



# FB23

THE 23<sup>rd</sup> INTERNATIONAL CONFERENCE ON  
FEW-BODY PROBLEMS IN PHYSICS (FB23)

Sept. 22 -27, 2024 • Beijing, China



## Neutrino Interactions in the Few-GeV Regime

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University of Warwick

FewBody23, Beijing  
2024 September 26



# Neutrino Mass

Standard Model

Beyond Standard Model

$$\begin{pmatrix} \nu_e \\ \nu_\mu \\ \nu_\tau \end{pmatrix}$$

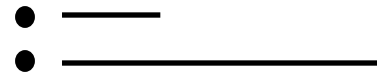
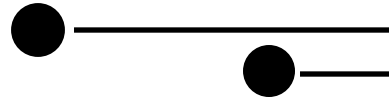
$\pm$

Pontecorvo–Maki–Nakagawa–Sakata

PMNS matrix

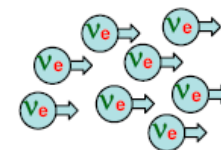
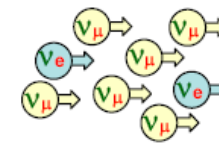
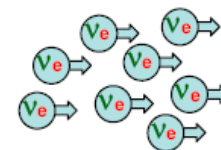
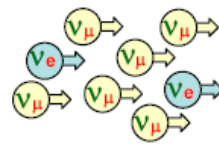
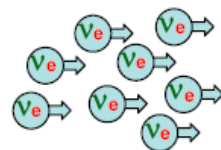
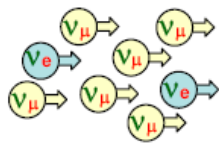
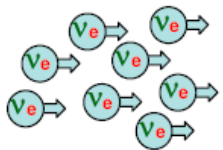
$$\begin{pmatrix} \nu_1 \\ \nu_2 \\ \nu_3 \end{pmatrix}$$

Mass Ordering



Normal      Inverted

$\Delta m^2$  leads to neutrino oscillations

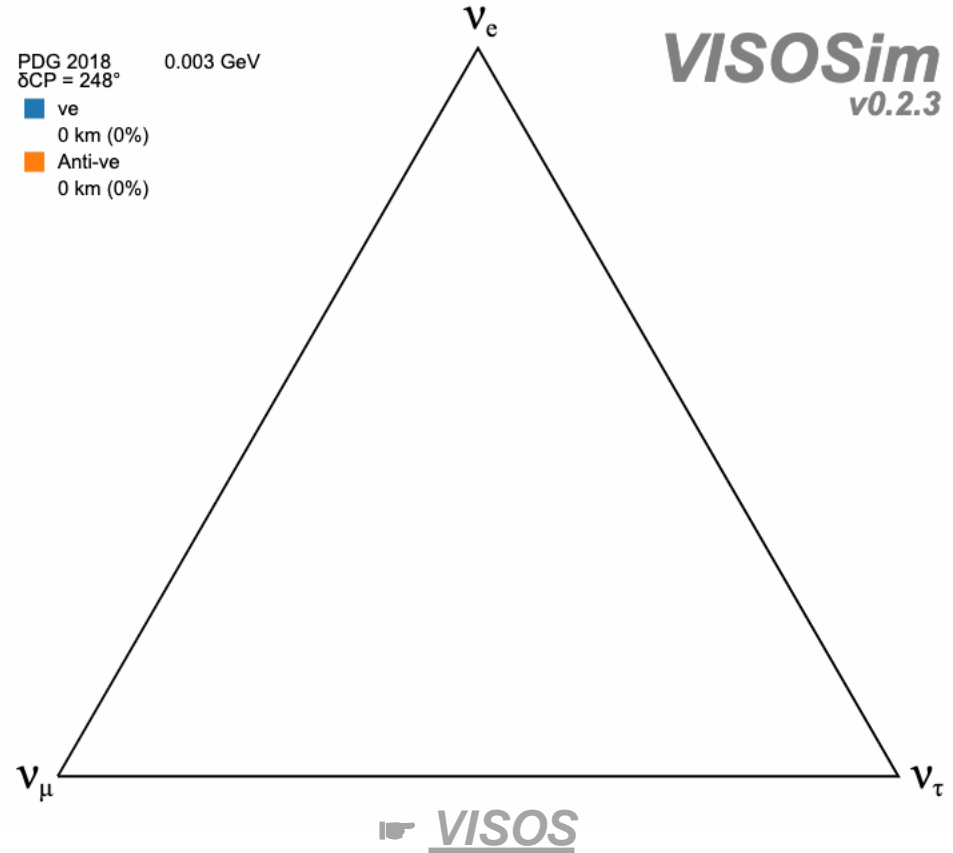
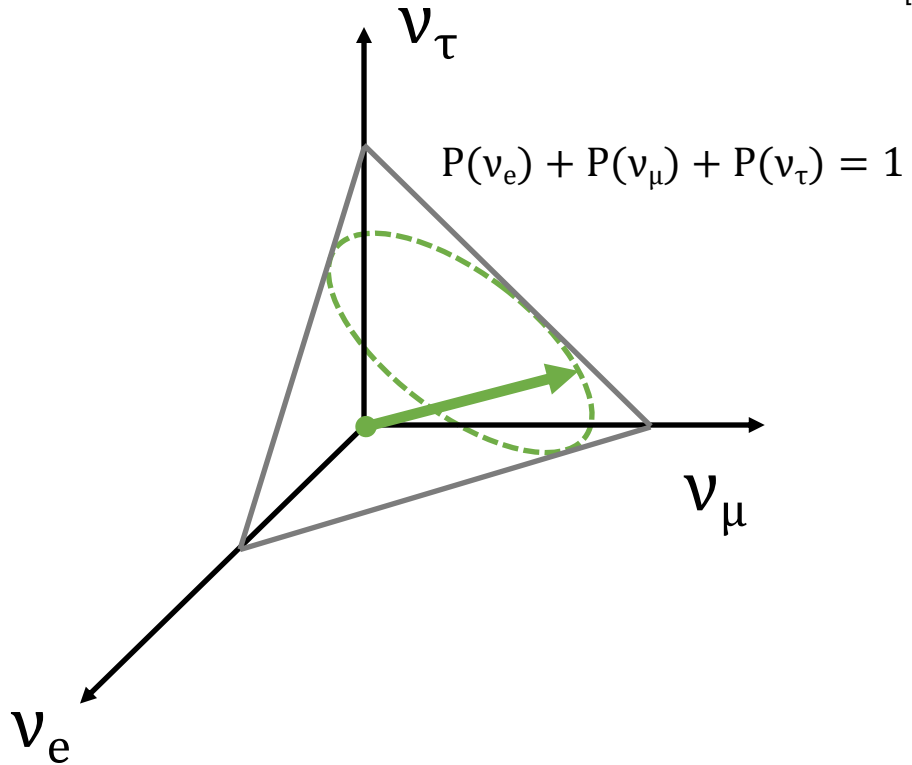


# PMNS matrix

$$\begin{bmatrix} |U_{e1}| & |U_{e2}| & |U_{e3}| \\ |U_{\mu1}| & |U_{\mu2}| & |U_{\mu3}| \\ |U_{\tau1}| & |U_{\tau2}| & |U_{\tau3}| \end{bmatrix}$$

$$= \begin{bmatrix} 0.801 \dots 0.845 & 0.513 \dots 0.579 & 0.143 \dots 0.156 \\ 0.233 \dots 0.507 & 0.461 \dots 0.694 & 0.631 \dots 0.778 \\ 0.261 \dots 0.526 & 0.471 \dots 0.701 & 0.611 \dots 0.761 \end{bmatrix}$$

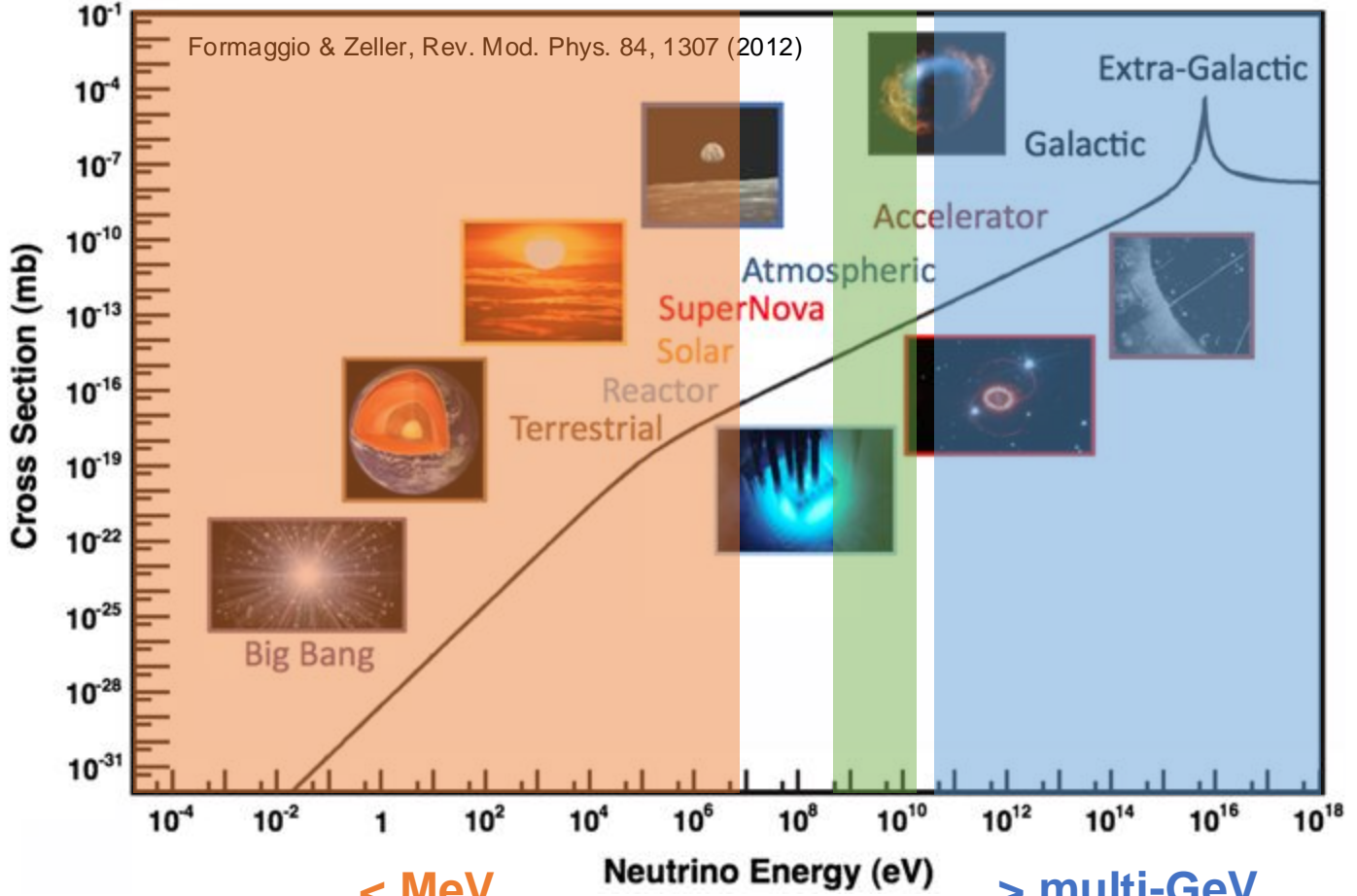
[PDG]



# Why Study GeV (= atmospheric + accelerator)?

GeV

See single/pair/cluster nucleons  
Models (+guess/intuition)



< MeV

See the whole nucleus  
Nuclear database

> multi-GeV

See individual quarks  
pQCD, EW

## Physical reasons

- Neutrino for CP-violation
- Need to detect *accelerator* neutrinos at  $O(1)$  GeV
- GeV-neutrinos also relevant for
- Mass hierarchy measurement via accelerator/atmospheric neutrino oscillations
- Background to rare event searches

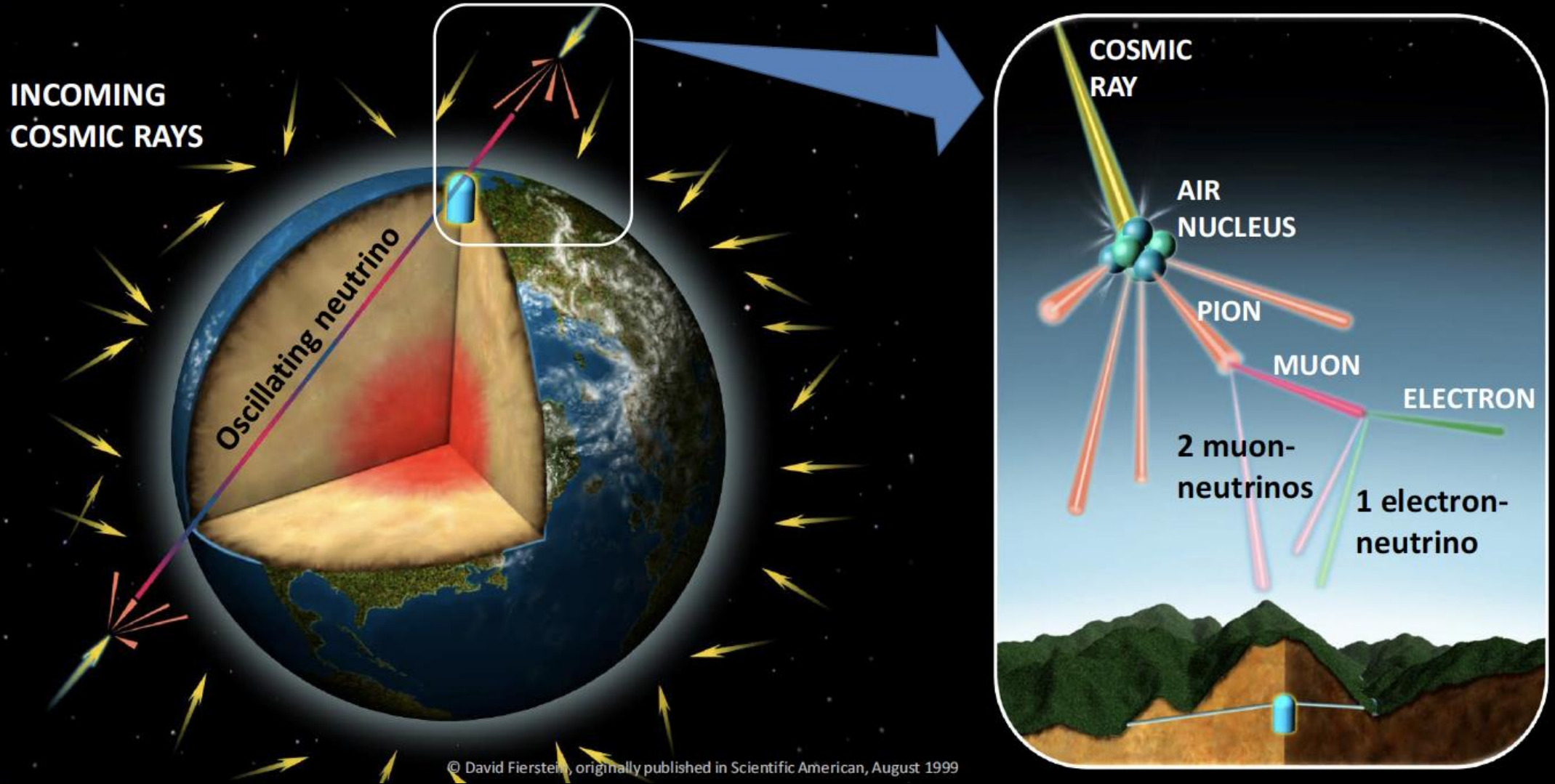
## Technical reasons:

Difficult to *control*

# Atmospheric Neutrinos

Kajita, Nobel Lecture

## Discovery of neutrino oscillations



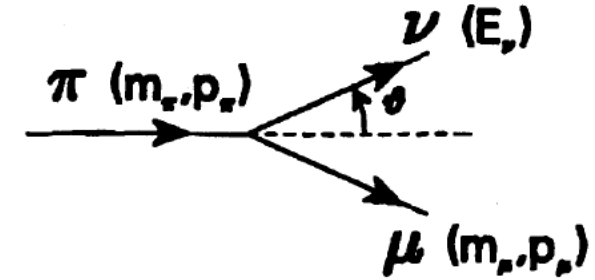
© David Fierstein, originally published in Scientific American, August 1999



# Accelerator Neutrinos

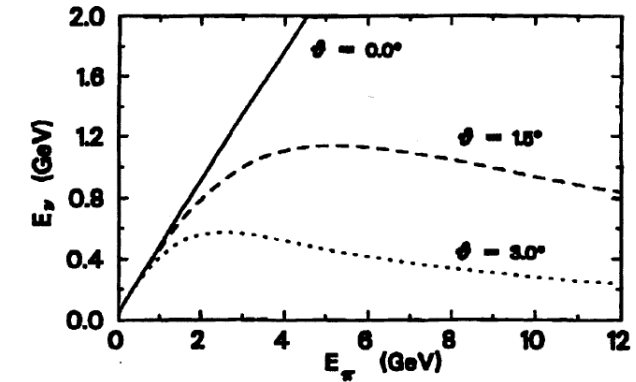
How to obtain a controlled sample of neutrinos?

