



Factorization and resummation of heavy quark pair angular correlations

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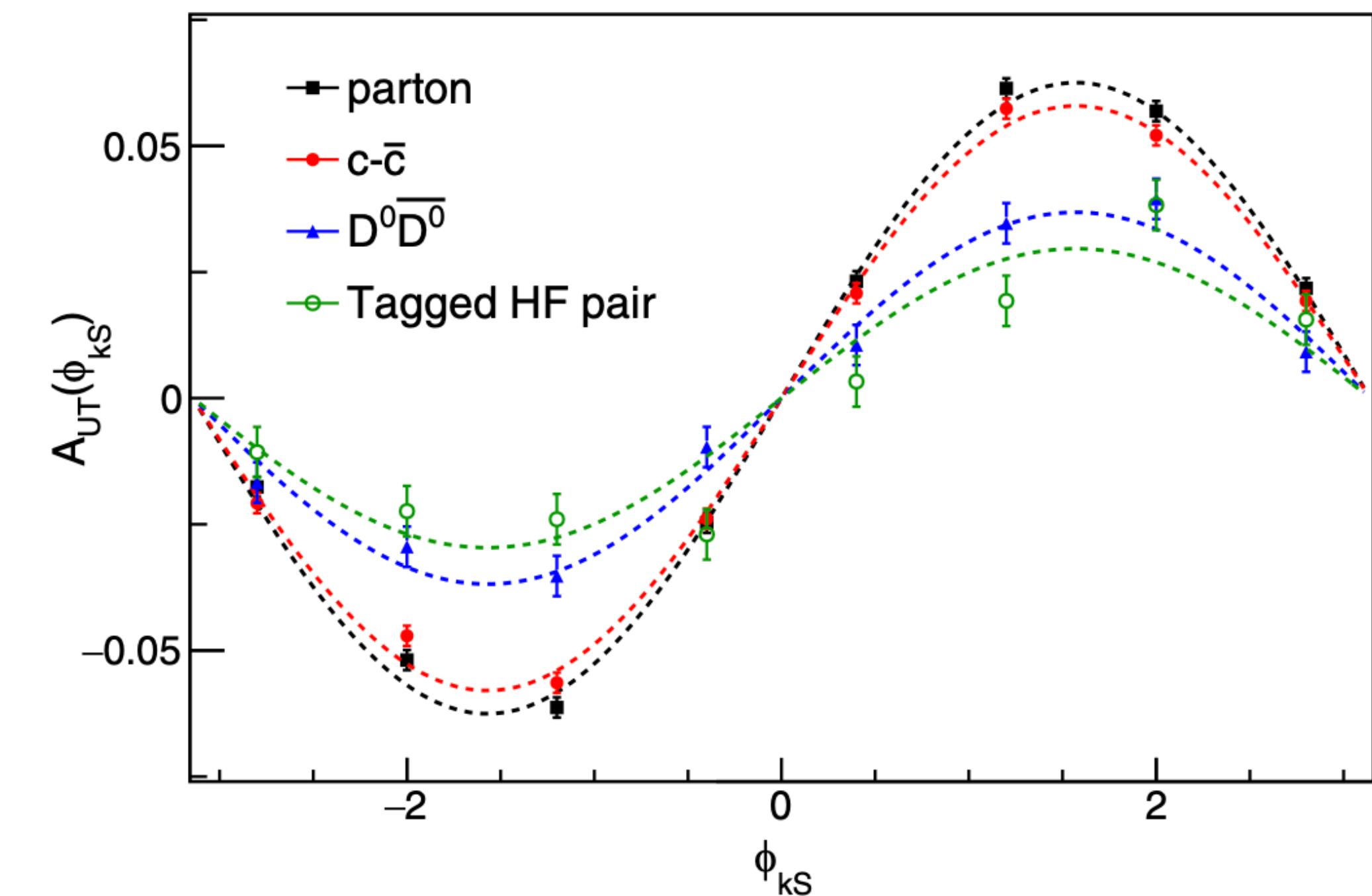
Gluon TMDs and spin asymmetry at the EIC

- The gluon transverse momentum dependent distributions (TMDs) are important towards understanding the transverse structure of the proton as well as QCD factorization
- **Gauge link dependent gluon TMDs** (TMD handbook '23)

$$\tilde{f}_{g/h}^{\alpha\beta 0(u)}(x, \mathbf{b}_T, \epsilon, \tau, xP^+) = \frac{1}{xP^+} \int \frac{db^-}{2\pi} e^{-ib^-(xP^+)} \langle h(P, S) | G^{+\alpha}(b^\mu) \mathcal{W}_\square(b^\mu, 0) G^{+\beta}(0) | h(P, S) \rangle$$

At the EIC , gluon TMDs can be probed via dihadron, open di-
charm, di-D-meson and dijet

- In the small x dijet process is the most promising channel
Zheng, Aschenauer, Lee, Xiao, Yin '18
- The heavy quark pair production is dominated by the gluon
channel at all x and gets only minor contribution from the
quark channel Dong, Ji, Kelsey, Radhakrishnan, Sichtermann, Zhao '23



TMD factorization of open heavy quark ($p_T \gg m_Q$) in DIS

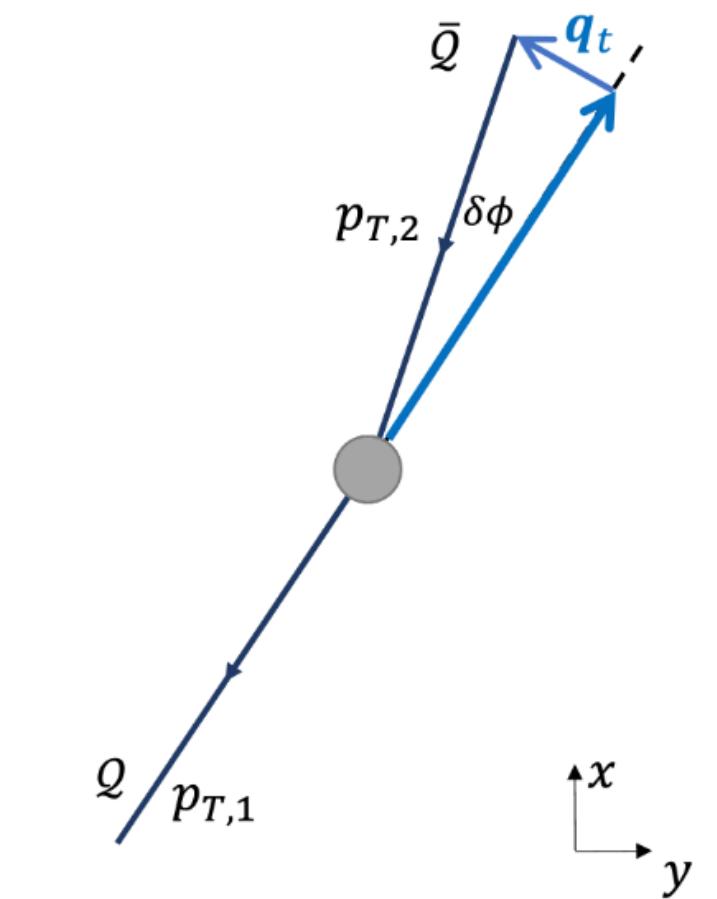
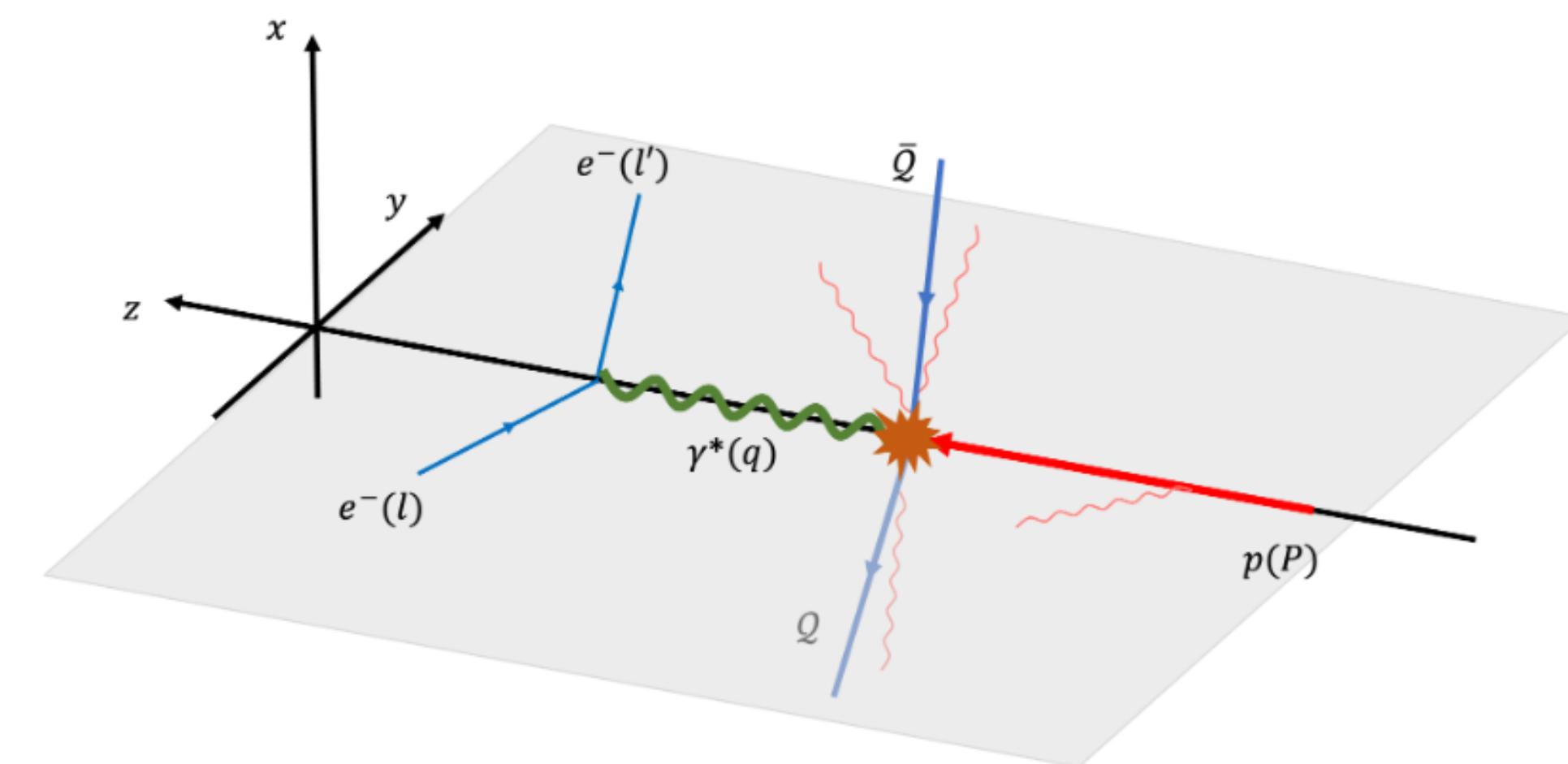
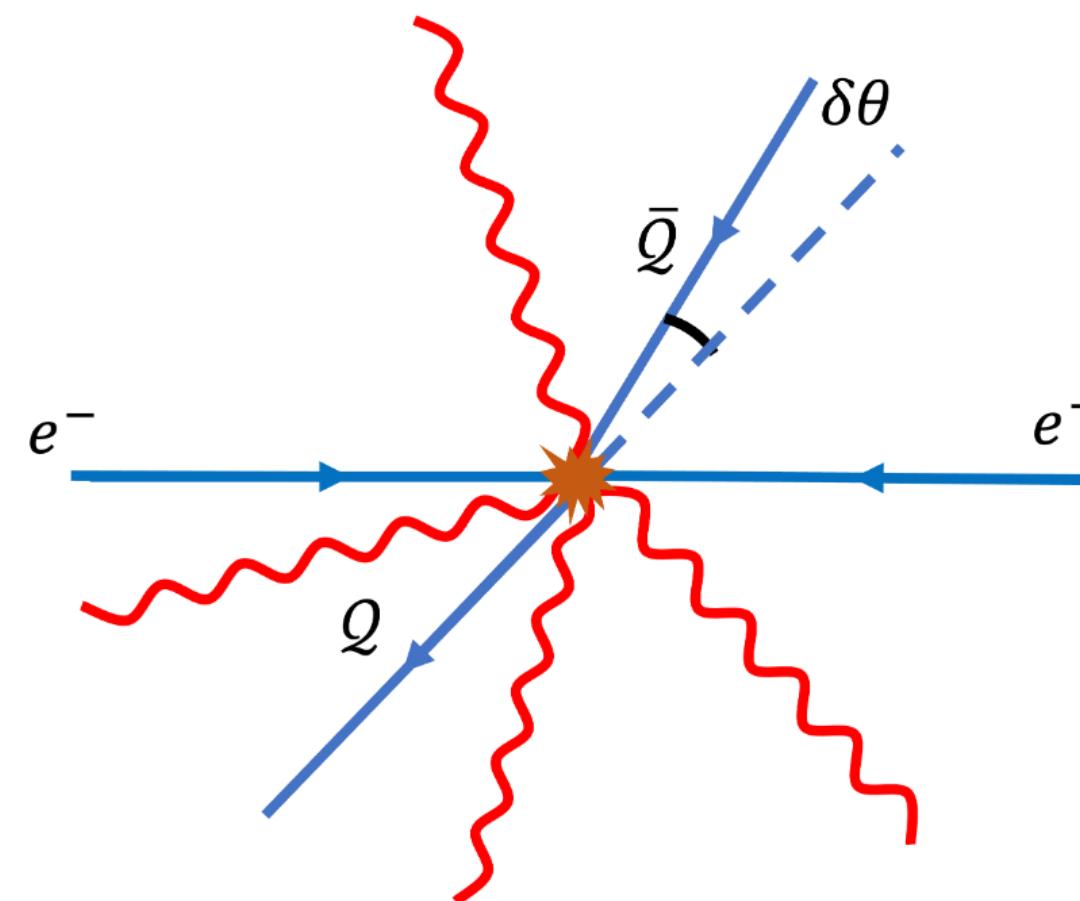
- **q_T factorization for heavy meson pair** (del Castillo, Echevarria, Makris, Scimemi '20 '22)
- **q_T factorization for heavy flavor dijet production, and study gluon Sivers asymmetry** (Kang, Reiten, DYS, Terry '20)
- **heavy quark q_T fragmentations** (Dai, Kim, Leibovich '23; Kuk, Michel, Sun '23 '24)
- **The anomalous dimensions of the q_T soft function are divergent as $\phi_x = \pi/2$**

$$\gamma^{S_{\text{global}}} \sim \frac{\alpha_s C_F}{\pi} \left[\ln(4 \cos^2 \phi_x) - i\pi \text{sign}(\cos \phi_x) \right]$$

- In addition to q_T, one can also study angle correlation to probe TMDs
 - A better angle on SIDIS (Gao, Michel, Stewart, Sun '22)
 - Lepton jet correction in DIS (Liu, Ringer, Vogelsang, Yuan '19, Arratia, Kang, Prokudin, Ringer '19, Fang, Ke, DYS, Terry '23)
- Discussions on azimuthal and radial correlation can be found in (Chien, Rahn, DYS, Waalewijn & Wu '22 + in progress)

