

# The symmetry energy from ground and excited state properties of atomic nuclei

### Xavier Roca-Maza

**Exploring nuclear physics across energy scales 2024:** 

intersection between nuclear structure and high energy nuclear collisions



Apr 15 - 27, 2024

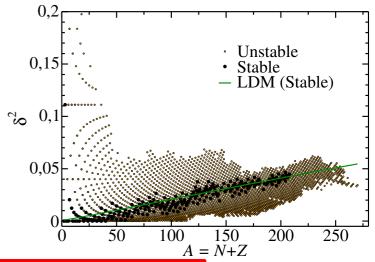
Beijing, China

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### **Nuclear Equation of State (EoS)**

Energy per nucleon (e) as a function of the total density  $\rho = \rho_n + \rho_p$  and the relative difference  $\delta = (\rho_n - \rho_p)/\rho$  for unpolarized uniform matter at T=0 (for connection to properties of finite nuclei in normal conditions) assuming isospin symmetry (even powers of  $\delta$ ). For  $\delta \rightarrow 0$ :



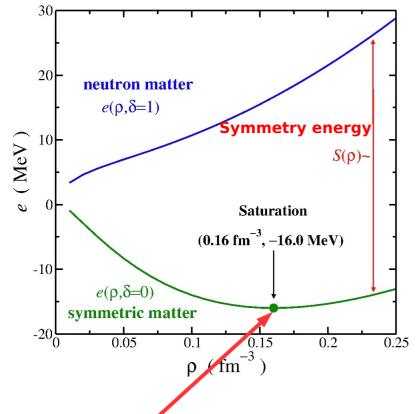
$$e(\rho, \delta) = e(\rho, 0) + S_2(\rho)\delta^2 + S_4(\rho)\delta^4 + \mathcal{O}[\delta^6]$$

Isaac Vidaña, Constança Providência, Artur Polls, and Arnau Rios Phys. Rev. C **80**, 045806 – Published 23 October 2009

# Nuclear Equation of State (EoS)

Unpolarized, uniform nuclear matter at T=0 assuming isospin symmetry

$$e(
ho,\delta)=e(
ho,0)+S_2(
ho)\delta^2$$



It is customary to also **expand**  $e(\rho,0)$  and  $S(\rho)$ around nuclear **saturation density**  $\rho_0 \sim 0.16 \text{ fm}^{-3}$ 

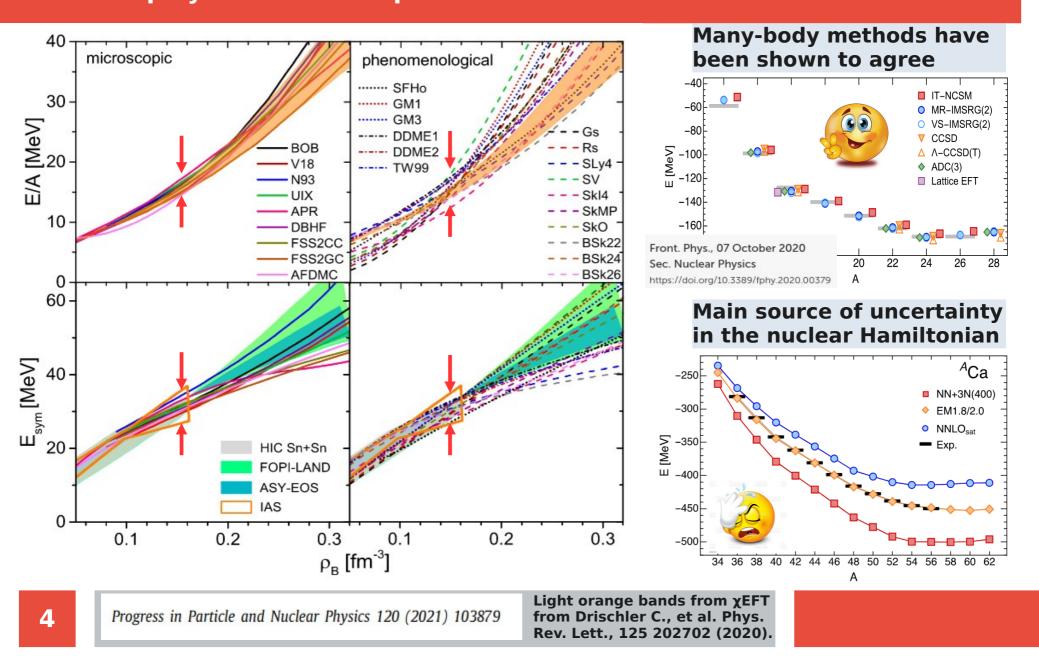
$$e(\rho, 0) = e(\rho_0, 0) + \frac{1}{2}K_0x^2 + \mathcal{O}[\rho^3] \text{ where } x = \frac{\rho - \rho_0}{3\rho_0}$$
$$S(\rho) = J + Lx + \frac{1}{2}K_{\text{sym}}x^2 + \mathcal{O}[\rho^3, \delta^4]$$

