

# Review of $\Sigma(1/2^-)$

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第九届手征有效场论研讨会

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EW, LSGeng, JJWu, JJXie, and BSZou, Chin. Phys. Lett. 41, 101401 [arXiv:2406.07839]

# Exotic states

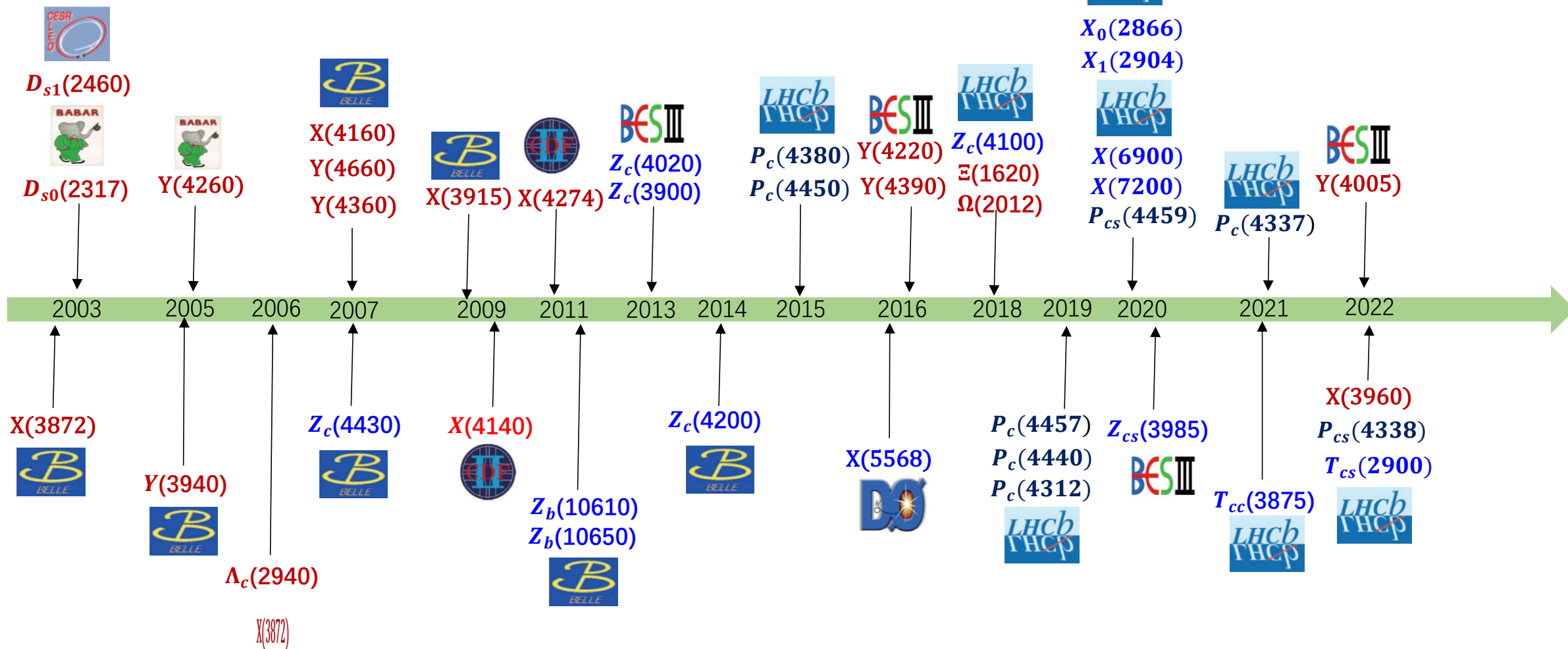


耿立升老师报告

## Exotic mesons or baryons

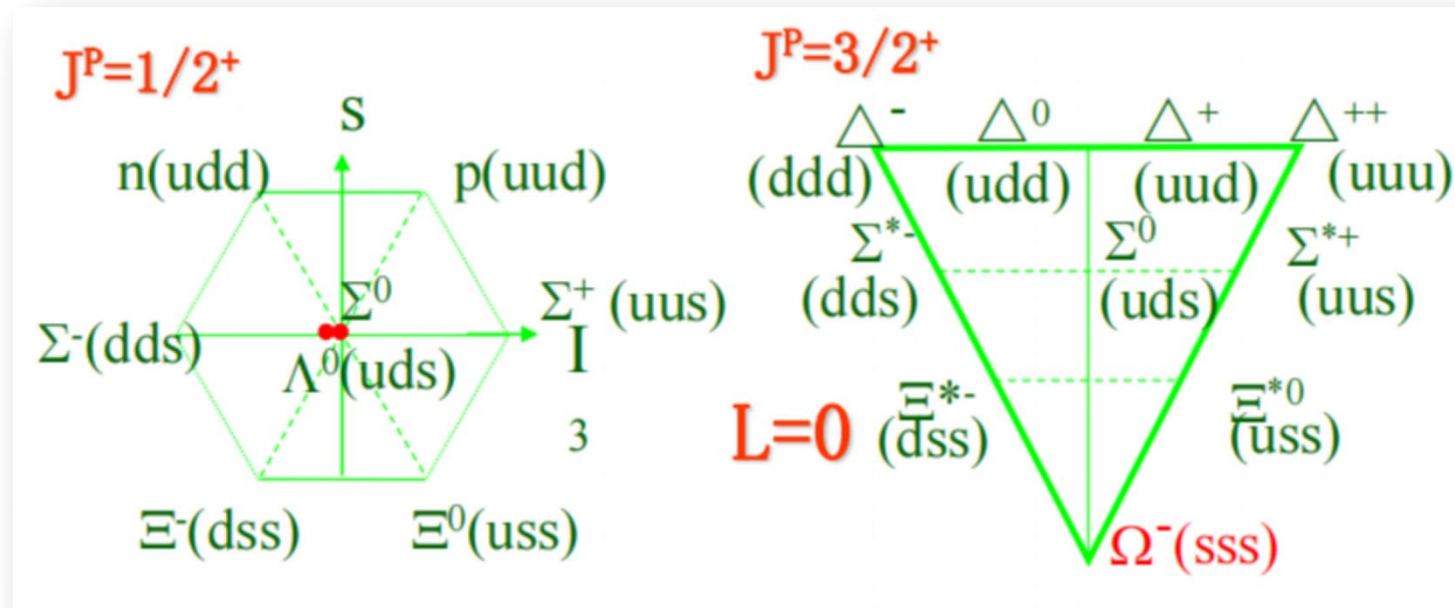
## Tetraquark states

## Pentaquark states



# Ground light baryons

## □ground baryons



**盖尔曼-大久保质量:**  $M = a + bY + c \left[ I(I + 1) - \frac{1}{4}Y^2 \right]$

**质量公式预言**  $m_{\Omega} = 1670 \text{ MeV}$   
**实验:**  $m_{\Omega} = 1672.45 \pm 0.29 \text{ MeV}$

# Low-lying baryons with $J^P=1/2^-$

- Two poles of  $\Lambda(1405)$
- mass reverse problem
- Large couplings of  $N(1535)$  to  $N\eta$ ,  $K\Lambda$
- Different lineshapes of  $\Lambda(1670)$
- Missing  $\Sigma(1/2^-)$

Citation: R.L. Workman et al. (Particle Data Group), Prog.Theor.Exp.Phys. **2022**, 083C01 (2022)

$\Sigma(1620) 1/2^-$   $I(J^P) = 1(\frac{1}{2}^-)$  Status: \*

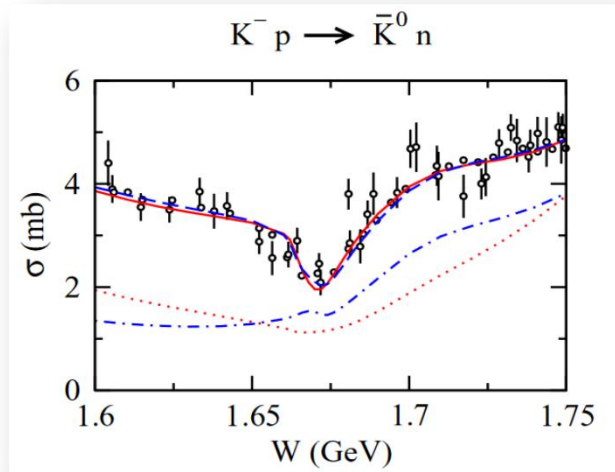
OMITTED FROM SUMMARY TABLE

Citation: M. Tanabashi et al. (Particle Data Group), Phys. Rev. D **98**, 030001 (2018) and 2019 update

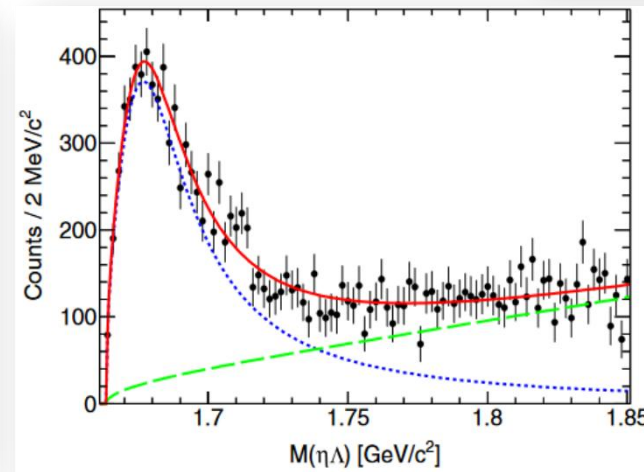
$\Sigma(1480)$  Bumps  $I(J^P) = 1(?^-)$  Status: \*

OMITTED FROM SUMMARY TABLE

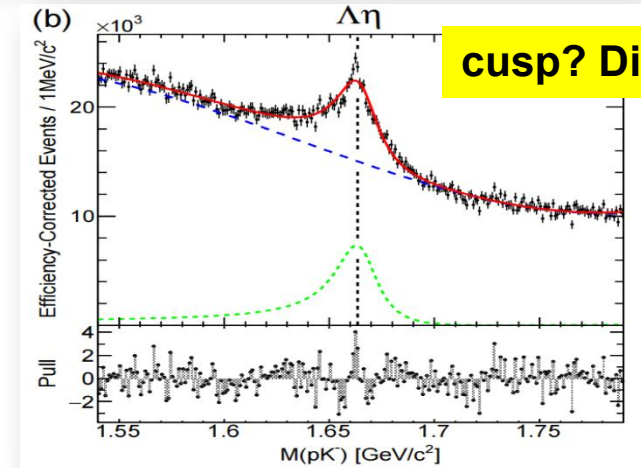
These are peaks seen in  $\Lambda\pi$  and  $\Sigma\pi$  spectra in the reaction  $\pi^+ p \rightarrow (Y\pi)K^+$  at 1.7 GeV/c. Also, the  $Y$  polarization oscillates in the same region.



PLB527(2002) 99

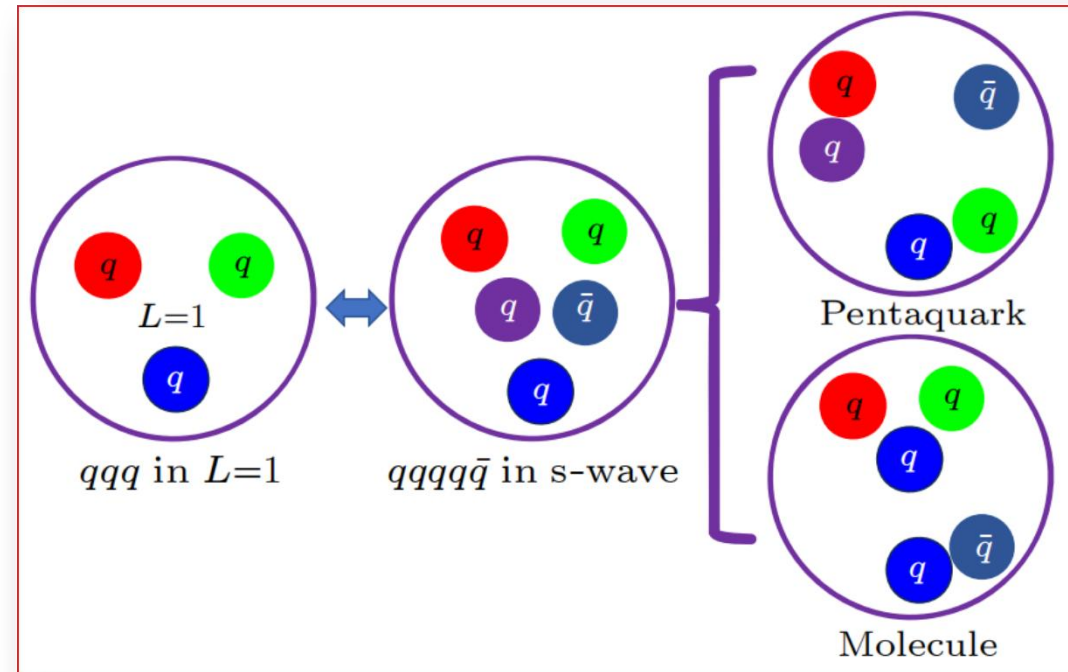
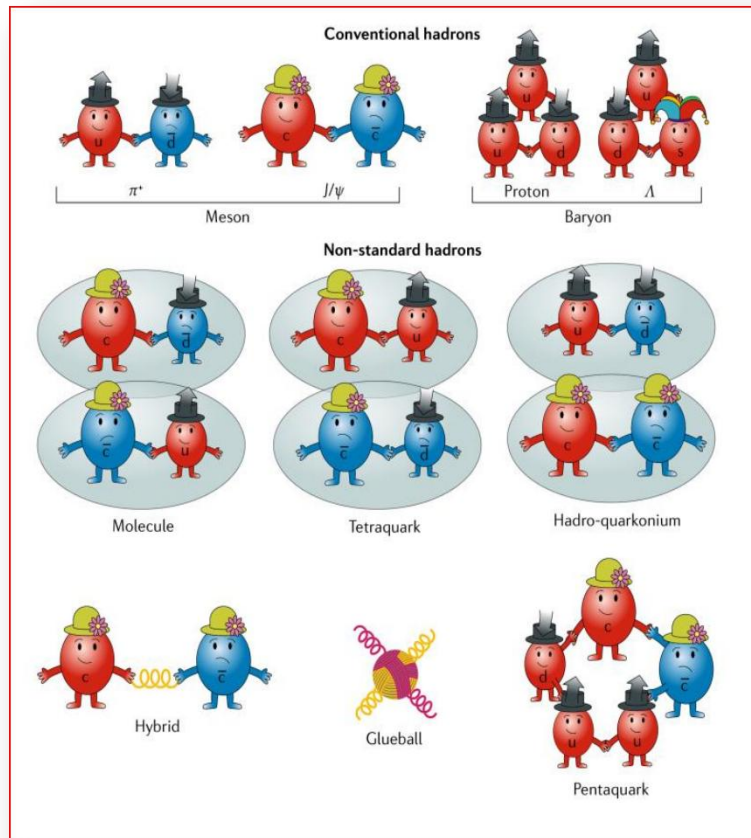


Belle,  
PRD103(2021)052005

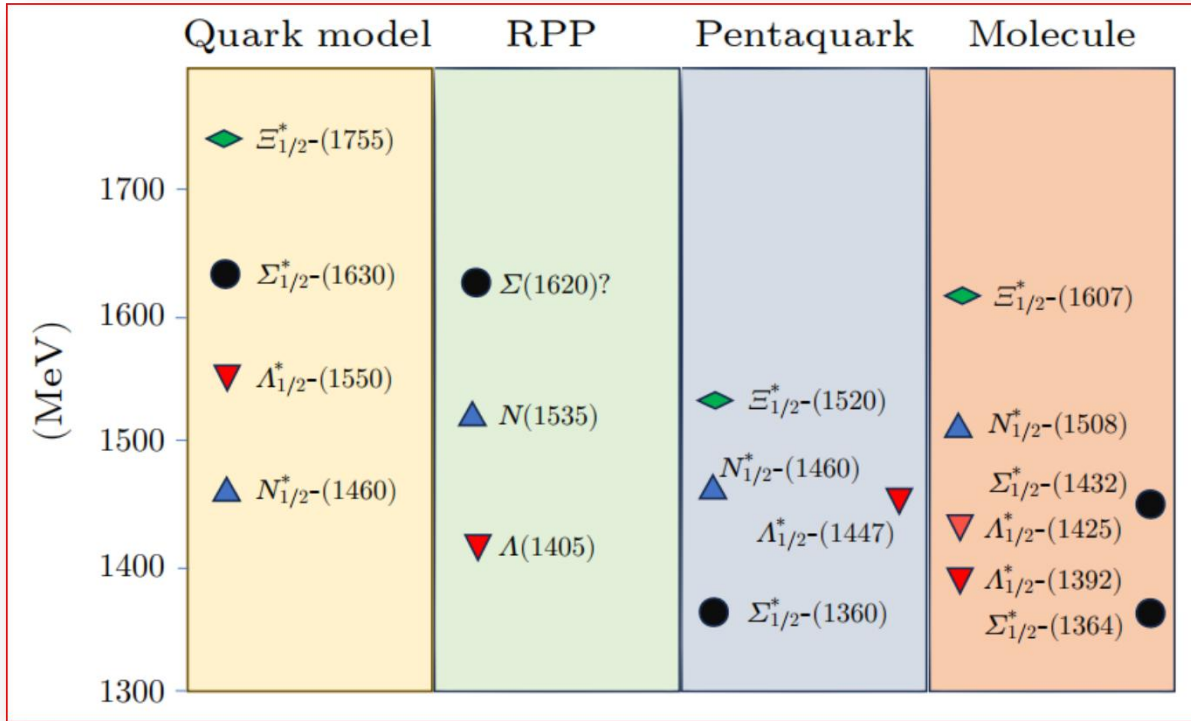


Belle: PRD108 (2023) L031104

# Exotic structures of Hadrons



C.Z.Yuan, Nature Rev. Phys. 1 (2019) 480



## 1/2<sup>-</sup> baryon nonet with strangeness

Zou, EPJA 35 (2008) 325

- Mass pattern : quenched or unquenched ?

$$\text{uds (L=1) } 1/2^- \sim \Lambda^*(1670) \sim [\text{us}][\text{ds}] \bar{s}$$

$$\text{uud (L=1) } 1/2^- \sim N^*(1535) \sim [\text{ud}][\text{us}] \bar{s}$$

$$\text{uds (L=1) } 1/2^- \sim \Lambda^*(1405) \sim [\text{ud}][\text{su}] \bar{u}$$

$$\text{uus (L=1) } 1/2^- \sim \Sigma^*(1390) \sim [\text{us}][\text{ud}] \bar{d}$$

