

# Recent Progress in Study of PDFs from CT Global Analysis

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CTEQ

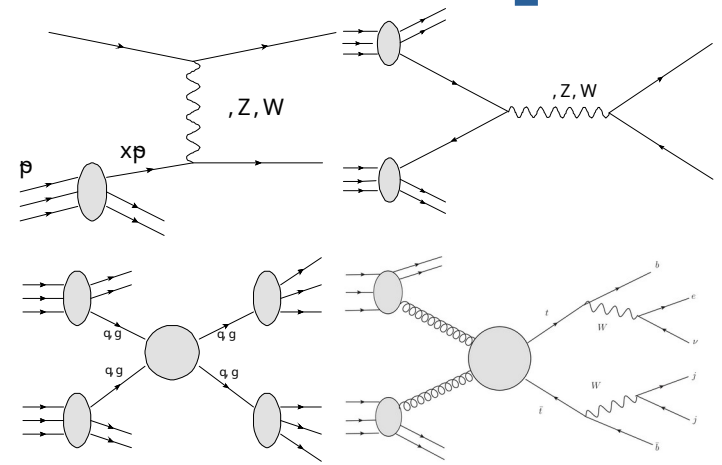
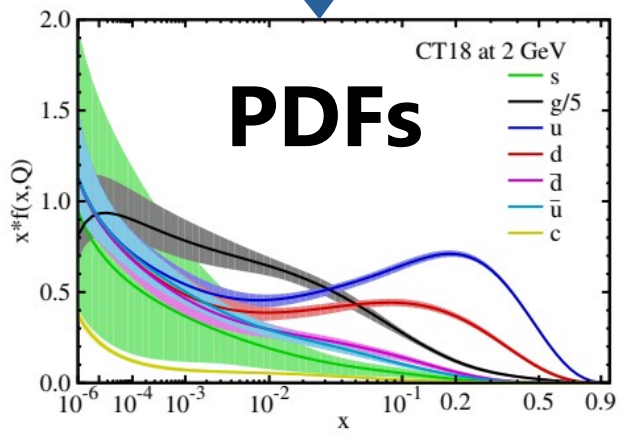
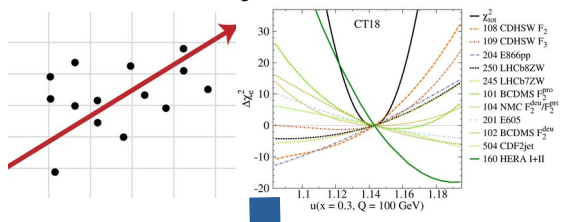
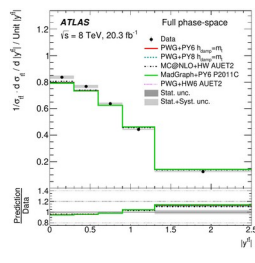
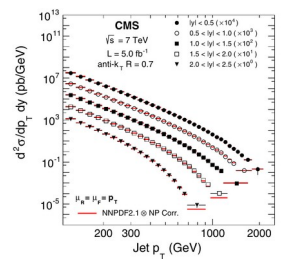
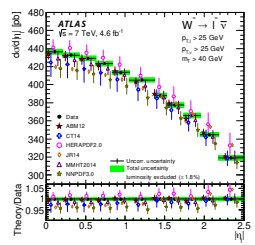
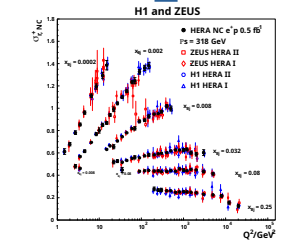
$$\sigma = f_a(x_1, \mu^2) \otimes f_b(x_2, \mu^2) \otimes \hat{\sigma}_{ab}(\mu^2)$$

**Expt. Data**

**Statistic**

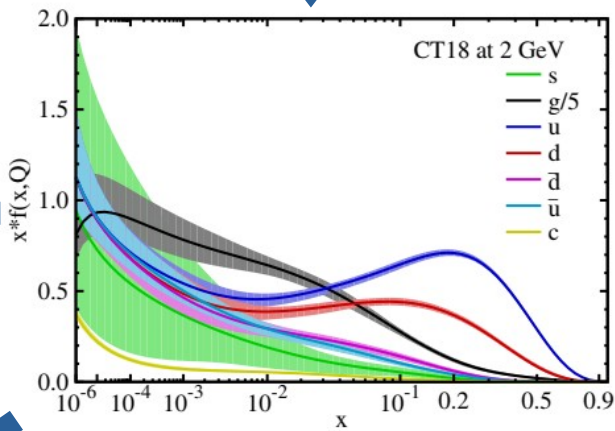
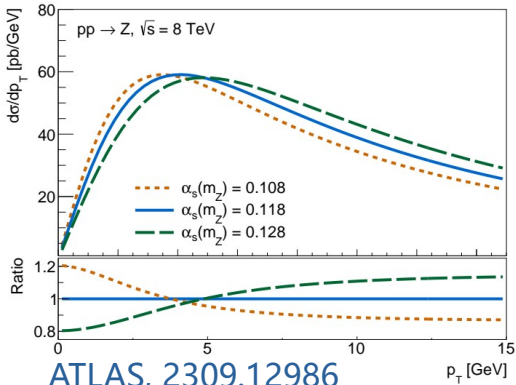
Regression analysis  
Uncertainty Estimation

**Theory**

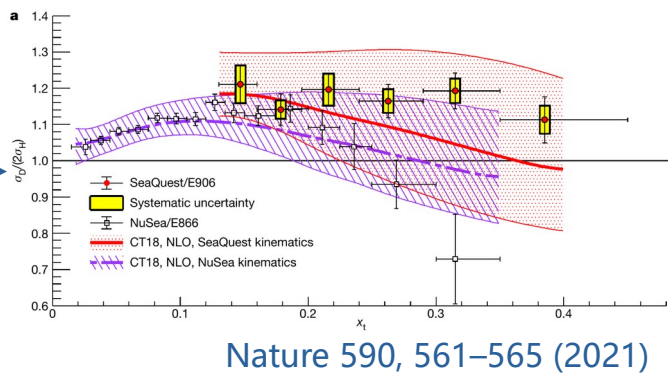


$$\sigma = f_a(x_1, \mu^2) \otimes f_b(x_2, \mu^2) \otimes \hat{\sigma}_{ab}(\mu^2)$$

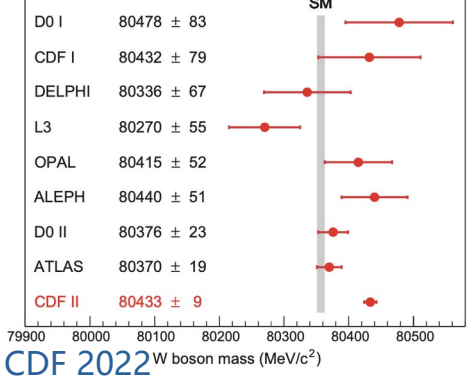
$\alpha_s$



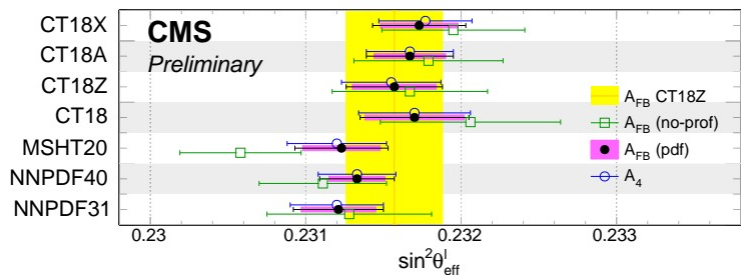
$\sigma_D / (2\sigma_H)$



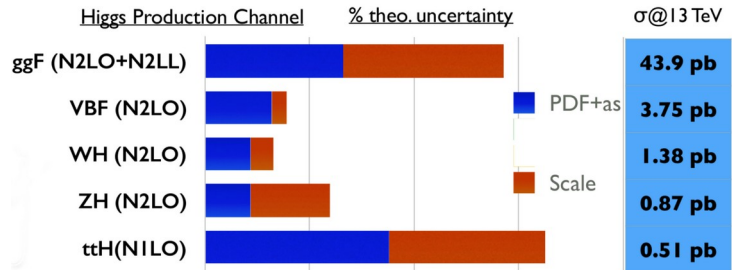
W Boson mass



$\sin^2 \theta_{\text{eff}}^l$



Higgs Production



Lucian, DIS2024

## • RESEARCH PROJECTS AND RESULTS •

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APS  
PHYSICAL REVIEW D  
covering particles, fields, gravitation, and cosmology

Editors' Suggestion

New parton distribution functions from a global analysis of quantum chromodynamics

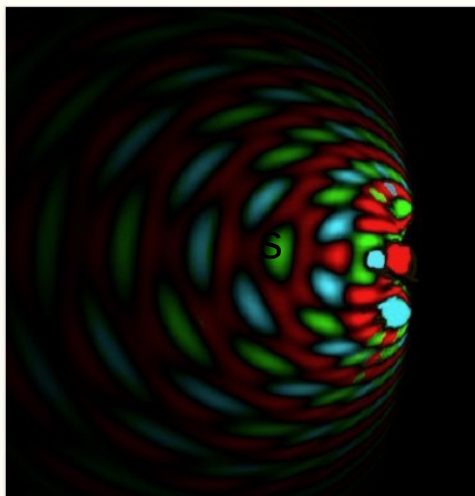
Sayipjamal Dulat, Tie-Jiun Hou, Jun Gao, Marco Guzzi, Joey Huston, Pavel Nadolsky, Jon Pumplin, Carl Schmidt, Daniel Stump, and C.-P. Yuan  
Phys. Rev. D **93**, 033006 – Published 16 February 2016

ABSTRACT

We present new parton distribution functions (PDFs) at next-to-next-to-leading order (NNLO) from the CTEQ-

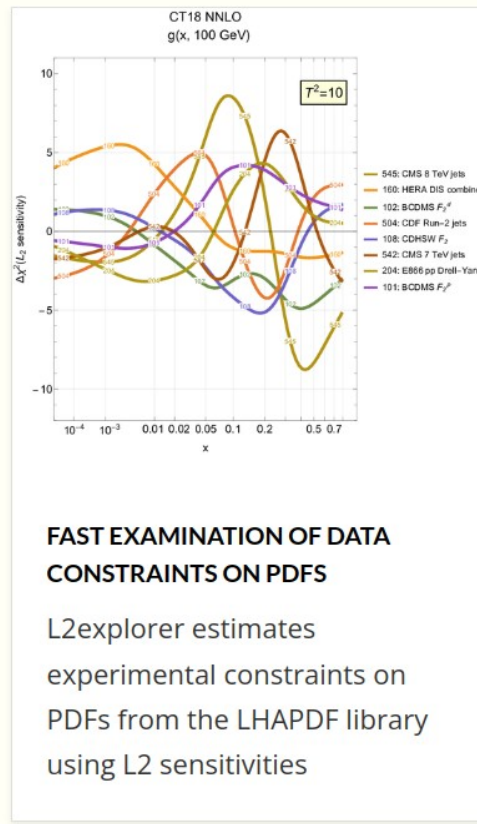
ARTICLES BY CTEQ-TEA AUTHORS

Representative publications of our research group and its collaborators listed in the INSPIRE-HEP database



### CTEQ-TEA PARTON DISTRIBUTION FUNCTIONS

CTEQ-TEA (CT) parametrizations of parton distribution functions in the nucleon



China:  
A. Ablat,  
S. Dulat,  
Y. Fu,  
T.-J. Hou,  
I. Sitiwaldi

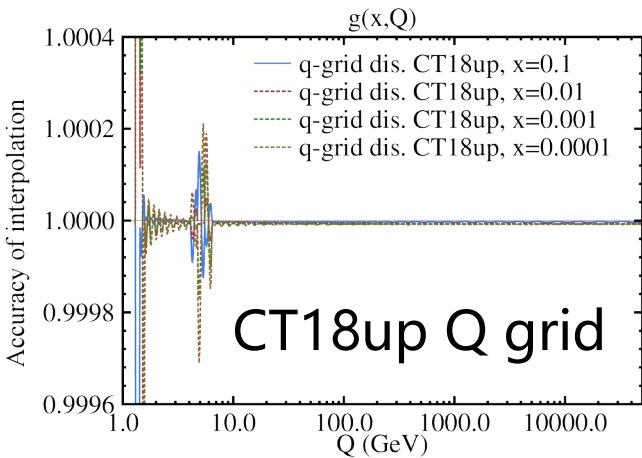
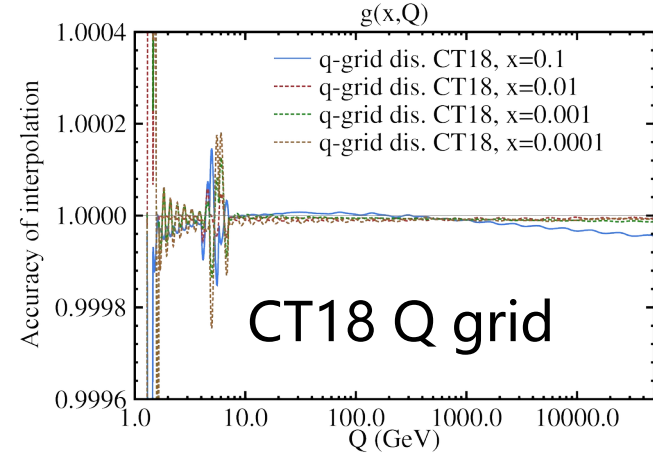
Mexico:  
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USA:  
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T.J. Hobbs,  
J. Huston,  
H.-W. Lin,  
C. Schmidt,  
K. Xie,  
C.-P. Yuan  
and other  
coauthors

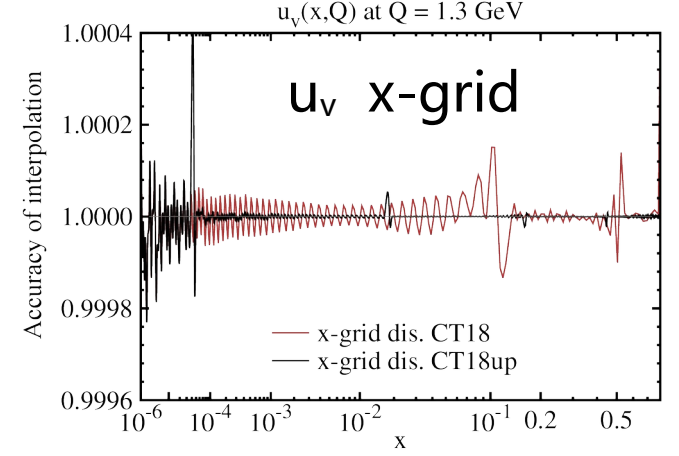
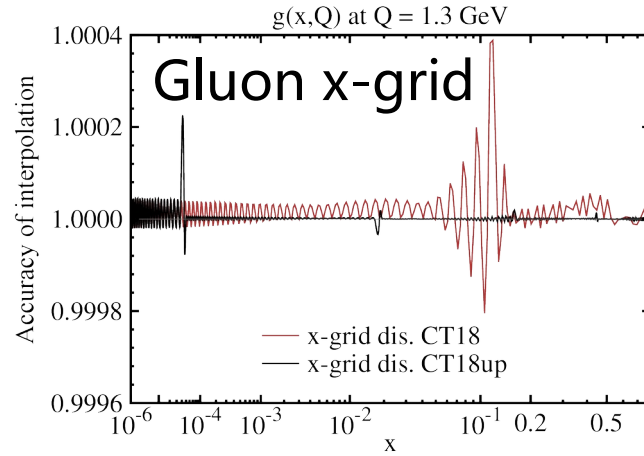
# Toward a new generation of CT PDFs

