

重味物理前沿论坛研讨会

Workshop of Frontiers in Heavy Flavor Physics



暨南大学  
JINAN UNIVERSITY

# Global Fits of $b \rightarrow s\ell^+\ell^-$

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合作者：温侨毅, PRD 108, 095038 (2023)

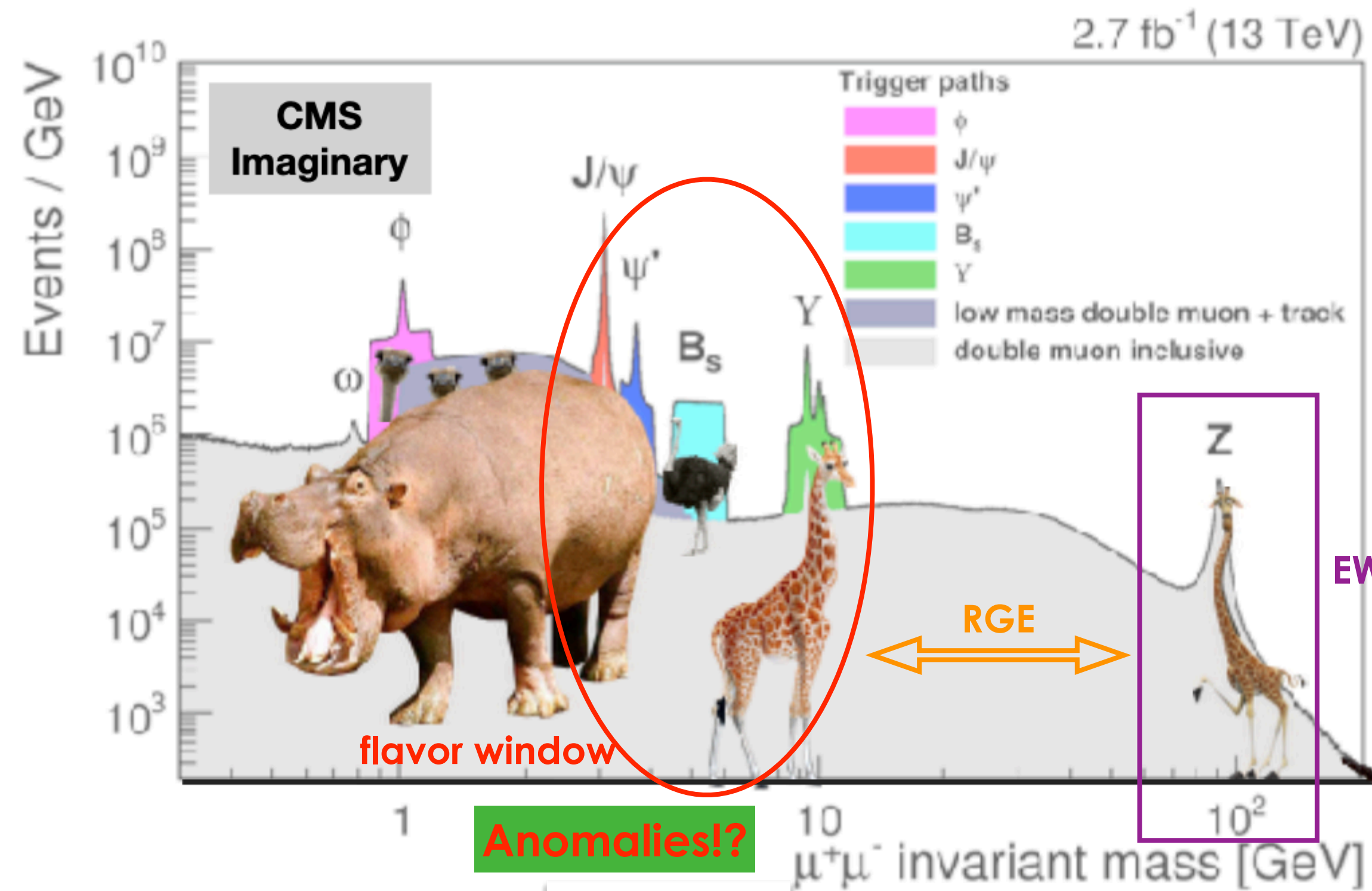
华中师范大学, 2023.11.26

# OUTLINE

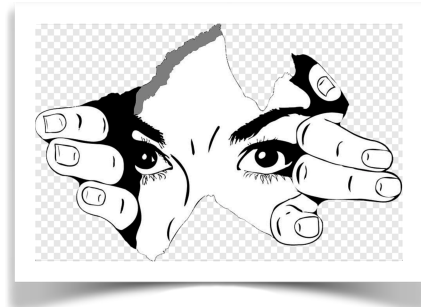
- Introduction
- Theory overview
- Fitting overview
- Our results and implications
- Summary

# INTRODUCTION

Flavor physics is a probe of new physics.



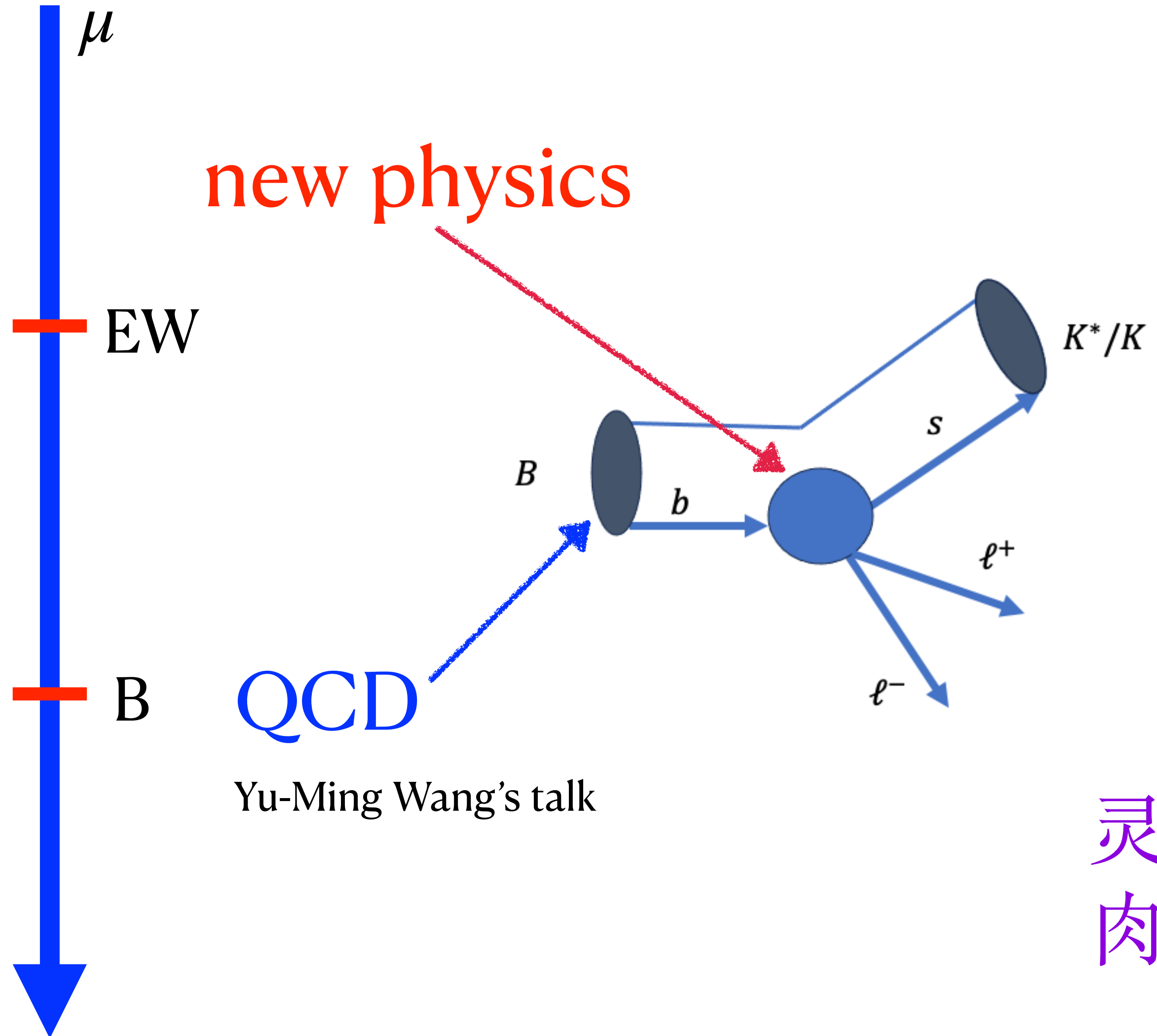
Anomalies!?





$[\text{quark}]_{\text{flavour}} = V_{CKM} [\text{quark}]_{\text{mass}}$   
 weakly interacting                      strongly produced

$$V_{CKM} = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix}$$



灵魂在天上  
肉身 在尘世

# EARLY PURSUIT OF NEW PHYSICS: LARGE BR & NON-ZERO AFB

RAPID COMMUNICATIONS

PHYSICAL REVIEW D, VOLUME 59, 011701

## Promising process to distinguish supersymmetric models with large $\tan\beta$ from the standard model: $B \rightarrow X_s \mu^+ \mu^-$

Chao-Shang Huang,<sup>\*</sup> Wei Liao,<sup>†</sup> and Qi-Shu Yan<sup>‡</sup>

*Institute of Theoretical Physics, Academia Sinica, P.O. Box 2735, Beijing 100080, People's Republic of China*

(Received 15 June 1998; published 17 November 1998)

It is shown that in supersymmetric models the large supersymmetric contributions to  $B \rightarrow X_s \mu^+ \mu^-$  come from the Feynman diagrams which consist of exchanging neutral Higgs boson loops and are proportional to  $m_b m_\mu \tan^3 \beta / m_h^2$  when  $\tan\beta$  is large and the mass of the lightest neutral Higgs boson  $m_h$  is not too large (say, less than 150 GeV). Numerical results show that the branching ratios of  $B \rightarrow X_s \mu^+ \mu^-$  can be enhanced by more than 100% compared to the standard model (SM) and the backward-forward asymmetry of the lepton is significantly different from that in the SM when  $\tan\beta \geq 30$ . [S0556-2821(98)50123-3]

PACS number(s): 12.60.Jv, 13.20.He

PHYSICAL REVIEW D, VOLUME 62, 094023

## Exclusive semileptonic rare decays $B \rightarrow (K, K^*) l^+ l^-$ in supersymmetric theories

Qi-Shu Yan<sup>\*</sup>

*Physics Department of Tsinghua University, People's Republic of China*

Chao-Shang Huang,<sup>†</sup> Wei Liao,<sup>‡</sup> and Shou-Hua Zhu<sup>§</sup>

*Institute of Theoretical Physics, the Chinese Academy Science, People's Republic of China*

(Received 1 May 2000; published 11 October 2000)

The invariant mass spectrum, forward-backward asymmetry, and lepton polarizations of the exclusive processes  $B \rightarrow K(K^*) l^+ l^-$ ,  $l = \mu, \tau$  are analyzed in a supersymmetric context. Special attention is paid to the effects of neutral Higgs bosons (NHB's). Our analysis shows that the branching ratio of the process  $B \rightarrow K \mu^+ \mu^-$  can be quite largely modified by the effects of neutral Higgs bosons and the forward-backward asymmetry would not vanish. For the process  $B \rightarrow K^* \mu^+ \mu^-$ , the lepton transverse polarization is quite sensitive to the effects of NHB's, while the invariant mass spectrum, forward-backward asymmetry, and lepton longitudinal polarization are not. For both  $B \rightarrow K \tau^+ \tau^-$  and  $B \rightarrow K^* \tau^+ \tau^-$ , the effects of NHB's are quite significant. The partial decay widths of these processes are also analyzed, and our analysis manifests that, even taking into account the theoretical uncertainties in calculating weak form factors, the effects of NHB's could make supersymmetry show up.

PACS number(s): 13.20.He, 12.60.Jv, 13.25.Hw

PHYSICAL REVIEW D, VOLUME 63, 114021

## $B_s \rightarrow l^+ l^-$ in a type-II two-Higgs-doublet model and the minimal supersymmetric standard model

Chao-Shang Huang,<sup>1,\*</sup> Liao Wei,<sup>1,†</sup> Qi-Shu Yan,<sup>2,‡</sup> and Shou-Hua Zhu<sup>1,3,§</sup>

<sup>1</sup>*Institute of Theoretical Physics, Academia Sinica, 100080 Beijing, China*

<sup>2</sup>*Physics Department of Tsinghua University, 100080 Beijing, China*

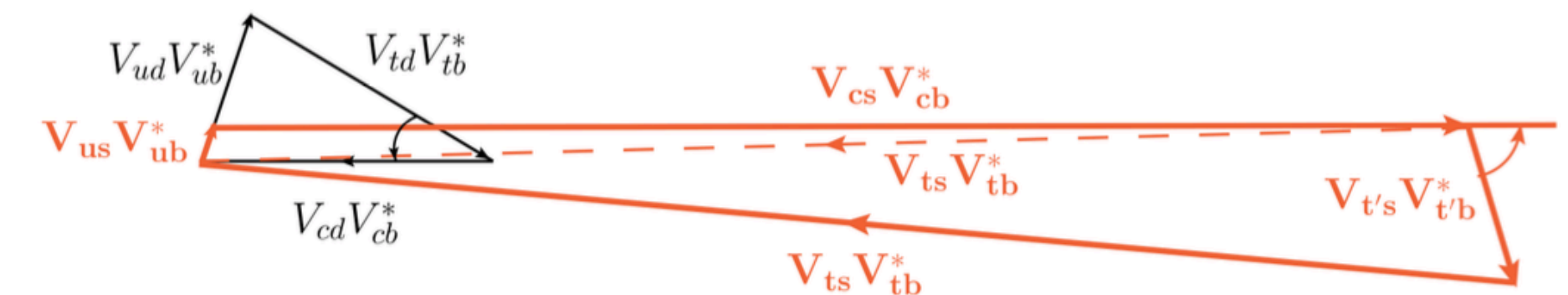
<sup>3</sup>*Institut für Theoretische Physik, Universität Karlsruhe, D-76128 Karlsruhe, Germany*

(Received 17 December 2000; published 7 May 2001)

In this paper we analyze the process  $B_s \rightarrow l^+ l^-$  in a type-II two-Higgs-doublet model (2HDM) and the minimal supersymmetric standard model (MSSM). All the leading terms of Wilson coefficients relevant to the process are given in the large  $\tan\beta$  limit. It is shown that the decay width for  $B_s \rightarrow l^+ l^-$  depends on all parameters except  $m_{A^0}$  in the 2HDM. The branching ratio of  $B_s \rightarrow \mu^+ \mu^-$  can reach its experimental bound in some large  $\tan\beta$  regions of the parameter space in the MSSM because the amplitude increases as  $\tan^3\beta$  in the regions. For  $l = \tau$ , the branching ratio can even reach  $10^{-4}$  in the regions. Therefore, the experimental measurements of leptonic decays of  $B_s$  could put a constraint on the contributions of neutral Higgs bosons and consequently the parameter space in the MSSM.

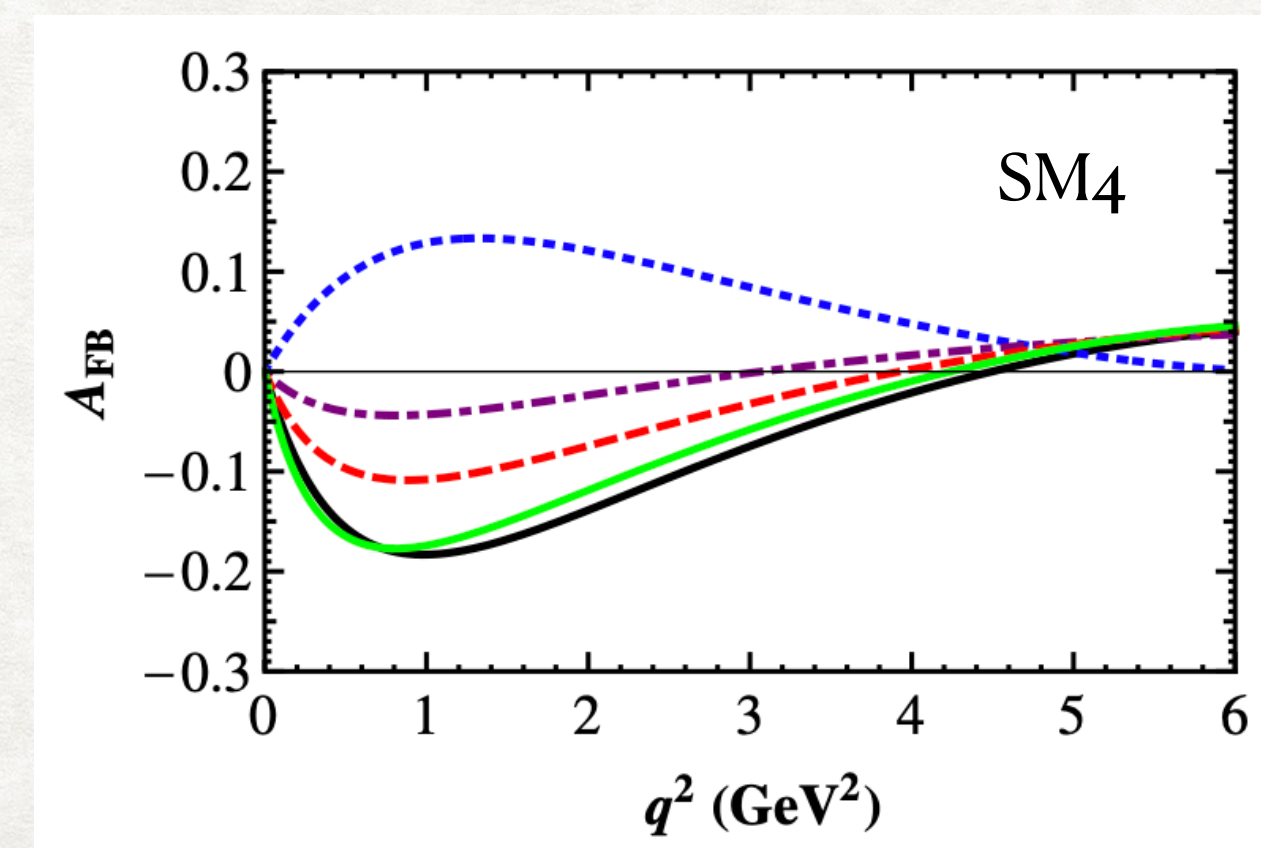
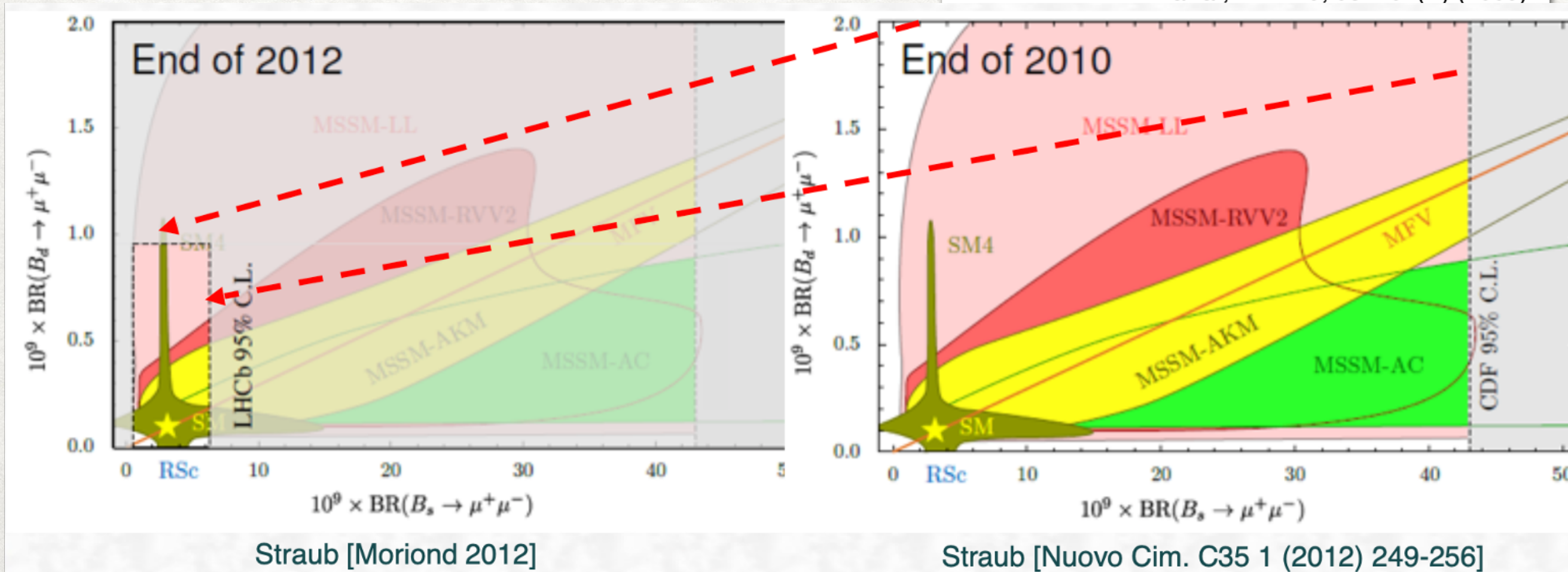
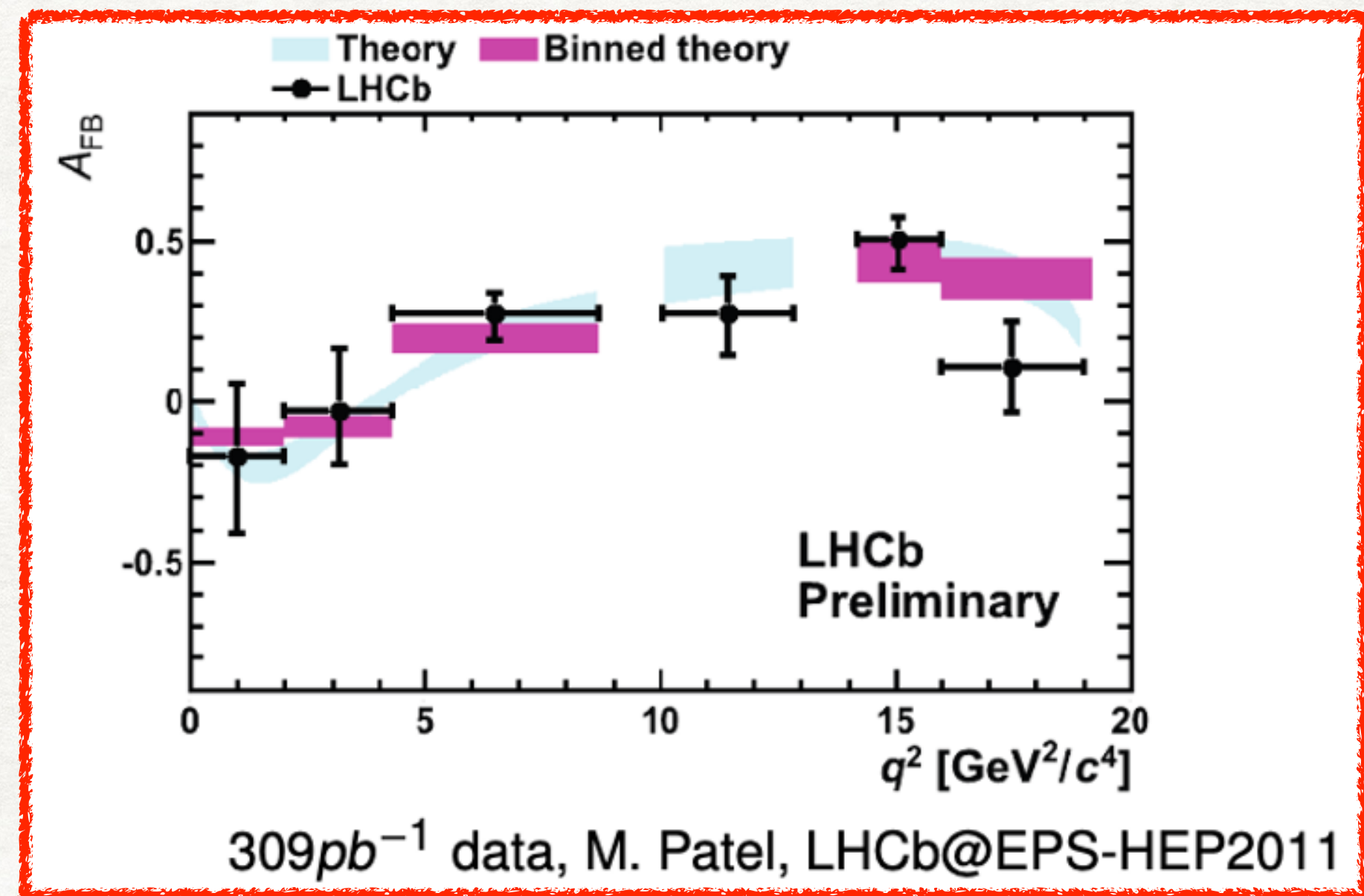
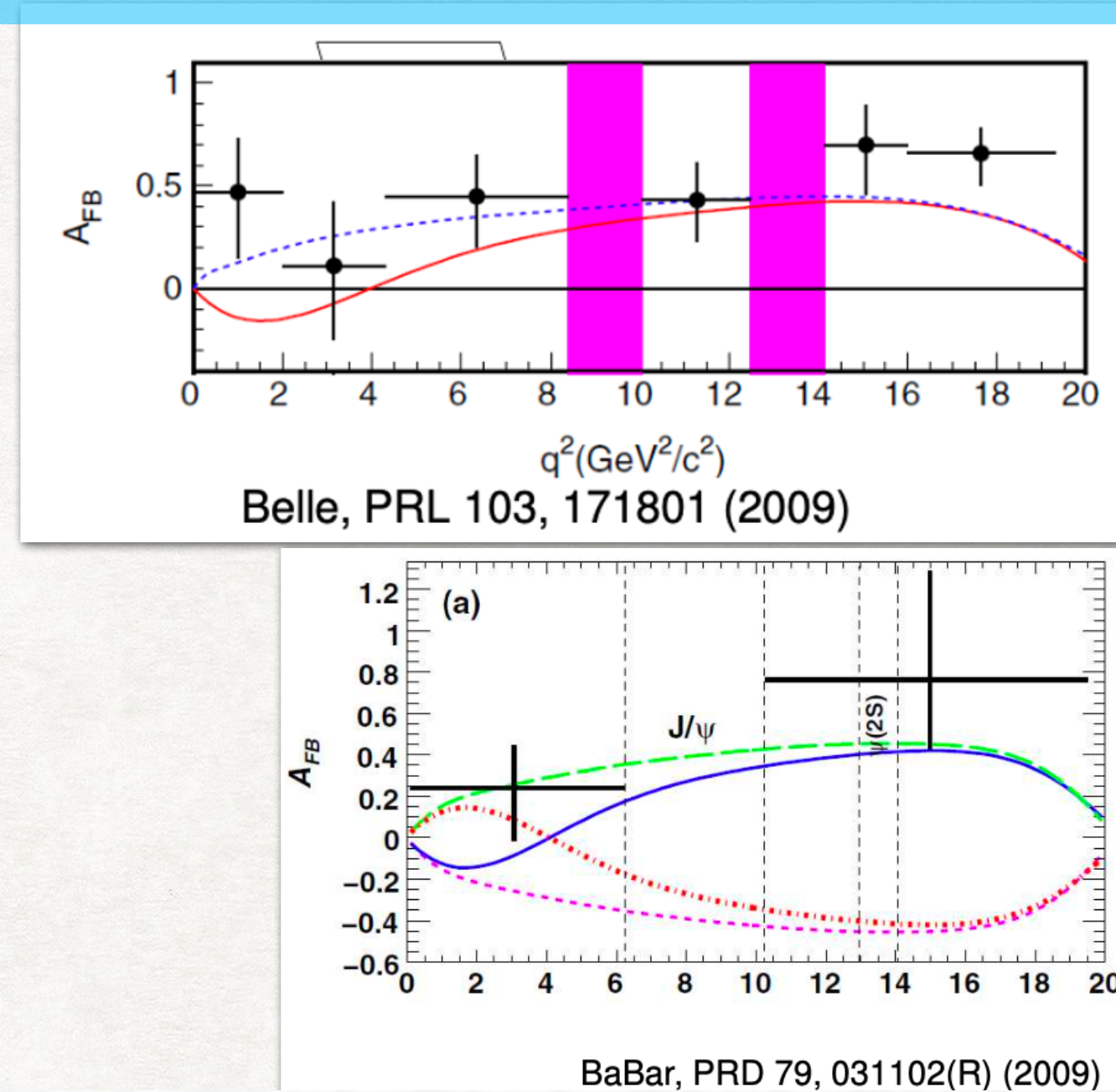
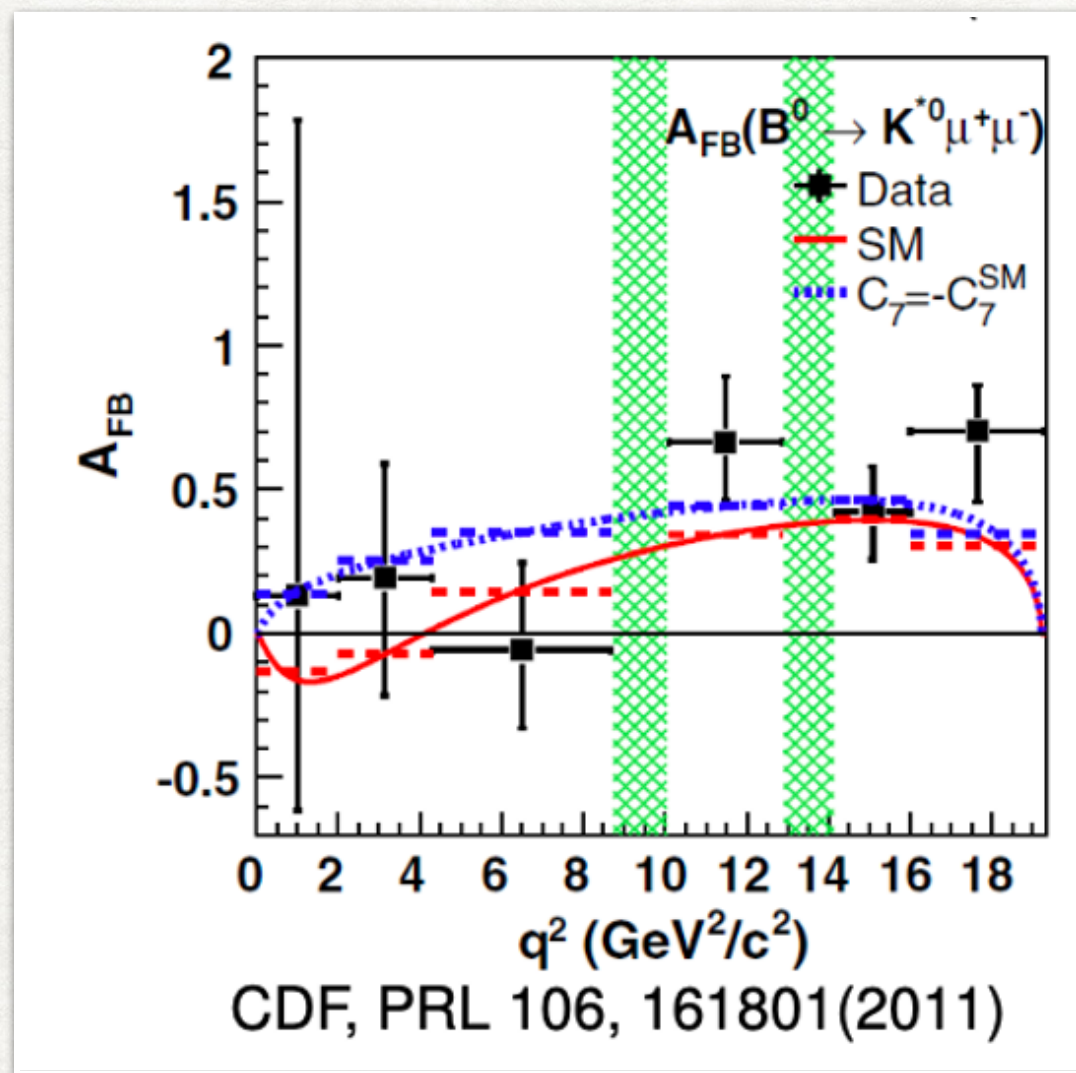
DOI: 10.1103/PhysRevD.63.114021

