



Belle(II)上粲重子实验进展

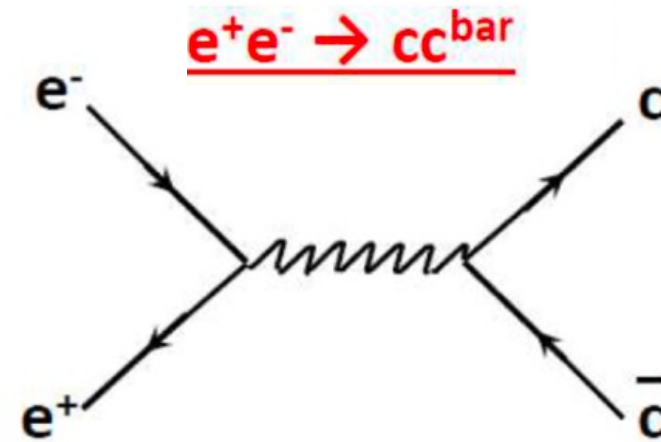
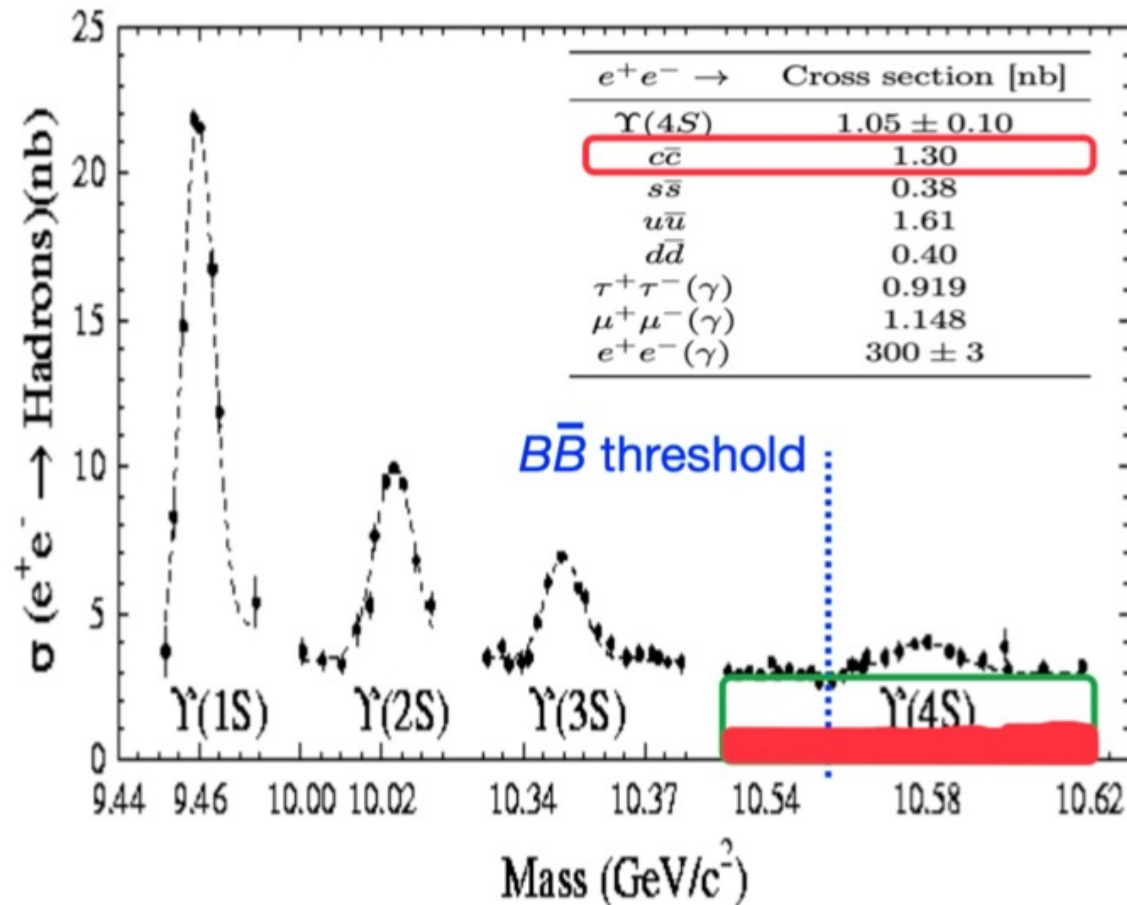
贾森 (东南大学)

on behalf of the Belle and Belle II Collaboration

第三届强子与重味物理理论与实验联合讨论会
2024年4月5 - 9日, 武汉

Dataset and charmed baryon production at Belle(II)

- In B-factories, e^+e^- collider at 10.58 GeV to make $\Upsilon(4S)$ resonance decaying into $B^0\bar{B}^0$ and B^+B^- in 96% of the time.
- Meanwhile, a large cross section for continuum processes $e^+e^- \rightarrow q\bar{q}$ ($q = u, d, s, c$).



Datasets	Luminosity
Belle	980 fb^{-1}
Belle II	426 fb^{-1}

Selected topics:

1. $\Xi_c^0 \rightarrow \Xi^0 h^0$ ($h^0 = \pi^0, \eta, \eta'$) [Preliminary results]
2. $\Xi_c^0 \rightarrow \Xi^0 \ell^+ \ell^-$ [PRD 109, 052003 (2024)]
3. $\Lambda_c^+ \rightarrow \Sigma^+ h^0$ ($h^0 = \pi^0, \eta, \eta'$) [PRD 107, 032003 (2023)]
4. $\Lambda_c^+ \rightarrow p K_S^0 K_S^0, p K_S^0 \eta$ [PRD 107, 032004 (2023)]
5. $\Lambda_c(2625)^+ \rightarrow \Sigma_c^{0,++} \pi$ [PRD 107, 032008 (2023)]
6. $\Lambda_c^+ \rightarrow \Lambda \pi^+ \pi^+ \pi^-$ [PRL 130, 151903 (2023)]
7. $\Omega_c^0 \rightarrow \Xi^- \pi^+ / \Xi^- K^+ / \Omega^- K^+$ [JHEP 01 (2023) 055]

Study of $\Xi_c^0 \rightarrow \Xi^0 h^0$ ($h^0 = \pi^0, \eta, \eta'$)

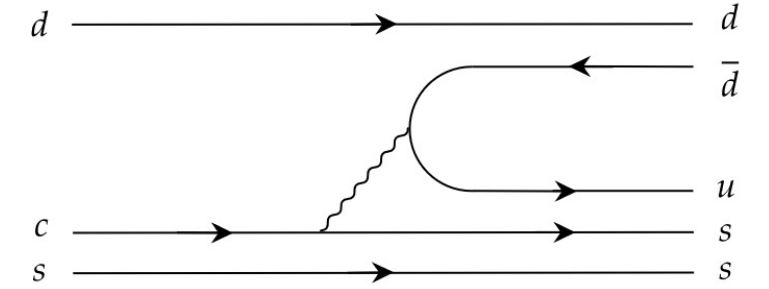
Motivation:

- **Nonfactorizable amplitudes** arising from internal W -emission and W -exchange lead to the difficulties for theoretical predictions in hadronic weak decay of charmed baryons.

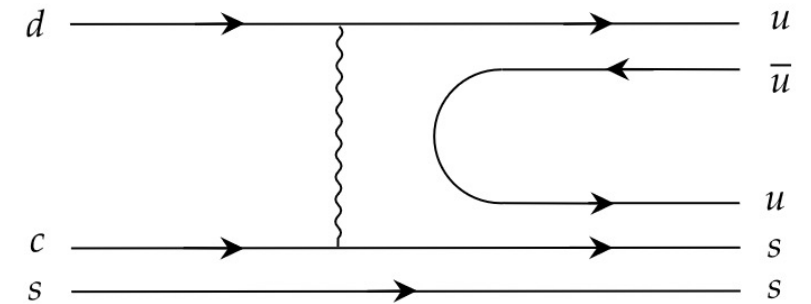
Theoretical predictions for branching fractions ($\times 10^{-3}$) and asymmetry parameters:

Reference	Model	$\mathcal{B}(\Xi_c^0 \rightarrow \Xi^0 \pi^0)$	$\mathcal{B}(\Xi_c^0 \rightarrow \Xi^0 \eta)$	$\mathcal{B}(\Xi_c^0 \rightarrow \Xi^0 \eta')$	$\alpha(\Xi_c^0 \rightarrow \Xi^0 \pi^0)$
Körner, Krämer [5]	quark	0.5	3.2	11.6	0.92
Xu, Kamal [7]	pole	7.7	-	-	0.92
Cheng, Tseng [8]	pole	3.8	-	-	-0.78
Cheng, Tseng [8]	CA	17.1	-	-	0.54
Żenczykowski [9]	pole	6.9	1.0	9.0	0.21
Ivanov <i>et al.</i> [6]	quark	0.5	3.7	4.1	0.94
Sharma, Verma [11]	CA	-	-	-	-0.8
Geng <i>et al.</i> [12]	SU(3) _F	4.3 ± 0.9	$1.7^{+1.0}_{-1.7}$	$8.6^{+11.0}_{-6.3}$	-
Geng <i>et al.</i> [13]	SU(3) _F	7.6 ± 1.0	10.3 ± 2.0	9.1 ± 4.1	$-1.00^{+0.07}_{-0.00}$
Zhao <i>et al.</i> [14]	SU(3) _F	4.7 ± 0.9	8.3 ± 2.3	7.2 ± 1.9	-
Zou <i>et al.</i> [10]	pole	18.2	26.7	-	-0.77
Huang <i>et al.</i> [15]	SU(3) _F	2.56 ± 0.93	-	-	-0.23 ± 0.60
Hsiao <i>et al.</i> [16]	SU(3) _F	6.0 ± 1.2	$4.2^{+1.6}_{-1.3}$	-	-
Hsiao <i>et al.</i> [16]	SU(3) _F -breaking	3.6 ± 1.2	7.3 ± 3.2	-	-
Zhong <i>et al.</i> [17]	SU(3) _F	$1.13^{+0.59}_{-0.49}$	1.56 ± 1.92	$0.683^{+3.272}_{-3.268}$	$0.50^{+0.37}_{-0.35}$
Zhong <i>et al.</i> [17]	SU(3) _F -breaking	$7.74^{+2.52}_{-2.32}$	$2.43^{+2.79}_{-2.90}$	$1.63^{+5.09}_{-5.14}$	$-0.29^{+0.20}_{-0.17}$
Xing <i>et al.</i> [18]	SU(3) _F	1.30 ± 0.51	-	-	-0.28 ± 0.18

