



# Neutrino Mass Measurement with Cosmic Gravitational Focusing

Shao-Feng Ge

葛韶锋

gesf@sjtu.edu.cn



Pedro Pasquini



Tan Liang

SFG, Pedro Pasquini, Liang Tan, **JCAP 05 (2024) 108** [arXiv:2312.16972]



上海交通大学

SHANGHAI JIAO TONG UNIVERSITY

青岛高能大会  
August 15, 2024

李政道研究所  
Tsung-Dao Lee Institute

## 1) Overview of $\nu$ Mass

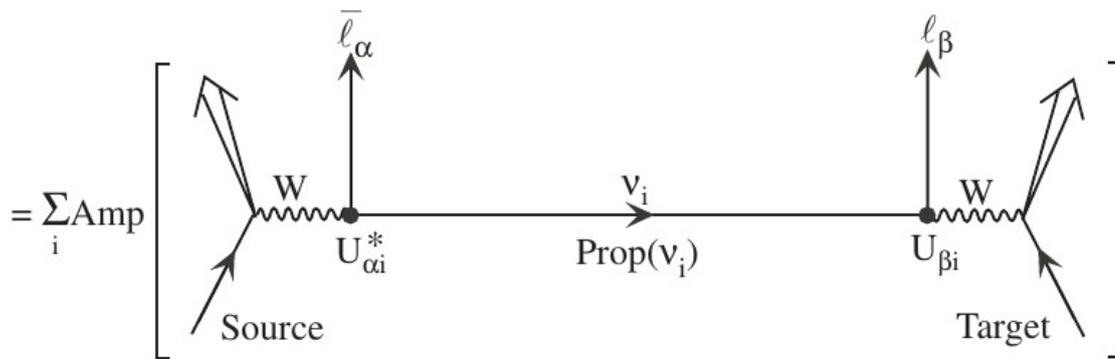
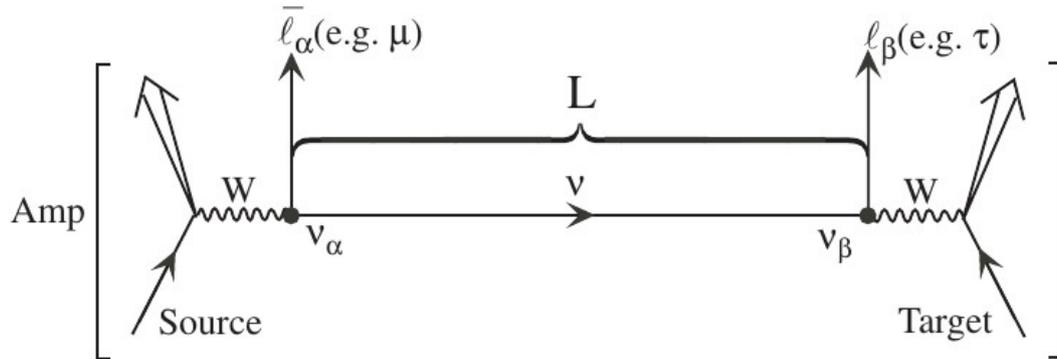
## 2) 3<sup>rd</sup> Cosmological Way

Cosmic Gravitational Focusing

Dipole Structure in Galaxy Correlation Function

## 3) Summary

# Neutrino Oscillation & Mass



$$\nu_\alpha = \sum_i U_{\alpha i} \nu_i$$

$$\rightarrow \sum_i U_{\alpha i} e^{i(E_i t - \vec{P}_i \cdot \vec{x})} \nu_i$$

$$= \sum_i U_{\alpha i} P_i U_{\beta i}^\dagger \nu_\beta$$

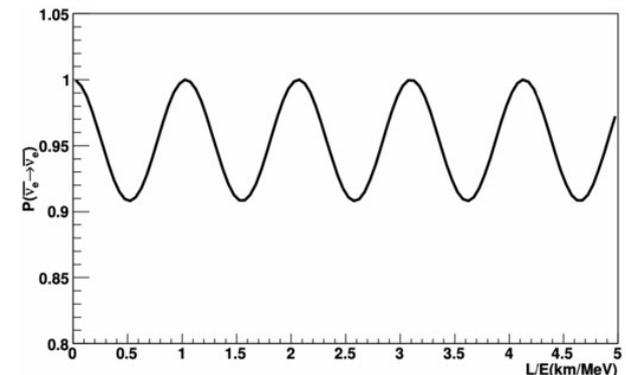
$$\equiv \sum_\beta A_{\alpha\beta} \nu_\beta$$

B. Kayser, [hep-ph/0506165]

$$P_{\alpha\beta} |_{\alpha \neq \beta} \equiv |A_{\alpha\beta}|^2 = \sin^2 2\theta \sin^2 \left( \delta m^2 \frac{L}{4E} \right)$$

1<sup>st</sup> New Physics

Mass



# Global Fit of Oscillation Parameters

(for <b>NO</b> )	$-1\sigma$	Best Value	$+1\sigma$
$\Delta m_s^2 \equiv \Delta m_{21}^2$ ( $10^{-5}\text{eV}^2$ )	7.30	7.50	7.72
$ \Delta m_a^2 \equiv \Delta m_{31}^2 $ ( $10^{-3}\text{eV}^2$ )	2.52	2.56	2.59
$\sin^2 \theta_s$ ( $\theta_s \equiv \theta_{12}$ )	0.302 ( $33.3^\circ$ )	0.318 ( $34.3^\circ$ )	0.334 ( $35.3^\circ$ )
$\sin^2 \theta_a$ ( $\theta_a \equiv \theta_{23}$ )	0.544 ( $47.54^\circ$ )	0.566 ( $48.79^\circ$ )	0.582 ( $49.72^\circ$ )
$\sin^2 \theta_r$ ( $\theta_r \equiv \theta_{13}$ )	0.02147 ( $8.43^\circ$ )	0.02225 ( $8.58^\circ$ )	0.02280 ( $8.69^\circ$ )
$\delta_D$	$191^\circ$	$216^\circ$	$257^\circ$
$\delta_{Mi}$	??	??	??

Salas, Forero, Gariazzo, Martinez-Mirave, Mena, Ternes, Tortola & Valle, [arXiv:2006.11237]

- Heavy neutrinos ( $N$ )

$$\bar{\nu} M_D \mathcal{N} + h.c. + \bar{\mathcal{N}} M_N \mathcal{N} = \begin{pmatrix} \bar{\nu} & \bar{\mathcal{N}} \end{pmatrix} \begin{pmatrix} 0 & M_D \\ M_D^T & M_N \end{pmatrix} \begin{pmatrix} \nu \\ \mathcal{N} \end{pmatrix}$$

required by **Grand Unification Theory (大统一理论)**

- Seeaw Mechanism

The diagonalization of the full mass matrix

$$\begin{pmatrix} 0 & M_D \\ M_D^T & M_N \end{pmatrix} \Rightarrow M_\nu = -M_D \frac{1}{M_N} M_D^T$$

$$M_D \sim O(100) \text{ GeV}, \quad M_N \sim O(10^{15}) \text{ GeV} \quad \rightarrow \quad M_\nu \sim O(0.01) \text{ eV}$$

**Light neutrino mass  $M_\nu$  is suppressed by the heavy ones**



Tsutomu Yanagida、  
Xiao-Gang He :  
**Let's play seesaw**

## $\nu$ Oscillation

## Beta Decay

## Radiative Emission of $\nu$ Pairs

SFG, Pedro Pasquini, **JHEP 12 (2023) 083** [arXiv:2306.12953]  
**Phys.Lett.B 841 (2023) 137911** [arXiv:2206.11717]  
**Eur.Phys.J.C 82 (2022) 3, 208** [arXiv:2110.03510]

## Supernova $\nu$ Time Delay

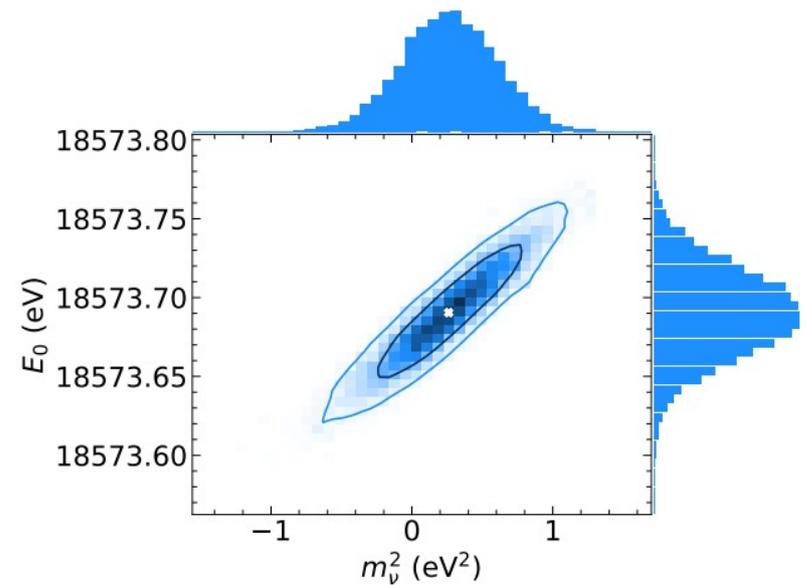
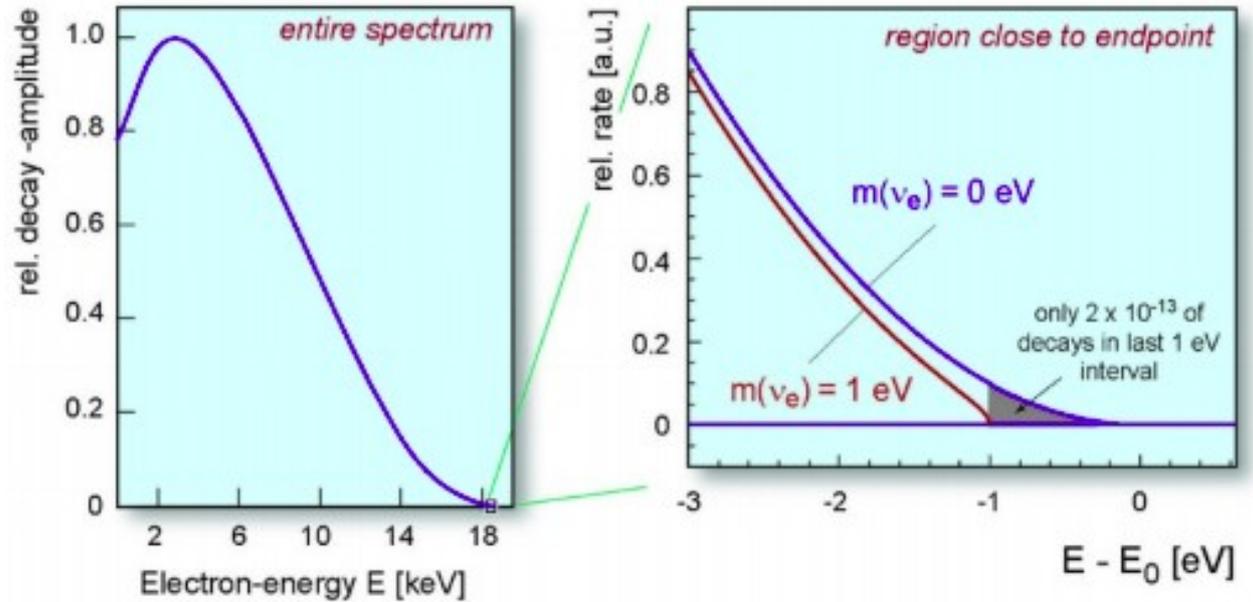
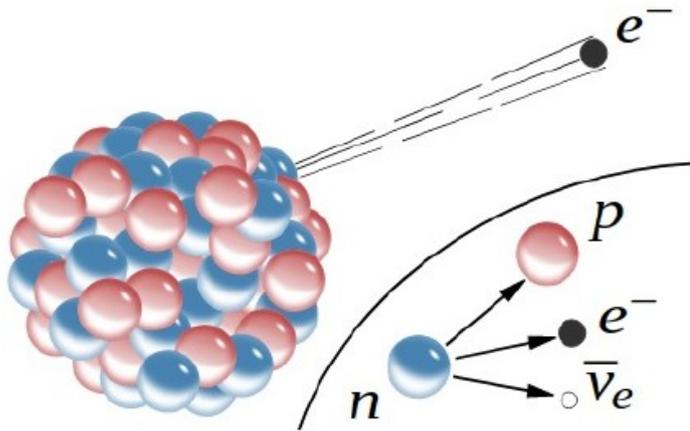
SFG, Chui-Fan Kong, Alexei Smirnov, **accepted by PRL** [arXiv:2404.17352]

