



**$B^+ \rightarrow K^+ \nu \bar{\nu}$  excess @ Belle II,**  
**(Dark) SMEFT and NP flavour structure**

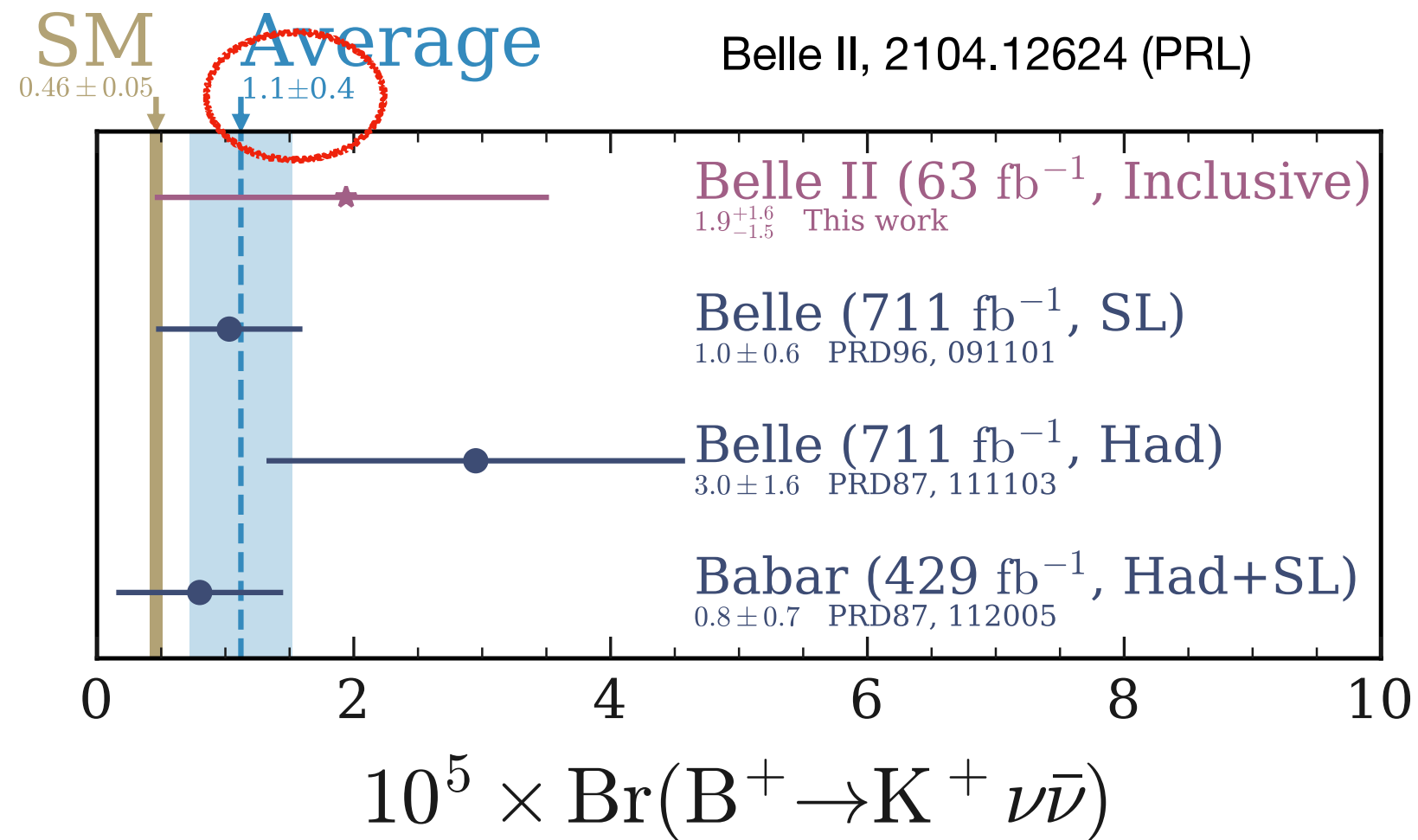
**Xing-Bo Yuan (袁兴博)**

**Central China Normal University (华中师范大学)**

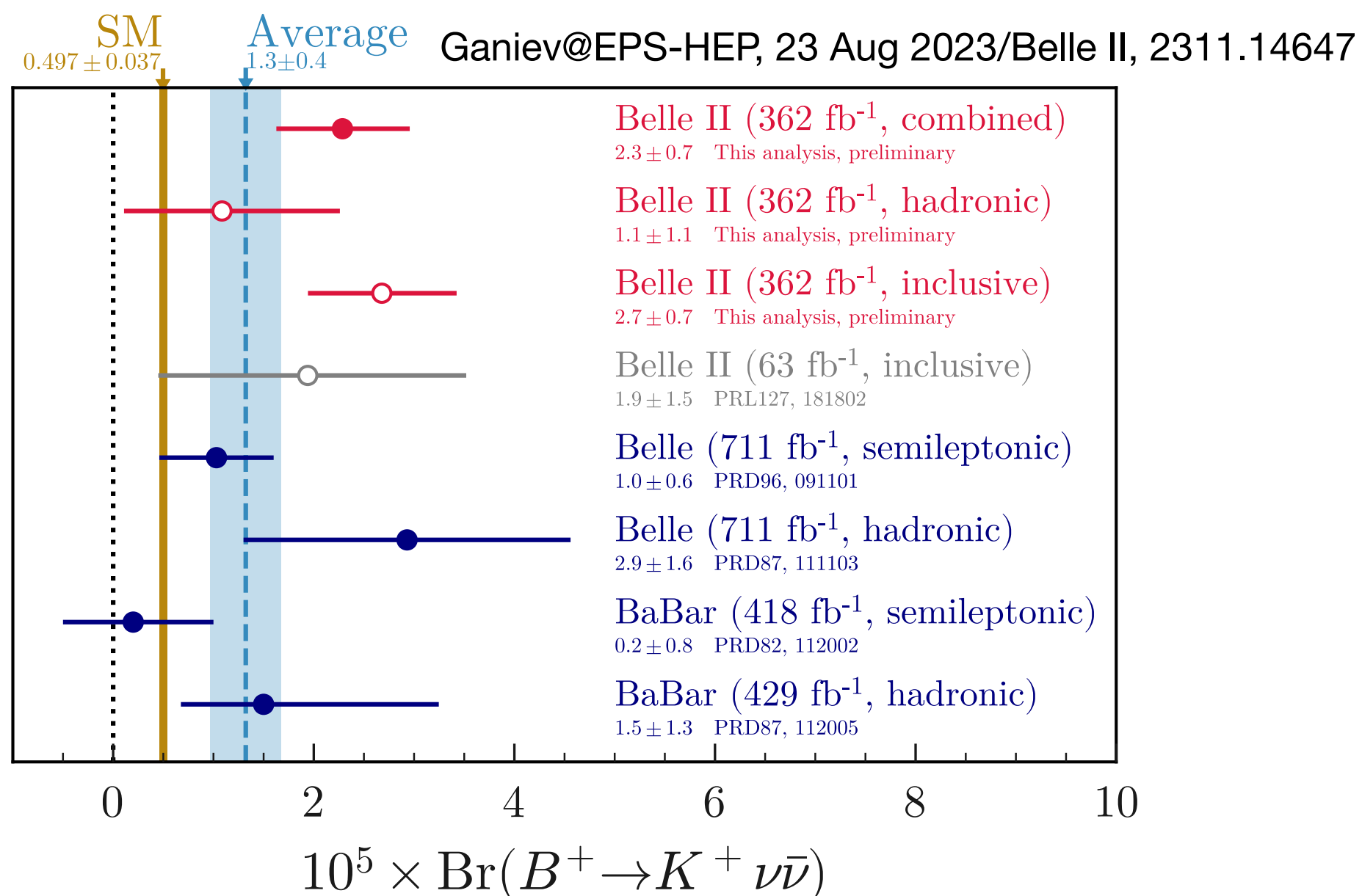
arXiv: 2402.19208, 侯镖锋, 李新强, 沈萌, 杨亚东, 袁兴博

# $b \rightarrow s\nu\bar{\nu}$ : exp & theory

## ► 2021 Apr



## ► 2023 Aug



**Impact of  $B \rightarrow K\nu\bar{\nu}$  measurements on beyond the Standard Model theories** #69  
 Thomas E. Browder (Hawaii U.), Nilendra G. Deshpande (Oregon U.), Rusa Mandal (Siegen U.), Rahul Sinha (IMSC, Chennai and Bhubaneswar, Inst. Phys.) (Jul 2, 2021)  
 Published in: *Phys.Rev.D* 104 (2021) 5, 053007 · e-Print: 2107.01080 [hep-ph]  
[pdf](#) [DOI](#) [cite](#) [claim](#) [reference search](#) [34 citations](#)

**A tale of invisibility: constraints on new physics in  $b \rightarrow s\nu\bar{\nu}$**  #65  
 Tobias Felki (New South Wales U.), Sze Lok Li (New South Wales U.), Michael A. Schmidt (New South Wales U.) (Nov 8, 2021)  
 Published in: *JHEP* 12 (2021) 118 · e-Print: 2111.04327 [hep-ph]  
[pdf](#) [DOI](#) [cite](#) [claim](#) [reference search](#) [24 citations](#)

**Phenomenological study of a gauged  $L_\mu - L_\tau$  model with a scalar leptoquark** #42  
 Chuan-Hung Chen (Taiwan, Natl. Cheng Kung U. and NCTS, Taipei), Cheng-Wei Chiang (Taiwan, Natl. Taiwan U. and NCTS, Taipei), Chun-Wei Su (Taiwan, Natl. Taiwan U.) (May 16, 2023)  
 Published in: *Phys.Rev.D* 109 (2024) 5, 5 · e-Print: 2305.09256 [hep-ph]  
[pdf](#) [DOI](#) [cite](#) [claim](#) [reference search](#) [3 citations](#)

**Explaining the  $B^+ \rightarrow K^+ \nu\bar{\nu}$  excess via a massless dark photon** #16  
 E. Gabrielli, L. Marzola, K. Mürsepp, M. Raidal (Feb 8, 2024)  
 e-Print: 2402.05901 [hep-ph]  
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**Higgs portal interpretation of the Belle II  $B^+ \rightarrow K^+ \nu\bar{\nu}$  measurement** #29  
 David McKeen (TRIUMF), John N. Ng (TRIUMF), Douglas Tuckler (TRIUMF and Simon Fraser U.) (Dec 1, 2023)  
 Published in: *Phys.Rev.D* 109 (2024) 7, 075006 · e-Print: 2312.00982 [hep-ph]  
[pdf](#) [DOI](#) [cite](#) [claim](#) [reference search](#) [10 citations](#)

**Decoding the  $B \rightarrow K\nu\bar{\nu}$  excess at Belle II: kinematics, operators, and masses** #27  
 Kåre Fridell, Mitrajyoti Ghosh, Takemichi Okui, Kohsaku Tobioka (Dec 19, 2023)  
 e-Print: 2312.12507 [hep-ph]  
[pdf](#) [cite](#) [claim](#) [reference search](#) [10 citations](#)

**Light new physics in  $B \rightarrow K^{(*)} \nu\bar{\nu}$ ?** #30  
 Wolfgang Altmannshofer (UC, Santa Cruz, Inst. Part. Phys.), Andreas Crivellin (Zurich U.), Huw Haigh (Vienna, OAW), Gianluca Inguglia (Vienna, OAW), Jorge Martin Camalich (IAC, La Laguna) (Nov 24, 2023)  
 Published in: *Phys.Rev.D* 109 (2024) 7, 075008 · e-Print: 2311.14629 [hep-ph]  
[pdf](#) [DOI](#) [cite](#) [claim](#) [reference search](#) [15 citations](#)

**Understanding the first measurement of  $B(B \rightarrow K\nu\bar{\nu})$**  #38  
 Lukas Allwicher (Zurich U.), Damir Becirevic (IJCLab, Orsay), Gioacchino Piazza (IJCLab, Orsay), Salvador Rosairo-Alcaraz (IJCLab, Orsay), Olcyr Sumensari (IJCLab, Orsay) (Sep 5, 2023)  
 Published in: *Phys.Lett.B* 848 (2024) 138411 · e-Print: 2309.02246 [hep-ph]  
[pdf](#) [DOI](#) [cite](#) [claim](#) [reference search](#) [26 citations](#)

**$B \rightarrow K\nu\bar{\nu}$ , MiniBooNE and muon  $g - 2$  anomalies from a dark sector** #31  
 Alakabha Datta (Mississippi U. and SLAC and UC, Santa Cruz), Danny Marfatia (Hawaii U.), Lopamudra Mukherjee (Nankai U.) (Oct 23, 2023)  
 Published in: *Phys.Rev.D* 109 (2024) 3, L031701 · e-Print: 2310.15136 [hep-ph]  
[pdf](#) [DOI](#) [cite](#) [claim](#) [reference search](#) [11 citations](#)

**Implications of an enhanced  $B \rightarrow K\nu\bar{\nu}$  branching ratio** #39  
 Rigo Bause (Tech. U., Dortmund (main)), Hector Gisbert (INFN, Padua and Padua U.), Gudrun Hiller (Tech. U., Dortmund (main) and Sussex U.) (Aug 31, 2023)  
 Published in: *Phys.Rev.D* 109 (2024) 1, 015006 · e-Print: 2309.00075 [hep-ph]  
[pdf](#) [DOI](#) [cite](#) [claim](#) [reference search](#) [31 citations](#)

**$B \rightarrow K^* M_X$  vs  $B \rightarrow K M_X$  as a probe of a scalar-mediator dark matter scenario** #33  
 Alexander Berezhnoy (SINP, Moscow), Dmitri Melikhov (SINP, Moscow and Dubna, JINR and Vienna U.) (Sep 29, 2023)  
 Published in: *EPL* 145 (2024) 1, 14001 · e-Print: 2309.17191 [hep-ph]  
[pdf](#) [DOI](#) [cite](#) [claim](#) [reference search](#) [10 citations](#)

**B meson anomalies and large  $B^+ \rightarrow K^+ \nu\bar{\nu}$  in non-universal  $U(1)'$  models** #40  
 Peter Athron (Nanjing Normal U.), R. Martinez (Colombia, U. Natl.), Cristian Sierra (Nanjing Normal U.) (Aug 25, 2023)  
 Published in: *JHEP* 02 (2024) 121 · e-Print: 2308.13426 [hep-ph]  
[pdf](#) [DOI](#) [cite](#) [claim](#) [reference search](#) [22 citations](#)

**Flavor anomalies in leptoquark model with gauged  $U(1)_{L_\mu - L_\tau}$**  #34  
 Chuan-Hung Chen (Taiwan, Natl. Cheng Kung U. and Unlisted, TW), Cheng-Wei Chiang (Taiwan, Natl. Taiwan U. and Unlisted, TW) (Sep 22, 2023)  
 Published in: *Phys.Rev.D* 109 (2024) 7, 075004 · e-Print: 2309.12904 [hep-ph]  
[pdf](#) [DOI](#) [cite](#) [claim](#) [reference search](#) [9 citations](#)

**SMEFT predictions for semileptonic processes** #4  
 Siddhartha Karmakar, Amol Dighe, Rick S. Gupta (Apr 15, 2024)  
 e-Print: 2404.10061 [hep-ph]  
[pdf](#) [cite](#) [claim](#) [reference search](#) [0 citations](#)

**Revisiting models that enhance  $B^+ \rightarrow K^+ \nu\bar{\nu}$  in light of the new Belle II measurement** #35  
 Belle-II Collaboration · Xiao-Gang He (Tsung-Dao Lee Inst., Shanghai and Taiwan, Natl. Taiwan U.) et al. (Sep 22, 2023)  
 Published in: *Phys.Rev.D* 109 (2024) 7, 075019 · e-Print: 2309.12741 [hep-ph]  
[pdf](#) [DOI](#) [cite](#) [claim](#) [reference search](#) [16 citations](#)

**Implications of  $B \rightarrow K\nu\bar{\nu}$  under Rank-One Flavor Violation hypothesis** #5  
 David Marzocca, Marco Nardecchia, Alfredo Stanzione, Claudio Toni (Apr 9, 2024)  
 e-Print: 2404.06533 [hep-ph]  
[pdf](#) [cite](#) [claim](#) [reference search](#) [0 citations](#)

**A new look at  $\bar{b} \rightarrow s$  observables in 331 models** #18  
 Francesco Loporco (Jan 22, 2024)  
 e-Print: 2401.11999 [hep-ph]  
[pdf](#) [cite](#) [claim](#) [reference search](#) [1 citation](#)

**Scalar dark matter explanation of the excess in the Belle II  $B^+ \rightarrow K^+ + \text{invisible}$  measurement** #9  
 Xiao-Gang He, Xiao-Dong Ma, Michael A. Schmidt, German Valencia, Raymond R. Volkas (Mar 19, 2024)  
 e-Print: 2403.12485 [hep-ph]  
[pdf](#) [cite](#) [claim](#) [reference search](#) [2 citations](#)

**Correlating  $B \rightarrow K^{(*)} \nu\bar{\nu}$  and flavor anomalies in SMEFT** #19  
 Feng-Zhi Chen, Qiaoyi Wen, Fanrong Xu (Jan 21, 2024)  
 e-Print: 2401.11552 [hep-ph]  
[pdf](#) [cite](#) [claim](#) [reference search](#) [8 citations](#)

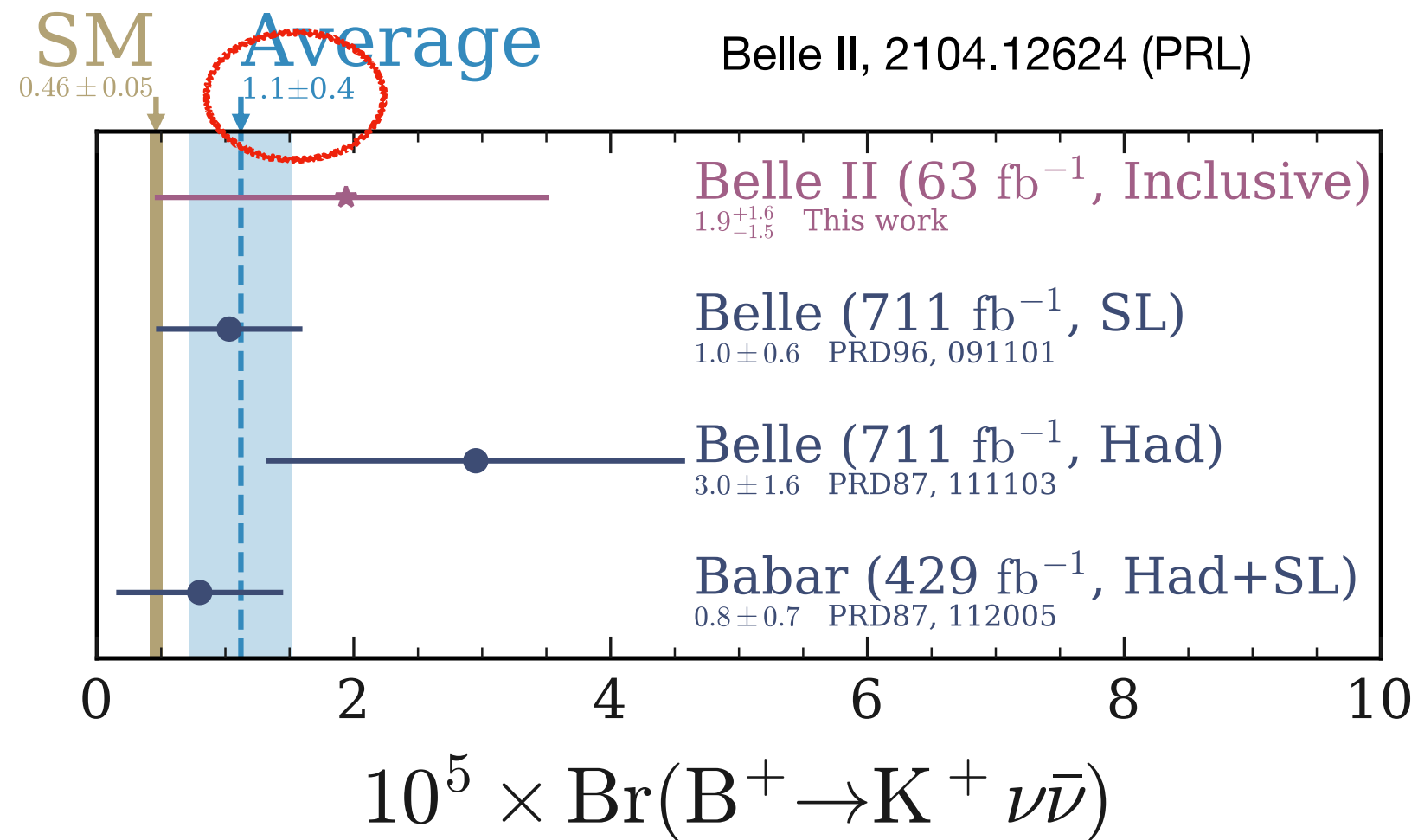
**Status and prospects of rare decays at Belle-II** #10  
 Elisa Manoni (Mar 12, 2024)  
 Published in: *PoS WIFAI2023* (2024) 024 · Contribution to: WIFAI 2023, 024  
[pdf](#) [DOI](#) [cite](#) [claim](#) [reference search](#) [0 citations](#)

**Recent  $B^+ \rightarrow K^+ \nu\bar{\nu}$  Excess and Muon  $g - 2$  Illuminating Light Dark Sector with Higgs Portal** #20  
 Shu-Yu Ho, Jongkuk Kim, Pyungwon Ko (Jan 18, 2024)  
 e-Print: 2401.10112 [hep-ph]  
[pdf](#) [cite](#) [claim](#) [reference search](#) [4 citations](#)

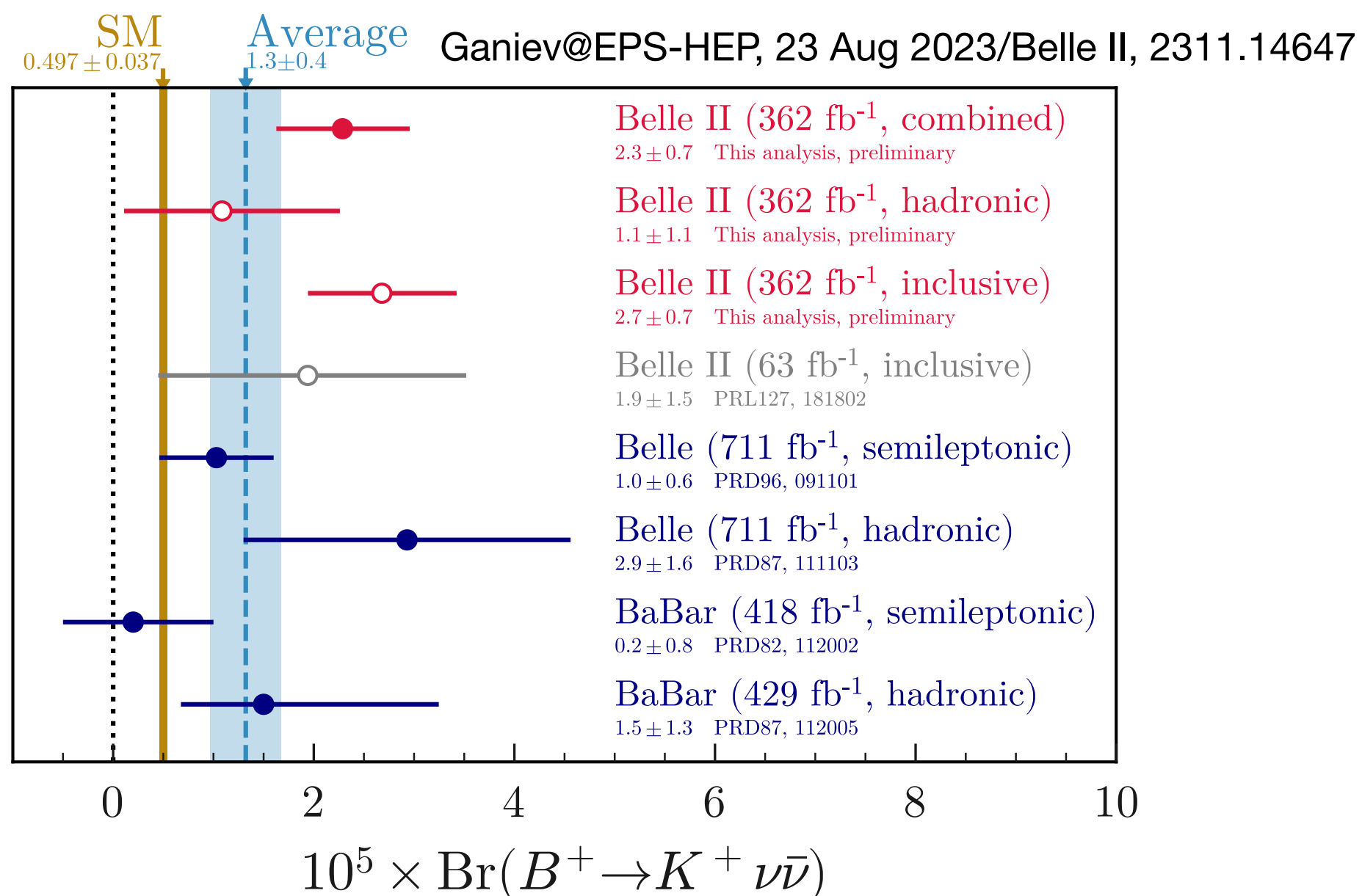
**Rare  $B$  and  $K$  decays in a scotogenic model** #11  
 Chuan-Hung Chen, Cheng-Wei Chiang (Mar 5, 2024)  
 e-Print: 2403.02897 [hep-ph]  
[pdf](#) [cite](#) [claim](#) [reference search](#) [2 citations](#)