Internal W -emission for $\Xi_c^0 \rightarrow \Xi^0 h^0$



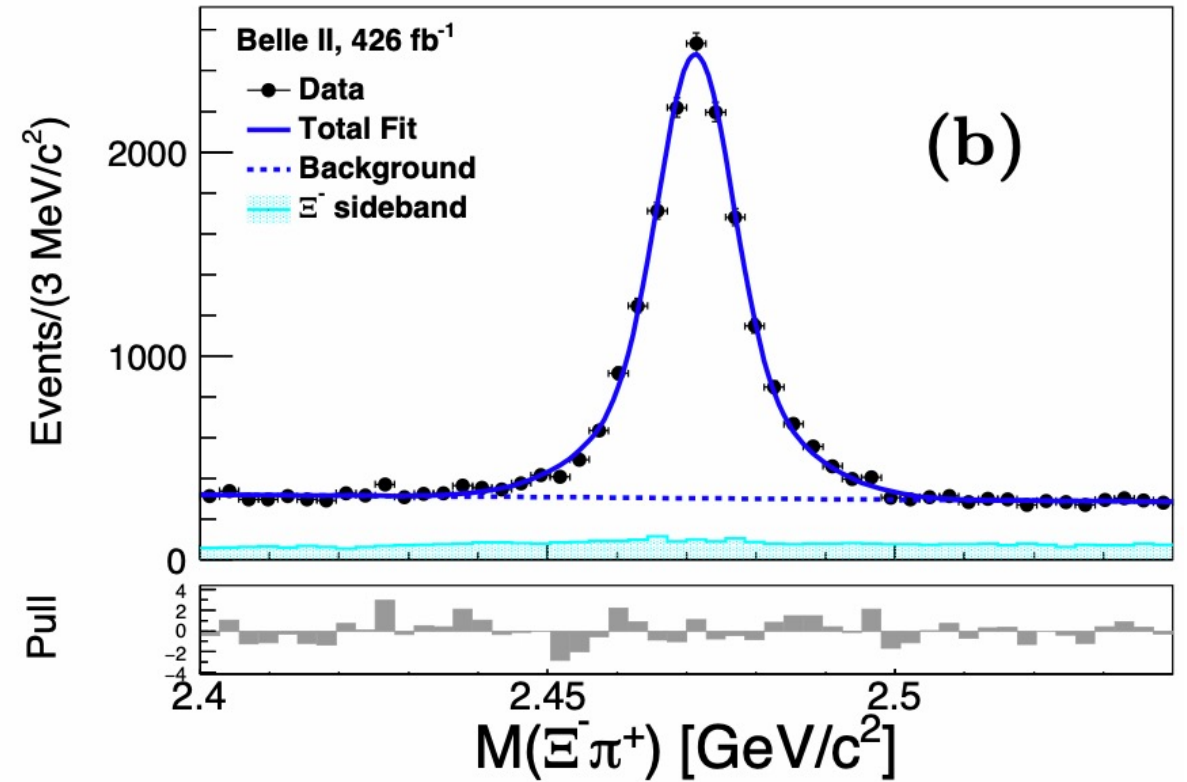
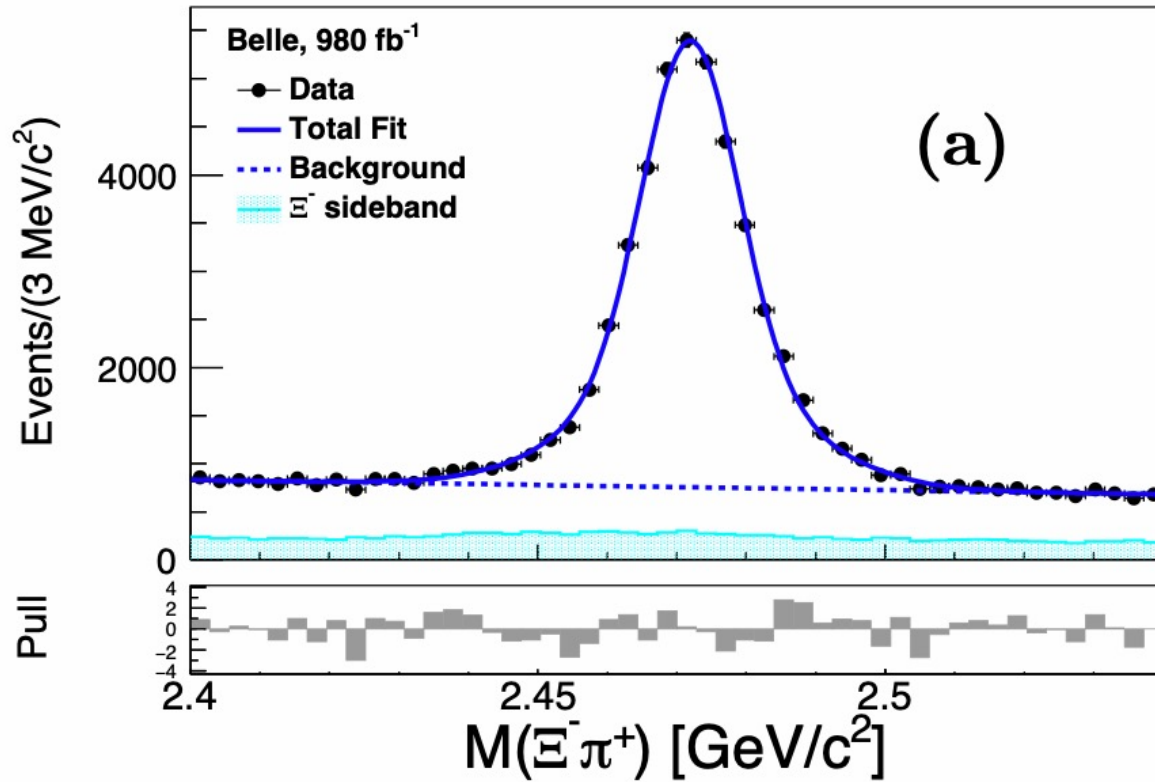
W -exchange for $\Xi_c^0 \rightarrow \Xi^0 h^0$



- [5] Z. Phys. C 55 (1992) 659 [6] PRD 57 (1998) 6532 [7] PRD 46 (1992) 053004 [8] PRD 48 (1993) 4188 [9] PRD 50 (1994) 5787
 [10] PRD 101 (2020) 014011 [11] EPJC 7 (1999) 217 [12] PRD 97 (2018) 073006 [13] PLB 794 (2019) 19 [14] JHEP 02 (2020) 165
 [15] JHEP 03 (2022) 143 [16] JHEP 09 (2022) 35 [17] JHEP 02 (2023) 235 [18] PRD 108 (2023) 053004

Reference mode of $\Xi_c^0 \rightarrow \Xi^- \pi^+$

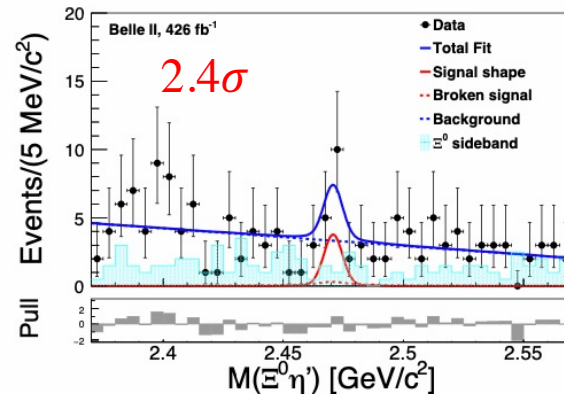
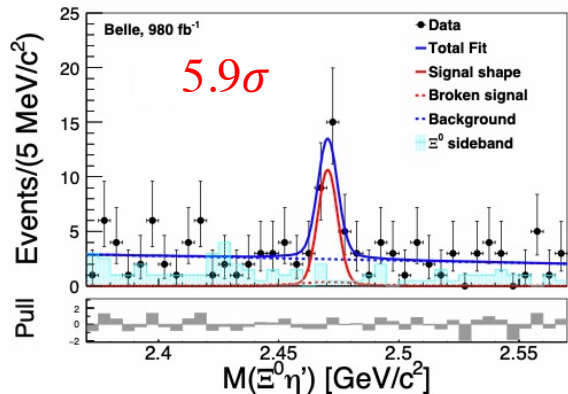
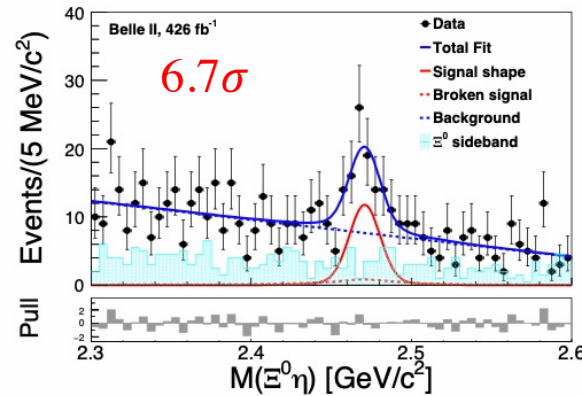
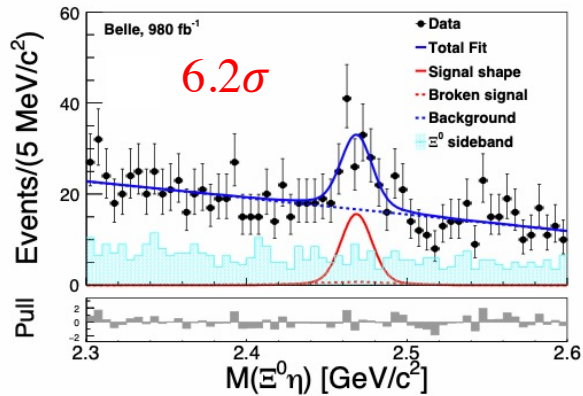
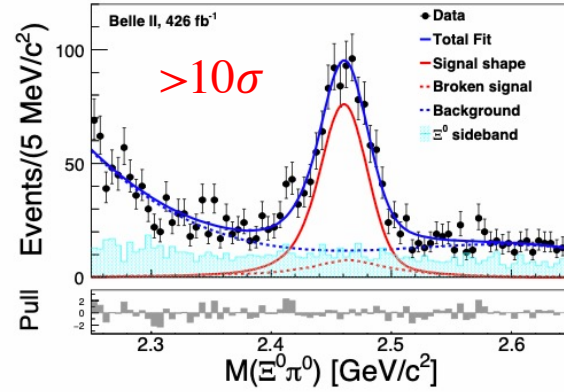
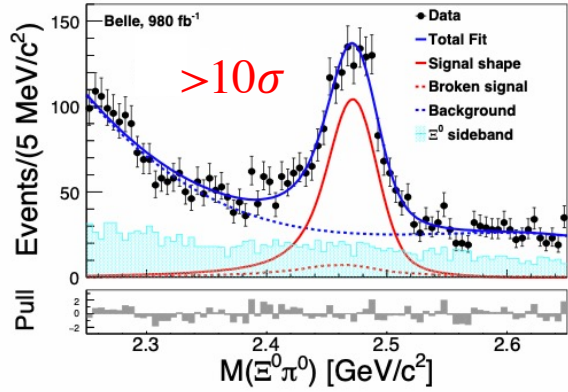
First BELLE + Belle II combined charm measurement.



Datasets	Signal yield
Belle	36340 ± 348
Belle II	13719 ± 184

Branching fractions for $\Xi_c^0 \rightarrow \Xi^0 h^0$ ($h^0 = \pi^0, \eta, \eta'$)

Preliminary results, will be submitted to JHEP



Signal yield:

Channel	Belle	Belle II
$\Xi_c^0 \rightarrow \Xi^0 \pi^0$	1315 ± 66	869 ± 46
$\Xi_c^0 \rightarrow \Xi^0 \eta$	81 ± 15	60 ± 11
$\Xi_c^0 \rightarrow \Xi^0 \eta'$	23 ± 6	8 ± 4

First measurement of the following BRs:

$$\mathcal{B}(\Xi_c^0 \rightarrow \Xi^0 \pi^0) = (6.9 \pm 0.3(\text{stat.}) \pm 0.5(\text{syst.}) \pm 1.5(\text{norm.})) \times 10^{-3}$$

$$\mathcal{B}(\Xi_c^0 \rightarrow \Xi^0 \eta) = (1.6 \pm 0.2(\text{stat.}) \pm 0.2(\text{syst.}) \pm 0.4(\text{norm.})) \times 10^{-3}$$

$$\mathcal{B}(\Xi_c^0 \rightarrow \Xi^0 \eta') = (1.2 \pm 0.3(\text{stat.}) \pm 0.1(\text{syst.}) \pm 0.3(\text{norm.})) \times 10^{-3}$$

They are compatible with theoretical prediction based on $SU(3)_F$ -breaking [JHEP 02, 235 (2023)].