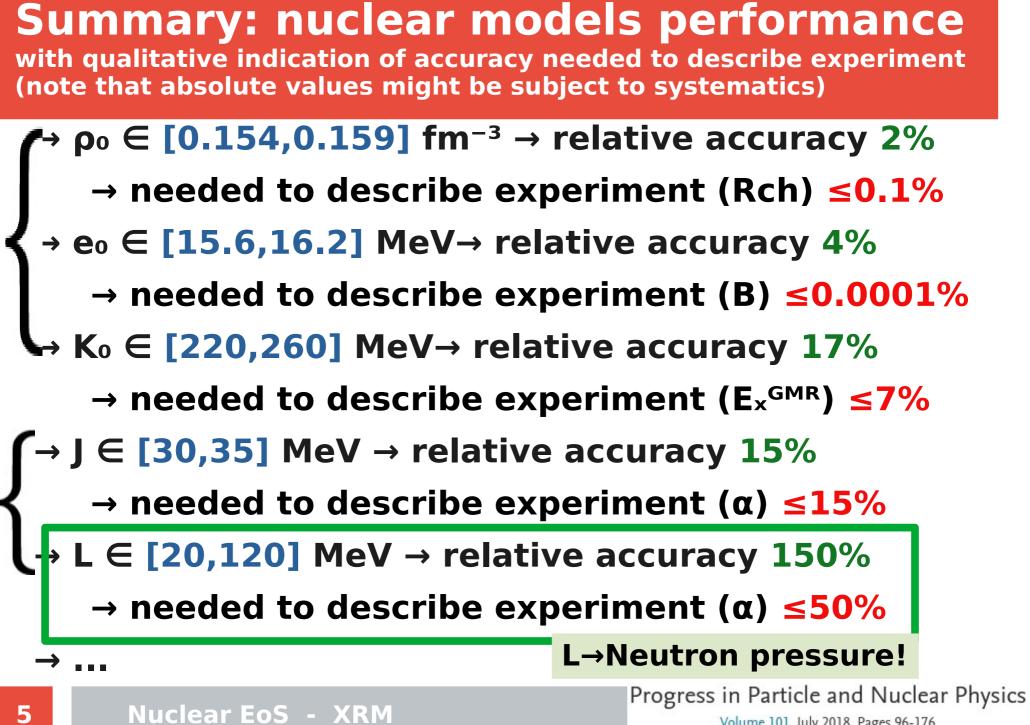
 $K_0 \rightarrow$  how **compressible** is symmetric matter at  $\rho_0$ 

 $J \rightarrow penalty energy$  for converting all protons into neutrons in symmetric matter at  $\rho_0$ 

 $P(\rho = \rho_0, \delta = 0) = 0 \text{ MeV fm}^{-3} \boldsymbol{L} \rightarrow \boldsymbol{pressure}$  in neutron matter at  $\rho_0$ 

### **EoS from current nuclear models** Micorscopic and phenomenological models constrainted by different data display similar discrepances on the EoS





