



北京大学
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BESIII

Semi-leptonic Λ_c^+ decays at BESIII

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Outline

→ Introduction

→ BESIII experiment

→ Published physics results

- ❖ $\Lambda_c^+ \rightarrow \Lambda e^+ \nu_e, \Lambda \mu^+ \nu_\mu$ Phys. Rev. Lett. 129, 231803 (2022). Phys. Rev. D 108, L031105 (2023).
- ❖ $\Lambda_c^+ \rightarrow X e^+ \nu_e$ Phys. Rev. D 107, 052005 (2023).
- ❖ $\Lambda_c^+ \rightarrow p K^- e^+ \nu_e$ Phys. Rev. D 106, 112010 (2022).
- ❖ $\Lambda_c^+ \rightarrow \Lambda \pi^+ \pi^- e^+ \nu_e, p K_S^0 \pi^- e^+ \nu_e$ Phys. Lett. B 843, 137993 (2023).

→ Other ongoing analysis

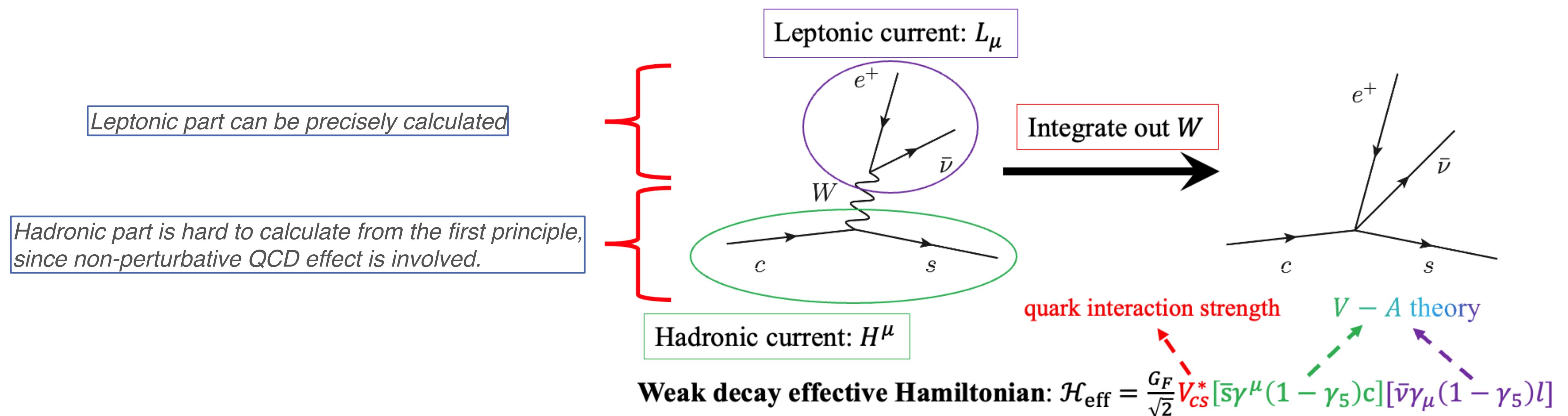
→ Summary & outlook

Introduction

Why semi-leptonic decay?

- Semi-leptonic (SL) decay: good platform to study weak/strong interaction and probe new physics beyond the Standard Model.
- Take $c(\Lambda_c^+) \rightarrow s(\Lambda)$ as an example

- ❖ Differential decay width: $d\Gamma = \frac{1}{2m_{\Lambda_c^+}}(2\pi)^n d\Phi_n |\bar{\mathcal{M}}|^2$
- ❖ Helicity amplitude: $\bar{\mathcal{M}} = \mathcal{H}^\mu \mathcal{L}_\mu$



Λ_c^+ SL decays in theory

- With the help of effective field theory, hadronic amplitude can be parameterized by **Form Factors (FFs)** which are hybrids of on-shell states and off-shell operators.

$$\langle \Lambda(p_2, s_2) | H_{\text{eff}} | \Lambda_c(p_1, s_1) \rangle = \langle \Lambda(p_2, s_2) | (V - A) | \Lambda_c(p_1, s_1) \rangle \quad \text{Form factor is a function of transfer momentum } q = p_1 - p_2$$

$$H_V(\lambda)_\mu = \langle \Lambda(p_2, s_2) | V_\mu | \Lambda_c(p_1, s_1) \rangle = \bar{u}(p_2, s_2) \left[\gamma_\mu f_1(q^2) + i\sigma_{\mu\nu} \frac{q^\nu}{m_1} f_2(q^2) + \frac{q^\mu}{m_1} f_3(q^2) \right] u(p_1, s_1)$$

$$H_A(\lambda)_\mu = \langle \Lambda(p_2, s_2) | A_\mu | \Lambda_c(p_1, s_1) \rangle = \bar{u}(p_2, s_2) \left[\gamma_\mu g_1(q^2) + i\sigma_{\mu\nu} \frac{q^\nu}{m_1} g_2(q^2) + \frac{q^\mu}{m_1} g_3(q^2) \right] u(p_1, s_1)$$

