

# Energy Correlators for Light Hadrons and Quarkonium

Xiaohui Liu

Heavy Flavor and QCD workshop @ Qingdao, 2024



XL, Zhu, [arxiv: 2403.08874](#)  
XL, Shao, Zhu, [in preparation](#)  
Chen, XL, Ma, [to appear](#)

# Outline

## Adapt EEC to QCD non-perturbative Studies

- TMDs out of the Semi-Inclusive Energy Correlators
- Hadronization in Quarkonium
- Conclusion

We are grateful to Miguel Arratia, Hao Chen, Zhong-bo Kang, Ian Moult, Jinlong Zhang, and Jian Zhou for insightful discussions. We are grateful for the hospitality of the committee for the “Heavy flavor and QCD” workshop held in Changsha where this work was initiated. We appreciate stimulating feedback from the EicC bi-week meeting. This work is supported by the Natural Science Foundation of China under Contract No. 12175016 (X. L.), No. 11975200 (H. X. Z.), and No. 12147103 (H. X. Z.).

# Motivation

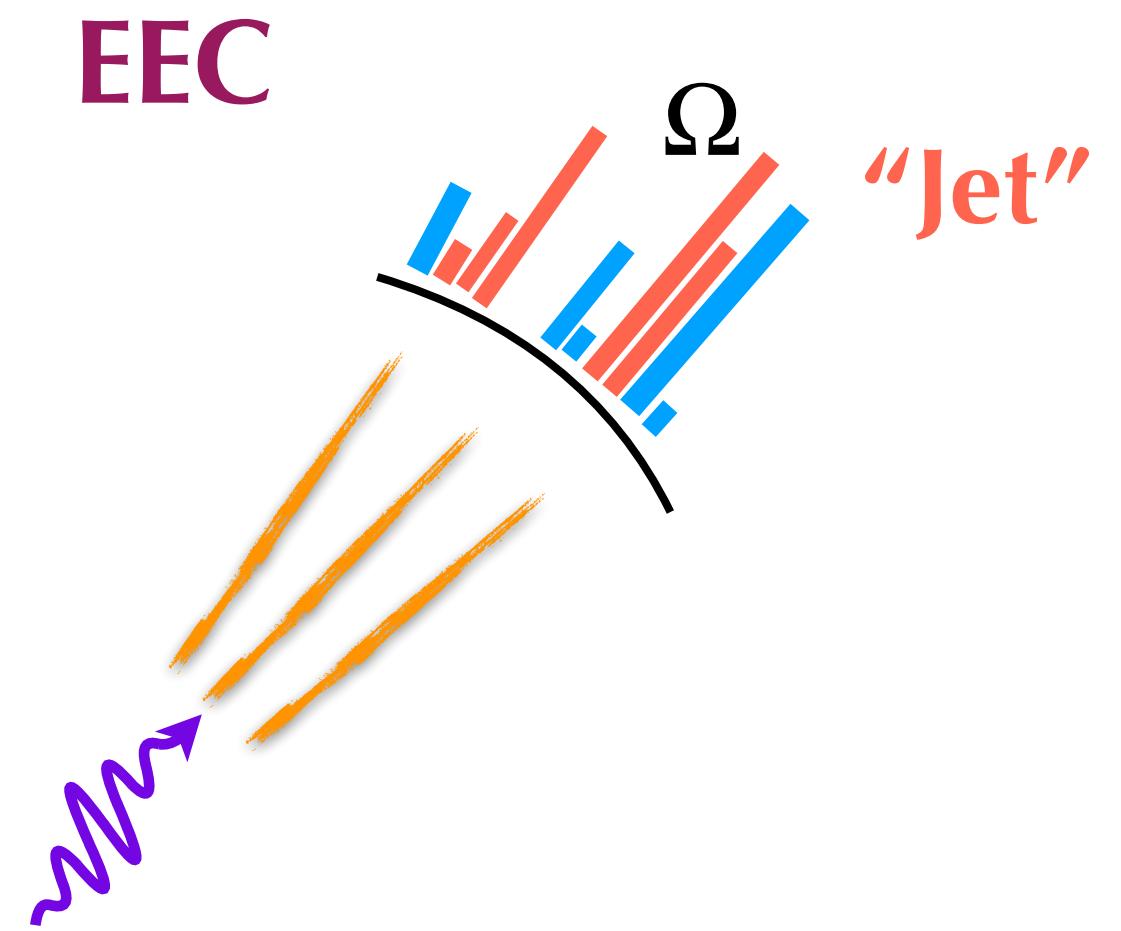
- Non-perturbative QCD/Confinement
- Hadron structures: TMDs, GPDs, ...
- Hadronization: FF? LFWFs? LDME? ...

How many energy emitted?

Distribution of the emissions?

Largely remains a mystery

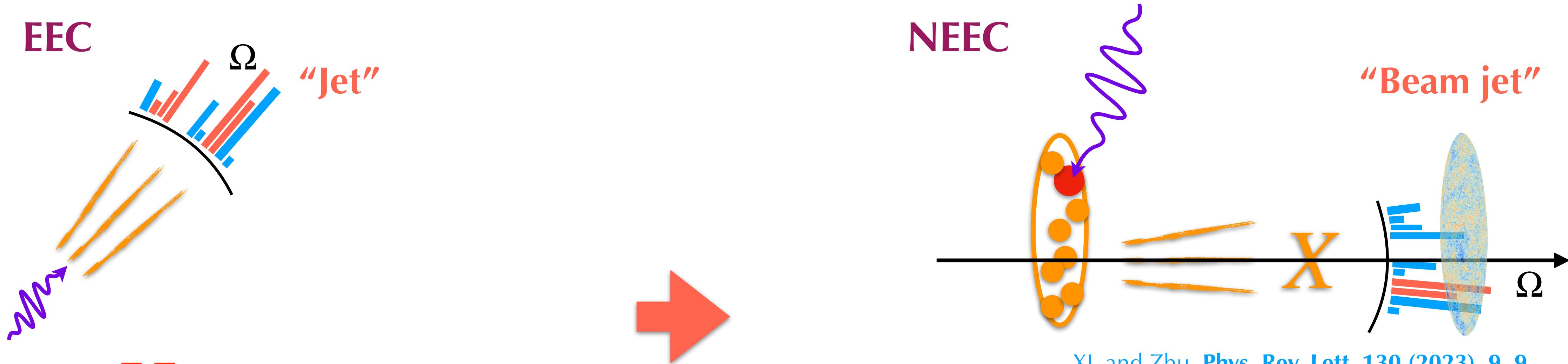
# Adapt EEC to Structure Studies



$$\Sigma_{\text{EEC}} \propto \frac{1}{\sigma} \int d\sigma \frac{E_i E_j}{Q^2} \delta(\Omega - \Omega_{ij})$$

- See Hua Xing's talk for theory details

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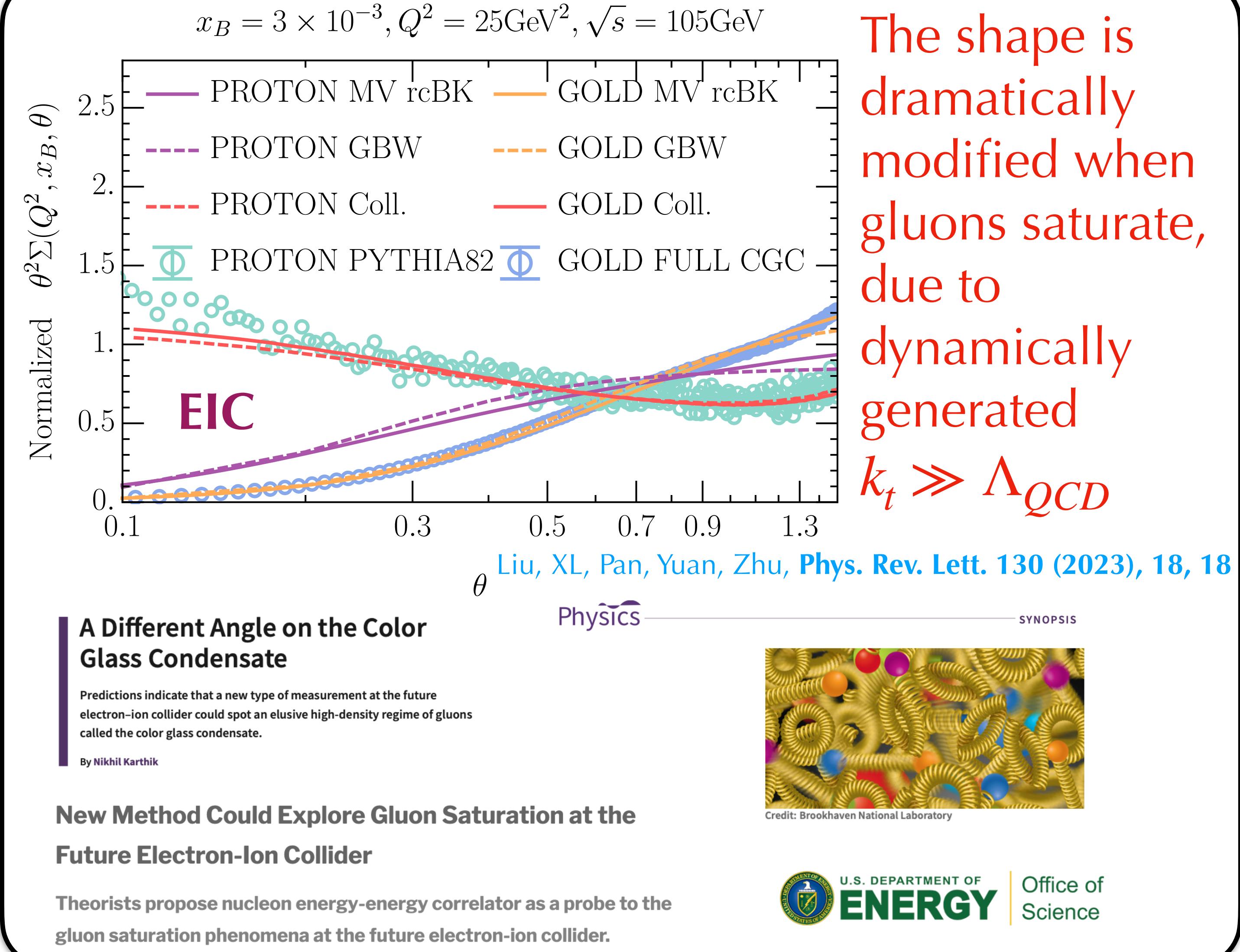
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XL and Zhu, Phys. Rev. Lett. 130 (2023), 9, 9

