





Triangle singularity in the hidden charm pentaquark decays and a feed-down mechanism at LHCb

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Outline

- **1. A brief review of the Pc's at LHCb**
- 2. Novel phenomena arising from the Pc three-body and four-body decays and a feed-down mechanism into $J/\psi \, p$
- 3. Comments on the J/psi photoproduction near threshold

1. A brief review of the Pc's at LHCb





The mass positions and the preferred quantum numbers indicate the hadronic molecule nature of these observed enhancements.

Theoretical predictions: [1] J. J. Wu, T. S. H. Lee, and B. S. Zou, PRC 403, 044002 (2012)

[2] Z. C. Yang, Z. F. Sun, J.He, X. Liu, and S. L. Zhu,CPC36, 6 (2012)

Run-I: LHCb, PRL115, 072001 (2015)

Run-II: LHCb, PRL122, 222001 (2019)

Observation of $P_c(4380)$ and $P_c(4450)$ in $\Lambda_b^0 \rightarrow J/\psi p\pi$



Figure 3: Background-subtracted data and fit projections onto $m_{J/\psi p}$ for (a) all events and (b) the $m_{p\pi} > 1.8$ GeV region. See the legend and caption of Fig. 2 for a description of the components.

LHCb, *Phys.Rev.Lett.* 117 (2016) 8, 082003, *Phys.Rev.Lett.* 117 (2016) 10, 109902 (addendum), *Phys.Rev.Lett.* 118 (2017) 119901 (addendum)



LHCb, Sci.Bull. 66 (2021) 1278-1287

LHCb, Phys.Rev.Lett. 131 (2023) 3, 031901

Crucial issues with the observed Pc pentaquarks

Questions:

• A direct production of Pc's would imply that a pair of $\Lambda_c^{(*)}\overline{D}^{(*)}$ will be created at leading order, while the production of the $\Sigma_c^{(*)}\overline{D}^{(*)}$ pair is via the color-suppressed transitions. What should be the production mechanism for the Pc's as the $\Sigma_c^{(*)}\overline{D}^{(*)}$ molecular states?



- What's the nature of the (*ud*) diquark?
- How $\Sigma_c \overline{D}$ get bound without pion exchange?

A novel feature that a loosely bound system is driven by the short-ranged interaction in the framework of hidden gauge symmetry dynamics.

[See Wu, Molina, Oset and Zou, PRL (2010).]

• The color suppressed diagram may not be so suppressed!



$$\langle Y_c \bar{K} \bar{D} | \hat{H}_w | \Lambda_b \rangle_{(c)}$$

$$= \frac{1}{2\sqrt{2}} \left[-\Sigma_c^{++} K^- D^- + \frac{1}{2} \Sigma_c^+ \bar{K}^0 D^- - \frac{1}{2} \Sigma_c^+ K^- \bar{D}^0 + \Sigma_c^0 \bar{K}^0 \bar{D}^0 + \frac{1}{2} \Lambda_c^+ K^- \bar{D}^0 - \frac{1}{2} \Lambda_c^+ \bar{K}^0 D^- \right]$$



ud diquark with quantum correlation



X.-H. Liu, Q. Wang, and Q. Zhao, PLB(2016); arXiv:1507.05359 [hep-ph]; P.-Y. Niu, J.-M. Richard, Q. Wang, Q. Zhao, Phys. Rev. D 102, 073005 (2020); Chin. Phys. C 45, no.1, 013101 (2021); P.-Y. Niu, Q. Wang and Q. Zhao, Phys. Lett. B 826, 136916
 (2022); M.-Y. Barabanov et al., Prog. Part. Nucl. Phys. 116, 103835 (2021)

An evidence for the quark correlation:

The hadronic weak decay of Λ_c

Color SU(3): $3 \otimes 3 \otimes 3 = (\overline{3} \oplus 6) \otimes 3 = (1 \oplus 8) \oplus (8 \oplus 10)$

Quark correlation \neq **compact structure**



U

P.-Y. Niu, J.-M. Richard, Q. Wang, Q. Zhao, Phys. Rev. D 102, 073005 (2020)

Rescattering to generate a pole?