PACS number(s): 13.20.He, 13.25.Hw



W.-S. Hou, M. Kohda, FX, PRD84 (2011), 094027

# EARLY PURSUIT OF NEW PHYSICS: LARGE BR & NON-ZERO AFB



# THE EMERGENCE OF LFU PROBLEM

PRL 113, 151601 (2014) week ending  
10 OCTOBER 2014

Selected for a **Viewpoint** in *Physics*  
PHYSICAL REVIEW LETTERS



## Test of Lepton Universality Using $B^+ \rightarrow K^+ \ell^+ \ell^-$ Decays

R. Aaij *et al.*\*

(LHCb Collaboration)

(Received 25 June 2014; published 6 October 2014)

A measurement of the ratio of the branching fractions of the  $B^+ \rightarrow K^+ \mu^+ \mu^-$  and  $B^+ \rightarrow K^+ e^+ e^-$  decays is presented using proton-proton collision data, corresponding to an integrated luminosity of  $3.0 \text{ fb}^{-1}$ , recorded with the LHCb experiment at center-of-mass energies of 7 and 8 TeV. The value of the ratio of branching fractions for the dilepton invariant mass squared range  $1 < q^2 < 6 \text{ GeV}^2/c^4$  is measured to be  $0.745^{+0.090}_{-0.074}(\text{stat}) \pm 0.036(\text{syst})$ . This value is the most precise measurement of the ratio of branching fractions to date and is compatible with the standard model prediction within 2.6 standard deviations.

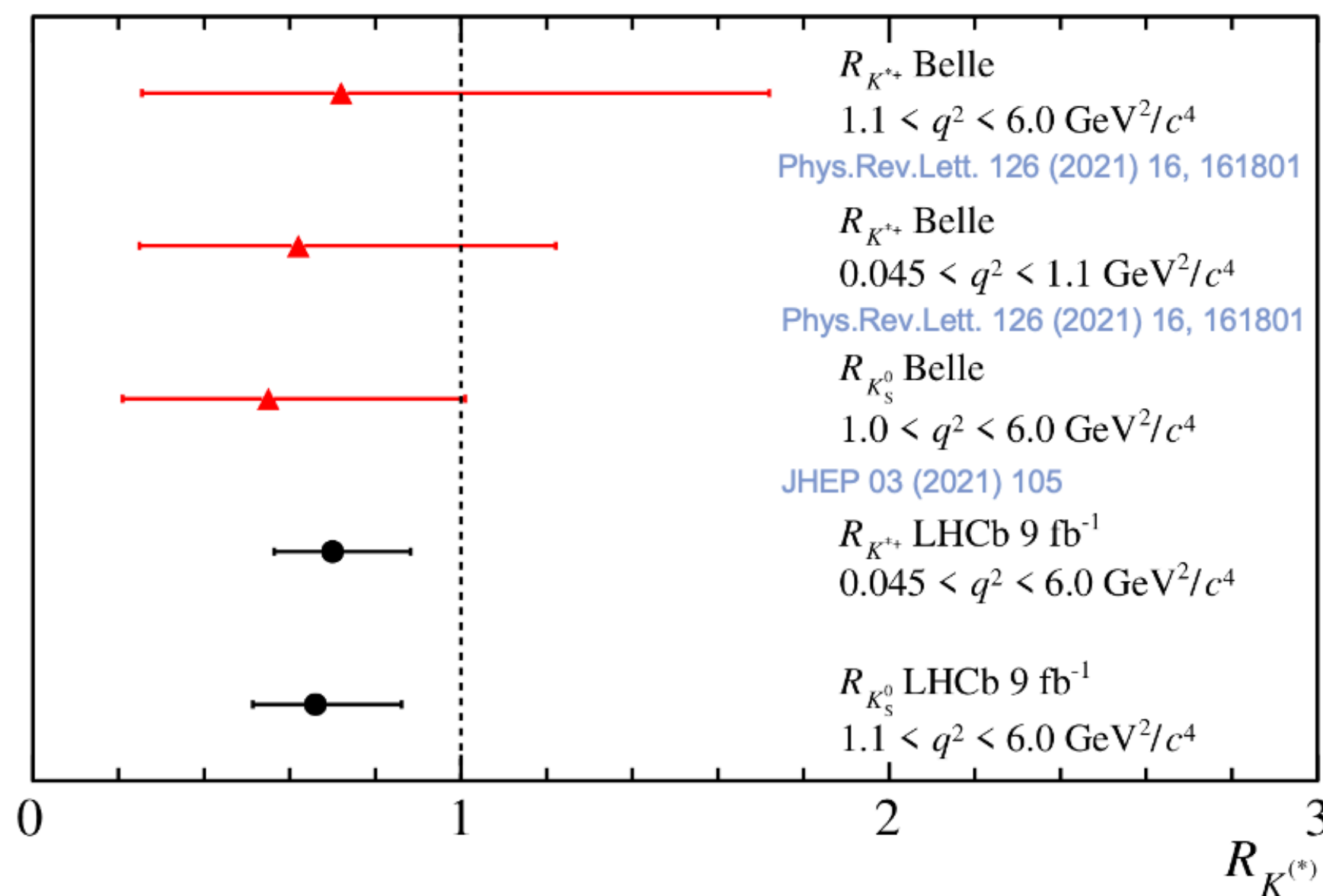
DOI: 10.1103/PhysRevLett.113.151601

PACS numbers: 11.30.Hv

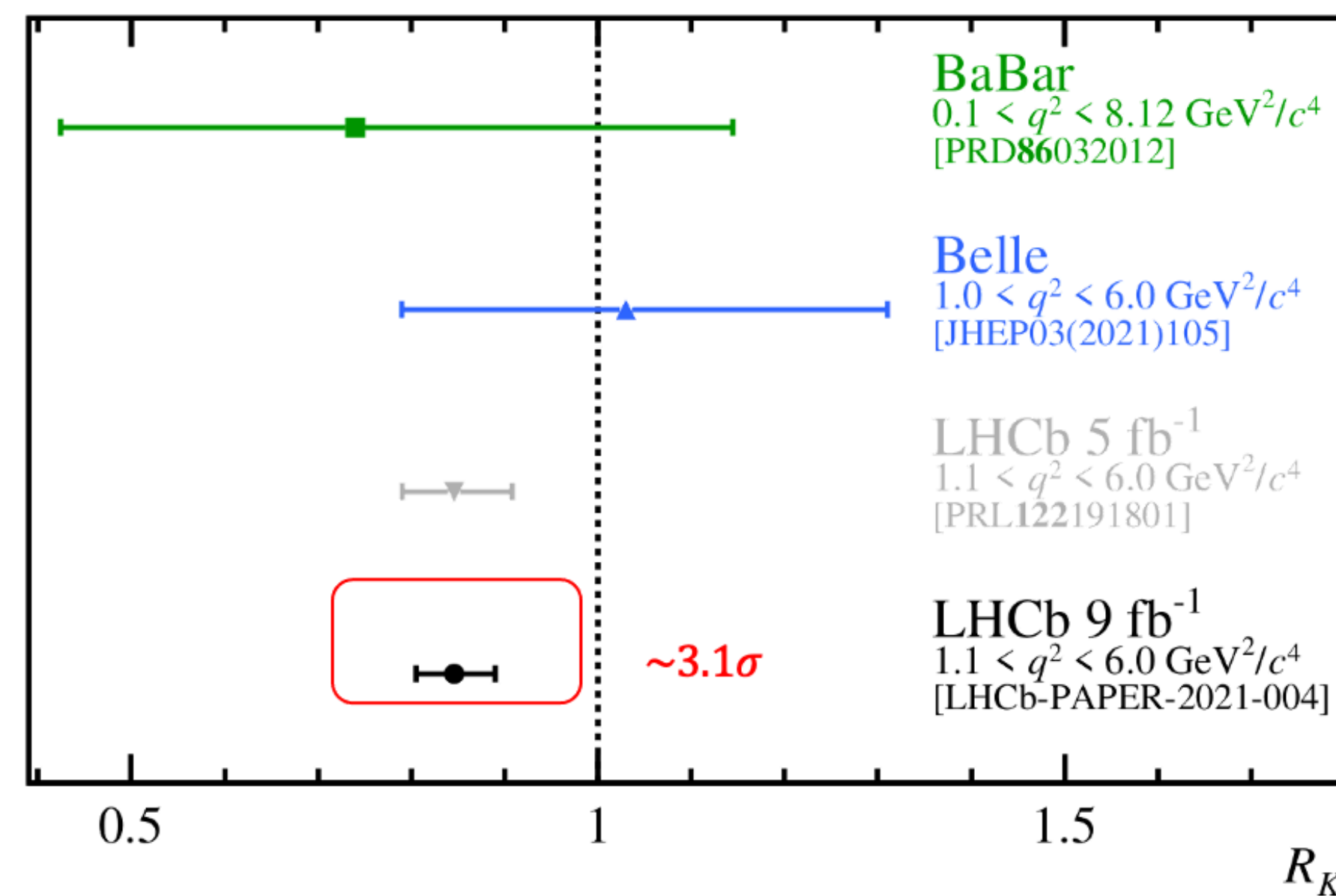
$$R_K = \frac{BR(B \rightarrow K \mu^+ \mu^-)}{BR(B \rightarrow K e^+ e^-)}$$

G. Hiller, F. Kruger  
hep-ph/0310219

$$R_{K^*} = \frac{BR(B \rightarrow K^* \mu^+ \mu^-)}{BR(B \rightarrow K^* e^+ e^-)}$$



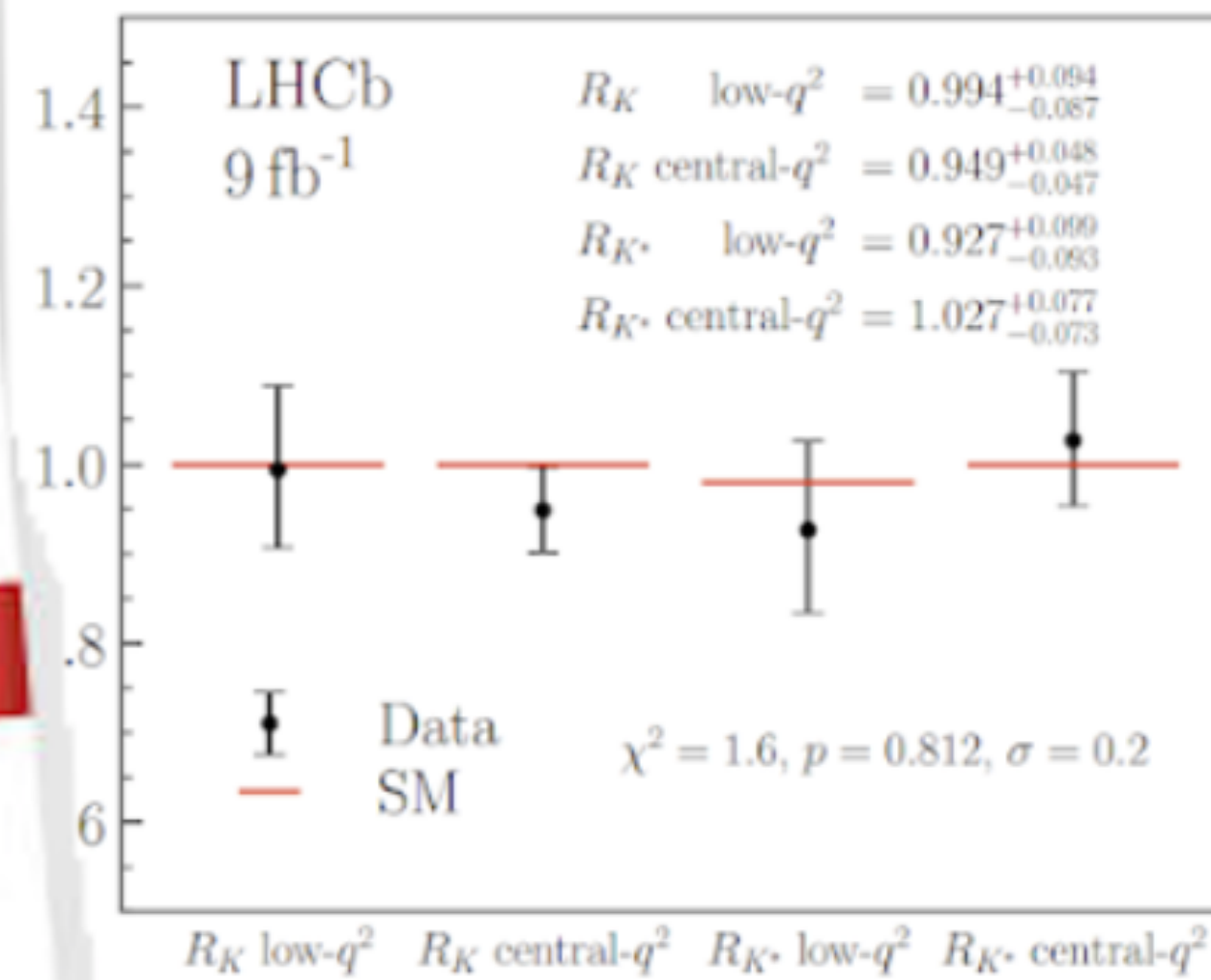
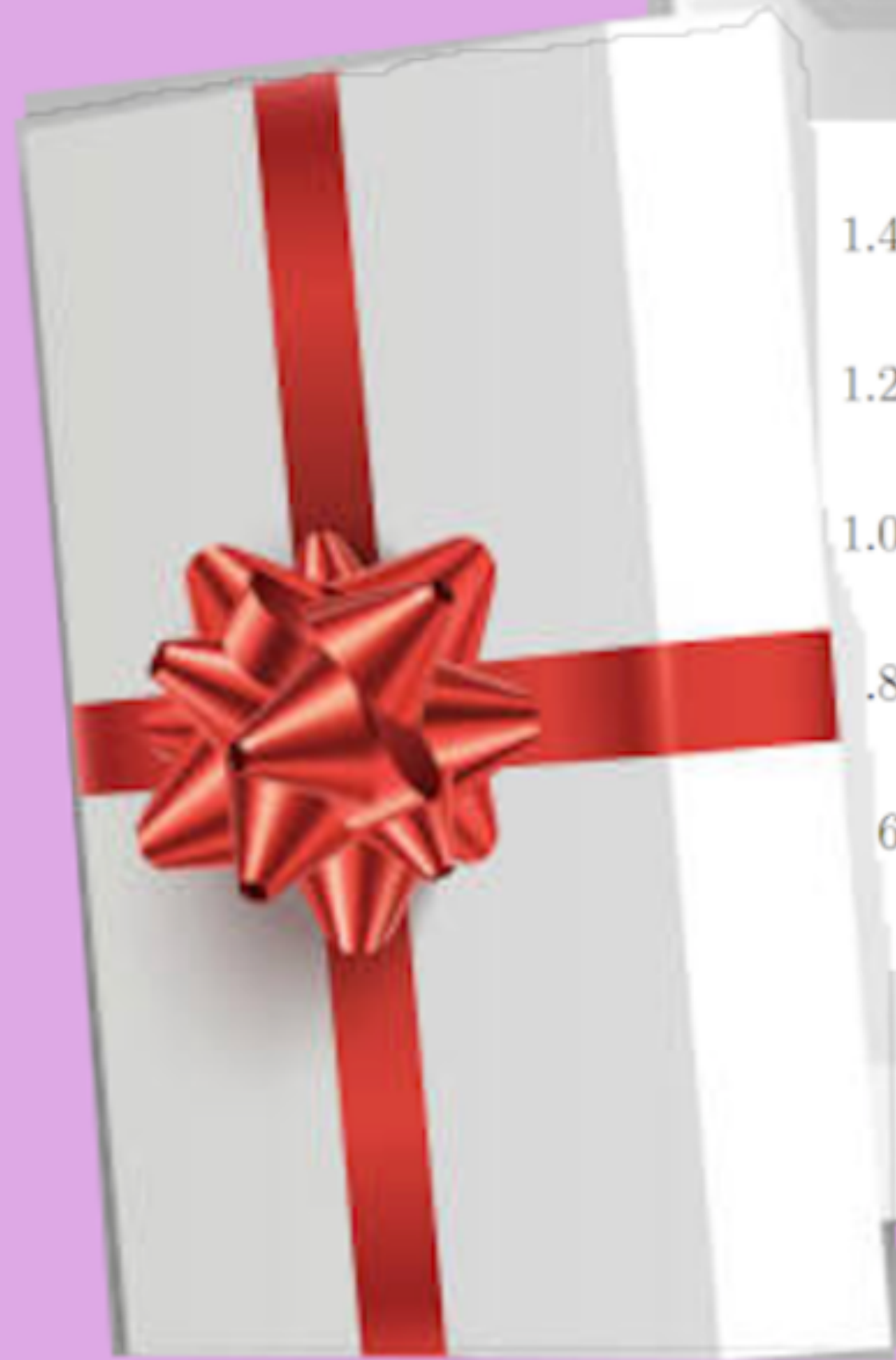
LHCb, Phys.Rev.Lett. 128 (2022) 19, 191802



LHCb, Nature Physics 18, (2022) 277-282

# LEPTON NON-UNIVERSALITY

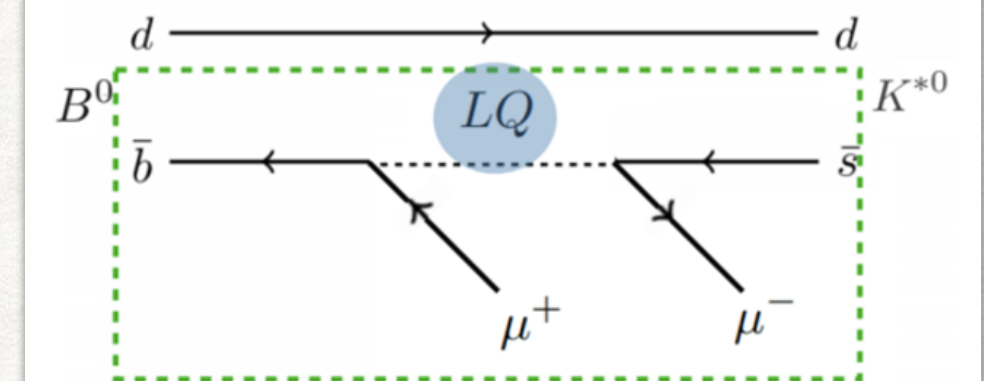
## LHCb's Xmas Letdown



low- $q^2$  region:  $0.1 < q^2 < 1.1 \text{ GeV}^2/c^4$   
 central- $q^2$  region:  $1.1 < q^2 < 6.0 \text{ GeV}^2/c^4$