Zou et al, NPA835 (2010) 199 ; CLAS, PRC87(2013)035206

- Strange decays of  $N^*(1535)$  and  $\Lambda^*(1670)$  :

$$N^*(1535) \text{ large couplings } g_{N^*N\eta}, g_{N^*K\Lambda}, g_{N^*N\eta'}, g_{N^*N\phi}$$

$$\Lambda^*(1670) \text{ large coupling } g_{\Lambda^*\Lambda\eta}$$

邹冰松老师报告

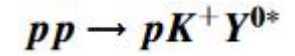
# Exp. signals of $\Sigma(1480)$



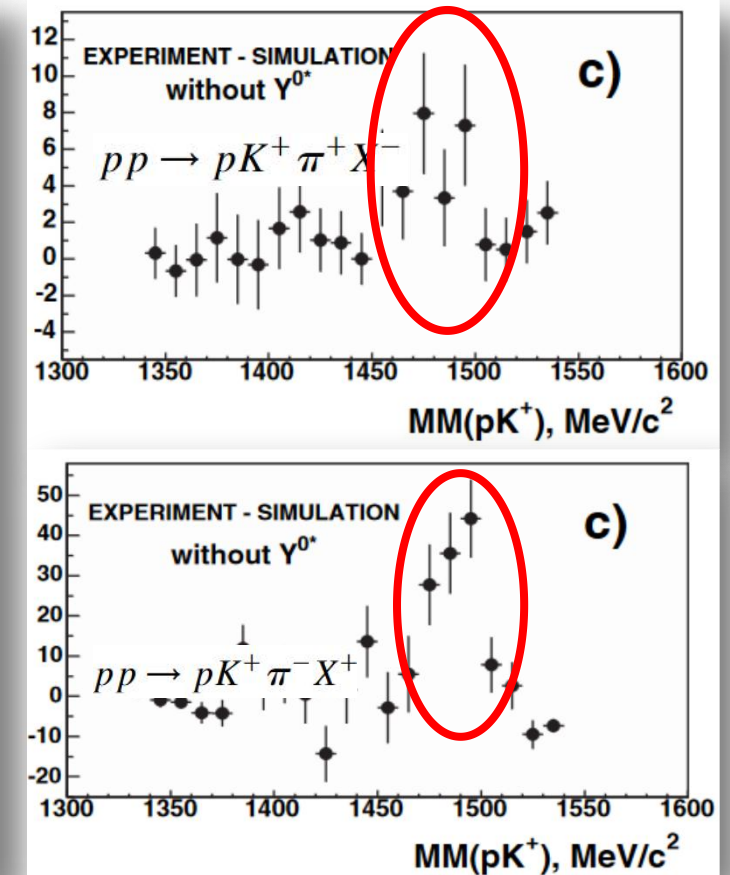
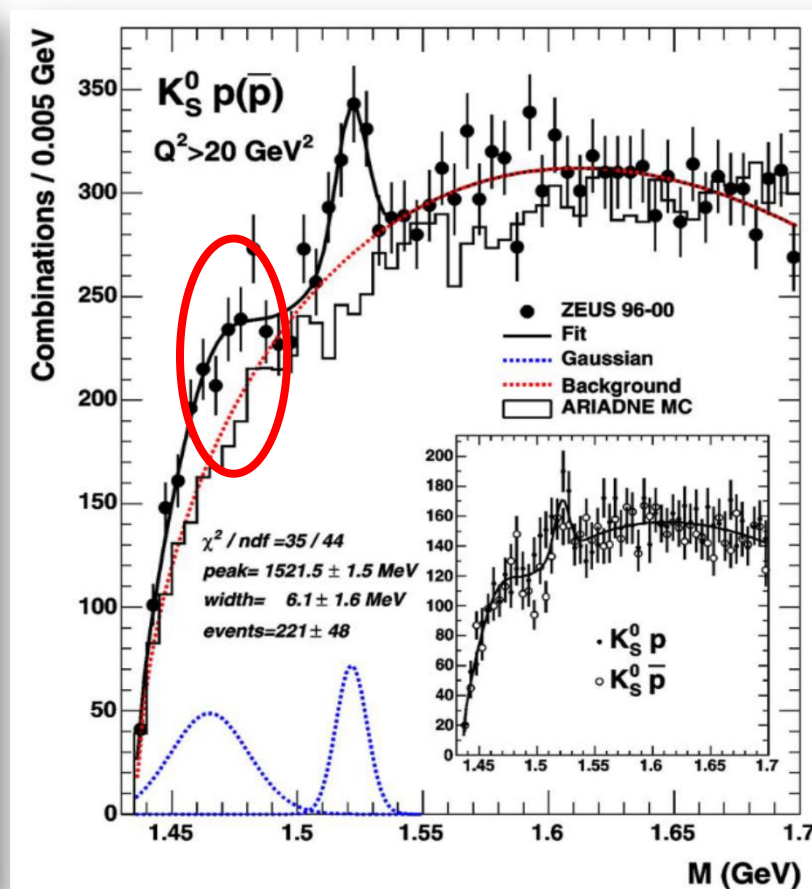
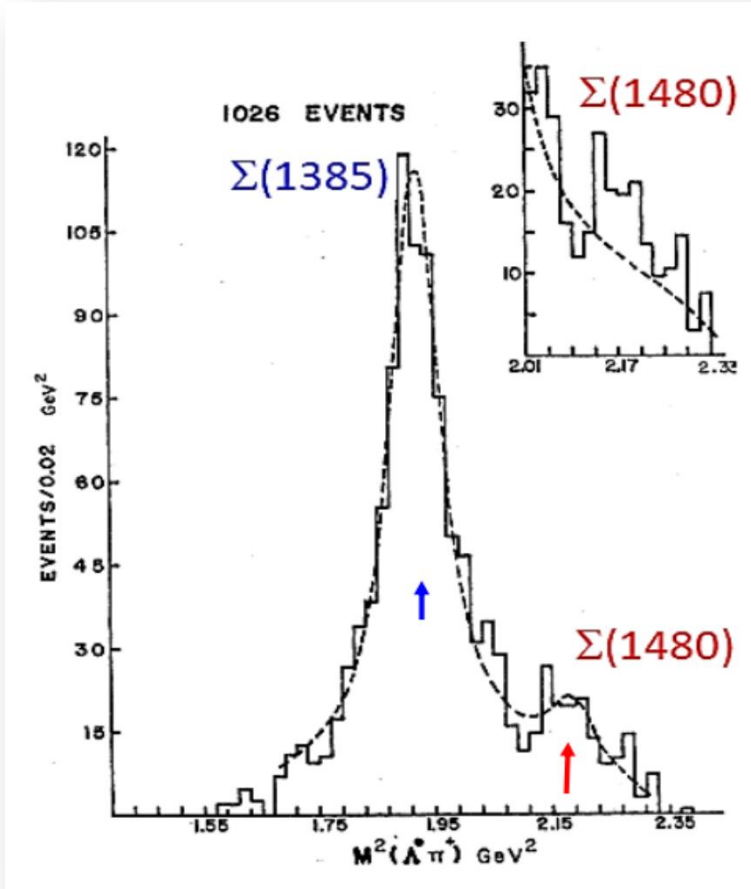
Yu-Li Pan et al, PRD2, 449 (1970)



ZEUS PLB591 (2004) 7-22

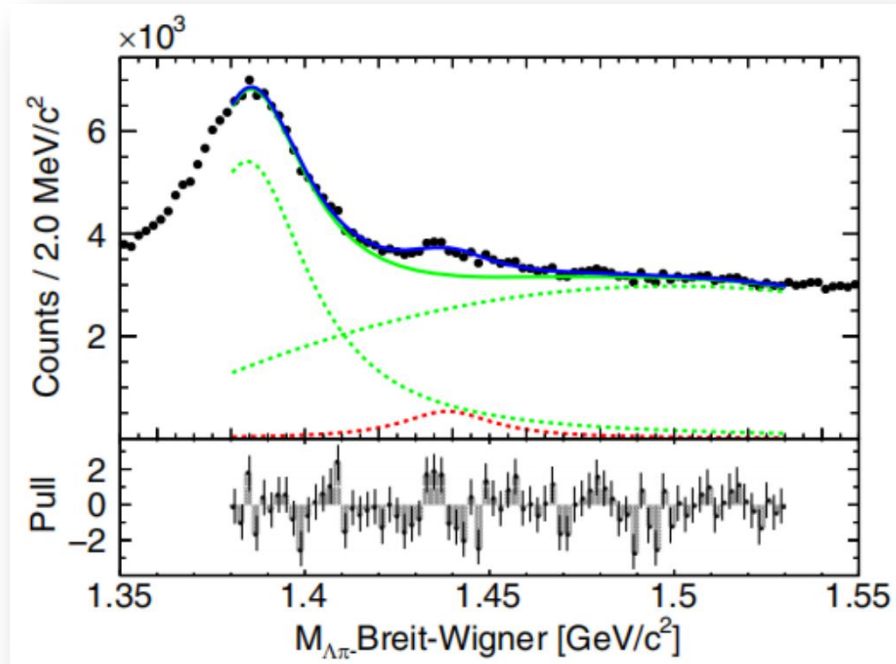
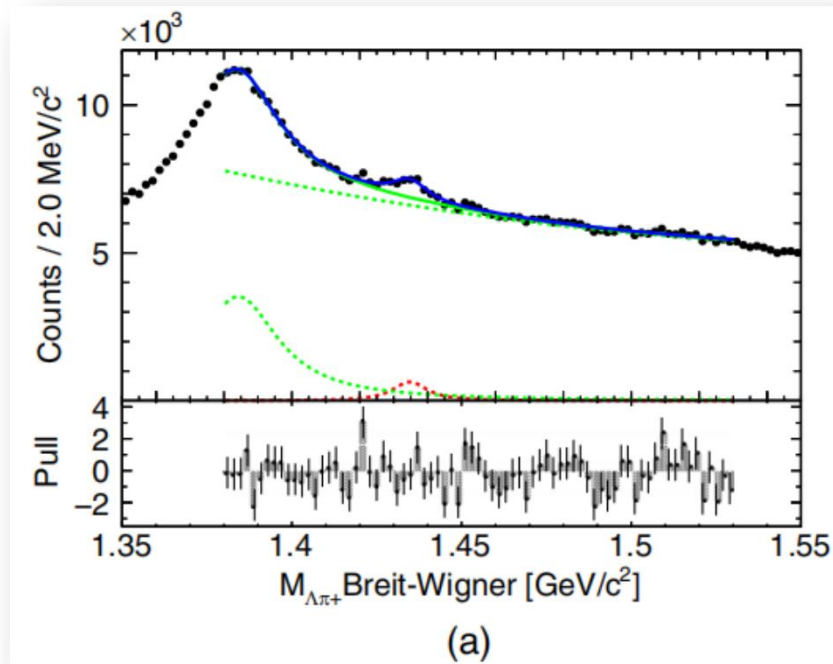


COSY-Ju;ich PRL 96, 012002 (2006)



# $\Sigma(1/2^-)$ -like structure

$\square \Lambda_c \rightarrow \Lambda \pi^+ \pi^+ \pi^-$ , Belle, PRL130, 151903 (2023)



| Mode            | $E_{\text{BW}}$ (MeV/ $c^2$ ) | $\Gamma$ (MeV/ $c^2$ ) | $\chi^2/\text{NDF}$ |
|-----------------|-------------------------------|------------------------|---------------------|
| $\Lambda \pi^+$ | $1434.3 \pm 0.6$              | $11.5 \pm 2.8$         | 74.4/68             |
| $\Lambda \pi^-$ | $1438.5 \pm 0.9$              | $33.0 \pm 7.5$         | 92.3/68             |

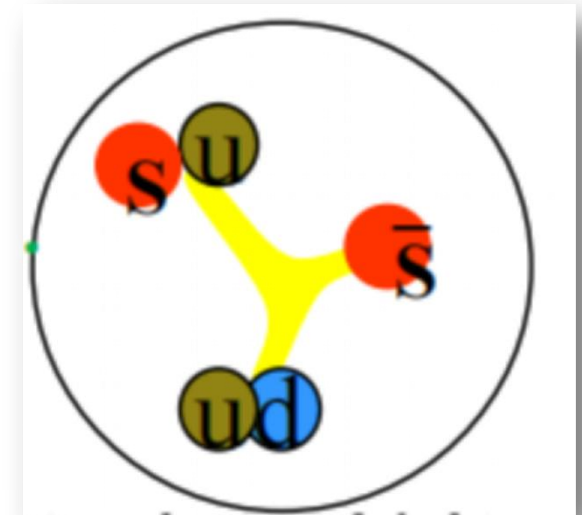


# Low-lying baryons with $J^P=1/2^-$

- **Pentaquark**, S. L. Zhu, etc. High Energy Phys. Nucl. Phys. 29, 250(2005).

Table 2. Flavor wave functions and masses of the  $\frac{1}{2}^-$  pentaquark octet and singlet.

|              | $(Y, I)$            | $I_3$          | flavor wave functions   | masses (MeV) |
|--------------|---------------------|----------------|---|--------------|
| $\rho_8$     | $(1, \frac{1}{2})$  | $\frac{1}{2}$  | $[su][ud]_-\bar{s}$   | 1460         |
| $n_8$        |                     | $-\frac{1}{2}$ | $[ds][ud]_-\bar{s}$   | 1460         |
| $\Sigma_8^+$ | $(0, 1)$            | 1              | $[su][ud]_-\bar{d}$   | 1360         |
| $\Sigma_8^0$ |                     | 0              | $\frac{1}{\sqrt{2}}([su][ud]_-\bar{u} + [ds][ud]_-\bar{d})$                   | 1360         |
| $\Sigma_8^-$ |                     | -1             | $[ds][ud]_-\bar{u}$   | 1360         |
| $\Delta_8$   | $(0, 0)$            | 0              | $\frac{[ud][su]_-\bar{u} + [ds][ud]_-\bar{d} - 2[su][ds]_-\bar{s}}{\sqrt{6}}$ | 1533         |
| $\Xi_8^0$    | $(-1, \frac{1}{2})$ | $\frac{1}{2}$  | $[ds][su]_-\bar{d}$   | 1520         |
| $\Xi_8^-$    |                     | $-\frac{1}{2}$ | $[ds][su]_-\bar{u}$   | 1520         |
| $\Delta_1$   | $(0, 0)$            | 0              | $\frac{[ud][su]_-\bar{u} + [ds][ud]_-\bar{d} + [su][ds]_-\bar{s}}{\sqrt{3}}$  | 1447         |





# Low-lying baryons with $J^P=1/2^-$

- **Pentaquark**, C. Helminen and D. O. Riska, NPA699, 624(2002).

PDG2001

$[4]_X[1111]_{CFS}[211]_C$   
 $[f]_{FS}[f]_F[f]_S$

Energy  
(MeV)

$J^P$

$\Lambda$  (emp.)

$\Sigma$  (emp.)

$\Sigma(1560)$  Bumps

$I(J^P) = 1(?^-)$  Status: \*\*

OMITTED FROM SUMMARY TABLE

This entry lists peaks reported in mass spectra around 1560 MeV without implying that they are necessarily related.

$[31]_{FS}[211]_F[22]_S$

1509

$\frac{1}{2}^-$

$\Lambda(1405)$

$\Sigma(1560)(**)$

$[31]_{FS}[211]_F[31]_S$

1565

$\frac{1}{2}^-$

$\Sigma(1560)(**), \Sigma(1620)(**)$

$\frac{3}{2}^-$

$\Lambda(1520)$

$\Sigma(1580)(**)$

VALUE (MeV) \_\_\_\_\_ EVTS

≈ 1560 OUR ESTIMATE

1553 ± 7 121

1572 ± 4 40

VALUE (MeV) \_\_\_\_\_

79 ± 30

15 ± 6

unknown. If indeed the  $\Lambda(1405)$  is partly a 5-quark state, **it would be natural to expect the  $\Sigma(1560)$  to be the analog of the  $\Lambda(1405)$ , and thus that it has  $J^P = \frac{1}{2}^-$ .** This is indeed what the structure of the  $qqqq\bar{q}$  spectrum shown in Table 7 indicates. This would also explain why the usual quark-model description of the baryons as 3-quark states cannot predict sufficiently low energies for the  $\Lambda(1405)$  and  $\Sigma(1560)$  [4]. The  $\Sigma(1480)(*)$

# Low-lying baryons with $J^P=1/2^-$

## □ Chiral Lagrangian

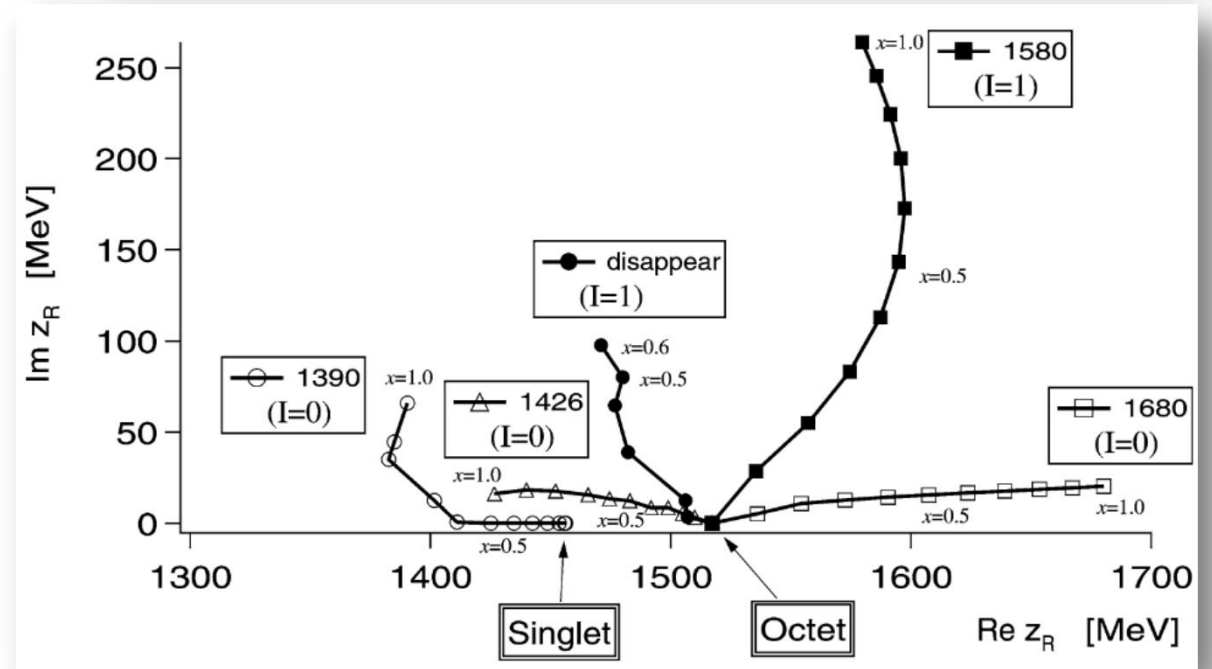
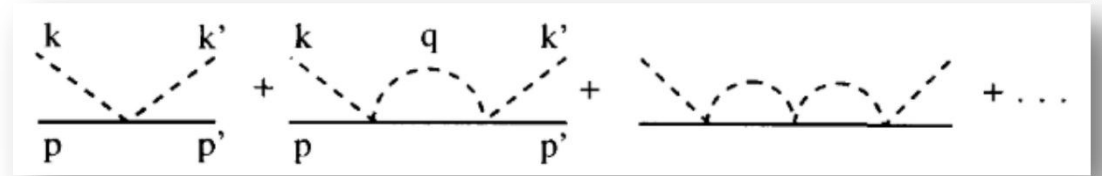
$$L_1^{(B)} = \langle \bar{B} i \gamma^\mu \nabla_\mu B \rangle - M_B \langle \bar{B} B \rangle + \frac{1}{2} D \langle \bar{B} \gamma^\mu \gamma_5 \{ u_\mu, B \} \rangle + \frac{1}{2} F \langle \bar{B} \gamma^\mu \gamma_5 [ u_\mu, B ] \rangle$$

$$V_{ij} = -C_{ij} \frac{1}{4f^2} (k^0 + k'^0)$$

$$T = [1 - VG]^{-1} V \quad T_{ij} = \frac{g_i g_j}{z - z_R}$$

$$G_l = i \int \frac{d^4 q}{(2\pi)^4} \frac{M_l}{E_l(\mathbf{q})} \frac{1}{k^0 + p^0 - q^0 - E_l(\mathbf{q}) + i\epsilon} \frac{1}{q^2 - m_l^2 + i\epsilon}$$

$$= \int \frac{d^3 q}{(2\pi)^3} \frac{1}{2\omega_l(q)} \frac{M_l}{E_l(\mathbf{q})} \frac{1}{p^0 + k^0 - \omega_l(\mathbf{q}) - E_l(\mathbf{q}) + i\epsilon}$$