Factorization and resummation of heavy quark pair angular correlations

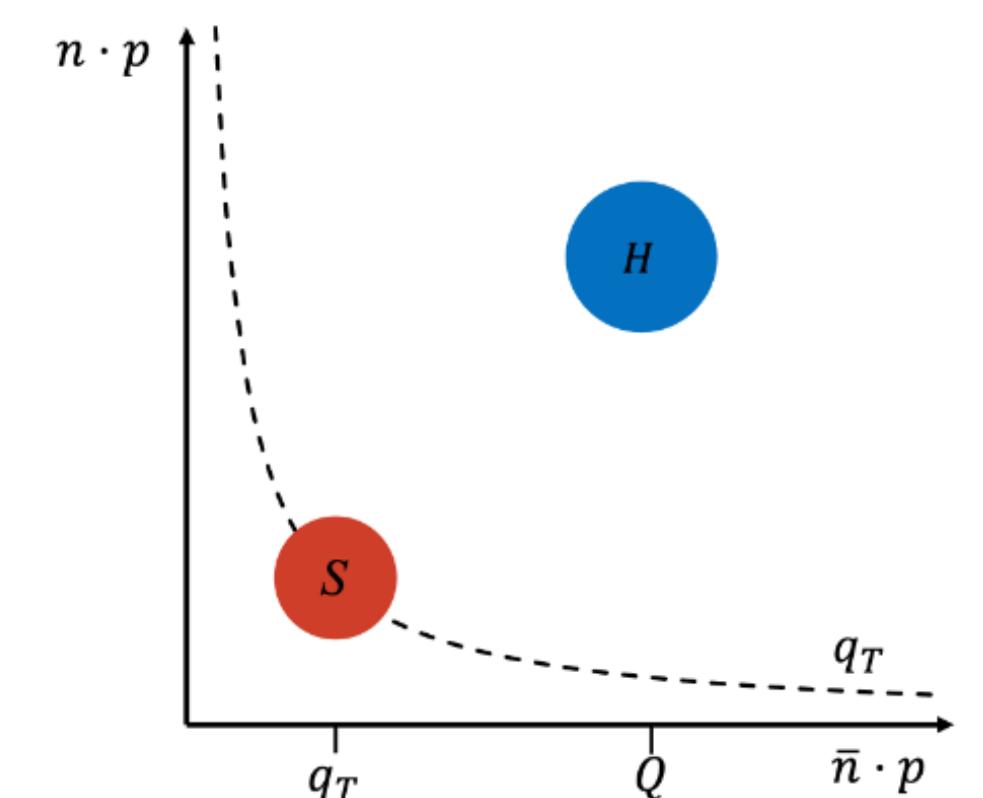
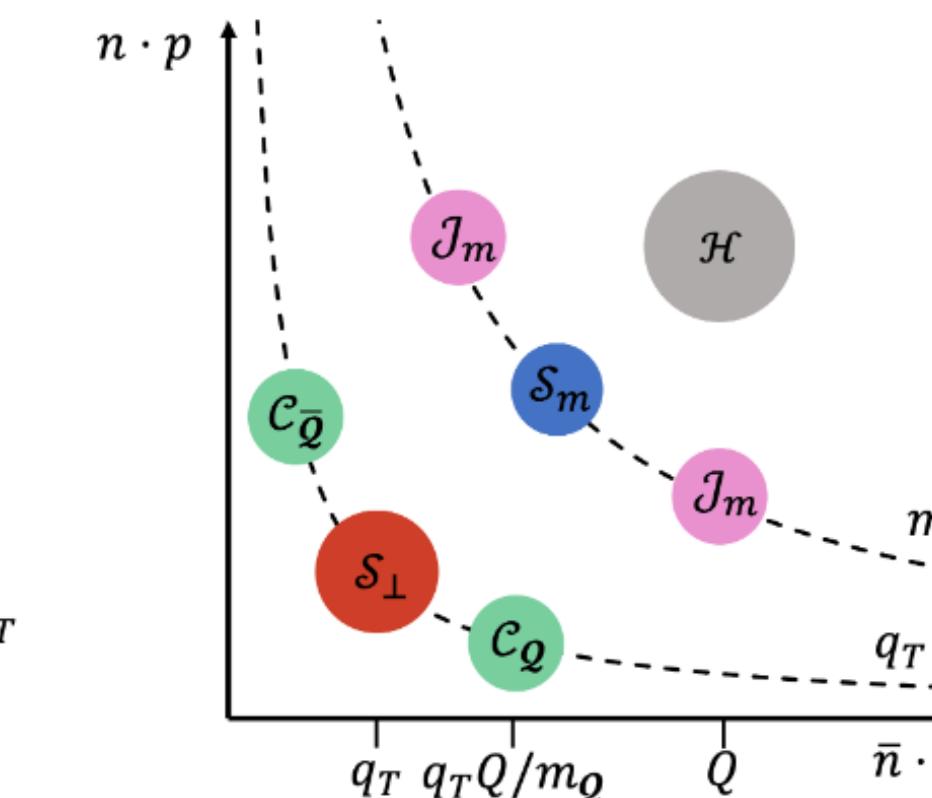
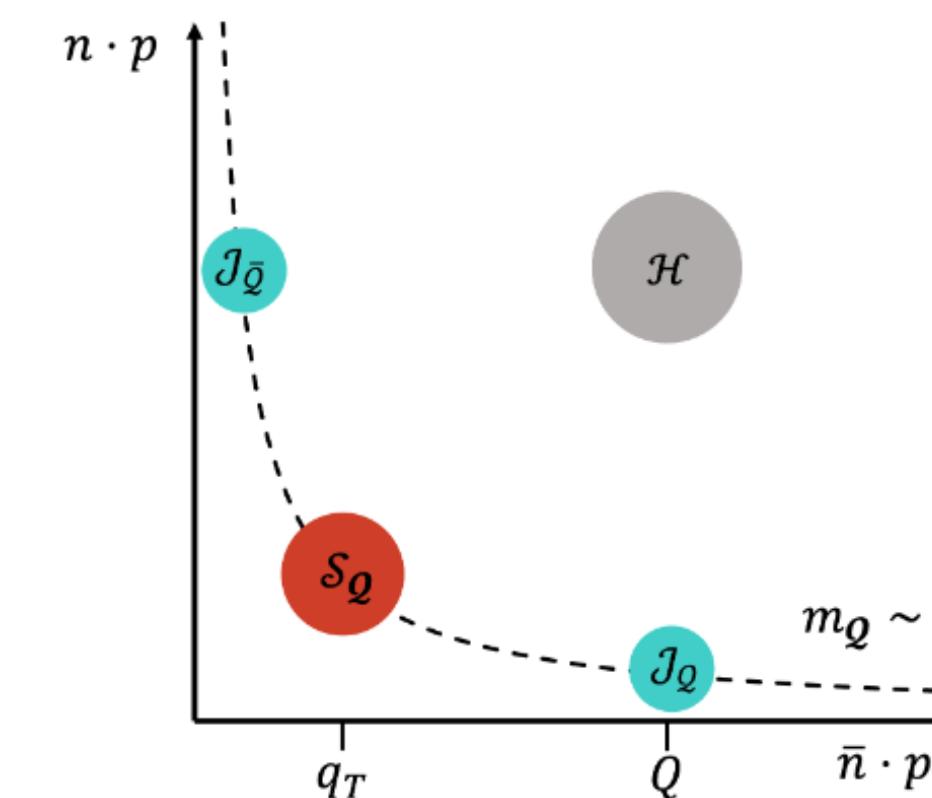
Dai, Jiang, DYS in progress



Region 1 : $Q \gg m_Q \sim q_T$,

Region 2 : $Q \gg m_Q \gg q_T$,

Region 3 : $Q \sim m_Q \gg q_T$.



Factorization in region 1 $Q \gg m_{\mathcal{Q}} \sim q_T$

Standard TMD factorization: two scales

$$\text{hard: } p_h^\mu \sim Q (1, 1, 1)$$

$$\text{collinear: } p_c^\mu \sim Q (1, \lambda^2, \lambda)$$

$$\text{soft: } p_s^\mu \sim q_T (1, 1, 1)$$

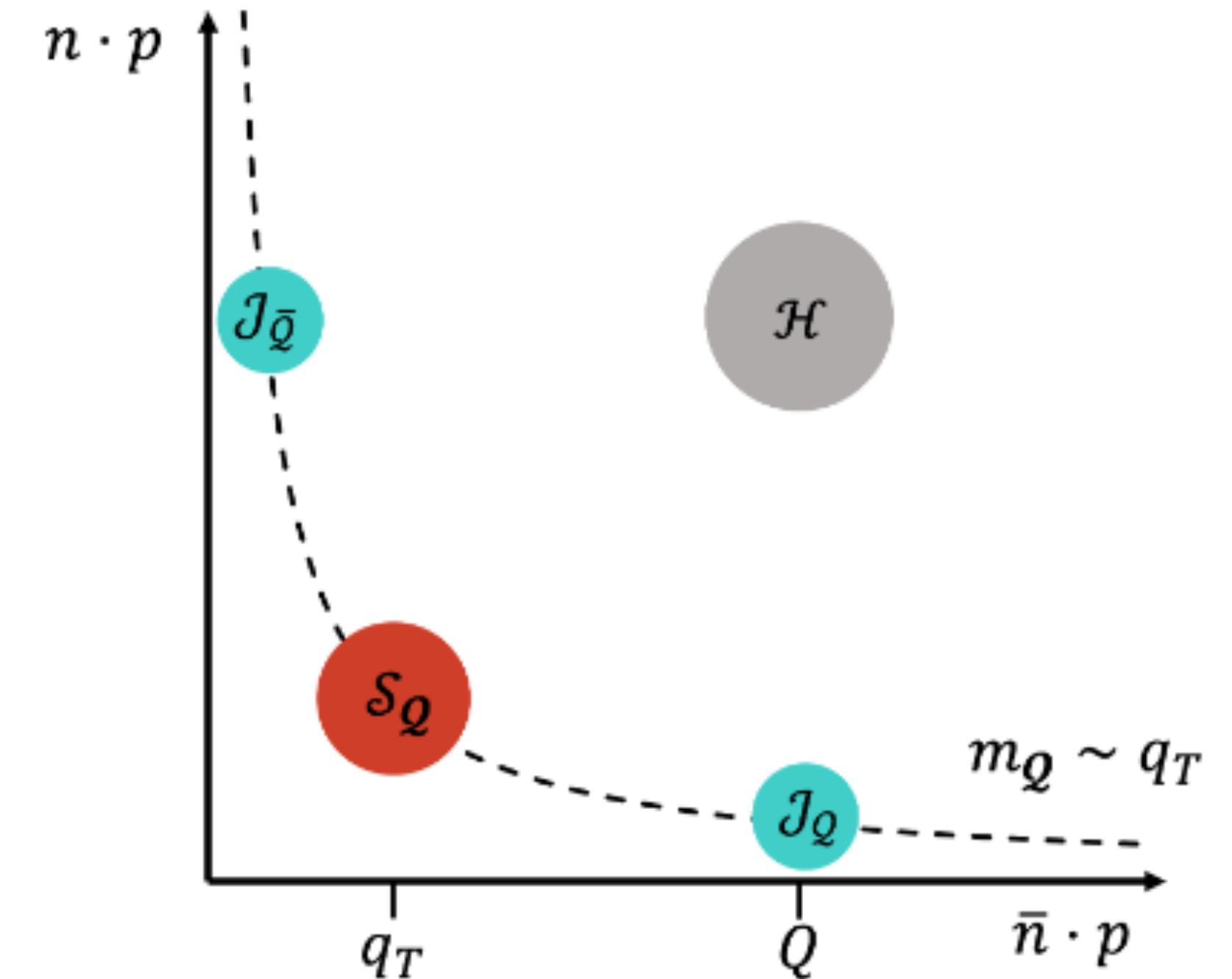
Match the quark current operator onto the SCET operator

$$\bar{\psi} \gamma^\mu \psi \rightarrow \mathcal{J}_{\text{SCET}} = \bar{\chi}_{\bar{n}} S_{\bar{n}}^\dagger \gamma_\perp^\mu S_n \chi_n$$

Factorization formula

$$\frac{d\sigma}{d^2 q_T} = \sigma_0 \mathcal{H}(Q, \mu) \int \frac{d^2 b_T}{(2\pi)^2} e^{i b_T \cdot q_T} \sum_f e_f^2 \mathcal{J}_{\mathcal{Q}/f}(b_T, m_{\mathcal{Q}}, \mu, \zeta/\nu^2) \mathcal{J}_{\overline{\mathcal{Q}}/\bar{f}}(b_T, m_{\mathcal{Q}}, \mu, \zeta/\nu^2) \mathcal{S}_{\mathcal{Q}}(b_T, m_{\mathcal{Q}}, \mu, \nu)$$

Jet and soft function depend on two scales: q_T and $m_{\mathcal{Q}}$



Factorization in region 1 $Q \gg m_Q \sim q_T$

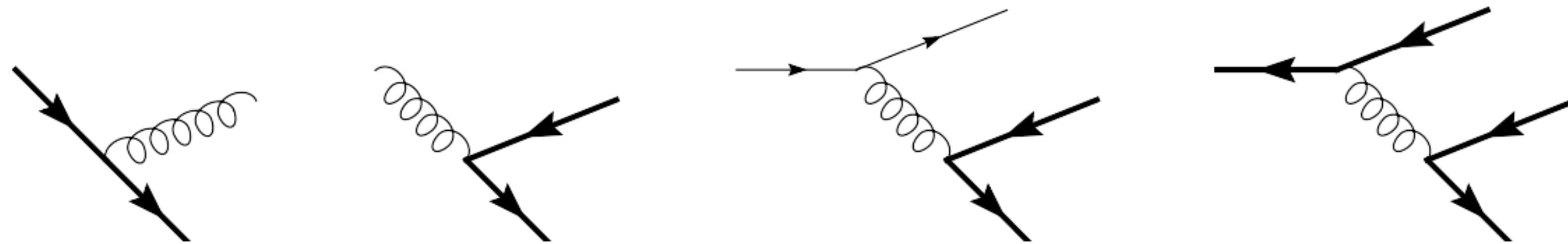
The Jet function can be expressed in terms of heavy quark TMD fragmentation function

Dai, Kim, Leibovich '23; Kuk, Michel, Sun '24

$$\mathcal{F}_{Q/f}(z_Q, P_{Q,\perp}) = \sum_X \frac{1}{z_Q} \int \frac{dx_+}{4\pi} \frac{d^{d-2}x_\perp}{(2\pi)^{d-2}} e^{ix_+ P_{Q,-}/(2z_Q)} \text{Tr} \langle 0 | \frac{\not{q}}{2} \chi_{\bar{n}}^f(x_+, 0, x_\perp) | Q(P_Q), X \rangle \langle Q(P_Q), X | \bar{\chi}_{\bar{n}}^f(0) | 0 \rangle$$

quark mass m_Q provides an infrared cutoff

Examples of fragmentation processes converting a parton a into a heavy quark

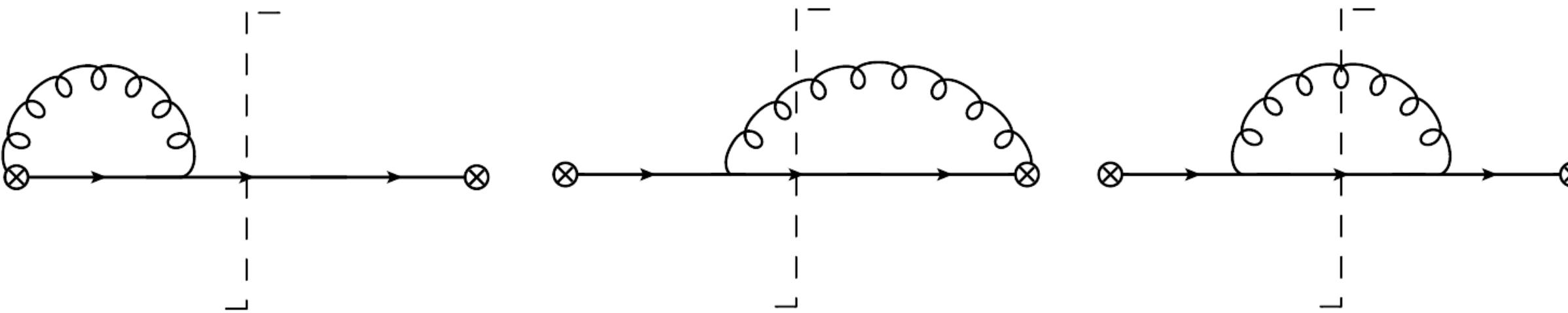


Define jet function (zero-moment of heavy quark fragmentation functions)

$$\mathcal{J}_{Q/f}(b_\perp, m_Q, \mu, \nu) = \int_0^1 dz_Q z_Q^{2-d} \int d^{d-2}P_{Q,\perp} e^{ib_\perp \cdot P_{Q,\perp}/z_Q} \mathcal{F}_{Q/f}(z_Q, P_{Q,\perp})$$

Factorization in region 1 $Q \gg m_Q \sim q_T$

NLO Jet function



$$\mathcal{J}_{Q/Q} = 1 + \frac{\alpha_s^{(n_f)} C_F}{4\pi} \left[\ln \frac{\mu^2 b_T^2}{b_0^2} \left(3 + 2 \ln \frac{\nu^2}{Q^2} \right) + 4 \ln^2 \left(\frac{b_T m_Q}{b_0} \right) - 2 \ln \left(\frac{b_T m_Q}{b_0} \right) + 4 + \frac{\pi^2}{3} + j_0(b_T m_Q) \right]$$

Auxiliary function (vanishes in the heavy quark limit $m_Q \gg q_T$)

$$j_0(x) = 2 \int_0^\infty dt e^{-xt} \left[\frac{2x^2 t^2 \arccos(t - i0^+)}{\sqrt{1 - t^2 + i0^+}} - \frac{3t\sqrt{1 - t^2 + i0^+}(t^2 - 2) + (8 - 9t^2 + 4t^4) \arccos(t - i0^+)}{(1 - t^2 + i0^+)^{5/2}} \right]$$