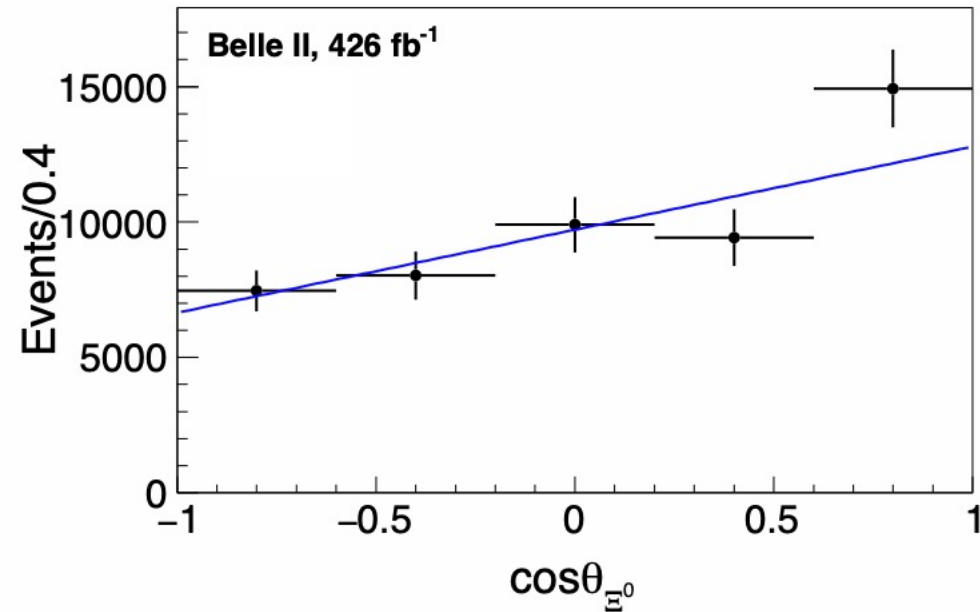
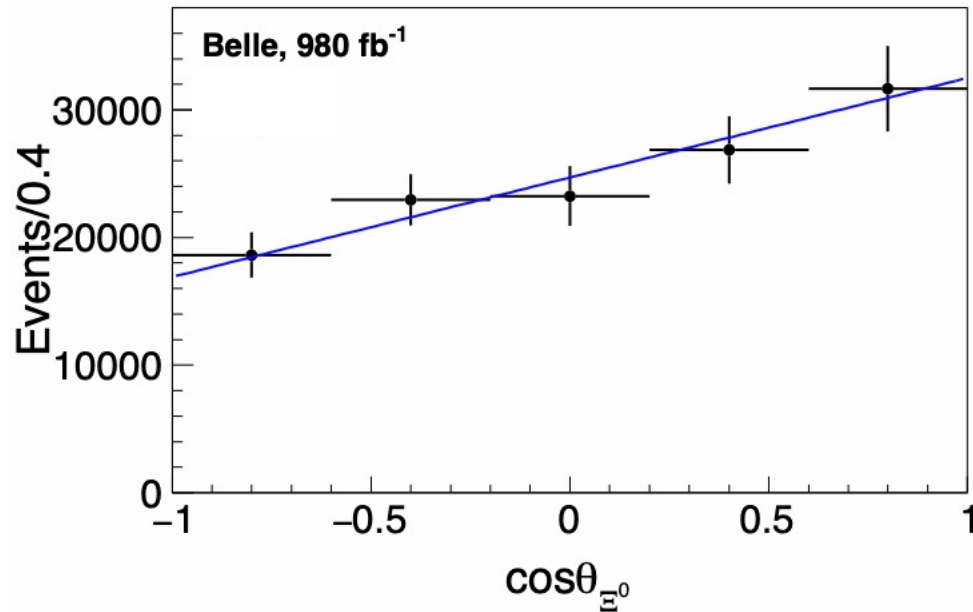
Asymmetry parameter for $\Xi_c^0 \rightarrow \Xi^0 \pi^0$

The asymmetry parameter, related to P-violation, is measured through **the differential decay rate**:

$$\frac{dN}{d \cos \theta_{\Xi^0}} \propto 1 + \alpha(\Xi_c^0 \rightarrow \Xi^0 h^0) \alpha(\Xi^0 \rightarrow \Lambda \pi^0) \cos \theta_{\Xi^0}$$

Preliminary results

The $\cos \theta_{\Xi^0}$ is the angle between the Λ momentum vector and the opposite of the Ξ_c^0 momentum vector in the Ξ^0 rest frame.



The $\alpha(\Xi_c^0 \rightarrow \Xi^0 \pi^0) = -0.90 \pm 0.15 \pm 0.23$, which is consistent with predictions based on the pole model [PRD 48 (1993) 4188, PRD 101 (2020) 014011], CA [EPJC 7 (1999) 217], and SU(3)_F flavor symmetry [PLB 794 (2019) 19] approaches.

Search for the semileptonic decays of $\Xi_c^0 \rightarrow \Xi^0 \ell^+ \ell^-$

Motivation

- Few baryonic neutrino-less semileptonic decays were observed experimentally [1-4].
- Only upper limits were set for $\Lambda_c^+ \rightarrow p \ell^+ \ell^-$ decay for the charmed baryons [5, 6].
- With the SU(3) flavor symmetry, $\mathcal{B}(\Xi_c^0 \rightarrow \Xi^0 e^+ e^-) \leq 2.35 \times 10^{-6}$ and $\mathcal{B}(\Xi_c^0 \rightarrow \Xi^0 \mu^+ \mu^-) \leq 2.25 \times 10^{-6}$ [PRD 103, 013007 (2021)].
- It will help the understanding of the recent anomalies in $b \rightarrow s \ell^+ \ell^-$ processes, i.e. $B \rightarrow K^{(*)} \ell^+ \ell^-$.

decays	Experimental results on \mathcal{B}_f	Ref.
$\Xi^0 \rightarrow \Lambda e^+ e^-$	$(7.6 \pm 0.4 \pm 0.4 \pm 0.2) \times 10^{-6}$	[1] PLB 650, 1 (2007)
$\Sigma^+ \rightarrow p \mu^+ \mu^-$	$(8.6_{-5.4}^{+6.6} \pm 5.5) \times 10^{-8}$	[2] PRL 94, 021801 (2005)
$\Lambda_b^0 \rightarrow \Lambda \mu^+ \mu^-$	$(1.73 \pm 0.42 \pm 0.55) \times 10^{-6}$	[3] PRL 107, 201802 (2011)
$\Lambda_b^0 \rightarrow \Lambda \mu^+ \mu^-$	$(0.96 \pm 0.16 \pm 0.13 \pm 0.21) \times 10^{-6}$	[4] JHEP 06, 115 (2015)
$\Lambda_c^+ \rightarrow p e^+ e^-$	$< 5.5 \times 10^{-6}$ @ 90% C. L.	[5] PRD 84, 072006 (2011)
$\Lambda_c^+ \rightarrow p \mu^+ \mu^-$	$< 44 \times 10^{-6}$ @ 90% C. L.	[5] PRD 84, 072006 (2011)
$\Lambda_c^+ \rightarrow p \mu^+ \mu^-$	$< 7.7 \times 10^{-8}$ @ 90% C. L.	[6] PRD 97, 091101(2018)

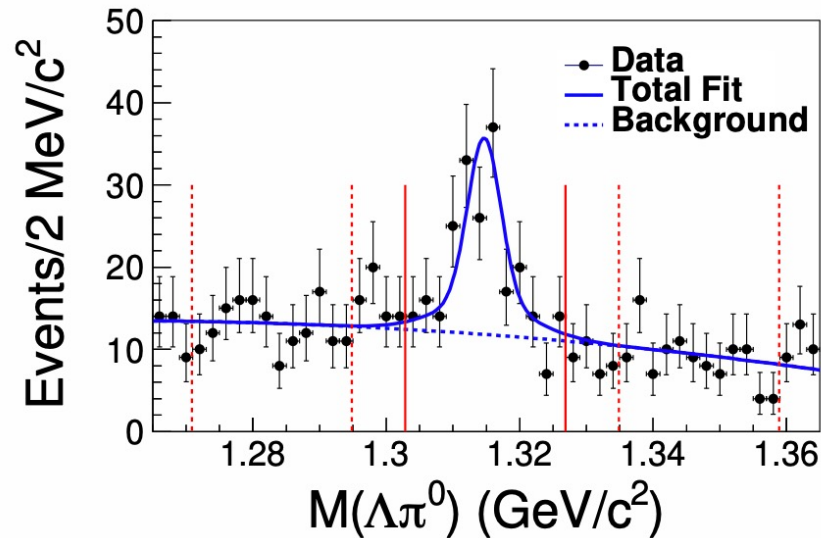
Search for the semileptonic decays of $\Xi_c^0 \rightarrow \Xi^0 \ell^+ \ell^-$

Results:

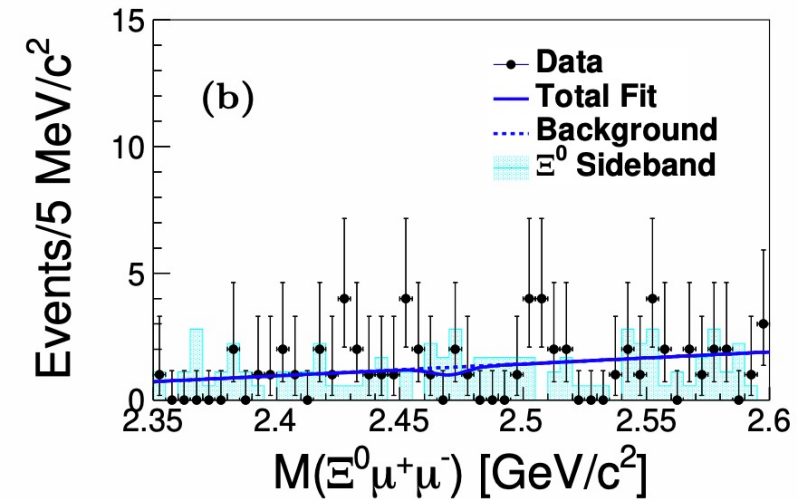
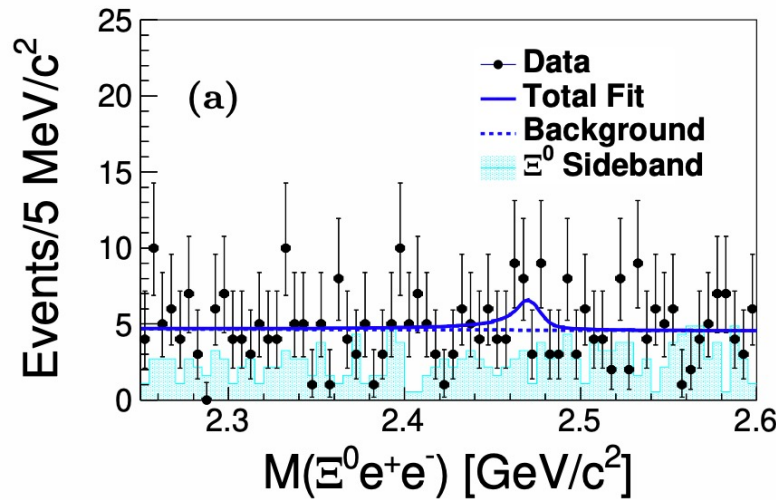
[PRD 109, 052003 (2024)]

*Full Belle
dataset*

Ξ^0 reconstruction



$\Xi^0 \ell^+ \ell^-$ invariant-mass spectra

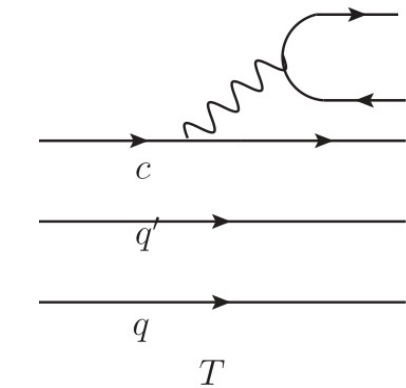


- No significant signals are observed in the $\Xi^0 \ell^+ \ell^-$ invariant-mass spectra.
- 90% credibility upper limits on branching fractions are set:
 - $B(\Xi_c^0 \rightarrow \Xi^0 \ell^+ \ell^-) / B(\Xi_c^0 \rightarrow \Xi^- \pi^+) < 6.7 (4.3) \times 10^{-3}$ and
 - $B(\Xi_c^0 \rightarrow \Xi^0 \ell^+ \ell^-) < 9.9 (6.5) \times 10^{-5}$ for electron (muon) mode.

