



Precision Hyperon (Semileptonic Decay) Physics at STCF



超级陶粲装置
Super Tau-Charm Facility

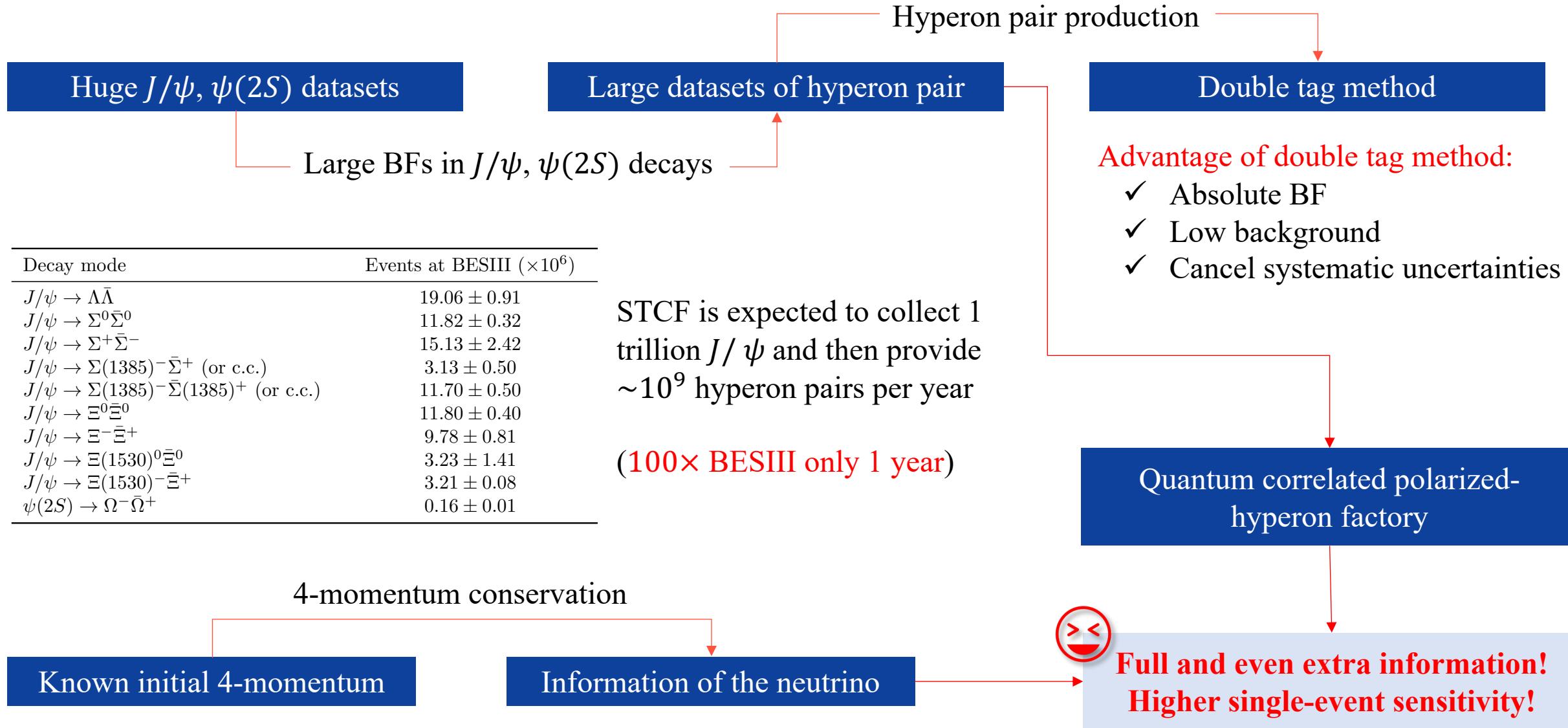
Shun(顺) Wang(王)^{*,1}

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中国物理学会高能物理分会第十四届全国粒子物理学学术会议

2024.08.15

Quantum correlated polarized-hyperon factory

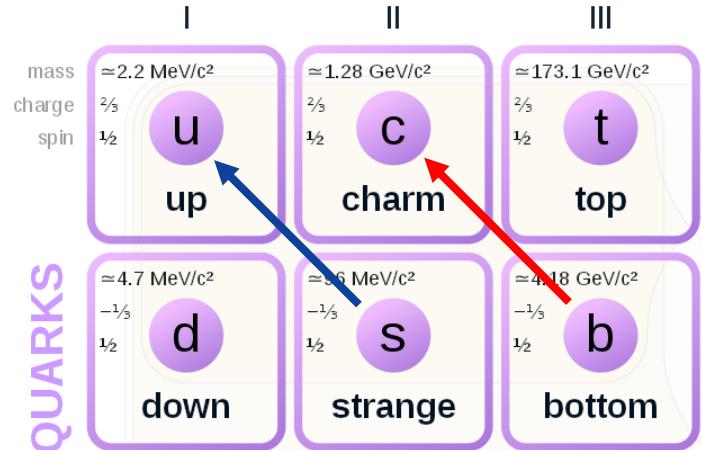
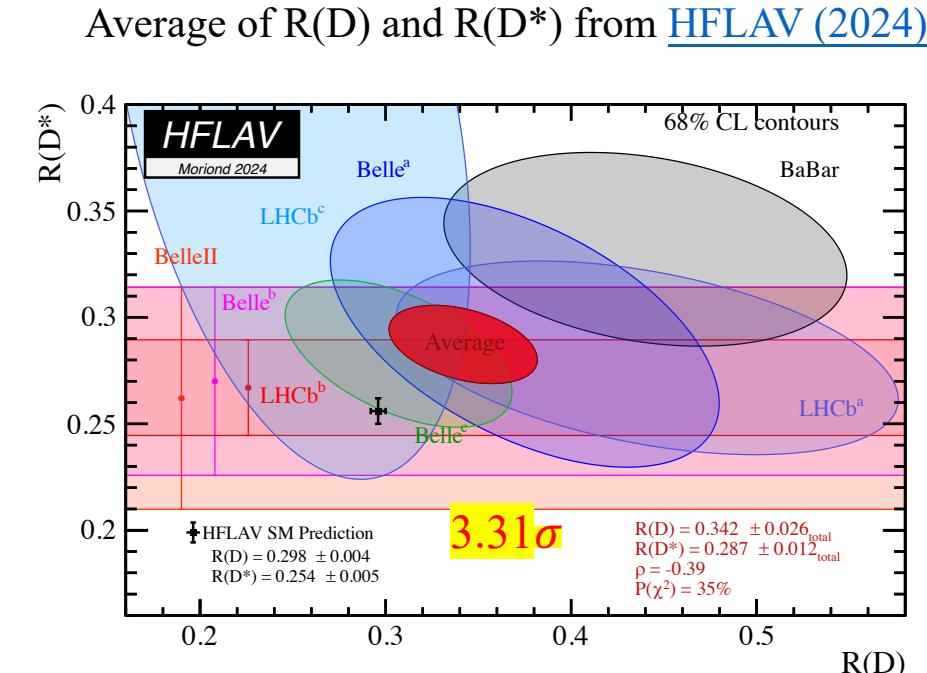


Test lepton flavor universality

Background

$$R(D^{(*)}) = \frac{\mathcal{B}(\bar{B} \rightarrow D^{(*)}\tau^-\bar{\nu}_\tau)}{\mathcal{B}(\bar{B} \rightarrow D^{(*)}l^-\bar{\nu}_l)}$$

$$R^{\mu e} = \frac{\mathcal{B}(B \rightarrow b\mu^-\bar{\nu}_\mu)}{\mathcal{B}(B \rightarrow be^-\bar{\nu}_e)}$$



Experiment vs. SM NLO for $R^{\mu e}$ from hyperon semileptonic decays[1].

