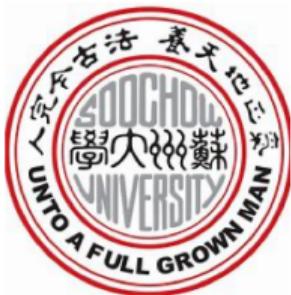


The (semi-)leptonic decays of charmed mesons at BESIII

潘祥

苏州大学



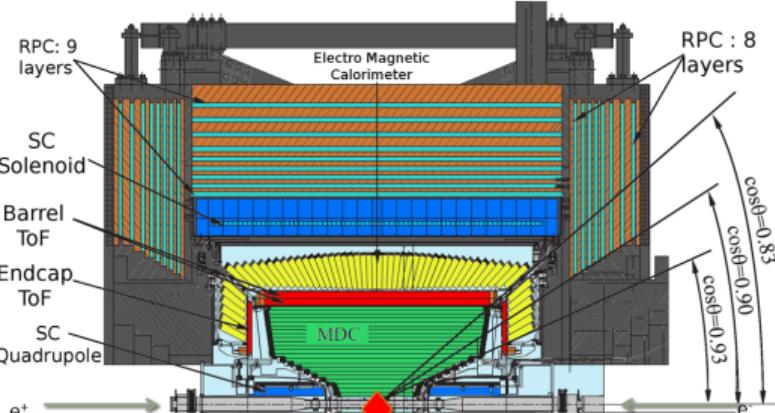
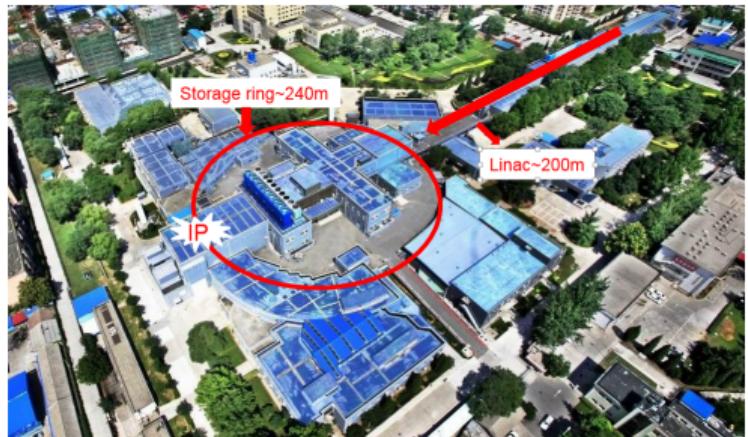
中国物理学会高能物理分会
第十四届全国粒子物理学术会议
山东大学
2024 年 8 月 14 日



Outline

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- 2 Main goal
- 3 BESIII dataset and double-tag method
- 4 Leptonic decays
- 5 Semileptonic decays
- 6 Summary and prospect

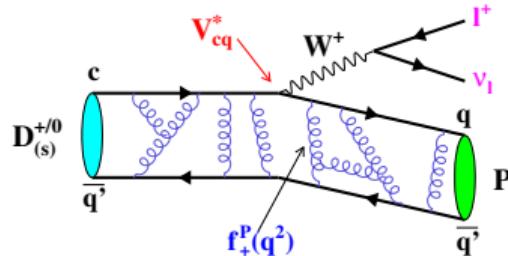
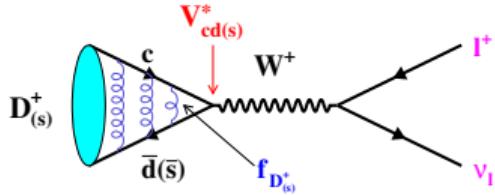
BESIII experiment



- $\sqrt{s} = (1.85 - 4.95) \text{ GeV}$
- Peak luminosity: $1.1 \times 10^{33} \text{ cm}^{-2}\text{s}^{-1}$ @ 3.773 GeV
- MDC: $\sigma_P/P = 0.5\%$ @ 1 GeV; $\sigma_{dE/dx} = 6\%$

- TOF: $\sigma_T = 68(110) \text{ ps}$ for barrel (endcap); endcap upgraded in 2015 $\sigma_T = 60 \text{ ps}$
- EMC: $\sigma_E/E = 2.5\%(5\%)$ for barrel (endcap)

Main goal



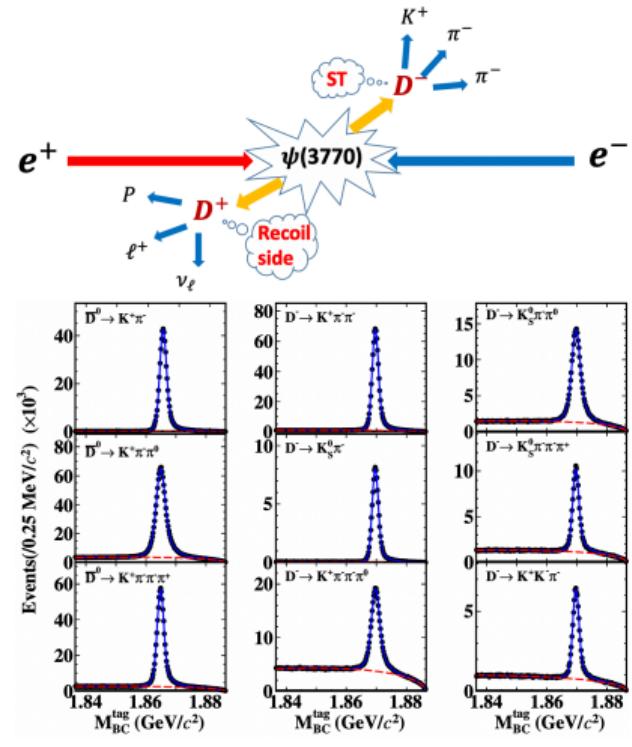
$$\Gamma = \frac{G_F^2}{8\pi} |V_{cq}|^2 |f_{D_{(s)}^+}|^2 m_\ell^2 m_{D_{(s)}^+} \left(1 - \frac{m_\ell^2}{m_{D_{(s)}^+}^2}\right)^2$$

$$\frac{d\Gamma}{dq^2} = X \frac{G_F^2 |\vec{p}_P|^3}{24\pi^3} |V_{cq}|^2 |f_+(q^2)|^2$$

