12th Workshop on Hadron Physics and Opportunities Worldwide

# Probing Nuclear Structure at the Ultra-Relativistic Heavy-Ion Collisions

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#### Nuclear structure at low energies

Atomic nuclei have rich phenomenology. Rooted in the strong nuclear force. Nuclear structure is a very old field. Many different approaches.



#### Modern ab-initio methods have successfully described light nuclei with A $\leq$ 50

For heavy nuclei, computational complexity rapidly arises due to the increasing number of nucleons



#### Nuclear structure at high energies



#### From final state to nuclear structure

nucleon density described by Woods-Saxon profile

$$\rho(r,\theta,\phi) = \frac{\rho_0}{1+e^{[r-R(\theta,\phi)]/a_0}},$$
  

$$R(\theta,\phi) = R_0(1+\beta_2[\cos\gamma Y_{2,0}+\sin\gamma Y_{2,2}]),$$

 $\beta_2$ : overall deformation parameter  $a_0$ : diffuseness parameter



#### From final state to nuclear structure

nucleon density described by Woods-Saxon profile

$$\rho(r,\theta,\phi) = \frac{\rho_0}{1+e^{[r-R(\theta,\phi)]/a_0}},$$
$$R(\theta,\phi) = R_0(1+\beta_2[\cos\gamma Y_{2,0}+\sin\gamma Y_{2,2}]),$$

 $\gamma$ : traxiality parameter





overlap

overlap

overlap

#### From final state to nuclear structure

Most of nuclear structure studies on GeV energies are inplemented in the isobar runs of  ${}^{96}Ru+{}^{96}Ru$  and  ${}^{96}Zr+{}^{96}Zr$  in RHIC

B. Bally et al., Phys.Rev.Lett. 128 (2022) 8, 082301

129Xe

<sup>129</sup>Xe is predicted to have deformed and triaxial structure ( $r_1 \neq r_2 \neq r_3$ ).

J. Jia, Phys. Rev. Lett. 131 no. 2, (2023) 022301
J. Jia, Chin. Phys. Lett. 40 no. 4, (2023) 042501
S. Zhao, Phys. Lett. B 839 (2023) 137838
etc...

 $\beta_2 = 0.2, \gamma = 30^{\circ}$ 



J. Jia, Phys.Rev.C 105 (2022) 4, 044905



At the LHC,

129Xe

## **Centrality determination**

A very important value in NS at high energies

Centrality: a percentage of the hadronic cross section corresponding to a particle multiplicity, directly related to the impact parameter

0% centrality: almost fully overlap 90% centrality: peripheral collisions



#### **ALICE detector and data sample**

#### 1. Inner Tracking System (ITS)

• Tracking and triggering

#### 2. V0 detector

- Triggering and event
- centrality determination

#### 3. Time Projection Chamber (TPC)

• Tracking



Kinematic region:  $0.2 < p_T < 3.0 \text{ GeV/c}$  $|\eta| < 0.8$ 



## Anisotropic flow



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# Sensitivity in model

stronger initial geometric anisotropy (more elliptical)

larger  $\beta_2$ 

stronger azimuthal anisotropy larger  $v_2$ 





AMP1: Z. Lu et al., Eur. Phys. J. A (2023) 279, arXiv:2309.09663

# Sensitivity in model



AMPT: Z. Lu et al., Eur. Phys. J. A 59 (2023) 279, arXiv:2309.09663

60

Centrality percentile



different azimuthal distributions of final-state particles

## **Probe nuclear deformation of <sup>129</sup>Xe with flow**



- Significant v<sub>2</sub> enhancements in central Xe-Xe collisions
- LHC data clearly suggests a non-zero  $\beta_2$  (deformation of <sup>129</sup>Xe)

## **Probe nuclear deformation of** <sup>129</sup>**Xe with differential flow**

![](_page_14_Figure_1.jpeg)

# Probe deformation of <sup>129</sup>Xe with $\Psi_n - \Psi_m$ correlation

 $\rho_{422} \approx \langle \cos(4\Psi_4 - 4\Psi_2) \rangle$ 

![](_page_15_Picture_2.jpeg)

ψ4

For Pb–Pb

Central collisions:

- Initial  $\phi_2$ ,  $\phi_4$  randomly fluctuate, weak correlations
- $<\cos 4(\psi_2 \psi_4) > \text{ is small}$

Peripheral collisions:

- Initial  $\varphi_2$ ,  $\varphi_4$  tend to align, strong correlations
- $<\cos 4(\psi_2 \psi_4) > \text{ is large}$

![](_page_15_Figure_11.jpeg)

• A stronger correlation is observed in the Xe-Xe collisions because of deformation

## Probe nuclear shape of <sup>129</sup>Xe with systematic flow studies

![](_page_16_Figure_1.jpeg)