# $b \rightarrow s\nu\bar{\nu}$ : exp & theory

## 2021 Apr



## 2023 Aug



## Exp vs SM [10<sup>-6</sup>]

$$\mathcal{B}(B^+ \rightarrow K^+ \nu \bar{\nu})_{\text{SM}} = 4.16 \pm 0.57$$

$$\mathcal{B}(B^+ \rightarrow K^+ \nu \bar{\nu})_{\text{exp}} = 23 \pm 7$$

$$\mathcal{B}(B^+ \rightarrow K^+ \nu \bar{\nu})_{\text{exp}} \gtrsim 10 \text{ (} 2\sigma \text{ lower bound)}$$

**2.7 $\sigma$  difference**

## Theoretical prediction

$$\mathcal{O}_L = (\bar{s}\gamma_\mu P_L b)(\bar{\nu}\gamma^\mu P_L \nu)$$

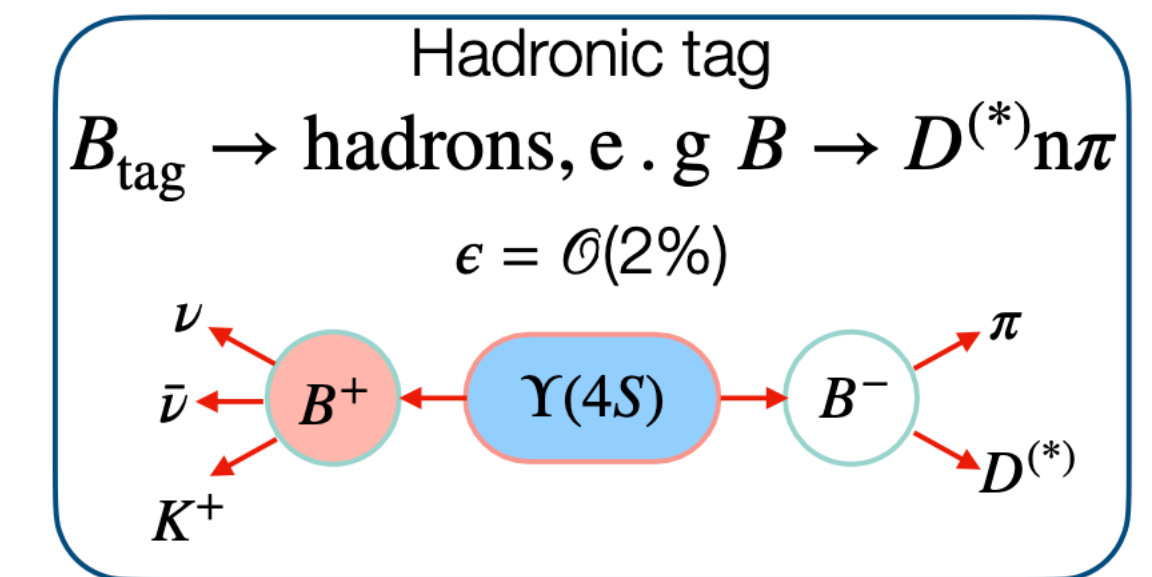
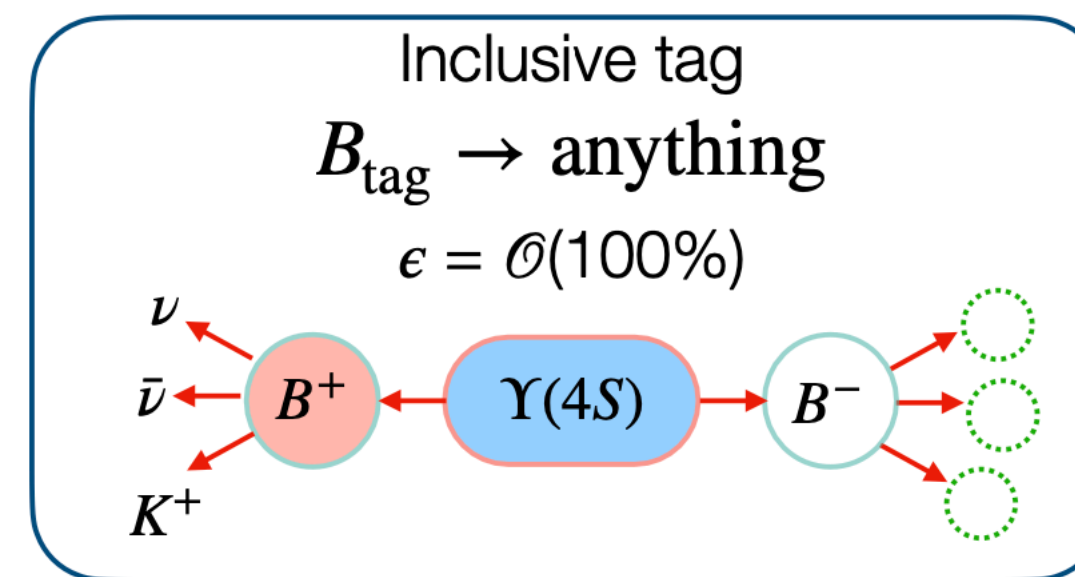
$$\mathcal{O}_R = (\bar{s}\gamma_\mu P_R b)(\bar{\nu}\gamma^\mu P_L \nu)$$

appear in BSM

## Factorization

$$\mathcal{A} \propto C_L \cdot \langle K | \bar{s}\gamma^\mu b | \bar{B} \rangle$$

**theoretically, simple and clean**



# $b \rightarrow s\nu\bar{\nu}$ : exp & theory

	Observable	SM	Exp	Unit
$b \rightarrow s$	$\mathcal{B}(B^+ \rightarrow K^+\nu\bar{\nu})$	$4.16 \pm 0.57$	$23 \pm 5_{-4}^{+5}$	$10^{-6}$
	$\mathcal{B}(B^0 \rightarrow K^0\nu\bar{\nu})$	$3.85 \pm 0.52$	$< 26$	$10^{-6}$
	$\mathcal{B}(B^+ \rightarrow K^{*+}\nu\bar{\nu})$	$9.70 \pm 0.94$	$< 61$	$10^{-6}$
	$\mathcal{B}(B^0 \rightarrow K^{*0}\nu\bar{\nu})$	$9.00 \pm 0.87$	$< 18$	$10^{-6}$
	$\mathcal{B}(B_s \rightarrow \phi\nu\bar{\nu})$	$9.93 \pm 0.72$	$< 5400$	$10^{-6}$
	$\mathcal{B}(B_s \rightarrow \nu\bar{\nu})$	$\approx 0$	$< 5.9$	$10^{-4}$
$b \rightarrow d$	$\mathcal{B}(B^+ \rightarrow \pi^+\nu\bar{\nu})$	$1.40 \pm 0.18$	$< 140$	$10^{-7}$
	$\mathcal{B}(B^0 \rightarrow \pi^0\nu\bar{\nu})$	$6.52 \pm 0.85$	$< 900$	$10^{-8}$
	$\mathcal{B}(B^+ \rightarrow \rho^+\nu\bar{\nu})$	$4.06 \pm 0.79$	$< 300$	$10^{-7}$
	$\mathcal{B}(B^0 \rightarrow \rho^0\nu\bar{\nu})$	$1.89 \pm 0.36$	$< 400$	$10^{-7}$
	$\mathcal{B}(B^0 \rightarrow \nu\bar{\nu})$	$\approx 0$	$< 1.4$	$10^{-4}$
$s \rightarrow d$	$\mathcal{B}(K^+ \rightarrow \pi^+\nu\bar{\nu})$	$8.42 \pm 0.61$	$10.6_{-3.4}^{+4.0} \pm 0.9$	$10^{-11}$
	$\mathcal{B}(K_L \rightarrow \pi^0\nu\bar{\nu})$	$3.41 \pm 0.45$	$< 300$	$10^{-11}$

Why such a large NP effect has not shown up in other  $b \rightarrow s$  decays ?  
in  $b \rightarrow d, s \rightarrow d$  decays ?

## ► Exp vs SM [10<sup>-6</sup>]

$$\mathcal{B}(B^+ \rightarrow K^+\nu\bar{\nu})_{\text{SM}} = 4.16 \pm 0.57$$

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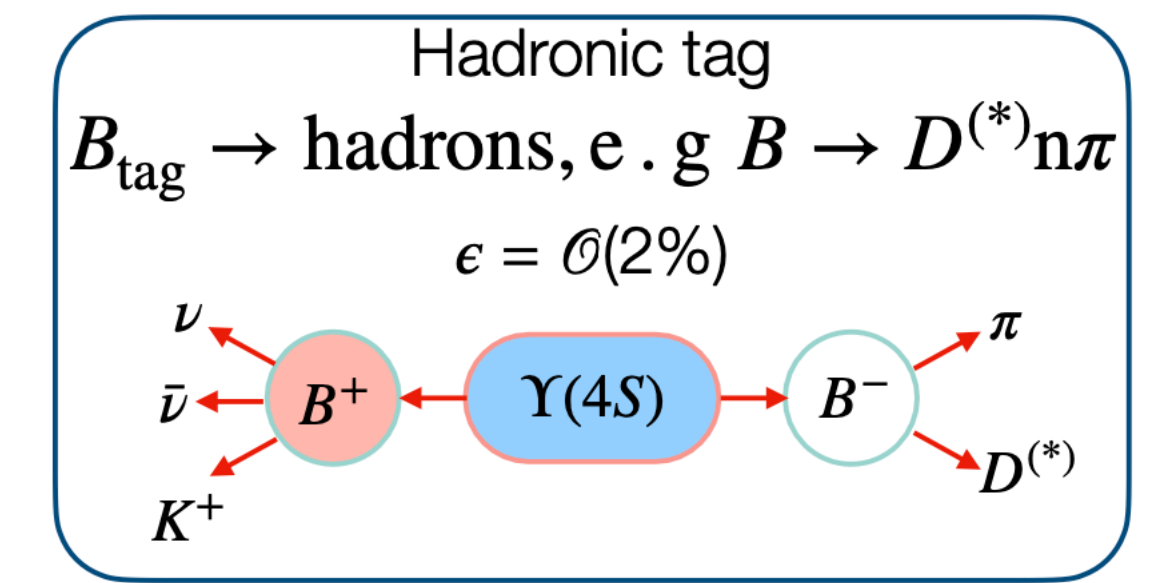
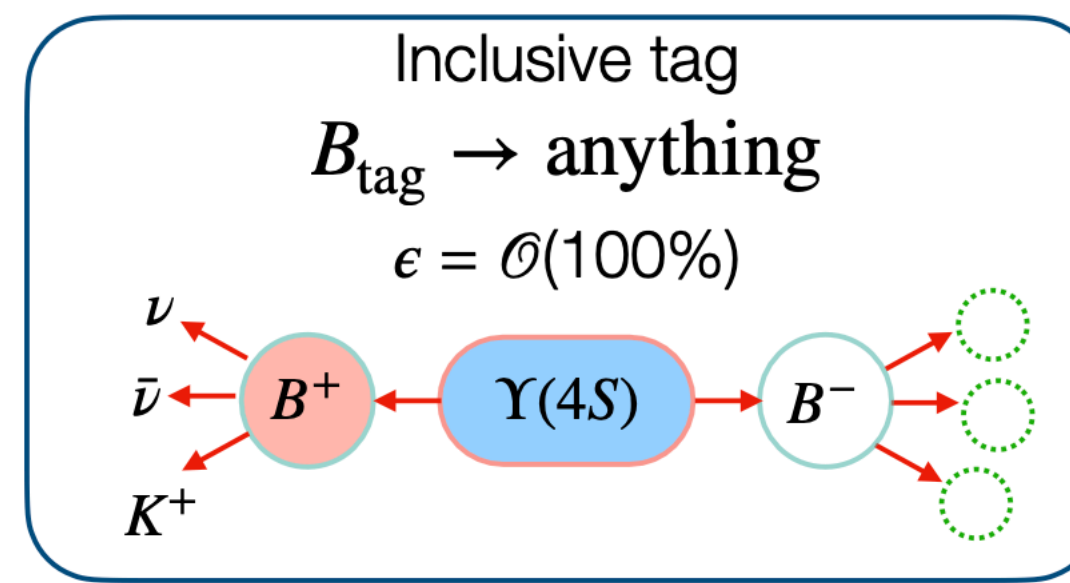
$$\mathcal{O}_R = (\bar{s}\gamma_\mu P_R b)(\bar{\nu}\gamma^\mu P_L \nu)$$

appear in BSM

## Factorization

$$\mathcal{A} \propto C_L \cdot \langle K | \bar{s}\gamma^\mu b | \bar{B} \rangle$$

**theoretically, simple and clean**



# $b \rightarrow s\nu\bar{\nu}$ : SMEFT

SMEFT

$$\mathcal{Q}_{Hq}^{(1)} = (H^\dagger i \overleftrightarrow{D}_\mu H) (\bar{q}_p \gamma^\mu q_r),$$

$$\mathcal{Q}_{Hq}^{(3)} = (H^\dagger i \overleftrightarrow{D}_\mu^I H) (\bar{q}_p \tau^I \gamma^\mu q_r),$$

$$\mathcal{Q}_{Hd} = (H^\dagger i \overleftrightarrow{D}_\mu H) (\bar{d}_p \gamma^\mu d_r),$$

$$\mathcal{Q}_{ld} = (\bar{l}_p \gamma^\mu l_r) (\bar{d}_s \gamma_\mu d_t),$$

$$\mathcal{Q}_{lq}^{(1)} = (\bar{l}_p \gamma^\mu l_r) (\bar{q}_s \gamma_\mu q_t),$$

$$\mathcal{Q}_{lq}^{(3)} = (\bar{l}_p \gamma^\mu \tau^I l_r) (\bar{q}_s \tau^I \gamma_\mu q_t),$$

$\mu_{EW}$

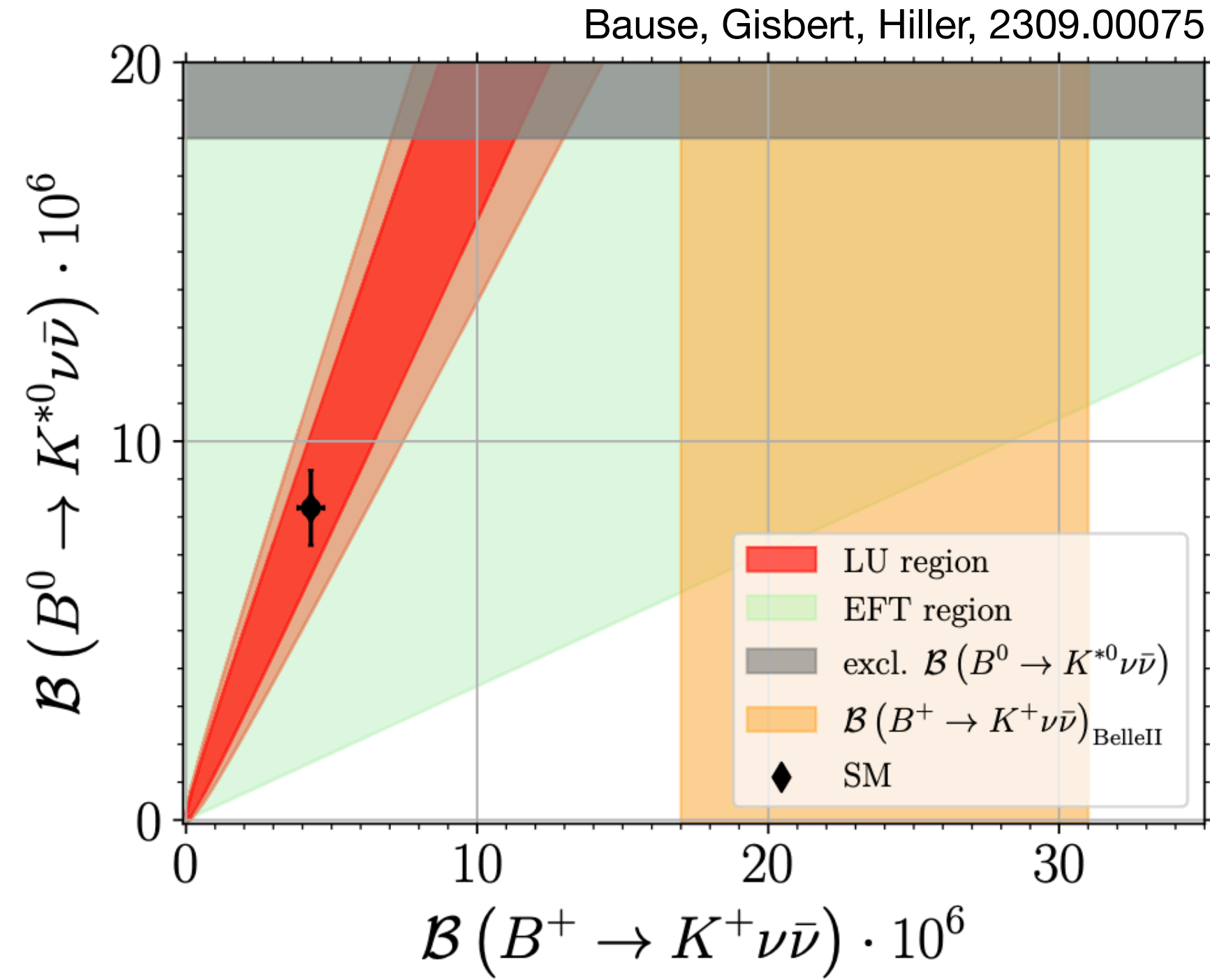
LEFT

$$\mathcal{O}_L^{\nu_i \nu_j} = (\bar{s} \gamma_\mu P_L b) (\bar{\nu}_i \gamma^\mu P_L \nu_j)$$

$$\mathcal{O}_R^{\nu_i \nu_j} = (\bar{s} \gamma_\mu P_R b) (\bar{\nu}_i \gamma^\mu P_L \nu_j)$$

$\mu_b$

operator structure highly  
constrained by Left-handed neutrino



$$\mathcal{B}(B^+ \rightarrow K^+ \nu \bar{\nu}) = A_+^{BK} x^+,$$

$$\mathcal{B}(B^0 \rightarrow K^{*0} \nu \bar{\nu}) = A_+^{BK^*} x^+ + A_-^{BK^*} x^-,$$

$$x^\pm = \sum_{\nu, \nu'} |C_L^{\nu \nu'} \pm C_R^{\nu \nu'}|^2,$$

Bause, Gisbert, Hiller, 2309.00075

Allwicher, Becirevic, Piazza, Rosauero-Alcaraz, Sumensari, 2309.02246

Chen, Wen, Xu, 2401.11552

# $b \rightarrow s\nu\bar{\nu}$ : SMEFT

<b>SMEFT</b>	↑	$\mathcal{Q}_{Hq}^{(1)} = (H^\dagger i \overleftrightarrow{D}_\mu H) (\bar{q}_p \gamma^\mu q_r),$
		$\mathcal{Q}_{Hq}^{(3)} = (H^\dagger i \overleftrightarrow{D}_\mu^I H) (\bar{q}_p \tau^I \gamma^\mu q_r),$
		$\mathcal{Q}_{Hd} = (H^\dagger i \overleftrightarrow{D}_\mu H) (\bar{d}_p \gamma^\mu d_r),$
		$\mathcal{Q}_{ld} = (\bar{l}_p \gamma^\mu l_r) (\bar{d}_s \gamma_\mu d_t),$
		$\mathcal{Q}_{lq}^{(1)} = (\bar{l}_p \gamma^\mu l_r) (\bar{q}_s \gamma_\mu q_t),$
		$\mathcal{Q}_{lq}^{(3)} = (\bar{l}_p \gamma^\mu \tau^I l_r) (\bar{q}_s \tau^I \gamma_\mu q_t),$
<b>LEFT</b>	↑	$\mathcal{O}_L^{\nu_i \nu_j} = (\bar{s} \gamma_\mu P_L b) (\bar{\nu}_i \gamma^\mu P_L \nu_j)$
		$\mathcal{O}_R^{\nu_i \nu_j} = (\bar{s} \gamma_\mu P_R b) (\bar{\nu}_i \gamma^\mu P_L \nu_j)$
$\mu_b$		operator structure highly constrained by Left-handed neutrino

$b \rightarrow s$

$b \rightarrow d$

$s \rightarrow d$

Observable	SM	Exp	Unit
$\mathcal{B}(B^+ \rightarrow K^+ \nu \bar{\nu})$	$4.16 \pm 0.57$	$23 \pm 5_{-4}^{+5}$	$10^{-6}$
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$\mathcal{B}(K_L \rightarrow \pi^0 \nu \bar{\nu})$	$3.41 \pm 0.45$	$< 300$	$10^{-11}$

Why such a large NP effect has not shown up in other  $b \rightarrow s$  decays ?  
in  $b \rightarrow d, s \rightarrow d$  decays ? **NP flavour structure**

# Minimal Flavour Violation

- ▶ Flavour symmetry without Yukawa

$$G_{\text{QF}} = SU(3)_q \otimes SU(3)_u \otimes SU(3)_d$$

- ▶ Flavour symmetry breaking

$$-\mathcal{L}_Y = \bar{q} Y_d H d + \bar{q} Y_u \tilde{H} u + \text{h.c.}$$

- ▶ Flavour symmetry recovering: Yukawa coupling  $\implies$  spurion field

$$Y_u \sim (\mathbf{3}, \bar{\mathbf{3}}, \mathbf{1}) \quad Y_d \sim (\mathbf{3}, \mathbf{1}, \bar{\mathbf{3}})$$

D'Ambrosio, Giudice, Isidori, Strumia, 2009

- ▶ EFT with MFV: operators, constructed from SM and Yukawa spurion fields, are invariant under CP and  $G_{\text{QF}}$

$$\mathcal{C}^{\text{MFV}} = \begin{cases} f(A, B) & \text{for } \bar{q} \gamma^\mu \mathcal{C} q, \\ f(A, B) Y_d & \text{for } \bar{q} \mathcal{C} d, \bar{q} \sigma^{\mu\nu} \mathcal{C} d, \\ \epsilon_0 \mathbb{1} + Y_d^\dagger g(A, B) Y_d & \text{for } \bar{d} \gamma^\mu \mathcal{C} d, \end{cases} \quad \begin{aligned} f(A, B) &= \epsilon_0 \mathbb{1} + \epsilon_1 A + \epsilon_2 B + \epsilon_3 A^2 + \epsilon_4 B^2 + \epsilon_5 AB + \dots \\ A &= Y_u Y_u^\dagger \\ B &= Y_d Y_d^\dagger \end{aligned}$$

# Minimal Flavour Violation

- ▶ Spurion function

$$f(A, B) = \epsilon_0 \mathbb{1} + \epsilon_1 A + \epsilon_2 B + \epsilon_3 A^2 + \epsilon_4 B^2 + \epsilon_5 AB + \dots$$

- ▶ Cayley-Hamilton identity for  $3 \times 3$  invertible matrix  $X$

$$X^3 = \text{Det}X \cdot \mathbb{1} + \frac{1}{2}[\text{Tr}X^2 - (\text{Tr}X)^2] \cdot X + \text{Tr}X \cdot X^2$$