$R^{\mu e}$	$\Lambda \rightarrow pl^-\bar{\nu}_l$	$\Sigma^- \rightarrow nl^-\bar{\nu}_l$	$\Xi^0 \rightarrow \Sigma^+ l^-\bar{\nu}_l$	$\Xi^- \rightarrow \Lambda l^-\bar{\nu}_l$
Experiment	0.189 ± 0.041	0.442 ± 0.039	0.0092 ± 0.0014	0.6 ± 0.5
SM NLO	0.153 ± 0.008	0.444 ± 0.022	0.0084 ± 0.0004	0.275 ± 0.014

Background

- Before our measurement, there are only **fixed-target experiments** performed about 50 years ago.
- All these previous branching fraction results are **relative with huge uncertainty**.
- The best previous result was obtained **based on only 14 events** selected from about 0.6M **bubble chamber pictures**.

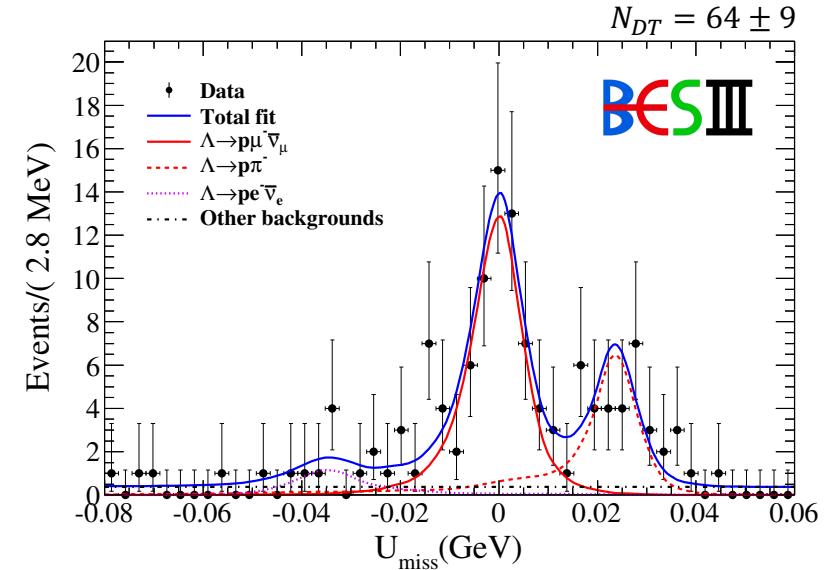
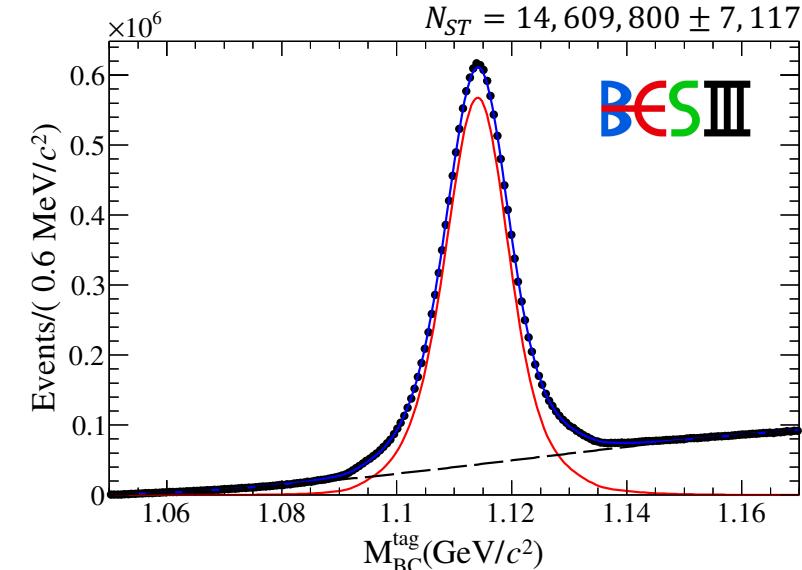
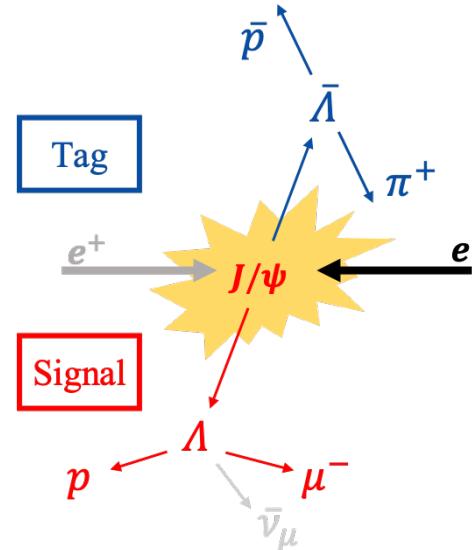
$\Lambda \rightarrow p\mu^-\bar{\nu}_\mu$