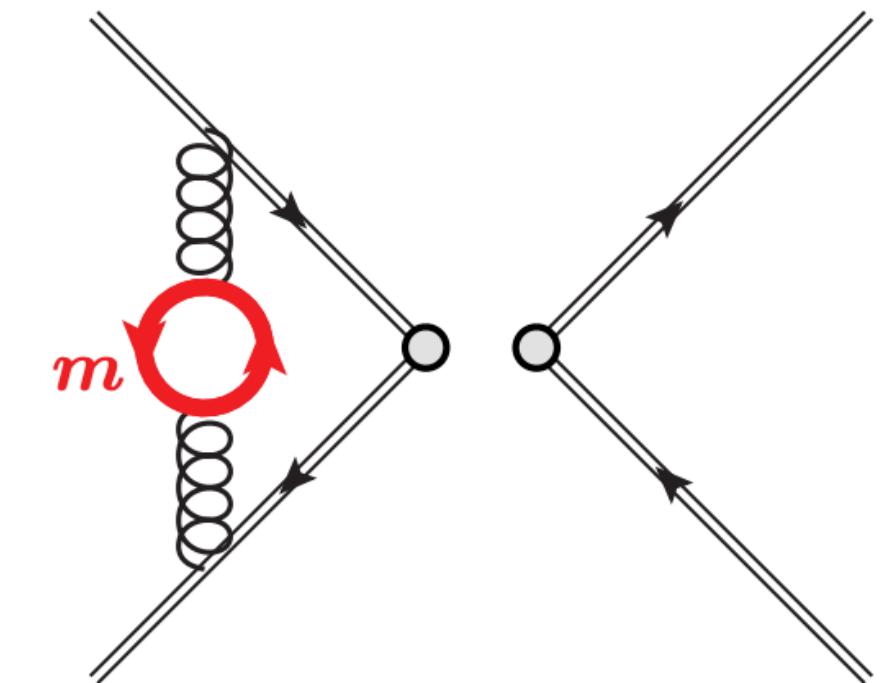
$$j_0(x) \xrightarrow{x \rightarrow \infty} 0.$$

Factorization in region 1 $Q \gg m_Q \sim q_T$

Soft function Pietrulewicz, Samitz, Spiering, Tackmann '17

$$\mathcal{S}_Q(b_\perp, m_Q) = \frac{1}{N_c} \text{Tr} \langle 0 | \bar{T}[S_n^\dagger(b_\perp) S_{\bar{n}}(b_\perp)] T[S_{\bar{n}}^\dagger(0) S_n(0)] | 0 \rangle$$

Different from the standard TMD soft function due to heavy-quark corrections



Two-loop anomalous dimensions (heavy quark corrections)

$$\begin{aligned} \gamma_\nu^{\mathcal{S}_Q(2,h)}(b_T, m_Q, \mu) = & C_F \left\{ -\frac{32}{3} L_b L_m - \frac{16}{3} L_m^2 - \frac{160}{9} L_m - \frac{448}{27} \right. \\ & \left. + \frac{8\sqrt{\pi}}{3} \left[2G_{1,3}^{3,0} \left(\begin{array}{c|c} \frac{3}{2} \\ 0, 0, 0 \end{array} \middle| m_Q^2 b_T^2 \right) + G_{1,3}^{3,0} \left(\begin{array}{c|c} \frac{5}{2} \\ 0, 0, 1 \end{array} \middle| m_Q^2 b_T^2 \right) \right] \right\} \end{aligned}$$

RG and RRG consistency relation

$$\gamma_\mu^{\mathcal{H}} + \gamma_\mu^{\mathcal{S}_Q} + 2\gamma_\mu^{\mathcal{J}_Q} = 0 \quad \gamma_\nu^{\mathcal{S}_Q} + 2\gamma_\nu^{\mathcal{J}_Q} = 0$$

NNLL resummation ingredients are known

Resummation in region 1 $Q \gg m_Q \sim q_T$

We apply Collins-Soper-Sterman treatment to resum rapidity logs

$$J_{Q/f}(b_T, m_Q, \mu, \zeta) \equiv \mathcal{J}_{Q/f}(b_T, m_Q, \mu, \zeta/\nu^2) \sqrt{\mathcal{S}_Q(b_T, m_Q, \mu, \nu)}$$

Evolve the jet function from the pair of initial and final scales $\{\mu_b, \zeta_i\} \rightarrow \{\mu, \zeta_f\}$

$$J_{Q/f}(b_T, m_Q, \mu, \zeta_f) = \exp \left[\int_{\mu_b}^{\mu} \frac{d\bar{\mu}}{\bar{\mu}} \gamma_{\mu}^{J_Q}(\bar{\mu}, \zeta_f) \right] \left(\frac{\zeta_f}{\zeta_i} \right)^{\frac{1}{2} \gamma_{\zeta}^{J_Q}(\mu_b, b_T)} J_{Q/f}(b_T, m_Q, \mu_b, \zeta_i)$$

We have the resummation formula

$$\frac{d\sigma}{d\delta\theta} = \frac{\sigma_0 Q^2 \delta\theta}{4} \mathcal{H}(Q, \mu_h) \int_0^\infty b_T db_T J_0(Q\delta\theta b_T/2) \sum_f e_f^2 J_{Q/f}(b_T, m_Q, \mu_h, \zeta_f) J_{\bar{Q}/\bar{f}}(b_T, m_Q, \mu_h, \zeta_f)$$

The scale choice $\mu_h = \sqrt{\zeta_f} = Q$ $\mu_b = \sqrt{\zeta_i} = \frac{b_0}{b_T}$

Factorization in region 2

$Q \gg m_Q \gg q_T$

- In the limit $m_Q \gg q_T$, jet function in region 1 contains $\alpha_s^n \log^m(m_Q/q_T)$
 - The factorization formula in region 1 with active flavors $n_f = n_l + 1$ should be matched onto a theory with n_l active flavors
- E.g. matching relation of α_s from region 1 to 2

$$\alpha_s^{(n_f)}(\mu) = \alpha_s^{(n_l)}(\mu) \left[1 + \frac{4}{3} T_F \frac{\alpha_s^{(n_l)}(\mu)}{4\pi} \ln \frac{\mu^2}{m_Q^2} + \mathcal{O}(\alpha_s^2) \right]$$

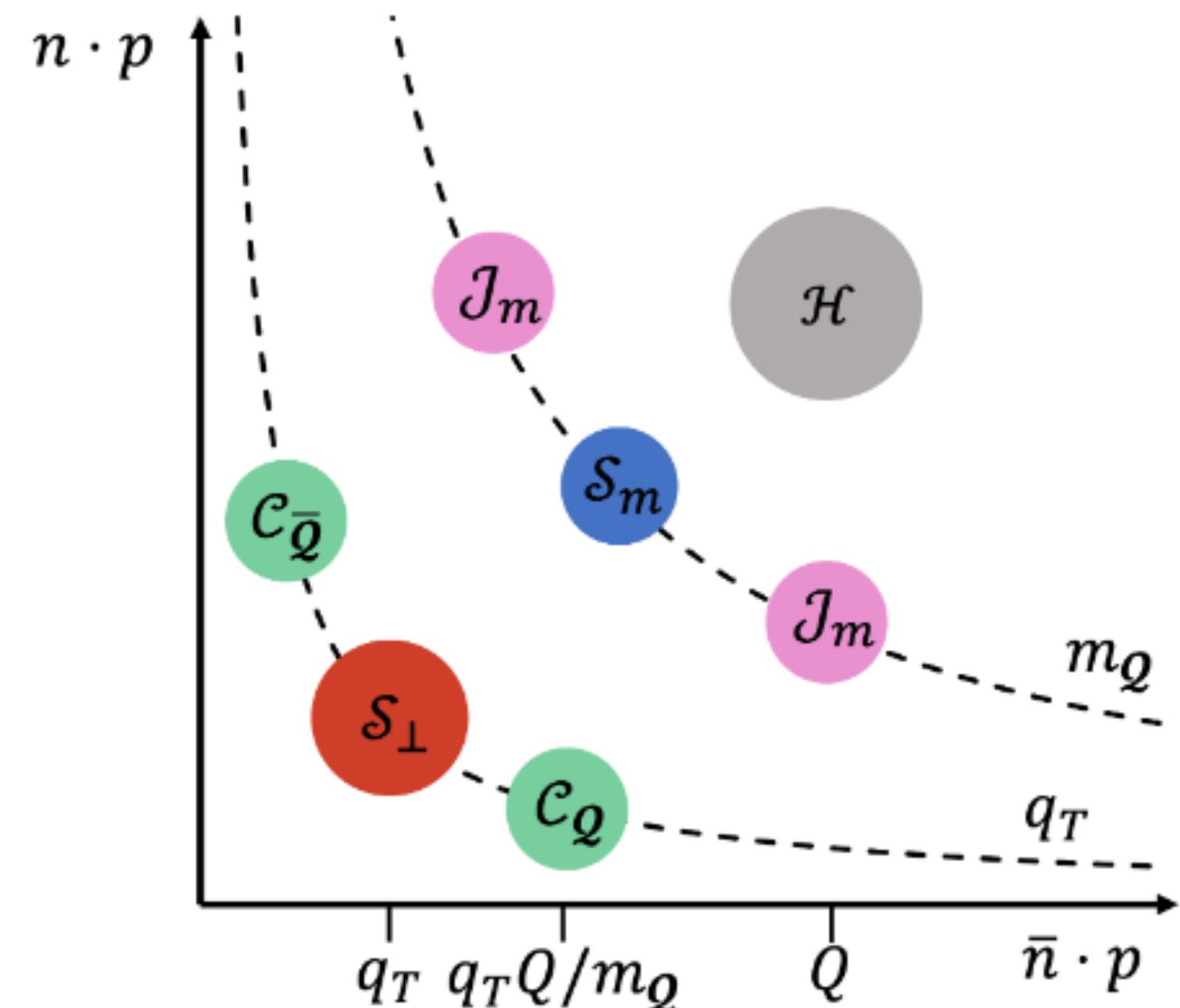
- Heavy quark momenta $P_Q^\mu = m_Q v_+^\mu + p^\mu$

$$v_+^\mu = \left(\frac{Q}{m_Q}, \frac{m_Q}{Q}, 0_\perp \right), \quad p_{uc}^\mu \sim q_T \left(\frac{Q}{m_Q}, \frac{m_Q}{Q}, 1 \right)$$

- Decouple the interaction between heavy quark and ultra-collinear modes; match SCET onto bHQET Fleming, Hoang, Mantry & Stewart '07

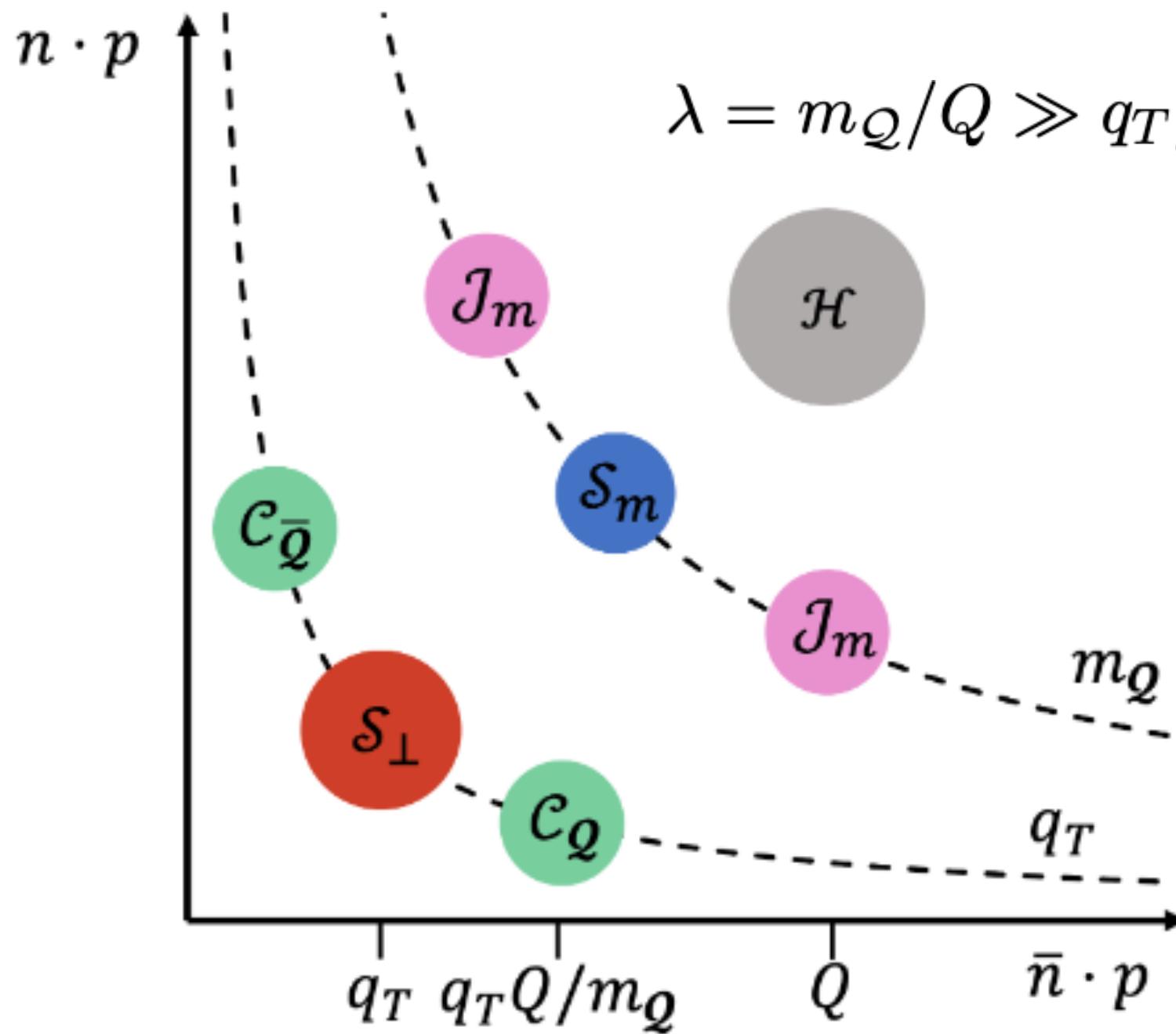
$$h_{v_\pm} \rightarrow Y_{v_\pm} h_{v_\pm}$$

$$\mathcal{J}_{\text{SCET}} \rightarrow \mathcal{J}_{\text{bHQET}} = \bar{h}_{v_-} W_{\bar{n}}^\dagger Y_{v_-}^\dagger \gamma_\perp^\mu Y_{v_+} W_n h_{v_+}$$



Factorization in region 2

$$Q \gg m_Q \gg q_T$$



- hard: $p_h^\mu \sim Q(1, 1, 1)$
- collinear: $p_c^\mu \sim Q(1, \lambda^2, \lambda)$
- massive-soft: $p_{ms}^\mu \sim Q(\lambda, \lambda, \lambda)$
- soft: $p_s^\mu \sim q_T(1, 1, 1)$
- ultra-collinear: $p_{uc}^\mu \sim q_T/\lambda(1, \lambda^2, \lambda)$

Factorization formula

Matching coefficients form SCET to bHQET

$$\frac{d\sigma}{d^2\mathbf{q}_T} = \sigma_Q \mathcal{H}(Q, \mu) \boxed{\mathcal{J}_m^2(m_Q, \mu, \zeta_J/\nu^2) \mathcal{S}_m(m_Q, \mu, \nu)}$$

Hoang, Pathak, Pietrulewicz
& Stewart, '15

$$\times \int \frac{d^2\mathbf{b}_T}{(2\pi)^2} e^{i\mathbf{b}_T \cdot \mathbf{q}_T} \boxed{\mathcal{C}_Q(b_T, \mu, \zeta_C/\nu^2) \mathcal{C}_{\bar{Q}}(b_T, \mu, \zeta_{\bar{C}}/\nu^2)} \boxed{\mathcal{S}_{\perp}(b_T, \mu, \nu)}$$