- ▶ Spurion function after resummation

Colangelo, Nikolidakis, Smith, 2009  
Mercolli, Smith, 2009

$$f(A, B) = \epsilon_0 \mathbb{1} + \epsilon_1 A + \epsilon_3 A^2 + \epsilon_5 AB + \epsilon_7 ABA + \epsilon_{10} AB^2 + \epsilon_{12} A^2 B^2 + \epsilon_{14} B^2 AB + \epsilon_{15} AB^2 A^2 \\ + \epsilon_2 B + \epsilon_4 B^2 + \epsilon_6 BA + \epsilon_9 BAB + \epsilon_8 BA^2 + \epsilon_{13} B^2 A^2 + \epsilon_{11} ABA^2 + \epsilon_{16} B^2 A^2 B.$$

- ▶ assumption #1: neglect tiny imaginary parts of  $\epsilon_i$
- ▶ assumption #2: neglect spurion B (suppressed by  $\mathcal{O}(\lambda_d)$ )

$$f(A, B) \approx \epsilon_0 \mathbb{1} + \epsilon_1 A + \epsilon_2 A^2$$



# Minimal Flavour Violation

- ▶ MFV coupling      FCNC controlled by CKM

$$C^{\text{MFV}} = \begin{cases} \epsilon_0 1 + \epsilon_1 \Delta_q & \text{for } \bar{d}_L \gamma^\mu C d_L \\ \epsilon_0 \hat{\lambda}_d + \epsilon_1 \Delta_q \hat{\lambda}_d & \text{for } \bar{d}_L C d_R, \bar{d}_L \sigma^{\mu\nu} C d_R \\ \epsilon_0 1 & \text{for } \bar{d}_R \gamma^\mu C d_R \end{cases} \quad \Delta_q = V^\dagger \hat{\lambda}_u^2 V$$

**No Right-handed down-type FCNC !**

- ▶ Numerics

$$\Delta_q = \begin{pmatrix} 0.8 & -3.3 - 1.5i & 79.3 + 35.4i \\ -3.3 + 1.5i & 16.6 & -397.5 + 8.1i \\ 79.3 - 35.4i & -397.5 - 8.1i & 9839.0 \end{pmatrix} \times 10^{-4}$$

$$\Delta_q \hat{\lambda}_d = \begin{pmatrix} 0.0021 & -0.18 - 0.08i & 191.3 + 85.4i \\ -0.009 + 0.004i & 0.88 & -958.7 + 19.6i \\ 0.21 - 0.10i & -21.1 - 0.4i & 23728.1 \end{pmatrix} \times 10^{-6}$$

# $b \rightarrow s\nu\bar{\nu}$ : SMEFT with MFV

## ► Prediction

$$\frac{\mathcal{B}(B^+ \rightarrow K^+ \nu \bar{\nu})}{\mathcal{B}(B^0 \rightarrow K^{*0} \nu \bar{\nu})} = \frac{\mathcal{B}(B^+ \rightarrow K^+ \nu \bar{\nu})_{\text{SM}}}{\mathcal{B}(B^0 \rightarrow K^{*0} \nu \bar{\nu})_{\text{SM}}} = 0.46 \pm 0.07$$

$$\frac{\mathcal{B}(B^+ \rightarrow K^+ \nu \bar{\nu})}{\mathcal{B}(B^+ \rightarrow \pi^+ \nu \bar{\nu})} = \frac{\mathcal{B}(B^+ \rightarrow K^+ \nu \bar{\nu})_{\text{SM}}}{\mathcal{B}(B^+ \rightarrow \pi^+ \nu \bar{\nu})_{\text{SM}}} = 29.7 \pm 5.6$$

## ► prediction

$$\mathcal{B}(B^0 \rightarrow K^{*0} \nu \bar{\nu})_{\text{SM}} = (9.00 \pm 0.87) \times 10^{-6}$$

$$\mathcal{B}(B^0 \rightarrow K^{*0} \nu \bar{\nu})_{\text{MFV}} = (50_{-16}^{+17}) \times 10^{-6}$$

$$\mathcal{B}(B^0 \rightarrow K^{*0} \nu \bar{\nu})_{\text{exp}} < 18 \times 10^{-6}$$

$$\mathcal{B}(B^+ \rightarrow \pi^+ \nu \bar{\nu})_{\text{SM}} = (1.40 \pm 0.18) \times 10^{-7}$$

$$\mathcal{B}(B^+ \rightarrow \pi^+ \nu \bar{\nu})_{\text{MFV}} = (7.8_{-2.6}^{+2.8}) \times 10^{-7}$$

$$\mathcal{B}(B^+ \rightarrow \pi^+ \nu \bar{\nu})_{\text{exp}} < 140 \times 10^{-7}$$

SMEFT

$$\begin{aligned} \mathcal{Q}_{Hq}^{(1)} &= (H^\dagger i \overleftrightarrow{D}_\mu H) (\bar{q}_p \gamma^\mu q_r), \\ \mathcal{Q}_{Hq}^{(3)} &= (H^\dagger i \overleftrightarrow{D}_\mu^I H) (\bar{q}_p \tau^I \gamma^\mu q_r), \\ \mathcal{Q}_{Hd} &= (H^\dagger i \overleftrightarrow{D}_\mu H) (\bar{d}_p \gamma^\mu d_r), \end{aligned}$$

induce  $\bar{s}bZ$  interaction,  
Thus, universally affect  
 $b \rightarrow se^+e^-, \mu^+\mu^-, \tau^+\tau^-$

$$\mathcal{Q}_{ld} = (\bar{l}_p \gamma^\mu l_r) (\bar{d}_s \gamma_\mu d_t),$$

forbidden by MFV

$$\begin{aligned} \mathcal{Q}_{lq}^{(1)} &= (\bar{l}_p \gamma^\mu l_r) (\bar{q}_s \gamma_\mu q_t), \\ \mathcal{Q}_{lq}^{(3)} &= (\bar{l}_p \gamma^\mu \tau^I l_r) (\bar{q}_s \tau^I \gamma_\mu q_t), \end{aligned}$$

$\mu_{\text{EW}}$

LEFT

$$\begin{aligned} \mathcal{O}_L^{\nu_i \nu_j} &= (\bar{s} \gamma_\mu P_L b) (\bar{\nu}_i \gamma^\mu P_L \nu_j) \\ \mathcal{O}_R^{\nu_i \nu_j} &= (\bar{s} \gamma_\mu P_R b) (\bar{\nu}_i \gamma^\mu P_L \nu_j) \end{aligned}$$

one LEFT operator !

$\mu_b$

# $b \rightarrow s\nu\bar{\nu}$ : SMEFT with MFV

## ► Prediction

$$\frac{\mathcal{B}(B^+ \rightarrow K^+ \nu \bar{\nu})}{\mathcal{B}(B^0 \rightarrow K^{*0} \nu \bar{\nu})} = \frac{\mathcal{B}(B^+ \rightarrow K^+ \nu \bar{\nu})_{\text{SM}}}{\mathcal{B}(B^0 \rightarrow K^{*0} \nu \bar{\nu})_{\text{SM}}} = 0.46 \pm 0.07$$

$$\frac{\mathcal{B}(B^+ \rightarrow K^+ \nu \bar{\nu})}{\mathcal{B}(B^+ \rightarrow \pi^+ \nu \bar{\nu})} = \frac{\mathcal{B}(B^+ \rightarrow K^+ \nu \bar{\nu})_{\text{SM}}}{\mathcal{B}(B^+ \rightarrow \pi^+ \nu \bar{\nu})_{\text{SM}}} = 29.7 \pm 5.6$$

## ► prediction

$$\mathcal{B}(B^0 \rightarrow K^{*0} \nu \bar{\nu})_{\text{SM}} = (9.00 \pm 0.87) \times 10^{-6}$$

$$\mathcal{B}(B^0 \rightarrow K^{*0} \nu \bar{\nu})_{\text{MFV}} = (50^{+17}_{-16}) \times 10^{-6}$$

$$\mathcal{B}(B^0 \rightarrow K^{*0} \nu \bar{\nu})_{\text{exp}} < 18 \times 10^{-6}$$

Inconsistent →

$$\mathcal{B}(B^+ \rightarrow \pi^+ \nu \bar{\nu})_{\text{SM}} = (1.40 \pm 0.18) \times 10^{-7}$$

$$\mathcal{B}(B^+ \rightarrow \pi^+ \nu \bar{\nu})_{\text{MFV}} = (7.8^{+2.8}_{-2.6}) \times 10^{-7}$$

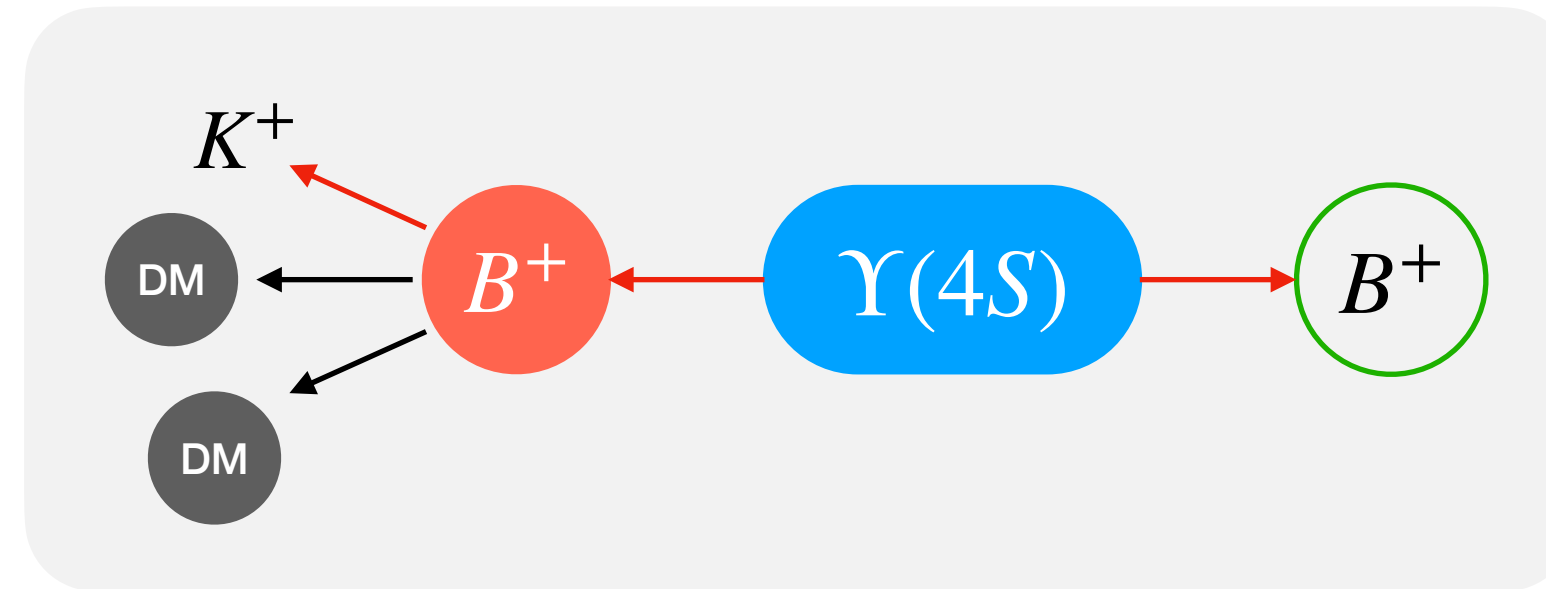
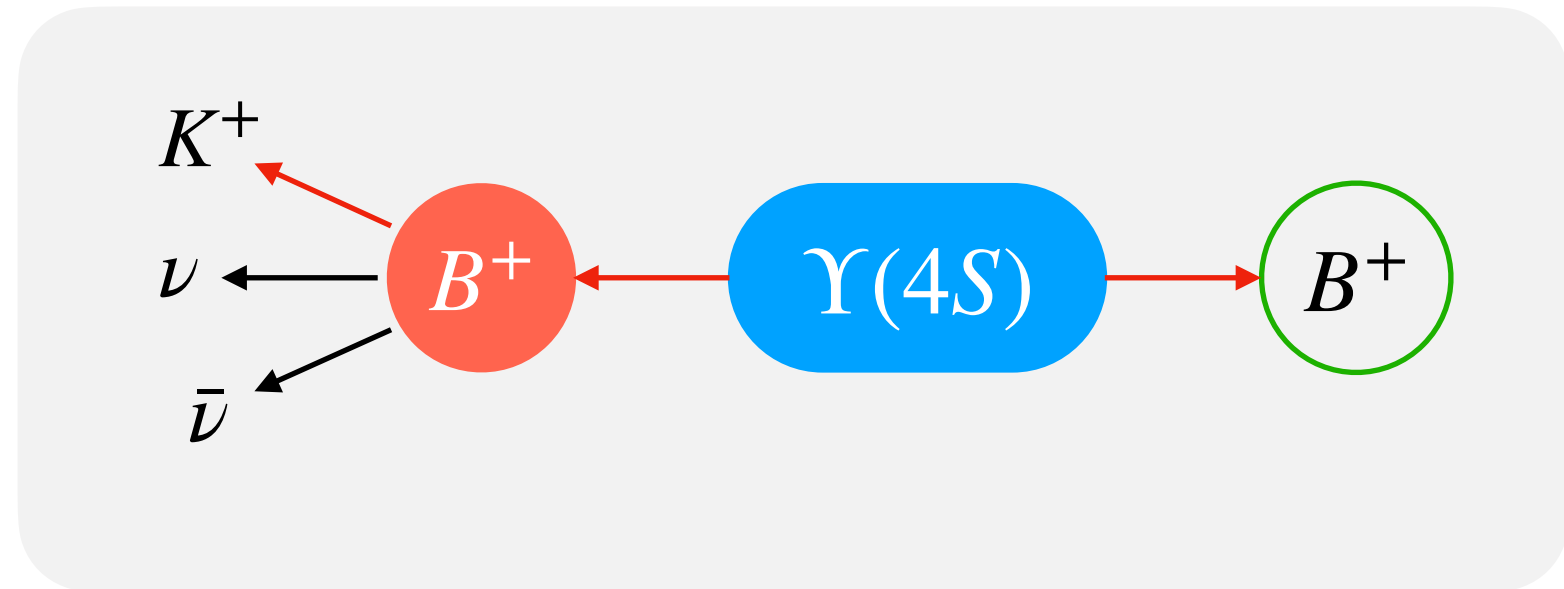
$$\mathcal{B}(B^+ \rightarrow \pi^+ \nu \bar{\nu})_{\text{exp}} < 140 \times 10^{-7}$$

Belle II excess (if confirmed in the future) implies:

- impossible to explain in SMEFT with MFV
- NP flavour structure is highly non-trivial
- **NP structure in quark sector is beyond MFV**
- **flavour violation is beyond Yukawa coupling**

This conclusion only assumes the quark MFV.  
No lepton flavour structure is assumed.

# $b \rightarrow s\nu\bar{\nu}$ : exp picture



$$Q_{Hq}^{(1)} = (H^\dagger i \overleftrightarrow{D}_\mu H) (\bar{q}_p \gamma^\mu q_r),$$

$$Q_{Hq}^{(3)} = (H^\dagger i \overleftrightarrow{D}_\mu^I H) (\bar{q}_p \tau^I \gamma^\mu q_r),$$

$$Q_{Hd} = (H^\dagger i \overleftrightarrow{D}_\mu H) (\bar{d}_p \gamma^\mu d_r),$$

$$Q_{ld} = (\bar{l}_p \gamma^\mu l_r) (\bar{d}_s \gamma_\mu d_t),$$

$$Q_{lq}^{(1)} = (\bar{l}_p \gamma^\mu l_r) (\bar{q}_s \gamma_\mu q_t),$$

$$Q_{lq}^{(3)} = (\bar{l}_p \gamma^\mu \tau^I l_r) (\bar{q}_s \tau^I \gamma_\mu q_t),$$

$$\mathcal{O}_L^{\nu_i \nu_j} = (\bar{s} \gamma_\mu P_L b) (\bar{\nu}_i \gamma^\mu P_L \nu_j)$$

$$\mathcal{O}_R^{\nu_i \nu_j} = (\bar{s} \gamma_\mu P_R b) (\bar{\nu}_i \gamma^\mu P_L \nu_j)$$

**SMEFT**

**Dark SMEFT**

example

$$Q_{d\phi^2} = (\bar{q}_p d_r H) \phi^2$$

$$Q_{d\chi} = (\bar{d}_p \gamma_\mu d_r) (\bar{\chi} \gamma^\mu \chi)$$

$$Q_{dX^2} = (\bar{q}_p d_r H) X_\mu X^\mu$$

$$Q_{qa} = (\bar{q}_p \gamma_\mu q_r) \partial^\mu a$$

- 2011 Kamenik, Smith
- 2014 Duch, Grzadkowski, Wudka
- 2017 Brod, Gootjes-Dreesbach, Tamaro, Zupan
- 2021 Criado, Djouadi, Perez-Victoria, Santiago
- 2022 Aebischer, Altmannshofer, Jenkins, Manohar ([basis@dim-6](mailto:basis@dim-6))
- 2023 Song, Sun, Yu ([basis@dim-8](mailto:basis@dim-8))

- Axion-like particle, see also H.Y.Cheng, Phys.Rept 1988
- 2020 Bauer, Neubert, Renner, Schnubel, Thamm
  - 2023 Song, Sun, Yu ([basis@dim-8](mailto:basis@dim-8))

$\mu_{EW}$   
**LEFT**

**Dark LEFT**

$$\mathcal{O}_{d\phi^2} = (\bar{d}_{Lp} d_{Rr}) \phi^2$$

$$\mathcal{O}_{d\chi}^{V,LR} = (\bar{d}_{Lp} \gamma_\mu d_{Lr}) (\bar{\chi}_a \gamma^\mu \chi_b)$$

$$\mathcal{O}_{dXX}^L = (\bar{d}_{Lp} \gamma_\mu d_{Lr}) X^{\mu\nu} X_\nu$$

$$\mathcal{O}_{da}^L = (\bar{d}_{Lp} \gamma_\mu d_{Lr}) \partial^\mu a$$

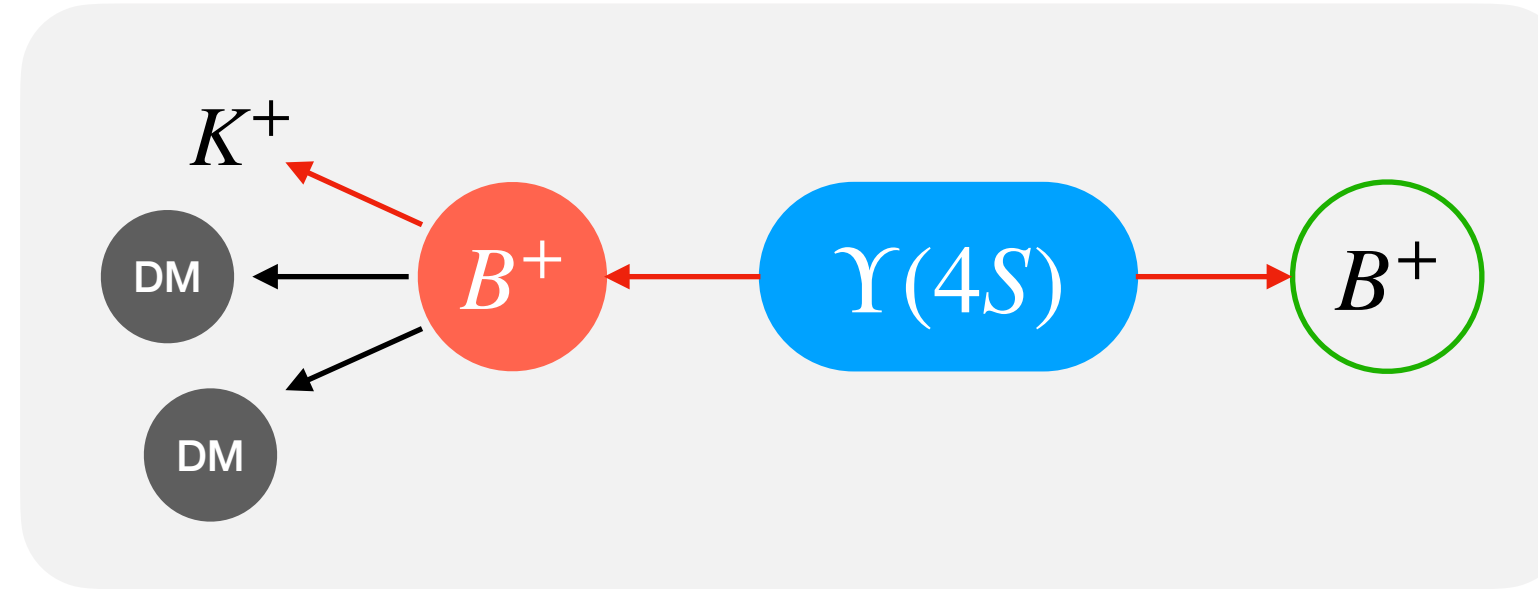
example

- 2022 Aebischer, Altmannshofer, Jenkins, Manohar ([basis@dim-6](mailto:basis@dim-6))
- 2022 He, Ma, Valencia ([basis@dim-6](mailto:basis@dim-6))
- 2023 Liang, Liao, Ma, Wang ([basis@dim-8](mailto:basis@dim-8))

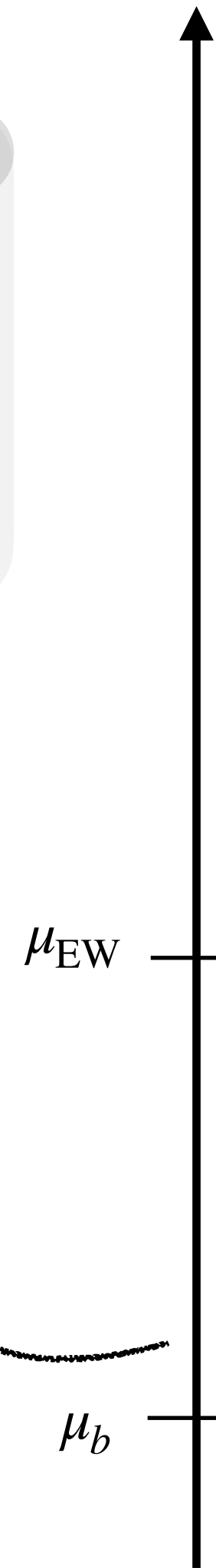
$\mu_b$

# $b \rightarrow s\nu\bar{\nu}$ : DSMEFT

Can DSMEFT operators explain the Belle II excess, while satisfy other  $b \rightarrow s$  bounds ?