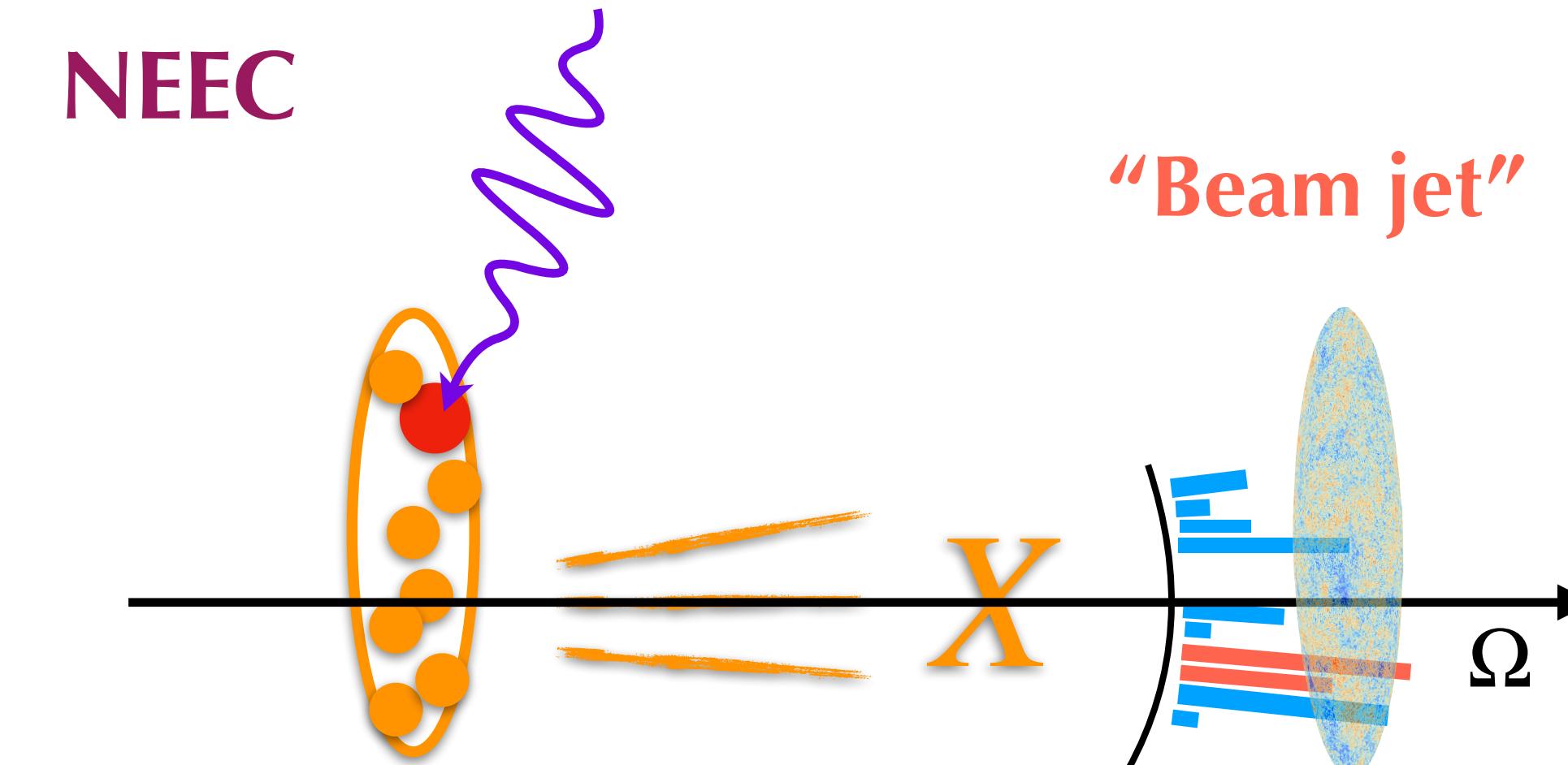
$$\Sigma_{\text{NEEC}} \propto \frac{1}{\sigma} \int d\sigma \frac{E_i}{E_P} \delta(\Omega - \Omega_i)$$

- $f_{\text{EEC}}(x, \theta) \propto \langle P | \bar{\psi}(y^-) \mathcal{E}(\Omega) \psi(0) | P \rangle$
- A new probe of/sensitive to the internal transverse dynamics

# Adapt EEC to Structure Studies



The shape is dramatically modified when gluons saturate, due to dynamically generated  $k_t \gg \Lambda_{QCD}$



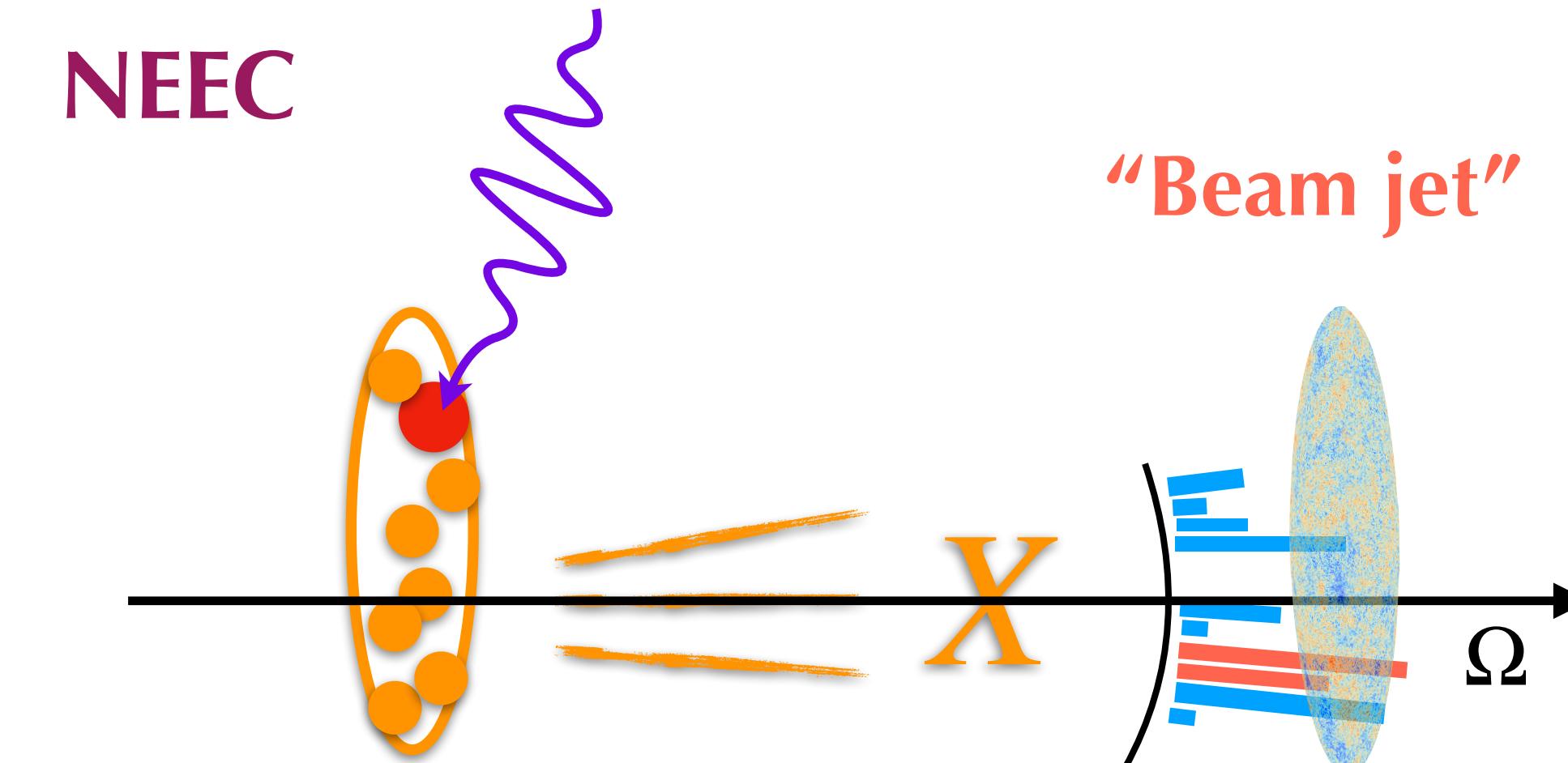
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# Adapt EEC to Structure Studies

Connection to TMDs?



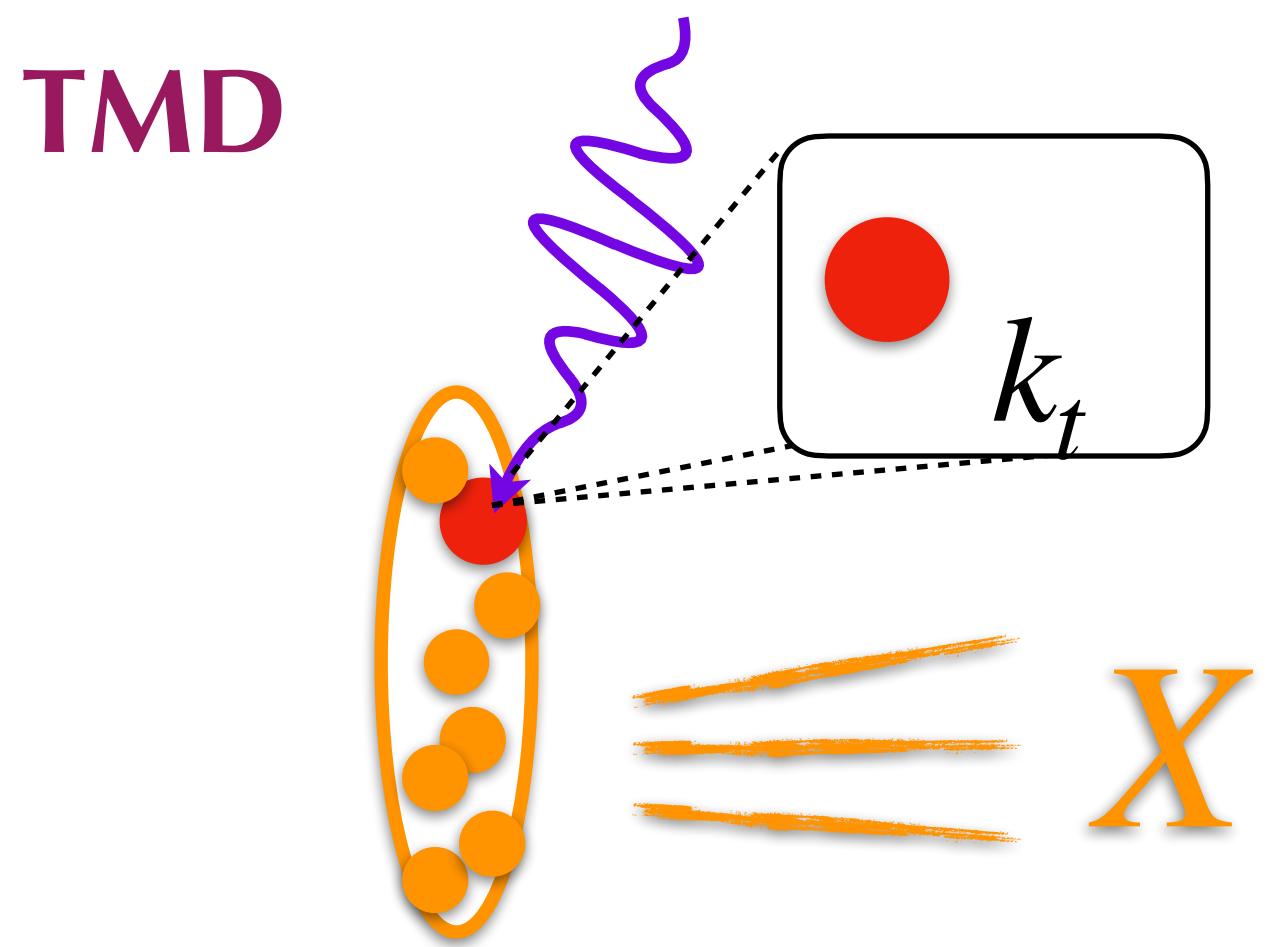
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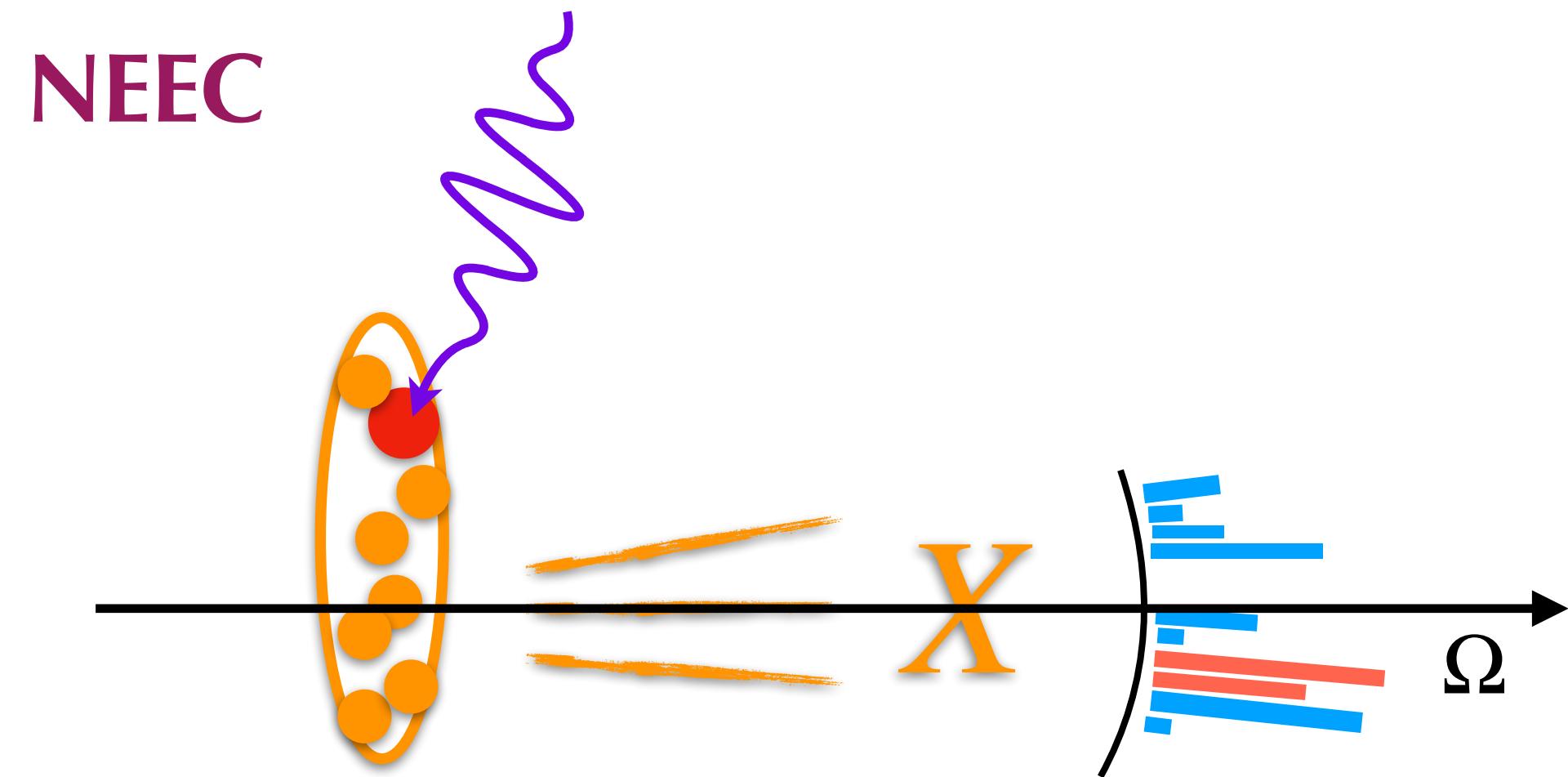
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# TMDs out of the Semi-inclusive ECs

