

$$\eta_{\text{opt}}(t) = -\frac{1}{2} \int_{t_i}^t \cos \theta(\tau) \dot{\phi}(\tau) d\tau$$