



中国科学技术大学

BESIII

Studies on Weak Radiative Hyperon Decays at BESIII

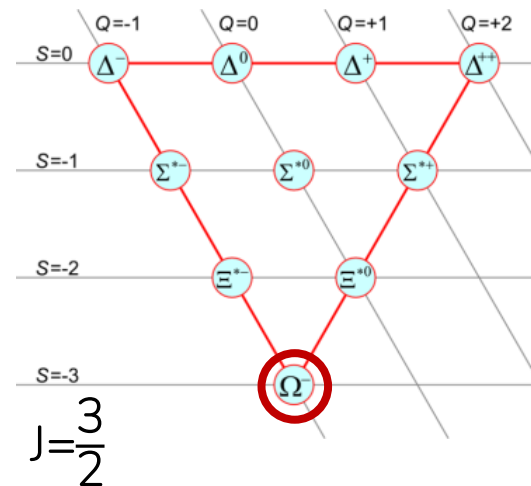
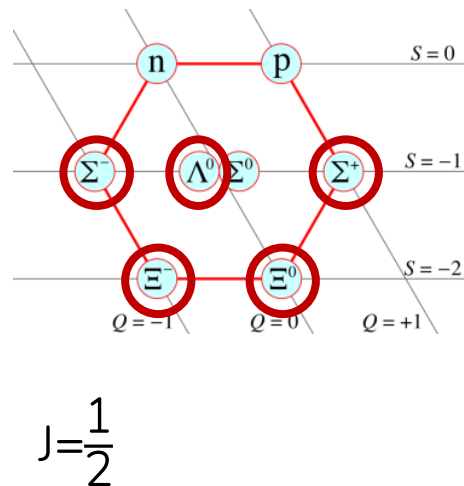
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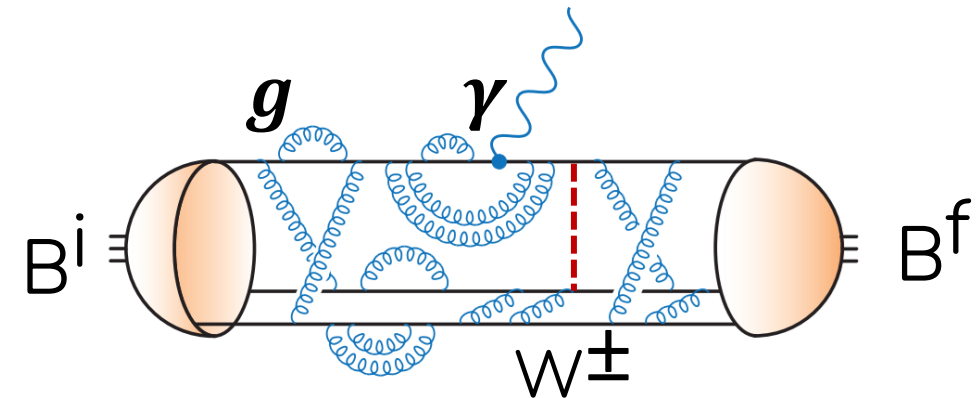
Physics Motivation

Overview

- Decay of ground hyperons:
 - Weak hadronic decay ($\Lambda \rightarrow p\pi^-$)
 - Semi-leptonic decay ($\Lambda \rightarrow p e \nu_e$)
 - Weak radiative decay (WRHD) ($\Lambda \rightarrow n\gamma$)



- Weak radiative decays
 - flavor changing neutral current (FCNC) process ($s \rightarrow d\gamma$ transition)
 - Significant non-perturbative QCD effects
 - A symphony of strong, weak and EM interaction



j.pnpnp.2016.07.001

Physics Motivation

Effective Theory Point-of-view

- Effective Lagrangian

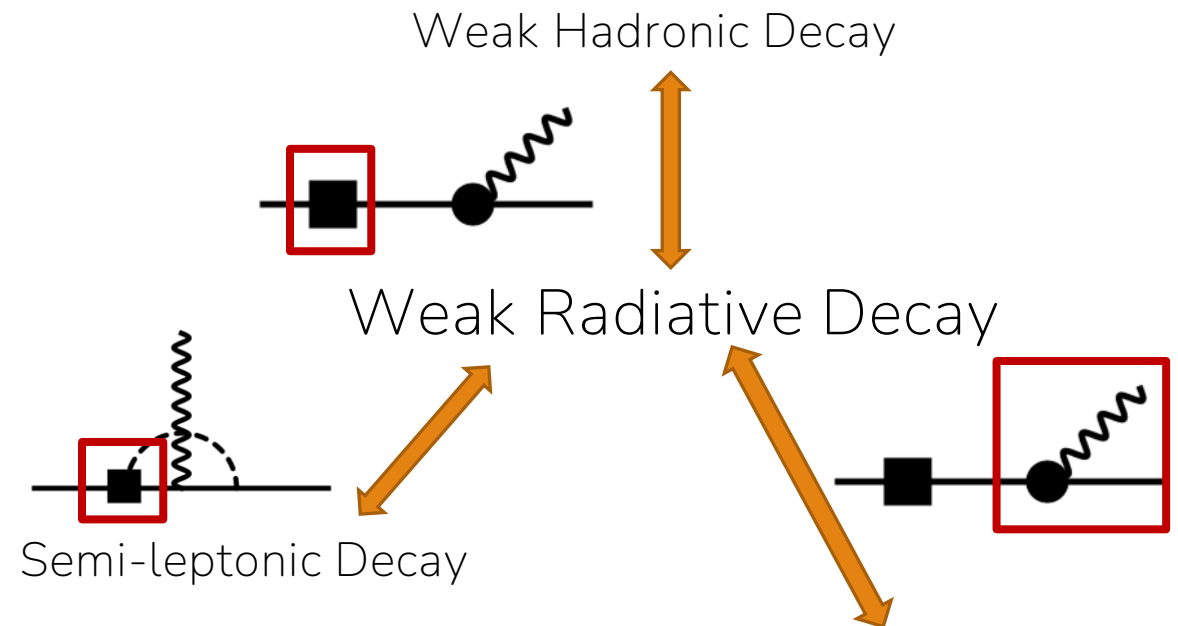
$$\mathcal{L} = \frac{eG_F}{2} \bar{B}_f (a^{\text{PC}} + b^{\text{PV}} \gamma_5) \sigma^{\mu\nu} B_i F_{\mu\nu}$$