XL, Zhu, arxiv: 2403.08874



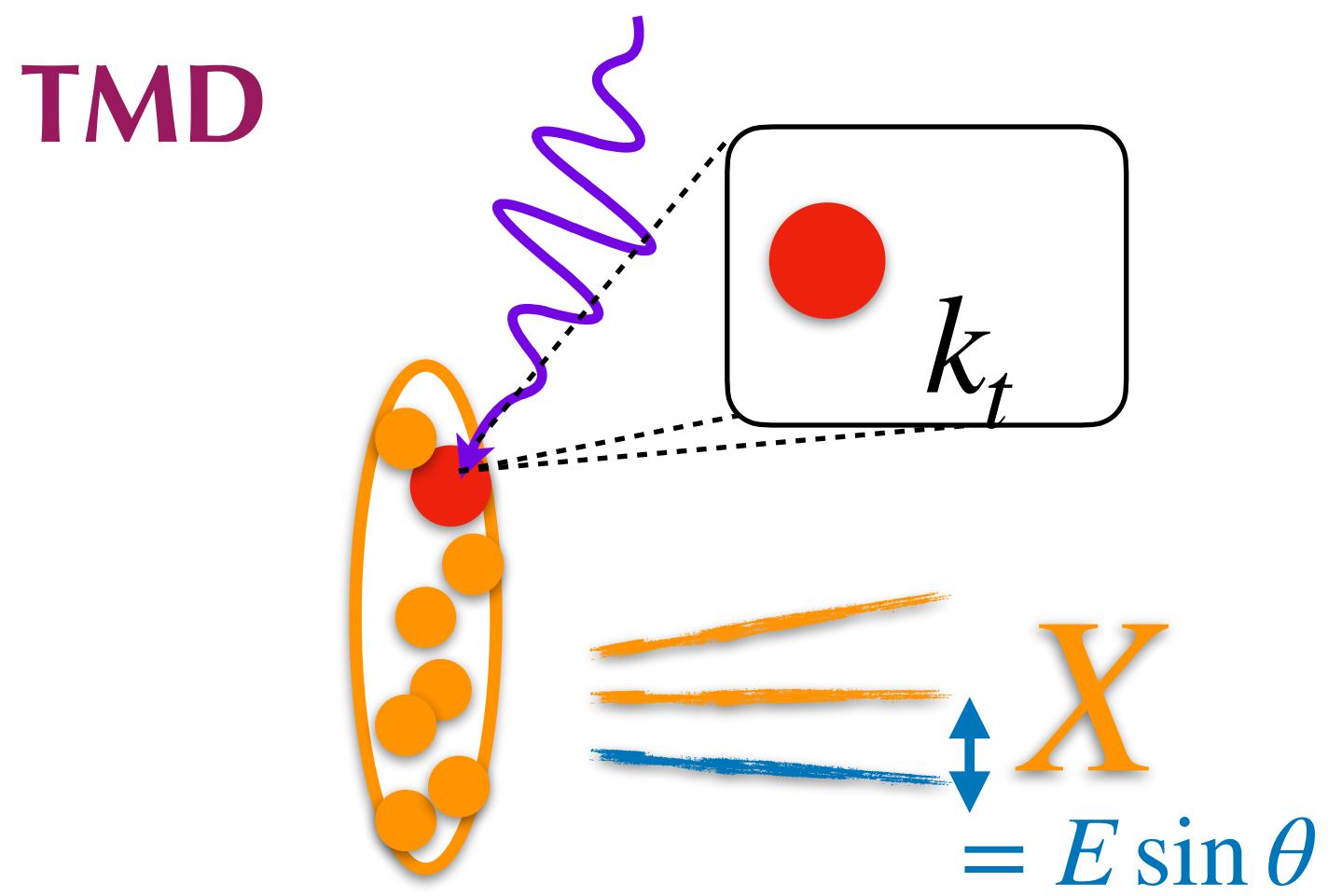
$$\vec{k}_t = - \sum_{i \in X} \vec{p}_{i,t} = - \sum_{i \in X} E_i \sin \theta_i (\cos \phi_i, \sin \phi_i)$$



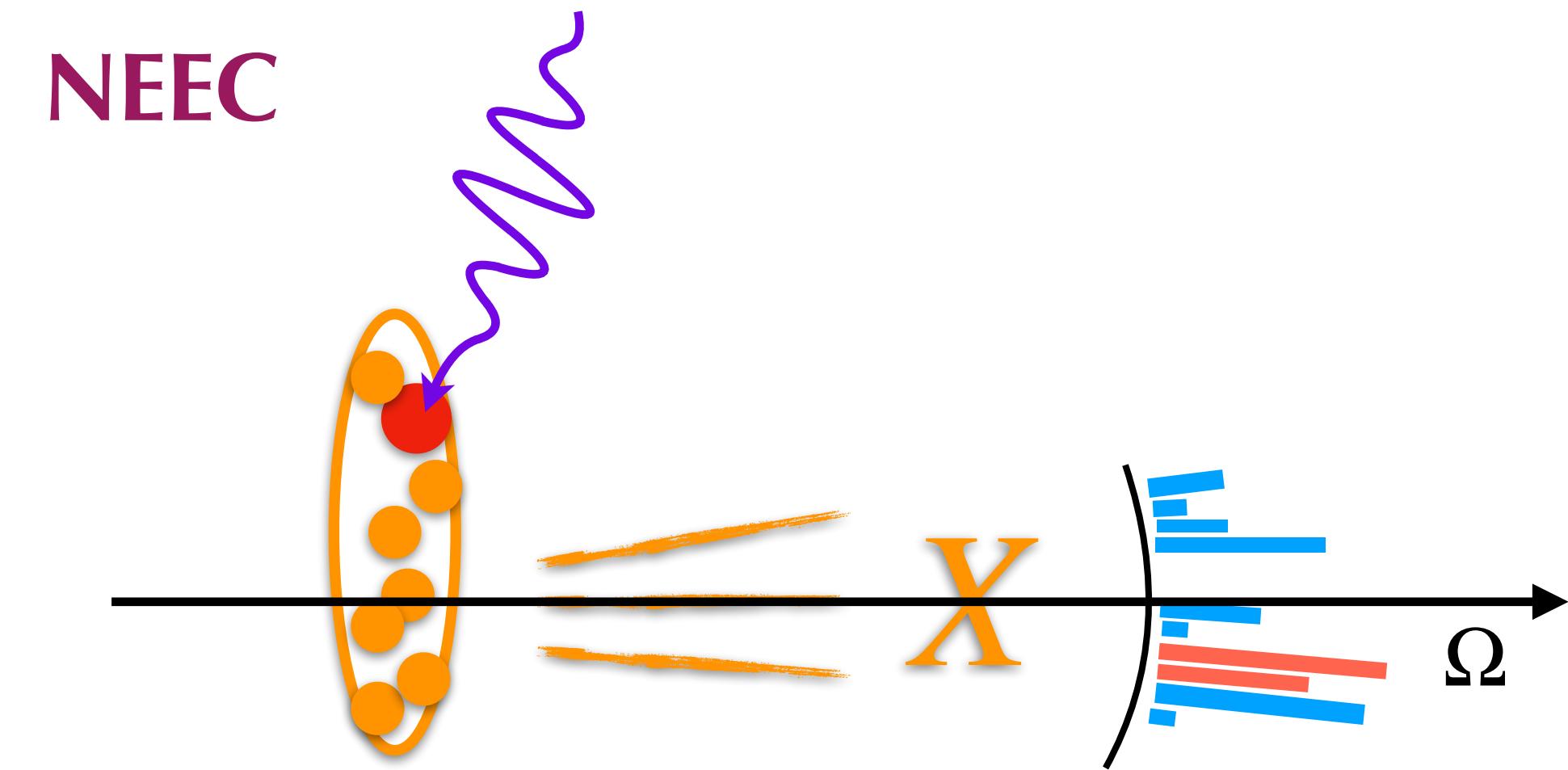
$$\mathcal{E}(\Omega) = \sum_{i \in X} E_i \delta(\Omega - \Omega_i)$$