## C $\nu$ B Detection

## CMB & LSS

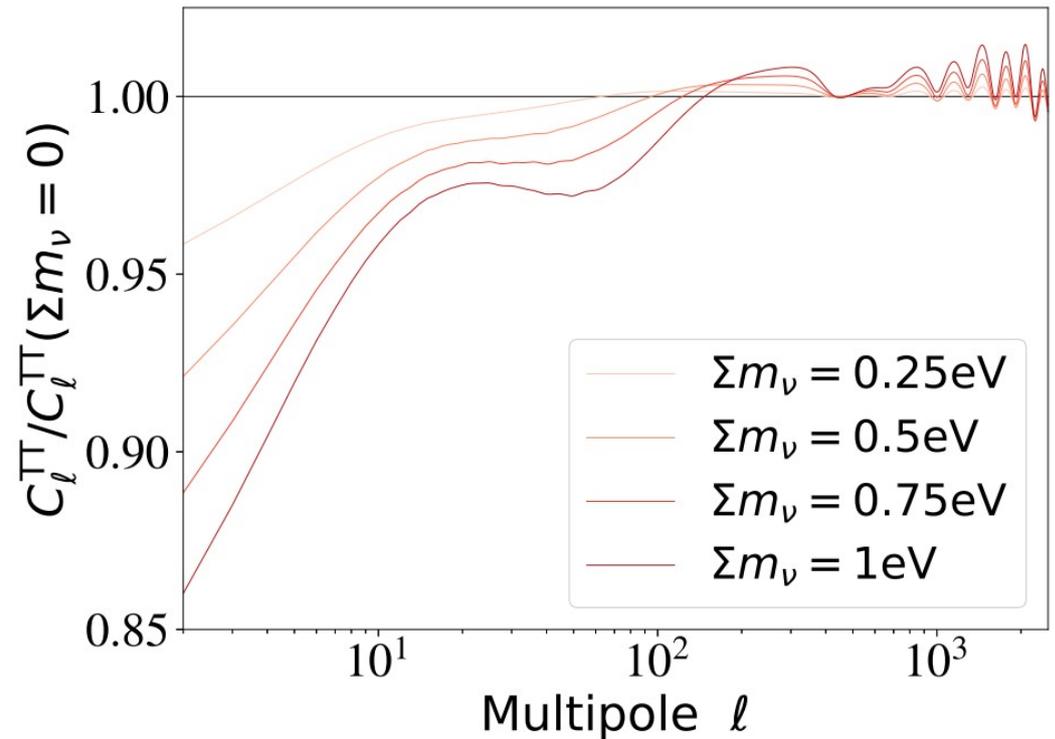
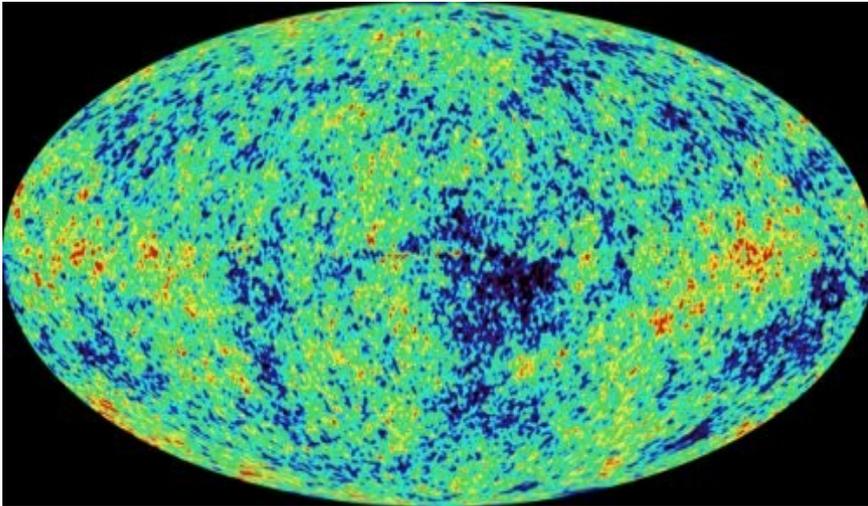
SFG, Pedro Pasquini, Liang Tan, **JCAP 05 (2024) 108** [arXiv:2312.16972]

# Neutrino Mass @ $\beta$ Decay



Nature Phys. 18 (2022) 2, 160-166

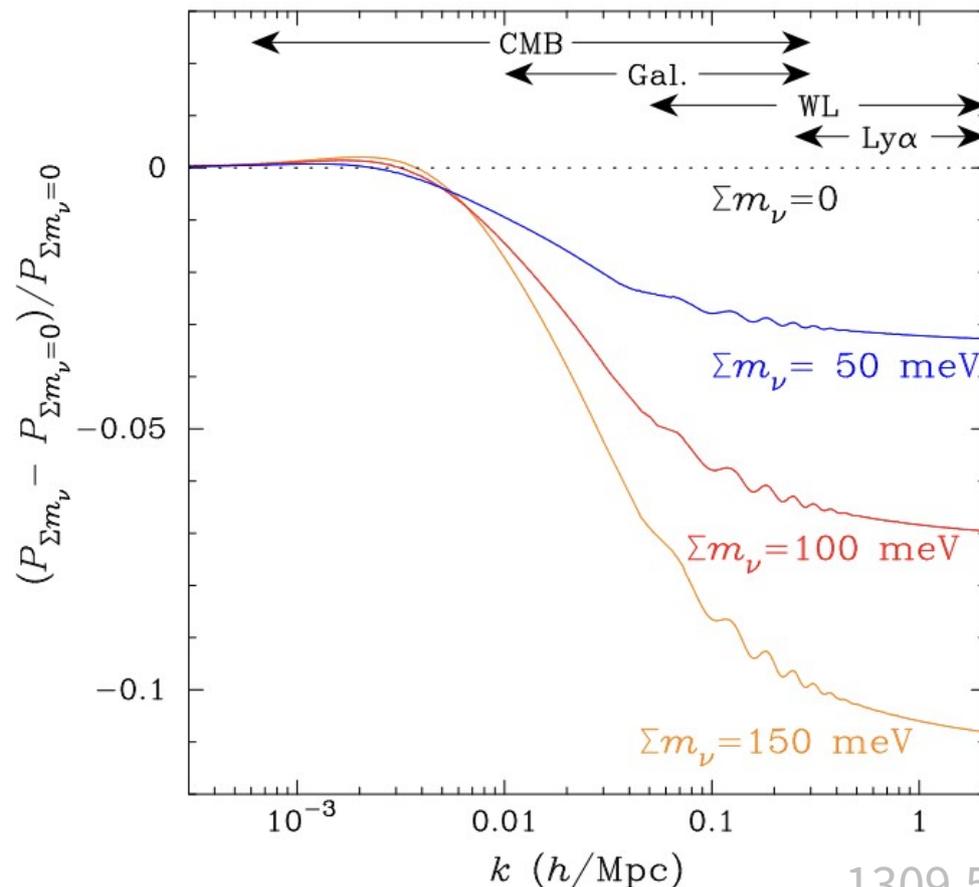
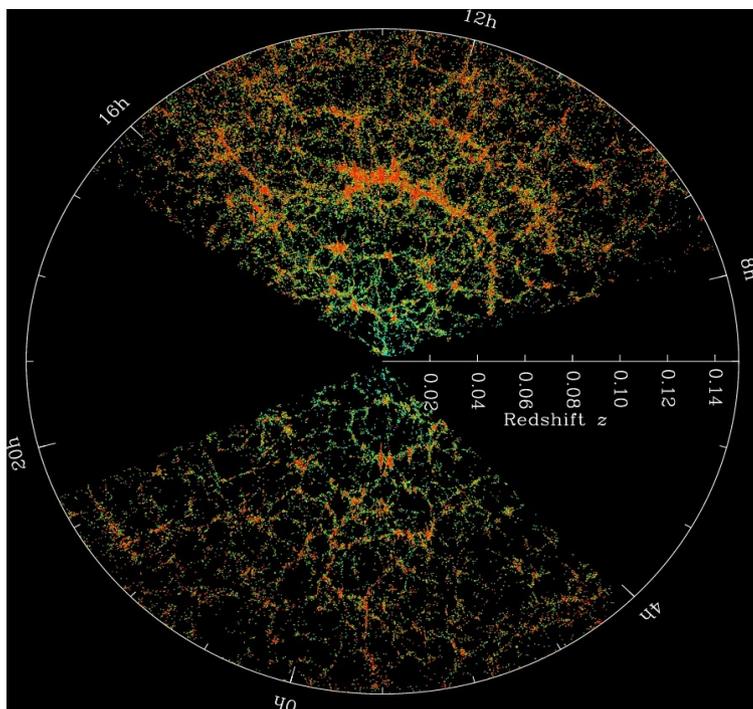
# Massive neutrino decreasing CMB power spectrum



$$\rho_\nu = n_\nu \sum_i m_i$$

PDG 2022 Neutrino in Cosmology

## Suppression matter power spectrum below neutrino free-streaming scale



1309.5383

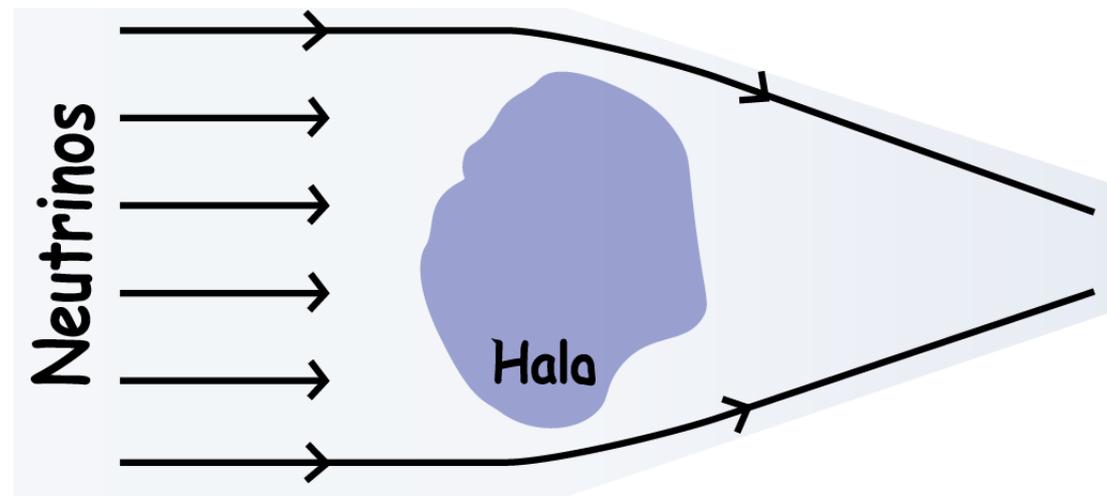
$$\rho_\nu = n_\nu \sum_i m_i$$

$$\sum m_\nu < 0.13 \text{ eV}$$

Planck18+BAO

# Cosmic $\nu$ Fluid (CvF) vs DM Halo

## Gravitational attraction between DM halo & CvF



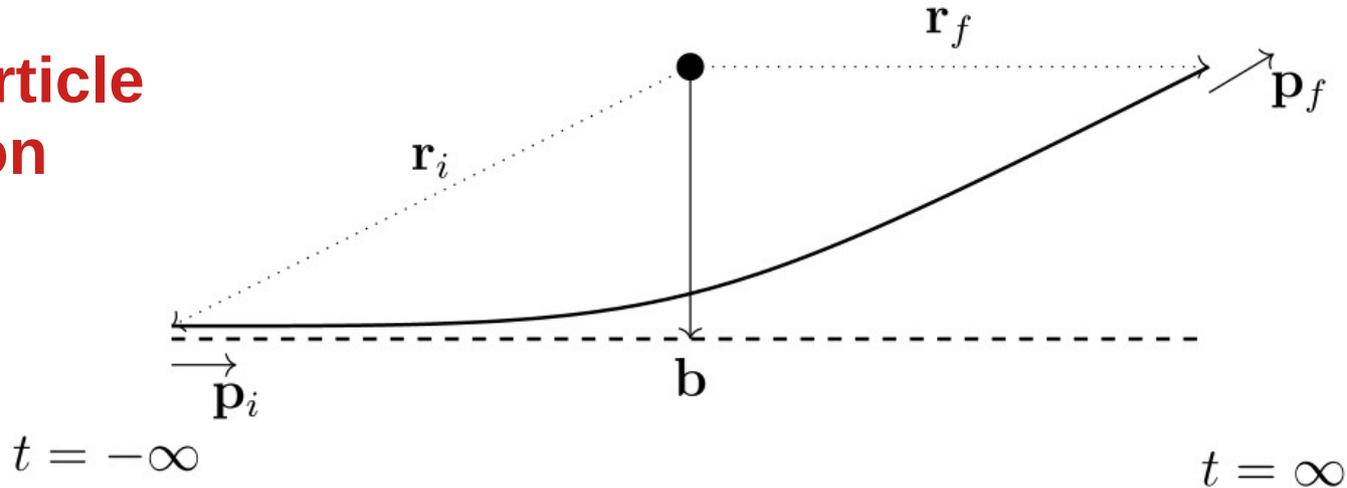
CvF

DM  
Halo

vs Stone in Water Flow

# Gravitational Deflection

## Single-particle description



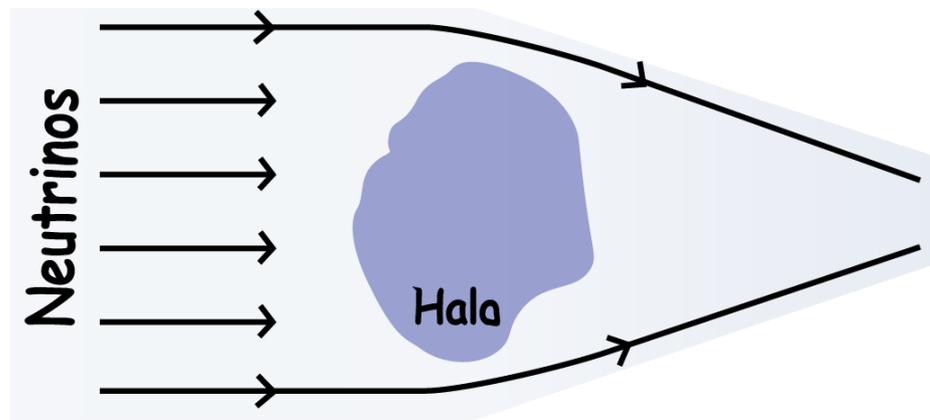
$$ds^2 \equiv - \left( 1 - \frac{2GM}{r} \right) dt^2 + \left( 1 - \frac{2GM}{r} \right)^{-1} dr^2 + r^2 d\Omega^2$$

$$\Delta\phi = 2|\mathbf{b}| \int_{r_{\min}}^{\infty} \frac{dr}{r^2} \left[ 1 + \frac{2b_{90}}{r} - \frac{|\mathbf{b}|^2}{r^2} + \frac{2GM|\mathbf{b}|^2}{r^3} \right]^{-1/2}$$

$$b_{90} \equiv GMm_{\nu}^2/|\mathbf{p}_i|^2$$

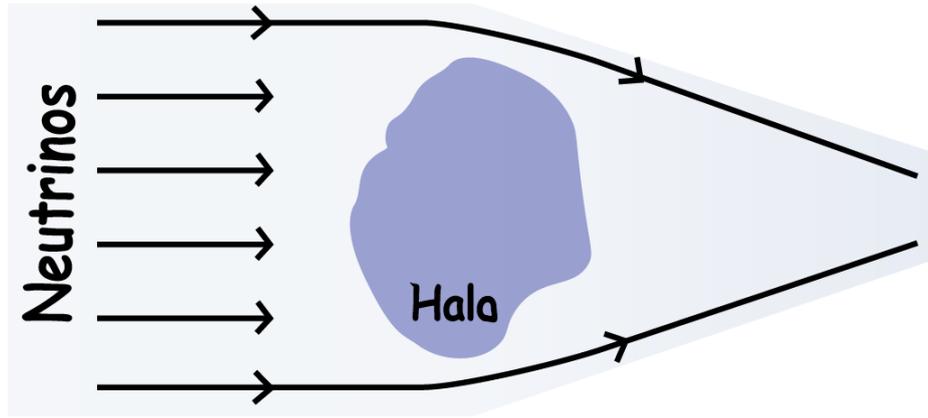
$$r_{\min}^3 + 2b_{90}r_{\min}^2 - |\mathbf{b}|^2r_{\min} + 2GM|\mathbf{b}|^2 = 0$$