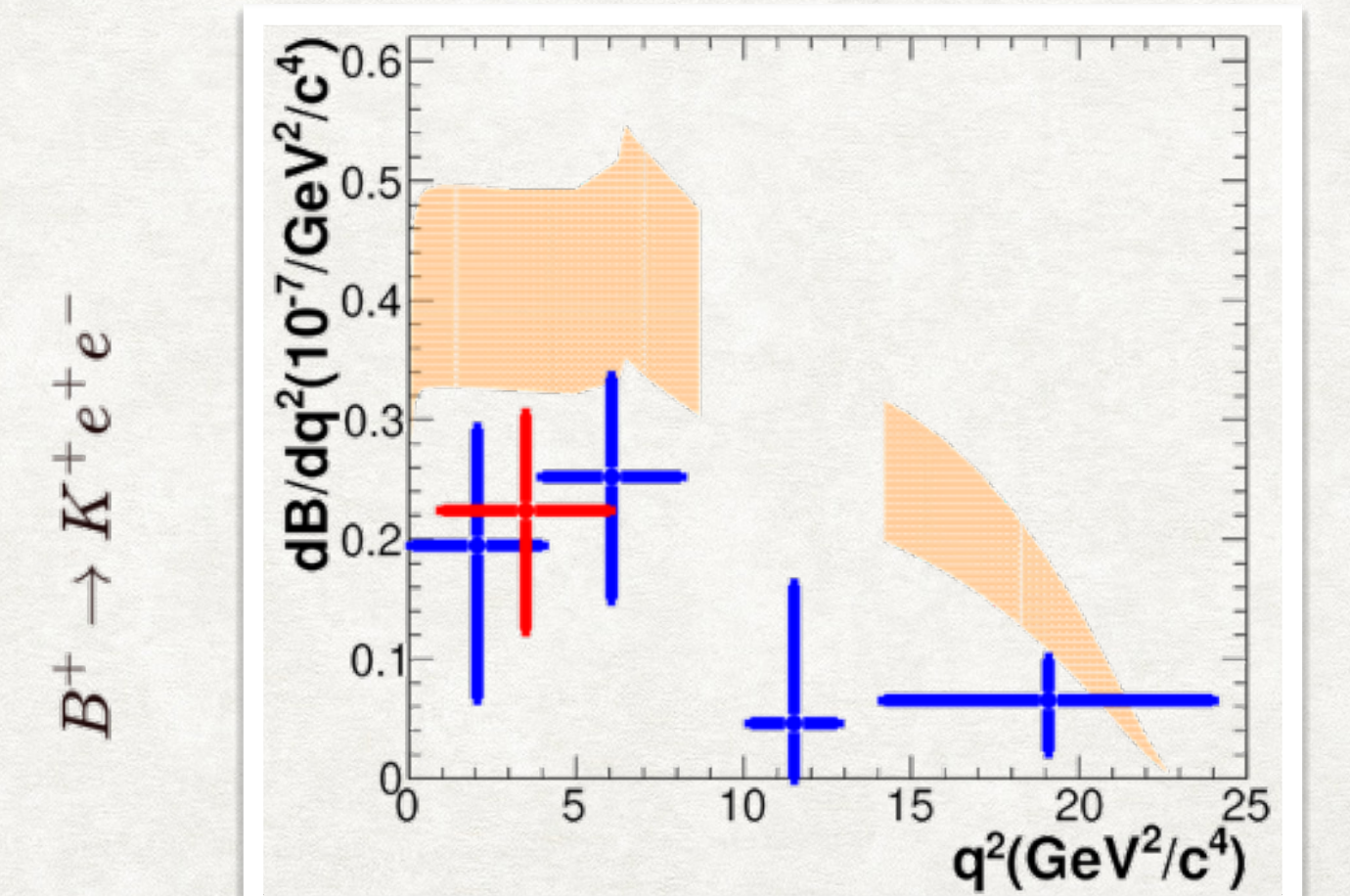
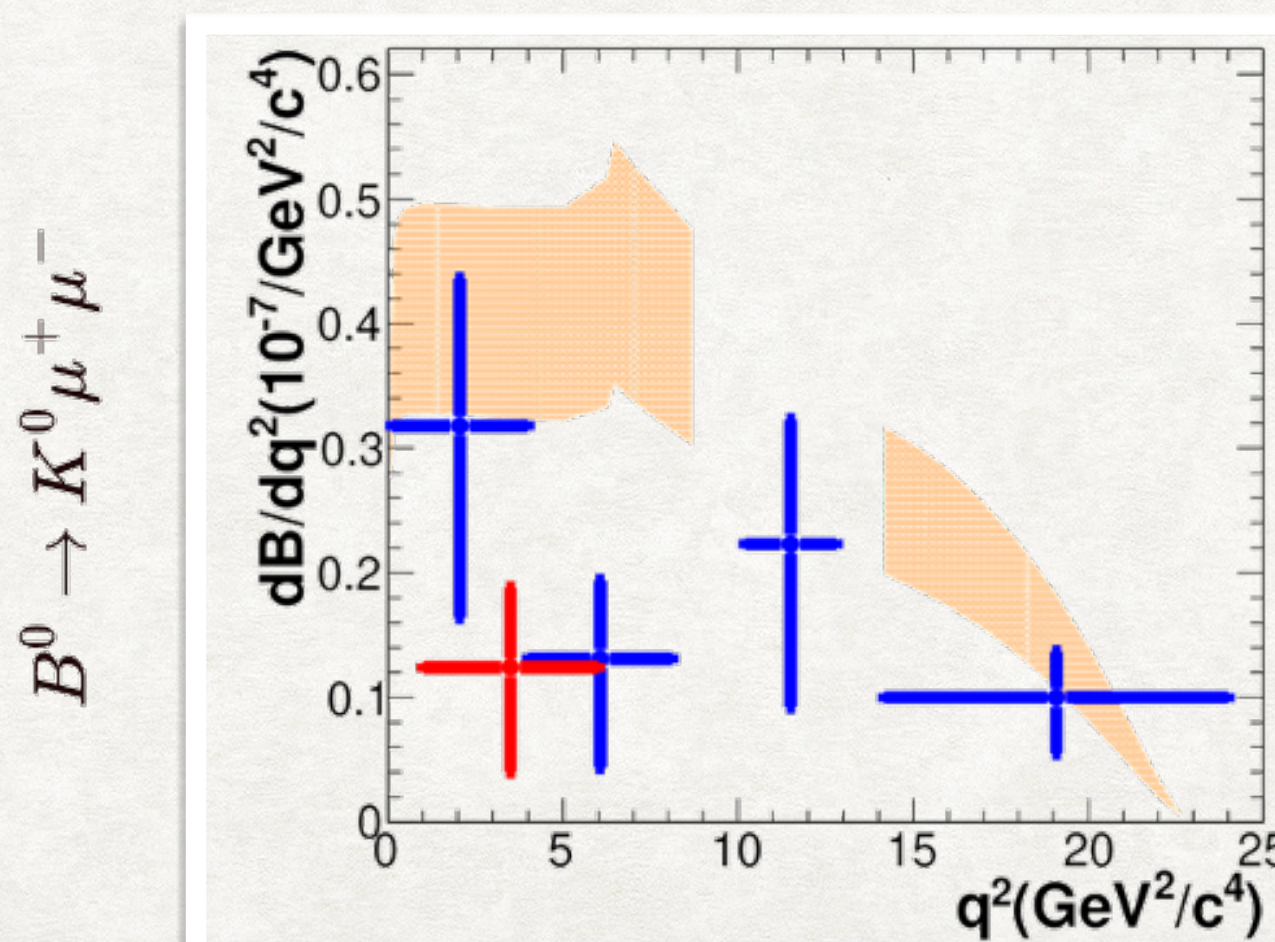
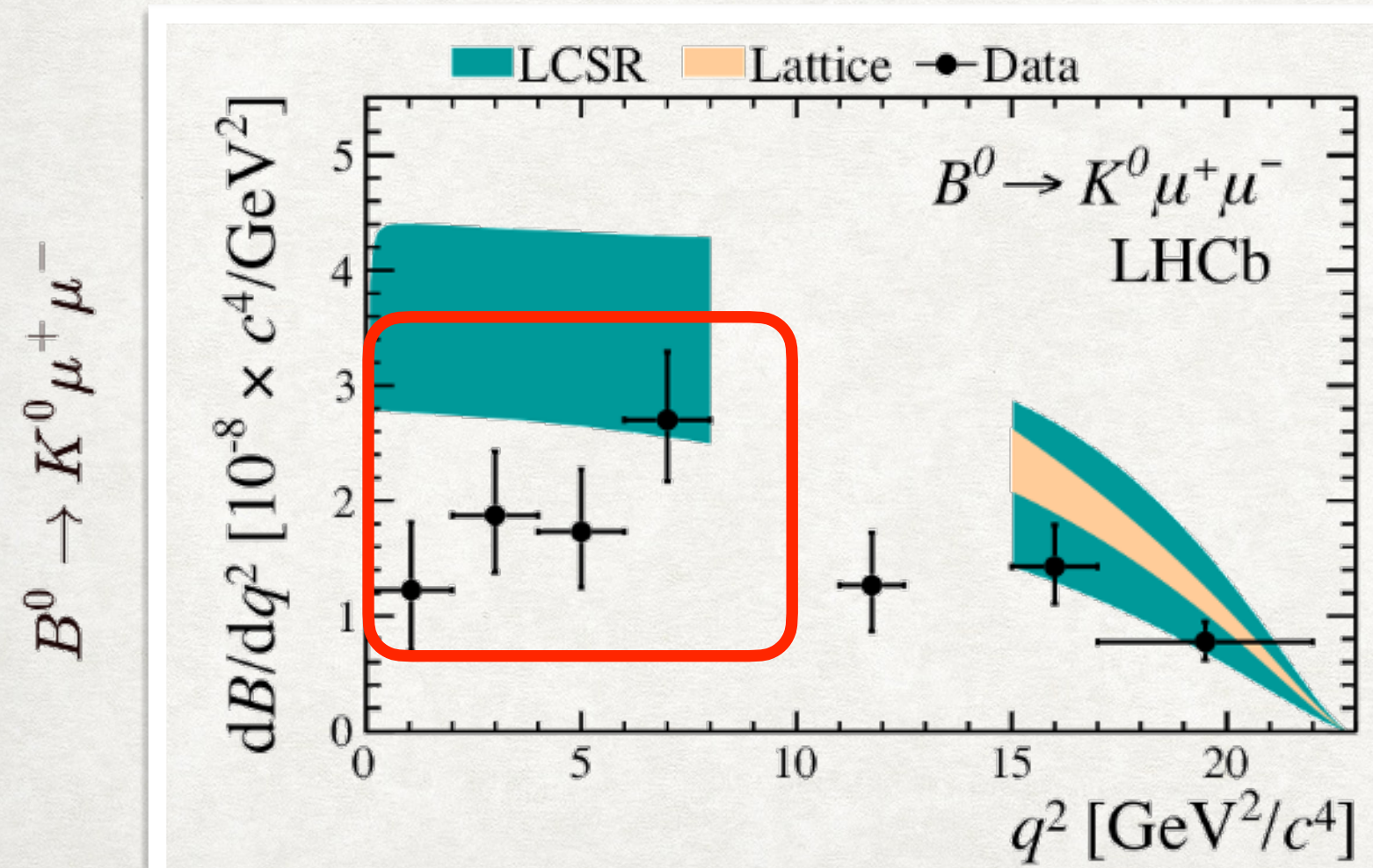
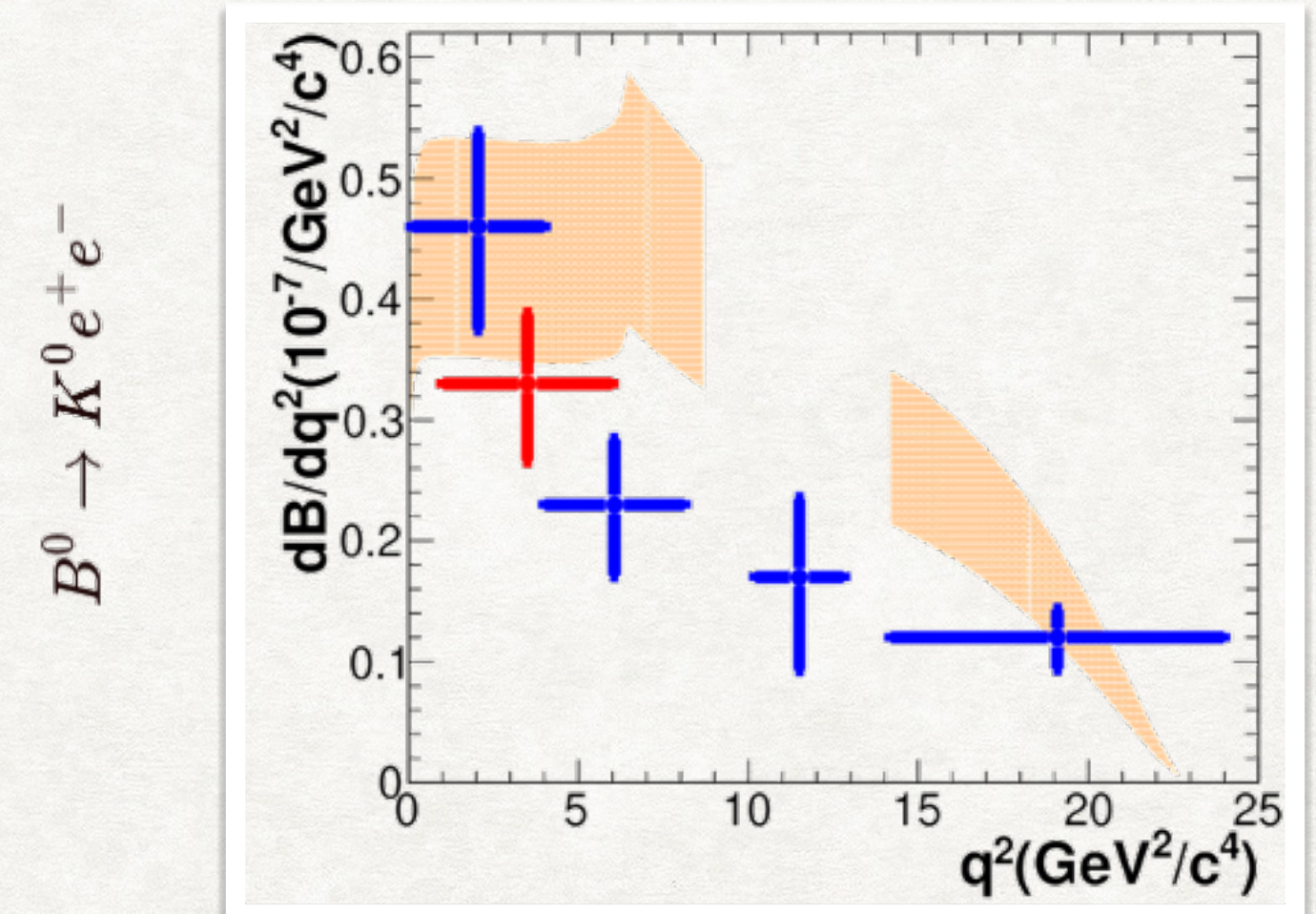
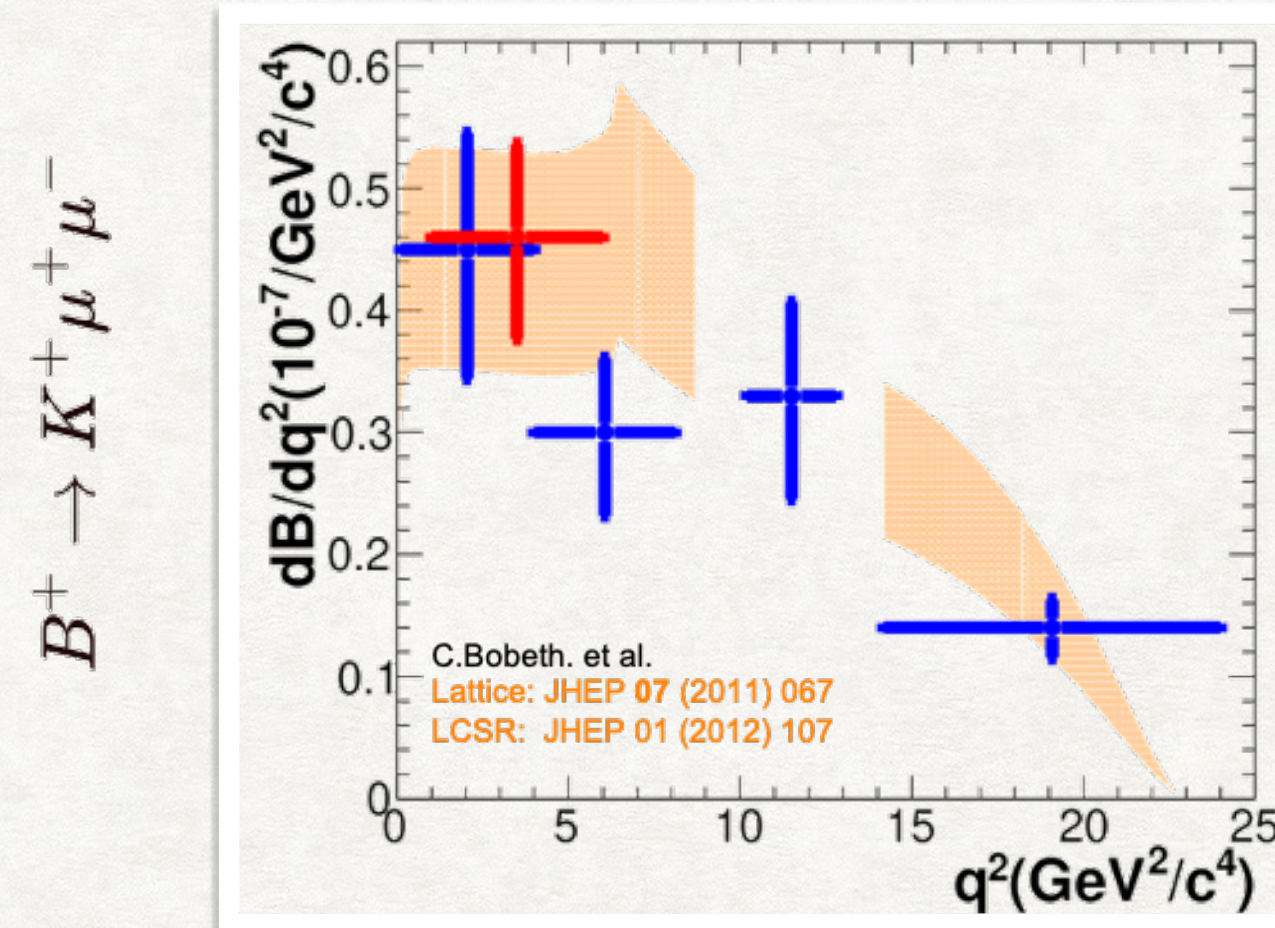
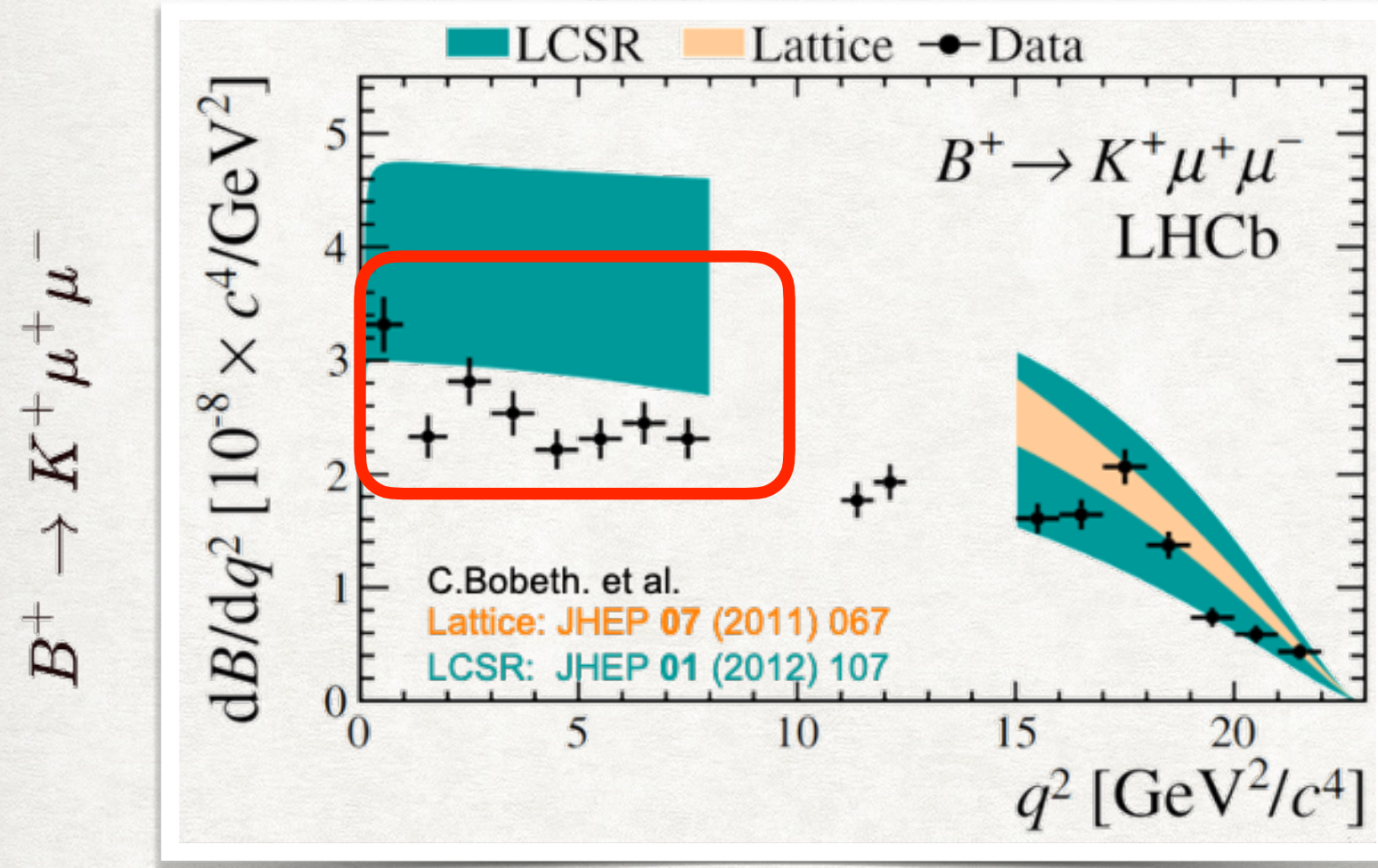
**LHCb , arXiv: 2212.09153V1**

New physics scenario

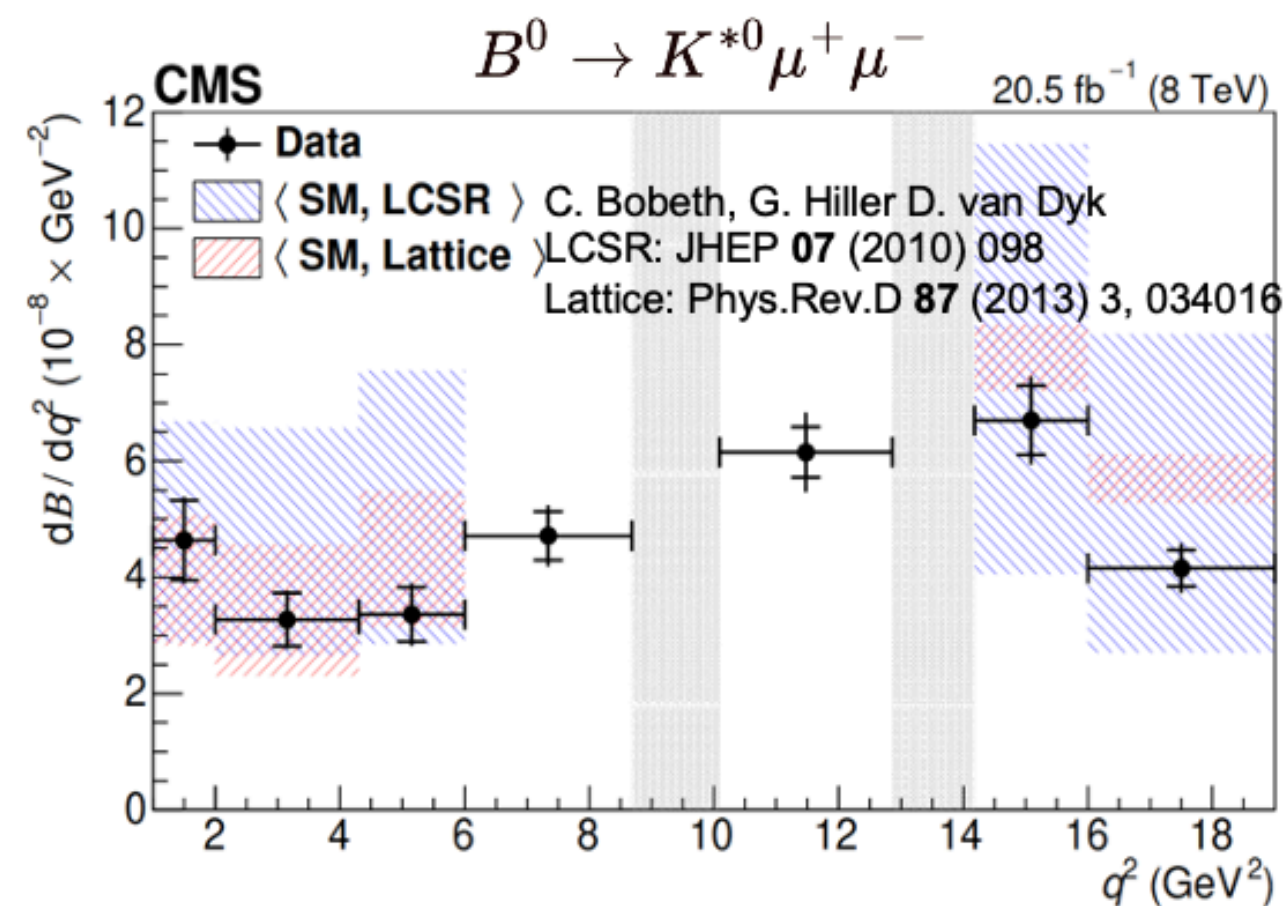
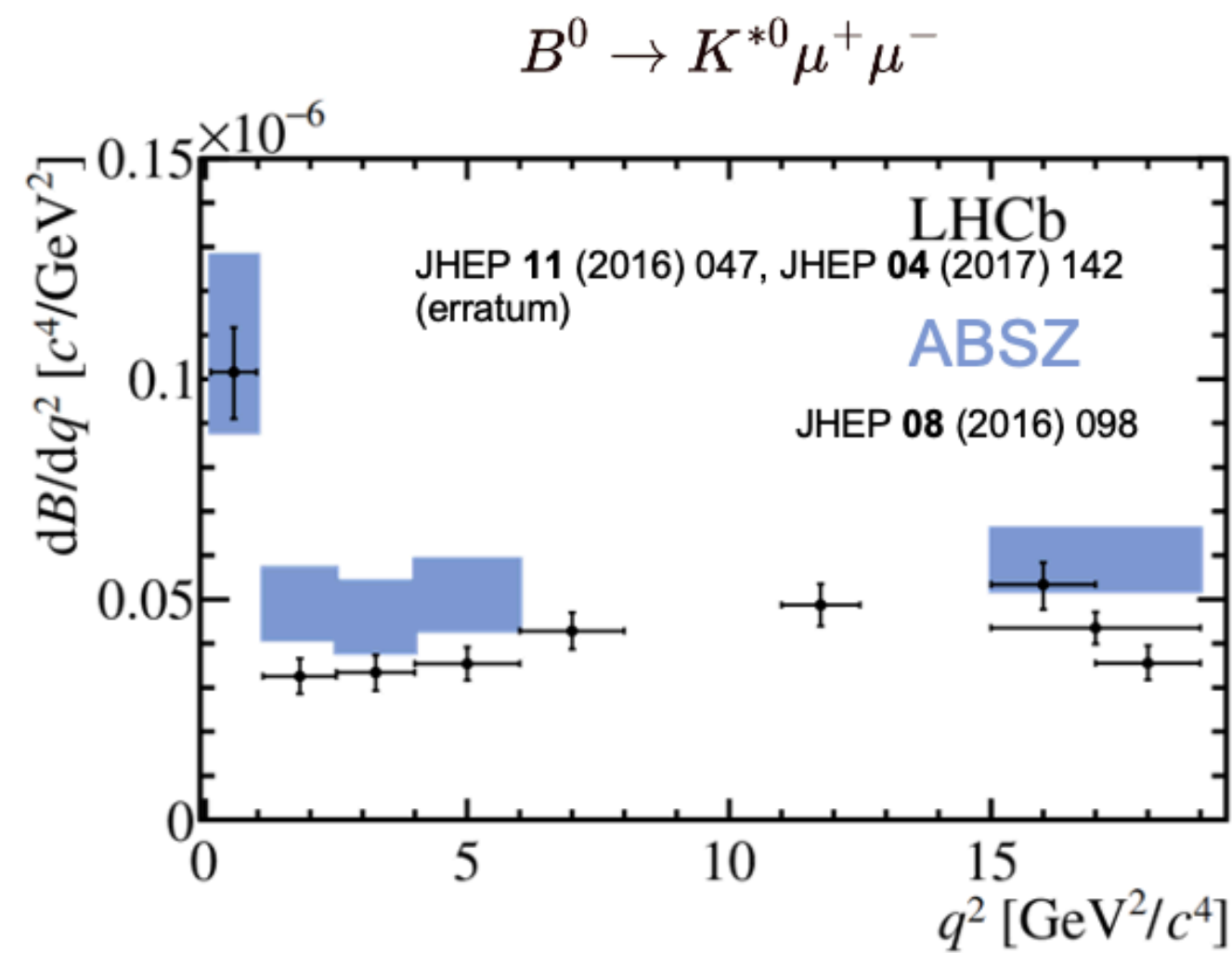