# TMDs out of the Semi-inclusive ECs

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$$\vec{k}_t = - \int d\theta d\phi \sin \theta (\cos \phi, \sin \phi) \mathcal{E}(\Omega)$$



$$\mathcal{E}(\Omega) = \sum_{i \in X} E_i \delta(\Omega - \Omega_i)$$

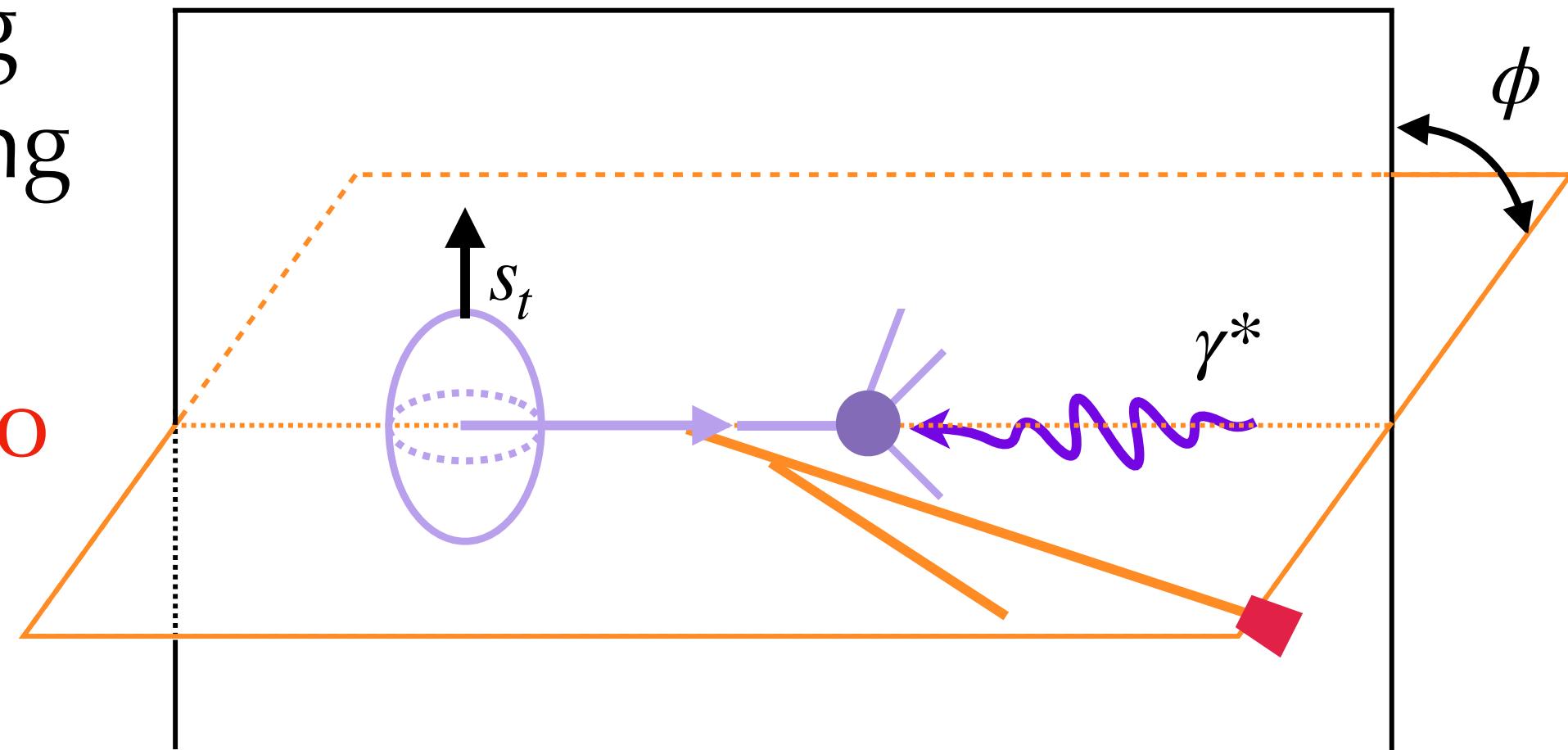
$$\int^\mu dk_t k_t^n f(k_t) = (-)^n \int_n^R \prod d\Omega w(\Omega_1) \dots w(\Omega_n) \langle P | \dots \mathcal{E}(\Omega_1) \dots \mathcal{E}(\Omega_n) \dots | P \rangle$$

# TMDs out of the Semi-inclusive ECs

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$$\int dk_t k_t^n f(k_t) = (-)^n \int \prod_n d\Omega w(\Omega_1) \dots w(\Omega_n) \langle P | \dots \mathcal{E}(\Omega_1) \dots \mathcal{E}(\Omega_n) \dots | P \rangle$$

- TMD PDFs (moment) can be obtained by measuring N-pt Nucleon Energy Correlator, by suitably selecting  $w(\Omega)$
- Inclusive measurement! Do not force b-to-b limit, no jets/fragmentation function involved !
- Nucleon Energy Correlator can be regarded as a generating observable, contains more comprehensive information



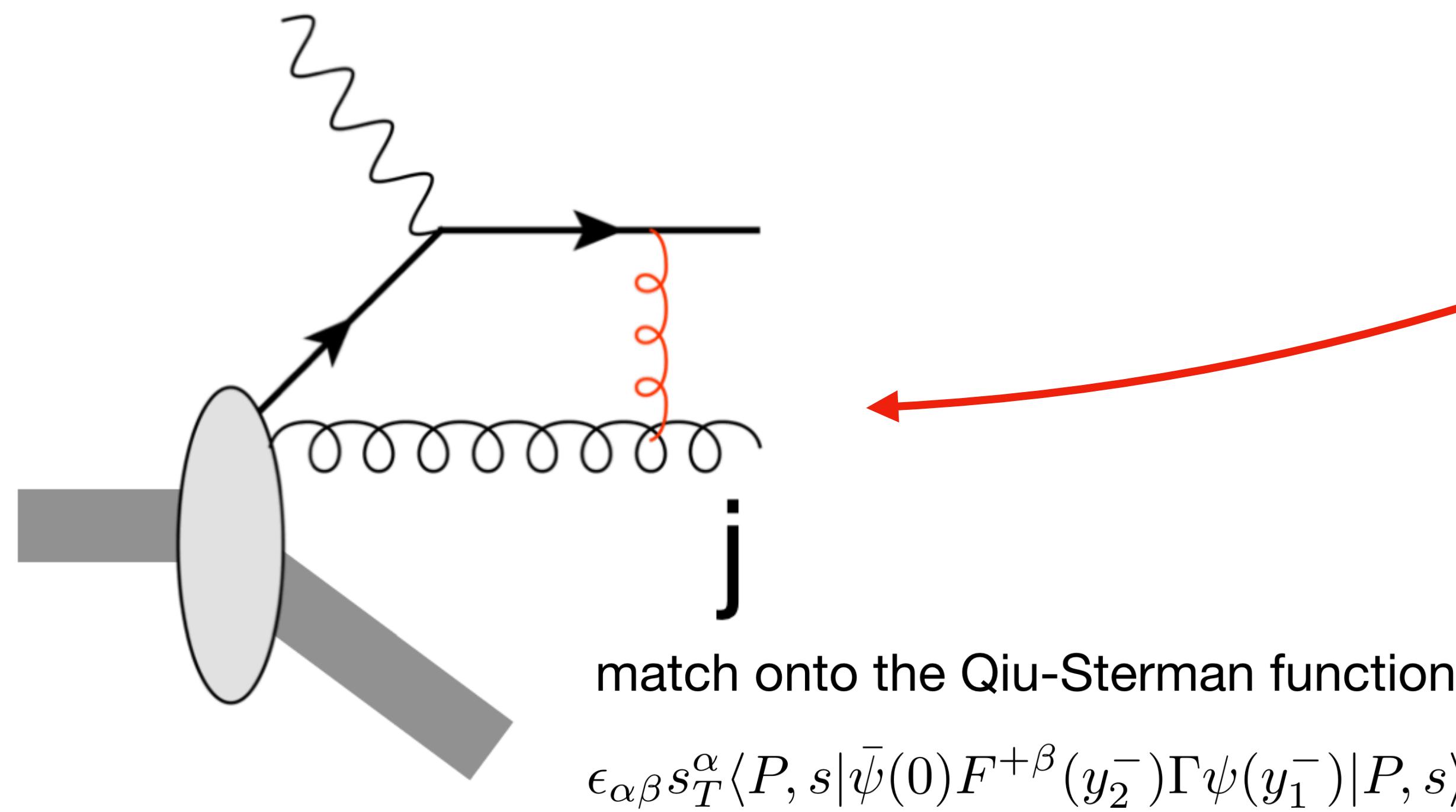
Sivers and only Sivers!

$$w \sim \sin \phi$$

# TMDs out of the Semi-inclusive ECs

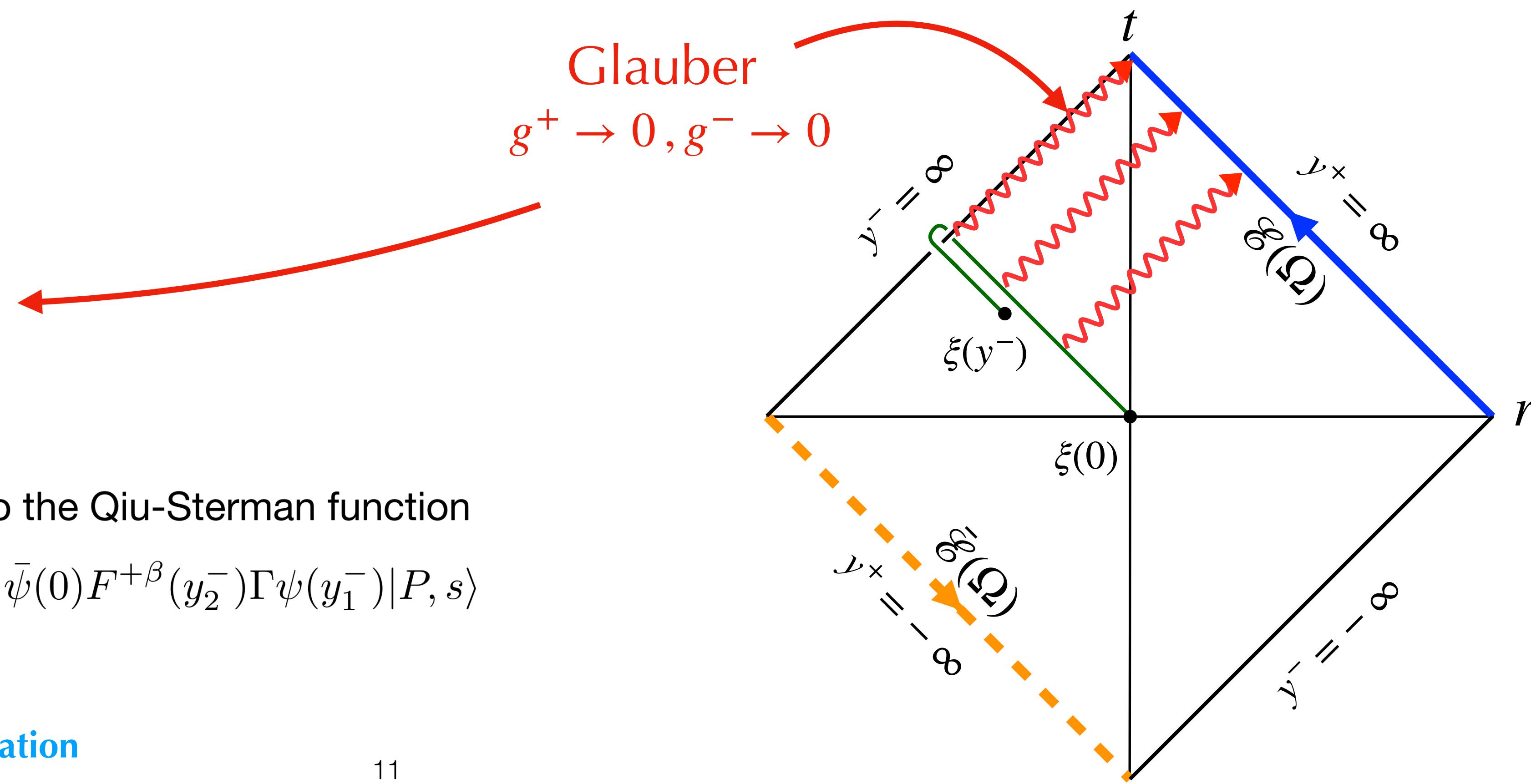
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$$f_{q,n=1}^{\text{DIS}}(x, \Omega) = \int \frac{dy^-}{2\pi} e^{-ixy^- P^+} \langle P s_t | \bar{\xi}(y^-, \mathbf{0}) \mathcal{L}(y^-, \infty) \mathcal{E}(\Omega) \frac{\gamma^+}{2} \mathcal{L}(\infty, 0) \xi(0) | P s_t \rangle$$