- Leptonic and semileptonic D decays are the most important way to determine $|V_{cd(s)}|$
- Latest LQCD: $f_{D_s^+} = 249.9(05)$ MeV ($\sigma = 0.2\%$), $f_{D^+} = 212.1(07)$ MeV ($\sigma = 0.3\%$), $f_+^{D \rightarrow K}(0) = 0.7452(31)$ ($\sigma = 2.4\% \rightarrow 0.4\%$), $f_+^{D \rightarrow \pi}(0) = 0.6300(51)$ ($\sigma = 4.4\% \rightarrow 0.8\%$)
- Decay constant $f_{D_{(s)}^+}$ and FF $f_+(0)$ measurements \Rightarrow Calibrate LQCD calculations
- BF ratios \Rightarrow Test lepton flavor universality (LFU)

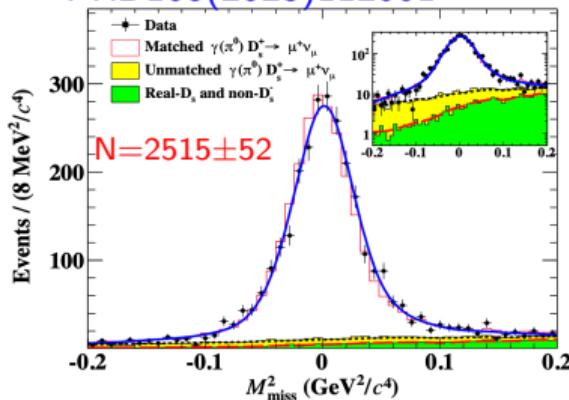
BESIII dataset and double-tag method

- $D^0(+)$ meson: $e^+e^- \rightarrow \psi(3770) \rightarrow D\bar{D}$ @3.773 GeV
 $\mathcal{L}_{\text{int}} = (2.932 + 4.995 + 8.157 + 4.191) \text{ fb}^{-1} = 20.27 \text{ fb}^{-1}$
- D_s^+ meson:
 $e^+e^- \rightarrow D_s^\pm D_s^{*\mp}$ @4.128-4.226 GeV, $\mathcal{L}_{\text{int}} = 7.33 \text{ fb}^{-1}$
 $e^+e^- \rightarrow D_s^{*+} D_s^{*-}$ @4.237-4.669 GeV, $\mathcal{L}_{\text{int}} = 10.64 \text{ fb}^{-1}$
- Advantages: Clean, double tag method
- Single-tag yields in data:
 • 2.93 fb^{-1} (**7.9 fb⁻¹**) (**20.27 fb⁻¹**) data
 $N_{\text{ST}}^{\bar{D}^0} \sim 2.4\text{M}$ (**6.6M**) (**16.9M**) with 3 golden tags
 $N_{\text{ST}}^{D^-} \sim 1.6\text{M}$ (**4.3M**) (**11.0M**) with 6 golden tags
- 7.33 fb^{-1} (**10.64 fb⁻¹**) data
 $N_{\text{ST}}^{D_s^-} \sim 0.8\text{M}$ (**0.12M**) with 16 possible tags



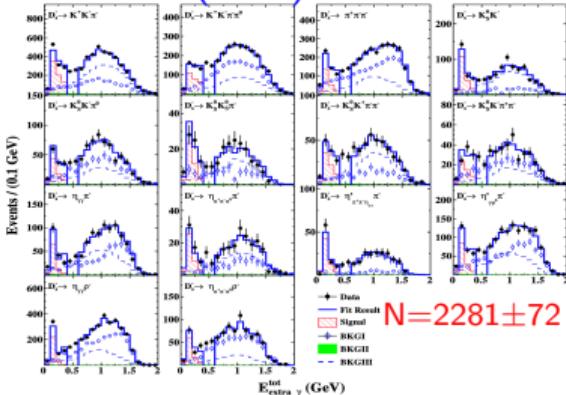
$D_s^+ \rightarrow \mu^+ \nu_\mu$ and $D_s^+ \rightarrow \tau^+ \nu_\tau$ via $e^+ e^- \rightarrow D_s^\pm D_s^{*\mp}$

7.33 fb⁻¹ @ 4.128-4.226 GeV
PRD108(2023)112001



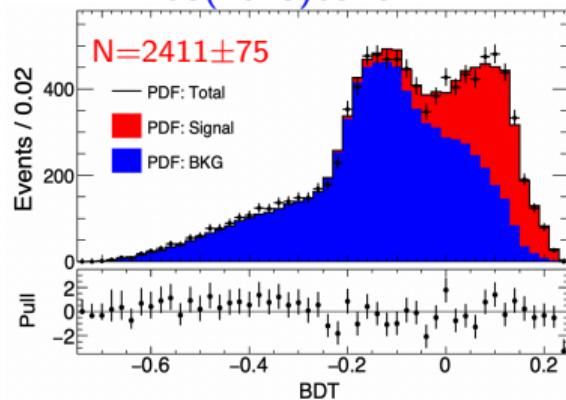
- $\mathcal{B}(D_s^+ \rightarrow \mu^+ \nu_\mu) = (5.294 \pm 0.108 \pm 0.085) \times 10^{-3}$
- $f_{D_s^+} = (248.4 \pm 2.5 \pm 2.2)$ MeV
- $|V_{cs}| = 0.968 \pm 0.010 \pm 0.009$
Highest precision to date
 $\sim 1.4\%$

$D_s^+ \rightarrow \tau^+ \nu_\tau, \tau^+ \rightarrow \mu^+ \nu_\mu \bar{\nu}_\tau$
JHEP09(2023)124



- $\mathcal{B}(D_s^+ \rightarrow \tau^+ \nu_\tau) = (5.37 \pm 0.17 \pm 0.15)\%$
- $f_{D_s^+} = (253.4 \pm 4.0 \pm 3.7)$ MeV
- $|V_{cs}| = 0.987 \pm 0.016 \pm 0.014$
Precision $\sim 2.2\%$

