

$$B_x(t) = (\partial_\eta \cos \phi \sin \theta - \partial_\theta \sin \phi) / 2$$