

Fully-heavy Tetraquark Productions and Decays

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April 7, 2024

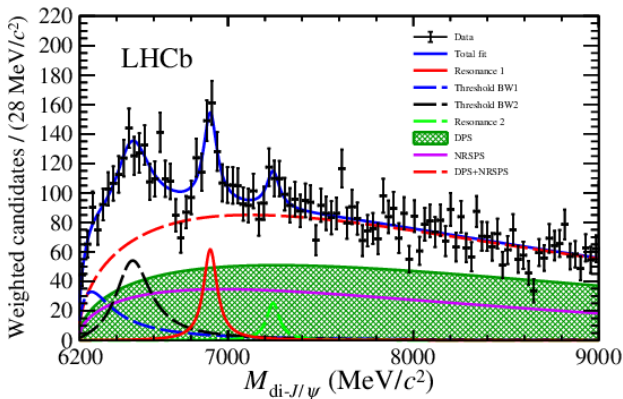
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Overview

Overview

Double J/ψ Resonances

- Double J/ψ resonances observed at the LHC



Questions

| | | | |
|------------------------|-----------------------|-----------------------|-----------------------|
| $T_{cc\bar{c}\bar{c}}$ | $^1S_0(^1S_0, ^1S_0)$ | $^1S_0(^3S_1, ^3S_1)$ | $^5S_2(^3S_1, ^3S_1)$ |
| $M_{J/\psi J/\psi}$ | 1S_0 | 5S_2 | |

- How to determine its J^{PC} ?
 - From first principle
 - Robust!

NRQCD Framework

NRQCD Framework

NRQCD Factorization

- Cross Section Factorization

$$d\sigma(H) = \sum_n d\hat{\sigma}(n) \langle \mathcal{O}^H(n) \rangle$$

- n : intermediate state
- $\hat{\sigma}(n)$: Short-distance coefficient
- $\langle \mathcal{O}^H(n) \rangle$: Long-distance Matrix Element

Replacement

- For J/ψ

$$v_i(p_b)\bar{u}_j(p_a) \rightarrow \Pi_{J/\psi} \equiv \frac{1}{2\sqrt{2}} \frac{1}{\sqrt{N_c}} \delta_{ij} \not{\epsilon}(\not{p} + m_{J/\psi})$$

$$d\Phi_a d\Phi_b \rightarrow d\Phi_{J/\psi} \equiv \frac{d^3p}{(2\pi)^3 2p_0} \frac{2}{m_{J/\psi}} |\psi_{J/\psi}(0)|^2$$

Replacement

- For Molecule

$$\epsilon^\mu \otimes \epsilon^\nu \rightarrow \epsilon_{ss_z}^{\mu\nu}$$

$$\epsilon_{00}^{\mu\nu} = \sqrt{\frac{1}{3}} \left(-g^{\mu\nu} + \frac{P^\mu P^\nu}{M^2} \right) \equiv \sqrt{\frac{1}{3}} \Pi^{\mu\nu}$$

$$\sum_{s_z} \epsilon_{2s_z}^{\mu\nu} \epsilon_{2s_z}^{\alpha\beta*} = \frac{1}{2} (\Pi^{\mu\alpha} \Pi^{\nu\beta} + \Pi^{\mu\beta} \Pi^{\nu\alpha}) - \frac{1}{3} \Pi^{\mu\nu} \Pi^{\alpha\beta}$$

Replacement

- For Genuine Tetraquark
 - CParity Transformation:

$$\begin{aligned} & \bar{u}_i^\alpha(p_b)(\not{k}_1 + m_1) \dots (\not{k}_n + m_n) v_j^\beta(p_{(c,d)}) \\ &= \bar{u}_j^\beta(p_{(c,d)})(-\not{k}_n + m_n) \dots (-\not{k}_1 + m_1) v_i^\alpha(p_b) \end{aligned}$$

- Replacement

$$\begin{aligned} & v_{i_b}(p_b) \bar{u}_{i_a}(p_a) \otimes v_{i_{(c,d)}}(p_{(c,d)}) \bar{u}_{i_{(d,c)}}(p_{(d,c)}) \\ & \rightarrow \frac{1}{32} \varepsilon_{ssz}^{\mu\nu} \frac{\delta_{i_a i_c} \delta_{i_b i_d} - \delta_{i_a i_d} \delta_{i_b i_c}}{\sqrt{12}} \times \gamma^\mu(\not{p} + M) \otimes \gamma^\nu(\not{p} + M) \end{aligned}$$

