Workshop on Hyperon Physics, 2024.4.13, 惠州







# Theoretical studies on weak radiative and non-leptonic decays of hyperons

#### Sci.Bull. 68 (2023) 779-782 and Sci.Bull. 67 (2022) 2298-2304

#### 史瑞祥 @ GXUN



Li-Sheng Geng @Beihang U.



Jun-Xu Lu @Beihang U.



Shuang-Yi Li @Beihang U.

### Contents

80

Y

=

**Background & purpose** 

**Theoretical framework** 

**Results and Discussions** 

Summary and outlook

### Contents

80

Y

=

**Background & purpose** 

**Theoretical framework** 

**Results and Discussions** 

Summary and outlook

### Weak decays of hyperons

- Weak radiative hyperon decays  $(B_i \rightarrow B_f \gamma)$ 
  - ✓ The long-standing WRHDs puzzle

<u>Sci.Bull. 68 (2023) 779-782</u> <u>Sci.Bull. 67 (2022) 2298-2304</u>

• Semi-leptonic decays of hyperons  $(B_i \rightarrow B_f \gamma^* \rightarrow B_f l l)$ 

and  $B_i \rightarrow B_f l \nu$ )

✓ Searching for new physics <u>JHEP</u> ✓  $V_{us}$ 

<u>JHEP 02 (2022) 178</u>



- Non-leptonic decays of hyperons  $(B_i \rightarrow B_f \pi)$ 
  - ✓ The long-standing S/P puzzle
     ✓ CP violation

#### What are weak radiative hyperon decays

 Weak radiative hyperon decays (WRHDs) are interesting physical processes involving the electromagnetic, weak, and strong interactions

•  $s \rightarrow d \gamma$  transitions in the quark level





• Six WRHDs channels of the ground-state octet baryons

$$\begin{array}{ll} \Lambda \to n\gamma & \Sigma^0 \to n\gamma & \Xi^0 \to \Sigma^0 \gamma \\ \Sigma^+ \to p\gamma & \Xi^0 \to \Lambda\gamma & \Xi^- \to \Sigma^- \gamma \end{array}$$

#### What are weak radiative hyperon decays

• The effective Lagrangian describing the  $B_i \rightarrow B_f \gamma$  WRHDs

$$\mathcal{L} = \frac{eG_F}{2}\bar{B}_f(a+b\gamma_5)\sigma^{\mu\nu}B_iF_{\mu\nu},$$

a: partity-conserving amplitude b: partity-violating amplitude

Observables for the WRHDs

$$\frac{d\Gamma}{d\cos\theta} = \frac{e^2 G_F^2}{\pi} (|a|^2 + |b|^2) [1 + \frac{2\text{Re}(ab^*)}{|a|^2 + |b|^2} \cos\theta] \cdot |\vec{k}|^3,$$

$$\alpha_{\gamma} = \frac{2\text{Re}(ab^*)}{|a|^2 + |b|^2}, \quad \Gamma = \frac{e^2 G_F^2}{\pi} (|a|^2 + |b|^2) \cdot |\vec{k}|^3, \quad |\vec{k}| = \frac{m_i^2 - m_f^2}{2m_i}$$



- $\alpha_{\gamma}$ : the asymmetry parameter
- **\theta:** the angle between the spin of the initial baryon  $B_i$  and the 3-momentum  $\vec{k}$  of the final baryon  $B_f$

#### Why to study WRHDs: the WRHDs puzzle

• The experimental measurement of a surprisingly large asymmetry for  $\Sigma^+ \rightarrow p \gamma$  decay [<u>PR188</u>, <u>2077 (1969</u>]], contradicting Hara's theorem based on gauge invariance, CP conservation, and U-spin symmetry [<u>Y. Hara, PRL12, 378 (1964</u>]]



• Although some models predictions are in agreement with the measurement of the large asymmetry for the  $\Sigma^+ \rightarrow p \gamma$  decay, they explain poorly the data of other WRHDs

#### Why to study WRHDs: experimentally challenging

**□ Significant changes** in the asymmetry parameters of  $\Xi^0 \rightarrow \Sigma^0 \gamma$  and  $\Xi^0 \rightarrow \Lambda \gamma$ 



### Why to study WRHDs-- $\Lambda \rightarrow n\gamma$



#### **D** New BESIII measurement for the $\Lambda \rightarrow n \gamma$ decay (PRL129(2022)21,212002)

Decay Mode	$\Lambda  o n\gamma$	$ar{\Lambda}  ightarrow ar{n} \gamma$		
$N_{ m ST}$ (×10 <sup>3</sup> )	$6853.2\pm2.6$	$7036.2 \pm 2.7$		
$\varepsilon_{\rm ST}$ (%)	$51.13 \pm 0.01$	$52.53 \pm 0.01$		
$N_{\rm DT}$	$723 \pm 40$	$498 \pm 41$	PDG2022	Γ <u>3</u> /Ι
$\varepsilon_{\mathrm{DT}}$ (%)	$6.58 {\pm} 0.04$	$4.32 \pm 0.03$	$\frac{VALUE \text{ (units } 10^{-3}\text{)}}{1.75 \pm 0.15 \text{ OUR FIT}} \xrightarrow{EVTS} DOCUMENT ID \underline{TECN} COMMENT$	- 57 -
$RE(\times 10^{-3})$	$0.820 \pm 0.045 \pm 0.066$	$0.862 {\pm} 0.071 {\pm} 0.084$	<b>1.75±0.15</b> 1816 LARSON 93 SPEC $K^-p$ at rest ••• We do not use the following data for averages, fits, limits, etc. •••	
BF(X10)	$0.832 \pm 0.0$	$038 \pm 0.054$	1.78±0.24 <sup>+0.14</sup> <sub>-0.16</sub> 287 NOBLE 92 SPEC See LARSON 93	
	$-0.13 {\pm} 0.13 {\pm} 0.03$	$0.21{\pm}0.15{\pm}0.06$		
$\alpha_{\gamma}$	$<-0.16\pm0$	$.10{\pm}0.05$		