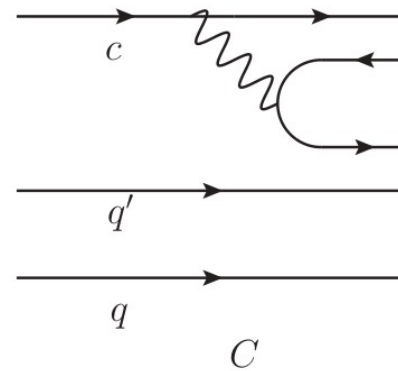
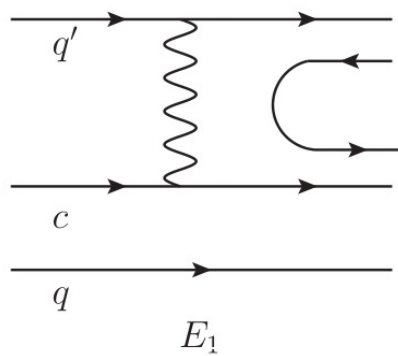
Measurements of $\Lambda_c^+ \rightarrow \Sigma^+ \pi^0, \Sigma^+ \eta,$ and $\Sigma^+ \eta'$

■ Motivation

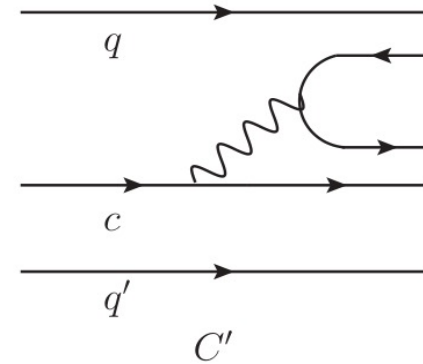
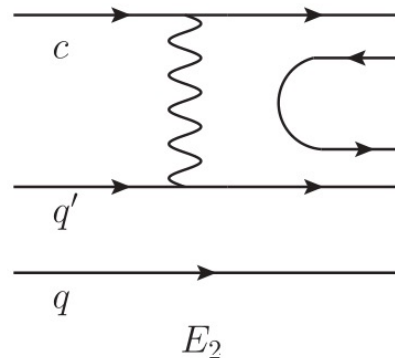
- For the charmed baryon weak decays: $\mathbf{B}_c \rightarrow \mathbf{B} + \mathbf{M}$, there are six topological diagrams. Among them, **T** and **C** are factorizable, while **C'** and **E₁₋₃** are nonfactorizable.
- All the nonfactorizable diagrams contribute to $\Lambda_c^+ \rightarrow \Sigma^+ \eta(\eta')$.



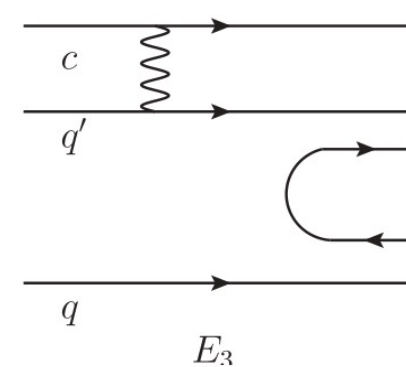
external W-emission T



internal W-emission C



inner W-emission C'



W-exchange diagrams E₁, E₂, E₃

Measurements of $\Lambda_c^+ \rightarrow \Sigma^+ \pi^0, \Sigma^+ \eta,$ and $\Sigma^+ \eta'$

■ Motivation

- **Theoretical predictions** on the branching fractions and asymmetry parameters of $\Lambda_c^+ \rightarrow \Sigma^+ \eta(\eta')$ vary across.
- Branching fractions of $\Lambda_c^+ \rightarrow \Sigma^+ \eta(\eta')$ are measured with large uncertainty ($\delta B/B > 40\%$). Decay **asymmetry parameters** for these two modes **have never been measured**.

Decay	Körner [1]	Ivanov [2]	Żenczykowski [7]	Sharma [8]	Zou [10]	Geng [11]	Experiment [18]	
$\Lambda_c^+ \rightarrow \Sigma^+ \eta$	0.16	0.11	0.90	0.57	0.74	0.32 ± 0.13	0.44 ± 0.20	$\times 10^{-2}$
$\Lambda_c^+ \rightarrow \Sigma^+ \eta'$	1.28	0.12	0.11	0.10	–	1.44 ± 0.56	1.5 ± 0.6	
$\Lambda_c^+ \rightarrow \Sigma^+ \pi^0$	0.70	0.43	0.39	–0.31	–0.76	-0.35 ± 0.27	-0.55 ± 0.11	
$\Lambda_c^+ \rightarrow \Sigma^+ \eta$	0.33	0.55	0.00	–0.91	–0.95	-0.40 ± 0.47	–	
$\Lambda_c^+ \rightarrow \Sigma^+ \eta'$	–0.45	–0.05	–0.91	0.78	0.68	$1.00^{+0.00}_{-0.17}$	–	

Branching fractions

Asymmetry parameters

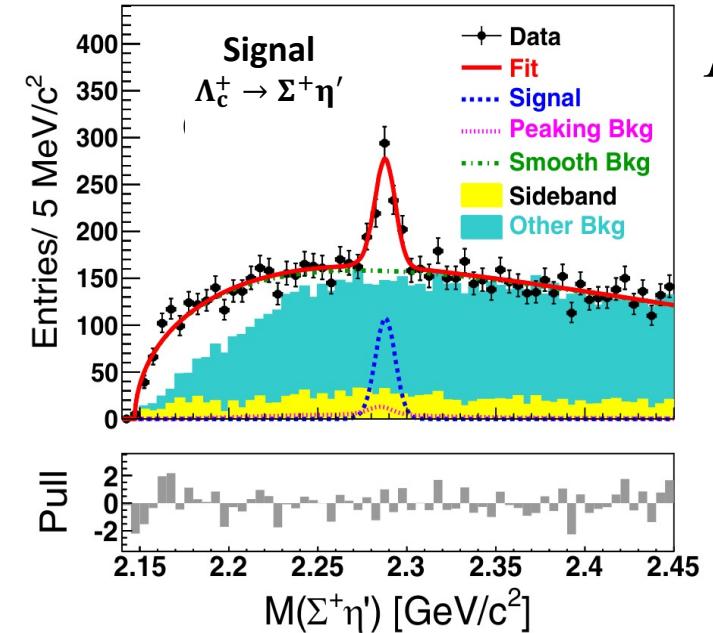
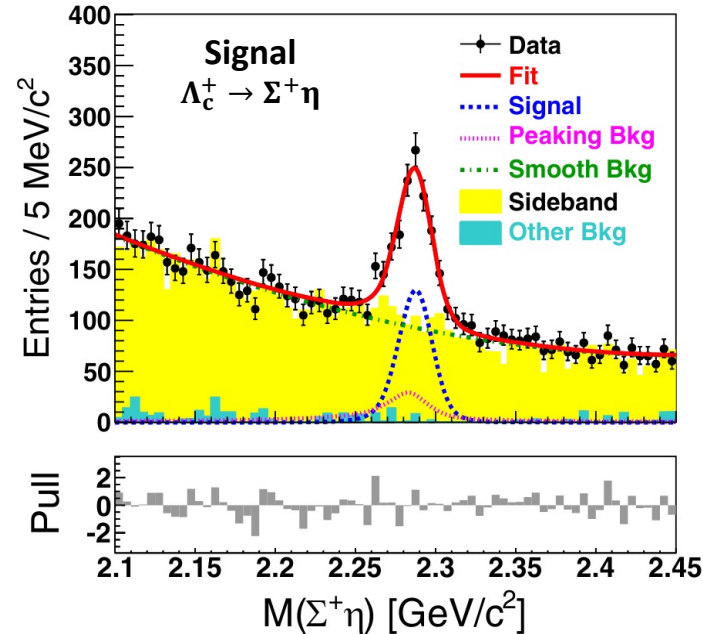
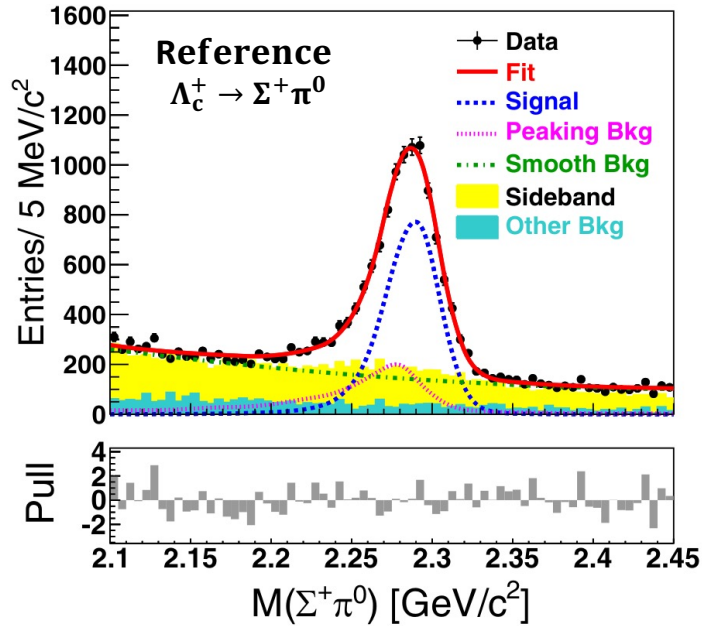
[1] Z. Phys. C 55, 659 (1992) [2] PRD 57, 5632 (1998) [7] PRD 50, 5787 (1994) [8] EPJC 7, 217 (1999) [10] PRD 49, 3417 (1994) [11] PLB 794, 19 (2019) [18] PTEP 2022, 083C01 (2022)

Measurements of $\Lambda_c^+ \rightarrow \Sigma^+ \pi^0$, $\Sigma^+ \eta$, and $\Sigma^+ \eta'$

Measurements of branching fractions of $\Lambda_c^+ \rightarrow \Sigma^+ \eta$ and $\Lambda_c^+ \rightarrow \Sigma^+ \eta'$

[PRD 107, 032003 (2023)]

($\Sigma^+ \rightarrow p\pi^0$; $\eta' \rightarrow \eta\pi\pi$; $\eta \rightarrow \gamma\gamma$)



Full Belle dataset

$$\frac{B(\Lambda_c^+ \rightarrow \Sigma^+ \eta)}{B(\Lambda_c^+ \rightarrow \Sigma^+ \pi^0)} = 0.25 \pm 0.03 \pm 0.01;$$

$$B(\Lambda_c^+ \rightarrow \Sigma^+ \eta) = (3.14 \pm 0.35 \pm 0.11 \pm 0.25) \times 10^{-3}$$

$$\frac{B(\Lambda_c^+ \rightarrow \Sigma^+ \eta')}{B(\Lambda_c^+ \rightarrow \Sigma^+ \pi^0)} = 0.33 \pm 0.06 \pm 0.02;$$

$$B(\Lambda_c^+ \rightarrow \Sigma^+ \eta') = (4.16 \pm 0.75 \pm 0.21 \pm 0.33) \times 10^{-3}$$

PDG: $B(\Lambda_c^+ \rightarrow \Sigma^+ \eta) = (4.4 \pm 2.0) \times 10^{-3}$

PDG: $B(\Lambda_c^+ \rightarrow \Sigma^+ \eta') = (15 \pm 6) \times 10^{-3}$

statistical systematical from $B(\Lambda_c^+ \rightarrow \Sigma^+ \pi^0)$

Consistent with PDG. Most precise result to date.