- Decay width & decay asymmetry

$$\Gamma = \frac{e^2 G_F^2}{\pi} (|a|^2 + |b|^2) \cdot |\vec{k}|^3$$

$$\alpha_\gamma = \frac{2\text{Re}(ab^*)}{|a|^2 + |b|^2}$$

- Reveal common hyperon properties
 - Decay mechanism
 - EM structure
 -



[j.scib.2022.10.026](https://doi.org/10.26434/chemrxiv-2022-10-026)

Baryon Magnetic Moment

Physics Motivation

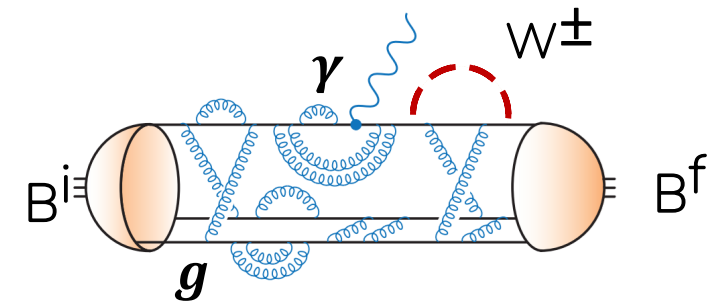
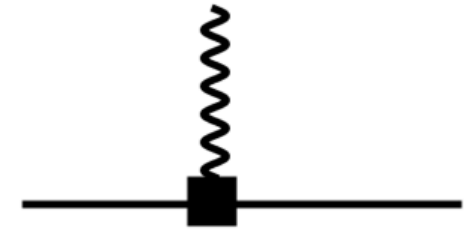
Effective Theory Point-of-view

- Unique contribution from “direct photon emission”
 - PV amplitude from direct photon emission:

$$\text{Re}(b)_{\Xi^0 \Sigma^0} = \sqrt{3} \text{Re}(b)_{\Xi^0 \Lambda}, \quad \text{Re}(b)_{\Lambda n} = -\text{Re}(b)_{\Xi^0 \Lambda}$$

$$\text{Re}(b)_{\Sigma^0 n} = -\sqrt{3} \text{Re}(b)_{\Xi^0 \Lambda}, \quad \text{Re}(b)_{\Sigma^+ p} = \text{Re}(b)_{\Xi^- \Sigma^- = 0}$$

- Need experiment input from $\Xi^0 \rightarrow \Lambda(\Sigma^0)\gamma$ or $\Lambda \rightarrow n\gamma$ process
- Two quark exchange suppressed $\Xi^- \rightarrow \Sigma^- \gamma$ and $\Omega^- \rightarrow \Xi^- \gamma$ process
 - Much smaller decay width
 - More sensitive to effective models?



Physics Motivation

Physics Beyond the Scope of QCD Phenomenon

- New physics in $B_i \rightarrow B_f l^+ l^-$ decay
 - Smoke screen of new physics in $\Sigma^+ \rightarrow p \mu^+ \mu^-$ decay ([PhysRevLett.94.021801](#))
 - Experiment results of WRHDs provide **SM expectations** on such decays – narrowing the range for NP! ([JHEP10\(2018\)040](#), [JHEP02\(2022\)178](#))
- CP Violation in WRHDs
 - CPV in heavy flavor radiative decays may be significantly enhanced by NP
 - Extensive experimental studies on **D and B meson decays**
 - Limited studies in **baryon sector**
 - WRHDs serve as a probe for CPV
 - [PhysRevLett.109.171801](#), [JHEP01\(2013\)027](#), [JHEP04\(2017\)027](#), [JHEP08\(2017\)09](#)
 - [PhysRevLett.70.2529](#), [PhysRevLett.109.191801](#), [PhysRevLett.118.051801](#), [PhysRevLett.119.191802](#)
 - [PhysRevD.51.2271](#), [PhysRevD.65.074038](#), [PhysRevD.105.116001](#), [Commun.Theor.Phys.19.4](#)
 - [PhysRevD.105.L051104](#)

Physics Motivation

Experiment Research Status

Fixed target experiments govern the results in 1965-2010 (~23 papers from over 5 experiments)

$\Sigma^+ \rightarrow p\gamma$			
时间	实验名或实验方案	分支比 ($\times 10^{-3}$)	α_γ
2023	BESIII	$0.996 \pm 0.021 \pm 0.018$	$-0.652 \pm 0.056 \pm 0.020$
1995	E761	1.20 ± 0.08	-
1992	SPEC	-	-0.720 ± 0.086
1989	CNTR	1.45 ± 0.31	-
1987	CNTR	1.23 ± 0.20	-
1985	CNTR	1.27 ± 0.18	-
1980	HBC	1.09 ± 0.20	-0.53 ± 0.36
1969	HBC	1.1 ± 0.2	-
1969	HBC	1.42 ± 0.26	-1.03 ± 0.52
1965	HBC	1.9 ± 0.4	-

$\Lambda \rightarrow n\gamma$			
时间	实验名或实验方案	分支比 ($\times 10^{-3}$)	α_γ
2022	BESIII	$0.846 \pm 0.039 \pm 0.052$	$-0.160 \pm 0.101 \pm 0.046$
1994	E761	1.75 ± 0.15	-
1992	SPEC	1.78 ± 0.24	-

$\Xi^0 \rightarrow \Lambda\gamma$			
时间	实验名或实验方案	分支比 ($\times 10^{-3}$)	α_γ
2010	NA48	-	-0.704 ± 0.064
2004	NA48	1.17 ± 0.09	-0.78 ± 0.18
2000	NA48	1.91 ± 0.34	-
1990	SPEC	1.06 ± 0.18	-0.43 ± 0.44

$\Xi^0 \rightarrow \Sigma^0\gamma$			
时间	实验名或实验方案	分支比 ($\times 10^{-3}$)	α_γ
2010	NA48	-	-0.729 ± 0.076
2001	KTEV	3.34 ± 0.09	-0.63 ± 0.09
2000	NA48	3.16 ± 0.76	-
1989	SPEC	3.56 ± 0.42	0.20 ± 0.32