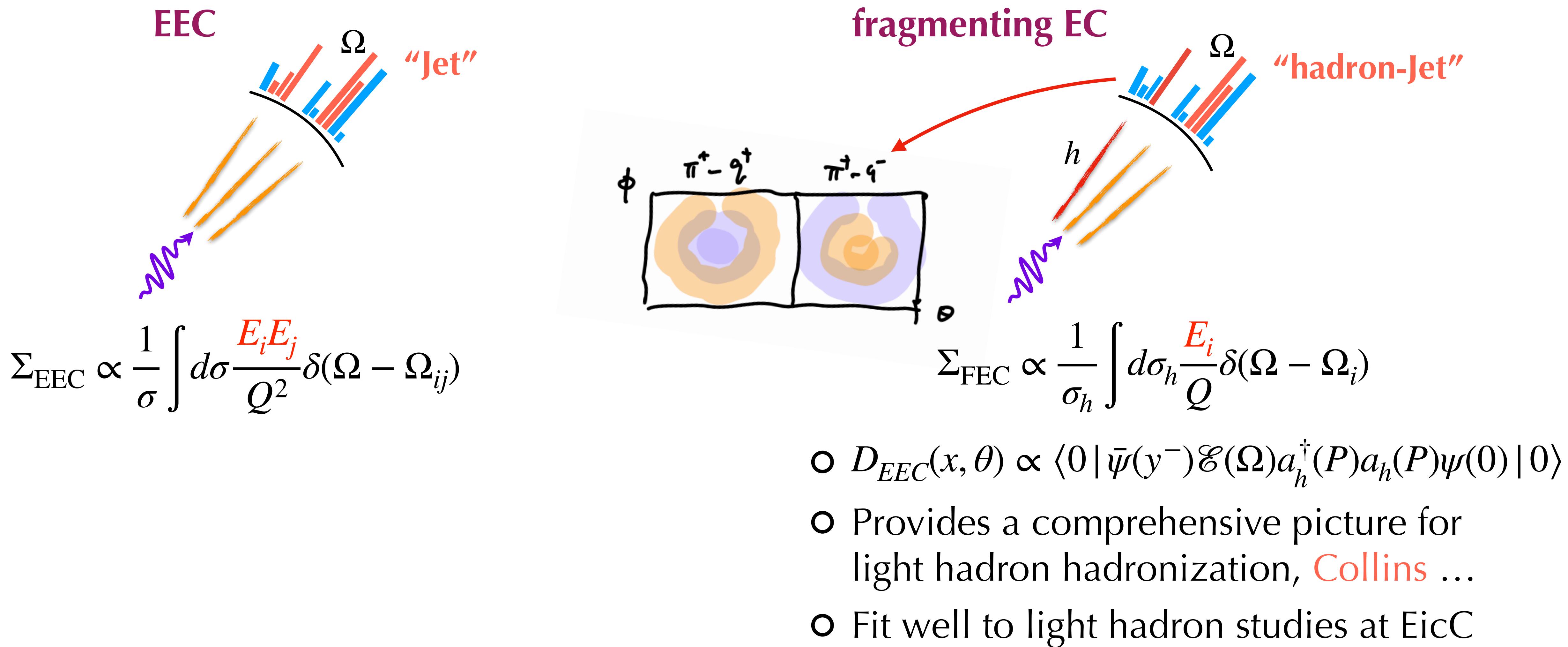
Hua Xing SCET talk

XL, Shao, Zhu, in preparation



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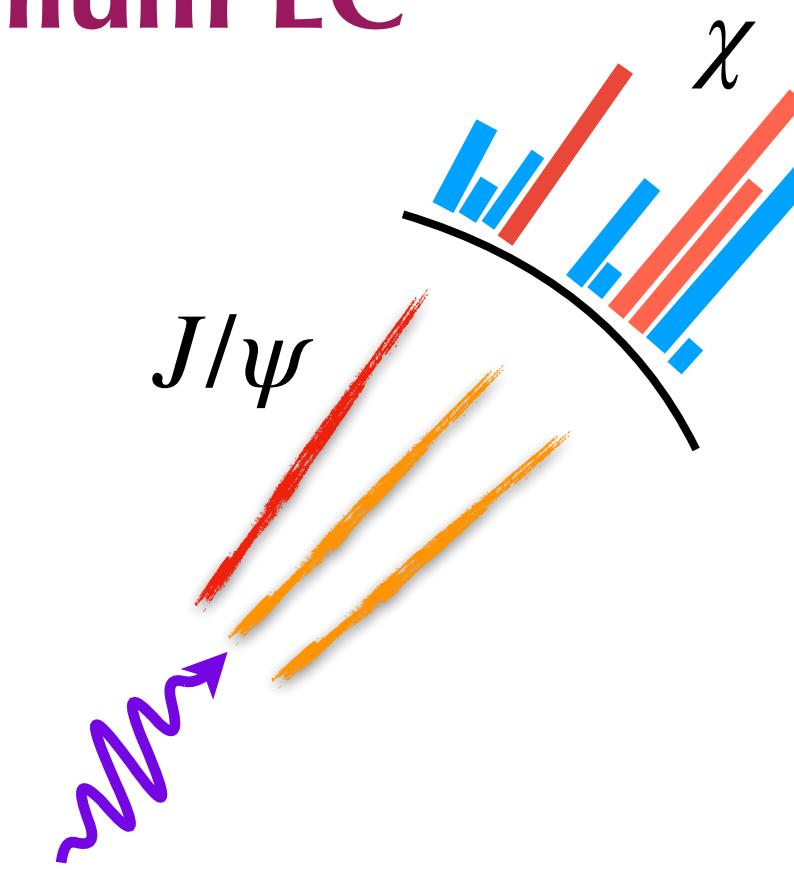


# Quarkonium Energy Correlator

Chen, XL, Ma, **to appear**

- NRQCD factorization for quarkonium production
- regarded as an excellent place to study non-pert phenomenon for a long time
- $\langle \mathcal{O}_1 \rangle, \langle \mathcal{O}_8 \rangle$
- Hadronization  $c\bar{c} \rightarrow J/\psi?$  remains largely unknown: amount of energy released? Energy Distribution?

Quarkonium EC



“quarkonium-Jet”  
Rest frame!!

$$\Sigma_{QEC} \propto \frac{1}{\sigma_{J/\psi}} \int d\sigma_{J/\psi} \frac{E_i}{M} \delta(\chi - \chi_i)$$

$\Sigma(\cos \chi)$  could provide new venue to these problems

# Quarkonium Energy Correlator

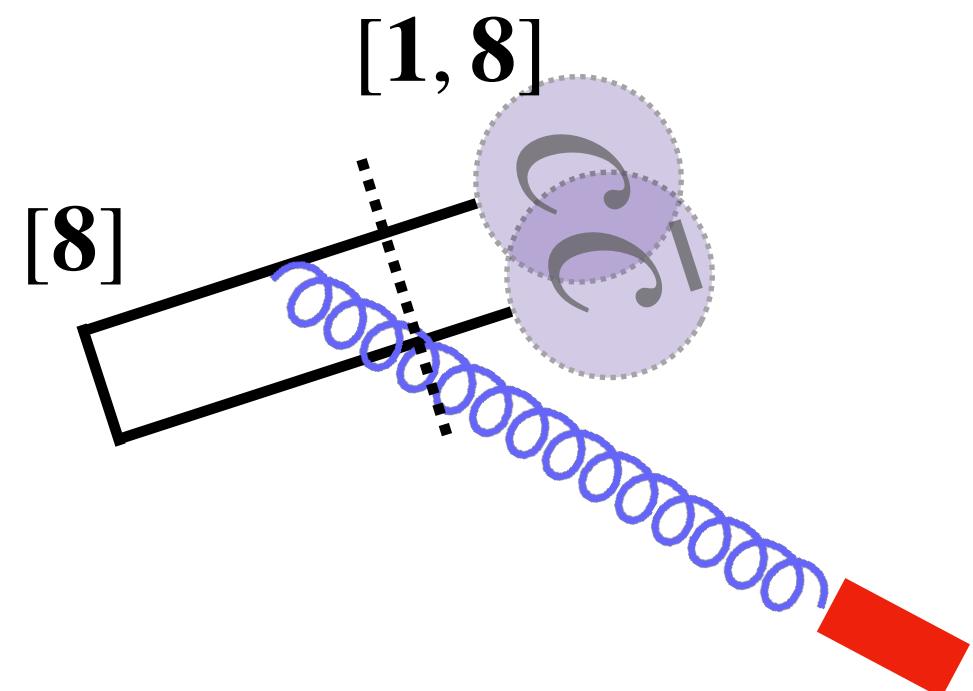
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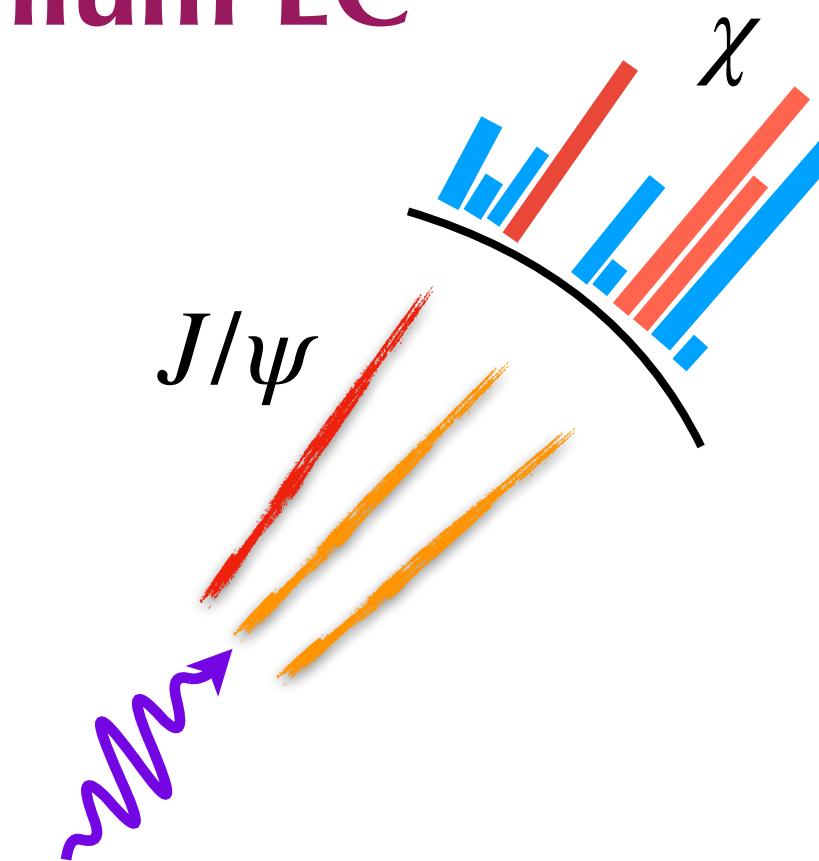
- $\Sigma_{QEC} = \Sigma_{QEC,P.T.} + \Sigma_{QEC,had.}$
- $\Sigma_{QEC,had.}$  relatively large  $\sim \frac{M\nu}{M} M^2 v^2 \langle \mathcal{O}_{1,8} \rangle$
- $\Sigma_{QEC,P.T.} \sim \alpha_s(\mu) \frac{E(\chi)}{M} E^2(\chi) \langle \mathcal{O}_{1,8} \rangle$

$$\alpha_s(M) \sim v^2, v \sim 0.5 \quad \text{for } J/\psi$$

$$\Sigma_{QEC,had.}/\Sigma_{QEC,P.T.} \sim \frac{v^3}{\alpha_s}, \text{ if } \frac{E}{M} \sim 1$$



## Quarkonium EC



“quarkonium-Jet”  
Rest frame!!

$$\Sigma_{QEC} \propto \frac{1}{\sigma_{J/\psi}} \int d\sigma_{J/\psi} \frac{E_i}{M} \delta(\chi - \chi_i)$$

$$\sim \frac{1}{\sigma} \int^{M\nu} \frac{E^2 dEd\Omega}{2E(2\pi)^3} \frac{E}{M} \langle \mathcal{O}_{1,8} \rangle \sim v(mv)^2 \langle \mathcal{O}_{1,8} \rangle$$