- Total helicity amplitude: $H_{\lambda_\Lambda \lambda_W} = H_\mu(\lambda_\Lambda) \epsilon^\mu(\lambda_W) = [H_V(\lambda_\Lambda) - H_A(\lambda_\Lambda)]_\mu \epsilon^\mu(\lambda_W) = H_V(\lambda_\Lambda \lambda_W) - H_A(\lambda_\Lambda \lambda_W)$

❖ 6 helicity amplitudes: $H_V\left(\frac{1}{2}, 0\right), H_V\left(\frac{1}{2}, 1\right), H_V\left(\frac{1}{2}, t\right), H_A\left(\frac{1}{2}, 0\right), H_A\left(\frac{1}{2}, 1\right), H_A\left(\frac{1}{2}, t\right)$

❖ In the limit of negligible lepton mass, only four of them remained

- Physical observables:

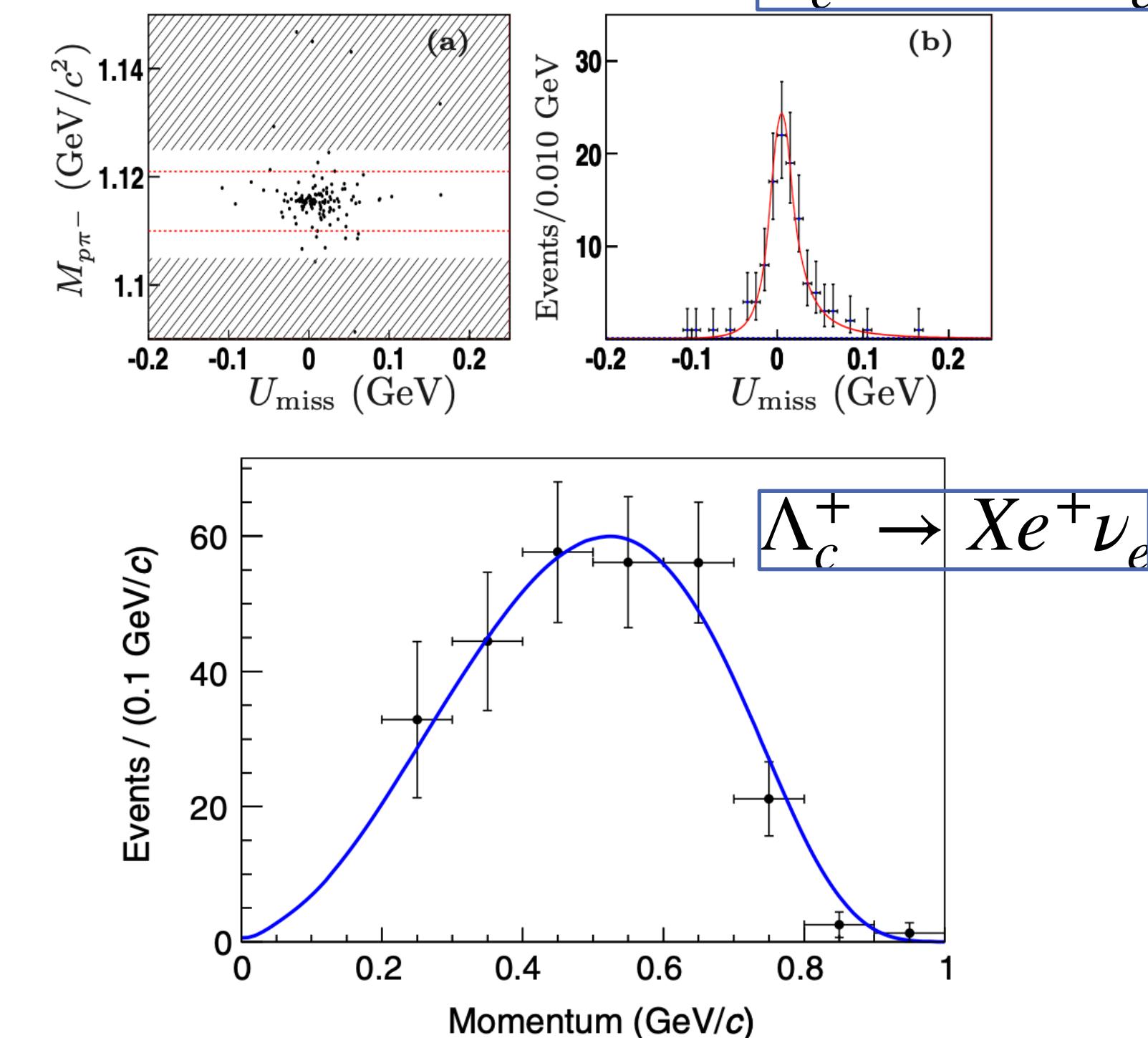
- ❖ Branching Fraction (BF), Lepton Flavor Universality (LFU)
- ❖ q^2 - and angular dependent differential decay width, FF, Forward-backward asymmetry (A_{FB}), decay asymmetry, polarization...
- ❖ New physics observables