- Favored by the molecular picture.
- Coupled channel picture?

[see Y. Yamaguchi and E. Santopinto, PRD96, 014018 (2017); N. Yalikun et al., PRD104, 094039 (2021)]





• Rescatterings via triangle diagrams



X.-H. Liu, Q. Wang, and Q. Zhao, PLB(2016); arXiv:1507.05359 [hep-ph] F.K. Guo, U.-G. Meissner, W. Wang and Z. Yang, PRD92, 071502 (2015); arXiv:1507.04950[hep-ph]

Thresholds for χ_{cJ} p

Threshold masses [MeV]	$\chi_{c0}(1P) 0^+$	$\chi_{c1}(1P) 1^+$	$\chi_{c2}(1P) 2^+$
$p \ 1/2^+$	4353	4449	4494





X.-H. Liu, Q. Wang, and Q. Zhao, PLB(2016); arXiv:1507.05359 [hep-ph]

Threshold structures arising from the TS mechanism involving both W emission and color-suppressed trans.



Threshold masses [MeV]	$\Lambda_c(2286) \ 1/2^+$	$\Lambda_c(2595) \ 1/2^-$	$\Lambda_c(2625) \ 3/2^-$	$\Lambda_c(2880) 5/2^+$
$\bar{D}_s(1968) \ 0^-$	4254	4563	4593	4848
$D_s^*(2112) \ 1^-$	4398	4707	4737	4994
$D_{s0}(2317) 0^+$	4585	4912	4942	5197
$D_{s1}(2460) \ 1^+$	4728	5055	50 85	5340
$\bar{D}_{s1}(2536) 1^+$	4822	5131	5161	5416
$\bar{D}_{s2}(2573) 2^+$	4859	5168	5198	5453
$\bar{D}_{s1}(2700) \ 1^-$	4986	5295	5325	5580
$D_{sJ}(2860)$??	5146	5455	5485	[5740]
$D_{sJ}(3040)$??	5331	[5636]	[5672]	[5926]

Threshold masses [GeV]	$\Sigma_c(2455) \ 1/2^+$	$\Sigma_c(2520) \ 3/2^+$	$\Sigma_c(2625)$??
$\bar{D}(1865) \ 0^{-}$	4.321	4.385	4.668
$\bar{D}^*(2007) \ 1^-$	4.463	4.527	4.810
$\bar{D}_1(2420) \ 1^+$	4.875	4.939	5.222
$\bar{D}_2(2460) \ 2^+$	4.917	4.981	5.264



- The TS is not sufficient for explaining the Run-II data. Pole structures are needed for those observed Pc signals.
- Do we have further evidences for understanding the nature of Pc's?

2. Novel phenomena arising from the Pc three-body and four-body decays

State	<i>M</i> [MeV]	Γ [MeV]	(95% C.L.)	R [%]
$P_c(4312)^+$	$4311.9\pm0.7^{+6.8}_{-0.6}$	$9.8\pm2.7^{+3.7}_{-4.5}$	(<27)	$0.30\pm0.07^{+0.34}_{-0.09}$
$P_c(4440)^+$	$4440.3 \pm 1.3^{+4.1}_{-4.7}$	$20.6 \pm 4.9^{+8.7}_{-10.1}$	(<49)	$1.11 \pm 0.33 ^{+0.22}_{-0.10}$
$P_c(4457)^+$	$4457.3\pm0.6^{+4.1}_{-1.7}$	$6.4\pm2.0^{+5.7}_{-1.9}$	(<20)	$0.53 \pm 0.16^{+0.15}_{-0.13}$

TABLE I. Summary of P_c^+ properties. The central values are based on the fit displayed in Fig. 6.

Two-body decay: Hidden charm decays are generally suppressed.