Observable	SM	Exp	Unit
$\mathcal{B}(B^+ \rightarrow K^+\nu\bar{\nu})$	$4.16 \pm 0.57$	$23 \pm 5_{-4}^{+5}$	$10^{-6}$
$\mathcal{B}(B^0 \rightarrow K^0\nu\bar{\nu})$	$3.85 \pm 0.52$	$< 26$	$10^{-6}$
$\mathcal{B}(B^+ \rightarrow K^{*+}\nu\bar{\nu})$	$9.70 \pm 0.94$	$< 61$	$10^{-6}$
$\mathcal{B}(B^0 \rightarrow K^{*0}\nu\bar{\nu})$	$9.00 \pm 0.87$	$< 18$	$10^{-6}$
$\mathcal{B}(B_s \rightarrow \phi\nu\bar{\nu})$	$9.93 \pm 0.72$	$< 5400$	$10^{-6}$
$\mathcal{B}(B_s \rightarrow \nu\bar{\nu})$	$\approx 0$	$< 5.9$	$10^{-4}$
$\mathcal{B}(B^+ \rightarrow \pi^+\nu\bar{\nu})$	$1.40 \pm 0.18$	$< 140$	$10^{-7}$
$\mathcal{B}(B^0 \rightarrow \pi^0\nu\bar{\nu})$	$6.52 \pm 0.85$	$< 900$	$10^{-8}$
$\mathcal{B}(B^+ \rightarrow \rho^+\nu\bar{\nu})$	$4.06 \pm 0.79$	$< 300$	$10^{-7}$
$\mathcal{B}(B^0 \rightarrow \rho^0\nu\bar{\nu})$	$1.89 \pm 0.36$	$< 400$	$10^{-7}$
$\mathcal{B}(B^0 \rightarrow \nu\bar{\nu})$	$\approx 0$	$< 1.4$	$10^{-4}$
$\mathcal{B}(K^+ \rightarrow \pi^+\nu\bar{\nu})$	$8.42 \pm 0.61$	$10.6_{-3.4}^{+4.0} \pm 0.9$	$10^{-11}$
$\mathcal{B}(K_L \rightarrow \pi^0\nu\bar{\nu})$	$3.41 \pm 0.45$	$< 300$	$10^{-11}$



## Dark SMEFT

$$\begin{aligned} \mathcal{Q}_{d\phi} &= (\bar{q}_p d_r H) \phi + \text{h.c.}, & \mathcal{Q}_{d\phi^2} &= (\bar{q}_p d_r H) \phi^2 + \text{h.c.}, \\ \mathcal{Q}_{\phi q} &= (\bar{q}_p \gamma_\mu q_r) (i\phi_1 \overleftrightarrow{\partial}^\mu \phi_2), & \mathcal{Q}_{\phi d} &= (\bar{d}_p \gamma_\mu d_r) (i\phi_1 \overleftrightarrow{\partial}^\mu \phi_2), \\ \mathcal{Q}_{q\chi} &= (\bar{q}_p \gamma_\mu q_r) (\bar{\chi} \gamma^\mu \chi), & \mathcal{Q}_{d\chi} &= (\bar{d}_p \gamma_\mu d_r) (\bar{\chi} \gamma^\mu \chi), \\ \mathcal{Q}_{dHX} &= (\bar{q}_p \sigma_{\mu\nu} d_r) H X^{\mu\nu} & \mathcal{Q}_{dX^2} &= (\bar{q}_p d_r H) X_\mu X^\mu \\ \mathcal{Q}_{qa} &= (\bar{q}_p \gamma_\mu q_r) \partial^\mu a & \mathcal{Q}_{da} &= (\bar{d}_p \gamma_\mu d_r) \partial^\mu a \end{aligned}$$

scalar: 4

fermion: 2

vector: 1+13

ALP: 2

## Dark LEFT

$$\begin{aligned} \mathcal{O}_{d\phi} &= (\bar{d}_{Lp} d_{Rr}) \phi + \text{h.c.}, & \mathcal{O}_{\phi d}^L &= (\bar{d}_{Lp} \gamma_\mu d_{Lr}) (i\phi_1 \overleftrightarrow{\partial}^\mu \phi_2), \\ \mathcal{O}_{d\chi}^{V,LR} &= (\bar{d}_{Lp} \gamma_\mu d_{Lr}) (\bar{\chi}_a \gamma^\mu \chi_b), & \mathcal{O}_{d\chi}^{V,RR} &= (\bar{d}_{Rp} \gamma_\mu d_{Rr}) (\bar{\chi}_a \gamma^\mu \chi_b), \\ \mathcal{O}_{dX}^T &= (\bar{d}_{Lp} \sigma_{\mu\nu} d_{Rr}) X_a^{\mu\nu} & \mathcal{O}_{dXX}^L &= (\bar{d}_{Lp} \gamma_\mu d_{Lr}) X^{\mu\nu} X_\nu \\ \mathcal{O}_{da}^L &= (\bar{d}_{Lp} \gamma_\mu d_{Lr}) \partial^\mu a, & \mathcal{O}_{da}^R &= (\bar{d}_{Rp} \gamma_\mu d_{Rr}) \partial^\mu a. \end{aligned}$$

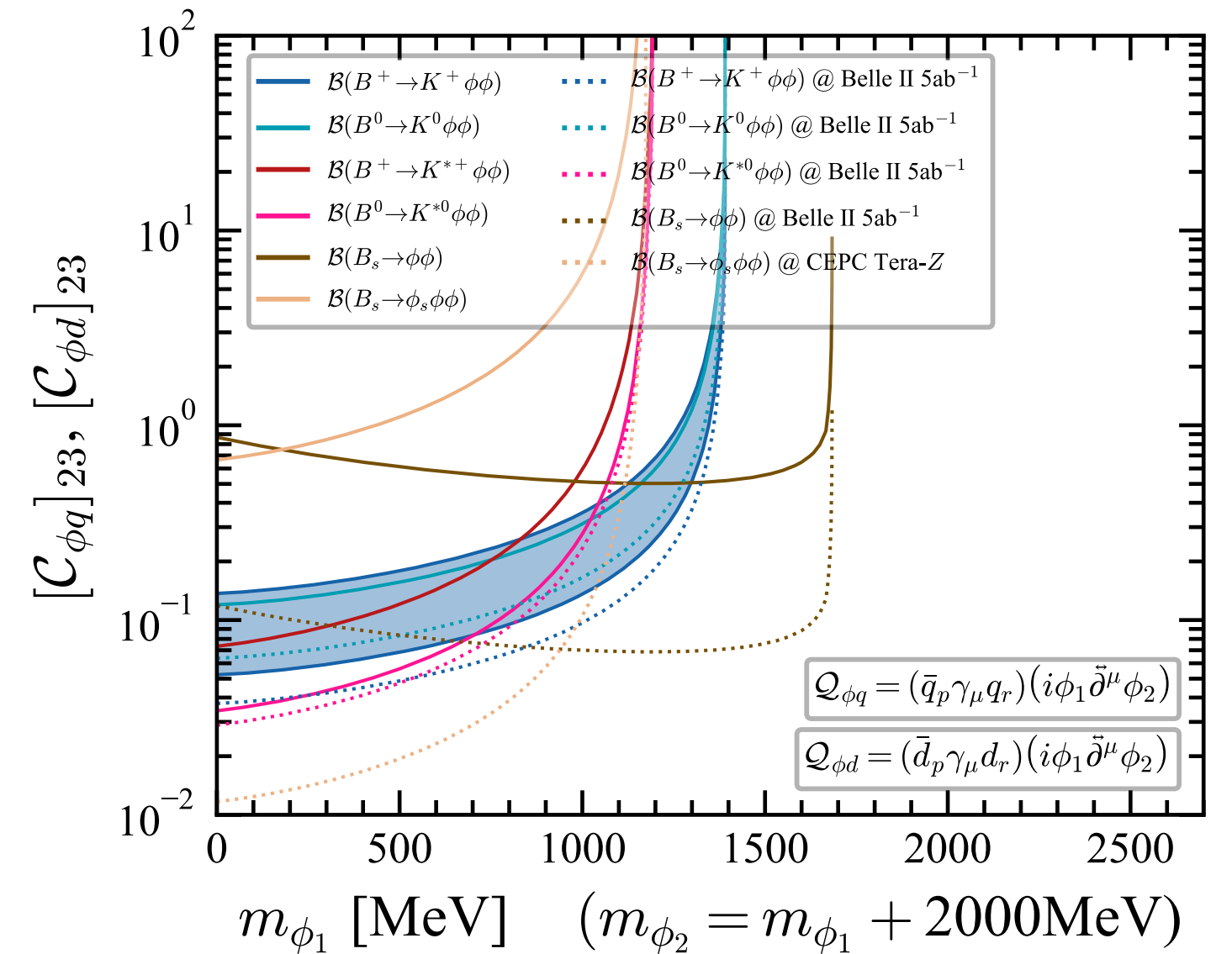
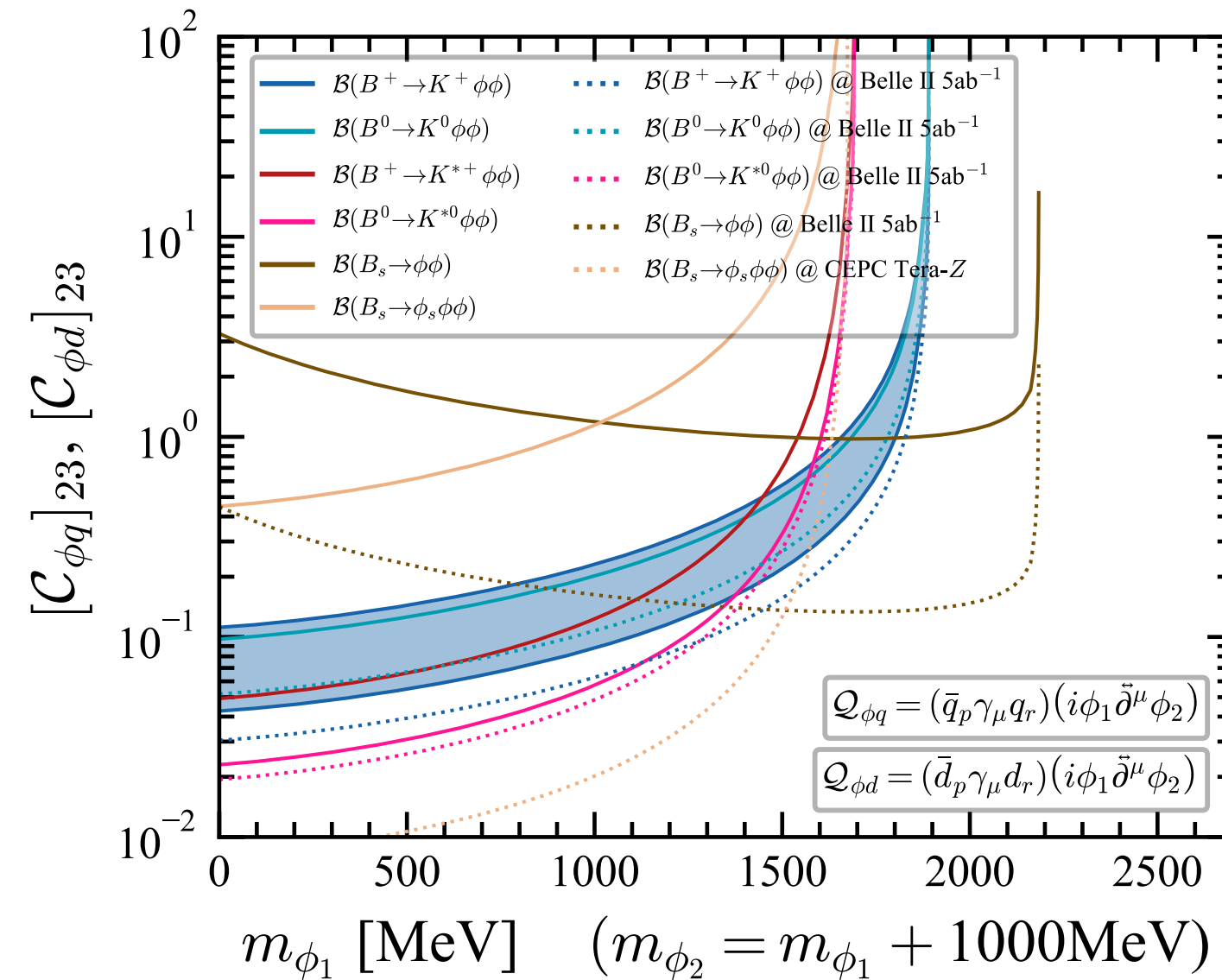
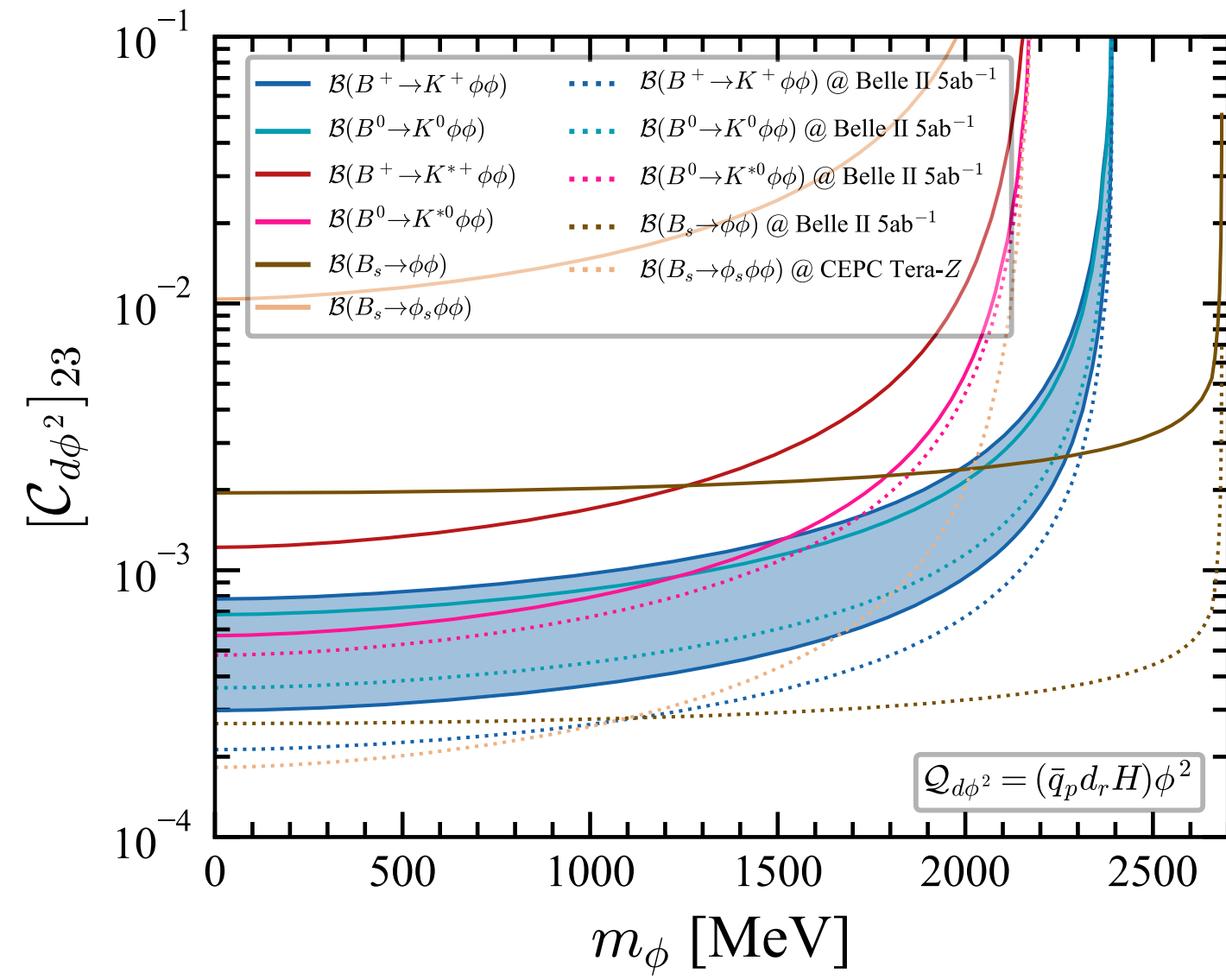
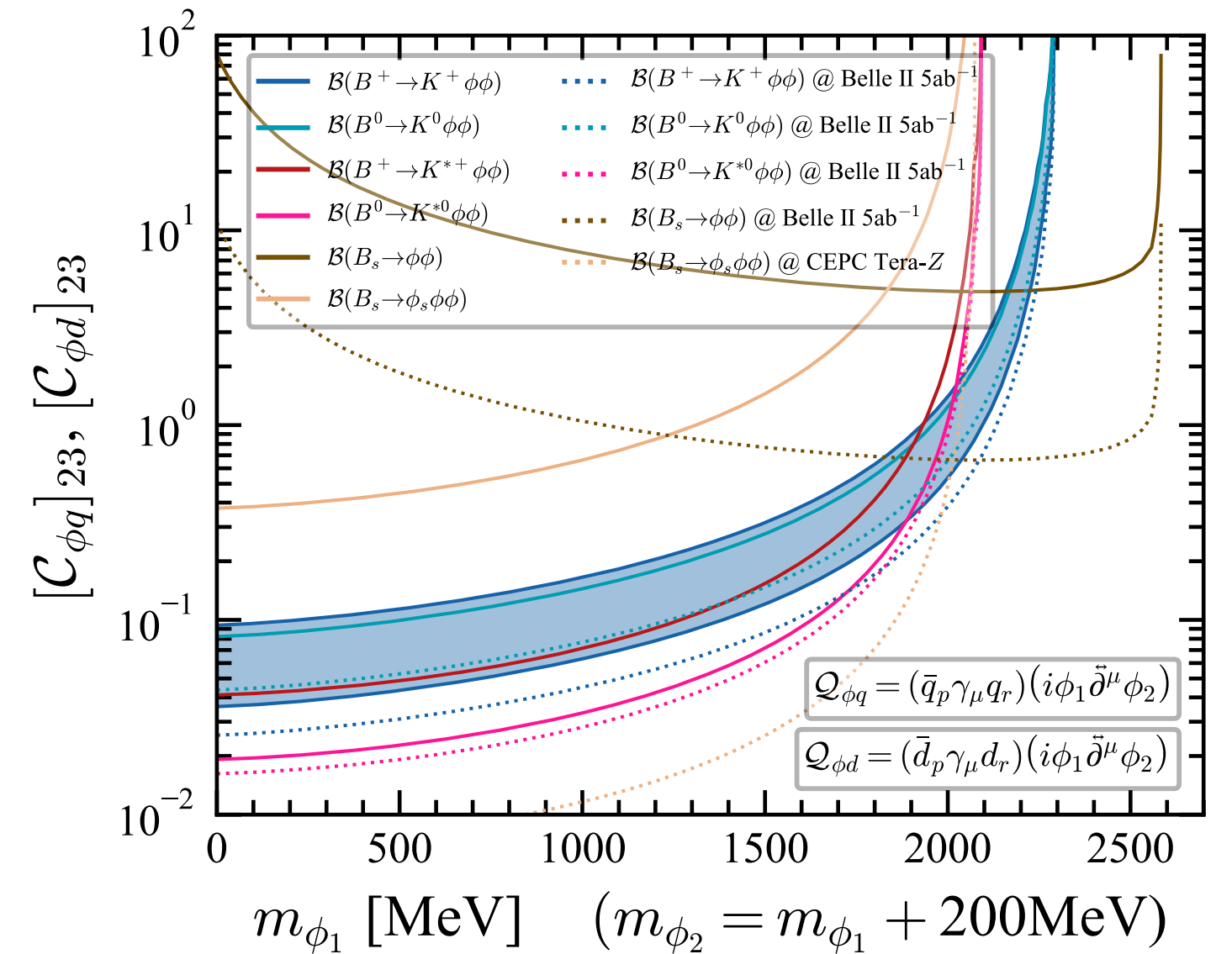
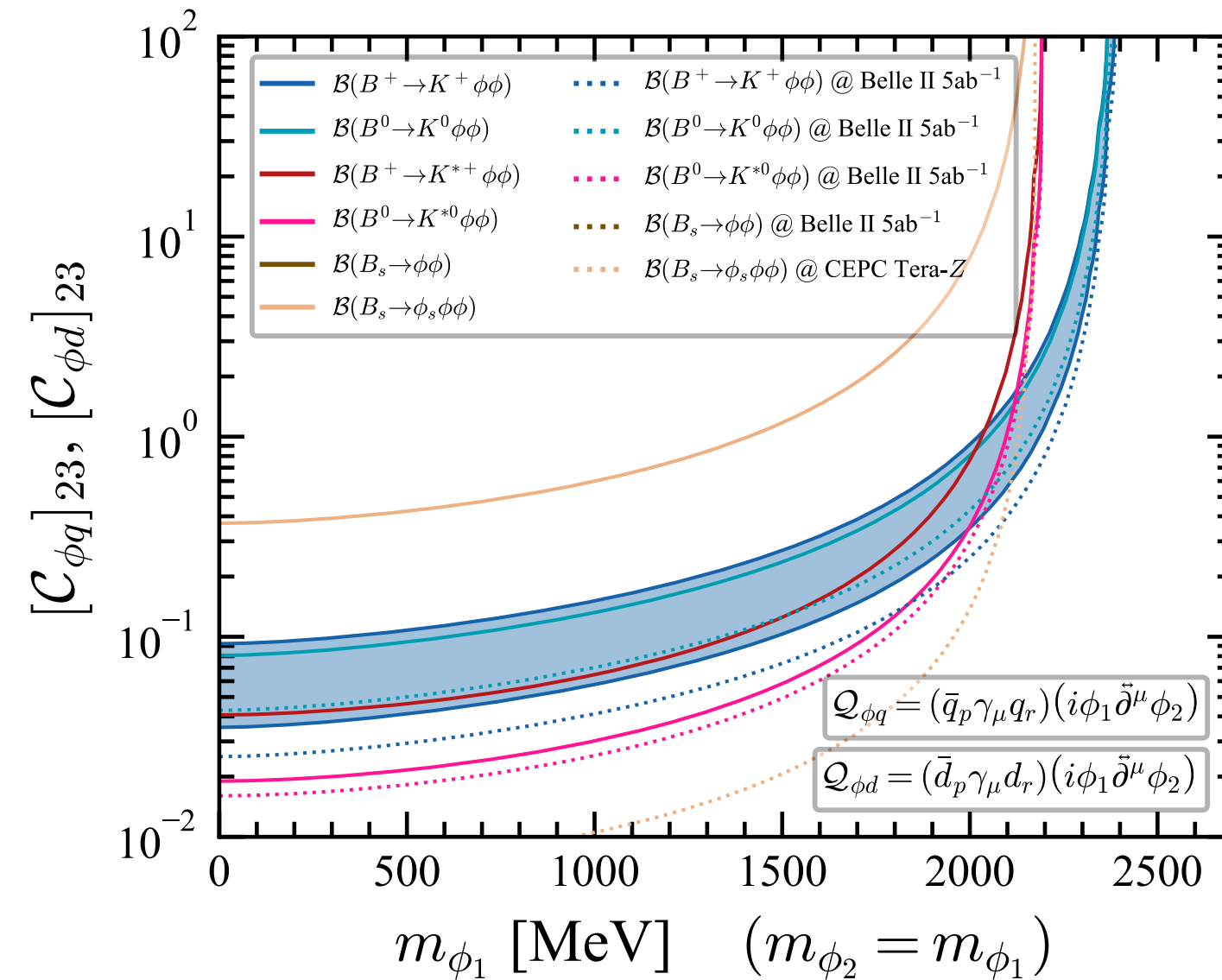
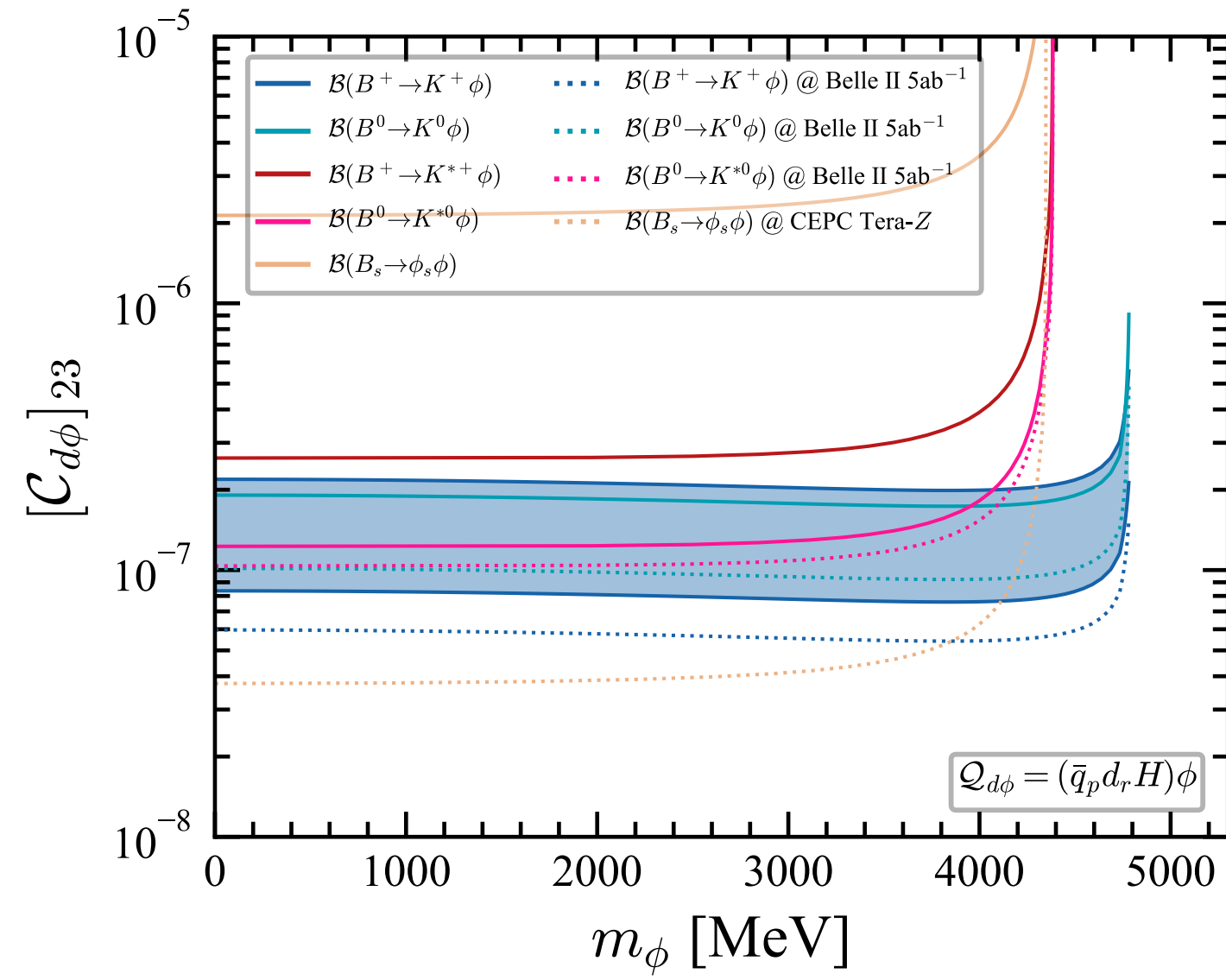
scalar: 4