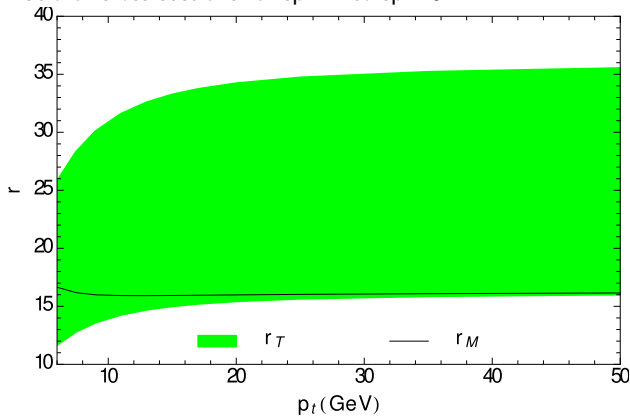
$$\begin{aligned} & v_{i_b}(p_b) \bar{u}_{i_a}(p_a) \otimes v_{i_{(c,d)}}(p_{(c,d)}) \bar{u}_{i_{(d,c)}}(p_{(d,c)}) \\ & \rightarrow \frac{1}{32} \text{sgn} \frac{\delta_{i_a i_c} \delta_{i_b i_d} + \delta_{i_a i_d} \delta_{i_b i_c}}{\sqrt{24}} \times \gamma^5(\not{p} + M) \otimes \gamma^5(\not{p} + M) \end{aligned}$$

Results

Results

Production

- Ratio of cross sections for spin-2 to spin-0



Decay

- Ratio of the branching fractions for charmed decay and non-charmed decay

$$\mathcal{R}(T_M(0)) = \frac{3\sqrt{3}}{338} \approx 0.0154,$$

$$\mathcal{R}(T_M(2)) = \frac{\sqrt{3}}{28} + \frac{12\sqrt{3}}{343}n_l \approx 0.0619 + 0.0606n_l,$$

$$\mathcal{R}(T_C^+(0)) = \frac{121\sqrt{3}}{6} \approx 34.9,$$

$$\mathcal{R}(T_C^-(0)) = \frac{243\sqrt{3}}{242} \approx 1.74,$$

$$\mathcal{R}(T_C^-(2)) = \frac{\sqrt{3}}{28} + \frac{12\sqrt{3}}{343}n_l \approx 0.0619 + 0.0606n_l.$$

Conclusion

Conclusion

Decay

- The observed resonances are likely spin-2
- Information can be accessed by measuring the ratio of the branching fractions for charmed decay and non-charmed decay

Thanks

Thanks!

Appendix

Appendix

New Ansatz

- Construct an eigenstate of angular momentum
- Spatial wave function

$$\psi = \sum_{mm' m_1 m_2} C_{LM}^{mm'} Y_{lm}(\theta, \vartheta) R_{nl}(r) C_{l'm'}^{m_1 m_2} \\ \times Y_{l_1 m_1}(\theta_1, \vartheta_1) R_{1n_1 l_1}(r_1) Y_{l_2 m_2}(\theta_2, \vartheta_2) R_{2n_2 l_2}(r_2)$$

- Functions to be solved: R_{nl} , $R_{1n_1 l_1}$, $R_{2n_2 l_2}$

Hartree-Fock Equations

- Hartree-Fock Equation via new ansatz

$$\left[-\frac{\hbar^2}{2m_q} \left(\frac{1}{r} \frac{d^2}{dr^2} r - \frac{l(l+1)}{r^2} \right) + V_0(r) - \mathcal{E}_0 \right] R_{nl}(r) = 0,$$

$$\left[-\frac{\hbar^2}{m_q} \left(\frac{1}{r_1} \frac{d^2}{dr_1^2} r_1 - \frac{l_1(l_1+1)}{r_1^2} \right) + V_{qq}(r_1) + V_1(r_1) - \mathcal{E}_1 \right] R_{1m_1 l_1}(r_1) = 0,$$

$$\left[-\frac{\hbar^2}{m_q} \left(\frac{1}{r_2} \frac{d^2}{dr_2^2} r_2 - \frac{l_2(l_2+1)}{r_2^2} \right) + V_{qq}(r_2) + V_2(r_2) - \mathcal{E}_2 \right] R_{2m_2 l_2}(r_2) = 0$$

$$V_{q\bar{q}}(\mathbf{r}, \mathbf{r}_1, \mathbf{r}_2) = \sum_{lm_1 m_1 l_2 m_2} V_{lm_1 m_1 l_2 m_2}(r, r_1, r_2) Y_{lm}(\theta, \vartheta) Y_{l_1 m_1}(\theta_1, \vartheta_1) Y_{l_2 m_2}(\theta_2, \vartheta_2)$$

$$V_0(r) = \int dr_1 dr_2 \varrho_1(r_1) \varrho_2(r_2) V_{lm_1 m_1 l_2 m_2}(r, r_1, r_2),$$

$$V_1(r_1) = \int dr dr_2 \varrho(r) \varrho_2(r_2) V_{lm_1 m_1 l_2 m_2}(r, r_1, r_2),$$

$$V_2(r_2) = \int dr dr_1 \varrho(r) \varrho_1(r_1) V_{lm_1 m_1 l_2 m_2}(r, r_1, r_2)$$

Thanks!