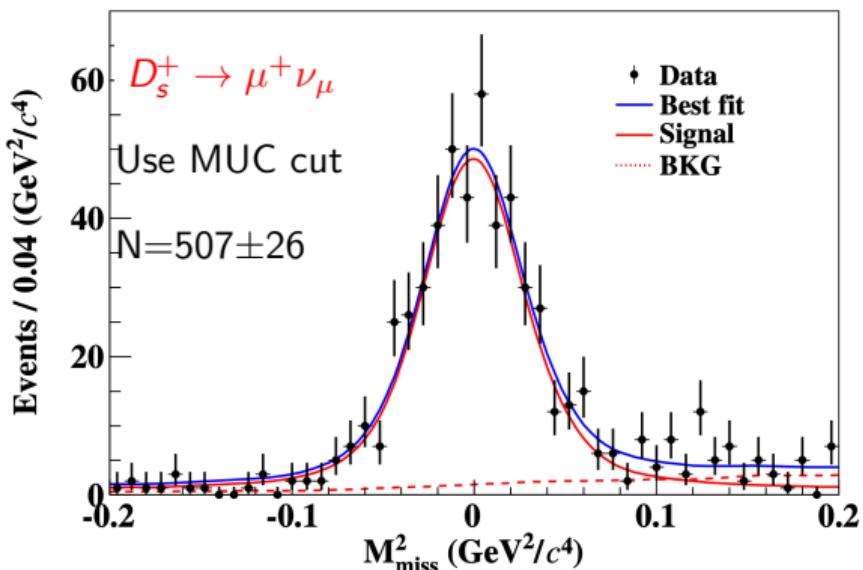
$D_s^+ \rightarrow \tau^+ \nu_\tau, \tau^+ \rightarrow \pi^+ \bar{\nu}_\tau$
PRD108(2023)092014



- Boosted decision tree method
- $\mathcal{B}(D_s^+ \rightarrow \tau^+ \nu_\tau) = (5.44 \pm 0.17 \pm 0.13)\%$
- $f_{D_s^+} = (255.0 \pm 4.0 \pm 3.4)$ MeV
- $|V_{cs}| = 0.993 \pm 0.015 \pm 0.013$
Precision $\sim 2.0\%$

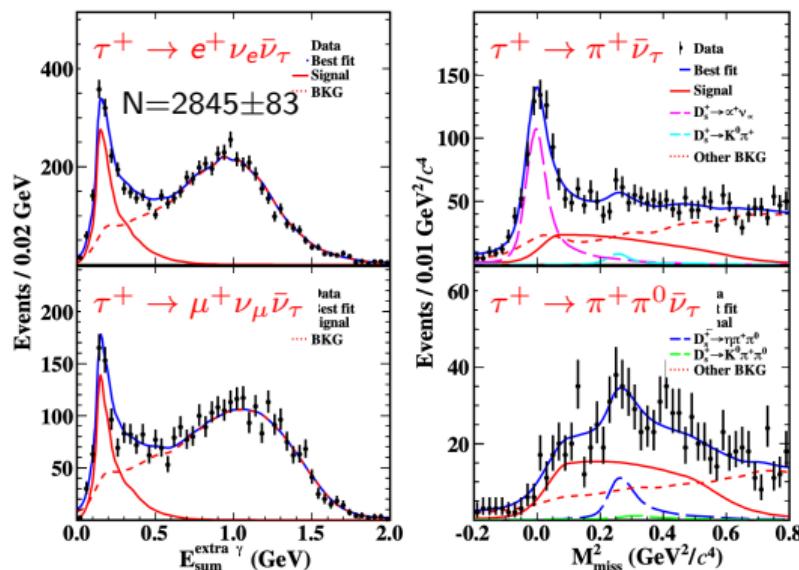
$D_s^+ \rightarrow \mu^+ \nu_\mu$ and $D_s^+ \rightarrow \tau^+ \nu_\tau$ via $e^+ e^- \rightarrow D_s^{*+} D_s^{*-}$

10.64 fb^{-1} @ 4.237-4.669 GeV arXiv:2407.11727



- $\mathcal{B}(D_s^+ \rightarrow \mu^+ \nu_\mu) = (0.547 \pm 0.026 \pm 0.016)\%$
- $\mathcal{B}(D_s^+ \rightarrow \tau^+ \nu_\tau) = (5.60 \pm 0.16 \pm 0.20)\%$
- $\mathcal{R}(\tau/\mu) = 10.24 \pm 0.57$ (SM: 9.75 ± 0.01)

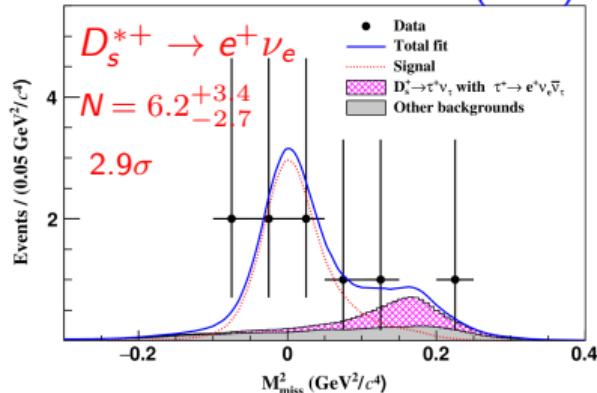
$D_s^+ \rightarrow \tau^+ \nu_\tau$, constrain the same BF



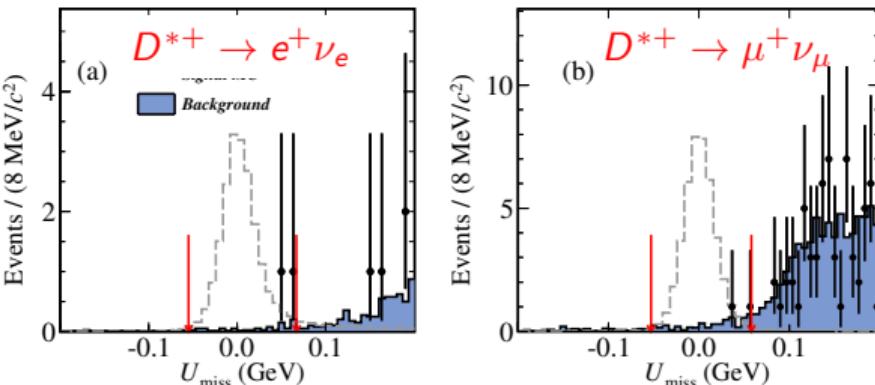
- $f_{D_s}|V_{\text{cs}}|_{\mu \nu_\mu} = (246.5 \pm 5.9 \pm 3.6) \text{ MeV} (\sim 2.8\%)$
- $f_{D_s}|V_{\text{cs}}|_{\tau \nu_\tau} = (252.7 \pm 3.6 \pm 4.5) \text{ MeV} (\sim 2.3\%)$