## Single-particle description



$$\Delta\phi \approx \pi + 2\frac{GM}{|\mathbf{b}|} \left( \frac{m_\nu^2}{|\mathbf{p}_i|^2} + 2 \right) \quad f_\nu(\mathbf{p}_i, \mathbf{v}) \approx \frac{2}{e^{|\mathbf{p}_i - E_{\mathbf{p}_i} \mathbf{v}/c|/T} + 1}$$

$$\Delta\mathbf{p}^\parallel \equiv \mathbf{p}_f^\parallel - \mathbf{p}_i = (-\cos \Delta\phi - 1) \mathbf{p}_i \approx -\frac{2G^2 M^2}{|\mathbf{b}|^2} \left( \frac{m_\nu^2}{|\mathbf{p}_i|^2} + 2 \right)^2 \mathbf{p}_i$$



**Boltzmann  
description**

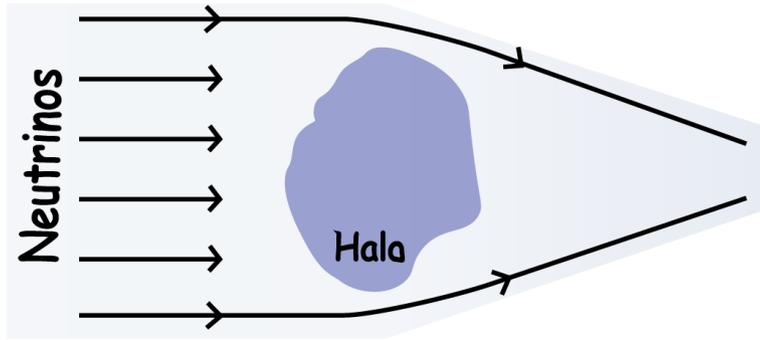
$$f_\nu(\mathbf{x}, \mathbf{p}) \equiv \bar{f}_\nu(\mathbf{p}) + \delta f_\nu(\mathbf{x}, \mathbf{p})$$

$$\left\{ \partial_t + \frac{\mathbf{p} \cdot \nabla_{\mathbf{x}}}{aE_{\mathbf{p}}} - \left[ (H + \dot{\Phi})\mathbf{p} + \frac{E_{\mathbf{p}}}{a} \nabla_{\mathbf{x}} \Psi - \frac{|\mathbf{p}|^2 \nabla_{\mathbf{x}} \Phi - \mathbf{p}(\mathbf{p} \cdot \nabla_{\mathbf{x}} \Phi)}{aE_{\mathbf{p}}} \right] \cdot \nabla_{\mathbf{p}} \right\} f_\nu(\mathbf{x}, \mathbf{p}) = 0$$

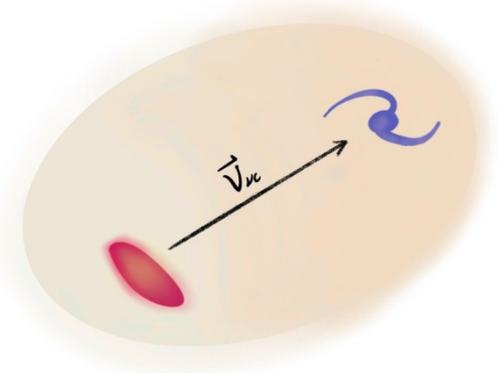
$$\delta \tilde{f}_\nu(\mathbf{k}, \mathbf{p}) = \tilde{\Psi}(\mathbf{k}) \left( \frac{m_\nu^2 + 2\mathbf{p}^2}{\mathbf{p} \cdot \mathbf{k}} \mathbf{k} - \mathbf{p} \right) \cdot \nabla_{\mathbf{p}} \bar{f}_\nu(\mathbf{p})$$

$$\text{Im}[\delta \tilde{\rho}_\nu] = - \frac{(\mathbf{v}_{\nu c} \cdot \hat{\mathbf{k}}) \tilde{\Psi}}{4\pi} \int d|\mathbf{p}'| (m_\nu^4 + 3m_\nu^2 |\mathbf{p}'|^2 + 2|\mathbf{p}'|^4) \frac{d\bar{f}_\nu}{d|\mathbf{p}'|} \Theta(|\mathbf{p}'| - E_{\mathbf{p}'} |\mathbf{v}_{\nu c} \cdot \hat{\mathbf{k}}|)$$

# Cosmic Gravitational Focusing



$$\delta_m = \delta_{m0} + \sum_{i=1}^3 \frac{\delta\rho_{\nu_i}}{\rho_m}$$



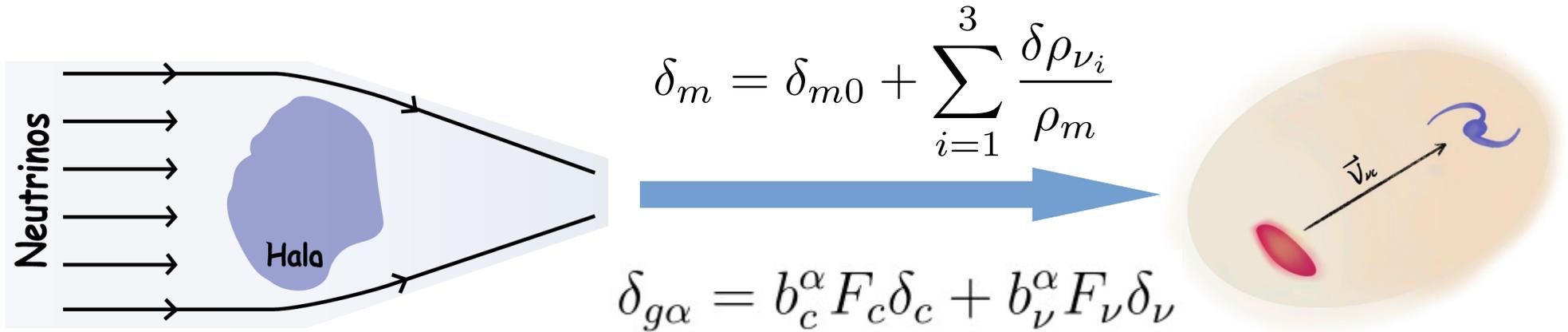
**Density enhancement downwind!**

$$\delta\rho_\nu(-\mathbf{x}) = -\delta\rho_\nu(\mathbf{x})$$

$$\tilde{\delta}_m \equiv \tilde{\delta}_{m0}(1 + i\tilde{\phi})$$

$$\begin{aligned} [\tilde{A}(\mathbf{k})]^* &= \int d\mathbf{x} e^{i\mathbf{k}\cdot\mathbf{x}} A(\mathbf{x}) = \int d\mathbf{x} e^{-i\mathbf{k}\cdot\mathbf{x}} A(-\mathbf{x}) \\ &= - \int d\mathbf{x} e^{-i\mathbf{k}\cdot\mathbf{x}} A(\mathbf{x}) = -\tilde{A}(\mathbf{k}) \end{aligned}$$

SFG, Pedro Pasquini, Liang Tan [arXiv:2312.16972]

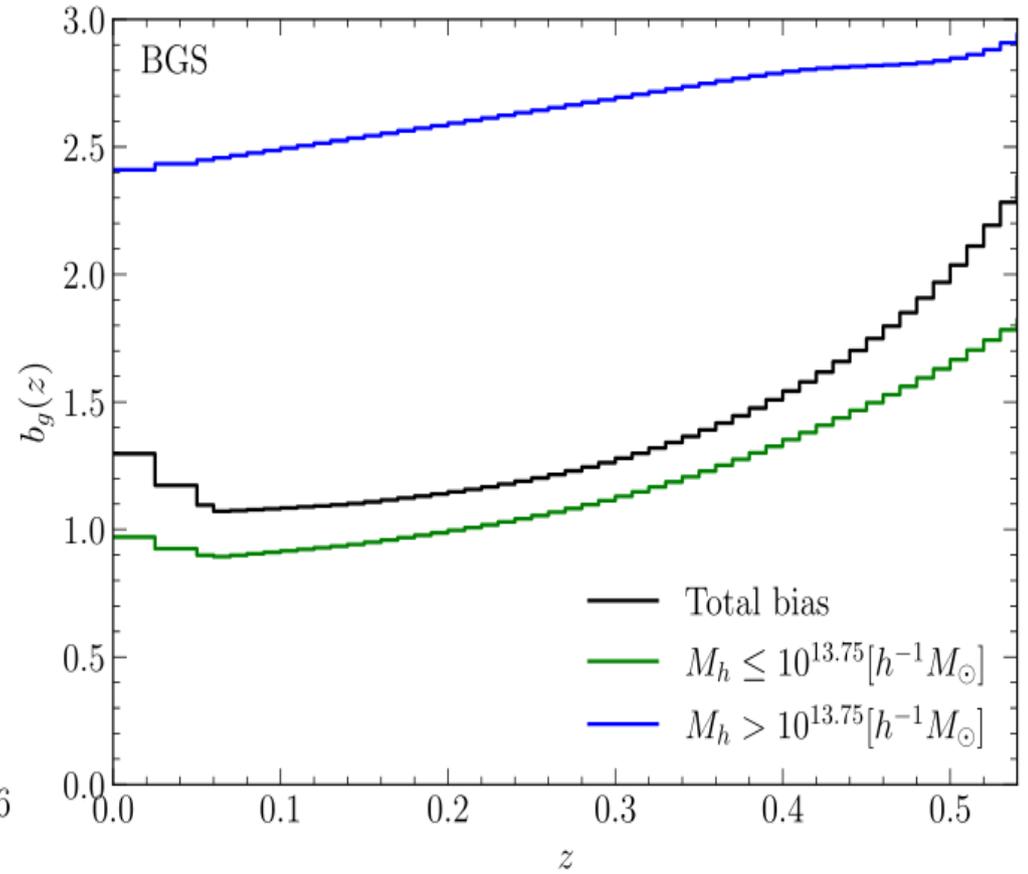
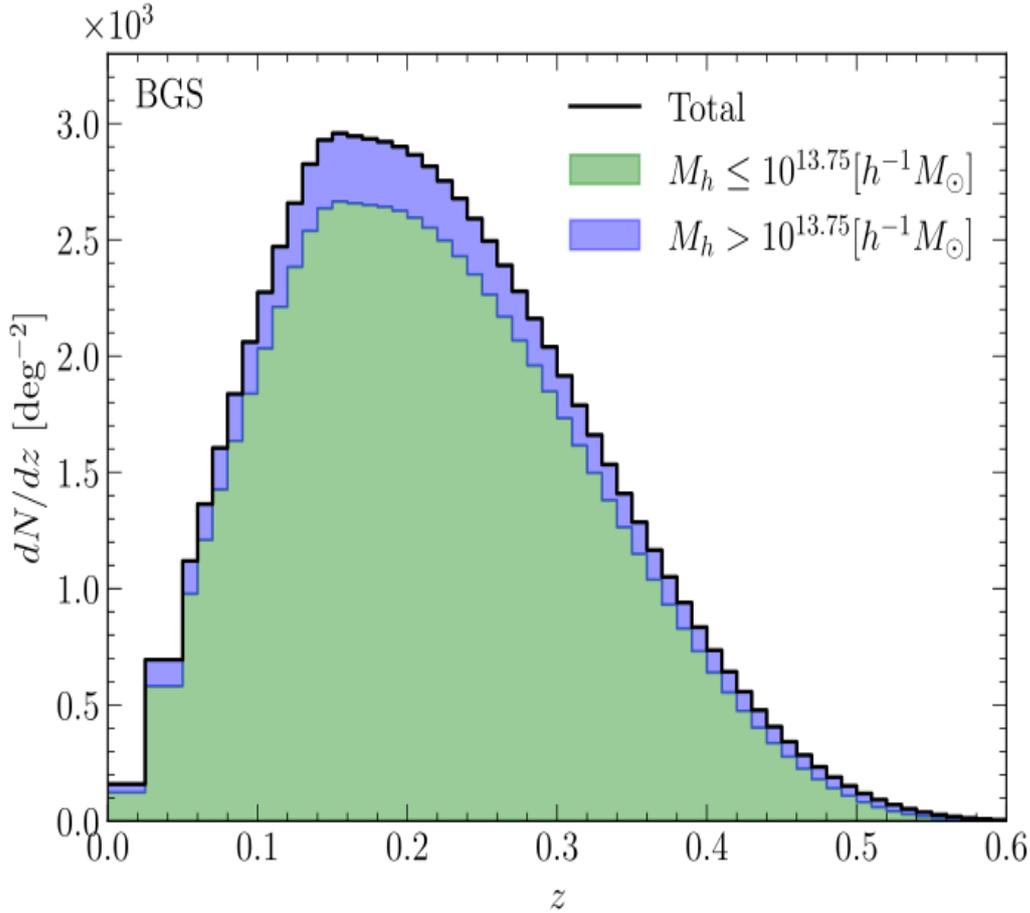


$$\delta_{g\alpha, \text{RSD}}(\mathbf{x}) \equiv \delta_{g\alpha}(\mathbf{x}) - \frac{\partial}{\partial x} \left( \frac{\mathbf{u}_m \cdot \hat{\mathbf{x}}}{aH} \right)$$