Standard TMD soft function

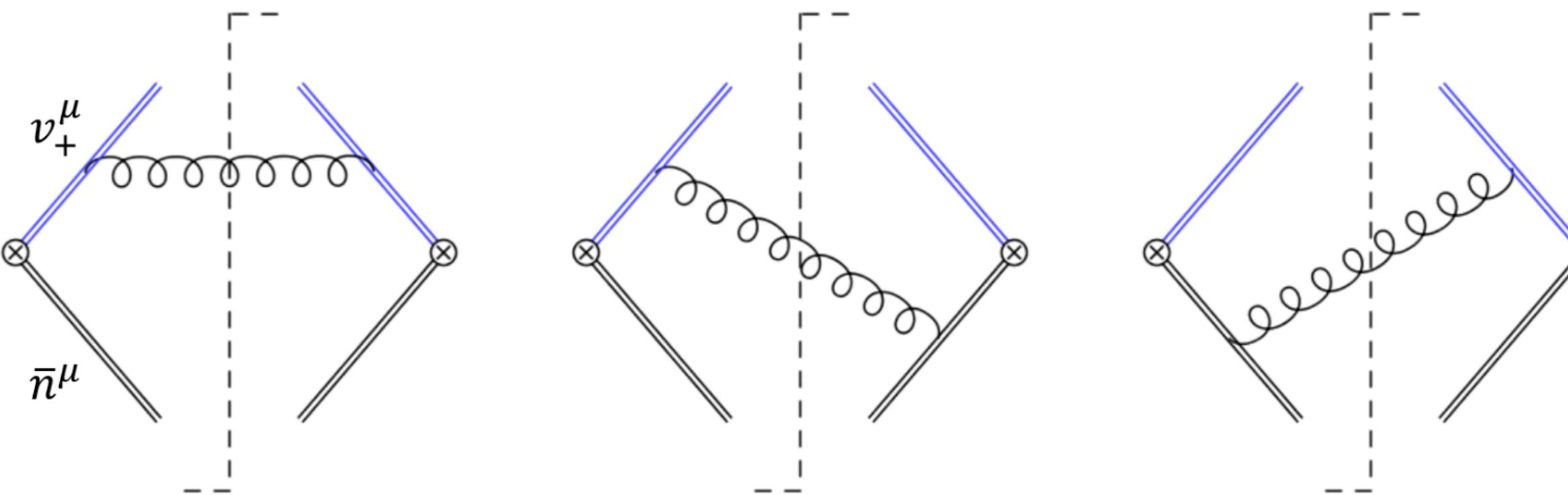
Factorization in region 2 $Q \gg m_Q \gg q_T$

Definition of ultra-collinear function

$$\mathcal{C}_Q(b_T, \mu, \zeta_C/\nu^2) = \frac{1}{N_c} \text{Tr} \langle 0 | \bar{T}[W_n^\dagger(b_\perp) Y_{v_+}(b_\perp)] T[Y_{v_+}^\dagger(0) W_n(0)] | 0 \rangle$$

$$v_+^\mu = \frac{Q}{m_Q} \frac{n^\mu}{2} + \frac{m_Q}{Q} \frac{\bar{n}^\mu}{2}$$

One-loop results



$$\mathcal{C}_Q^{\text{bare}} = 1 + \frac{\alpha_s^{(n_l)} C_F}{4\pi} \left[\left(\frac{2}{\eta} + \ln \frac{\nu^2 m_Q^2}{Q^2 \mu^2} \right) \left(\frac{2}{\epsilon} + 2L_b \right) - \frac{2}{\epsilon^2} + \frac{2}{\epsilon} + L_b^2 + 2L_b + \frac{\pi^2}{6} \right]$$

Anomalous dimensions (n_l flavor)

$$\gamma_\mu^{\mathcal{C}_Q} = -C_F \gamma^{\text{cusp},(n_l)} \ln \frac{\mu^2 Q^2}{\nu^2 m_Q^2} + \gamma^{\mathcal{C},(n_l)} \quad \gamma_0^{\mathcal{C}} = 4C_F$$

Refactorization of jet function in region 1

$$\mathcal{J}_{Q/Q}(b_T, m_Q) \xrightarrow{m_Q \gg q_T} \mathcal{J}_m(m_Q) \mathcal{C}_Q(b_T)$$

Factorization in region 2 $Q \gg m_{\mathcal{Q}} \gg q_T$

RG consistency relation

$$\begin{aligned}\gamma_\mu^H + 2\gamma_\mu^{\mathcal{J}_m} + \gamma_\mu^{S_m} + \gamma_\mu^S + 2\gamma_\mu^{\mathcal{C}_{\mathcal{Q}}} &= 0, \\ \gamma_\nu^{S_m} + 2\gamma_\nu^{\mathcal{J}_m} &= 0, \quad \gamma_\nu^S + 2\gamma_\nu^{\mathcal{C}_{\mathcal{Q}}} = 0\end{aligned}$$

$$\gamma_\mu^{\mathcal{H}} = 2C_F \gamma^{\text{cusp},(n_f)} \ln \frac{Q^2}{\mu^2} + 4\gamma^{q,(n_f)}$$

$$\gamma_\mu^{\mathcal{C}_{\mathcal{Q}}} = -C_F \gamma^{\text{cusp},(n_l)} \ln \frac{\mu^2 Q^2}{\nu^2 m_{\mathcal{Q}}^2} + \gamma^{\mathcal{C},(n_l)}$$

$$\gamma_\mu^S = -2C_F \gamma^{\text{cusp},(n_l)} \ln \frac{\nu^2}{\mu^2} + \gamma^{S,(n_l)}$$

hard: $p_h^\mu \sim Q(1, 1, 1)$

collinear: $p_c^\mu \sim Q(1, \lambda^2, \lambda)$

massive-soft: $p_{ms}^\mu \sim Q(\lambda, \lambda, \lambda)$

soft: $p_s^\mu \sim q_T(1, 1, 1)$

ultra-collinear: $p_{uc}^\mu \sim q_T/\lambda(1, \lambda^2, \lambda)$

$$\gamma_\mu^{\mathcal{J}_m} = -C_F \gamma^{\text{cusp},(n_l)} \ln \frac{m_{\mathcal{Q}}^2}{\mu^2} + \gamma^{J_m,(n_l)} + \mathcal{O}(\alpha_s^2)$$

$$\gamma_\mu^{S_m} = \mathcal{O}(\alpha_s^2) \quad \text{Hoang, Pathak, Pietrulewicz \& Stewart, '15}$$

Two-loop anomalous dimension of the ultra-collinear function

$$\gamma_1^{\mathcal{C}} = C_A C_F \left(22\zeta_3 - \frac{184}{27} - \frac{13\pi^2}{18} \right) - C_F T_F n_f \left(\frac{128}{27} + \frac{2\pi^2}{9} \right)$$

NNLL resummation ingredients are known

Resummation in region 2 $Q \gg m_Q \gg q_T$

Evolve the jet and ultra-collinear function

$$J_m(m_Q, \mu, \zeta_{J,f}) = \exp \left[\int_{\mu_m}^{\mu} \frac{d\bar{\mu}}{\bar{\mu}} \gamma_{\mu}^{J_m}(\bar{\mu}, \zeta_{J,f}) \right] \left(\frac{\zeta_{J,f}}{\zeta_{J,i}} \right)^{\frac{1}{2} \gamma_{\zeta}^{J_m}(m_Q, \mu_j)} J_m(m_Q, \mu_m, \zeta_{J,i})$$

$$C_Q(b, \mu, \zeta_{C,f}) = \exp \left[\int_{\mu_b}^{\mu} \frac{d\bar{\mu}}{\bar{\mu}} \gamma_{\mu}^{C_Q}(\bar{\mu}, \zeta_{C,f}) \right] \left(\frac{\zeta_{C,f}}{\zeta_{C,i}} \right)^{\frac{1}{2} \gamma_{\zeta}^{C_Q}(b, \mu_b)} C_Q(b, \mu_b, \zeta_{C,i}).$$

We have the resummation formula

$$\frac{d\sigma}{d\delta\theta} = \frac{\sigma_Q Q^2 \delta\theta}{4} \mathcal{H}(Q, \mu_h) J_m^2(m_Q, \mu_h, \zeta_{J,f}) \int_0^\infty b db J_0(Q\delta\theta b/2) C_Q^2(b, \mu_h, \zeta_{S,f})$$

The scale choice

$$\mu_h = Q, \quad \mu_m = m_Q, \quad \mu_b = b_0/b_T,$$

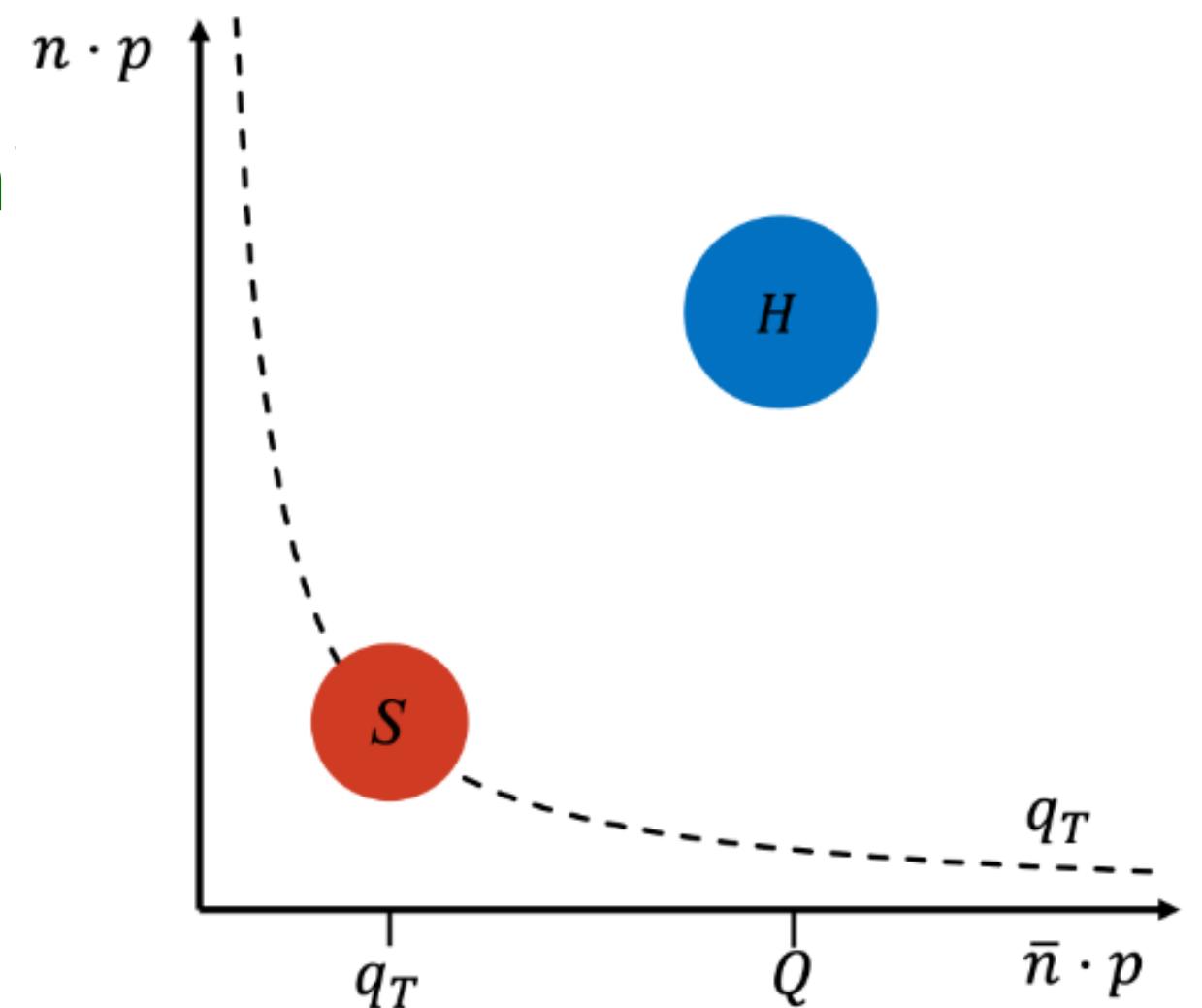
$$\zeta_{J,f} = Q^2, \quad \zeta_{J,i} = m_Q^2, \quad \zeta_{C,f} = \frac{Q^2 \mu_b^2}{m_Q^2}, \quad \zeta_{C,i} = \mu_b^2$$

Factorization in region 3 $Q \sim m_Q \gg q_T$

- In region 3, TMD factorization of heavy quark pair production are well studied
 - Factorization and resummation (Li, Li, DYS, Yang, Zhu '12 '13 & Catani, Grazzini, Torre '14 & Catani, Grazzini & Sargsyan '18; Ju, Schönher '22)
 - Two-loop soft function Angeles-Martinez, M. Czakon, and S. Sapeta'18; Catani Mazzitelli '23

- Factorization formula

$$\frac{d\sigma}{d^2\mathbf{q}_T} = \sigma_Q H(Q, m_Q, \mu) \int \frac{d^2\mathbf{b}_T}{(2\pi)^2} e^{i\mathbf{b}_T \cdot \mathbf{q}_T} S(\mathbf{b}_T, \beta_Q, \mu)$$