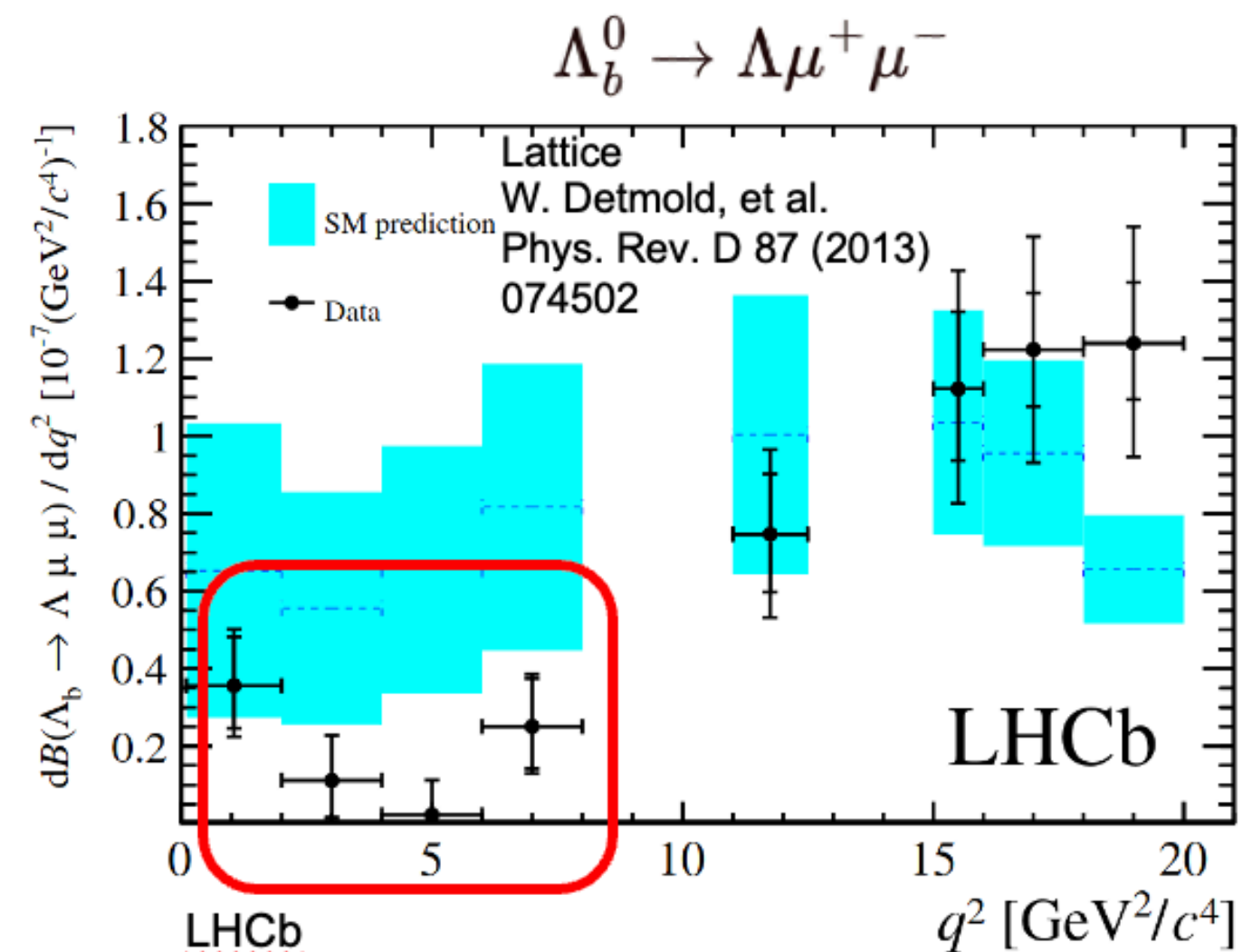
# BRANCHING FRACTION



# BRANCHING FRACTION

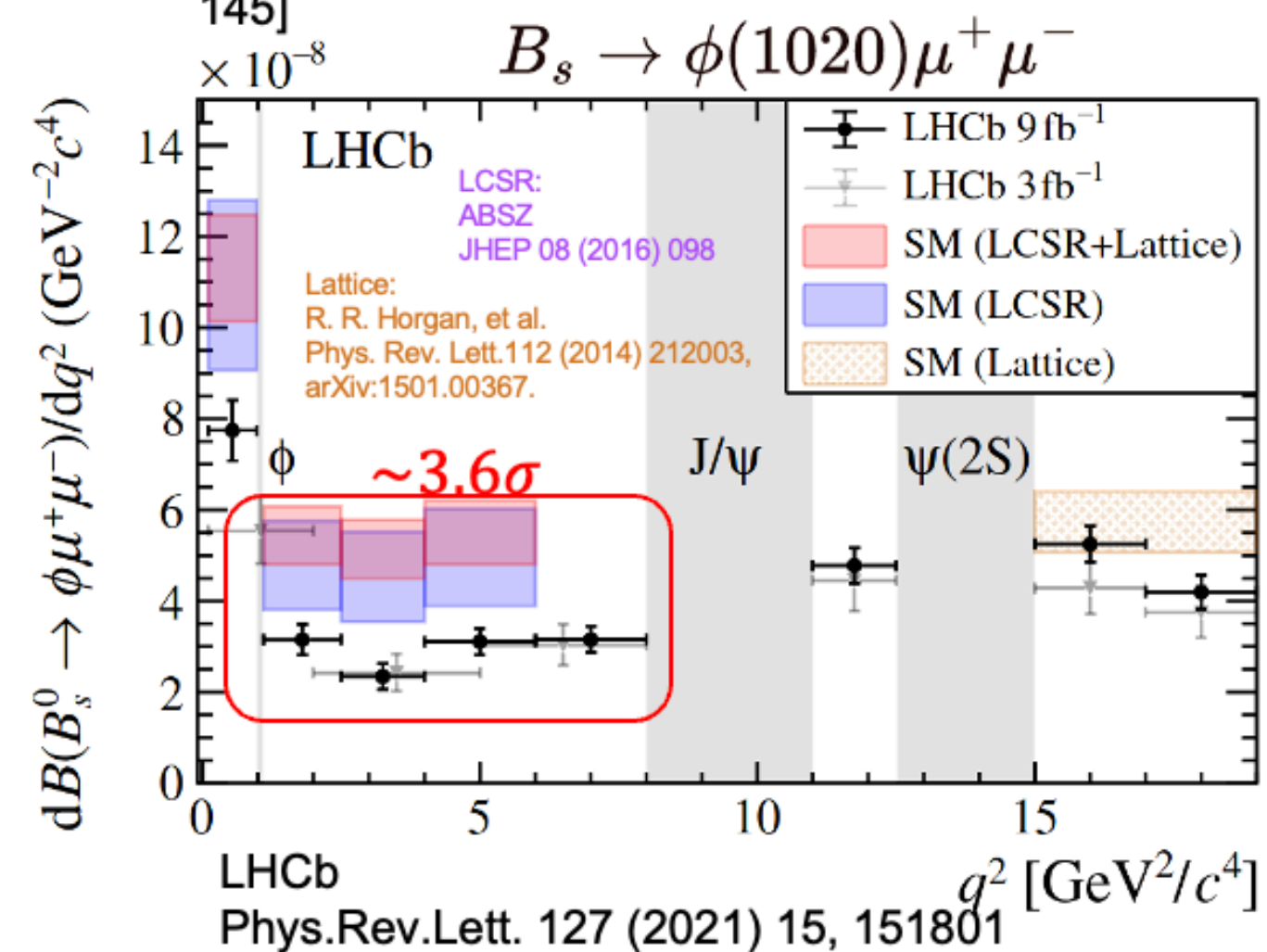


CMS  
Phys.Lett.B 753 (2016) 424-448



LHCb  
JHEP 06 (2015), 115 [erratum: JHEP 09 (2018), 145]

Angular analysis refers to:  
LHCb, JHEP 09 (2018), 146



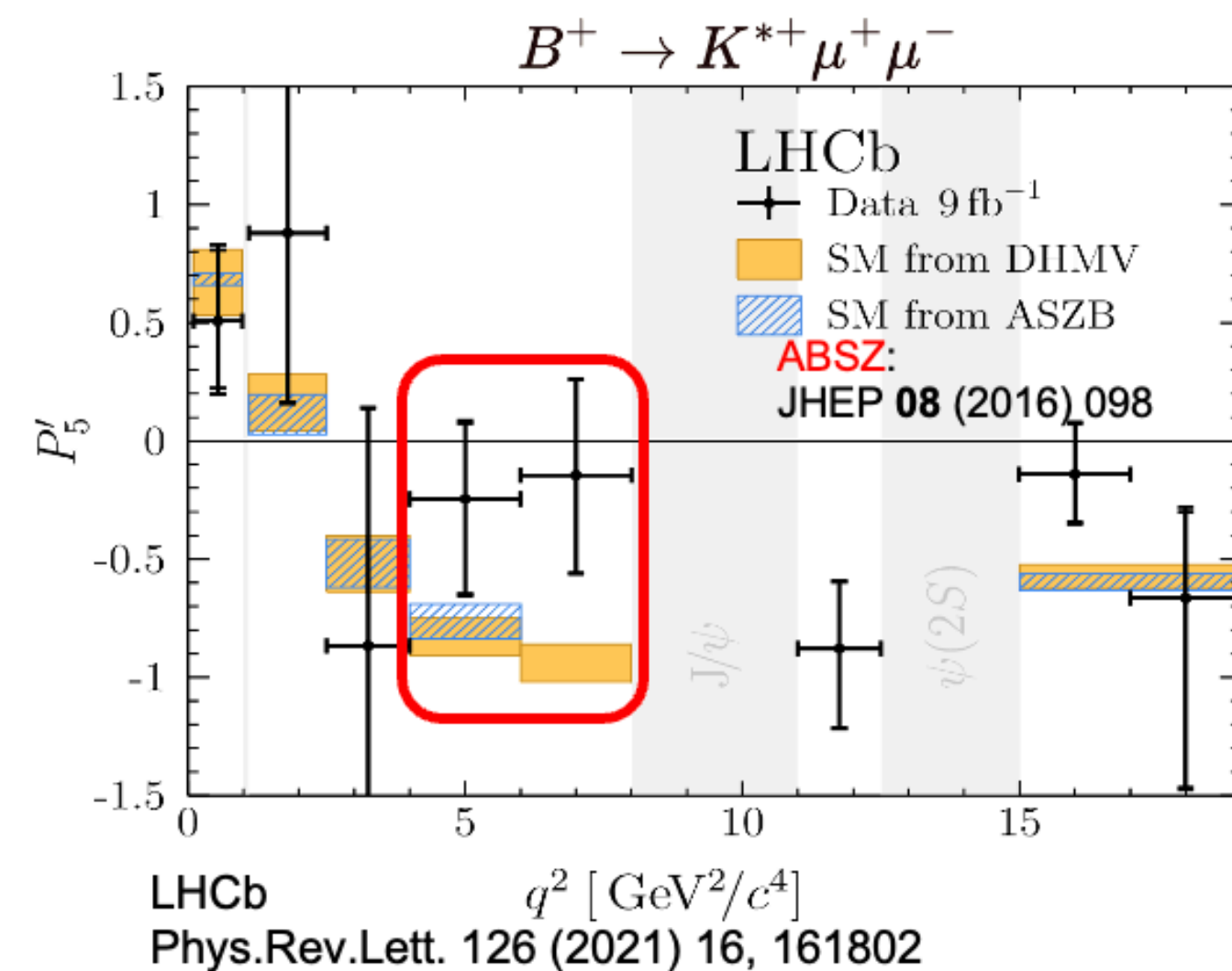
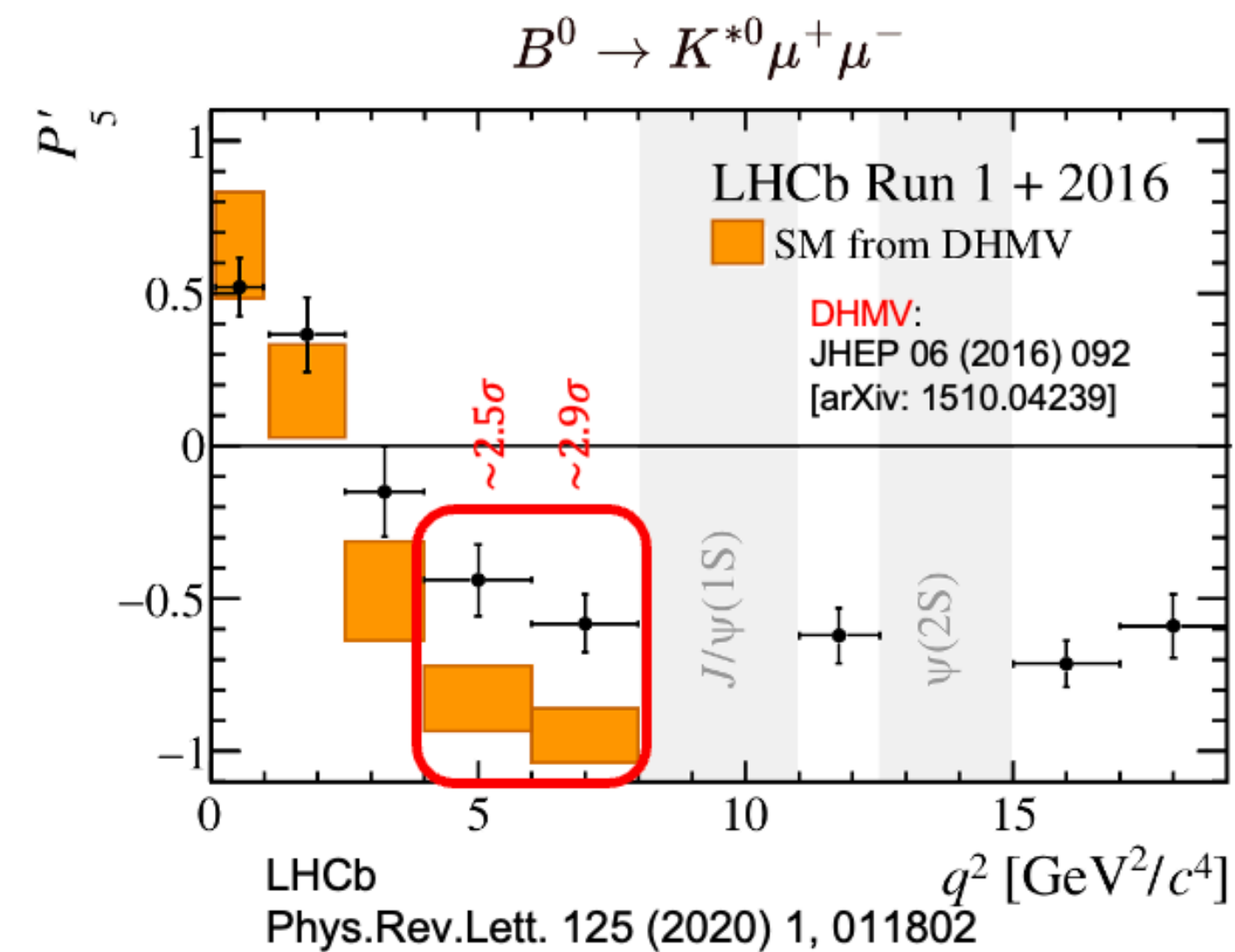
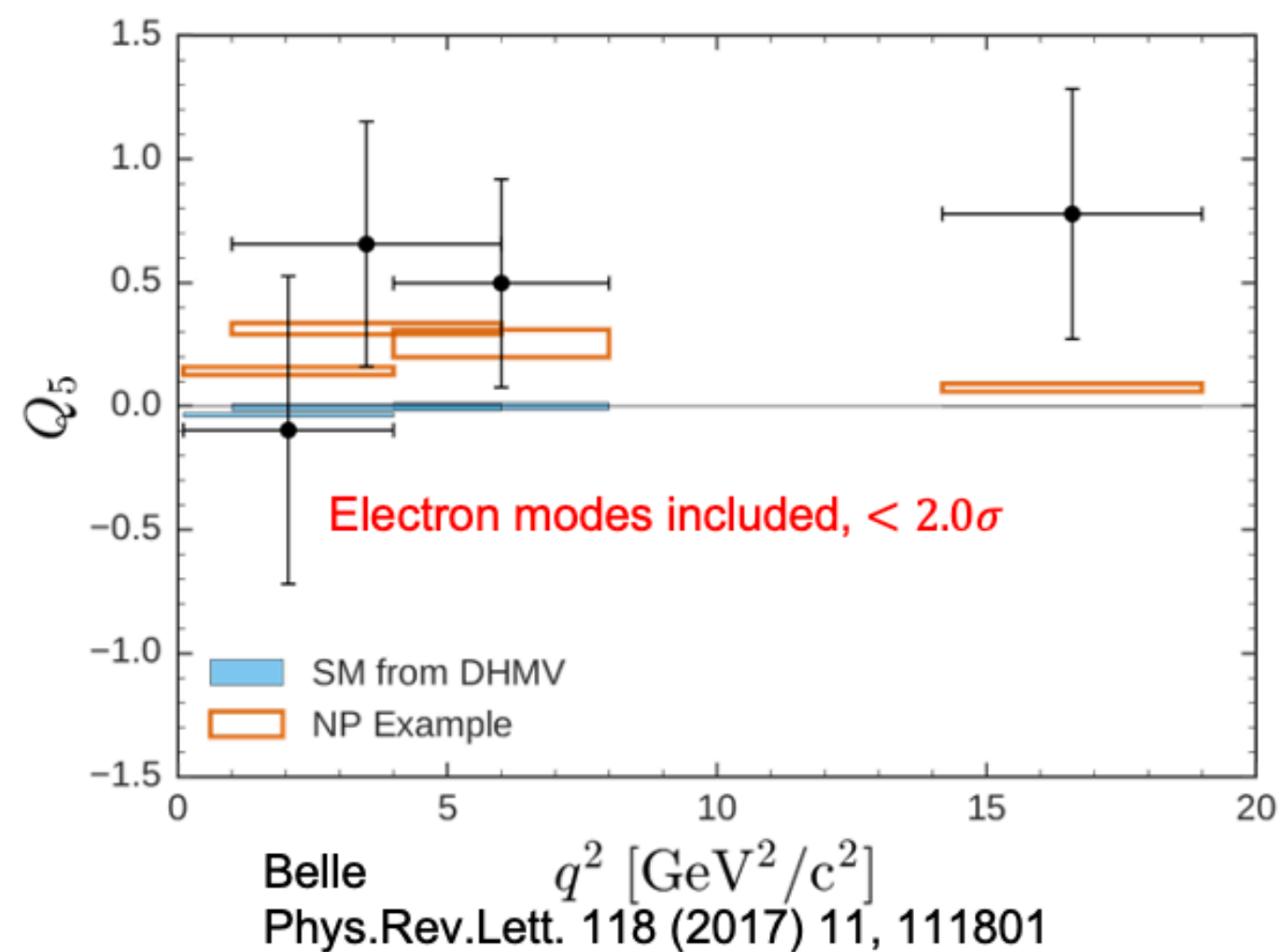
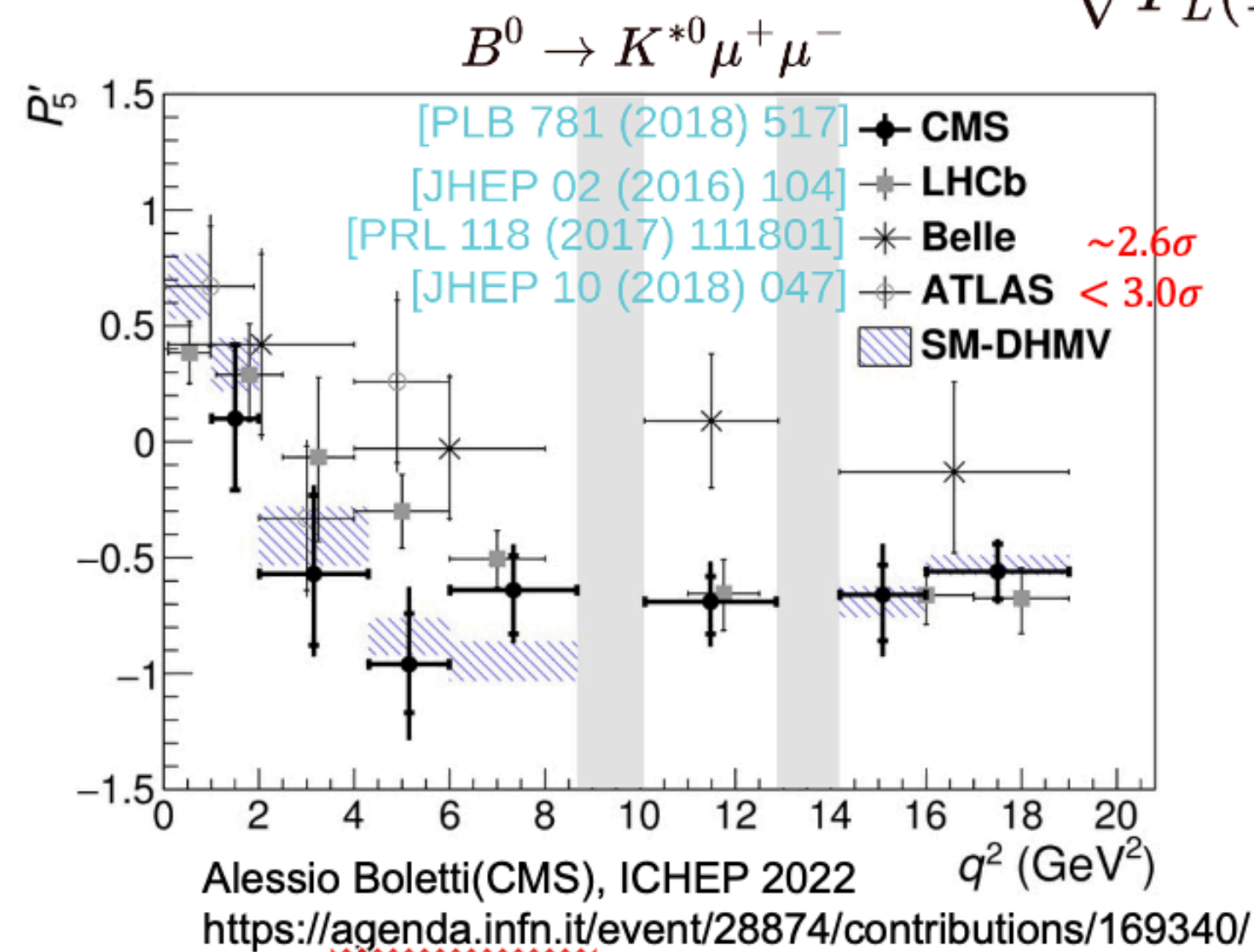
LHCb  
Phys.Rev.Lett. 127 (2021) 15, 151801

Angular analysis could be found in:  
LHCb, JHEP 11 (2021) 043  
arXiv: 2107.13428

# ANGULAR DISTRIBUTION

$$P'_5 = \frac{S_5}{\sqrt{F_L(1-F_L)}}$$

$$Q_5 = P_i^{\mu} - P_i^{e}$$



# THEORETICAL SKELETON OF FCNC PROCESS $b \rightarrow s$

effective Hamiltonian:

$$\mathcal{H} = -\frac{4G_F}{\sqrt{2}} V_{tb} V_{ts}^* \frac{e^2}{16\pi^2} \sum_i (C_i \mathcal{O}_i + C'_i \mathcal{O}'_i) + h.c.$$

high energy information

$$C_i^{(\prime)\ell} = C_i^{(\prime)\ell;SM} + \Delta C_i^{(\prime)\ell;NP} = C_i^{(\prime)\ell;SM} + \Delta C_i^{(\prime)\ell}$$