fermion: 5

vector: 1+10

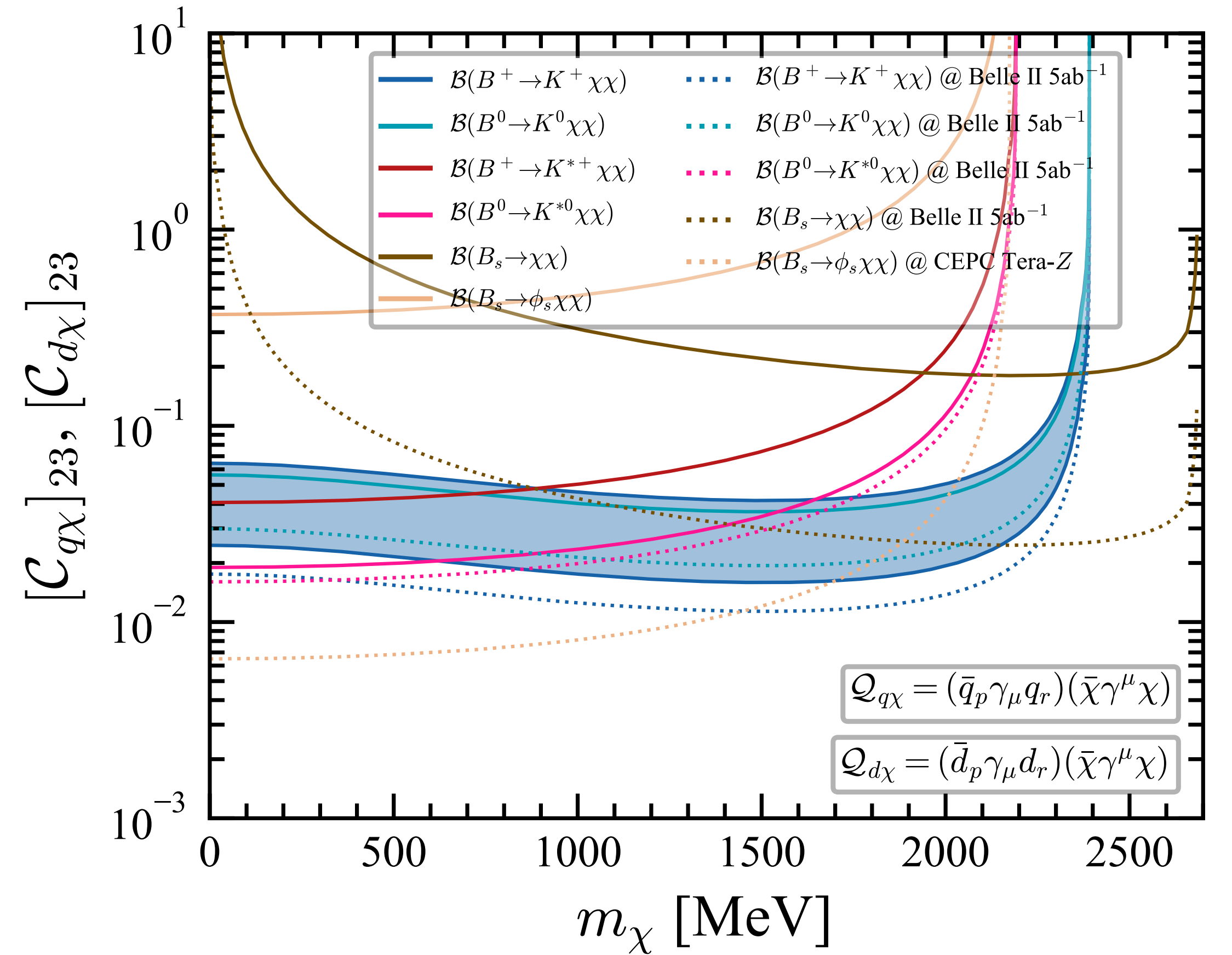
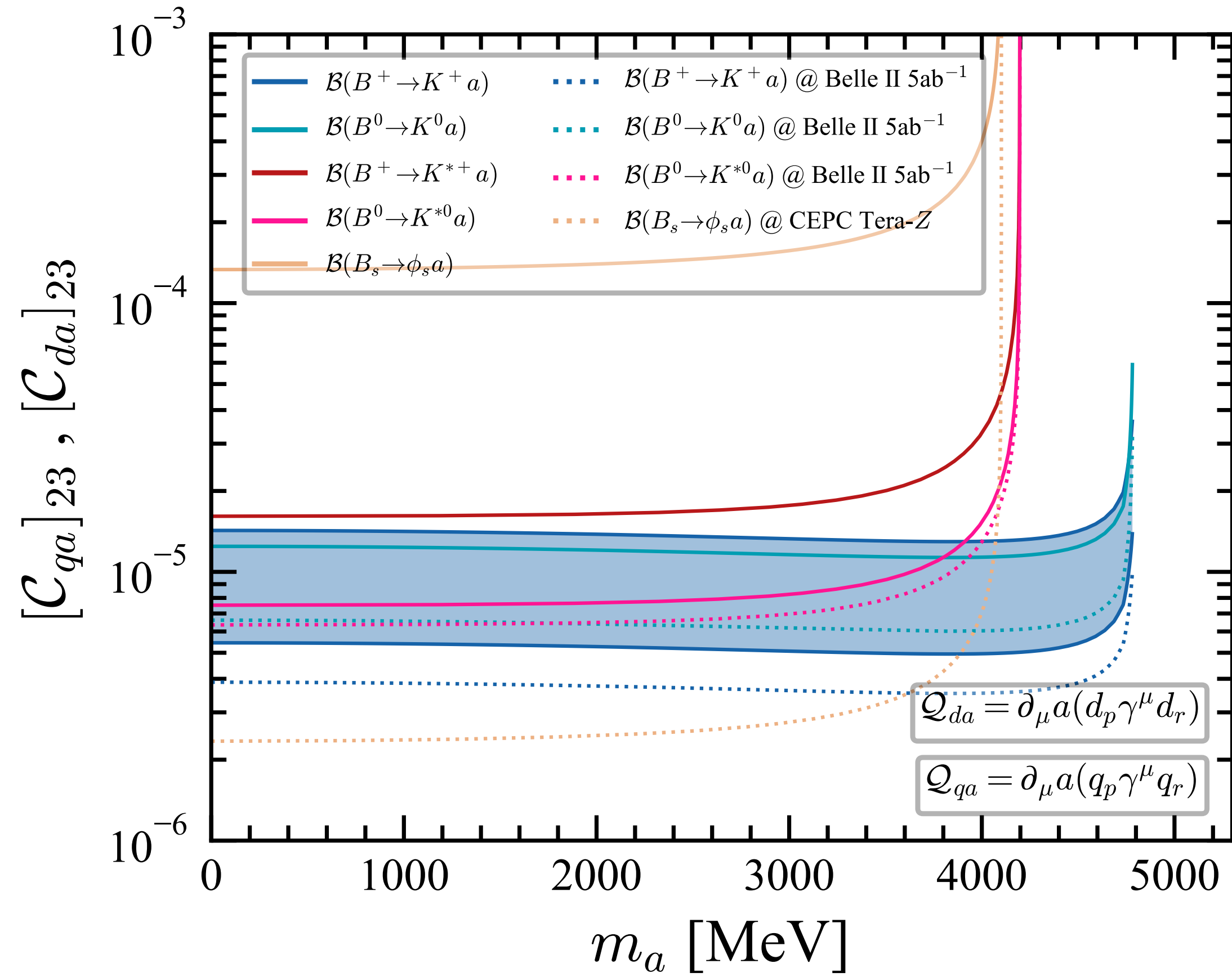
ALP:

# Dark SMEFT: Scalar



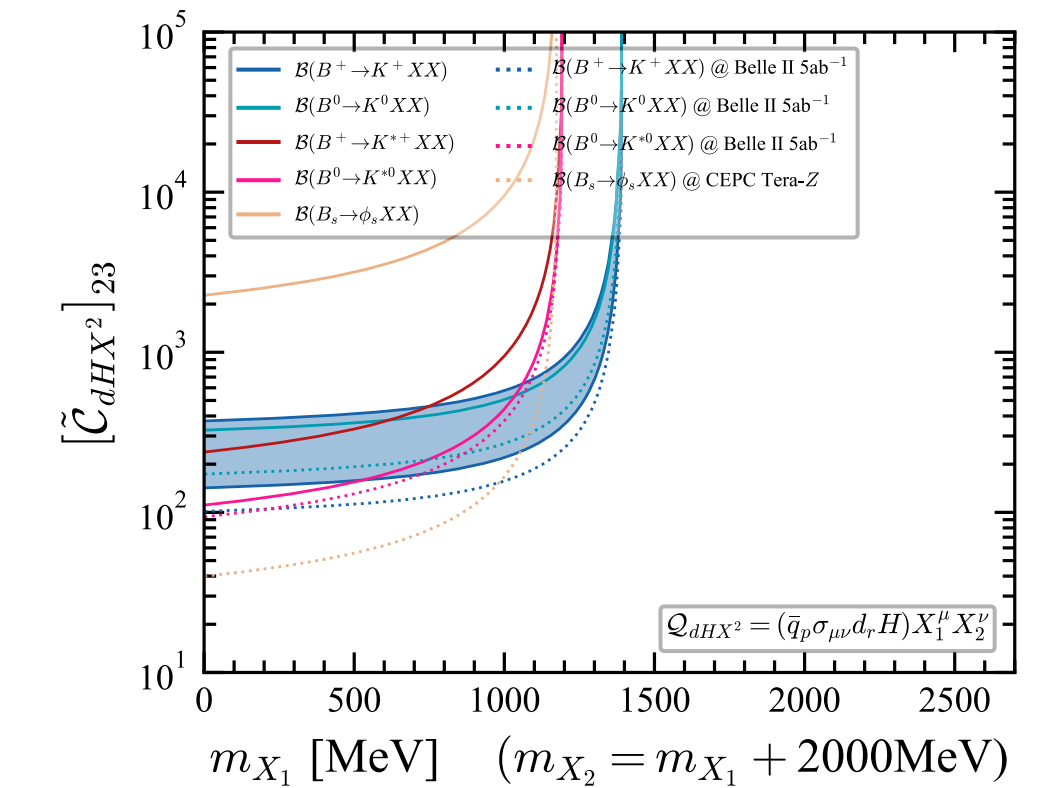
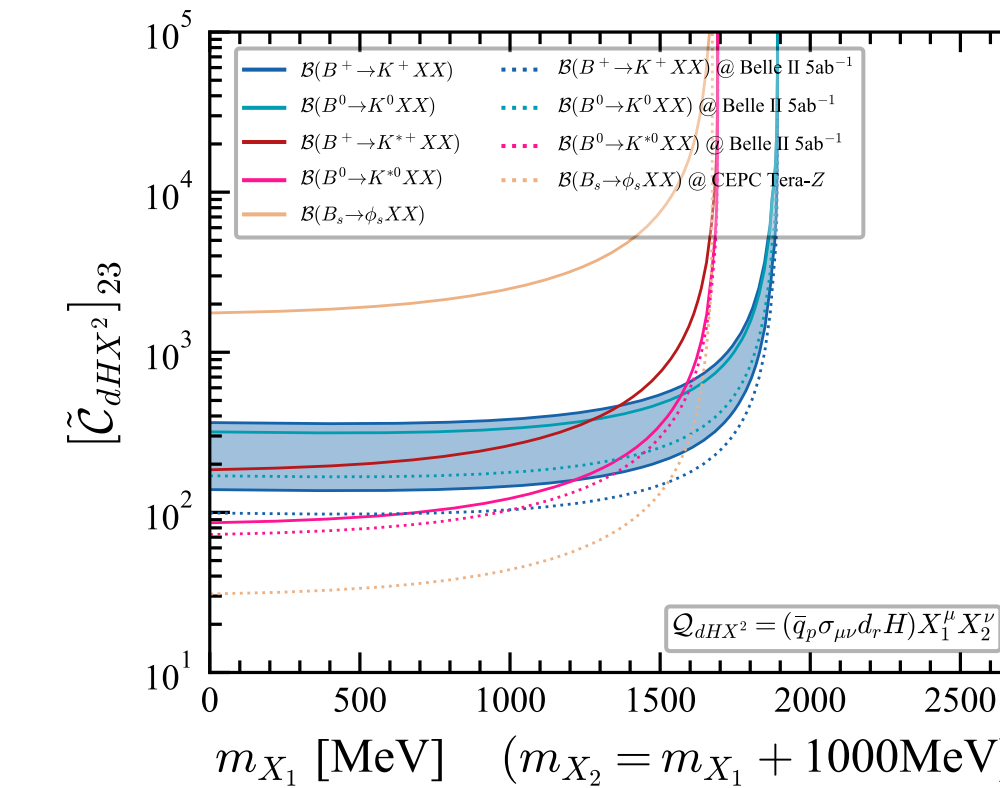
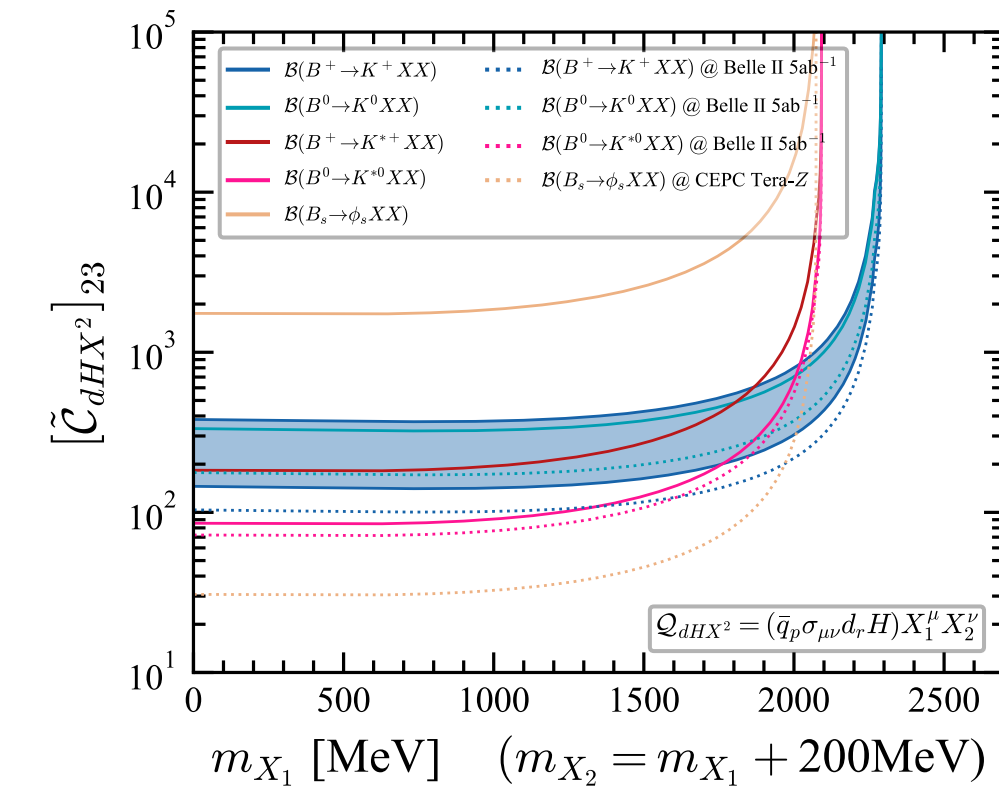
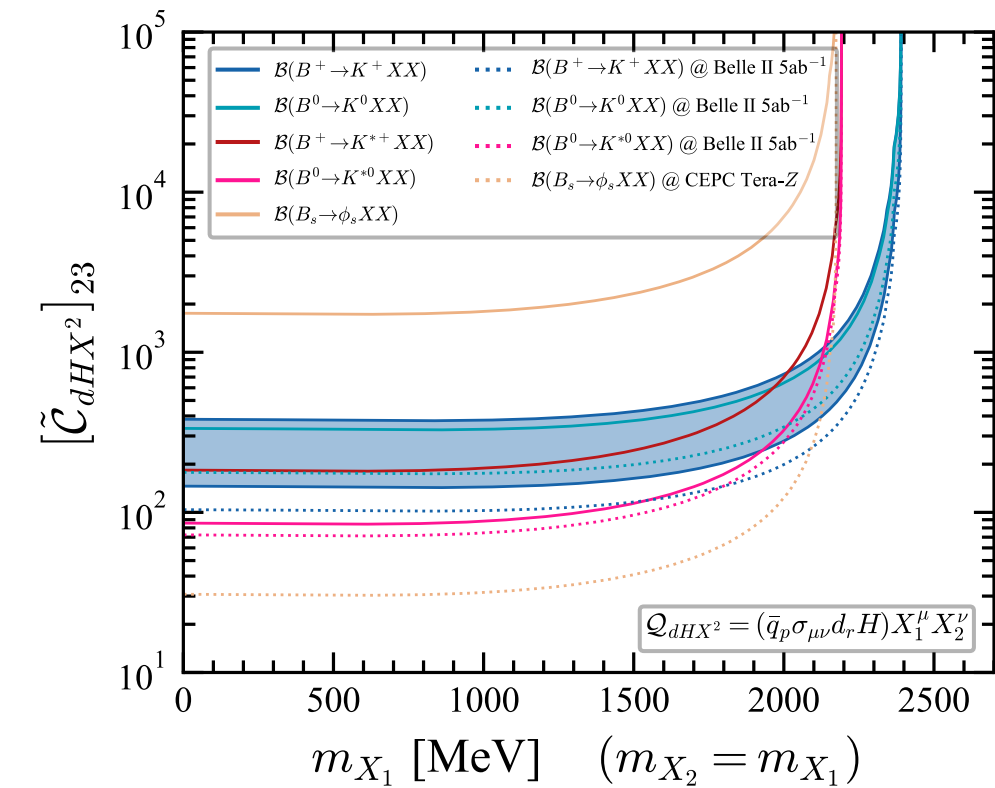
