# Semileptonic decay of heavy flavor mesons

### **康现伟** 北京师范大学 Email: xwkang@bnu.edu.cn

Based on PRD2014, EPJC2017, PLB2018, EPJC2018, JHEP2021, PRD2022

at Wuhan, Nov. 26, 2023



### Theoretical tool: relativistic quark model

### Helicity formalism and physical observables

### Introduction

- Extraction of CKM matrix element compared to pure hadronic decay, clean compared to pure leptonic decay, larger Br  $B \rightarrow e v_e$  helicity suppression
- Experimental side, huge data sample Belle, LHCb, BES, STCF

Form factor is crucial, related to understanding of QCD quark model, dispersion relation, sum rule, PQCD

### **Experimental status**

$\frown$	current	planned
$D^+D^-$	$(8.296 \pm 0.031 \pm 0.064) \times 10^6$	$\sim 5\times 10^7$
$D^0 \bar{D}^0$	$(10.597 \pm 0.028 \pm 0.087) \times 10^{6}$	$\sim 6.4 \times 10^7$
$D_s \bar{D}_s$	$\sim 3.3 \times 10^6$	$\sim 2 \times 10^7$

TABLE I. The total numbers of  $D^+D^-$ ,  $D^0\bar{D}^0$ ,  $D_s^+D_s^-$  pairs from BESIII collaboration, where in the data-taking plan the future data samples will be 6 times as large as the current ones. The number of  $D\bar{D}$  pair is from Ref. [27].

$\frown$	Belle	BelleII	
BB	$(7.72 \pm 0.11) \times 10^8$	$\sim 3.9 \times 10^{10}$	
$B_s \bar{B}_s$	$(6.53 \pm 0.66) \times 10^{6}$	$\sim 3.3 \times 10^8$	

TABLE II. The total numbers of  $B\bar{B}$  and  $B_s^+B_s^-$  pairs from Belle collaboration, while BelleII will have the data samples of 50 times as large as Belle by the mid of next decade. The number of  $B\bar{B}$ and  $B_s\bar{B}_s$  pairs for Belle collaboration are from Refs. [15, 16].

### Form factor: general Lorentz structure

$$\mathcal{M}(D_{(s)} \to P(V)\ell\nu_{\ell}) = \frac{G_F}{\sqrt{2}} V_{cq} H^{\mu} L_{\mu},$$
  
where  $L_{\mu} = \bar{\nu}_{\ell} \gamma_{\mu} (1 - \gamma_5)\ell$  and  $H^{\mu} = \langle P(V) | \bar{q} \gamma_{\mu} (1 - \gamma_5)c | D_{(s)} \rangle$ 

• For  $D_{(s)}$  transitions to pseudoscalar P  $(\pi, K, \eta, \eta')$  mesons

$$\langle P(p_P) | \bar{q} \gamma^{\mu} c | D_{(s)}(p_{D_{(s)}}) \rangle = f_+(q^2) \left[ p_{D_{(s)}}^{\mu} + p_P^{\mu} - \frac{M_{D_{(s)}}^2 - M_P^2}{q^2} q^{\mu} \right] + f_0(q^2) \frac{M_{D_{(s)}}^2 - M_P^2}{q^2} q^{\mu},$$

$$\langle P(p_P) | \bar{q} \gamma^{\mu} \gamma_5 c | D_{(s)}(p_{D_{(s)}}) \rangle = 0, \quad \longleftarrow \quad \text{Parity conservation}$$

$$(16)$$

• For  $D_{(s)}$  transitions to vector V  $(\rho, \omega, K^*, \phi)$  mesons

$$\langle V(p_V) | \bar{q} \gamma^{\mu} c | D_{(s)}(p_{D_{(s)}}) \rangle = \frac{2iV(q^2)}{M_{D_{(s)}} + M_V} \epsilon^{\mu\nu\rho\sigma} \epsilon^*_{\nu} p_{D_{(s)}\rho} p_{V\sigma},$$