- Various theoretical prediction: LQCD, HQET, Quark models, Bag model, Sum rules, $SU(3)_F$, ...

Λ_c^+ SL decays in experiment

$\Lambda_c^+ \rightarrow \Lambda e^+ \nu_e$

- Before 2019, few Λ_c^+ SL decay channels were measured
 - ❖ Before 2005, $\Lambda_c^+ \rightarrow \Lambda e^+ \nu_e$ studied by ARGUS & CLEO
 - $\Lambda_c^+ \rightarrow \Lambda e^+ \nu_e$ observed by ARGUS^[1], decay asymmetry & FFs measured by CLEO^[2,3,4]
 - ❖ Using 587 fb^{-1} data, BESIII reported several absolute BF measurement results
 - $\mathcal{B}(\Lambda_c^+ \rightarrow \Lambda e^+ \nu_e) = (3.63 \pm 0.38_{\text{stat.}} \pm 0.20_{\text{syst.}}) \%$ ^[5]
 - $\mathcal{B}(\Lambda_c^+ \rightarrow \Lambda \mu^+ \nu_\mu) = (3.49 \pm 0.46_{\text{stat.}} \pm 0.27_{\text{syst.}}) \%$ ^[6]
 - $\mathcal{B}(\Lambda_c^+ \rightarrow Xe^+ \nu_e) = (3.95 \pm 0.34_{\text{stat.}} \pm 0.09_{\text{syst.}}) \%$ ^[7]
 - $\mathcal{B}(\Lambda_c^+ \rightarrow \Lambda \mu^+ \nu_\mu) / \mathcal{B}(\Lambda_c^+ \rightarrow \Lambda e^+ \nu_e) = (96 \pm 16_{\text{stat.}} \pm 4_{\text{syst.}}) \%$ ^[6]
 - $\mathcal{B}(\Lambda_c^+ \rightarrow \Lambda e^+ \nu_e) / \mathcal{B}(\Lambda_c^+ \rightarrow Xe^+ \nu_e) = (91.9 \pm 12.5_{\text{stat.}} \pm 5.4_{\text{syst.}}) \%$ ^[5]