Three-body decay:

Hidden charm decays are further suppressed by the phase space. However, the presence of triangle singularity (TS) or box singularity (BS) may produce unique structures.





Exotics of Type-III:

Peak structures caused by kinematic effects, in particular, by triangle singularity.

$$\begin{split} \Gamma_3(s_1, s_2, s_3) \ &= \ \frac{1}{i(2\pi)^4} \int \frac{d^4 q_1}{(q_1^2 - m_1^2 + i\epsilon)(q_2^2 - m_2^2 + i\epsilon)(q_3^2 - m_3^2 + i\epsilon)} \\ &= \ \frac{-1}{16\pi^2} \int_0^1 \int_0^1 \int_0^1 da_1 \, da_2 \, da_3 \, \frac{\delta(1 - a_1 - a_2 - a_3)}{D - i\epsilon} \,, \end{split}$$

$$D \equiv \sum_{i,j=1}^{3} a_i a_j Y_{ij}, \ Y_{ij} = \frac{1}{2} \left[m_i^2 + m_j^2 - (q_i - q_j)^2 \right]$$

The TS occurs when all the three internal particles can approach their on-shell condition simultaneously:

$$\partial D/\partial a_j = 0$$
 for all j=1,2,3. \Box det $[Y_{ij}] = 0$

L. D. Landau, Nucl. Phys. 13, 181 (1959);

J.J. Wu, X.-H. Liu, Q. Zhao, B.-S. Zou, Phys. Rev. Lett. 108, 081003 (2012)
Q. Wang, C. Hanhart, Q. Zhao, Phys. Rev. Lett. 111, 132003 (2013); Phys. Lett. B 725, 106 (2013)
X.-H. Liu, M. Oka and Q. Zhao, PLB753, 297(2016)
M.-C. Du and Q. Zhao, Phys.Rev.D 100 (2019) 3, 036005
F.-K. Guo, C. Hanhart, U.-G. Meissner, Q. Wang, Q. Zhao, B.-S. Zou, Rev. Mod. Phys. 90, 015004 (2018)
F.-K. Guo, X.-H. Liu, and S. Sakai, Prog.Part.Nucl.Phys. 112 (2020) 103757

Triangle and box singularity in Pc three and four-body decays



- Although the $\Lambda_c \overline{D}^{(*)}$ interactions would not dynamically generate pole structures, narrow peaks may appear at the thresholds of $\Lambda_c \overline{D}^{(*)}$ due to the TS and BS mechanism.
- Near-threshold $\Sigma_c^{(*)}\overline{D}^{(*)}$ interactions will feed into the TS and BS mechanism and contribute to the $\Lambda_c\overline{D}^{(*)}$ peaks in the $J/\psi p$ invariant mass spectrum.

A feed-down mechanism for producing the enhancements at the $\Lambda_c \overline{D}^{(*)}$ thresholds



Collinear pairs of $\Sigma_c^{(*)}\overline{D}^{(*)}$ produced at LHC may rescatter into the $J/\psi p\pi$ or $J/\psi p\pi\pi$ channel via the TS/BS mechanism, and produce narrow structures at the $\Lambda_c\overline{D}^{(*)}$ thresholds in the $J/\psi p$ or $J/\psi p\pi$ spectra. Effective Lagrangians for the interaction vertices:

$$\begin{aligned} \mathcal{L}_{P_{c}(4312)\Sigma_{c}\bar{D}} &= g_{P_{c}(4312)}\bar{D}^{\dagger}\bar{\Sigma}_{c}P_{c}, \\ \mathcal{L}_{P_{c}(4380)\Sigma_{c}^{*}\bar{D}} &= g_{P_{c}(4380)}\bar{D}^{\dagger}\bar{\Sigma}_{c}^{*}\cdot P_{c}, \\ \mathcal{L}_{P_{c}(4440)\Sigma_{c}\bar{D}^{*}} &= g_{P_{c}(4440)}\bar{D}^{*\mu\dagger}\bar{\Sigma}_{c}\gamma_{5}\tilde{\gamma}_{\mu}(p_{A})P_{c}, \\ \mathcal{L}_{P_{c}(4457)\Sigma_{c}\bar{D}^{*}} &= g_{P_{c}(4457)}\bar{\Sigma}_{c}\bar{D}^{*\dagger}\cdot P_{c}, \end{aligned}$$