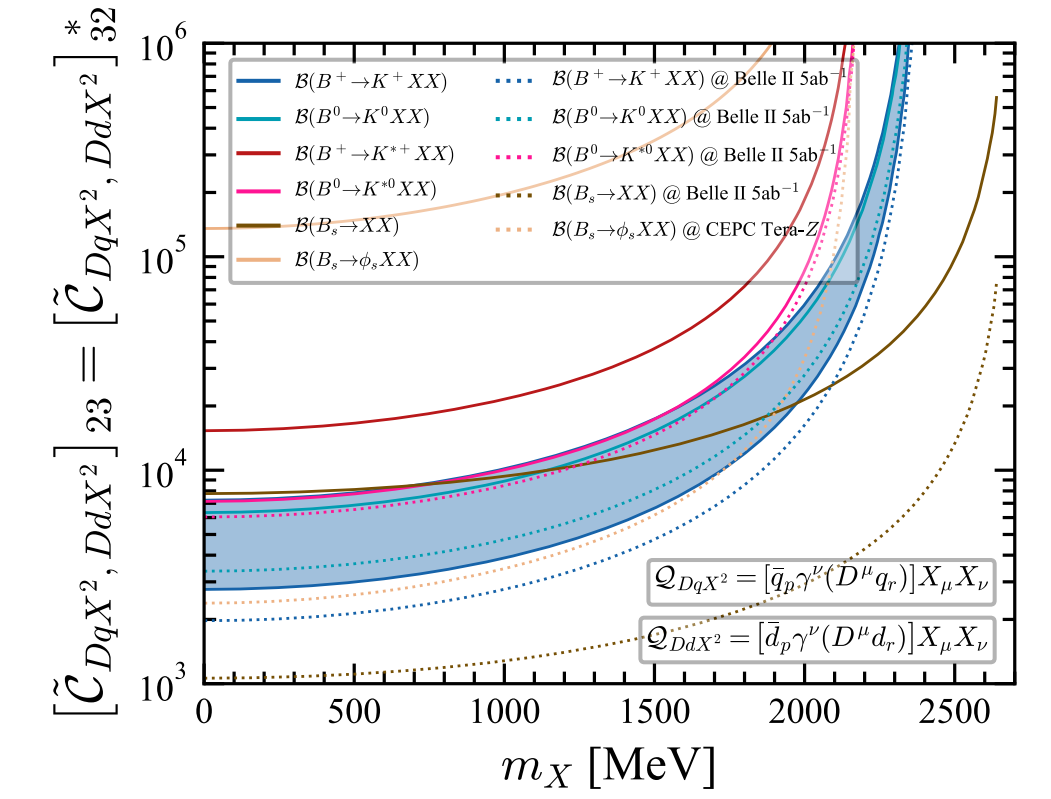
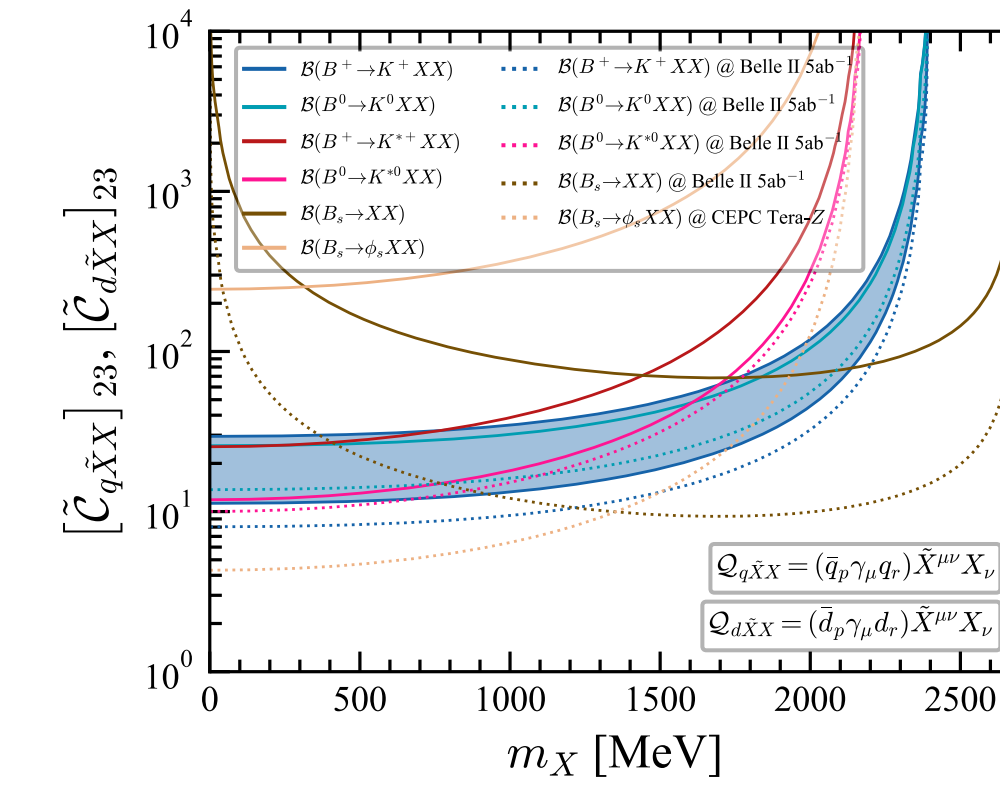
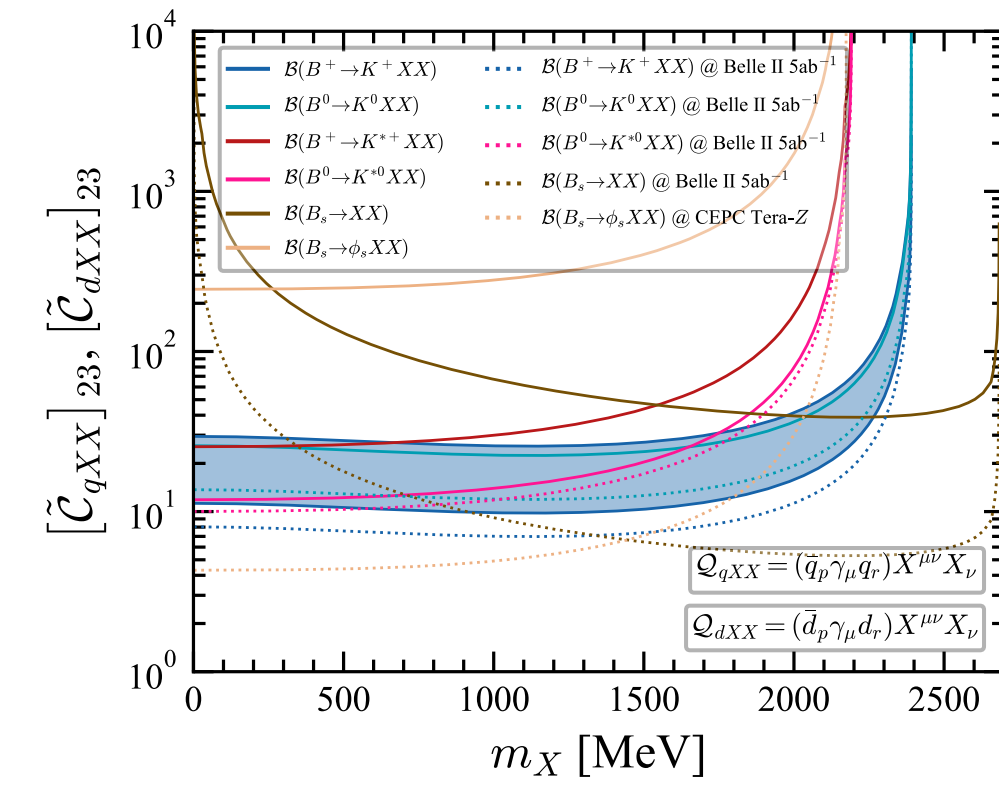
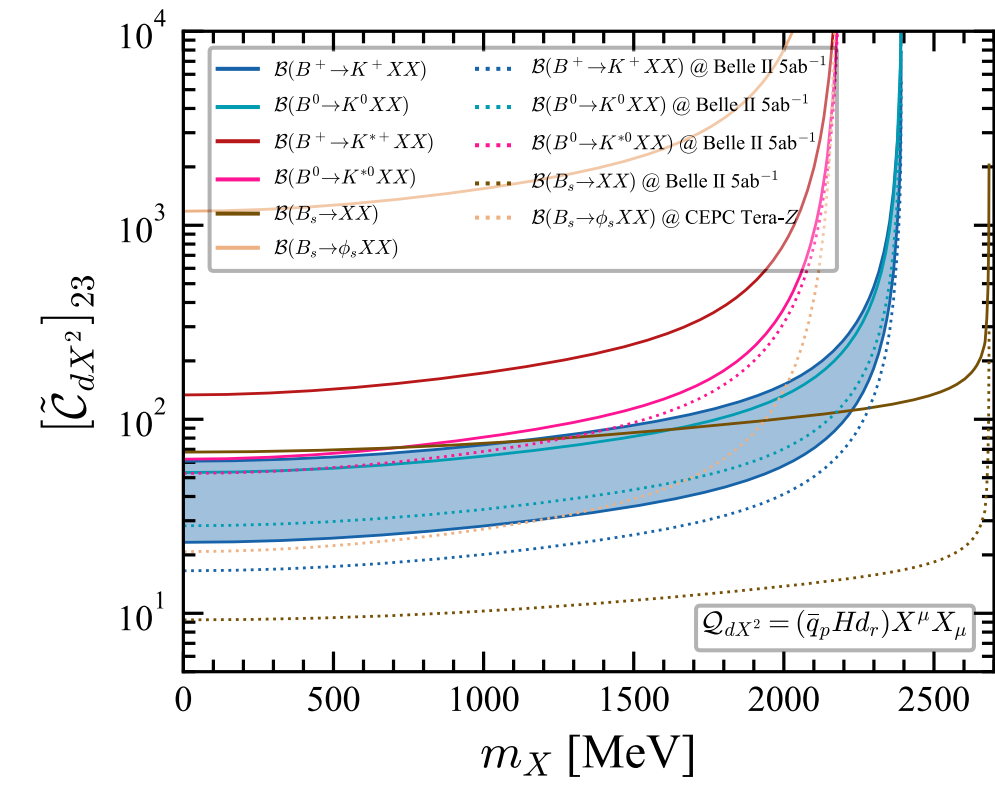
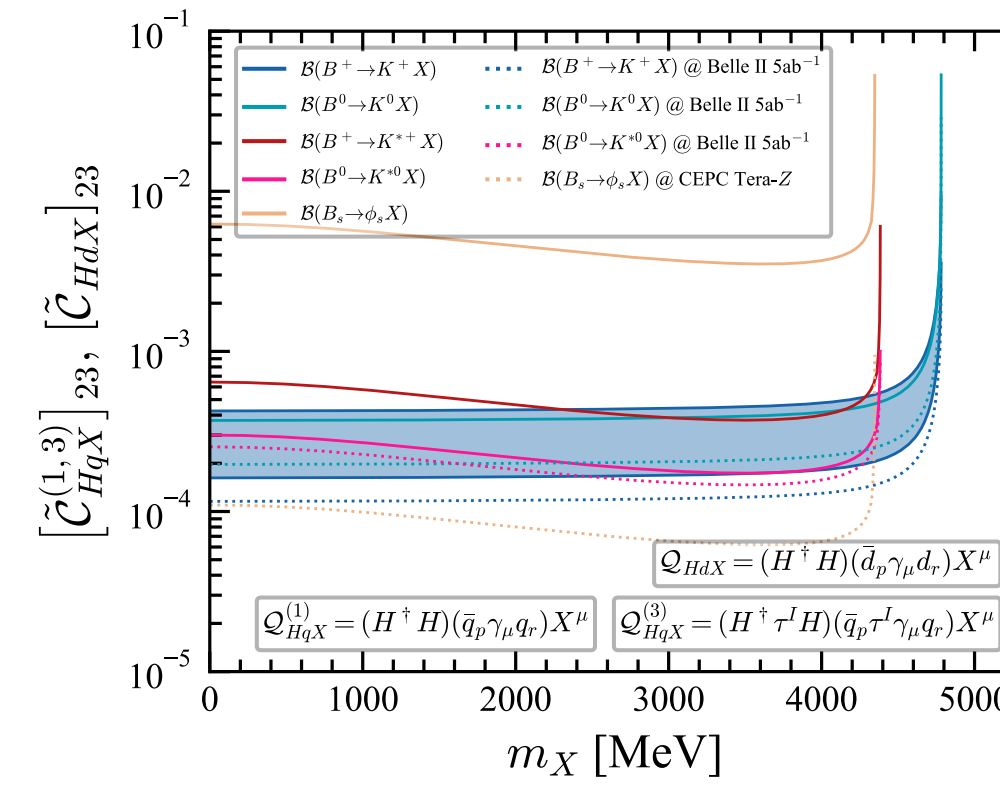
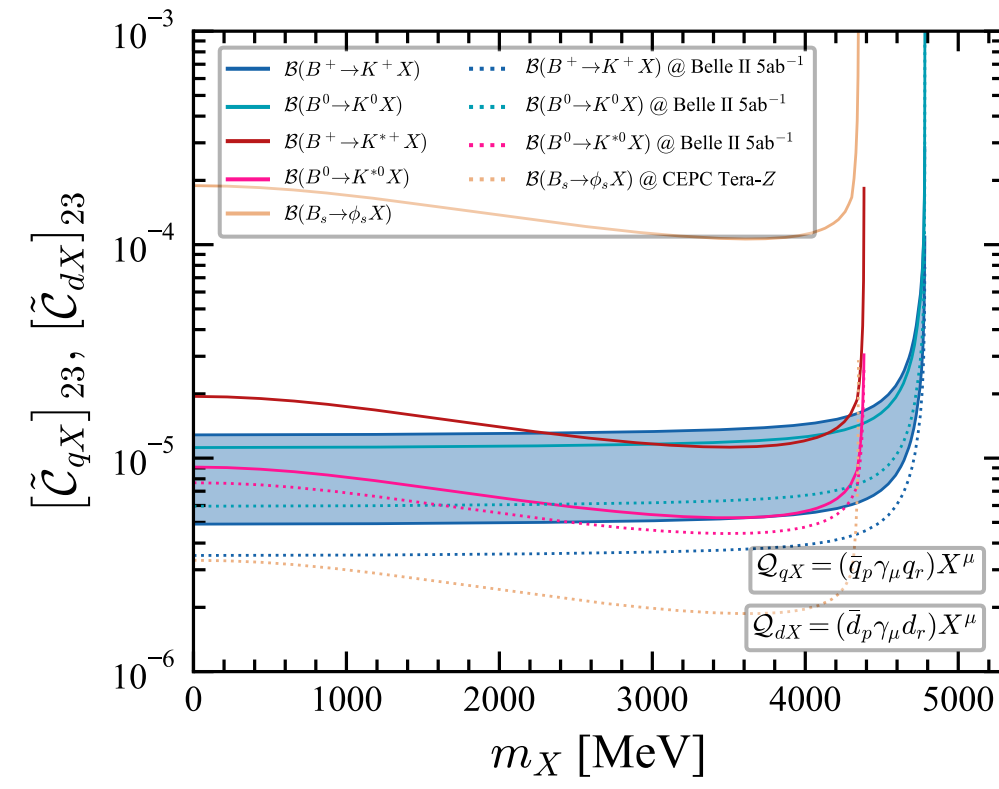
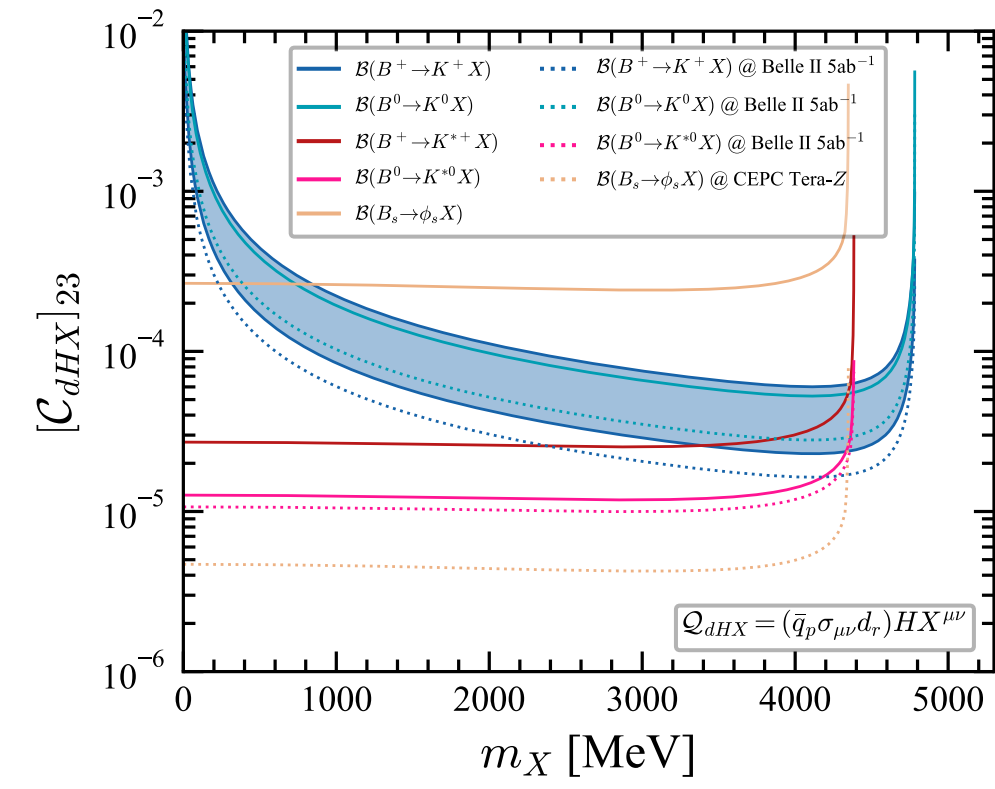
all the operators survive