1. Upgrade of PDF grids
2. Multiple based on preliminary the selections NNLO fits with
  - vector boson [2305.10733]
  - $t\bar{t}$  data [2307.11153]
  - LHC Run-2 (di)jet [work in progress]
3. Work on implementation of N3LO contributions [work in progress]
4. Next-generation PDF uncertainty quantification:
  - Bézier curves [2311.08447]
  - multi-Gaussian approaches [2406.01664]
5. Physics applications
  - QCD+QED PDFs for a neutron [2305.10497]
  - PDF dependence of forward-backward asymmetry [2307.07839]
  - Gluon determination with the help of lattice input [work in progress]

# Upgrade of PDF grids



# Ratio between PDF read from grids and fitting code

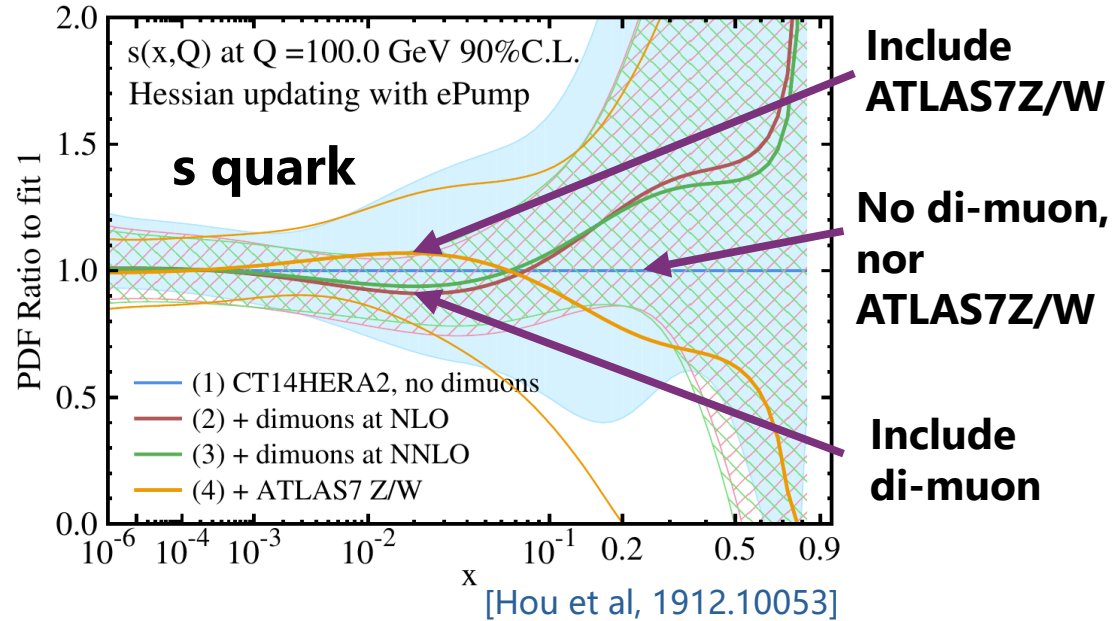
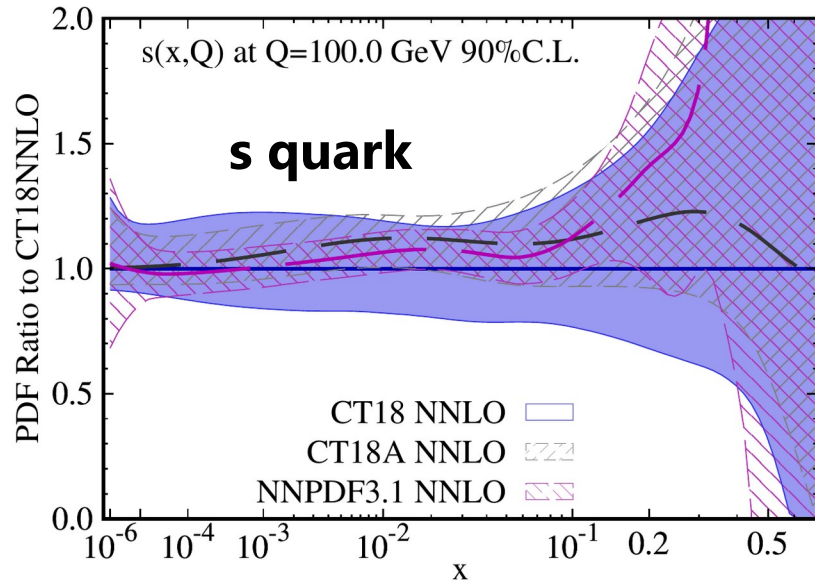


| intervals in x        | CT18 | CT18up | intervals in x | CT18 | CT18up |
|-----------------------|------|--------|----------------|------|--------|
| $[10^{-10}, 10^{-9}]$ | 1    | 1      | $[0.1, 0.2]$   | 7    | 18     |
| $[10^{-9}, 10^{-8}]$  | 11   | 11     | $[0.2, 0.3]$   | 6    | 16     |
| $[10^{-8}, 10^{-7}]$  | 12   | 12     | $[0.3, 0.4]$   | 5    | 12     |
| $[10^{-7}, 10^{-6}]$  | 11   | 11     | $[0.4, 0.5]$   | 3    | 13     |
| $[10^{-6}, 10^{-5}]$  | 12   | 12     | $[0.5, 0.6]$   | 6    | 15     |
| $[10^{-5}, 10^{-4}]$  | 11   | 15     | $[0.6, 0.7]$   | 6    | 12     |
| $[10^{-4}, 10^{-3}]$  | 12   | 23     | $[0.7, 0.8]$   | 8    | 11     |
| $[10^{-3}, 10^{-2}]$  | 11   | 23     | $[0.8, 0.9]$   | 14   | 17     |
| $[10^{-2}, 10^{-1}]$  | 12   | 40     | $[0.9, 1.0]$   | 15   | 38     |
|                       |      |        | Total          | 161  | 300    |

| intervals in Q   | CT18 | CT18up |
|------------------|------|--------|
| $[Q_0, m_c]$     | 2    | 4      |
| $[m_c, m_b]$     | 8    | 11     |
| $[m_b, m_t]$     | 14   | 18     |
| $[m_t, Q_{max}]$ | 13   | 16     |
| Total            | 37   | 49     |

PDFs grid in .pds and LHAPDF format are updated from  $[N_x, N_Q]=[161, 37]$  to  $[300, 49]$  to have better precision

# CT18 Drell-Yan data



- Noticeable tensions between the SIDIS di-muon data and the precision ATLAS 7 TeV Z/W data were found in global analysis.
- Two versions of PDFs: **CT18**(w/o ATLAS 7 Z/W data) and **CT18A**(w/ ATLAS 7 Z/W data) were released

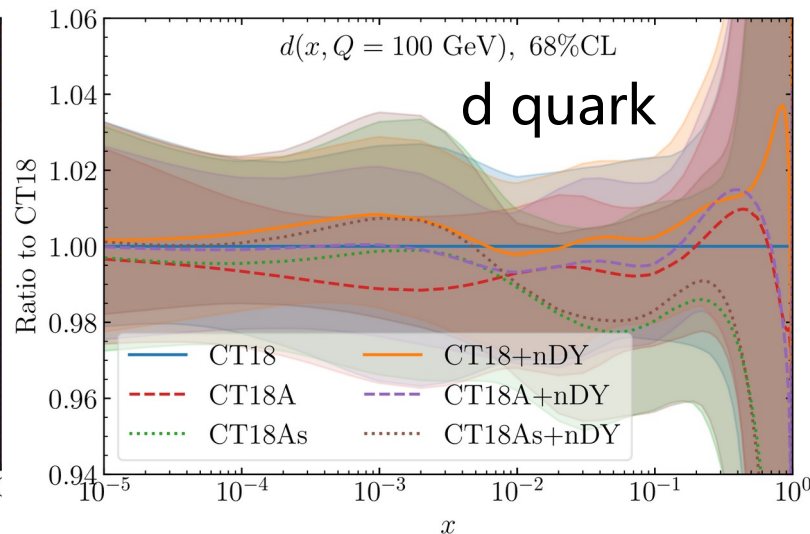
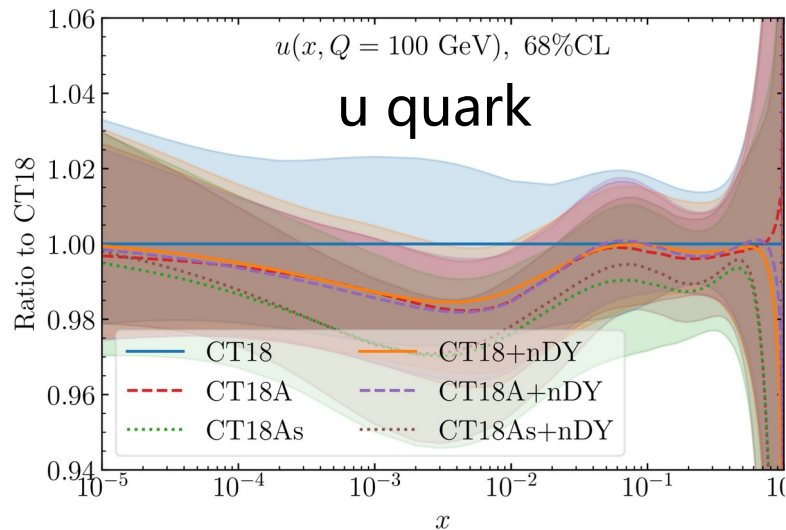
# Post-CT18 LHC Drell-Yan data

| ID  | Exp                | $N_{pt}$ | $\chi^2/N_{pt}$                                      |
|-----|--------------------|----------|--|
| 215 | ATLAS 5.02 TeV W,Z | 27       | $0.82^{+0.55}_{-0.16}$ ( $1.15^{+1.22}_{-0.43}$ )    |
| 211 | ATLAS 8 TeV W      | 22       | $2.42^{+2.49}_{-1.51}$ ( $4.25^{+6.39}_{-3.34}$ )    |
| 214 | ATLAS 8 TeV Z3D    | 188      | $1.12^{+0.46}_{-0.02}$ ( $1.99^{+5.10}_{-1.85}$ )    |
| 212 | CMS 13 TeV Z       | 12       | $2.48^{+4.76}_{-0.88}$ ( $12.03^{+38.04}_{-21.84}$ ) |
| 217 | LHCb 8 TeV W       | 14       | $1.35^{+0.59}_{-0.61}$ ( $1.35^{+0.72}_{-0.64}$ )    |
| 218 | LHCb 13 TeV Z      | 16       | $1.18^{+1.42}_{-0.60}$ ( $1.49^{+1.74}_{-0.89}$ )    |

**CT18:** w/o ATL7ZW

**CT18A:** w/ ATL7ZW

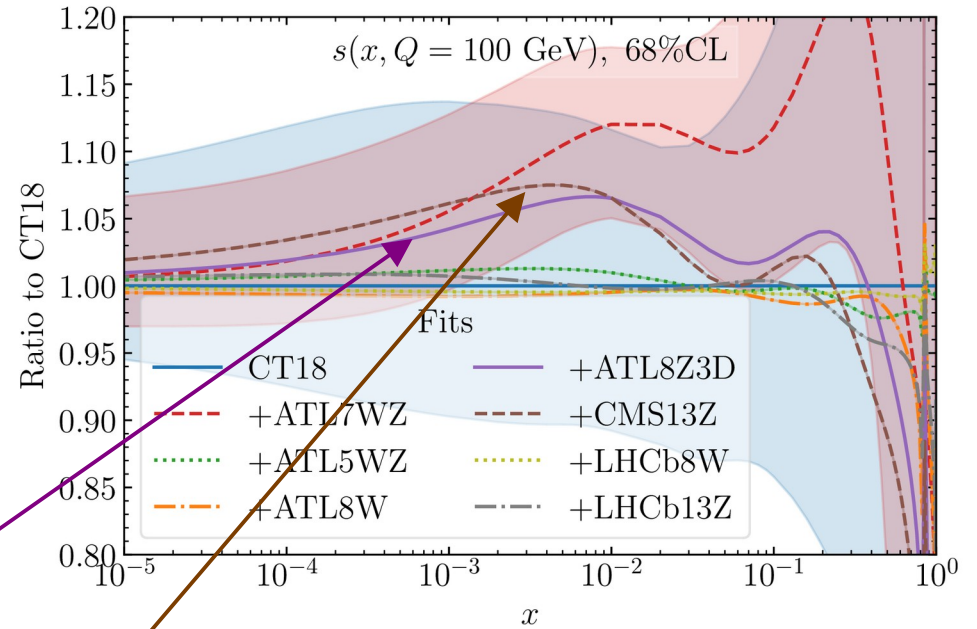
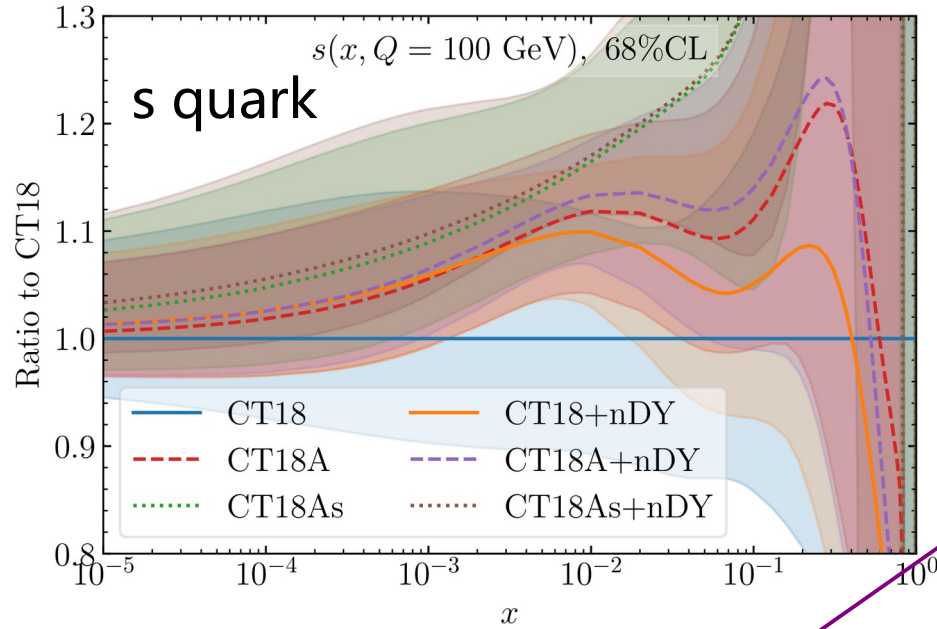
**CT18As:** CT18A w/ s asym.



New DY data drive new fitted PDFs closer to CT18A PDFs rather than CT18 PDFs.



# CT18 or CT18A?



- The new Drell-Yan data **ATL8Z3D** and **CMS13Z** drive the strange PDF closer to CT18A than CT18.
- Mild tension in the strange PDF comes from the ATL8W and LHCb8W data sets.