• The branching fraction is only **about one half** of the current PDG average

• The asymmetry parameter  $\alpha_{\gamma}$  is determined for the first time

### Why to study WRHDs-- $\Lambda \rightarrow n\gamma$

**None of the existing predictions can describe** the new BESIII measurement

for the  $\Lambda \rightarrow n \gamma$  decay



Data: <u>BESIII, PRL129(2022)21,212002</u>
HB χPT: E. E. Jenkins et al, NPB 397, 84 (1993)
BχPT: H. Neufeld, Nucl. Phys. B 402, 166 (1993)
NRCQM: <i>Qiang Zhao et al, CPC45, 013101 (2021)</i>
PM1: <i><u>M. B. Gavela et al, PLB 101, 417 (1981)</u></i>
PM2: <u><i>G. Nardulli, PLB 190, 187 (1987)</i></u>
VDM: <u>P. Zenczykowski, PRD 44, 1485 (1991)</u>
χPT: <u><i>B. Borasoy et al, PRD 59, 054019 (1999)</i></u>
BSU(3): <u>P. Zenczykowski, PRD 73, 076005 (2006)</u>
QM: <u>E. N. Dubovik et al, Phys. Atom. Nucl. 71, 136 (2008)</u>





#### **D** New BESIII and CLAS data for the hyperon non-leptonic decays

CLAS: PRL123,182301 (2019)

BESIII: PRL129,131801 (2022)

BESIII: Nature Phys. 15, 631 (2019) BESIII: Nature 606, 64 (2022)



• Definition of decay parameter for the  $\Lambda \rightarrow p \pi^-$  decay  $\mathcal{M}(B_i \rightarrow B_f \pi) = i G_F m_{\pi}^2 \bar{B}_f (A_S - A_P \gamma_5) B_i$ 

$$\alpha_{\pi} = \frac{2\text{Re}\,(s \cdot p)}{|s|^2 + |p|^2} \qquad s = A_S \qquad p = A_P |\vec{q}| / (E_f + m_f)$$

- Featured by a larger statistics and a small uncertainty and very different from previous PDG average
- A significant change for the baryon decay parameter of  $\Lambda \rightarrow p \ \pi^-$  may greatly affect the values of LECs hD, hF and hyperon non-leptonic decay amplitudes as inputs WRHDs

#### Why to study WRHDs—theoretical tools

 $\Box$  Theoretically, **two phenomenological models** are able to explain the current experimental data of WRHDs at least qualitatively except for the  $\Lambda \rightarrow n \gamma$  decay

E. N. Dubovik et al, Phys. Atom. Nucl. 71, 136 (2008) P. Zenczykowski, PRD 73, 076005 (2006)

**Chiral perturbation theory (xPT)** studies on the WRHDs

B. Borasoy et al, PRD 59, 054019 (1999) (Tree level)

E. E. Jenkins et al, NPB397, 84 (1993)
J. W. Bos et al, PRD 51, 6308 (1995)
J. W. Bos et al, PRD 54, 3321 (1996)
J. W. Bos, et al, PRD 57, 4101 (1998)

H. Neufeld, NPB 402, 166 (1993) (Loop level in the covariant formulation) 12





- The work in the BχPT *H. Neufeld, NPB* 402, 166 (1993)
- ✓ The used low energy constants (LECs) and hyperon non-leptonic decay amplitudes are out of date
- ✓ No efforts were taken to ensure a consistent power counting

Updating the relevant LECs and hyperon non-leptonic decay amplitudes Calculating the branching fractions and asymmetry parameters, i.e., **amplitudes a and b**, of the WRHDs order by order

Comparing our predictions with those from other approaches/experimental data

### Contents

80

Ŷ

=

**Background & purpose** 

**Theoretical framework** 

**Results and Discussions** 

Summary and outlook

#### **Chiral perturbation theory : a bottom-up approach**



Effective theory: the physics in low energy regions does not depend on the details of the higher energy physics, which has been integrated out

# Chiral perturbation theory is a powerful tool to study the WRHDs

### **Chiral perturbation theory**

**D**The effective Lagrangian of the general form

$$\mathcal{L} = \sum_{i} c_i \left( Q, \Lambda \right) O_i(\{\psi\})$$

**Q** is the soft scale,  $\Lambda$  is the hard scale,  $C_i$  are LECs,  $O_i$  refer to operators containing field  $\psi$ .