# Dark SMEFT: Fermion, ALP



all the operators survive

# Dark SMEFT: Vector



all the operators survive



# Dark SMEFT with MFV

- ▶ MFV coupling  $b \rightarrow s, b \rightarrow d, s \rightarrow d$  are connected with each other.

$$c_i^{\text{MFV}} = \begin{cases} \epsilon_0^i \hat{\lambda}_d + \epsilon_1^i \Delta_q \hat{\lambda}_d & \text{for } Q_i = Q_{d\phi}, Q_{d\phi^2}, Q_{dHX}, Q_{dHX^2}, Q_{dX^2}, \\ \epsilon_0^i \mathbb{1} + \epsilon_1^i \Delta_q & \text{for } Q_i = Q_{\phi q}, Q_{q\chi}, Q_{qXX}, Q_{q\tilde{X}X}, Q_{DqX^2}, Q_{qX}, Q_{HqX}^{(1,3)}, Q_{qa}, \\ \epsilon_0^i \mathbb{1} & \text{for } Q_i = Q_{\phi d}, Q_{d\chi}, Q_{dXX}, Q_{d\tilde{X}X}, Q_{DdX^2}, Q_{dX}, Q_{HdX}, Q_{da}, \end{cases}$$

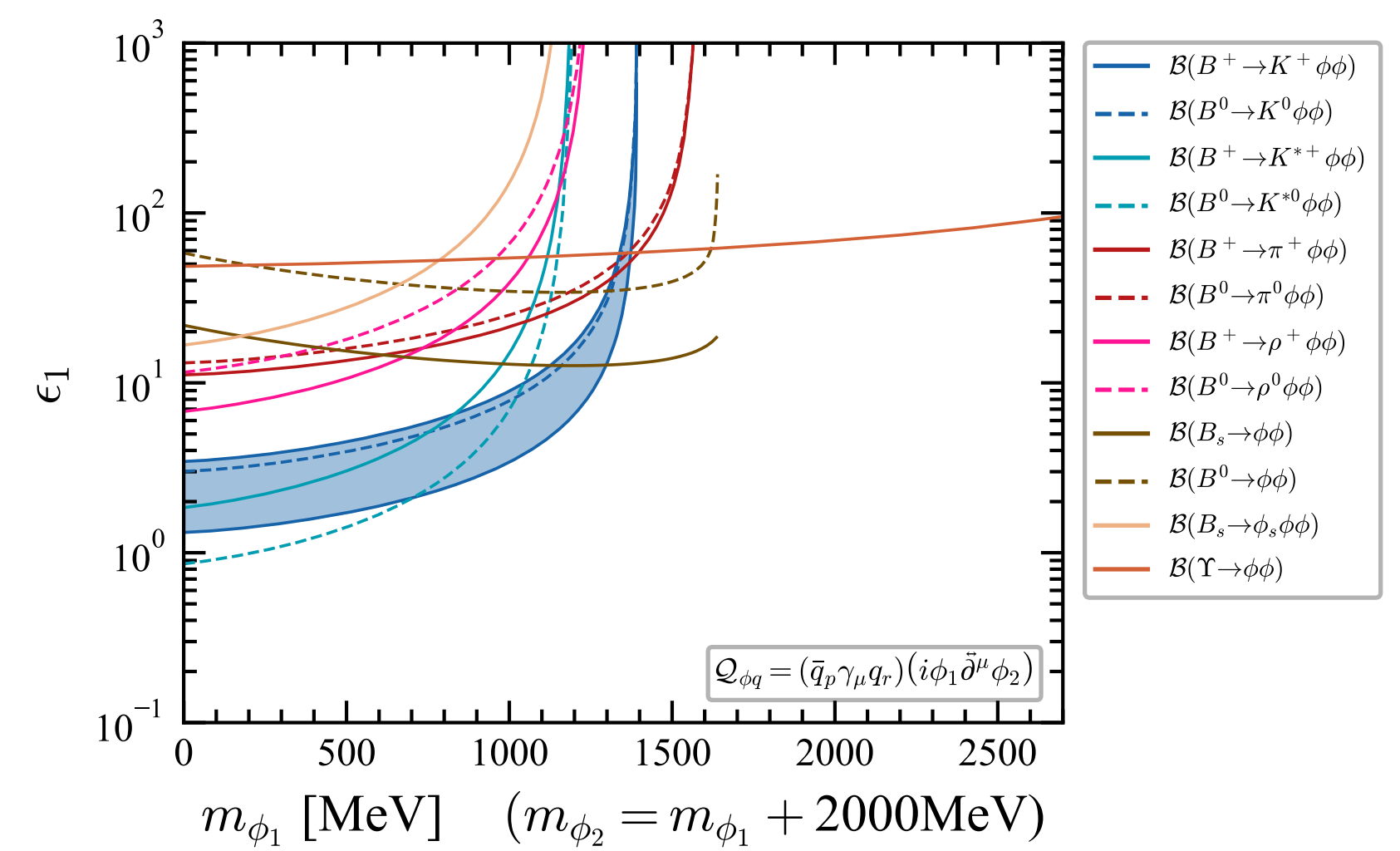
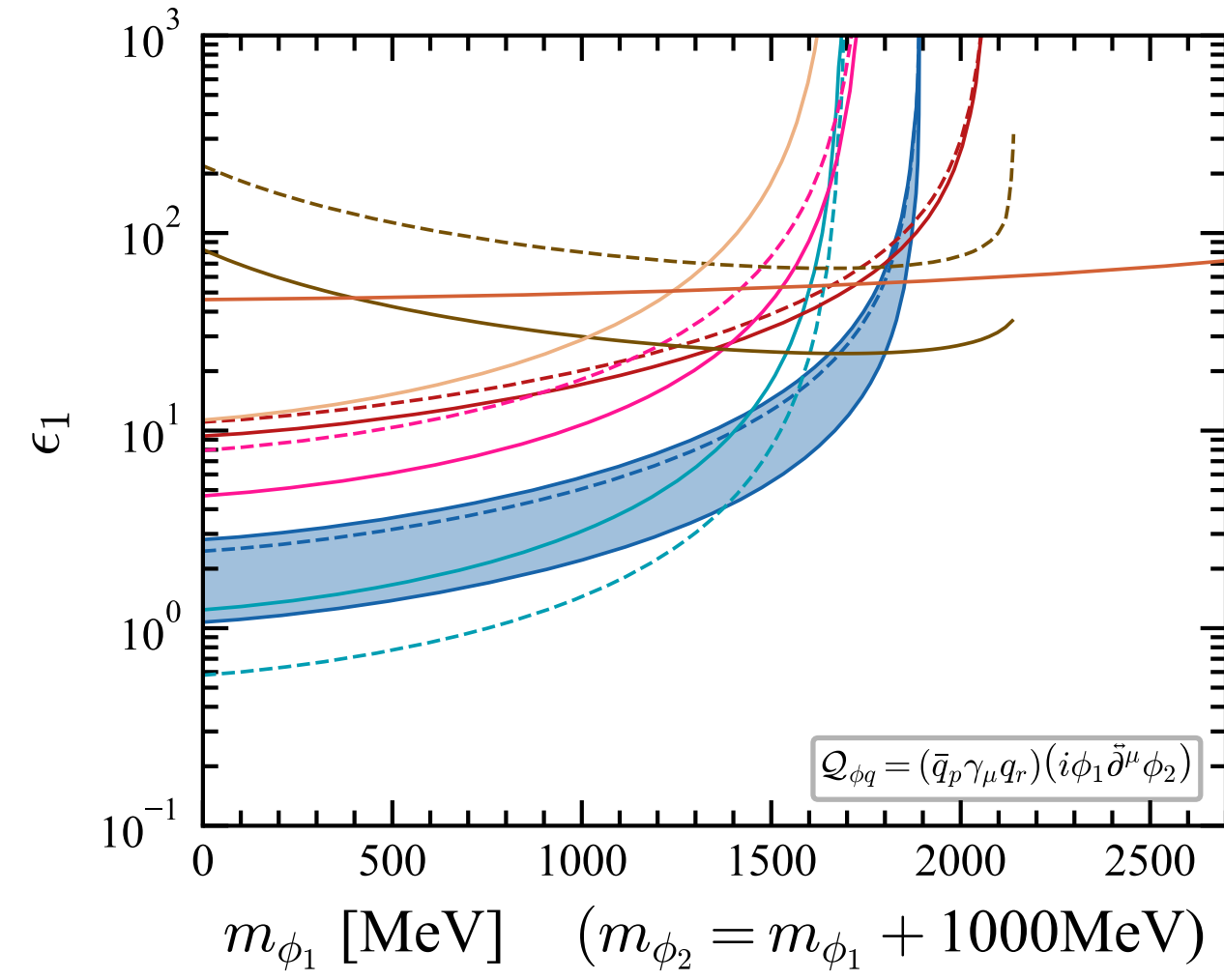
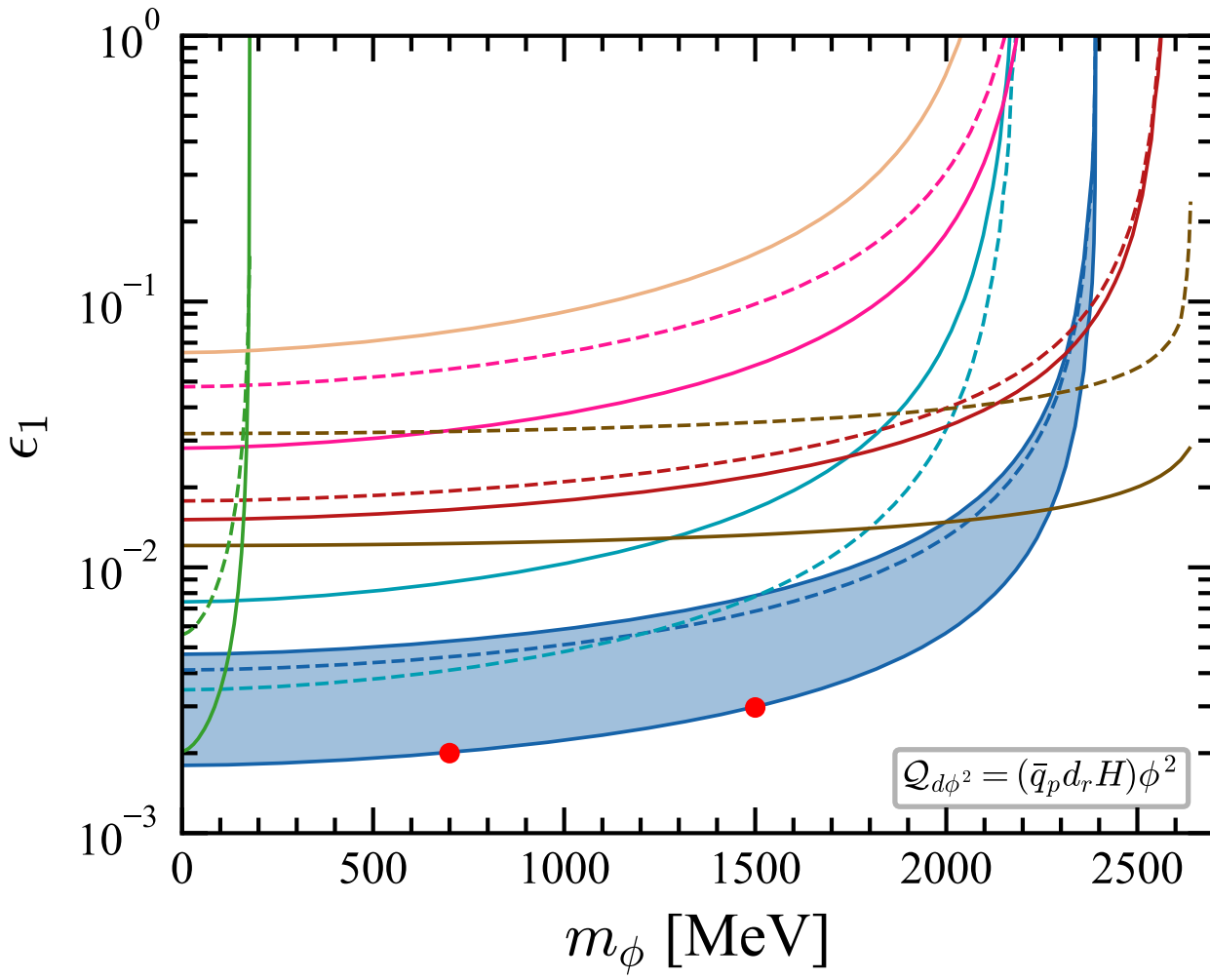
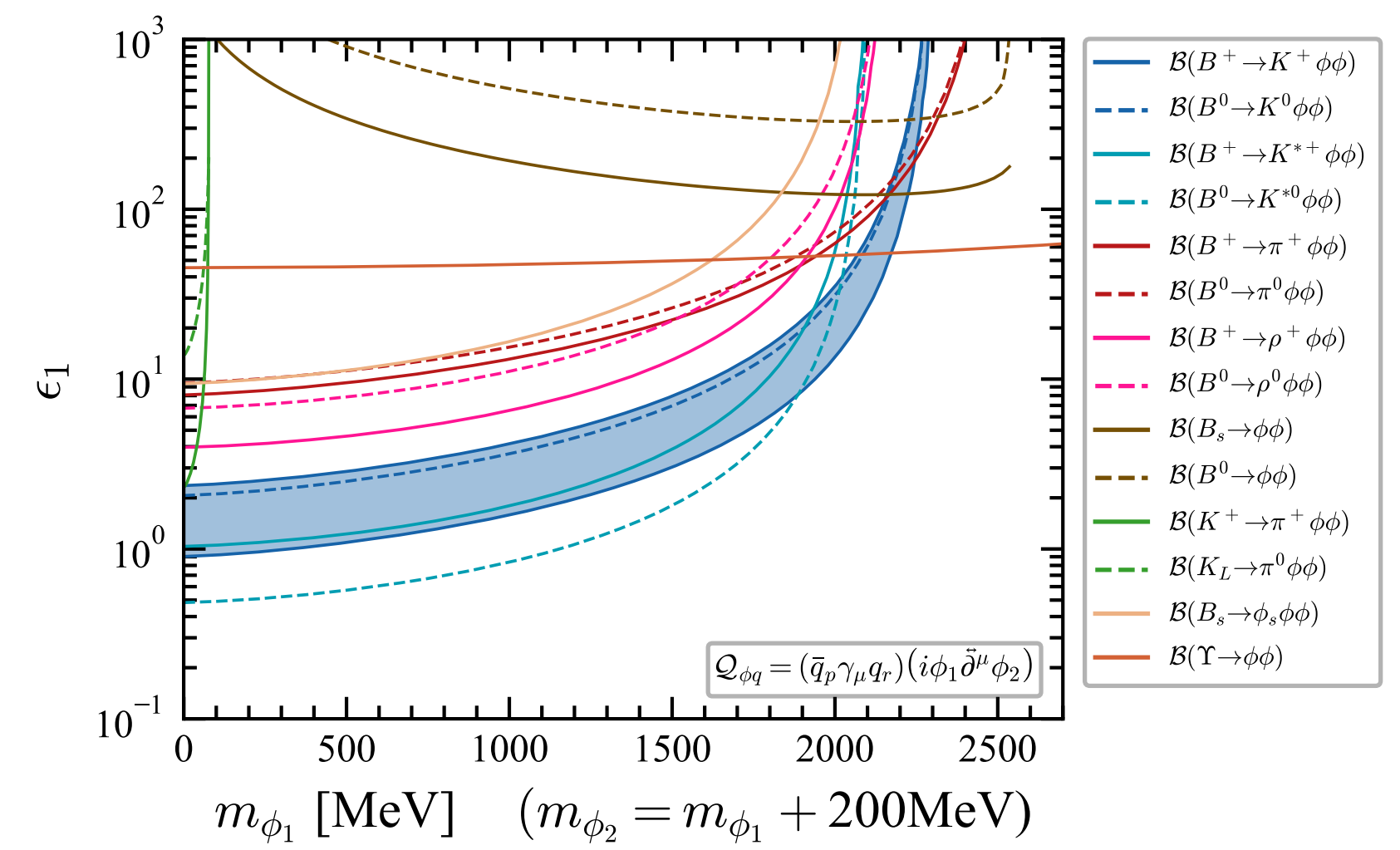
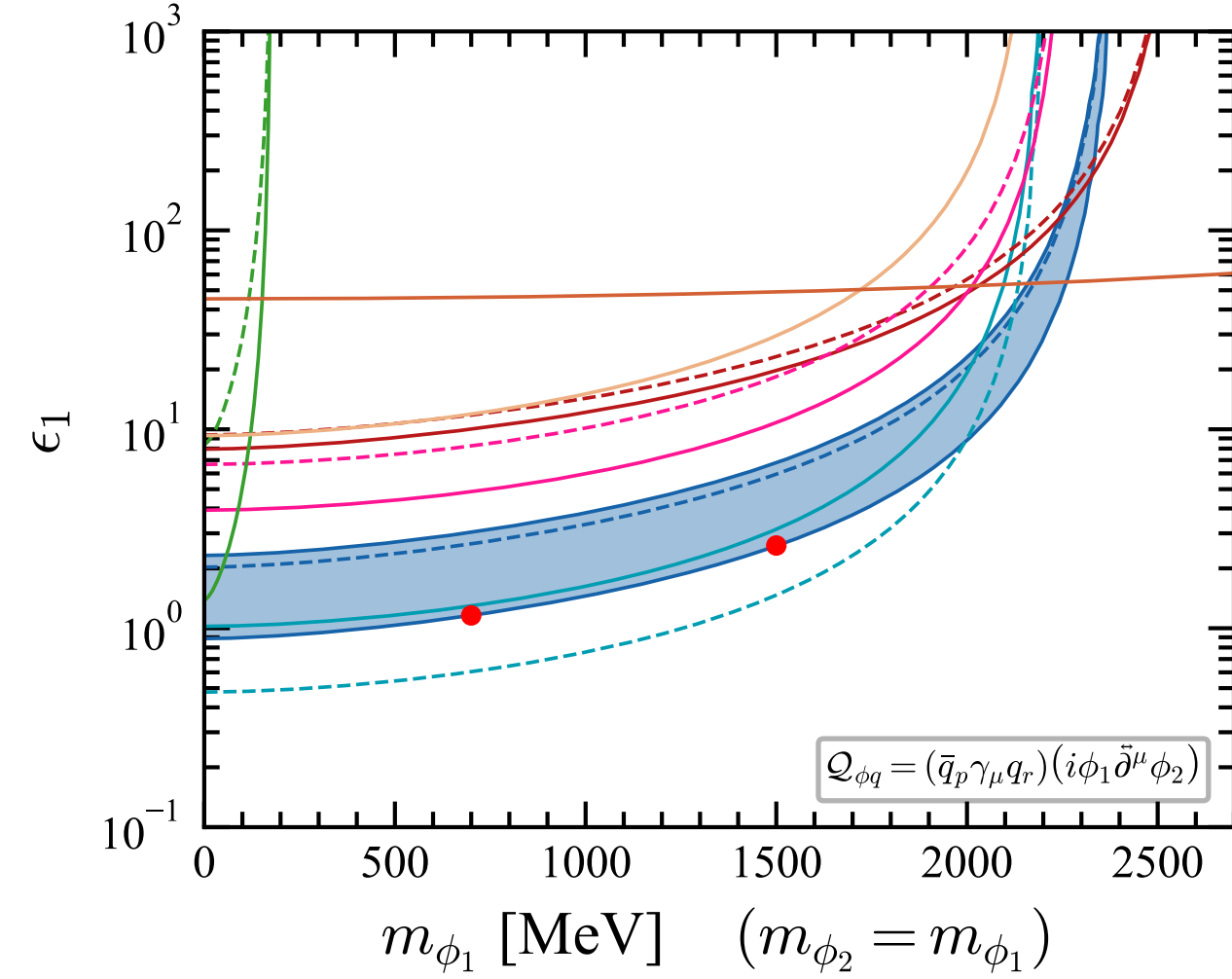
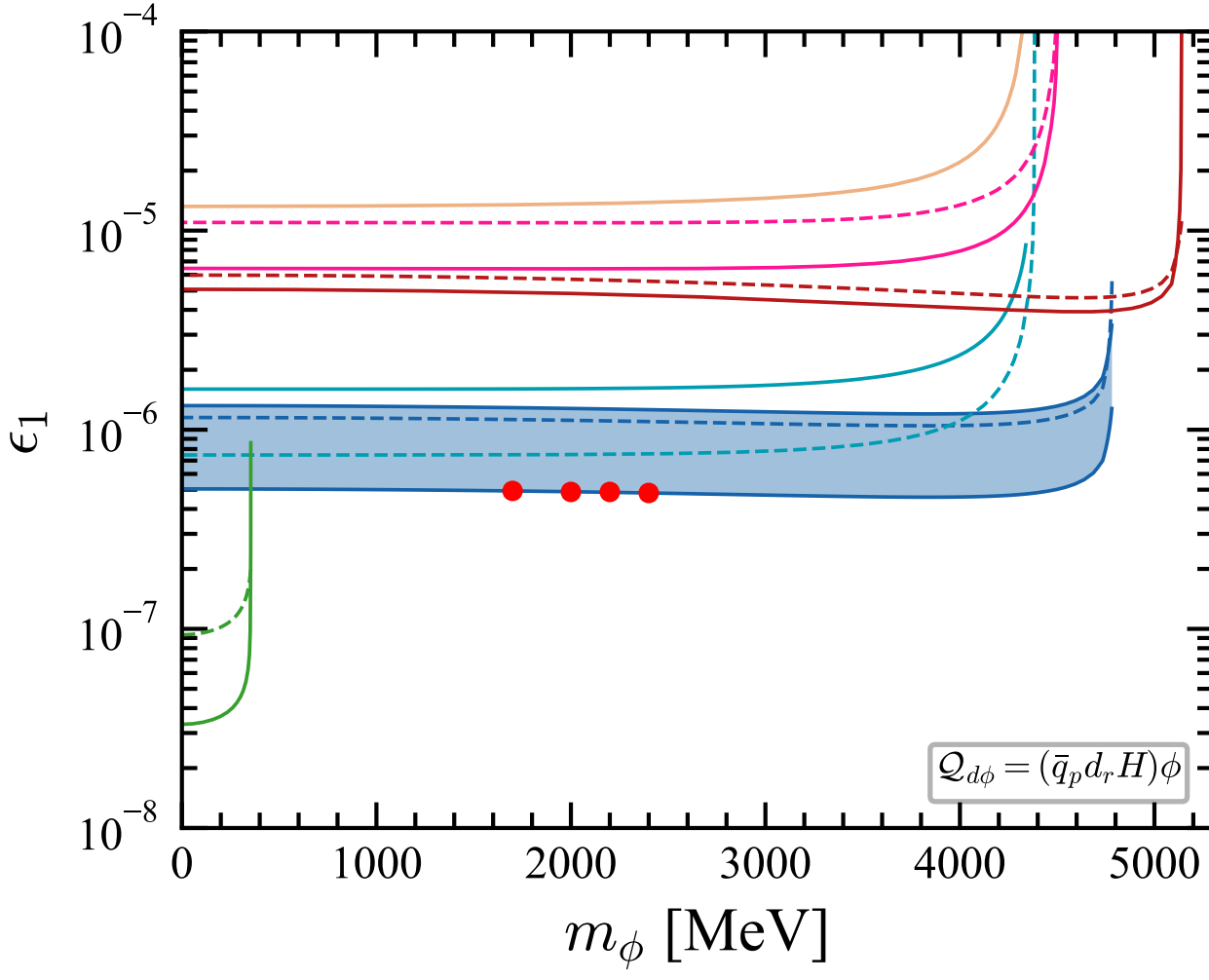
**8 operators are eliminated**

- ▶ Numerics

$$\Delta_q = \begin{pmatrix} 0.8 & -3.3 - 1.5i & 79.3 + 35.4i \\ -3.3 + 1.5i & 16.6 & -397.5 + 8.1i \\ 79.3 - 35.4i & -397.5 - 8.1i & 9839.0 \end{pmatrix} \times 10^{-4}$$

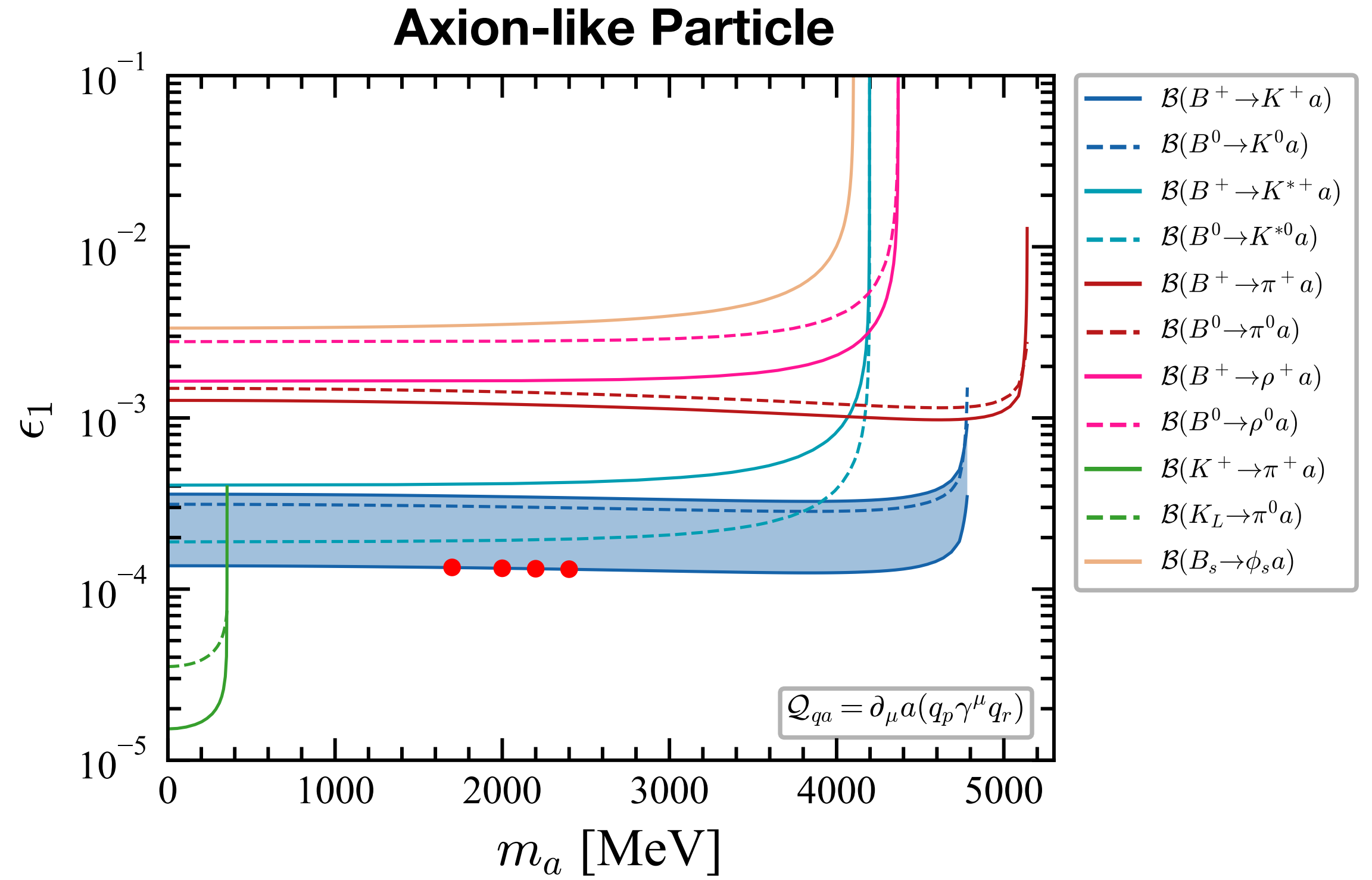
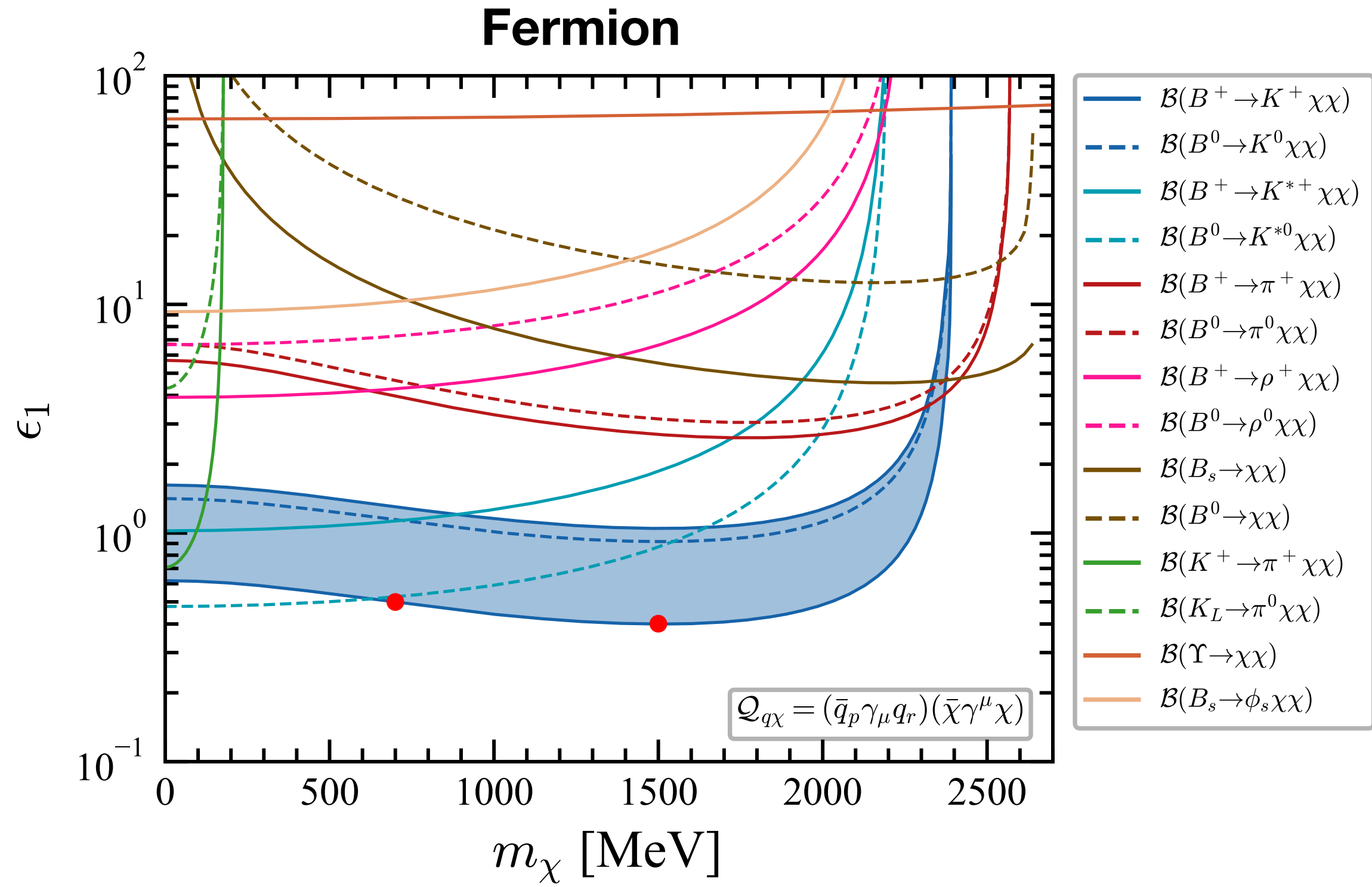
$$\Delta_q \hat{\lambda}_d = \begin{pmatrix} 0.0021 & -0.18 - 0.08i & 191.3 + 85.4i \\ -0.009 + 0.004i & 0.88 & -958.7 + 19.6i \\ 0.21 - 0.10i & -21.1 - 0.4i & 23728.1 \end{pmatrix} \times 10^{-6}$$