Let's start from  $\pi$  decays



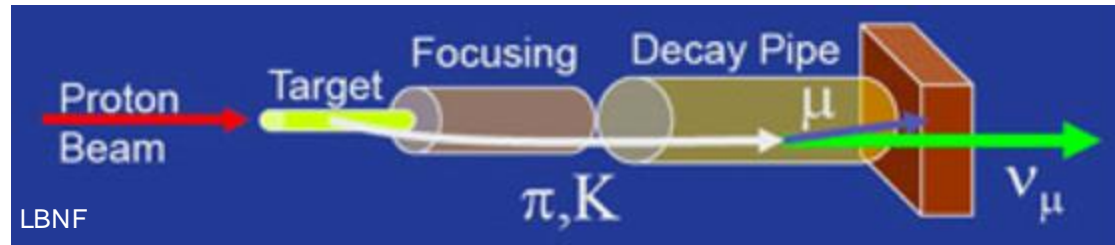
From energy, momentum conservation

$$E_\nu = \frac{m_\pi^2 - m_\mu^2}{2(E_\pi - p_\pi \cos \theta)}$$



Off-axis (OA) technique  $\rightarrow$  Narrow-band beams

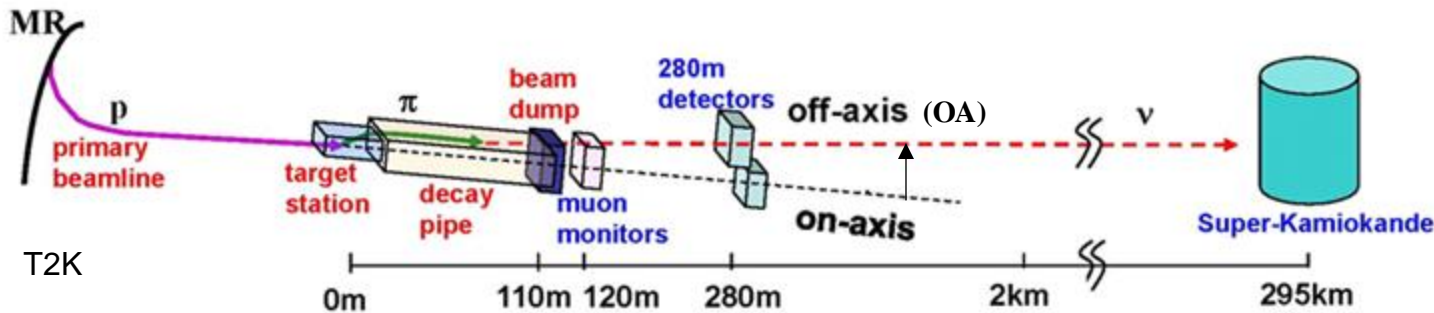
[D. Beavis, et al., P889: long baseline neutrino oscillation experiment at the AGS, Report No. BNL-52459, April, 1995](#)



“ $\beta$  decay” of energetic collision products (mostly  $\nu_\mu$  from  $\pi$ )

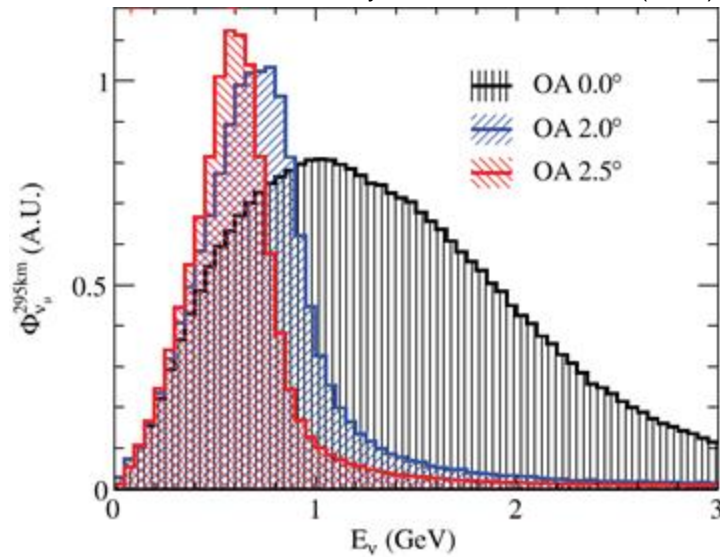
Neutrino beams from accelerators  $\rightarrow$  Directional

Charge selection on  $\pi \rightarrow$  High purity  $\nu$  or  $\bar{\nu}$  beams



# Accelerator Neutrino Experiments

T2K, Phys. Rev. D 87, 012001 (2013)



Super-Kamiokande  
(ICRR, Univ. Tokyo)

Far  
Detector

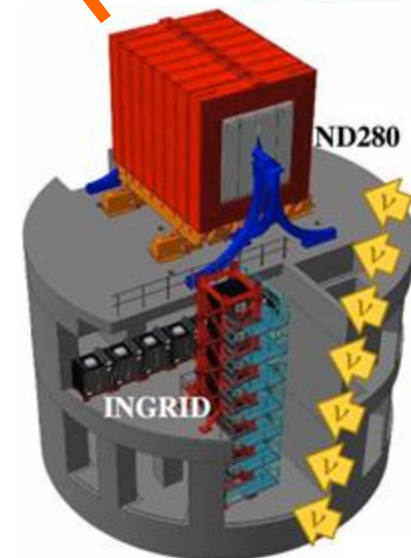
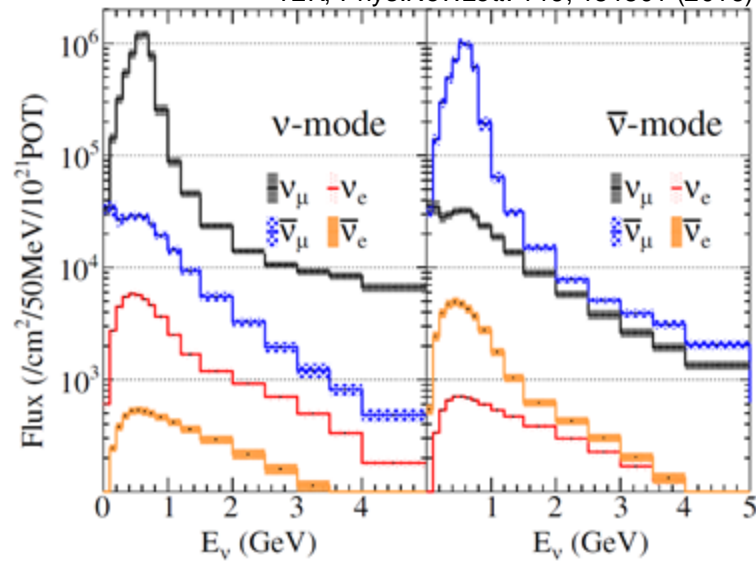


T2K

J-PARC Main Ring  
(KEK-JAEA, Tokai)



T2K, Phys.Rev.Lett. 116, 181801 (2016)