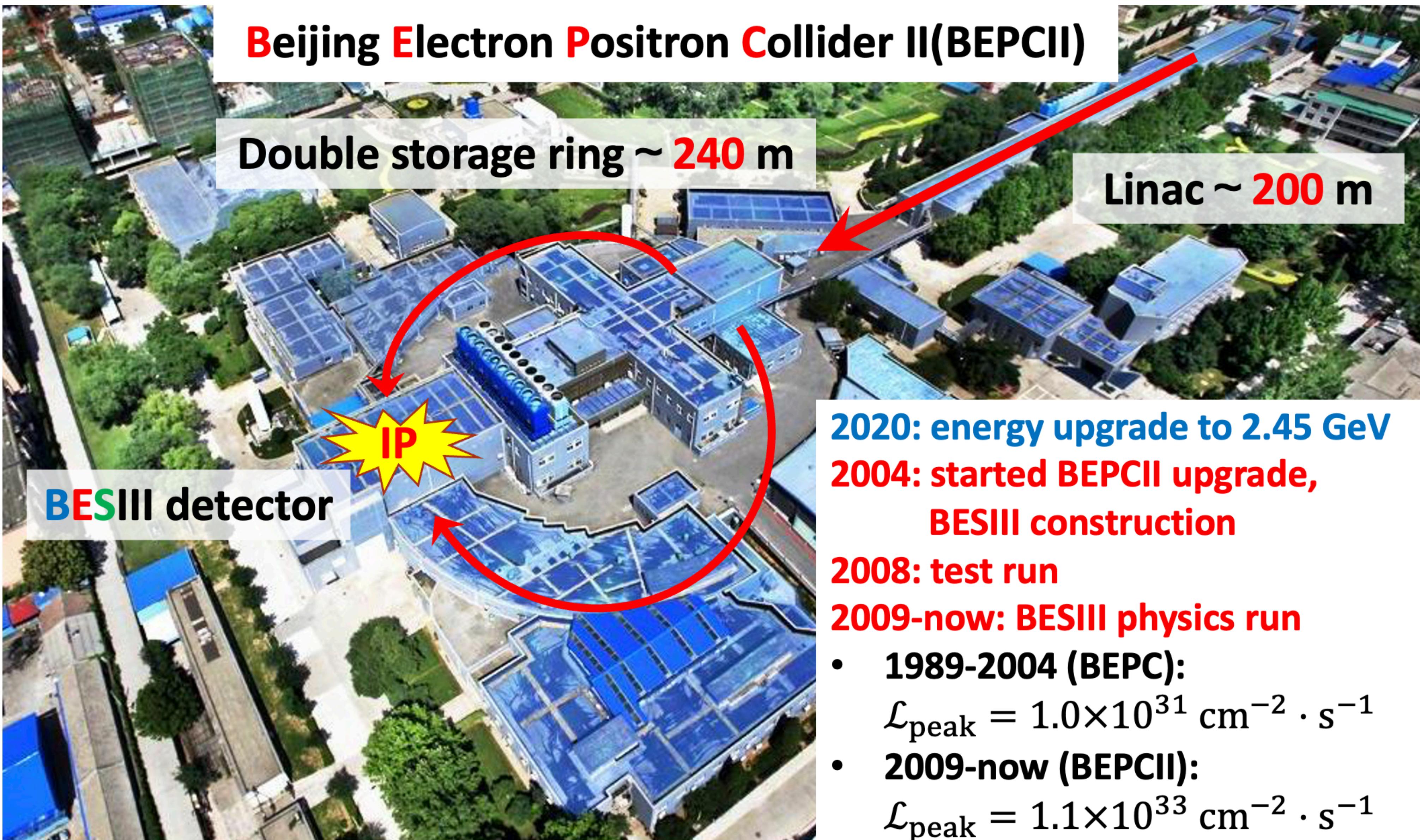


- After 2019, BESIII took new $\Lambda_c^+ \bar{\Lambda}_c^-$ data. What we do?
 - ❖ Precise measurement of golden channel $\Lambda_c^+ \rightarrow \Lambda e^+ \nu_e, \Lambda \mu^+ \nu_\mu$
 - Improve precision (BF, LFU), dynamics study (FF)
 - ❖ Search for other Λ_c^+ SL decays
 - Any rooms? 80% or 100%? Much less than D case \Rightarrow improve precision of BF of inclusive decay
 - Excited state: $\Lambda_c^+ \rightarrow \Lambda^*$? Cabibbo-suppressed: $\Lambda_c^+ \rightarrow n$?