# Quarkonium Energy Correlator

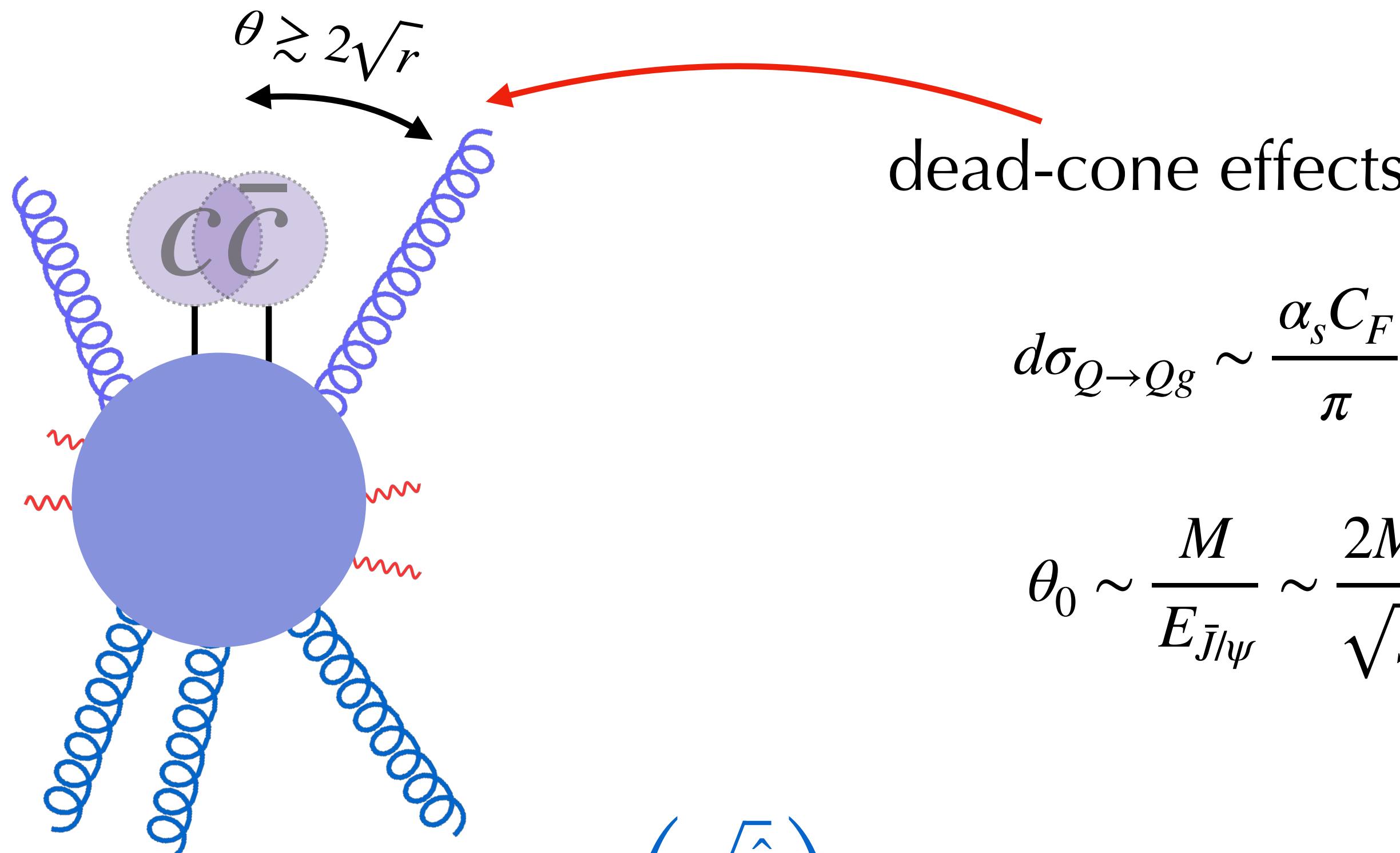
Chen, XL, Ma, **to appear**

Generic  $J/\psi$  production configuration in pQCD

COM frame

$$r \equiv \frac{M^2}{\hat{s}} \ll 1$$

$$E_s \sim \mathcal{O}(M), E_{J_{near}} \sim E_{J_{away}} \sim \mathcal{O}\left(\frac{\sqrt{\hat{s}}}{2}\right)$$



dead-cone effects

Dokshitzer et al., **J. Phys. G**

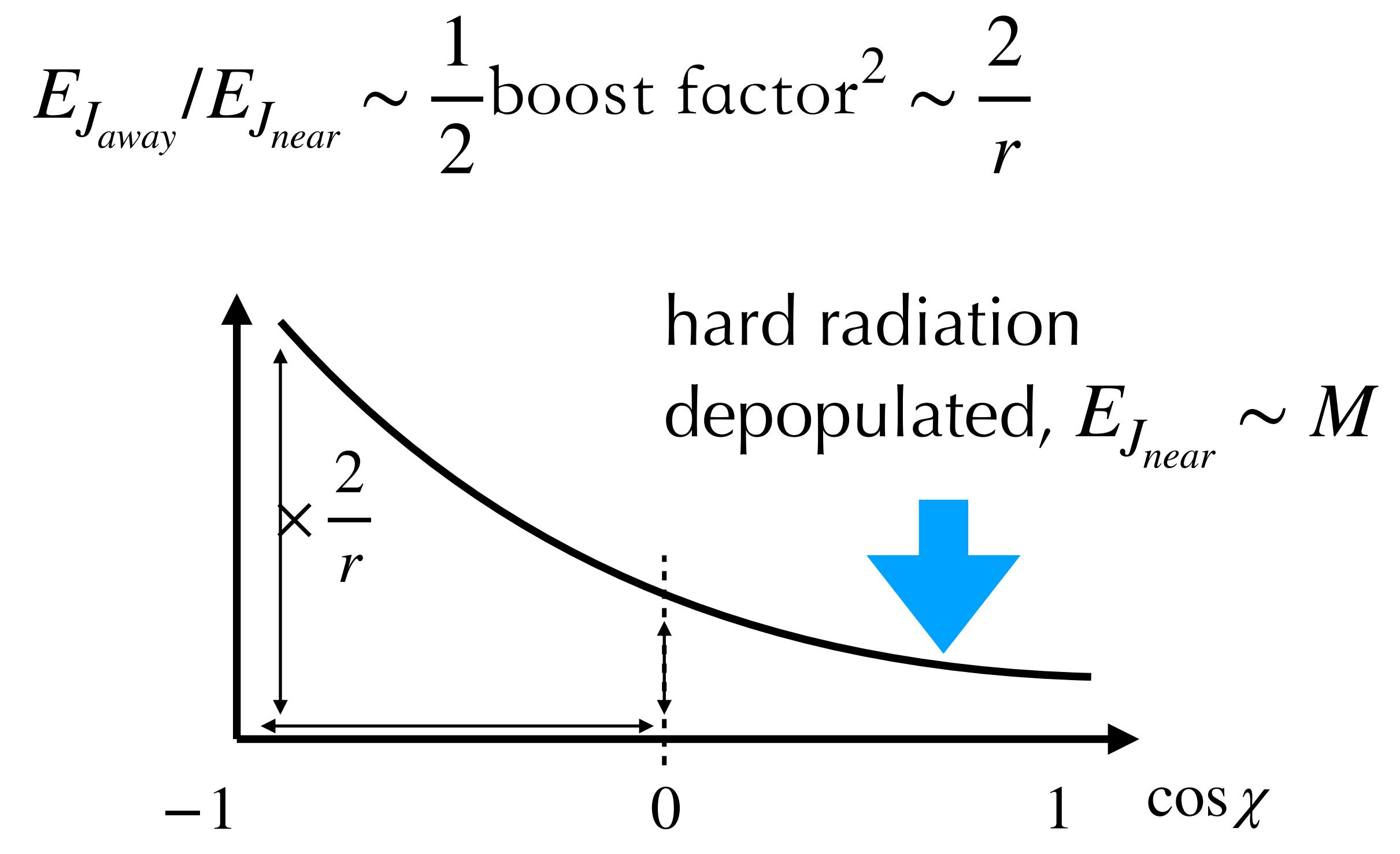
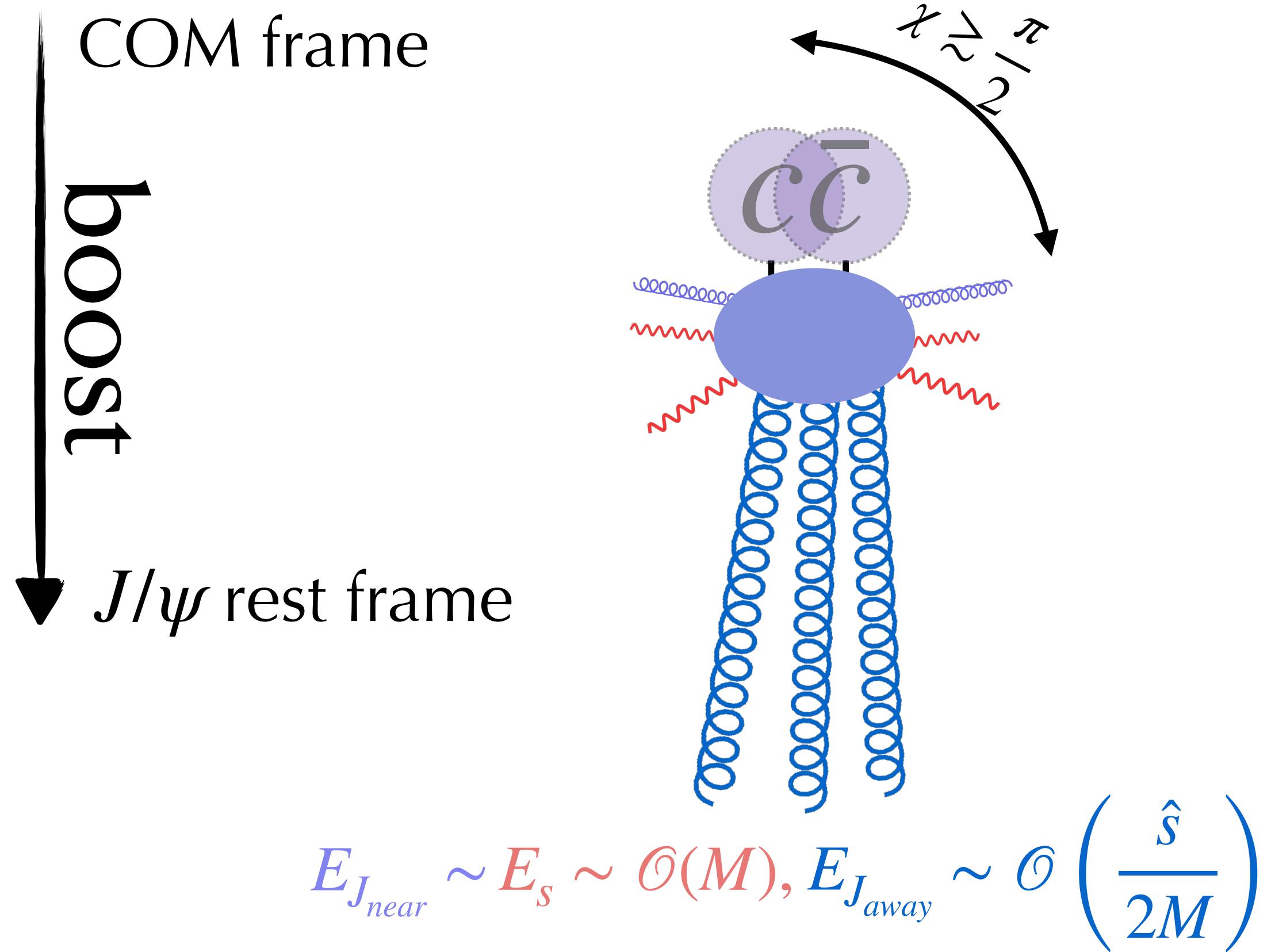
$$d\sigma_{Q \rightarrow Qg} \sim \frac{\alpha_s C_F}{\pi} \frac{dE_g}{E_g} \frac{\theta^2 d\theta^2}{[\theta^2 + \theta_0^2]^2}$$

$$\theta_0 \sim \frac{M}{E_{J/\psi}} \sim \frac{2M}{\sqrt{\hat{s}}} = 2\sqrt{r}$$

