# Nucleon-Deuteron Scattering to Investigate Three-Nucleon Forces





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# Frontier of Nuclear Force Study

History **1935** Yukawa's meson theory - Two-Nucleon Forces (2NFs) 1990's Realistic Modern Nucleon-Nucleon Potentials (CD Bonn, Argonne v18, Nijmegen)

To understand Nuclear Forces from Quarks ~ Lattice QCD ~

To understand Nuclei and Nuclear Matter from bare Nuclear Forces  $\sim$  with 3-Nucleon Forces  $\sim$ 





 $\pi,\rho,\omega$ 

•  $2\pi$ -exchange 3NF :

1957 Fujita-Miyazawa 3NF Prog. Theor. Phys. 17, 360 (1957) - Main Ingredients :  $\Delta$ -isobar excitations in the intermediate







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- Main Ingredients :  $\Delta$ -isobar excitations

Urbana IX 3NF natural Brazil, Texas etc... Excitation Energy • Quark 300 0 proton (*uud*) proton / neutron / neutron (*ddu*)  $(J^P, I) = \left(\frac{1}{2}^+, \frac{1}{2}\right)$ 





Fujita

N







# Where ?

### **3NFs in Finite Nuclei**

## Ab Initio Calculations for Light Nuclei ( $A \leq 12$ ): <sup>4</sup>He to <sup>12</sup>C

Green's Function Monte Carlo No-Core Shell Model etc..

- 3NF effects in B.E.
- **10-25%**
- Attractive

### Note :

Isospin T=3/2 3NFs (three-neutron force) play important roles to explain B.E. in neutron rich nuclei.

3NFs in A > 3 - (1) -







### **3NFs in Finite Nuclei**

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### **3NFs in Finite Nuclei**

- Coupled cluster theory
- Nuclear Lattice Simulations

Heavy Mass Nuclei (*up to* <sup>208</sup>Pb) 3NFs provide key mechanisms, - Shell-evolution,



3NFs in A>3 - (1) -



8Pb

sms,

### **3NFs in Finite Nuclei**

## **RIKEN RIBF**



ei etc. IMP / HIAF RAON GANIL / ISOLDE **GSI/FAIR** ISAC-I & II etc.

3NFs in A>3 - (1) -

## Experiment

Experiment at RIBF  $2_1^+$  Energy of  ${}^{54}Ca \Rightarrow$  Shell • N = 30- 52 Ca N = 32N = 3454 Ca

22

18

Nature 502, 207 (2013)

26

30



50

40

30  $\sim$  on number N



### **3NFs in Infinite Nuclei - Neutron Star -**

## "Endpoint of stellar evolution"

### Supernovae Explosion



### Discovery of Heaviest Neutron Star with 2 solar-mass M<sub>sun</sub> (PSR J1614-2230)





- 3NF
  - Short & Repulsive
  - Large effects at high density.



# 3NFs in A>3 - (2)



### NNN + NNA in Infinite Nuclei





• 3NF is a key to understand nuclear phenomena quantitatively. • How to constrain the properties of 3NF?

# How?



# Two & Three-Nucleon Force







# Nucleon-Deuteron Scattering

## a good probe to study the dynamical aspects of 3NFs.

✓ Momentum dependence

✓ Spin & Iso-spin dependence

## **Direct Comparison between Theory and Experiment**

• Theory : Faddeev / Faddeev-Yakubovsky Calculations

Rigorous Numerical Calculations of 3, 4N System

**2NF Input** 

- **CDBonn**
- Argonne V18 (AV18)
- Nijmegen I, II, 93

- **3NF Input**
- Urbana IX
- etc..

## **Experiment : Precise Data**

•  $d\sigma/d\Omega$ , Spin Observables ( $A_{i}, K_{ii}, C_{ii}$ )

## **Extract fundamental information of Nuclear Forces**

• Tucson-Melbourne

**2NF & 3NF Input** 

• Chiral Effective Field Theory



# Where is the hot spot for study of 3NFs ?





## Nd Scattering at Low Energies ( $E \leq 30 \text{ MeV/A}$ )



Weigh precision data are explained by Faddeev calculations based on 2NF.
 (Exception : A<sub>y</sub>, iT<sub>11</sub>)

## No signatures of 3NF

Exp. Data from Kyushu, TUNL, Cologne etc..