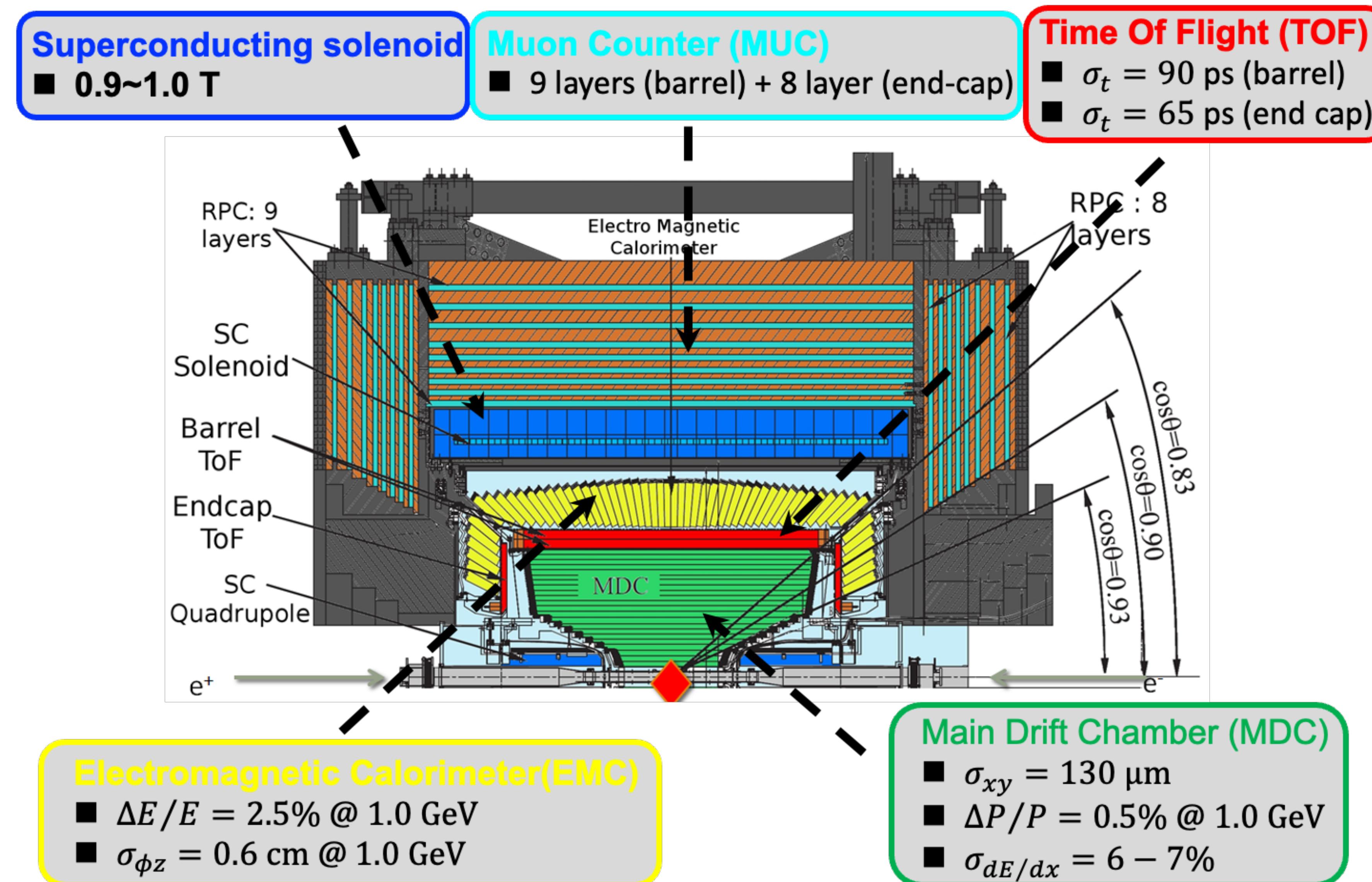
- [1] Phys. Lett. B 269, 234 (1991)
- [2] Phys. Lett. B 323, 219 (1994)
- [3] Phys. Rev. Lett. 75, 624 (1995)
- [4] Phys. Rev. Lett. 94, 191801 (2005)
- [5] Phys. Rev. Lett. 115, 221805 (2015)
- [6] Phys. Lett. B 767, 42 (2017)
- [7] Phys. Rev. D 121, 251801 (2018)