#### **D**Power counting rule

Chiral order:  $N = 4L - 2N_M - N_B + \sum k V_k$ 

#### **D**Power counting breaking (PCB) problem







#### Single baryon /meson system

Red dots: PCB terms

#### **Chiral perturbation theory**



✓ Covariant formulation (We adopt EOMS) Li-Sheng Geng, Front. Phys. (Beijing) 8 (2013) 328-348





Removing all the PCB terms and remaining partly the higher order terms

#### **Chiral perturbation theory**

• Baryon magnetic moments

Geng LS et al, PRL101 (2008) 222002

• Compton scattering off protons

Lensky V et al, EPJC 65 (2010) 195-209

 $\bullet \pi N$  -scattering

Alarcón J M et al, Annals Phys. 336 (2013) 413-461 and Chen Y H et al, PRD 87 (2013) 054019

• High-precision relativistic chiral nuclear force

Lu JX et al, PRL 128 (2022) 14, 142002

#### WRHDs in the EOMS B<sub>X</sub>PT

$$a_{B_iB_f} = a_{B_iB_f}^{(1,\text{tree})} + a_{B_iB_f}^{(2,\text{tree})} + a_{B_iB_f}^{(2,\text{loop})}$$
$$b_{B_iB_f} = b_{B_iB_f}^{(2,\text{tree})} + b_{B_iB_f}^{(2,\text{loop})}$$

#### **Feynman diagrams**







#### Lagrangians $\mathcal{L}_{\Lambda S=1}^{(0)} = \sqrt{2} G_F m_{\pi}^2 F_{\phi} \langle h_D \bar{B} \{ u^{\dagger} \lambda u, B \} + h_F \bar{B} [ u^{\dagger} \lambda u, B ] \rangle,$ $\mathcal{L}_{MB}^{(2)} = \frac{b_6^D}{8m_P} \langle \bar{B}\sigma^{\mu\nu} \{F_{\mu\nu}^+, B\} \rangle + \frac{b_6^F}{8m_P} \langle \bar{B}\sigma^{\mu\nu} [F_{\mu\nu}^+, B] \rangle,$ $\mathcal{L}_{\alpha}^{(2)} = C_{\alpha} \langle \bar{B} \sigma^{\mu\nu} F_{\mu\nu} \lambda Q B \rangle,$ $\mathcal{L}_{\beta}^{(2)} = C_{\beta} \langle \sigma^{\mu\nu} F_{\mu\nu} \bar{B} Q B \lambda \rangle,$ $\mathcal{L}_{\gamma}^{(2)} = C_{\gamma} \langle \bar{B} \sigma^{\mu\nu} F_{\mu\nu} B \lambda Q \rangle,$ $\mathcal{L}_{\sigma}^{(2)} = C_{\sigma} \langle \bar{B} \sigma^{\mu\nu} F_{\mu\nu} \lambda B Q \rangle,$ $\mathcal{L}_{\rho}^{(2)} = C_{\rho} \left( \langle \bar{B} \sigma^{\mu\nu} \gamma_5 F_{\mu\nu} Q \rangle \langle B \lambda \rangle - \langle \bar{B} \sigma^{\mu\nu} \gamma_5 F_{\mu\nu} \lambda \rangle \langle B Q \rangle \right)$ $\mathcal{L}_{\Lambda S=1}^{(0)} = \sqrt{2}G_F m_{\pi}^2 F_{\phi} \langle h_D \bar{B} \{ u^{\dagger} \lambda u, B \} + h_F \bar{B} [u^{\dagger} \lambda u, B] \rangle$ $\mathcal{L}_{B}^{(1)} = \langle \bar{B}i\gamma^{\mu}D_{\mu}B - m_{0}\bar{B}B\rangle,$ $\mathcal{L}_{M}^{(2)} = \frac{F_{\phi}^{2}}{4} \langle u_{\mu}u^{\mu} + \chi^{+} \rangle,$ $\mathcal{L}_{MB}^{(1)} = \frac{D}{2} \langle \bar{B} \gamma^{\mu} \gamma_5 \{ u_{\mu}, B \} \rangle + \frac{F}{2} \langle \bar{B} \gamma^{\mu} \gamma_5 [ u_{\mu}, B ] \rangle,$

#### **Order contributions**

 $a_{B_iB_f}^{(1,\text{tree})}$ LECs  $b_6^D$  and  $b_6^F$ : <u>the experimental data of Octet</u> <u>baryon magnetic moment</u>

$$a_{B_iB_f}^{(2,\text{tree})}$$
  $b_{B_iB_f}^{(2,\text{tree})}$ 

LECs D and F have been determined in Ref. <u>L. S. Geng</u> et al, PRD 90, 054502 (2014)

$$a_{B_iB_f}^{(2,\text{loop})} \quad b_{B_iB_f}^{(2,\text{loop})}$$

For the amplitude a, weak vertex is  $\gamma_5^{19}$ 

### Contents

80

Y

=

**Background & purpose** 

**Theoretical framework** 

**Results and Discussions** 

Summary and outlook

### LECs hD, hF and hyperon non-leptonic decay amplitudes

The hyperon non-leptonic decay amplitudes for the octet-to-octet transitions have the following form

$$\mathcal{M}(B_i \to B_f \pi) = i G_F m_\pi^2 \bar{B}_f \left( A_S - A_P \gamma_5 \right) B_i$$