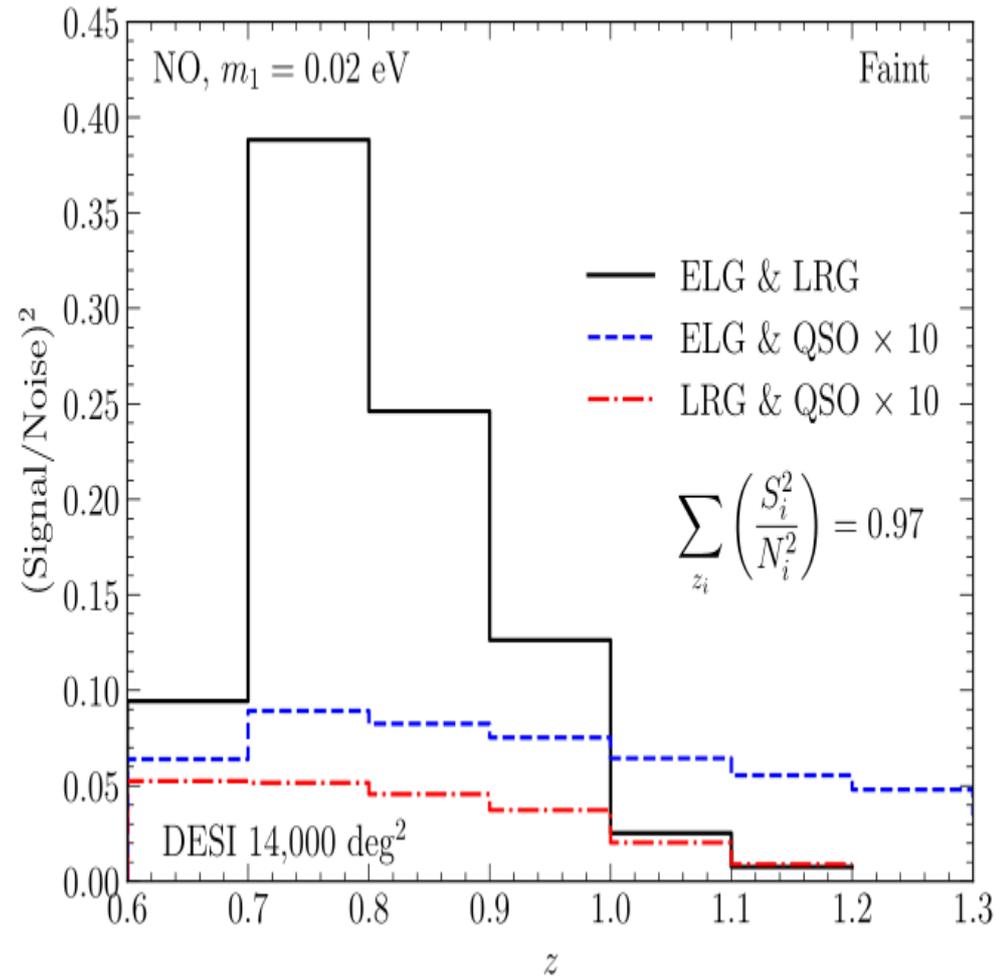
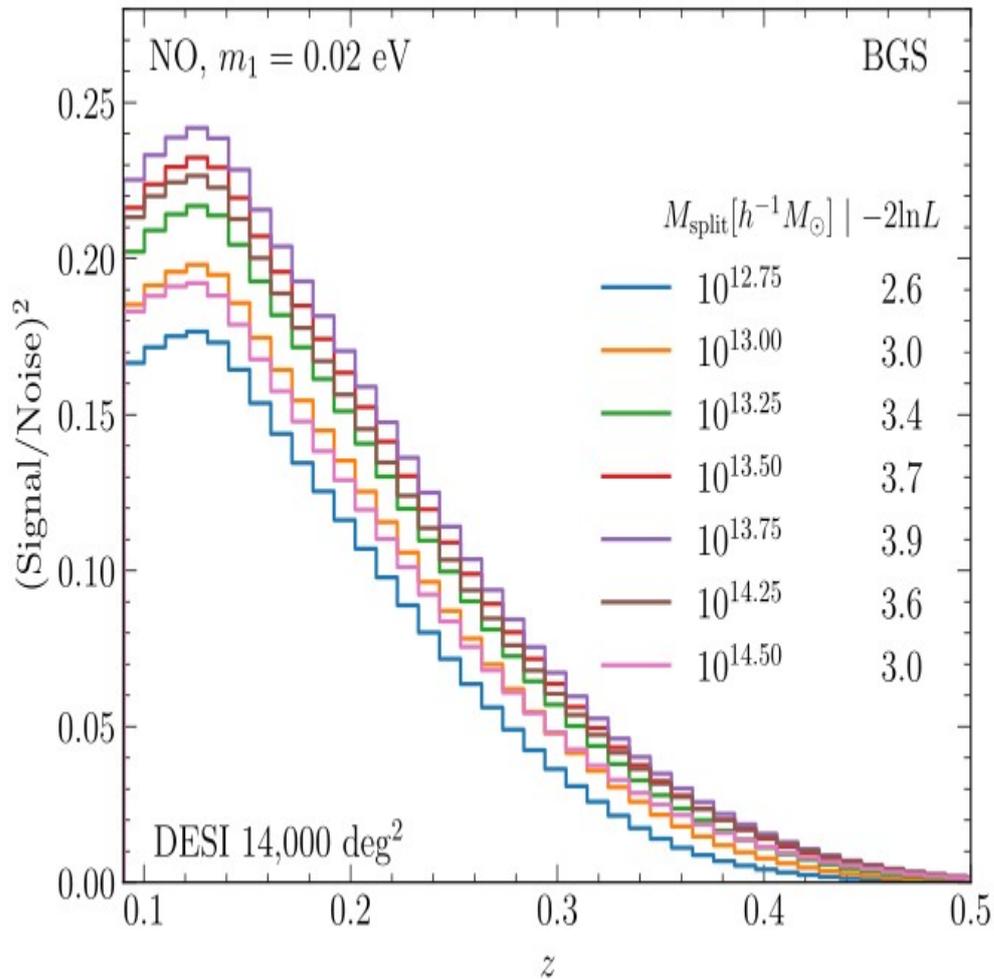
$$\text{Im}[\tilde{\delta}_{g\alpha, \text{RSD}} \tilde{\delta}_{g\beta, \text{RSD}}^*] = -i\Delta b \left[ \mu_{\mathbf{k}}^2 \frac{\dot{\tilde{\phi}}}{H} + (f\mu_{\mathbf{k}}^2 + 1)\tilde{\phi} \right] \tilde{\delta}_{m0}^2$$

**Galaxies with different bias**

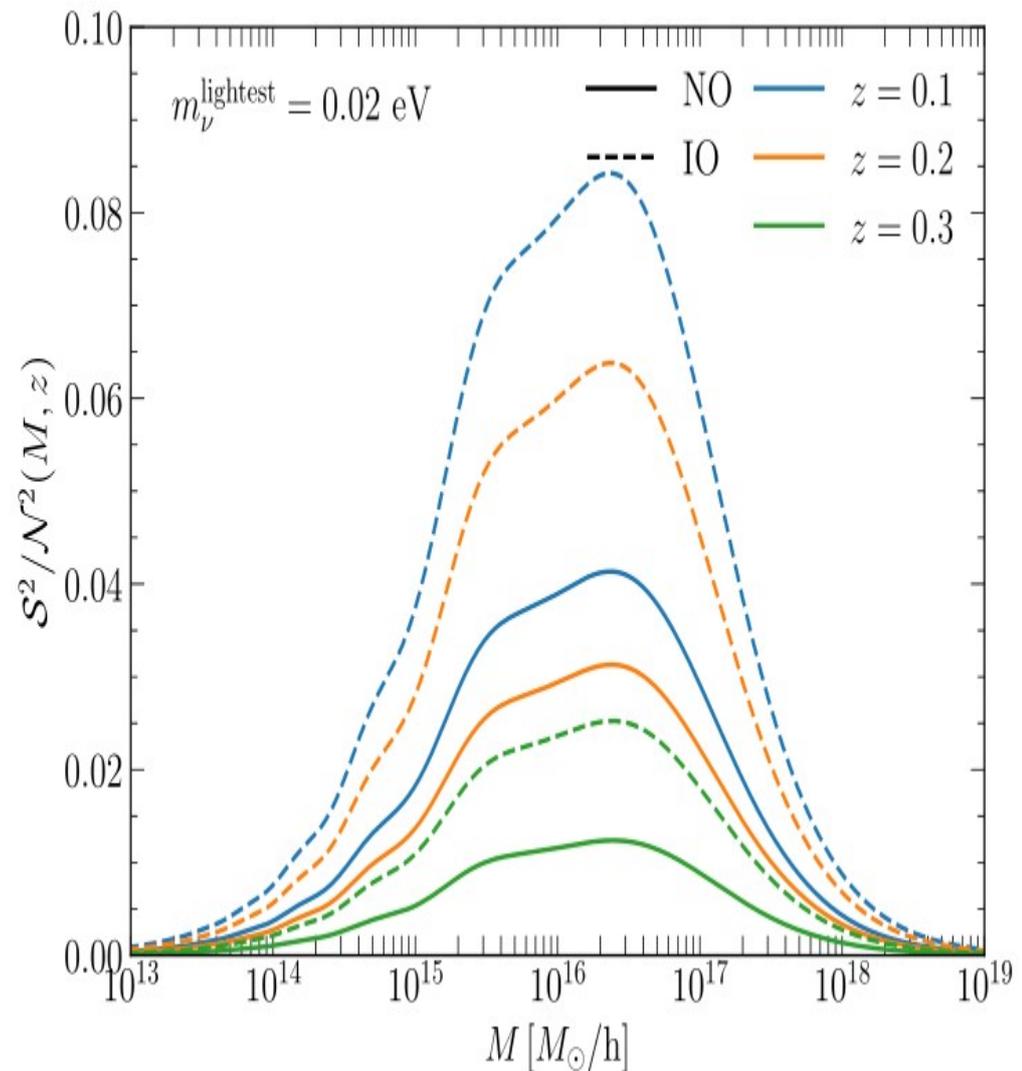
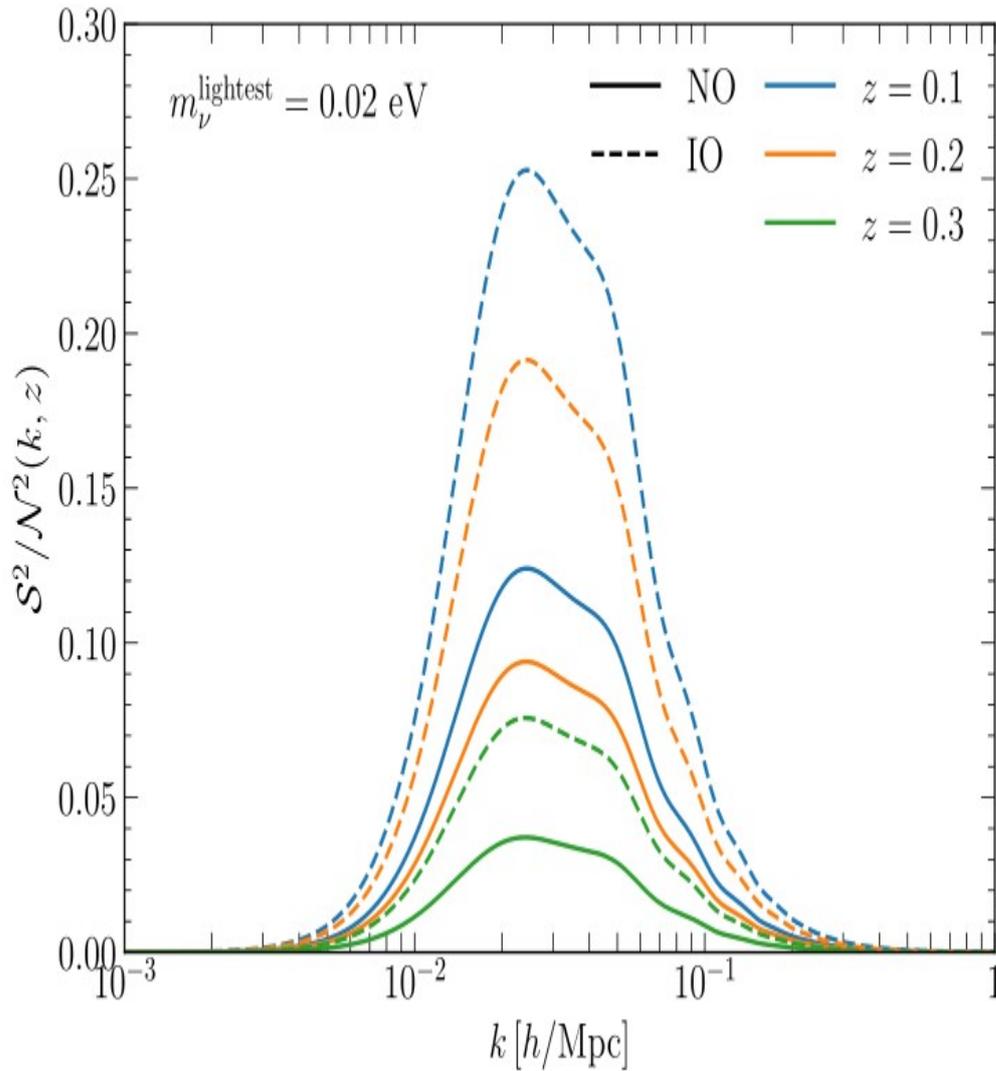
$$\Delta b \equiv b_c^\alpha - b_c^\beta$$



$$n_g(z) \equiv \int d \ln M_h \frac{dn(z)}{d \ln M_h} \langle N(M_h) \rangle \quad b_g(z) \equiv \frac{1}{n_g} \int d \ln M_h \frac{dn(z)}{d \ln M_h} \langle N(M_h) \rangle b_h(M_h, z)$$