W. Glöckle et al., Phys. Rep. 274, 107 (1996).





## Facilities





## Facilities

## **RIKEN RI Beam Factory (RIBF) Polarized deuteron beam**

- acceleration by AVF+RRC : 65-135 MeV/nucleon
- acceleration by AVF+RRC+SRC : 190-300 MeV/nucleon
- polarization : 60-80% of theoretical maximum values
- Beam Intensity : < 100 nA







## RCNP, Osaka University





# Deuteron-Proton Systems

•  $d + p \rightarrow d + p$  $\theta$ c.m. = 0° ~ 180° **Momentum transfer**  $q = 0 - 3.4 \text{ fm}^{-1}$ ( at E = 135 MeV/A)  $-d+p \rightarrow p+p+n_{o}$ Many kinematical configurations 120°/  $q = 0 - 3 \text{ fm}^{-1}$ **\**120° ( at E = 135 MeV/A) 120° Star Configuration 

• 
$$d + p \rightarrow {}^{3}\text{He} + \gamma$$
  
 $\theta_{\text{c.m.}} = 0^{\circ} \sim 180^{\circ}$   
 $q = 1.5 - 2.5 \text{ fm}^{-1}$   
( at  $E = 135 \text{ MeV/A}$ )





# deuteron-nucleon scattering at ~100 MeV/nucleon

deuteron proton : 1 neutron : 1



# Differential Cross section



2NF (CDBonn, AV18, Nijmegen I,II) : Large discrepancy in Cross Section Minimum (~30%)

 $2\pi$ -exchange 3NFs (Tucson-Melbourne, : First Clear Signatures of 3NF

<b>Urbana IX) : Good Agreement</b>
effects in 3-Nucleon Scattering





**Disagreement at very forward angles : Coulomb effects.** 

A. Deltuva et al., PRC 68, 024005 (2003) A. Deltuva et al., PRC 71, 054005 (2005)



Spin Observables

## Analyzing Powers



### K. Sekiguchi et al. PRC 65, 034003 (2002)

180

180





Spin Observables  $(A_{ij}, K_{ij})$ :



# Energy Dependence

## Energy Dependent Study for *dp* Scattering - Cross Section & Analyzing Powers -



K. Hatanaka et al., Phys. Rev. C. 66, 044002 (2002) Y. Maeda et al., Phys. Rev. C 76, 014004 (2007) K. S. et al., Phys. Rev. C 83, 061001 (2011) K. S. et al., Phys. Rev. C 89, 064007 (2014)



## Summary of Results of Comparison for *dp* elastic scattering

- Cross section at ~100 MeV/nucleon
  - First clear signature of 3NF effects in 3N scattering
    - Magnitudes of 3NFs is O.K. .
- Spin observables
  - Solution Not always described by  $2\pi$ -3NFs
    - Defects of spin-dependent parts of 3NFs
- At higher energies ...
  - Serious discrepancy at backward angles
    - Short Range 3NFs are required.



## Nd Elastic Scattering Data at Intermediate Energies

pd and nd Elastic Scattering at 65-400 MeV/nucleon

Observable	100	200	300	400
$rac{d\sigma}{d\Omega}$				•
$\begin{vmatrix} \vec{p} & A_y^{p} \\ \vec{n} & A_y^{n} \end{vmatrix}$			•	•
$\vec{d}$ $iT_{11}$				•
$\begin{array}{ c c } & T_{20} \\ & T_{22} \end{array}$				
T 21	•••		• •	
$\vec{p} \rightarrow \vec{p}  K_y^{y'}$ $K_x^{x'}$ $K_z^{z'}$ $K_z^{x'}$ $K_z^{z'}$	π thr	reshold		
$\vec{d} \rightarrow \vec{p}  K_y^{y'}$ $K_{xx}^{y'}$ $K_{yy}^{y'}$ $K_{yy}^{y'}$ $K_{xz}^{y'}$				
$\begin{vmatrix} \vec{p} & \rightarrow \vec{d} & K_y^{y'} \end{vmatrix}$				•
$ \begin{vmatrix} \vec{p}  \vec{d} & C_{i,j} \\ & C_{ij,k} \end{vmatrix} $				

~2024

 High precision data set of dσ/dΩ & Analyzing Powers
 from
 RIKEN, RCNP, KVI, IUCF, LANSCE
 etc.