Near Detector

# Accelerator Neutrino Experiments



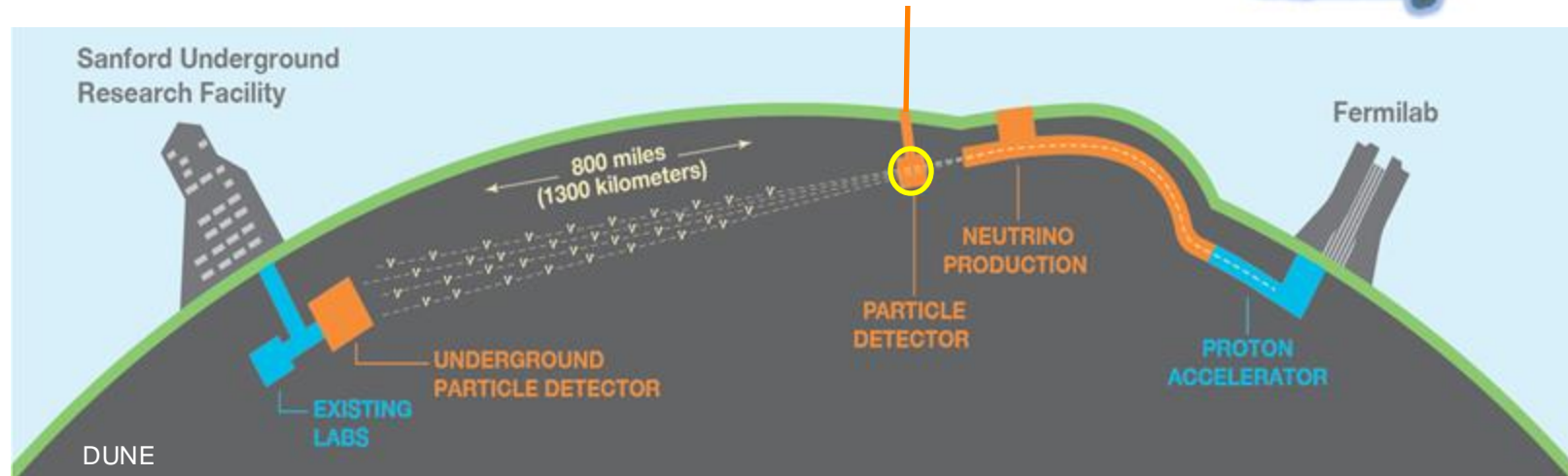
T2K / Hyper-K



Near Detectors to measure  $\nu$  interaction

NOvA

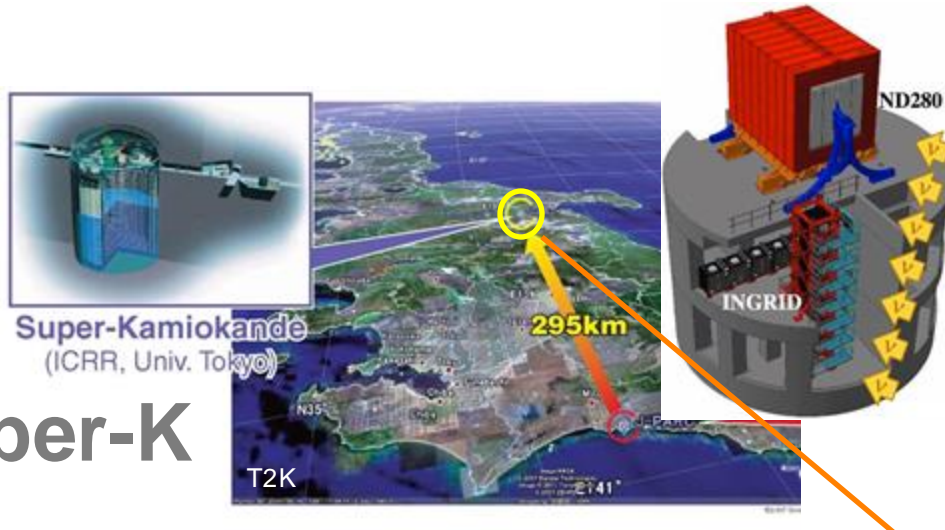
DUNE





# Accelerator Neutrino Experiments

T2K / Hyper-K

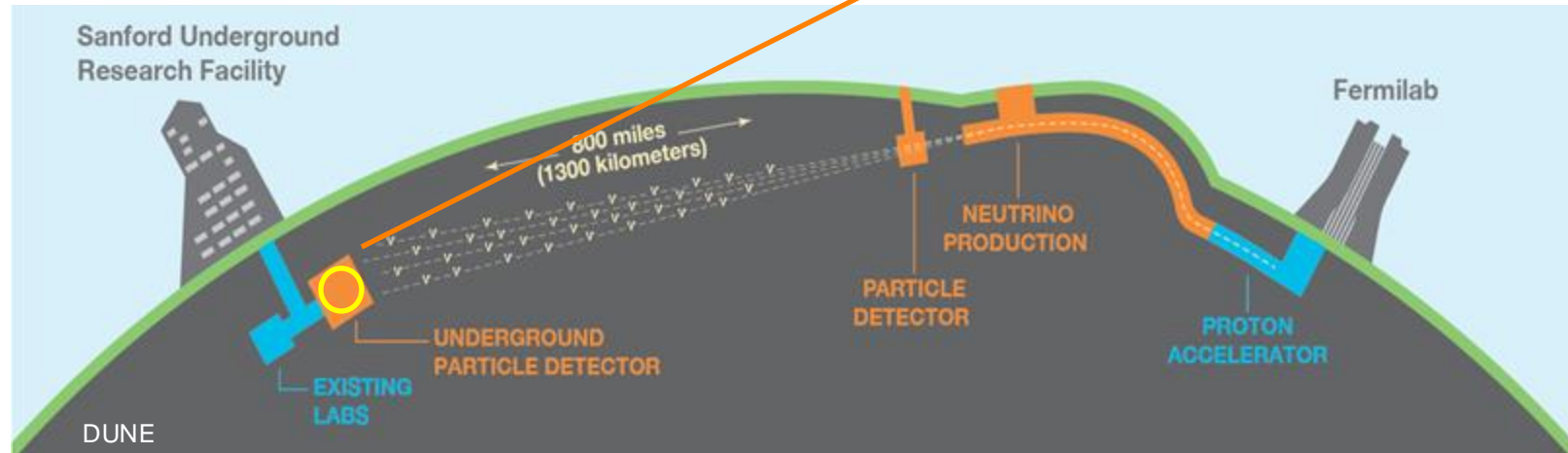


Far Detectors to measure  $\nu$  oscillation

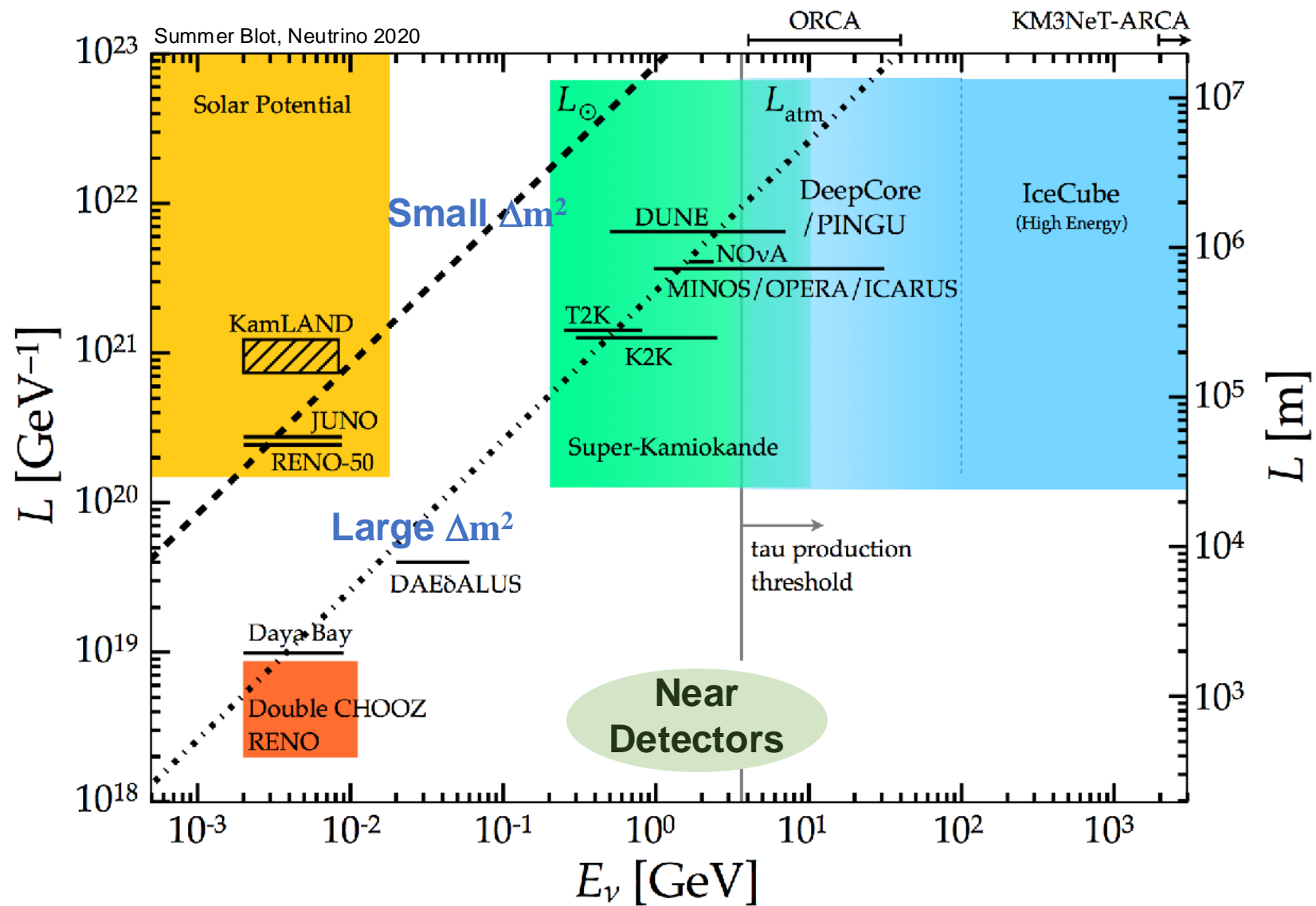
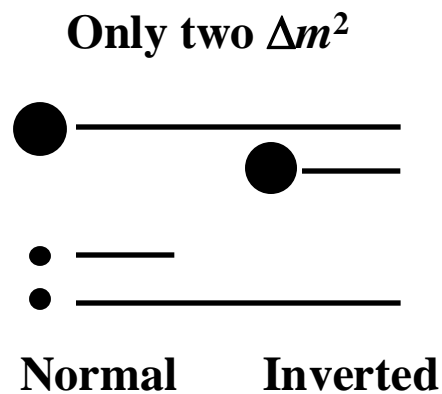


NOvA

DUNE



Oscillation phase  $\sim \Delta m^2 L/E$



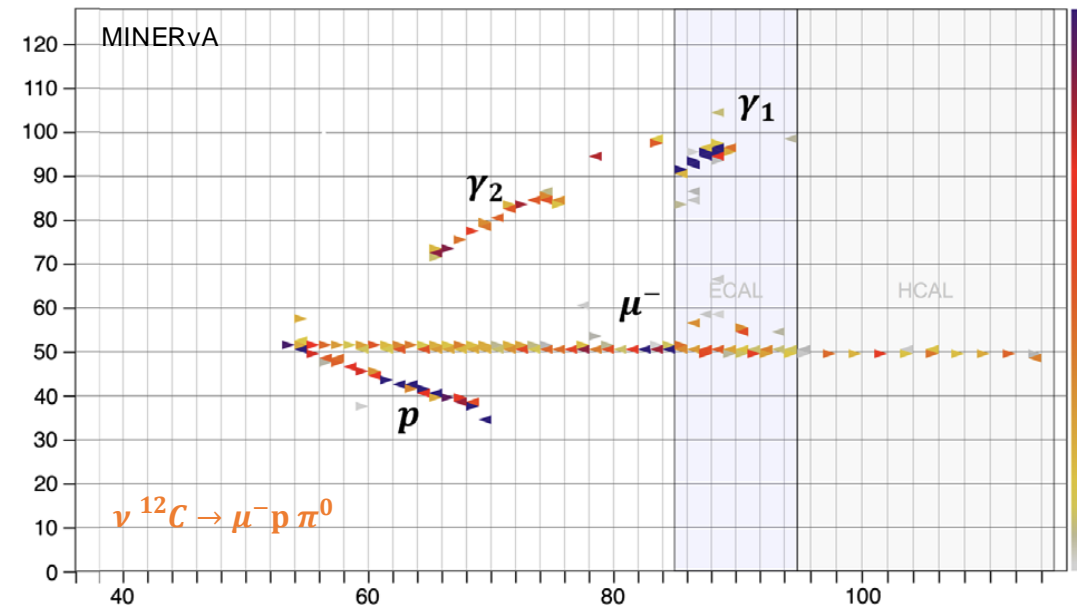
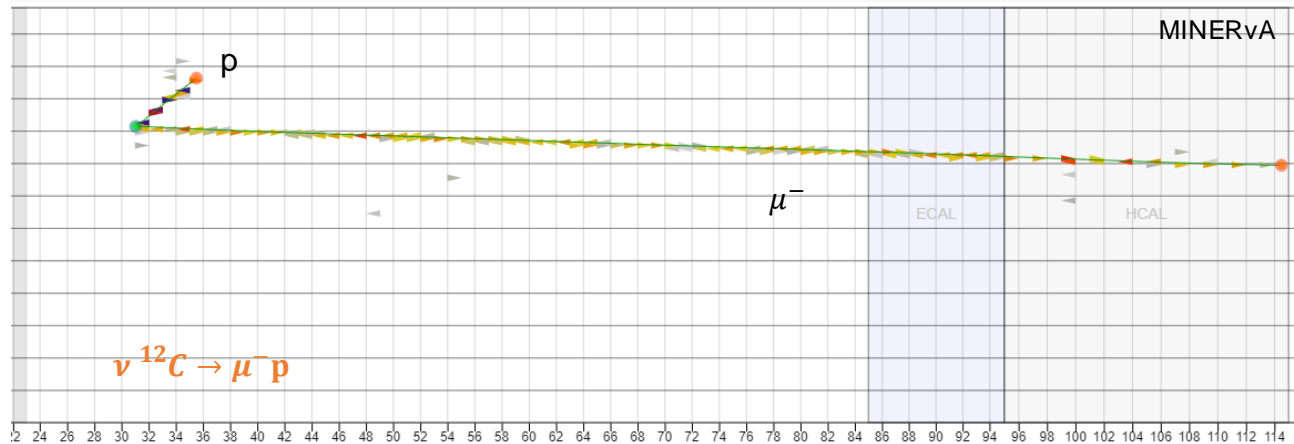
# $\nu$ @ detector: e.g. plastic scintillator tracker

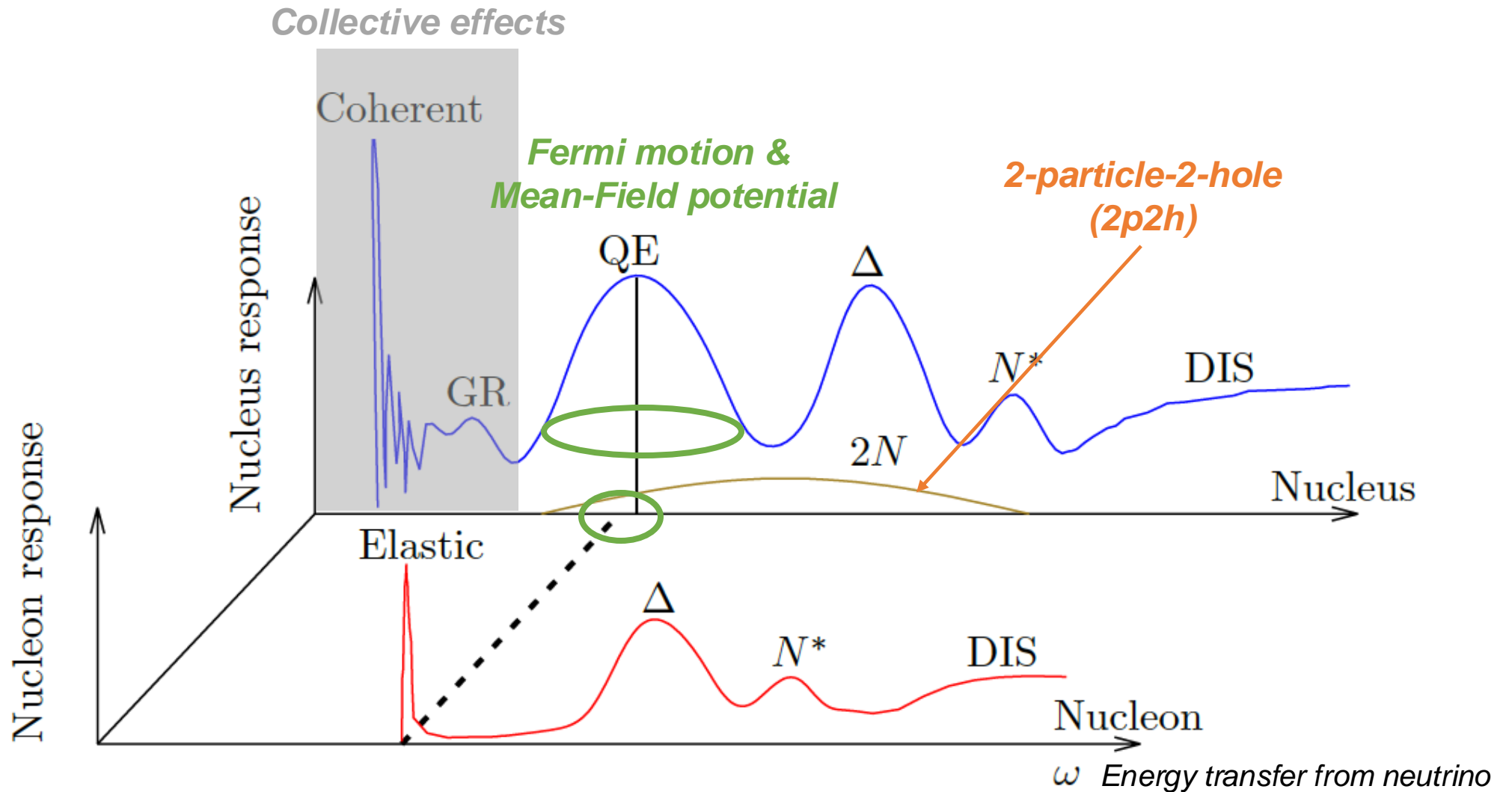
- ❑ Tracker, also **active target**
  - ❖ Tracking + **calorimetry**

Current role in studying  $\nu$  interactions

- ❑ Largest data set
- ❑ Systematic investigation, cf. e.g. MINERvA, Eur. Phys. J. ST **230**, 4243 (2021)

Typical event display w/ plastic scintillator tracker

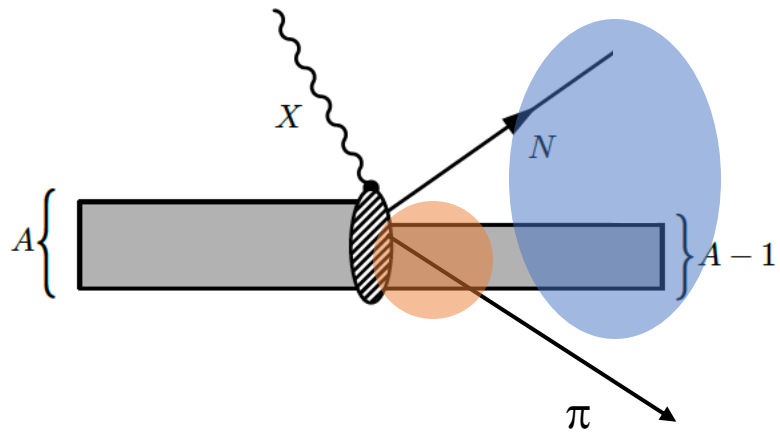




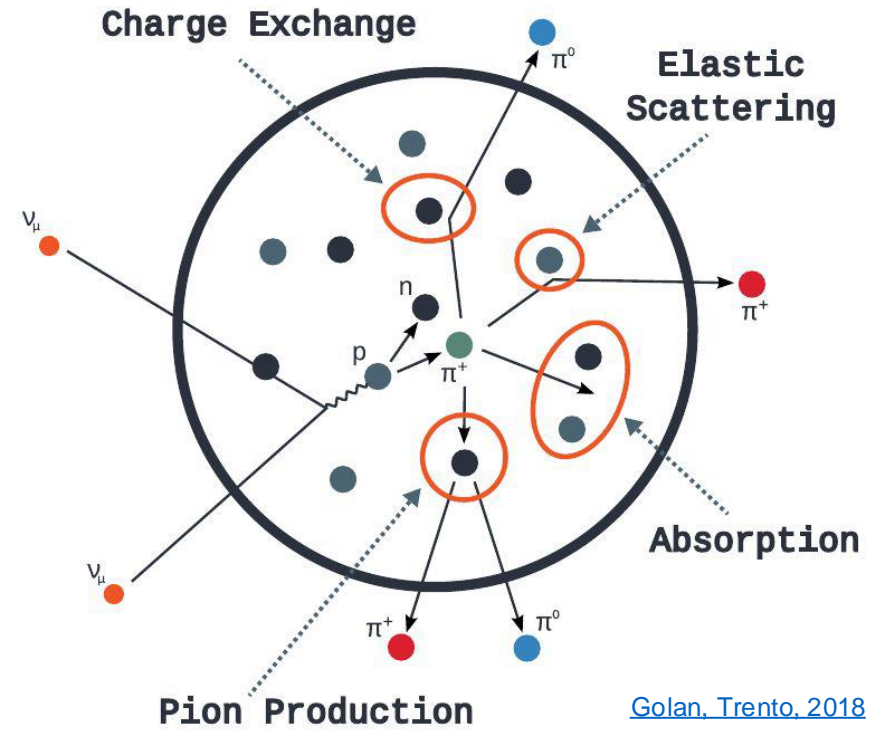
Van Cuyck, PhD Thesis, Ghent University (2017)



# Final-state interaction (FSI)

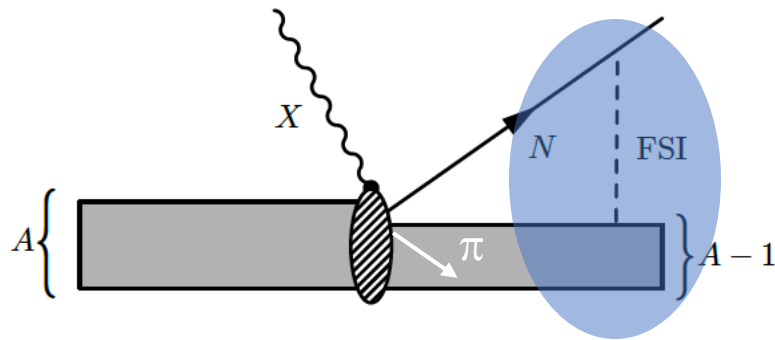


Van Cuyck, PhD Thesis, Ghent University (2017)