The coupling strength is determined by the t-channel scattering with the heavy meson exchange and the Lagrangians are:

$$\begin{aligned} \mathcal{L}_{\Lambda_c Dp} &= i g_{DN\Lambda_c} D^{\dagger} \bar{N} \gamma_5 \Lambda_c, \\ \mathcal{L}_{J/\psi D\bar{D}} &= g_{J/\psi D\bar{D}} (D \partial_{\mu} \bar{D} - \partial_{\mu} D \bar{D}) \psi^{\mu}, \end{aligned}$$



The triangle loop amplitudes have the following forms:

$$\begin{split} \mathcal{M}^{P_{c}(4312) \rightarrow J/\psi p\pi} \\ &= \int \frac{dp_{\Lambda_{c}}^{4}}{(2\pi)^{4}} \bar{u}_{p} \gamma_{5} \gamma_{\mu} \varepsilon_{J/\psi}^{*\mu} (p_{\Lambda_{c}} + m_{\Lambda_{c}}) \gamma_{5} \gamma_{\nu} p_{\pi}^{\mu} (p_{\Sigma_{c}} + m_{\Sigma_{c}}) u_{P_{c}} \\ &\times \frac{g_{P_{c}(4312)} g_{\Sigma_{c}\Lambda_{c}\pi} g_{x} \mathcal{F}^{2}(p_{\Lambda_{c}}^{2})}{(p_{\Sigma_{c}}^{2} - m_{\Sigma_{c}}^{2})(p_{D}^{2} - m_{D}^{2})(p_{\Lambda_{c}}^{2} - m_{\Lambda_{c}}^{2})}, \end{split}$$

 $\mathcal{M}^{P_c(4440)\to J/\psi p\pi\pi}$

$$= \int \frac{d^4 p_D}{(2\pi)^4} (-g^{\alpha \rho} + \frac{p_{D^*}^{\alpha} p_{D^*}^{\rho}}{m_{D^*}^2}) p_{\pi \rho} \\ \times \bar{u}_p \gamma_5 \gamma_\mu \varepsilon_{J/\psi}^{*\mu} (p_{\Lambda_c} + m_{\Lambda_c}) \gamma_5 \gamma_\nu p_{\pi}^{\nu} (p_{\Sigma_c} + m_{\Sigma_c}) \gamma_5 \tilde{\gamma}_\alpha u_{P_c} \\ \times \frac{g_{P_c}(4440) g_{\Sigma_c^* \Lambda_c \pi} g_x g_{D^* D \pi} \mathcal{F}^2(p_{\Lambda_c}^2)}{(p_{\Sigma_c}^2 - m_{\Sigma_c}^2)(p_{D^*}^2 - m_{D^*}^2)(p_{\Lambda_c}^2 - m_{\Lambda_c}^2)(p_D^2 - m_D^2)},$$

$$\begin{split} \mathcal{M}^{P_{c}(4380) \to J/\psi p\pi} \\ &= \int \frac{d^{4} p_{\Lambda_{c}}}{(2\pi)^{4}} \bar{u}_{p} \gamma_{5} \gamma_{\mu} \varepsilon_{J/\psi}^{*\mu} (p_{\Lambda_{c}} + m_{\Lambda_{c}}) p_{\pi\nu} (p_{\Sigma_{c}} + m_{\Sigma_{c}}) \\ &\times [-g^{\nu\alpha} + \frac{1}{3} \gamma^{\nu} \gamma^{\alpha} + \frac{1}{3m_{\Sigma_{c}}} (\gamma^{\nu} p^{\alpha} - \gamma^{\alpha} p^{\nu}) + \frac{2}{3p_{\Sigma_{c}}^{2}} p_{\Sigma_{c}}^{\nu} p_{\Sigma_{c}}^{\alpha}] \\ &\times u_{P_{c}\alpha} \frac{g_{P_{c}(4380)} g_{\Sigma_{c}^{*}\Lambda_{c}\pi} g_{x} \mathcal{F}^{2}(p_{\Lambda_{c}}^{2})}{(p_{\Sigma_{c}^{*}}^{2} - m_{\Sigma_{c}^{*}}^{2})(p_{D}^{2} - m_{D}^{2})(p_{\Lambda_{c}}^{2} - m_{\Lambda_{c}}^{2})}, \end{split}$$