$$\langle V(p_V) | \bar{q} \gamma^{\mu} \gamma_5 c | D_{(s)}(p_{D_{(s)}}) \rangle = 2M_V A_0(q^2) \frac{\epsilon^* \cdot q}{q^2} q^{\mu} + (M_{D_{(s)}} + M_V) A_1(q^2) \left(\epsilon^{*\mu} - \frac{\epsilon^* \cdot q}{q^2} q^{\mu}\right)$$

$$-A_2(q^2) \frac{\epsilon^* \cdot q}{M_{D_{(s)}} + M_V} \left[ p_{D_{(s)}}^{\mu} + p_V^{\mu} - \frac{M_{D_{(s)}}^2 - M_V^2}{q^2} q^{\mu} \right].$$
(17)

- all the dynamic information is contained in the form factor. Calculation of form factor is a central task of theorists.
- No full description in QCD theory: various models, typically a limited range of applicability, and a combination of them give a better picture of underline physics

# Calculated in **a typically limited range**, extrapolate to further assuming an asymptotic behavior:

Heavy meson ChPT, large  $q^2$  region, due to soft pion ; QCD light cone sum rule for small  $q^2$  region for B-> $\pi$ 

But there exits models that enable predicting the form factor in the whole kinematic region: <u>relativistic quark model (RQM)</u> <u>introduced below</u>.

## Relativistic Quark Model (RQM)

# developed by Ebet, Faustov, Galkin, e.g., refers to 1705.07741, my recent collaborator

wave function  $\Psi_{\Lambda_Q}$ , which satisfy the relativistic quasipotential equation of the Schrödinger type [8]

$$\left(\frac{b^2(M)}{2\mu_R} - \frac{\mathbf{p}^2}{2\mu_R}\right)\Psi_{\Lambda_Q}(\mathbf{p}) = \int \frac{d^3q}{(2\pi)^3} V(\mathbf{p}, \mathbf{q}; M)\Psi_{\Lambda_Q}(\mathbf{q}),\tag{1}$$

where the relativistic reduced mass and and the center-of-mass system relative momentum squared on the mass shell are given by

$$\mu_R = \frac{M_{\Lambda_Q}^4 - (m_Q^2 - m_d^2)^2}{4M_{\Lambda_Q}^3},$$
$$b^2(M) = \frac{[M_{\Lambda_Q}^2 - (m_Q + m_d)^2][M_{\Lambda_Q}^2 - (m_Q - m_d)^2]}{4M_{\Lambda_Q}^2}.$$

Based on quasipotential approach, 4 dimension reduced to 3 dimension
 Wave function is solvable, not just assume a Gaussian type function

#### Relativistic effects: (1) negative-energy part of the propagator



FIG. 1: Lowest order vertex function  $\Gamma^{(1)}$  contributing to the current matrix element.



FIG. 2: Vertex function  $\Gamma^{(2)}$  taking the quark interaction into account. Dashed lines correspond to the effective quark-diquark quasipotential  $\mathcal{V}_1$  Bold lines denote the negative-energy part of the quark propagator.

#### Relativistic effects: (2) wave functions boosted

 $\Psi_{\Lambda \mathbf{P}}(\mathbf{p}) = D_q^{1/2}(R_{L_{\mathbf{P}}}^W) D_d(R_{L_{\mathbf{P}}}^W) \Psi_{\Lambda \mathbf{0}}(\mathbf{p}),$ 

where  $\Psi_{\Lambda 0}$  is the baryon wave function in the rest frame,  $R^W$  is the Wigner rotation,  $L_{\mathbf{P}}$  is the Lorentz boost from the baryon rest frame to a moving one with momentum  $\mathbf{P}$ , and  $D_q^{1/2}(R^W)$  is the rotation matrix of the quark spin [16], while the rotation matrix for the scalar diquark spin  $D_d(R^W) = 1$ .