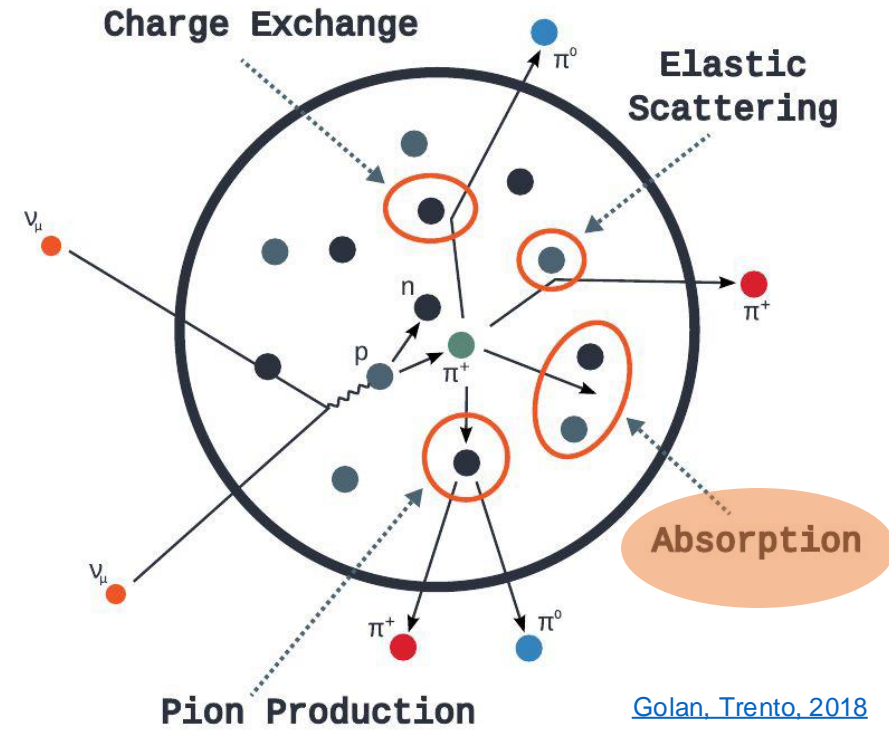


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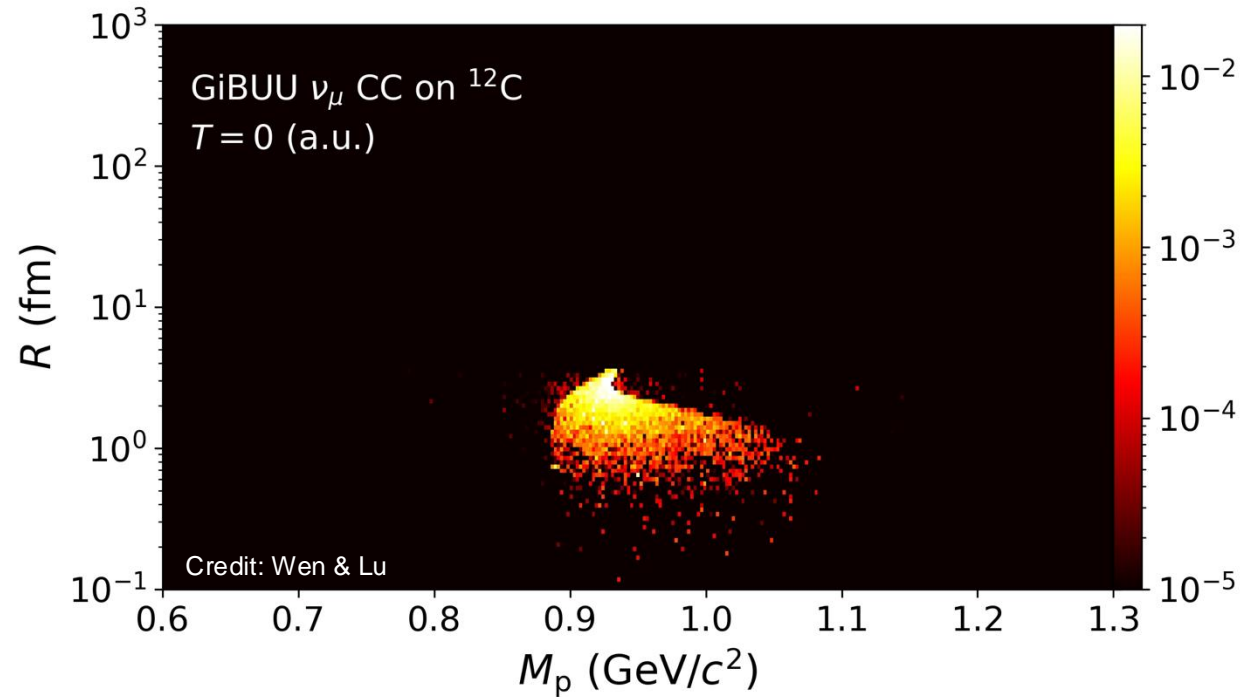
Can not identify *resonant production* (RES) experimentally



Van Cuyck, PhD Thesis, Ghent University (2017)



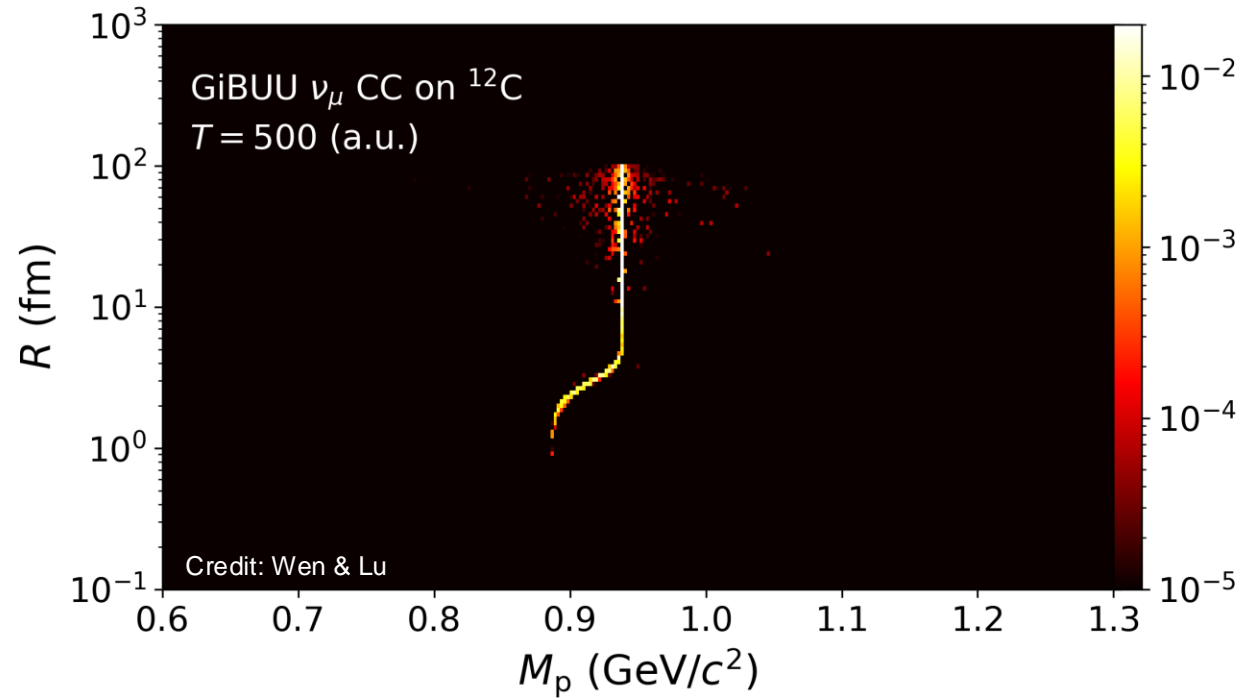
# Final-state interaction (FSI)



† Proton in GiBUU final-state transport  
 $R$ : radial position,  $M_p$ : mass

Final-state proton inside nucleus: **mass** evolves as it propagates out of the nucleus.

# Final-state interaction (FSI)

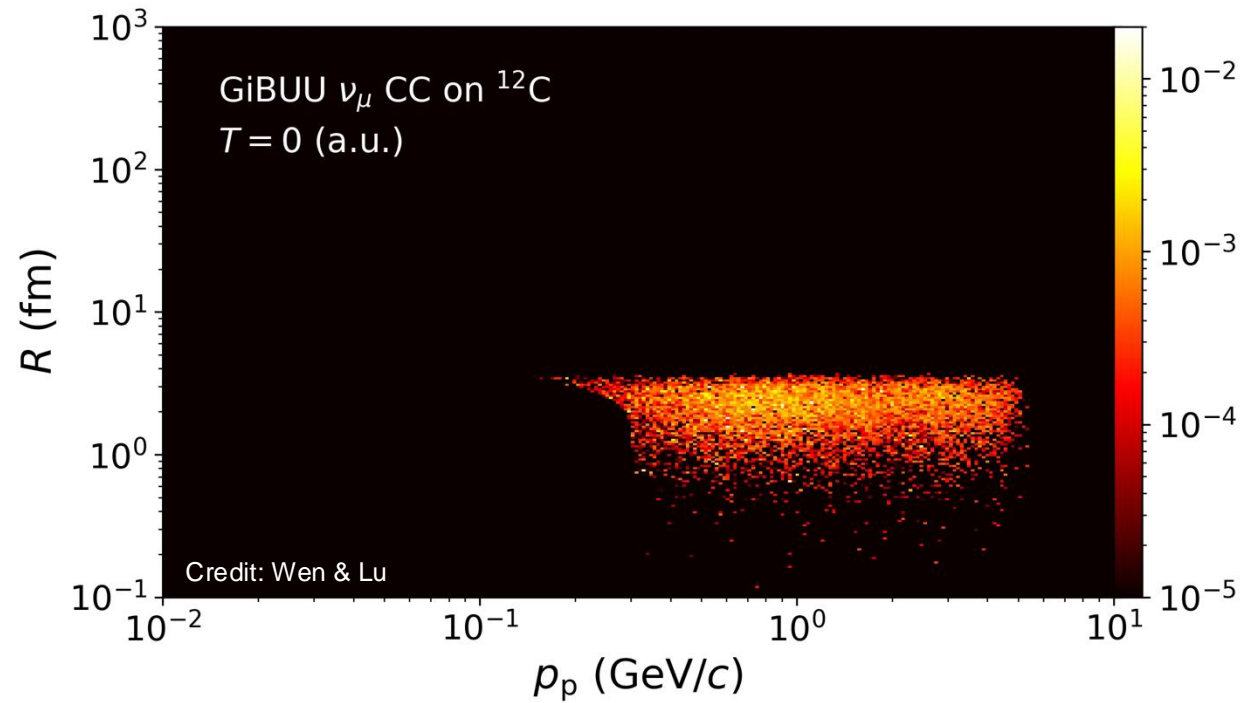


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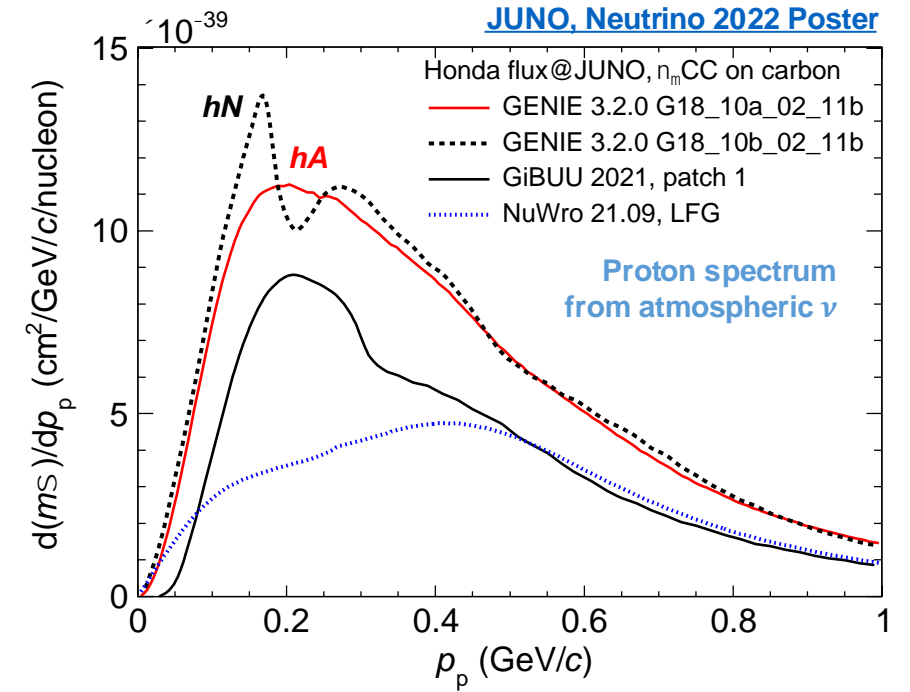
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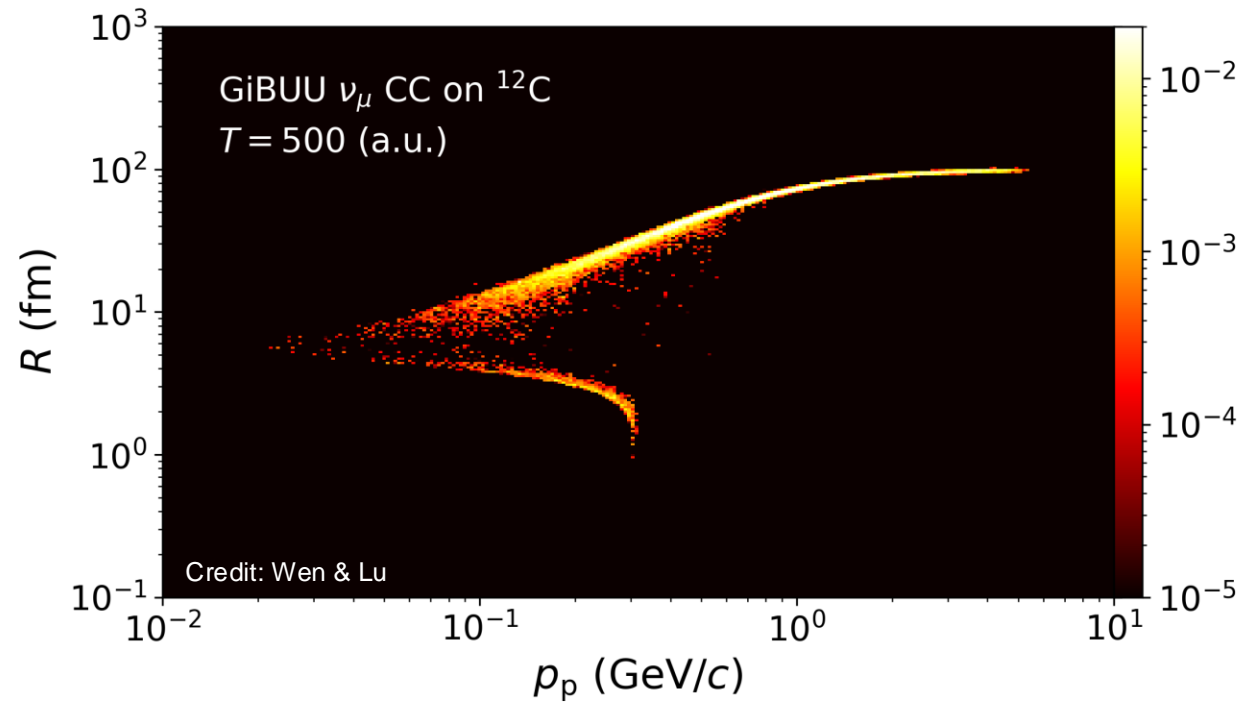


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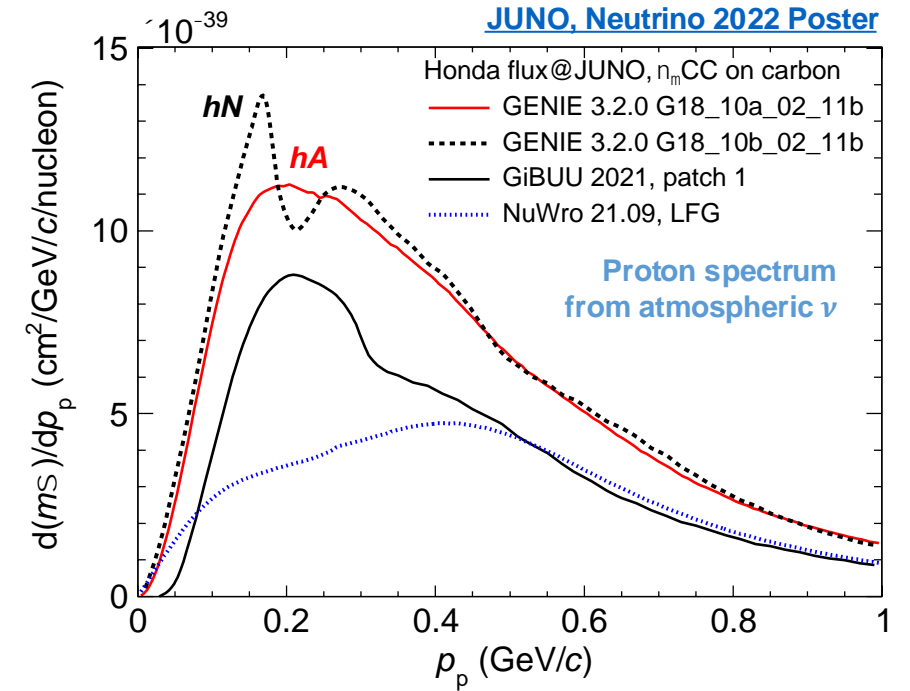


Final-state proton in neutrino interactions: **momentum** evolves as it propagates out of the nucleus.