$\Xi^- \rightarrow \Sigma^-\gamma$			
时间	实验名或实验方案	分支比 ($\times 10^{-3}$)	α_γ
1994	E761	0.122 ± 0.023	-
1987	SPEC	0.227 ± 0.102	-

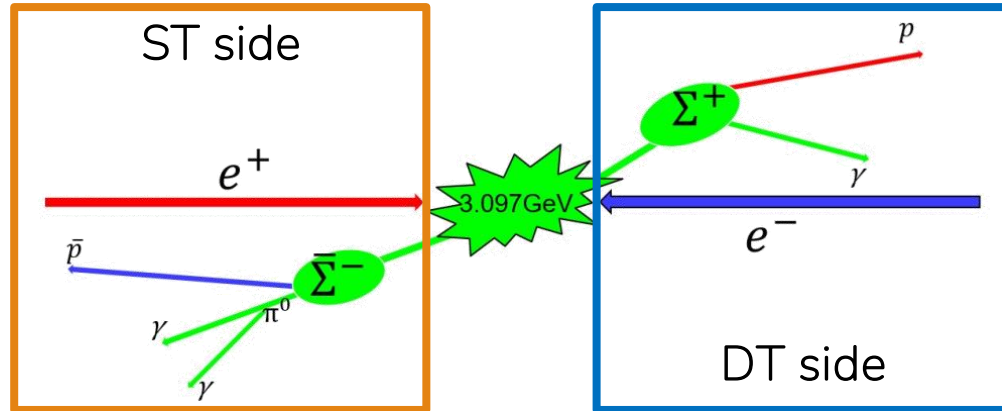
$\Omega^- \rightarrow \Xi^-\gamma$			
时间	实验名或实验方案	分支比 ($\times 10^{-3}$)	α_γ
1994	E761	<0.46	-
1984	SPEC	<0.22	-
1979	SPEC	<0.31	-

Research Methods

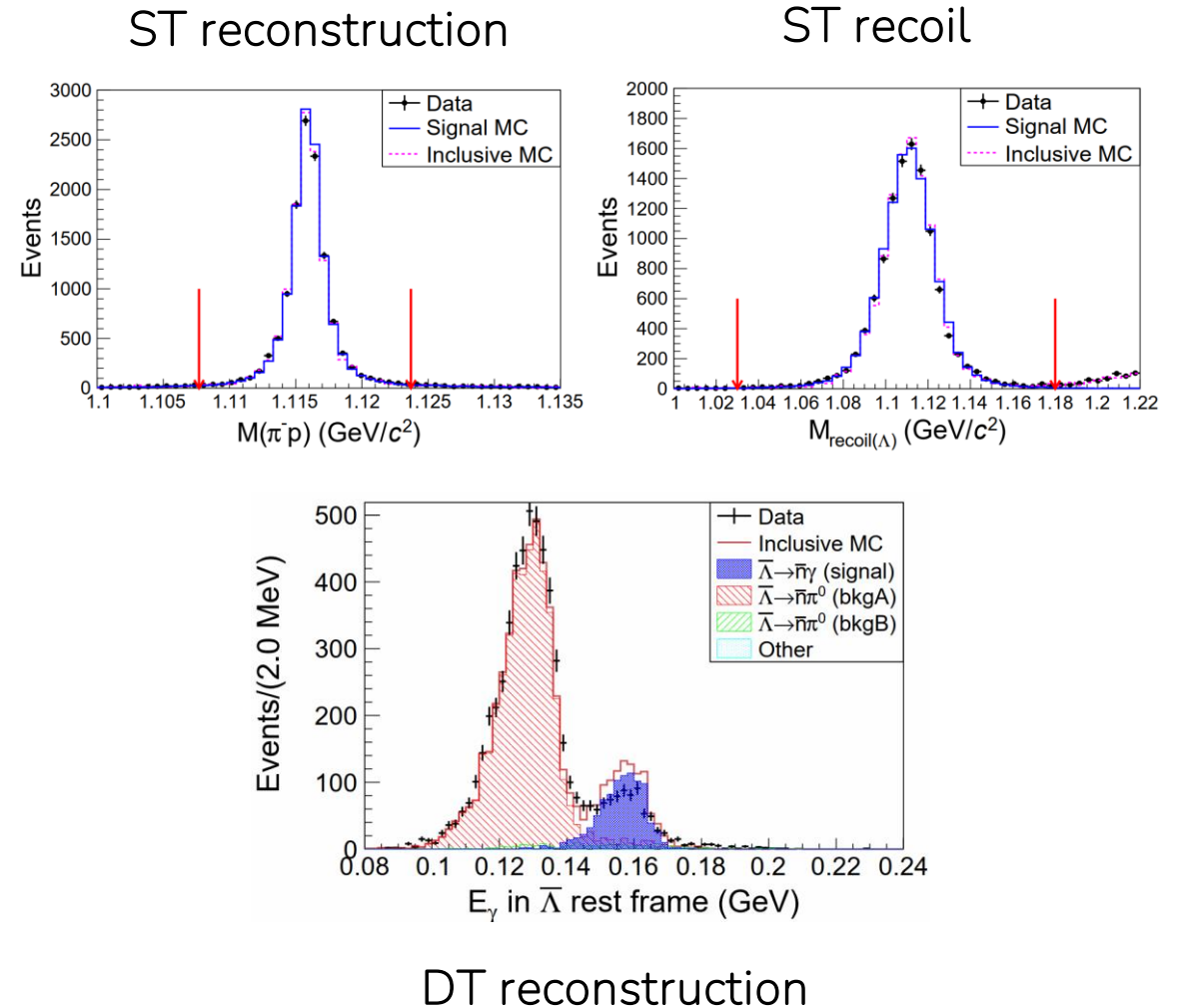
Absolute BF Measurement

Double-tag method for BF measurement

$$BF = \frac{N_{DT}}{N_{ST}} \times \frac{\varepsilon_{ST}}{\varepsilon_{DT}}$$



- Well constrained kinematics
- Absolute BF measurement
- Canceled ST selection syst. uncertainty