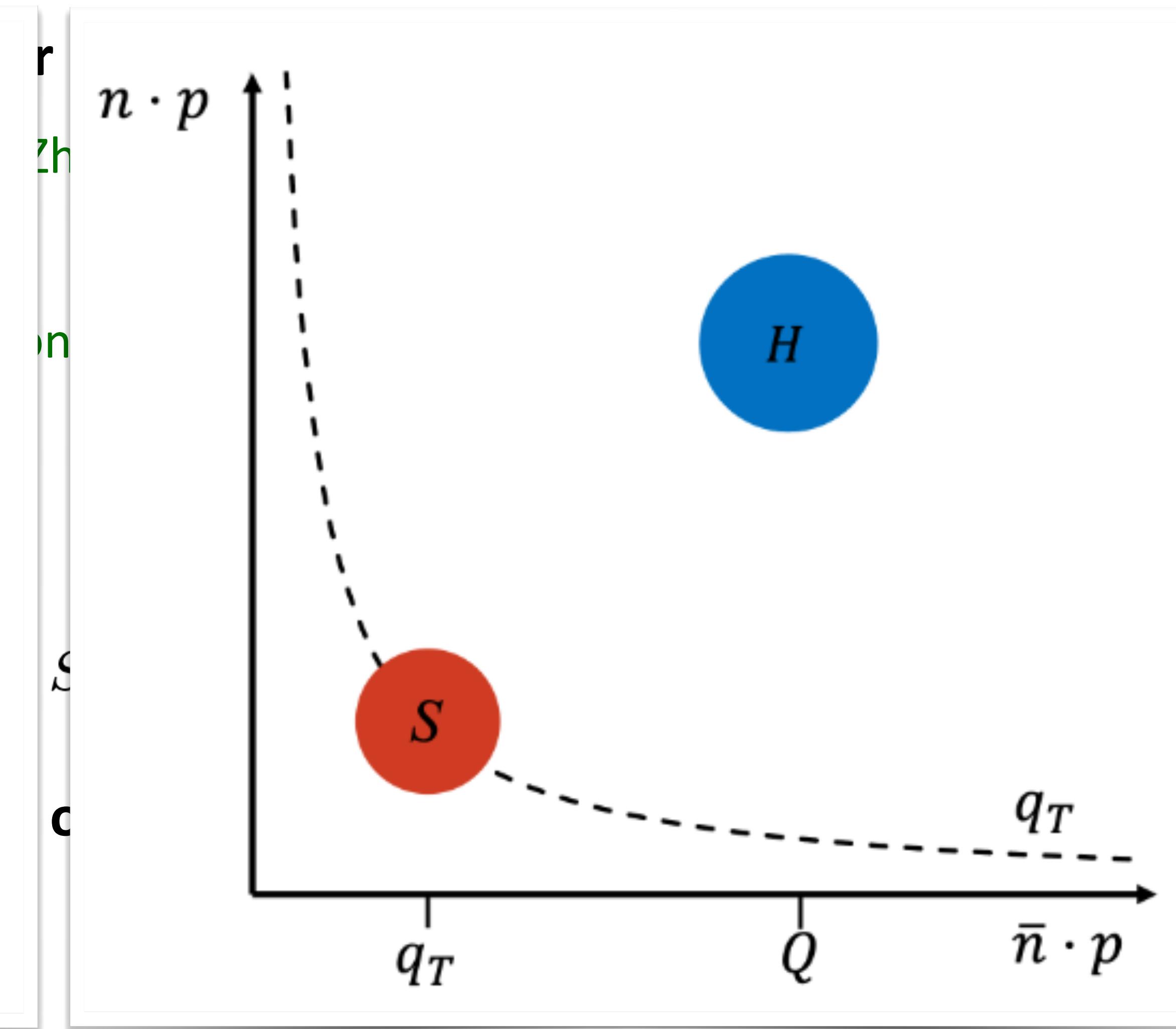
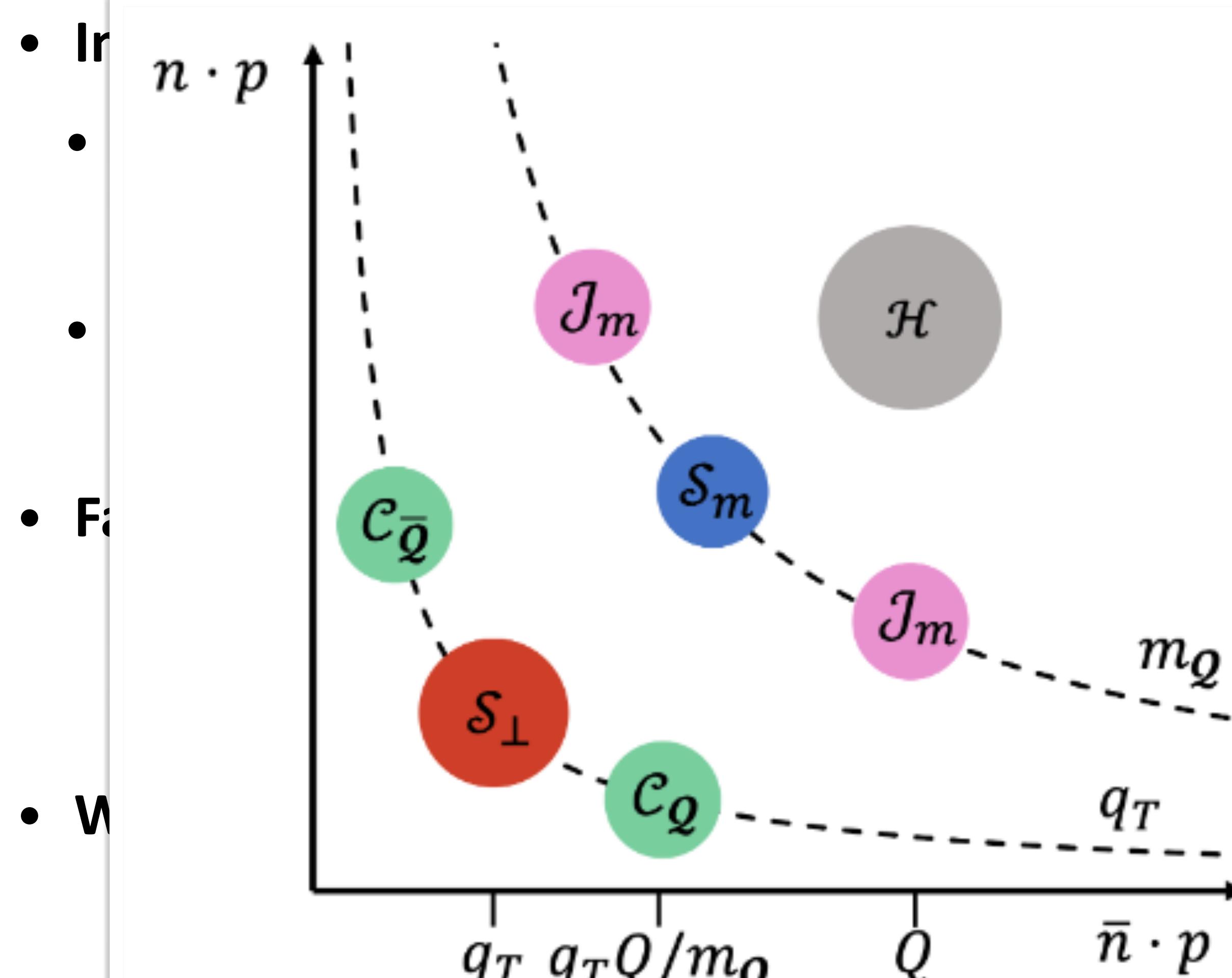
- We use their expressions to verify refactorization of soft function at two loop

$$\gamma_\mu^S \xrightarrow{Q \gg m_Q} 2\gamma_\mu^{\mathcal{C}_Q} + \gamma_\mu^S$$

- Two loop ultra-collinear function can be determined based on $S \xrightarrow{Q \gg m_Q} \mathcal{C}_Q^2 \mathcal{S}_\perp$

Factorization in region 3

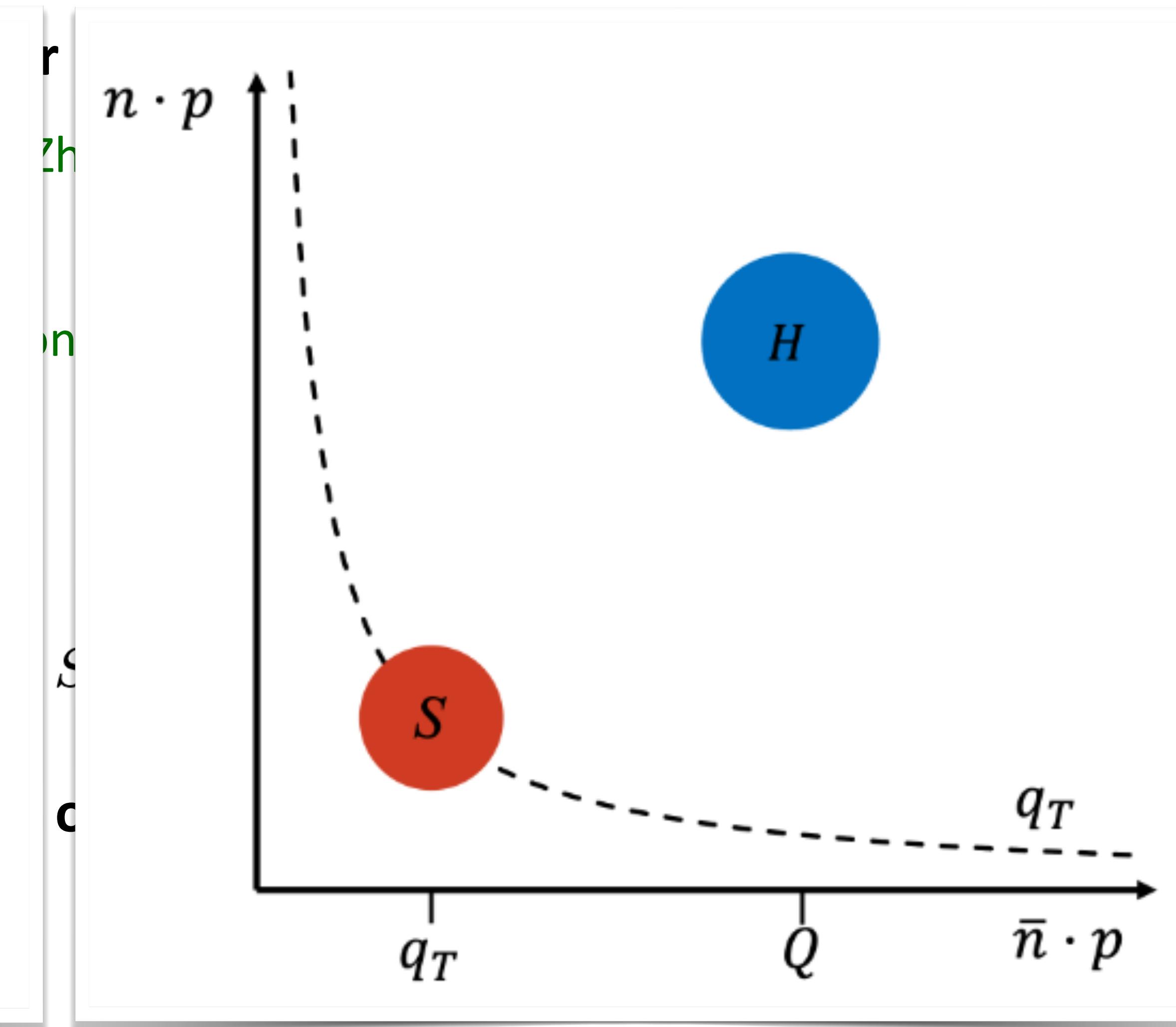
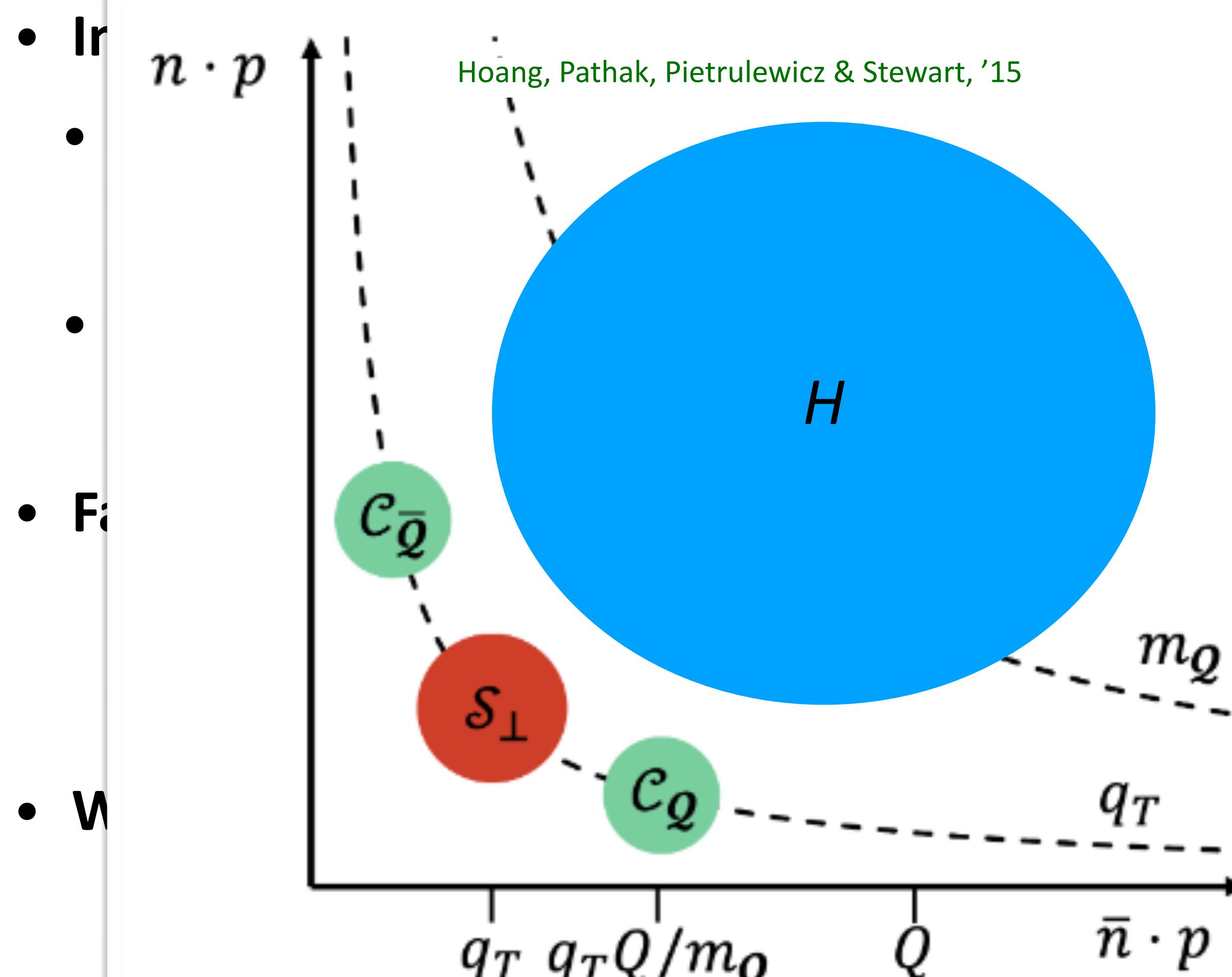
$$Q \sim m_Q \gg q_T$$



- Two loop ultra-collinear function can be determined based on $S \xrightarrow{Q \gg m_Q} C_Q^2 S_{\perp}$

Factorization in region 3

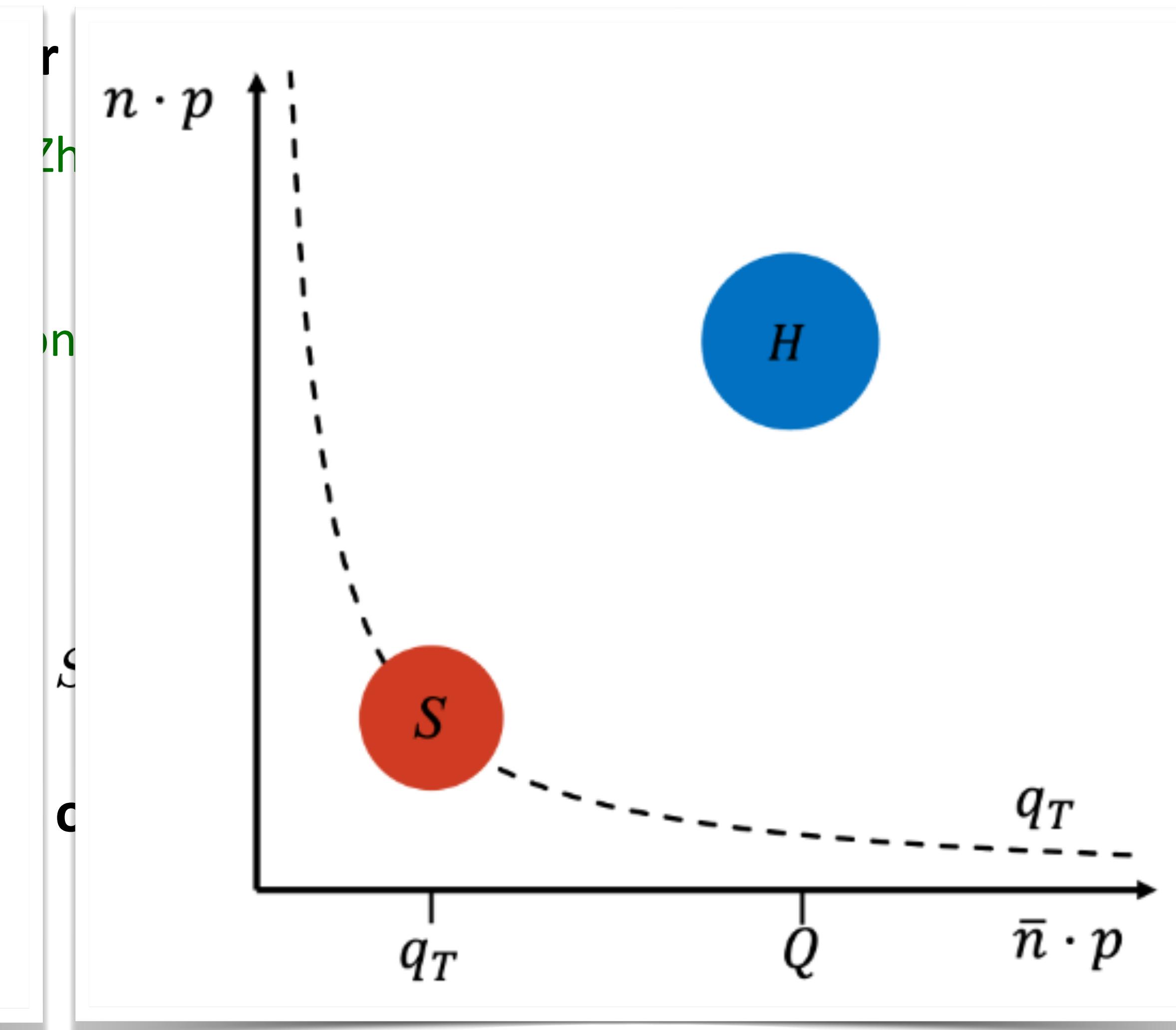
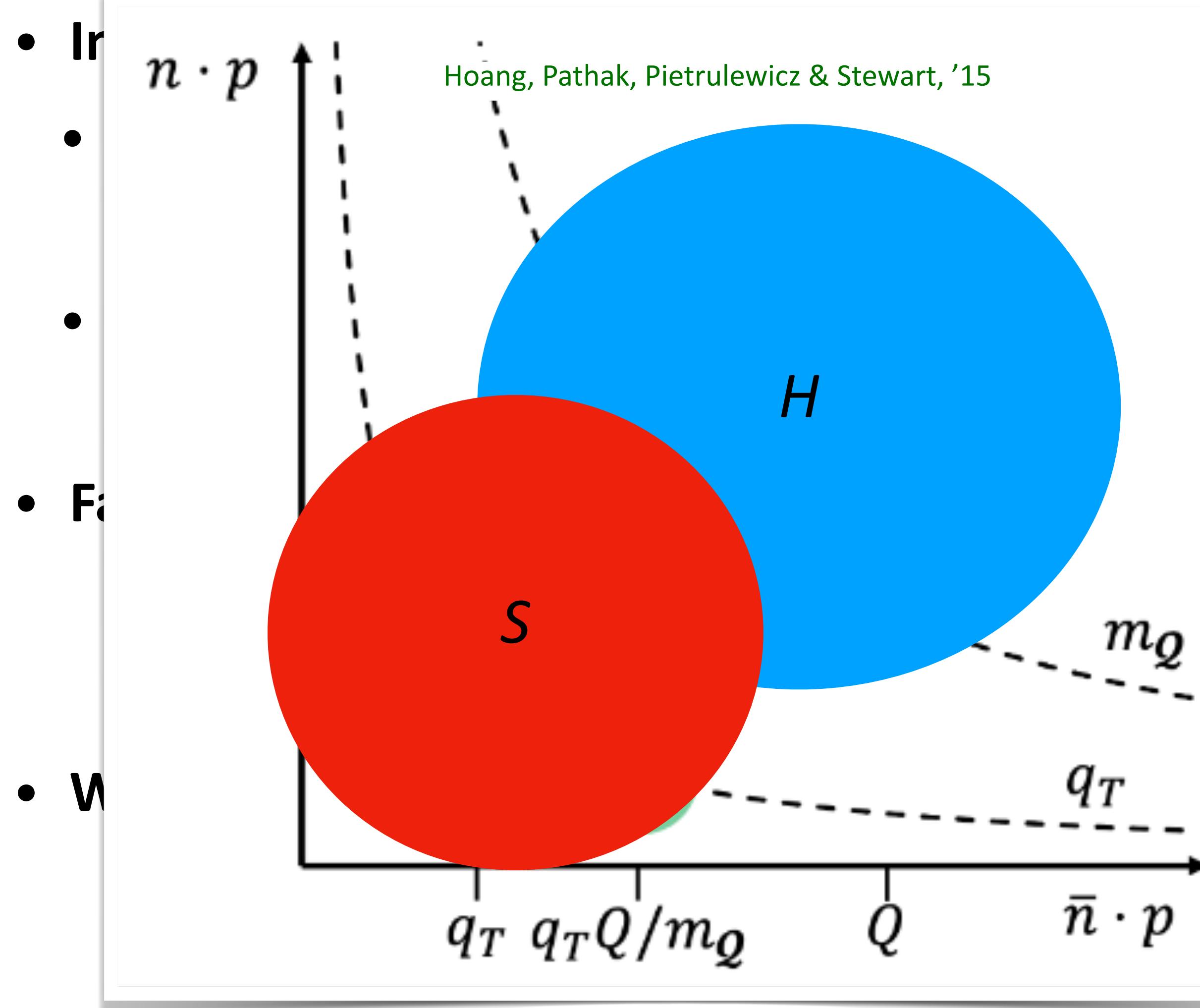
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Factorization in region 3