# How one can connect finite nuclear properties with the EoS:

### **Example:** Neutron skin thickness $(\Delta r_{np} = r_n - r_p)$ is a good proxy to L

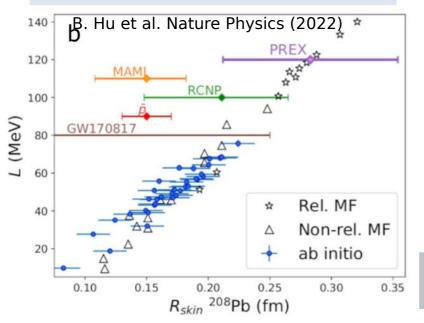
B. Alex Brown Phys. Rev. Lett. 85, 5296 (2000)

 $\Delta r_{np}$  in a heavy neutron rich nucleus is related to the neutron pressure  $(\delta=1)$  around  $\rho_0$  (L).

→ EoS:

$$\overline{P(
ho_0,\delta)}=
ho_0^2rac{\partial e(
ho,\delta)}{\partial
ho}igg|_{
ho=
ho_0}=rac{1}{3}
ho_0\delta^2L$$

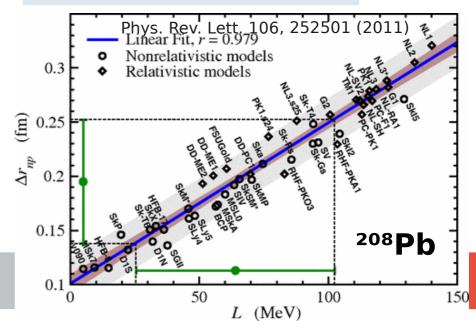
### → Micro & Pheno models:



### → More Pheno models:

 $\Delta r_{np} \approx \frac{1}{12} \frac{N - Z}{A} \frac{R}{I} L$ 

→ Macro Model:



 $\Delta r_{np}$ 

### How to measure $\Delta r_{np}$ ? (just two examples) Parity violating and parity conserving elastic electron scattering

### **Polarized electron-Nucleus scattering:**

 $\Delta r_{ch} = r_{ch}({}^{54}Ni) - r_{ch}({}^{54}Fe) = \Delta r_{np}({}^{54}Fe)$  $\rightarrow$  In good approximation, the weak interaction probes the neutron distribution in nuclei while Coulomb interaction probes the proton distribution 0.066 (a) fim) Phys. Paul-Gerhard Reinhard and Witold Nazarewicz  $A_{pv} = \frac{d\sigma_+/d\Omega - d\sigma_-/d\Omega}{d\sigma_+/d\Omega + d\sigma_-/d\Omega} \sim \frac{\text{Weak}}{\text{Coulomb}}$ HF+EFA (0.77)Rev. (<sup>54</sup>Ni/Fe) 0 0.062 105 HFB Linear Fit, r = 0.995(0.69)L021301 Nonrelativistic models  $R_{\rm ch}^{\rm mir}$ Relativistic models BCS From strong probes 0.058 (0.44)Published 7.2 Large theoretical  $A_{pV}$ uncertainties (b) 0.20 ω 7.0 February 2022  $(^{208}Pb)$ 0.18 **DWBA** 6.8  $R_{\rm skin}$  ( 0.16 HF(0.99)0.14 0.15 0.10.2 0.25 0.3 Small theoretical  $\Delta r_{np}$ (fm)uncertainties 0.12Neutron Skin of 208Pb, Nuclear Symmetry Energy, and the Parity Radius Experiment

X. Roca-Maza, M. Centelles, X. Viñas, and M. Warda Phys. Rev. Lett. 106, 252501 (2011)

Nuclear EoS - XRM

Skyy V. Pineda, Kristian König, Dominic M. Rossi, B. Alex Brown, Anthony Incorvati, Jeremy Lantis, Kei Minamisono, Wilfried Nörtershäuser, Jorge Piekarewicz, Robert Powel, and Felix Sommer Phys. Rev. Lett. **127**, 182503 – Published 29 October 2021

10 20 30 40 50 60 70 80

L (MeV)

Isospin symmetry  $\rightarrow$ 

# Other Observables? Dipole polarizability, J and Δr<sub>np</sub>

The electric dipole **polarizability** measures the **tendency** of the nuclear **charge distribution** to be **distorted** by an **external electric field**.