 $\mathcal{M}^{P_c(4457)\to J/\psi p\pi\pi}$

$$= \int \frac{d^4 p_D}{(2\pi)^4} \bar{u}_p \gamma_5 \gamma_\mu \varepsilon_{J/\psi}^{*\mu} (p_{\Lambda_c} + m_{\Lambda_c}) \gamma_5 \gamma_\nu p_\pi^\nu (p_{\Sigma_c} + m_{\Sigma_c}) u_{P_c \alpha} \\ \times (-g^{\alpha\beta} + \frac{p_{D^*}^\alpha p_{D^*}^\beta}{m_{D^*}^2}) p_{\pi\beta} \\ \times \frac{g_{P_c}(4457) g_{\Sigma_c^* \Lambda_c \pi} g_x g_{D^* D \pi} \mathcal{F}^2(p_{\Lambda_c}^2)}{(p_{\Sigma_c}^2 - m_{\Sigma_c}^2)(p_{D^*}^2 - m_{D^*}^2)(p_{\Lambda_c}^2 - m_{\Lambda_c}^2)(p_D^2 - m_D^2)}.$$

where a monopole form factor is adopted to regularize the UV divergence:

$$\mathcal{F}(q^2) = (\Lambda^2 - m_q^2)/(q^2 - m_q^2)$$
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The invariant mass spectra of $J/\psi p$ for the exclusive decays of Pc states into $J/\psi p\pi$ and/or $J/\psi p\pi\pi$ channels.



• Relatively large phase space for $\Sigma_c^* \to \Lambda_c \pi$ within the TS kinematic region leads to the strong enhancement in $Pc(4380) \to J/\psi p\pi$.

• Such an effect actually will add additional partial decay widths to the Pc(4380) decay.

The $J/\psi p\pi$ invariant mass spectra for $P_c(4440), P_c(4457) \rightarrow J/\psi p\pi\pi$





- Note that the $\Lambda_c \overline{D}^{(*)}$ thresholds also appear in $\Lambda_b \to K^- J/\psi p$. However, they only contribute as CUSP structures which is subleading to the TS/BS contributions.
- A narrow structure in the $\Lambda_c \overline{D}^{(*)}$ spectra is a direct evidence for the TS/BS mechanisms.



The accumulated $J/\psi p$ (left) and $J/\psi p\pi$ (right) invariant mass spectra from all different Pc states

$P_c(4380)$ (red dashed) dominant



Feed-down mechanism:

All semi-inclusive $J/\psi p$ events in heavy-ion collisions may produce narrow structures at the thresholds of $\Lambda_c \overline{D}$ and $\Lambda_c \overline{D}^*$.

 $P_c(4457)$ (red dashed)

 $P_c(4440)$ (blue dot-dashed)

3. Comments on the J/psi photoproduction near threshold

Photoproduction will provide crucial evidence for understanding the Pc's nature



Photoproduction mechanism:



S. Adhikari et al. [GlueX], Phys. Rev. C 108, no.2, 025201 (2023)

Exclusive and inclusive contributions from different open threshold channels



- The photoproduction process will pick up the open threshold first.
- The production of Pc's is relatively suppressed by their small couplings to *J*/ψ*p* which means that higher statistics are still needed.
- Processes of $\gamma p \rightarrow J/\psi p\pi$ and $J/\psi p\pi\pi$ are useful for further disentangling the role played by the TS/BS though the measurement would be challenging.