$D_s^{*+} \rightarrow e^+ \nu_e$ and $D^{*+} \rightarrow \ell^+ \nu_\ell$

7.33 fb $^{-1}$ @4.128-4.226 GeV PRL131(2023)141802



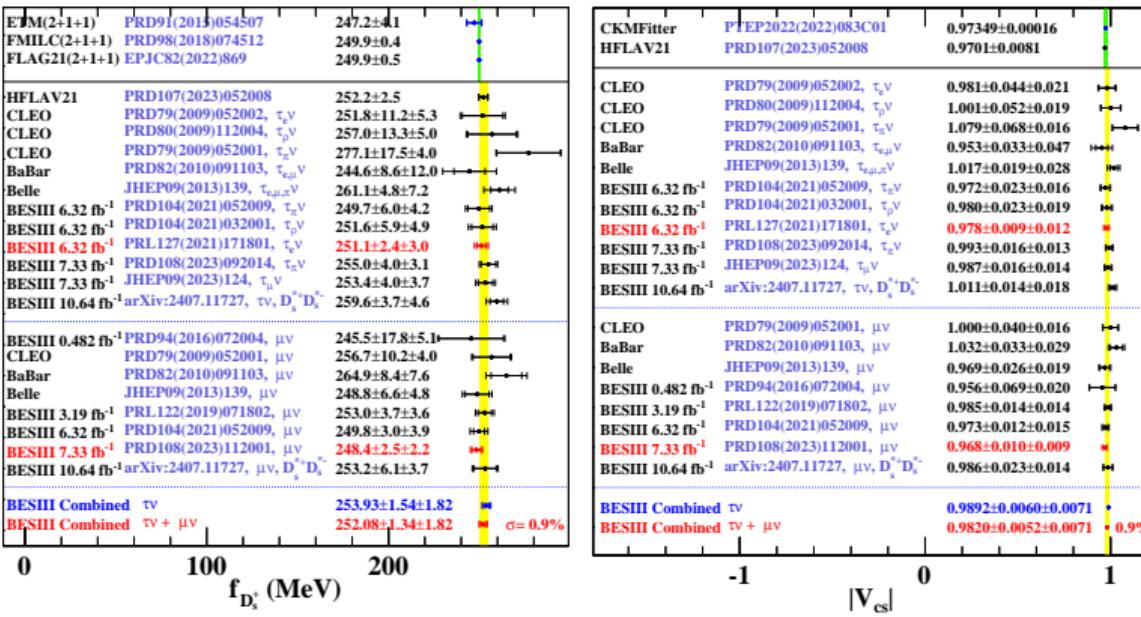
6.32 fb $^{-1}$ @4.178-4.226 GeV PRD110(2024)012003



- First experimental study of the $D_{(s)}^{*+}$ purely leptonic decay
- $\mathcal{B}(D_s^{*+} \rightarrow e^+ \nu_e) = (2.1^{+1.2}_{-0.9} \pm 0.2) \times 10^{-5}$
- $\Gamma_{D_s^{*+}}^{\text{total}} = 70 \pm 28 \text{ eV}$ (LQCD) $\Rightarrow f_{D_s^{*+}} = (214^{+61}_{-46} \pm 44) \text{ MeV}$
- $f_{D_s^{*+}}/f_{D_s^+} = 1.12 \pm 0.01$ (LQCD) $\Rightarrow \Gamma_{D_s^{*+}}^{\text{total}} = (122^{+70}_{-52} \pm 12) \text{ eV}$
- Indirectly constrains the upper limit on the $\Gamma_{D_s^{*+}}^{\text{total}}$ from the MeV ($< 1.9 \text{ MeV}$ @ 90% C.L. PDG2024) to sub-keV level

- Upper limits are set at 90% C. L.
- $\mathcal{B}(D^{*+} \rightarrow e^+ \nu_e) < 1.1 \times 10^{-5}$
- $\mathcal{B}(D^{*+} \rightarrow \mu^+ \nu_\mu) < 4.3 \times 10^{-6}$

Summary of leptonic D_s decays

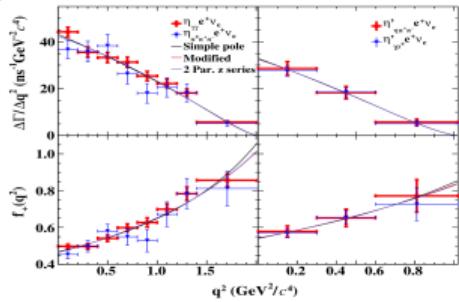


- Averaged BESIII results, precisions of f_{D_s} and $|V_{cs}|$: 0.9%
- $\mathcal{B}(D_s^+ \rightarrow \mu^+ \nu_\mu) = (0.5310 \pm 0.0099 \pm 0.0053)\%$ and $\mathcal{B}(D_s^+ \rightarrow \tau^+ \nu_\tau) = (5.359 \pm 0.067 \pm 0.074)\%$
- $\mathcal{R}(\tau/\mu) = 10.09 \pm 0.28$ ($\sigma \sim 2.8\%$), consistent within SM (9.75 ± 0.01) 1.2σ

$D_s^+ \rightarrow \eta^{(\prime)} e^+ \nu_e$ and $D_s^+ \rightarrow \eta^{(\prime)} \mu^+ \nu_\mu$

Data: 7.33 fb^{-1} @ 4.128-4.226 GeV

$D_s^+ \rightarrow \eta^{(\prime)} e^+ \nu_e$ PRD108(2023)092003



- Precision of BFs and FFs are improved by a factor of ~ 1.4

$$\mathcal{B}(D_s^+ \rightarrow \eta e^+ \nu_e) = (2.255 \pm 0.039 \pm 0.051)\%$$