# LHC 13 TeV $t\bar{t}$ data set

|     |          |            |                                      |
|-----|----------|------------|--------------------------------------|
| 521 | ATL13had | 2006.09274 | ATLAS all-hadronic channel at 13 TeV |
| 528 | CMS13ll  | 1811.06625 | CMS dilepton channel at 13 TeV       |
| 581 | CMS13lj  | 2108.02803 | CMS lepton + jets channel at 13 TeV  |
| 587 | ATL13lj  | 1908.07305 | ATLAS lepton+jets channel at 13 TeV  |

- Distributions  $m_{t\bar{t}}, y_{t\bar{t}}, y_{t\bar{t}}^{Boost} = \frac{1}{2}(y^{t,had} + y^{t,lep})$  and  $H_T^{t\bar{t}} = p_T^{t,had} + P_T^{t,lep}$  are concerned.
- ATL13lj releases two binning: ATL-bin and CMS-bin

| Npts    | $m_{t\bar{t}}$ | $y_{t\bar{t}}$ | $y_{t\bar{t}}^{Boost}$ | $H_T^{t\bar{t}}$ | $p_{T,t}$ | $y_t$ |
|---------|----------------|----------------|------------------------|------------------|-----------|-------|
| ATL bin | 9              | 7              | 9                      | 9                |           |       |
| CMS bin | 7              | 10             |                        |                  | 6         | 10    |

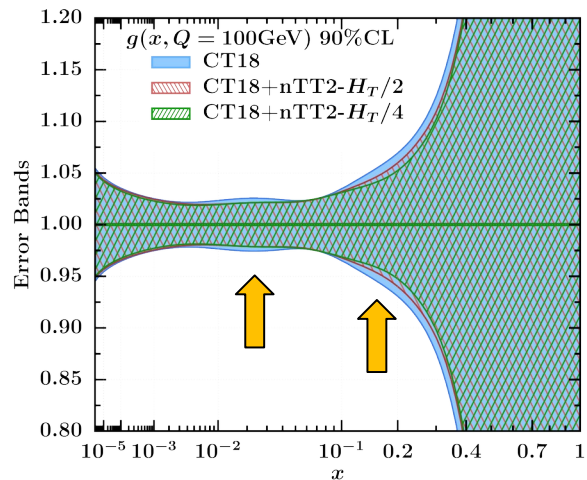
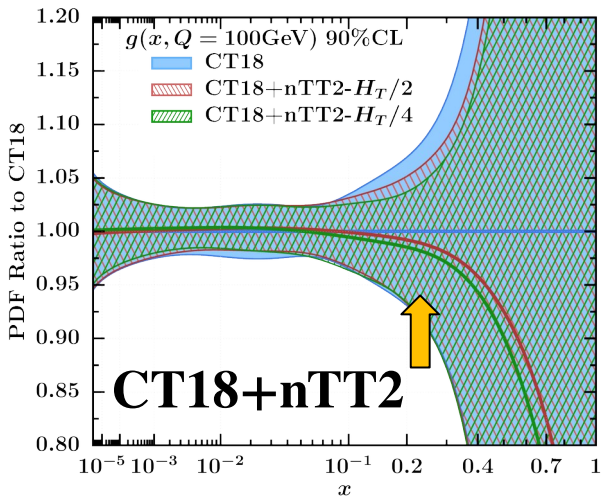
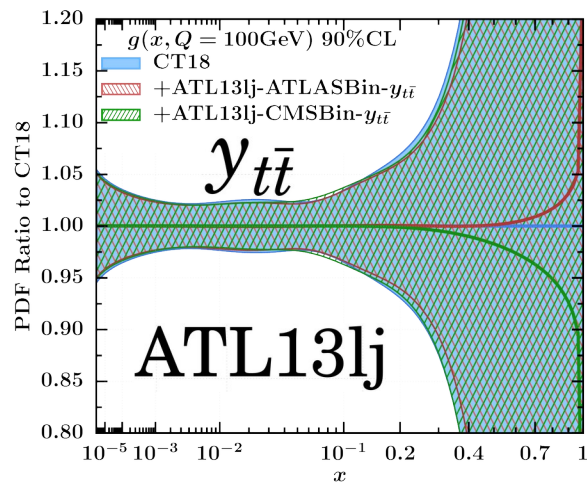
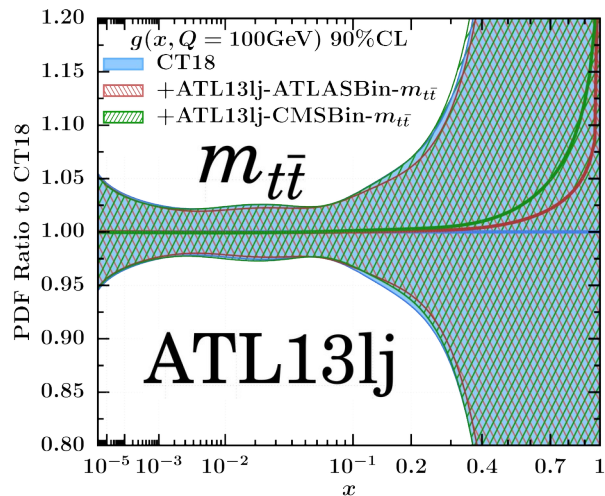
Bin-by-bin statistical correlations are made available for ATL bin.

- NNLO theoretical prediction is done by using MATRIX.

$$\text{NNLO} = \text{NLO}(\text{Applgrid, MCFM 6.8}) \times K \left( \frac{\text{NNLO}(\text{MATRIX})}{\text{NLO}(\text{MCFM 6.8})} \right)$$

- Central-scale choices  $\mu_R = \mu_f = H_T/4$  or  $H_T/2$  are examined.

# LHC 13 TeV $t\bar{t}$ data set: Stronger Impact

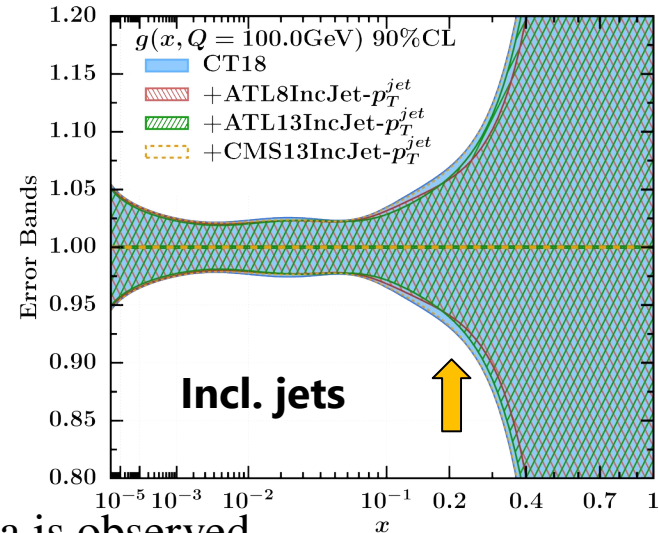
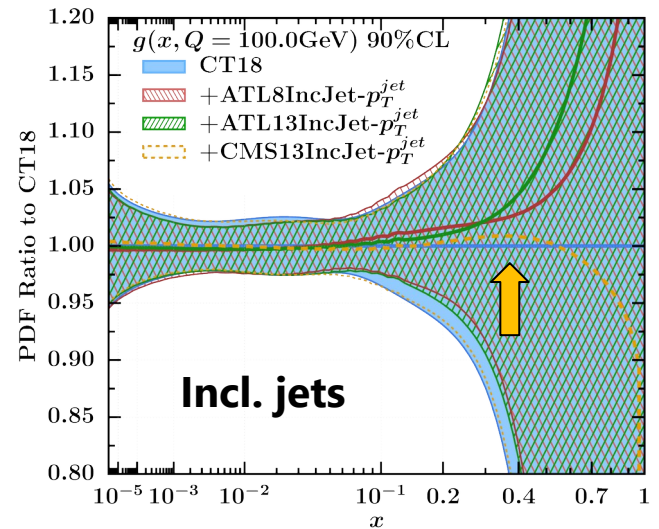


- The ATL13lj data provide minor impact to gluon PDF in large  $x$  region.
- The difference between CMS-bin and ATL-bin is mild.
- Statistical correlations have a negligible impact on the gluon PDF errors.
- $n\text{TT}2 = \text{ATL13had-}y_{t\bar{t}} + \text{CMS13ll-}y_{t\bar{t}} + \text{CMS13lj-}m_{t\bar{t}} + \text{ATL13lj-}y_{t\bar{t}} + y_{t\bar{t}}^{\text{B}} + m_{t\bar{t}} + H_T^{t\bar{t}}$  w/o stat. corr. (ATL bin)
- New  $t\bar{t}$  data prefer softer gluon for  $x > 0.2$ .
- Stronger ability to reduce the uncertainty of gluon PDF as compared to that in CT18.

# Incl. Jet v.s. dijet data set

| Data          | Ref  | $\sqrt{s}$<br>[TeV] | $\mathcal{L}_{int}$<br>[fb $^{-1}$ ] | $N_{pt}$ | anti- $k_T$<br>$R$ | Observable                                      | Kinematics   | Scale<br>$\mu_R, \mu_F$          |
|---------------|------|---------------------|--------------------------------------|----------|--------------------|---|--|----------------------------------|
| Inclusive Jet |      |                     |                                      |          |                    |   |  |                                  |
| ATLAS [56]    | [56] | 8                   | 20.3                                 | 171      | 0.6                | $\frac{d^2\sigma}{dp_T dy}$                     | $ y  < 3.0$<br>$p_T^{\text{jet}} \in [70, 2500]$       | $p_T^{\text{jet}}, \hat{H}_T$    |
| ATLAS [58]    | [58] | 13                  | 3.2                                  | 177      | 0.4                | $\frac{d^2\sigma}{dp_T dy}$                     | $ y  < 3.0$<br>$p_T^{\text{jet}} \in [100, 3937]$      | $p_T^{\text{jet}}, \hat{H}_T$    |
| CMS [60]      | [60] | 13                  | 36.5                                 | 78       | 0.7                | $\frac{d^2\sigma}{dp_T dy}$                     | $ y  < 2.0$<br>$p_T^{\text{jet}} \in [97, 3103]$       | $p_T^{\text{jet}}, \hat{H}_T$    |
| Dijet         |      |                     |                                      |          |                    |   |  |                                  |
| ATLAS [61]    | [61] | 7                   | 4.5                                  | 90       | 0.6                | $\frac{d^2\sigma}{dm_{12} dy^*}$                | $y^* < 3.0$<br>$m_{12} \in [260, 5040]$                | $m_{12}$                         |
| CMS [62]      | [62] | 7                   | 5.0                                  | 54       | 0.7                | $\frac{d^2\sigma}{dm_{12}  y_{\text{max}} }$    | $y_{\text{max}} < 2.5$<br>$m_{12} \in [197, 5058]$     | $m_{12}$                         |
| CMS [63]      | [63] | 8                   | 19.7                                 | 122      | 0.7                | $\frac{d^3\sigma}{dp_{T,\text{avg}} dy^* dy^b}$ | $y^* < 3.0$<br>$y^b < 3.0$<br>$m_{12} \in [133, 1784]$ | $m_{12}$<br>$p_{T,1} e^{0.3y^*}$ |
| ATLAS [58]    | [58] | 13                  | 3.2                                  | 136      | 0.4                | $\frac{d^2\sigma}{dm_{12} dy^*}$                | $y^* < 3.0$<br>$m_{12} \in [260, 9066]$                | $m_{12}$                         |

- NNLO theoretical prediction was done by NNLOJET
- Scales choice  $\mu_R = \mu_f = p_T^{\text{jet}}$  or  $H_T$  were examined.
- Incl. jet data prefer harder gluon in large  $x$ .
- Mild reduction in gluon PDF uncertainty from incl. jet data is observed.



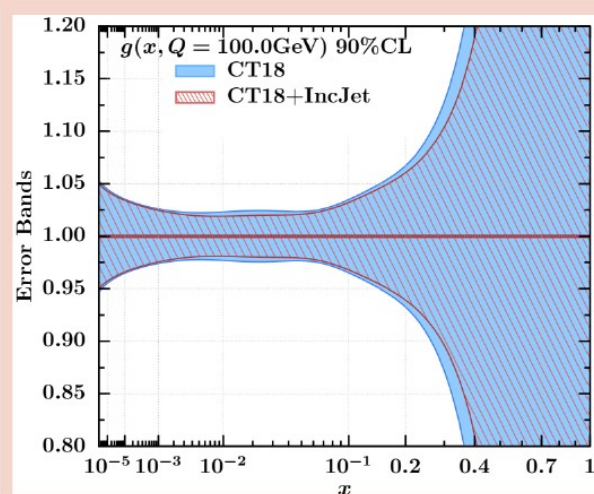
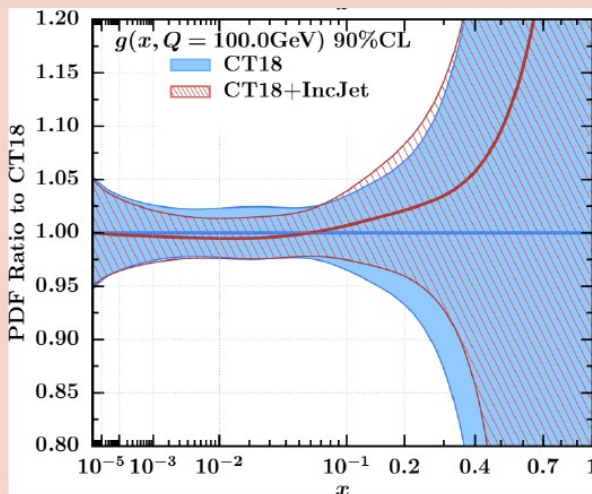
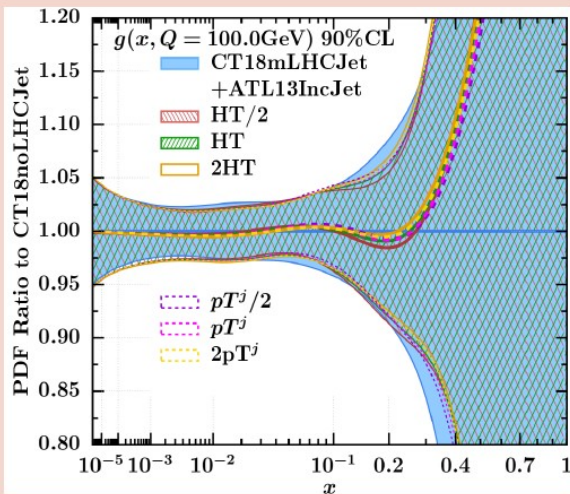
## $\chi^2/N_{pt}$ for fits that add one inclusive jet or dijet data set to the CT18 (without LHC jets) baseline at a time

| Inclusive jets |          | $\chi^2/N_{pt}$ using $\mu_{R,F} \propto HT$ or $p_T^j$                              |          |           |           |         |          |
|----------------|----------|--|----------|-----------|-----------|---------|----------|
| Experiment     | $N_{pt}$ | $HT/2$   | $HT$     | $2HT$     | $p_T^j/2$ | $p_T^j$ | $2p_T^j$ |
| ATL8IncJet     | 171      | 1.7  | 1.74     | 1.87      | 1.75      | 1.66    | 1.7      |
| ATL13IncJet    | 177      | 1.42   | 1.36     | 1.4       | 1.52      | 1.31    | 1.28     |
| CMS13IncJet    | 78       | 1.2  | 1.16     | 1.2       | 1.08      | 1.09    | 1.1      |
| Dijets         |          | $\chi^2/N_{pt}$ using $\mu_{R,F} \propto HT$ or $p_T^* = p_T^{leading} \exp(0.3y^*)$ |          |           |           |         |          |
| Experiment     | $N_{pt}$ | $M_{jj}/2$   | $M_{jj}$ | $2M_{jj}$ | $p_T^*/2$ | $p_T^*$ | $2p_T^*$ |
| ATL7DiJet      | 90       | 0.81   | 0.79     | 0.87      |           |         |          |
| CMS7DiJet      | 54       | 1.55   | 1.55     | 1.63      |           |         |          |
| CMS8DiJet      | 122      | 0.95   | 1.2      | 1.9       | 1.25      | 1       | 1.01     |
| ATL13DiJet     | 136      | 0.9  | 0.87     | 0.93      |           |         |          |

