

$$\frac{d^2\phi}{dt^2} = -2\cot\theta\left(\frac{d\phi}{dt}\frac{d\theta}{dt}\right)$$