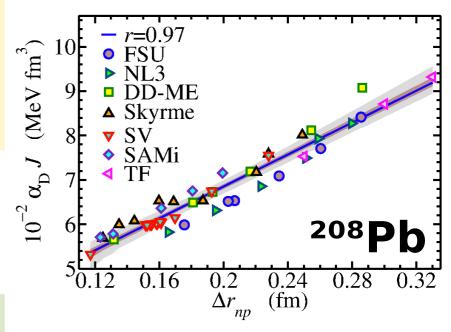
From a macroscopic point of view  $\alpha \sim$  (electric dipole moment)/(Eexternal)

→ For guidance, using the **dielectric theorem**, the polarizability can be calculated assuming the **Droplet model**:  $\alpha_D = \frac{8\pi e^2}{9}m_{-1}(E1)$ 

Meyer et al. NPA385 (1982) 269-284

$$\alpha_{D} \approx \frac{\pi e^{2}}{54} \frac{\langle r^{2} \rangle}{\mathcal{O}} A \left( 1 + \frac{5}{2} \frac{\Delta r_{np} - \Delta r_{np}^{\text{surf}} - \Delta r_{np}^{\text{Coul}}}{\langle r^{2} \rangle^{1/2} (I - I_{\text{Coul}})} \right)$$

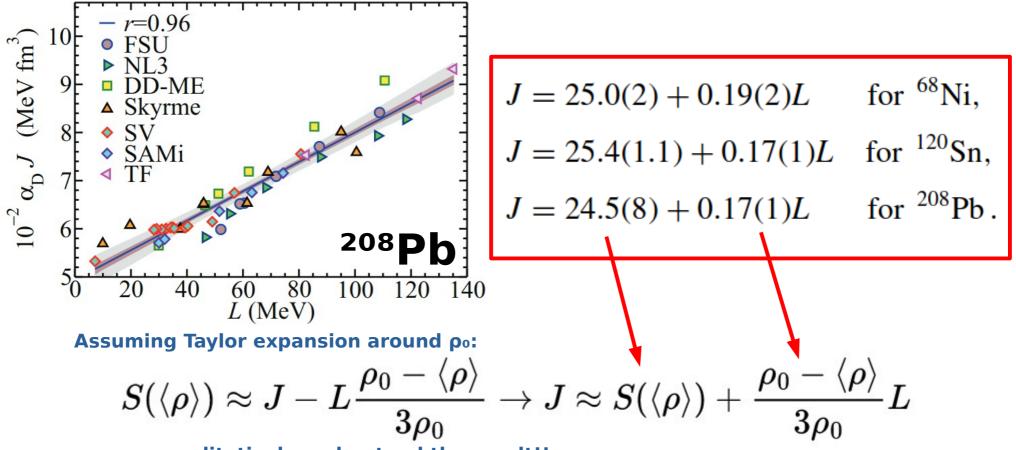
Polarizability increases with the mass (for the dipole  $A^{5/3}$ , for the <u>quadrupole  $A^{7/3}$ </u> and so on ... ) and it **sets a relation between the** <u>EoS parameters J and L</u>



*Electric dipole polarizability in 208Pb: Insights from the droplet model - X. Roca-Maza, M. Brenna, G. Colò, M. Centelles, X. Viñas, B. K. Agrawal, N. Paar, D. Vretenar, and J. Piekarewicz Phys. Rev. C 88, 024316 (2013)* 