QCDF

decay amplitude:

$$\begin{aligned} \mathcal{M}(\bar{B} \rightarrow P \ell^+ \ell^-) \\ = \frac{G_F \alpha}{2\sqrt{2}\pi} c_P^{-1} \xi_P \left[ (\lambda_t C_{9,P}^{(t)} + \lambda_u C_{9,P}^{(u)}) (p^\mu + p'^\mu) (\bar{\ell} \gamma_\mu \ell) + \lambda_t C_{10} (p^\mu + p'^\mu) (\bar{\ell} \gamma_\mu \gamma_5 \ell) \right] \end{aligned}$$

observables:

$$\begin{aligned} \frac{dB}{dq^2}(\bar{B} \rightarrow P \ell^+ \ell^-) \\ = S_{PTB} \frac{G_F^2 M_B^3}{96\pi^3} \left( \frac{\alpha}{4\pi} \right)^2 \lambda(q^2, m_P^2)^3 \xi_P(q^2)^2 \left( \left| \lambda_t C_{9,P}^{(t)}(q^2) + \lambda_u C_{9,P}^{(u)}(q^2) \right|^2 + |\lambda_t|^2 C_{10}^2 \right) \end{aligned}$$

SM

$$\mathcal{O}_7 = \frac{m_b}{e} (\bar{s} \sigma_{\mu\nu} P_R b) F^{\mu\nu},$$

$$\mathcal{O}'_7 = \frac{m_b}{e} (\bar{s} \sigma_{\mu\nu} P_L b) F^{\mu\nu},$$

$$\mathcal{O}_8 = \frac{g_s m_b}{e^2} (\bar{s} \sigma_{\mu\nu} T^a P_R b) G_a^{\mu\nu},$$

$$\mathcal{O}'_8 = \frac{g_s m_b}{e^2} (\bar{s} \sigma_{\mu\nu} T^a P_L b) G_a^{\mu\nu},$$

$$\mathcal{O}_9 = (\bar{s} \gamma_\mu P_L b) (\bar{\ell} \gamma^\mu \ell),$$

$$\mathcal{O}'_9 = (\bar{s} \gamma_\mu P_R b) (\bar{\ell} \gamma^\mu \ell),$$

$$\mathcal{O}_{10} = (\bar{s} \gamma_\mu P_L b) (\bar{\ell} \gamma^\mu \gamma_5 \ell),$$

$$\mathcal{O}'_{10} = (\bar{s} \gamma_\mu P_R b) (\bar{\ell} \gamma^\mu \gamma_5 \ell),$$

$$\mathcal{O}_S = m_b (\bar{s} P_R b) (\bar{\ell} \ell),$$

$$\mathcal{O}'_S = m_b (\bar{s} P_L b) (\bar{\ell} \ell),$$

$$\mathcal{O}_P = m_b (\bar{s} P_R b) (\bar{\ell} \gamma_5 \ell),$$

$$\mathcal{O}'_P = m_b (\bar{s} P_L b) (\bar{\ell} \gamma_5 \ell).$$

$$C_{9,P}^{(t)}(q^2) = C_9 + \frac{2m_b}{M_B} \frac{\mathcal{T}_P^{(t)}(q^2)}{\xi_P(q^2)}$$

$$C_{9,P}^{(u)}(q^2) = \frac{2m_b}{M_B} \frac{\mathcal{T}_P^{(u)}(q^2)}{\xi_P(q^2)}$$

$$\mathcal{T}_P^{(i)} = \xi_P C_P^{(i)} + \frac{\pi^2 f_B f_P}{N_c M_B} \sum_{\pm} \int_0^\infty \frac{d\omega}{\omega} \Phi_{B,\pm}(\omega) \int_0^1 du \phi_P(u) T_{P,\pm}^{(i)}(u, \omega)$$

# PHYSICS FROM EW SCALE

- High energy information: Wilson coefficients in SM

- EW scale

- $C_{9,10}$ : NNLL;

- $C_{1-6}, C_{7,8}$ : NLL

- 2-loop matching: [C. Bobeth, M. Misiak, J. Urban, NPB 574, 291 \(2000\)](#)

- RGE running

- 3-loop anomalous dimension matrix:

[K.G. Chetyrkin, M. Misiak, M. Munz, PLB 400, 206 \(1997\); 425, 414\(E\) \(1998\);](#)

[P. Gambino, M. Gorbahn, U. Haisch, NPB673, 238 \(2003\);](#)

[M. Gorbahn, U. Haisch, NPB713, 291 \(2005\);](#)

TABLE III. The SM Wilson coefficients at the scale  $\mu = 4.6$  GeV in leading logarithmic (LL), next-to-leading logarithmic (NLL) and next-to-next-to-leading logarithmic order (NNLL). Input parameters listed in Table II are used.

	$C_1$	$C_2$	$C_3$	$C_4$	$C_5$	$C_6$	$C_7^{\text{eff}}$	$C_8^{\text{eff}}$	$C_9$	$C_{10}$
LL	-0.5093	1.0256	-0.0050	-0.0686	0.0005	0.0010	-0.3189	-0.1505	2.0111	0
NLL	-0.3001	1.0080	-0.0047	-0.0827	0.0003	0.0009	-0.2969	-0.1642	4.1869	-4.3973
NNLL	-	-	-	-	-	-	-	-	4.2607	-4.2453

# THE ENCODED NEW PHYSICS

- New physics effect
- Deviations from SM Wilson coefficients

$$C_i^{(\prime)\ell} = C_i^{(\prime)\ell;\text{SM}} + \Delta C_i^{(\prime)\ell;\text{NP}} = C_i^{(\prime)\ell;\text{SM}} + \boxed{\Delta C_i^{(\prime)\ell}}$$

- BSM operators

$\mathcal{O}_7 = \frac{m_b}{e} (\bar{s} \sigma_{\mu\nu} P_R b) F^{\mu\nu},$	$\mathcal{O}'_7 = \frac{m_b}{e} (\bar{s} \sigma_{\mu\nu} P_L b) F^{\mu\nu},$
$\mathcal{O}_8 = \frac{g_s m_b}{e^2} (\bar{s} \sigma_{\mu\nu} T^a P_R b) G_a^{\mu\nu},$	$\mathcal{O}'_8 = \frac{g_s m_b}{e^2} (\bar{s} \sigma_{\mu\nu} T^a P_L b) G_a^{\mu\nu},$
$\mathcal{O}_9 = (\bar{s} \gamma_\mu P_L b) (\bar{\ell} \gamma^\mu \ell),$	$\mathcal{O}'_9 = (\bar{s} \gamma_\mu P_R b) (\bar{\ell} \gamma^\mu \ell),$
$\mathcal{O}_{10} = (\bar{s} \gamma_\mu P_L b) (\bar{\ell} \gamma^\mu \gamma_5 \ell),$	$\mathcal{O}'_{10} = (\bar{s} \gamma_\mu P_R b) (\bar{\ell} \gamma^\mu \gamma_5 \ell),$
$\mathcal{O}_S = m_b (\bar{s} P_R b) (\bar{\ell} \ell),$	$\mathcal{O}'_S = m_b (\bar{s} P_L b) (\bar{\ell} \ell),$
$\mathcal{O}_P = m_b (\bar{s} P_R b) (\bar{\ell} \gamma_5 \ell),$	$\mathcal{O}'_P = m_b (\bar{s} P_L b) (\bar{\ell} \gamma_5 \ell).$

## Scenario I: muon-specific

$$\Delta C_{9,10,S,P}^{(\prime)e} = 0$$

## Scenario II: lepton-universal

$$\Delta C_{9,10,S,P}^{(\prime)\mu} = \Delta C_{9,10,S,P}^{(\prime)e}$$

## Scenario III: lepton-specific

all parameters are taken except C7,C8

## Scenario IV: full scenario

all parameters are taken

# THE $b \rightarrow s$ PROCESSES

- B meson leptonic decays
- B meson radiative decays
- B meson inclusive semi-leptonic decay
- B meson exclusive semi-leptonic decay: **QCDF approach**
  - $B \rightarrow P\ell^+\ell^-$
  - $B \rightarrow V\ell^+\ell^-$
- Bottomed baryon semi-leptonic decays: **naive factorization**

# KINEMATICS & OBSERVABLES

- Kinematics

$$\frac{d^4\Gamma}{dq^2 d\cos\theta_l d\cos\theta_{K^*} d\phi} = \frac{9}{32\pi} I(q^2, \theta_l, \theta_{K^*}, \phi)$$

- transversity amplitude

$$\begin{aligned} I(q^2, \theta_l, \theta_{K^*}, \phi) &= I_1^s \sin^2 \theta_{K^*} + I_1^c \cos^2 \theta_{K^*} + (I_2^s \sin^2 \theta_{K^*} + I_2^c \cos^2 \theta_{K^*}) \cos 2\theta_l \\ &+ I_3 \sin^2 \theta_{K^*} \sin^2 \theta_l \cos 2\phi + I_4 \sin 2\theta_{K^*} \sin 2\theta_l \cos \phi \\ &+ I_5 \sin 2\theta_{K^*} \sin \theta_l \cos \phi \\ &+ (I_6^s \sin^2 \theta_{K^*} + I_6^c \cos^2 \theta_{K^*}) \cos \theta_l + I_7 \sin 2\theta_{K^*} \sin \theta_l \sin \phi \\ &+ I_8 \sin 2\theta_{K^*} \sin 2\theta_l \sin \phi + I_9 \sin^2 \theta_{K^*} \sin^2 \theta_l \sin 2\phi. \end{aligned}$$

W. Altmannshofer, P. Ball, A. Bharucha, A.J. Buras, D. Straub, M. Wick, 0811.1214

$$\begin{aligned} I_1^s &= \frac{(2 + \beta_\mu^2)}{4} [|A_\perp^L|^2 + |A_\parallel^L|^2 + (L \rightarrow R)] + \frac{4m_\mu^2}{q^2} \text{Re}(A_\perp^L A_\perp^{R*} + A_\parallel^L A_\parallel^{R*}) \\ I_1^c &= |A_0^L|^2 + |A_0^R|^2 + \frac{4m_\mu^2}{q^2} [|A_t|^2 + 2\text{Re}(A_0^L A_0^{R*})] + \beta_\mu^2 |A_S|^2, \\ I_2^s &= \frac{\beta_\mu^2}{4} [|A_\perp^L|^2 + |A_\parallel^L|^2 + (L \rightarrow R)], \\ I_2^c &= -\beta_\mu^2 [|A_0^L|^2 + (L \rightarrow R)], \\ I_3 &= \frac{1}{2} \beta_\mu^2 [|A_\perp^L|^2 - |A_\parallel^L|^2 + (L \rightarrow R)], \\ I_4 &= \frac{1}{\sqrt{2}} \beta_\mu^2 [\text{Re}(A_0^L A_\parallel^{L*}) + (L \rightarrow R)], \end{aligned}$$

$$\begin{aligned} A_{\parallel L,R} &= -N\sqrt{2}(m_B^2 - m_{K^*}^2) \left[ [(C_9^{\text{eff}} - C_9^{\text{eff}'}) \mp (C_{10}^{\text{eff}} - C_{10}^{\text{eff}'})] \frac{A_1(q^2)}{m_B - m_{K^*}} \right. \\ &\quad \left. + \frac{2m_b}{q^2} (C_7^{\text{eff}} - C_7^{\text{eff}'}) T_2(q^2) \right], \\ A_{0L,R} &= -\frac{N}{2m_{K^*}\sqrt{q^2}} \left\{ [(C_9^{\text{eff}} - C_9^{\text{eff}'}) \mp (C_{10}^{\text{eff}} - C_{10}^{\text{eff}'})] \right. \\ &\quad \times \left[ (m_B^2 - m_{K^*}^2 - q^2)(m_B + m_{K^*})A_1(q^2) - \lambda \frac{A_2(q^2)}{m_B + m_{K^*}} \right] \\ &\quad \left. + 2m_b(C_7^{\text{eff}} - C_7^{\text{eff}'}) \left[ (m_B^2 + 3m_{K^*}^2 - q^2)T_2(q^2) - \frac{\lambda}{m_B^2 - m_{K^*}^2} T_3(q^2) \right] \right\}, \\ A_t &= \frac{N}{\sqrt{q^2}} \lambda^{1/2} \left[ 2(C_{10}^{\text{eff}} - C_{10}^{\text{eff}'}) + \frac{q^2}{m_\mu} (C_P - C_P') \right] A_0(q^2), \\ A_S &= -2N\lambda^{1/2} (C_S - C_S') A_0(q^2), \end{aligned}$$

- helicity amplitude

S. Jager, J. M. Camalich 1212.2263

$$\begin{aligned} I_1^c &= F \left\{ \frac{1}{2} (|H_V^0|^2 + |H_A^0|^2) + |H_P|^2 + \frac{2m_\ell^2}{q^2} (|H_V^0|^2 - |H_A^0|^2) + \beta^2 |H_S|^2 \right\}, \\ I_1^s &= F \left\{ \frac{\beta^2 + 2}{8} (|H_V^+|^2 + |H_V^-|^2 + (V \rightarrow A)) + \frac{m_\ell^2}{q^2} (|H_V^+|^2 + |H_V^-|^2 - (V \rightarrow A)) \right\} \\ I_2^c &= -F \frac{\beta^2}{2} (|H_V^0|^2 + |H_A^0|^2), \\ I_2^s &= F \frac{\beta^2}{8} (|H_V^+|^2 + |H_V^-|^2) + (V \rightarrow A), \\ I_3 &= -\frac{F}{2} \text{Re}[H_V^+(H_V^-)^*] + (V \rightarrow A), \end{aligned}$$

$$\begin{aligned} H_V(\lambda) &= -iN \left\{ C_9 \tilde{V}_{L\lambda} + C_9' \tilde{V}_{R\lambda} + \frac{m_B^2}{q^2} \left[ \frac{2\hat{m}_b}{m_B} (C_7 \tilde{T}_{L\lambda} + C_7' \tilde{T}_{R\lambda}) - 16\pi^2 h_\lambda \right] \right\}, \\ H_A(\lambda) &= -iN (C_{10} \tilde{V}_{L\lambda} + C_{10}' \tilde{V}_{R\lambda}), \\ H_{TR}(\lambda) &= -iN \frac{4\hat{m}_b m_B}{m_W \sqrt{q^2}} C_T \tilde{T}_{L\lambda}, \\ H_{TL}(\lambda) &= -iN \frac{4\hat{m}_b m_B}{m_W \sqrt{q^2}} C_T' \tilde{T}_{R\lambda}, \\ H_S &= iN \frac{\hat{m}_b}{m_W} (C_S \tilde{S}_L + C_S' \tilde{S}_R), \\ H_P &= iN \left\{ \frac{\hat{m}_b}{m_W} (C_P \tilde{S}_L + C_P' \tilde{S}_R) \right. \\ &\quad \left. + \frac{2m_\ell \hat{m}_b}{q^2} \left[ C_{10} \left( \tilde{S}_L - \frac{m_s}{m_b} \tilde{S}_R \right) + C_{10}' \left( \tilde{S}_R - \frac{m_s}{m_b} \tilde{S}_L \right) \right] \right\} \end{aligned}$$



# FITS BEFORE XMAS 2022

## $b \rightarrow s\ell^+\ell^-$ Global Fits after $R_{K_S}$ and $R_{K^{*+}}$

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<sup>b</sup>Institut de Física d'Altes Energies (IFAE), The Barcelona Institute of Science and Technology, Campus UAB, E-08193 Bellaterra (Barcelona), Catalunya.

<sup>c</sup>Università di Torino and INFN Sezione di Torino, Via P. Giuria 1, Torino I-10125, Italy.

<sup>d</sup>Université Paris-Saclay, CNRS/IN2P3, IJCLab, 91405 Orsay, France.

<sup>e</sup>Istituto Nazionale di Fisica Nucleare, Sezione di Bari, Via Orabona 4, I-70126 Bari, Italy

ACDMN, 2104.08921

private code

## New Physics in Rare $B$ Decays after Moriond 2021

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<sup>b</sup> Albert Einstein Center for Fundamental Physics, Institute for Theoretical Physics, University of Bern, Sidlerstrasse 5, CH-3012 Bern, Switzerland

AS, 2103.13370

Flavio

## Implications of new evidence for lepton-universality violation in $b \rightarrow s\ell^+\ell^-$ decays

Li-Sheng Geng,<sup>1,2</sup> Benjamín Grinstein,<sup>3</sup> Sebastian Jäger,<sup>4</sup> Shuang-Yi Li,<sup>5</sup> Jorge Martin Camalich,<sup>6,7</sup> and Rui-Xiang Shi<sup>5</sup>

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<sup>2</sup>School of Physics and Microelectronics, Zhengzhou University, Zhengzhou, Henan 450001, China

<sup>3</sup>Department of Physics, University of California, San Diego, La Jolla, California, 92093, USA

<sup>4</sup>Department of Physics and Astronomy, University of Sussex, Brighton BN1 9QH, United Kingdom

<sup>5</sup>School of Physics, Beihang University, Beijing 102206, China

<sup>6</sup>Instituto de Astrofísica de Canarias, C/ Via Lactea, s/n E38205 - La Laguna (Tenerife), Spain

<sup>7</sup>Universidad de La Laguna, Departamento de Astrofísica, La Laguna, Tenerife E-38205, Spain

GGJLCS, 2103.12378

private code

## Neutral current $B$ -decay anomalies

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HMMN, 2210.07221

SuperIso

# FITTING PACKAGES ON THE MARKET

Brands					
Developers	David M. Straub, Peter Stangl, Jason Aebischer, Jacky Kumar et al.		Jorge de Blas, Debtosh Chowdhury, Marco Ciuchini et al.	Danny van Dyk, Christoph Bobeth, Frederik Beaujean et al.	Farvah Nazila Mahmoudi, A. Arbey et al.
Related works (& Manuals)	arXiv: <b>1810.08132</b> 1704.07397 1608.02556 1704.07397	arXiv: <b>1810.07698</b> 1911.07866 2103.13370 2212.10497	arXiv: <b>1910.14012</b> 1902.05564 1512.07157 1306.4644	arXiv: <b>2111.15428</b> 2305.06301 2208.08937 1912.09335	arXiv: <b>0710.2067</b> <b>0808.3144</b> 1410.4545 1806.11489
First edition (as far as we know)	v0.1.3 (2016.2)	(2018.10)	SUSYfit (2013.06)	D. van Dyk, thesis, 2011	2007.10 2008.08
latest update (as far as we know)	v2.5.5 (2023.6.1)	v2.4.0 (2023.4.27)	v1.0 (2023.5.19)	v1.0.9 (2023.8.8)	v4.1 (2020.11.4)
Code PL	Pure Python3	Based on Flavio	Pure C++11	C++20 with python API	C
Statistic FrameWork	<b>MLE</b> (Bayesian Estimation can be self-defined)	Same as flavio	<b>Bayesian Estimation</b>	<b>Bayesian Estimation</b>	<b>MLE</b>
Scientific Library	     	 	   	 	

# FITTING PACKAGES ON THE MARKET

Brands					
Theo. FrameWork	<b>WEFT</b> (below EW scale) <b>SMEFT(dim-6)</b> (above EW scale)	<b>SMEFT(dim-6)</b> (above EW scale)	1. <b>WEFT/SMEFT(dim6)</b> 2. <b>2HDM/MSSM</b> 3. <b>Georgi-Machacek model</b>	<b>WEFT</b> (below EW scale)	1. <b>WEFT/SMEFT(dim6)</b> 2. <b>2HDM</b> 3. <b>Different scenarios in MSSM</b>
Basis of WEFT	<b>arXiv: 1606.00916</b> (with tensor Operators?)	<b>arXiv: 1606.00916</b> (with tensor Operators?)	<b>arXiv: 1903.09632</b> (no tensor Operators)	<b>arXiv: 2107.04822</b> (with tensor Operators?)	<b>arXiv: 0808.3144</b> (no tensor Operators)
FFs (part of it)	(Heavy to light) <b>B -&gt; VII</b> <b>arXiv: 1503.05534, etc.</b> <b>B -&gt; PII</b> <b>arXiv: 1811.00983, etc.</b> <b>Lambda_b -&gt; Lambda II</b> <b>arXiv: 1602.01399</b> (Heavy to Heavy) <b>B -&gt; D^{(*)} l nu</b> <b>arXiv: 1703.05330 (HQET)</b>	Same as flavio	(Heavy to light) <b>B -&gt; VII</b> <b>arXiv: 1503.05534</b> <b>B -&gt; PII</b> <b>arXiv: hep-ph/0406232</b>	(Heavy to light) <b>B -&gt; VII</b> <b>arXiv: 1503.05534, etc.</b> <b>B -&gt; PII</b> <b>arXiv: 1004.3249, etc.</b> <b>Lambda_b -&gt; Lambda II</b> <b>arXiv: 1602.01399, etc.</b> (Heavy to Heavy) <b>B -&gt; D^{(*)} l nu</b> <b>arXiv: 1503.07237, etc.</b>	(Heavy to light) <b>B -&gt; VII</b> <b>arXiv: 1503.05534, etc.</b> <b>B -&gt; PII</b> <b>arXiv: 1811.00983, etc.</b>
Focused Processes	More than 1400 observables. Observables library.  Higgs production/decays, b/c/s hadron decays, dipole moments, W/Z decays, nucleon decays, EWPO, etc.	EWPO, FCCC, FCNC, LFV processes, Z decays, tau muon decays, meson mixing, Higgs signal strengths.	EWPO, oblique parameter, Higgs observables (strengths and direct searches).  Flavour observables.	Mainly flavour observables	FCNC, LFU, $B \rightarrow V(P)ll$ , $b \rightarrow s\gamma$ , $B \rightarrow X_s ll$ , g-2.

# OUR HOME-MADE FIT

- Statistics: Bayesian statistics
  - weak prior dependence confirmed
  - relied package: emcee
- Theoretical framework: dynamics
  - most generic WEFT/LEFT operator basis (tensor to be added)
  - self-controllable Wilson coefficients
  - the up-to-date FF parameterization
- Observables & kinematics
  - transversity amplitude convention adopted
  - all observables (Br, ADO, LFU...) have been encompassed