# Expression for form factor: overlap between initial and final state wave functions

$$\begin{split} \langle \Lambda(P) | J_{\mu}^{W} | \Lambda_{b}(Q) \rangle &= \int \frac{d^{3}p \, d^{3}q}{(2\pi)^{6}} \bar{\Psi}_{\Lambda \mathbf{P}}(\mathbf{p}) \Gamma_{\mu}(\mathbf{p}, \mathbf{q}) \Psi_{\Lambda_{b} \mathbf{Q}}(\mathbf{q}), \\ f_{1}^{TV(1)}(q^{2}) &= -\int \frac{d^{3}p}{(2\pi)^{3}} \bar{\Psi}_{F}\left(\mathbf{p} + \frac{2\epsilon_{d}}{E_{F} + M_{F}} \Delta\right) \sqrt{\frac{\epsilon_{Q}(p) + m_{Q}}{2\epsilon_{Q}(p)}} \sqrt{\frac{\epsilon_{q}(p + \Delta) + m_{q}}{2\epsilon_{q}(p + \Delta)}} \\ &\times \left\{ \frac{\epsilon_{d}}{E_{F} + M_{F}} \left[ \frac{M_{F}}{\epsilon_{q}(p + \Delta) + m_{q}} + \frac{M_{I}}{\epsilon_{Q}(p) + m_{Q}} + \frac{(M_{I} + M_{F})\epsilon_{d}}{(\epsilon_{q}(p + \Delta) + m_{q})(\epsilon_{Q}(p) + m_{Q})} \frac{E_{F} - M_{F}}{E_{F} + M_{F}} \right] \right. \\ &+ \frac{\mathbf{p}\Delta}{\Delta^{2}} \left[ \frac{M_{F}}{\epsilon_{q}(p + \Delta) + m_{q}} - \frac{M_{I}}{\epsilon_{Q}(p) + m_{Q}} \right] \\ &- \frac{1}{3} \frac{M_{I} + M_{F}}{E_{F} + M_{F}} \frac{\mathbf{p}^{2}}{(\epsilon_{q}(p + \Delta) + m_{q})(\epsilon_{Q}(p) + m_{Q})} \right\} \Psi_{I}(\mathbf{p}); \end{split}$$

 $\Delta = \mathbf{P} - \mathbf{Q}; \ \epsilon(p) = \sqrt{m^2 + \mathbf{p}^2}$   $M_I, M_F$  mass of initial and final meson

$$|\mathbf{\Delta}| = \sqrt{\frac{(M_I^2 + M_F^2 - q^2)^2}{4M_I^2} - M_F^2},$$

in the rest frame of mother particle

As it should be, the form factor depends only on  $q^2$ 

11

1. form factor are calculated in the framework of quarsipotential approach

2. systematic account of the relativistic effects including transformation of the meson wave function from the rest to moving reference frame and contributions of the intermediate negativeenergy states.

3. meson wave functions are taken from previous studies of meson spectroscopy. Parameters have been fixed.

4. calculated in the whole range of the transferred momentum q<sup>2</sup>

#### Semileptonic decays of D and $D_s$ mesons in the relativistic quark model

R. N. Faustov<sup>\*</sup> and V. O. Galkin<sup>®†</sup>

Institute of Cybernetics and Informatics in Education, FRC CSC RAS, Vavilov Street 40, 119333 Moscow, Russia

Xian-Wei Kang<sup>‡</sup>

College of Nuclear Science and Technology, Beijing Normal University, Beijing 100875, China

#### Relativistic description of the semileptonic decays of bottom mesons

R. N. Faustov<sup>®</sup>,<sup>1,\*</sup> V. O. Galkin<sup>®</sup>,<sup>1,†</sup> and Xian-Wei Kang<sup>2,3,‡</sup>

<sup>1</sup>Federal Research Center "Computer Science and Control", Russian Academy of Sciences, Vavilov Street 40, 119333 Moscow, Russia
<sup>2</sup>Key Laboratory of Beam Technology of the Ministry of Education, College of Nuclear Science and Technology, Beijing Normal University, Beijing 100875, China
<sup>3</sup>Institute of Radiation Technology, Beijing Academy of Science and Technology, Beijing 100875, China

