



Test of lepton flavor universality at Belle and Belle II

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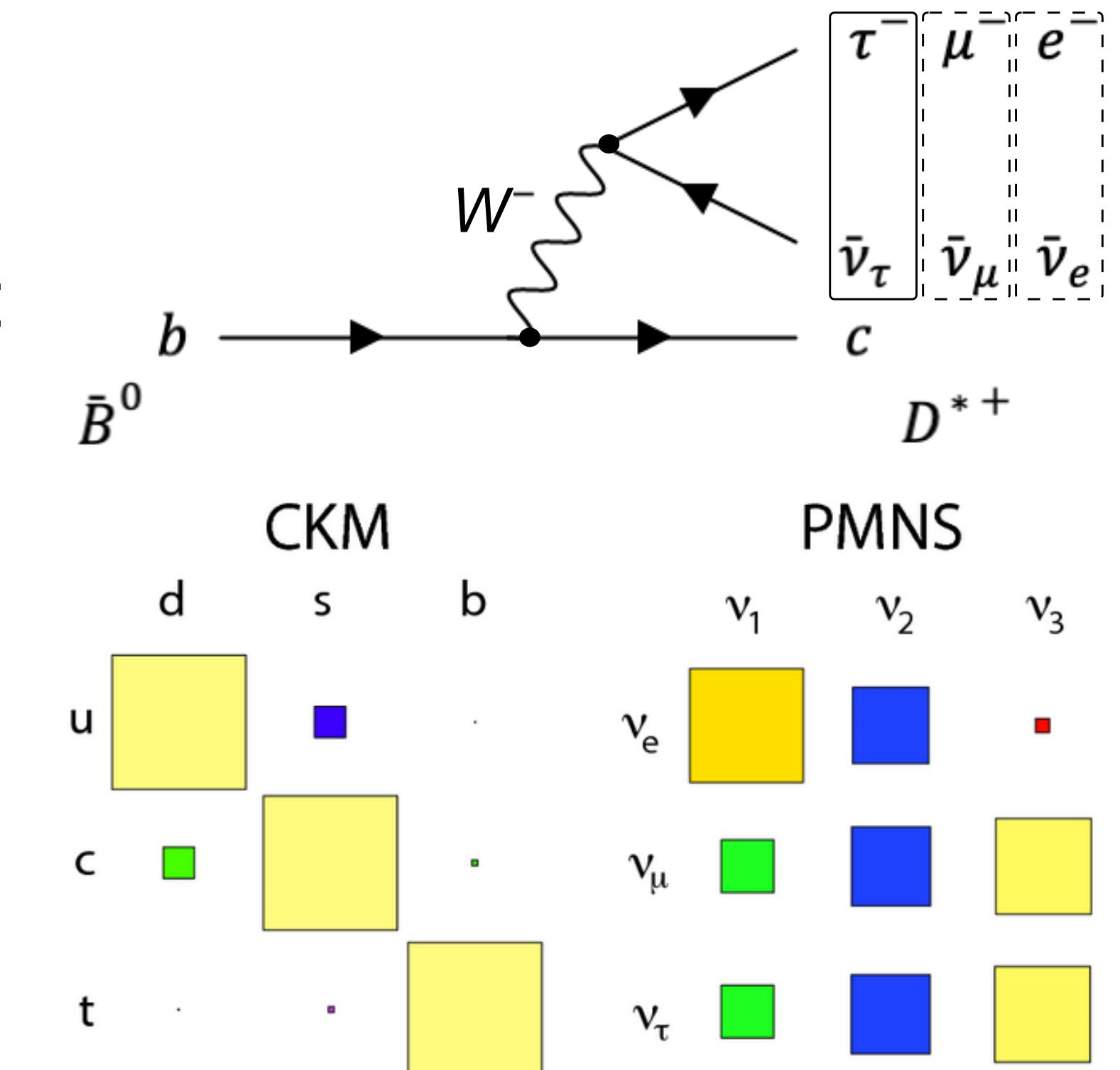
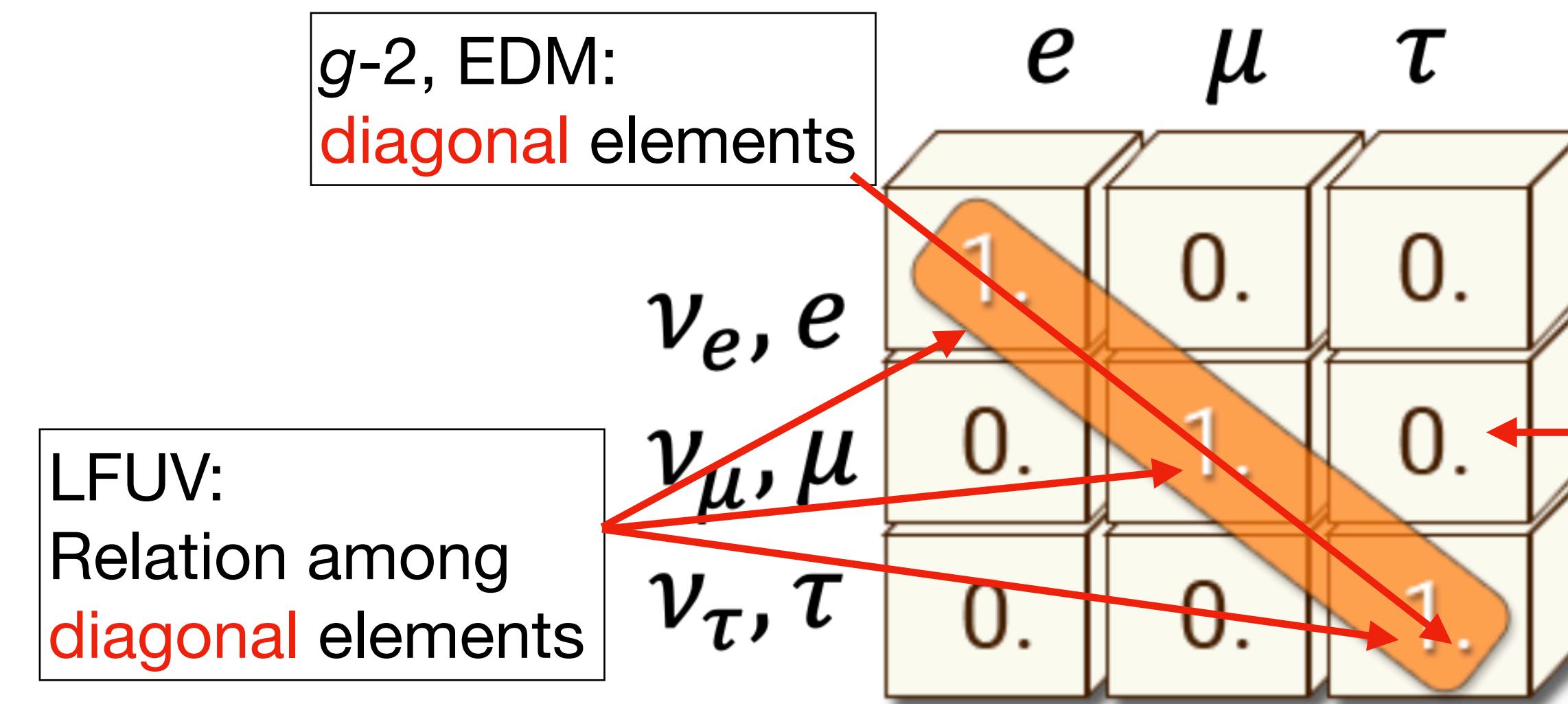
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2024年8月13-18日, 山东大学, 青岛
第十四届全国粒子物理学学术会议

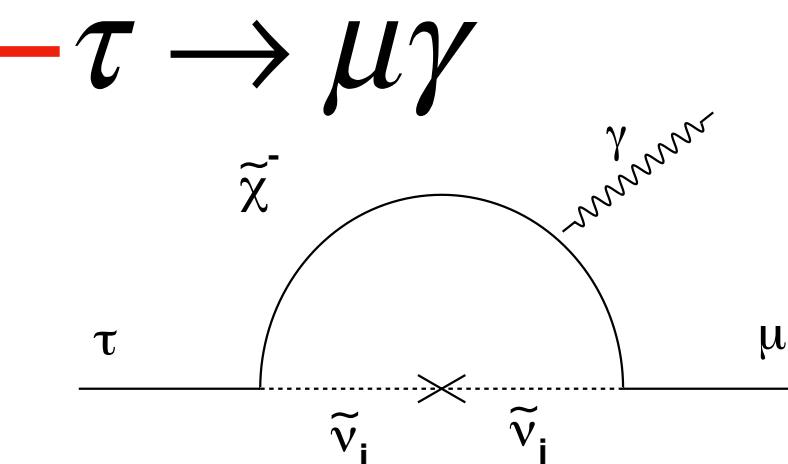


Motivation for studying LFUV

- Lepton Flavor Universality (LFU): W boson couples to leptons with equal strength
 - Difference in kinematics and Higgs coupling due to different lepton masses
- SM fields do mix:
 - Quarks sector \rightarrow CKM matrix
 - Neutrinos sector \rightarrow PMNS matrix
 - Charged leptons \rightarrow **the matrix purely diagonal?**
 - LFUV: diagonal terms not all equal

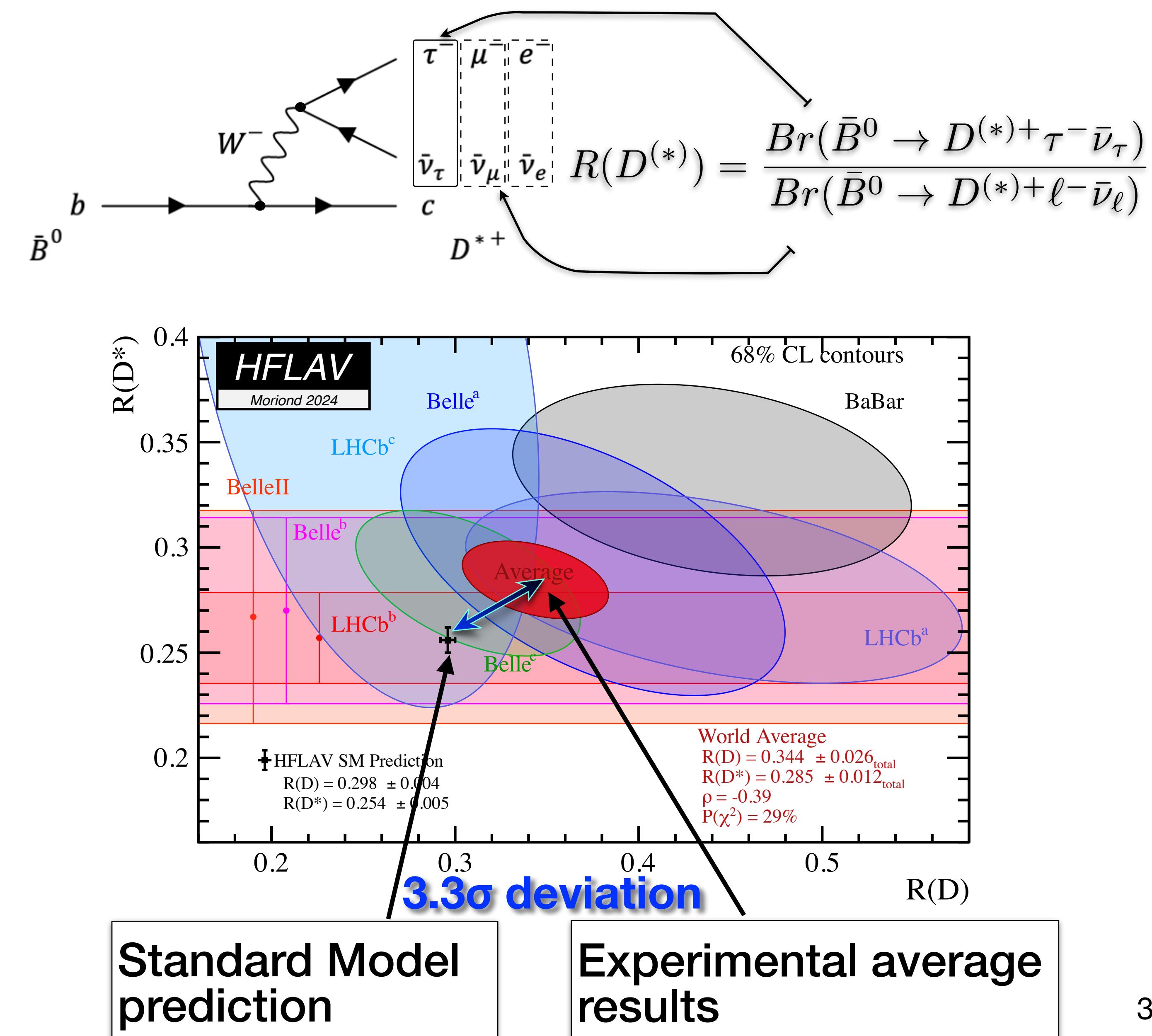
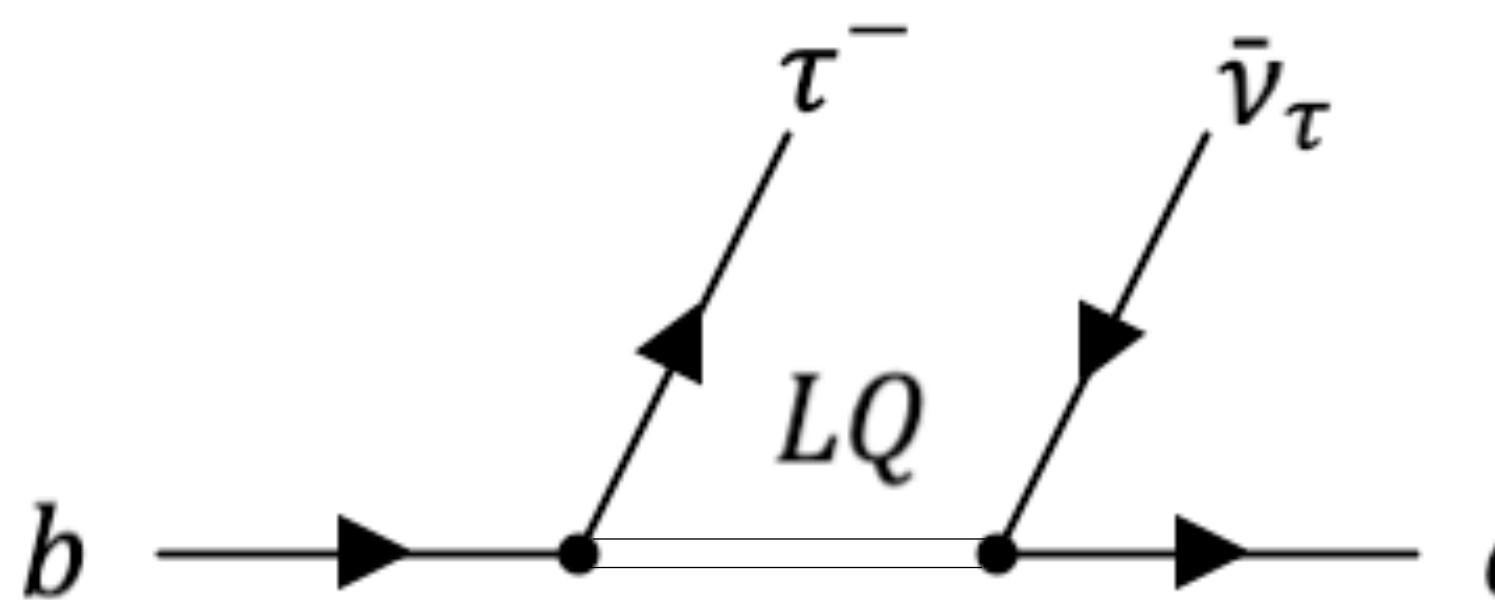