# OUR RESULTS (I)

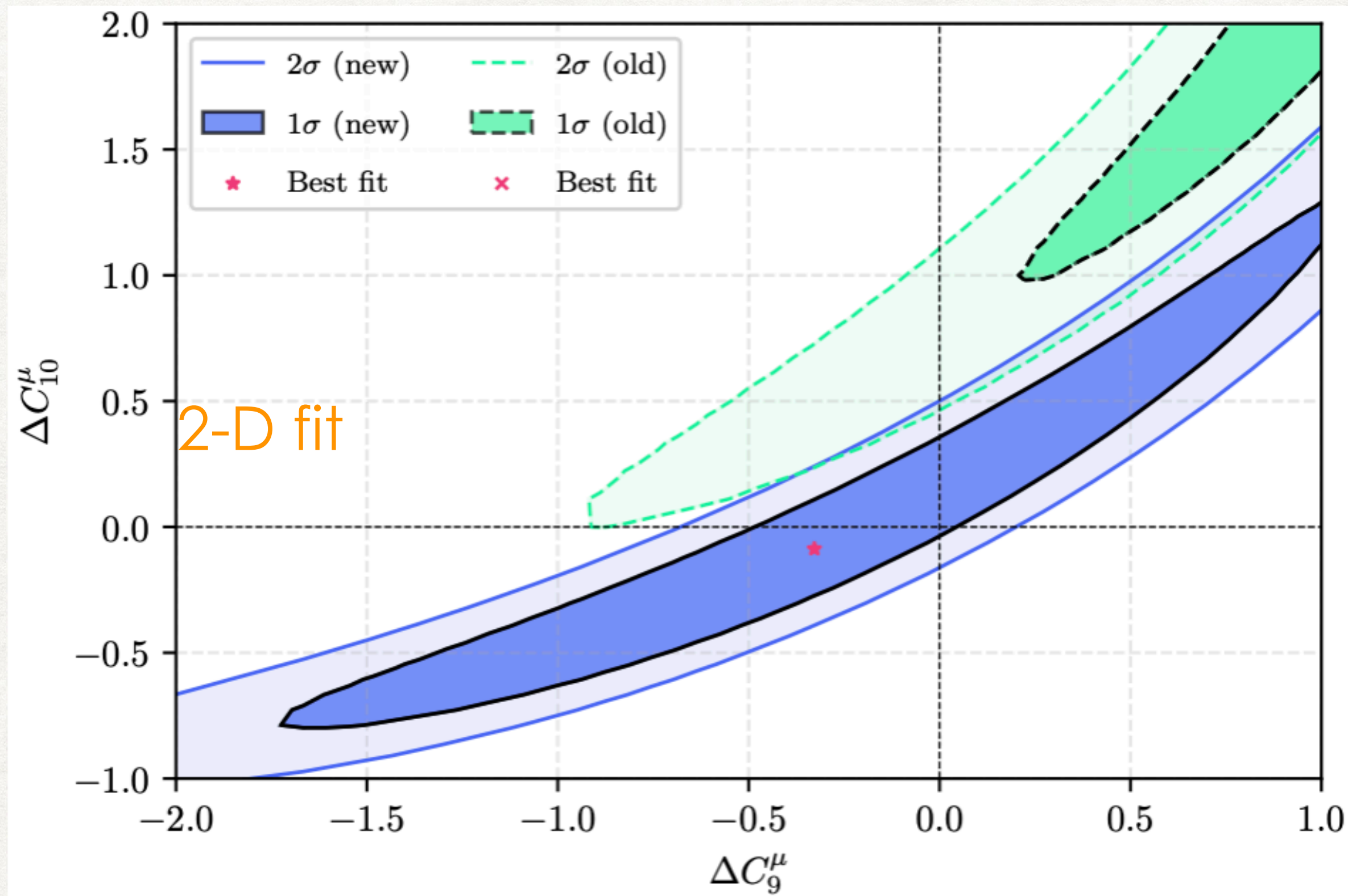
Params	S-I'	S-II'	S-III'	S-IV'	S-I	S-II	S-III	S-IV	ADCMN [23]	AS [24]	HMMN [25]	GGJLCS [26]
Reduced $\chi^2$	183.404/(n-12)	197.556/(n-12)	182.869/(n-16)	176.807/(n-20)	190.044/(n-12)	177.891/(n-12)	185.386/(n-16)	178.953/(n-20)	260.66/(254-6)		179.1/(183-20)	96.88/90
$\chi^2_{\min}/\text{d.o.f}$	= 0.970	= 1.045	= 0.988	= 0.977	= 0.995	= 0.931	= 0.991	= 0.978	= 1.05		= 1.1	= 1.08
$\Delta C_7$	$-0.003^{+0.020}_{-0.019}$	$-0.001^{+0.015}_{-0.015}$	...	$0.001^{+0.016}_{-0.015}$	$-0.000^{+0.020}_{-0.020}$	$-0.001^{+0.015}_{-0.015}$	...	$-0.000^{+0.016}_{-0.015}$	$0.00^{+0.01}_{-0.02}$	...	$0.06^{+0.03}_{-0.03}$	...
$\Delta C_7'$	$0.017^{+0.018}_{-0.019}$	$0.020^{+0.014}_{-0.015}$	...	$0.020^{+0.014}_{-0.014}$	$0.017^{+0.020}_{-0.018}$	$0.020^{+0.015}_{-0.014}$	...	$0.023^{+0.014}_{-0.016}$	$+0.00^{+0.02}_{-0.01}$	...	$-0.01^{+0.01}_{-0.01}$	...
$\Delta C_8$	$-0.788^{+0.595}_{-0.514}$	$-0.885^{+0.435}_{-0.398}$	...	$-0.773^{+0.451}_{-0.449}$	$-0.995^{+0.540}_{-0.463}$	$-0.921^{+0.443}_{-0.378}$	...	$-0.773^{+0.465}_{-0.424}$	...	...	$-0.80^{+0.40}_{-0.40}$	...
$\Delta C_8'$	$-0.073^{+1.089}_{-1.000}$	$-0.093^{+0.921}_{-0.831}$	...	$-0.089^{+0.996}_{-0.922}$	$-0.080^{+1.046}_{-0.942}$	$-0.076^{+0.893}_{-0.833}$	...	$-0.258^{+1.007}_{-0.802}$	...	...	$-0.30^{+1.30}_{-1.30}$	...
$\Delta C_9^\mu$	$-0.806^{+0.257}_{-0.272}$	$-0.795^{+0.205}_{-0.210}$	$-1.068^{+0.161}_{-0.164}$	$-0.863^{+0.214}_{-0.227}$	$-0.752^{+0.262}_{-0.265}$	$-0.789^{+0.198}_{-0.210}$	$-1.054^{+0.163}_{-0.171}$	$-0.872^{+0.215}_{-0.215}$	$-1.08^{+0.18}_{-0.17}$	$-0.82^{+0.23}_{-0.23}$	$-1.14^{+0.19}_{-0.19}$	$-1.07^{+0.29}_{-0.29}$
$\Delta C_9^{\prime\mu}$	$0.194^{+0.395}_{-0.416}$	$0.056^{+0.338}_{-0.342}$	$0.112^{+0.393}_{-0.397}$	$0.020^{+0.346}_{-0.362}$	$0.174^{+0.434}_{-0.441}$	$0.048^{+0.338}_{-0.348}$	$0.130^{+0.439}_{-0.437}$	$0.088^{+0.342}_{-0.378}$	$0.16^{+0.37}_{-0.36}$	$-0.10^{+0.34}_{-0.34}$	$0.05^{+0.32}_{-0.32}$	$0.32^{+0.21}_{-0.21}$
$\Delta C_{10}^\mu$	$0.236^{+0.216}_{-0.193}$	$0.145^{+0.166}_{-0.156}$	$0.164^{+0.181}_{-0.180}$	$0.213^{+0.166}_{-0.155}$	$-0.019^{+0.206}_{-0.175}$	$0.163^{+0.165}_{-0.160}$	$0.112^{+0.166}_{-0.184}$	$0.171^{+0.157}_{-0.175}$	$0.15^{+0.13}_{-0.13}$	$+0.14^{+0.23}_{-0.23}$	$0.21^{+0.20}_{-0.20}$	$0.21^{+0.14}_{-0.14}$
$\Delta C_{10}^{\prime\mu}$	$-0.096^{+0.251}_{-0.237}$	$-0.108^{+0.186}_{-0.177}$	$-0.115^{+0.200}_{-0.198}$	$-0.089^{+0.177}_{-0.176}$	$-0.118^{+0.266}_{-0.247}$	$-0.093^{+0.183}_{-0.179}$	$-0.115^{+0.215}_{-0.213}$	$-0.062^{+0.197}_{-0.180}$	$-0.18^{+0.20}_{-0.18}$	$-0.33^{+0.23}_{-0.23}$	$-0.03^{+0.19}_{-0.19}$	$-0.26^{+0.14}_{-0.14}$
$\Delta C_S^\mu$	$0.066^{+1.091}_{-1.142}$	$-0.004^{+1.102}_{-1.131}$	$-0.008^{+0.883}_{-0.899}$	$-0.043^{+0.842}_{-0.875}$	$0.023^{+1.064}_{-1.097}$	$0.060^{+1.188}_{-1.230}$	$-0.066^{+0.944}_{-0.929}$	$0.009^{+0.858}_{-0.845}$	...	...	$0.01^{+0.05}_{-0.05}$	...
$\Delta C_S^{\prime\mu}$	$0.065^{+1.087}_{-1.140}$	$0.003^{+1.103}_{-1.126}$	$-0.002^{+0.873}_{-0.936}$	$-0.059^{+0.844}_{-0.869}$	$0.014^{+1.064}_{-1.086}$	$0.061^{+1.188}_{-1.225}$	$-0.070^{+0.957}_{-0.930}$	$0.012^{+0.858}_{-0.862}$	...	...	$-0.01^{+0.05}_{-0.05}$	...
$\Delta C_P^\mu$	$0.167^{+1.172}_{-1.225}$	$1.017^{+0.735}_{-0.816}$	$0.092^{+1.076}_{-0.994}$	$0.117^{+0.847}_{-0.894}$	$0.079^{+1.159}_{-1.146}$	$0.478^{+0.808}_{-0.899}$	$0.189^{+1.018}_{-1.028}$	$0.124^{+0.902}_{-0.910}$	...	...	$-0.04^{+0.02}_{-0.02}$	...
$\Delta C_P^{\prime\mu}$	$0.053^{+1.169}_{-1.227}$	$0.891^{+0.729}_{-0.812}$	$0.010^{+1.083}_{-1.002}$	$0.040^{+0.854}_{-0.895}$	$-0.032^{+1.158}_{-1.145}$	$0.370^{+0.803}_{-0.897}$	$0.098^{+1.009}_{-1.024}$	$0.038^{+0.894}_{-0.913}$	...	...	$-0.04^{+0.02}_{-0.02}$	...
$\Delta C_9^e$	...	$-0.795^{+0.205}_{-0.210}$	$-1.753^{+0.781}_{-0.772}$	$-1.551^{+0.627}_{-0.599}$	...	$-0.789^{+0.198}_{-0.210}$	$-1.623^{+0.662}_{-0.734}$	$-1.511^{+0.561}_{-0.533}$	...	$-0.24^{+1.17}_{-1.17}$	$-6.50^{+1.90}_{-1.90}$	...
$\Delta C_9^{te}$	...	$0.056^{+0.338}_{-0.342}$	$1.725^{+1.724}_{-2.286}$	$1.710^{+1.466}_{-1.764}$	...	$0.048^{+0.338}_{-0.348}$	$1.090^{+1.610}_{-1.793}$	$0.864^{+1.483}_{-1.608}$	...	...	$1.40^{+2.30}_{-2.30}$	...
$\Delta C_{10}^e$	...	$0.145^{+0.166}_{-0.156}$	$0.108^{+1.456}_{-0.661}$	$0.058^{+1.193}_{-0.661}$	...	$0.163^{+0.165}_{-0.160}$	$0.555^{+1.042}_{-0.576}$	$0.383^{+0.840}_{-0.424}$	...	$-0.24^{+0.78}_{-0.78}$	$\sim 0$	...
$\Delta C_{10}^{te}$	...	$-0.108^{+0.186}_{-0.177}$	$0.600^{+1.208}_{-1.099}$	$0.655^{+0.958}_{-0.841}$	...	$-0.093^{+0.183}_{-0.179}$	$0.088^{+0.969}_{-0.956}$	$0.002^{+0.881}_{-0.815}$	...	...	$\sim 0$	...
$\Delta C_S^e$	...	$-0.004^{+1.102}_{-1.131}$	$-0.719^{+1.861}_{-1.227}$	$-0.549^{+1.602}_{-1.232}$	...	$0.060^{+1.188}_{-1.230}$	$-0.952^{+2.122}_{-1.139}$	$-0.806^{+1.900}_{-1.238}$	...	...	$-0.38^{+0.41}_{-0.41}$	...
$\Delta C_S^{te}$	...	$0.003^{+1.103}_{-1.126}$	$-0.699^{+1.837}_{-1.224}$	$-0.550^{+1.618}_{-1.326}$	...	$0.061^{+1.188}_{-1.225}$	$-1.051^{+2.251}_{-1.075}$	$-0.803^{+1.861}_{-1.194}$	...	...	$-0.36^{+0.50}_{-0.50}$	...
$\Delta C_P^e$	...	$1.017^{+0.735}_{-0.816}$	$-1.592^{+1.552}_{-0.979}$	$-1.688^{+1.366}_{-0.978}$	...	$0.478^{+0.808}_{-0.899}$	$-1.568^{+1.544}_{-1.149}$	$-1.837^{+1.376}_{-0.930}$	...	...	$-0.98^{+0.21}_{-0.21}$	...
$\Delta C_P^{te}$	...	$0.891^{+0.729}_{-0.812}$	$-1.360^{+1.318}_{-1.149}$	$-1.431^{+1.212}_{-1.017}$	...	$0.370^{+0.803}_{-0.897}$	$-1.477^{+1.409}_{-1.083}$	$-1.652^{+1.200}_{-0.979}$	...	...	$-0.95^{+0.29}_{-0.29}$	...

Before Dec. 2022

After Dec. 2022

- we carried out a 20-D fit
- fitting results depend on the numbers of fitting d.o.f.
- both old and new fits imply NP exists in  $\Delta C_9^\mu$  in various fitting scenarios
- both old and new fits imply: NP possibility in  $\Delta C_{10}^\mu$  is less hopeful
- new fits implies: NP may be hidden in  $\Delta C_9^e$ , and its inverse process  $e^+e^- \rightarrow bs$  calls for **CEPC**

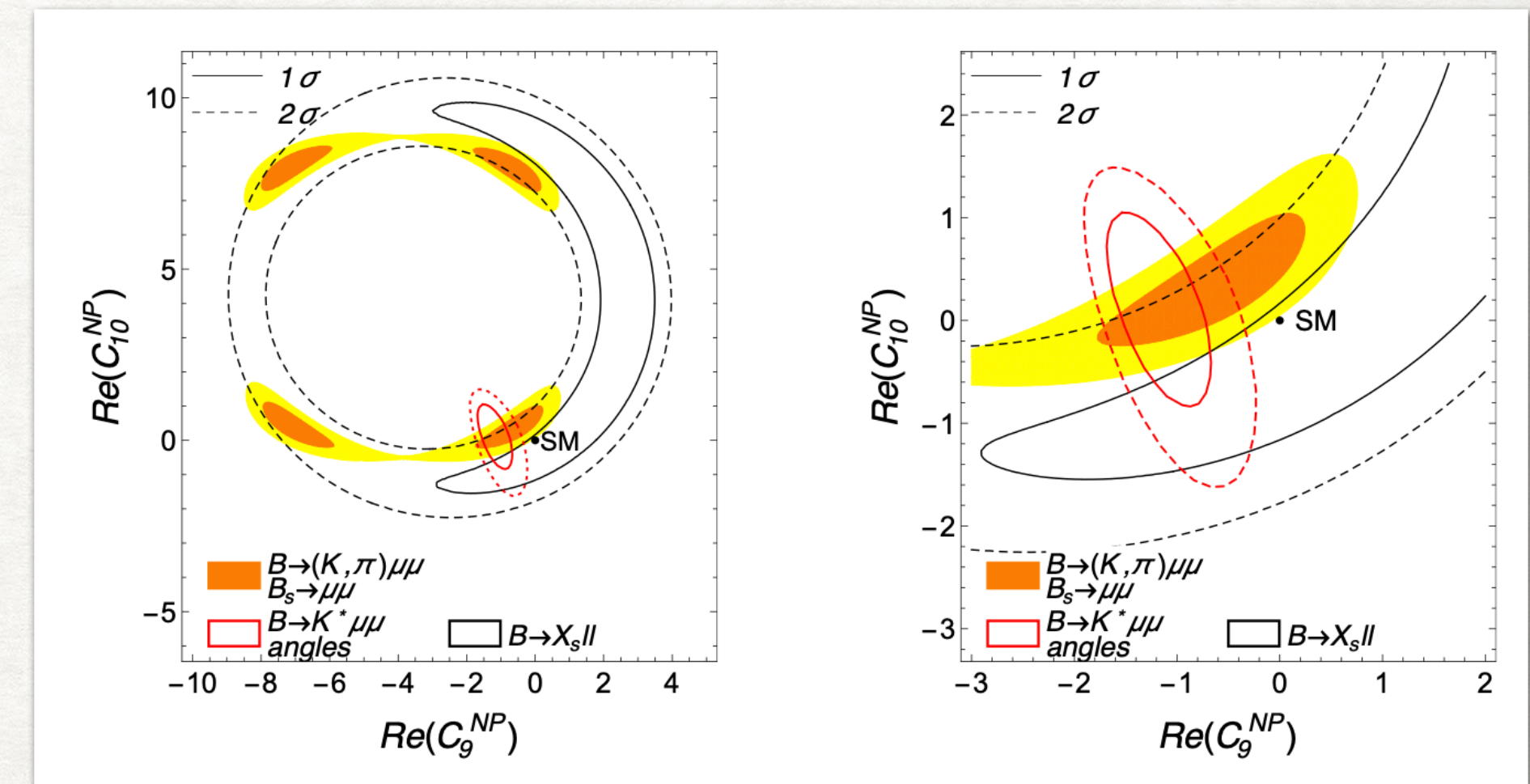
# UNDERSTANDING THE ROLE OF $R_{K^{(*)}}$



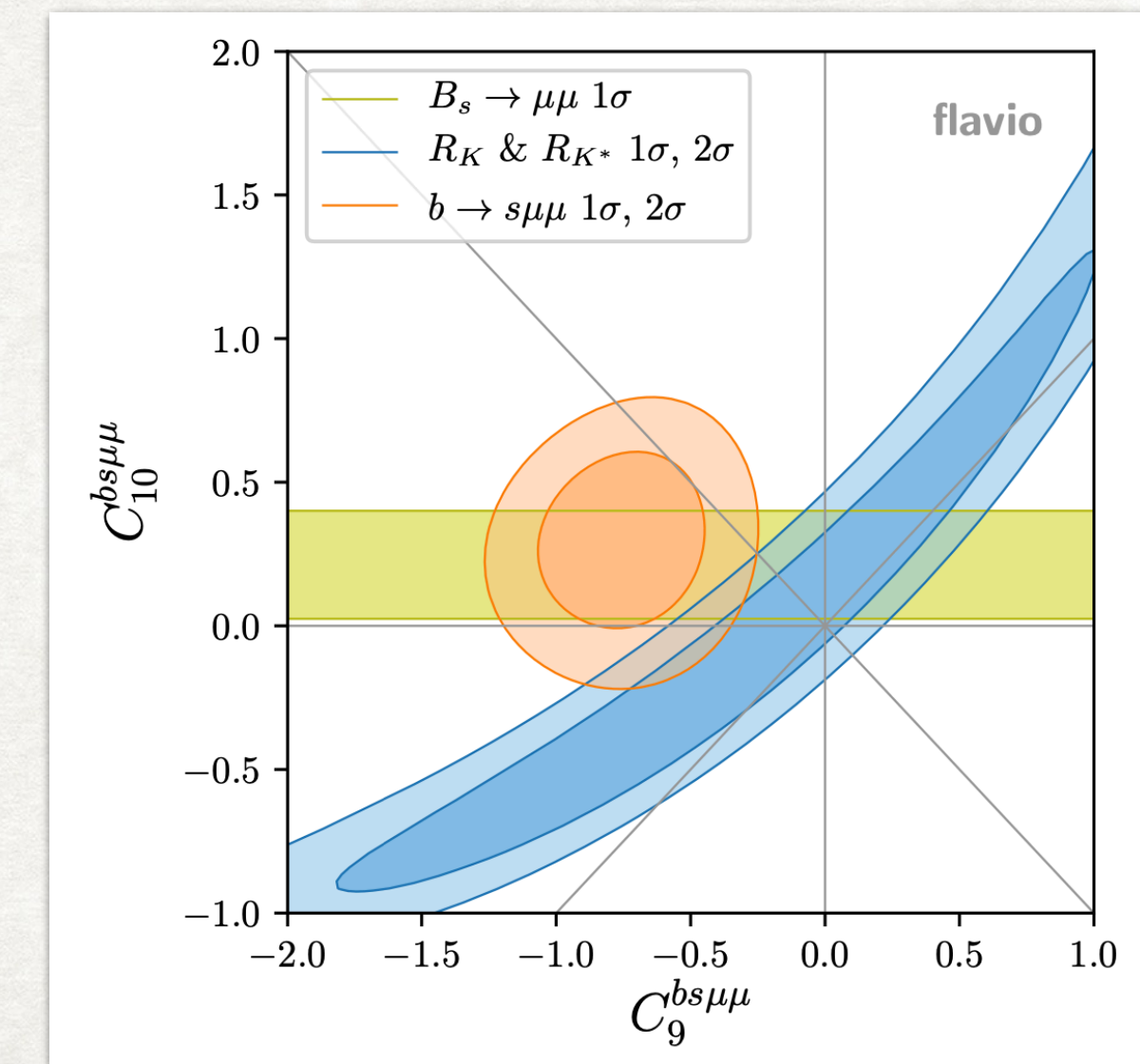
Pure  $R_{K^{(*)}}$  constraints on  $(\Delta C_9^\mu, \Delta C_{10}^\mu)$  :

still with large uncertainty

$R_{K^{(*)}}$  is not main determiner of  $\Delta C_9^\mu$ , slightly shift  $\Delta C_{10}^\mu$

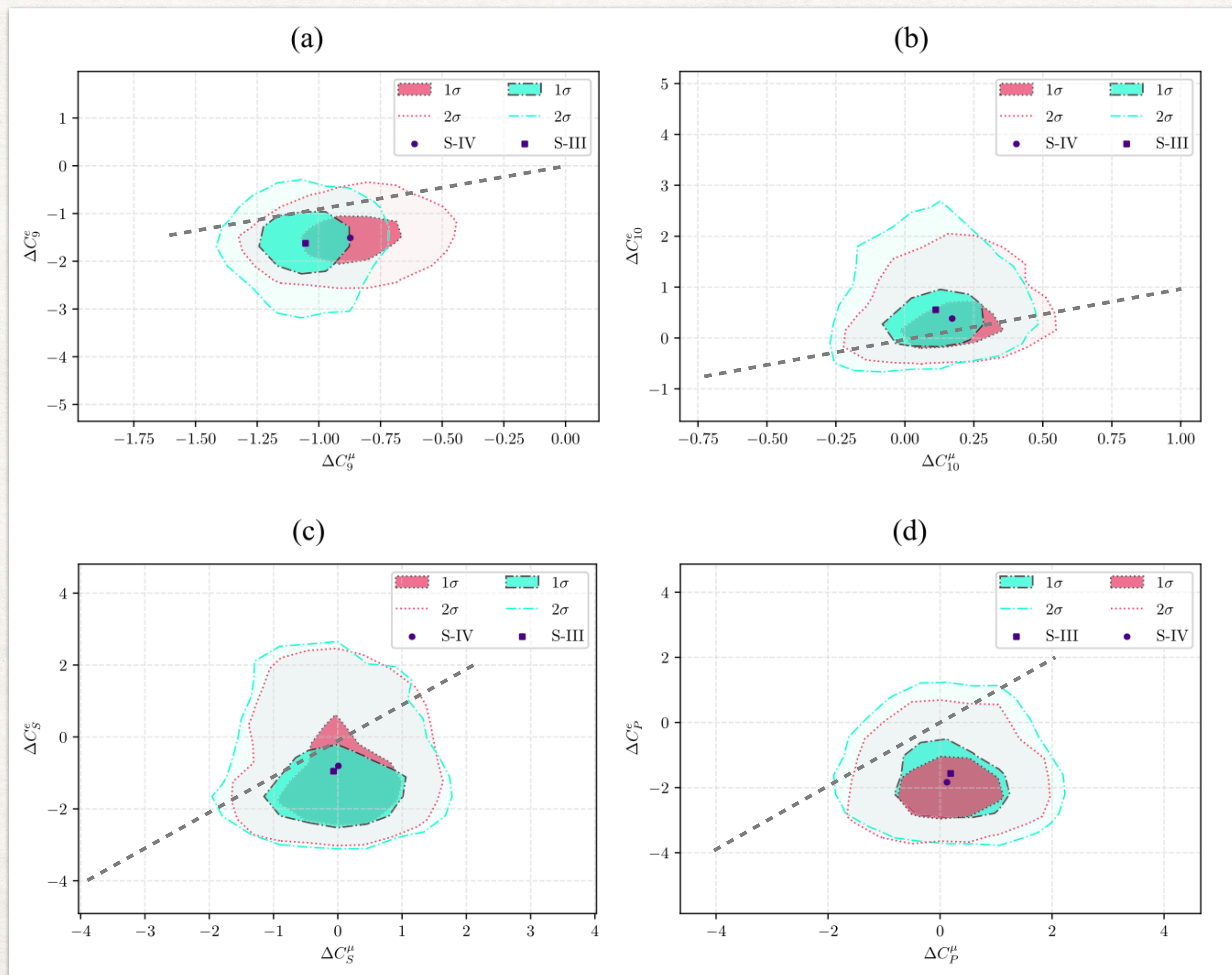


Daping Du, et.al. 1510.02349



Admir Greljo, et.al. 2212.10497

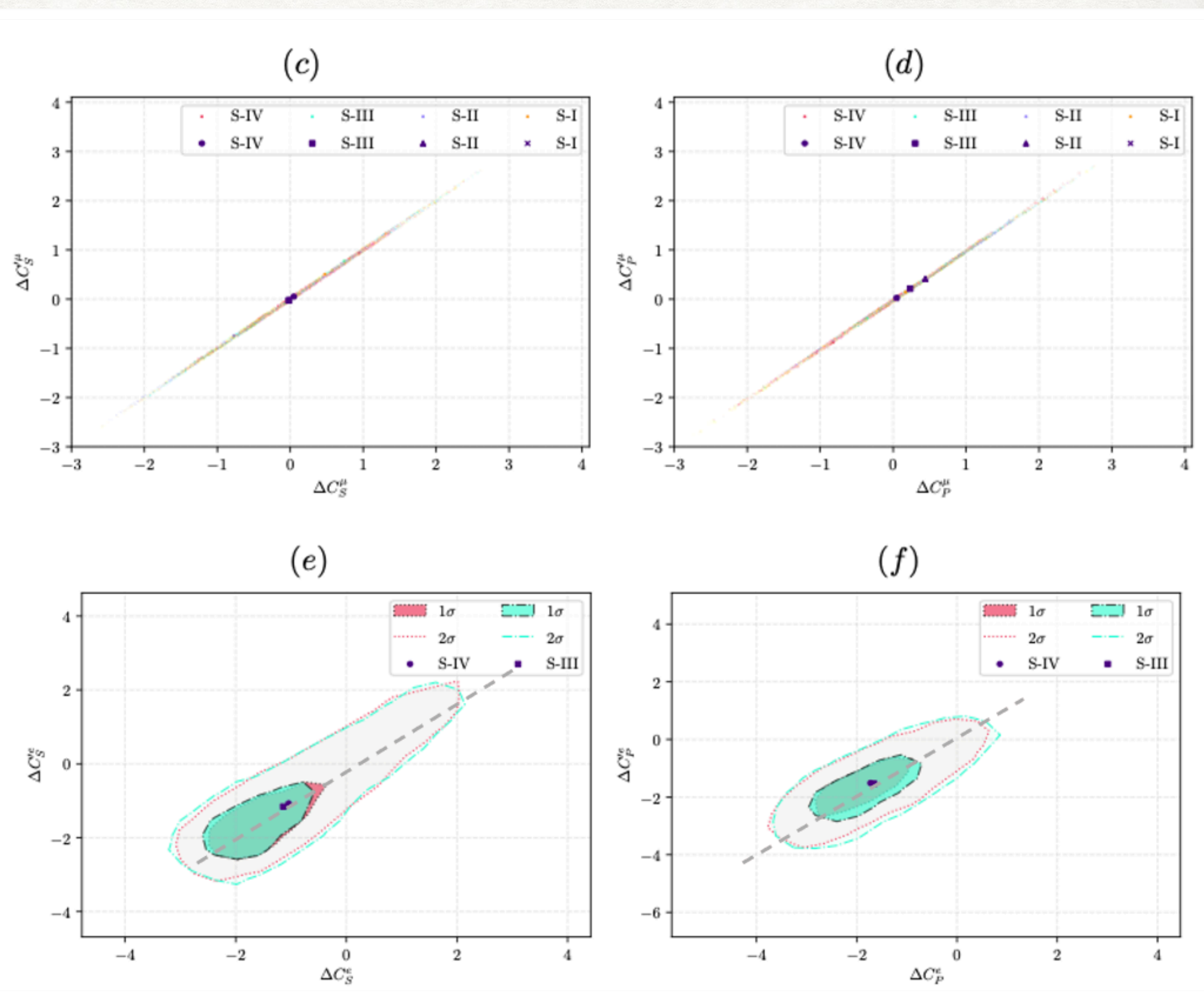
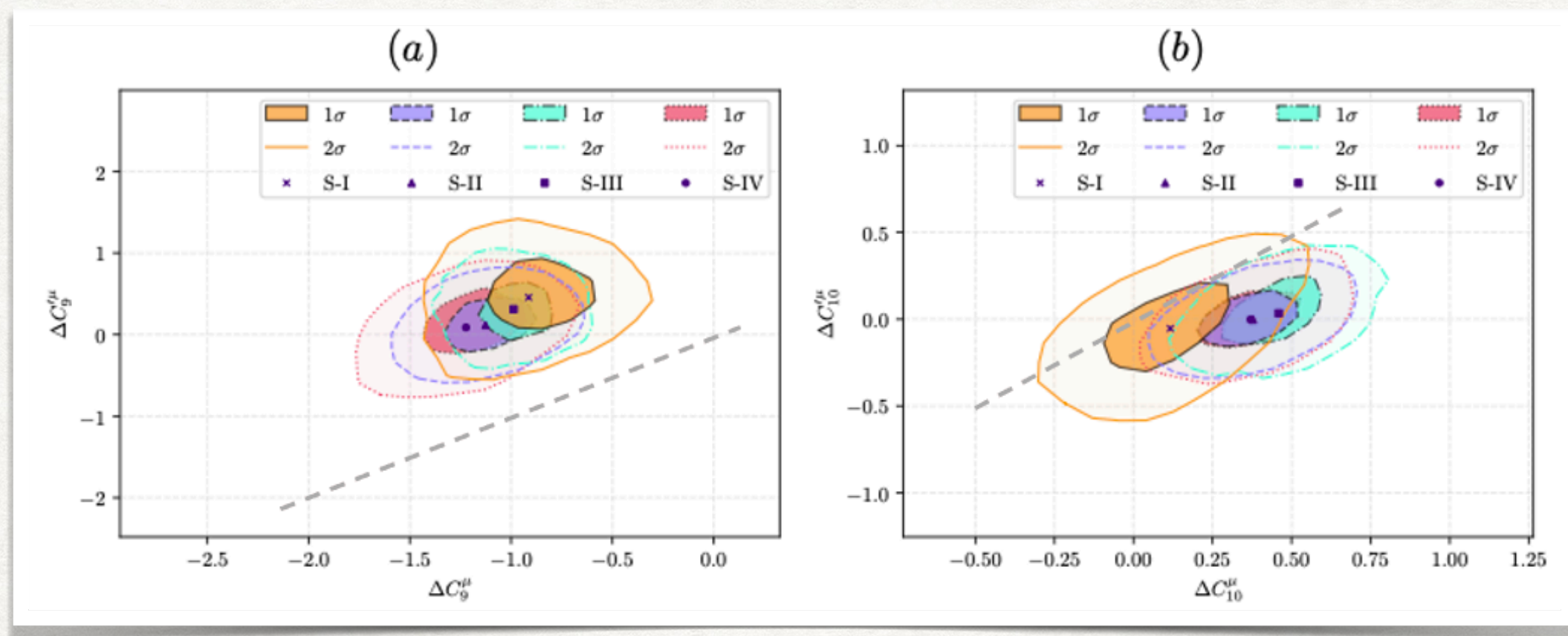
# OUR RESULTS (II): FLAVOR CORRELATION