#### A full calculation without the heavy quark approximation.

Decay	Form factor	F(0)	$F(q_{\max}^2)$	$\sigma_1$	$\sigma_2$
$D \to K$	$f_+$	0.716	1.538	0.902	1.07
	$f_0$	0.716	1.086	0.360	1.657
$D \to K^*$	V	0.927	1.305	0.356	-0.490
	$A_0$	0.655	1.048	0.432	-0.840
	$A_1$	0.608	0.660	0.410	0.166
	$A_2$	0.520	0.623	0.582	-0.917

TABLE I: Form factors of the weak D meson transitions.

double-pole form:

$$F(q^2) = \frac{F(0)}{\left(1 - \sigma_1 \frac{q^2}{M_{D_{(s)}^*}^2} + \sigma_2 \frac{q^4}{M_{D_{(s)}^*}^4}\right)},$$



14

Comparison between CLFQM and RQM: work in the same way for heavy to heavy transition, but differ for heavy to light transition, which should be due to the different treatment of relativistic effects.



FIG. 2: Same as in Fig. 1, but for the form factors of the weak  $B_s \to K$  transitions. For the orange dashed lines, the upper one below  $q^2 < 15 \text{ GeV}^2$  corresponds to  $f_+(q^2)$ , and the lower one  $f_0(q^2)$ . HPQCD, MILC and UKQCD data are from Refs. [29], [36] and [32], respectively.



FIG. 4: Differential branching fractions of the semileptonic  $B \rightarrow \pi \tau \nu_{\tau}$  decay. Comparison of theoretical predictions (RQM – solid blue lines, CLFQM – orange dashed lines).

# Helicity formalism

- To conveniently express observables, otherwise may be cumbersome.
- Conveniently work in the partial-wave basis
- The polarization observables are clearly identified.
- Often used in the experimental analysis (partial wave analysis)

#### Virtual W boson has 4 polarization components

orthonormality property

$$\epsilon^{\dagger}_{\mu}(\lambda_W)\epsilon^{\mu}(\lambda'_W) = g_{\lambda_W\lambda'_W}, \quad (\lambda_W, \lambda'_W = t, \pm, 0)$$
(7)

and satisfy the completeness relation

$$\epsilon_{\mu}(\lambda_{W})\epsilon_{\nu}^{\dagger}(\lambda_{W}')g_{\lambda_{W}\lambda_{W}'} = g_{\mu\nu}.$$
(8)

We can rewrite the contraction of leptonic and hadronic tensors by using the orthonormality and completeness relations as

$$L^{\mu\nu}H_{\mu\nu} = L_{\mu'\nu'}g^{\mu'\mu}g^{\nu'\nu}H_{\mu\nu}$$
  
=  $L_{\mu'\nu'}\epsilon^{\mu'}(\lambda_W)\epsilon^{\dagger\mu}(\lambda_W'')g_{\lambda_W\lambda_W''}\epsilon^{\dagger\nu'}(\lambda_W')\epsilon^{\nu}(\lambda_W'')g_{\lambda_W'\lambda_W''}H_{\mu\nu}$  (9)  
=  $L\left(\lambda_W,\lambda_W'\right)g_{\lambda_W\lambda_W''}g_{\lambda_W'\lambda_W''}H\left(\lambda_W''\lambda_W'''\right),$ 

where  $L(\lambda_W, \lambda'_W)$  and  $H(\lambda_W, \lambda'_W)$  are the leptonic and hadronic tensors in the helicity-component space:

$$L\left(\lambda_W, \lambda'_W\right) = \epsilon^{\mu}(\lambda_W)\epsilon^{\dagger\nu}(\lambda'_W)L_{\mu\nu}, \quad H\left(\lambda_W, \lambda'_W\right) = \epsilon^{\dagger\mu}(\lambda_W)\epsilon^{\nu}(\lambda'_W)H_{\mu\nu}.$$
 (10)