▼ $\Gamma(\Lambda \rightarrow p\mu^-\bar{\nu}_\mu)/\Gamma(\Lambda \rightarrow N\pi)$

PDG 2020 

VALUE (10^{-4})	EVTS	DOCUMENT ID	TECN	COMMENT
1.57 ± 0.35	OUR FIT			
1.57 ± 0.35	OUR AVERAGE			
1.4 ± 0.5	14	BAGGETT	1972B HBC	$K^- p$ at rest
2.4 ± 0.8	9	CANTER	1971B HBC	$K^- p$ at rest
1.3 ± 0.7	3	LIND	1964 RVUE	
1.5 ± 1.2	2	RONNE	1964 FBC	

Test lepton flavor universality



[BESIII, PRL 127, 121802 \(2021\)](#)

First absolute BF measurement

$$\mathcal{B}(\Lambda \rightarrow p\mu^-\bar{\nu}_\mu) = (1.48 \pm 0.21 \pm 0.08) \times 10^{-4}$$

- ✓ Update measurement after about 50 years break
- ✓ The first study at a collider experiment
- ✓ The most precise result to date

Test lepton flavor universality

$$R^{\mu e} = \frac{\mathcal{B}(\Lambda \rightarrow p\mu^-\bar{\nu}_\mu)_{BESIII}}{\mathcal{B}(\Lambda \rightarrow pe^-\bar{\nu}_e)_{PDG}} = 0.178 \pm 0.028$$

Consistent
with LFU

$$R_{SM}^{\mu e} = 0.153 \pm 0.008$$

[PRL 114, 161802 \(2015\)](#)

Test lepton flavor universality

Discussion and perspective

$$R^{\mu e} = \frac{\mathcal{B}(\Lambda \rightarrow p\mu^-\bar{\nu}_\mu)_{BESIII}}{\mathcal{B}(\Lambda \rightarrow pe^-\bar{\nu}_e)_{PDG}} = 0.178 \pm 0.028$$

[BESIII, PRL 127, 121802 \(2021\)](#)



$$R_{SM}^{\mu e} = 0.153 \pm 0.008$$

[PRL 114, 161802 \(2015\)](#)

100× statistics at STCF

Assuming the central values are same and the systematical uncertainty is comparable to the statistical one.

$$R^{\mu e} = \frac{\mathcal{B}(\Lambda \rightarrow p\mu^-\bar{\nu}_\mu)_{STCF}}{\mathcal{B}(\Lambda \rightarrow pe^-\bar{\nu}_e)_{STCF}} = 0.178 \pm 0.0036$$



$$R_{SM}^{\mu e} = 0.153 \pm 0.004$$

Half uncertainty

Inputs from theorists
are needed !!!



Background

- About second-class currents, previous nuclear β decay experiments gave contradictory conclusions.
 - ✓ Refs. [1-4] are in favor of the existence of the second-class currents
 - ✓ Refs. [5-8] reported the absence of second-class currents.
- In hyperon β decay, flavor-SU(3)-symmetry-breaking effects [9-10] or second-class currents [11] can cause a nonzero axial-vector form factor g_2 , and some of the experiments suggest a large g_2 [12].

[1] Phys. Rev. Lett. **35**, 1566 (1975).
[2] Phys. Rev. Lett. **34**, 1533 (1975).
[3] Phys. Rev. C **59**, 1113 (1999).
[4] Phys. Rev. C **95**, 035501 (2017).

[5] Phys. Rev. Lett. **26**, 1127 (1971).
[6] Phys. Rev. Lett. **32**, 314 (1974).
[7] Eur. Phys. J. A **7**, 307 (2000).
[8] Phys. Rev. C **84**, 055501 (2011).