Hyperon non-leptonic decay amplitudes: S-wave amplitude  $A_S$  and P-wave amplitude  $A_P$ **Decay width and baryon decay parameters**  $\alpha_{\pi}$ ,  $\beta_{\pi}$  and  $\gamma_{\pi}$  for  $B_i \rightarrow B_f \pi$  decays

$$\begin{split} \Gamma(B_i \to B_f \pi) &= \frac{\left(G_F m_\pi^2\right)^2}{8\pi m_i^2} \left| \vec{q} \right| \left\{ \left[ (m_i + m_f)^2 - m_\pi^2 \right] |s|^2 + \left[ (m_i - m_f)^2 - m_\pi^2 \right] \left| p \cdot \frac{(E_f + m_f)}{\left| \vec{q} \right|} \right|^2 \right\}, \\ \alpha_\pi &= \frac{2\text{Re}\left(s \cdot p\right)}{|s|^2 + |p|^2}, \ \beta_\pi = \frac{2\text{Im}\left(s \cdot p\right)}{|s|^2 + |p|^2}, \ \gamma_\pi = \frac{|s|^2 + |p|^2}{|s|^2 + |p|^2}, \end{split}$$

with

$$s = A_S$$
  $p = A_P |\vec{q}| / (E_f + m_f)$ 

where  $E_f$  and  $\vec{q}$  are the energy and 3-momentum of the final baryon

### LECs hD, hF and hyperon non-leptonic decay amplitudes

Table: By means of isospin symmetry, the Lee-Sugawara relations and the criterion that  $A_S(\Lambda \rightarrow p\pi^-)$  is conventionally positive, **S** - and **P**-wave hyperon non-leptonic decay amplitudes are uniquely determined by fitting to the recent data [3,51-53] of branching fraction **B**, baryon decay parameters  $\alpha_{\pi}$  and  $\gamma_{\pi}$ 

Dagay modes	@ [2]	a. [2 51 52]	A (°) [2 52]	$s = A_s^{(\text{Expt})}$		$p = A_P^{(\text{Expt})}  \vec{q}  / (E_f + m_f)$	
Decay modes	iy modes $\mathcal{B}[5] = \alpha_{\pi}[5, 51-53] = \phi_{\pi}(5, 52] = -\frac{1}{\Gamma h}$		This work	[49]	This work	[49]	
$\Sigma^+ \rightarrow n\pi^+$	0.4831(30)	0.068(13)	167(20)	0.06(1)	0.06(1)	1.81(1)	1.81(1)
$\Sigma^- \rightarrow n\pi^-$	0.99848(5)	-0.068(8)	10(15)	1.88(1)	1.88(1)	-0.06(1)	-0.06(1)
$\Lambda \rightarrow p\pi^{-}$	0.639(5)	0.7462(88)	-6.5(35)	1.38(1)	1.42(1)	0.62(1)	0.52(2)
$\Xi^- \rightarrow \Lambda \pi^-$	0.99887(35)	-0.376(8)	0.6(12)	-1.99(1)	-1.98(1)	0.39(1)	0.48(2)
$\Sigma^+ \to p \pi^0$	0.5157(30)	-0.982(14)	36(34)	-1.50(3)	-1.43(5)	1.29(4)	1.17(7)
$\Lambda \rightarrow n\pi^0$	0.358(5)	0.74(5)	••••	-1.09(2)	-1.04(1)	-0.48(4)	-0.39(4)
$\Xi^0 \to \Lambda \pi^0$	0.99524(12)	-0.356(11)	21(12)	1.62(10)	1.52(2)	-0.30(10)	-0.33(2)

• Comparing our results with those of Ref. [49]:

$$\gamma_{\pi} = \sqrt{1 - \alpha_{\pi}^2} \cos{(\phi_{\pi})}$$

- ✓ P-wave amplitudes, especially for  $A_P(\Lambda \to p\pi^-)$  and  $A_P(\Xi^- \to \Lambda\pi^-)$ , differ a lot, which would affect the imaginary parts of the parity-conserving amplitude a
- $\checkmark$  the experimental S -wave amplitudes are almost unchanged

[3] P. A. Zyla et al. PDG, PTEP 2020, 083C01(2020) [49] E. E. Jenkins, NPB 375, 561 (1992) [51] M. Ablikim et al., BESIII, 2204.11058 (2022) [52] M. Ablikim et al. (BESIII), Nature 606, 64, 2105.11155 (2022) [53] D. G. Ireland et al, PRL 123,182301 (2019)

#### **D**Amplitudes of hyperon non-leptonic decay

$$\mathcal{M}(B_i \to B_f \pi) = i G_F m_\pi^2 \bar{B}_f \left( A_S - A_P \gamma_5 \right) B_i$$

Here, both S-wave amplitude A<sub>S</sub> and P-wave amplitude A<sub>P</sub> are as functions of LECs hD and hF

**The so-called S/P puzzle:** if the two LECs hD and hF can describe well the experimental S-wave amplitudes, they reproduce very poorly the P-wave amplitudes

As a result, we only updated the values of hD and hF by fitting to the experimental S -wave amplitudes for hyperon non-leptonic decays

### LECs hD, hF and hyperon non-leptonic decay amplitudes

Table: LECs hD and hF determined by fitting to the S –wave hyperon non-leptonic decay amplitudes.