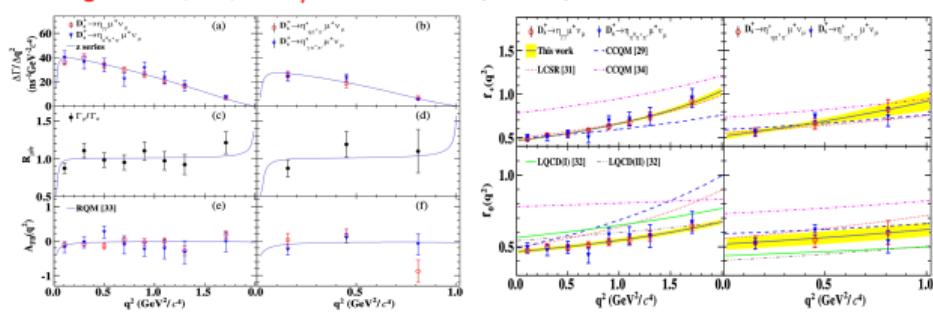
$$\mathcal{B}(D_s^+ \rightarrow \eta' e^+ \nu_e) = (0.810 \pm 0.038 \pm 0.024)\%$$

$$f_+^\eta(0) = 0.4642 \pm 0.0073 \pm 0.0066$$

$$f_+^{\eta'}(0) = 0.540 \pm 0.025 \pm 0.009$$

$$\eta - \eta' \text{ mixing angle } \phi_P = (40.0 \pm 2.0 \pm 0.6)^\circ$$

$D_s^+ \rightarrow \eta^{(\prime)} \mu^+ \nu_\mu$ PRL132(2024)091802



- Precision of BFs are improved by a factor of ~ 6

$$\mathcal{B}(D_s^+ \rightarrow \eta \mu^+ \nu_\mu) = (2.235 \pm 0.051 \pm 0.052)\%$$

$$\mathcal{B}(D_s^+ \rightarrow \eta' \mu^+ \nu_\mu) = (0.801 \pm 0.055 \pm 0.028)\%$$
- First extraction of the FFs via semimuonic decays

$$f_+^\eta(0) = 0.465 \pm 0.010 \pm 0.007; f_+^{\eta'}(0) = 0.518 \pm 0.038 \pm 0.012$$
- Most precision test of lepton flavor universality in D_s sector

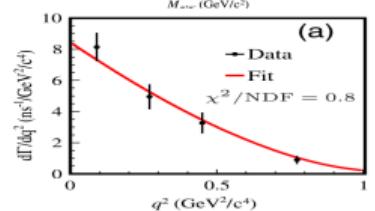
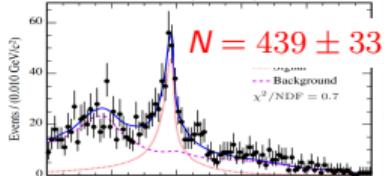
$$\mathcal{R}_{\mu/e}^\eta = 0.991 \pm 0.029 \pm 0.016; \mathcal{R}_{\mu/e}^{\eta'} = 0.988 \pm 0.082 \pm 0.031$$
- First extraction of the forward-backward asymmetry parameters

$$\langle A_{FB}^\eta \rangle = -0.059 \pm 0.031 \pm 0.005; \langle A_{FB}^{\eta'} \rangle = -0.064 \pm 0.079 \pm 0.006$$

$D_s^+ \rightarrow \pi^+ \pi^- e^+ \nu_e$ and $D^+ \rightarrow \pi^+ \pi^- \ell^+ \nu_\ell$

7.33 fb⁻¹ @ 4.128-4.226 GeV PRL132(2024)141901

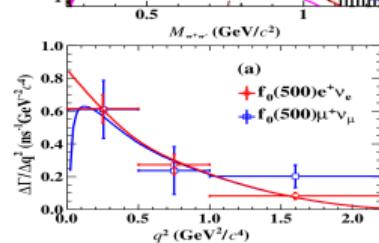
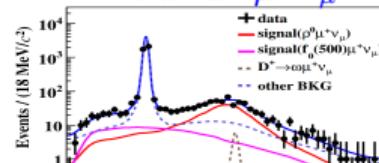
$D_s^+ \rightarrow f_0(980)^0 e^+ \nu_e$



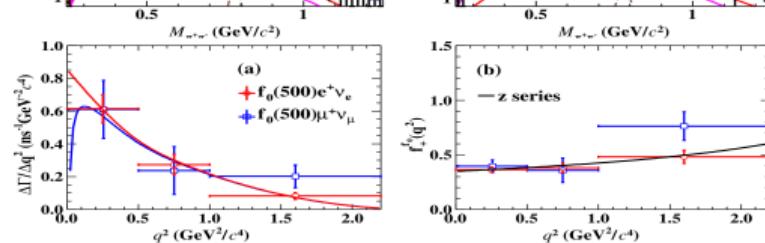
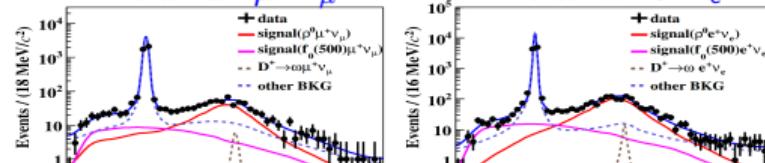
- $\mathcal{B}(D_s^+ \rightarrow f_0(980)_{\pi^+ \pi^-} e^+ \nu_e) = (1.72 \pm 0.13 \pm 0.10) \times 10^{-3} = 4.22 \times 10^{-3} \cos^2 \phi$
- $q\bar{q}$ mixing angle: $\sin \phi (1/\sqrt{2})(u\bar{u} + d\bar{d}) + \cos \phi s\bar{s}$
 $\phi = (19.7 \pm 12.8)^\circ \Rightarrow \text{s}\bar{s} \text{ component dominates}$
- $f_+^{D_s^+ \rightarrow f_0(980)}(0) = 0.518 \pm 0.018 \pm 0.036$
- $\mathcal{B}(D_s^+ \rightarrow f_0(500)_{\pi^+ \pi^-} e^+ \nu_e) < 3.3 \times 10^{-4} @ 90\% \text{ C. L.}$