## Muon-type operator as an example

- The lepton flavor for  $\Delta C_{10}^\mu$  is indistinguishable at  $1\sigma$  level.
- All WCs are flavor identical at  $2\sigma$  level

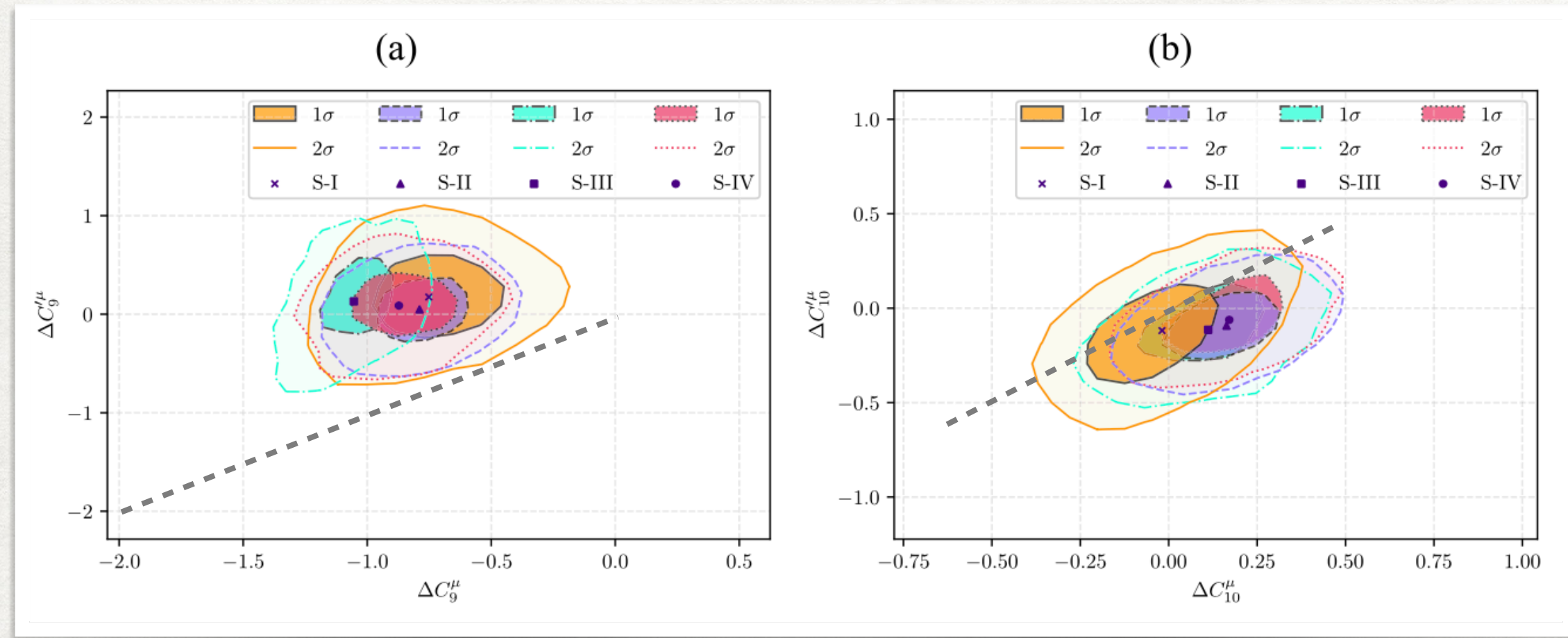
# OUR RESULTS (III): CHIRAL CORRELATION



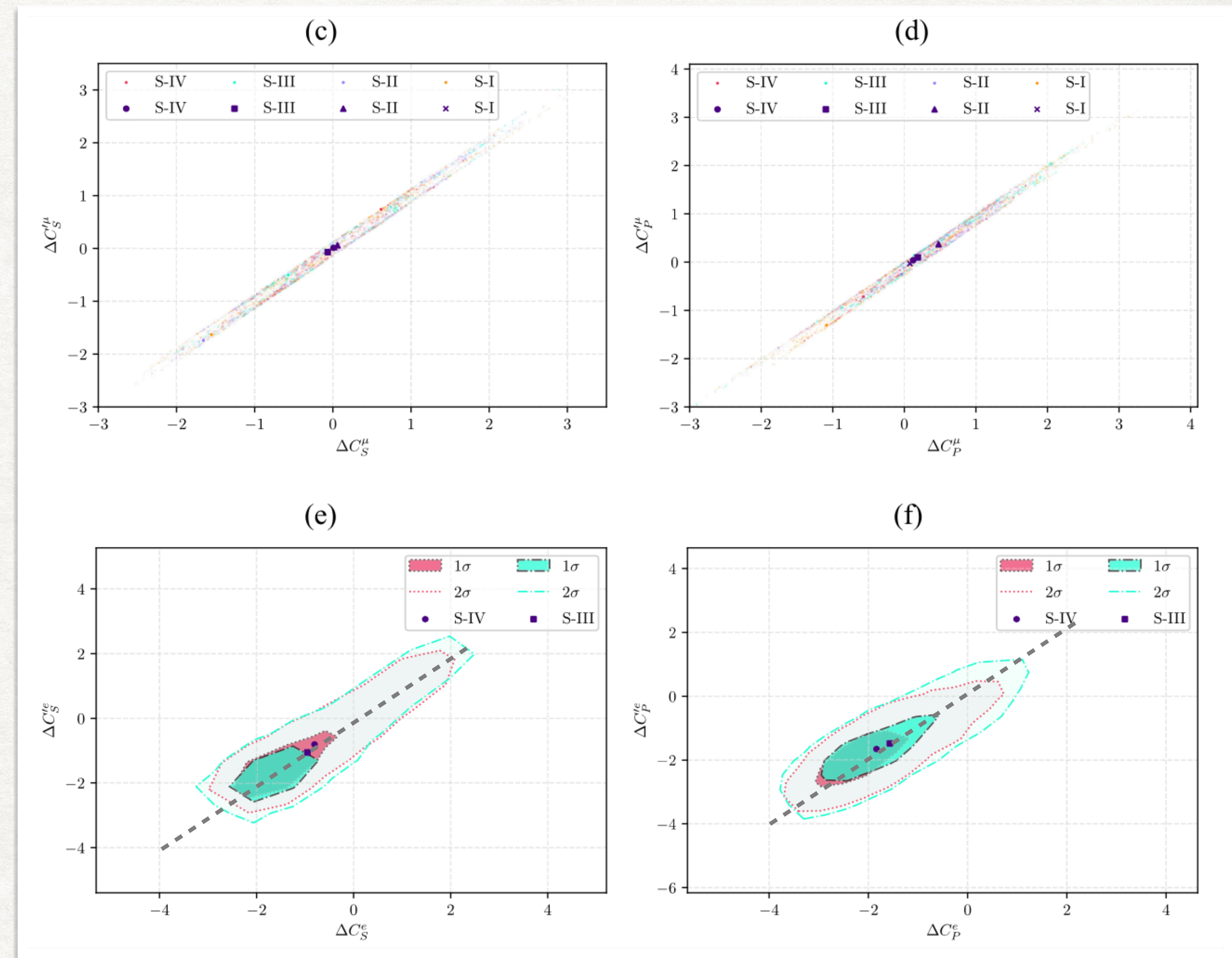
- $\Delta C_9^\mu$  deviates from its chiral dual one more than  $2\sigma$  level, while  $\Delta C_{10}^\mu$  is within  $1\sigma$  region which is scenario dependent.
- scalar WCs have better chiral identity, and muon type is strictly respected.



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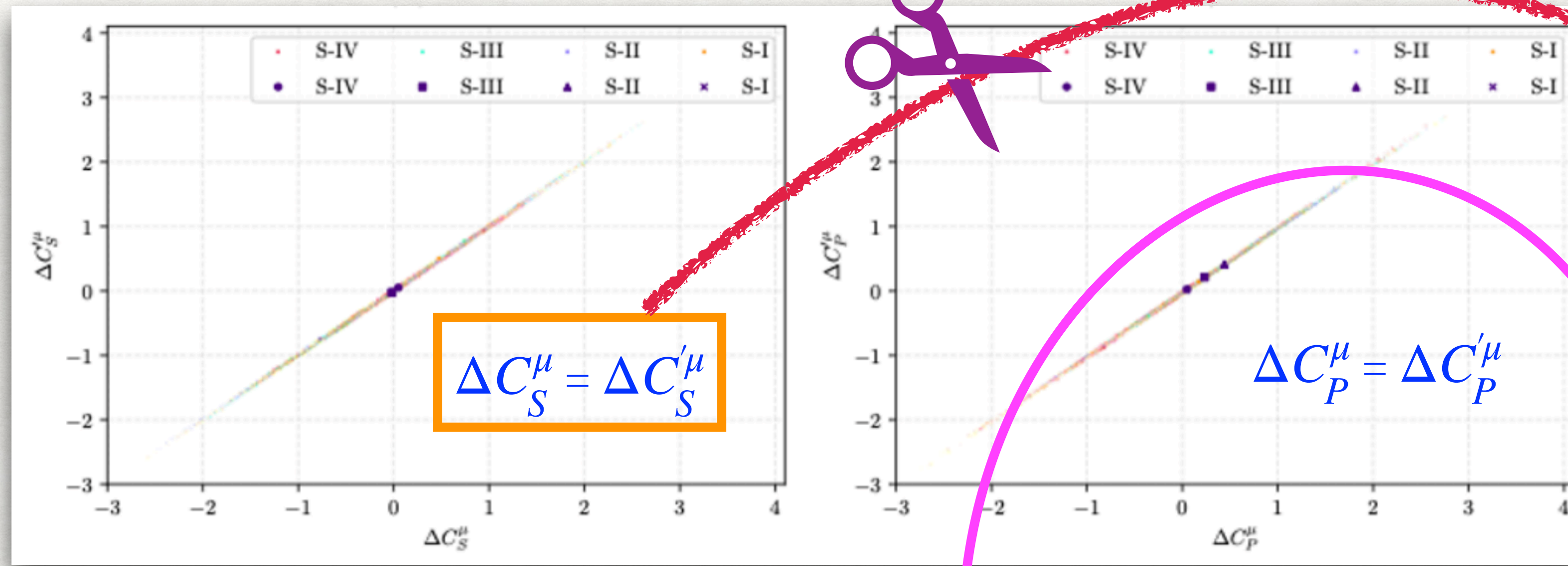
- $\Delta C_9^\mu$  deviates from its chiral dual one more than  $2\sigma$  level, while  $\Delta C_{10}^\mu$  is within  $1\sigma$  region which is scenario dependent.
- scalar WCs have better chiral identity, and muon type is strictly respected.



# IMPLICATIONS

Two options:

- Non-SMEFT NP
- SMEFT: vanishing scalar operator



- SMEFT (Jenkins, Manohar and Stoffer, 1709.04486)

$$\begin{aligned} \lambda_1 C_7 &= c_7, \\ \lambda_2 C_9 &= c_\ell^{V,LL} + c_\ell^{V,LR}, \\ \lambda_2 C'_9 &= c_\ell^{V,LR} + c_\ell^{V,RR}, \\ \lambda_2 C_S &= c_\ell^{S,RR} + c_\ell^{S,RL}, \\ \lambda_2 C'_S &= c_\ell^{S,RL} + c_\ell^{S,RR}, \\ \lambda_2 C_T &= c_\ell^{T,RR} + c_\ell^{T,RR}, \end{aligned}$$

$$\begin{aligned} \lambda_1 C'_7 &= c'_7, \\ \lambda_2 C_{10} &= -c_\ell^{V,LL} + c_\ell^{V,LR}, \\ \lambda_2 C'_{10} &= -c_\ell^{V,LR} + c_\ell^{V,RR}, \\ \lambda_2 C_P &= c_\ell^{S,RR} - c_\ell^{S,RL}, \\ \lambda_2 C'_P &= c_\ell^{S,RL} - c_\ell^{S,RR}, \\ \lambda_2 C_{T5} &= -c_\ell^{T,RR} + c_\ell^{T,RR}, \end{aligned}$$

$$C_S + C_P = 0, \quad C'_S - C'_P = 0, \quad C_T = 0, \quad C_{T5} = 0.$$

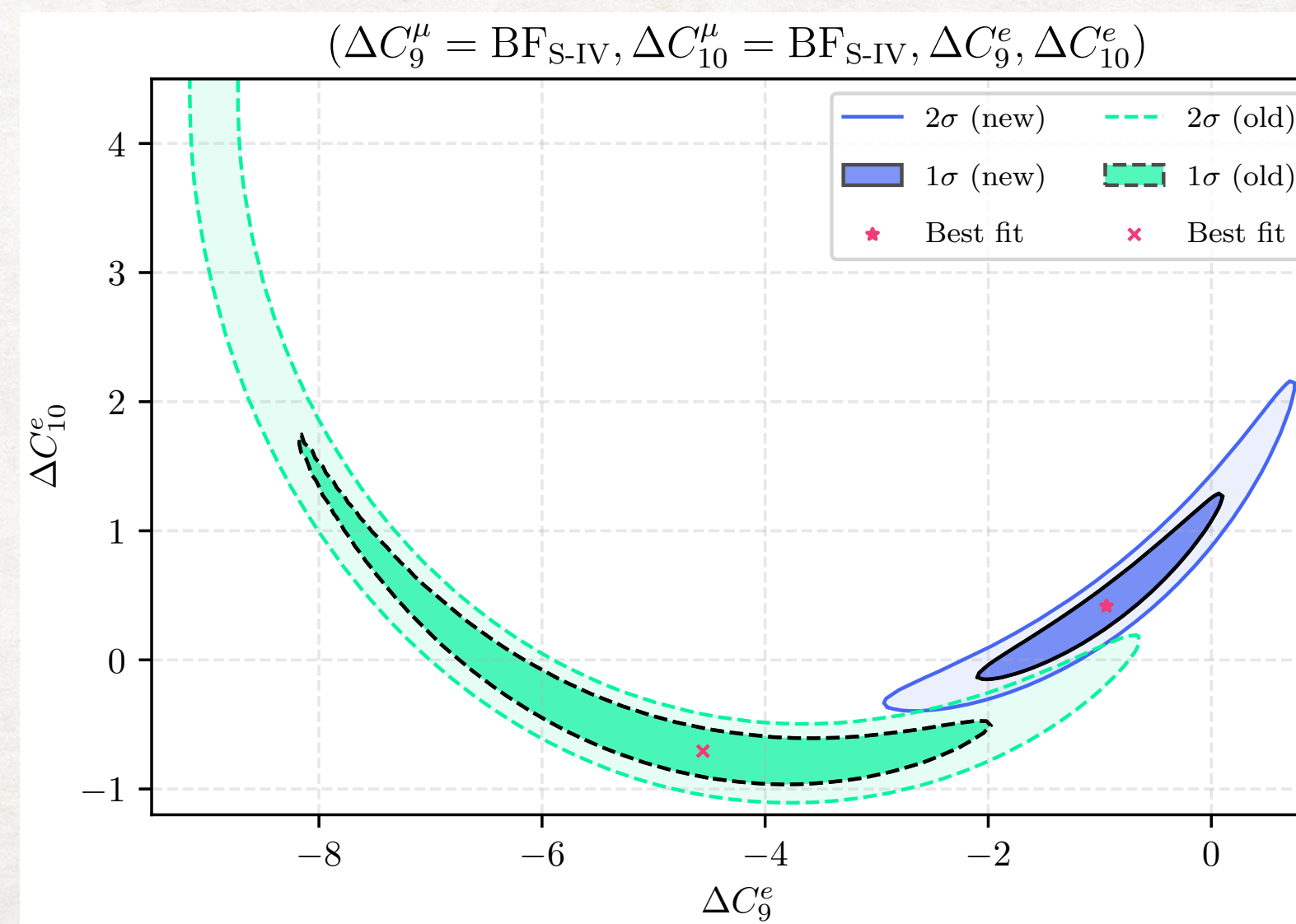
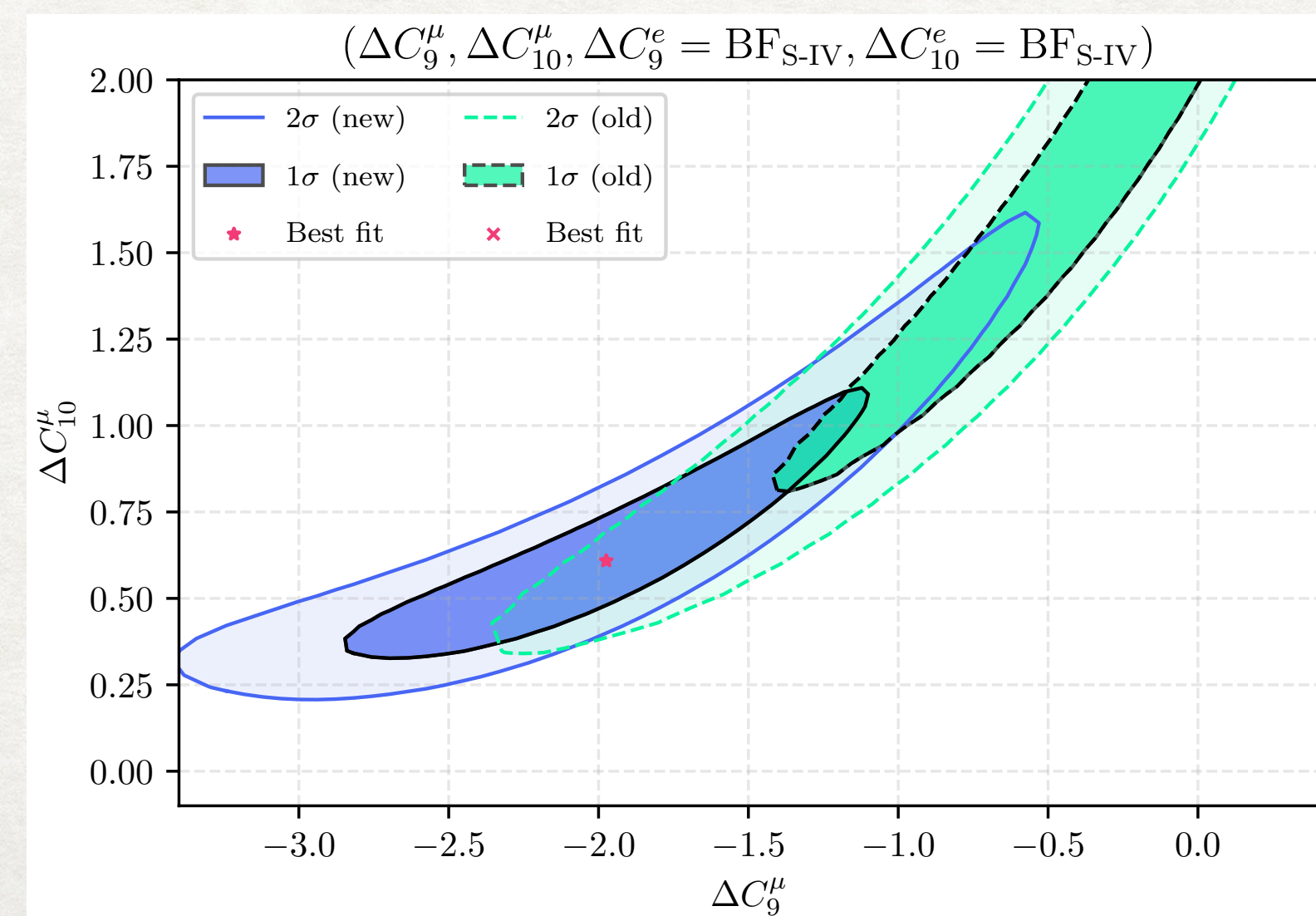
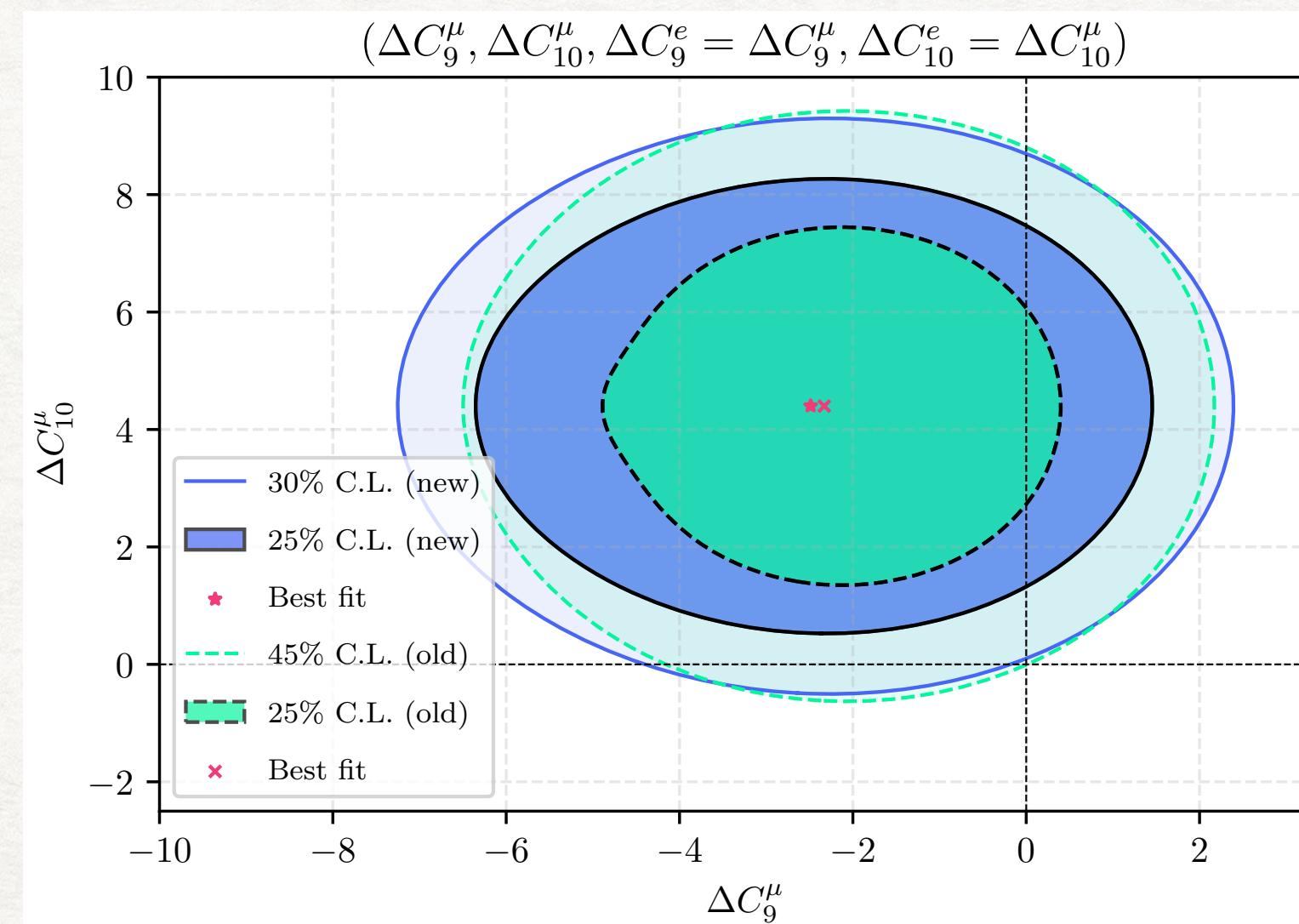
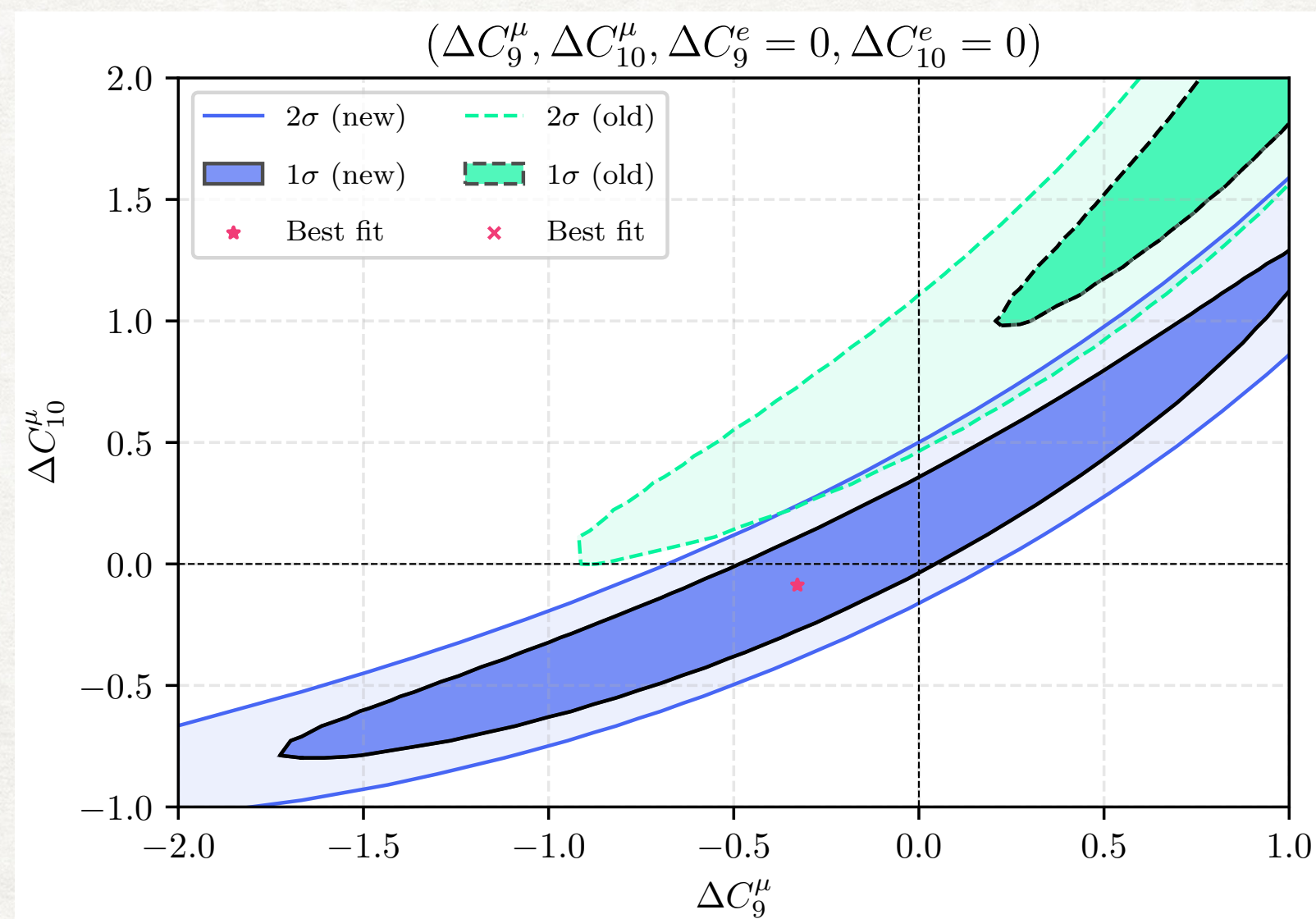
# SUMMARY

- Based on 2 datasets, global fits have been carried out in four different operator basis/scenarios, including the 20-D fit with specific lepton flavors.
- NP possibility in  $b \rightarrow s$  window still exists. It turns up most likely in terms of  $\Delta C_9^\mu$ , and  $\Delta C_9^e$  is also possible.
- Experimentally, CEPC may provide complementary view via  $e^+e^- \rightarrow bs$  process.
- Theoretically, the obtained linear relation between scalar operator provides useful information to NP exploration: non-SMEFT or certain vanishing SMEFT operators.
- More serious studies on bottomed baryon decays are expected!