## Nd Elastic Scattering Data at Intermediate Energies

### pd and nd Elastic Scattering at 70-400 MeV/A

Observat	ble	10	00	200	)	30	00	40	)0
$rac{d\sigma}{d\Omega}$				0	00				
$ \begin{vmatrix} \vec{p} & A_{3} \\ \vec{n} & A_{3} \end{vmatrix} $	p y n y		8	•					
$ \vec{d}  A_{3} \\ A_{4} \\ A_{4} \\ A_{5} \\ A_{5$	d y yy xx				π	thresh	ıold		
$\begin{array}{c} A_{2} \\ \vec{p} \rightarrow \vec{p} & K_{2} \\ K_{3} \\ K_{4} \\ K_{5} \\ K$	x z y' y x' x z' x x z z'								
$\vec{d} \rightarrow \vec{p}  K_{q}$ $\vec{d} \rightarrow \vec{k}  K_{q}$ $K_{q}$ $K_{q}$	~ z ·y' y ·y' xx ·y' yy ·y' xz								
$\vec{p} \rightarrow \vec{d} K_{i}$	- y' Y								
$\vec{p} \vec{d} = C_y$	yy ij								







## Nd Elastic Scattering Data at Intermediate Energies

pd and nd Elastic Scattering at 65-400 MeV/nucleon

Observable	100	200	300	400
$rac{d\sigma}{d\Omega}$				
$\begin{vmatrix} \vec{p} & A_y^{p} \\ \vec{n} & A_y^{n} \end{vmatrix}$			•	•
$\vec{d}  iT_{11}$ $T_{20}$ $T_{22}$ $T_{21}$				
$\vec{p} \rightarrow \vec{p}  K_{y}^{y'}$ $K_{x}^{x'}$ $K_{z}^{z'}$ $K_{z}^{z'}$ $K_{z}^{z'}$	π thr	eshold		
$\vec{d} \rightarrow \vec{p}  K_y^{y'}$ $K_{xx}^{y'}$ $K_{yy}^{y'}$ $K_{yy}^{y'}$ $K_{xz}^{y'}$				
$\vec{p} \rightarrow \vec{d} K_y^{y'}$	V			•
$\begin{vmatrix} \vec{p}  \vec{d} & C_{i,j} \\ & C_{ij,k} \end{vmatrix}$		•		

~2024

• High precision data set of  $d\sigma/d\Omega$  & Analyzing Powers from RIKEN, RCNP, KVI, IUCF, LANSCE etc. After 89 Years of Yukawa's Meson Thory (1935) & After **67** Years of Fujita-Miyazawa 3NF (1957) Quantitative discussions on 3NFs start via Theor. & Exp. .



So far ...

Nucleon-Deuteron Scattering at ~100 MeV/nucleon

- First Evidence of 3NF effects
- Defects of existing 3NF models

From here > Determine 3NFs based on χEFT Nuclear Potential High-precision measurement of Spin Correlation Coefficients Proton-<sup>3</sup>He Scattering at  $\sim$ 100 MeV/N : New Probe of 3NF Study > 3NFs of isospin channel of T=3/2 First Step from Few to Many

- Deuteron-Proton Scattering at ~100 MeV/N : Golden window of 3NFs













# Chiral EFT Nuclear Force & dp elastic scattering

## $\simeq \chi EFT$ 2NFs have achieved to high-precision.

5th order of NN potentials (N4LO<sup>+</sup>) reproduce pp(np) data with  $\chi^2$ /datum=1.00

P. Reinert, H. Krebs, E. Epelbaum EPJA 54, 86 (2018)





# Chiral EFT Nuclear Force & dp elastic scattering

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*dp* elastic scattering data show necessities of the N4LO 3NFs.

Cross section minimum region for *dp* elastic scattering at  $\sim 100$  MeV/nucleon is

"Golden window" for the N4LO 3NFs.