2.93 fb⁻¹ @ 3.773 GeV arXiv:2401.13225

$D^+ \rightarrow \pi^+ \pi^- \mu^+ \nu_\mu$



$D^+ \rightarrow \pi^+ \pi^- e^+ \nu_e$

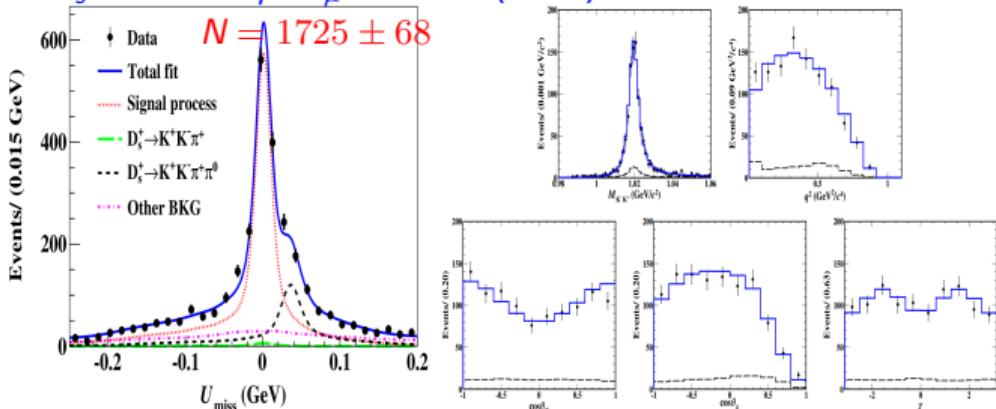


- $\mathcal{B}_{D^+ \rightarrow f_0(500)\pi^+\pi^-\mu^+\nu_\mu} = (0.72 \pm 0.13 \pm 0.10) \times 10^{-3}$
 \Rightarrow closer to tetraquark assumption
- $\mathcal{B}_{D^+ \rightarrow \rho^0\pi^+\pi^-\mu^+\nu_\mu} = (1.64 \pm 0.13 \pm 0.11) \times 10^{-3}$
- $f_+^{D^+ \rightarrow f_0(500)}(0) = 0.350 \pm 0.027 \pm 0.015$
- $\mathcal{R}_{\mu/e}^{\rho^0} = 0.88 \pm 0.10$ (SM ~ 0.96),
 $\mathcal{R}_{\mu/e}^{f_0(500)} = 1.14 \pm 0.28$ (SM ~ 0.90)

$D_s^+ \rightarrow K^+ K^- \mu^+ \nu_\mu$ and $D \rightarrow K \bar{K} e^+ \nu_e$

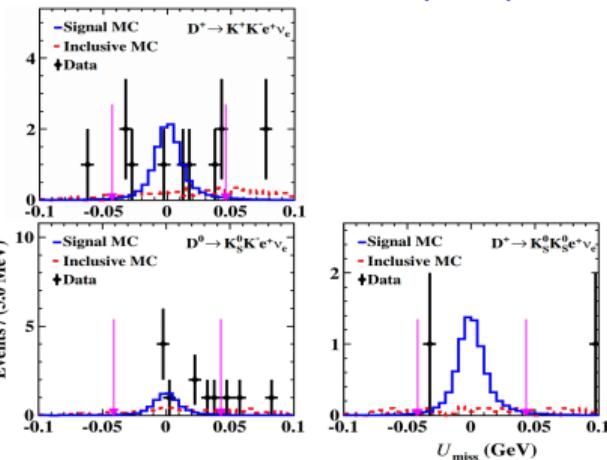
7.33 fb^{-1} @ 4.128-4.226 GeV

$D_s^+ \rightarrow K^+ K^- \mu^+ \nu_\mu$ JHEP12(2023)072



- $\mathcal{B}(D_s^+ \rightarrow \phi \mu^+ \nu_\mu) = (2.25 \pm 0.09 \pm 0.07)\%$, precision improved by 4.3
- Assume S-wave is $f_0(980)$:
 $\mathcal{B}(D_s^+ \rightarrow f_0(980) \mu^+ \nu_\mu, f_0(980) \rightarrow K^+ K^-) < 5.45 \times 10^{-4}$ @ 90% C. L.
- $\mathcal{R}_{\mu/e}^\phi = 0.94 \pm 0.08$
- $r_V = \frac{V(0)}{A_1(0)} = 1.58 \pm 0.17 \pm 0.02$, $r_2 = \frac{A_2(0)}{A_1(0)} = 0.71 \pm 0.14 \pm 0.02$

7.9 fb^{-1} @ 3.773 GeV PRD109(2024)072003

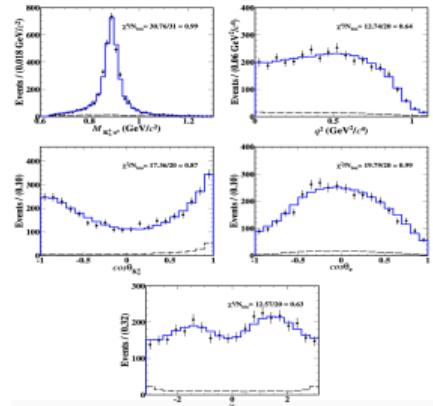
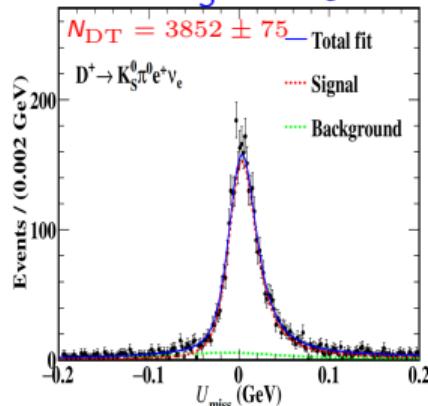


- Explore $a_0(980) \rightarrow K \bar{K}$, $D \rightarrow a_0(980) K \bar{K} e^+ \nu_e$ is expected within $(1 \sim 3) \times 10^{-5}$
- Upper limits are set at 90% C. L.
- $\mathcal{B}(D^0 \rightarrow K_S^0 K^- e^+ \nu_e) < 2.13 \times 10^{-5}$
- $\mathcal{B}(D^+ \rightarrow K_S^0 K_S^- e^+ \nu_e) < 1.54 \times 10^{-5}$
- $\mathcal{B}(D^+ \rightarrow K^+ K^- e^+ \nu_e) < 2.10 \times 10^{-5}$