# Dark SMEFT with MFV: Scalar, ALP



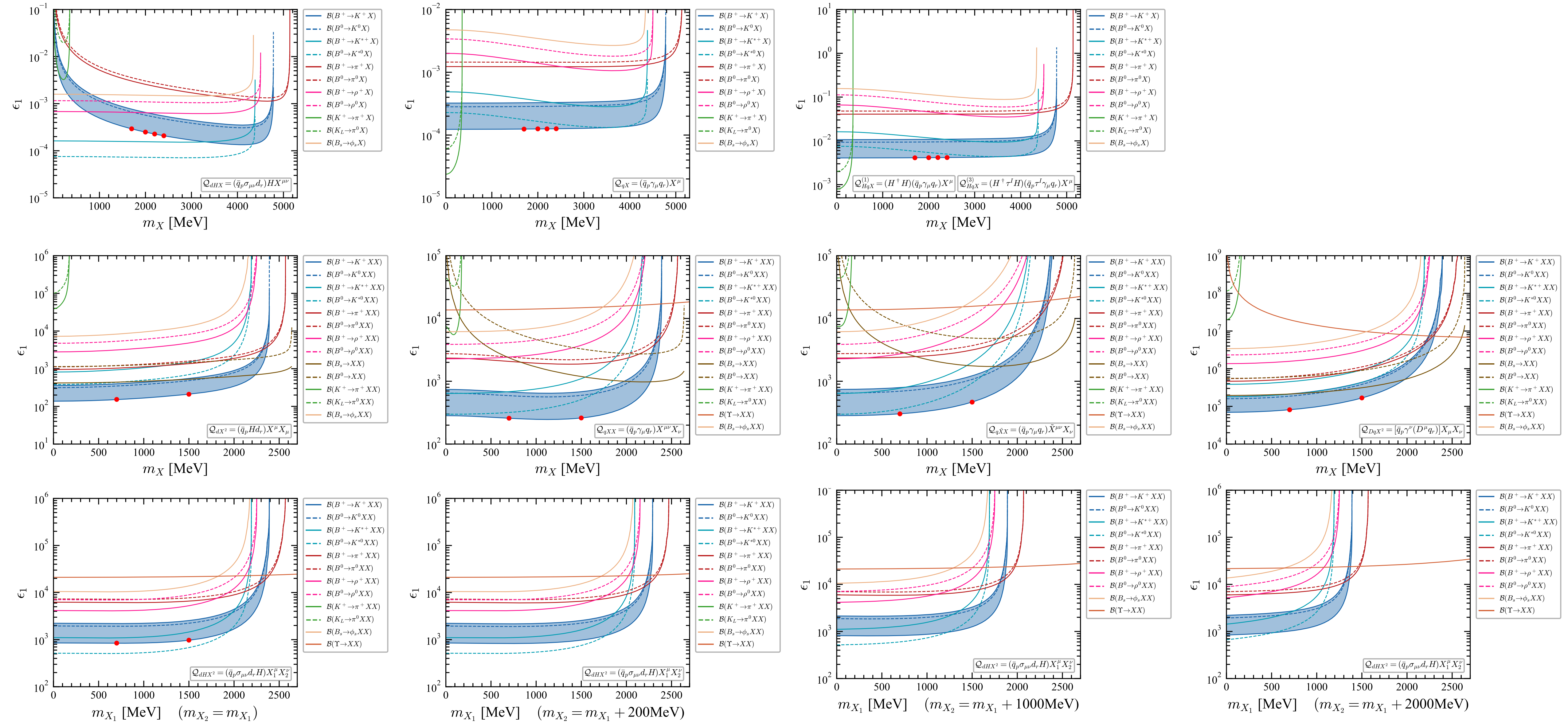
all the operators survive

# Dark SMEFT with MFV: Fermion, ALP



all the operators survive

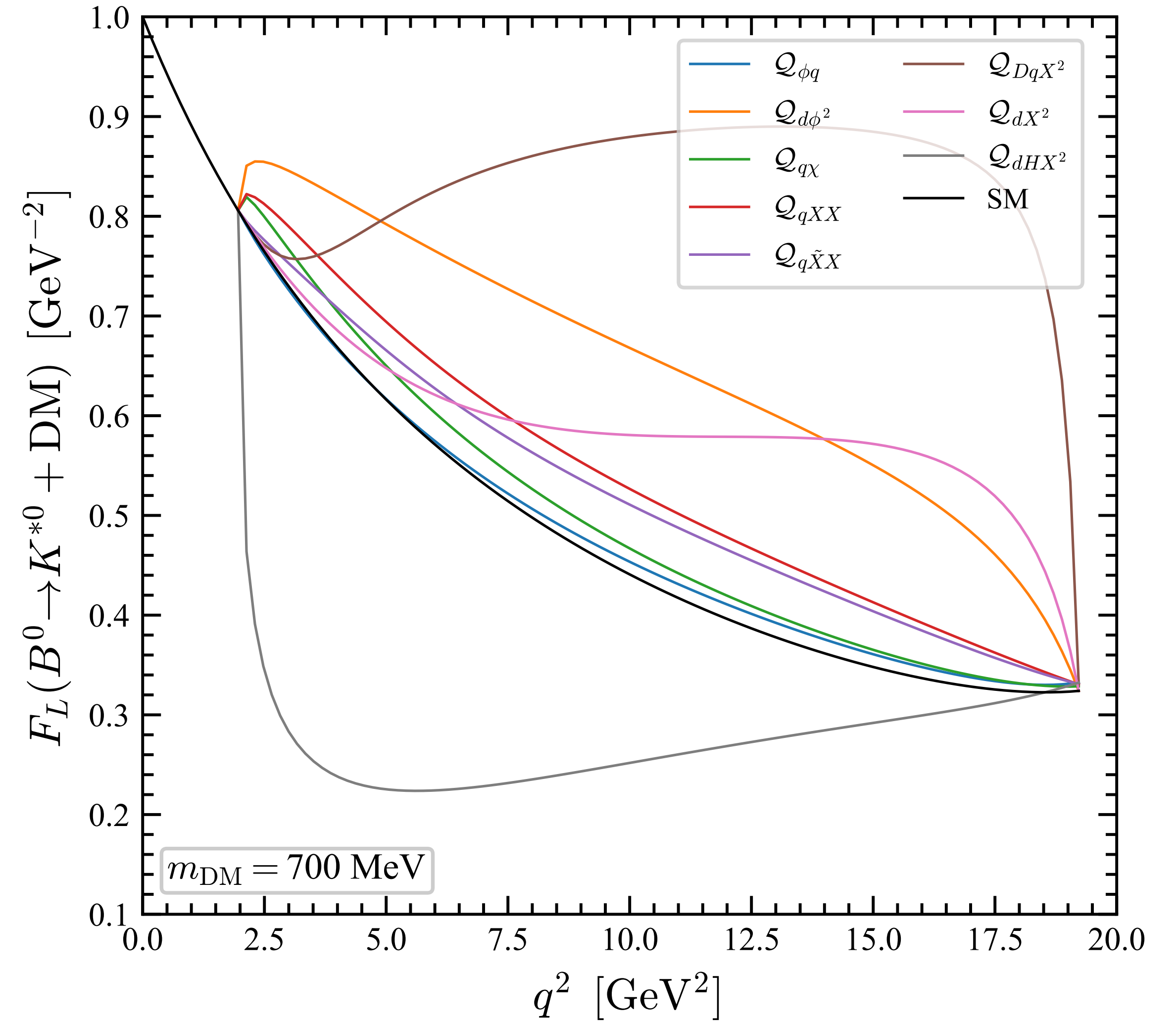
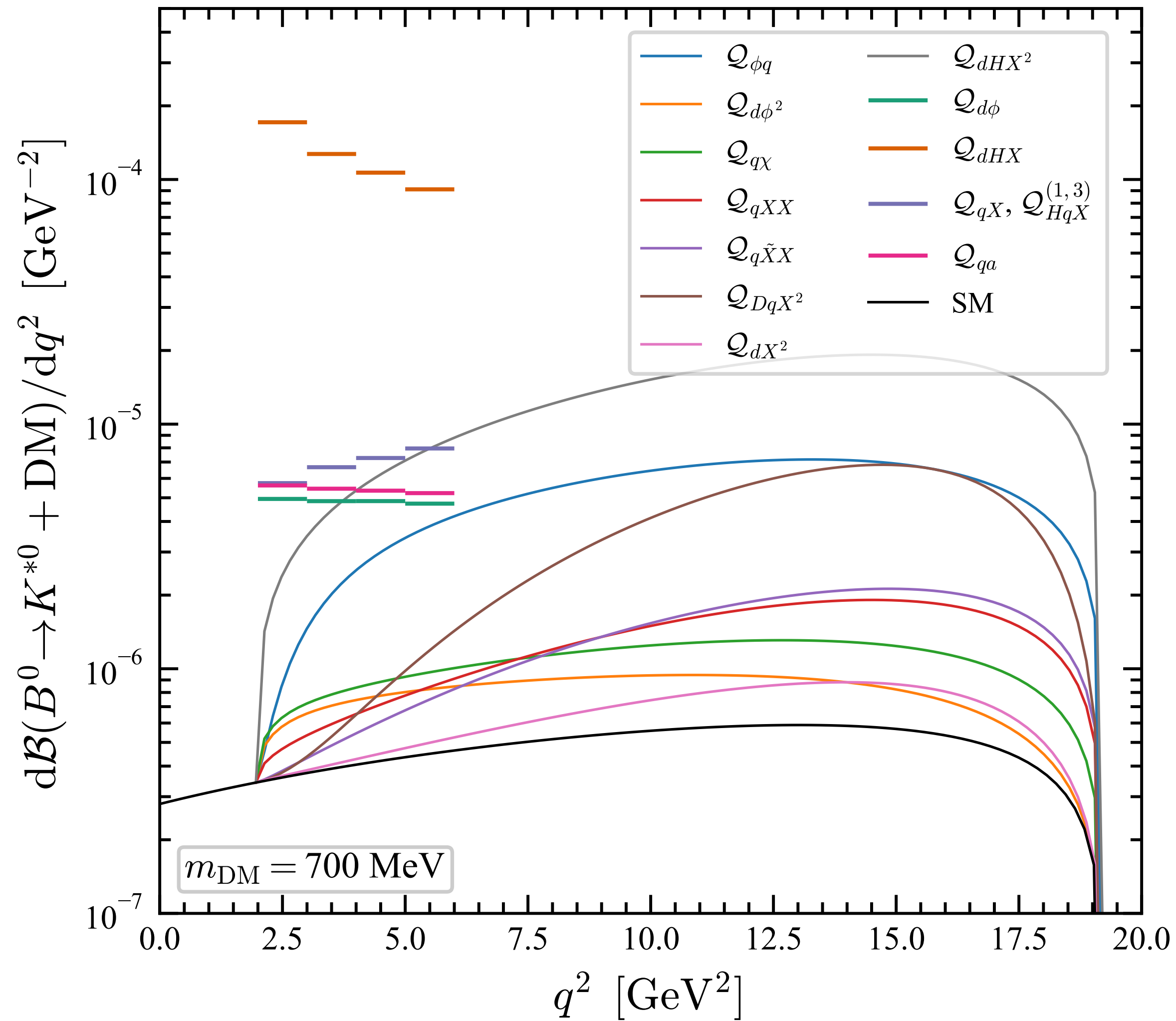
# Dark SMEFT with MFV: Vector



all the operators survive

# Dark SMEFT: $dB/dq^2, F_L$

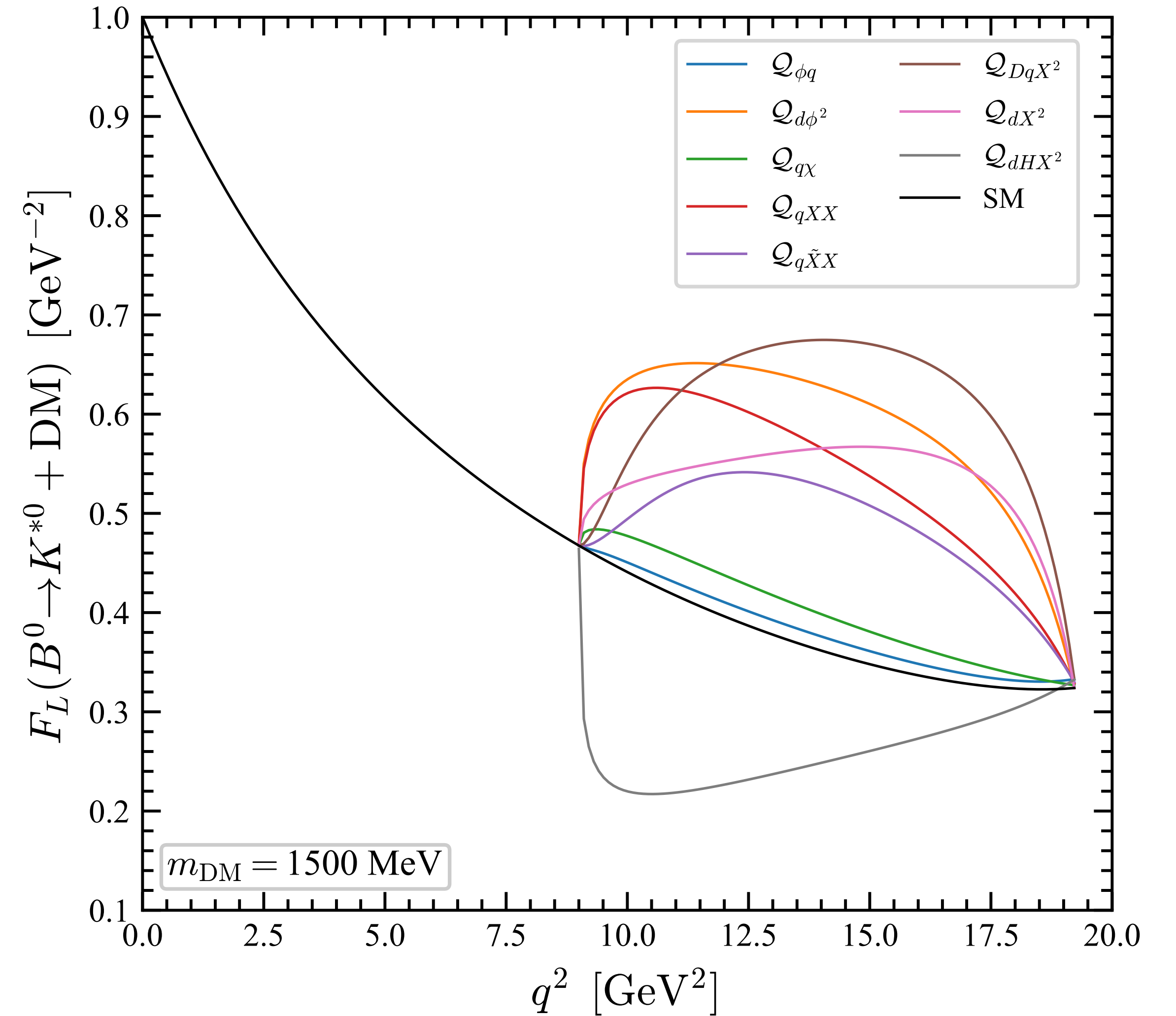
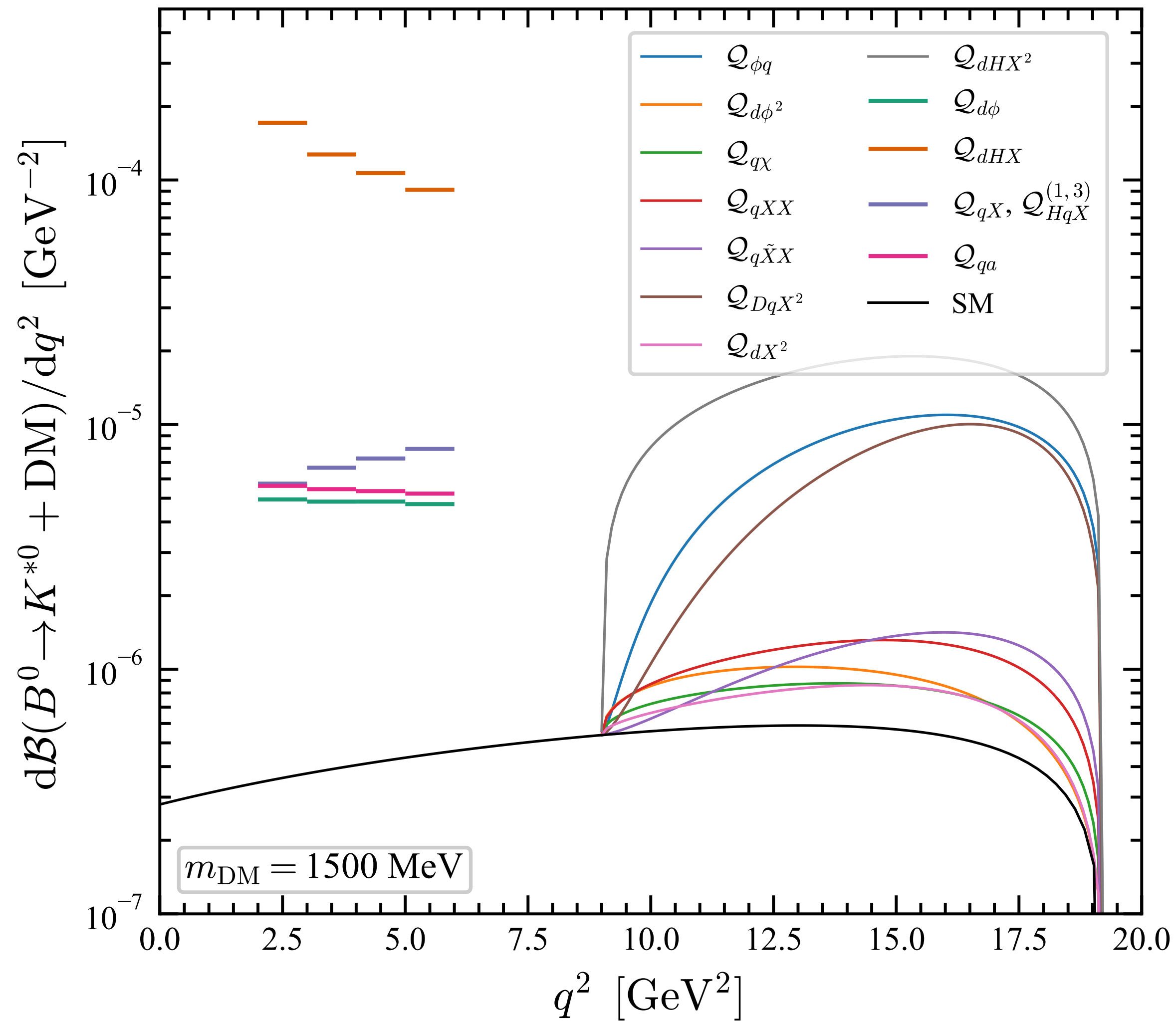
$m_{\text{DM}} = 700 \text{ MeV}$



All the operators are distinguishable from each other by combing these observables, except  $\mathcal{Q}_{qXX}$  and  $\mathcal{Q}_{q\tilde{X}X}$

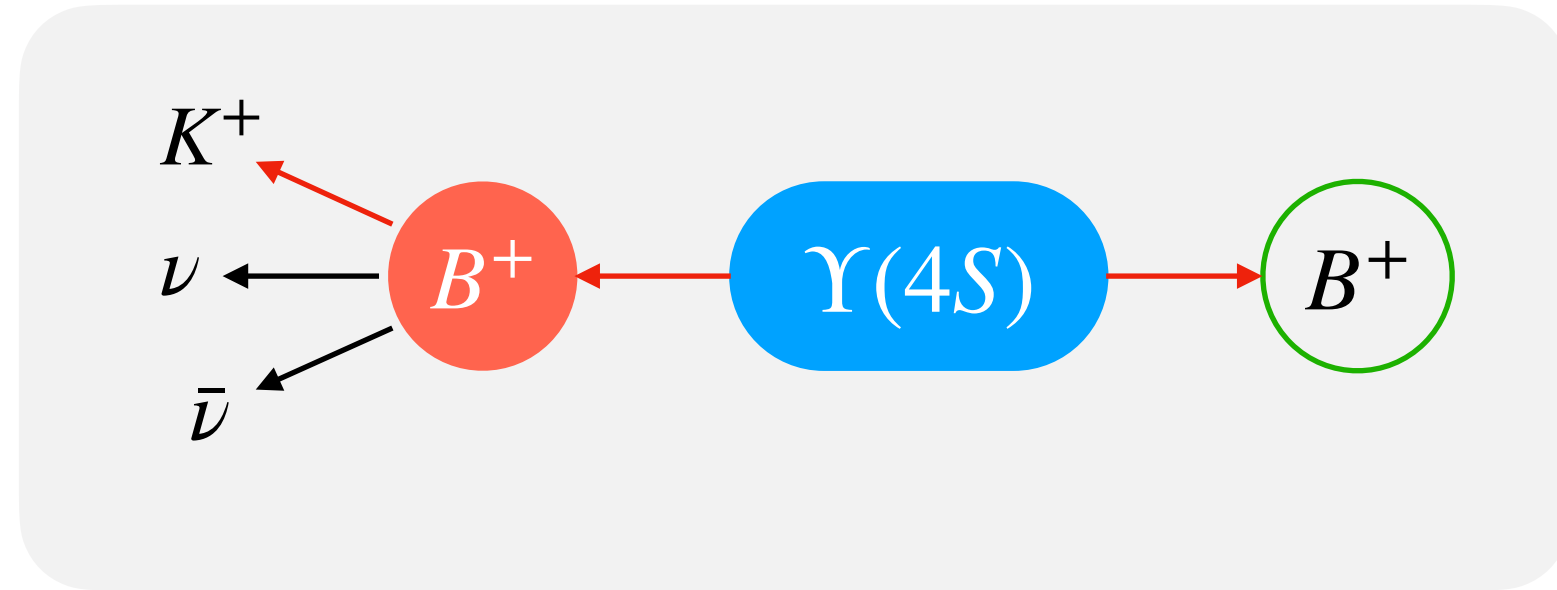
# Dark SMEFT: $dB/dq^2, F_L$

$m_{\text{DM}} = 1500 \text{ MeV}$



All the operators are distinguishable from each other by combing these observables, ~~except  $\mathcal{Q}_{qXX}$  and  $\mathcal{Q}_{q\tilde{X}X}$~~

# Conclusion



SMEFT

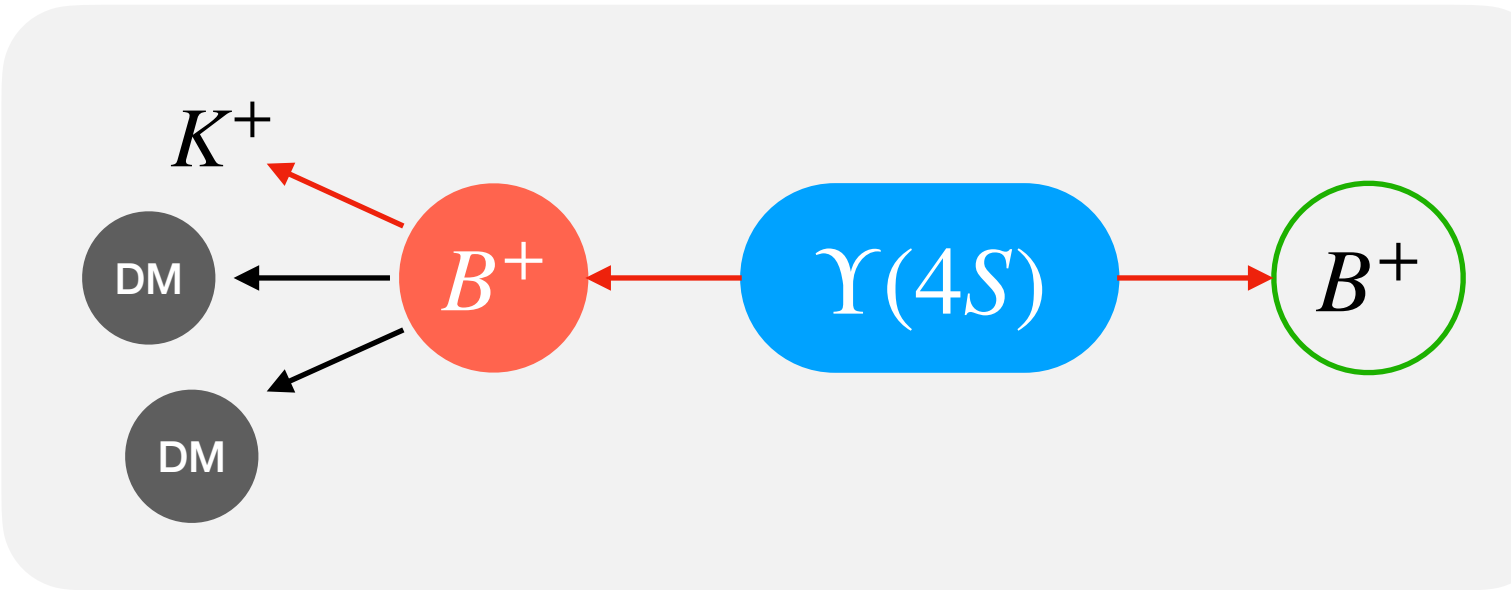
$$\frac{\mathcal{B}(B^+ \rightarrow K^+ \nu \bar{\nu})}{\mathcal{B}(B^0 \rightarrow K^{*0} \nu \bar{\nu})} = \frac{\mathcal{B}(B^+ \rightarrow K^+ \nu \bar{\nu})_{\text{SM}}}{\mathcal{B}(B^0 \rightarrow K^{*0} \nu \bar{\nu})_{\text{SM}}} = 0.46 \pm 0.07$$

$$\frac{\mathcal{B}(B^+ \rightarrow K^+ \nu \bar{\nu})}{\mathcal{B}(B^+ \rightarrow \pi^+ \nu \bar{\nu})} = \frac{\mathcal{B}(B^+ \rightarrow K^+ \nu \bar{\nu})_{\text{SM}}}{\mathcal{B}(B^+ \rightarrow \pi^+ \nu \bar{\nu})_{\text{SM}}} = 29.7 \pm 5.6$$

Belle II excess (if confirmed in the future) implies:

- impossible to explain in SMEFT with MFV
- NP flavour structure is highly non-trivial
- **NP structure in quark sector is beyond MFV**
- **flavour violation is beyond Yukawa coupling**

$\mu_{\text{EW}}$   
LEFT



Dark SMEFT

Observable	SM	Exp	Unit
$\mathcal{B}(B^+ \rightarrow K^+ \nu \bar{\nu})$	$4.16 \pm 0.57$	$23 \pm 5_{-4}^{+5}$	$10^{-6}$
$\mathcal{B}(B^0 \rightarrow K^0 \nu \bar{\nu})$	$3.85 \pm 0.52$	$< 26$	$10^{-6}$
$\mathcal{B}(B^+ \rightarrow K^{*+} \nu \bar{\nu})$	$9.70 \pm 0.94$	$< 61$	$10^{-6}$
$\mathcal{B}(B^0 \rightarrow K^{*0} \nu \bar{\nu})$	$9.00 \pm 0.87$	$< 18$	$10^{-6}$
$\mathcal{B}(B_s \rightarrow \phi \nu \bar{\nu})$	$9.93 \pm 0.72$	$< 5400$	$10^{-6}$
$\mathcal{B}(B_s \rightarrow \nu \bar{\nu})$	$\approx 0$	$< 5.9$	$10^{-4}$
$\mathcal{B}(B^+ \rightarrow \pi^+ \nu \bar{\nu})$	$1.40 \pm 0.18$	$< 140$	$10^{-7}$
$\mathcal{B}(B^0 \rightarrow \pi^0 \nu \bar{\nu})$	$6.52 \pm 0.85$	$< 900$	$10^{-8}$
$\mathcal{B}(B^+ \rightarrow \rho^+ \nu \bar{\nu})$	$4.06 \pm 0.79$	$< 300$	$10^{-7}$
$\mathcal{B}(B^0 \rightarrow \rho^0 \nu \bar{\nu})$	$1.89 \pm 0.36$	$< 400$	$10^{-7}$
$\mathcal{B}(B^0 \rightarrow \nu \bar{\nu})$	$\approx 0$	$< 1.4$	$10^{-4}$
$\mathcal{B}(K^+ \rightarrow \pi^+ \nu \bar{\nu})$	$8.42 \pm 0.61$	$10.6_{-3.4}^{+4.0} \pm 0.9$	$10^{-11}$
$\mathcal{B}(K_L \rightarrow \pi^0 \nu \bar{\nu})$	$3.41 \pm 0.45$	$< 300$	$10^{-11}$

Dark LEFT

All DSMEFT operators survive in general and MFV  $dB/dq^2$  and  $F_L$  are useful to distinguish them

$\mu_b$

HadronToNP: a package to calculate decay of hadron to new particles

$B \rightarrow K + \text{DM}$ ,  $B \rightarrow \rho + \text{DM}$ ,  $\Lambda_b \rightarrow \Lambda + \text{DM}$ ,  $\Upsilon \rightarrow \text{DM}$ , ...

$D \rightarrow \pi + \text{DM}$ ,  $D \rightarrow \rho + \text{DM}$ ,  $\Xi_c \rightarrow \Xi + \text{DM}$ ,  $J/\psi \rightarrow \text{DM}$ , ...