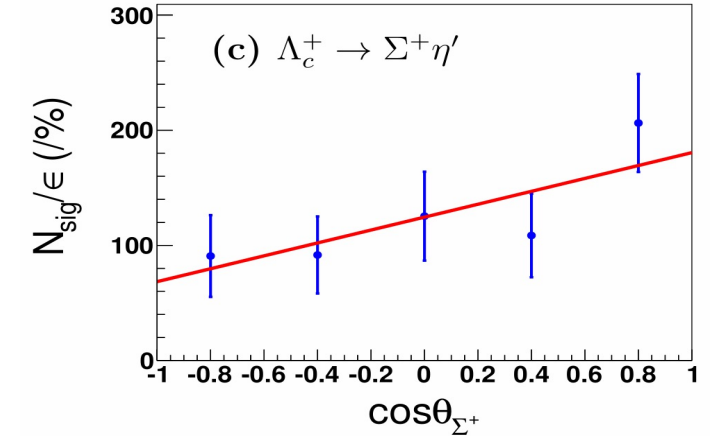
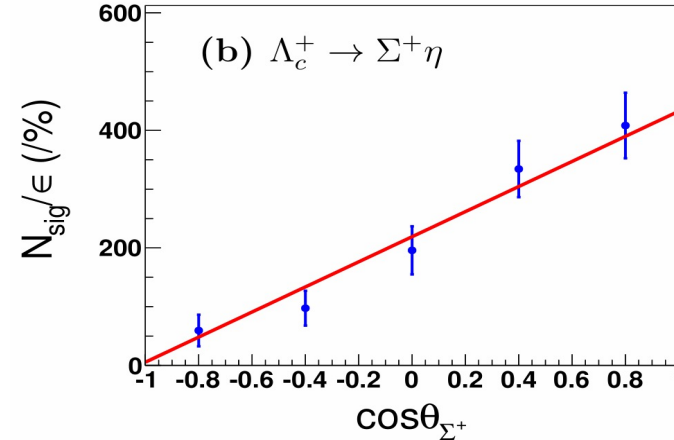
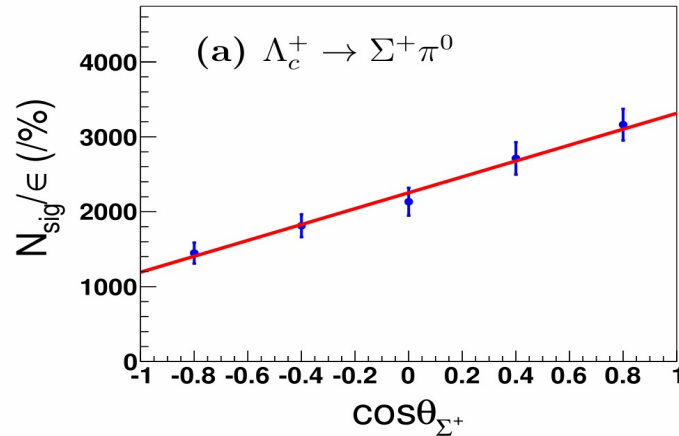
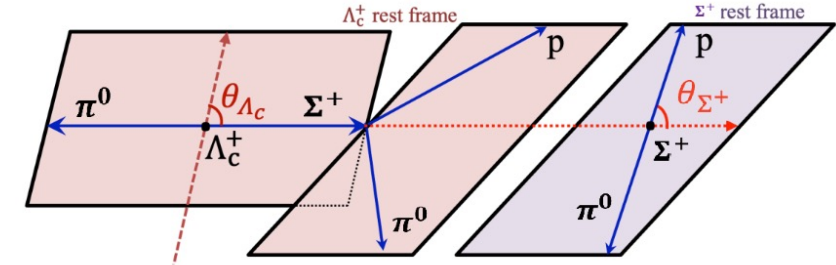
Measurements of $\Lambda_c^+ \rightarrow \Sigma^+ \pi^0, \Sigma^+ \eta,$ and $\Sigma^+ \eta'$

■ Measurements of asymmetry parameters of $\Lambda_c^+ \rightarrow \Sigma^+ \pi^0, \Sigma^+ \eta,$ and $\Sigma^+ \eta'$ [PRD 107, 032003 (2023)]

The differential decay rate depends on the asymmetry parameter $\alpha_{\Sigma^+ X}$ as:

$$\frac{dN}{d\cos\theta_{\Sigma^+}} \propto 1 + \alpha_{\Sigma^+ X} \alpha_{p\pi^0} \cos\theta_{\Sigma^+}$$

$\alpha_{p\pi^0} = -0.982 \pm 0.014$ from world average value.



- $\alpha_{\Sigma^+ \pi^0} = -0.48 \pm 0.02 \pm 0.02$

- agrees with the world average value: -0.55 ± 0.11 .

- with much improved precision

- The consistency with $\alpha_{\Sigma^0 \pi^+} = -0.463 \pm 0.016 \pm 0.008$ [Sci.Bull. 68 (2023) 583] indicates no isospin symmetry broken.

- $\alpha_{\Sigma^+ \eta} = -0.99 \pm 0.03 \pm 0.05$ and $\alpha_{\Sigma^+ \eta'} = -0.46 \pm 0.06 \pm 0.03$

- measured for the first time

Branching fractions of $\Lambda_c^+ \rightarrow pK_S^0 K_S^0, pK_S^0 \eta$

■ Motivation

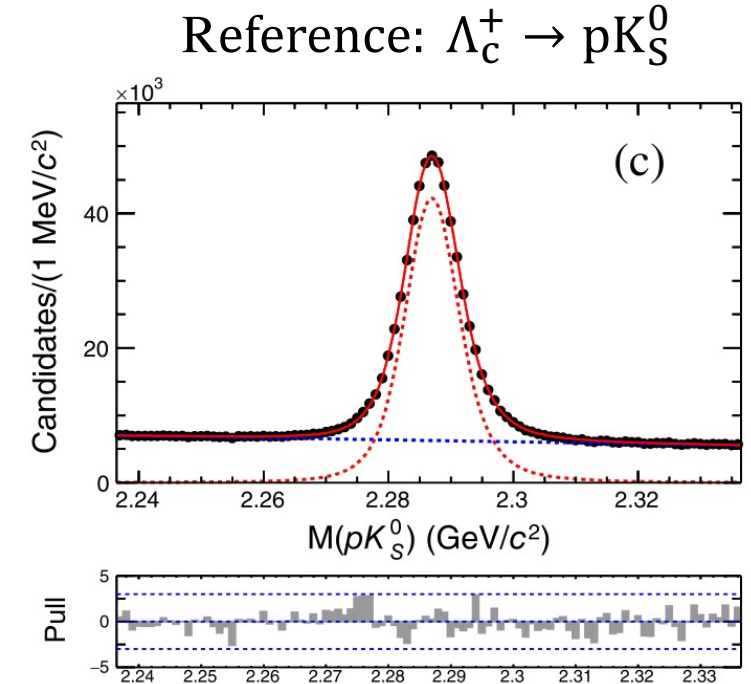
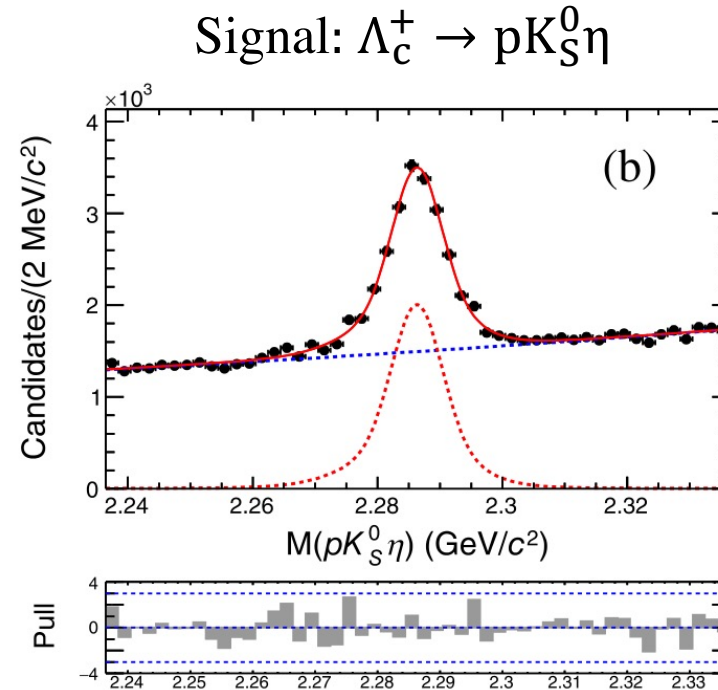
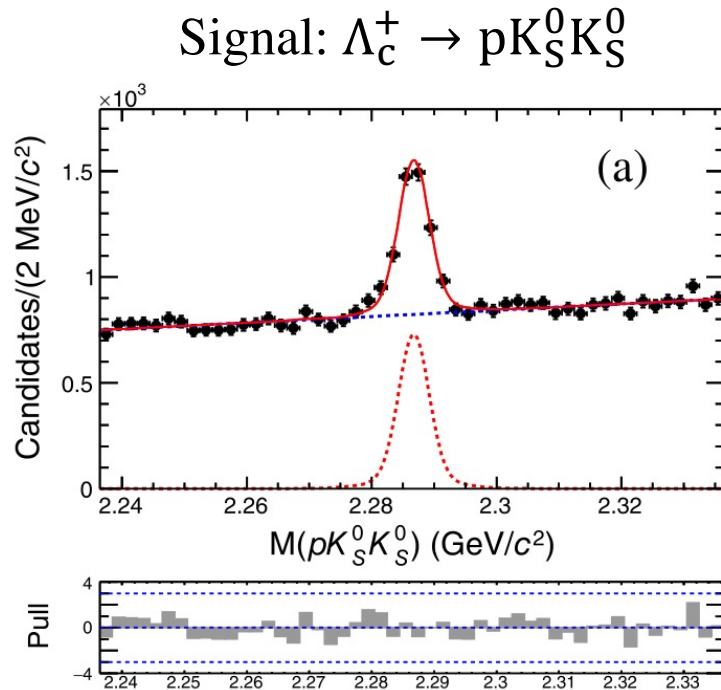
- No result of branching fraction for $\Lambda_c^+ \rightarrow pK_S^0 K_S^0$ (singly Cabibbo-suppressed) is reported. According to theoretical results based on $SU(3)_F$ symmetry [EPJC 79 (2019) 946], $\mathcal{B}(\Lambda_c^+ \rightarrow pK_S^0 K_S^0) = (1.9 \pm 0.4) \times 10^{-3}$.
- Measured branching fraction $\mathcal{B}(\Lambda_c^+ \rightarrow pK_S^0 \eta) = (4.15 \pm 0.90) \times 10^{-3}$ has large uncertainty ($\delta B/B \sim 20\%$) [PDG].
- Check Dalitz-plot for the intermediate resonances existence, e.g. $N^*(1535) \rightarrow p\eta$.

Branching fractions of $\Lambda_c^+ \rightarrow pK_S^0K_S^0, pK_S^0\eta$

■ Signal Yield Extraction

[PRD 107, 032004 (2023)]

*Full Belle
dataset*

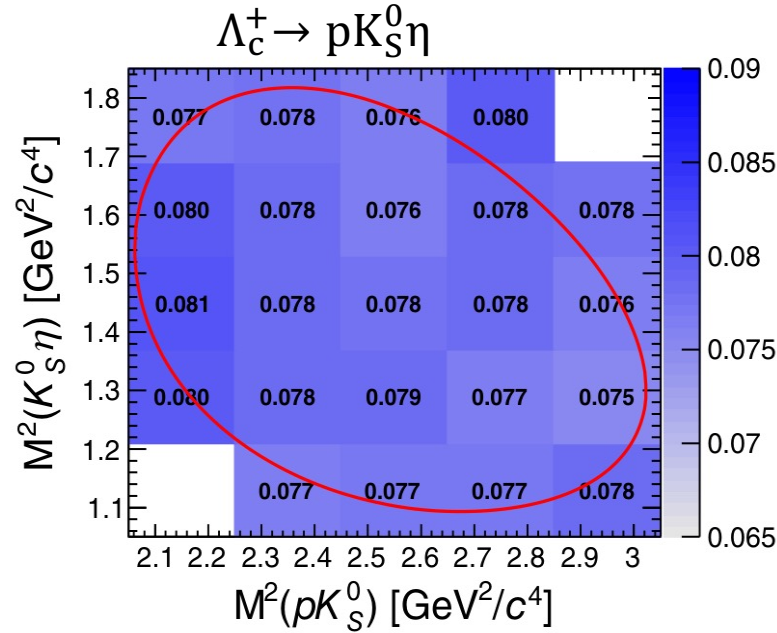
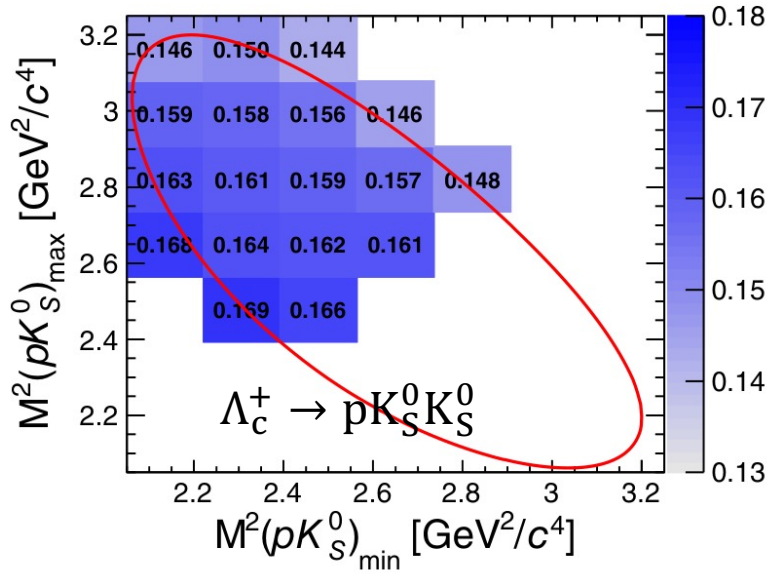