Lepton Flavor Violation (LFV):
off diagonal term



“ B anomaly” in semileptonic decays

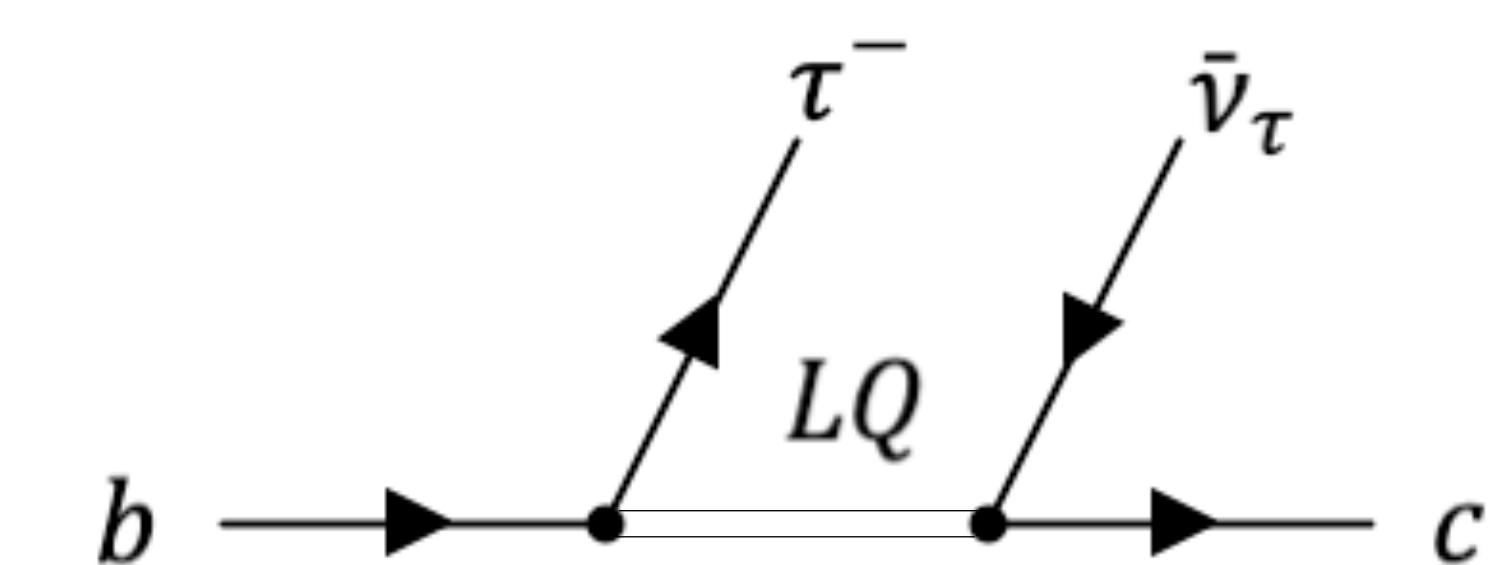
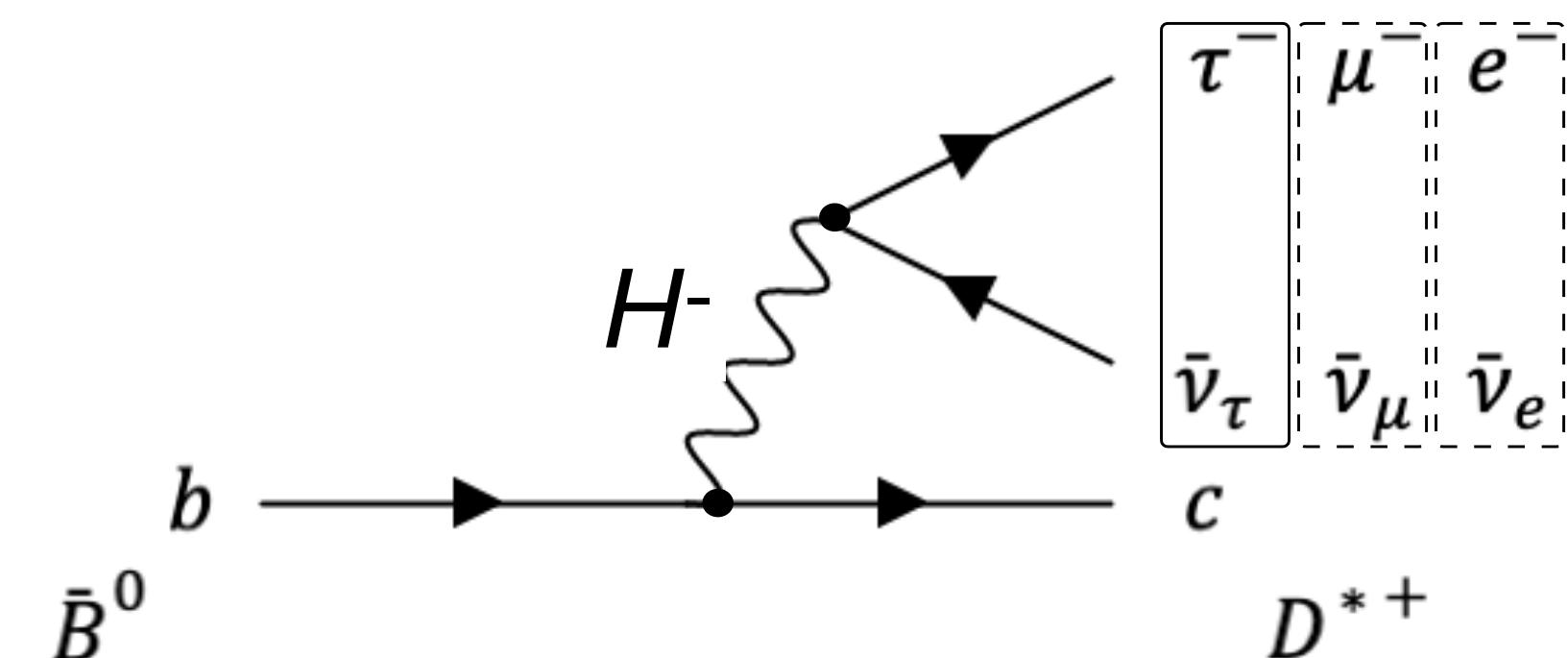
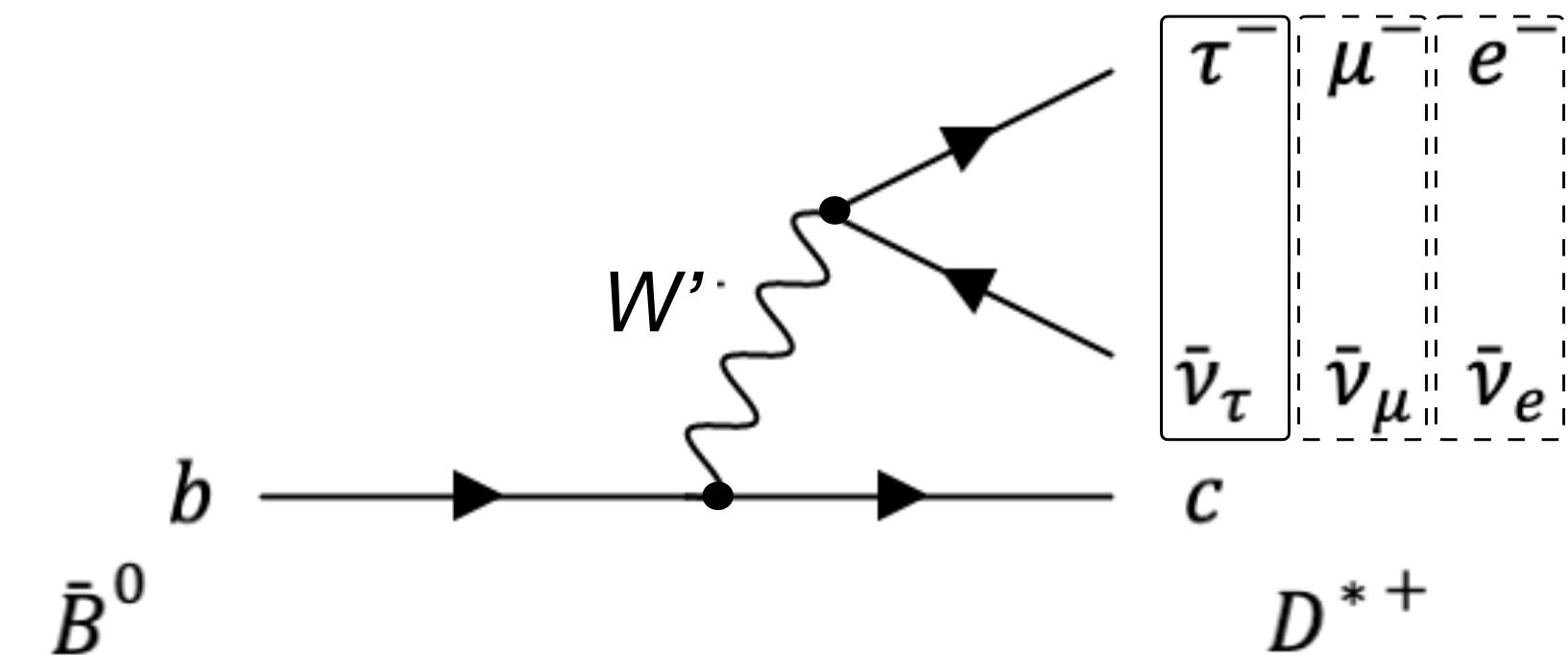
- Ratios of $b \rightarrow q\tau\nu/q\mu\nu/qe\nu$ branch fractions cancel out most of the uncertainties on $|V_{cb}|$, form factors and the experimental systematics
- $B \rightarrow D^{(*)}\tau\nu$ sensitive to New Physics (NP) because the massive 3rd generation **b quark** and **τ lepton** are involved
- Sensitivities to high energy scale; ~ 10 TeV [[Belle II phys. book](#)]



New physics scenarios for the $R(D^{(*)})$ anomaly

In general, there are three typical candidate scenarios to explain the anomaly observed in $R(D^{(*)})$