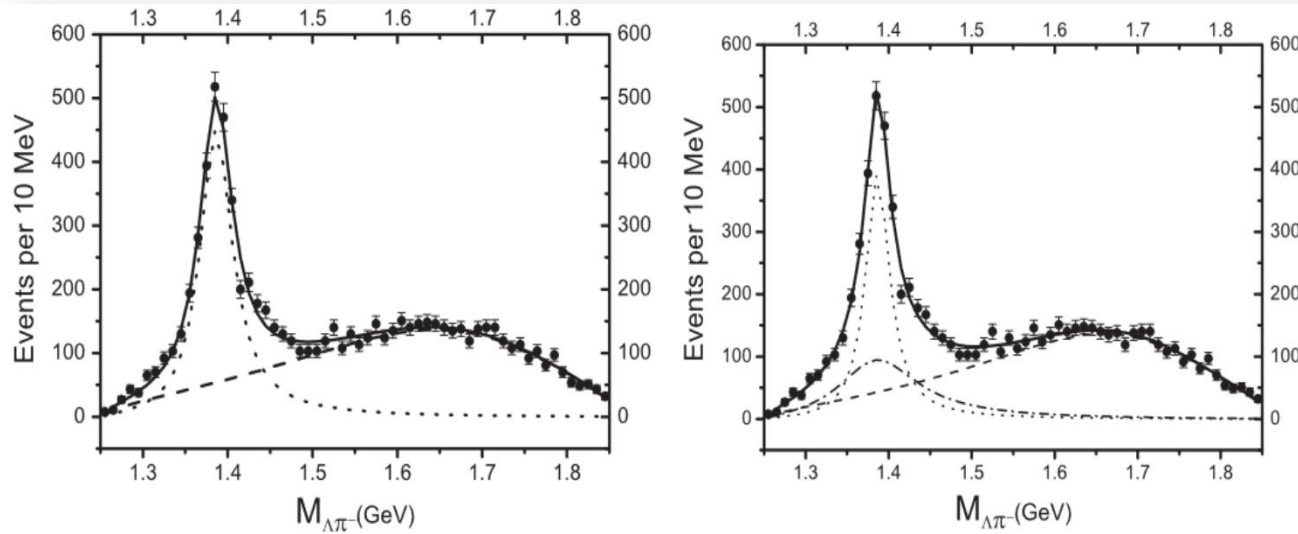
# Search for $\Sigma(1/2^-)$

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- hadron-hadron scattering,  $Kp$ ,  $\Lambda p$
- $\gamma$ -production,  $\nu$ -production
- charmed baryon decays
- charmonium decays

# Hadron-hadron scattering

□  $K^- p \rightarrow \Lambda \pi^+ \pi^-$ , Wu-Dulat-Zou, PRD80(2009)017503

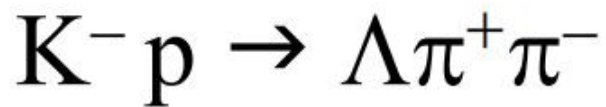


$$\frac{dN}{dm_{\Lambda\pi^-}} \propto p_1 \times p_2 \times \sum_{i=1}^3 \frac{|a_i|}{(m_{\Lambda\pi^-}^2 - m_i^2)^2 + m_i^2 \times \Gamma_i^2}$$

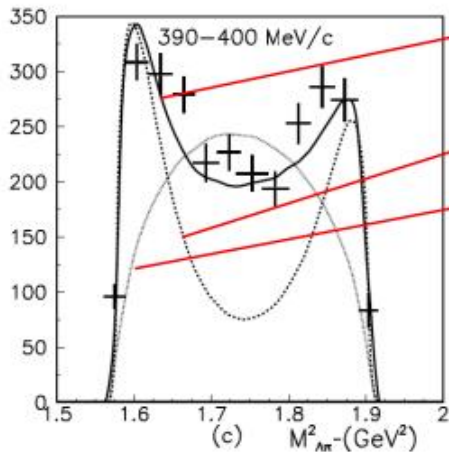
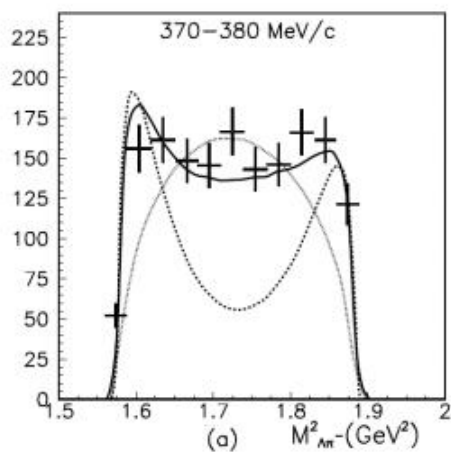
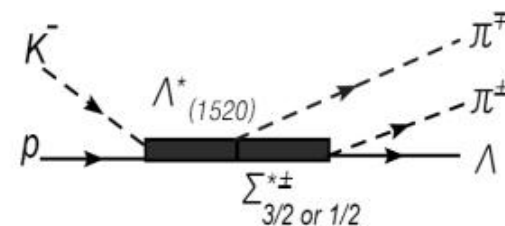
Here we reexamine some old data of the  $K^- p \rightarrow \Lambda \pi^+ \pi^-$  reaction and find that besides the well-established  $\Sigma^*(1385)$  with  $J^P = 3/2^+$ , there is indeed some evidence for the possible existence of a new  $\Sigma^*$  resonance with  $J^P = 1/2^-$  around the same mass but with broader decay width. There are also indications for such a possibility in the  $J/\psi \rightarrow \bar{\Sigma} \Lambda \pi$  and  $\gamma n \rightarrow K^+ \Sigma^{*-}$  reactions. At present, the evidence is not strong. Therefore, high statistics studies

|      | $M_{\Sigma^*(3/2)}$    | $\Gamma_{\Sigma^*(3/2)}$ | $M_{\Sigma^*(1/2)}$    | $\Gamma_{\Sigma^*(1/2)}$ | $\chi^2/\text{ndf}$ (Fig. 1) | $\chi^2/\text{ndf}$ (Fig. 2) |
|------|------------------------|--------------------------|------------------------|--------------------------|------------------------------|------------------------------|
| Fit1 | $1385.3 \pm 0.7$       | $46.9 \pm 2.5$           |                        |                          | 68.5/54                      | 10.1/9                       |
| Fit2 | $1386.1^{+1.1}_{-0.9}$ | $34.9^{+5.1}_{-4.9}$     | $1381.3^{+4.9}_{-8.3}$ | $118.6^{+55.2}_{-35.1}$  | 58.0/51                      | 3.2/9                        |

J.J.Wu's slide



$P_K=0.3-0.6$  GeV J. J. Wu, S. Dulat and B. S. Zou PRC 81,045210

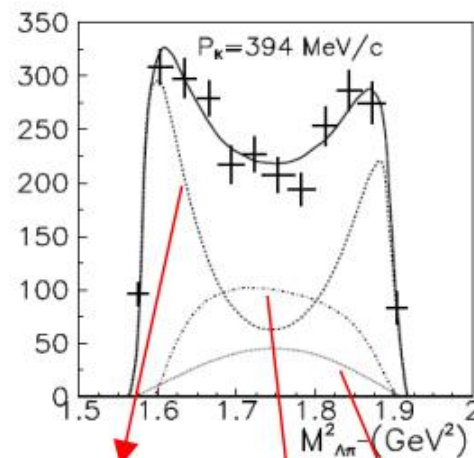


59%  $\Sigma^*(3/2^+)$  + 41%  $\Sigma^*(1/2^-)$

100%  $\Sigma^*(3/2^+)$

Phase space

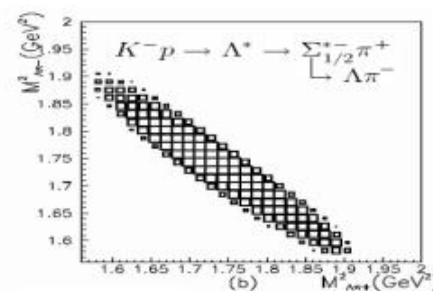
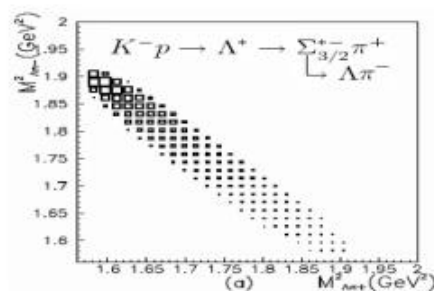
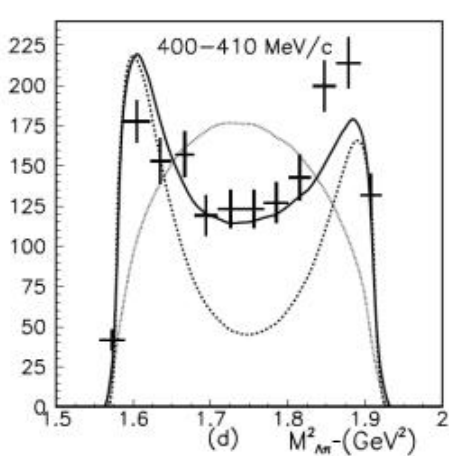
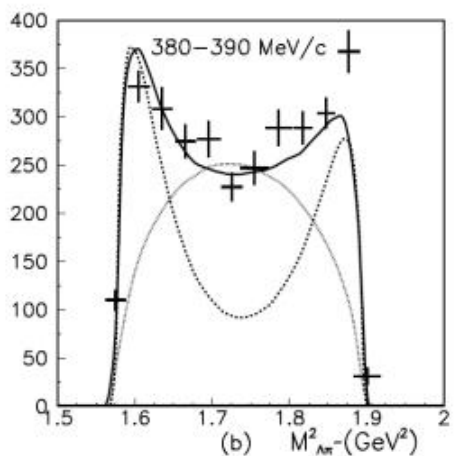
First reason: S-wave between the  $\Sigma^*(3/2^+)$  and  $\pi^+$ ; but P-wave between the  $\Sigma^*(1/2^-)$  and  $\pi^+$ .



59%  $\Sigma^*(3/2^+)$

Interference

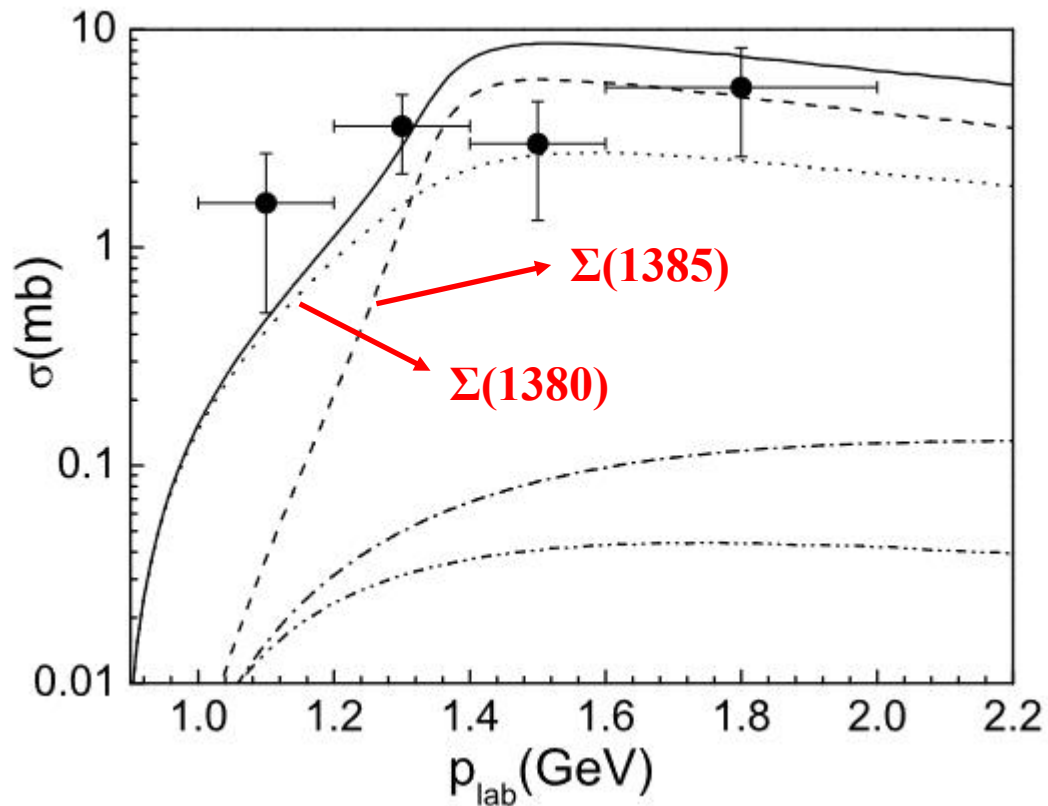
12.5%  $\Sigma^*(1/2^-)$



Second reason: the width of  $\Sigma^*(3/2^+)$  is 35.5MeV; but that of  $\Sigma^*(1/2^-)$  is 118.6MeV from fit before.

# Hadron-hadron scattering

- $\Lambda p \rightarrow \Lambda p \pi^0$ , JJXie, JJWu, and BSZou, PRC90(2014)055204

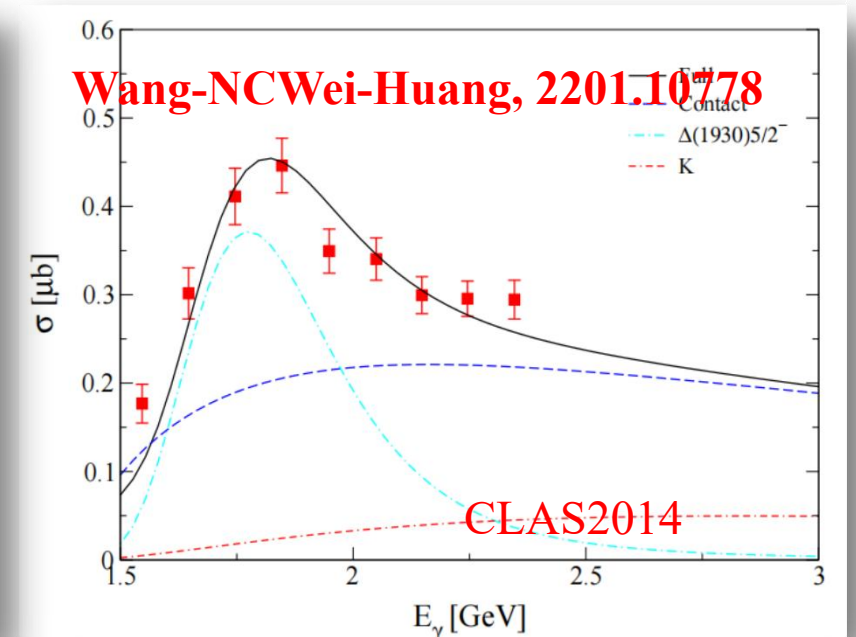
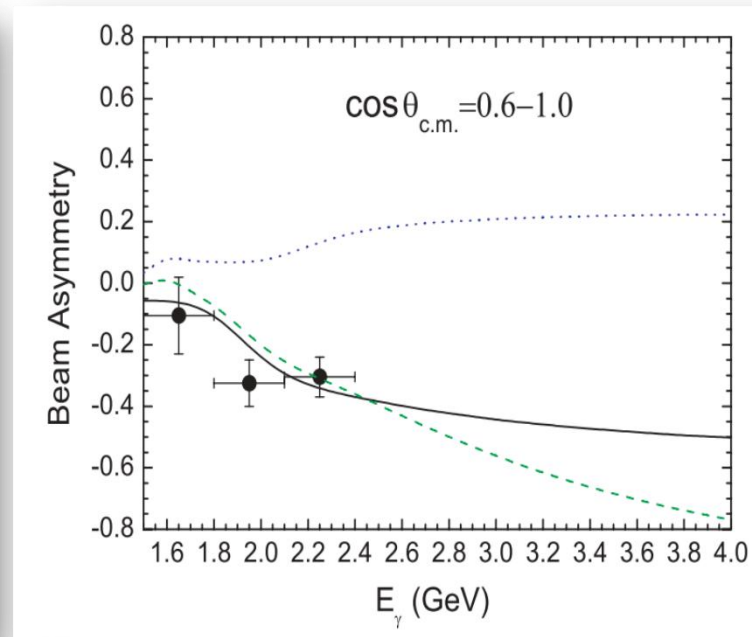
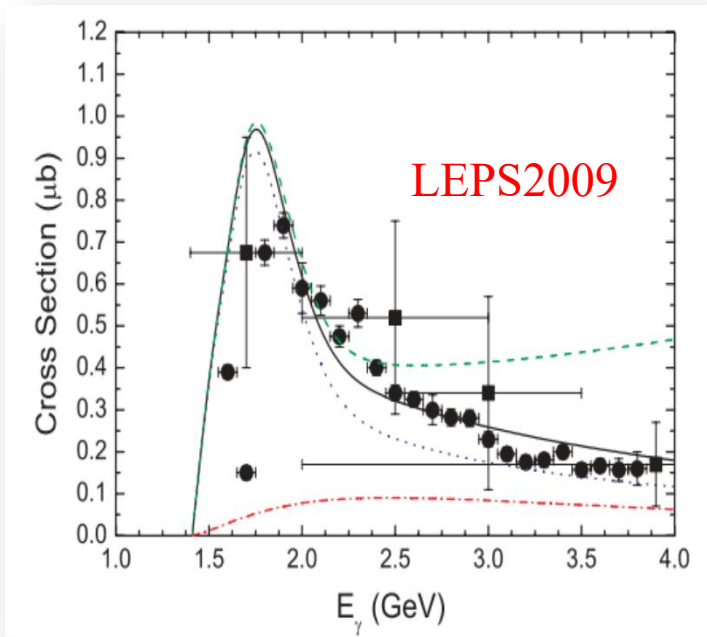


strong  $\Lambda p$  P.SI.