[9] Phys. Rev. D **8**, 2963 (1973).
[10] Phys. Rev. D **79**, 074508 (2009).
[11] Annu. Rev. Nucl. Part. Sci. **53**, 39 (2003).
[12] Phys. Rev. D **3**, 2638 (1971).

Background

- In order to confirm the existence of second-class currents, a unique observable (R) was first proposed by S. Weinberg in 1958.

$$R \equiv \frac{\Gamma(\Sigma^- \rightarrow \Lambda e^- \bar{\nu}_e)}{\Gamma(\Sigma^+ \rightarrow \Lambda e^+ \nu_e)}$$

- If there is no second-class currents, R value should be just the phase-space ratio for these two decays , no matter flavor-SU(3)-symmetry-breaking effects exist or not, so any experimental deviation from this deduction would be decisive evidence for the existence of second-class currents.

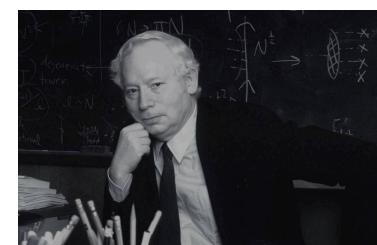
PHYSICAL REVIEW

VOLUME 112, NUMBER 4

NOVEMBER 15, 1958

Charge Symmetry of Weak Interactions*

STEVEN WEINBERG
Columbia University, New York, New York
(Received June 25, 1958)



[Phys. Rev. 112, 1375 \(1958\)](#)

Background

- T. D. Lee and C. N. Yang calculate R on the basis of no second-class currents.

$$R_{\text{theory}} \cong 1.57$$

PHYSICAL REVIEW

VOLUME 119, NUMBER 4

AUGUST 15, 1960

Implications of the Intermediate Boson Basis of the Weak Interactions: Existence of a Quartet of Intermediate Bosons and Their Dual Isotopic Spin Transformation Properties

T. D. LEE

Columbia University, New York, New York

AND

C. N. YANG

Institute for Advanced Study, Princeton, New Jersey

(Received April 11, 1960)



Chen Ning Yang



Tsung-Dao Lee

[Phys. Rev. 119, 1410 \(1960\)](#)

Background

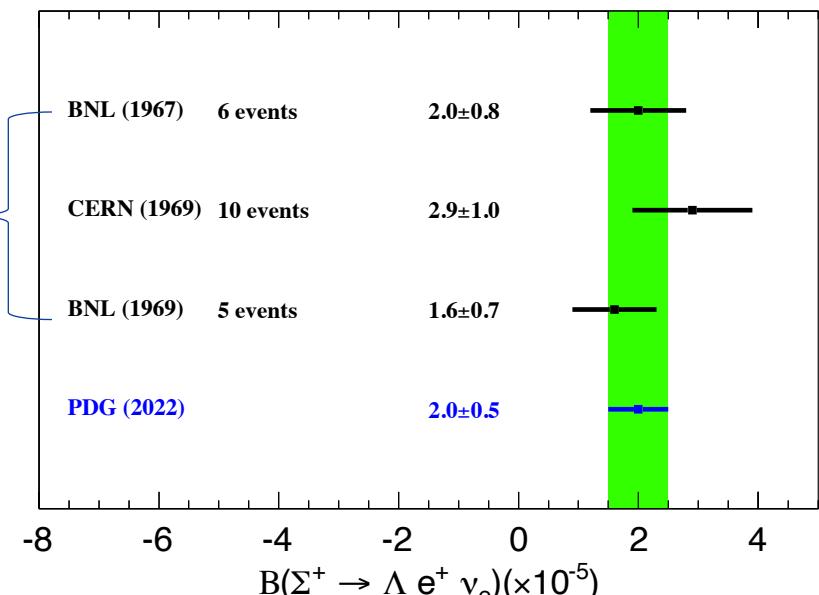
$$R \equiv \frac{\Gamma(\Sigma^- \rightarrow \Lambda e^- \bar{\nu}_e)}{\Gamma(\Sigma^+ \rightarrow \Lambda e^+ \nu_e)} = \frac{\mathcal{B}(\Sigma^- \rightarrow \Lambda e^- \bar{\nu}_e) \cdot \tau_{\Sigma^+}}{\mathcal{B}(\Sigma^+ \rightarrow \Lambda e^+ \nu_e) \cdot \tau_{\Sigma^-}}$$