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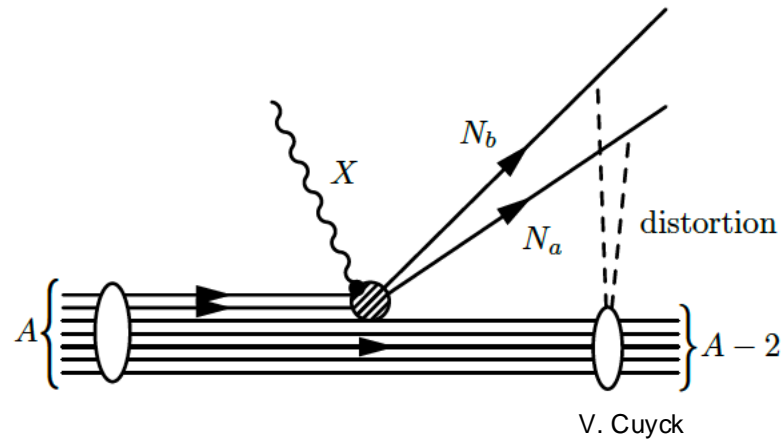
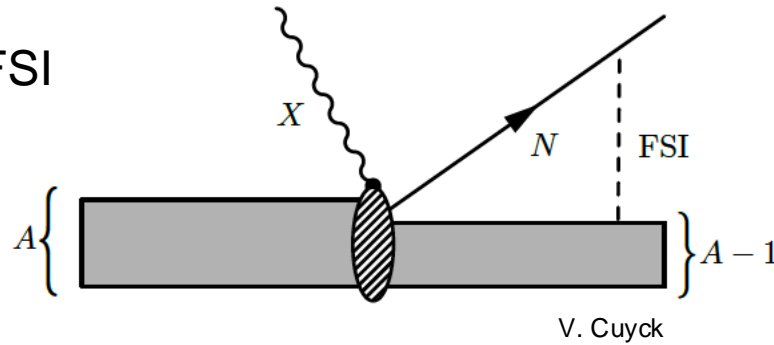
# Intranuclear Dynamics and Neutrino Oscillation Measurements

How well can we measure neutrino energy?

(reminder: oscillation very sensitive to baseline and energy,  $L/E$ )

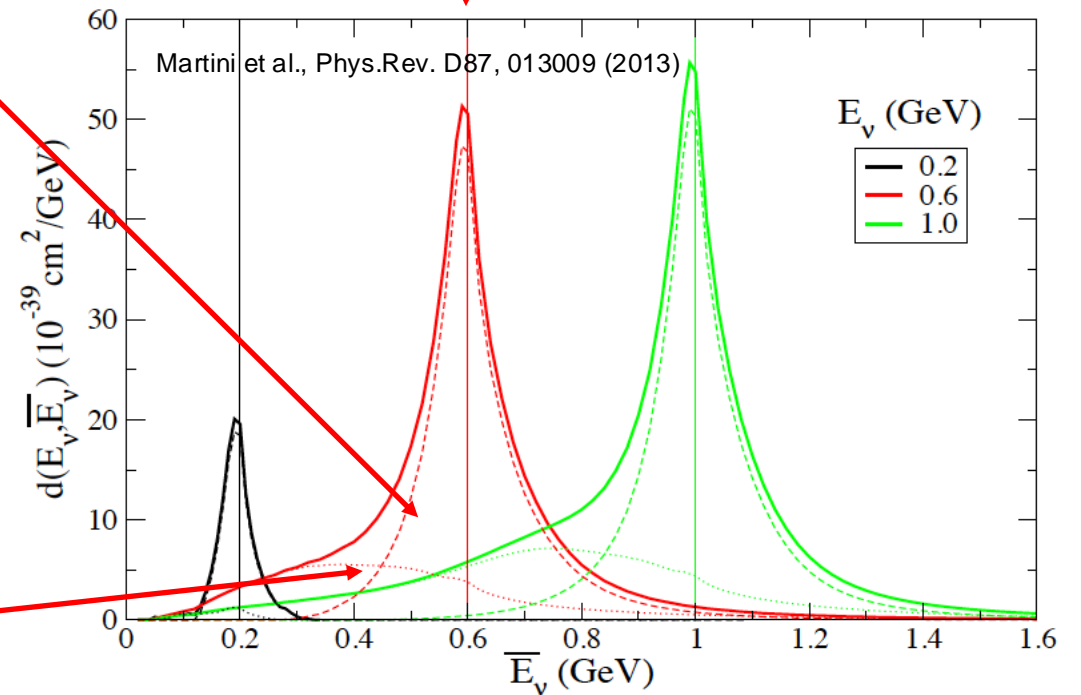
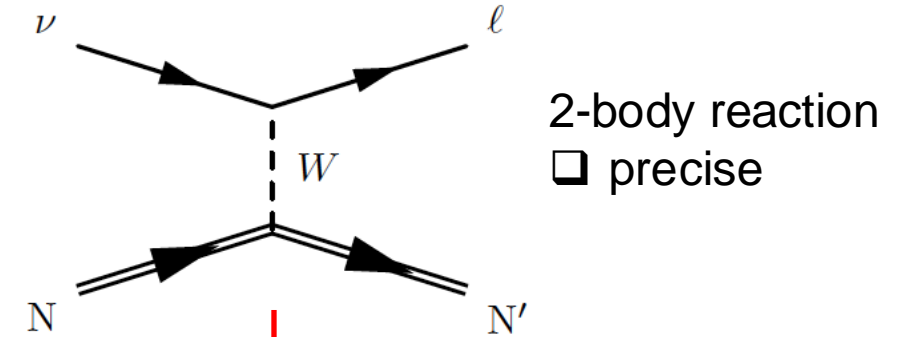
Fermi motion, FSI

□ spread

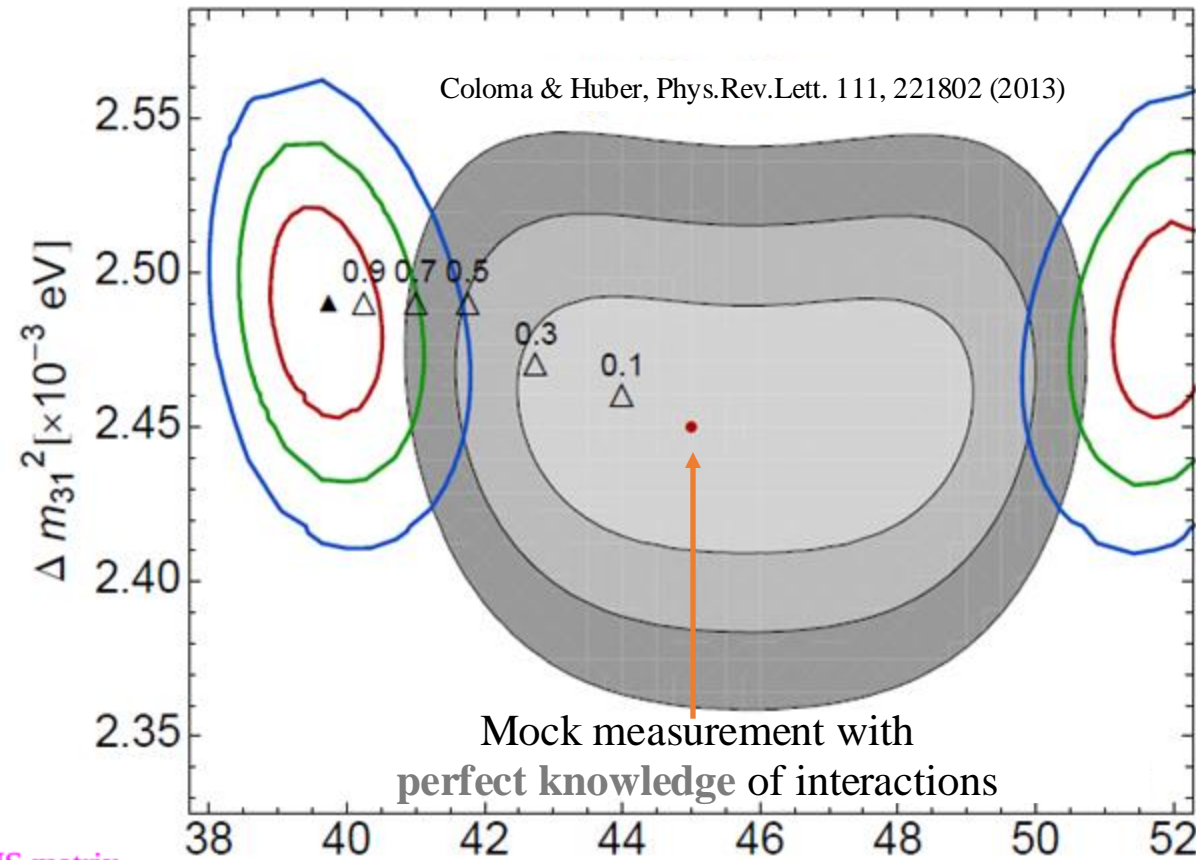


2p2h, pion absorption (missing particles)

□ Large fraction of large bias and spread



# Intranuclear Dynamics and Neutrino Oscillation Measurements



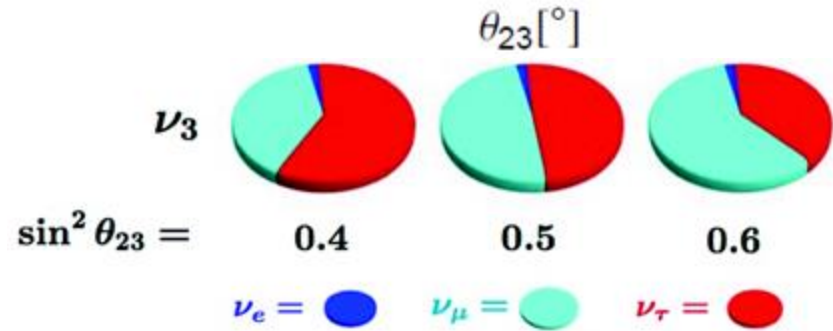
Mixing between  $\mu$  and  $\tau$  flavors

$$c_{ij} = \cos\theta_{ij}$$

$$s_{ij} = \sin\theta_{ij}$$

PMNS matrix

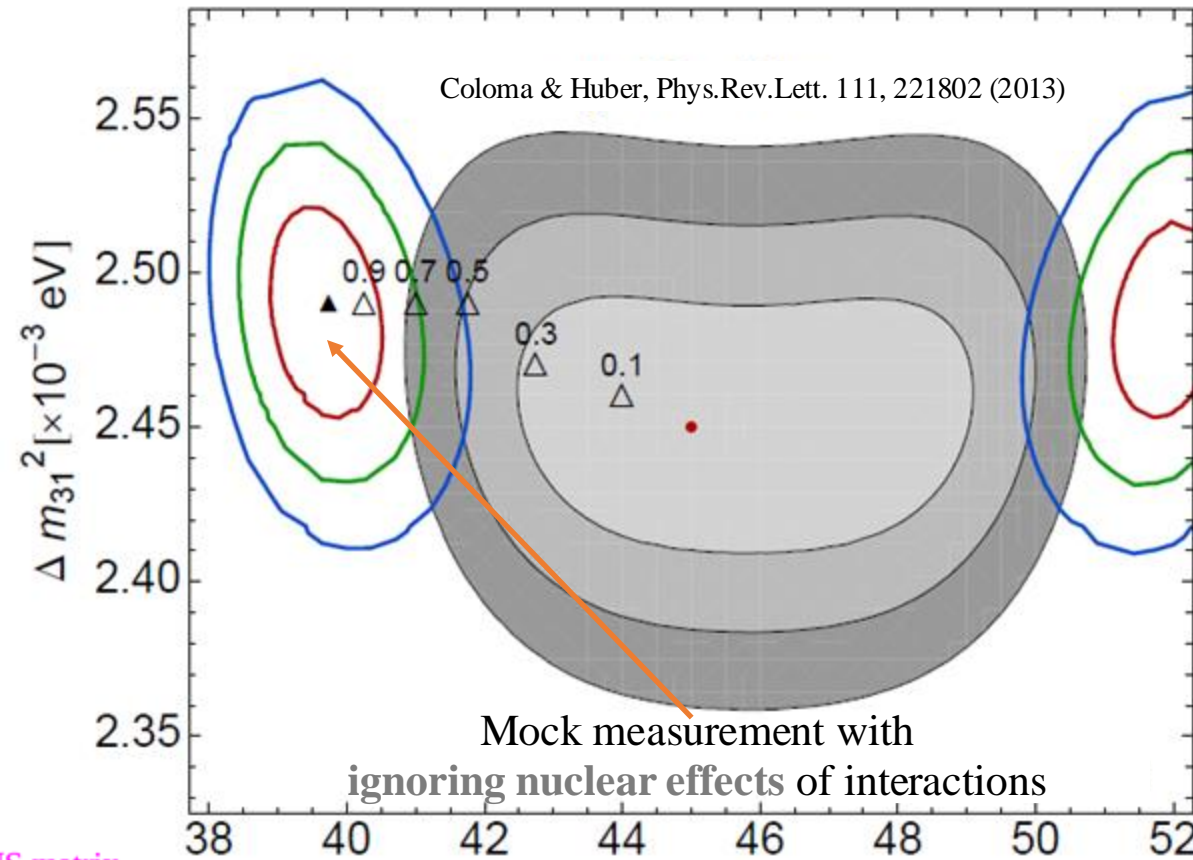
$$\begin{pmatrix} \nu_e \\ \nu_\mu \\ \nu_\tau \end{pmatrix} = \begin{pmatrix} 1 & 0 & 0 \\ 0 & c_{23} & s_{23} \\ 0 & -s_{23} & c_{23} \end{pmatrix}$$