- Heavy vector bosons
 - Constrained from $W' \rightarrow \tau\nu$ and $Z' \rightarrow \tau\tau$ search
- Charged Higgs
 - Constrained from $B_c \rightarrow \tau\nu$ and $H^\pm \rightarrow \tau\nu$, still allowed
 - Previously, it was rejected by $B_c \rightarrow \tau\nu$ measurement, however, recovered by recalculating the B_c lifetime.
- [arXiv:2201.06565](#)
- Leptoquark
 - $gg \rightarrow LQ \ LQ^*$, still broad parameter regions are allowed



LFU test program at Belle II

- The analyses presented in this talk
 - $R_{\tau/\ell}(D^*)$ at Belle II (189 fb^{-1}), preliminary, arXiv:2401.02840
 - $R_{\tau/\ell}(X)$ at Belle II (189 fb^{-1}), PRL132, 211804
 - $R_{e/\mu}(X)$ from Belle II (189 fb^{-1}), PRL 131, 051804
 - $R_{e/\mu}(D^*)$ from **Belle** (711 fb^{-1}), PRD 108, 012002
 - Test of LFU in angular asymmetries of $B \rightarrow D^* l \nu$ at Belle II (189 fb^{-1}),
PRL 131, 181801
 - Test of LFU in τ decays at Belle II (362 fb^{-1}), preliminary,
arXiv:2405.14625

Belle II detector and dataset

Vertex detector (VXD)

Inner 2 layers: pixel detector (PXD)
Outer 4 layers: strip sensor (SVD)

Central Drift Chamber (CDC)

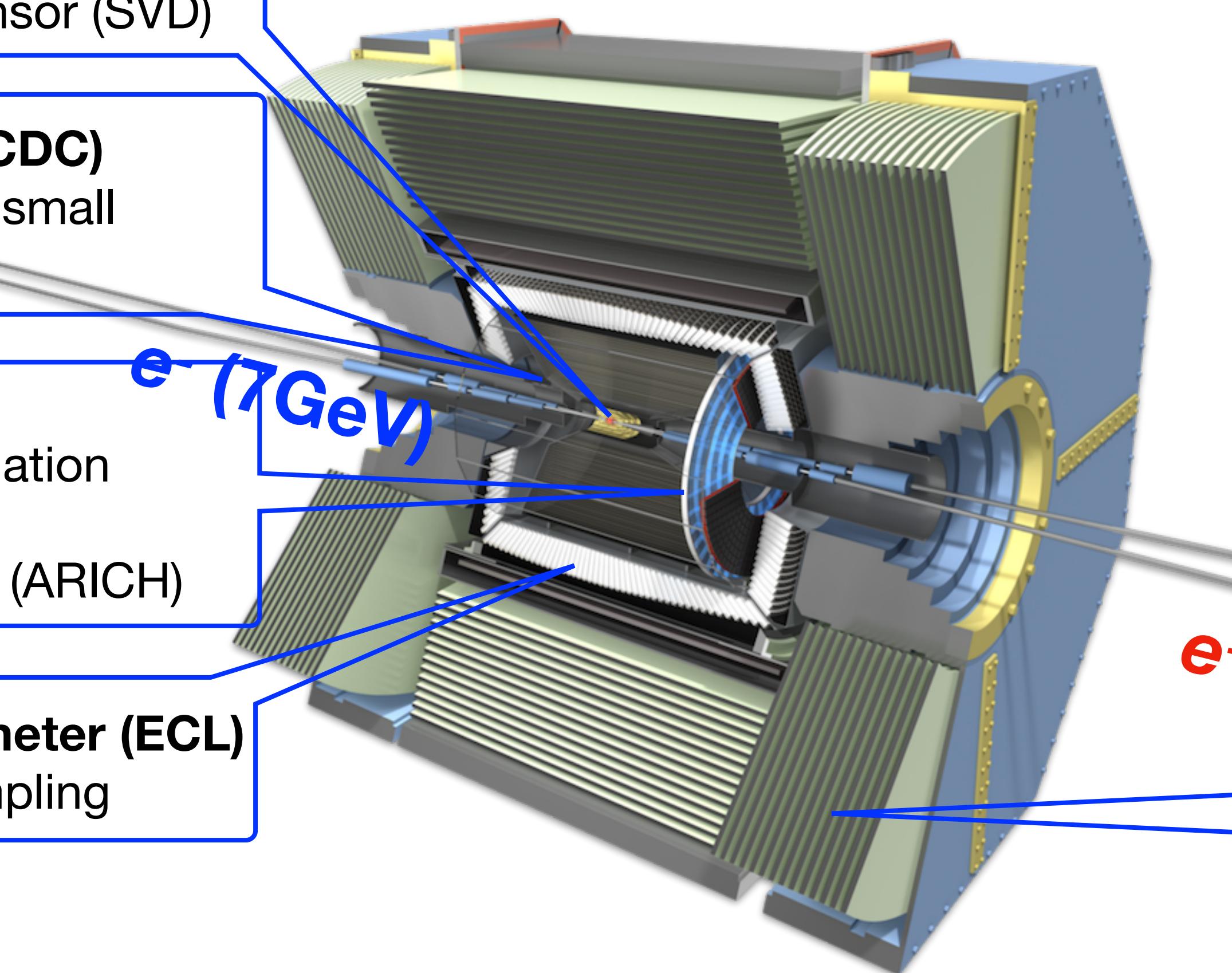
He (50%), C₂H₆ (50%), small cells, long lever arm

Particle Identification

Barrel: Time-Of-Propagation counters (TOP)
Forward: Aerogel RICH (ARICH)

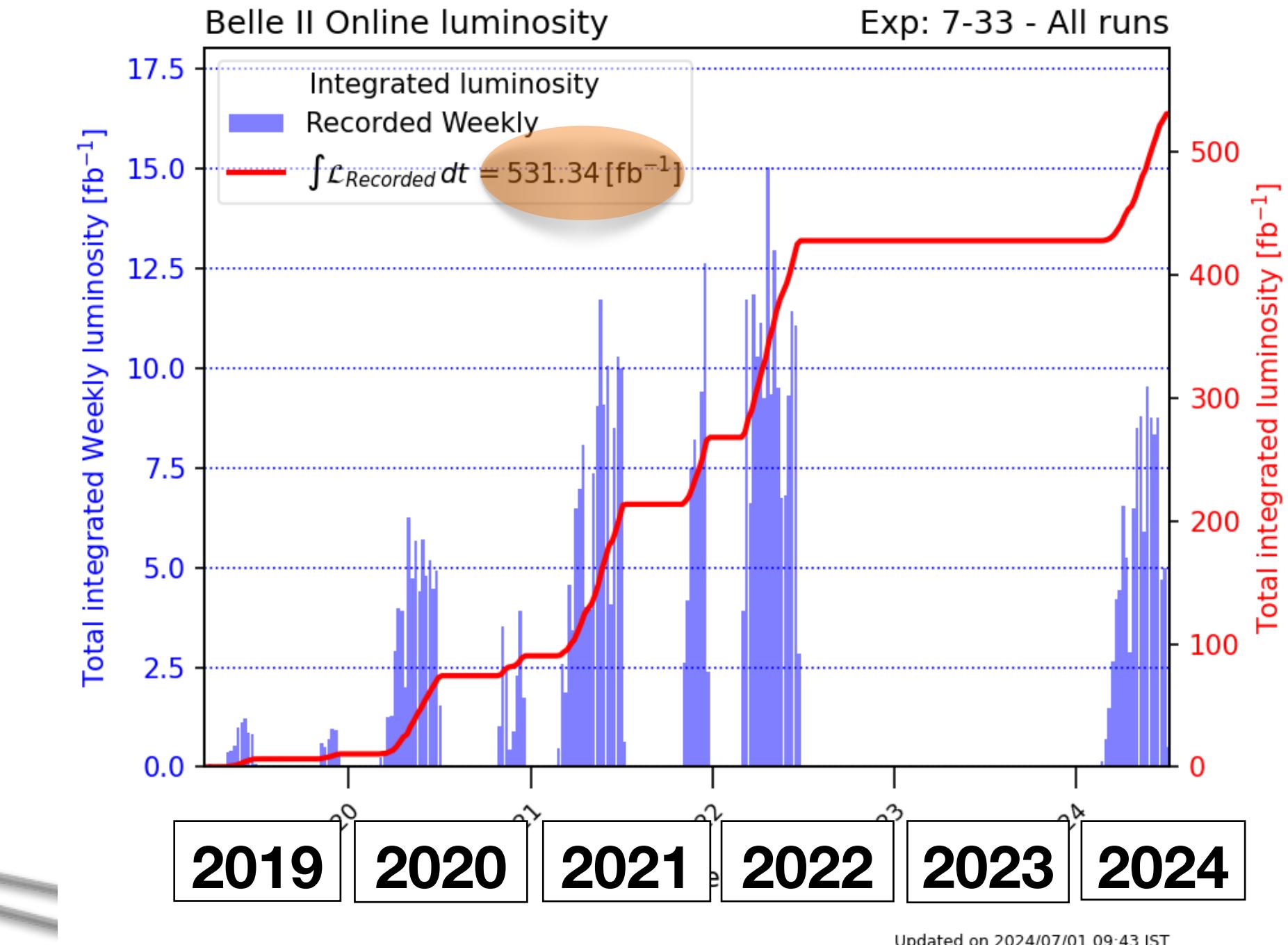
ElectroMagnetic Calorimeter (ECL)

CsI(Tl) + waveform sampling



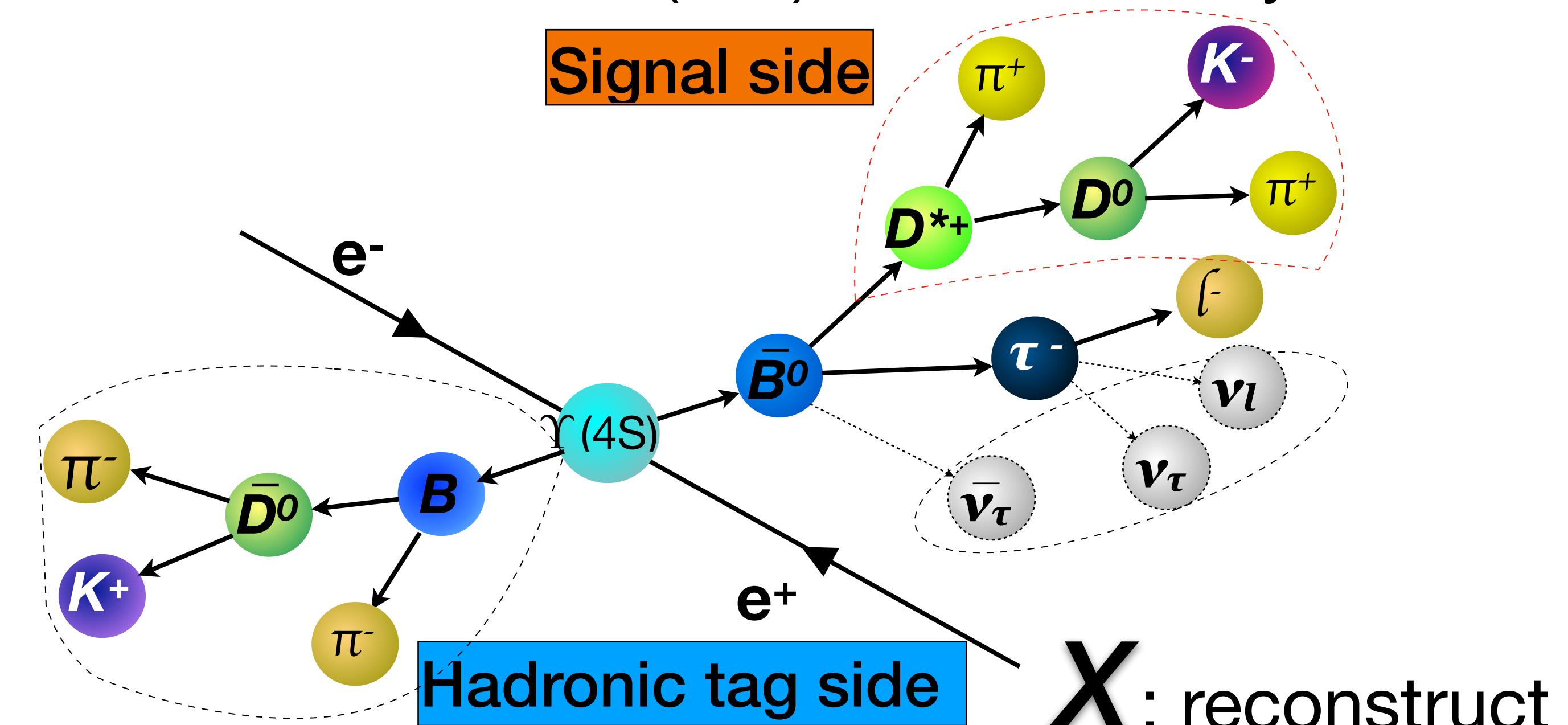
- Features:

- Near-hermetic detector
- Vertexing and tracking: σ vertex $\sim 15\mu\text{m}$, CDC spatial res. $100\mu\text{m}$ $\sigma(P_T)/P_T \sim 0.4\%$
- Good at measuring neutrals, π^0 , γ , K_L ... $\sigma(E)/E \sim 2-4\%$



Tagging methods

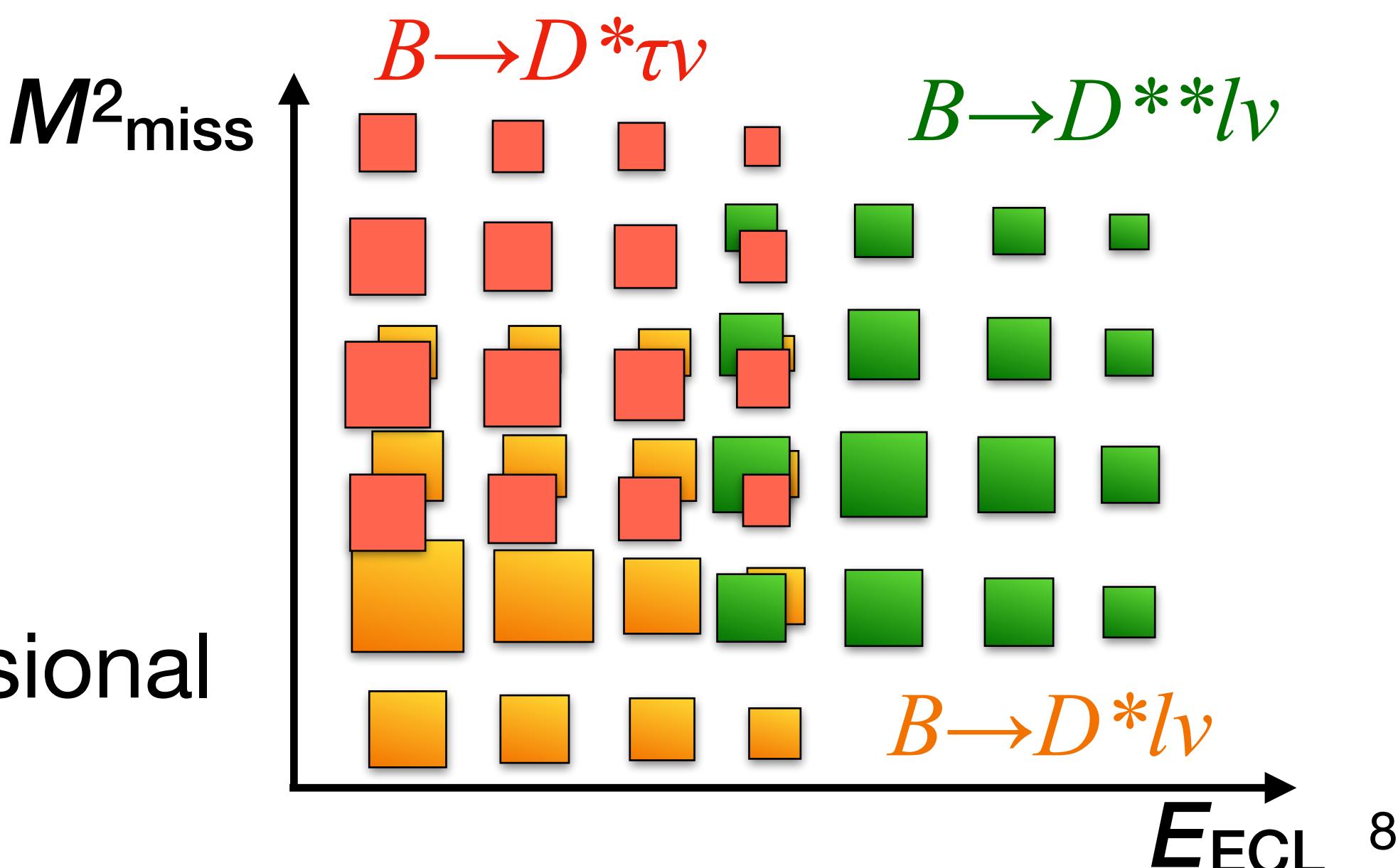
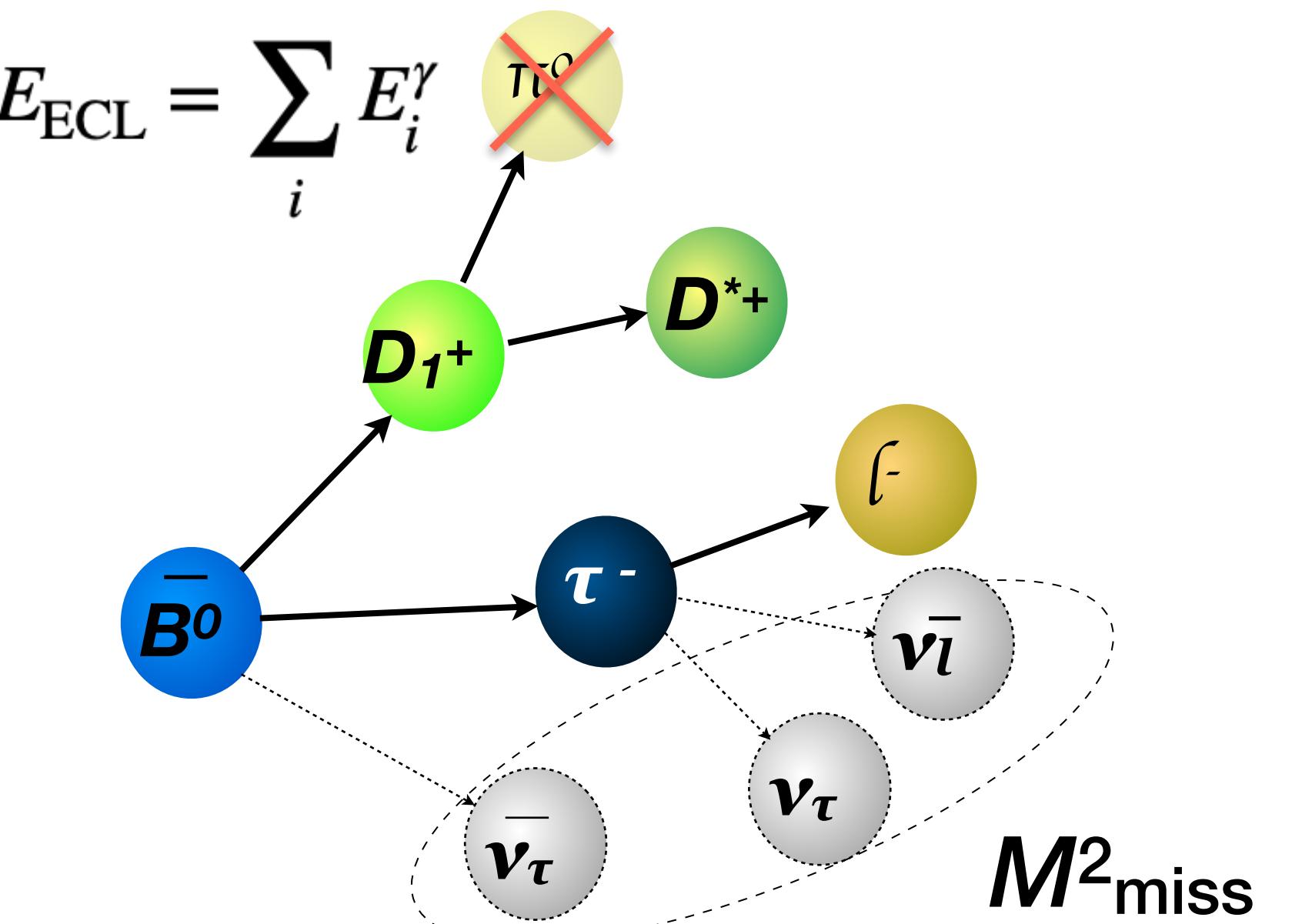
- The $B\bar{B}$ pairs are produced near threshold
- B tagging is necessary to measure $B \rightarrow X / D^* \tau\nu$, $B \rightarrow X / D^* l\nu$ ($\nu \geq 2$) simultaneously
- Hadronic tag
 - Fully reconstruct $B \rightarrow D^{(*)}(/J/\psi/\Lambda)X$
 - Tagging efficiency 0.2~0.4%
 - less background



- Fully reconstruct one of the B mesons (B tag), possible to measure momentum of other B meson (B signal)
- Indirectly measure missing momentum of neutrinos in signal B decays
- $M_{\text{miss}}^2 = (p_{\text{beam}} - p_{B\text{tag}} - p_{D^{(*)}} - p_l)^2$
- E_{ECL} unassigned neutral energy in the calorimeter $E_{\text{ECL}} = \sum_i E_i^\gamma$

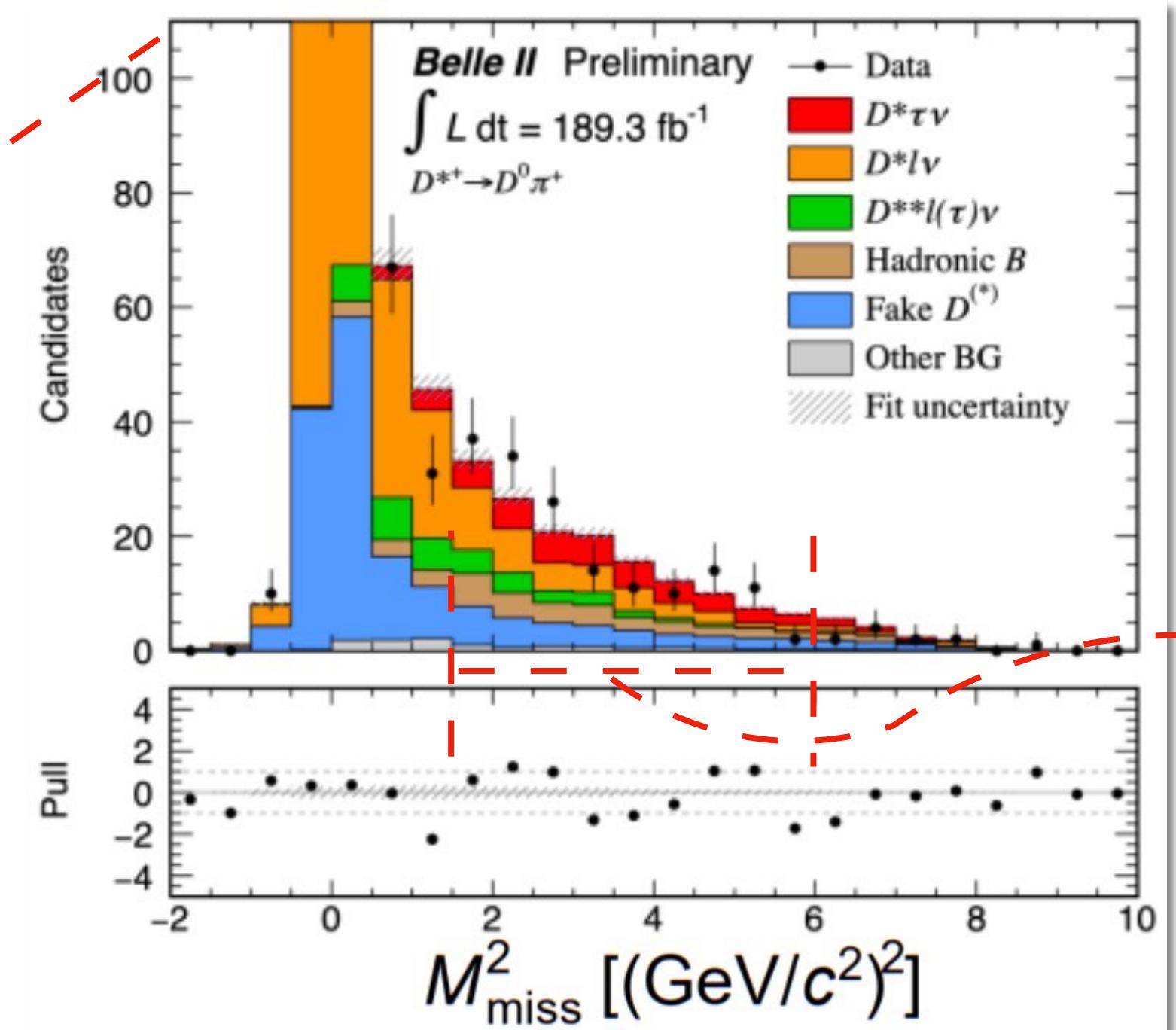
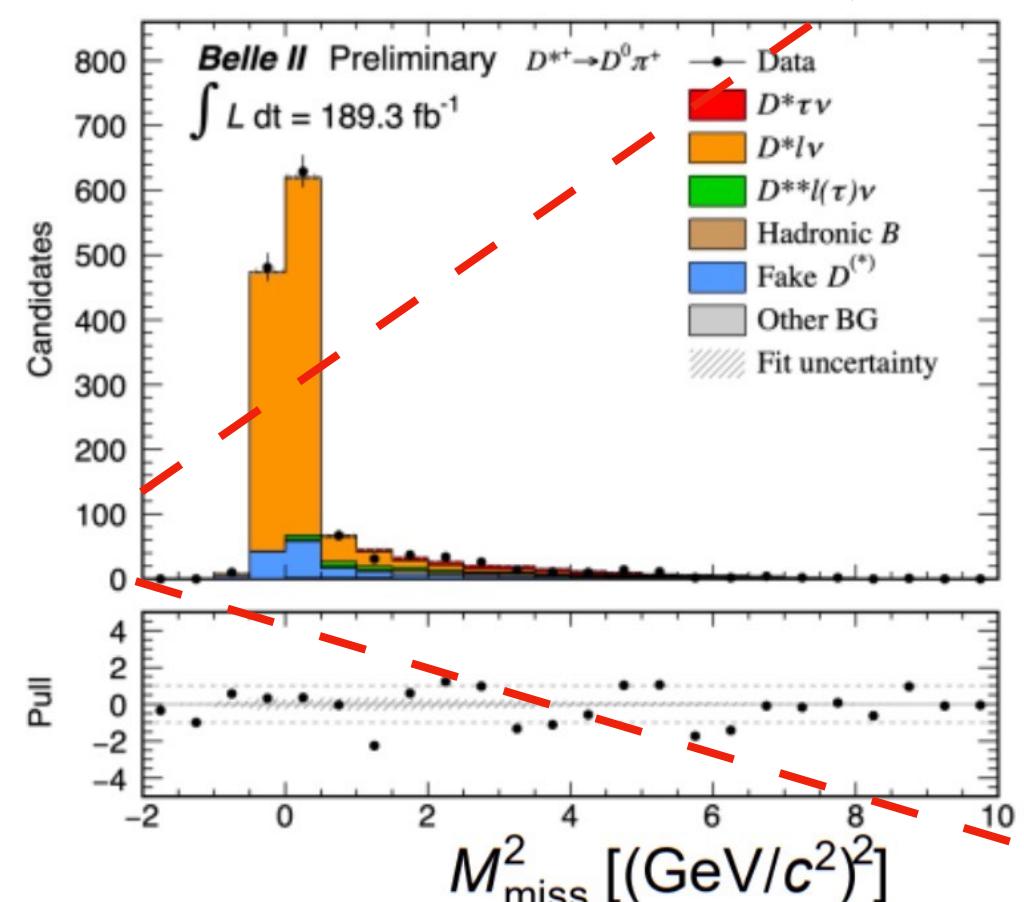
Analysis strategy