Polarized beam asymmetry measurement:

The density matrix elements of the vector meson is defined as:

$$\rho_{\lambda_{v}\lambda_{v}'}(V) = \frac{1}{N} \sum_{\lambda_{f}\lambda_{\gamma}\lambda_{i}\lambda_{\gamma}'} T_{\lambda_{v}\lambda_{f},\lambda_{\gamma}\lambda_{i}} \rho_{\lambda_{\gamma}\lambda_{\gamma}'}(\gamma) T_{\lambda_{v}'\lambda_{f},\lambda_{\gamma}'\lambda_{i}}^{*}$$

with $N \equiv \frac{1}{2} \sum_{\lambda_v \lambda_f \lambda_\gamma \lambda_i} |T_{\lambda_v \lambda_f, \lambda_\gamma \lambda_i}|^2$ as the normalization factor.

The polarized-photon density matrix element is defined as:

$$\rho(\boldsymbol{\gamma}) = \frac{1}{2}(I_{\boldsymbol{\gamma}} + \boldsymbol{\sigma} \cdot \mathbf{P}_{\boldsymbol{\gamma}})$$

 P_{γ} determines both the degree of polarization (via its magnitude p_{γ}) and the polarization direction.

$$\begin{bmatrix} \mathbf{P}_{\gamma} = P_{\gamma}(-\cos 2\Phi, -\sin 2\Phi, 0) & \text{for transversely polarized photon} \\ \mathbf{P}_{\gamma} = P_{\gamma}(0, 0, \lambda_{\gamma}) \text{ with } \lambda_{\gamma} = \pm 1 & \text{for longitudinally polarized photon} \end{bmatrix}$$



The familiar form of the vector meson density matrix elements can be obtained:

$$\begin{split} \rho_{\lambda_{v}\lambda_{v}'}^{0} &= \frac{1}{2N} \sum_{\lambda_{\gamma}\lambda_{f}\lambda_{i}} T_{\lambda_{v}\lambda_{f},\lambda_{\gamma}\lambda_{i}} T_{\lambda_{v}'\lambda_{f},\lambda_{\gamma}\lambda_{i}}^{*}, \\ \rho_{\lambda_{v}\lambda_{v}'}^{1} &= \frac{1}{2N} \sum_{\lambda_{\gamma}\lambda_{f}\lambda_{i}} T_{\lambda_{v}\lambda_{f},-\lambda_{\gamma}\lambda_{i}} T_{\lambda_{v}'\lambda_{f},\lambda_{\gamma}\lambda_{i}}^{*}, \\ \rho_{\lambda_{v}\lambda_{v}'}^{2} &= \frac{i}{2N} \sum_{\lambda_{\gamma}\lambda_{f}\lambda_{i}} \lambda_{\gamma} T_{\lambda_{v}\lambda_{f},-\lambda_{\gamma}\lambda_{i}} T_{\lambda_{v}'\lambda_{f},\lambda_{\gamma}\lambda_{i}}^{*}, \\ \rho_{\lambda_{v}\lambda_{v}'}^{3} &= \frac{i}{2N} \sum_{\lambda_{\gamma}\lambda_{f}\lambda_{i}} \lambda_{\gamma} T_{\lambda_{v}\lambda_{f},\lambda_{\gamma}\lambda_{i}} T_{\lambda_{v}'\lambda_{f},\lambda_{\gamma}\lambda_{i}}^{*}. \end{split}$$

The decomposition of the vector meson decay distribution in terms of the initial photon polarizations gives $W(\cos \theta_c, \phi_c, \rho) = W^0(\cos \theta_c, \phi_c, \rho^0)$ $+ \sum^3 P^{\alpha}_{\gamma} W^{\alpha}(\cos \theta_c, \phi_c, \rho^{\alpha})$

The polarized beam asymmetry can be expressed as

 $\alpha = 1$

$$\check{\Sigma} = \frac{\rho_{00}^1 + 2\rho_{11}^1}{\rho_{00}^0 + 2\rho_{11}^0}$$

Thanks for your attention!