- Promising sensitivities to the nuclear deformation  $\beta_2$  in central Xe-Xe collisions and nuclear skin  $a_0$  in the mid-central collisions
- Insensitive to triaxial structure

## **Radial flow and [p<sub>T</sub>] correlation**

![](_page_17_Figure_1.jpeg)

![](_page_17_Figure_2.jpeg)

![](_page_17_Picture_3.jpeg)

system expansion leads to an additional overall boost in momentum

Size of the QGP: radial flow, [p<sub>T</sub>]

## **Radial flow and [p<sub>T</sub>] correlation**

![](_page_18_Figure_1.jpeg)

ALICE, PRC88 (2013) 044910, PRL111 (2013) 222301

![](_page_18_Figure_3.jpeg)

![](_page_18_Figure_4.jpeg)

[G. Giacalone et al., PRC103 (2021) 2, 024909]

8-Aug-2024

## **Radial flow and [p<sub>T</sub>] correlation**

Multi-particle [p<sub>T</sub>] correlations:

![](_page_19_Figure_2.jpeg)

[p<sub>T</sub>] and its event-by-event fluctuations measured in heavy-ion collisions at the LHC -> probe initial size and size fluctuations

## Probe NS of <sup>129</sup>Xe with 2-particle [p<sub>T</sub>] correlation

$$[p_{\mathrm{T}}^{(m)}] = rac{\displaystyle\sum_{k_1
eq \ldots
eq k_m}^M w_{k_1}\cdot\ldots\cdot w_{k_m} p_{\mathrm{T},k_1}\cdot\ldots\cdot p_{\mathrm{T},k_m}}{\displaystyle\sum_{k_1
eq \ldots
eq k_m}^M w_{k_1}\cdot\ldots\cdot w_{k_m}},$$

[p<sub>T</sub>] cumulants in recursion formula:

$$\kappa_m = \langle [p_{\mathrm{T}}^{(m)}] \rangle - \sum_{k=1}^{m-1} \binom{m-1}{k-1} \langle [p_{\mathrm{T}}^{(m-k)}] \rangle \kappa_k$$

Final state cumulant	Initial state cumulant	Liquid-drop model
$\kappa_2$	$\left< \left( rac{\delta d_\perp}{d_\perp}  ight)^2 \right>$	$rac{1}{32\pi}\langleeta_2^2 angle$
$\kappa_3$	$\left< \left( rac{\delta d_\perp}{d_\perp}  ight)^3 \right>$	$rac{\sqrt{5}}{896\pi^{3/2}}\langle\cos(3\gamma)eta_2^3 angle$

$$d_{\perp} = \sqrt{N_{\mathrm{part}}/\langle r_{\perp}^2 
angle},$$

![](_page_20_Figure_6.jpeg)

These two-particle p<sub>T</sub> correlations provide a new way to probe deformation structures of <sup>129</sup>Xe

# Probe NS of <sup>129</sup>Xe with multi-particle [p<sub>T</sub>] correlation

$$[p_{\mathrm{T}}^{(m)}] = rac{\displaystyle\sum_{k_1 
eq \dots 
eq k_m}^M w_{k_1} \cdot \dots \cdot w_{k_m} p_{\mathrm{T},k_1} \cdot \dots \cdot p_{\mathrm{T},k_m}}{\displaystyle\sum_{k_1 
eq \dots 
eq k_m}^M w_{k_1} \cdot \dots \cdot w_{k_m}},$$
 $\kappa_m = \langle [p_{\mathrm{T}}^{(m)}] 
angle - \sum_{k=1}^{m-1} inom{m-1}{k-1} \langle [p_{\mathrm{T}}^{(m-k)}] 
angle \kappa_k.$ 
Final state Initial state Liquid-drop model
 $rac{1}{\kappa_2} \left\langle \left(rac{\delta d_{\perp}}{d_{\perp}}
ight)^2 
ight
angle rac{1}{32\pi} \langle eta_2^2 
angle}{\displaystyle\kappa_3} \left\langle \left(rac{\delta d_{\perp}}{d_{\perp}}
ight)^3 
ight
angle rac{\sqrt{5}}{896\pi^{3/2}} \langle \cos(3\gamma) eta_2^3,$ 

• Multi-particle [p<sub>T</sub>] correlation reflects the initial size fluctuations, also bring new information on the triaxial structure.