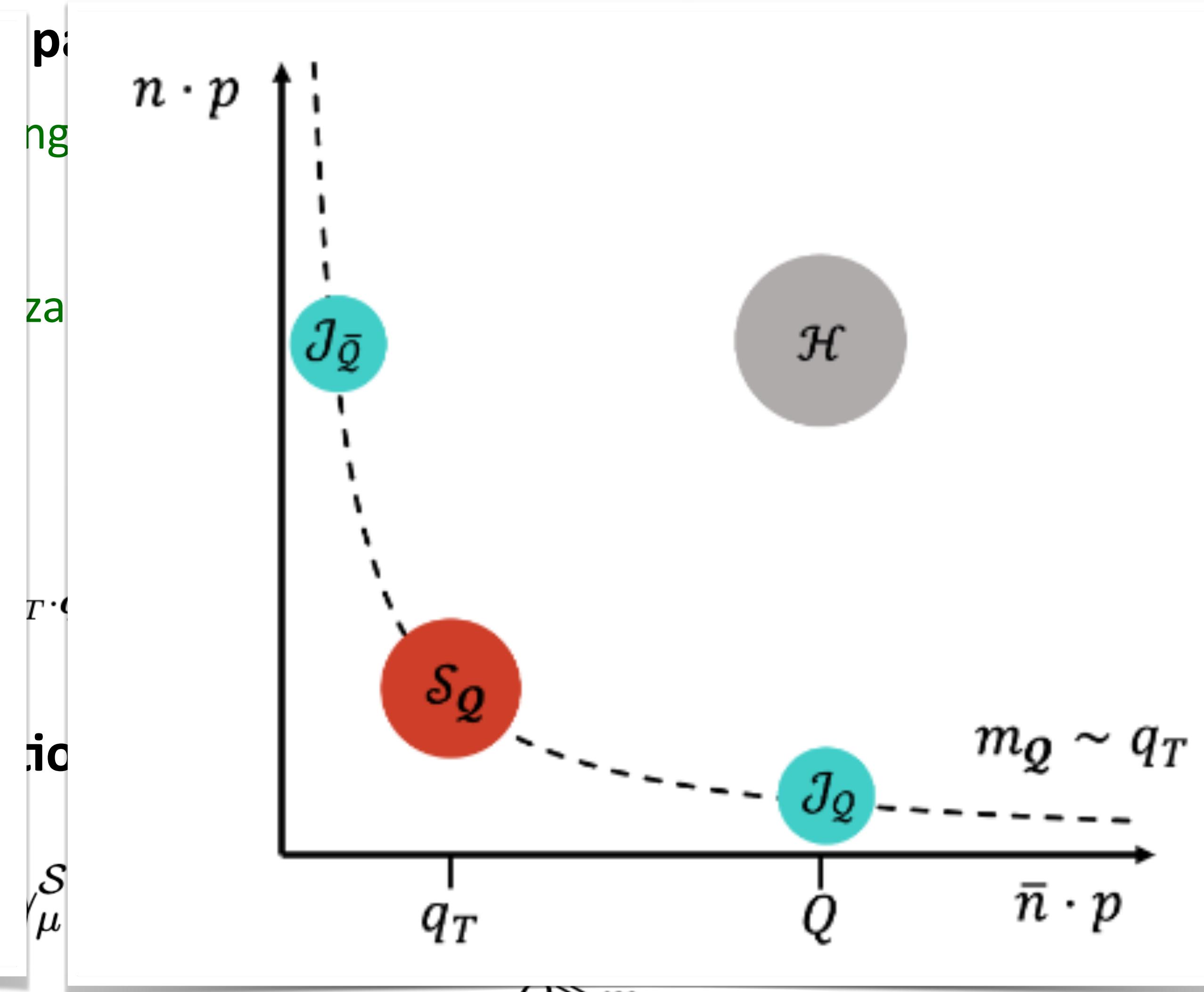
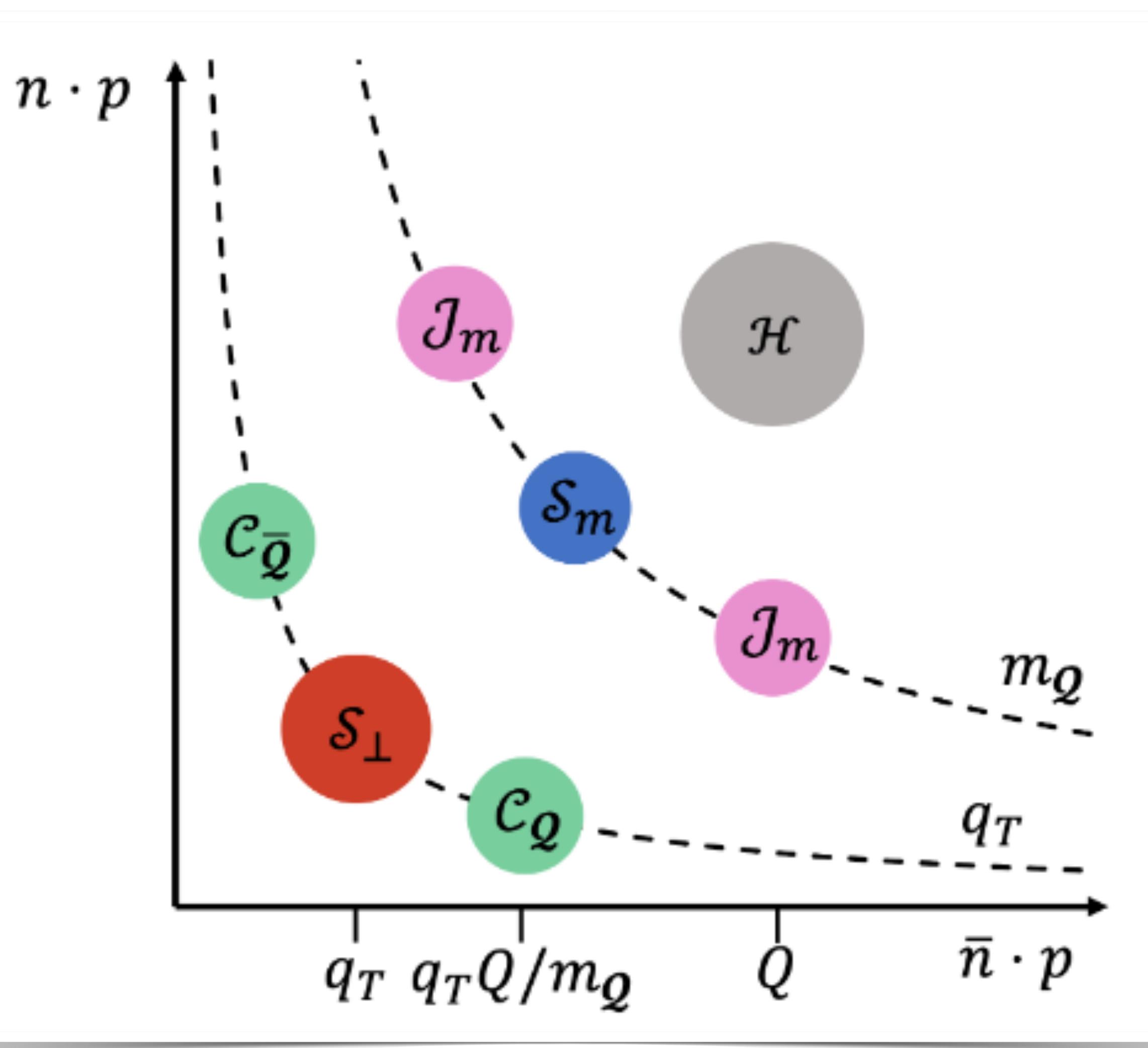
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Factorization in region 3

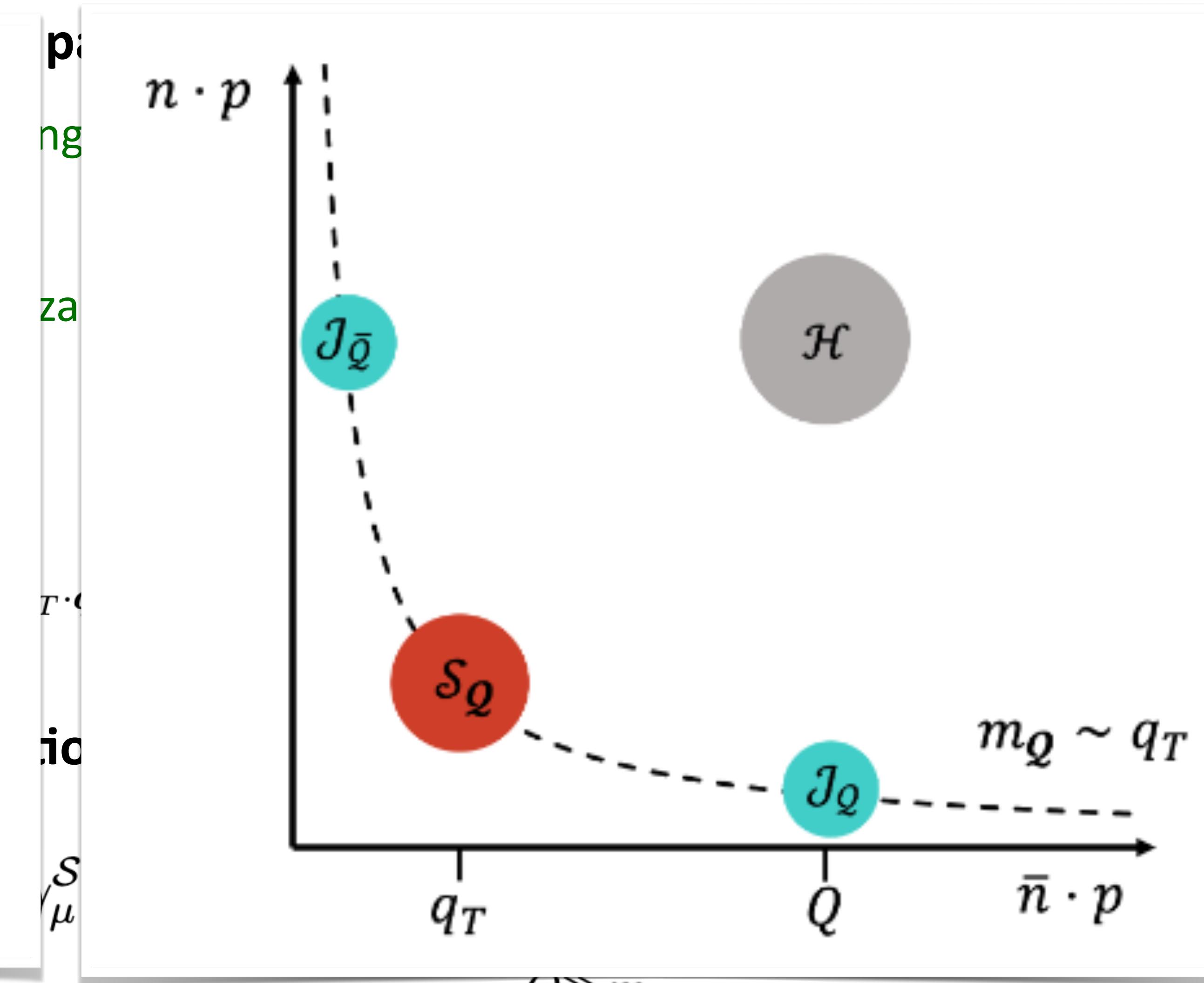
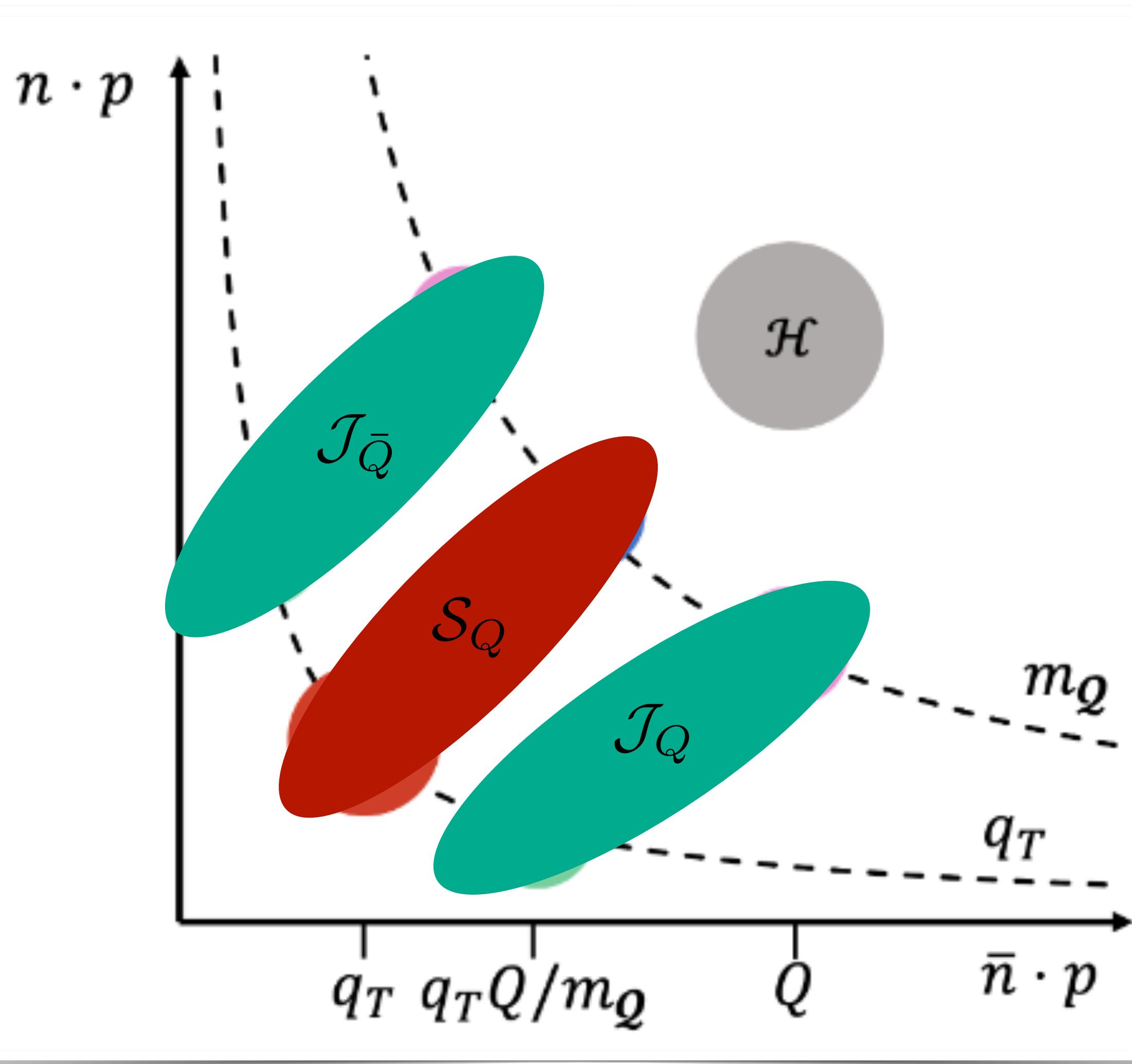
$$Q \sim m_Q \gg q_T$$