BESIII experiment

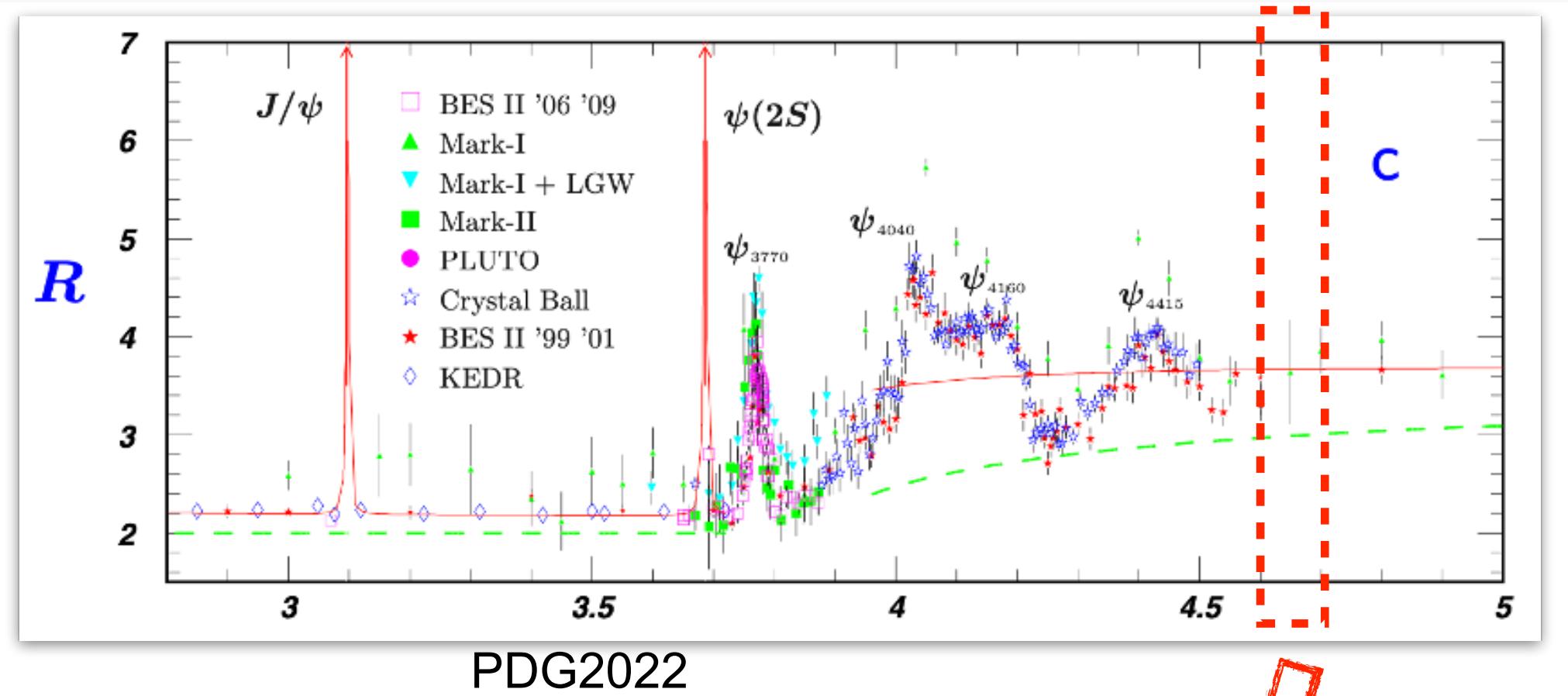
BEPCII



BESIII detector



Pair production at threshold



Sample	\sqrt{s} (MeV)	$\mathcal{L}_{\text{int}}^i$ (pb^{-1})
4600	$4599.53 \pm 0.07 \pm 0.74$	$586.9 \pm 0.1 \pm 3.9$
4612	$4611.86 \pm 0.12 \pm 0.30$	$103.65 \pm 0.05 \pm 0.55$
4626	$4628.00 \pm 0.06 \pm 0.32$	$521.53 \pm 0.11 \pm 2.76$
4640	$4640.91 \pm 0.06 \pm 0.38$	$551.65 \pm 0.12 \pm 2.92$
4660	$4661.24 \pm 0.06 \pm 0.29$	$529.43 \pm 0.12 \pm 2.81$
4680	$4681.92 \pm 0.08 \pm 0.29$	$1667.39 \pm 0.21 \pm 8.84$
4700	$4698.82 \pm 0.10 \pm 0.36$	$535.54 \pm 0.12 \pm 2.84$

- **Threshold effect:** pair production of charmed baryons without accompanying hadrons
 - ❖ $e^+e^- \rightarrow \gamma^* \rightarrow \Lambda_c^+\bar{\Lambda}_c^-$
- Center-of-mass energy: $E_{\text{cms}} = 4.6 \sim 4.7 \text{ GeV}$
 - ❖ $2M_{\Lambda_c} < E_{\text{cms}} < (2M_{\Lambda_c} + M_\pi)$
- Clean backgrounds and well constrained kinematics
 - ❖ $\Delta E = E_{\Lambda_c} - E_{\text{beam}}$
 - ❖ $M_{\text{BC}} = \sqrt{E_{\text{beam}}^2/c^4 - p^2 c^2}$
- Integrated luminosity: 4.5 fb^{-1} ($\sim 7.5 \times 4600$ data)
 - ❖ 1.9 fb^{-1} data @ $4740 \sim 4950 \text{ GeV}$ (not used in published SL analysis)

Double tag method & Partial reconstruction

→ Double Tag (DT) Method

- ❖ Reconstruct $\bar{\Lambda}_c^-$ by dominant and clean decay modes, e.g., $\bar{\Lambda}_c^- \rightarrow \bar{p}K_S^0, \bar{p}K^+\pi^-, \dots$
- ❖ Search for Λ_c^+ signal decay in the recoiling side

❖ BF formula:

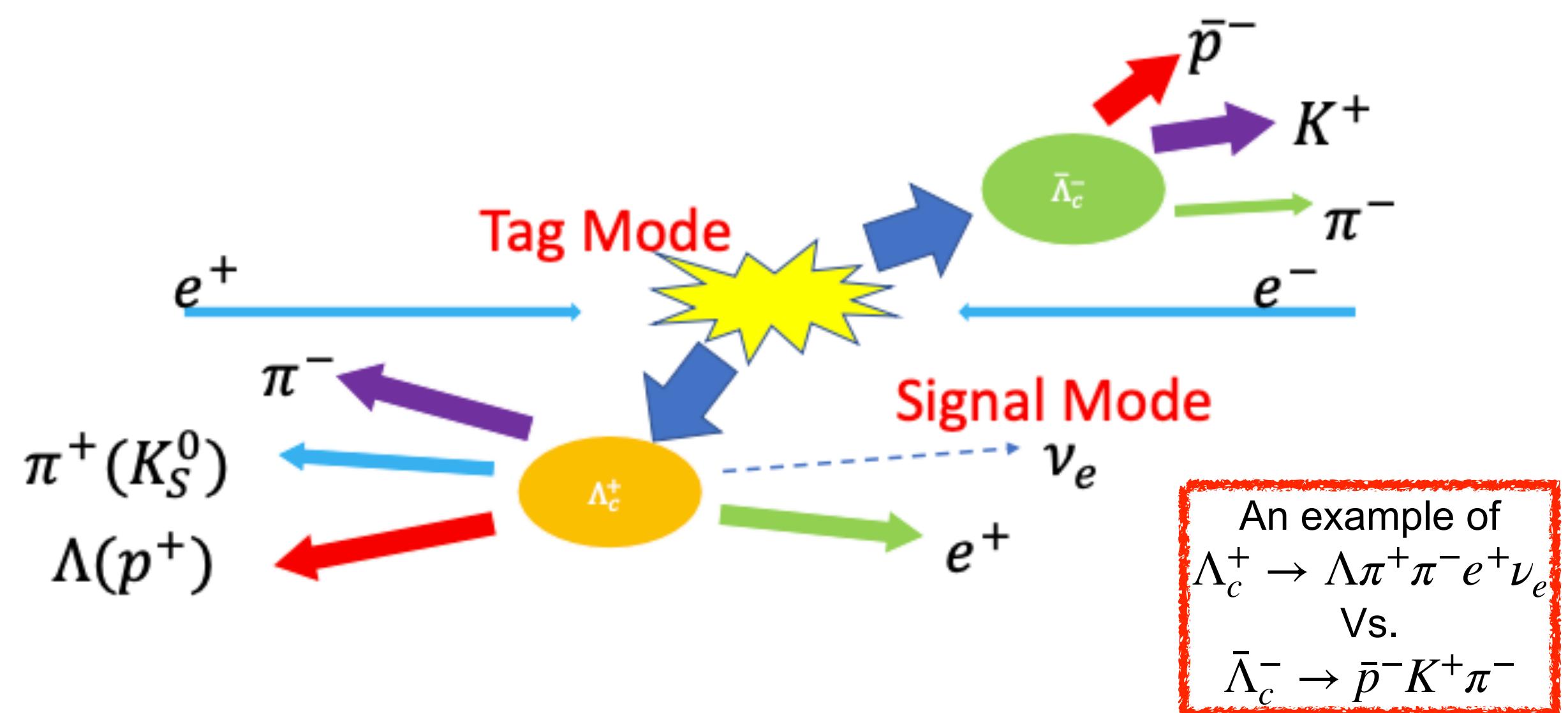
$$N_{\text{ST}}^{i,j} = 2N_{\Lambda_c^+ \bar{\Lambda}_c^-}^j \mathcal{B}_{\text{tag}}^i \epsilon_{\text{ST}}^{i,j},$$

$$N_{\text{DT}}^{i,j} = 2N_{\Lambda_c^+ \bar{\Lambda}_c^-}^j \mathcal{B}_{\text{tag}}^i \mathcal{B}_{\text{sig}} \epsilon_{\text{DT}}^{i,j},$$

$$\mathcal{B}_{\text{sig}} = \frac{\sum_{i,j} N_{\text{DT}}^{i,j}}{\sum_{i,j} \left(\frac{N_{\text{ST}}^{i,j}}{\epsilon_{\text{ST}}^{i,j}} \cdot \epsilon_{\text{DT}}^{i,j} \right)} = \frac{N_{\text{DT}}}{\sum_{i,j} \left(\frac{N_{\text{ST}}^{i,j}}{\epsilon_{\text{ST}}^{i,j}} \cdot \epsilon_{\text{DT}}^{i,j} \right)} = \frac{N_{\text{DT}}}{N_{\text{ST}} \cdot \epsilon^{\text{sig}}},$$