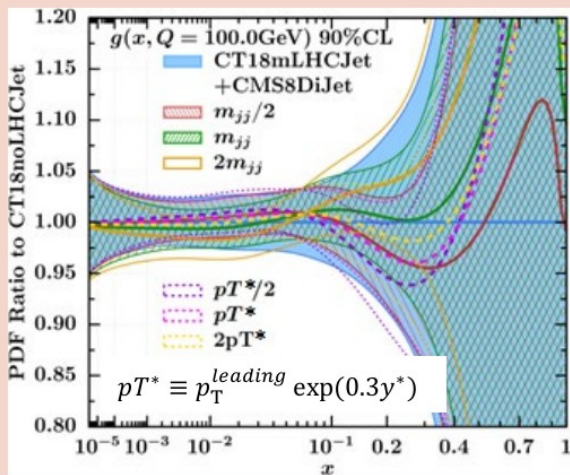
- Dijet data sets tend to have larger uncertainties than inc. jets, on facilitating PDFs better  $\chi^2$  for similar constraints on PDF.
- Dijet data are dominated by the CMS 8 TeV dataset

# Incl. jet vs. dijet data sets: impact on the gluon

+ inclusive jets: small scale dependence, a harder  $g(x, Q)$



+ dijets: significant scale dependence, varied pulls on  $g(x, Q)$



The impact of the Inc. jet data on  $g(x, Q)$  is relatively independent of the scale choice. The final fit uses  $\mu_{R,F} = p_T^j$ , giving better  $\chi^2$ .

The impact of dijet data substantially depends on scale choices, especially in the case of CMS8 TeV dijet.

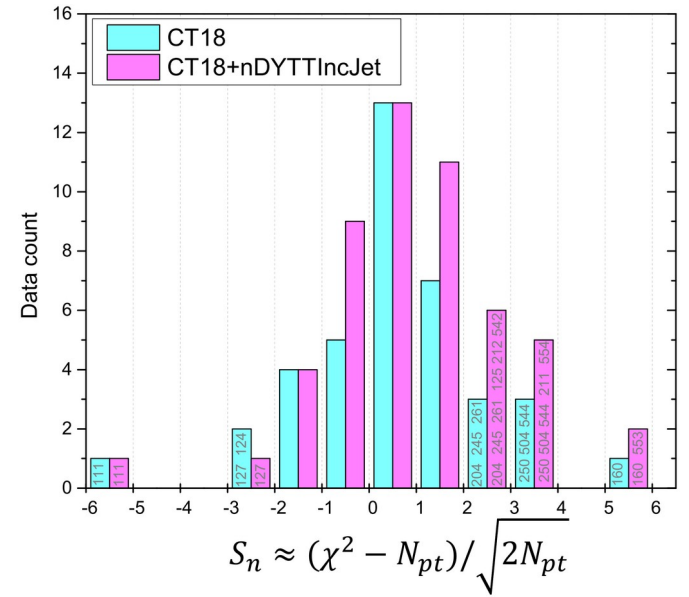
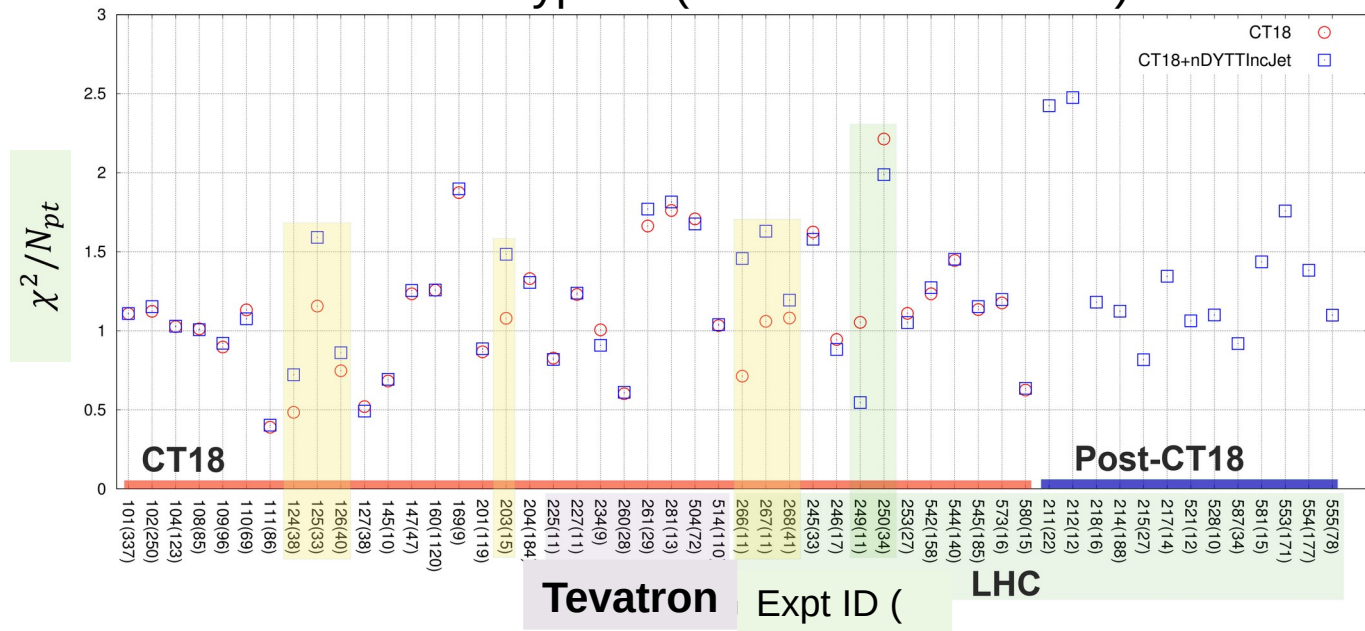
# NNLO fits with new data at 8 and 13 TeV

for CT18+new data (CT18 in parentheses) NNLO fits; 68% CL

| ID                | Exp   | $N_{pt}$ | $\chi^2 / N_{pt}$      |                               |           |
|-------------------|---|----------|------------------------|-------------------------------|-----------|
| Drell-Yan         |   |          |                        |                               |           |
| 215               | ATLAS 5.02 TeV W,Z  | 27       | $0.82^{+0.55}_{-0.16}$ | ( $1.15^{+1.22}_{-0.43}$ )    | } nDY     |
| 211               | ATLAS 8 TeV W   | 22       | $2.42^{+2.49}_{-1.51}$ | ( $4.25^{+6.39}_{-3.34}$ )    |           |
| 214               | ATLAS 8 TeV Z3D   | 188      | $1.12^{+0.46}_{-0.02}$ | ( $1.99^{+5.10}_{-1.85}$ )    |           |
| 212               | CMS 13 TeV Z  | 12       | $2.48^{+4.76}_{-0.88}$ | ( $12.03^{+38.04}_{-21.84}$ ) |           |
| 217               | LHCb 8 TeV W  | 14       | $1.35^{+0.59}_{-0.61}$ | ( $1.35^{+0.72}_{-0.64}$ )    |           |
| 218               | LHCb 13 TeV Z   | 16       | $1.18^{+1.42}_{-0.60}$ | ( $1.49^{+1.74}_{-0.89}$ )    |           |
| 13 TeV $t\bar{t}$ |   |          |                        |                               |           |
| 521               | ATLAS all-hadronic $y_{t\bar{t}}$   | 12       | $1.06^{+0.14}_{-0.09}$ | ( $1.05^{+0.21}_{-0.10}$ )    | } nTT     |
| 528               | CMS dilep $y_{t\bar{t}}$  | 10       | $1.10^{+1.08}_{-0.68}$ | ( $1.03^{+1.60}_{-0.74}$ )    |           |
| 587               | ATLAS lep+Jet $m_{t\bar{t}} + y_{t\bar{t}} + y_{t\bar{t}}^B + H_T^{t\bar{t}}$ | 34       | $0.92^{+0.32}_{-0.14}$ | ( $0.94^{+0.59}_{-0.16}$ )    |           |
| 581               | CMS lep+jet $m_{t\bar{t}}$  | 15       | $1.44^{+1.18}_{-0.73}$ | ( $1.37^{+1.86}_{-0.82}$ )    |           |
| Inclusive Jet     |   |          |                        |                               |           |
| 553               | ATLAS 8 IncJet  | 171      | $1.76^{+0.20}_{-0.12}$ | ( $1.80^{+0.33}_{-0.16}$ )    | } nIncJet |
| 554               | ATLAS 13 IncJet   | 177      | $1.38^{+0.13}_{-0.10}$ | ( $1.39^{+0.20}_{-0.11}$ )    |           |
| 555               | CMS 13 IncJet   | 78       | $1.10^{+0.24}_{-0.17}$ | ( $1.11^{+0.30}_{-0.16}$ )    |           |

Fits with 1 type of new data      A fit with all 3 types

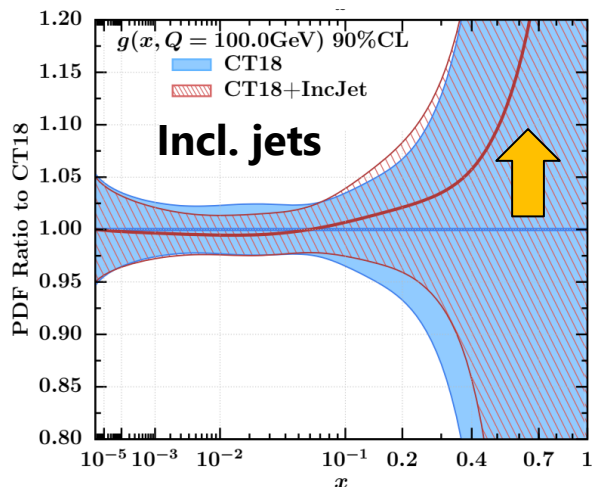
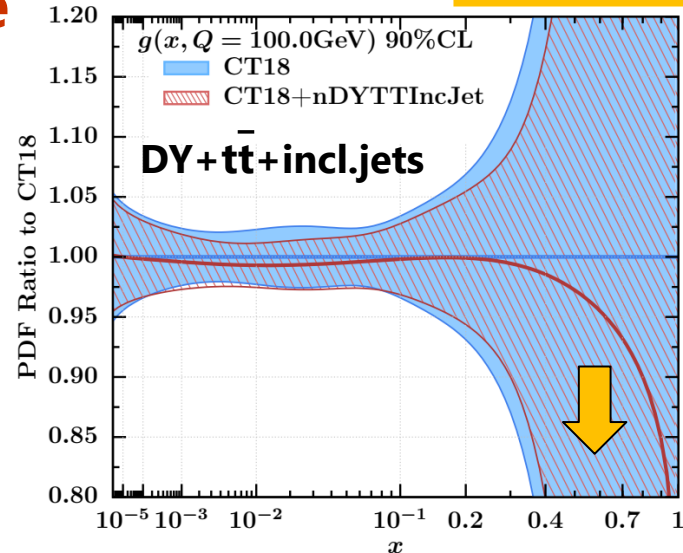
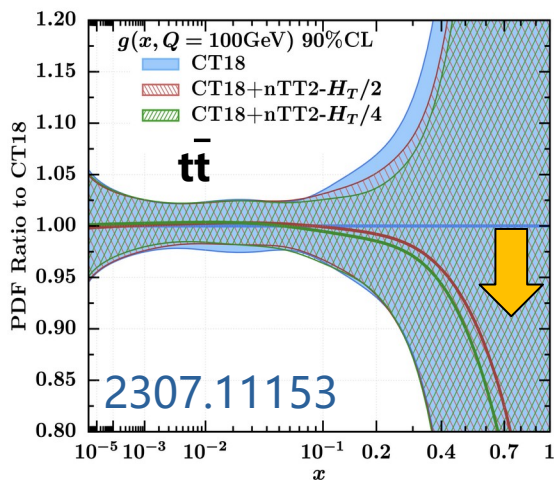
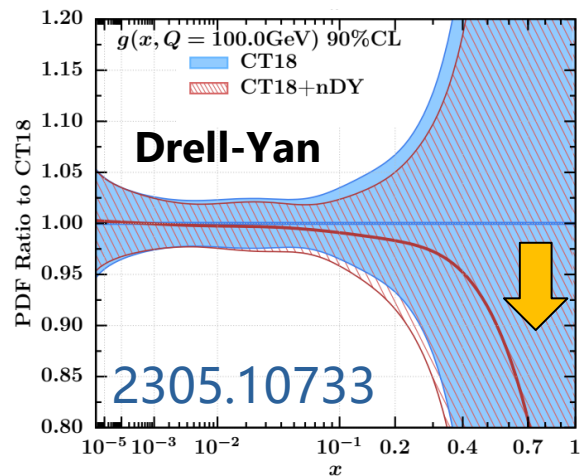
### A 3-data-type fit (CT18+nDYTTIncJet)



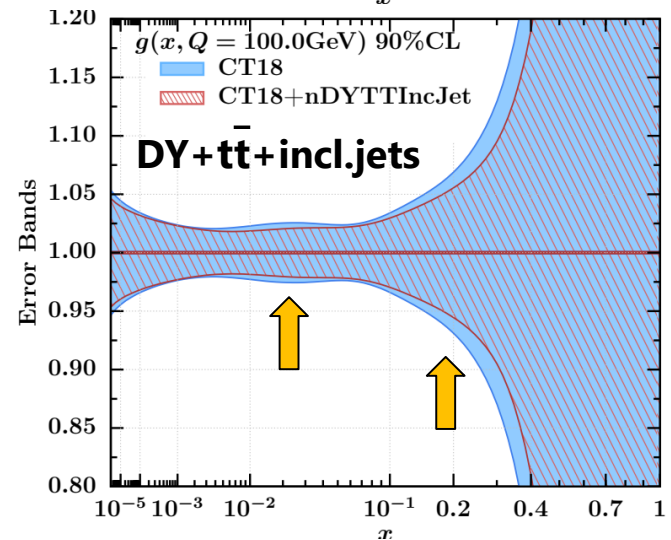
- The most precise new experiments tend to have an elevated, in the same pattern as observed for CT18
- $\chi^2/N_{pt}$  increases for experiments 124 and 125 (NuTeV), 126 and 127 (CCFR) and 203 (E866 DY), 266 and 267 (CMS 7TeV Ach), 268 (ATLAS 7TeV W, Ach).
- $\chi^2/N_{pt}$  decreases for experiments 249 (CMS 8 TeV Ach), 250 (LHCb 8 TeV W/Z)