Parke, 1801.09643



# Intranuclear Dynamics and Neutrino Oscillation Measurements



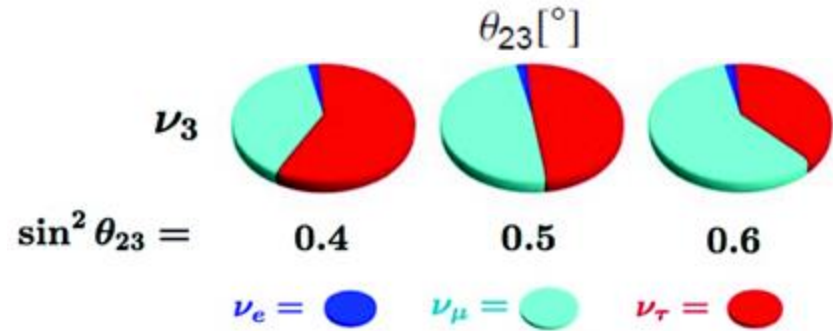
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Parke, 1801.09643

# $\nu_e/\bar{\nu}_e$ interactions

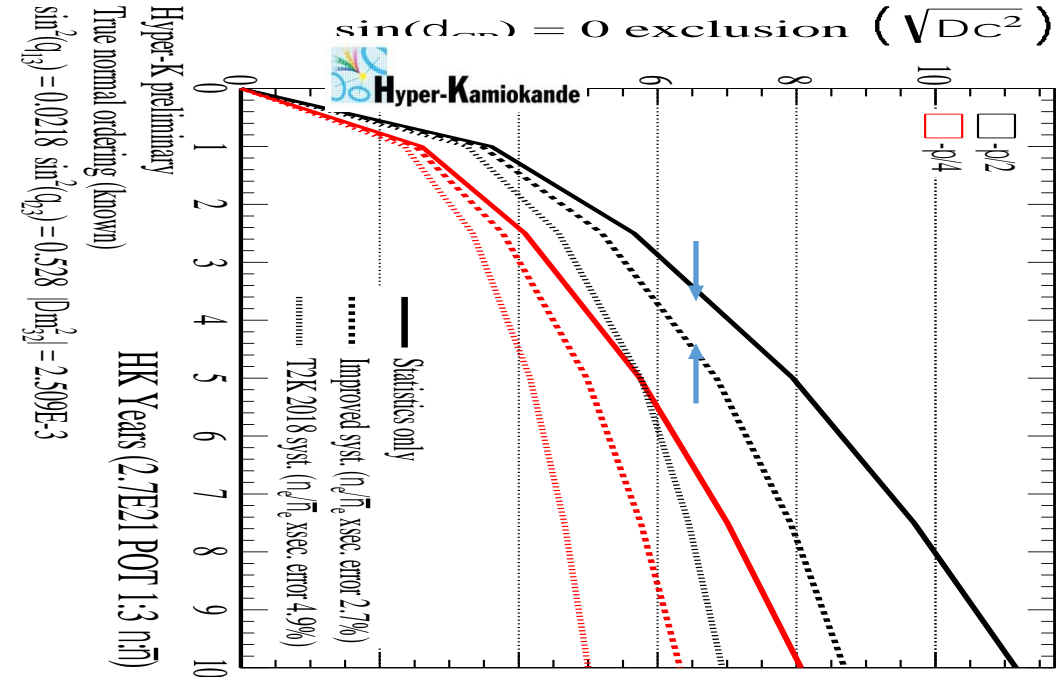
- ❑  $\delta_{CP}$  requires  $\nu_e$  and  $\bar{\nu}_e$  appearance
  - ✓ Suppress  $\nu_e$  and  $\bar{\nu}_e$  bkg in beams
- ❑ Need  $\nu_e/\bar{\nu}_e$  interaction data
- ❑  $\nu_\mu$ -A + lepton universality constrains  $\nu_e$ -A to 1<sup>st</sup> order precision
- ❑ Oscillation requires 2<sup>nd</sup> order precision
  - ✓ *Higher statistics and better-understood fluxes*

Lepton mass correction Hadronic/nuclear response

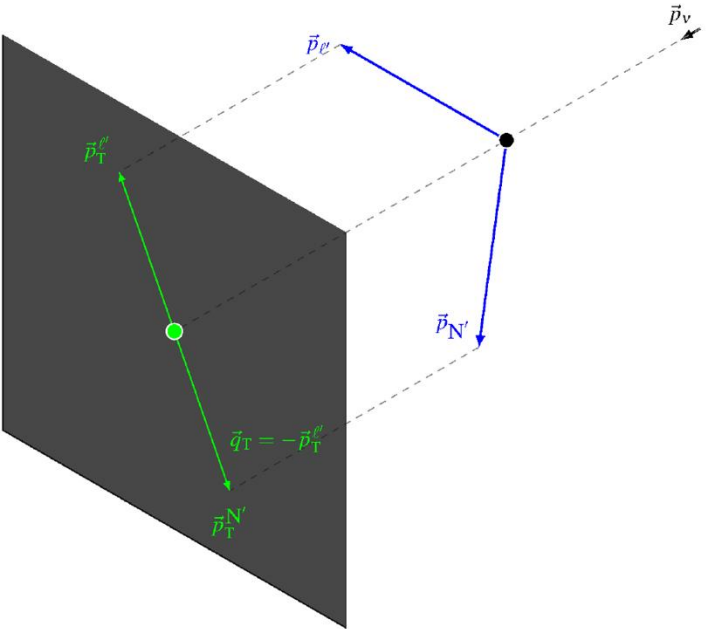
$$E_\nu^{\text{tree-level}} = \frac{m_\ell^2 + Q^2}{2(E_\ell - p_\ell \cos \theta_\ell)}$$

Lepton observables

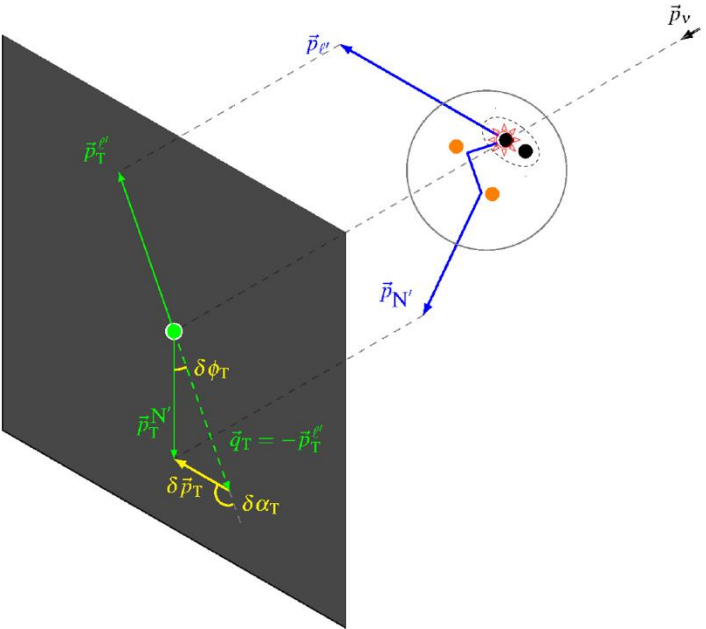
❖ QED radiative corrections and lepton mass “nudge”  $Q^2$ , shifting internal  $(q_0, \vec{q}_3)$  phase space



# Transverse Kinematic Imbalance (TKI) to measure intranuclear dynamics



Stationary free nucleon target



- Nuclear target ( $A > 1$ )
- Fermi motion
  - FSI
  - 2p2h

## Missing energy



From Wikipedia, the free encyclopedia

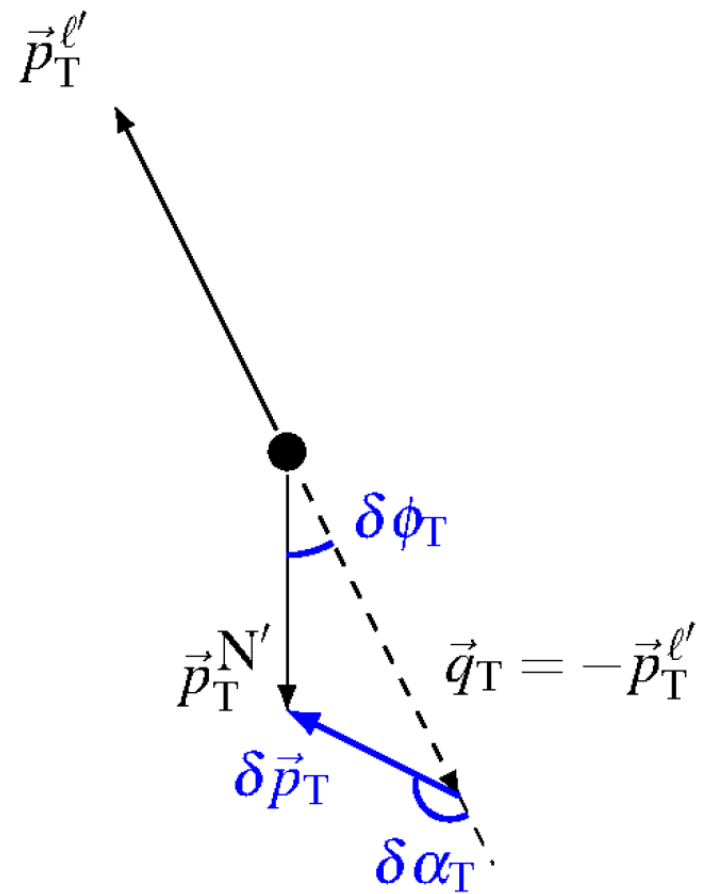
[...]  
[neutrinos](#).<sup>[1]</sup> In general, missing energy is used to infer the presence of non-detectable particles and is expected to be a signature of many theories of [physics beyond the Standard Model](#).<sup>[2][3][4]</sup>  
 [...]  
[hadron colliders](#).<sup>[5]</sup> The initial momentum of the colliding [partons](#) along the beam axis is not known —

## TKI

- Multi-dimensional observation
- Momentum (magnitude)
  - Angle
  - Asymmetry

[Lu, et al., Phys.Rev.D 92, 051302 \(2015\)](#)  
[Lu, et al., Phys.Rev.C 94, 015503 \(2016\)](#)

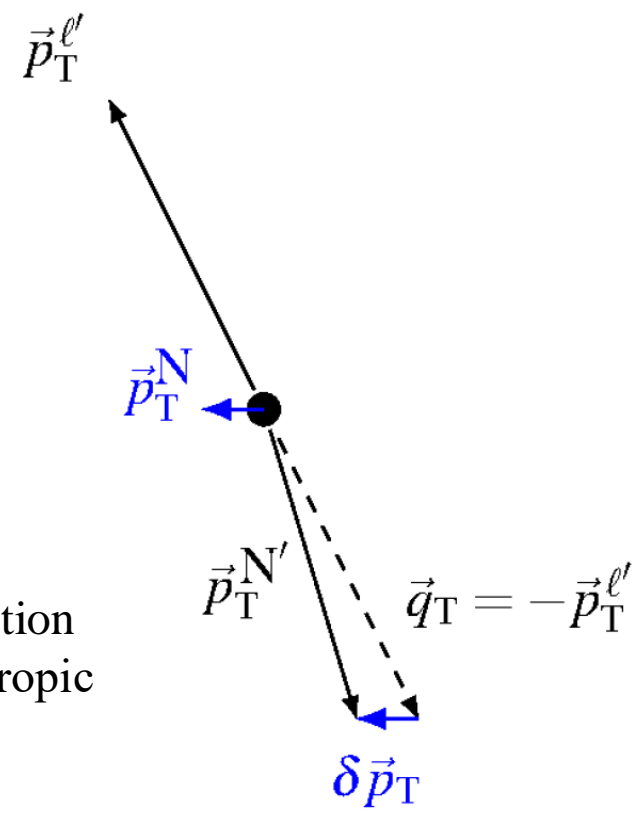
# Transverse Boosting Angle $\delta\alpha_T$



if Fermi motion only



$\delta\vec{p}_T = \vec{p}_T^N$   
 $\delta\alpha_T$  is Fermi motion  
 direction  $\rightarrow$  isotropic



In full

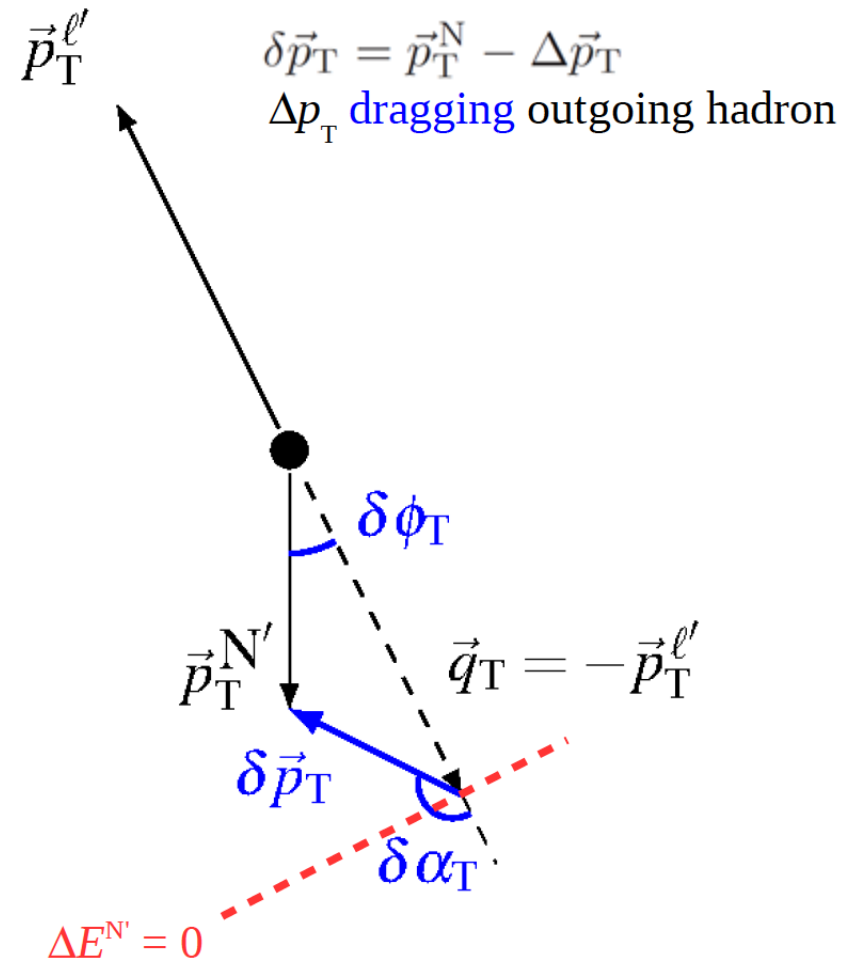
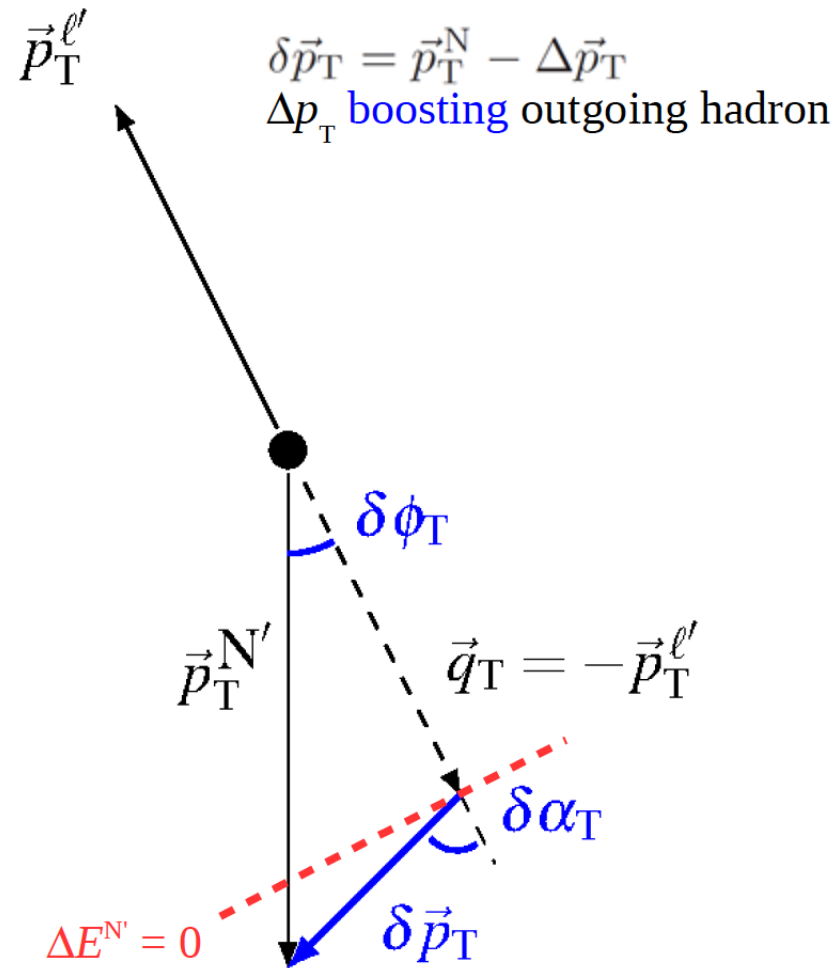
$$\delta\vec{p}_T = \vec{p}_T^N - \Delta\vec{p}_T$$

$\Delta\vec{p}_T$  — FSI and missing particles

- $\delta\vec{p}_T$
- total transverse momentum
- transverse momentum imbalance
- missing pT
- ...