#### Calculations of hadronic current and leptonic current are <sup>18</sup> performed in their respective frames!

 $D \rightarrow P$  transition, we obtain

$$H_t = \frac{1}{\sqrt{q^2}} (m_1^2 - m_2^2) F_0(q^2),$$
  

$$H_{\pm} = 0,$$
  

$$H_0 = \frac{2m_1 |\vec{p}_2|}{\sqrt{q^2}} F_1(q^2).$$

the transition  $D \to V l^+ \nu_l$ :

$$\begin{aligned} H_t &\equiv \epsilon^{\dagger \mu}(t) \epsilon_2^{\dagger \nu}(0) T_{\mu \nu} = -\frac{2m_1 |\vec{p}_2|}{\sqrt{q^2}} A_0(q^2), \\ H_{\pm} &\equiv \epsilon^{\dagger \mu}(\pm) \epsilon_2^{\dagger \nu}(\pm) T_{\mu \nu} = -(m_1 + m_2) A_1(q^2) \pm \frac{2m_1 |\vec{p}_2|}{m_1 + m_2} V(q^2), \\ H_0 &\equiv \epsilon^{\dagger \mu}(0) \epsilon_2^{\dagger \nu}(0) T_{\mu \nu} = -\frac{m_1 + m_2}{2m_2 \sqrt{q^2}} \left( m_1^2 - m_2^2 - q^2 \right) A_1(q^2) + \frac{1}{m_1 + m_2} \frac{2m_1^2 |\vec{p}_2|^2}{m_2 \sqrt{q^2}} A_2(q^2). \end{aligned}$$

19

### Observables

#### Differential decay rates

Then, we obtain the twofold differential decay distribution on  $q^2$  and  $\cos \theta$ :

$$\frac{d\Gamma\left(D \to P(V)l^+\nu_l\right)}{dq^2 d\cos\theta} = \frac{G_F^2 |V_{cq}|^2 |\vec{p_2}| q^2 v^2}{32(2\pi)^3 m_1^2} \times \left[ \left(1 + \cos^2\theta\right) \mathcal{H}_U + 2\sin^2\theta \mathcal{H}_L + 2\cos\theta \mathcal{H}_P + 2\delta_l \left(\sin^2\theta \mathcal{H}_U + 2\cos^2\theta \mathcal{H}_L + 2\mathcal{H}_S - 4\cos\theta \mathcal{H}_{SL}\right) \right].$$

Further integrating over  $\cos \theta$ , the differential  $q^2$  distribution will be

$$\frac{d\Gamma\left(D \to P(V)l^+\nu_l\right)}{dq^2} = \frac{G_F^2 |V_{cq}|^2 |\vec{p}_2| q^2 v^2}{12(2\pi)^3 m_1^2} \times \mathcal{H}_{tot}$$

with  $\mathcal{H}_{tot} = \mathcal{H}_U + \mathcal{H}_L + \delta_l \left( \mathcal{H}_U + \mathcal{H}_L + 3\mathcal{H}_S \right).$ 



FIG. 4: The differential decay rate for the decays  $D \to Ke^+\nu_e$  and  $D \to \pi e^+\nu_e$ . The solid line indicates our central values and the band indicates the estimated uncertainty. We have used the experimental data from BES III for neutral  $D^0$  [83] (red dots with error bars) and charged  $D^+$  [50] (green dots with error bars), BaBar [84, 85] (blue dots and error bars) and CLEO [86] for neutral  $D^0$  (orange dots and error bars) and charged  $D^+$  (brown dots with error bars).