From PDG2022 [1]:

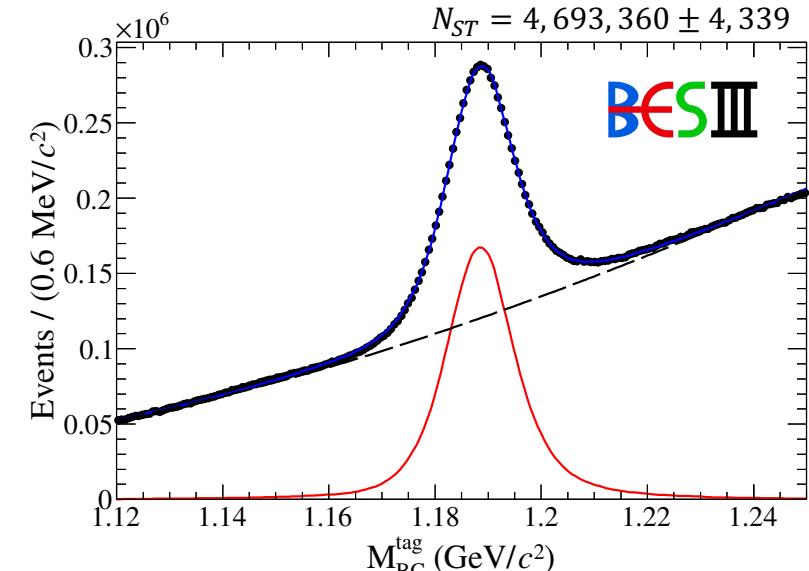
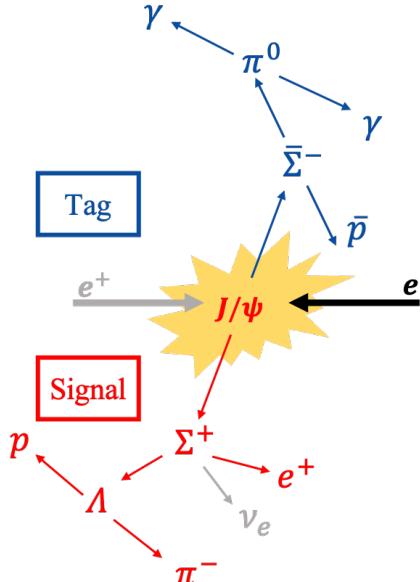
$$\begin{aligned}\sigma(\tau_{\Sigma^+}) &\sim 0.3\% & \sigma[\mathcal{B}(\Sigma^- \rightarrow \Lambda e^- \bar{\nu}_e)] &\sim 4.7\% \\ \sigma(\tau_{\Sigma^-}) &\sim 0.7\% & \sigma[\mathcal{B}(\Sigma^+ \rightarrow \Lambda e^+ \nu_e)] &\sim 25\%\end{aligned}$$



1. Fixed-target experiments
2. Bubble chamber pictures
3. Indirect measurement



Search for second-class currents



[BESIII, PRD 107, 072010 \(2023\)](#)