The  $\Sigma^*(1385)$  resonance can not reproduce the near threshold enhancement for the  $\Lambda p \rightarrow \Lambda p \pi^0$  reaction because it decays to  $\pi\Lambda$  in relative  $P$ -wave and is suppressed at low energies. On the contrary, the newly  $\Sigma^*(1380)$  state decays to  $\pi\Lambda$  in relative  $S$ -wave, and can describe the near threshold enhancement fairly well, which indicate that the  $\Lambda p \rightarrow \Lambda p \pi^0$  data support the existence of this  $\Sigma^*(1380)$  state, and more accurate data for this reaction can be used to improve our knowledge on the

# $\gamma/\nu$ -production

- $\gamma N \rightarrow K\Sigma(1385)$ , Gao-Wu-Zou, PRC 81(2010) 055203



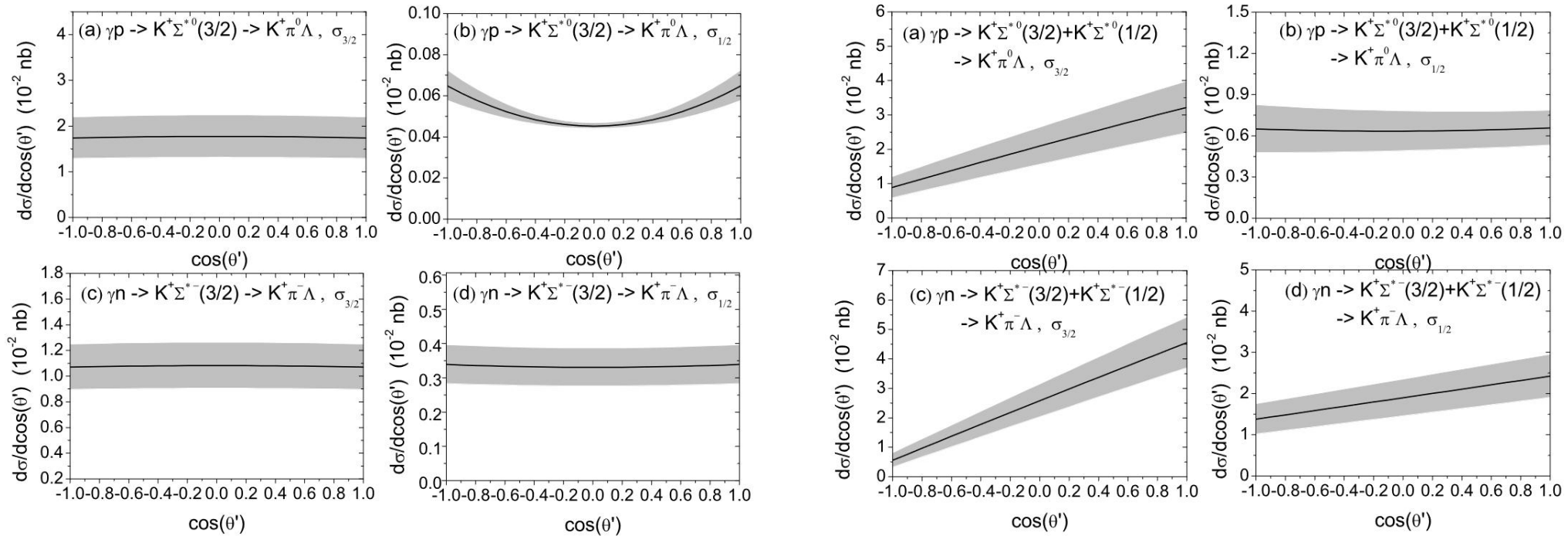
the case that the  $\Sigma(\frac{1}{2}^-)$  may contribute to the observables of the  $K\Sigma^*(1385)$  photoproduction in our experiments. Our results show that the  $\Sigma(\frac{1}{2}^-)$  production can provide a large negative contribution to beam asymmetry, which helps to explain the large negative linear beam asymmetry observed by the LEPS experiment. With a portion of the  $\Sigma(\frac{1}{2}^-)$ , the same set of parameters can reproduce both the data for  $\gamma n \rightarrow K^+\Sigma^{*-}$

and, in particular, to figure out which one of the  $N(1895)1/2^-$ ,  $\Delta(1900)1/2^-$ , and  $\Delta(1930)5/2^-$  resonances is really capable for a simultaneous description of the data for both  $K^+\Sigma^0(1385)$  and  $K^+\Sigma^-(1385)$  photoproduction reactions. The results show that the available data on differential and total cross sections and photo-beam asymmetries for  $\gamma n \rightarrow K^+\Sigma^-(1385)$  can be reproduced only with the inclusion of the  $\Delta(1930)5/2^-$  resonance rather than the other two. The generalized contact term and the  $t$ -channel  $K$  exchange are found to dominate the background contributions



# $\gamma/\nu$ -production

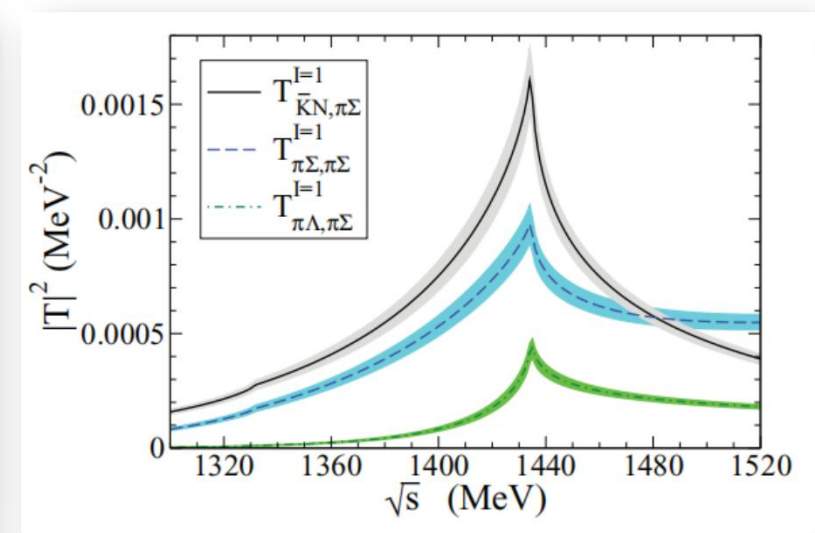
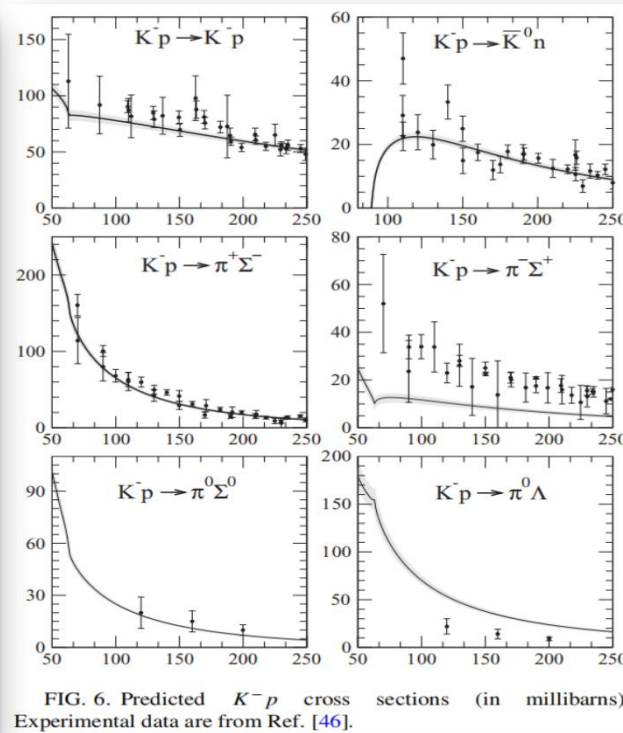
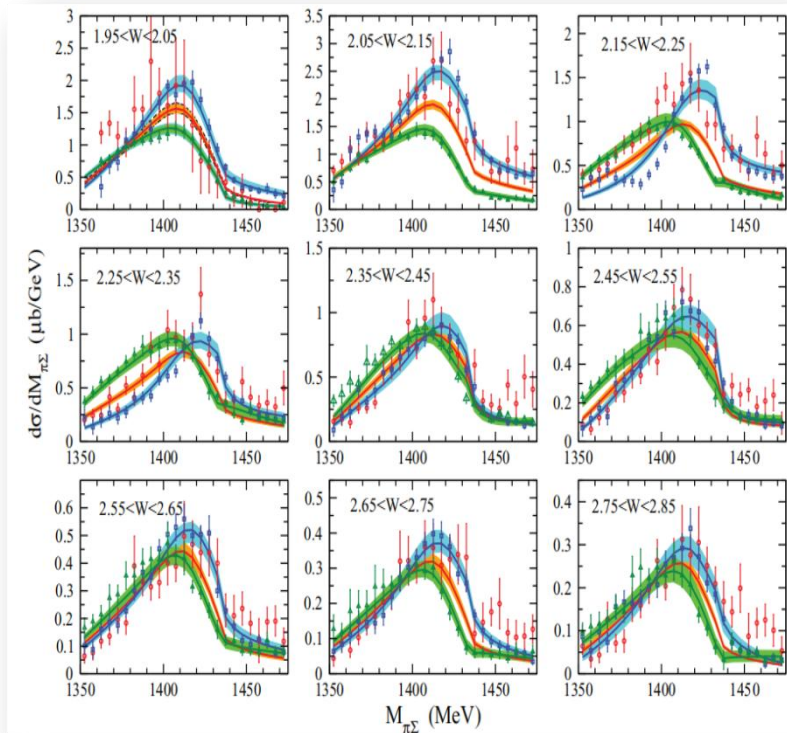
□  $\gamma p \rightarrow K^+ \pi \Lambda$ , YHChen, BSZou, PRC 88, 024304(2013)



**The angular distribution of the  $\pi$  are distinctly different assuming that the  $\Sigma(1/2^-)$  exists or not.**

# $\gamma/\nu$ -production

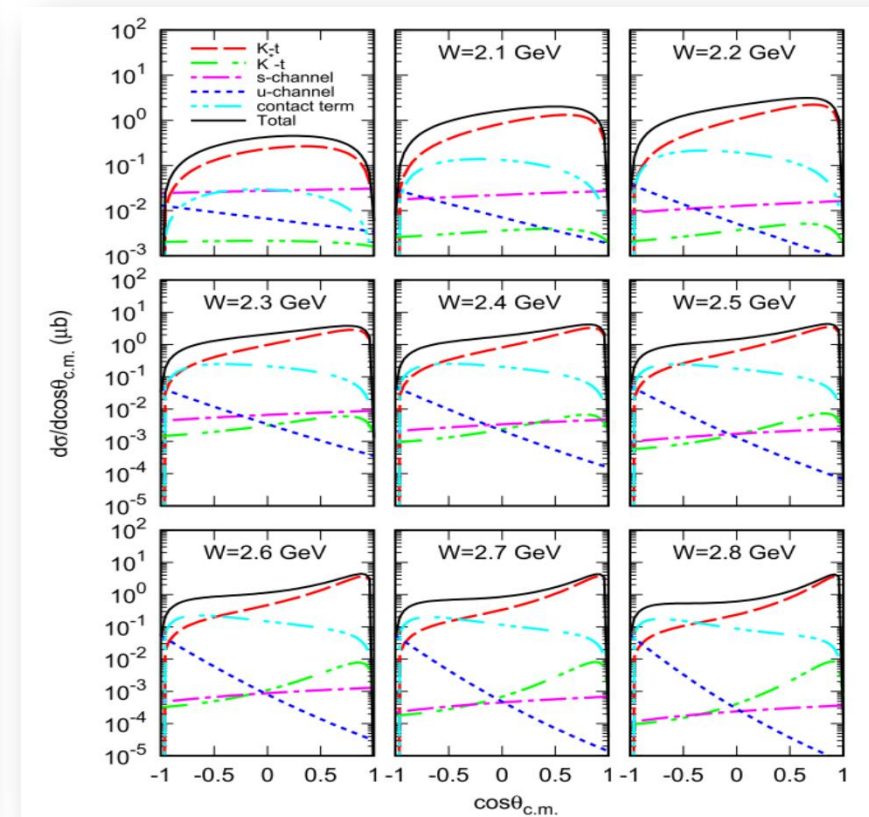
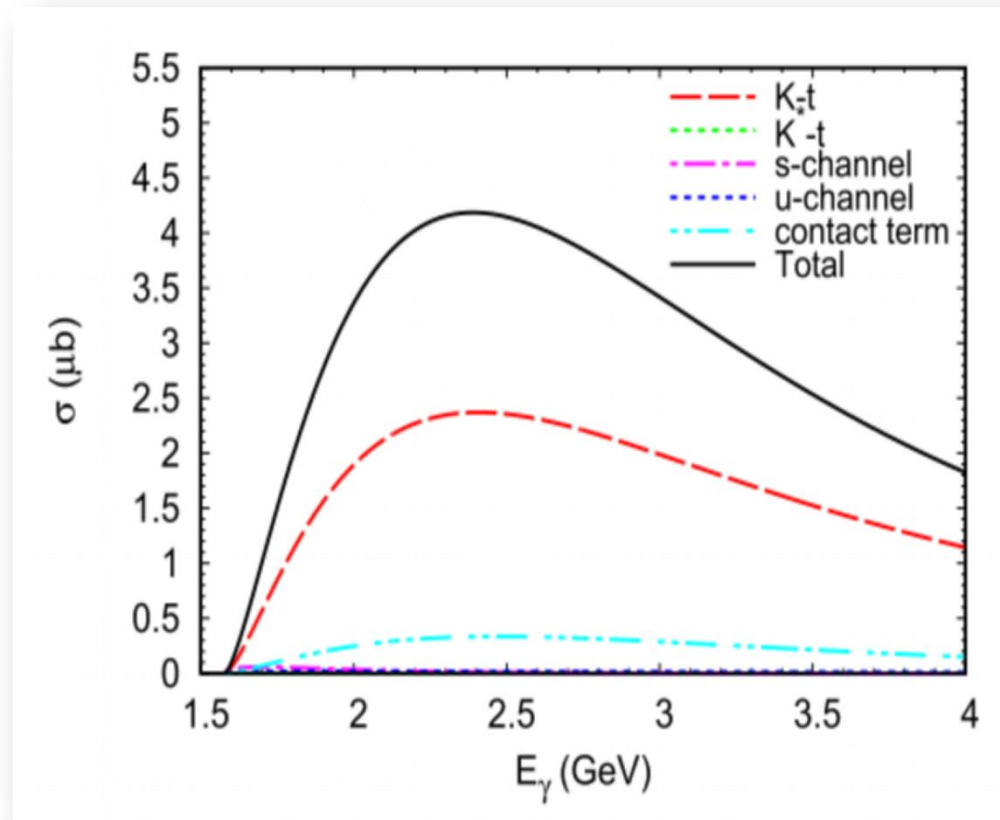
## $\pi\Sigma$ photoproduction, Roca-Oset, PRC 88, 055206 (2013)



Oset-Ramos, NPA635 (1998)  
 PB,VB, Hosaka, PRD 85, 114020 (2012)  
 Oller-Meißner, Phys. Lett. B 500 (2001) 263

# $\gamma/\nu$ -production

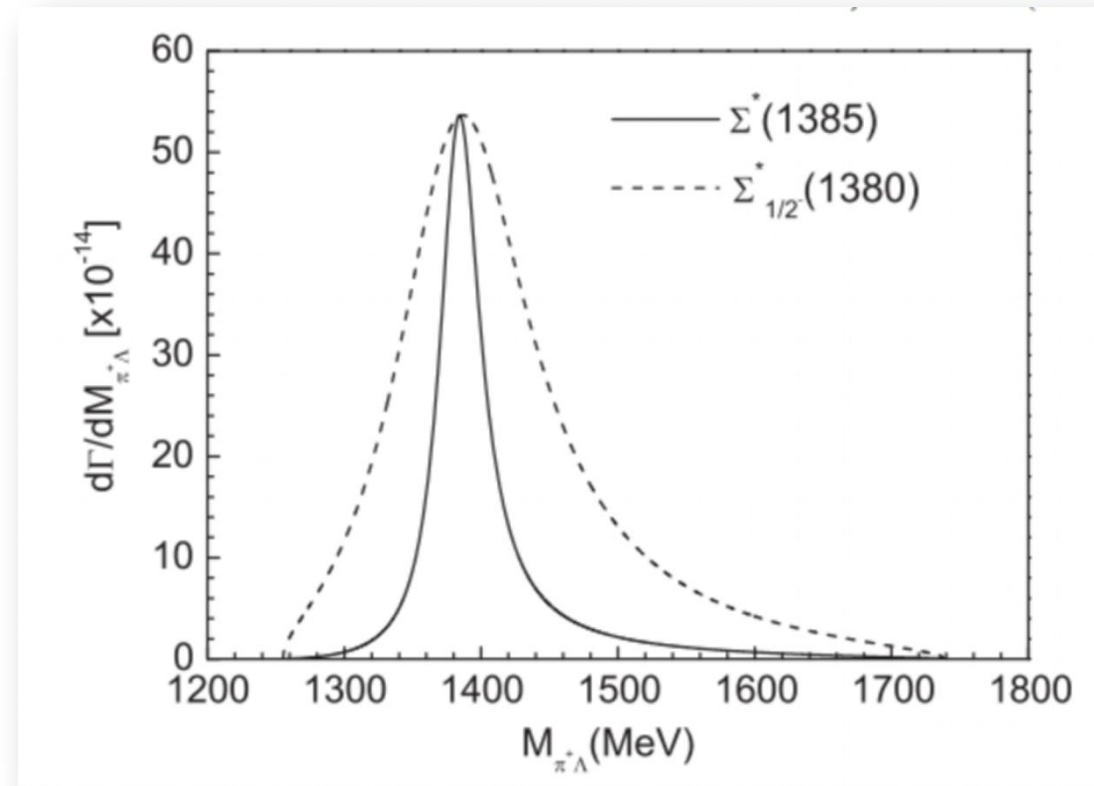
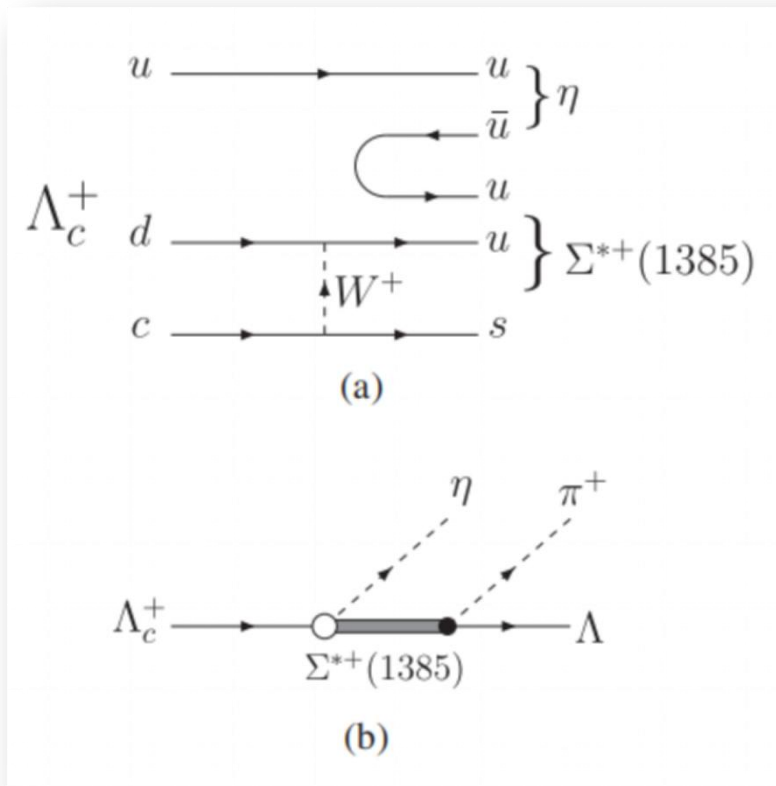
- $\gamma N \rightarrow K\Sigma(1/2^-)$ , **Lyu-EW-Xie-Wei, CPC47 (2023) 053108**