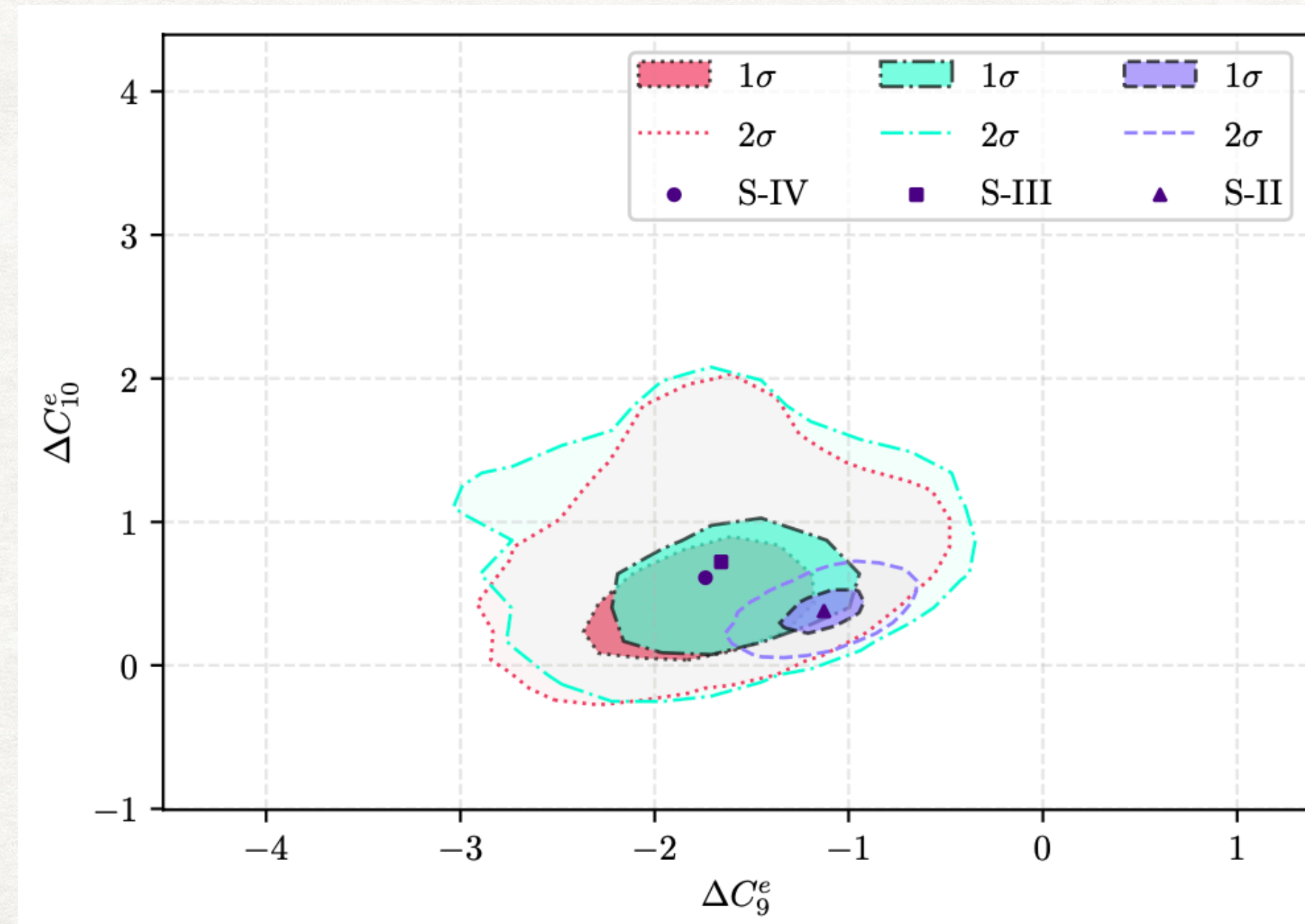
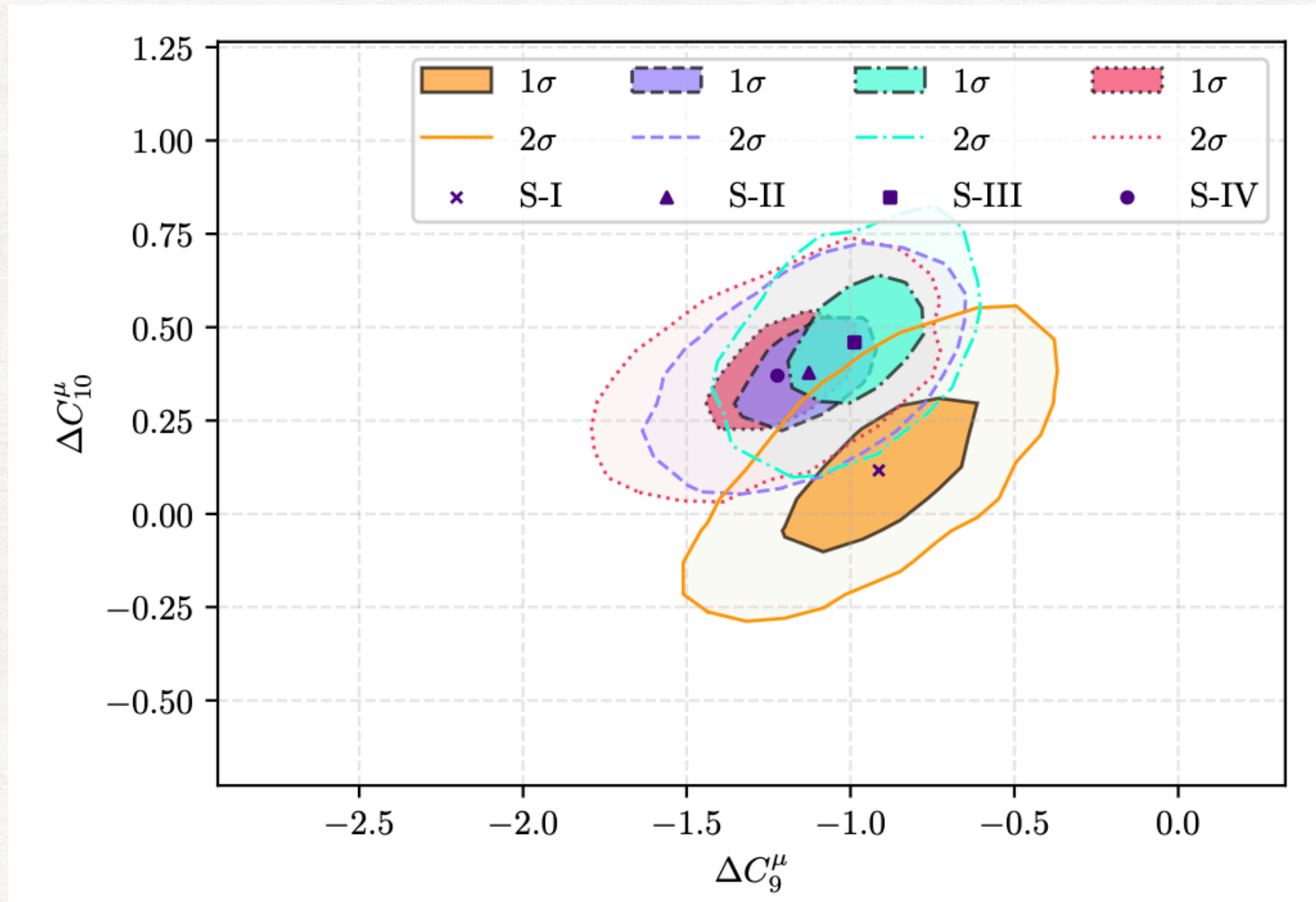
*Thank you for your attention!*

**BACKUP SLIDES**

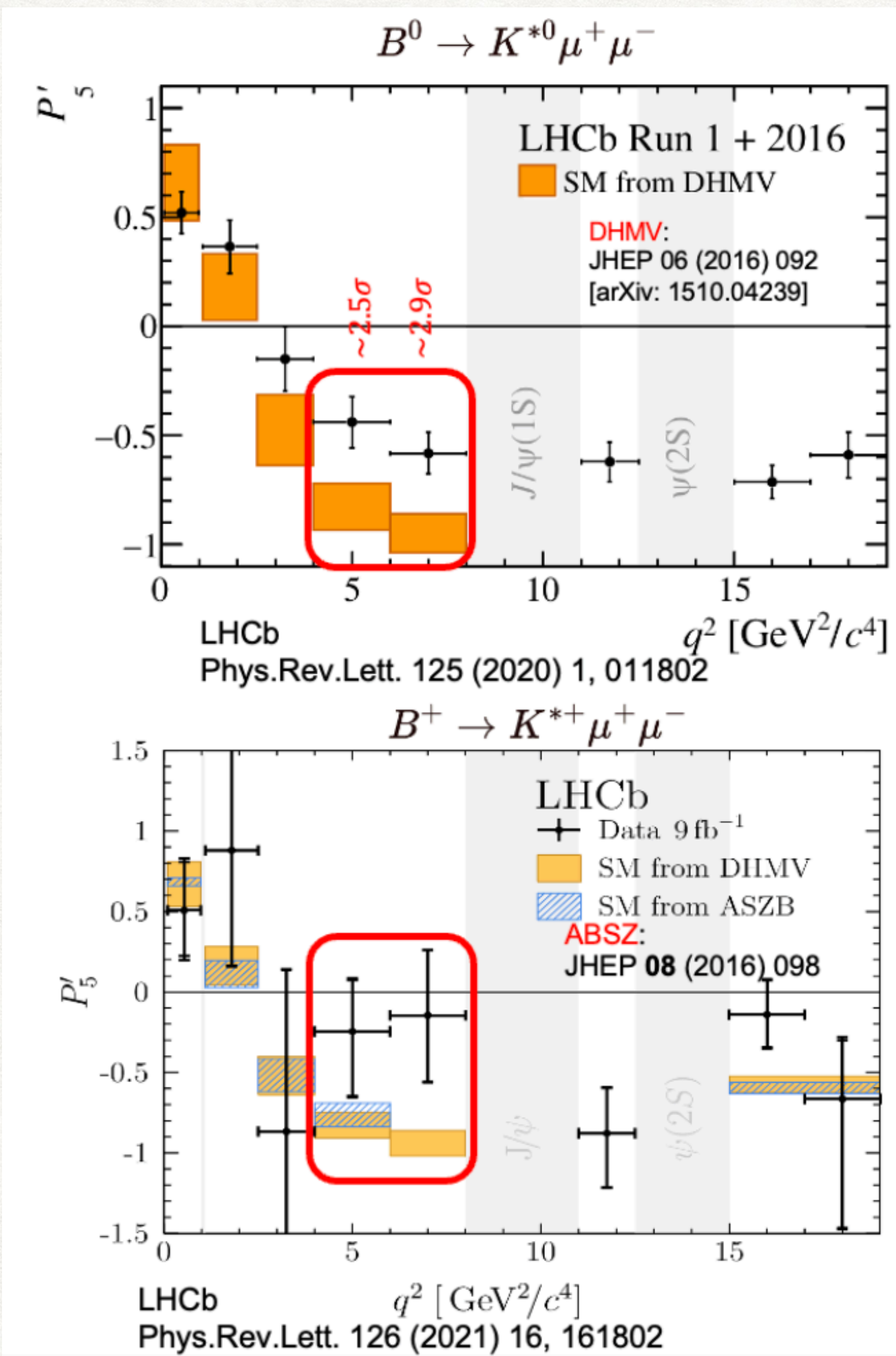
# LEPTON FLAVOR DEPENDENCE



# THE LATEST $(\Delta C_9, \Delta C_{10})$ RANGE



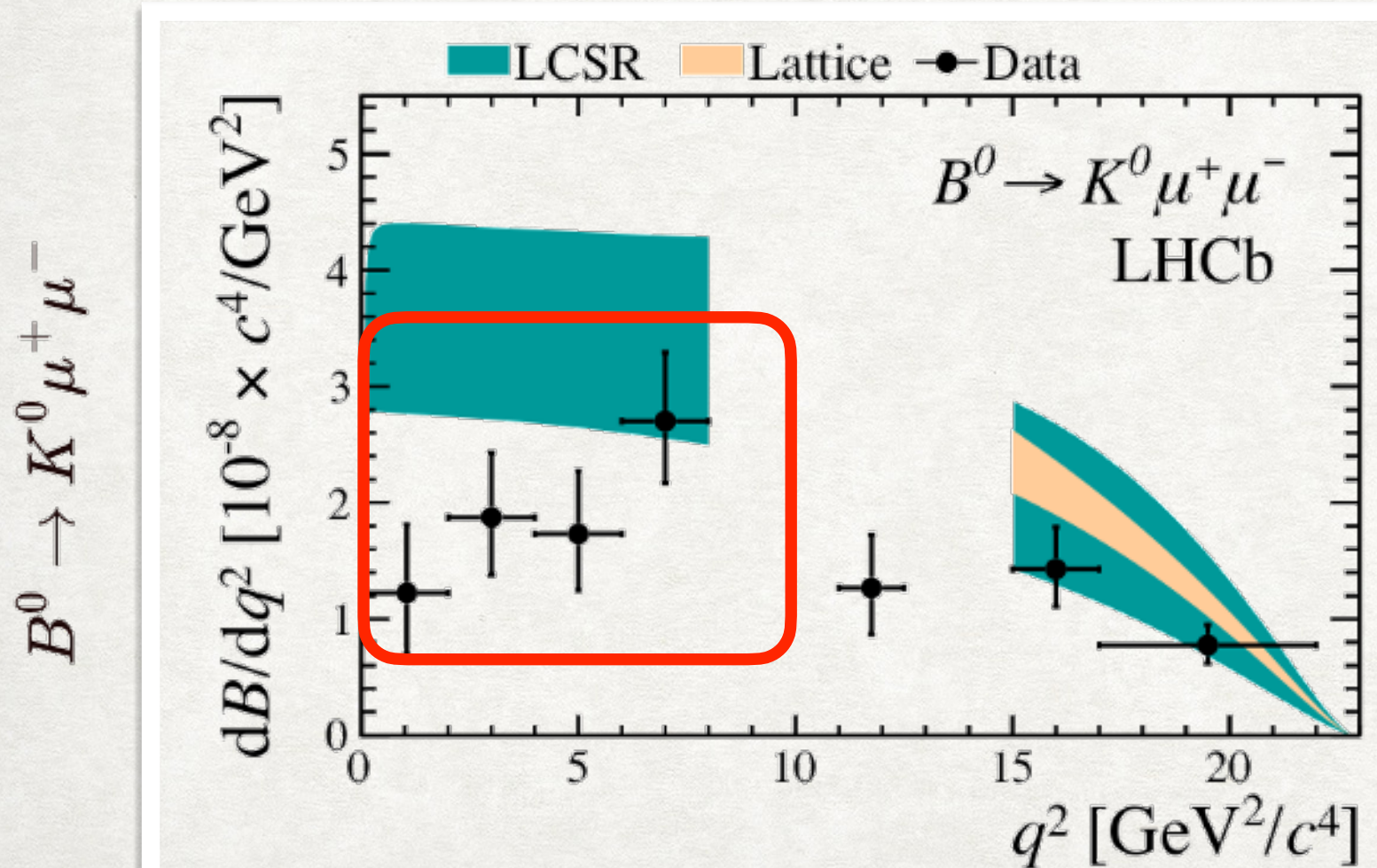
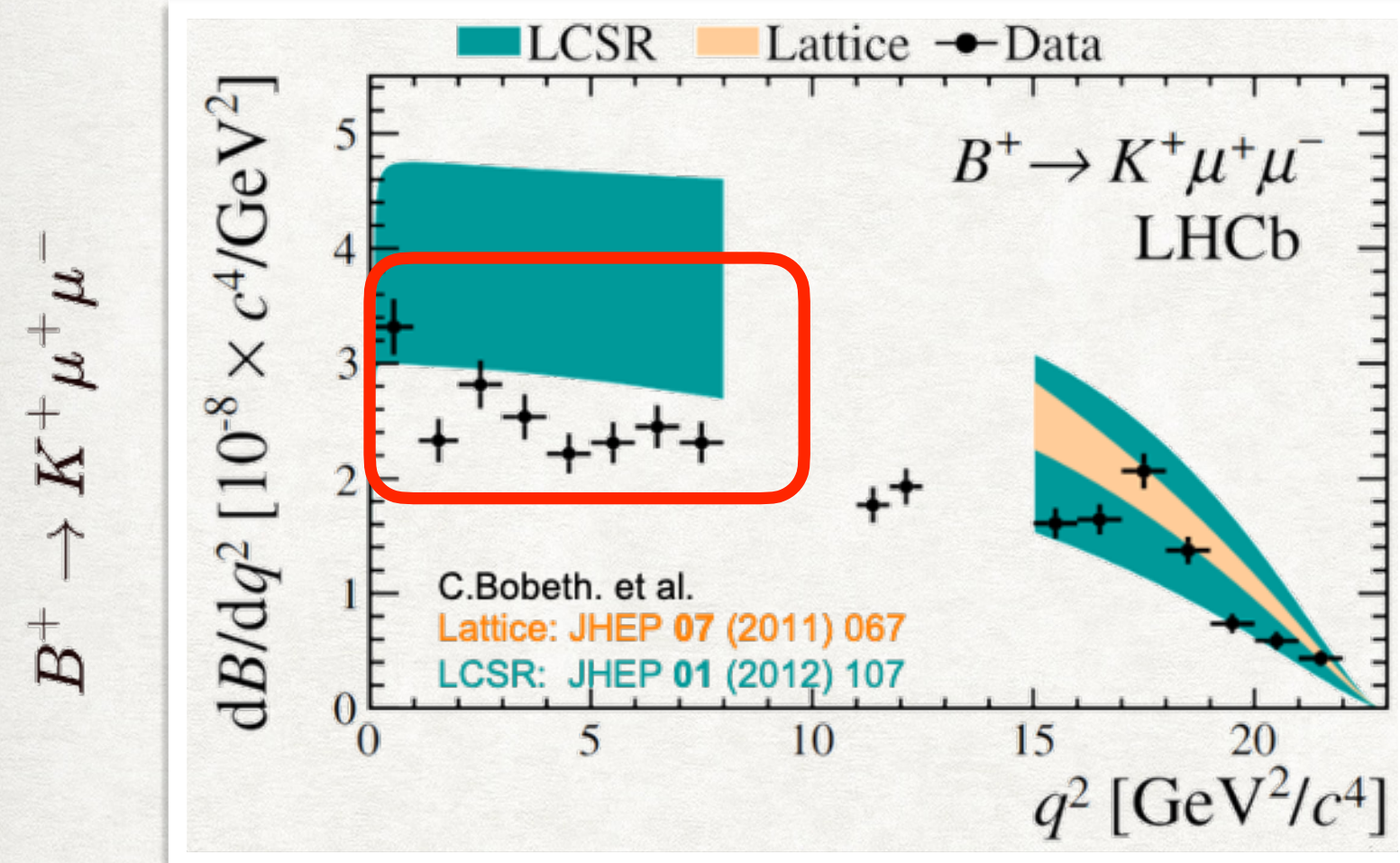
# DATA & PREDICTION: P5'



$P'_5$	$q^2$ [GeV <sup>2</sup> ]	Experimental value	This work	Flavio [49]
	[1.1, 6.0]	$-0.114 \pm 0.068 \pm 0.026$	$-0.406 \pm 0.110$	$-0.447 \pm 0.096$
	[1.1, 2.5]	$0.365 \pm 0.122 \pm 0.013$	$0.208 \pm 0.055$	$0.139 \pm 0.075$
	[2.5, 4.0]	$-0.150 \pm 0.144 \pm 0.032$	$-0.451 \pm 0.126$	$-0.501 \pm 0.102$
	[4.0, 6.0]	$-0.439 \pm 0.111 \pm 0.036$	$-0.752 \pm 0.191$	$-0.759 \pm 0.069$

Observable	$q^2$ (GeV <sup>2</sup> )	Experimental value	This work	Flavio [49]
$P'_4$	[1.1, 2.5]	$0.58^{+0.62}_{-0.56} \pm 0.11$	$-0.052 \pm 0.015$	$-0.063 \pm 0.043$
	[2.5, 4.0]	$-0.81^{+1.09}_{-0.84} \pm 0.14$	$-0.371 \pm 0.098$	$-0.391 \pm 0.044$
	[4.0, 6.0]	$-0.79^{+0.47}_{-0.28} \pm 0.09$	$-0.487 \pm 0.120$	$-0.502 \pm 0.027$
	[1.1, 6.0]	$-0.41^{+0.28}_{-0.28} \pm 0.07$	$-0.335 \pm 0.096$	$-0.353 \pm 0.042$
$P'_5$	[1.1, 2.5]	$0.88^{+0.70}_{-0.71} \pm 0.10$	$0.180 \pm 0.050$	$0.113 \pm 0.113$
	[2.5, 4.0]	$-0.87^{+1.00}_{-1.68} \pm 0.09$	$-0.467 \pm 0.125$	$-0.517 \pm 0.098$
	[4.0, 6.0]	$-0.25^{+0.32}_{-0.40} \pm 0.09$	$-0.756 \pm 0.187$	$-0.764 \pm 0.083$
	[1.1, 6.0]	$-0.07^{+0.25}_{-0.25} \pm 0.04$	$-0.421 \pm 0.123$	$-0.461 \pm 0.086$

# DATA & PREDICTION: BR



LHCb  
JHEP 06 (2014) 133 arXiv: 1403.8044v1

Observable	$q^2$ (GeV <sup>2</sup> )	Experimental value	This work	Flavio [49]
LHCb ( $B^+ \rightarrow K^+ \mu^+ \mu^-$ ) [13]				
$10^9 dB/dq^2$	[1.1, 2.0]	$23.3 \pm 1.5 \pm 1.2$	$37.243 \pm 11.219$	$35.256 \pm 6.385$
	[2.0, 3.0]	$28.2 \pm 1.6 \pm 1.4$	$36.911 \pm 11.308$	$35.095 \pm 6.056$
	[3.0, 4.0]	$25.4 \pm 1.5 \pm 1.3$	$36.540 \pm 11.480$	$34.908 \pm 6.329$
	[4.0, 5.0]	$22.1 \pm 1.4 \pm 1.1$	$36.128 \pm 11.715$	$34.689 \pm 5.610$
	[5.0, 6.0]	$23.1 \pm 1.4 \pm 1.2$	$35.664 \pm 11.996$	$34.429 \pm 5.908$
	[1.1, 6.0]	$24.2 \pm 0.7 \pm 1.2$	$36.482 \pm 11.472$	$34.868 \pm 5.777$

LHCb ( $B^0 \rightarrow K^0 \mu^+ \mu^-$ ) [13]				
$10^9 dB/dq^2$	[0.1, 2.0]	$12.2^{+5.9}_{-5.2} \pm 0.6$	$34.658 \pm 10.247$	$32.668 \pm 5.650$
	[2.0, 4.0]	$18.7^{+5.5}_{-4.9} \pm 0.9$	$34.073 \pm 10.450$	$32.448 \pm 6.185$
	[4.0, 6.0]	$17.3^{+5.3}_{-4.8} \pm 0.9$	$33.283 \pm 10.899$	$32.034 \pm 6.330$
	[1.1, 6.0]	$18.7^{+3.5}_{-3.2} \pm 0.9$	$33.842 \pm 10.537$	$32.323 \pm 5.907$