Decay modes	$A_S^{ m th}$	$A_S^{\text{Expt}}$
$\Sigma^+ \rightarrow n\pi^+$	0	0.06(1)
$\Sigma^- \rightarrow n\pi^-$	$-h_D + h_F$	1.88(1)
$\Lambda \rightarrow p\pi^{-}$	$\frac{1}{\sqrt{6}}(h_D+3h_F)$	1.38(1)
$\Xi^-  ightarrow \Lambda \pi^-$	$\frac{1}{\sqrt{6}}(h_D-3h_F)$	-1.99(1)
$\Sigma^+ \to p \pi^0$	$\frac{1}{\sqrt{2}}(h_D - h_F)$	-1.50(3)
$\Lambda \rightarrow n\pi^0$	$-\frac{1}{2\sqrt{3}}(h_D + 3h_F)$	-1.09(2)
$\Xi^0 \to \Lambda \pi^0$	$-\frac{1}{2\sqrt{3}}(h_D - 3h_F)$	1.62(10)
$\chi^2/d.o.f. = 0.24$	$h_D = -0.61(24)$	$h_F = 1.42(1-1)$

- In our least-squares fit, an absolute uncertainty of 0.3 is added to each S -wave amplitude in order to match the theoretical predictions with the experimental data at 1σ confidence level
- The tree-level formulae for the S -wave amplitudes derived from the following Lagrangian

$$\mathcal{L}^{(0)}_{\Delta S=1} = \sqrt{2} G_F m_\pi^2 F_\phi \langle h_D \bar{B} \{ u^\dagger \lambda u, B \} + h_F \bar{B} [u^\dagger \lambda u, B] \rangle$$

#### Real part of amplitude a at $O(p^1)$ --tree



$$\begin{aligned} \mathcal{L}_{\Delta S=1}^{(0)} &= \sqrt{2} G_F m_\pi^2 F_\phi \langle h_D \bar{B} \{ u^\dagger \lambda u, B \} + h_F \bar{B} [ u^\dagger \lambda u, B ] \rangle, \\ \mathcal{L}_{MB}^{(2)} &= \frac{b_6^D}{8m_B} \langle \bar{B} \sigma^{\mu\nu} \{ F_{\mu\nu}^+, B \} \rangle + \frac{b_6^F}{8m_B} \langle \bar{B} \sigma^{\mu\nu} [ F_{\mu\nu}^+, B ] \rangle, \end{aligned}$$

hD and hF are LECs

baryon magnetic moments

$$a_{B_iB_f} = a_{B_iB_f}^{(1,\text{tree})} + a_{B_iB_f}^{(2,\text{tree})} + a_{B_iB_f}^{(2,\text{loop})}$$
$$b_{B_iB_f} = b_{B_iB_f}^{(2,\text{tree})} + b_{B_iB_f}^{(2,\text{loop})}$$

#### Amplitude b and imaginary part of amplitude a at $O(p^2)$ --loop



$$\begin{aligned} \mathcal{L}_{\Delta S=1}^{(0)} &= \sqrt{2} G_F m_{\pi}^2 F_{\phi} \langle h_D \bar{B} \{ u^{\dagger} \lambda u, B \} + h_F \bar{B} [ u^{\dagger} \lambda u, B ] \rangle \\ \mathcal{L}_B^{(1)} &= \langle \bar{B} i \gamma^{\mu} D_{\mu} B - m_0 \bar{B} B \rangle, \\ \mathcal{L}_M^{(2)} &= \frac{F_{\phi}^2}{4} \langle u_{\mu} u^{\mu} + \chi^+ \rangle, \\ \mathcal{L}_{MB}^{(1)} &= \frac{D}{2} \langle \bar{B} \gamma^{\mu} \gamma_5 \{ u_{\mu}, B \} \rangle + \frac{F}{2} \langle \bar{B} \gamma^{\mu} \gamma_5 [ u_{\mu}, B ] \rangle, \end{aligned}$$

Real part of amplitude a in the loop level cannot be reliably determined due to S/P puzzle in hyperon non-leptonic decays.

$$a_{B_iB_f} = a_{B_iB_f}^{(1,\text{tree})} + a_{B_iB_f}^{(2,\text{tree})} + a_{B_iB_f}^{(2,\text{loop})} + a_{B_iB_f}^{(2,\text{loop})}$$
$$b_{B_iB_f} = b_{B_iB_f}^{(2,\text{tree})} + b_{B_iB_f}^{(2,\text{loop})}$$

#### Real part of amplitude a and b at $O(p^2)$ --tree



$\mathcal{L}_{\alpha}^{(2)} = C_{\alpha} \langle \bar{B} \sigma^{\mu\nu} F_{\mu\nu} \lambda Q B \rangle,$	
$\mathcal{L}_{\beta}^{(2)} = C_{\beta} \langle \sigma^{\mu\nu} F_{\mu\nu} \bar{B} Q B \lambda \rangle,$	
$\mathcal{L}_{\gamma}^{(2)} = C_{\gamma} \langle \bar{B} \sigma^{\mu\nu} F_{\mu\nu} B \lambda Q \rangle,$	counter-terms
$\mathcal{L}_{\sigma}^{(2)} = C_{\sigma} \langle \bar{B} \sigma^{\mu\nu} F_{\mu\nu} \lambda B Q \rangle,$	
$\mathcal{L}_{\rho}^{(2)} = C_{\rho} \left( \langle \bar{B} \sigma^{\mu\nu} \gamma_5 F_{\mu\nu} Q \rangle \langle B \sigma^{\mu\nu} Q \rangle \langle B \rho^{\mu\nu} Q \rangle $	$\langle B\lambda \rangle - \langle \bar{B}\sigma^{\mu\nu}\gamma_5 F_{\mu\nu}\lambda \rangle \langle BQ \rangle$