Yields	$\Lambda_c^+ \rightarrow pK_S^0K_S^0$	$\Lambda_c^+ \rightarrow pK_S^0\eta$	$\Lambda_c^+ \rightarrow pK_S^0$
$N_{\text{sig}}^{\text{FR}}$	2442 ± 103	12877 ± 317	515296 ± 1129

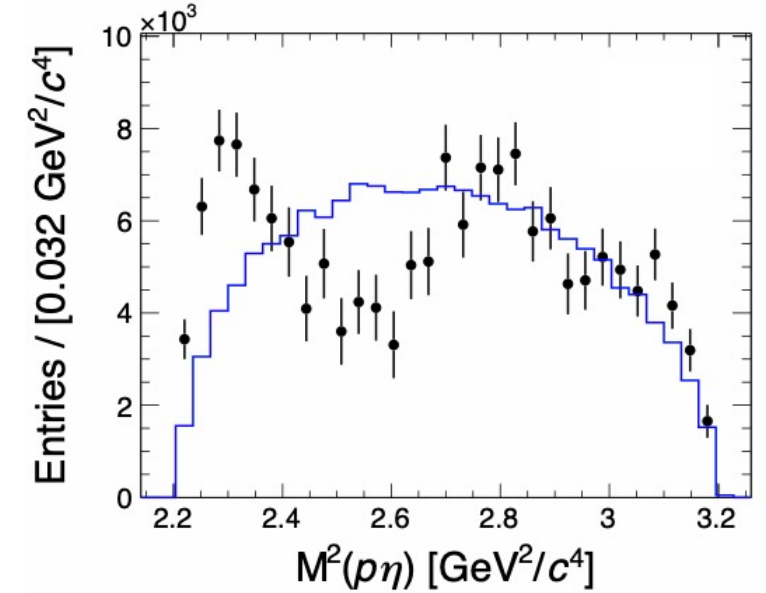
Branching fractions of $\Lambda_c^+ \rightarrow pK_S^0 K_S^0, pK_S^0 \eta$

[PRD 107, 032004 (2023)]

Efficiency Plane



$N^*(1535)$ is observed in $M(p\eta)$.



Branching fraction

● $\frac{B(\Lambda_c^+ \rightarrow pK_S^0 K_S^0)}{B(\Lambda_c^+ \rightarrow pK_S^0)} = (1.48 \pm 0.08 \pm 0.04) \times 10^{-2} \quad \rightarrow \quad B(\Lambda_c^+ \rightarrow pK_S^0 K_S^0) = (2.35 \pm 0.12 \pm 0.07 \pm 0.12) \times 10^{-4}$

➤ First observation

● $\frac{B(\Lambda_c^+ \rightarrow pK_S^0 \eta)}{B(\Lambda_c^+ \rightarrow pK_S^0)} = (2.73 \pm 0.06 \pm 0.13) \times 10^{-1} \quad \rightarrow \quad B(\Lambda_c^+ \rightarrow pK_S^0 \eta) = (4.35 \pm 0.10 \pm 0.20 \pm 0.22) \times 10^{-3}$

➤ Consistent with world average value $(4.15 \pm 0.90) \times 10^{-3}$ and **threefold improvement in precision.**

Mass and width of $\Lambda_c(2625)^+$ and BR of $\Lambda_c(2625)^+ \rightarrow \Sigma_c^{0,++} \pi$

■ Motivation

- $\Lambda_c(2625)^+$ ($J^P = 3/2^-$) is the excited state of Λ_c^+ . It dominantly decays to $\Lambda_c^+ \pi^+ \pi^-$ via P-wave decay. The D-wave decay $\Lambda_c(2625)^+ \rightarrow \Sigma_c^{0,++} \pi$ is also allowed, but its contribution is known to be small.
- The **mass** of the $\Lambda_c(2625)^+$, relative to the Λ_c^+ mass, is already relatively well known [PRD 84,012003 (2011)], but the large Belle data sample allows for a **more precise** measurement.
- No **intrinsic width** of the $\Lambda_c(2625)^+$ has yet been measured, and the current upper limit $\Gamma < 0.97 \text{ MeV}/c^2$ at 90% confidence level is based on the CDF measurement in 2011 [PRD 84,012003 (2011)].

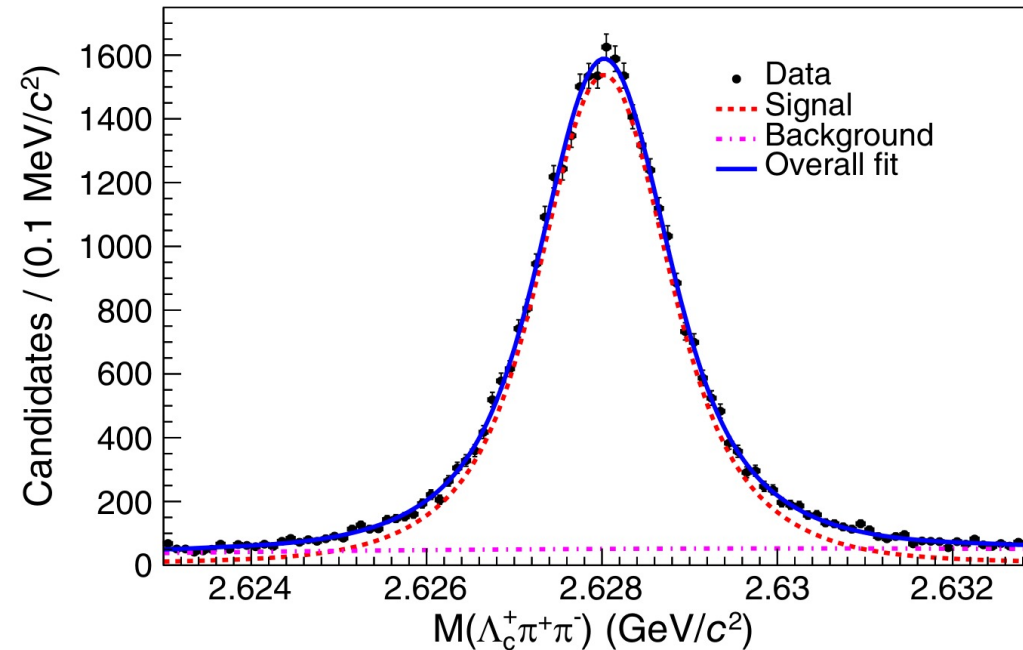
Mass and width of $\Lambda_c(2625)^+$ and BR of $\Lambda_c(2625)^+ \rightarrow \Sigma_c^{0,++} \pi$

■ Measurements of mass and width

[PRD 107, 032008 (2023)]

Reconstruction mode: $\Lambda_c(2625)^+ \rightarrow \Lambda_c^+ \pi^+ \pi^-$, $\Lambda_c^+ \rightarrow p K^- \pi^+$

*Full Belle
dataset*



□ $M[\Lambda_c(2625)^+] - M(\Lambda_c^+) = 341.518 \pm 0.006 \pm 0.049 \text{ MeV}/c^2$

- consistent with the world average value $341.65 \pm 0.13 \text{ MeV}/c^2$
- has approximately half the uncertainty

□ $\Gamma[\Lambda_c(2625)^+] < 0.52 \text{ MeV}$

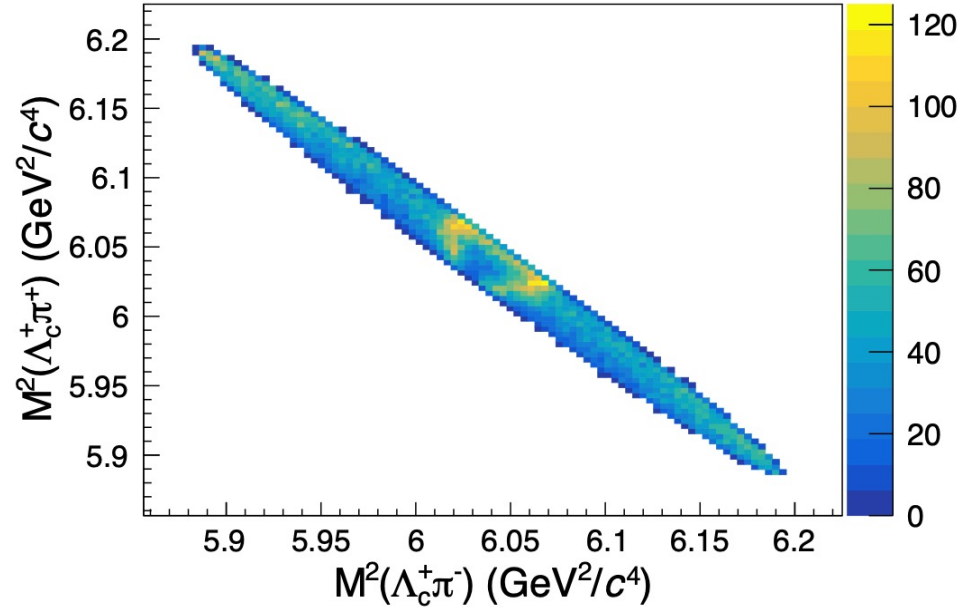
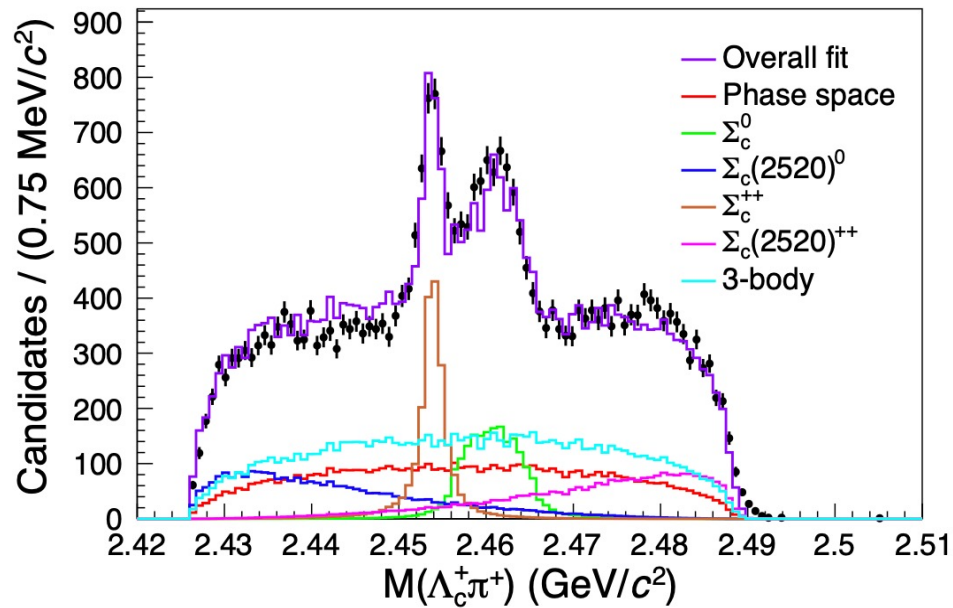
- a factor of 2 more stringent than the previous limit $\Gamma < 0.97 \text{ MeV}$
- An improved limit on the width of the $\Lambda_c(2625)^+$ will help to constrain various theoretical predictions.