# Pulls on the gluon PDF by the new data type



- After including DY,  $t\bar{t}$ , and inc. jet data simultaneously, we get a softer gluon.
- Note that new DY and  $t\bar{t}$  data favor a softer gluon, new inc. jet data prefer a harder gluon.
- Mild changes in the gluon uncertainty

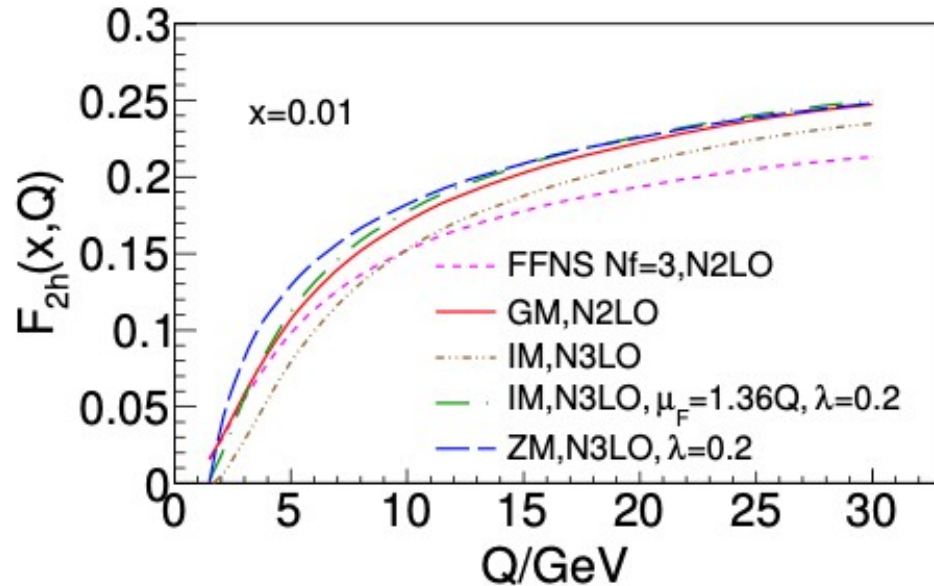


# Necessary components of an N3LO PDF analysis

| Component           |  | Availability  |
|---------------------|--|---|
| Splitting functions |  | Partial N3LO  |
| Hard cross sections | DIS, light flavors   | Full N3LO   |
|                     | NC DIS, heavy flavors                                      | Full N3LO (Blümlein et al.), not yet in fitting codes         |
|                     | Vector boson production                                    | Full N3LO for some processes, fixed N3LO/N2LO K-factor tables |
|                     | CC DIS, jet, production                                    | N2LO  |
|                     | $pp \rightarrow w+c, pp \rightarrow z+b, pp \rightarrow b$ | NLO (massive); NNLO (ZM)                                      |

- Looking forward to including all components exactly and fully to reduce the QCD scale uncertainty and guarantee the N3LO accuracy in the near future.
- CTEQ-TEA and other groups include some N3LO contributions in their fitting codes: remarkable progress of MSHT and NNPDF in aN3LO fits.
- These extended (N2LO+, or aN3LO) calculations agree with N2LO within their scale dependence

# QCD cross sections @N3LO



- **DIS:** The CTEQ-TEA code implements complete flavor decompositions of DIS SFs at N3LO using approximate zero-mass Wilson coefficients with a rescaling variable (the **Intermediate-Mass VFN scheme**, cf. the figure)

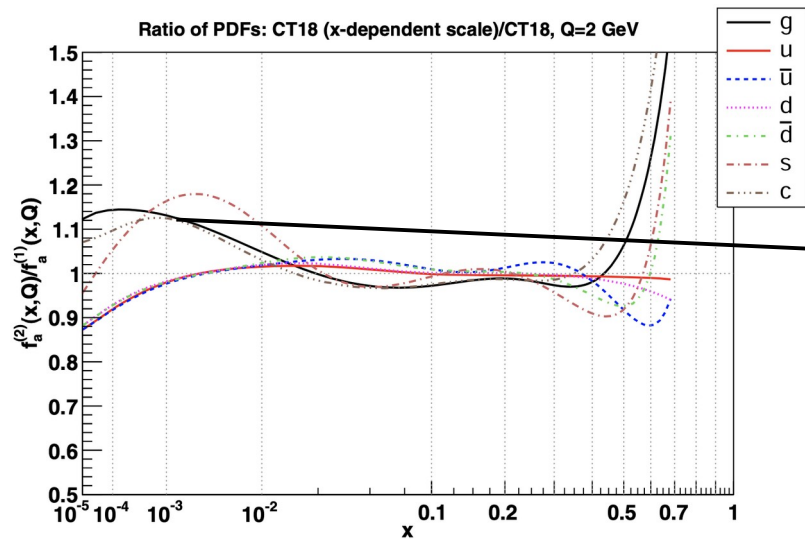
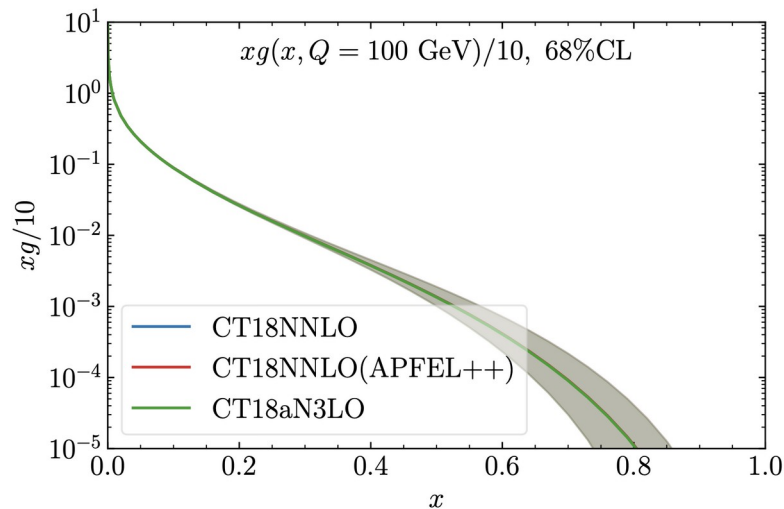
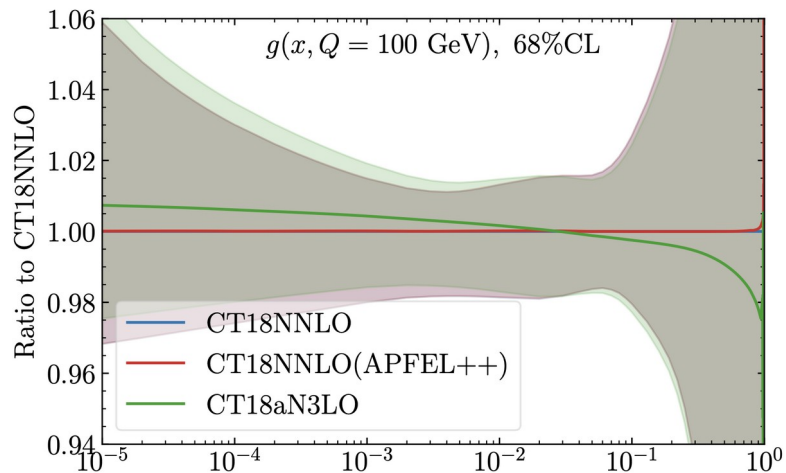
*Boting Wang's and Keping Xie's Theses, SMU*

- **Working on the implementation of massive N3LO heavy-quark coefficients to obtain N3LO**

| Factorization schemes | Mass dependence in the FC terms | Mass dependence of the FE and subtraction terms | Introduce heavy-quark PDFs at large $Q$ |
|-----------------------|---------------------------------|---|---|
| FFN                   | Exact                           | N/A   | no                                      |
| ZM                    | None                            | None  | yes                                     |
| IM                    | Approximate                     | Approximate                                     | yes                                     |
| GM                    | Exact                           | Approximate                                     | yes                                     |

- **DGLAP evolution** is performed at N3LO with APFEL/APFEL++.
- **Drell-Yan:** Ongoing work to include N3LO DY effects using NNLO ApplFast + N3LO/N2LO K-factor tables

# CT18aN3LO gluon

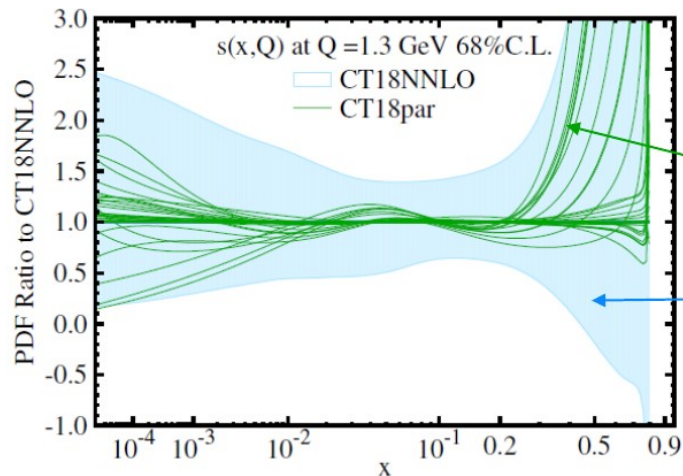


Some of the aN3LO gluon features reproduced by suitable scale choice in DIS NNLO (cfr. CT18X)

# Taming PDF uncertainties

Several efforts to refine PDF uncertainty quantification:

- understand conceptual underpinnings of the multivariate inverse problem. Much can be learned from non-HEP statistics applications
- suppress aleatory and perturbative uncertainties (e.g., from higher-order contributions)
- comprehensively estimate epistemic uncertainties (e.g., due to the PDF parametrization forms)



**CT approach: “Bayesian exploration with Gaussian emulation”**

preliminary PDFs for alternative parametrizations

final uncertainty with one parametrization

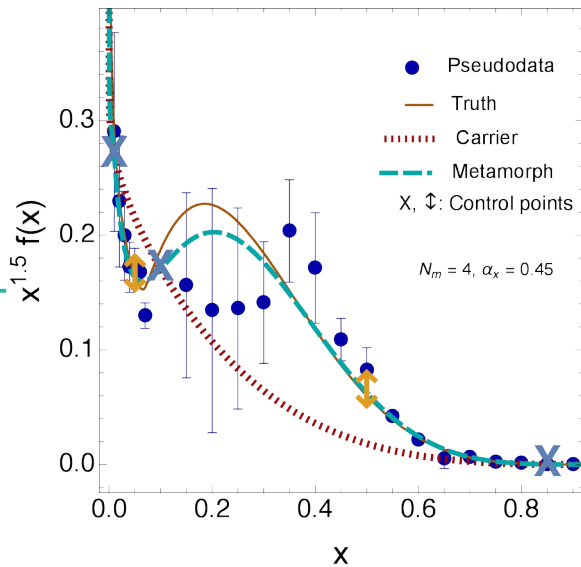
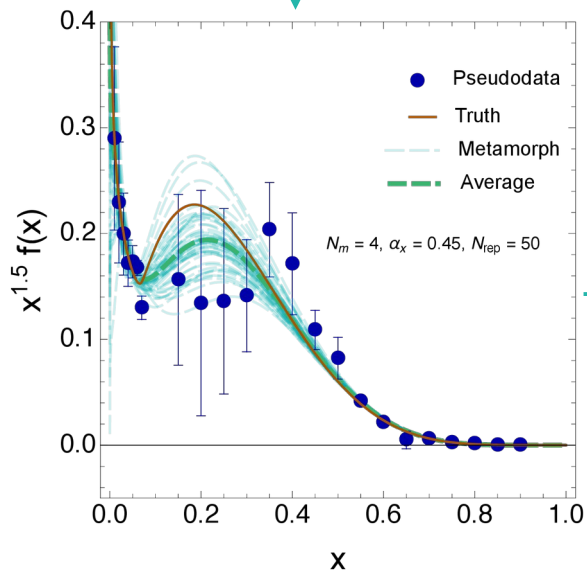
Preliminary fits explore experimental, theoretical, parametrization, methodological uncertainties

The final Hessian error set (50-60) approximates the total uncertainty due to the above factors.

# Bézier-curves methodology for global analyses – A toy model

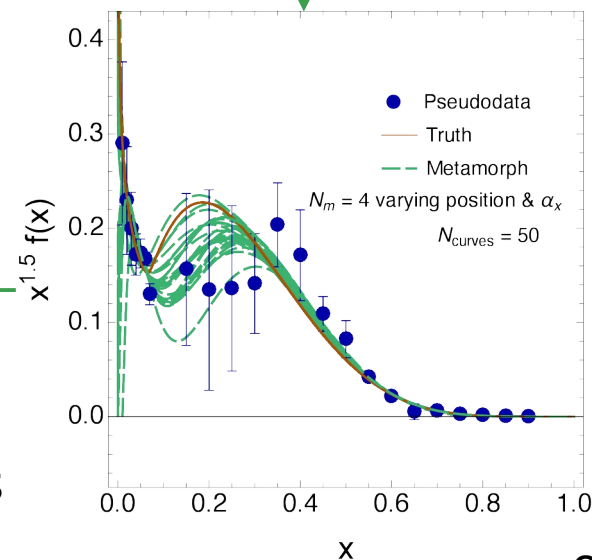
sampling on the distribution of data uncertainties

bootstrapped



sampling over parametrizations based on **Bézier curves**

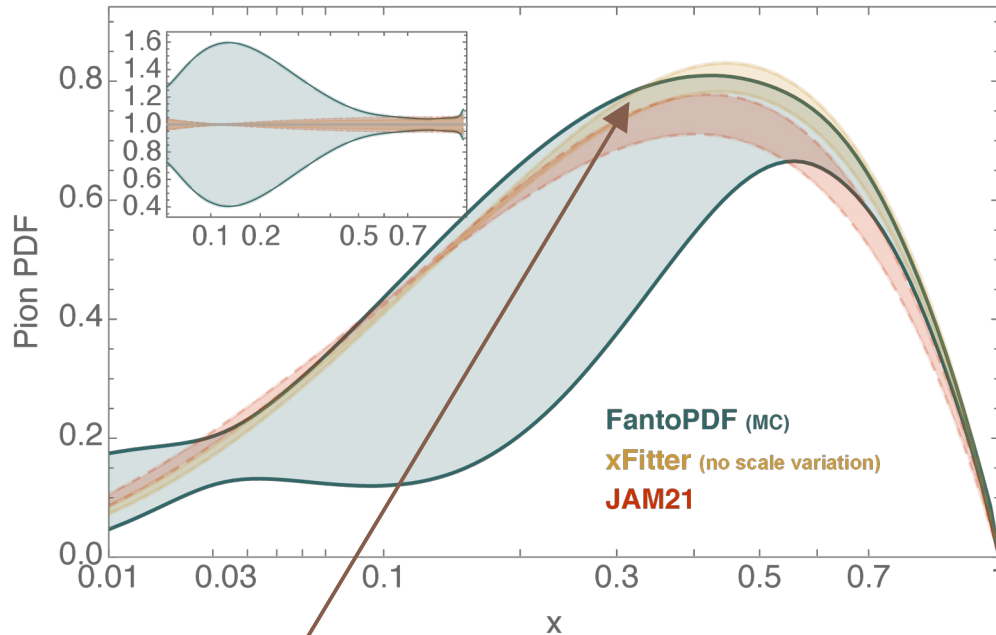
metamorph



A C++ package with the *metamorph* parametrizations

# The Fantômas pion PDFs

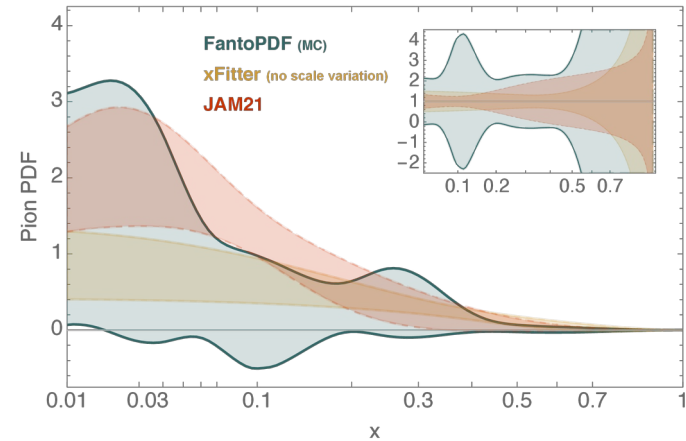
$xV(x,Q)$  at  $Q=1.4$  GeV, 68% c.l. (band)



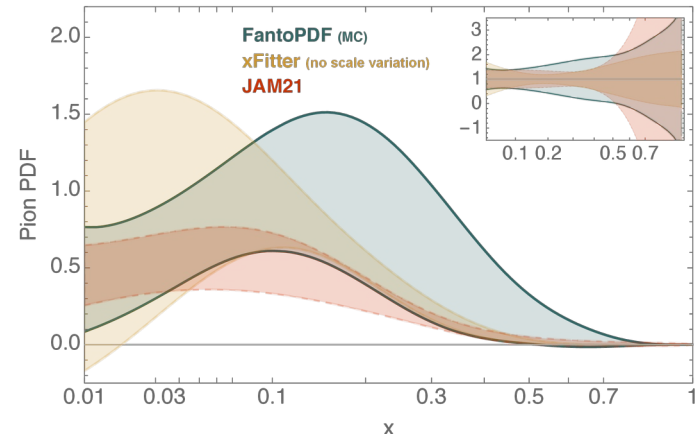
without parametrization dependence

- Fantômas was incorporated into the xFitter fitting program
- Framework to access pion PDFs available on xFitter.