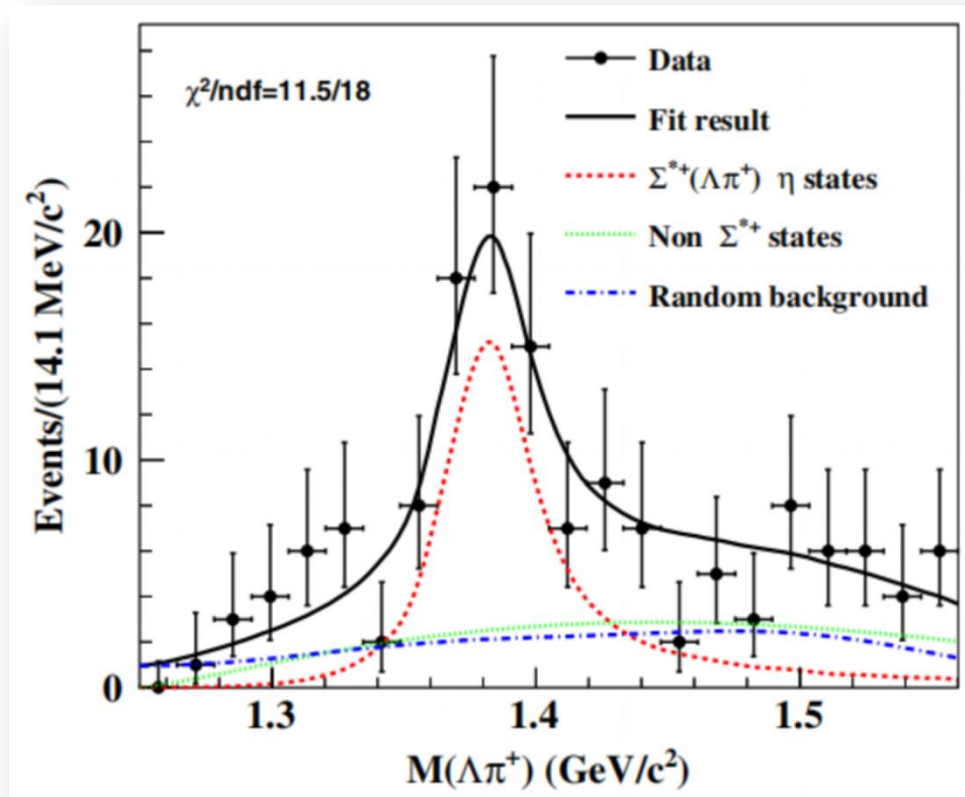
# Charmed baryon decays

$\square \Lambda_c \rightarrow \Lambda \eta \pi$ , J.J.Xie, L.S.Geng, EPJC76(2016) 496, PRD95(2017) 074024

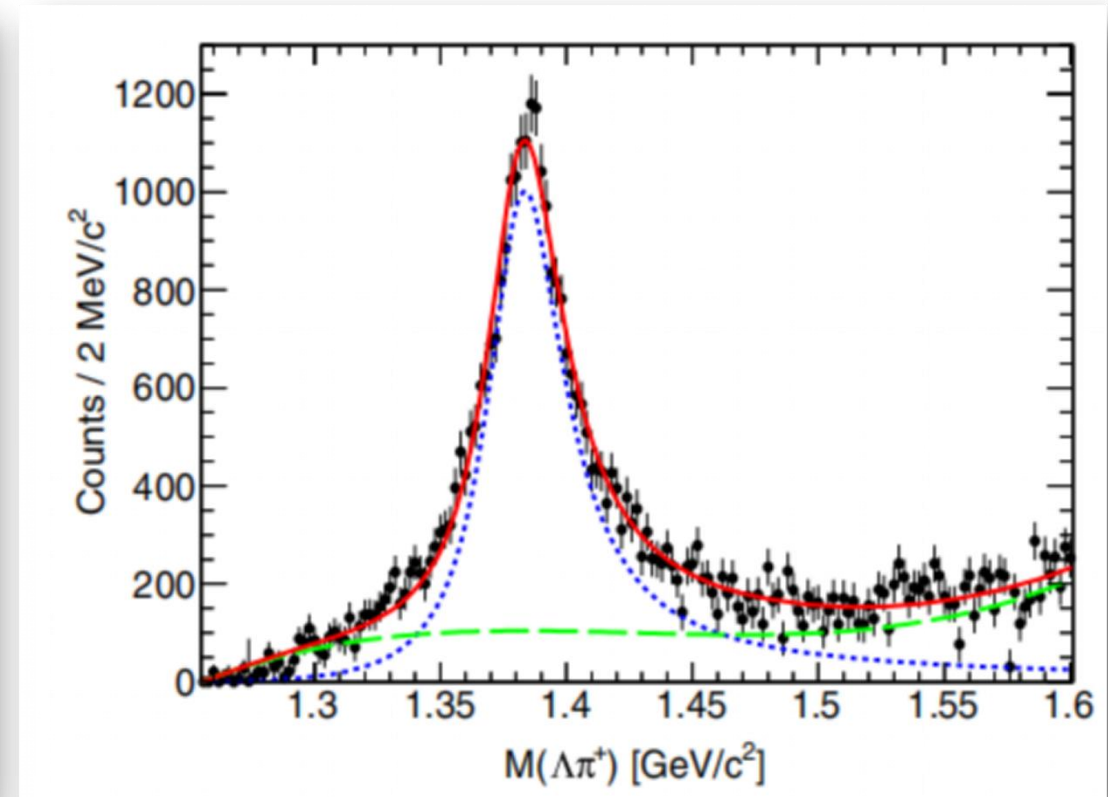


# Belle and BESIII measurements

□  $\Lambda_c \rightarrow \Lambda \eta \pi$

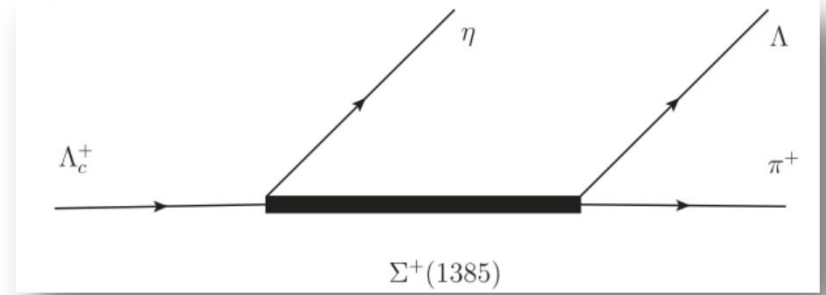
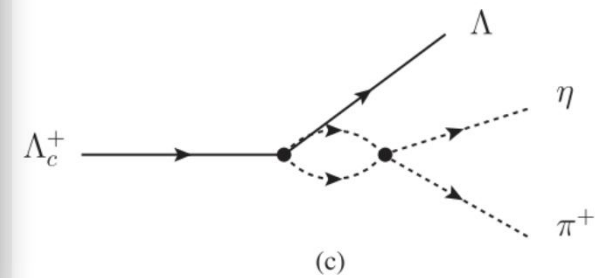
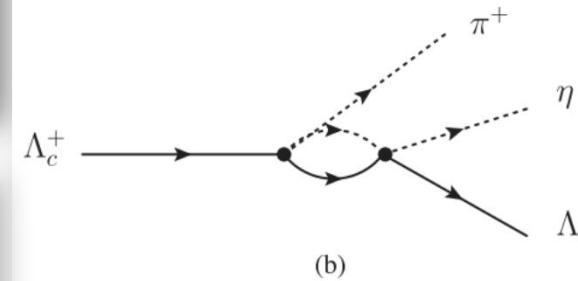
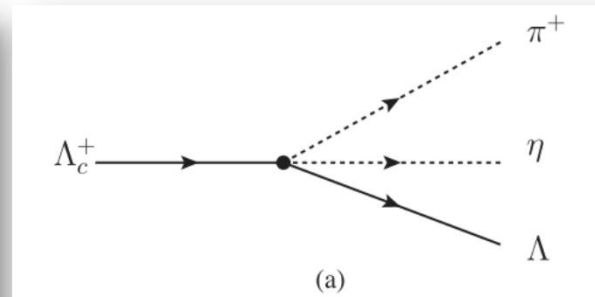
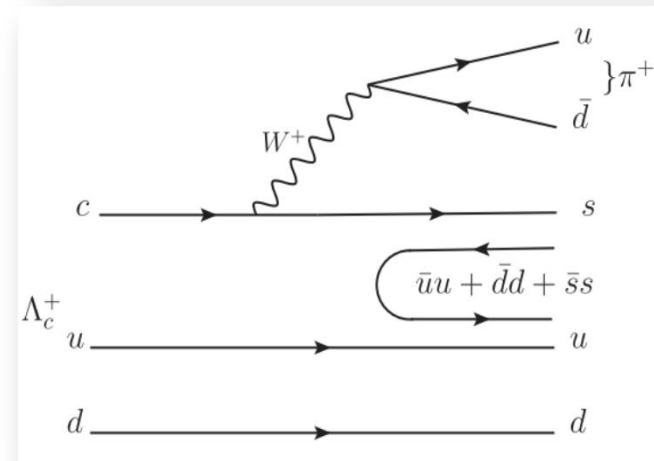
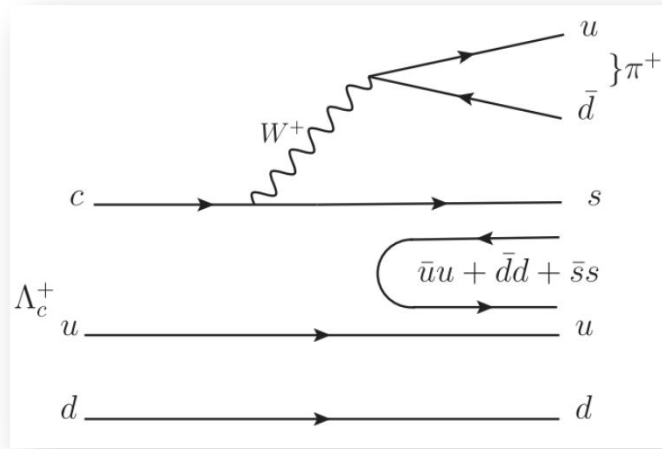


**BESIII: PRD99, 032010 (2019)**



**Belle: PRD103(2021)052005**

# Mechanism of $\Lambda_c \rightarrow \eta\Lambda\pi$



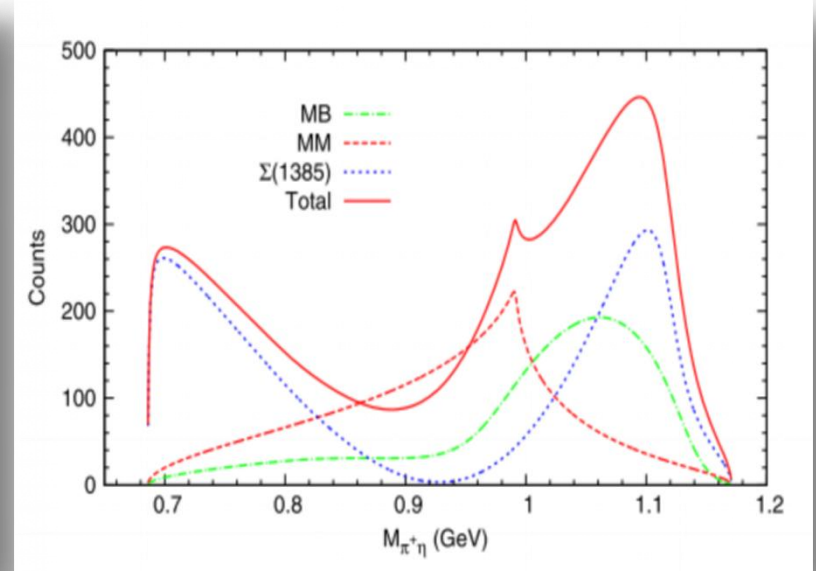
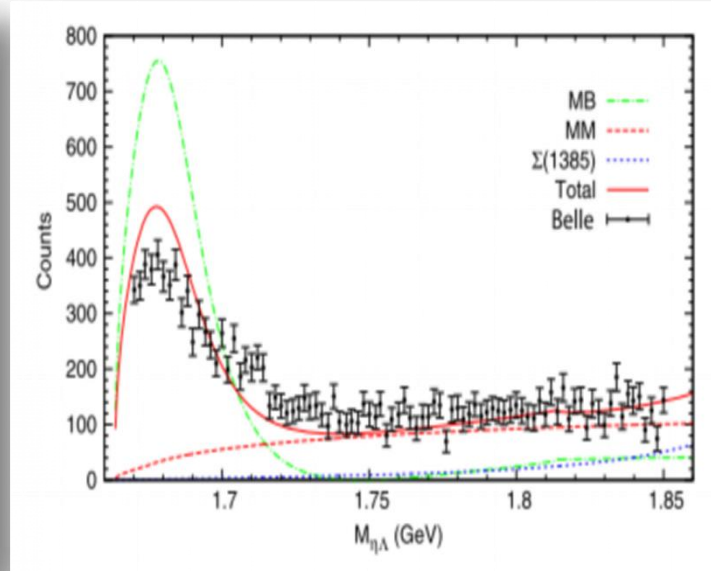
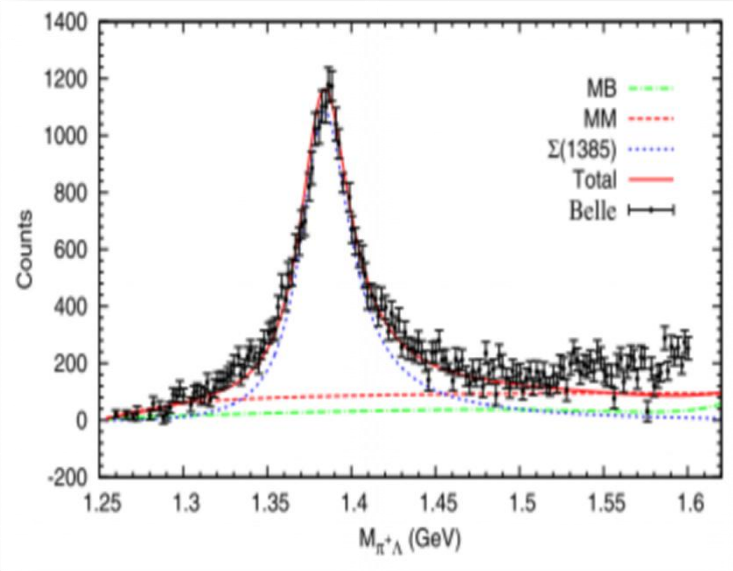
$$T^{\Sigma^*}(M_{\pi^+\Lambda}) = V_P'' \frac{|\vec{p}_\pi| \cdot |\vec{p}_\eta| \cdot \cos\theta}{M_{\pi^+\Lambda} - M_{\Sigma^*} + i\frac{\Gamma_{\Sigma^*}}{2}},$$

$$T^{\text{MB}}(M_{\eta\Lambda}) = V_P \left\{ -\frac{\sqrt{2}}{3} + G_{K^-p}(M_{\eta\Lambda})t_{K^-p \rightarrow \eta\Lambda}(M_{\eta\Lambda}) + G_{\bar{K}^0n}(M_{\eta\Lambda})t_{\bar{K}^0n \rightarrow \eta\Lambda}(M_{\eta\Lambda}) - \frac{\sqrt{2}}{3}G_{\eta\Lambda}(M_{\eta\Lambda})t_{\eta\Lambda \rightarrow \eta\Lambda}(M_{\eta\Lambda}) \right\},$$

$$T^{\text{MM}}(M_{\pi^+\eta}) = V_P' \frac{2\sqrt{2}}{3} \left\{ 1 + G_{\pi^+\eta}(M_{\pi^+\eta})t_{\pi^+\eta \rightarrow \pi^+\eta}(M_{\pi^+\eta}) + \frac{\sqrt{3}}{2}G_{K^+\bar{K}^0}(M_{\pi^+\eta})t_{K^+\bar{K}^0 \rightarrow \pi^+\eta}(M_{\pi^+\eta}) \right\}, \quad ($$