Mass and width of $\Lambda_c(2625)^+$ and BR of $\Lambda_c(2625)^+ \rightarrow \Sigma_c^{0,++}\pi$

■ Measurements of branching fractions

[PRD 107, 032008 (2023)]

Full Dalitz plot fitted with AmpTools is performed [PRD 98, 114007 (2018)].



$$\frac{B(\Lambda_c(2625)^+ \rightarrow \Sigma_c^0 \pi)}{B(\Lambda_c(2625)^+ \rightarrow \Lambda_c^+ \pi^+ \pi^-)} = (5.19 \pm 0.23 \pm 0.40)\%$$

$$\frac{B(\Lambda_c(2625)^+ \rightarrow \Sigma_c^{++} \pi)}{B(\Lambda_c(2625)^+ \rightarrow \Lambda_c^+ \pi^+ \pi^-)} = (5.13 \pm 0.26 \pm 0.32)\%$$

□ The measured branching fraction ratios agree with PDG values and are the **most precise** to date.

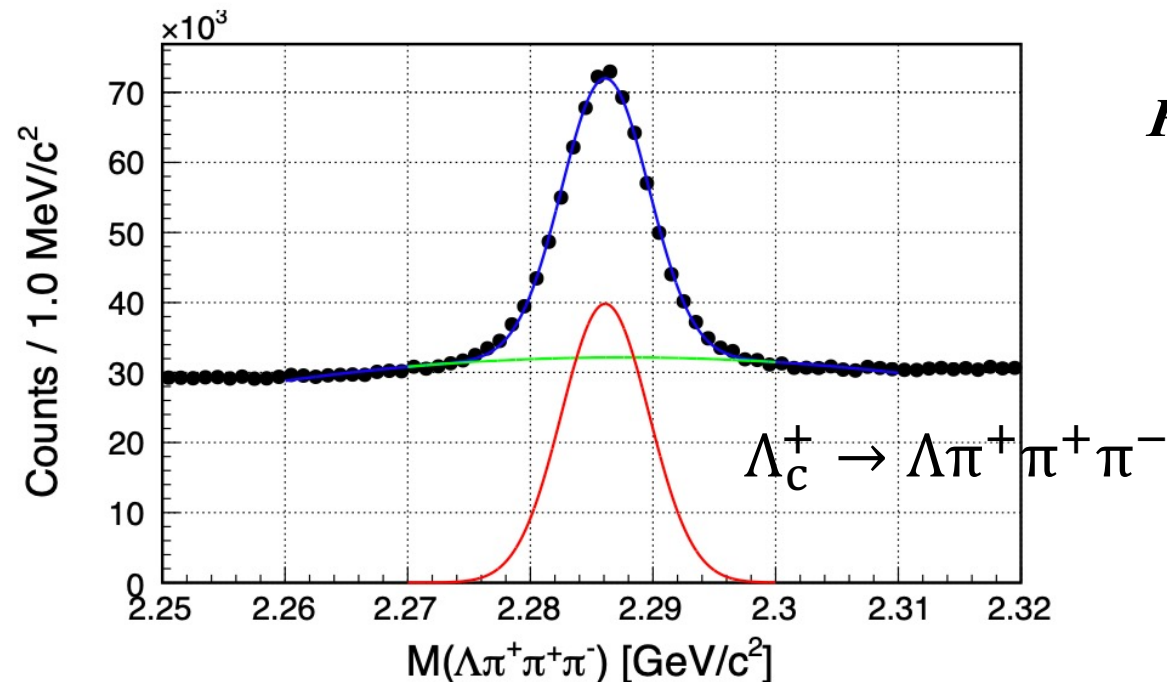
□ Our measurements **align with the prediction** that assuming $\Lambda_c(2625)^+$ is a λ mode excitation [PRD 98, 114007 (2018)]. 19

Peak at $\bar{K}N$ threshold in $\Lambda_c^+ \rightarrow \Lambda \pi^+ \pi^+ \pi^-$

[PRL 130, 151903 (2023)]

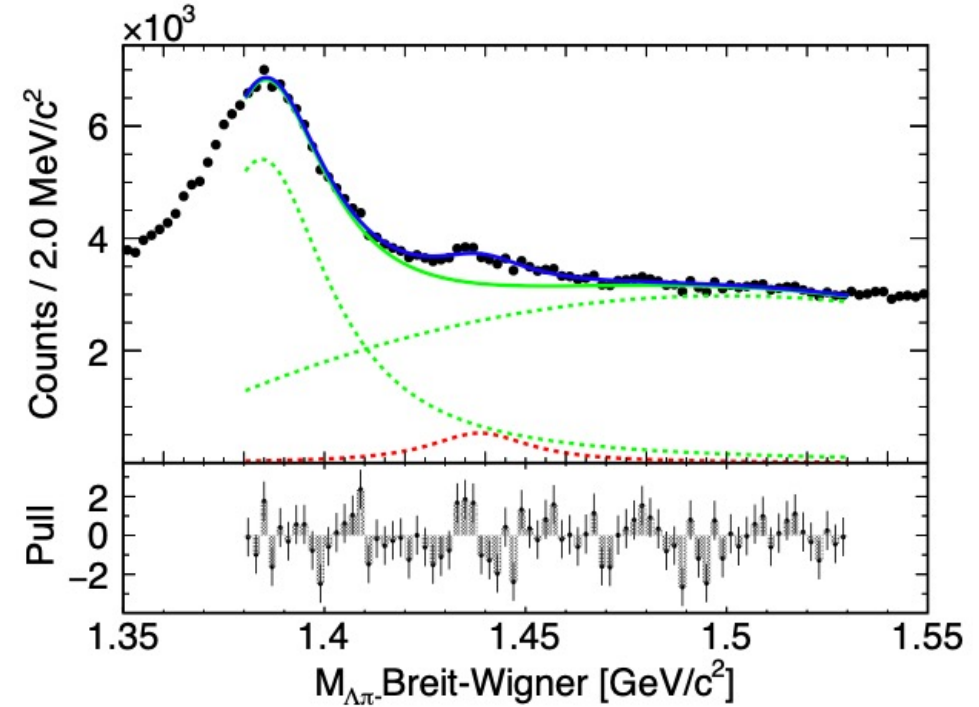
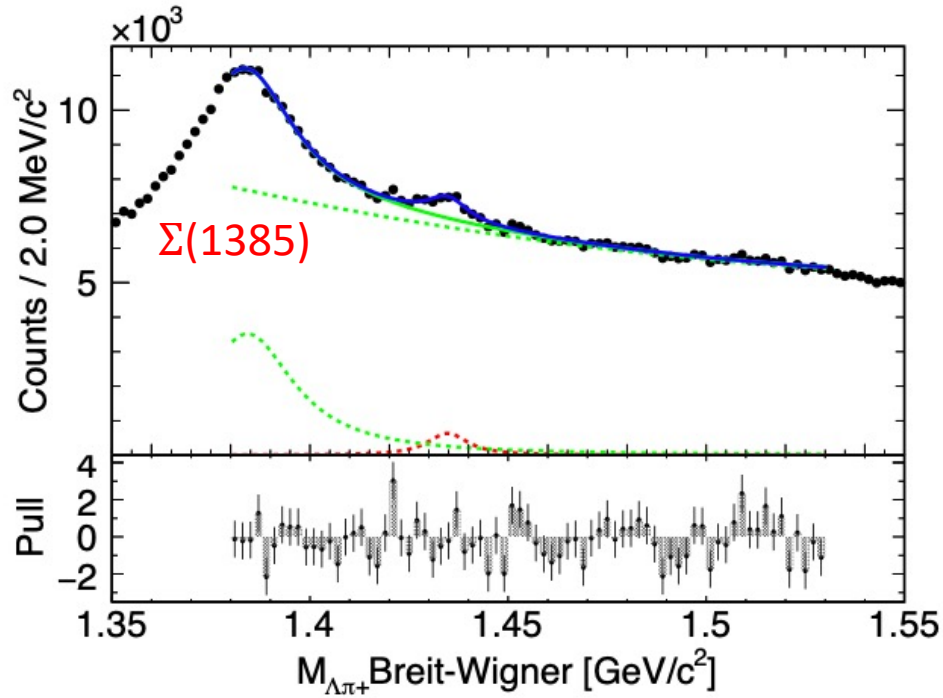
■ Motivation

- The $\Lambda(1405)$ ($I = 0$) state, which has been interpreted as an orbitally excited quark-diquark [PRC 49, 2831 (1994)], or as a $\bar{K}N$ bound state [PRL 114, 132002 (2015)].
- The $\bar{K}N$ ($I = 1$) interaction is a virtual state could exist [PLB 500, 263 (2001)] and could be observed as a **threshold cusp**.



Peak at $\bar{K}N$ threshold in $\Lambda_c^+ \rightarrow \Lambda \pi^+ \pi^+ \pi^-$

[PRL 130, 151903 (2023)]



Full Belle dataset

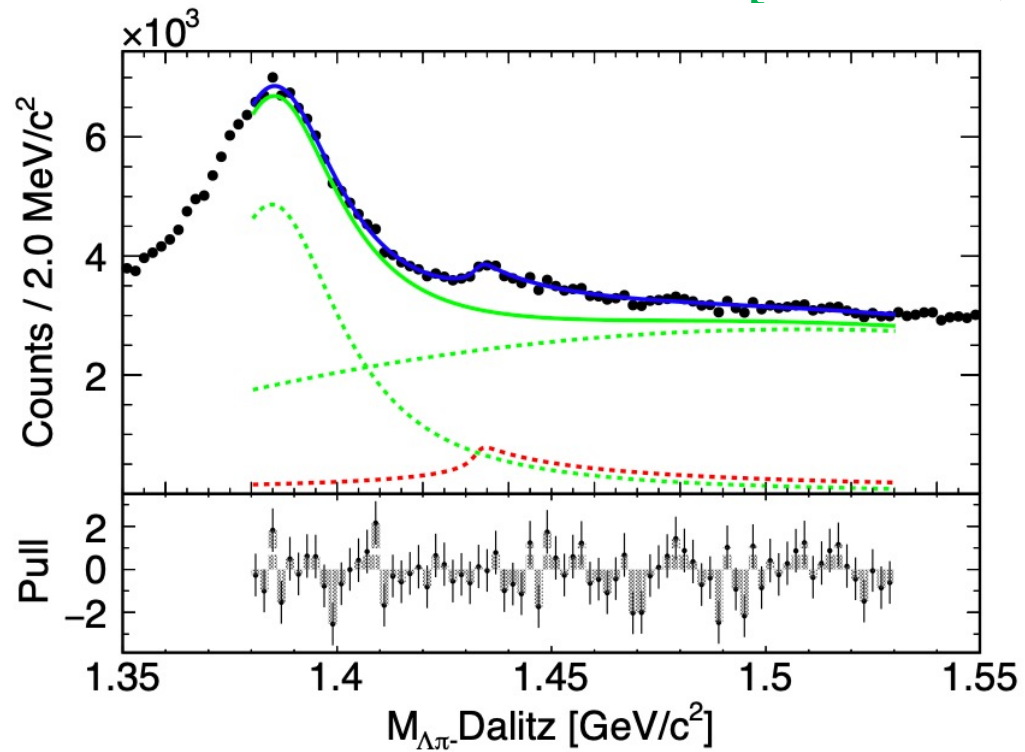
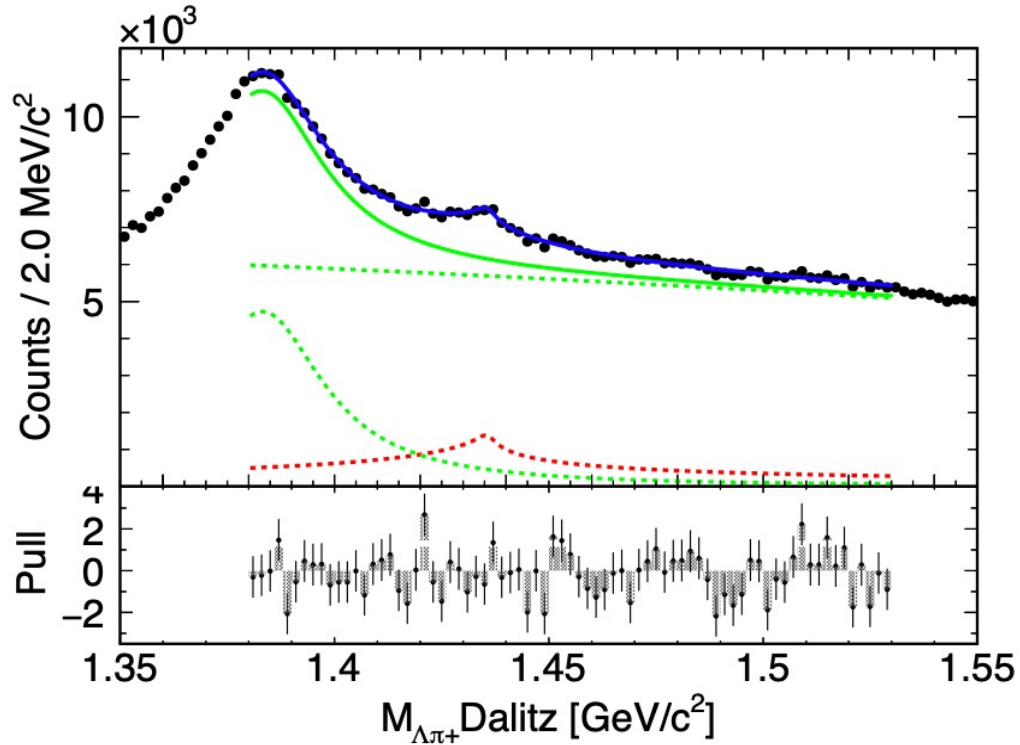
Standard Breit-Wigner