- Reconstruct $B \rightarrow D^* \tau \nu$ and $B \rightarrow D^* l \nu$ with same selections
- τ lepton reconstruct with $\ell (e, \mu) \nu \nu$
- D/D^* meson reconstruct with $K^\pm, \pi^\pm, K_s, \pi^0$
 - 8 D^0 modes ($\text{Br} \sim 36\%$), 4 D^+ modes ($\text{Br} \sim 12.3\%$)
 - $D^{*+} \rightarrow D^0 \pi^+/D^+ \pi^0$ ($\text{Br} \sim 98\%$), $D^{*0} \rightarrow D^0 \pi^0$ ($\text{Br} \sim 65\%$)
- Both neutral and charged B^\pm/B^0 mesons reconstruct with D^{*+}/D^{*0} and $\tau/\ell = (e, \mu)$
- $M_{\text{miss}}^2 = (p_{\text{beam}} - p_{B\text{tag}} - p_{D^*(*)} - p_\ell)^2$
- E_{ECL} : extra neutral energy in the calorimeter **NOT** associate with signal
- Extracting $B \rightarrow D^* \tau \nu, B \rightarrow D^* l \nu$ yields by a two-dimensional simultaneously fit

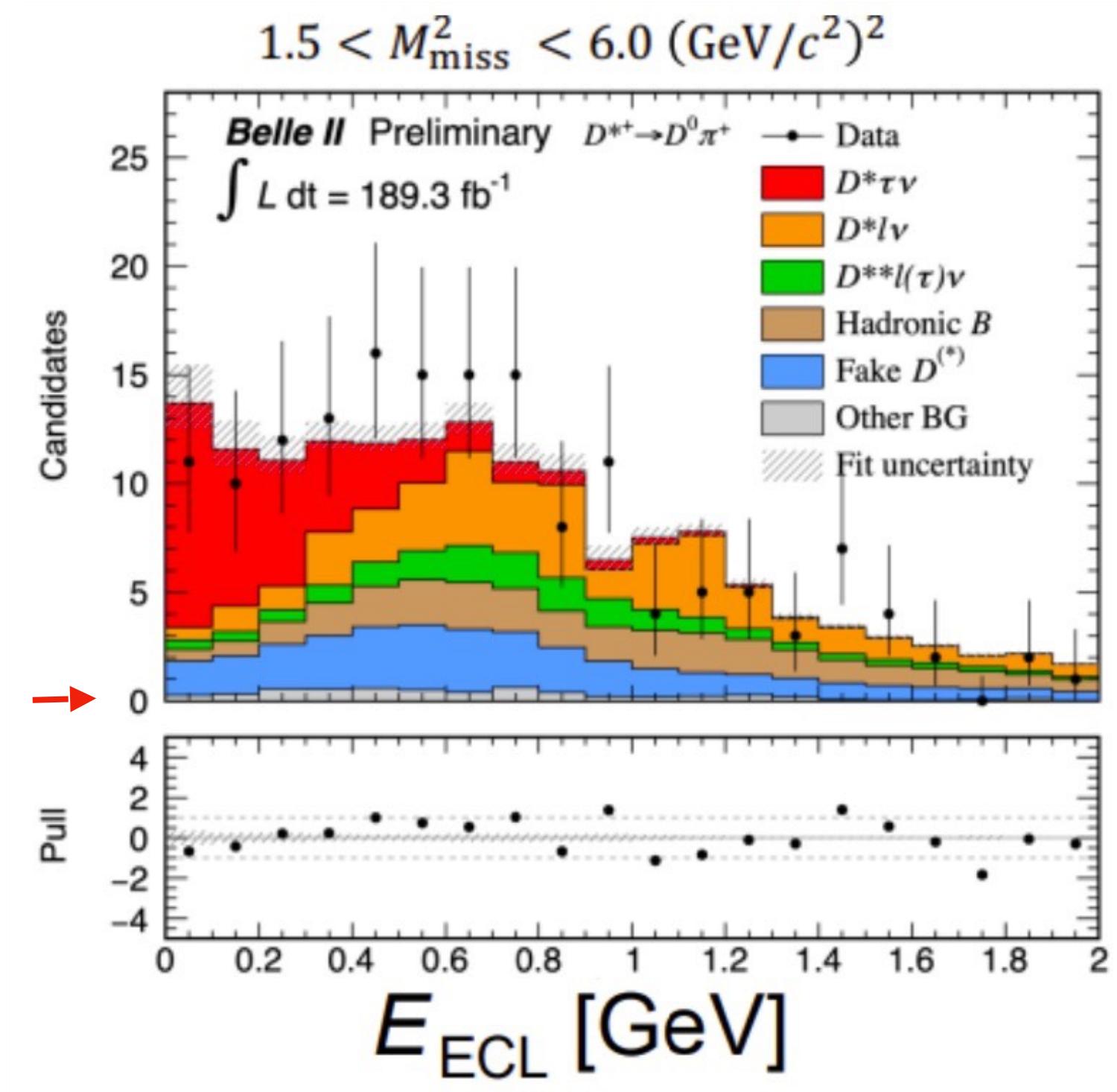


$R_{\tau/\ell}(D^*)$ results

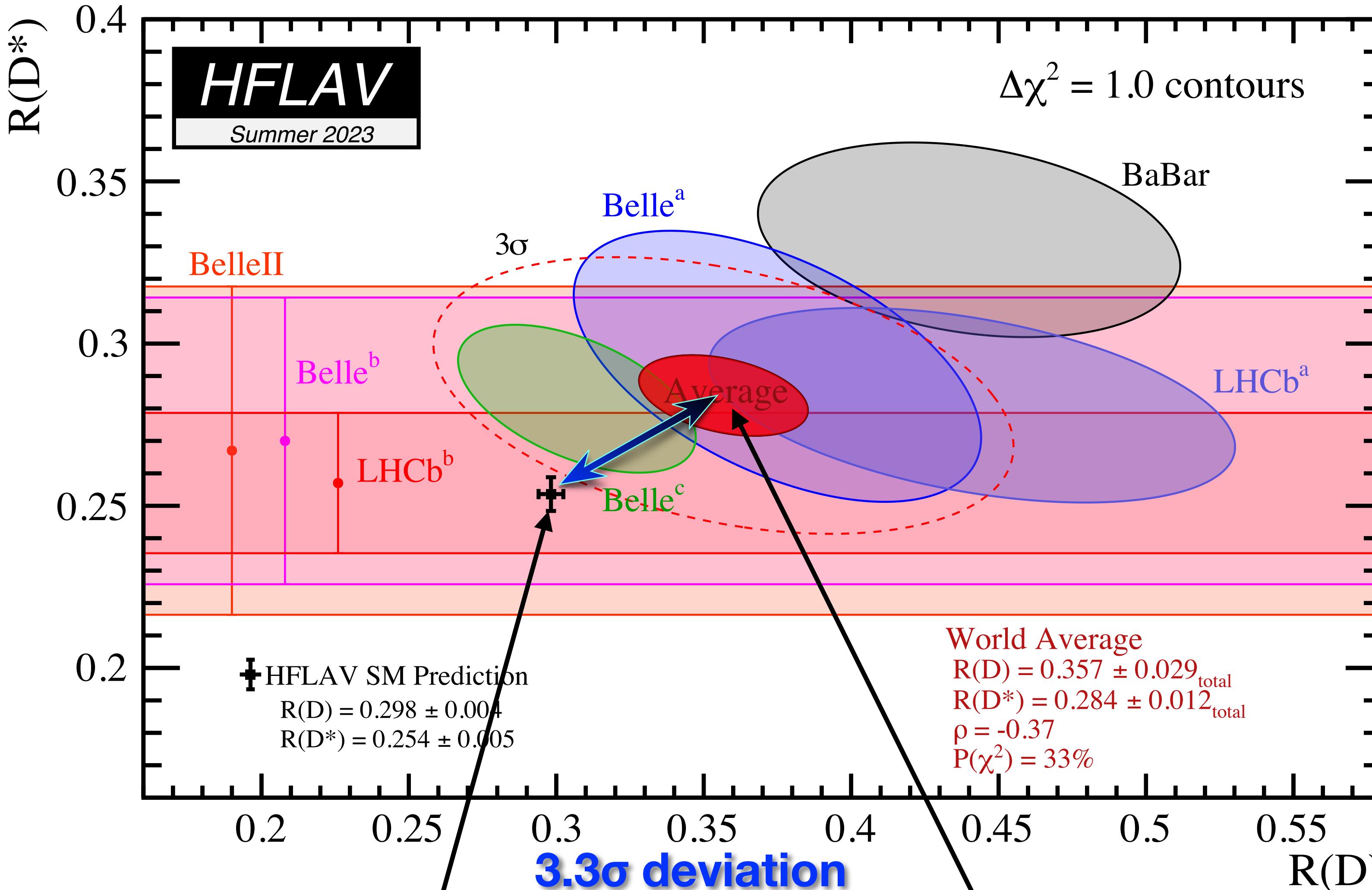
- Similarly sensitivity as Belle 15' result @ 711 fb^{-1} with only 189 fb^{-1}
- Belle II first preliminary result for $R(D^*)$
- $R(D^*) = 0.267^{+0.041}_{-0.039}(\text{stat})^{+0.028}_{-0.033}(\text{sys})$
- Consistent with
SM: 0.254 ± 0.005 ,
HFLAV23: 0.284 ± 0.013
- SM vs. experimental average deviation: $3.2\sigma \rightarrow 3.3\sigma$



Source	Uncertainty
Statistical uncertainty	+15.4% -14.6%
E_{ECL} PDF shape	+5.5% -9.3%
MC statistics	$\pm 7.0\%$
$B \rightarrow D^{**} l \nu$ modeling	+4.7% -2.7%