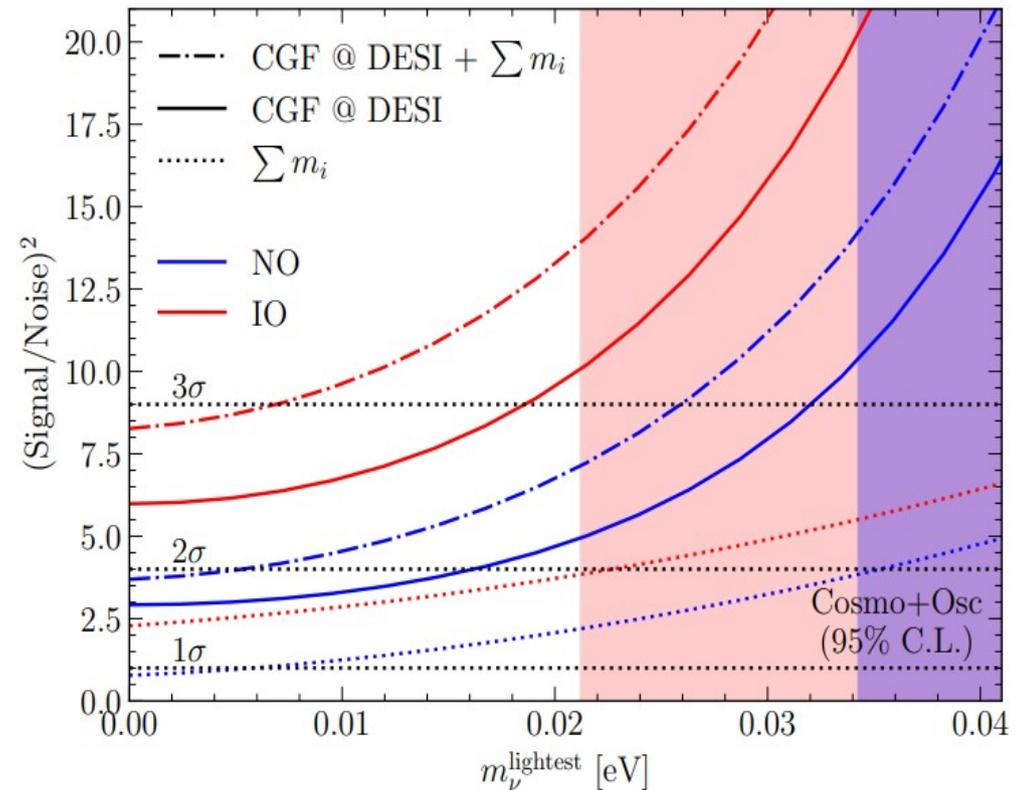
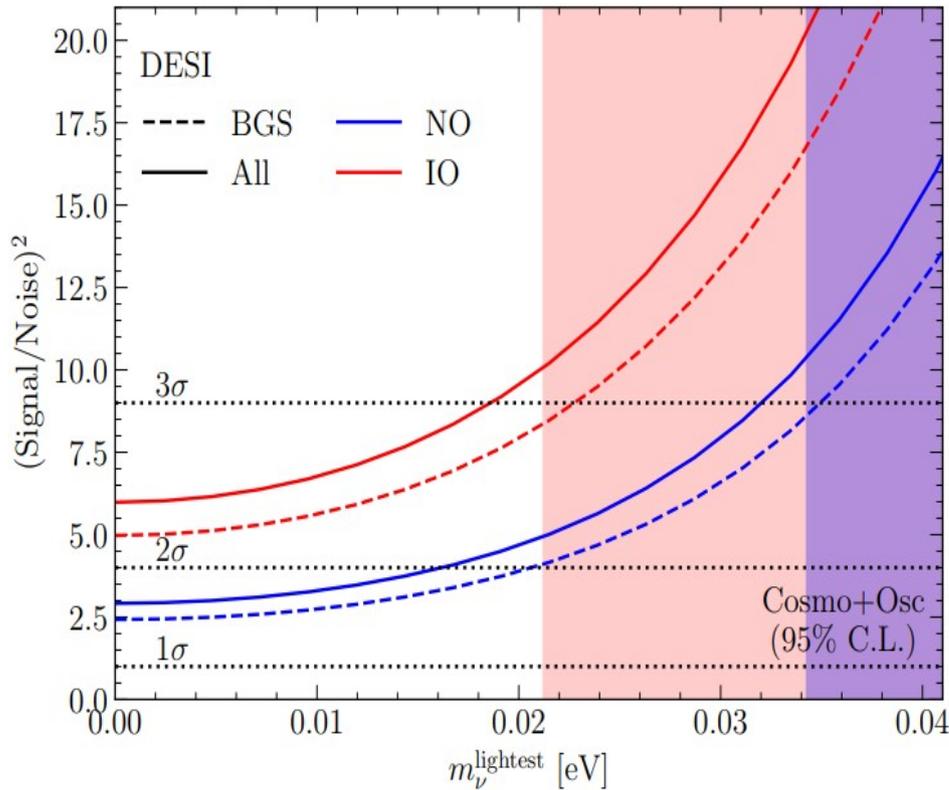


# Redshift Distribution



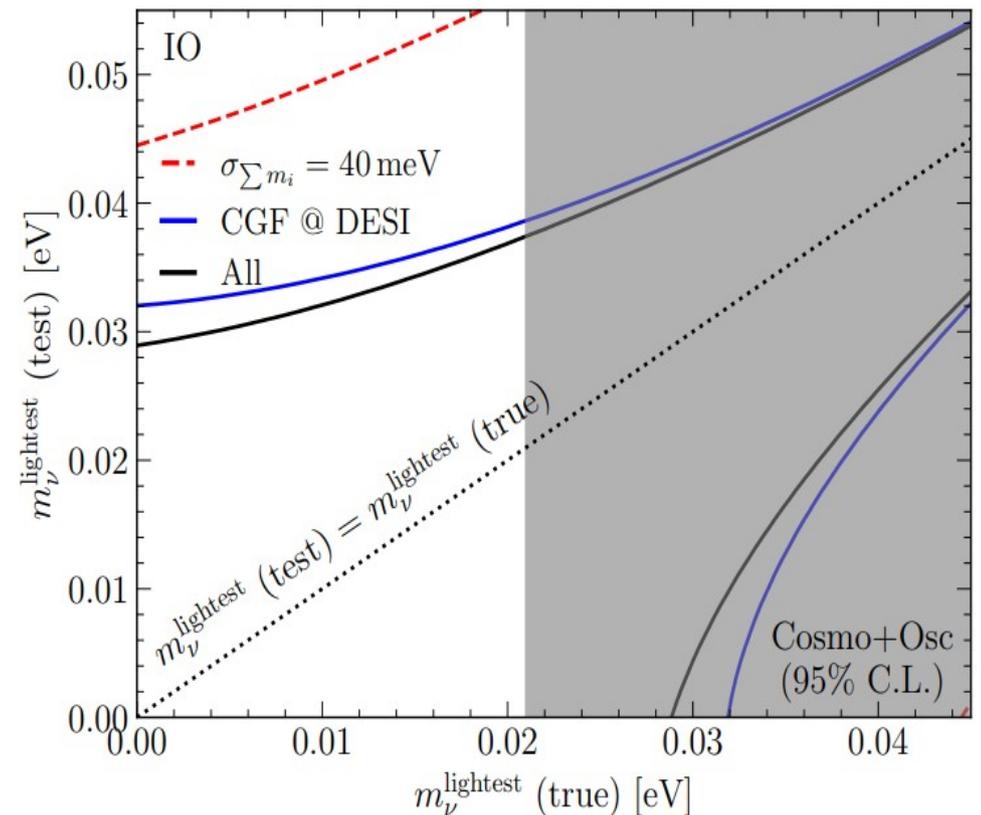
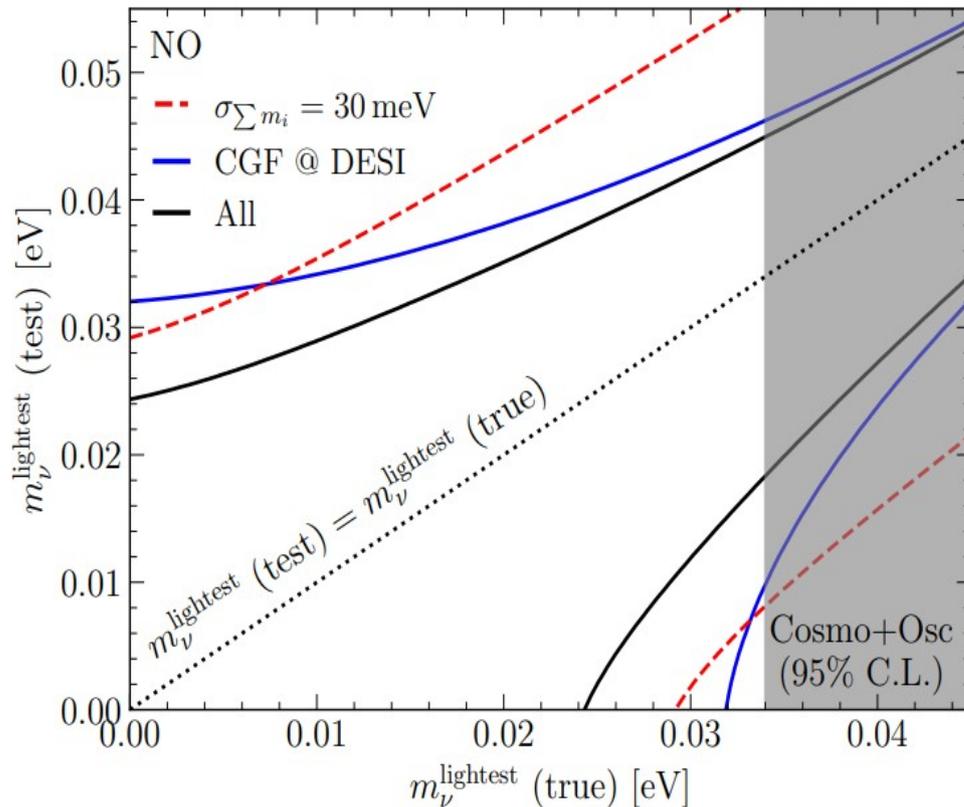
# 3<sup>rd</sup> Cosmic Measurement of $\nu$ Masses

$$\text{Im} \left[ \tilde{\delta}_{g\alpha} \left( \tilde{\delta}_{g\beta} \right)^* \right] \propto \left( \mathbf{v}_{\nu c} \cdot \hat{\mathbf{k}} \right) \left( f_0 m_\nu^4 + f_1 m_\nu^2 T^2 + f_2 T^4 \right)$$



SFG, Pedro Pasquini, Liang Tan [arXiv:2312.16972]

$$\text{Im} \left[ \tilde{\delta}_{g\alpha} \left( \tilde{\delta}_{g\beta} \right)^* \right] \propto \left( \mathbf{v}_{\nu c} \cdot \hat{\mathbf{k}} \right) \left( f_0 m_\nu^4 + f_1 m_\nu^2 T^2 + f_2 T^4 \right)$$



DESI, Euclid, Subaru PFS, **CSST**

SFG, Pedro Pasquini, Liang Tan [arXiv:2312.16972]

## 1) Overview of Neutrino Mass

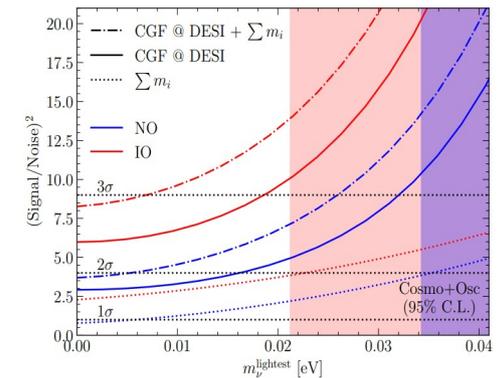
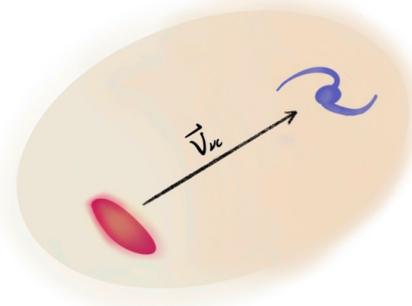
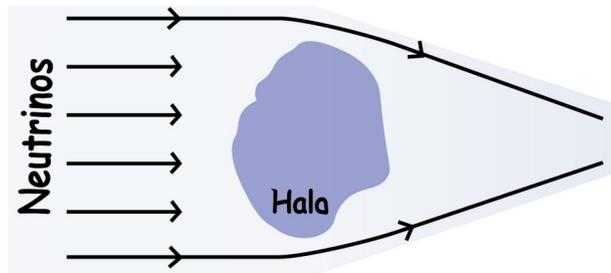
## 2) 3<sup>rd</sup> Cosmological Way

Dynamical Friction

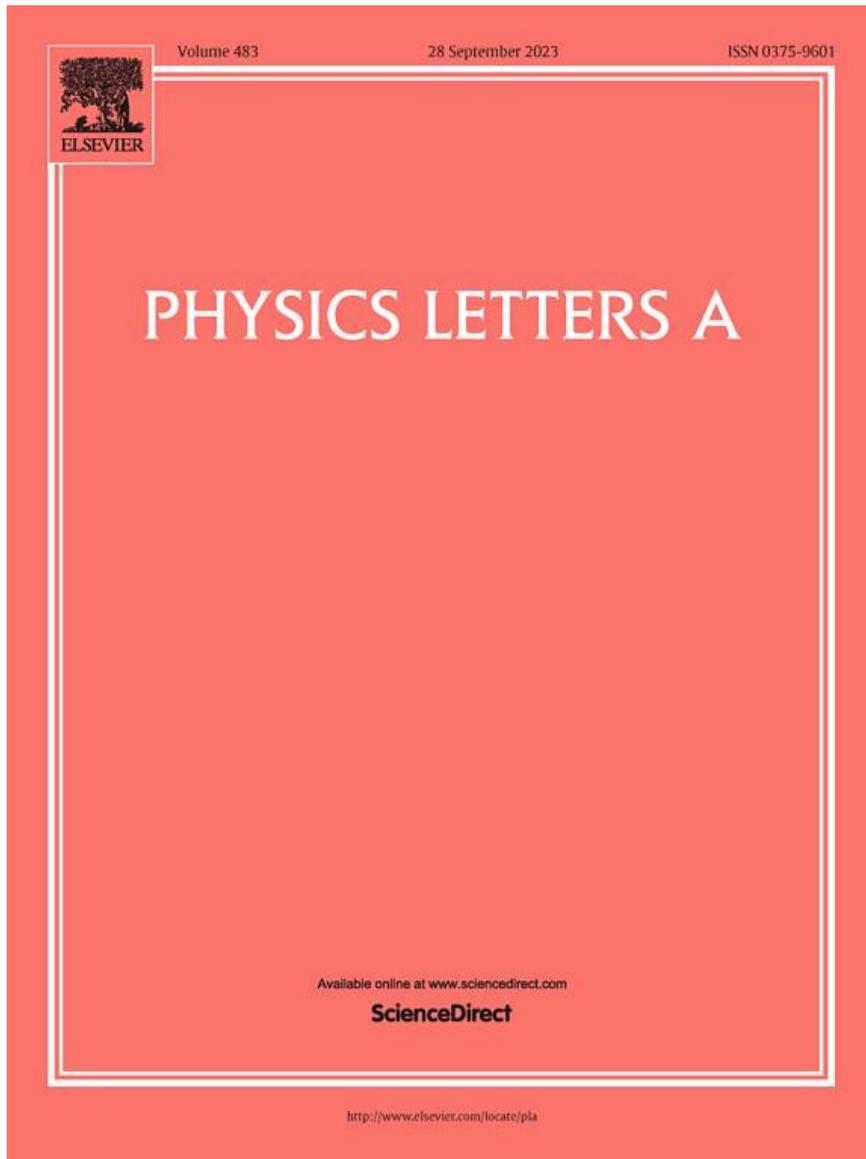
Cosmic Gravitational Focusing

Dipole Structure in Galaxy Correlation Function

Neutrino Mass Measurement @ DESI & CSST



## 3) Summary



## Aims & Scope

- Nonlinear science,
- Statistical physics,
- Mathematical and computational physics,
- AMO and physics of complex systems,
- Plasma and fluid physics,
- Optical physics,
- General and cross-disciplinary physics,
- Biological physics and nanoscience,
- Astrophysics, Particle physics and Cosmology.