# Analysis the Belle data

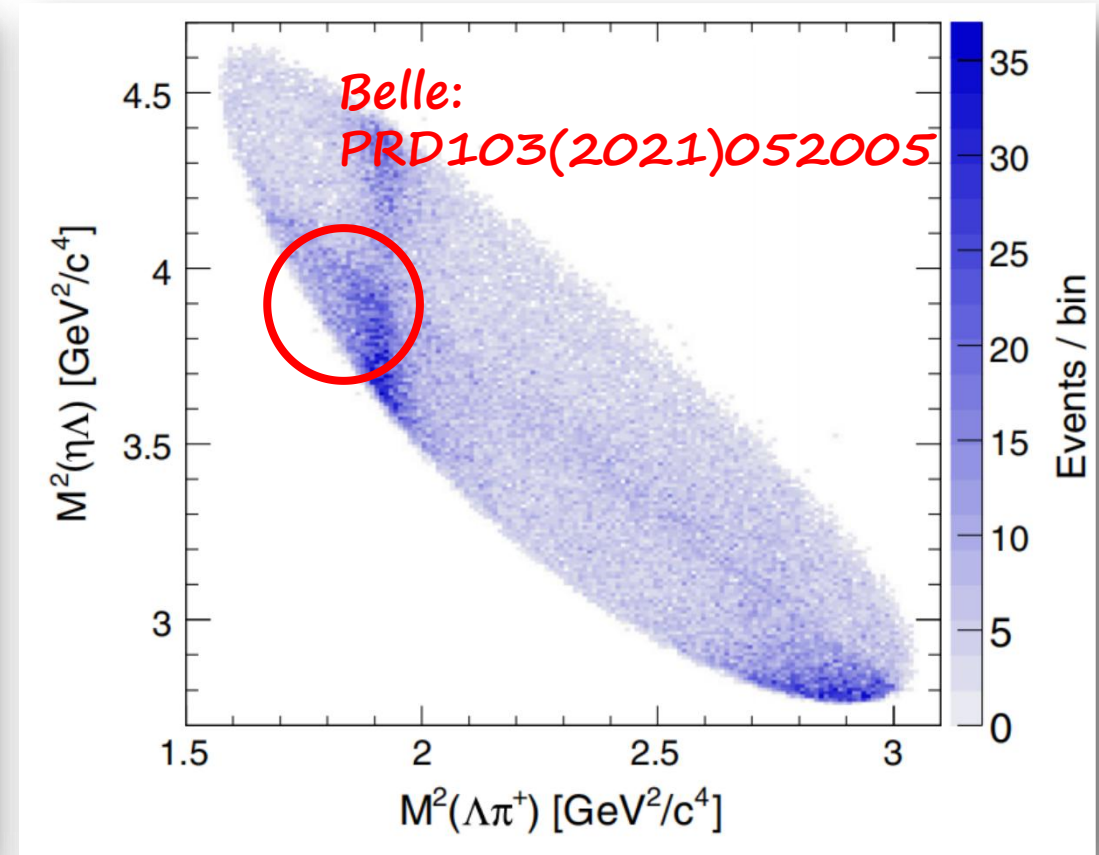
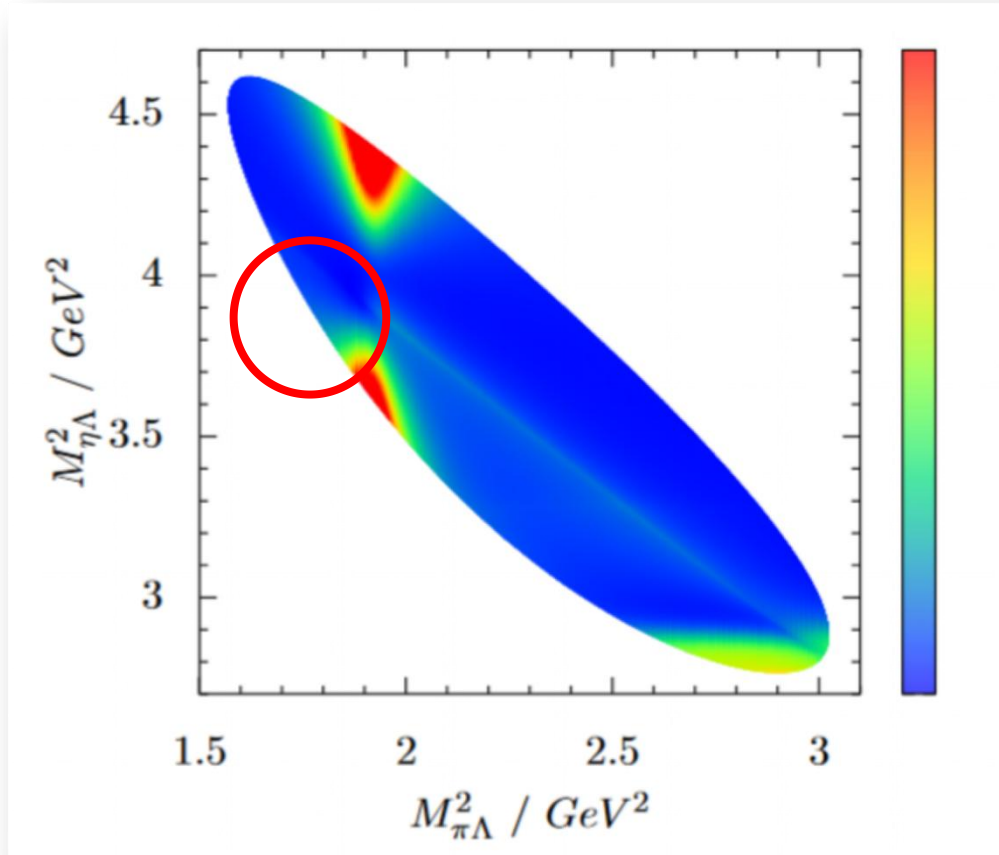
□  $\Lambda_c \rightarrow \Lambda \eta \pi$  , GYW-EW-Xie-Geng-Wei, PRD 106, 056001 (2022)



**By regarding the  $\Lambda(1670)$  as the molecule, we could well reproduce the Belle data of the mass distributions.**

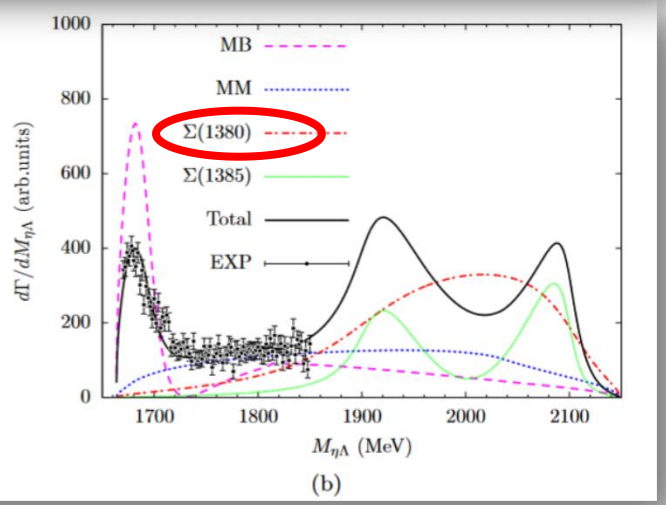
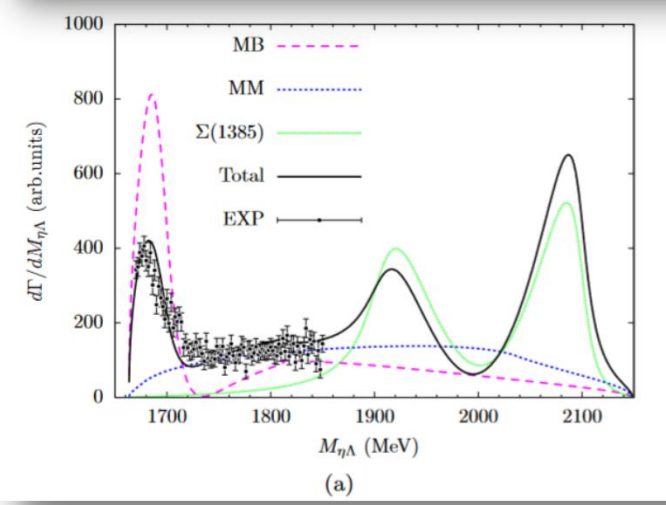
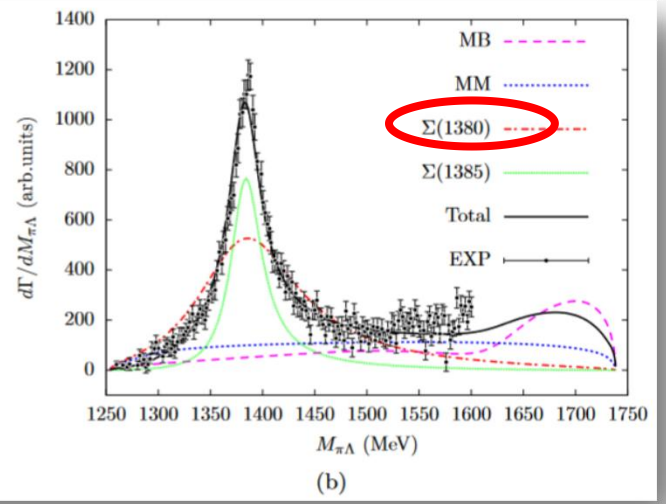
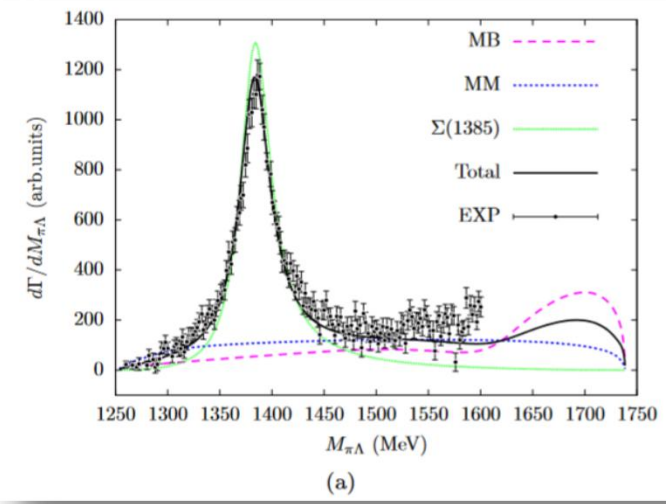
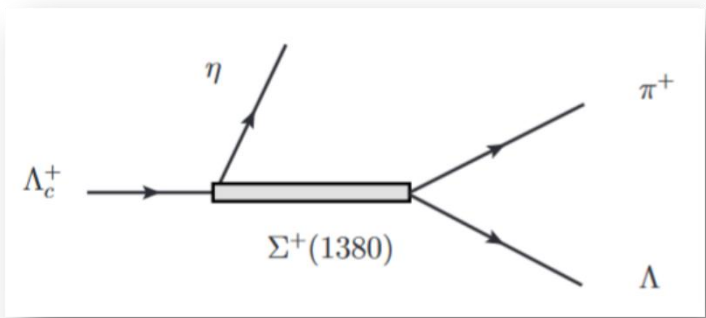


# Dalitz plot of $\Lambda_c \rightarrow \eta\Lambda\pi$



# $\Sigma(1/2^-)$ in $\Lambda_c \rightarrow \eta \Lambda \pi$

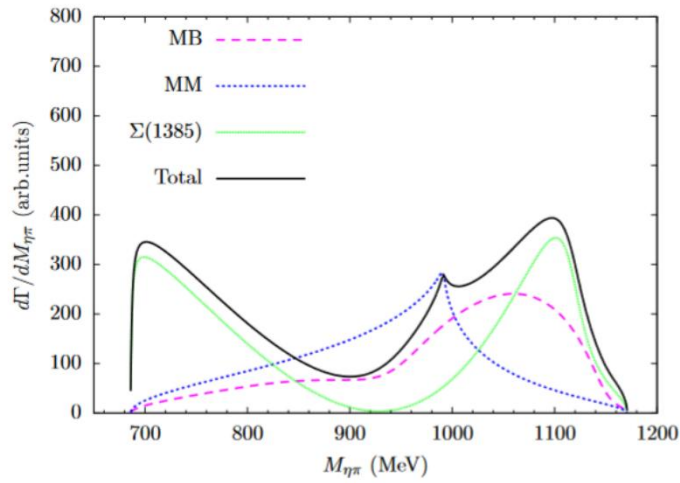
Intermediate of  $\Sigma(1/2^-)$



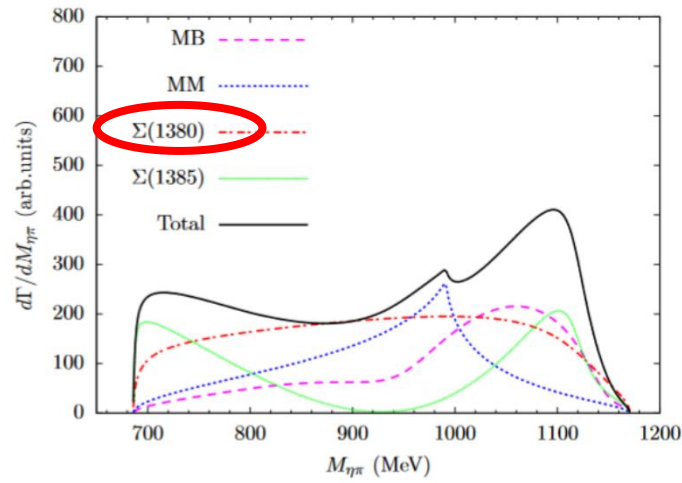
$$\mathcal{T}^{\Sigma(1/2^-)} = \frac{V^{\Sigma(1/2^-)} M_{\Sigma(1/2^-)} \Gamma_{\Sigma(1/2^-)}}{M_{\pi^+\Lambda}^2 - M_{\Sigma(1/2^-)}^2 + i M_{\Sigma(1/2^-)} \Gamma_{\Sigma(1/2^-)}}$$

EW, JJWu, to be prepared

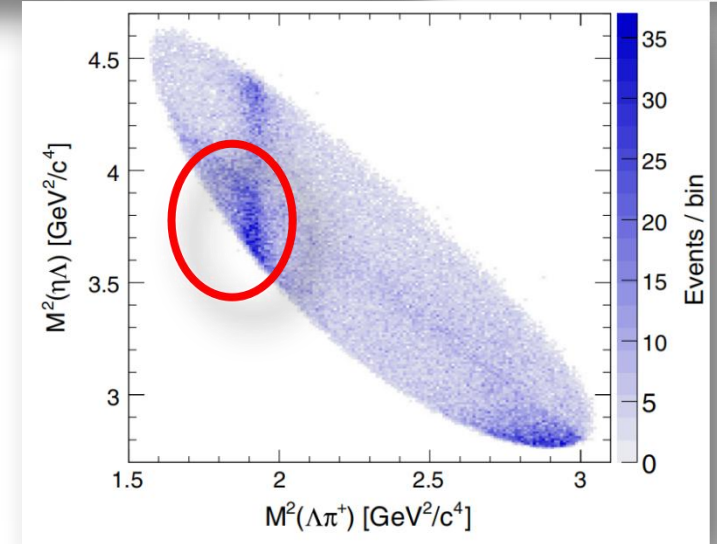
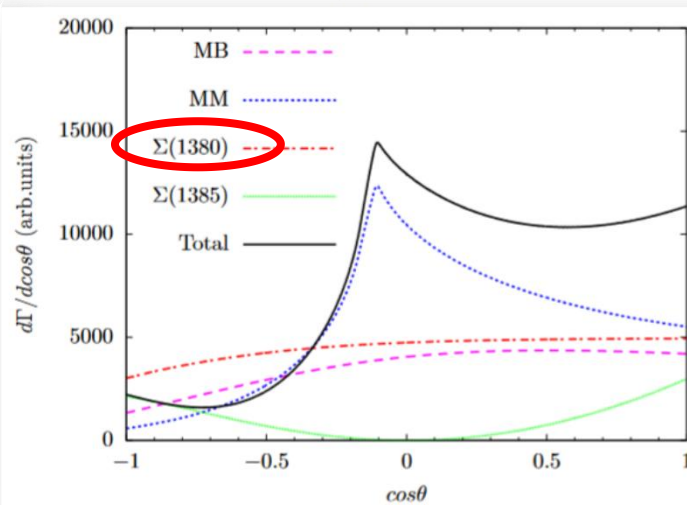
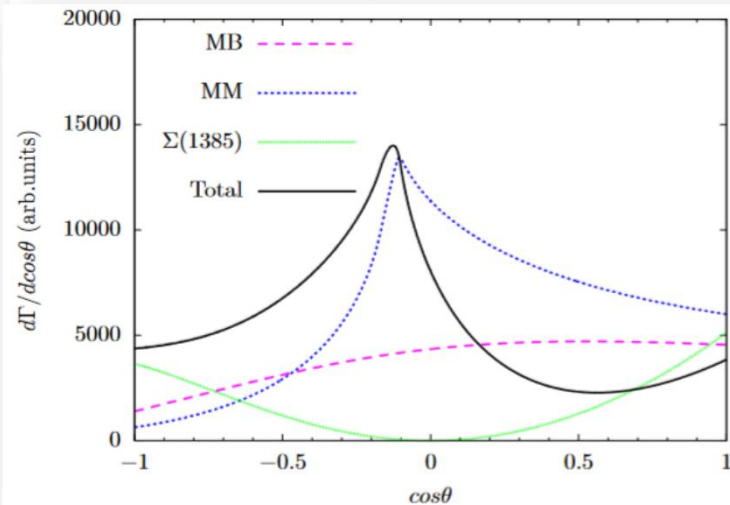
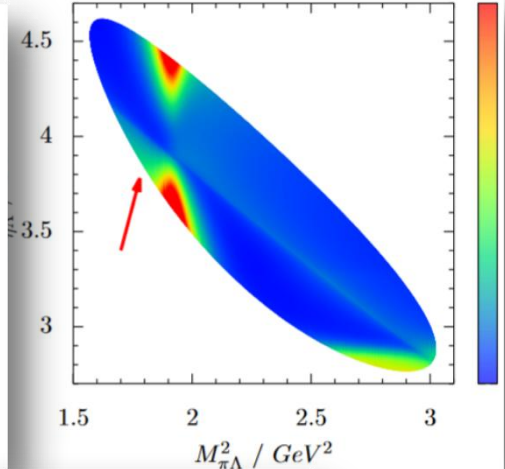
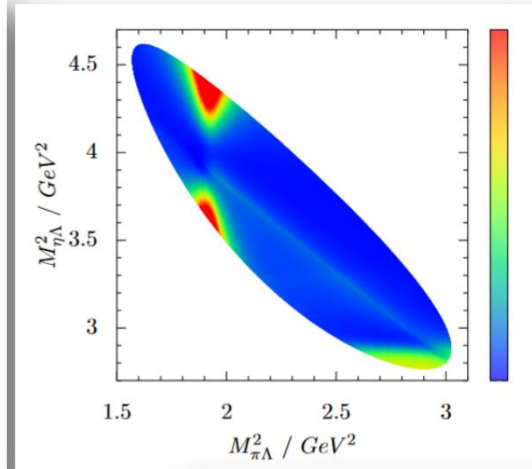
# The results with/without $\Sigma(1380)$



(a)



(b)