“B anomaly” in semileptonic decays



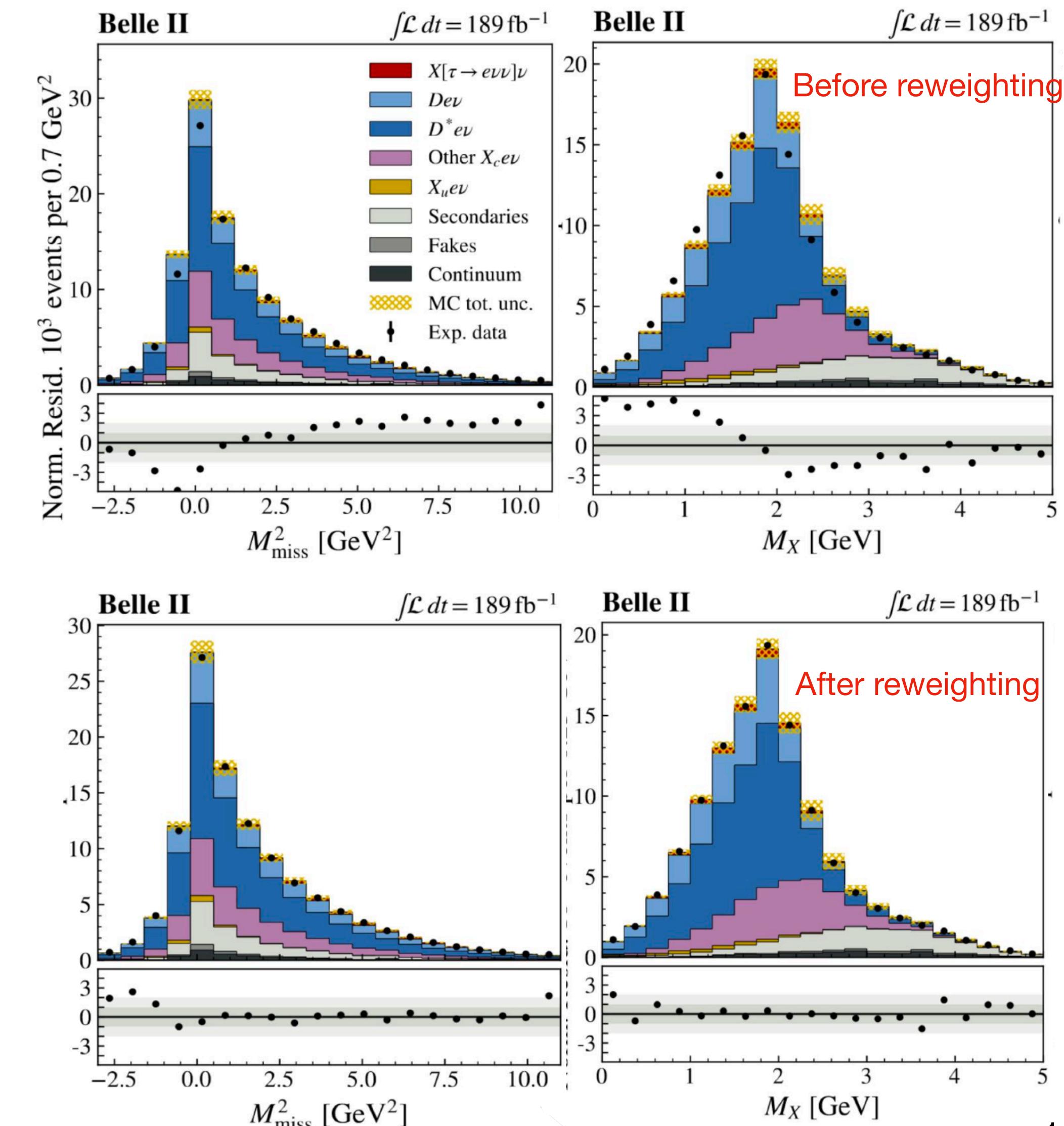
Standard Model prediction

Experimental average results

Update the modeling for $R_{\tau/\ell}(X)$ measurement

- Approach employed at Belle II: M_X reweighting
 - Events weights from data/MC ratio in M_X distribution, applied to all events
 - q^2, M_{miss}^2 can be expressed by reliable parts and M_X part
- Detailed adjustments to MC (FFs, B and D BFs)
- Signal yields are extracted by a binned maximum-likelihood simultaneous fit to lepton momentum at different M_{miss}^2 bins

PRL132, 211804



Results of $R_{\tau/\ell}(X)$ for LFU test

- Main systematics
 - Adjustment to MC (form factor, D and B branching fractions)
 - Sample size in sideband for reweighting
- First Belle II preliminary $R_{\tau/\ell}(X)$ result

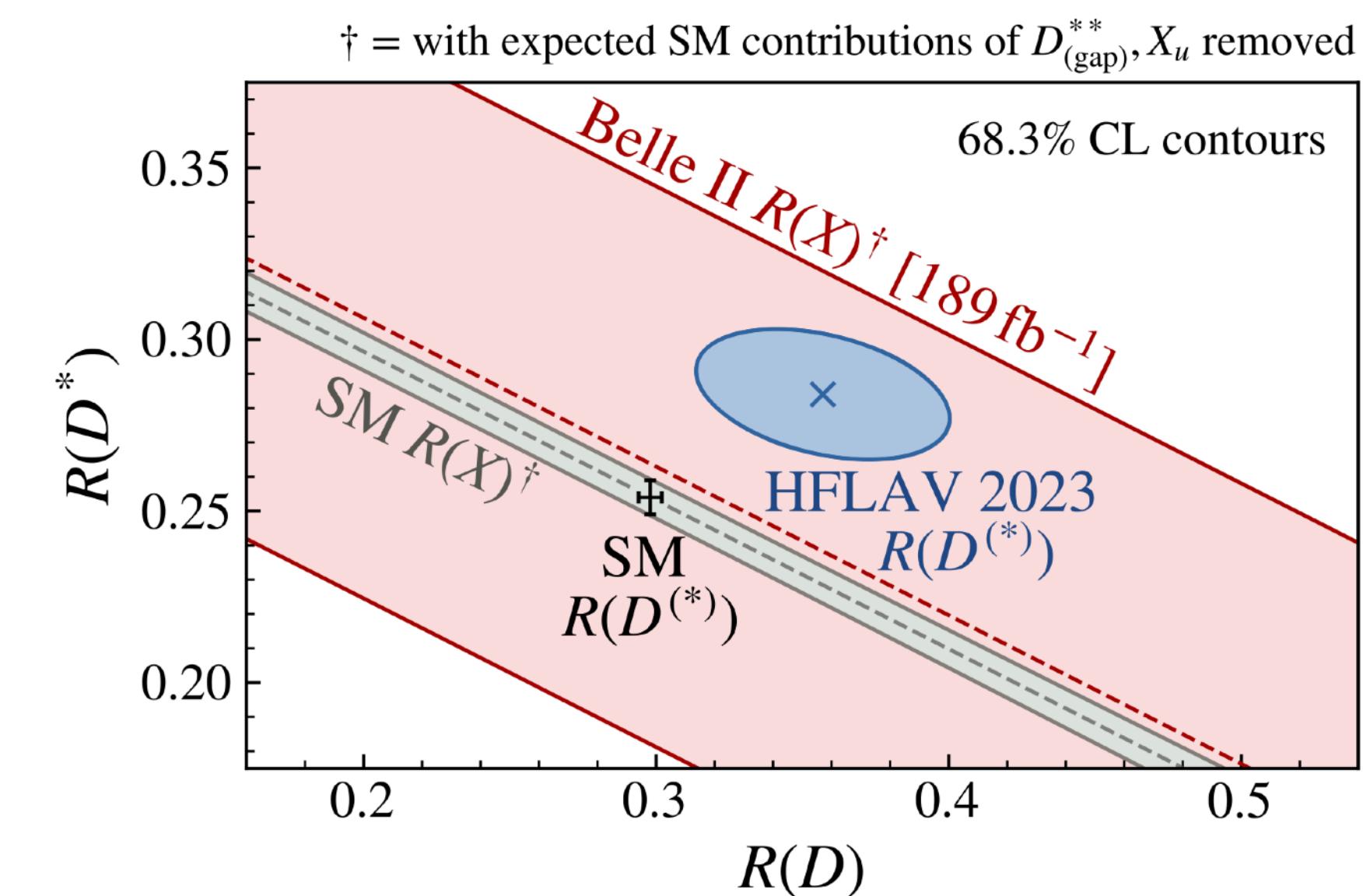
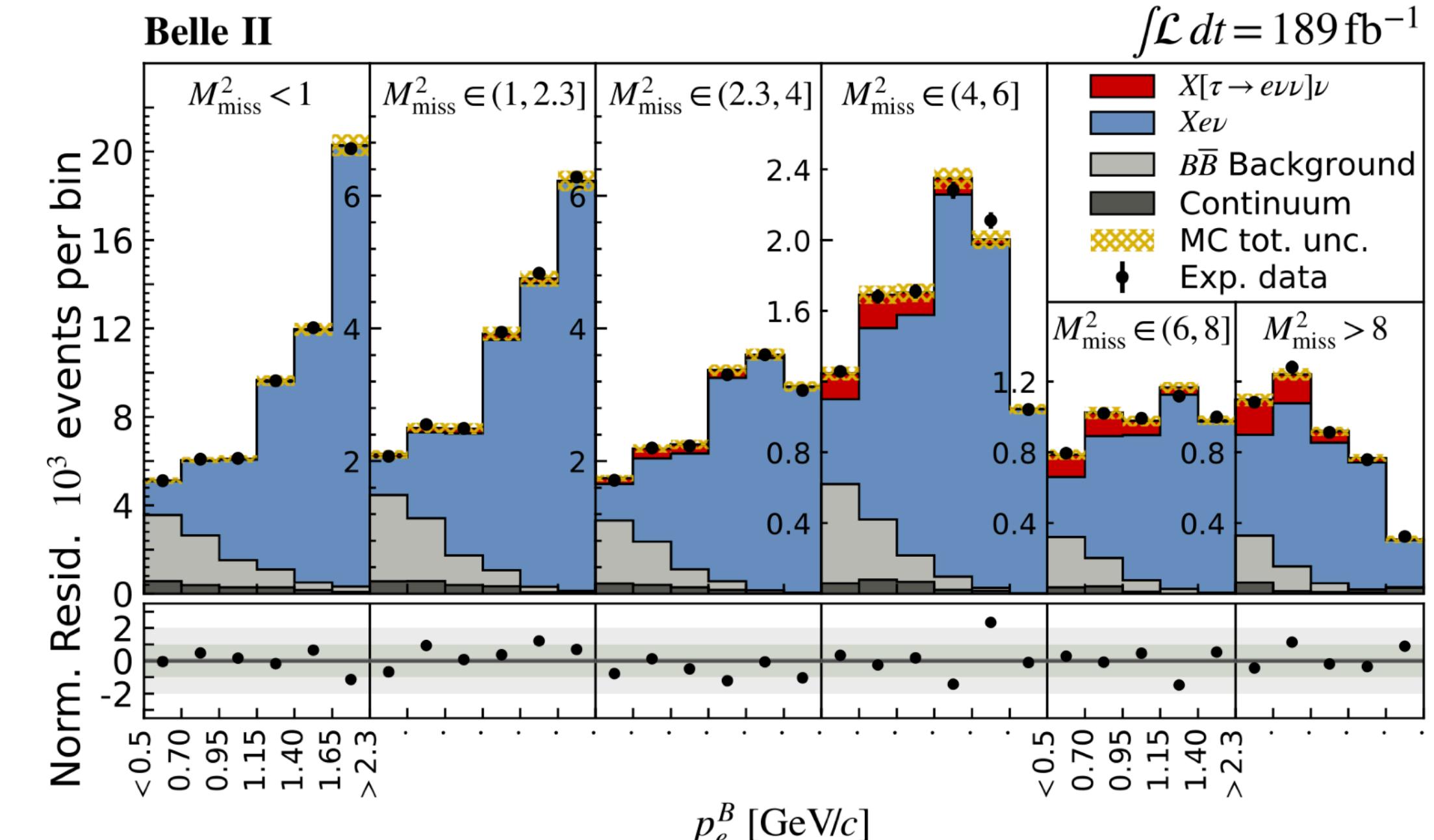
$$R_{\tau/\ell}(X) = 0.228 \pm 0.016 \text{ (stat)} \pm 0.036 \text{ (syst)}$$

$$R_{\tau/e}(X) = 0.232 \pm 0.020 \text{ (stat)} \pm 0.037 \text{ (syst)}$$

$$R_{\tau/\mu}(X) = 0.222 \pm 0.027 \text{ (stat)} \pm 0.050 \text{ (syst)}$$

- Consistent with rough SM expectation

$$R_{\tau/\ell}(X)_{\text{SM}} \approx 0.222$$



Light-lepton universality test

PRL 131, 051804

- First $R(X_{e/\mu})$ measurement

$$R(X_{e/\mu}) = 1.007 \pm 0.009 \text{ (stat)} \pm 0.019 \text{ (syst)}$$

- Most precise BF based LFU test of e- μ universality with semileptonic B decays to date

- Consistent with SM value by 1.2σ

$$R(X_{e/\mu})_{\text{SM}} = 1.006 \pm 0.001 \quad \text{JHEP 11 (2022) 007}$$

- Compatible with exclusive Belle (711 fb^{-1}) measurements

$$R(D^*_{e/\mu}) = 1.01 \pm 0.01 \text{ (stat)} \pm 0.03 \text{ (syst)} \quad \text{PRD 100, 052007 (2019)}$$

