

$$\frac{d^2\theta}{dt^2} = \sin\theta\cos\theta\left(\frac{d\phi}{dt}\right)^2$$