# Dipole polarizability, J and L

# Determination of the J vs L relation from experimental data according to EDFs

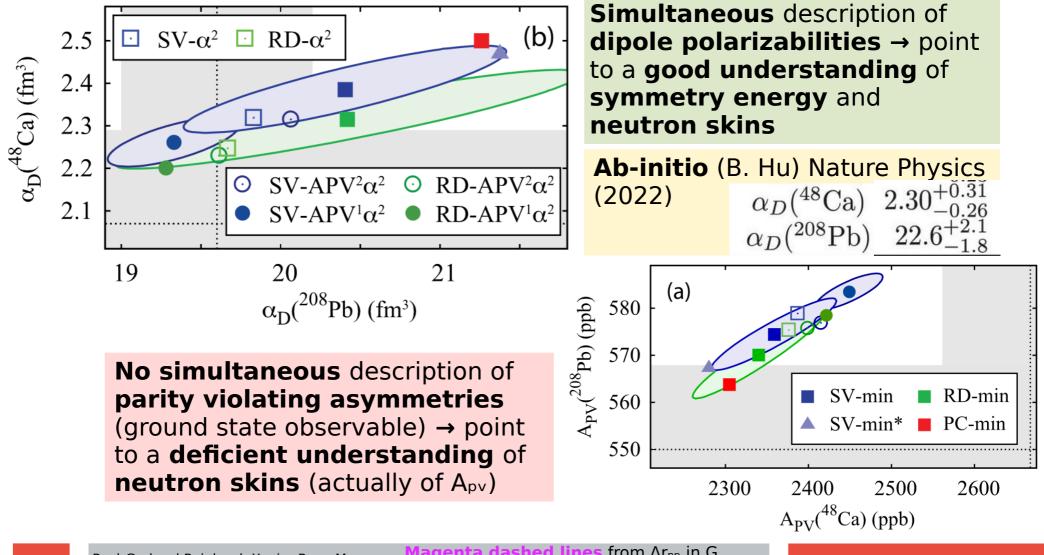


#### one can qualitatively understand the result!!

X. Roca-Maza, M. Brenna, G. Colò, M. Centelles, X. Viñas, B. K. Agrawal, N. Paar, D. Vretenar, and J. Piekarewicz Phys. Rev. C 88, 024316 – Published 20 August 2013

X. Roca-Maza, X. Viñas, M. Centelles, B. K. Agrawal, G. Colò, N. Paar, J. Piekarewicz, and D. Vretenar Phys. Rev. C **92**, 064304 – Published 8 December 2015  $S(\langle
ho
anglepprox 0.08~{
m fm}^{-3})pprox 25~{
m MeV}$ 

## How models perform for $A_{PV}$ (sensitive to $\Delta r_{np}$ ) and $\alpha_{D}$ (sensitive to J and $\Delta r_{np}$ ) in <sup>48</sup>Ca and <sup>208</sup>Pb?



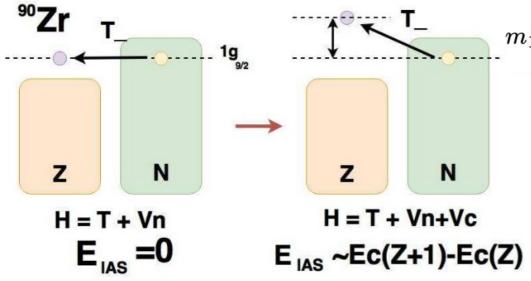
Paul-Gerhard Reinhard, Xavier Roca-Maza, and Witold Nazarewicz, PRL 127 232501 (2021) and PRL 129 232501 (2022)

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**Magenta dashed lines** from  $\Delta r_{np}$  in G. Hagen et al. Nature Physics 12, 186–190 (2016) and H. Bu et al. Nature Physics (2022)

## Fermi or Isobaric Analog Resonance and Δr<sub>np</sub>

$$F=T_{\pm}=\sum_{i}^{A}t_{\pm}(i)$$



→ non-energy weighted sum rule:  $m_0^- - m_0^+ = \langle 0|T_+T_-|0\rangle - \langle 0|T_-T_+|0\rangle$   $= \langle 0|[T_+, T_-]|0\rangle = \langle 0|2T_z|0\rangle$  = N - ZNote: If no isospin-mixing it would be zero!!  $\rightarrow$  energy weighted sum rule:

$$n_1=\sum_
u(E_
u-E_0)|\langle
u|F|0
angle|^2=\langle 0|T_+[\mathcal{H},T_-]|0
angle$$