$xg(x,Q)$  at  $Q=1.4$  GeV, 68% c.l. (band)



$xS(x,Q)$  at  $Q=1.4$  GeV, 68% c.l. (band)

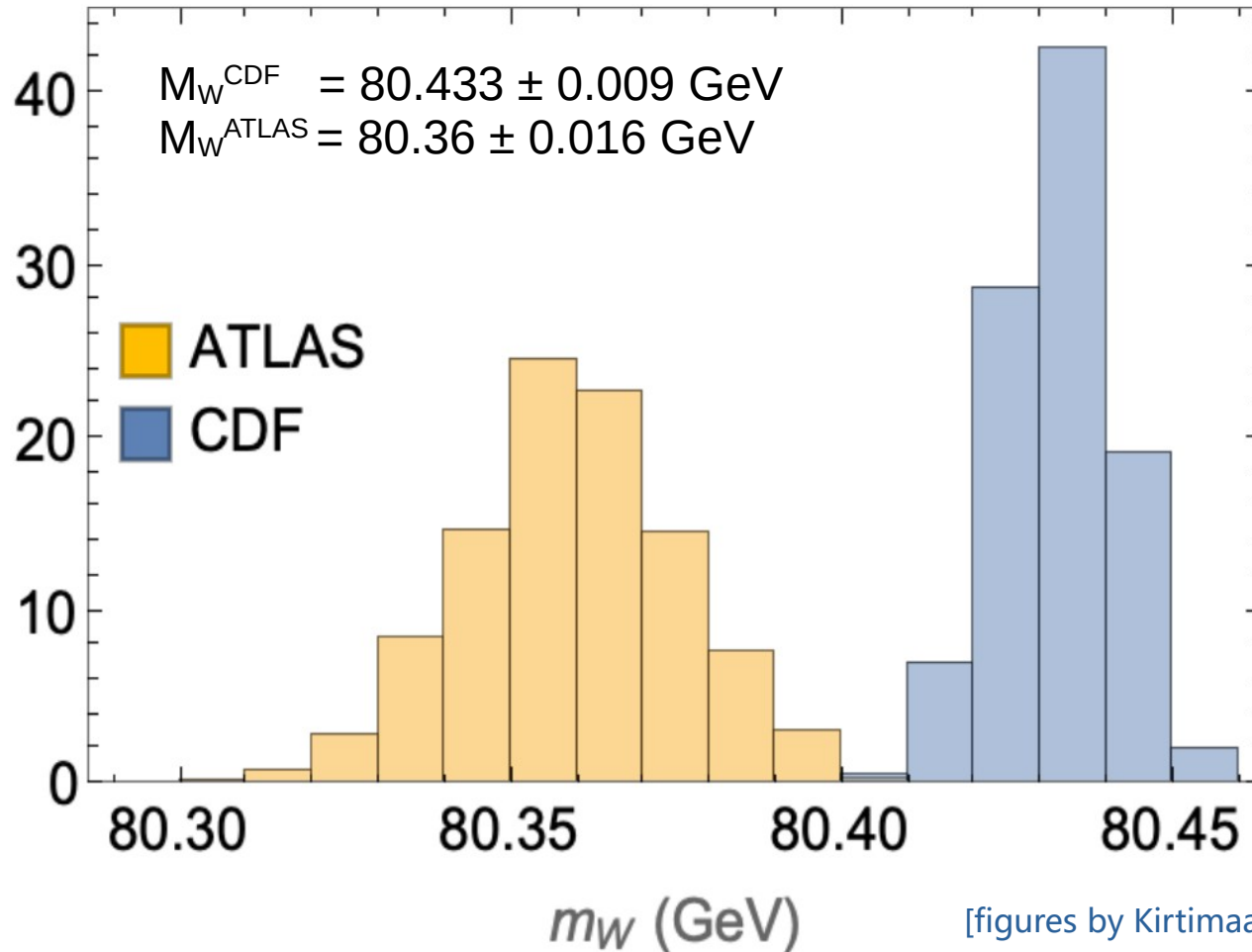


# Statistic analysis

## Improve precision:

CDF Science,376 (2022)

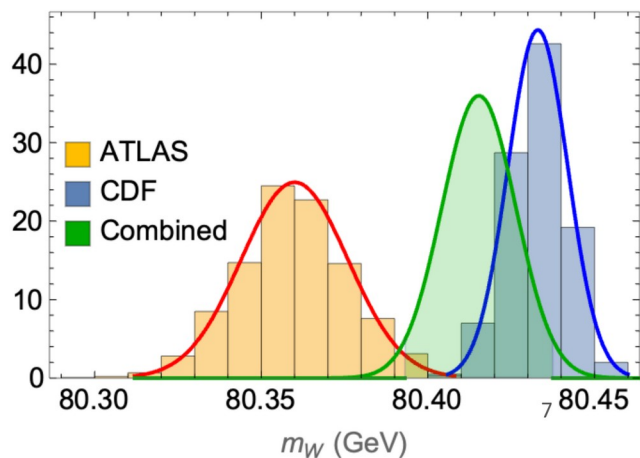
Repeat measurements with more precise balance



[figures by Kirtimaan Mohan, DIS2023]

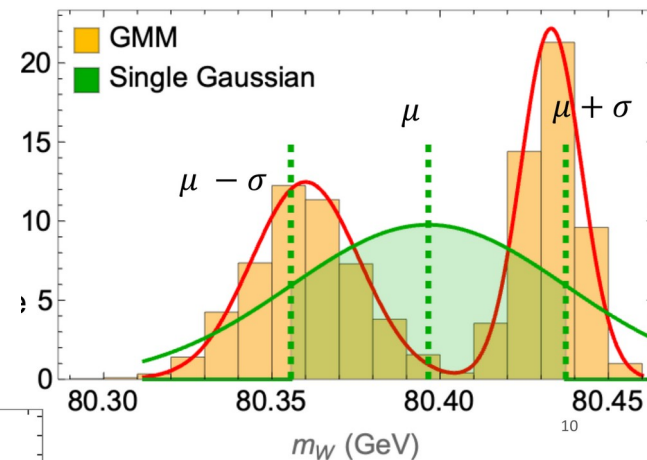


# Gaussian Mixture Model (GMM)



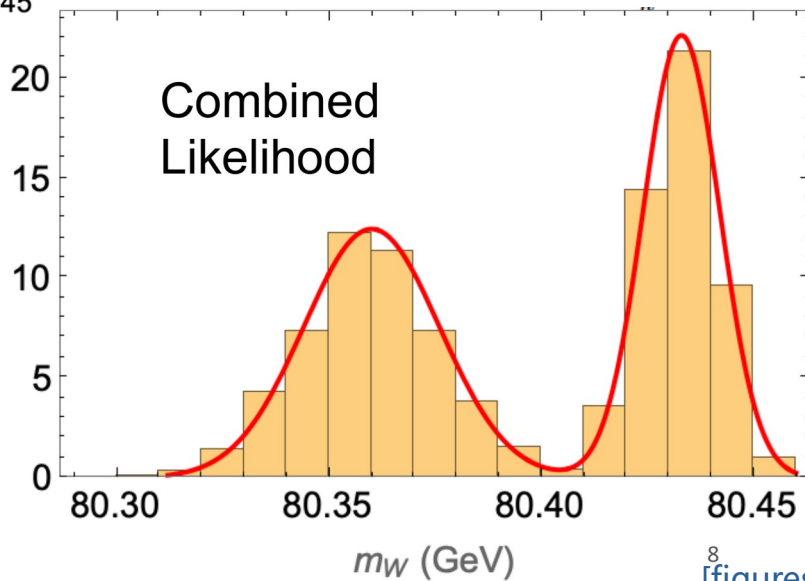
## Gaussian Mixture Model

- parameterizing the likelihood as a sum of Gaussians
- 2 Gaussians is needed in this case



## Combine?

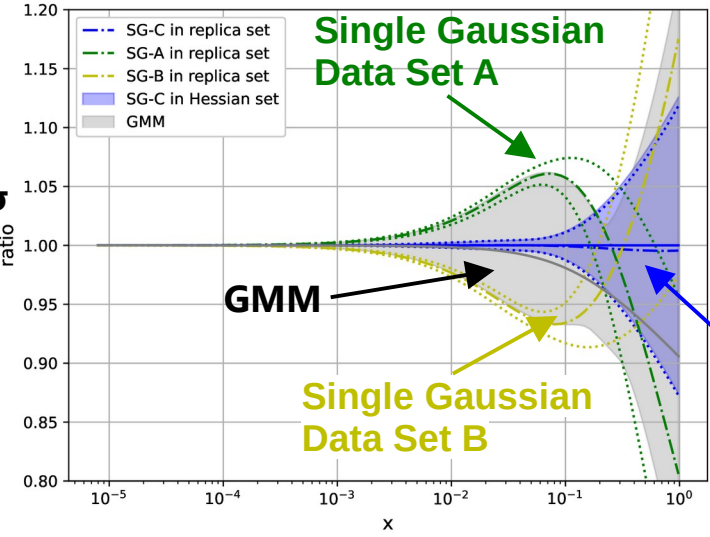
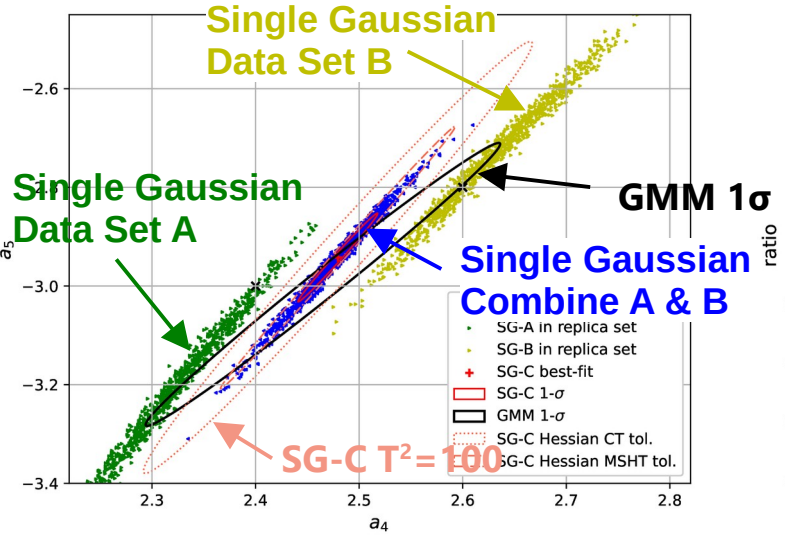
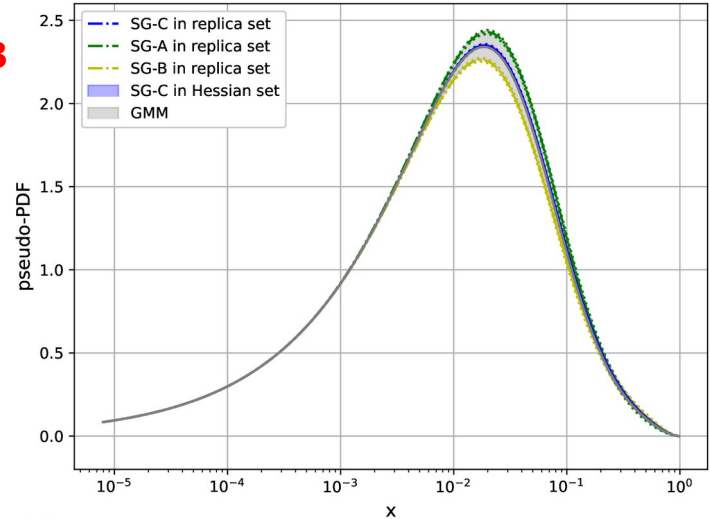
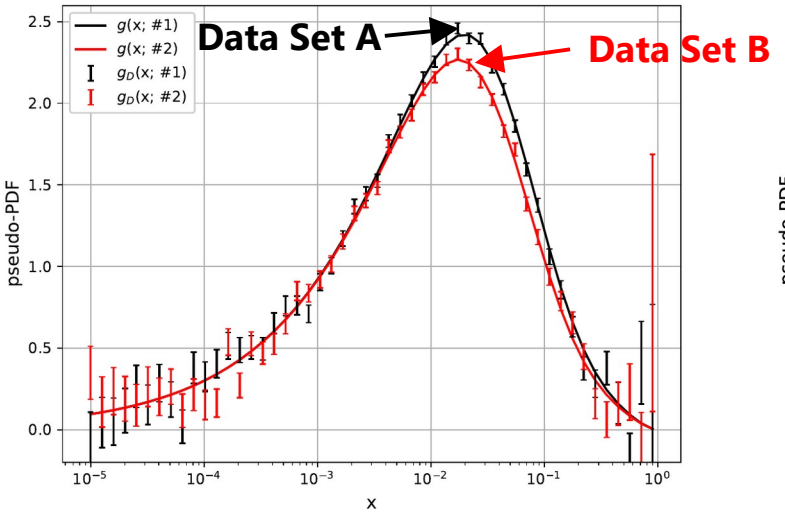
- $2\sigma$  band does not cover both means
- Increase tolerance  
 $\Delta\chi^2 = T^2$ ;  $T > 1$   
Does not provide a faithful representation of the probability distribution