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http://fb23.ihep.ac.cn/

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Kinematic features of the production mechanism



1) Forward angle peaking is predominant due to the diffractive process, i.e. Pomeron

- 2) S-channel resonance excitations contribute to the cross sections at middle and backward
- 3) U-channel contributes to backward angles.

Interferences from different transition

Q. Wang, X.-H. Liu, and Q. Z., PRD92, 034022 (2015); arXiv:1508.00339 [hep-ph]

s and u-channel pentaquark production



Coupling vertices for γNP_c **:**

$$\begin{split} \mathcal{L}_{\gamma N P_{c}}^{3/2^{\pm}} &= \frac{ieh_{1}}{2M_{N}} \bar{N} \Gamma_{\nu}^{(\pm)} F^{\mu\nu} P_{c\mu} - \frac{eh_{2}}{(2M_{N})^{2}} \partial_{\nu} \bar{N} \Gamma^{(\pm)} F^{\mu\nu} P_{c\mu} \\ &+ \text{H.c.}, \\ \mathcal{L}_{\gamma N P_{c}}^{5/2^{\pm}} &= \frac{eh_{1}}{(2M_{N})^{2}} \bar{N} \Gamma_{\nu}^{(\mp)} \partial^{\alpha} F^{\mu\nu} P_{c\mu\alpha} \\ &- \frac{ieh_{2}}{(2M_{N})^{3}} \partial_{\nu} \bar{N} \Gamma_{\nu}^{(\mp)} \partial^{\alpha} F^{\mu\nu} P_{c\mu\alpha} + \text{H.c.}, \qquad \Gamma_{\mu}^{(\pm)} \equiv \binom{\gamma_{\mu} \gamma_{5}}{\gamma_{\mu}}, \qquad \Gamma^{(\pm)} \equiv \binom{\gamma_{5}}{1}, \end{split}$$

S. H. Kim, S. i. Nam, Y. Oh and H. C. Kim, PRD 84, 114023 (2011) Q. Wang, X.-H. Liu, and Q. Zhao, PRD92 (2015) 034022; arXiv:1508.00339 [hep-ph]

Coupling vertices for $J/\psi NP_c$:

$$\mathcal{L}_{P_{c}N\psi}^{3/2^{\pm}} = -\frac{ig_{1}}{2M_{N}}\bar{N}\Gamma_{\nu}^{(\pm)}\psi^{\mu\nu}P_{c\mu} - \frac{g_{2}}{(2M_{N})^{2}}\partial_{\nu}\bar{N}\Gamma^{(\pm)}\psi^{\mu\nu}P_{c\mu} + \frac{g_{3}}{(2M_{N})^{2}}\bar{N}\Gamma^{(\pm)}\partial_{\nu}\psi^{\mu\nu}P_{c\mu} + H.c. ,$$

$$\mathcal{L}_{P_{c}N\psi}^{5/2^{\pm}} = \frac{g_{1}}{(2M_{N})^{2}}\bar{N}\Gamma_{\nu}^{(\mp)}\partial^{\alpha}\psi^{\mu\nu}P_{c\mu\alpha} - \frac{ig_{2}}{(2M_{N})^{3}}\partial_{\nu}\bar{N}\Gamma^{(\mp)}\partial^{\alpha}\psi^{\mu\nu}P_{c\mu\alpha} + \frac{ig_{3}}{(2M_{N})^{3}}\bar{N}\Gamma^{(\mp)}\partial^{\alpha}\partial_{\nu}\psi^{\mu\nu}P_{c\mu\alpha} + H.c.$$