- CPS is CP followed by the SU(3) transformation of  $u \rightarrow -u$ ,  $d \rightarrow s$  and
  - $s \rightarrow d$  which exchanges s and d quarks.

27

• CPS symmetry dictates the existence of five unknown LECs

Table: Contributions to the real parts of amplitudes a and b at tree-level  $O(p)^2$ . The normalization  $2(eG_F)^{-1}$  has been factored out.

	$\Lambda \to n\gamma$	$\Sigma^{+} \to p \gamma$	$\Sigma^0 \to n\gamma$	$\Xi^0  ightarrow \Lambda \gamma$	$\Xi^0  ightarrow \Sigma^0 \gamma$	$\Xi^-  ightarrow \Sigma^- \gamma$
$a^{(2,\text{tree})}$	$\frac{2C_{\alpha}-C_{\beta}-C_{\gamma}+2C_{\sigma}}{3\sqrt{6}}$	$\frac{2C_{\beta}-C_{\gamma}}{3}$	$\frac{C_{\beta}+C_{\gamma}}{3\sqrt{2}}$	$-\frac{C_{\alpha}-2C_{\beta}-2C_{\gamma}+C_{\sigma}}{3\sqrt{6}}$	$\frac{C_{\alpha}+C_{\sigma}}{3\sqrt{2}}$	$\frac{2C_{\sigma}-C_{\alpha}}{3}$
b <sup>(2,tree)</sup>	$-\frac{C_{ ho}}{\sqrt{6}}$	0	$-\frac{C_{\rho}}{\sqrt{2}}$	$\frac{C_{\rho}}{\sqrt{6}}$	$\frac{C_{\rho}}{\sqrt{2}}$	0

$$b_{\Xi^{0}\Sigma^{0}}^{(2,\text{tree})} = \sqrt{3}b_{\Xi^{0}\Lambda}^{(2,\text{tree})}, \quad b_{\Lambda n}^{(2,\text{tree})} = -b_{\Xi^{0}\Lambda}^{(2,\text{tree})}, \\ b_{\Sigma^{0}n}^{(2,\text{tree})} = -\sqrt{3}b_{\Xi^{0}\Lambda}^{(2,\text{tree})}, \quad b_{\Sigma^{+}p}^{(2,\text{tree})} = 0, \quad b_{\Xi^{-}\Sigma^{-}}^{(2,\text{tree})} = 0.$$

#### **Determining the contributions of counter-terms**

**□**Total amplitudes a and b are a sum of the tree and loop contributions and read:

$$a_{B_iB_f} = a_{B_iB_f}^{(1,\text{tree})} + a_{B_iB_f}^{(2,\text{tree})} + a_{B_iB_f}^{(2,\text{loop})} = \text{Re} \ a_{B_iB_f} + \text{Im} \ a_{B_iB_f}^{(2,\text{loop})}$$
$$b_{B_iB_f} = b_{B_iB_f}^{(2,\text{tree})} + b_{B_iB_f}^{(2,\text{loop})}$$

 $\Box \text{Using } b_{\Xi^0\Sigma^0}^{(2,\text{tree})} = \sqrt{3}b_{\Xi^0\Lambda}^{(2,\text{tree})} \text{ and fitting to } \mathcal{B} \text{ and } \alpha_{\gamma} \text{ for } \Xi^0 \to \Sigma^0 \gamma \text{ and } \Xi^0 \to \Lambda \gamma \text{ decays,}$ we determine for the first time the contributions of counter-terms

Solution I	Solution II
5.62(53)	-8.34(48)
-9.56(34)	3.89(45)
-32.22(64)	32.50(61)
0.04	1.22
	Solution I 5.62(53) -9.56(34) -32.22(64) 0.04

- The  $\chi^2/d.o.f.$  of Solution I much smaller than that of Solution II.
- Contributions of counter-terms for other WRHDs obtained by the following relations  $b_{\Lambda n}^{(2,\text{tree})} = -b_{\Xi^0\Lambda}^{(2,\text{tree})} b_{\Sigma^0 n}^{(2,\text{tree})} = -\sqrt{3}b_{\Xi^0\Lambda}^{(2,\text{tree})}, \quad b_{\Sigma^+ p}^{(2,\text{tree})} = 0, \quad b_{\Xi^-\Sigma^-}^{(2,\text{tree})} = 0$

$$a_{B_{i}B_{f}} = a_{B_{i}B_{f}}^{(1,\text{tree})} + a_{B_{i}B_{f}}^{(2,\text{tree})} + a_{B_{i}B_{f}}^{(2,\text{loop})} = \text{Re} \ a_{B_{i}B_{f}} + \text{Im} \ a_{B_{i}B_{f}}^{(2,\text{loop})}$$
$$b_{B_{i}B_{f}} = b_{B_{i}B_{f}}^{(2,\text{tree})} + b_{B_{i}B_{f}}^{(2,\text{loop})}$$