# Quarkonium Energy Correlator

Chen, XL, Ma, **to appear**

Generic  $J/\psi$  production configuration in pQCD

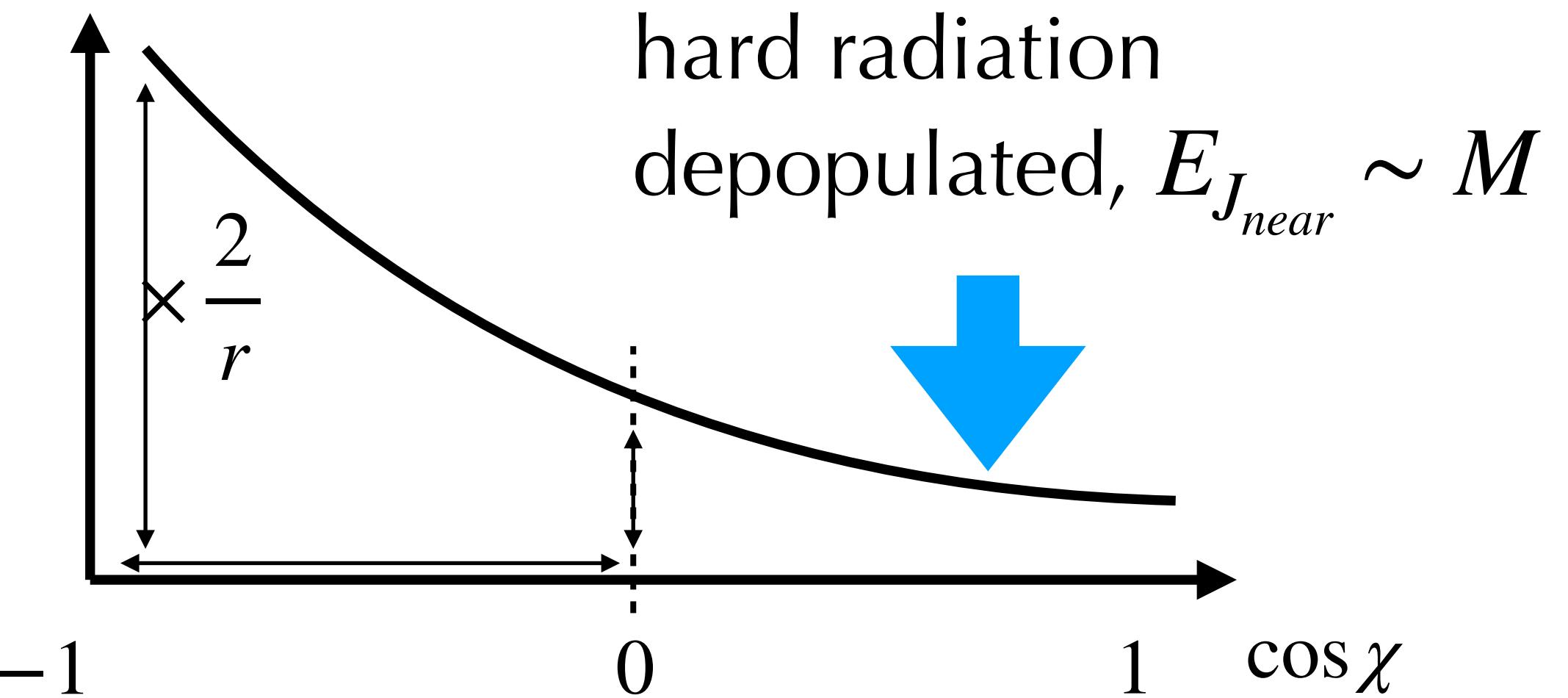
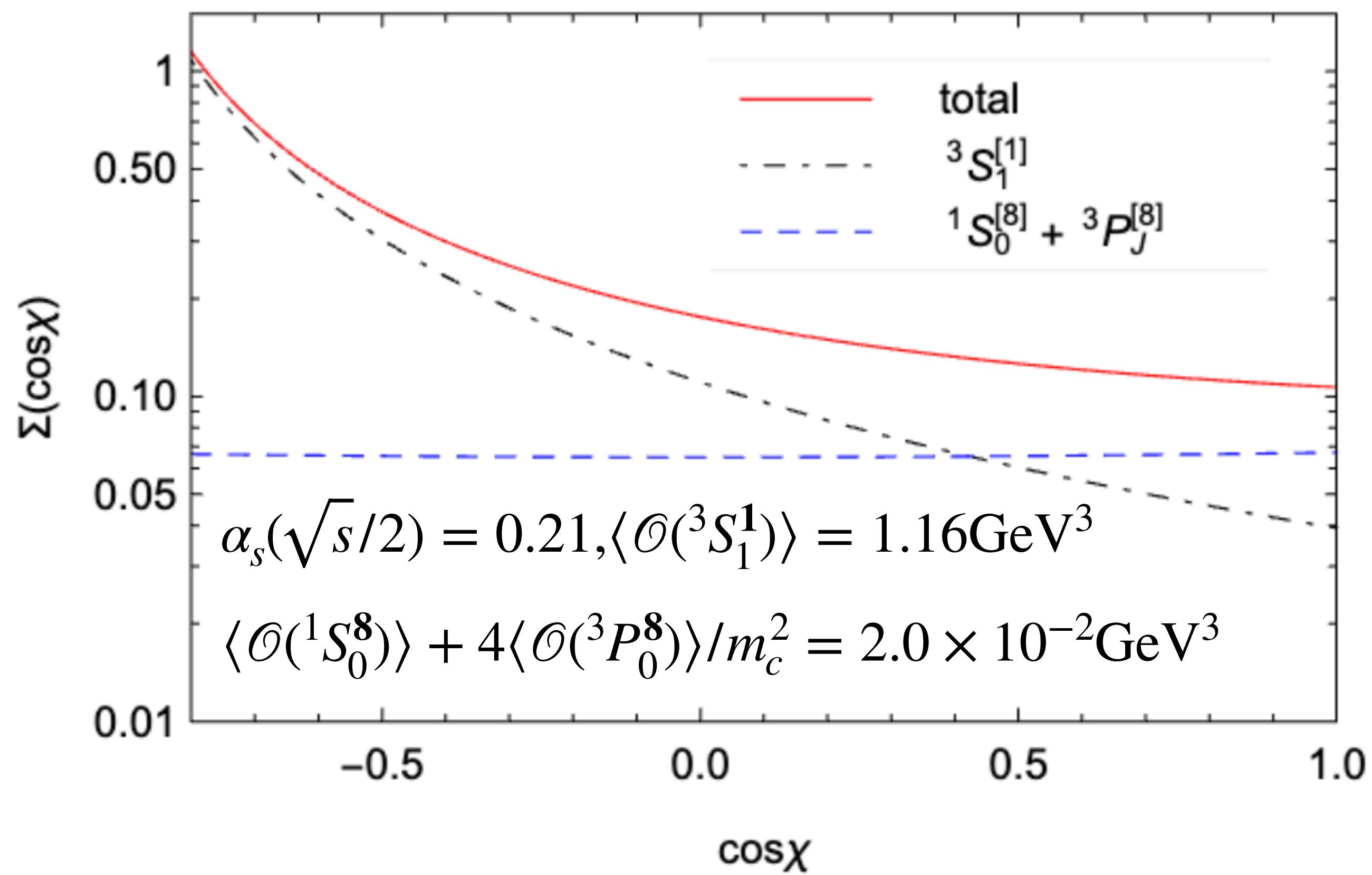


# Quarkonium Energy Correlator

Chen, XL, Ma, to appear

Sizable hadronization effect!!