Channel	$D \to \pi$	$D\to \bar{K}$	$D \to \eta$	$D  ightarrow \eta'$	$D_s \to K$	$D_s \rightarrow \eta$	$D_s \to \eta'$
Theory $(10^{-2})$	$0.41\pm0.03$	$10.32\pm0.93$	$0.12\pm0.01$	$0.018 \pm 0.002$	$0.27\pm0.02$	$2.26\pm0.21$	$0.89\pm0.09$
PDG $(10^{-2})$	$0.41\pm0.02$	$8.82\pm0.13$	$0.11\pm0.01$	$0.022\pm0.005$	$0.39\pm0.09$	$2.29\pm0.19$	$0.74\pm0.14$
Channel	$D \to \rho$	$D \to \omega$	$D\to \bar{K}^*$	$D_s \to K^*$	$D_s \rightarrow \phi$		
Theory $(10^{-2})$	$0.23\pm0.02$	$0.21\pm0.02$	$7.5\pm0.7$	$0.19\pm0.02$	$3.1\pm0.3$		
PDG $(10^{-2})$	$0.22\substack{+0.02\\-0.03}$	$0.17\pm0.01$	$5.40\pm0.10$	$0.18\pm0.04$	$2.39\pm0.23$		
Channel	$D \rightarrow a_0(1450)$	$D \rightarrow f_0(1500)$	$D \rightarrow f_0(1710)$	$D \to K_0^*(1450)$	$D_s \rightarrow K_0^*(1450)$	$D_s \rightarrow f_0(1500)$	$D_s \rightarrow f_0(1710)$
Theory $(10^{-5})$	$0.54\pm0.05$	$0.11\pm0.02$	$(4.7\pm0.8)\cdot10^{-4}$	$29\pm3$	$2.7\pm0.2$	$15\pm3$	$0.034 \pm 0.006$
Channel	$D \rightarrow f_1(1285)$	$D \rightarrow f_1(1420)$	$D \rightarrow b_1(1235)$	$D \rightarrow h_1(1170)$	$D \rightarrow h_1(1380)$	$D_s \rightarrow h_1(1170)$	$D_s \rightarrow h_1(1380)$
Theory $(10^{-5})$	$3.7\pm0.8$	$\{0.02,  0.14\}$	$7.4\pm0.7$	$14\pm1.5$	$\{0, 0.02\}$	$\{0, 19.7\}$	$64\pm7$

Table 1	$\frown$			
Channel	$D \rightarrow K_1(1270)$	$D \rightarrow K_1(1400)$	$D_s \rightarrow K_1(1270)$	$D_s \rightarrow K_1(1400)$
Theory $(10^{-5})$	$320 \pm 40$	{0.5, 2.0}	$17\pm2$	{0.05, 0.14}

Confirmed by the recent measurements by BESIII, refers to PRL 123 (2019) 231801, 1907.11370

$$\begin{aligned} \mathcal{A}_{FB}^{l}(q^{2}) &= \frac{\int_{0}^{1} d\cos\theta \frac{d\Gamma}{dq^{2}d\cos\theta} - \int_{-1}^{0} d\cos\theta \frac{d\Gamma}{dq^{2}d\cos\theta}}{\int_{0}^{1} d\cos\theta \frac{d\Gamma}{dq^{2}d\cos\theta} + \int_{-1}^{0} d\cos\theta \frac{d\Gamma}{dq^{2}d\cos\theta}} \\ &= \frac{3}{4} \frac{H_{P} - 4\delta_{l}H_{SL}}{H_{tot}}. \end{aligned}$$

• Forward-backward asymmetry, lepton polarization, and convexity parameters for semileptonic decays of  $\bar{B}^0 \rightarrow D^+ l^- \bar{\nu}_l$  and  $\bar{B}^0 \rightarrow D^{*+} l^- \bar{\nu}_l$ 