$D^+ \rightarrow K_S^0 \pi^0 e^+ \nu_e$ and $D^0 \rightarrow K^- \pi^0 \mu^+ \nu_\mu$

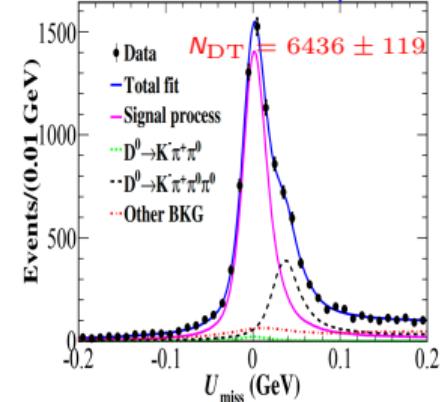
7.9 fb⁻¹ @ 3.773 GeV

$D^+ \rightarrow K_S^0 \pi^0 e^+ \nu_e$ arXiv:2408.04422



- $\mathcal{B}(D^+ \rightarrow K_S^0 \pi^0 e^+ \nu_e) = (0.881 \pm 0.017 \pm 0.016)\%$
- $\mathcal{B}(D^+ \rightarrow \bar{K}^*(892)^0 e^+ \nu_e) = (4.97 \pm 0.11 \pm 0.12)\%$
- $r_V = \frac{V(0)}{A_1(0)} = 1.43 \pm 0.07 \pm 0.03$
- $r_2 = \frac{A_2(0)}{A_1(0)} = 0.72 \pm 0.06 \pm 0.02$

$D^0 \rightarrow K^- \pi^0 \mu^+ \nu_\mu$ arXiv:2403.10877

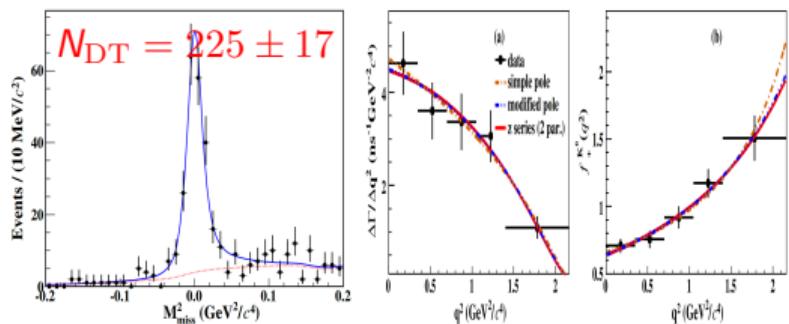


- Precision of BF is improved by a factor of 5
 - $\mathcal{B}(D^0 \rightarrow K^- \pi^0 \mu^+ \nu_\mu) = (0.729 \pm 0.014 \pm 0.011)\%$
 - $\mathcal{B}(D^0 \rightarrow K^*(892)^- \mu^+ \nu_\mu) = (2.062 \pm 0.039 \pm 0.032)\%$
- $r_V = \frac{V(0)}{A_1(0)} = 1.37 \pm 0.09 \pm 0.03$
- $r_2 = \frac{A_2(0)}{A_1(0)} = 0.76 \pm 0.06 \pm 0.02$
- $\frac{\mathcal{B}(D^0 \rightarrow K^*(892)^- \mu^+ \nu_\mu)}{\mathcal{B}(D^0 \rightarrow K^*(892)^- e^+ \nu_e)} = 0.96 \pm 0.08$, agree with LFU

$D_s^+ \rightarrow K^0 e^+ \nu_e$ and $D_s^+ \rightarrow h e^+ \nu_e$

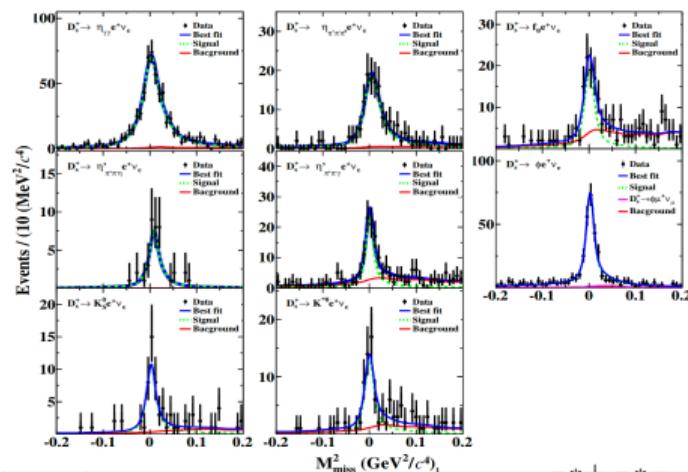
7.33 fb $^{-1}$ @ 4.128-4.226 GeV

$D_s^+ \rightarrow K^0 e^+ \nu_e$ arXiv:2406.19190



- Precision of BF is improved by a factor of 1.6
 $\mathcal{B}(D_s^+ \rightarrow K^0 e^+ \nu_e) = (2.93 \pm 0.23 \pm 0.12) \times 10^{-3}$
- Precision of FF is improved by a factor of 1.7
 $f_+^{K^0}(0) = 0.636 \pm 0.049 \pm 0.013$

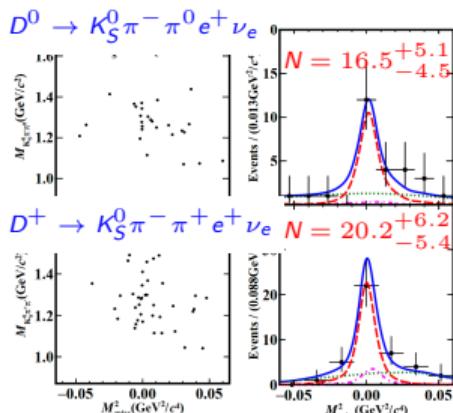
10.64 fb $^{-1}$ @ 4.237-4.699 GeV arXiv:2406.01332