First direct measurement of absolute BF

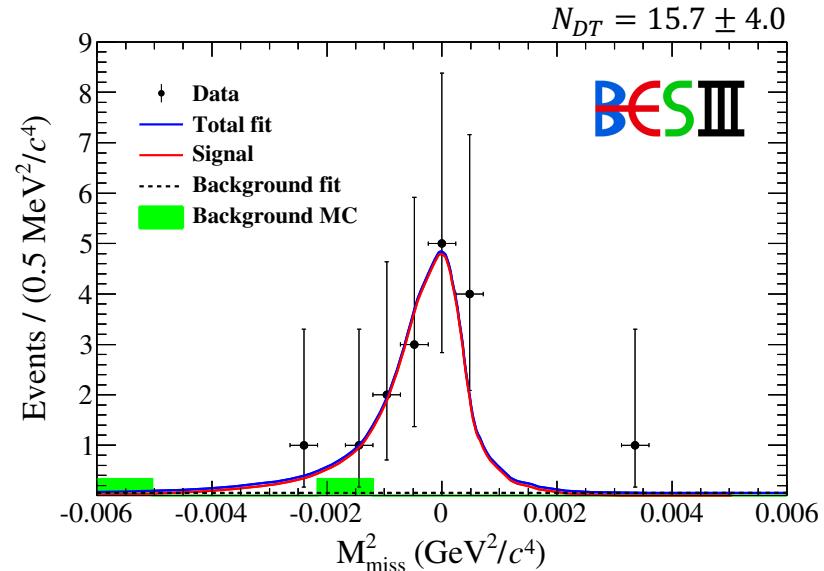
$$\mathcal{B}(\Sigma^+ \rightarrow \Lambda e^+ \bar{\nu}_e) = (2.93 \pm 0.74 \pm 0.13) \times 10^{-5}$$

- ✓ Update measurement after about 50 years break
- ✓ The first study at a collider experiment
- ✓ The most precise result in a single experiment

Search for second-class currents

$$R \equiv \frac{\Gamma(\Sigma^- \rightarrow \Lambda e^- \bar{\nu}_e)}{\Gamma(\Sigma^+ \rightarrow \Lambda e^+ \bar{\nu}_e)} = \frac{\mathcal{B}(\Sigma^- \rightarrow \Lambda e^- \bar{\nu}_e)_{PDG} \cdot \tau_{\Sigma^+}_{PDG}}{\mathcal{B}(\Sigma^+ \rightarrow \Lambda e^+ \bar{\nu}_e)_{BESIII} \cdot \tau_{\Sigma^-}_{PDG}} = 1.06 \pm 0.28$$

NO evidence for second-class currents



Discussion and perspective

BESIII

$$R = \frac{\mathcal{B}(\Sigma^- \rightarrow \Lambda e^- \bar{\nu}_e)_{PDG} \cdot \tau_{\Sigma^+ PDG}}{\mathcal{B}(\Sigma^+ \rightarrow \Lambda e^+ \nu_e)_{BESIII} \cdot \tau_{\Sigma^- PDG}} = 1.06 \pm 0.28$$

[BESIII, PRD 107, 072010 \(2023\)](#)

$$R_{\text{theory}} \cong 1.57$$

[Phys. Rev. 119, 1410 \(1960\)](#)

Assuming the central values are same and the systematical uncertainty is comparable to the statistical one.

$$R = \frac{\mathcal{B}(\Sigma^- \rightarrow \Lambda e^- \bar{\nu}_e)_{STCF} \cdot \tau_{\Sigma^+ PDG}}{\mathcal{B}(\Sigma^+ \rightarrow \Lambda e^+ \nu_e)_{STCF} \cdot \tau_{\Sigma^- PDG}} = 1.06 \pm 0.05$$

超级陶粲装置
Super Tau-Charm Facility**10 σ deviation**

Inputs from theorists
are needed !!!



Without the certain mean value and the corresponding uncertainty, we cannot claim the observation of second-class currents.

Extract the CKM matrix element $|V_{us}|$

In the SM : First-row unitarity relation

$$|V_{ud}|^2 + |V_{us}|^2 + |V_{ub}|^2 = 1$$

2.3σ tension
A hint of new physics?

PDG 2024 : Independent measurements

$$|V_{ud}|^2 + |V_{us}|^2 + |V_{ub}|^2 = 0.9984 \pm 0.0007$$



$|V_{ub}|$: Small ($|V_{ub}|^2 \cong 1.7 \times 10^{-5}$) → The effect could be ignored in current precision



$|V_{ud}|$: Most precise; results from different decays are consistent at $\mathcal{O}(10^{-4})$ → Precise and reliable



$|V_{us}|$: $\sigma(|V_{us}|) = 2.7 \times \sigma(|V_{ud}|)$; inconsistency between results from different decays