- Two loop ultra-collinear function can be determined based on $S \xrightarrow{Q \gg m_Q} \mathcal{C}_Q^2 \mathcal{S}_\perp$

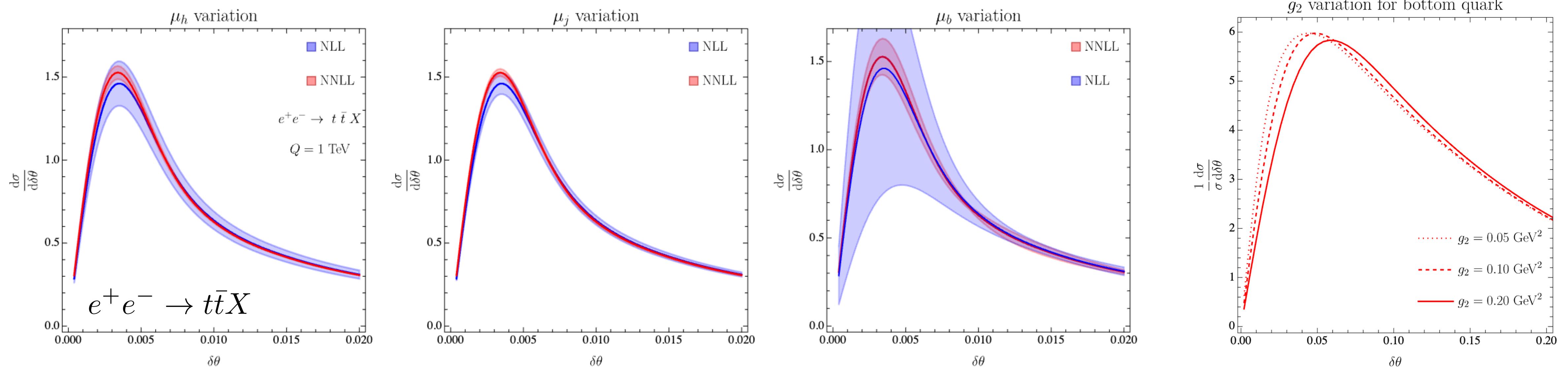
Factorization in region 3

$$Q \sim m_Q \gg q_T$$



- Two loop ultra-collinear function can be determined based on $S \xrightarrow{Q \gg m_Q} C_Q^2 S_\perp$

NNLL resummation in region 2



- We apply b^* -prescription to avoid Landau pole

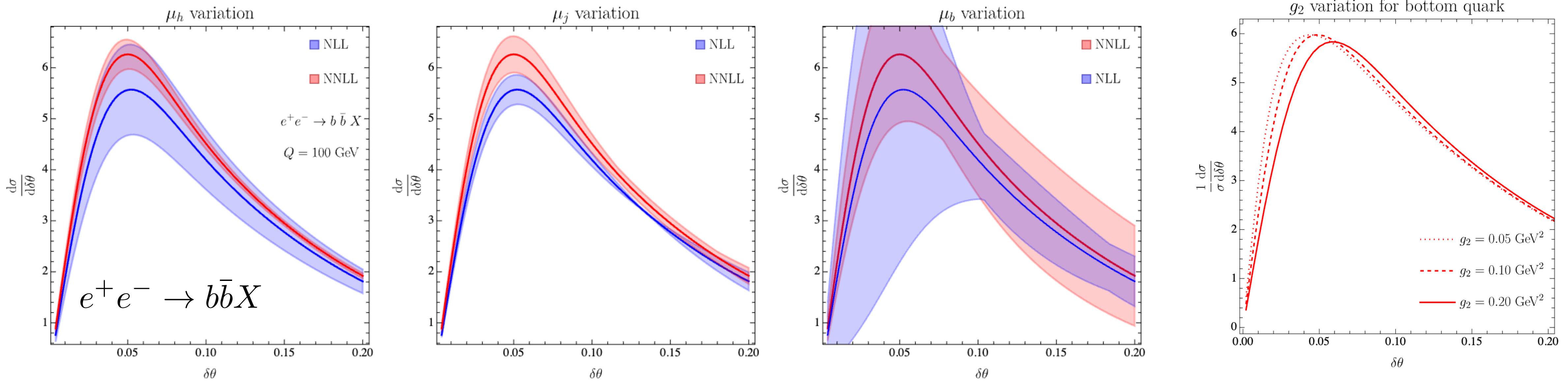
$$\mu_b = \frac{2e^{\gamma_E}}{b^*}, \quad b^* = \frac{b}{\sqrt{1 + b^2/b_{max}^2}}$$

- Leading non-perturbative effects are estimated based on the modification of CS kernel

$$\gamma_\zeta^{S_Q} \rightarrow \gamma_\zeta^{S_Q} - g_2 b^2$$

Becher, Bell '13; Vladimirov '20

NNLL resummation in region 2



- We apply b^* -prescription to avoid Landau pole

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Becher, Bell '13; Vladimirov '20

Heavy quark pairs azimuthal decorrelation in the RHIC

Liu, Ke, DYS in progress

$$N(P_a) + N(P_b) \rightarrow b(p_c) + \bar{b}(p_d) + X(p_X)$$

$$\frac{d^4\sigma_{pp}}{dy_c dy_d dp_T^2 d\delta\phi} = \sum_{ab} \frac{p_T}{16\pi\hat{s}^2} \int_0^\infty \frac{2 db_x}{\pi} \cos(b_x p_T \delta\phi) x_a f_{a/p}(x_a, \mu_{b_*}) x_b f_{b/p}(x_b, \mu_{b_*})$$

$$\times \exp \left\{ - \int_{\mu_{b_*}}^{\mu_h} \frac{d\mu}{\mu} \left[\gamma_{\text{cusp}}(\alpha_s) C_H \ln \frac{\hat{s}}{\mu^2} + 2\gamma_H(\alpha_s) \right] \right\}$$

$$\times \sum_{KK'} \exp \left[- \int_{\mu_{b_*}}^{\mu_h} \frac{d\mu}{\mu} \gamma_{\text{cusp}}(\alpha_s) (\lambda_K + \lambda_{K'}^*) \right] \mathbf{H}_{KK'}(\hat{s}, \hat{t}, \mu_h) \mathbf{W}_{K'K}(b_*, \mu_{b_*})$$

$$\times \exp \left[- \int_{\mu_{b_*}}^{\mu_j} \frac{d\mu}{\mu} \Gamma^{J_c}(\alpha_s) - \int_{\mu_{b_*}}^{\mu_j} \frac{d\mu}{\mu} \Gamma^{J_d}(\alpha_s) \right]$$

$$\times \exp \left[-S_{\text{NP}}^a(b, Q_0, \sqrt{\hat{s}}) - S_{\text{NP}}^b(b, Q_0, \sqrt{\hat{s}}) \right].$$

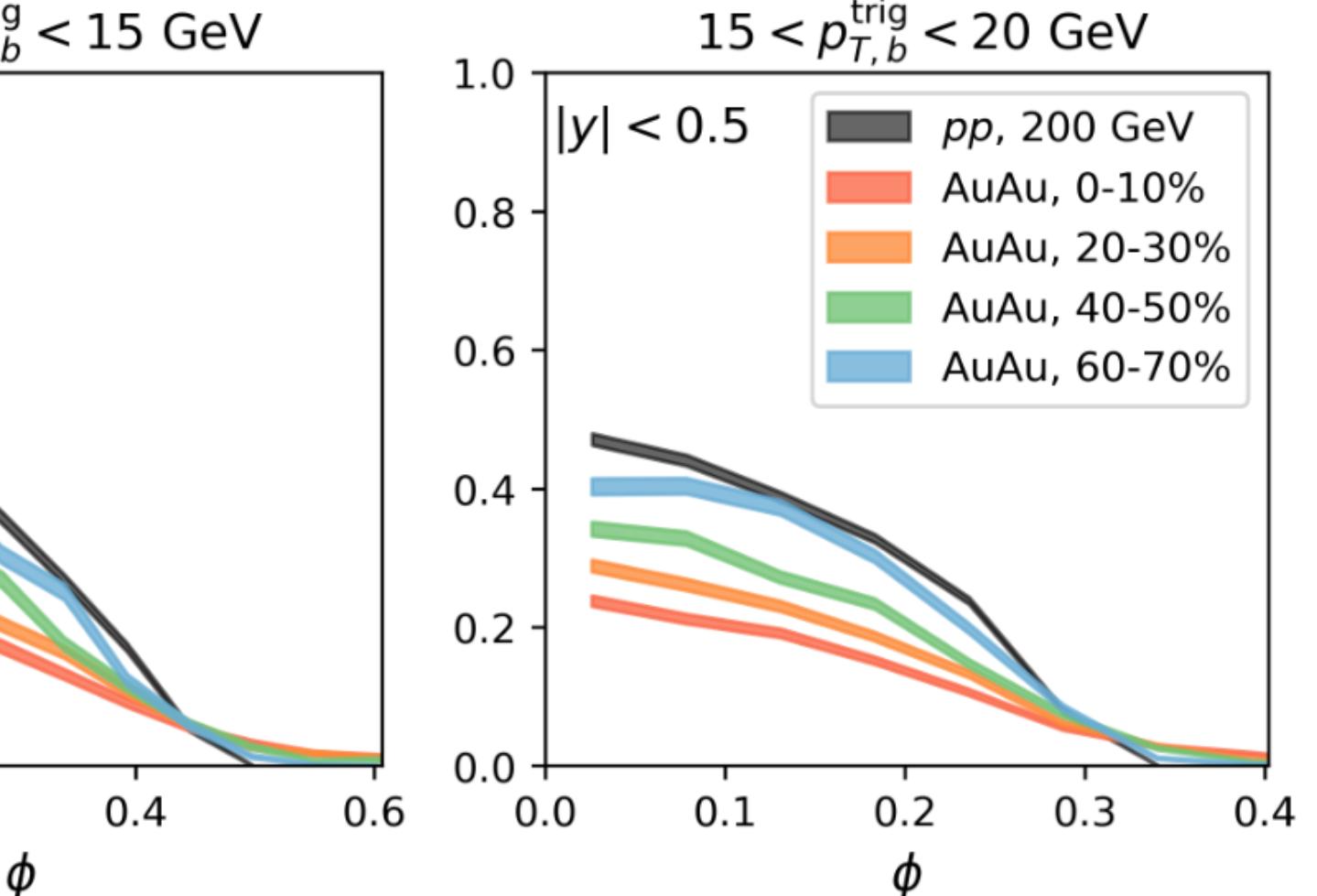
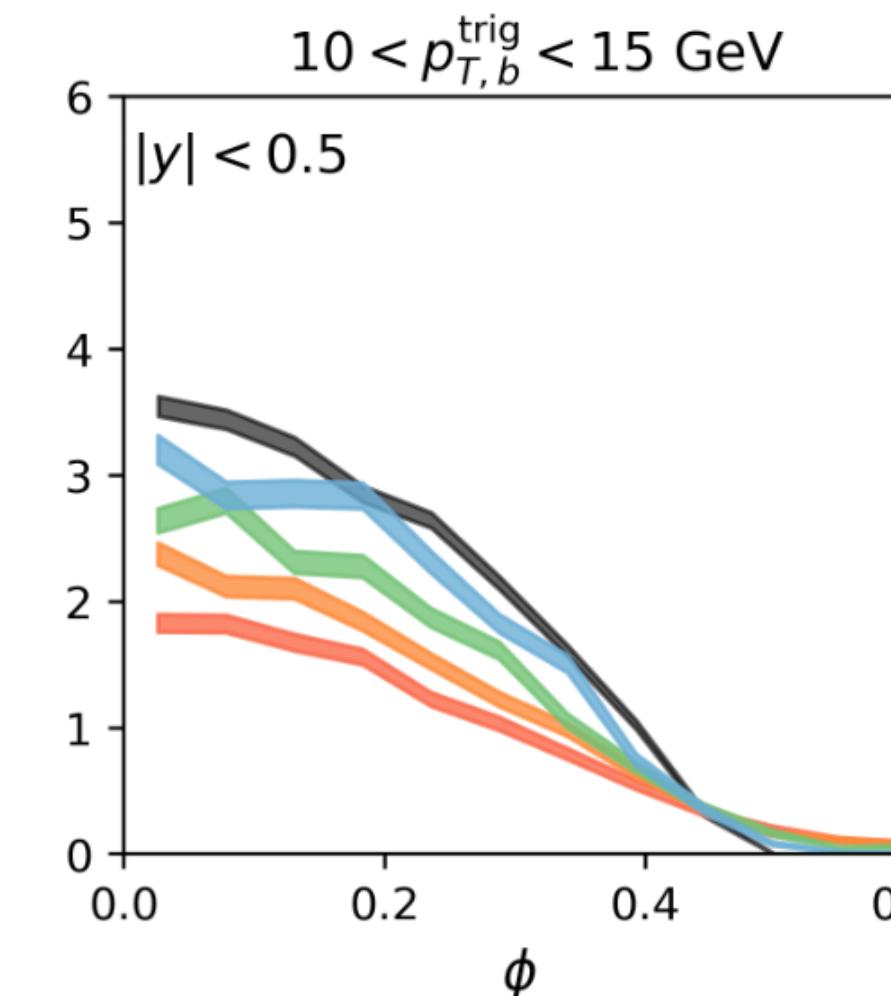
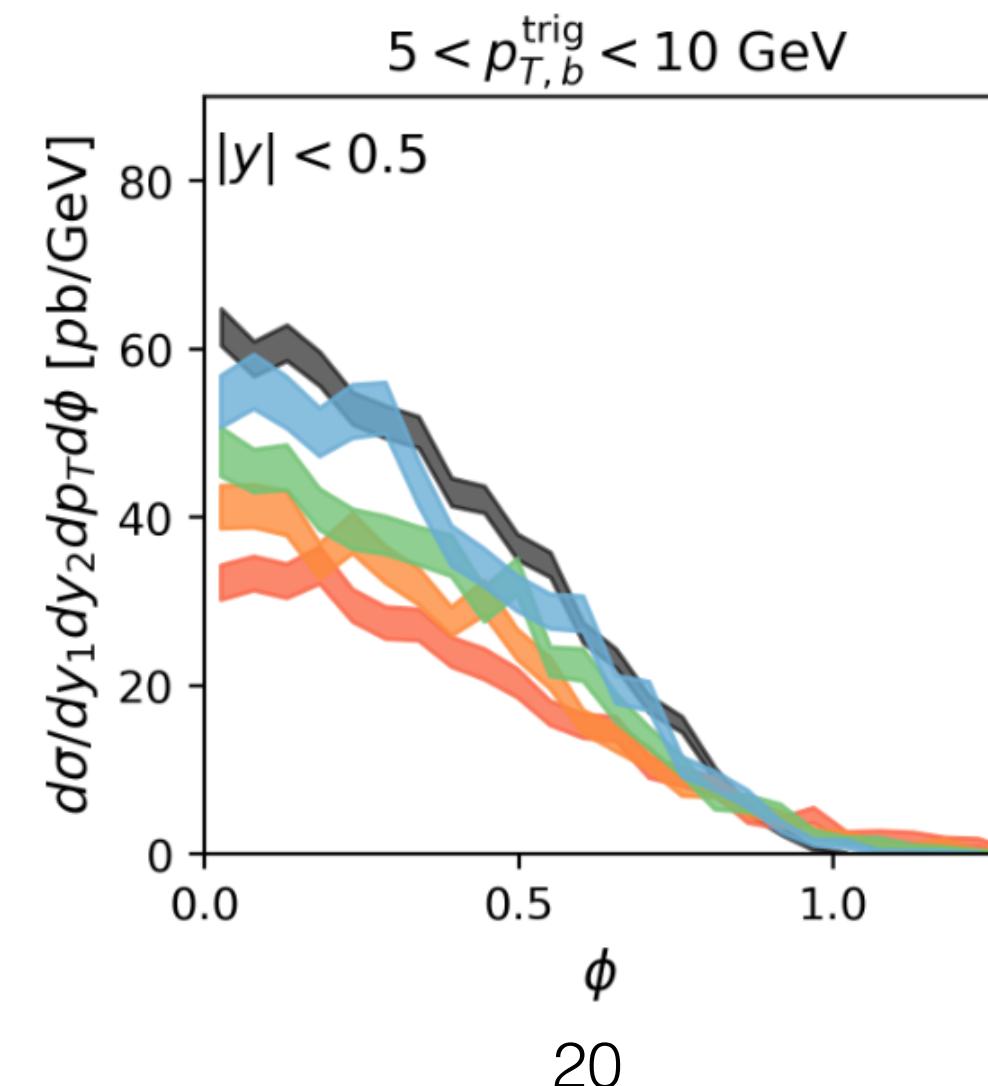
hard: $p_h \sim p_T(1, 1, 1)$