Research Methods

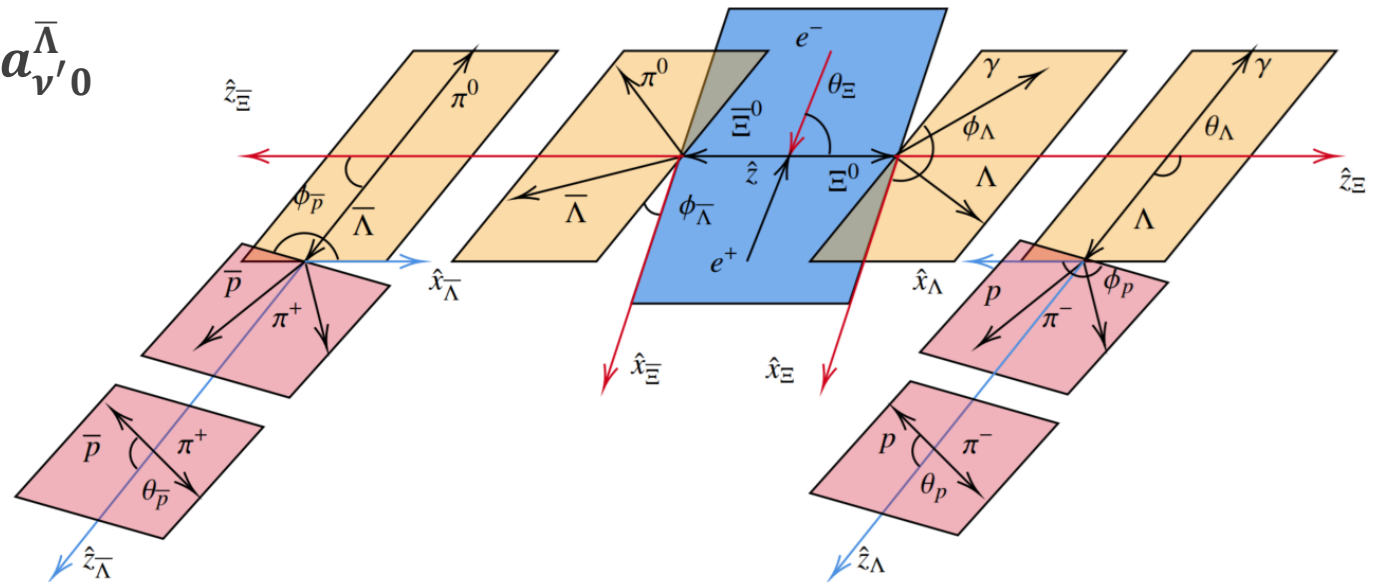
Decay Parameter Measurement

Uniquely **pair-produced** hyperons from ψ decay

- e.g. $e^+e^- \rightarrow J/\psi \rightarrow \Xi^0(\rightarrow \Lambda\gamma)\bar{\Xi}^0(\rightarrow \bar{\Lambda}\pi^0)$ $\Lambda \rightarrow p\pi^-$, $\bar{\Lambda} \rightarrow \bar{p}\pi^+$

Decay amplitude (Helicity):

$$\mathcal{W} = \sum_{\mu,\nu=0}^3 \sum_{\mu'=0}^3 \sum_{\nu'=0}^3 C_{\mu\nu} a_{\mu\mu'}^{\Xi} a_{\mu'0}^{\Lambda} a_{\nu\nu'}^{\bar{\Xi}} a_{\nu'0}^{\bar{\Lambda}}$$



Helicity angles:

$$\theta_{\Xi}, \theta_{\Lambda}, \phi_{\Lambda}, \theta_{\bar{\Lambda}}, \phi_{\bar{\Lambda}}, \theta_p, \phi_p, \theta_{\bar{p}}, \phi_{\bar{p}}$$

Decay parameters:

$$\alpha_{J/\psi}, \Delta\Phi_{J/\psi}, \alpha_{\Xi}, \Delta\Phi_{\Xi}, \alpha_{\bar{\Xi}}, \Delta\Phi_{\bar{\Xi}}, \alpha_{\Lambda}, \alpha_{\bar{\Lambda}}$$

Research Methods

Decay Parameter Measurement

\mathbf{C} : polarization and spin correlation matrix of $B\bar{B}$ \mathbf{a} : decay matrices of hyperons

$$\begin{aligned}
 C_{00} &= 2(1 + \alpha_\Psi \cos^2 \theta_{\Xi^0}), & C_{20} &= -C_{02}, \\
 C_{02} &= 2\sqrt{1 - \alpha_\Psi^2} \sin \theta_{\Xi^0} \cos \theta_{\Xi^0} \sin(\Delta\Phi_\Psi), & C_{22} &= \alpha_\Psi C_{11}, \\
 C_{11} &= 2 \sin^2 \theta_{\Xi^0}, & C_{31} &= -C_{13}, \\
 C_{13} &= 2\sqrt{1 - \alpha_\Psi^2} \sin \theta_{\Xi^0} \cos \theta_{\Xi^0} \cos(\Delta\Phi_\Psi), & C_{33} &= -2(\alpha_\Psi + \cos^2 \theta_{\Xi^0}),
 \end{aligned}$$

BESIII observation of non-zero $\Delta\Phi_\Psi$

- Transverse polarization and spin-correlation between hyperon pairs ([Nat. Phys. 15, 631–634 \(2019\)](#))

衰变道	α_ψ	$\Delta\Phi_\psi$	最大极化率 (%)
$J/\psi \rightarrow \Lambda\bar{\Lambda}$	$0.475 \pm 0.002 \pm 0.003$	$0.752 \pm 0.004 \pm 0.007$	24.7
$J/\psi \rightarrow \Sigma^+\bar{\Sigma}^-$	$-0.508 \pm 0.006 \pm 0.004$	$-0.270 \pm 0.012 \pm 0.009$	16.4
$J/\psi \rightarrow \Xi^-\bar{\Xi}^+$	$0.586 \pm 0.012 \pm 0.010$	$1.213 \pm 0.046 \pm 0.016$	30.1
$J/\psi \rightarrow \Xi^0\bar{\Xi}^0$	$0.514 \pm 0.006 \pm 0.015$	$1.168 \pm 0.019 \pm 0.018$	32.1

$$\beta = \sqrt{1 - \alpha^2} \sin(\Delta\Phi), \quad \gamma = \sqrt{1 - \alpha^2} \cos(\Delta\Phi)$$