**Thank You**

Georg G. Raffelt

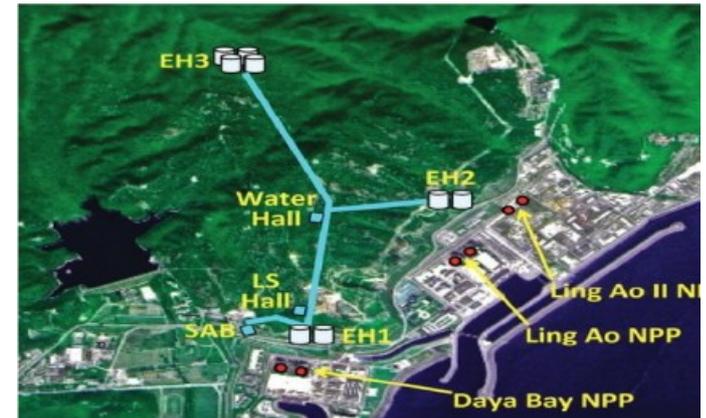
## Stars as Laboratories for Fundamental Physics

The Astrophysics of Neutrinos, Axions, and Other  
Weakly Interacting Particles

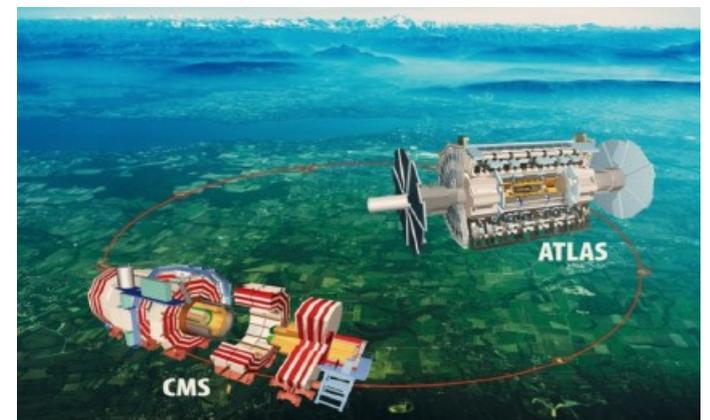
In the standard model, neutrinos have been assigned the most minimal properties compatible with experimental data: zero mass, zero charge, zero dipole moments, zero decay rate, zero almost everything.

# Neutrino vs Higgs

- **Higgs boson**  $\Rightarrow$  electroweak symmetry breaking & mass.  $\sim O(100)\text{GeV}$
- **Chiral symmetry breaking**  $\Rightarrow$  majority of mass.
- The world seems not affected by the tiny neutrino mass?
  - Neutrino mass  $\Rightarrow$  Mixing
  - 3 Neutrino  $\Rightarrow$  possible **CP violation**
  - CP violation  $\Rightarrow$  **Leptogenesis**
  - $\Rightarrow$  **Matter-Antimatter Asymmetry**
  - There is something left in the Universe.
  - **EW Baryogenesis** is not enough.

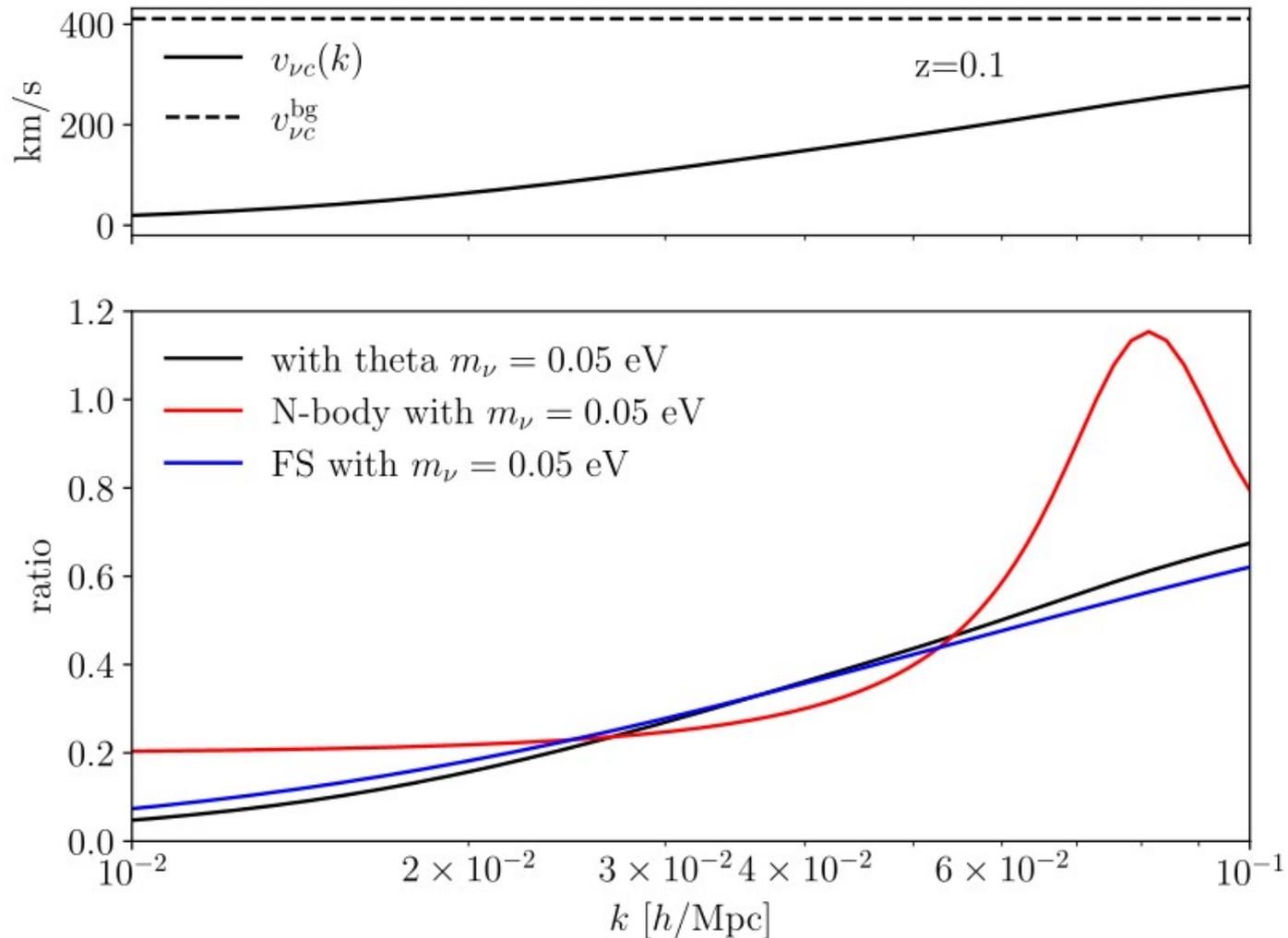


Daya Bay @ **March 8, 2012**

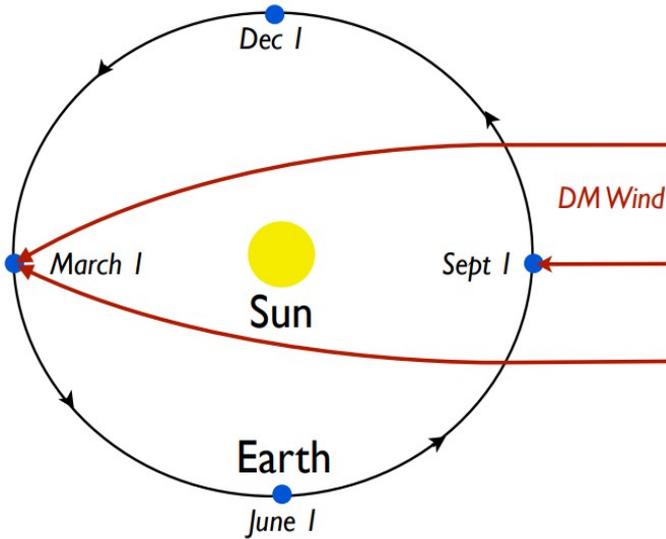


LHC @ **July 4, 2012**

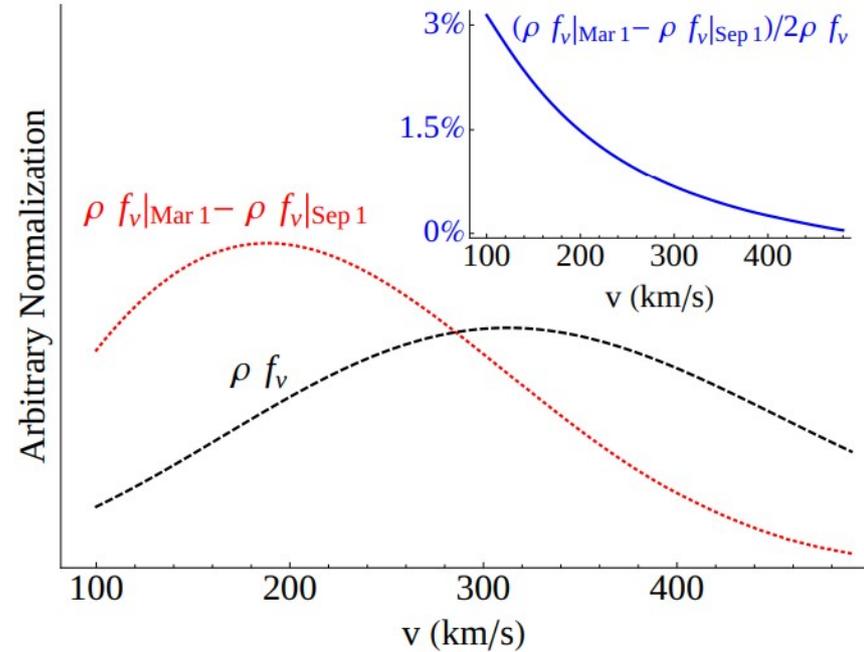
$$\langle (\mathbf{v}_{\nu c} \cdot \hat{\mathbf{k}})^2 \rangle = \frac{1}{3} \int \frac{d|\mathbf{k}'|}{|\mathbf{k}'|} \Theta(|\mathbf{k}| - |\mathbf{k}'|) \left| \widetilde{W}(|\mathbf{k}'|R) \right|^2 \Delta_{\zeta}^2(\mathbf{k}') \left| \frac{T_{\theta_{\nu ic}}(\mathbf{k}', z)}{|\mathbf{k}'|} \right|^2$$



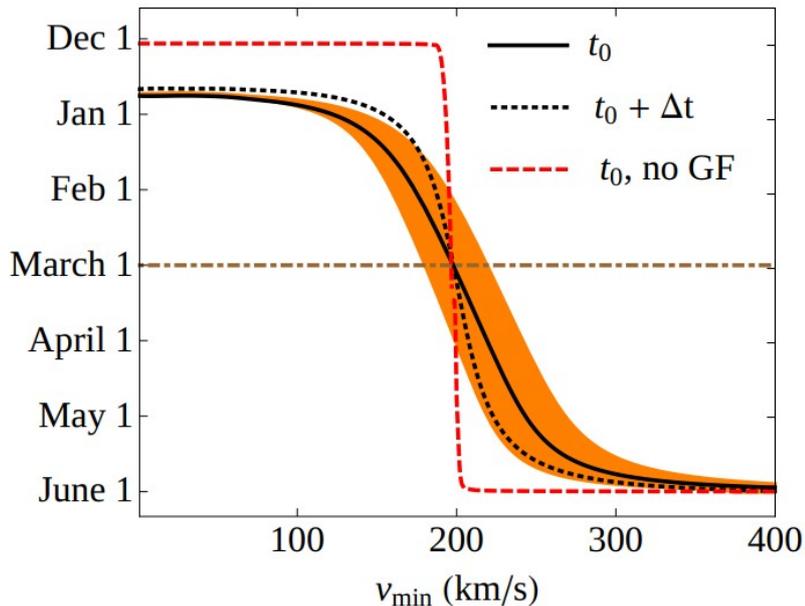
# DM Gravitational Focusing



- Density enhancement



- Modulation phase shift

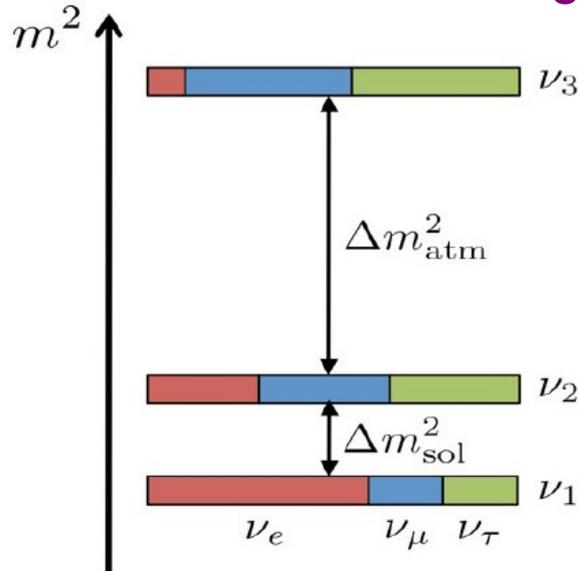


Lee, Lisanti, Peter, Safdi, Phys. Rev. Lett. 112, 011301 (2014) [arXiv:1308.1953]