soft: $p_s \sim q_t(1, 1, 1)$

beam: $p_b \sim p_T(1, \delta\phi^2, \delta\phi)$

jet: $p_j \sim p_T(1, \lambda^2, \lambda)_{\mathcal{J}}$

ultra-collinear: $p_{uc} \sim q_t/\lambda(1, \lambda^2, \lambda)_{\mathcal{J}}$



QED resummation of lepton pair azimuthal correlation in UPCs

DYS, Zhang, Zhou, Zhou '23

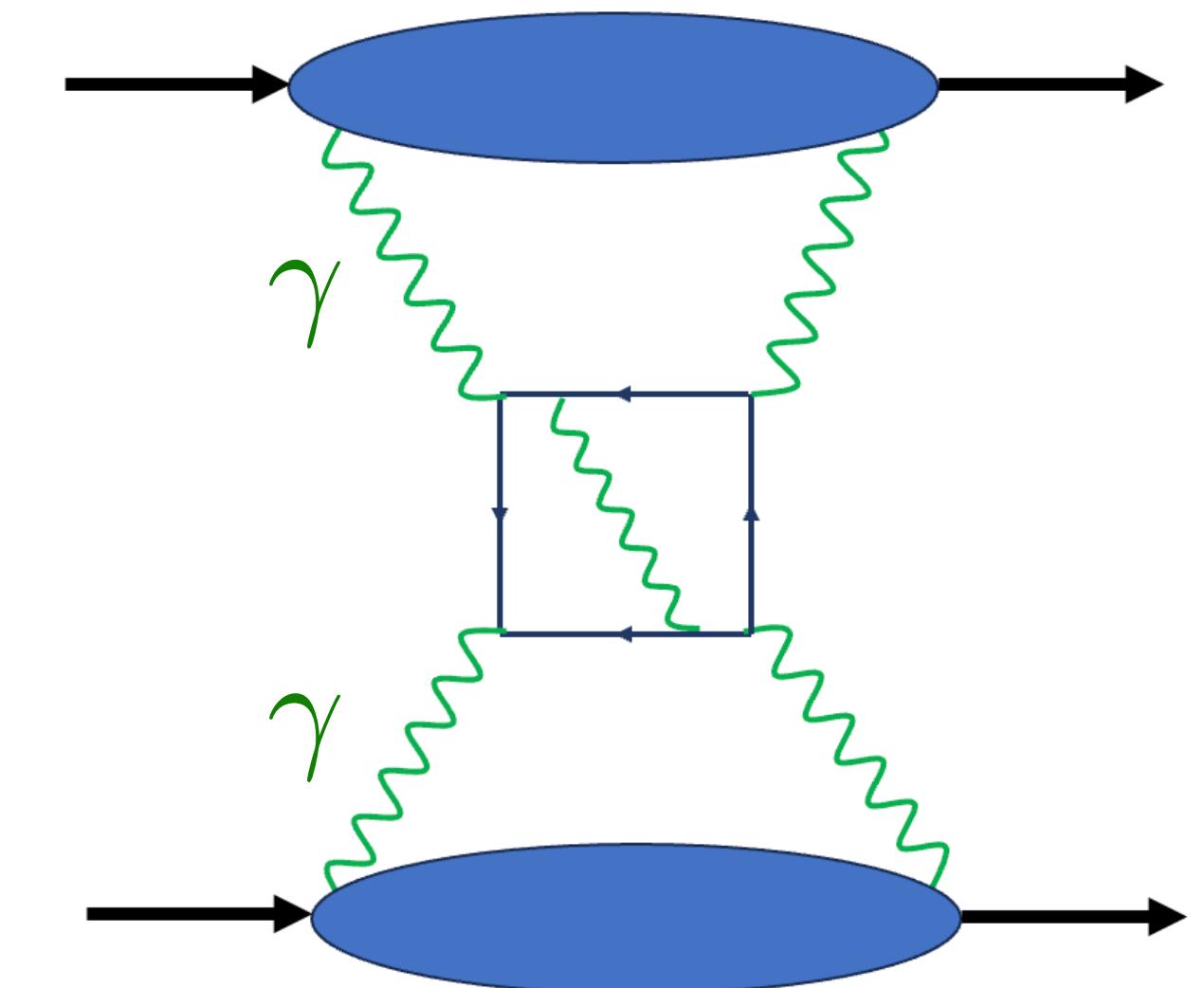
- Ultra-peripheral heavy ion collisions without nuclear breakup $AA \rightarrow AA l^+ l^-$

- Set a baseline for QGP study

- Determine photon flux

- Photon Wigner distribution: (Klein, Mueller, Xiao, Yuan, '20)

$$x f_\gamma(x, k_T; b_\perp) = \int \frac{d^2 \Delta_\perp}{(2\pi)^2} e^{i \Delta_\perp \cdot b_\perp} \int \frac{d\xi^- d^2 r_\perp}{(2\pi)^3} e^{ix P^+ \xi^- - ik_T \cdot r_\perp} \\ \times \left\langle A, -\frac{\Delta_\perp}{2} \right| F^{+\perp} \left(0, \frac{r_\perp}{2} \right) F^{+\perp} \left(\xi^-, -\frac{r_\perp}{2} \right) \left| A, \frac{\Delta_\perp}{2} \right\rangle$$



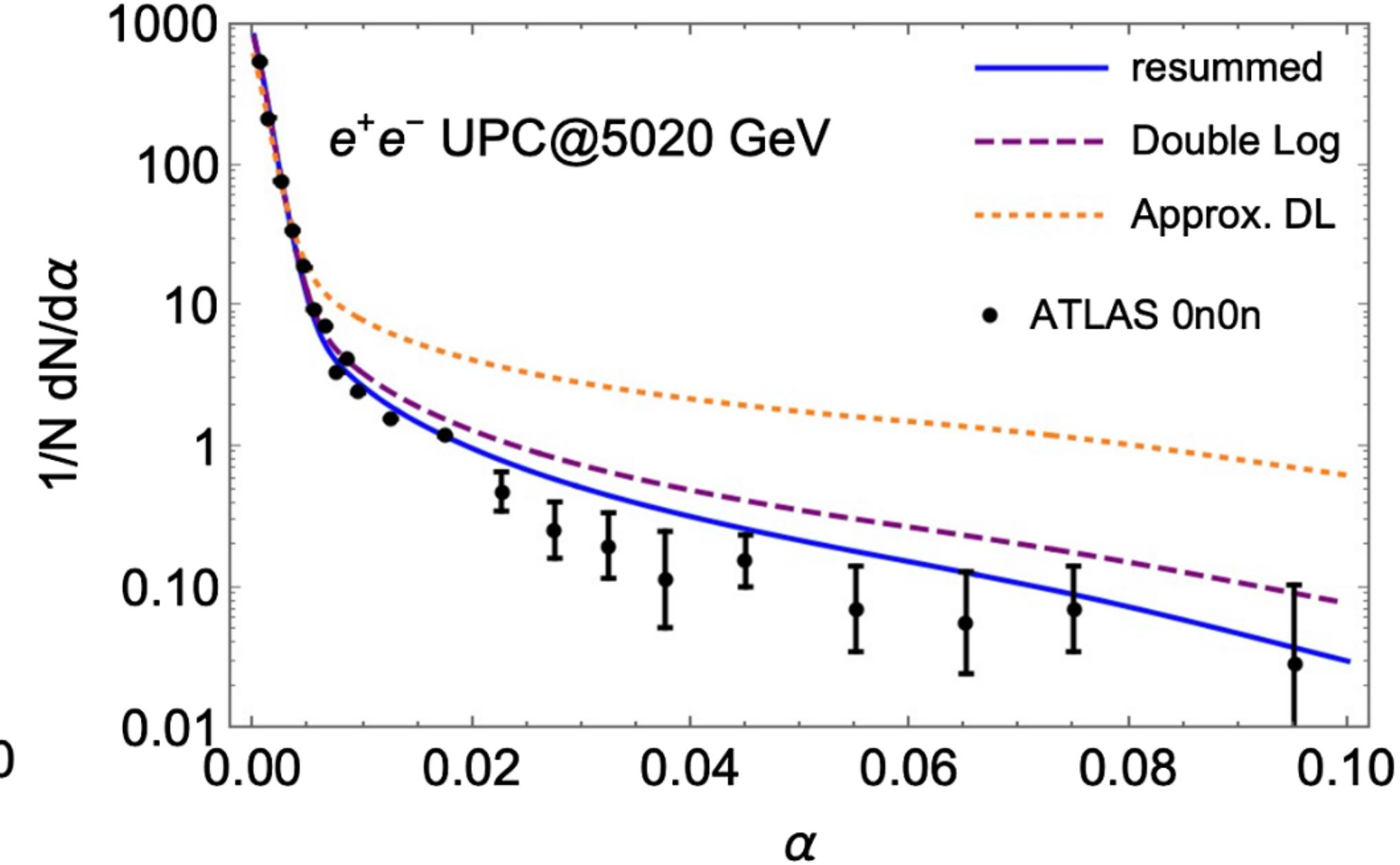
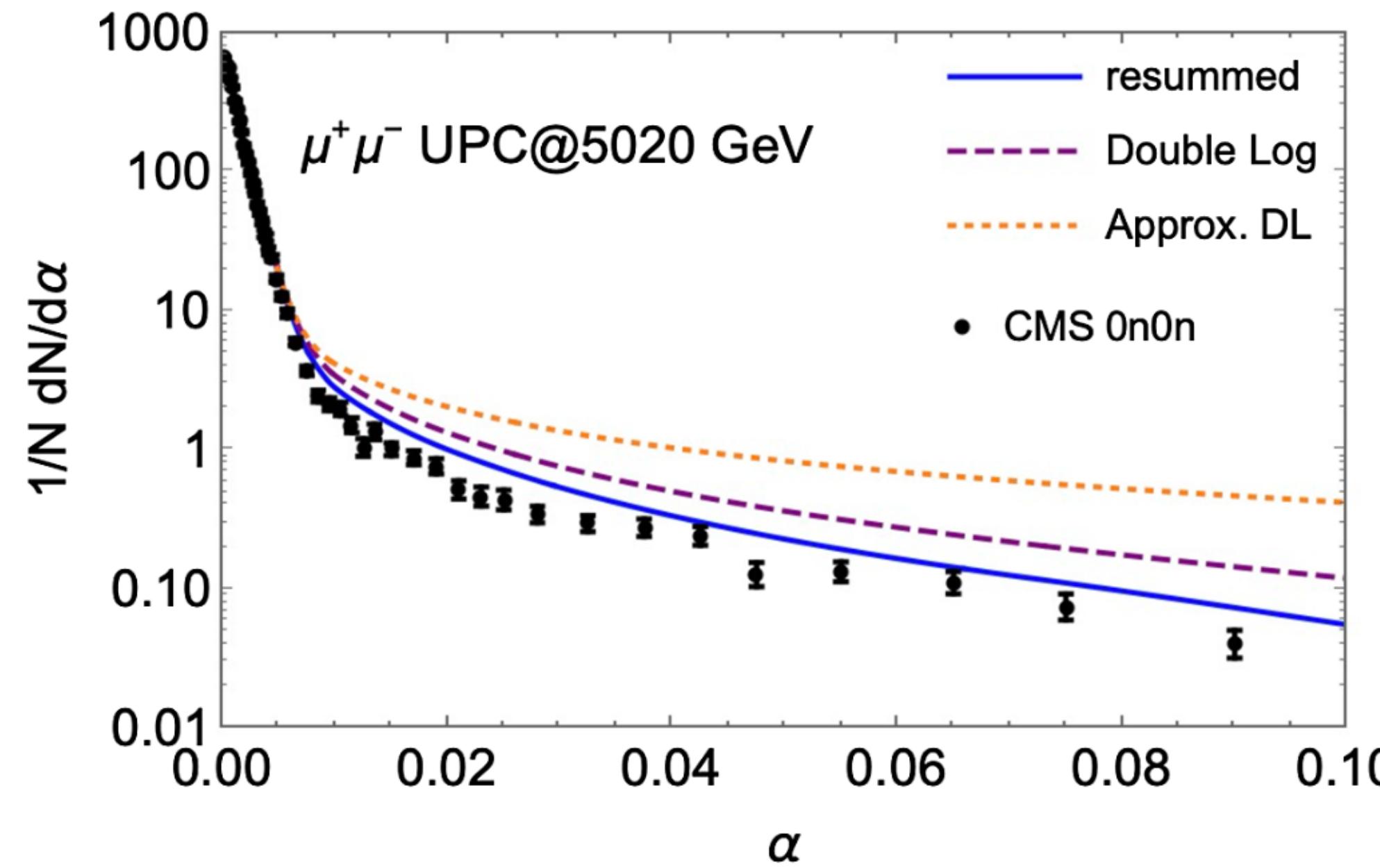
- BSM search: E.g. tau g-2 and tau EDM (ATLAS, '23; CMS '23; DYS, Yan, Yuan, Zhang '24)

- We apply impact parameter dependent formalism and factorization in region 2 to derive the resummation formula

$$\frac{d\sigma}{dq_x d^2 P_\perp dy_1 dy_2 d^2 b_\perp} = \int \frac{dr_x}{2\pi} e^{ir_x q_x} e^{-\text{Sud}(r_x)} \int dq'_x dq'_y e^{-ir_x q'_x} \frac{d\sigma_0(q'_\perp)}{d\mathcal{P.S.}},$$

QED resummation of lepton pair azimuthal correlation in UPCs

DYS, Zhang, Zhou, Zhou '23



- Single log contribution is sizable

$$\text{Sud}_a(r_x) = \frac{\alpha_e}{2\pi} \left[\left(\ln^2 \frac{M^2}{\mu_{rx}^2} - 3 \ln \frac{M^2}{\mu_{rx}^2} \right) - \left(\ln^2 \frac{m^2}{\mu_{rx}^2} - \ln \frac{m^2}{\mu_{rx}^2} \right) \right]$$

- Our findings demonstrate the accessibility of these single log resummation effects through the analysis of angular correlations in lepton pairs.

Conclusion

- We investigate the factorization and resummation formula for heavy quark pair production in back to back limit
- We analyze factorization in three distinct scale hierarchies within SCET, bHQET, HQET

$$Q \gg m_Q \sim q_T$$

$$Q \gg m_Q \gg q_T$$

$$Q \sim m_Q \gg q_T$$

- Refactorization jet function in region 1 are verified at one loop
- In region 2 two-loop ultra-collinear function results are given by RG consistency and refactorization of the soft function in region 3
- We perform the NNLL resummation predictions of heavy quark pair angular correlation in region 2
- We also apply our formalism to study QED resummation of lepton pair azimuthal correlation in UPCs, and find sizable single log contribution
- Our findings demonstrate the accessibility of these single log resummation effects through the analysis of angular correlations in lepton pairs.

Thank you