- For $\frac{1}{2}^+ \rightarrow \frac{1}{2}^+ + \mathbf{0}^-$ decay ($\Xi^0 \rightarrow \Lambda\pi^0$)

$$a_h^{\Xi} = \begin{pmatrix} 1 & 0 & 0 & \alpha \\ \alpha \cos \phi \sin \theta & \gamma \cos \theta \cos \phi - \beta \sin \phi & -\beta \cos \theta \cos \phi - \gamma \sin \phi & \sin \theta \cos \phi \\ \alpha \sin \theta \sin \phi & \beta \cos \phi + \gamma \cos \theta \sin \phi & \gamma \cos \phi - \beta \cos \theta \sin \phi & \sin \theta \sin \phi \\ \alpha \cos \theta & -\gamma \sin \theta & \beta \sin \theta & \cos \theta \end{pmatrix}$$

- For $\frac{1}{2}^+ \rightarrow \frac{1}{2}^+ + \mathbf{1}^-$ decay ($\Xi^0 \rightarrow \Lambda\gamma$)

$$a_r^{\Xi} = \begin{pmatrix} 1 & 0 & 0 & -\alpha \\ \alpha \cos \phi \sin \theta & 0 & 0 & -\sin \theta \cos \phi \\ \alpha \sin \theta \sin \phi & 0 & 0 & -\sin \theta \sin \phi \\ \alpha \cos \theta & 0 & 0 & -\cos \theta \end{pmatrix}$$

Decay parameters fitted from amplitude

- Sensitivity multiplied by ~ 10 times ([Chin. Phys. C 47, 093103 \(2023\)](#))

$\Lambda \rightarrow n\gamma$ Analysis

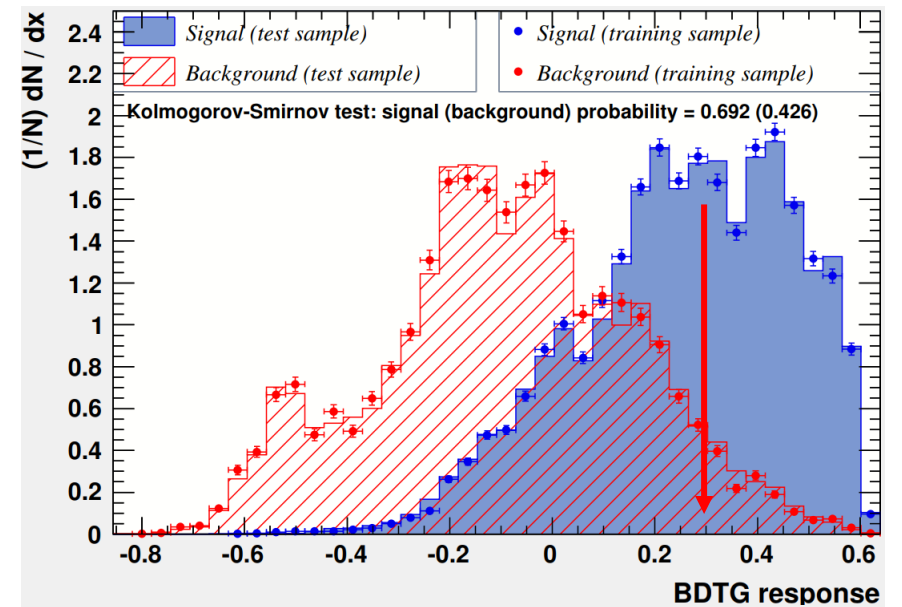
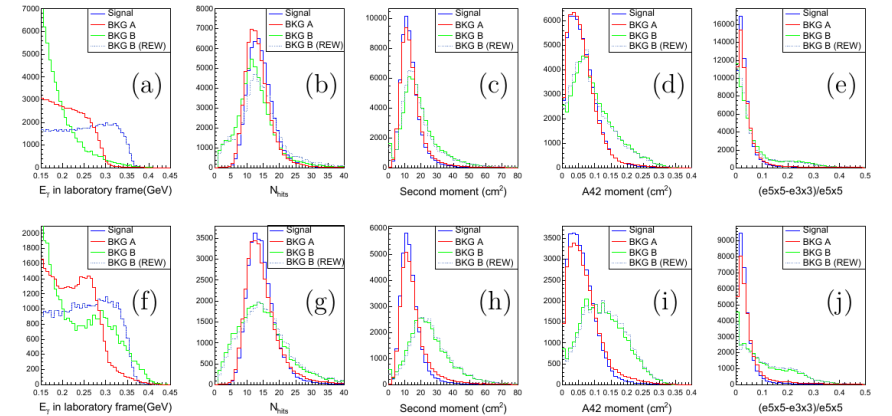
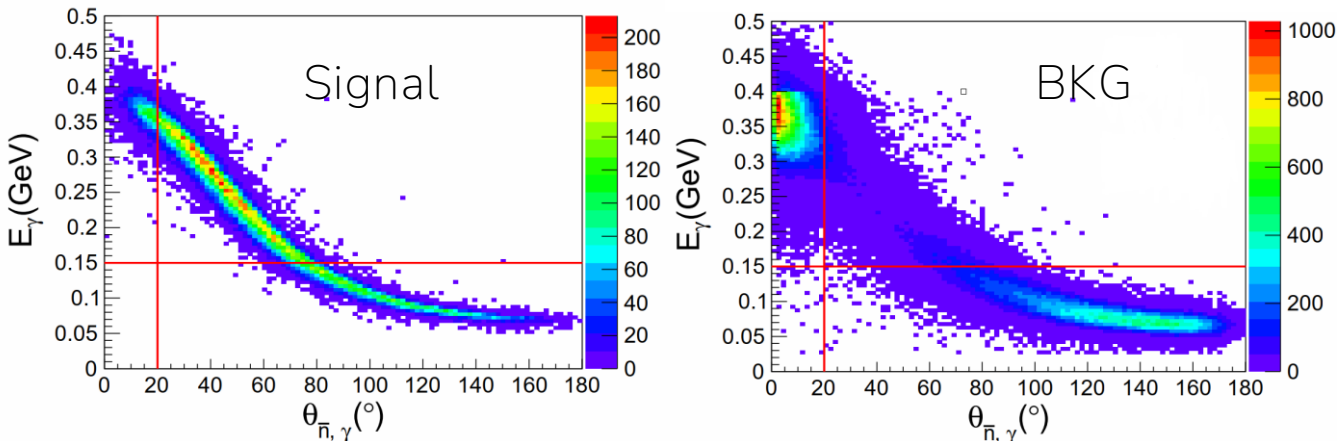
Analysis Method Highlights