## Model as a single Gaussian?

- not a faithful representation of the likelihood

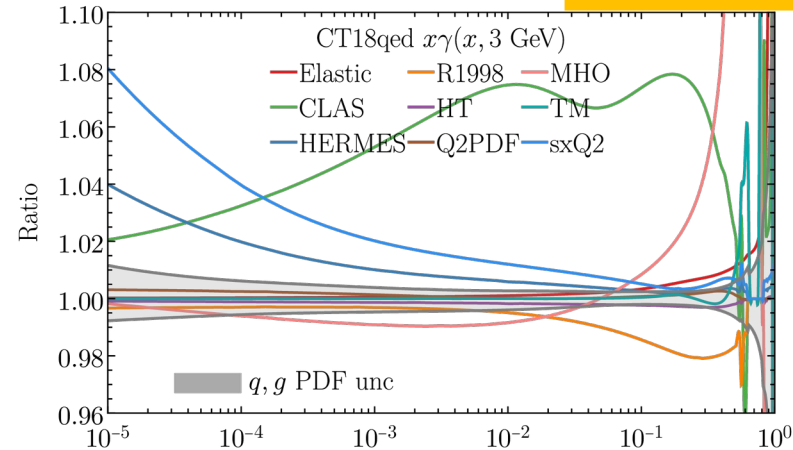
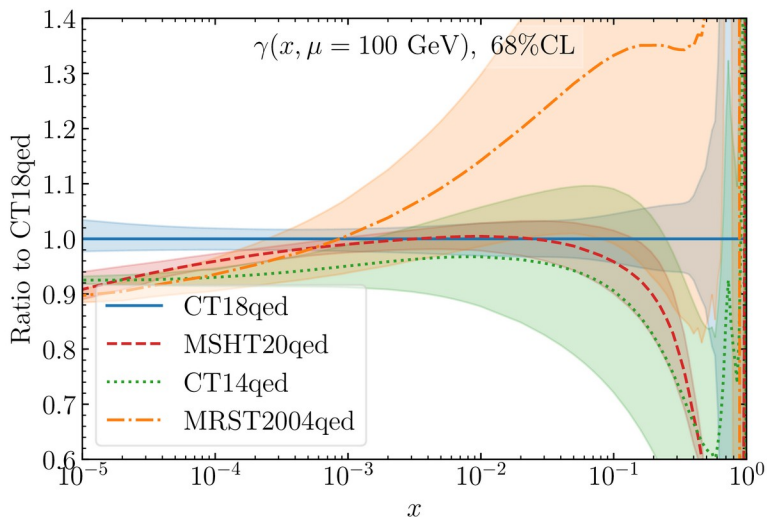
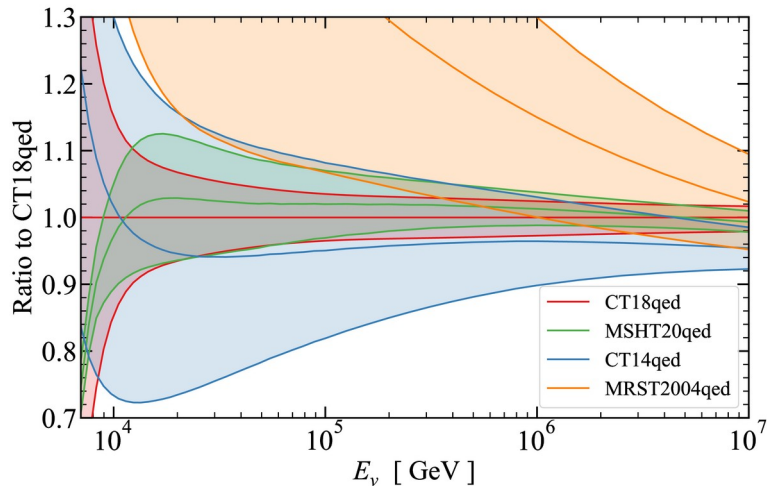
# Gaussian Mixture Model (GMM)



- Single Gaussian fit with combined data set A and B do not cover the likelihood of data set A or data set B
- Enlarge tolerance do not help too much
- The uncertainty band of GMM cover the means of data set A and B

**Single Gaussian Data Set A**  
**Single Gaussian Data Set B**  
**Single Gaussian Combine A & B**  
**GMM**

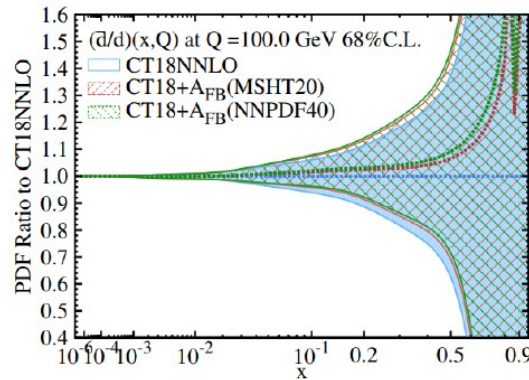
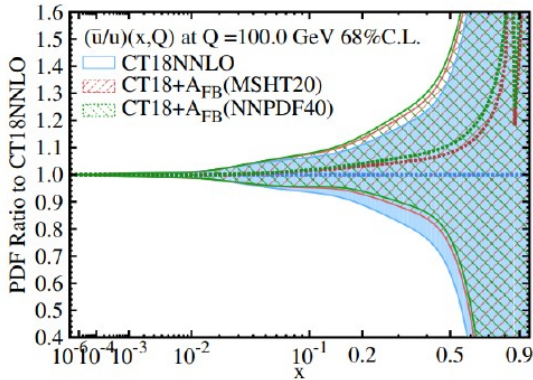
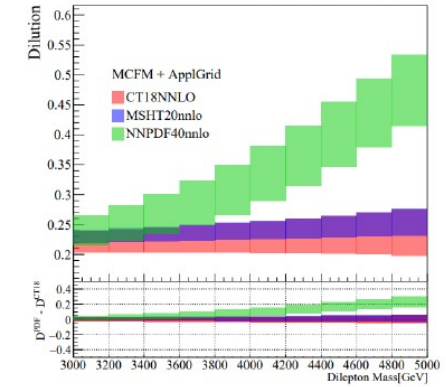
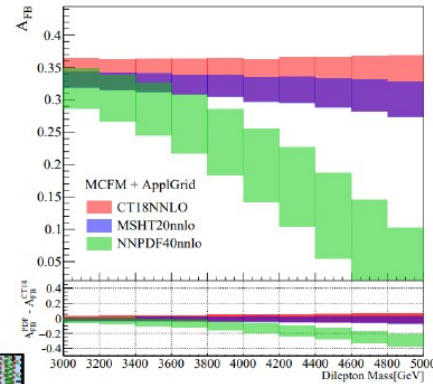
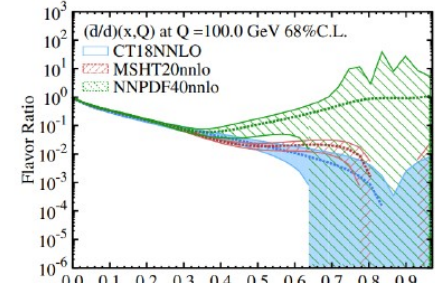
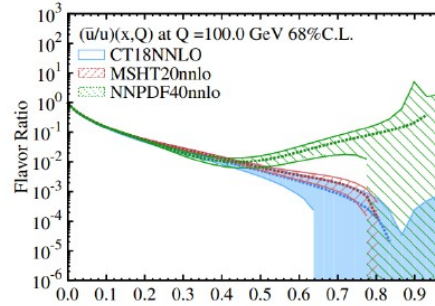
# Neutron's photon PDF



- We have determined the neutron's photon PDF using a similar methodology as for the proton one.
- The structure function is determined using pQCD at high  $Q^2$  and HERMES and CLAS/CB data at a low  $Q^2$
- We estimated many low- $Q^2$  uncertainties, including the isospin symmetry violation and the QED evolution effects. We also explored implications for W-boson production, etc.
- CT18qed and MSHT20qed are in a good agreement
- In comparison to the first generation of photon PDFs, the uncertainty is significantly reduced.

# Impact of $A_{FB}$ in the high-mass Drell-Yan process

- $A_{FB}$  at the LHC is sensitive to the energy dilution factor  $D$  (probability of  $k_q^0 < k_{\bar{q}}^0$  in the Collins-Soper frame)
- $A_{FB}^h = \frac{N_F^h - N_B^h}{N_F^h + N_B^h} \approx (1 - 2D)A_{FB}^q$
- $A_{FB}$  at high invariant mass region probes  $\bar{u}/u, \bar{d}/d$  at  $x > 0.2$



- CT18, MSHT20, and NNPDF4.0 predict very different  $\bar{q}/q$  at  $x > 0.2$
  - The article quantified the potential effect of high-mass  $A_{FB}$  on large- $x$  antiquarks
- See also NNPDF (2209.08115), Fiaschi et al. (2211.06188)

# Uncertainty of Gluon PDF

Jet data sets included in each fits

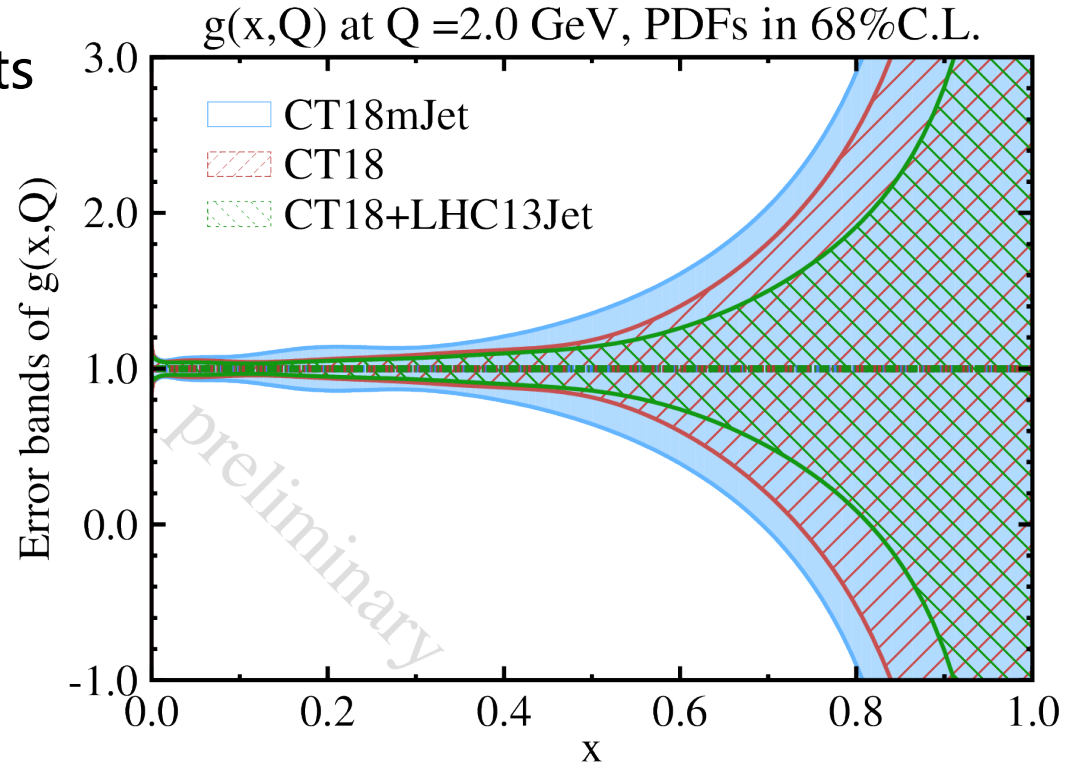
**CT18mJet**: no jet data

**CT18**:

|      |            |                       |
|------|------------|-----------------------|
| CDF  | 0807.2204  | 1.13 fb <sup>-1</sup> |
| D0   | 0802.2400  | 0.7 fb <sup>-1</sup>  |
| CMS7 | 1406.0324  | 5.0 fb <sup>-1</sup>  |
| ATL7 | 1410.8857  | 4.5 fb <sup>-1</sup>  |
| CMS8 | 1609.05331 | 19.7 fb <sup>-1</sup> |

**CT18+LHC13jet**:

|       |            |                       |
|-------|------------|-----------------------|
| ATL8  | 1706.03192 | 20.2 fb <sup>-1</sup> |
| ATL13 | 1711.02692 | 3.2 fb <sup>-1</sup>  |
| CMS13 | 2111.10431 | 36.3 fb <sup>-1</sup> |



The uncertainty of the gluon PDF in the large- $x$  region receives constraints from jet data.

# Uncertain

Jet data  
CT18m

CT18:

CDF

D0

CMS7

ATL7

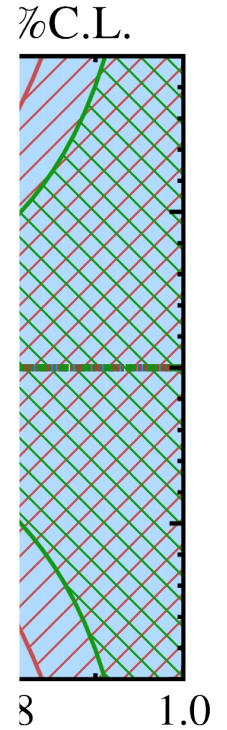
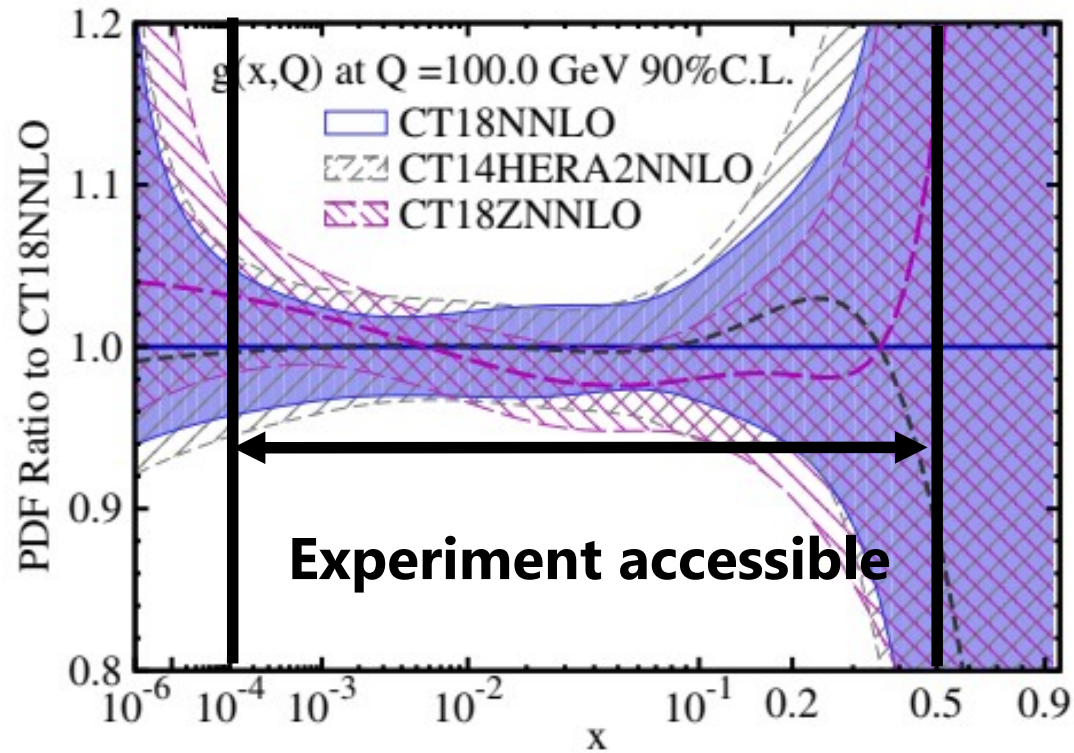
CMS8