Bozorgnia & Schwetz, JCAP 08 (2014) 013 [arXiv:1405.2340]

# $\nu$ Mass Ordering

Normal Ordering (正序)



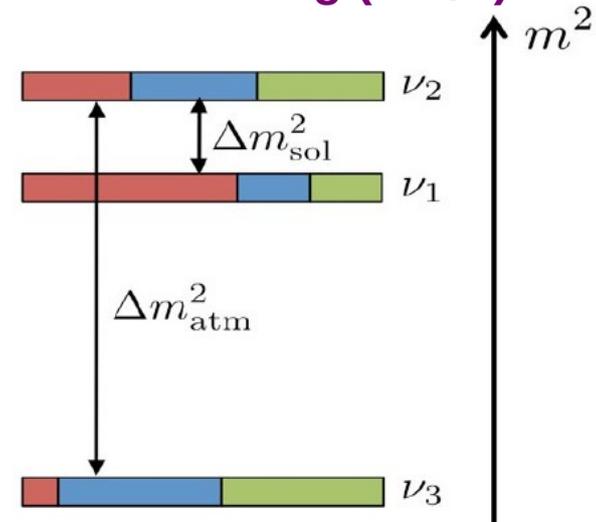
$$m_1 \lesssim m_2 < m_3$$

$m_1$

$$m_2 = \sqrt{m_1^2 + \Delta m_s^2}$$

$$m_3 = \sqrt{m_1^2 + \Delta m_a^2}$$

Inverted Ordering (反序)



$$m_3 < m_1 \lesssim m_2$$

$$m_1 = \sqrt{m_3^2 + \Delta m_a^2}$$

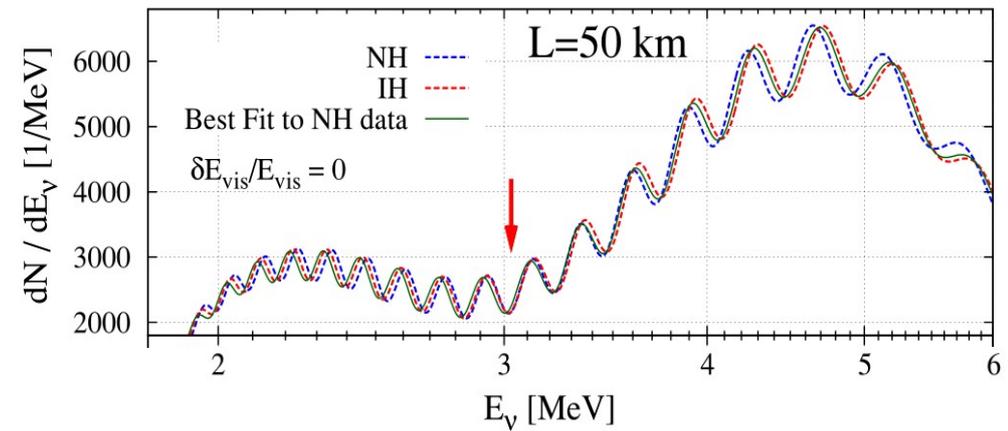
$$m_2 = \sqrt{m_3^2 + \Delta m_a^2 + \Delta m_s^2}$$

$m_3$

江门中微子实验 (JUNO)

However,  $\nu$  oscillation experiment cannot measure the absolute mass!

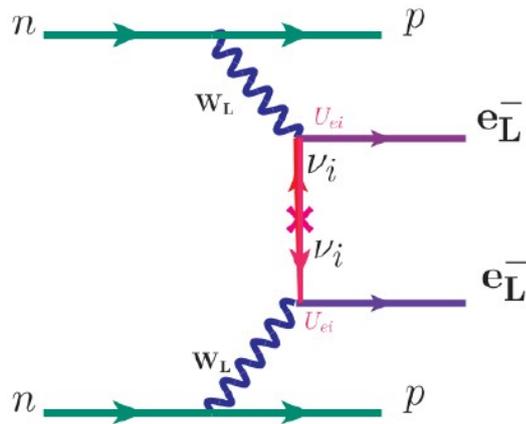
# $\nu$ Mass Hierarchy @ JUNO



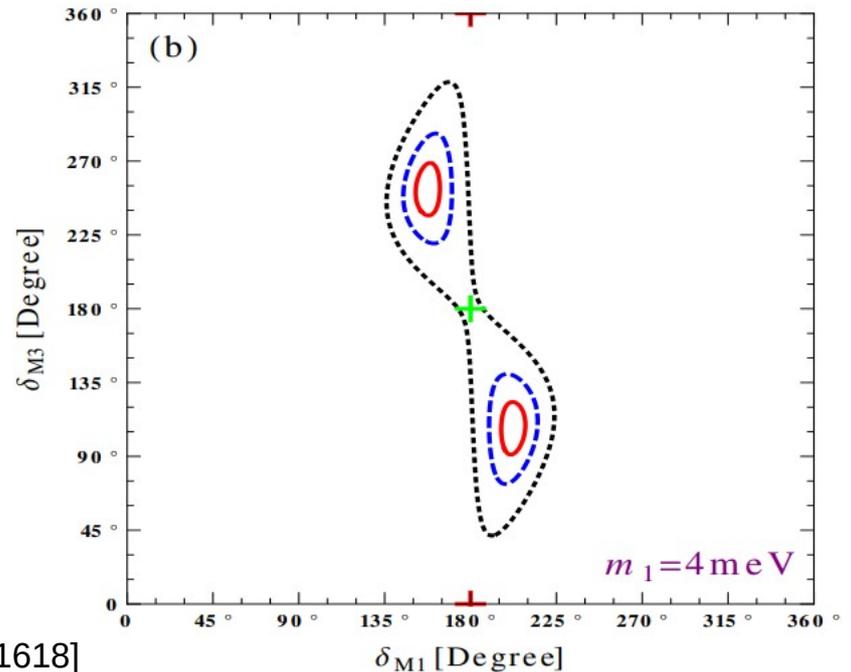
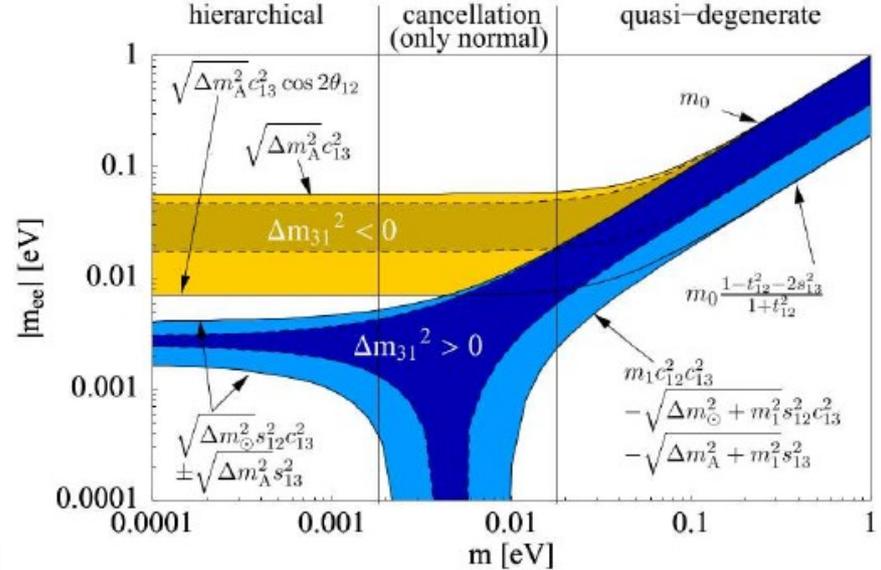
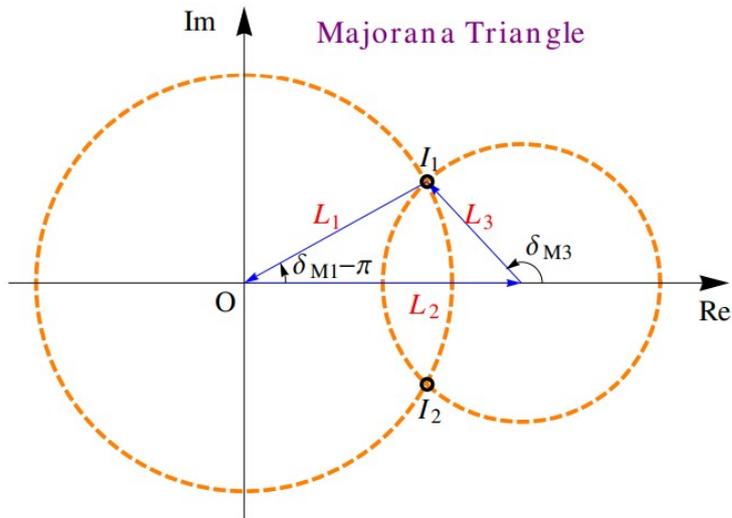
$$P_{ee} = 1 - \cos^4 \theta_{13} \sin^2 2\theta_{12} \sin^2 (\Delta_{21}) \\ - \cos^2 \theta_{12} \sin^2 2\theta_{13} \sin^2 (\Delta_{31}) \\ - \sin^2 \theta_{12} \sin^2 2\theta_{13} \sin^2 (\Delta_{32})$$

3 frequencies:

# Neutrinoless Double Beta Decay

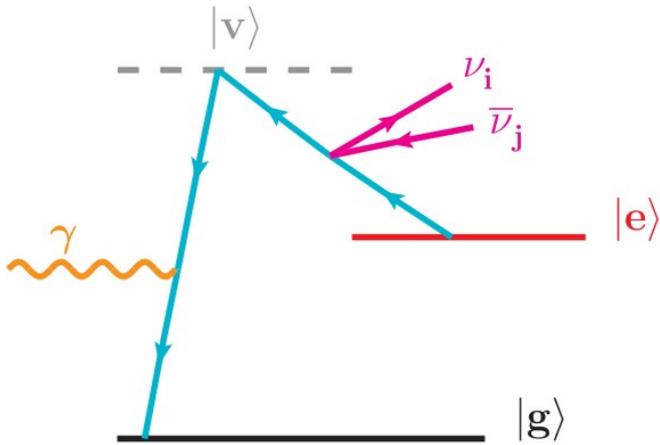


$$\langle m \rangle_{ee} \equiv \left| \sum_i m_i U_{ei}^2 \right| = \left| c_s^2 c_r^2 m_1 e^{i\delta_{M1}} + s_s^2 c_r^2 m_2 + s_r^2 m_3 e^{i\delta_{M3}} \right|$$



SFG & Manfred Lindner, PRD 95 (2017) No.3, 033003 [arXiv:1608.01618]

# Radiative Emission of $\nu$ Pairs

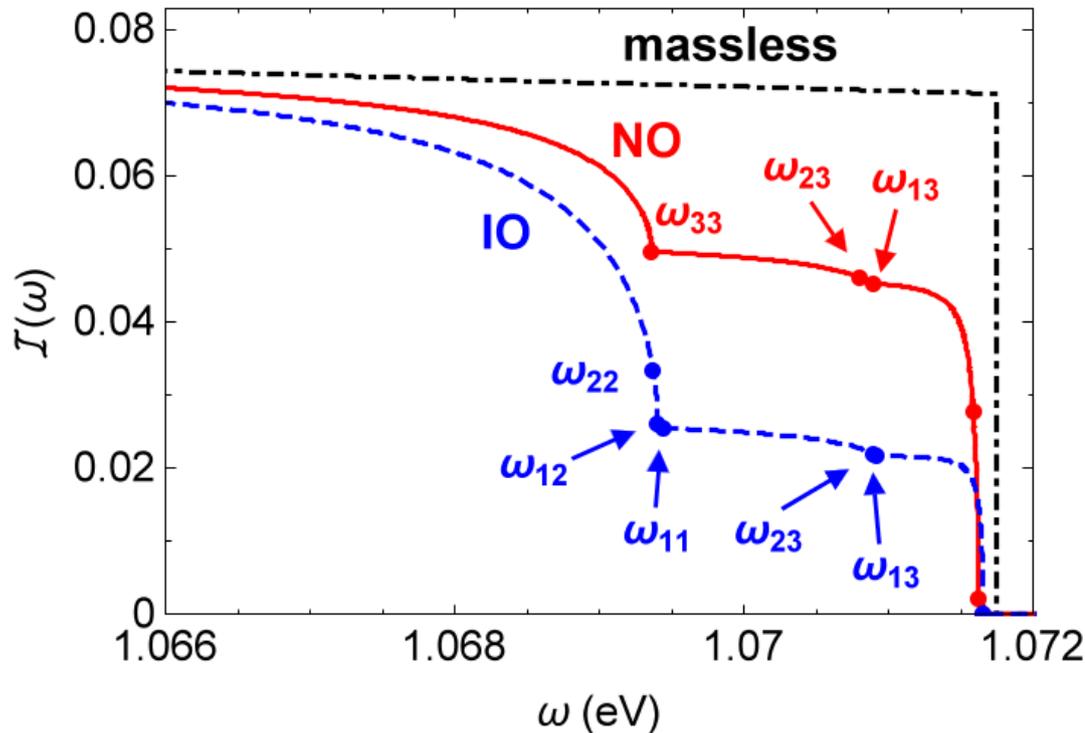


$$|e\rangle \rightarrow |v\rangle + \nu\bar{\nu}$$

$$E1 \times M1$$

M. Yoshimura, Phys. Rev. D 75, 113007 (2007)

Jue Zhang & Shun Zhou, Phys.Rev.D 93 (2016) 11, 113020



$$\omega_{ij}^{\max} \equiv \frac{E_e - E_g}{2} - \frac{1}{2} \frac{(m_i + m_j)^2}{(E_e - E_g)}$$