Kinematic fit with missing particle/energy

- Hypothesis: $\bar{\Lambda}(\rightarrow \bar{p}\pi^+)\gamma + n(\text{missing particle})$
- Hypothesis: $\Lambda(\rightarrow p\pi^-)\gamma + \bar{n}(\text{missing energy})$
- Superiority of well-constrained kinematics

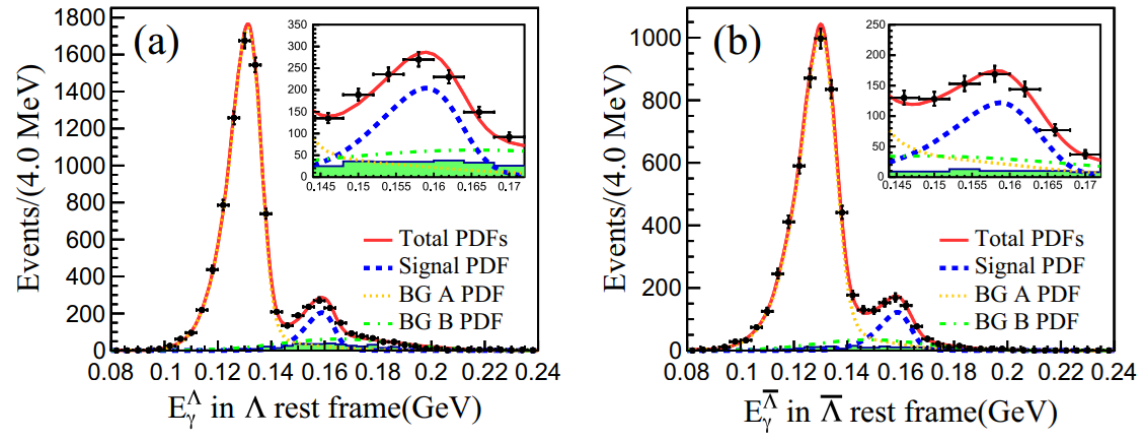
MVA-based fake photon suppression

- $\epsilon_{\text{bkg}} = 3.1\%$, $\epsilon_{\text{sig}} = 50.1\%$

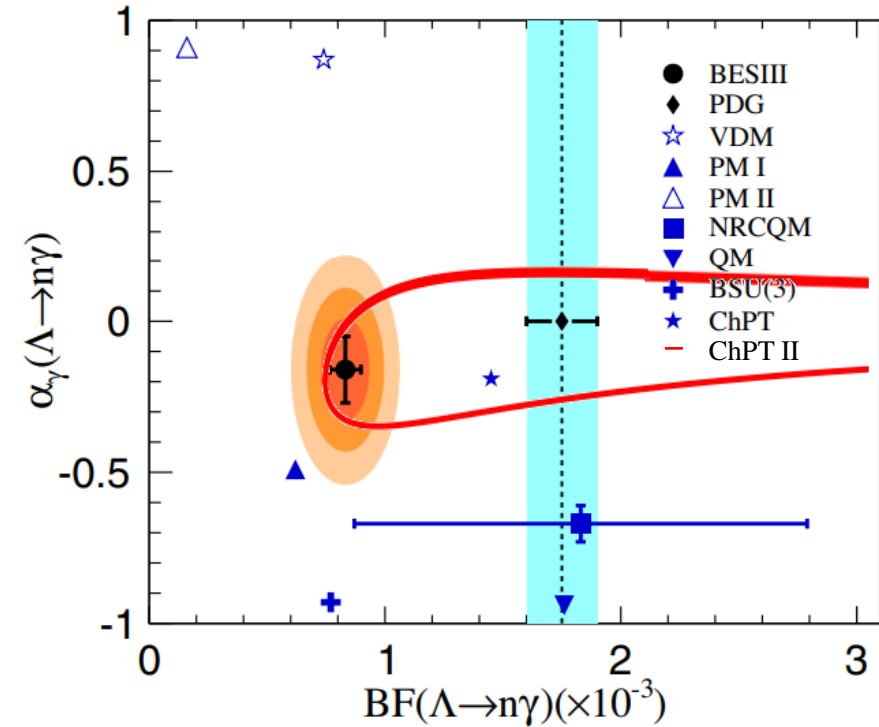


$\Lambda \rightarrow n\gamma$ Analysis

Analysis Results



Decay mode	$\Lambda \rightarrow n\gamma$	$\bar{\Lambda} \rightarrow \bar{n}\gamma$
$N_{ST} (\times 10^3)$	6853.2 ± 2.6	7036.2 ± 2.7
$\varepsilon_{ST} (\%)$	51.13 ± 0.01	52.53 ± 0.01
N_{DT}	723 ± 40	498 ± 41
$\varepsilon_{DT} (\%)$	6.58 ± 0.04	4.32 ± 0.03
$BF (\times 10^{-3})$	$0.820 \pm 0.045 \pm 0.066$	$0.862 \pm 0.071 \pm 0.084$
	$0.832 \pm 0.038 \pm 0.054$	
α_γ	$-0.13 \pm 0.13 \pm 0.03$	$0.21 \pm 0.15 \pm 0.06$
	$-0.16 \pm 0.10 \pm 0.05$	