[H,T\_] different from zero only if H contains terms that breaks isospin symmetry

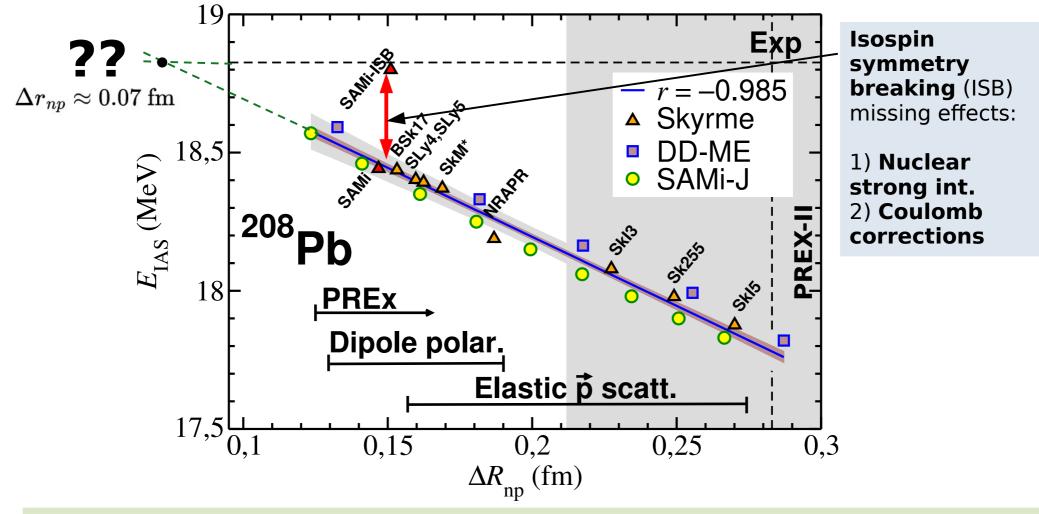
→ **Coulomb** leading ISB:

$$E_{\mathrm{IAS}} = rac{\langle 0|T_+[\mathcal{H},T_-]|0
angle}{\langle 0|T_+T_-|0
angle}$$

$$\approx \frac{6}{5} \frac{Ze^2}{r_0 A^{1/3}} \left( 1 - \sqrt{\frac{5}{12}} \frac{N}{N - Z} \frac{\Delta R_{\rm np}}{r_0 A^{1/3}} \right)$$