![](_page_21_Figure_3.jpeg)

# v<sub>n</sub>-[p<sub>T</sub>] correlations

![](_page_22_Figure_1.jpeg)

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#### Probe triaxial structure of <sup>129</sup>Xe

![](_page_23_Figure_1.jpeg)

- "Standard" flow observables fail to probe  $\gamma$  (EPJA 59 (2023) 279)
- $v_n$ -[ $p_T$ ] correlations have significant sensitivities to  $\gamma$
- Better agreement between LHC data and calculations with  $\gamma = 26.93^{\circ}$

#### Neutron skin of <sup>208</sup>Pb

#### PRL 131, 202302

![](_page_24_Figure_2.jpeg)

## Extracting neutron skin of <sup>208</sup>Pb

#### CERN

#### Thick-skinned: Using heavy-ion collisions at the LHC, scientists determine the thickness of neutron "skin" in lead-208 nuclei

This is the first measurement of the neutron skin of lead-208 using exchanges predominantly involving gluons and it can provide insight into the structure of nuclei and neutron stars

15 NOVEMBER, 2023 | By Naomi Dinmore

![](_page_25_Picture_5.jpeg)

![](_page_25_Figure_6.jpeg)

## more applications at HIC

#### More than just flow and [pT]

PHYSI covering nucle	CAL R	REVIEW	С						
Highlights	Recent	Accepted	Collections	Authors	Referees	Search	Press	About	Editorial Tean
Open Access									
Effect of initial nuclear deformation on dielectron photoproduction in hadronic heavy-ion collisions									
Jiaxuan Luo, Xinbai Li, Zebo Tang, Xin Wu, and Wangmei Zha Phys. Rev. C <b>108</b> , 054906 – Published 27 November 2023									

![](_page_26_Picture_3.jpeg)

 Experimental measurements at the RHIC/LHC enable a novel tool to probe the nuclear structure, complementary to the lowenergy studies

- NS at low energies covers much wider range in the nuclide chart
- NS at high energies enables novel opportunity to resolve some challenging questions (many-body, shape etc) with a few selected nuclei

## **Thanks for your attention!** 28

![](_page_28_Picture_0.jpeg)

![](_page_28_Picture_1.jpeg)

#### Zhiyong Lu(CIAE)

#### **Final state cancellation**

Theorist:

- the cancellation can be seen in the PCC correlation between the initial state and final state
- Basically, the two systems have the same linear correlation between initial and final, which suggests the same final state effects.

 $Q_n = \frac{\langle v_n \varepsilon_n \cos n \left( \psi_n - \phi_n \right) \rangle}{\sqrt{\langle v_n^2 \rangle \langle \varepsilon_n^2 \rangle}}$ 

![](_page_29_Figure_6.jpeg)

#### Zhiyong Lu(CIAE)

# multi-particle [pT] correlation

$$\frac{\delta d_{\perp}}{d_{\perp}} = \sqrt{\frac{5}{16\pi}} \beta_2 \left( \cos(\gamma) D_{0,0}^2(\Omega) + \frac{\sin(\gamma)}{\sqrt{2}} [D_{0,2}^2(\Omega) + D_{0,-2}^2(\Omega)] \right)$$