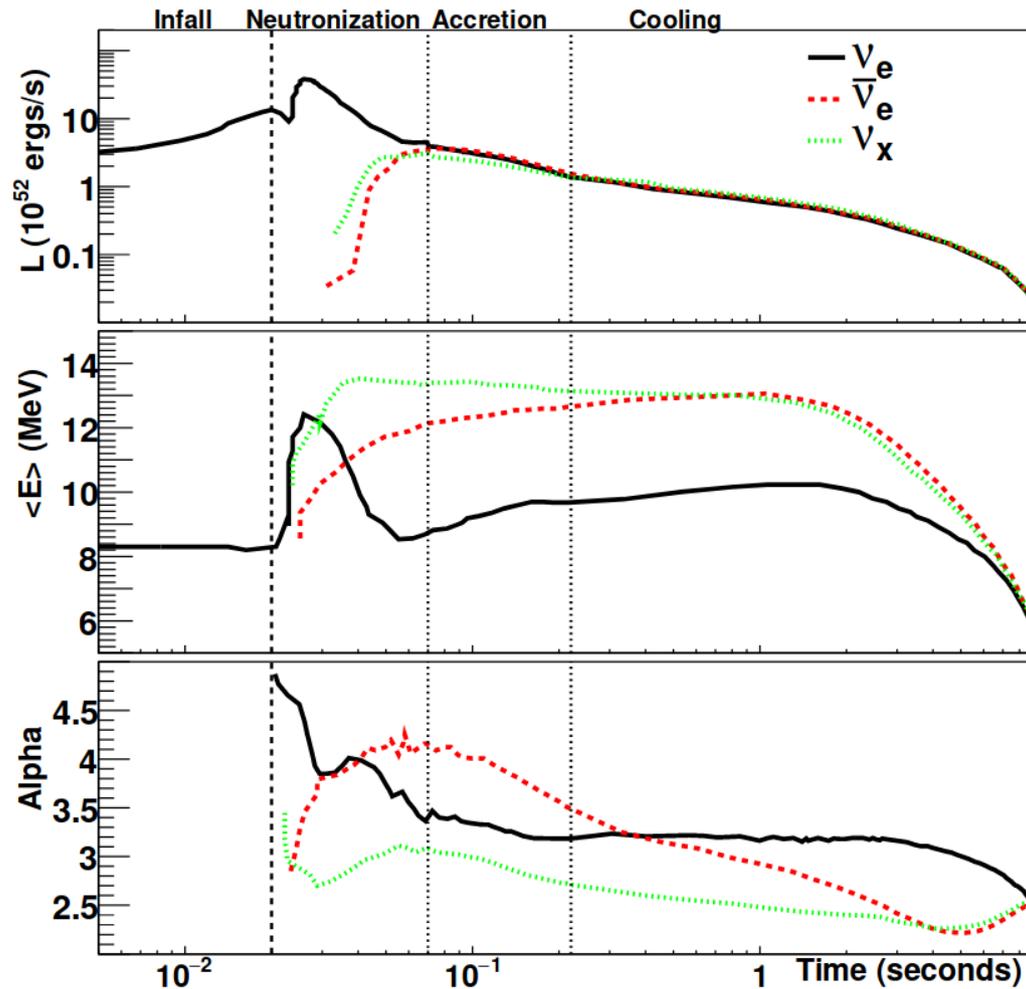
SFG & Pasquini

Eur.Phys.J.C 82 (2022) 3, 208;

Phys.Lett.B 841 (2023) 137911;

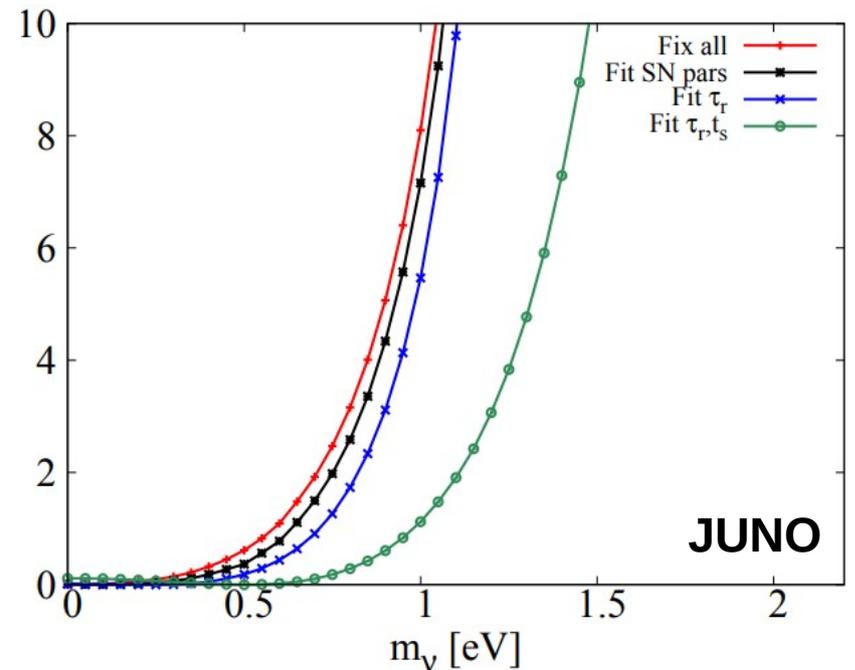
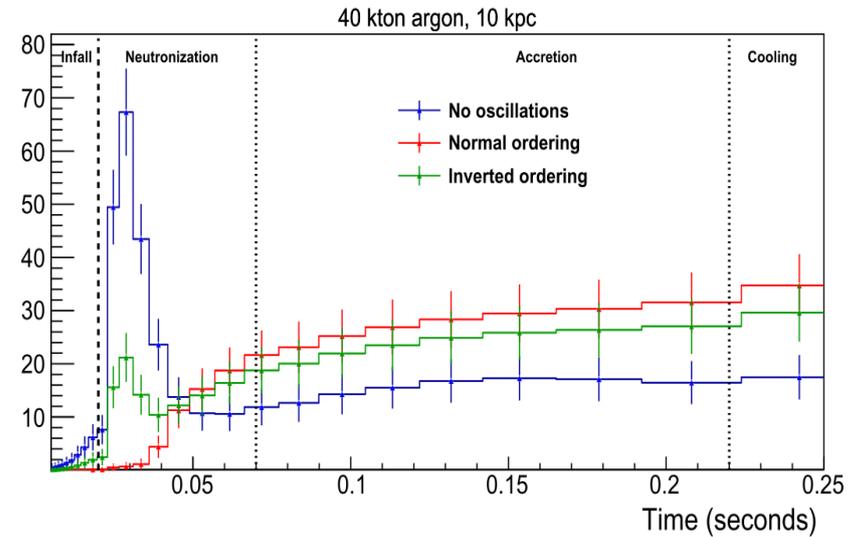
JHEP 12 (2023) 083

# Time Delay in Supernova $\nu$ 's



DUNE, 2008.06647

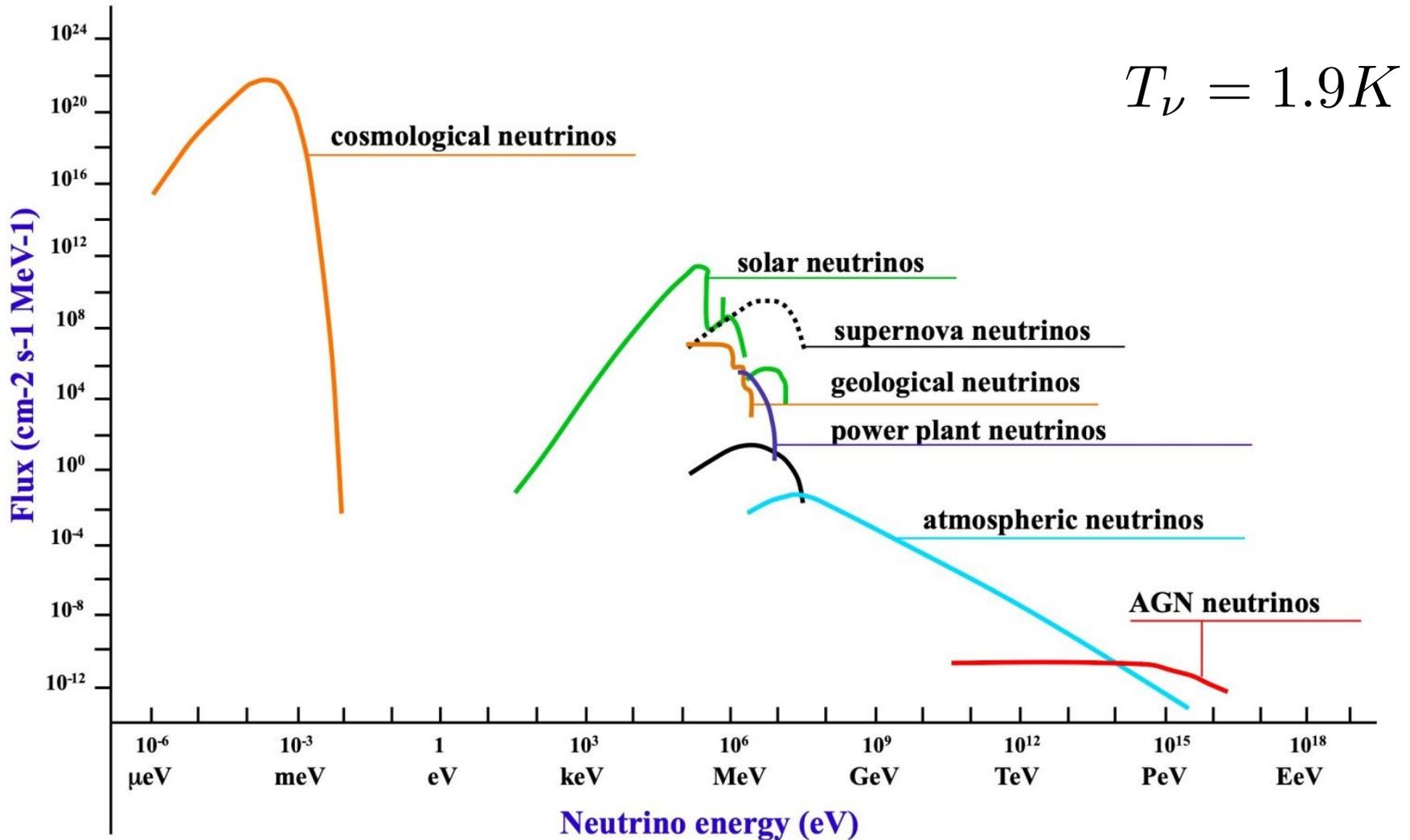
SFG, Chui-Fan Kong, Alexei Smirnov,  
accepted by PRL [arXiv:2404.17352]



JUNO

Lu, Cao, Li & Zhou [JCAP 05 (2015) 044]

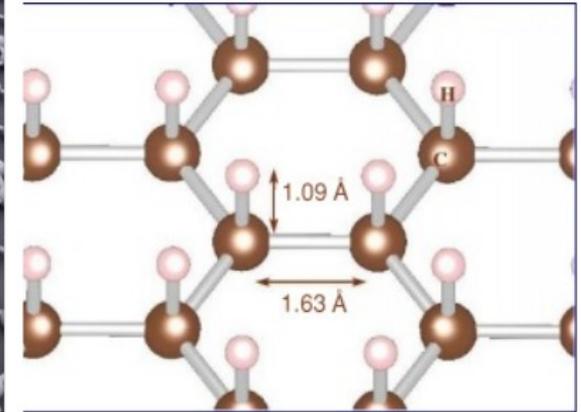
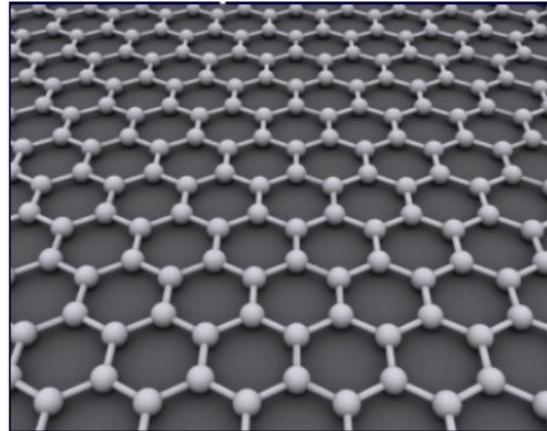
# Cosmic $\nu$ Background



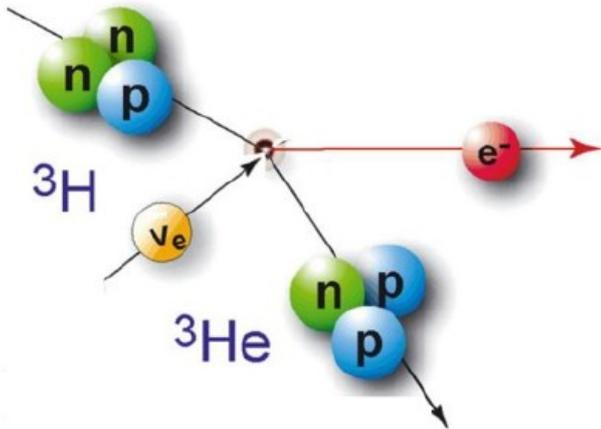
# PTOLEMY Experiment



P on-  
T ecorvo  
O bservatory for  
L ight,  
E arly-universe,  
M assive-neutrino  
Y ield

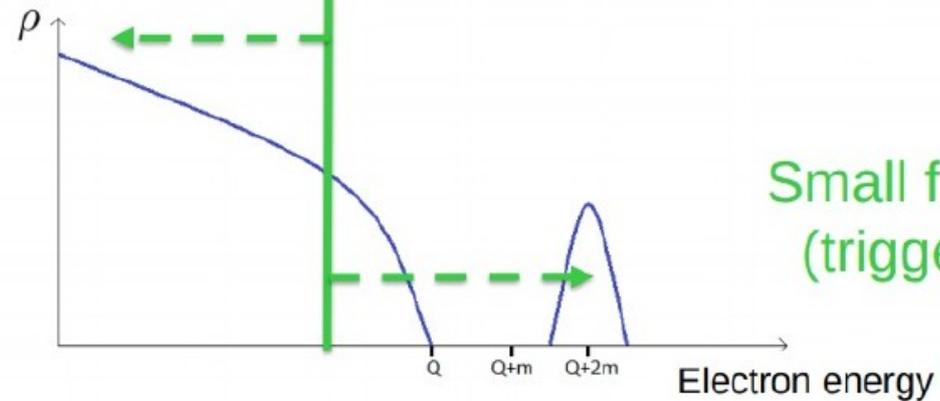


## Graphene Substrate



Too much rate  
(need to filter)

Need very high energy  
resolution ( $\sigma \sim m_\nu$ )



Small fraction  
(triggering)

SFG & Pasquini, Phys.Lett.B 811 (2020) 135961