CT18+

ATL8

ATL13

CMS13



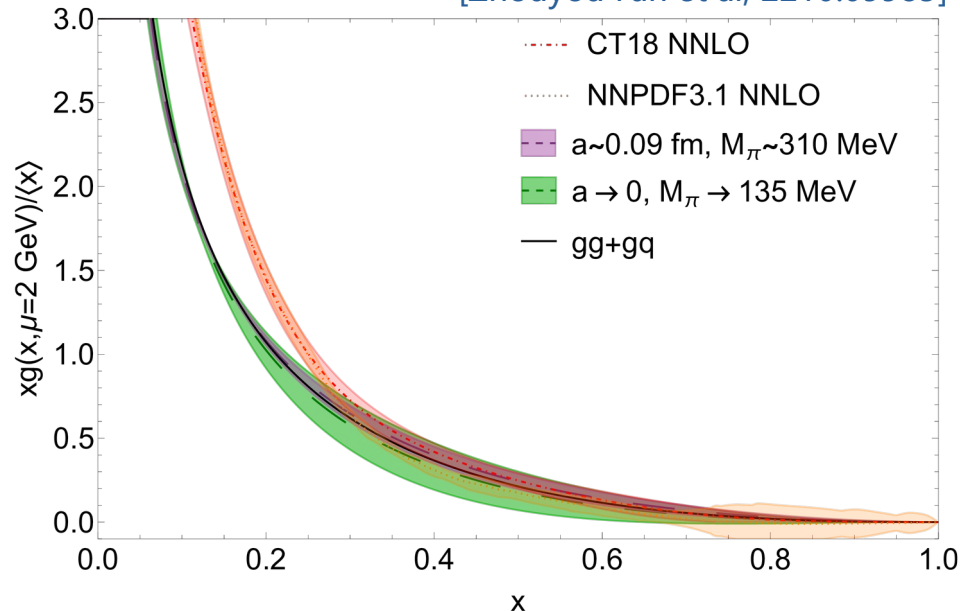
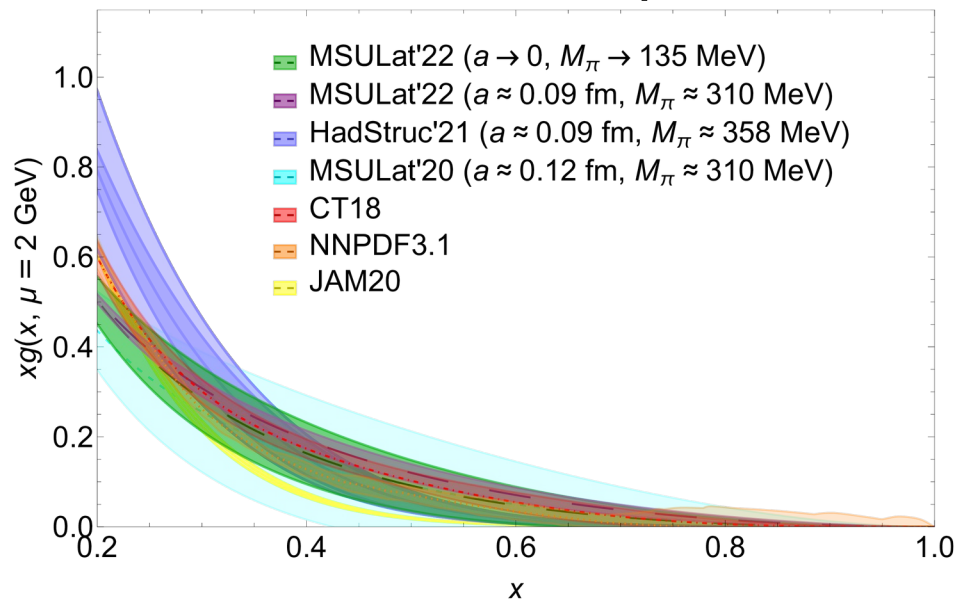
- PDFs are well determined in "middle-x" region:  $10^{-4} \lesssim x \lesssim 0.4$
- Region of  $x \rightarrow 1$  and  $x \rightarrow 0$  are not experimental accessible.

in the  
from

# CT18 with Lattice input on gluon

## Result from MSULat/quasi-PDF method

[Zhouyou Fan et al, 2210.09985]

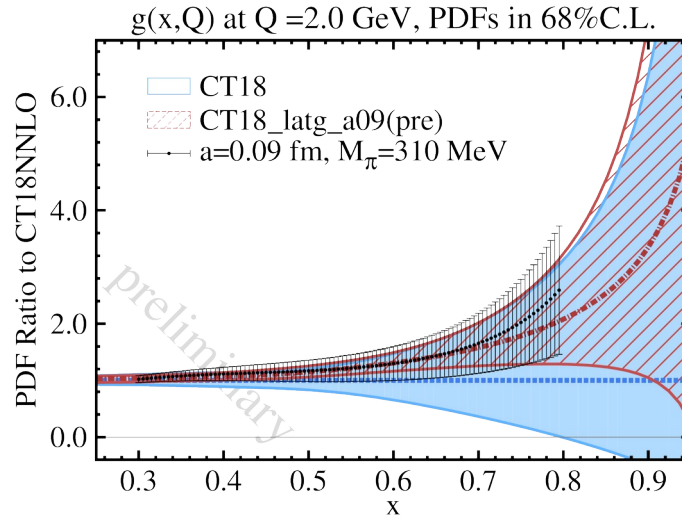
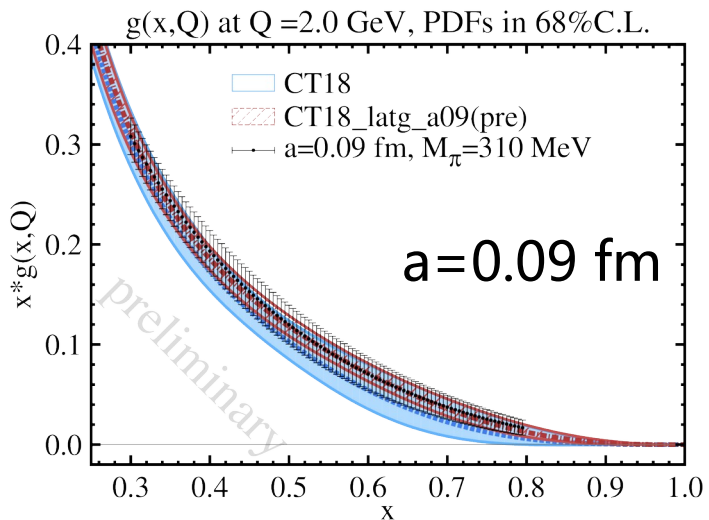
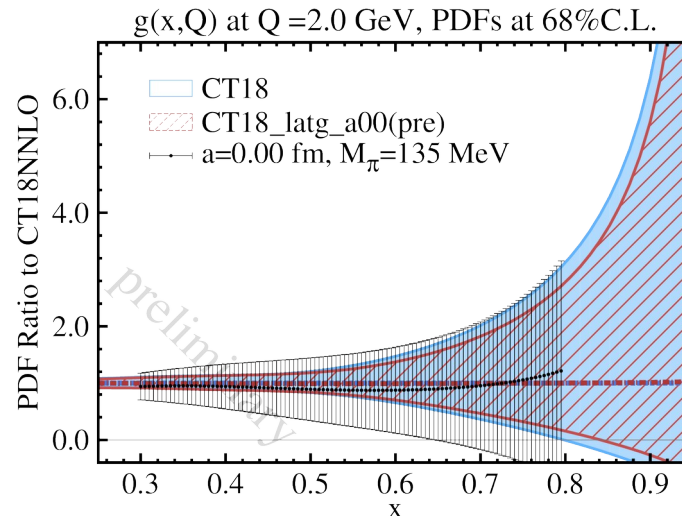
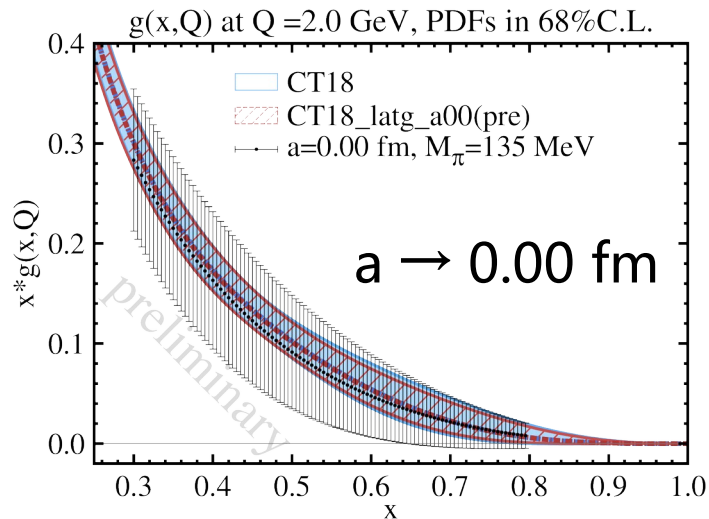


- Clover on 2+1+1 HISQ
- $a \rightarrow 0 \text{ fm}$ ,  $M_\pi \rightarrow 135 \text{ MeV}$  and  $a \approx 0.09 \text{ fm}$ ,  $M_\pi \approx 310 \text{ MeV}$  which represent the current and future levels of uncertainty.

$$\mathcal{M}(\nu, z^2) = \int_0^1 dx \frac{xg(x, \mu^2)}{\langle x \rangle_g} R_{gg}(x\nu, z^2\mu^2)$$

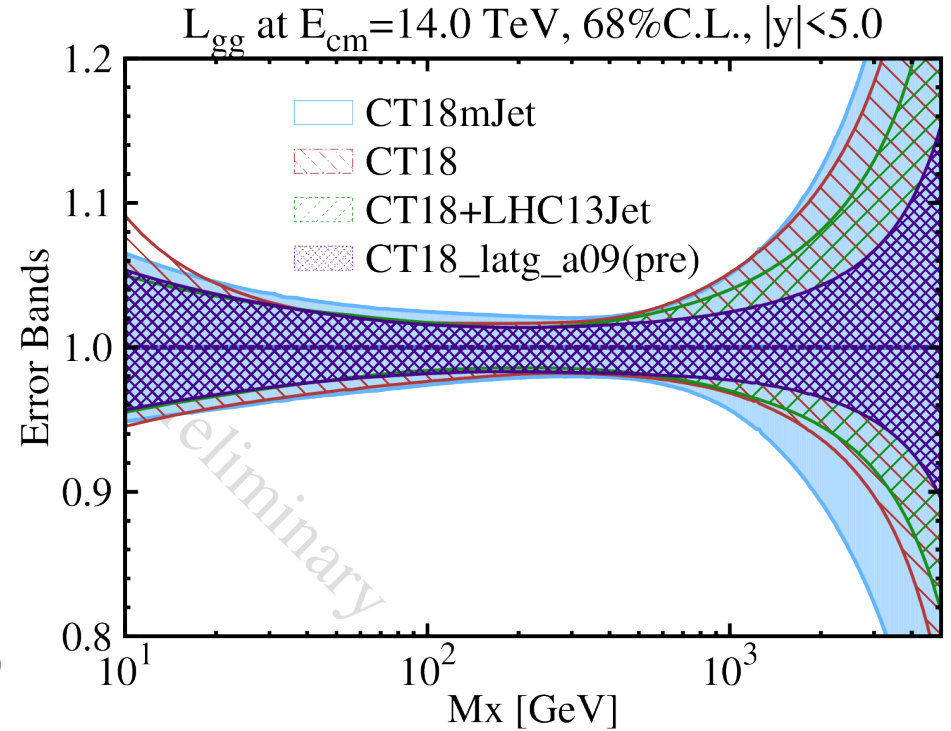
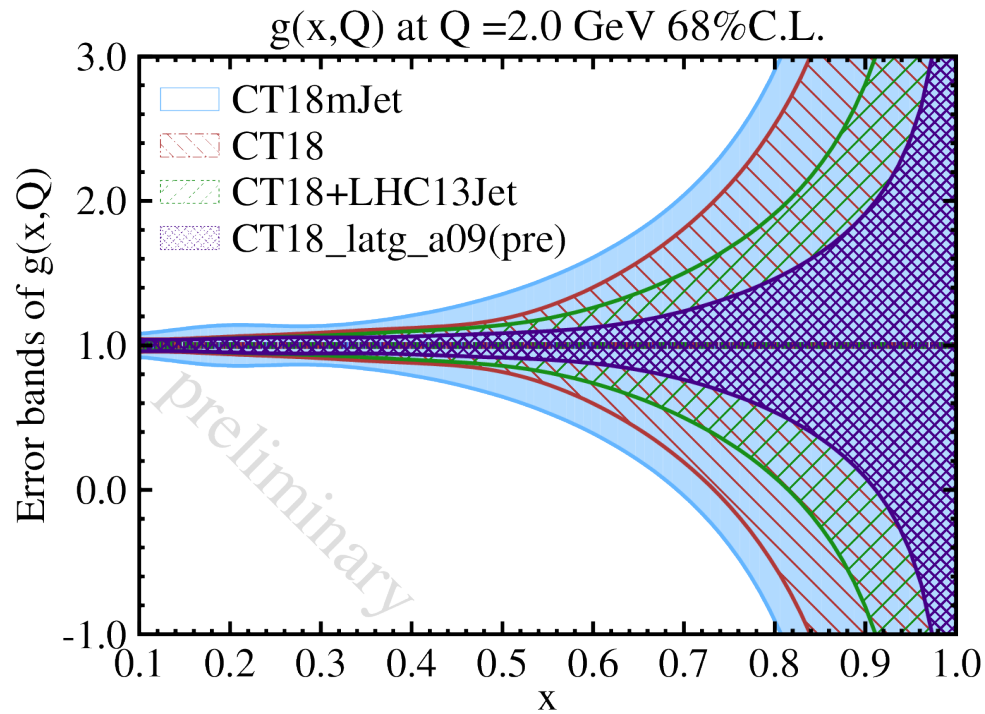
- Good agreement with CT18 and NNPDF3.1
- Gluon PDF  $xg(x)$  extra at 2 GeV

# CT18 with Lattice input on gluon



- Inclusion of lattice input in the CT18 global analysis has the potential to reduce its uncertainty.
- Here,  $a \rightarrow 0.00$  fm case represents the current status, while  $a=0.09$  fm case represents future potential.





- The precision of the gluon PDF in the large- $x$  region could potentially be improved by both incorporating jet data and lattice QCD input.

# Near-future plans

1. Final selection of experiments for NNLO PDFs planned for the next year
2. Work on N3LO contributions
3. Next-generation PDF uncertainty quantification
4. Recent and imminent releases
  - Study on impact of the LHC incl. jet data on the proton structure
  - QCD+QED PDFs for protons and neutrons
  - Subtracted S-ACOT-MPS PDFs
  - Fantômas 1.0 pion PDFs (Hessian)
  - Release of the Fantômas PDF parametrization package in xFitter
  - Impact of lattice large-x gluon data in the CTEQ-TEA global analysis

**Thank you for your attention!**