		$\langle \mathcal{A}^e_{FB}  angle$	$\langle {\cal A}^{ au}_{FB}  angle$	$\langle P^e_L\rangle$	$\langle P_L^\tau \rangle$	$\langle P_T^e \rangle$	$\langle P_T^\tau \rangle$	$\left< C_F^e \right>$	$\left< C_F^\tau \right>$
$\bar{B}^0 \to D^+ l^- \bar{\nu}_l$	CLFQM	$-1.04\times10^{-6}$	-0.36	-1	0.32	$1.06\times 10^{-3}$	0.84	-1.5	-0.27
	CCQM	$-1.17\times10^{-6}$	-0.36	-1	0.33		0.84	-1.5	-0.26
$\bar{B}^0 \to D^{*+} l^- \bar{\nu}_l$	CLFQM	0.22	0.054	-1	-0.51	$0.46  imes 10^{-3}$	0.47	-0.42	-0.056
	CCQM	0.19	0.027	-1	-0.50		0.46	-0.47	-0.062

the longitudinal polarization vector:

$$s_L^{\mu} = \frac{1}{m_l} \left( |\vec{k}_1|, \ E_1 \sin \theta, \ 0, \ E_1 \cos \theta \right)$$

Polarized differential decay rate

$$\begin{aligned} \frac{d\Gamma(s_L)}{dq^2} &= \frac{G_F^2 |V_{cq}|^2 |\vec{p}_2| q^2 v^2}{12(2\pi)^3 m_1^2} \left[ -3\delta_l |H_t|^2 + (1-\delta_l) \left( |H_+|^2 + |H_-|^2 + |H_0|^2 \right) \right] \\ &= \frac{G_F^2 |V_{cq}|^2 |\vec{p}_2| q^2 v^2}{12(2\pi)^3 m_1^2} \left[ \mathcal{H}_U + \mathcal{H}_L - \delta_l \left( \mathcal{H}_U + \mathcal{H}_L + 3\mathcal{H}_S \right) \right]. \end{aligned}$$

Longitudinal polarization of lepton

$$P_L^l(q^2) = \frac{\mathcal{H}_U + \mathcal{H}_L - \delta_l \left(\mathcal{H}_U + \mathcal{H}_L + 3\mathcal{H}_S\right)}{\mathcal{H}_{tot}}$$

Longitudinal polarization of vector meson 🚽 🛶

$$F_L^l(q^2) = \frac{d\Gamma(\lambda_V = 0)/dq^2}{d\Gamma/dq^2} = \frac{(1+\delta_l)\mathcal{H}_L + 3\delta_l\mathcal{H}_S}{\mathcal{H}_{tot}},$$
 24

# Polarization observables are very sensitive to different New Physics models.

# Branching ratio is not the whole landscape, and we need more observables both in theory and experiment

TABLE X: Our predictions for  $F_L^{\tau}(D_{(s)}^*)$  and  $P_L^{\tau}(D_{(s)}^{(*)})$ , compared with other models as well as experimental values. In parenthesis, we also include the value of  $F_L^e(D^*)$  for  $\bar{B} \to D^* \tau^- \bar{\nu}_{\tau}$ .

Observables	Approach	$\bar{B} \rightarrow D \tau^- \bar{\nu}_{\tau}$	$\bar{B} \to D^* \tau^- \bar{\nu}_\tau \left( e^- \bar{\nu}_e \right)$	$B_s \rightarrow D_s \tau^- \bar{\nu}_{\tau}$	$B_s \to D_s^* \tau^- \bar{\nu}_\tau$
	CLFQM	-	0.451 (0.521)	-	0.453
	SM1 [70]	-	$0.46\pm0.04$	-	-
DT(D*)	SM2 [71]	-	0.455	-	0.433
$F_{L}(D_{(s)})$	PQCD [72]	-	0.43	-	0.43
	Belle [73]	-	$0.60 \pm 0.08 \pm 0.04  (0.56 \pm 0.02)$	-	- 1
	CLFQM	0.32	-0.51	0.33	-0.51
	SM1	$0.325 \pm 0.09  [74]$	$-0.497 \pm 0.013 \; [75]$	-	- 1
$DT(D^{(*)})$	SM2 [71]	0.352	-0.501	-	-0.520
$P_{L}(D_{(s)})$	PQCD [72]	0.30	-0.53	0.30	-0.53
	Belle [76]	-	$-0.38\pm0.51^{+0.21}_{-0.16}$	-	-