- Independent measurements via $e^+ e^- \rightarrow D_s^{*+} D_s^{*-}$
 $\mathcal{B}(D_s^+ \rightarrow \eta e^+ \nu_e) = (2.35 \pm 0.11 \pm 0.10)\%$
 $\mathcal{B}(D_s^+ \rightarrow \eta' e^+ \nu_e) = (0.82 \pm 0.09 \pm 0.02)\%$
 $\mathcal{B}(D_s^+ \rightarrow \phi e^+ \nu_e) = (2.21 \pm 0.16 \pm 0.11)\%$
 $\mathcal{B}(D_s^+ \rightarrow f_0(980)|_{\pi^+\pi^-} e^+ \nu_e) = (0.15 \pm 0.02 \pm 0.01)\%$
 $\mathcal{B}(D_s^+ \rightarrow K^0 e^+ \nu_e) = (0.24 \pm 0.04 \pm 0.01)\%$
 $\mathcal{B}(D_s^+ \rightarrow K^{*0} e^+ \nu_e) = (0.19 \pm 0.03 \pm 0.01)\%$

$D_{(s)} \rightarrow K_1(1270)e^+\nu_e$ and $D_{(s)} \rightarrow b_1(1235)e^+\nu_e$

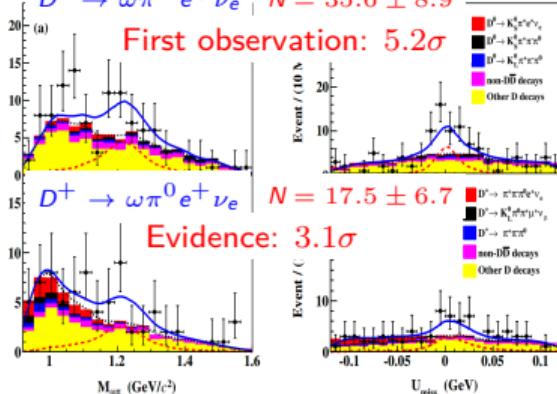
2.93 fb⁻¹ @ 3.773 GeV arXiv:2403.19091



7.9 fb⁻¹ @ 3.773 GeV arXiv:2407.20551

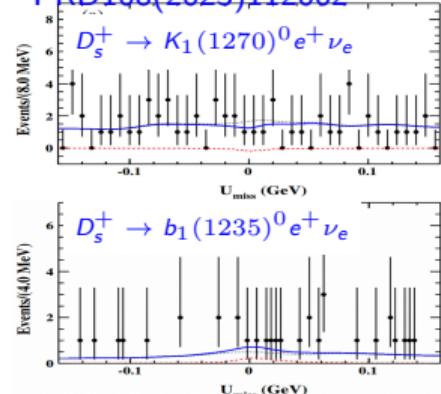
$D^0 \rightarrow \omega\pi^- e^+\nu_e$, $N = 35.6 \pm 8.9$

First observation: 5.2 σ



7.33 fb⁻¹ @ 4.128-4.226 GeV

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- Dominated by $K_1(1270)$
- $\mathcal{B}(D^0 \rightarrow K_1(1270)^- e^+\nu_e) = (1.05^{+0.33}_{-0.28} \pm 0.17) \times 10^{-3}$
- $\mathcal{B}(D^+ \rightarrow \bar{K}_1(1270)^0 e^+\nu_e) = (1.29^{+0.40}_{-0.35} \pm 0.23) \times 10^{-3}$

- $\mathcal{B}(D^0 \rightarrow b_1(1235)^- |_{\omega\pi^-} e^+\nu_e) = (0.72 \pm 0.18^{+0.06}_{-0.08}) \times 10^{-4}$
- $\mathcal{B}(D^+ \rightarrow b_1(1235)^0 |_{\omega\pi^0} e^+\nu_e) = (1.16 \pm 0.44 \pm 0.16) \times 10^{-4}$
- $\frac{\Gamma(D^0 \rightarrow b_1^- e^+\nu_e)}{2\Gamma(D^+ \rightarrow b_1^0 e^+\nu_e)} = 0.78 \pm 0.19 \pm 0.05$, consistent with isospin

- Upper limits are set at 90% C. L.
- $\mathcal{B}(D_s^+ \rightarrow b_1(1235)^0 |_{\omega\pi^0} e^+\nu_e) < 6.4 \times 10^{-4}$
- $\mathcal{B}(D_s^+ \rightarrow K_1(1270)^0 e^+\nu_e) < 4.1 \times 10^{-4}$

Summary and prospect

Channel	Current precision (%)			Expected precision (%)		
	$f_{D_s^+}$	$ V_{cs} $	$\mathcal{R}(\tau/\mu)$	$f_{D_s^+}$	$ V_{cs} $	$\mathcal{R}(\tau/\mu)$
$D_s^+ \rightarrow \mu^+ \nu_\mu$	1.09	1.09	2.8	0.97	0.97	2.5
$D_s^+ \rightarrow \tau^+ \nu_\tau$	0.94	0.94		0.88	0.88	
Channel	Form factor	$ V_{cs} $	$\mathcal{R}(\mu/e)$	Form factor	$ V_{cs} $	$\mathcal{R}(\mu/e)$
$D^0 \rightarrow K^- e^+ \nu_e$	0.60	0.73	1.42	0.50	0.66	1.26
$D^0 \rightarrow K^- \mu^+ \nu_\mu$	0.66	0.79		0.45	0.63	
$D_s^+ \rightarrow \eta e^+ \nu_e$	2.1	6.4	3.3	1.9	6.3	2.9
$D_s^+ \rightarrow \eta \mu^+ \nu_\mu$	2.6	6.6		2.4	6.5	
Channel	f_{D^+}	$ V_{cd} $	$\mathcal{R}(\tau/\mu)$	f_{D^+}	$ V_{cd} $	$\mathcal{R}(\tau/\mu)$
$D^+ \rightarrow \mu^+ \nu_\mu$	2.8	2.8	24	1.3	1.3	15
$D^+ \rightarrow \tau^+ \nu_\tau$	11.3	11.3		6.4	6.4	
Channel	Form factor	$ V_{cd} $	$\mathcal{R}(\mu/e)$	Form factor	$ V_{cd} $	$\mathcal{R}(\mu/e)$
$D^0 \rightarrow \pi^- e^+ \nu_e$	1.43	1.60	4.0	0.84	1.11	2.8
$D^0 \rightarrow \pi^- \mu^+ \nu_\mu$	-	-		-	-	

Expected precision with 20.27 fb^{-1} @ 3.773 GeV (ready now) and another 3 fb^{-1} @ 4.178 GeV (plan)
 New and more precision (semi-)leptonic decays will be explored

Thanks for your attention