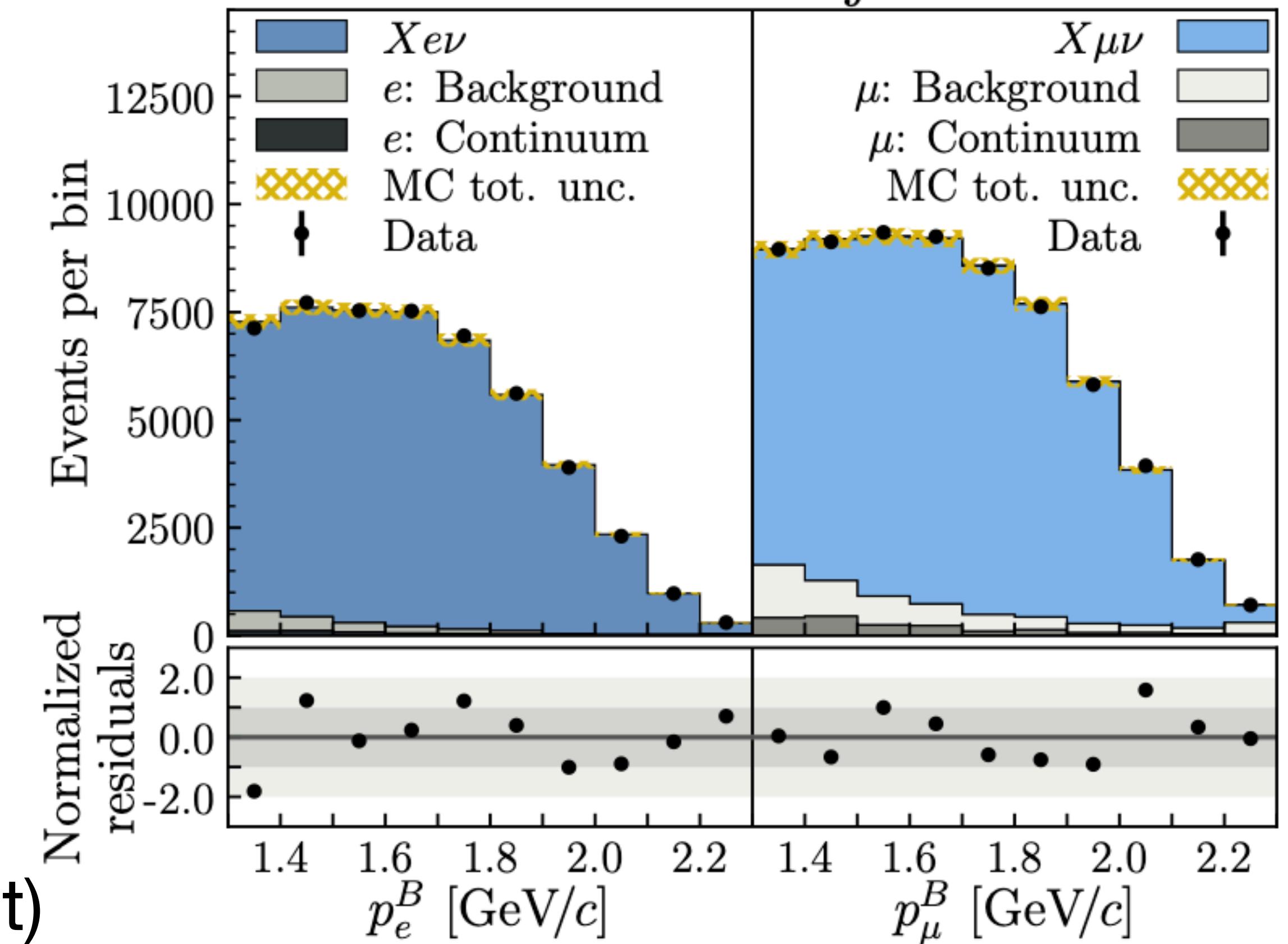
$$R(D^*_{e/\mu}) = 0.993 \pm 0.023 \text{ (stat)} \pm 0.023 \text{ (syst)}$$

[PRD 108, 012002](#)

Signal channel ($B^0\bar{B}^0/B^+B^-$)

Belle II

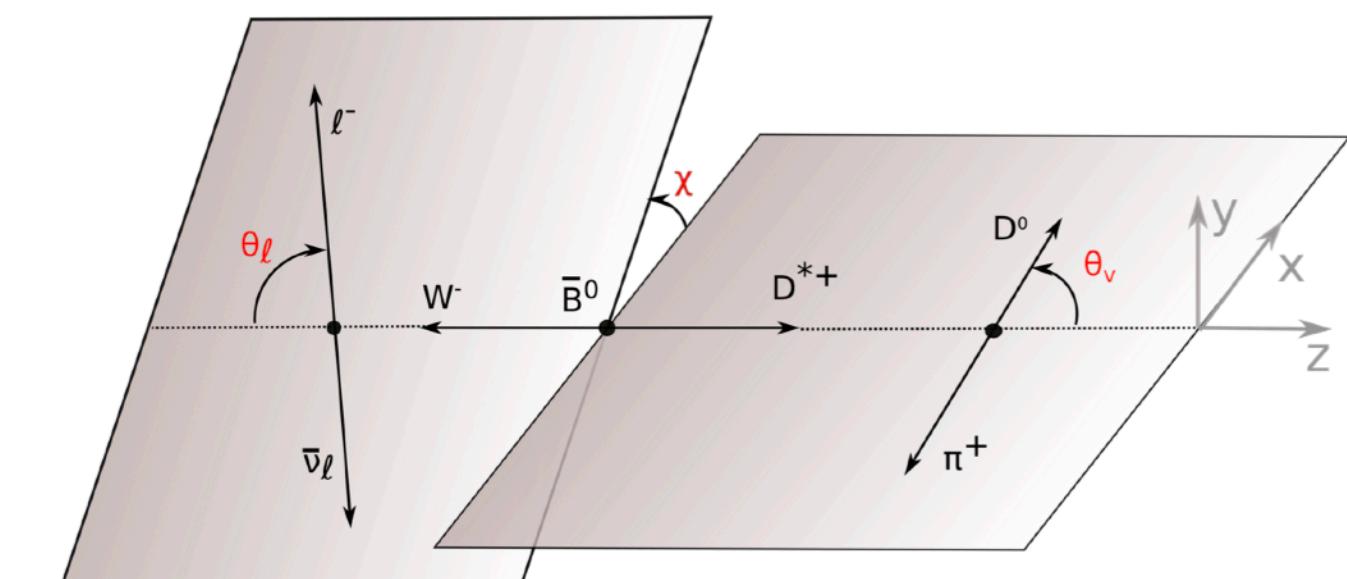
$$\int \mathcal{L} dt = 189 \text{ fb}^{-1}$$



LFU tests in $B \rightarrow D^* l \bar{\nu}$ angular asymmetries

- Measure angular asymmetries separately for $D^* e \bar{\nu}$ and $D^* \mu \bar{\nu}$ final states; their differences are sensitive to LFU violation
- Belle II measures A_{FB} , S_3 , S_5 , S_7 , S_9 (defined in [PRD 107,015011](#)) as a function of w , with $x = \cos\theta_l$ for $A_x(w)$, other choices for S_3-S_9

$$\mathcal{A}_x(w) \equiv \left(\frac{d\Gamma}{dw} \right)^{-1} \left[\int_0^1 - \int_{-1}^0 \right] dx \frac{d^2\Gamma}{dw dx} \quad \mathcal{A}_x(w) = \frac{N_x^+(w) - N_x^-(w)}{N_x^+(w) + N_x^-(w)}$$

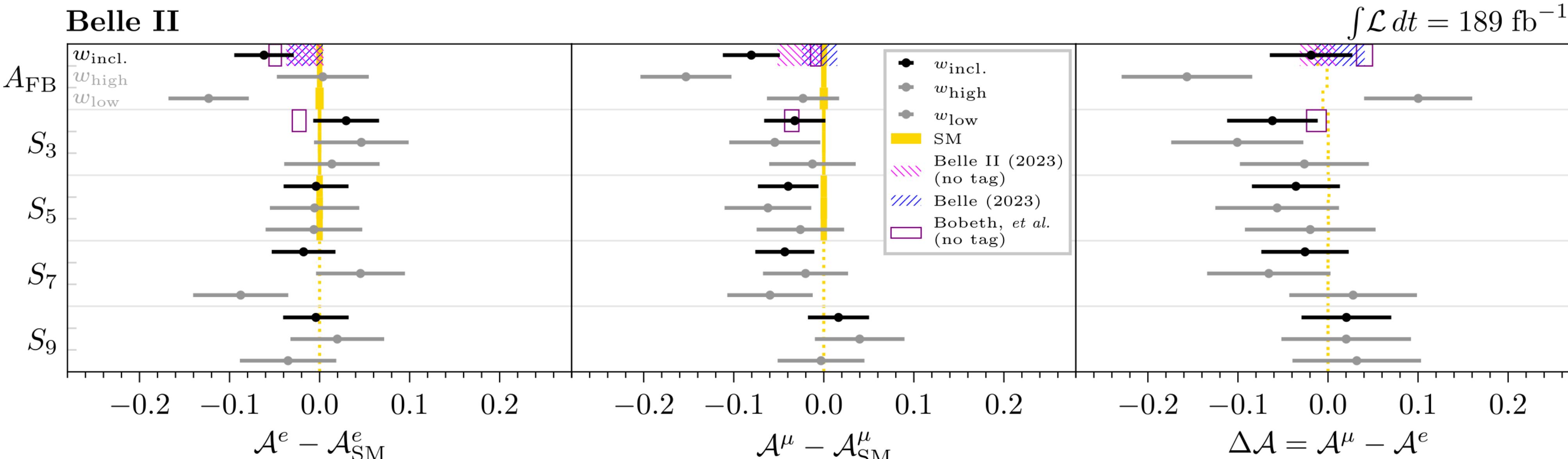
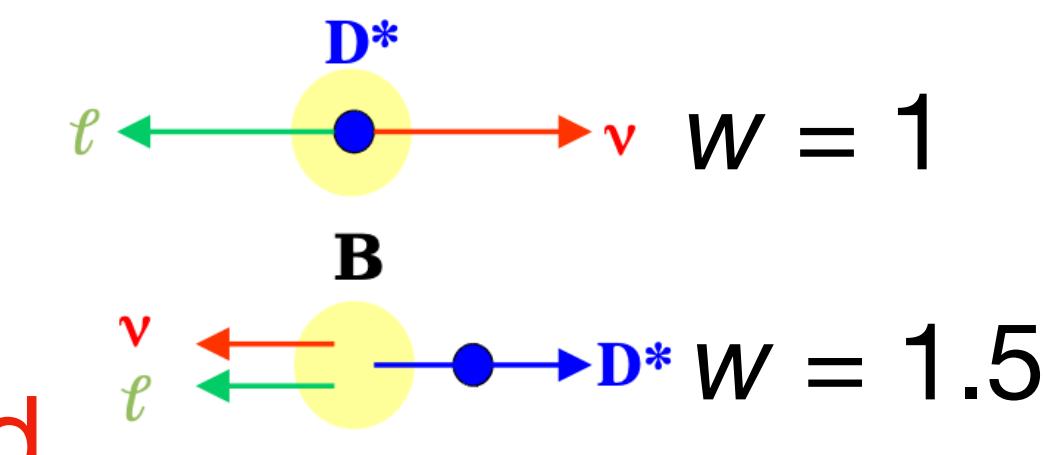