#### Forward-backward asymmetry



#### Longitudinal polarization



### **FRONTIERS OF PHYSICS**



# Two-body nonleptonic decays of the heavy mesons in the factorization approach

Shuo-Ying Yu<sup>1,2</sup>, Xian-Wei Kang<sup>1,2,†</sup>, V. O. Galkin<sup>3</sup>

- Key Laboratory of Beam Technology of the Ministry of Education, College of Nuclear Science and Technology, Beijing Normal University, Beijing 100875, China
- 2 Institute of Radiation Technology, Beijing Academy of Science and Technology, Beijing 100875, China
- 3 Federal Research Center "Computer Science and Control", Russian Academy of Sciences, Vavilov Street 40, 119333 Moscow, Russia Corresponding author. E-mail: <sup>†</sup>xwkang@bnu.edu.cn Received March 7, 2023; accepted April 25, 2023

© Higher Education Press 2023

Transition			Theory	Experiment
	RQM	CLFQM	Lattice/SM analysis	[3] PDG [1] HFLAV [40] [3]
$B \rightarrow D$	0.271	0.302	0.298(3)	$0.429(82)(52)(B^+)$ $0.339(26)(14)$ $0.337(30)$
				$0.469(84)(53)(B^0)$
$B \to D^*$	0.231	0.246	0.250(3)	$0.335(34)(B^+)$ $0.295(10)(10)$ $0.298(14)$
				$0.309(16)(B^0)$
$B \to \pi$	0.631	0.680	0.641(16)	1.05(51)
$B\to\rho$	0.561	0.543	0.535(8)	
$B \to \eta$	0.629	0.611		Consistency between theories.
$B  o \eta'$	0.544	0.538		but may be lower than even by
$B\to \omega$	0.566	0.531	0.546(15)	but may be lower than exp by
$B_s \to D_s$	0.287	0.298	0.297(3)	1-3 $\sigma$
$B_s \to D_s^*$	0.244	0.248	0.247(8)	
$B_s \to K$	0.588	0.673		
$B_s \to K^*$	0.553	0.520		
$B_c \to \eta_c$	0.373			
$B_c \to J/\psi$	0.284		0.2582(38)	0.71(17)(18)
$B_c \to D$	0.833			29
$B_c \to D^*$	0.656			

TABLE IX: Ratios of the decay rates with  $\tau$  and  $\mu$  leptons  $\mathcal{R}(F) = \Gamma(B \to F \tau \nu_{\tau}) / \Gamma(B \to F \mu \nu_{\mu})$ in comparison with available lattice or experimental data, cf. Ref. [3] and references therein.

From heavy flavor averaging group. The SM uncertainty is currently subject to debate that HFLAV is following without taking a stance in this.

Experiment	R(D*)	R(D)	Rescaled Correlation (stat/syst/total)
BaBar	0.332 ± 0.024 ± 0.018	0.440 ± 0.058 ± 0.042	-0.45/-0.07/-0.31
BELLE	0.293 ± 0.038 ± 0.015	0.375 ± 0.064 ± 0.026	-0.56/-0.11/-0.50
LHCb	0.336 ± 0.027 ± 0.030	-	-
BELLE	0.270 ± 0.035 <sup>+</sup> 0.028 -0.025	7	-
LHCb	0.280 ± 0.018 ± 0.029	-	-
BELLE	0.283 ± 0.018 ± 0.014	0.307 ± 0.037 ± 0.016	-0.53/-0.51/-0.51
Average .txt	0.295 ± 0.011 ± 0.008	0.340 ± 0.027 ± 0.013	-0.39/-0.34/-0.38

30



# Thank you for your attention