LENPIC collaboration, Phys. Rev. C 98, 014002 (2018)















# New Experiment at RIKEN **Measurement of Spin Correlation Coefficients** for *dp* elastic scattering at $\sim 100$ MeV/nucleon

pd and nd Elastic Scattering at 65-400 MeV/nucleon 200 100 300 400 Observable  $rac{d\sigma}{d\Omega}$  $\vec{p}$  $A_y^p$  $\vec{n}$  $A_y^n$  $\overrightarrow{d}$  $iT_1$  $T_{20}$  $T_{22}$  $T_{21}$  $\vec{p} \rightarrow \vec{p}$  $K_x^{x'}K_y^{y'}$  $K_{\boldsymbol{x}}^{\boldsymbol{z}'}K_{\boldsymbol{z}}^{\boldsymbol{x}'}K_{\boldsymbol{z}}^{\boldsymbol{z}'}$  $\vec{d} \rightarrow \vec{p}$  $K_{yy}^{y'}$  $\pi$  threshold  $K_{xx}^{y'} K_{xz}^{y'}$  $\vec{p} \rightarrow \vec{d} K_{u}^{y'}$  $\vec{p} \vec{d}$  $C_{x,x}$   $C_{y,y}$   $C_{z,x}$  $C_{x,z}$   $C_{z,z}$  $C_{xx,y} C_{yy,y}$  $C_{xz,y} C_{yz,x} C_{xy,x}$ 

for investigation of N4LO 3NFs - determination of LECs of N4LO 3NFs from *dp* scattering data

# + new detector system









with High-predictive Power

### Term Oct. 2023-Mar.2029

# TOMOE





### **Polarization Experiment** - Few-Nucleon Systems-

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## **High Precision** NN+NNN Force

Nuclear Forces from Chiral Effective Field Theory



### **Polarization Experiment** - Few-Nucleon Systems-

Ultra Cold Atom Experiment

Establishment of Quantum Many-Body Simulation Tool of Nuclear Phenomena with High-predictive Power

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# TOMOE

High-Accuracy Quantum Many-Body Calculations

## **High Precision** NN+NNN Force

Nuclear Forces from Chiral Effective Field Theory

## Fundamental Science Descriptions of Nuclei from First Principles





### Term Oct. 2023-Mar.2029

# TOMOE

# Summary

Frontiers of nuclear force study to understand nuclear forces from quarks

- a few, many- and infinite nucleon systems -

## in Progress

- High precision NN+3N-forces from theory and experiment
- Roles of 3NFs (3BFs) in A > 3

- To understand nuclear forces is a hot topic of nuclear physics.

  - to understand nuclei/matter from NN & 3N-forces
- 3NFs are key elements to fully understand nuclear properties;
- *deuteron-proton* scattering at ~100 MeV/nucleon inspires quantitative discussions of 3NFs.

 $\sim$ Consistent Understanding From Quarks to the Universe $\sim$ 

![](_page_48_Picture_18.jpeg)

### To explore the laws of the nature, step in 1 ightarrow 2 ightarrow 3 .

道経 -萬 第四十 一章 老子

# Tao produced One, One produced Two, Two produced Three, and

![](_page_49_Picture_3.jpeg)

Three produced Everything. "Tao-te Ching", Lao Zi in B.C. 400

![](_page_49_Picture_5.jpeg)

## RIBF-d. Collaboration (2009 $\sim$ )

### Department of Physics, Tokyo Tech

A. Watanabe, K. Suzuki, H. Sugahara, D. Takahashi

### **Department of Physics, Tohoku University**

Y. Saito, Y. Wada, A. Watanabe, D. Eto, T. Akieda, H. Kon,

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Y. Maruta, T. Matsui, K. Kameya, R. Urayama

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S. Kawase, Y. Kubota, C.S. Lee

### RCNP, Osaka University

H. Okamura

### Kyungpook National University

S. Chebotaryov, E. Milman

![](_page_50_Picture_19.jpeg)

## Theoretical Supports from

Ruhr-Universität, Bochum E. Epelbaum, H. Krebs, W. Glöckle Jagellonian University H.Witała, J. Golak, R. Skibinski Kyushu Institute of Technology H. Kamada Forshungszentrum of Jülich A. Nogga Vilnius University A. Deltuva Hannover University P.U. Sauer, S. Nemoto Lisbon University

A. Sa. Fonseca

S. Ishikawa

![](_page_51_Picture_4.jpeg)

Bad Honnef (2006)

## Hosei University

![](_page_51_Picture_8.jpeg)