Therefore, we take the Re a for each WRHD as a free parameter due to the unknown real parts of amplitudes a in tree and loop levels<sup>8</sup>

#### Predictions for parity-conserving a and -violating b amplitudes

Table: Decomposition of the contributions to the parity-violating amplitudes b (in units of MeV)

EOMS $B\chi PT$			Т
Decay modes	b <sup>(2,tree)</sup>	$b^{(2,\text{loop})}$	$b^{(2,tot)}$
$\Lambda \rightarrow n\gamma$	-5.62(53)	7.87(73) + 10.04(81)i	2.25(90) + 10.04(81)i
$\Sigma^+ \to p\gamma$	0	-1.96(11)-1.75(12)i	-1.96(11) - 1.75(12)i
$\Sigma^0 \to n\gamma$	-9.73(92)	1.41(11) + 10.09(78)i	-8.32(93) + 10.09(78)i
$\Xi^0  ightarrow \Lambda \gamma$	5.62(53)	-1.60(48)	4.02(72)
$\Xi^0  ightarrow \Sigma^0 \gamma$	9.73(92)	2.91(67)	12.64(114)
$\Xi^-  ightarrow \Sigma^- \gamma$	0	-3.00(29) - 8.64(54)i	-3.00(29) - 8.64(54)i

Table: Imaginar conservin	Table: Imaginary parts of the loop contributions to the parity- conserving amplitudes a at ${\cal O}(p^2)$ (in units of MeV)				
	Decay modes	EOMS $B\chi PT$ Im $a^{(2,loop)}$			
	$\frac{Decay \text{ modes}}{\Lambda \to n\gamma}$	-1.01(2)			
	$\Sigma^+ \to p\gamma$ $\Xi^- \to \Sigma^- \gamma$	2.70(4) -0.57(1)			

#### $\alpha_{\gamma}$ of the $\Lambda ightarrow n \gamma$ decay as a function of $\sqrt{|a|^2 + |b|^2}$



Data: <u>BESIII, PRL129(2022)21,212002</u>
HB χPT : <i>Ε. Ε. Jenkins et al, NPB 397, 84 (1993)</i>
HB* χPT : <i>E. E. Jenkins et al, NPB 397, 84 (1993) with</i>
counter-term contributions
NRCQM: <i>Qiang Zhao et al, CPC45, 013101 (2021)</i>
PM1: <i><u>M. B. Gavela et al, PLB 101, 417 (1981)</u></i>
PM2: <u><i>G. Nardulli, PLB 190, 187 (1987)</i></u>
VDM: <u><i>P. Zenczykowski, PRD 44, 1485 (1991)</i></u>
χPT: <u><i>B. Borasoy et al, PRD 59, 054019 (1999)</i></u>
BSU(3): <u>P. Zenczykowski, PRD 73, 076005 (2006)</u>
OM: F. N. Dubovik et al. Phys. Atom. Nucl. 71, 136 (20

- Interestingly, only **EOMS BxPT agrees with** the latest BESIII measurement
- The prediction in the HB χPT with counter-term contributions is very close to the BESIII data
- The vector dominance model (VDM) and the pole model (PM II) are disfavored by the BESIII data

#### $\alpha_{\gamma}$ of the other WRHDs as a function of $\sqrt{|a|^2 + |b|^2}$



- EOMS
   HB
   Data
   NRCQM
   PM I
   PM II
   VDM
   ★ χPT
   BSU(3)
   QM
- For the  $\Sigma^0 \rightarrow n \gamma$  decay, not yet measured, our result contradicts the predictions of PM I and NRCQM
- For the  $\Xi^- \rightarrow \Sigma^- \gamma$  decay, our prediction agrees better with the experimental measurement, and the current PDG data disfavor the results of PM II and tree-level  $\chi$ PT
  - For the  $\Sigma^+ \rightarrow p \gamma$  decay, the results predicted in all the  $\chi$ PT deviate from the PDG average but our prediction is closer

Hara's theorem:  $\alpha_{\gamma}$  for  $\Xi^- \to \Sigma^- \gamma$  and  $\Sigma^+ \to p \gamma$  should not be too large.

### Contents

80

Ŷ

**Background & purpose** 

**Theoretical framework** 

**Results and Discussions** 

Summary and outlook

0

- ■We first updated the two relevant low energy constants hD, hF and hyperon nonleptonic decay amplitudes determined by fitting to the latest experimental data on the  $B_i \rightarrow B_f \pi$  decays
- □ We determined the  $O(p^2)$  counter-term contributions determined by fitting to  $\Xi^0 \to \Sigma^0 \gamma$  and  $\Xi^0 \to \Lambda \gamma$  for the first time
- **D**We showed that the latest precise measurement of the branching fraction and asymmetry parameter of  $\Lambda \rightarrow n \gamma$  by the BESIII Collaboration can be well explained in covariant baryon chiral perturbation theory with the EOMS renormalization scheme
- **The**  $\Sigma^+ \rightarrow p \gamma$  channel with observed results cannot still be described well



 $\Box$ A more precise measurement of  $\alpha_{\gamma}(\Xi^- \to \Sigma^- \gamma)$  is highly desirable in order to test Hara's theorem and confirm the present experimental result.