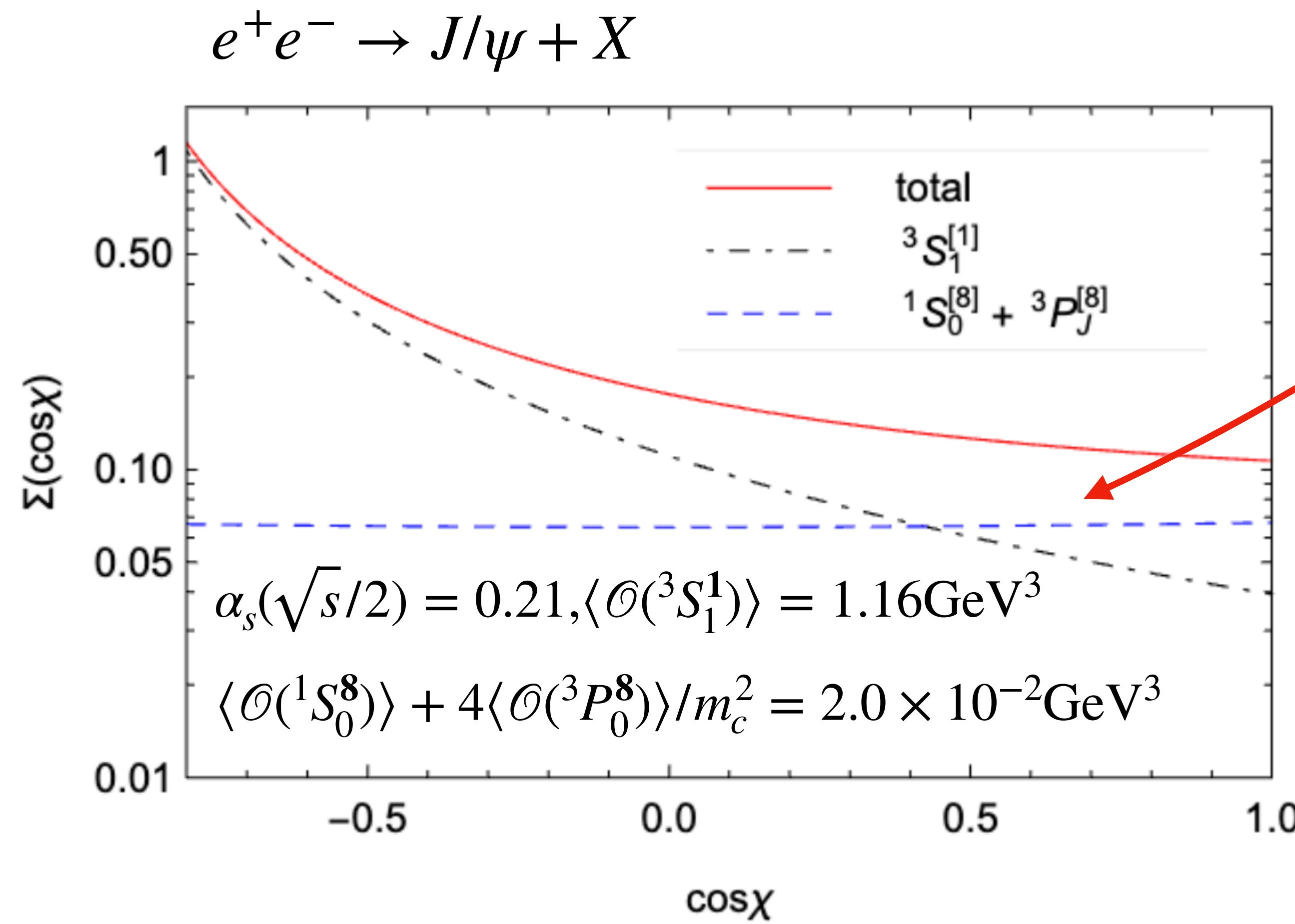
$$e^+e^- \rightarrow J/\psi + X$$



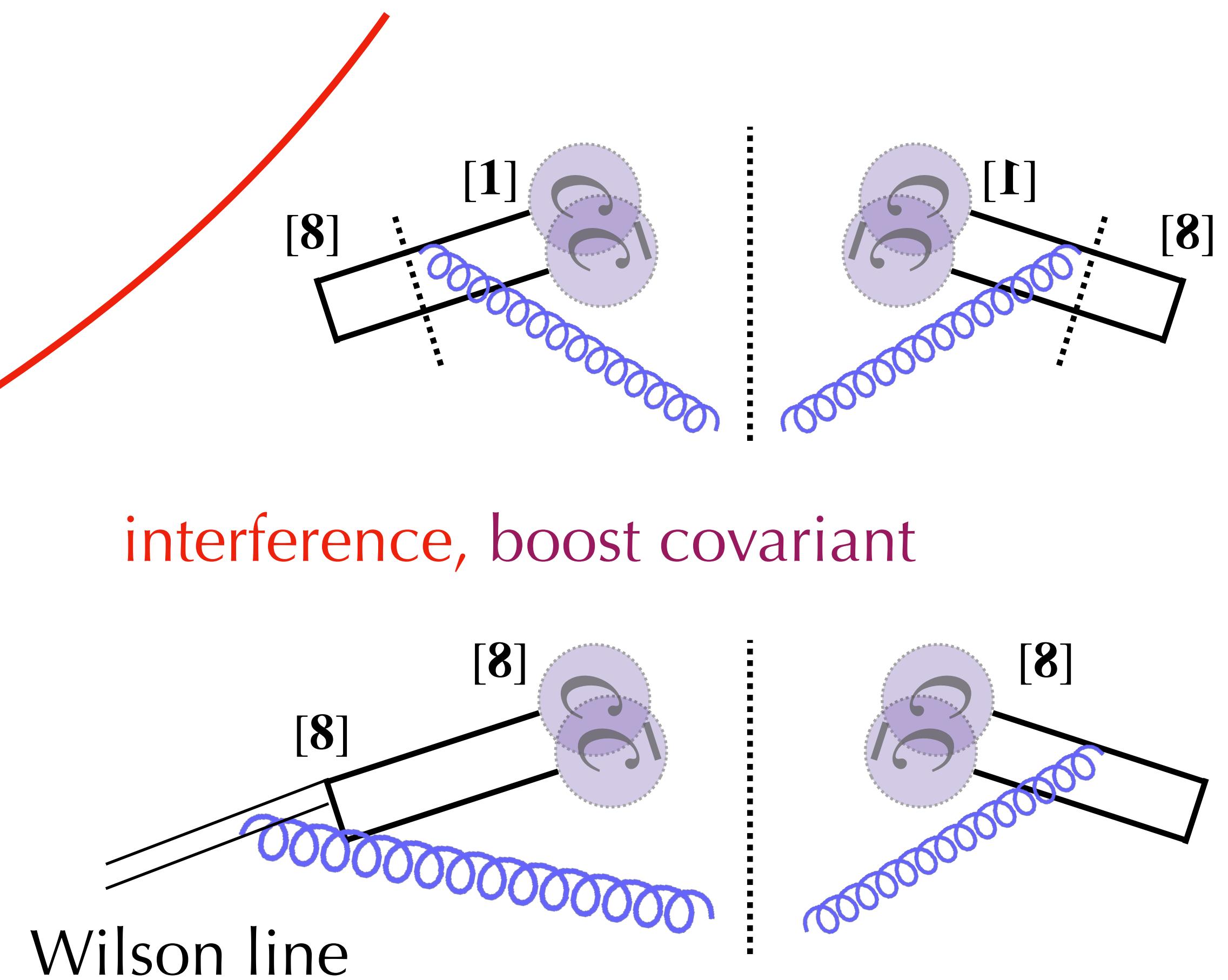
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Chen, XL, Ma, [to appear](#)

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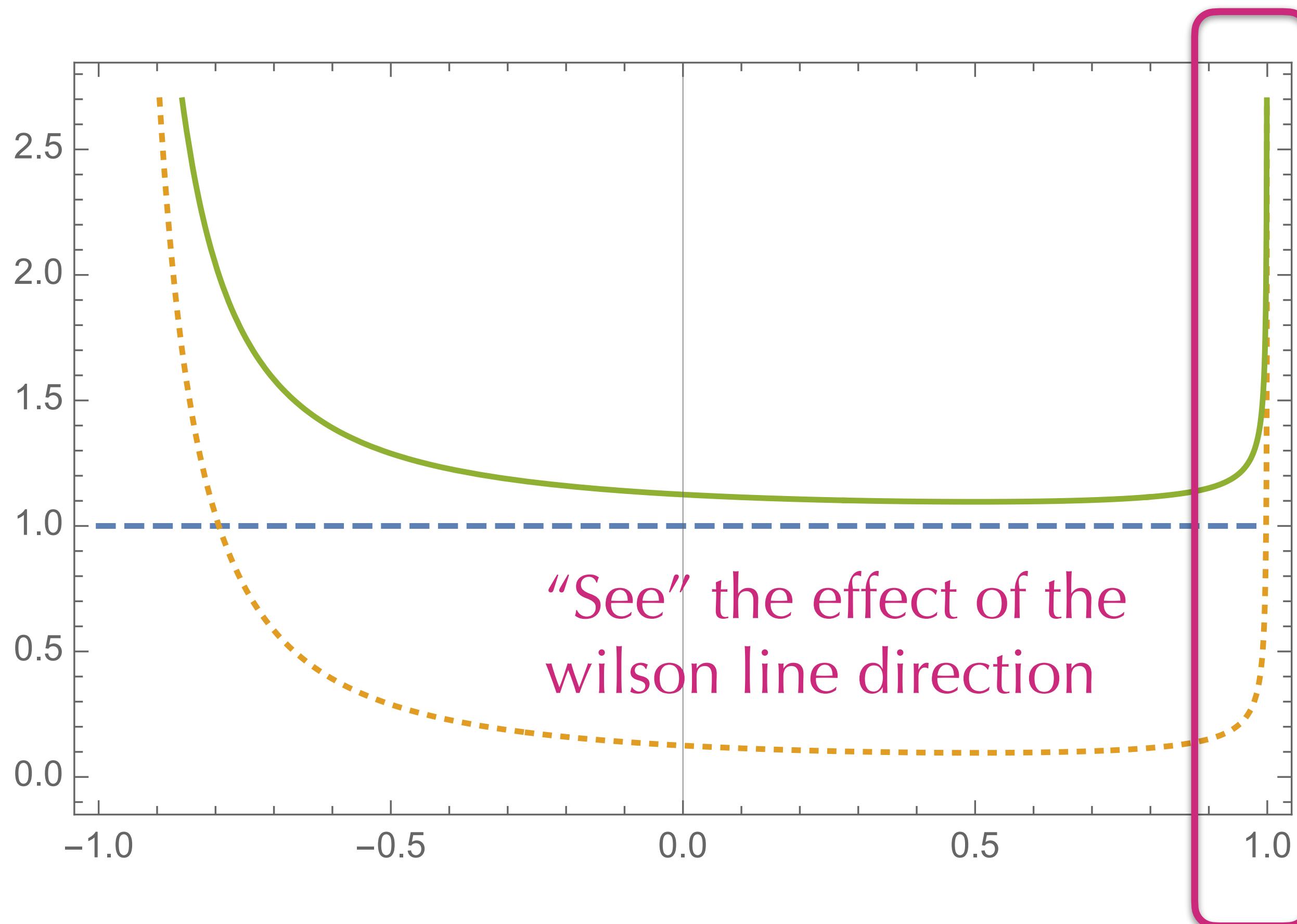
Ignore interference, rotational covariant



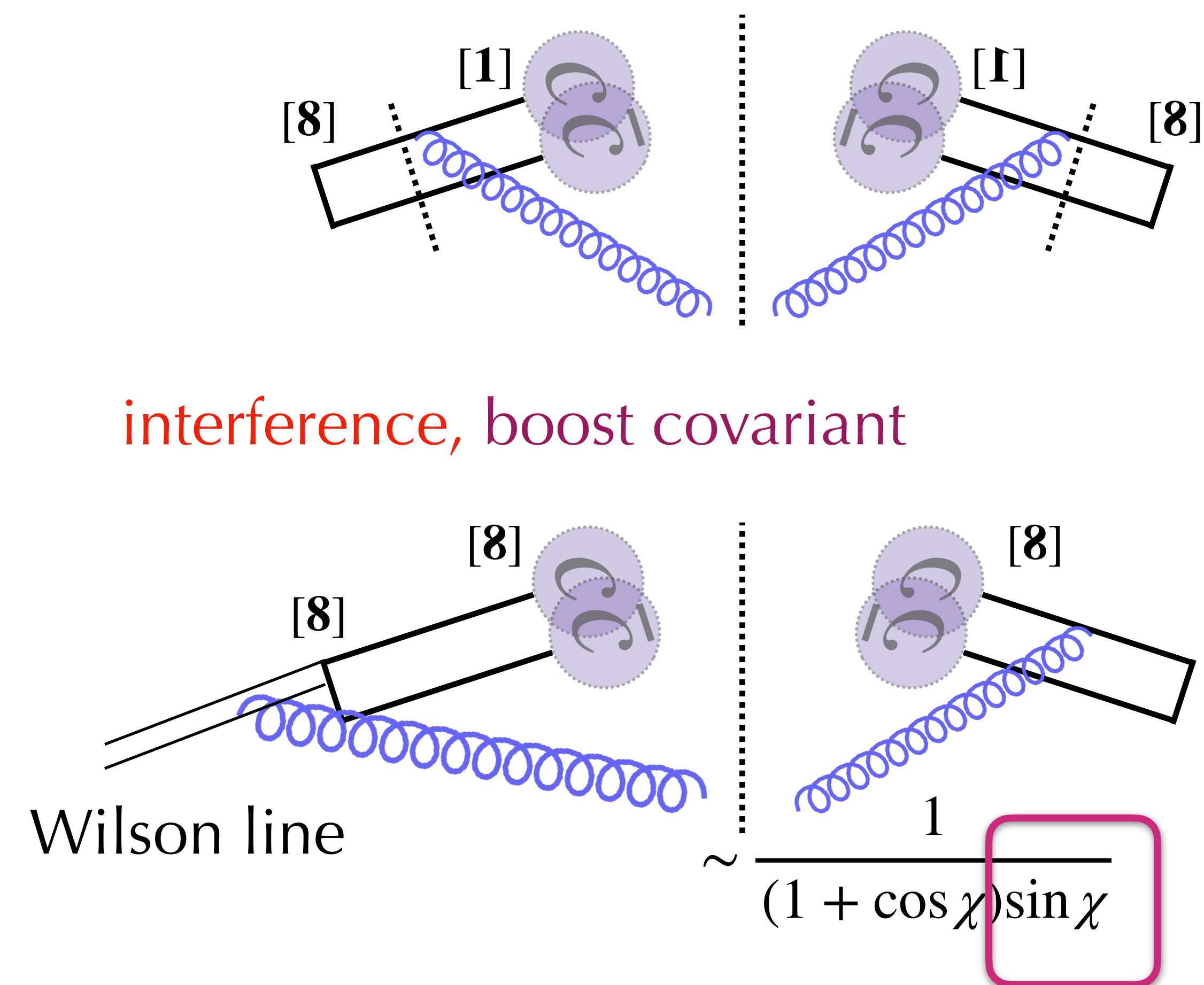
# Quarkonium Energy Correlator

Chen, XL, Ma, **to appear**

Relative size between non-inter vs interference



Ignore interference, rotational covariant



# Conclusion

- Energy correlators provide new insight/tool to non-pert. studies
- Suitable for EicC, Belle ...
- More (theory/pheno) in the future

Thanks

# Backup slides

# Exp. Measures

$$\Sigma(\chi) = \frac{1}{\sigma} \int d\sigma \sum_{ij} \frac{E_i E_j}{Q^2} \delta(\chi - \theta_{ij})$$