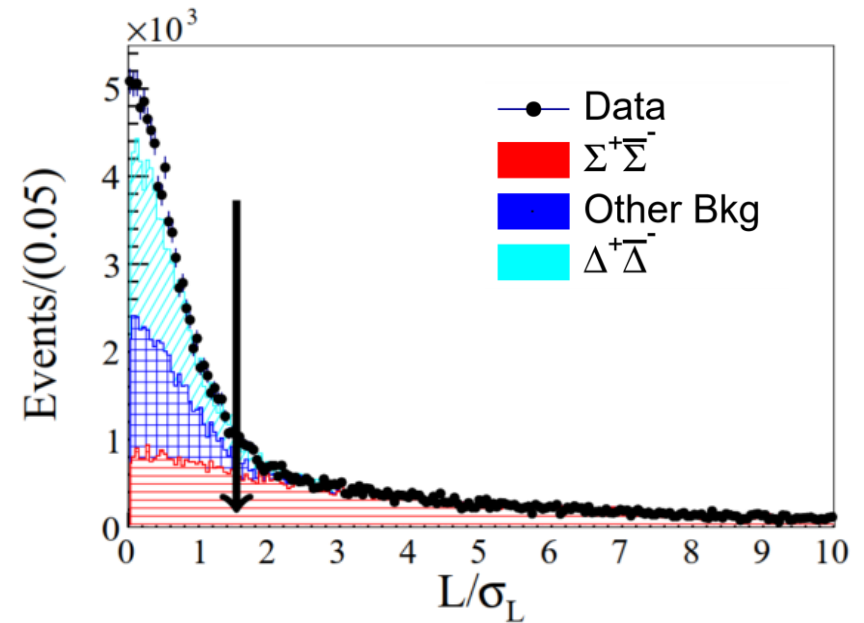
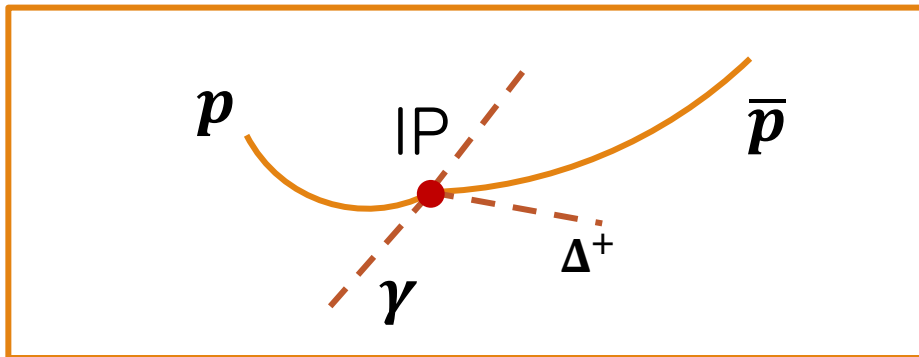
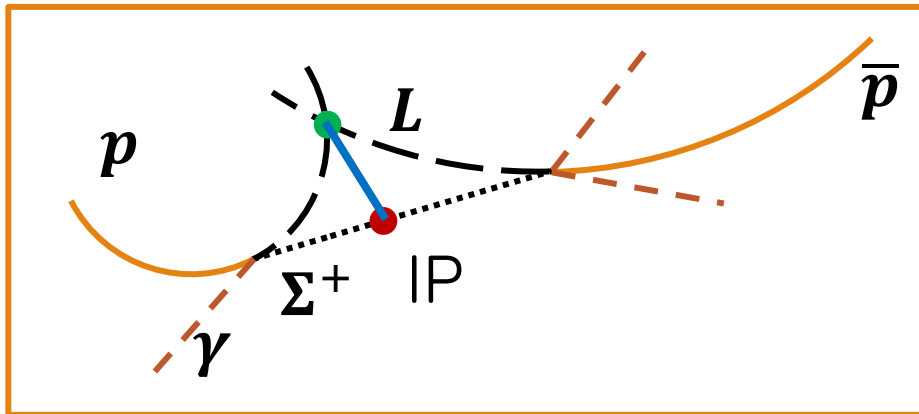
First measurement on α_γ

5.6σ deviation of BF

$\Sigma^+ \rightarrow p\gamma$ Analysis

Analysis Method Highlights

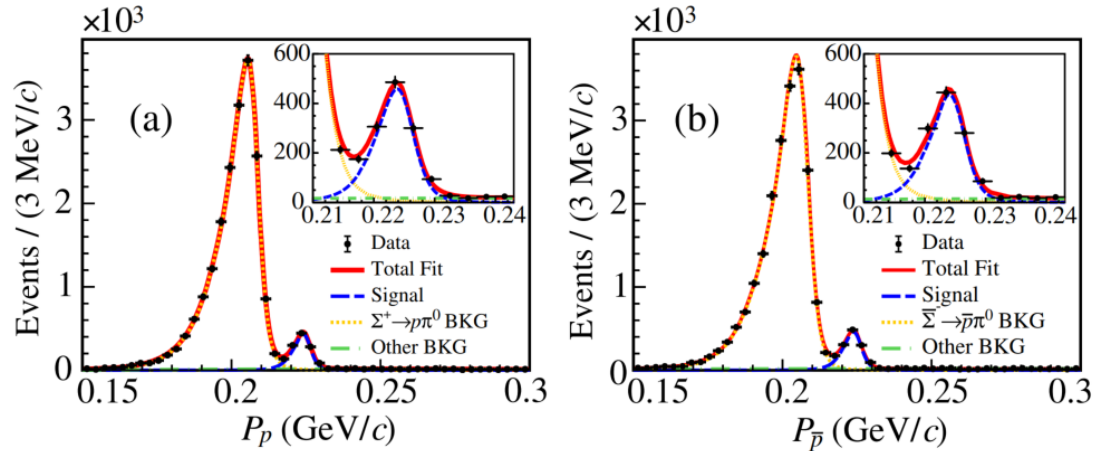
Utilize joint decay length to discriminate short-lived baryons from signals