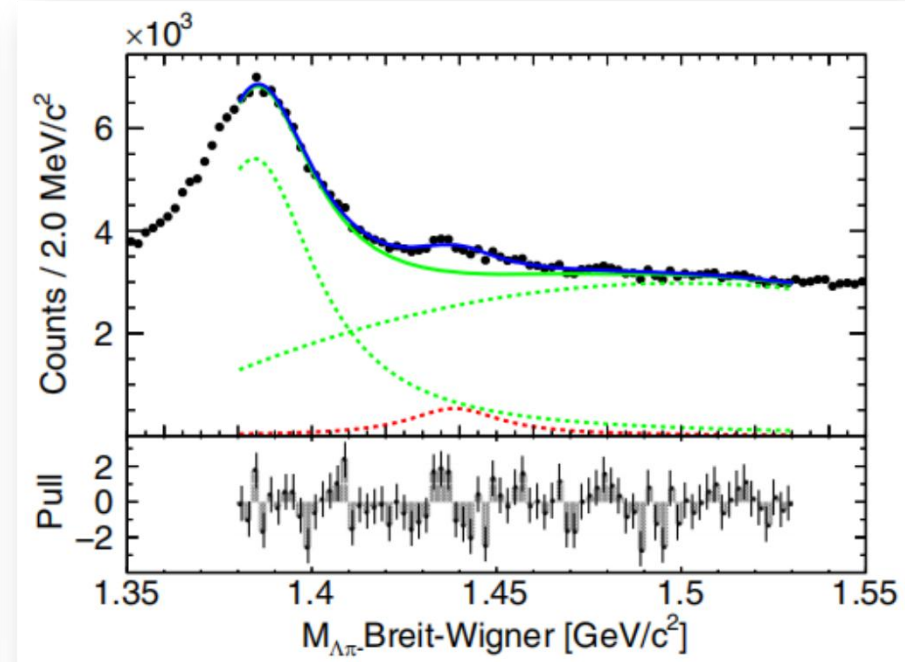
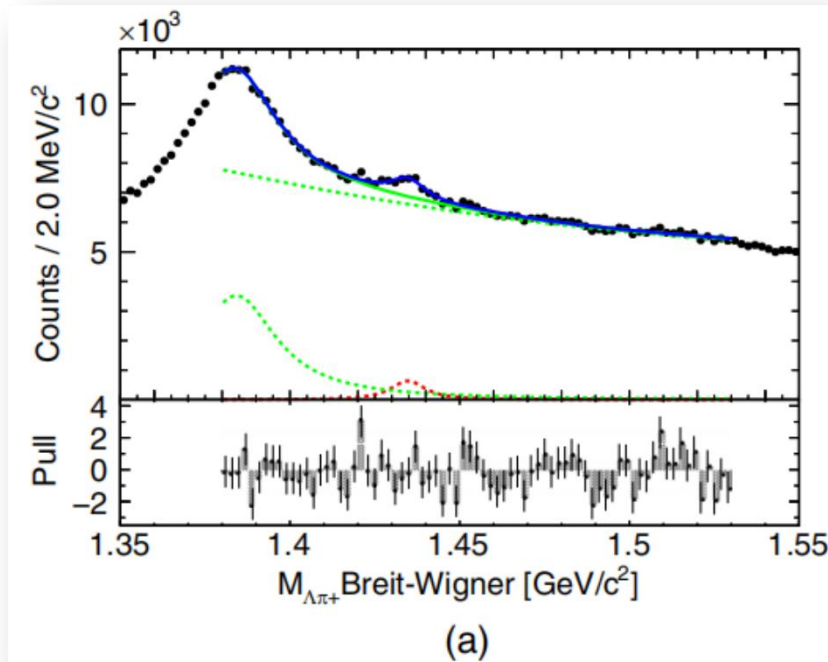


$$M_{\pi\Lambda} \geq 1450 \text{ MeV and } M_{\eta\Lambda} \geq 1760 \text{ MeV.}$$

EW, JJWu, to be prepared

# Belle measurements

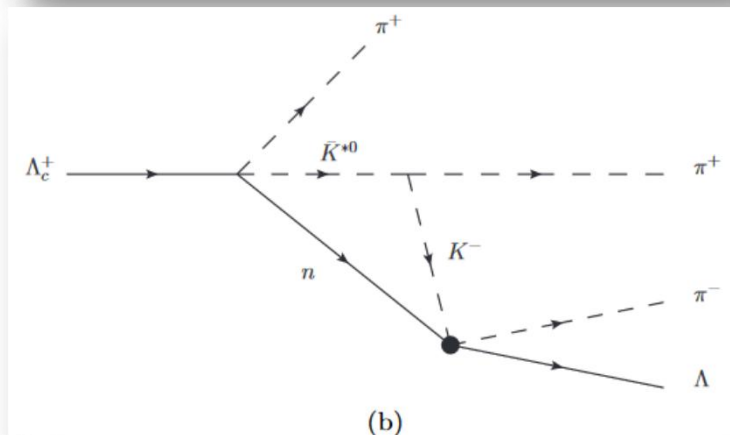
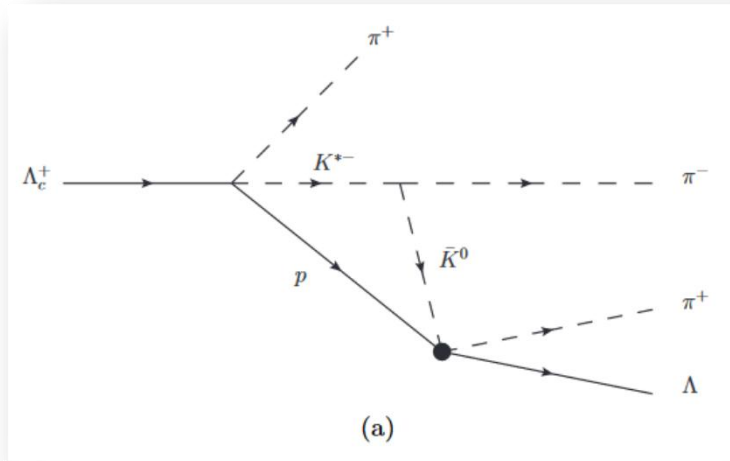
□  $\Lambda_c \rightarrow \Lambda \pi^+ \pi^+ \pi^-$ , Belle, PRL130, 151903 (2023)



| Mode           | $E_{\text{BW}}$ (MeV/ $c^2$ ) | $\Gamma$ (MeV/ $c^2$ ) | $\chi^2/\text{NDF}$ |
|----------------|-------------------------------|------------------------|---------------------|
| $\Lambda\pi^+$ | $1434.3 \pm 0.6$              | $11.5 \pm 2.8$         | 74.4/68             |
| $\Lambda\pi^-$ | $1438.5 \pm 0.9$              | $33.0 \pm 7.5$         | 92.3/68             |

# Evidence of $\Sigma(1430)$

$$\square \Lambda_c \rightarrow \Lambda \pi^+ \pi^+ \pi^-$$



**Dai-Pavao-Sakai-Oset, PRD 97, 116004 (2018)**  
**Xie-Oset, PLB 792, 450-453 (2019)**

$$t_{\Lambda_c^+ \rightarrow \pi^+ K^{*-} p} = A \vec{\sigma} \cdot \vec{\epsilon},$$

$$\frac{d\Gamma_{\Lambda_c^+ \rightarrow \pi^+ K^{*-} p}}{dM_{\text{inv}}(K^{*-} p)} = \frac{1}{(2\pi)^3} \frac{2M_{\Lambda_c^+} 2M_p}{4M_{\Lambda_c^+}^2} p_{\pi^+} \tilde{p}_{K^{*-}} \times \sum \sum |t_{\Lambda_c^+ \rightarrow \pi^+ K^{*-} p}|^2,$$

$$\mathcal{B}(\Lambda_c^+ \rightarrow \pi^+ \hat{K}^{*-} p) = (1.4 \pm 0.5) \times 10^{-2}$$

$$|A|^2 = (3.9 \pm 1.4) \times 10^{-16} \text{ MeV}^{-2}$$

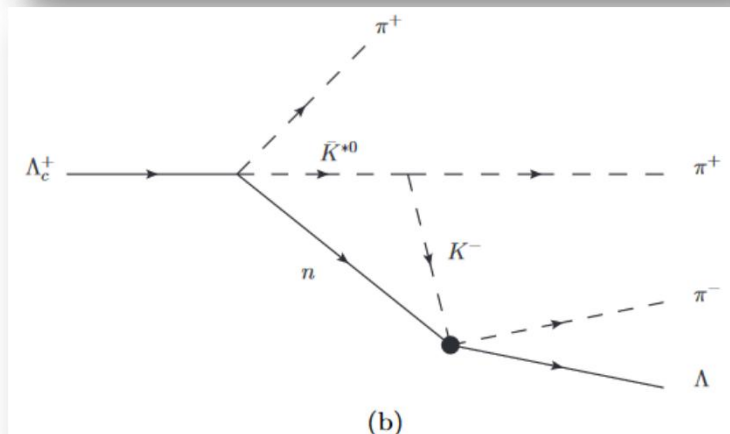
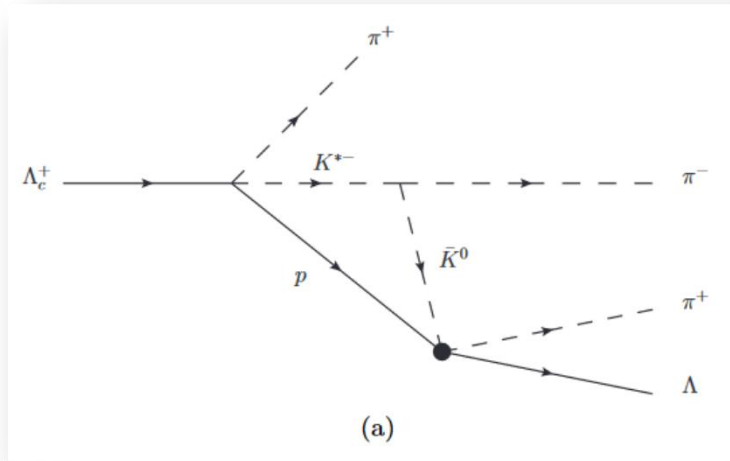
$$\mathcal{L}_{VPP} = -ig \langle V^\mu [P, \partial P] \rangle$$

$$\mathcal{L}_{\bar{K}^* \rightarrow \pi \bar{K}} = -ig (K^{*-})^\mu (\pi^- \partial_\mu \bar{K}^0 - \partial_\mu \pi^- \bar{K}^0).$$

# Evidence of $\Sigma(1430)$



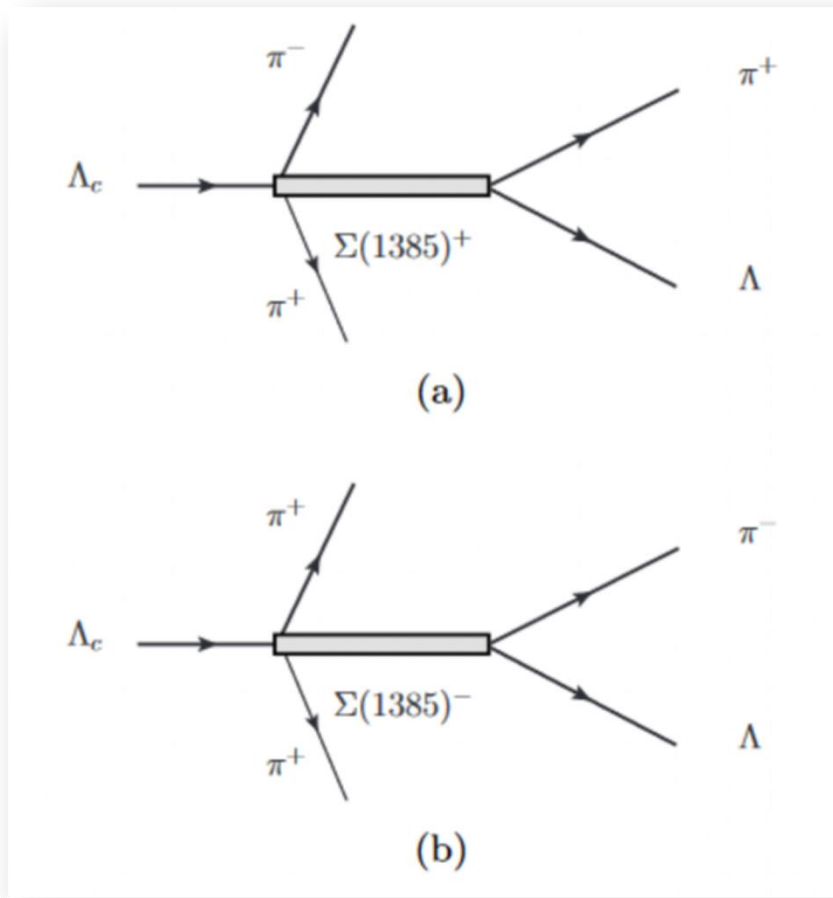
Dai-Pavao-Sakai-Oset, PRD 97, 116004 (2018)  
 Xie-Oset, PLB 792, 450-453 (2019)



$$\begin{aligned}
 t_T^a = & \int \frac{d^3q}{(2\pi)^3} \frac{2M_p}{8\omega_p \omega_{K^{*-}} \omega_{\bar{K}^0}} \frac{1}{k_a^0 - \omega_{K^{*-}} - \omega_{\bar{K}^0} + i\frac{\Gamma_{K^{*-}}}{2}} \\
 & \times \frac{1}{P^0 + \omega_p + \omega_{\bar{K}^0} - k_a^0} \left(2 + \frac{\vec{q} \cdot \vec{k}}{|\vec{k}|^2}\right) \\
 & \times \frac{2P^0 \omega_p + 2k_a^0 \omega_{\bar{K}^0} - 2(\omega_p + \omega_{\bar{K}^0})(\omega_p + \omega_{\bar{K}^0} + \omega_{K^{*-}})}{P^0 - \omega_{K^{*-}} - \omega_p + i\frac{\Gamma_{K^{*-}}}{2}} \\
 & \times \frac{1}{P^0 - \omega_p - \omega_{\bar{K}^0} - k_a^0 + i\epsilon}, \tag{19}
 \end{aligned}$$

# Evidence of $\Sigma(1430)$

$\square \Lambda_c \rightarrow \Lambda \pi^+ \pi^+ \pi^-$



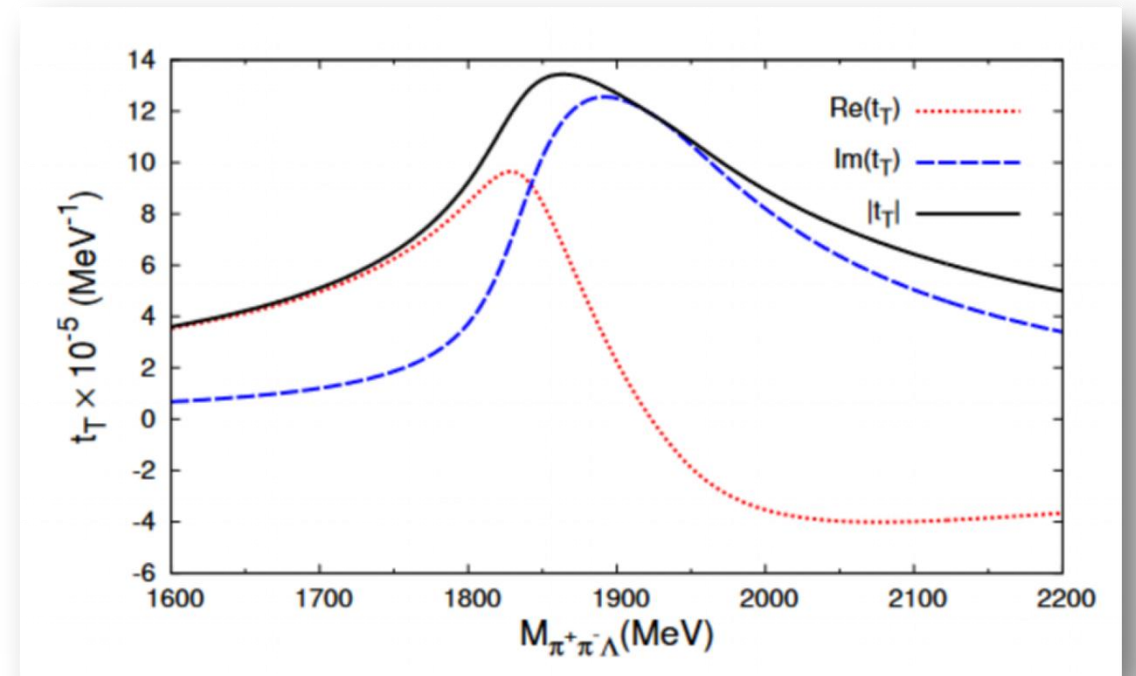
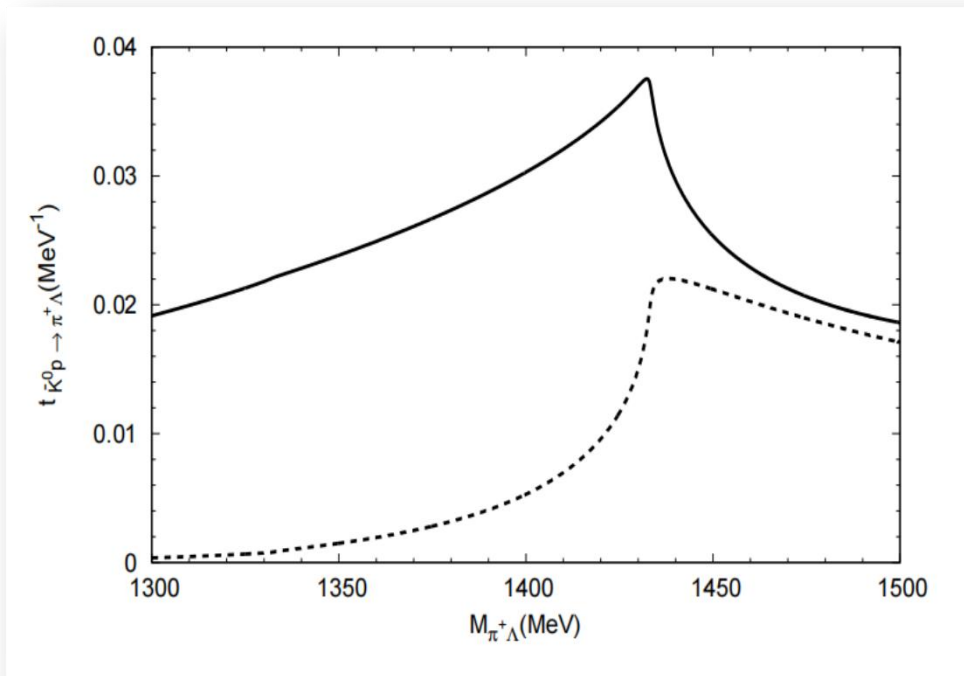
$$T^{\Sigma^{*+}(1385)} = \frac{V_p |p_{\pi^+}|}{M_{\pi^+\Lambda} - M_{\Sigma^{*+}} + i \frac{\Gamma_{\Sigma^{*+}}}{2}},$$

$$T^{\Sigma^{*-}(1385)} = \frac{V_p |p_{\pi^-}|}{M_{\pi^-\Lambda} - M_{\Sigma^{*-}} + i \frac{\Gamma_{\Sigma^{*-}}}{2}},$$

$$\frac{d^3\Gamma}{dM_{\pi^+\pi^-\Lambda} dM_{\pi^+\Lambda} dM_{\pi^-\Lambda}} = \frac{g^2 |A|^2 M_\Lambda}{64\pi^5 M_{\Lambda_c^+}} \tilde{p}_{\pi^+} \frac{M_{\pi^+\Lambda} M_{\pi^-\Lambda}}{M_{\pi^+\pi^-\Lambda}} \left\{ |\vec{k}_a|^2 |t_T^a \mathcal{M}^a|^2 + |\vec{k}_b|^2 |t_T^b \mathcal{M}^b|^2 + 2\text{Re}[t_T^a \mathcal{M}^a (t_T^b \mathcal{M}^b)^*] \right. \\ \left. \times \vec{k}_a \cdot \vec{k}_b + |T^{\Sigma^{*+}(1385)}|^2 + |T^{\Sigma^{*-}(1385)}|^2 \right\}, \quad (29)$$