# Transverse Boosting Angle $\delta\alpha_T$



FSI and momentum sharing with extra particles

- pion absorption
- 2p2h

# Emulated Nucleon Momentum $p_N$

[Furmanski & Sobczyk, Phys.Rev.C 95, 065501 (2017)]

A more general analysis of kinematic imbalance

Transverse:  $0 = \vec{p}_T^{\ell'} + \vec{p}_T^{N'} - \delta\vec{p}_T$

Longitudinal:  $E_\nu = p_L^{\ell'} + p_L^{N'} - \delta p_L$

New variable:  $p_n \equiv \sqrt{\delta p_T^2 + \delta p_L^2}$

Neutrino energy is unknown (in the first place), equations are not closed.

Assuming exclusive  $\mu$ -p-A' final states

Use energy conservation to close the equations

$$E_\nu + m_A = E_{\ell'} + E_{N'} + E_{A'}$$

$$E_{A'} = \sqrt{m_{A'}^2 + p_n^2}$$

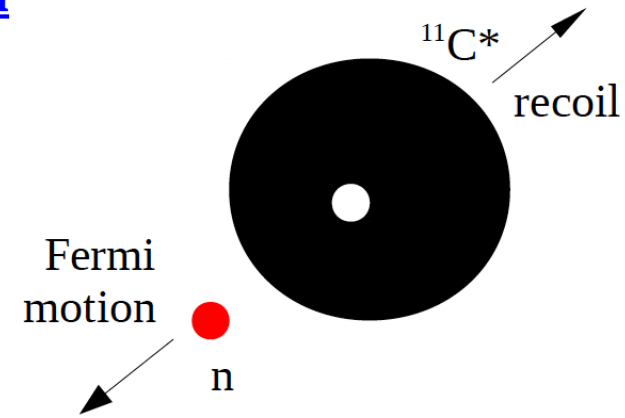
$p_n$ : recoil momentum of the nuclear remnant

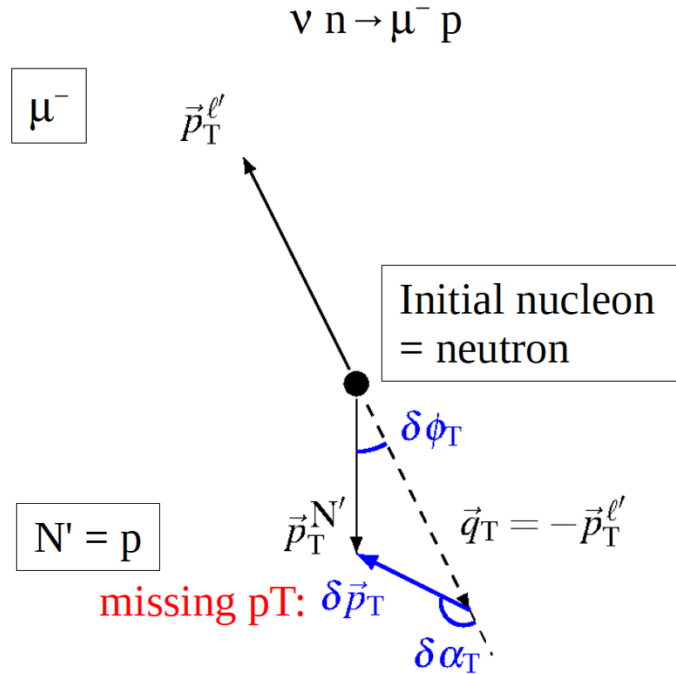
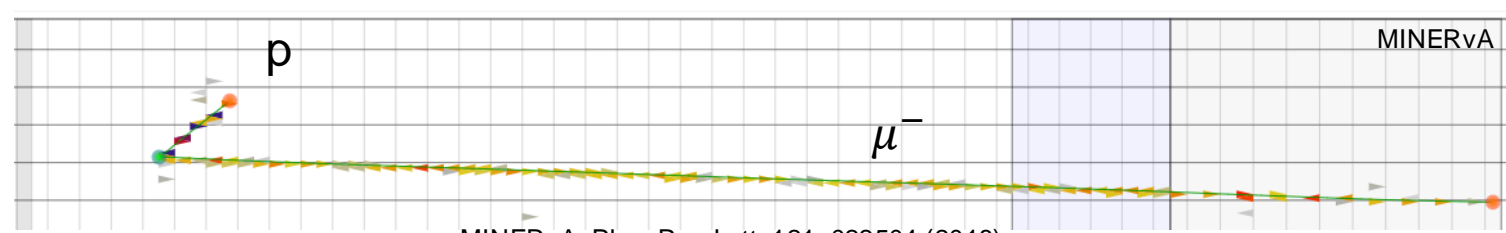
final-state

**Dual Interpretation**

For CCQE,  $A' = {}^{11}\text{C}^*$   
No more unknowns  
 $p_n$ : neutron Fermi motion

initial-state

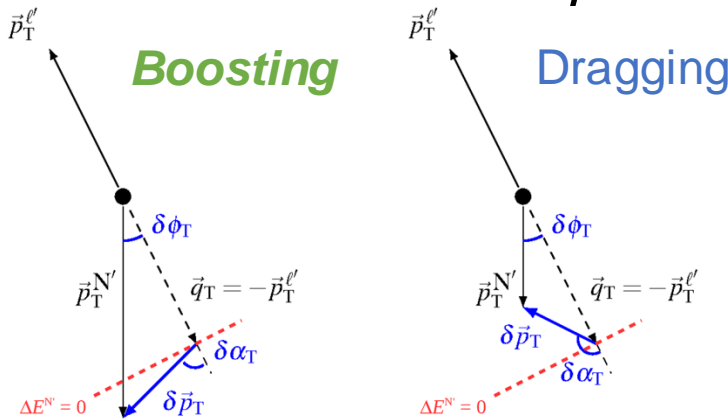
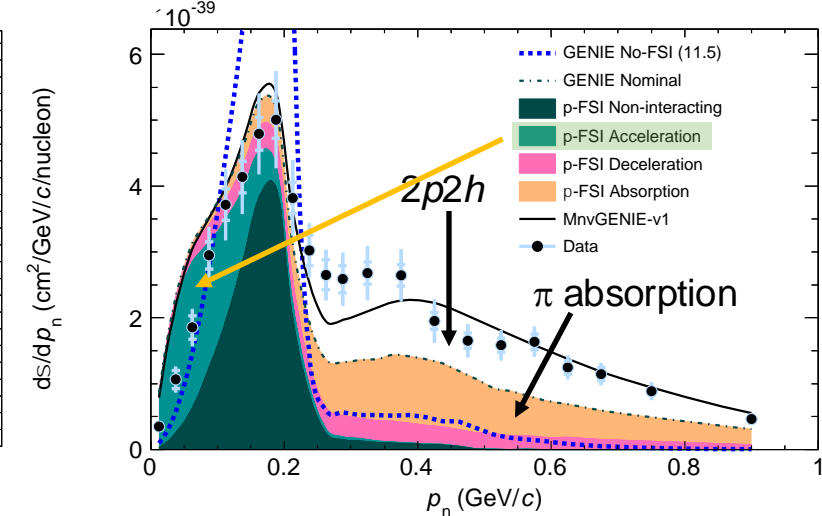
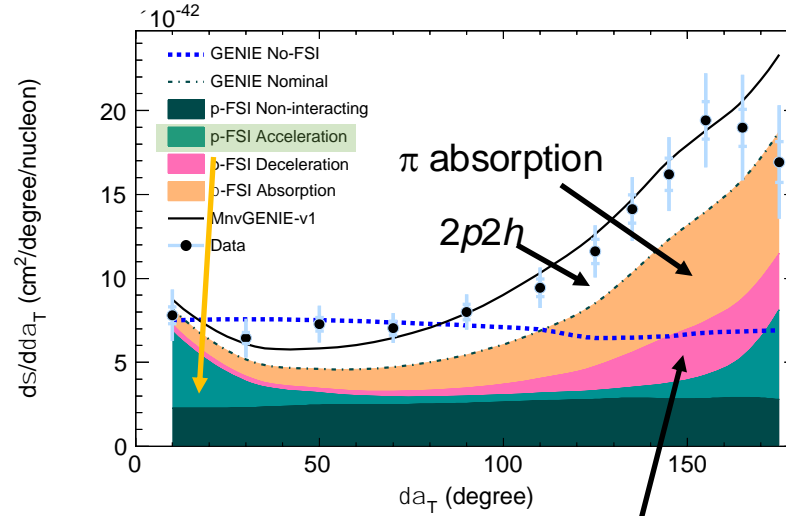
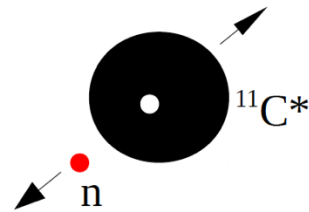




Assuming target remnant  $^{11}\text{C}^*$

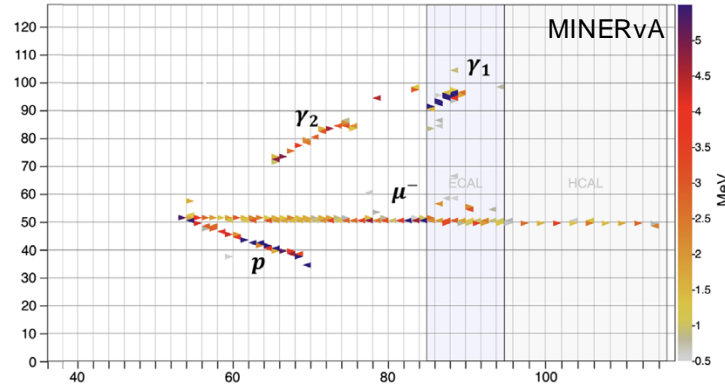
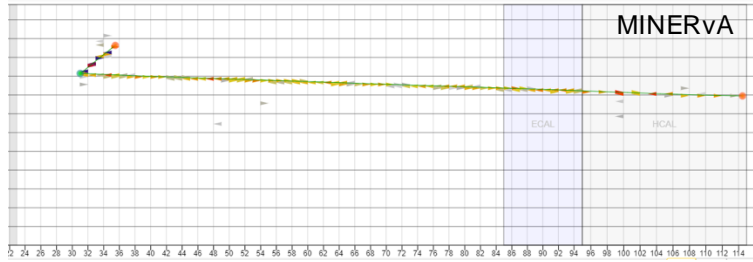
$$p_n \equiv \sqrt{\delta p_T^2 + \delta p_L^2}$$

$$\sim [1 + O(10\%)] \times \delta p_T$$

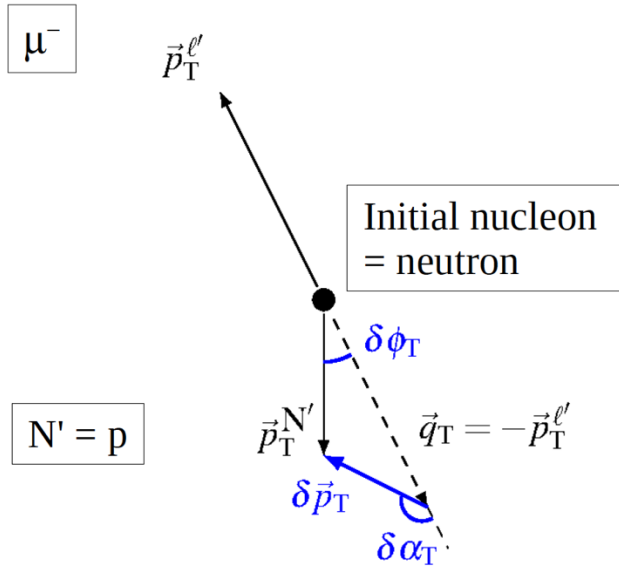


## Abnormal acceleration?!

- ☐ GENIE FSI (v2.8 hA)
- ✓ *Not dark energy*
- ✓ *Identified by  $\delta\alpha_T$  prior to measurement*
- ✓ Fixed after measurement

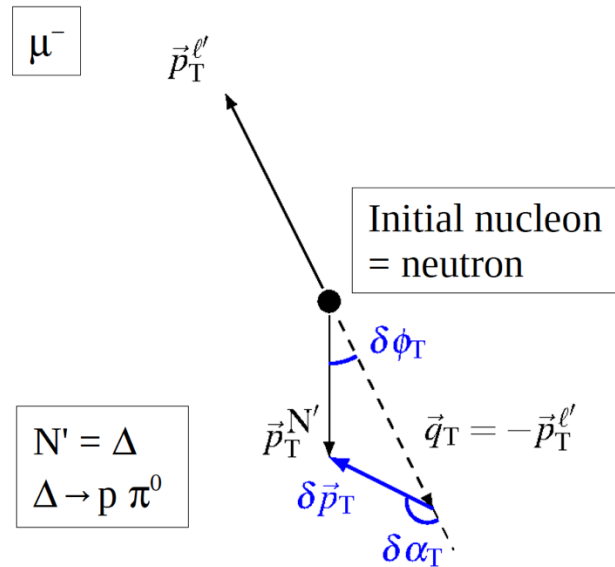


$$\nu n \rightarrow \mu^- p$$



via  $CC0\pi$  measurement

$$\nu n \rightarrow \mu^- p \pi^0$$

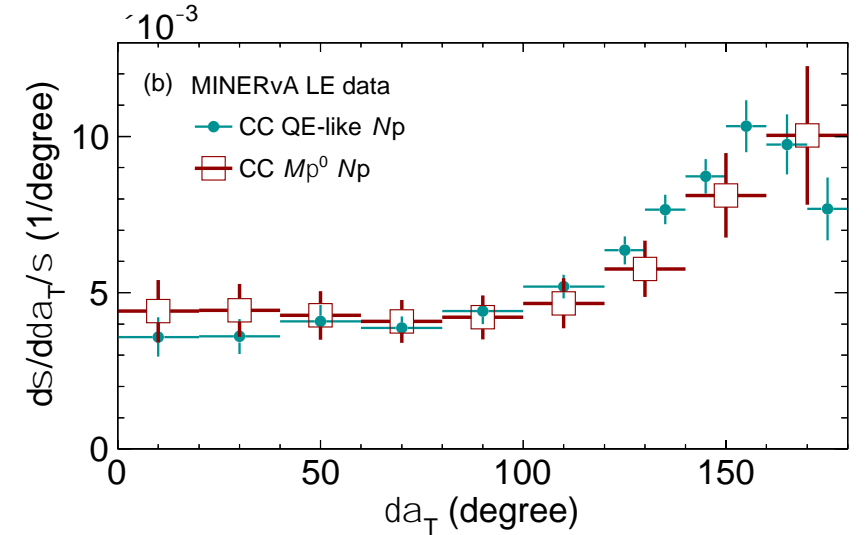
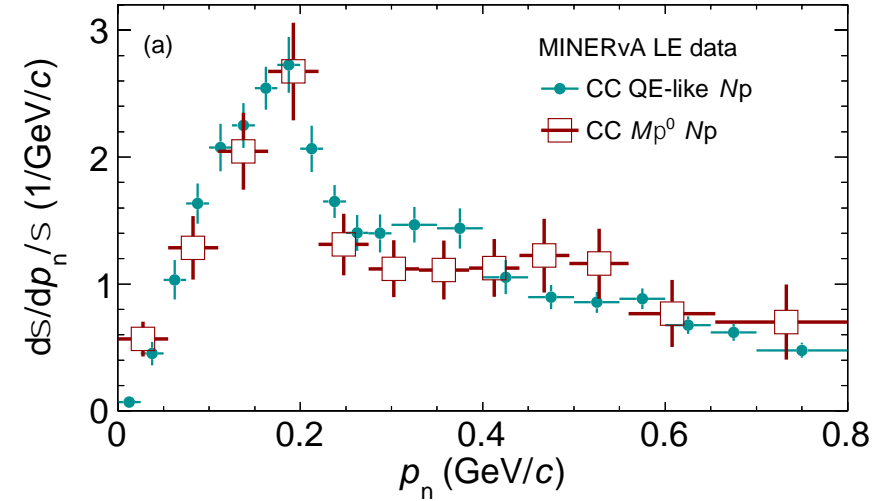