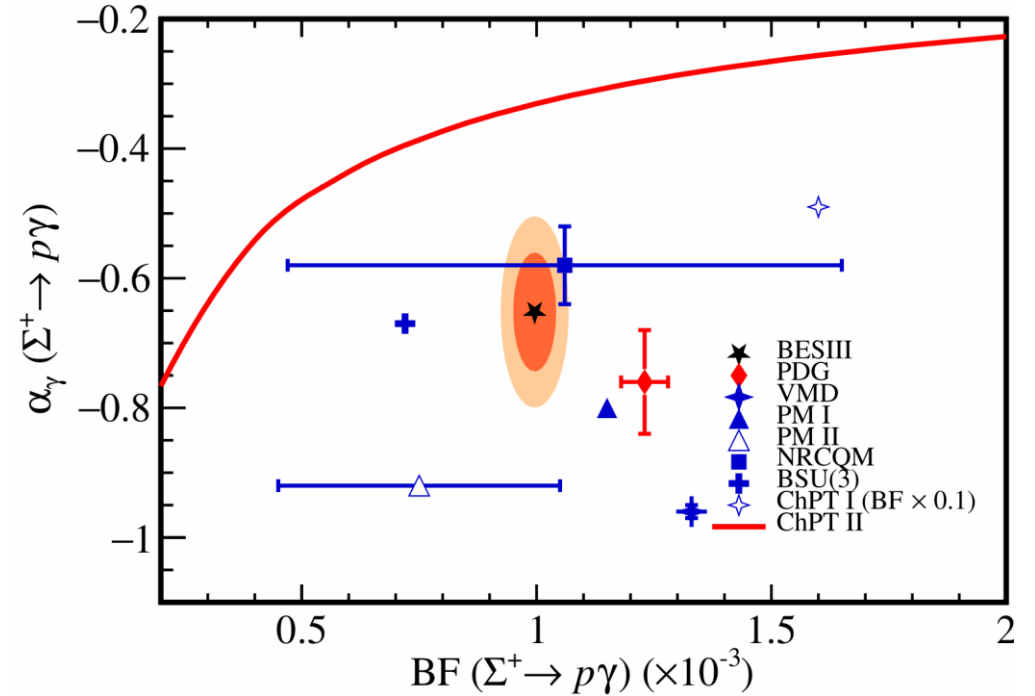
Signal efficiency > 78%
Background efficiency < 7%

$\Sigma^+ \rightarrow p\gamma$ Analysis

Analysis Results



Mode	$\Sigma^+ \rightarrow p\gamma$	$\Sigma^- \rightarrow \bar{p}\gamma$
N_{ST}^{obs}	$2\,177\,771 \pm 2285$	$2\,509\,380 \pm 2301$
ϵ_{ST} (%)	39.00 ± 0.04	44.31 ± 0.04
N_{DT}^{obs}	1189 ± 38	1306 ± 39
ϵ_{DT} (%)	21.16 ± 0.03	23.20 ± 0.03
Individual BF (10^{-3})	1.005 ± 0.032	0.993 ± 0.030
Simultaneous BF (10^{-3})	$0.996 \pm 0.021 \pm 0.018$	
Individual α_γ	-0.587 ± 0.082	0.710 ± 0.076
Simultaneous α_γ	$-0.652 \pm 0.056 \pm 0.020$	



Significantly improved accuracy

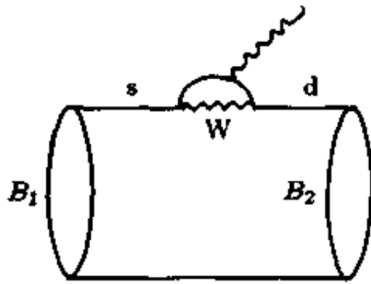
- BF: 78%
- α_γ : 34%

$\Sigma^+ \rightarrow p\gamma$ Analysis

CP Asymmetry Test

Potential **CP** asymmetry sources:

- Loop diagram contribution:



- Other terms - strong phase dependent on QCD models:

$$S = \sum_j S_j e^{i(\xi_j^S + \delta_{2I}^S)}$$

$$P = \sum_j P_j e^{i(\xi_j^P + \delta_{2I}^P)}$$

First Measurement of CP asymmetry of $\Sigma^+ \rightarrow p\gamma$ decay

- Statistical uncertainty dominated
- Need more statistics to reach the precision of theory predictions

$$\Delta_{CP} = \frac{\mathcal{B}_+ - \mathcal{B}_-}{\mathcal{B}_+ + \mathcal{B}_-} = 0.006 \pm 0.011_{\text{stat.}} \pm 0.004_{\text{sys.}},$$

$$A_{CP} = \frac{\alpha_- + \alpha_+}{\alpha_- - \alpha_+} = 0.095 \pm 0.087_{\text{stat.}} \pm 0.018_{\text{sys.}}$$

	Δ_{CP}	A_{CP}
PhysRevD.51.2271	$10^{-5} - 10^{-4}$	
Commun. Theor. Phys. 19.475		$10^{-5} - 10^{-4}$
arxiv:2312.17568	2×10^{-5}	

Summary & Prospects

Since 2022, BESIII experiment has provided fresh results to the field

Inconsistency between exp. results and theory predictions still exist

More results with higher precision expected

$\Lambda \rightarrow n\gamma$ ([Phys.Rev.Lett. 129 \(2022\)](#))

	BF ($\times 10^{-3}$)	α_γ
2022, BESIII	$0.846 \pm 0.039 \pm 0.052$	$-0.160 \pm 0.101 \pm 0.046$
PDG	1.75 ± 0.15	---

$\Sigma^+ \rightarrow p\gamma$ ([Phys. Rev. Lett. 130, 211901 \(2023\)](#))

Experiment	BF ($\times 10^{-3}$)	α_γ
2022, BESIII	$0.996 \pm 0.021 \pm 0.018$	$-0.652 \pm 0.056 \pm 0.020$
PDG	1.23 ± 0.05	-0.76 ± 0.08

Significantly improved precision

$\Xi^0 \rightarrow \Lambda\gamma$ ([BAM-760](#))

Experiment	BF ($\times 10^{-3}$)	α_γ
2024, BESIII	xxx	xxx
PDG	1.17 ± 0.07	-0.70 ± 0.07

$\Xi^0 \rightarrow \Sigma^0\gamma$

Experiment	BF ($\times 10^{-3}$)	α_γ
BESIII	xxx	xxx
PDG	3.33 ± 0.10	-0.69 ± 0.06

Competitive precision

Summary & Prospects

Studies on $\Xi^- \rightarrow \Sigma^- \gamma$ and $\Omega^+ \rightarrow \Xi^- \gamma$ decays undergoing

“The last piece of the puzzle”

$\Xi^- \rightarrow \Sigma^- \gamma$		
Experiment	BF ($\times 10^{-3}$)	α_γ
BESIII	?	?
PDG	1.27 ± 0.23	---

$\Omega^+ \rightarrow \Xi^- \gamma$		
Experiment	BF ($\times 10^{-3}$)	α_γ
BESIII	?	
PDG	< 0.46	---

Special thanks to Prof. L.-S. Geng and Dr. R.-X. Shi