$$d_{\perp} = \sqrt{N_{\rm part}/\langle r_{\perp}^2 \rangle}$$

Final state cumulant	Initial state cumulant	Liquid-drop model			
$\kappa_2$	$\left< \left( rac{\delta d_\perp}{d_\perp}  ight)^2 \right>$	$\frac{1}{32\pi}\langle eta_2^2  angle$			
$\kappa_3$	$\left< \left( \frac{\delta d_\perp}{d_\perp} \right)^3 \right>$	$\frac{\sqrt{5}}{896\pi^{3/2}}\langle\cos(3\gamma)\beta_2^3\rangle$			
$\kappa_4$	$\left\langle \left( \frac{\delta d_{\perp}}{d_{\perp}} \right)^4 \right\rangle - 3 \cdot \left\langle \left( \frac{\delta d_{\perp}}{d_{\perp}} \right)^2 \right\rangle^2$	$-rac{3}{14336\pi^2}(7\langleeta_2^2 angle-5\langleeta_2^4 angle)$			
$\kappa_5$	$\left\langle \left(\frac{\delta d_{\perp}}{d_{\perp}}\right)^5 \right\rangle - 10 \cdot \left\langle \left(\frac{\delta d_{\perp}}{d_{\perp}}\right)^3 \right\rangle \cdot \left\langle \left(\frac{\delta d_{\perp}}{d_{\perp}}\right)^2 \right\rangle$	$-\frac{5\sqrt{5}}{315392\pi^{5/2}}(11\langle\cos(3\gamma)\beta_2^3\rangle\langle\beta_2^2\rangle-5\langle\beta_2^5\rangle)$			
$\kappa_6$	$\left\langle \left(\frac{\delta d_{\perp}}{d_{\perp}}\right)^{6} \right\rangle - 15 \cdot \left\langle \left(\frac{\delta d_{\perp}}{d_{\perp}}\right)^{4} \right\rangle \cdot \left\langle \left(\frac{\delta d_{\perp}}{d_{\perp}}\right)^{2} \right\rangle$	$\frac{5}{918412504\pi^3} (42042\langle\beta_2^2\rangle^3 - 5720\langle\cos(3\gamma)\beta_2^3\rangle^2$			
	$+30 \cdot \left\langle \left(\frac{\delta d_{\perp}}{d_{\perp}}\right)^2 \right\rangle^3 - 10 \cdot \left\langle \left(\frac{\delta d_{\perp}}{d_{\perp}}\right)^3 \right\rangle^2$	$-45045\langle\beta_2^2\rangle\langle\beta_2^4\rangle+8575\langle\beta_2^6\rangle+700\langle\cos(6\gamma)\beta_2^6\rangle)$			
$\kappa_7$	$\left\langle \left(\frac{\delta d_{\perp}}{d_{\perp}}\right)^7 \right\rangle - 21 \cdot \left\langle \left(\frac{\delta d_{\perp}}{d_{\perp}}\right)^5 \right\rangle \cdot \left\langle \left(\frac{\delta d_{\perp}}{d_{\perp}}\right)^2 \right\rangle$	$-\frac{15\sqrt{5}}{524812288}(2002\langle\beta_{2}^{2}\rangle^{2}\langle\cos(3\gamma)\beta_{2}^{3}\rangle$			
	$+210 \cdot \left\langle \left(\frac{\delta d_{\perp}}{d_{\perp}}\right)^3 \right\rangle \cdot \left\langle \left(\frac{\delta d_{\perp}}{d_{\perp}}\right)^2 \right\rangle^2$	$+715\langle\cos(3\gamma)\beta_2^3\rangle\langle\beta_2^4\rangle$			
	$-35 \cdot \left\langle \left(\frac{\delta d_{\perp}}{d_{\perp}}\right)^3 \right\rangle \cdot \left\langle \left(\frac{\delta d_{\perp}}{d_{\perp}}\right)^4 \right\rangle$	$+910\langle\cos(3\gamma)\beta_2^5\rangle\langle\beta_2^2\rangle-175\cos(3\gamma)\beta_2^7\rangle)$			
κ8	$\left\langle \left(\frac{\delta d_{\perp}}{d_{\perp}}\right)^{8} \right\rangle - 28 \cdot \left\langle \left(\frac{\delta d_{\perp}}{d_{\perp}}\right)^{6} \right\rangle \cdot \left\langle \left(\frac{\delta d_{\perp}}{d_{\perp}}\right)^{2} \right\rangle$	$\frac{5}{142748942336\pi^4} (2144142 \langle \beta_2^2 \rangle^4 - 3063060 \langle \beta_2^2 \rangle^2 \langle \beta_2^4 \rangle$			
	$+420 \cdot \left\langle \left(\frac{\delta d_{\perp}}{d_{\perp}}\right)^4 \right\rangle \left\langle \left(\frac{\delta d_{\perp}}{d_{\perp}}\right)^2 \right\rangle^2$	$-340\langle\beta_2^2\rangle \bigg(2288\langle\cos(3\gamma)\beta_2^3\rangle^2 - 35\bigl(49\langle\beta_2^6\rangle$			
	$-35\left\langle \left(\frac{\delta d_{\perp}}{d_{\perp}}\right)^4 \right\rangle^2 - 630 \cdot \left\langle \left(\frac{\delta d_{\perp}}{d_{\perp}}\right)^2 \right\rangle^4$	$+4\langle\cos(6\gamma)\beta_2^6\rangle)\Big)+25\Big(21879\langle\beta_2^4\rangle^2$			
	$+560 \cdot \left\langle \left(\frac{\delta d_{\perp}}{d_{\perp}}\right)^3 \right\rangle^2 \cdot \left\langle \left(\frac{\delta d_{\perp}}{d_{\perp}}\right)^2 \right\rangle$	$+14144\langle\cos(3\gamma)\beta_2^3\rangle\langle\cos(3\gamma)\beta_2^5\rangle$			
	$-56 \cdot \left\langle \left(\frac{\delta d_{\perp}}{d_{\perp}}\right)^5 \right\rangle \cdot \left\langle \left(\frac{\delta d_{\perp}}{d_{\perp}}\right)^3 \right\rangle$	$-35(79\langle\beta_2^8\rangle+16\langle\cos(6\gamma)\beta_2^8\rangle))$			

8-Aug-2024

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#### Enhanced yn correlations in models

![](_page_31_Figure_2.jpeg)

A stronger correlation is well explained by the transport model using deformed <sup>129</sup>Xe nuclei using transport model

#### Status of vn-[pT] studies

#### Zhiyong Lu(CIAE)

![](_page_32_Figure_2.jpeg)