Leading transition matrix elements:

$$\mathcal{M}^{3/2^{\pm}} = \frac{1}{s - M_{P_c}^2} \frac{eh_1 g_1}{(2M_N)2} \epsilon^*_{\psi\nu} \bar{u}_N \Gamma^{(\pm)}_{\sigma} \Delta_{\beta\alpha} (P_c, k+p) \Gamma^{(\pm)}_{\delta} (k^{\alpha} g^{\mu\delta} - k^{\delta} g^{\alpha\mu}) u_N \epsilon_{\gamma\mu} ,$$

$$\mathcal{M}^{5/2^{\pm}} = \frac{1}{s - M_{P_c}^2} \frac{eh_1 g_1}{(2M_N)4} \epsilon^*_{\psi\nu} \bar{u}_N q^{\sigma} (q^{\rho} g^{\nu\delta} - q^{\delta} g^{\nu\rho}) \Delta_{\rho\sigma; \alpha\beta} (P_c, k+p) \Gamma^{(\mp)}_{\lambda} k^{\beta} (k^{\alpha} g^{\mu\lambda} - k^{\lambda} g^{\alpha\mu}) u_N \epsilon_{\gamma\mu} ,$$

Rarita-Schwinger spin projections:

$$\begin{split} \Delta_{\beta\alpha}(B,p) &= \left(\not\!\!p + M_B \right) \left[-g_{\beta\alpha} + \frac{1}{3} \gamma_\beta \gamma_\alpha + \frac{1}{3M_B} (\gamma_\beta p_\alpha - \gamma_\alpha p_\beta) + \frac{2}{3M_B^2} p_\beta p_\alpha \right] , \\ \Delta_{\rho\sigma; \ \alpha\beta}(B,p) &= \left(\not\!\!p + M_B \right) \left[\frac{1}{2} (\bar{g}_{\rho\alpha} \bar{g}_{\sigma\beta} + \bar{g}_{\rho\beta} \bar{g}_{\sigma\alpha}) - \frac{1}{5} \bar{g}_{\rho\sigma} \bar{g}_{\alpha\beta} - \frac{1}{10} (\bar{\gamma}_\rho \bar{\gamma}_\alpha \bar{g}_{\sigma\beta} + \bar{\gamma}_\rho \bar{\gamma}_\beta \bar{g}_{\sigma\alpha} + \bar{\gamma}_\sigma \bar{\gamma}_\alpha \bar{g}_{\rho\beta} + \bar{\gamma}_\sigma \bar{\gamma}_\beta \bar{g}_{\rho\alpha}) \right] \\ \mathbf{with} \quad - \begin{bmatrix} \bar{g}_{\alpha\beta} &= g_{\alpha\beta} - \frac{p_\alpha p_\beta}{M_B^2} , \\ \bar{\gamma}_\alpha &= \gamma_\alpha - \frac{p_\alpha}{M_B^2} \not\!\!p . \end{split}$$

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Vector meson dominance



By assuming that the $J/\psi\,p$ saturate the decay widths of the Pc states, we have

$$g_{\frac{3}{2}^+} = 1.07, \quad g_{\frac{3}{2}^-} = 1.40, \quad g_{\frac{5}{2}^+} = 2.56, \quad g_{\frac{5}{2}^-} = 5.58 \ ,$$

A form factor is included:

$$\mathcal{F}(p^2) = \frac{\Lambda^4}{\Lambda^4 + (p^2 - M_{P_c}^2)^2}$$
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Total cross sections predicted:









Predicted differential cross sections at different energies:



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Predicted differential cross sections at different energies:



Invariant mass distribution of J/ ψ p with different K-p momentum cuts

(a) $m_{Kp} < 1.55 \text{ GeV}$, (b) 1.55 GeV $< m_{Kp} < 1.07 \text{ GeV}$, (c) 1.07 GeV $< m_{Kp} < 12.0 \text{ GeV}$, (d) $m_{Kp} > 2.0 \text{ GeV}$.



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The ATS can mimic a resonance behavior in certain cases



F.K. Guo, U.-G. Meissner, W. Wang and Z. Yang, PRD92, 071502 (2015); arXiv:1507.04950[hep-ph] 38