Most precise

Kaon : 2.3σ tension from CKM unitarity

$$|V_{us}| = 0.22431 \pm 0.00085$$

PDG 2024

Second most precise

Tau : 3.7σ deviation from CKM unitarity

$$|V_{us}| = 0.2207 \pm 0.0014$$

HFLAV 2022

2.2σ tension

Largest uncertainty

Hyperon : consistent with CKM unitarity

$$|V_{us}| = 0.2250 \pm 0.0027$$

Dominated by the $\Lambda \rightarrow p e^- \bar{\nu}_e$

Decay width of $\Lambda \rightarrow p e^- \bar{\nu}_e$ in the SM

$$\Gamma_{\text{SM}} = \frac{\mathcal{B}_{\Lambda \rightarrow p e^- \bar{\nu}_e}}{\tau_\Lambda} = \frac{G_F^2 |V_{us}|^2 f_1(0)^2 \Delta^5}{60\pi^3} [(1 - \frac{3}{2}\delta + \frac{6}{7}\delta^2) + \frac{4}{7}\delta^2 g_w^2 + (3 - \frac{9}{2}\delta + \frac{12}{7}\delta^2) g_{av}^2 + \frac{12}{7}\delta^2 g_{av2}^2 + \frac{6}{7}\delta^2 g_w + (-4\delta + 6\delta^2) g_{av}g_{av2}]$$

[PRD 70, 114036 \(2004\)](#)

$$\Delta \equiv M_\Lambda - M_p$$

$$\delta \equiv \frac{M_\Lambda - M_p}{M_\Lambda}$$

➤ Extracting $|V_{us}|$, requires $\mathcal{B}_{\Lambda \rightarrow p e^- \bar{\nu}_e}$, $f_1(0)$, $g_{av} \equiv \frac{g_1(0)}{f_1(0)}$, $g_w \equiv \frac{f_2(0)}{f_1(0)}$, and $g_{av2} \equiv \frac{g_2(0)}{f_1(0)}$,

□ $f_1(0)$: From LQCD

□ $\mathcal{B}_{\Lambda \rightarrow p e^- \bar{\nu}_e}$, g_{av} , g_w , and g_{av2} : From experimental measurement

Current status

 $\mathcal{B}_{\Lambda \rightarrow p e^- \bar{\nu}_e}$

No absolute measurement [1]



The assumption of $g_{av2} = 0$ has not been verified

 g_{av2}

No measurement [1]

 g_{av} Measured based on two assumptions of $g_{av2} = 0$ and $g_w = 0.97$ [1] g_w The latest and most precise measurement is $g_w = 0.15 \pm 0.30$ [2]

The assumption of $g_w = 0.97$ deviates from the measurement 2.7σ

BESIII

STCF
Super Tau-Charm Facility

First measurement of the absolute $\mathcal{B}_{\Lambda \rightarrow p e^- \bar{\nu}_e}$
(Double tag method)



First simultaneous measurement of the g_{av} , g_w , and g_{av2}
(Complete information of the whole decay chain)



More solid $|V_{us}|$ from hyperon

Discussion and perspective

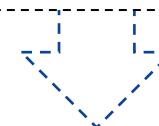
BESIII

~2k events of $\Lambda \rightarrow p e^- \bar{\nu}_e$

$|V_{us}| = xxx \pm (\sim 0.010_{\text{exp}})$, using Cabibbo $f_1(0)$

100× statistics at STCF

Assuming the systematical uncertainty is comparable to the statistical one.



~0.2M events of $\Lambda \rightarrow p e^- \bar{\nu}_e$

$|V_{us}| = xxx \pm (\sim 0.0013_{\text{exp}})$, using Cabibbo $f_1(0)$

Comparable to the averaged $\sigma_{|V_{us}|}$ from Kaon (~ 0.0009) are Tau (~ 0.0014)

Inputs from theorists are needed !!!



$f_1(0)$ from LQCD

Precision calculation for the radiative correction

Summary

- The proposed STCF is expected to collect 1 trillion J/ψ and then provide $\sim 10^9$ hyperon pairs per year, which enables us to pursue precision hyperon semileptonic decay physics including:
 - ① Test the lepton flavor universality
 - ② Search for second-class currents
 - ③ Test the CKM matrix unitarity



- ▣ To achieve these goals, **inputs from theorists are needed !!!**

Thank you~!

