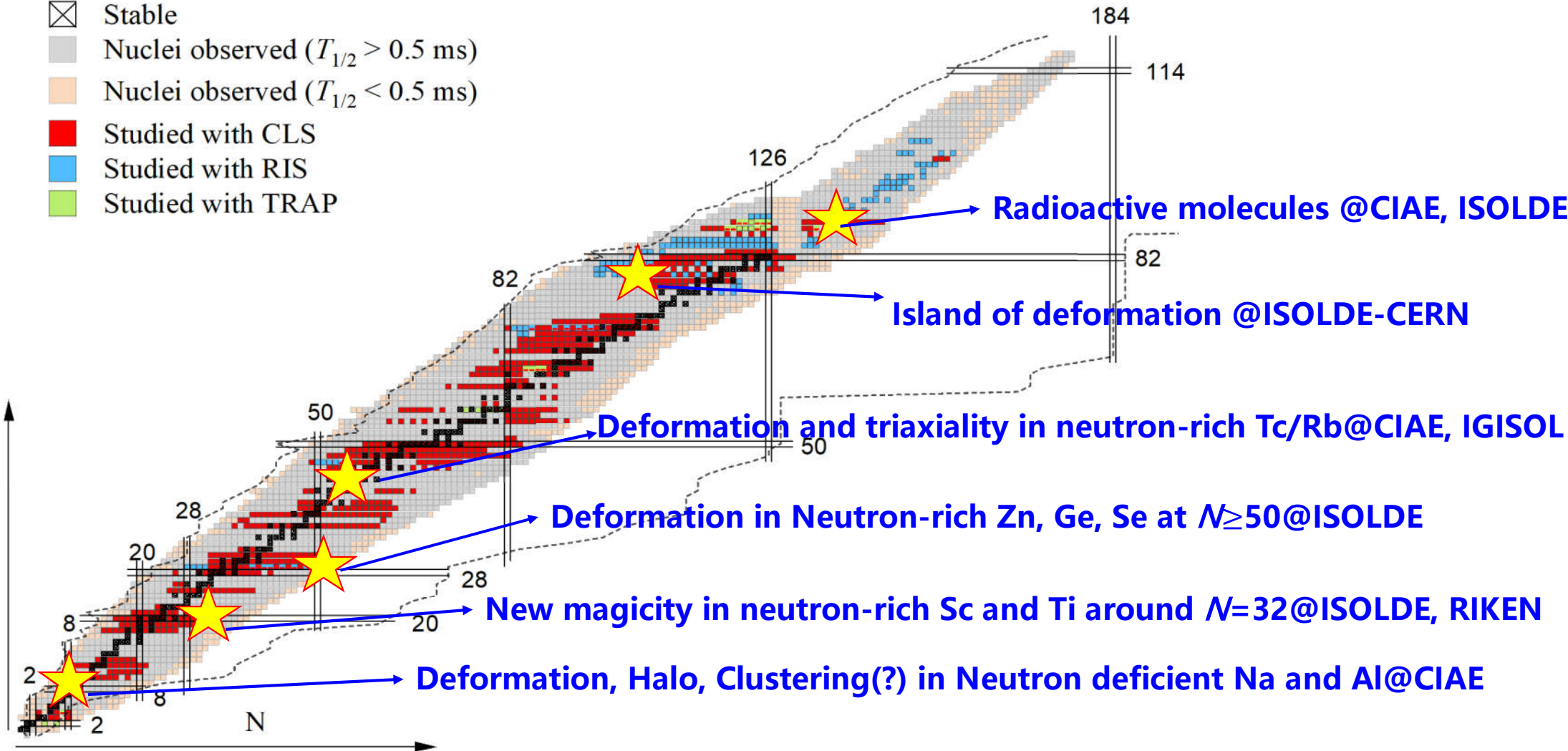


- MR-TOF
 - Decay spectroscopy
 - Collinear laser spectroscopy
-

Near future work: more exotic cases

Approved or planned experiments

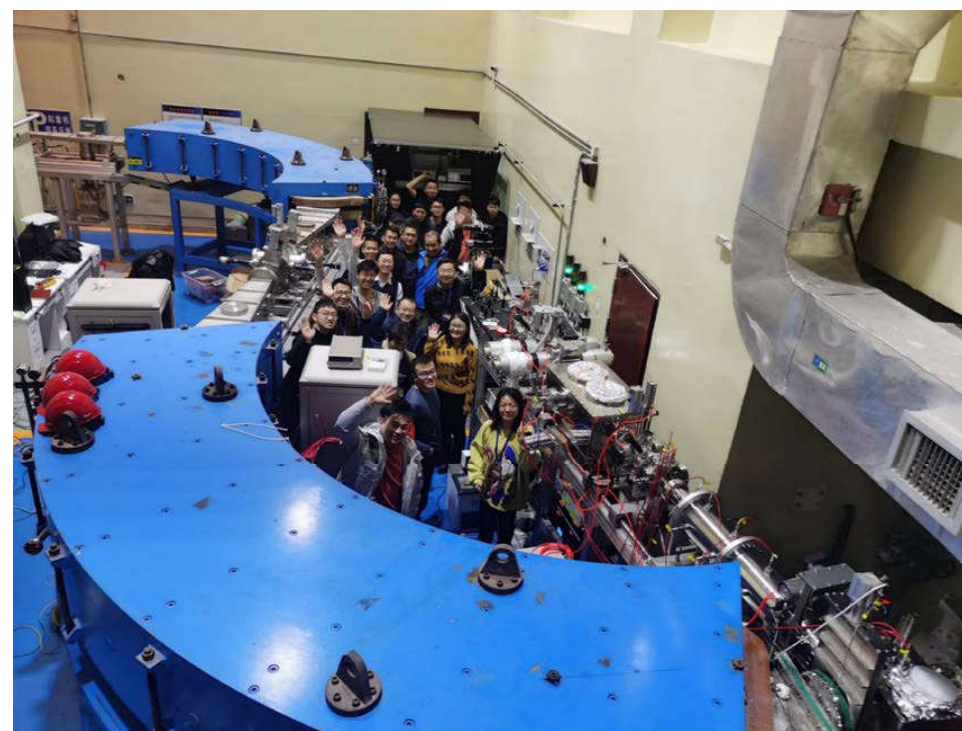
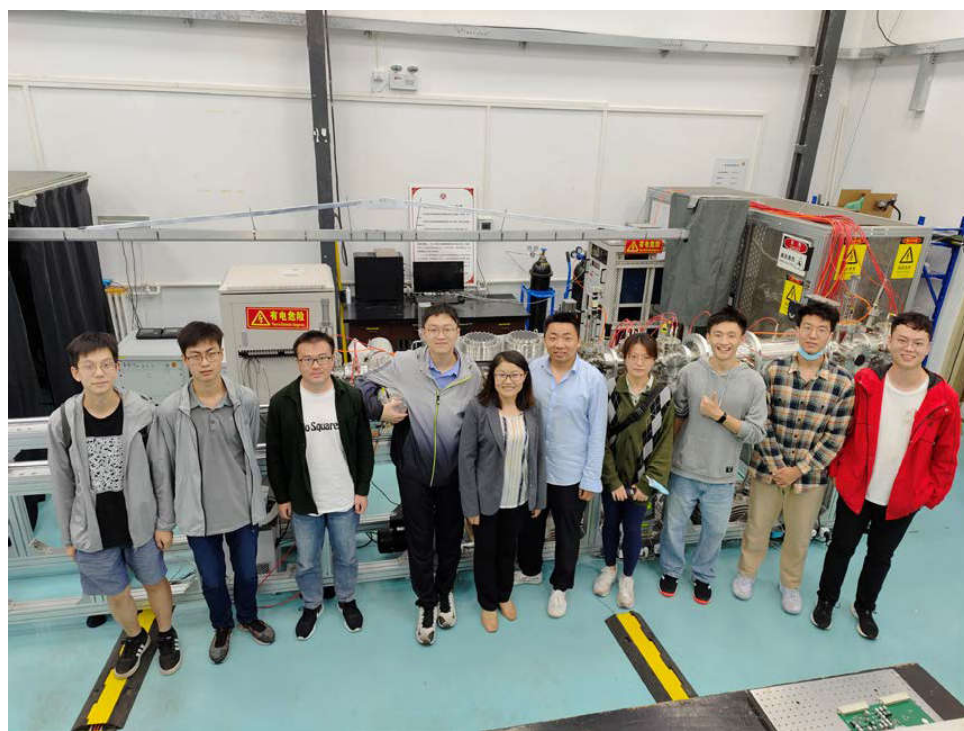
- ☒ Stable
- Nuclei observed ($T_{1/2} > 0.5$ ms)