$$f_{\text{BW}} = \frac{\Gamma/2}{(E - E_{\text{BW}})^2 + \Gamma^2/4}$$

Mode	Mass (MeV/c ²)	Width (MeV)	χ^2/NDF
$\Lambda\pi^+$	1434.3±0.6±0.9	11.5±2.8±5.3	74/68
$\Lambda\pi^-$	1438.5±0.9±2.5	33.0±7.5±23.6	92/68

Peak at $\bar{K}N$ threshold in $\Lambda_c^+ \rightarrow \Lambda \pi^+ \pi^+ \pi^-$

[PRL 130, 151903 (2023)]



*Full Belle
dataset*

Dalitz model gives slightly better χ^2/NDF , but the difference is not significant.

Dalitz model (cusp) [Czech. J. Phys. B 32, 1021 (1982)]

For scattering length $A=a+ib$ and decay momentum k/κ .

$$f_D = \frac{4\pi b}{(1+kb)^2 + (ka)^2}, E > m_{\bar{K}N}$$

$$= \frac{4\pi b}{(1+\kappa a)^2 + (\kappa b)^2}, E < m_{\bar{K}N}$$

Mode	a [fm]	b [fm]	χ^2/NDF
$\Lambda\pi^+$	$0.48 \pm 0.32 \pm 0.38$	$1.22 \pm 0.83 \pm 2.54$	69/68
$\Lambda\pi^-$	$1.24 \pm 0.57 \pm 1.56$	$0.18 \pm 0.13 \pm 0.20$	78/68

Obtained center values for a are larger than most theories (e.g., $a(K^-n)=0.3\sim 0.6$ fm for [Nucl. Phys. A 881, 98 (2012)]), but with large uncertainties.

Evidence for $\Omega_c^0 \rightarrow \Xi^- \pi^+$ and search for $\Omega_c^0 \rightarrow \Xi^- K^+$ and $\Omega^- K^+$ decays

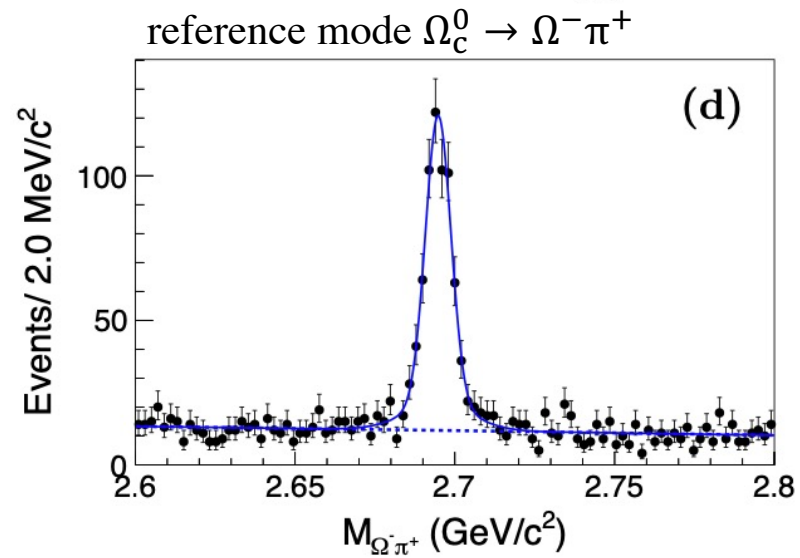
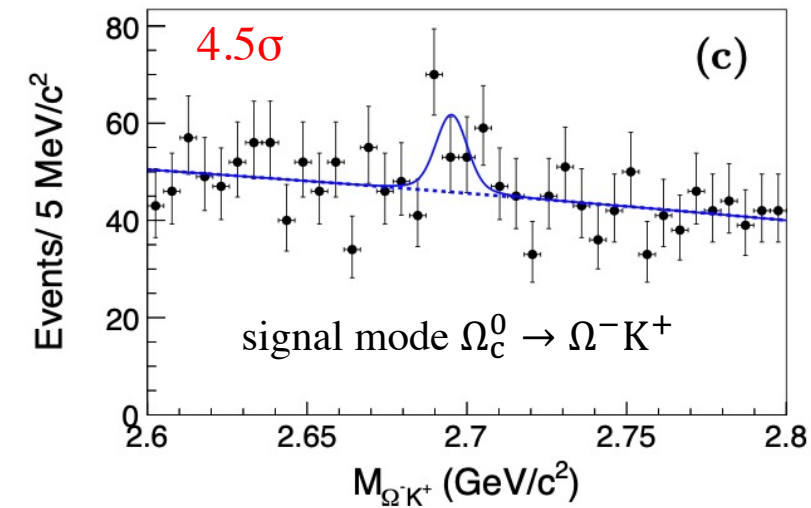
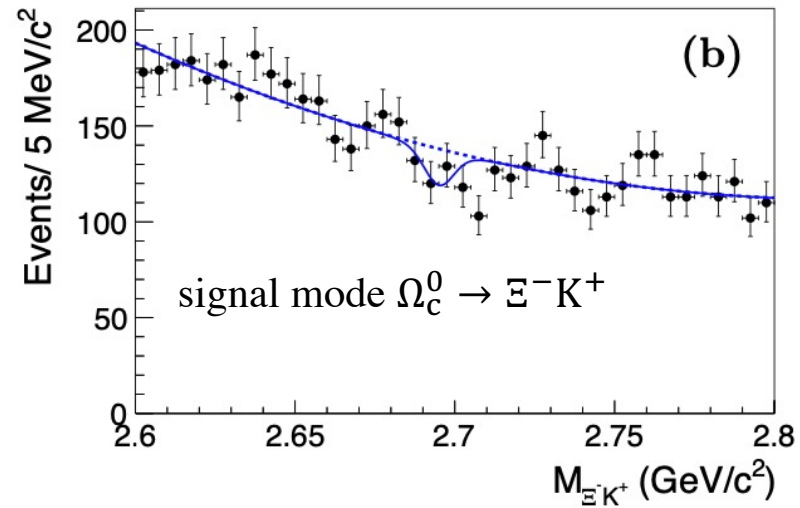
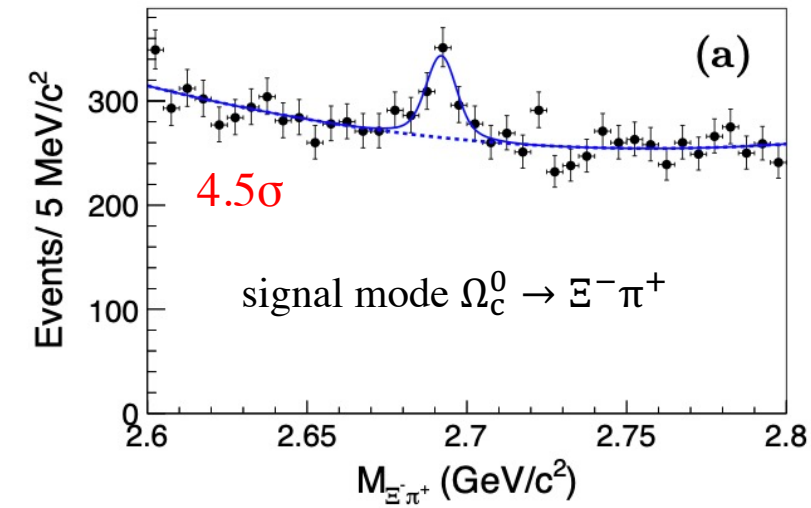
- The theoretical study of hadronic weak decays of the Ω_c^0 has a long history. But due to **the low production rate of Ω_c^0 and low detection efficiency** for long-lived final states, our knowledge of the Ω_c^0 state is very limited.
- The **singly Cabibbo-suppressed decay $\Omega_c^0 \rightarrow \Xi^- \pi^+$ and doubly Cabibbo-suppressed decay $\Omega_c^0 \rightarrow \Xi^- K^+$** decays have been studied systematically in various theoretical models.

Predicted ratios of branching fractions for using light-front quark model (LFQM), pole model, and current algebra (CA).

Branching fraction ratios	LFQM CPC 42, 093101 (2018)	Pole model and CA PRD 101, 094033 (2020)
$\mathcal{B}(\Omega_c^0 \rightarrow \Xi^- \pi^+)/\mathcal{B}(\Omega_c^0 \rightarrow \Omega^- \pi^+)$	1.96×10^{-3}	1.04×10^{-1}
$\mathcal{B}(\Omega_c^0 \rightarrow \Xi^- K^+)/\mathcal{B}(\Omega_c^0 \rightarrow \Omega^- \pi^+)$	1.74×10^{-4}	1.06×10^{-2}

The first evidence of $\Omega_c^0 \rightarrow \Xi^- \pi^+$ with a signal significance of 4.5σ including systematic uncertainties.

No significant signals are found in $\Omega_c^0 \rightarrow \Omega^- K^+$ and $\Omega_c^0 \rightarrow \Omega^- \pi^+$.



$$\mathcal{B}(\Omega_c^0 \rightarrow \Xi^- \pi^+) / \mathcal{B}(\Omega_c^0 \rightarrow \Omega^- \pi^+) = 0.253 \pm 0.053(\text{stat.}) \pm 0.030(\text{syst.})$$

$$\mathcal{B}(\Omega_c^0 \rightarrow \Xi^- K^+) / \mathcal{B}(\Omega_c^0 \rightarrow \Omega^- \pi^+) < 0.070$$

$$\mathcal{B}(\Omega_c^0 \rightarrow \Omega^- K^+) / \mathcal{B}(\Omega_c^0 \rightarrow \Omega^- \pi^+) < 0.29$$

Summary

- At Belle, we are still producing excited results for Λ_c , Ξ_c , and Ω_c charmed baryons.
- We are combining Belle and Belle II data to study charmed baryon decays.
- These experimental results will be useful to future constrain the parameter space of the theoretical models [quark model, chiral symmetry...] and can be applied to other heavy quark systems.
- In the future, Belle II will provide greater sensitivity and precise measurements in charmed baryon physics with 50 ab^{-1} .

Thanks for your attentions!