via inclusive  $\pi^0$  production

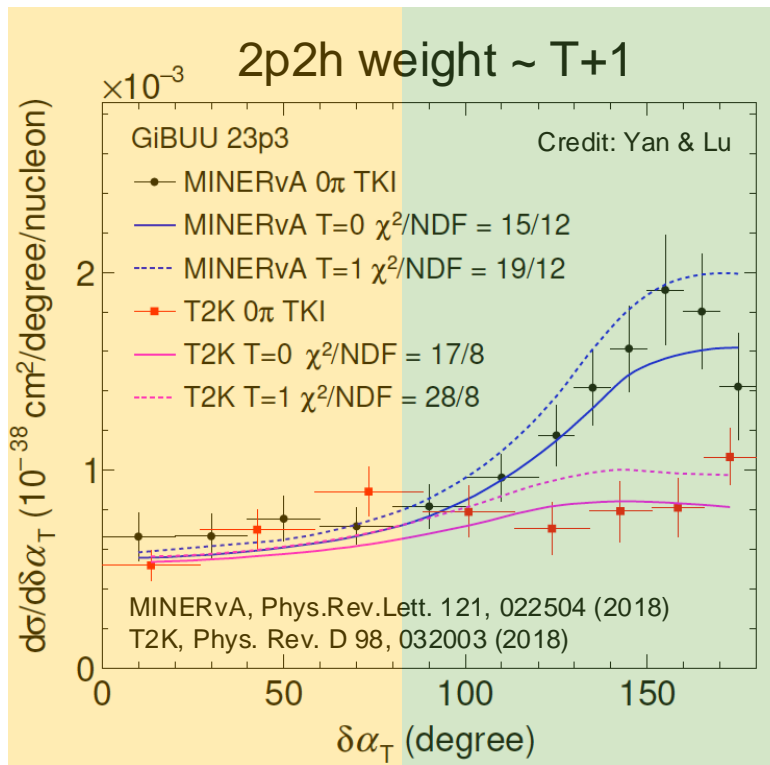
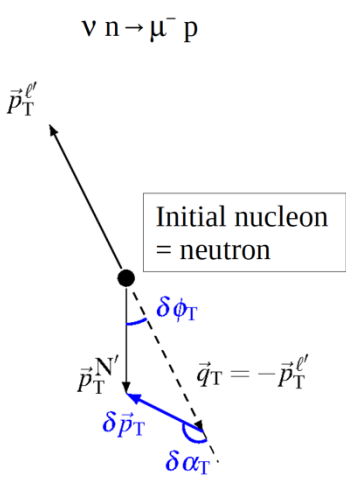
[Lu & Sobczyk, Phys.Rev.C 99, 055504 (2019)]

## Surprising consistency!

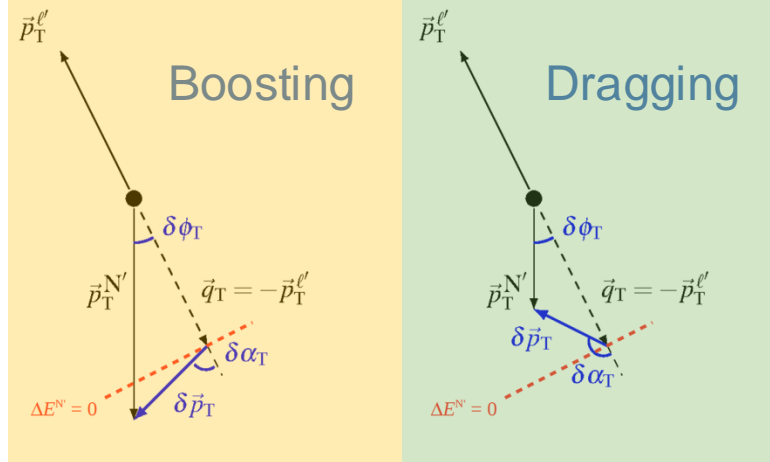
[More detailed discussions see Q. Yan (严启宇)'s talk in the afternoon session]



# TKI: FSI and 2p2h

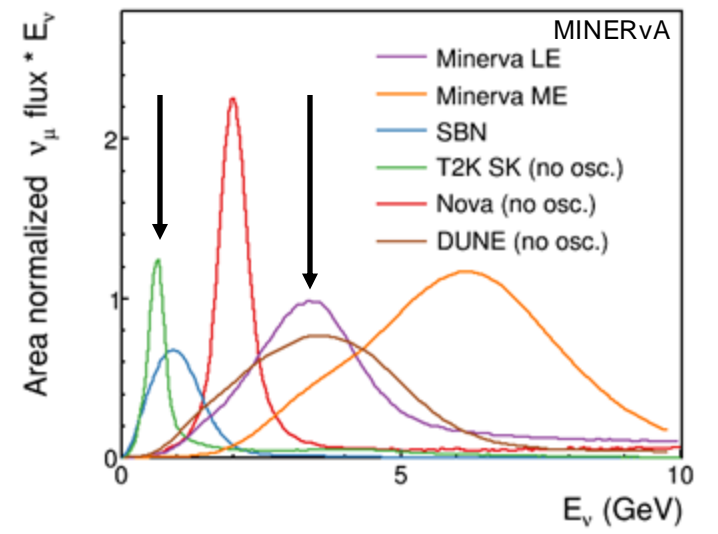
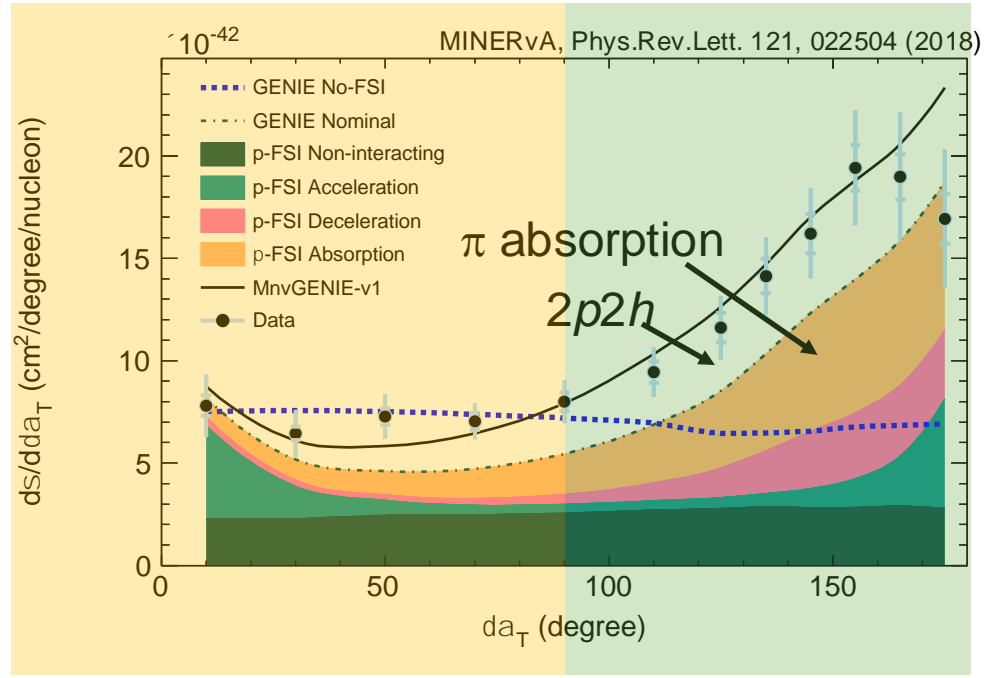


➤ Consistent QE xsec



➤ At T2K energy: smaller pion production and absorption

➤ Also sensitive to 2p2h





# Summary and Conclusion

1. Neutrino interactions: critical for precise oscillation measurements
  - Affect energy reconstruction through Fermi motion, FSI, and 2p2h
  - Ambiguous event category: require practical topology (CC0 $\pi$ , CC1 $\pi$ , etc.) rather than physical interactions (quasi-elastic, resonant, DIS, etc.)
  - $\delta_{CP}$  measurement: sensitive to  $\nu_e$  interactions deviation from  $\nu_\mu$
2. Neutrino interactions: essential for studying nuclear dynamics.
  - Nuclear medium response to electroweak probe
  - Rich phenomenology + a growing field beyond neutrino = *no conclusion yet*
3. Transverse Kinematic Imbalance (TKI): a new tool for probing individual intranuclear medium effects.
  - Enlarging body of individual and joint analyses with data from T2K, MINERvA and others

# *BACKUP*

# PMNS Matrix

$$c_{ij} = \cos\theta_{ij}$$

$$s_{ij} = \sin\theta_{ij}$$

PMNS matrix

$$\begin{pmatrix} \nu_e \\ \nu_\mu \\ \nu_\tau \end{pmatrix} = \begin{pmatrix} 1 & 0 & 0 \\ 0 & c_{23} & s_{23} \\ 0 & -s_{23} & c_{23} \end{pmatrix} \begin{pmatrix} c_{13} & 0 & s_{13}e^{-i\delta_{CP}} \\ 0 & 1 & 0 \\ -s_{13}e^{i\delta_{CP}} & 0 & c_{13} \end{pmatrix} \begin{pmatrix} c_{12} & s_{12} & 0 \\ -s_{12} & c_{12} & 0 \\ 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} \nu_1 \\ \nu_2 \\ \nu_3 \end{pmatrix}$$

$\theta_{13} \neq 0 \rightarrow \delta_{CP}$  can be observed

$\theta_{12}$ : mixing between  $\nu_1$  and  $\nu_2$

$\theta_{23}$ : mixing between  $\nu_\mu$  and  $\nu_\tau$

$\theta_{13}$ : if 0, effective 2 flavour mixing

$$\begin{pmatrix} \nu_e \\ \nu_\mu \\ \nu_\tau \end{pmatrix} = \begin{pmatrix} 1 & 0 & 0 \\ 0 & c_{23} & s_{23} \\ 0 & -s_{23} & c_{23} \end{pmatrix} \begin{pmatrix} \nu_1' \\ \nu_2' \\ \nu_3 \end{pmatrix}$$

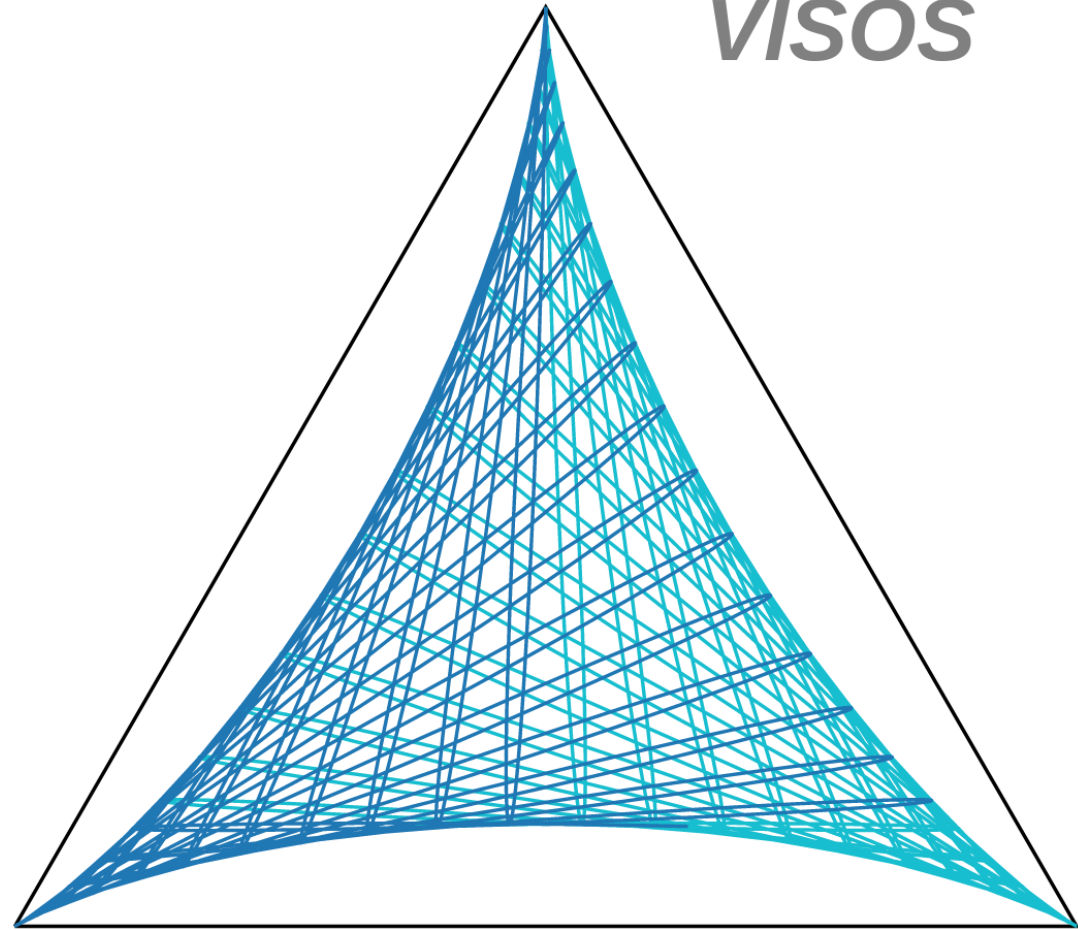
# PMNS

$$\begin{bmatrix} \nu_e \\ \nu_\mu \\ \nu_\tau \end{bmatrix} = \begin{bmatrix} U_{e1} & U_{e2} & U_{e3} \\ U_{\mu1} & U_{\mu2} & U_{\mu3} \\ U_{\tau1} & U_{\tau2} & U_{\tau3} \end{bmatrix} \begin{bmatrix} \nu_1 \\ \nu_2 \\ \nu_3 \end{bmatrix}$$

Trimaximal mixing  
— maximally CP-violating

$$\left( |U_{i\alpha}|^2 \right) = \begin{bmatrix} \frac{1}{3} & \frac{1}{3} & \frac{1}{3} \\ \frac{1}{3} & \frac{1}{3} & \frac{1}{3} \\ \frac{1}{3} & \frac{1}{3} & \frac{1}{3} \end{bmatrix}$$

VISOS



VISOS

Beautiful but *not* how Nature works  $\_ \_ (\_ \_ ) \_ \_ /$

# Counting oscillated $\nu$

At **far detector**, interactions **cannot** be measured with **unknown oscillated flux**

$$\text{Measurement} = (\text{flux} \times \text{interaction}) \oplus \text{detector effects}$$

No two unknowns at the same time