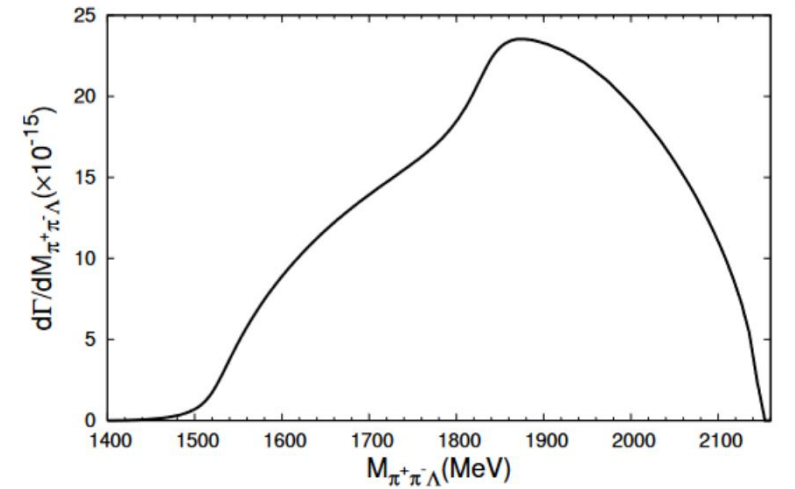
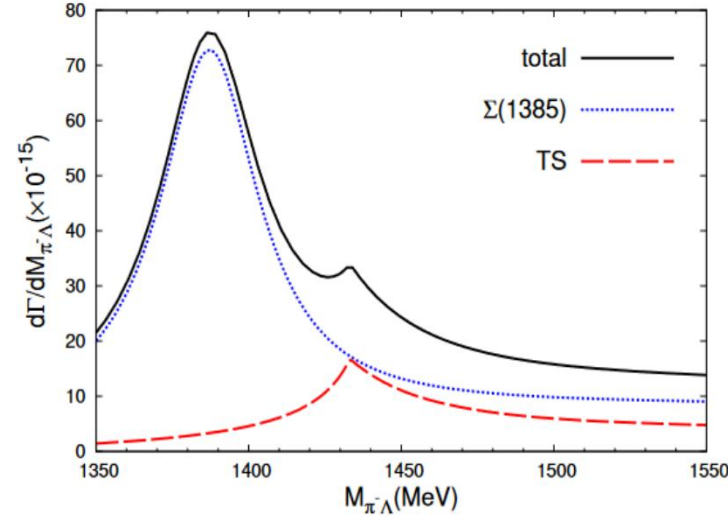
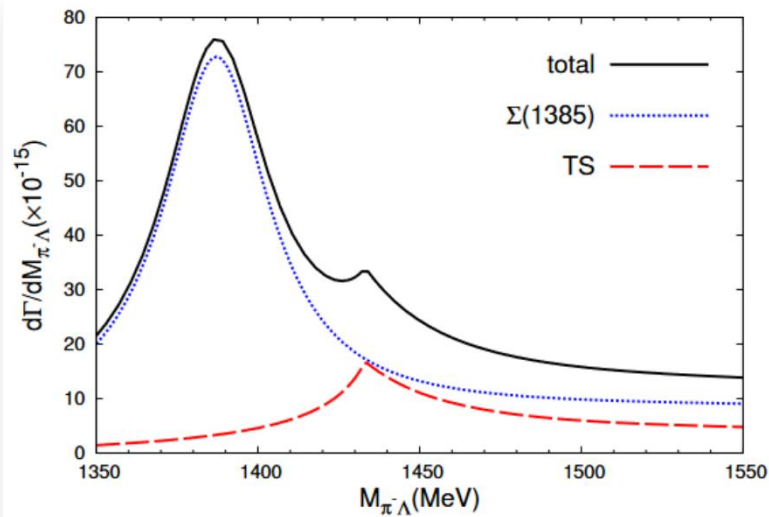
# Evidence of $\Sigma(1430)$

□  $\Lambda_c \rightarrow \Lambda \pi^+ \pi^+ \pi^-$ , Lyu-GYW-EW-Xie-Geng, to prepare





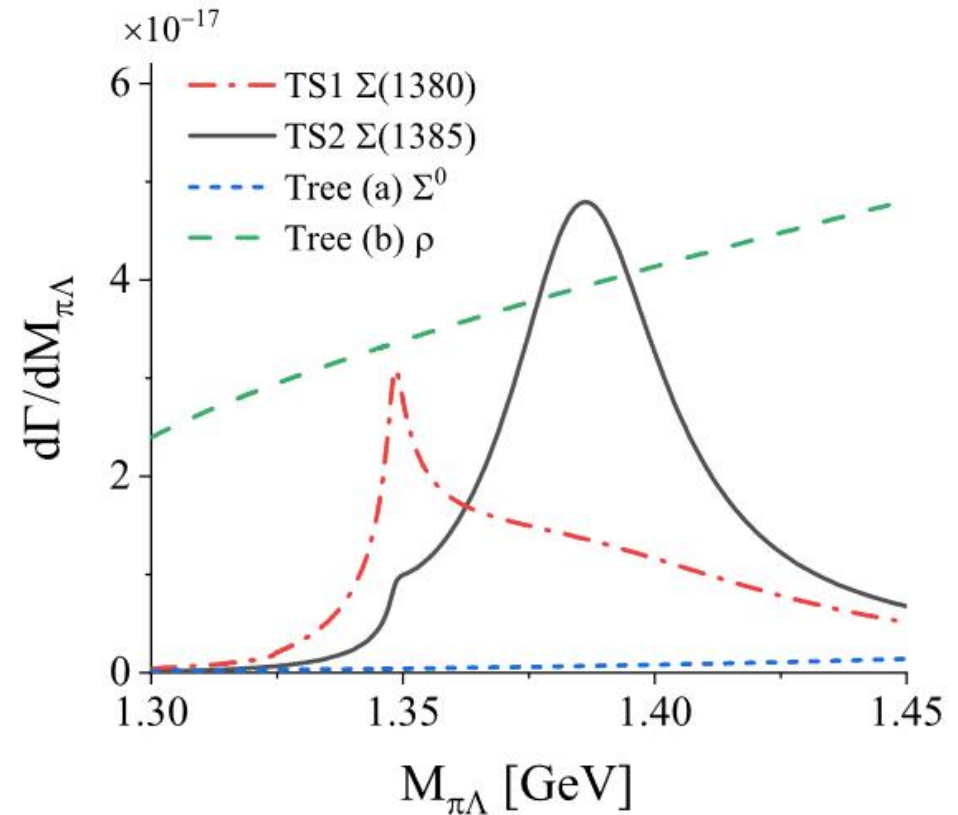
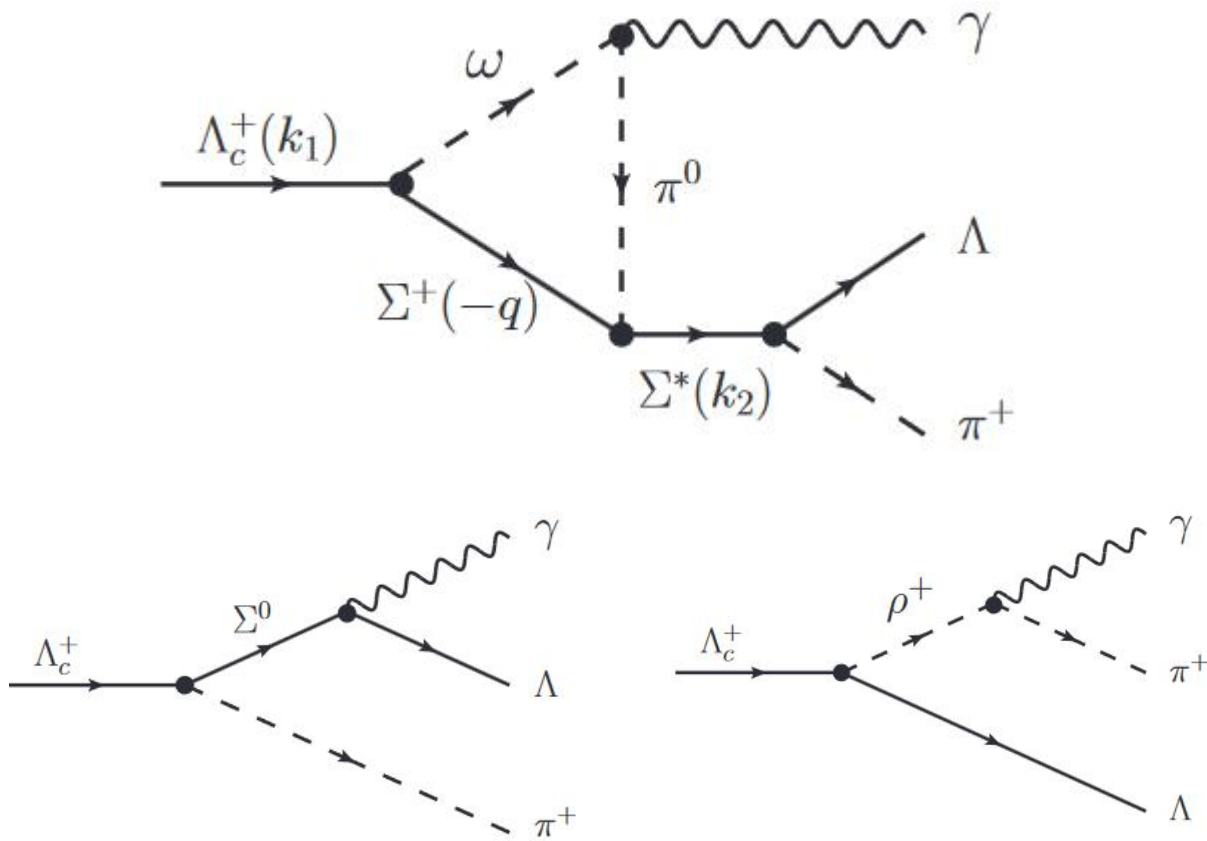
# Results of $\Lambda_c \rightarrow \Lambda \pi^+ \pi^+ \pi^-$



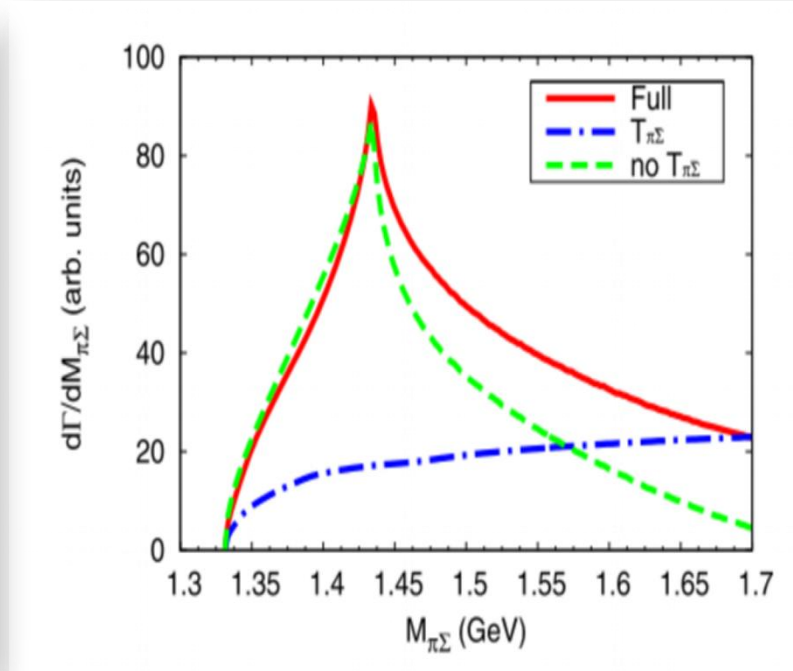
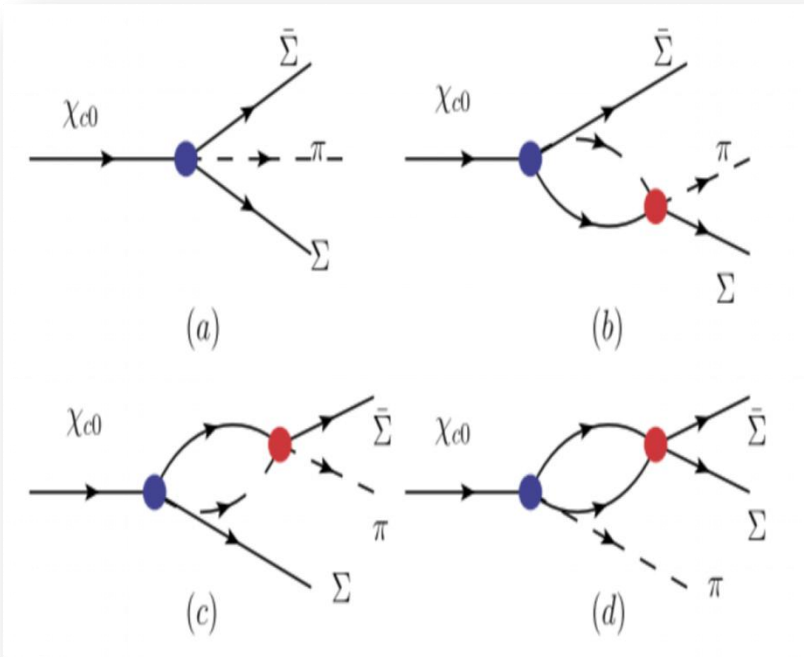
**Cusp signal of  $\Sigma(1/2^-)$  around  $\bar{K}N$  threshold!**

# Charmed baryon decay

- $\Lambda_c^+ \rightarrow \gamma \Lambda \pi$ , KWang, YFWang, BCLiu, and Fhuang, 2408.12965

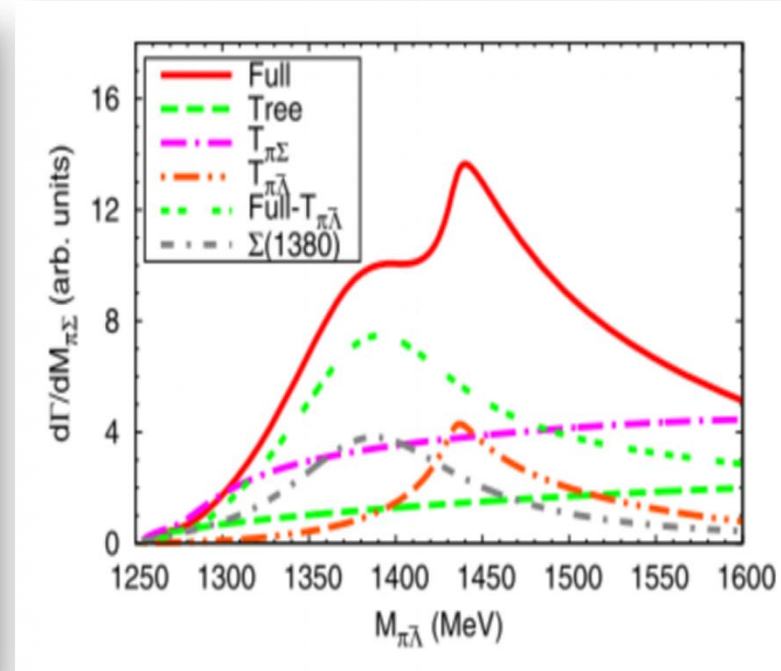


# Charmonium decays



$\chi_{c0} \rightarrow \bar{\Sigma} \Sigma \pi$

PLB753(2016)526



$\chi_{c0} \rightarrow \bar{\Lambda} \Sigma \pi$

PRD98(2018)114017

# Two poles of $\Sigma(1/2^-)$

PHYSICAL REVIEW LETTERS **130**, 071902 (2023)

## Cross-Channel Constraints on Resonant Antikaon-Nucleon Scattering

Jun-Xu Lu<sup>1,2</sup>, Li-Sheng Geng<sup>3,2,4,5,\*</sup>, Michael Doering<sup>6,7</sup> and Maxim Mai<sup>8,6</sup>

<sup>1</sup>School of Space and Environment, Beijing 102206, China

<sup>2</sup>School of Physics, Beihang University, Beijing 102206, China

It is interesting to note that in our NNLO fit there exist two  $I = 1$  states around the  $\bar{K}N$  threshold located at (1435, -39) MeV and (1440, -135) MeV on the  $(- - + + +)$  sheet, the order of which corresponds to  $\pi\Lambda$ ,  $\pi\Sigma$ ,  $\bar{K}N$ ,  $\eta\Lambda$ ,  $\eta\Sigma$ ,  $K\Xi$  respectively. Both states are well above the  $K^-p$  threshold and appear as cusps on the real axis. In the Fit “NNLO\*” in which the constraints from baryon masses are omitted, the two  $I = 1$  states are located at (1364, -110) MeV and (1432, -18) MeV also on the  $(- - + + +)$  sheet. In this case, the narrower state still shows up as a cusp but the broader one becomes a broad enhancement on the  $I = 1$  amplitude on the real axis. We note that the existence of a  $\Sigma^*(\frac{1}{2}^-)$  state has been predicted in a number of UChPT

**Are there two poles of  $\Sigma(1/2^-)$  ?**

# Summary

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- The missing  $\Sigma(1/2^-)$  is important for understanding the baryon spectrum.
- Internal structure: compact pentaquark & molecule
- Searching for  $\Sigma(1/2^-)$  in
  - Hadron-hadron scattering
  - $\gamma/\nu$ -production
  - Charmed baryon decays
  - Charmonium decays

<https://indico.ihep.ac.cn/event/23232/>

第六届粒子物理天问论坛

2024年11月8日-12日，河南洛阳

**Thank you very much!**