# Isobaric Analog State, ISB and Δr<sub>np</sub>

$$F=T_{\pm}=\sum_{i}^{A}t_{\pm}(i)$$

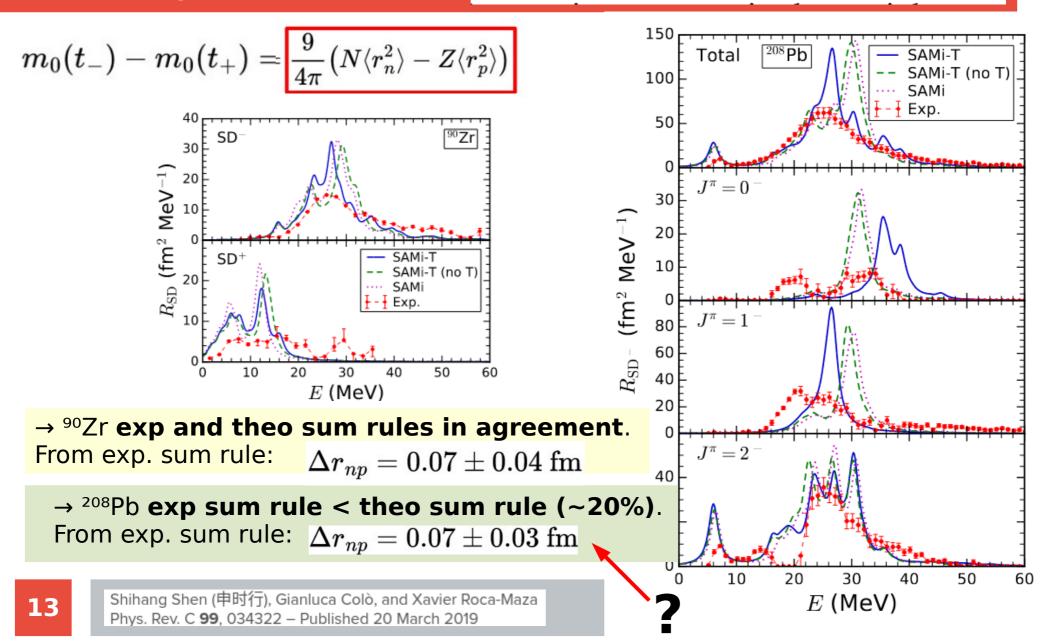


The larger the Δr<sub>np</sub>, the larger the ISB contributions to IAS in <sup>208</sup>Pb

X. Roca-Maza, G. Colò, and H. Sagawa Phys. Rev. Lett. **120**, 202501 – Published 18 May 2018

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### **Spin Dipole Resonance and \Delta r\_{np}** Difficult to measure and analyze? $\sum_{i=1}^{A} \sum_{M} \tau_{\pm}(i) r_{i}^{L} [Y_{L}(\hat{r}_{i}) \otimes \sigma(i)]_{JM}$



# Conclusions



**Different ways** to investigate properties of the **symmetry energy**  $(\rho < \rho_0)$  using **different observables** provide **different answers**.

#### **Theory:**

- $\rightarrow$  An effort to understand the **parity violating asymmetry** and the **beam normal spin asymmetry** in <sup>208</sup>Pb is needed.
- $\rightarrow$  An effort to better understand the **systematics** on the **dipole polarizability** is needed (e.g. along the Sn isotopic chain).
- → An effort to better understand **Isospin Symmetry Breaking** in nuclei in connection to the experimental knowledge of the **IAS** could provide robust insights into the symmetry energy
- $\rightarrow$  Study of **charge-exchange resonances** that naturally isolate differences between protons and neutrons could be useful to propose new experiments sensitive to the symmetry energy.

### **Experiment:**

 $\rightarrow$  An effort to improve the accuracy in the **parity violating asymmetry in** <sup>208</sup>**Pb** (and/or measure other Q values) and confirm the measured values for the beam normal spin asymmetry is needed.

 $\rightarrow$  An effort to measure the **dipole polarizability** in neutron-rich Sn isotopes (N>74) will help understanding structure effects as well as provide information on the symmetry energy.

→ Measure **charge-exchange resonances** like Spin-Dipole Resonance / Isovector Monopole / ... ? (any medium/heavy nucleus)

# Collaborators

- → Gianluca **Colò** (University of Milan)
- → Hiroyuki Sagawa (University of Aizu & RIKEN)
- → Tomoya Naito (University of Tokyo & RIKEN)
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- → Xavier **Vinyes** & Mario **Centelles** (University of Barcelona)
- → Jorge **Piekarewicz** (Florida State University)
- → Nils **Paar** & Dario **Vretenar** (University of Zagreb)
- → Bijay K. **Agrawal** (Saha Institute of Nuclear Physics)
- → P.-G. **Reinhard** (University of Erlangen-Nürnberg)
- → Witold **Nazarewicz** (FRIB and Michigan State University)

# QCD-Based Charge Symmetry Breaking Interaction ACD-based Charge Symmetry breaking interaction and the Okamoto-Nolen-Schiffer anomaly

Hiroyuki Sagawa (佐川弘幸), Tomoya Naito (内藤智也), Xavier Roca-Maza, and Tetsuo Hatsuda (初田哲男)

Phys. Rev. C 109, L011302 – Published 25 January 2024