- Nuclei observed ($T_{1/2} < 0.5$ ms)
- Studied with CLS
- Studied with RIS
- Studied with TRAP





北京大學
PEKING UNIVERSITY

Thanks for your attention!

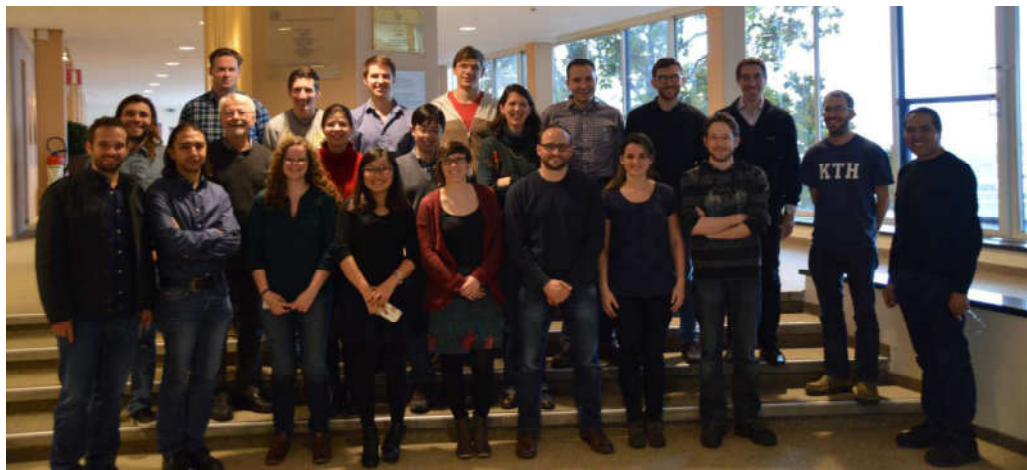




北京大學
PEKING UNIVERSITY

Thanks for your attention!

<https://collaps.web.cern.ch/>



<https://isolde-cris.web.cern.ch/>