Super tau-charm factory:

Zhou XR, PoSCHARM2020(2021)007 A.Y.Barnyakov, JPhysConfSer1561(1)(2020)012004

**\Box** Considering the contribution of heavier resonances, such as the Delta, Roper and  $\Delta(1405)$  multiplets

B. Borasoy et al, PRD 59, 054019(1999) B. Borasoy et al, EPJC 6, 85 (1999)

<u>B. Borasoy et al, PRD 59, 094025(1999)</u>

 $\square$  Revisiting the S/P puzzle in the  $B_i \rightarrow B_f \pi$  decays

#### **Summary and outlook**

#### • Non-leptonic decays of hyperons $(B_i \rightarrow B_f \pi)$

A ar DD

CPV observables	SM predictions	BESIII data
$A^{\Lambda}_{CP}$	$(-3 \sim 3) \times 10^{-5}$	$(-2.5 \pm 4.6 \pm 1.2) \times 10^{-3}$
$A_{CP}^{\Xi}$	$(0.5 \sim 6) \times 10^{-5}$	$(6 \pm 13.4 \pm 5.6) \times 10^{-3}$
$B_{CP}^{\Xi}$	$(-3.8 \sim -0.3) \times 10^{-4}$	$(1.2 \pm 3.4 \pm 0.8) \times 10^{-2}$

Jusak Tandean et al , PRD 67 (2003) 056001 ۲

Salone N et al , PRD 105 (2022) 11, 116022

Wang XF,arXiv:2312.17486

• 
$$\Delta I = 1/2$$
 rule problem  
BESIII: PRL 132 (2024) 10, 101801  
 $\langle \alpha_{\Lambda 0} \rangle / \langle \alpha_{\Lambda -} \rangle = 0.870 \pm 0.012^{+0.011}_{-0.010}$ 

• Including the counterterms contributions and intermediated decuplet-baryon contributions

Borasoy B et al, EPJC 6 (1999) 85-107 HB  $\chi$ PT: Abd El-Hady A, PRD 61 (2000) 114014

Decay amplitudees  $M = C m^2 \cdot \overline{D} (A)$ Hyperon non-leptonic decays  $A_{CP} = \frac{\alpha + \alpha}{\alpha - \overline{\alpha}} \, \, \text{for} \, \, B_{CP} = \frac{p + p}{\alpha - \overline{\alpha}}$ 

Decay ampirtudes: 
$$M = G_F m_{\pi} \cdot B_f (A_S - A_P \gamma_5) B_i$$
  

$$S = A_S \text{ and } P = A_P \cdot \frac{|\vec{p}_f|}{E_f + m}$$
Asymmetry parameters:  $\alpha^2 + \beta^2 + \gamma^2 = 1$   
 $\alpha = \frac{2\text{Re}(S^*P)}{|S|^2 + |P|^2}, \quad \beta = \frac{2\text{Im}(S^*P)}{|S|^2 + |P|^2} \text{ for } \gamma = \frac{|S|^2 - |P|^2}{|S|^2 + |P|^2}$ 
CPV observables:  
 $\alpha + \overline{\alpha} = \alpha + \overline{\beta} + \overline{\beta}$ 







## Thanks for your attention !



Li-Sheng Geng @Beihang U.



Jun-Xu Lu @Beihang U.



Shuang-Yi Li @Beihang U.

36

$$\alpha_{\gamma} \text{ of } \Xi^0 \to \Sigma^0 \gamma \text{ and } \Xi^0 \to \Lambda \gamma \text{ as a function of } \sqrt{|a|^2 + |b|^2}$$





- Based on gauge invariance, CP conservation, and U-spin symmetry
- Hara's theorem dictates that the WRHDs  $B \rightarrow B'\gamma$  and  $B' \rightarrow B\gamma$ must be identical under the U-spin transformation  $s \leftrightarrow d$

$$\mathcal{L}_{B\to B'\gamma} \propto \bar{B}'(a+b\gamma_5)\sigma^{\mu\nu}$$
$$\mathcal{L}_{B'\to B\gamma} \propto \bar{B}(a-b\gamma_5)\sigma^{\mu\nu}B'F_{\mu\nu}$$

leads to

b = 0, where B and B' refer to  $(\Sigma^+, \Xi^-)$  and  $(p, \Sigma^-)$  respectively.

#### Branching fractions *B* and asymmetry parameters $\alpha_{\gamma}$ data for WRHDs

Decay modes	$\mathcal{B} \times 10^{-3}$	$\alpha_{\gamma}$
$\Lambda \rightarrow n\gamma$	0.832(38)(54)	-0.16(10)(50)
$\Sigma^+ \rightarrow p\gamma$	1.23(5)	-0.76(8)
$\Sigma^0 \to n\gamma$	• • •	•••
$\Xi^0  ightarrow \Lambda \gamma$	1.17(7)	-0.704(19)(64)
$\Xi^0 \to \Sigma^0 \gamma$	3.33(10)	-0.69(6)
$\Xi^- \rightarrow \Sigma^- \gamma$	0.127(23)	1.0(13)