$$w \equiv \frac{m_{B^0}^2 + m_{D^*}^2 - q^2}{2m_B m_{D^*}}$$

- The differences are expected to be small in SM

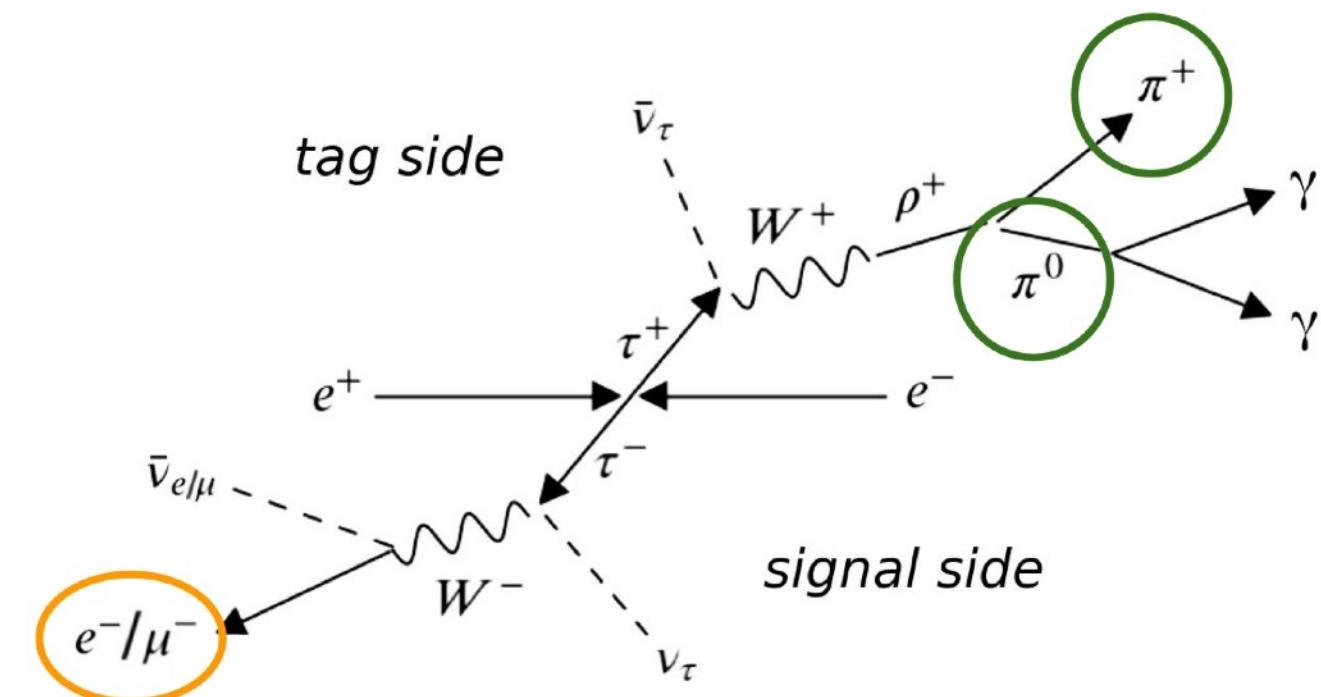
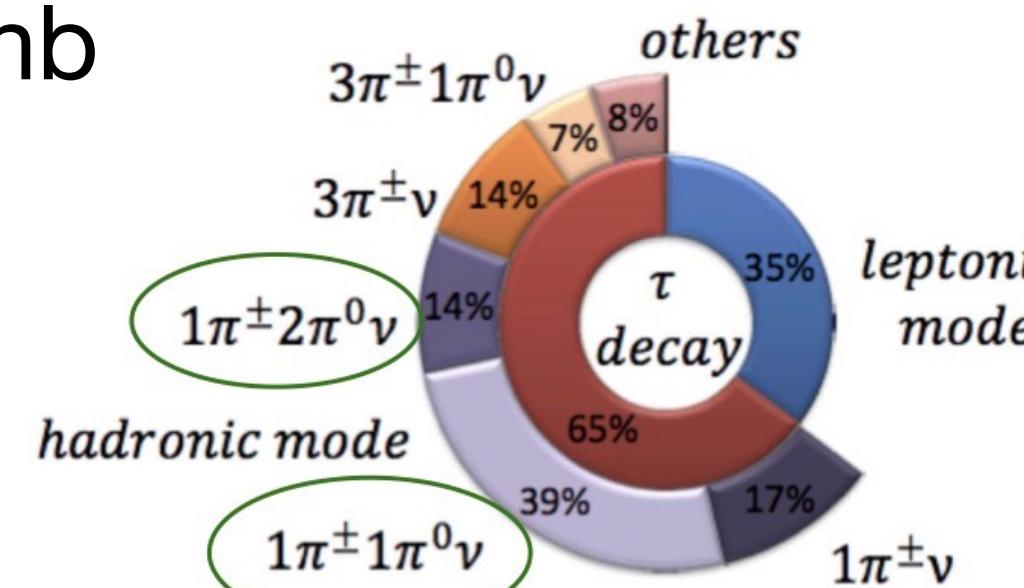
$$\Delta \mathcal{A}_x(w) \equiv \mathcal{A}_x^\mu(w) - \mathcal{A}_x^e(w)$$

- All asymmetry consistent with SM, the measurements are statistics limited



LFU test: τ decays

- Belle II is also a τ factory, $\sigma_\tau = 0.92 \text{ nb} \leftrightarrow \sigma_B = 1.12 \text{ nb}$
 - Produced as τ pairs; tag τ and signal τ
- New analysis: 362 fb^{-1}
 - 1×1 event topology
- Main systematics
 - Particle identification (0.32%)
 - Trigger (0.10%)
- Consistent with the SM at 1.4σ



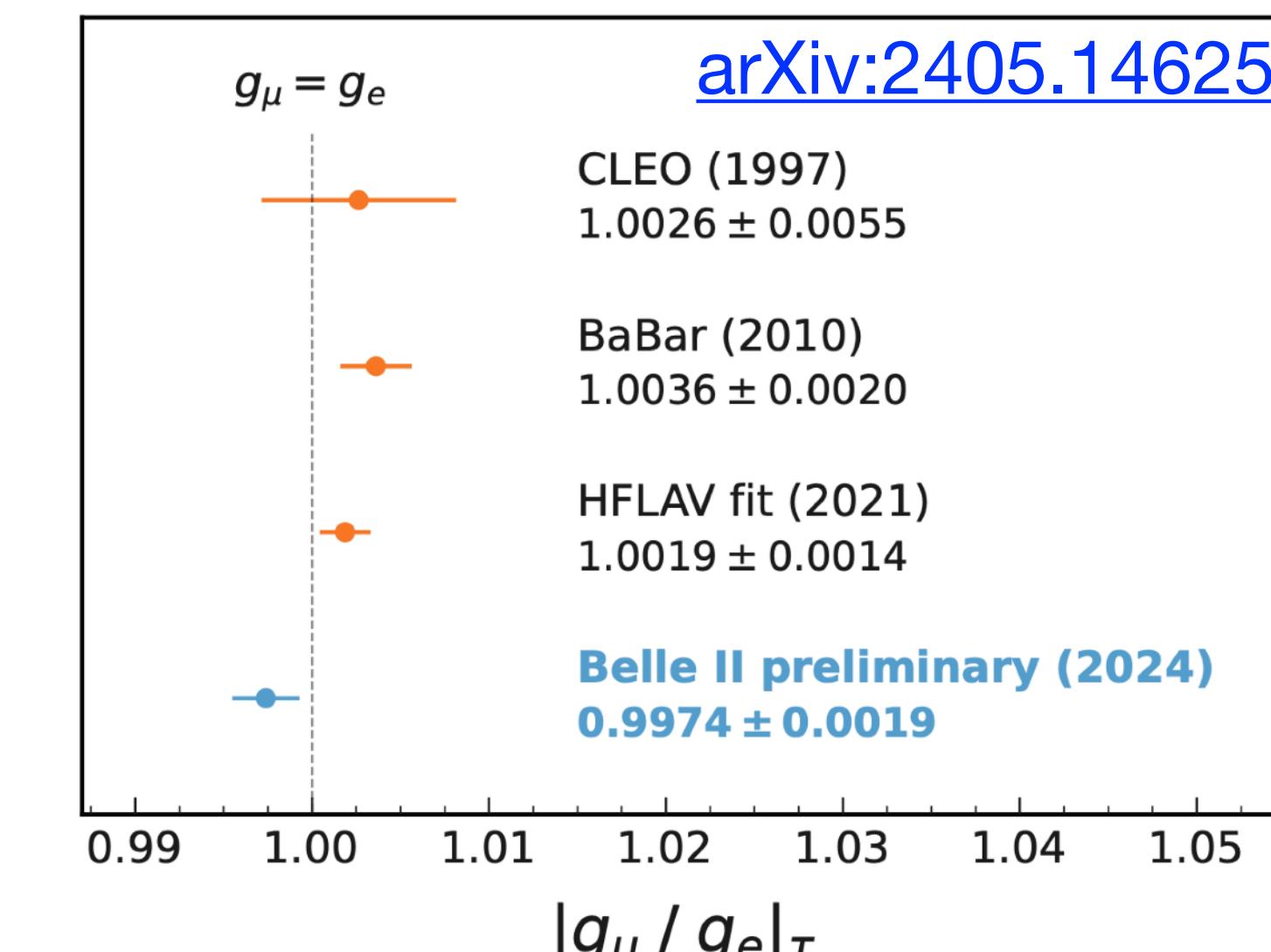
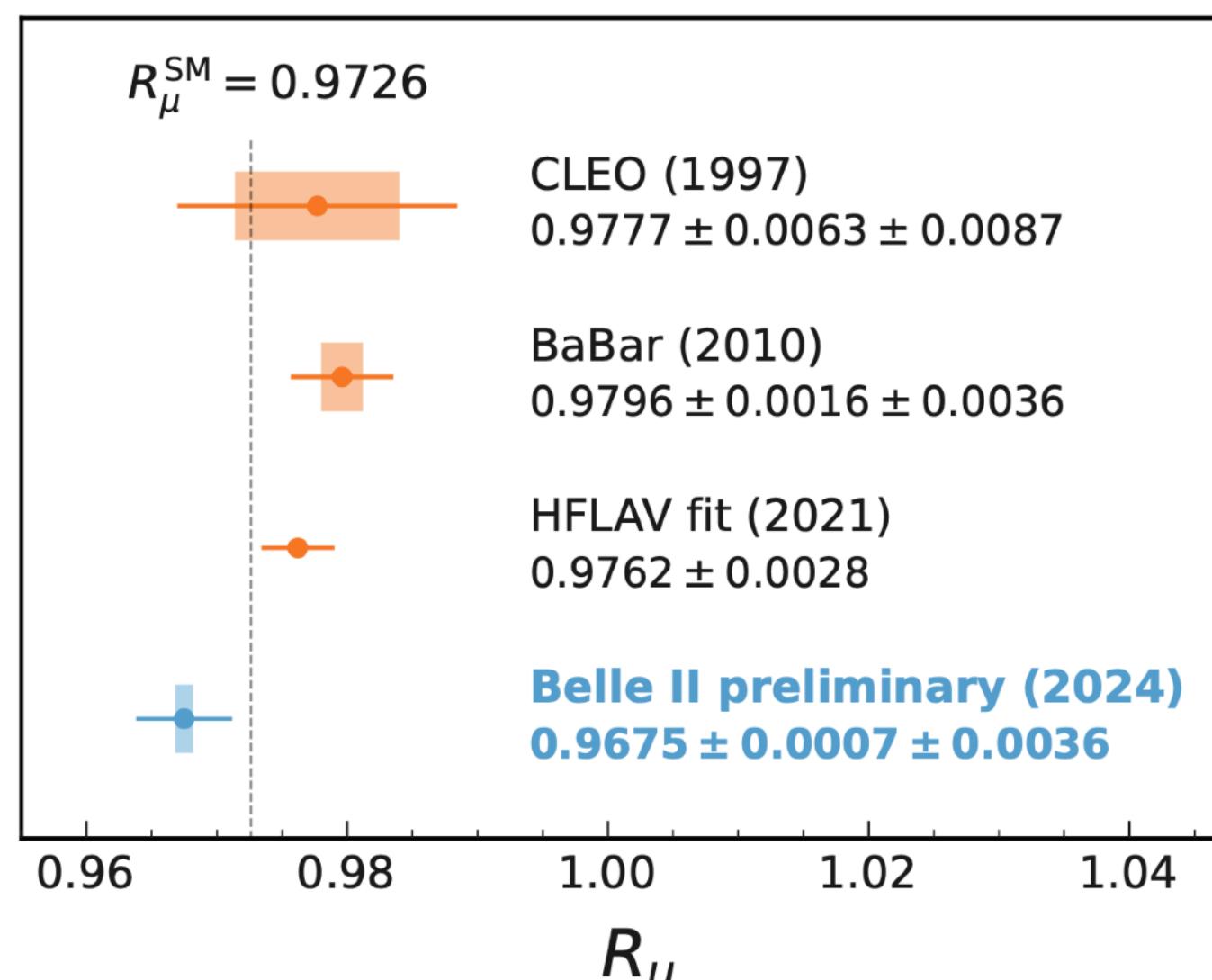
$$R_\mu = \frac{\mathcal{B}(\tau^- \rightarrow \mu^- \bar{\nu}_\mu \nu_\tau)}{\mathcal{B}(\tau^- \rightarrow e^- \bar{\nu}_e \nu_\tau)}$$

Slightly smaller than 1 in the SM due to e-u mass difference ($R_\mu^{\text{SM}} = 0.9726$)

$$\left| \frac{g_\mu}{g_e} \right|_\tau = \sqrt{R_\mu \frac{f(m_e^2/m_\tau^2)}{f(m_\mu^2/m_\tau^2)}}$$

$$f(x) = 1 - 8x + 8x^3 - x^4 - 12x^2 \ln x$$

1 in the SM



Most precise test of LFU in τ decays

Summary and prospects

- $R(D^*)$ shows 3.3σ deviation between experimental average value and standard model prediction
 - Hint of Lepton Flavor Universality Violation
- Belle II performed new tests of LFU based on 189 fb^{-1} data
 - $R_{\tau/\ell}(D^*) = 0.267^{+0.041}_{-0.039} \text{ (stat)}^{+0.028}_{-0.033} \text{ (syst)}$
 - $R_{\tau/\ell}(X) = 0.228 \pm 0.016 \text{ (stat)} \pm 0.036 \text{ (syst)}$
- Light lepton universality, angular asymmetry differences ΔAx also measured, statistics limited
- Most precise test of LFU in τ decays 362 fb^{-1} data
- SuperKEKB/Belle II will resume operation at the beginning of 2024 after LS1