→ Partial reconstruction technique

- ❖ Neutrino can not be detected at BESIII
- ❖ Determinant variable $U_{\text{miss}} = E_{\text{miss}} - c |\vec{p}_{\text{miss}}|$
- ❖ Signal events peak at 0 in U_{miss}



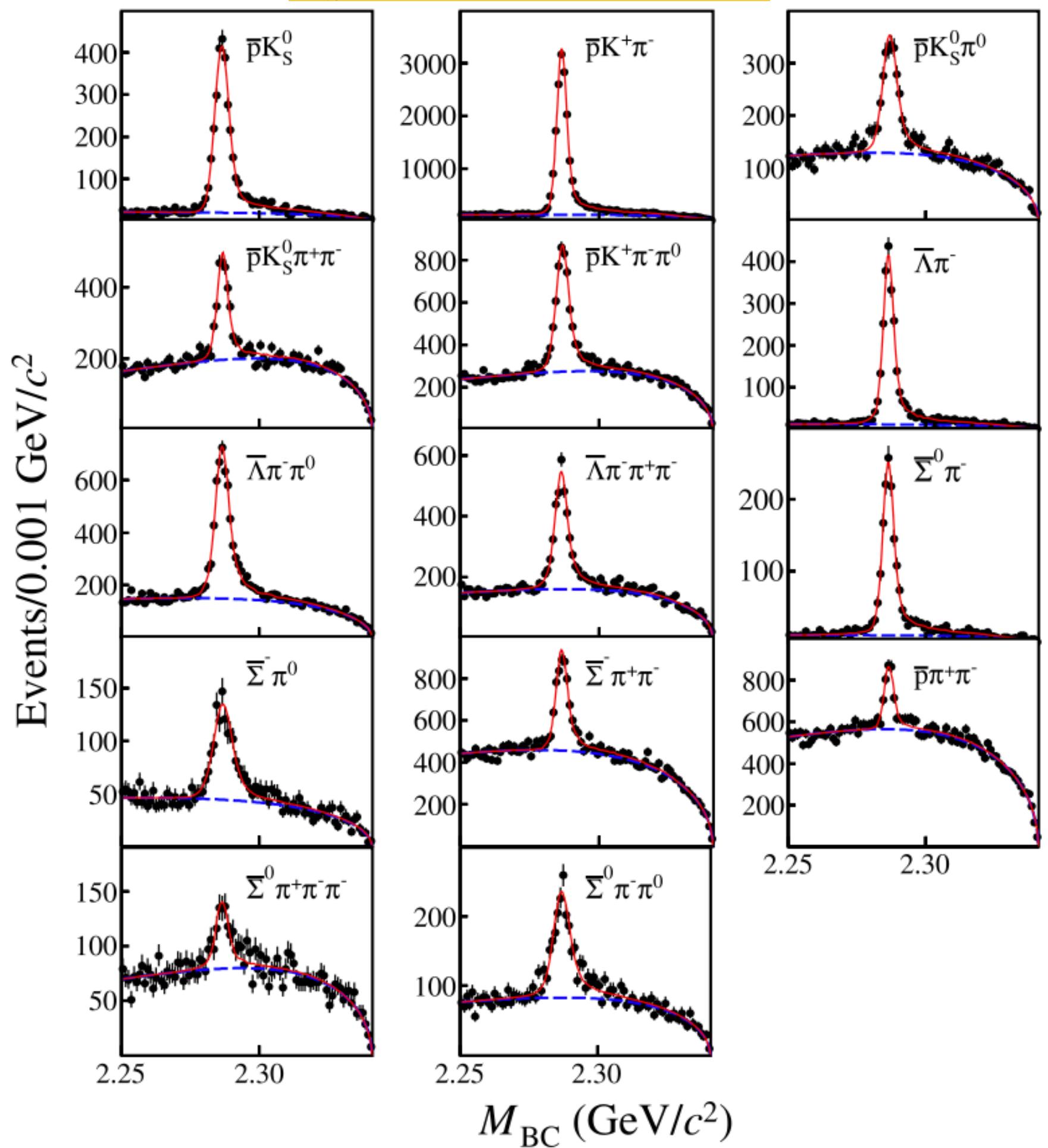
Published physics results

$\Lambda_c^+ \rightarrow \Lambda e^+ \nu_e$

Highlight

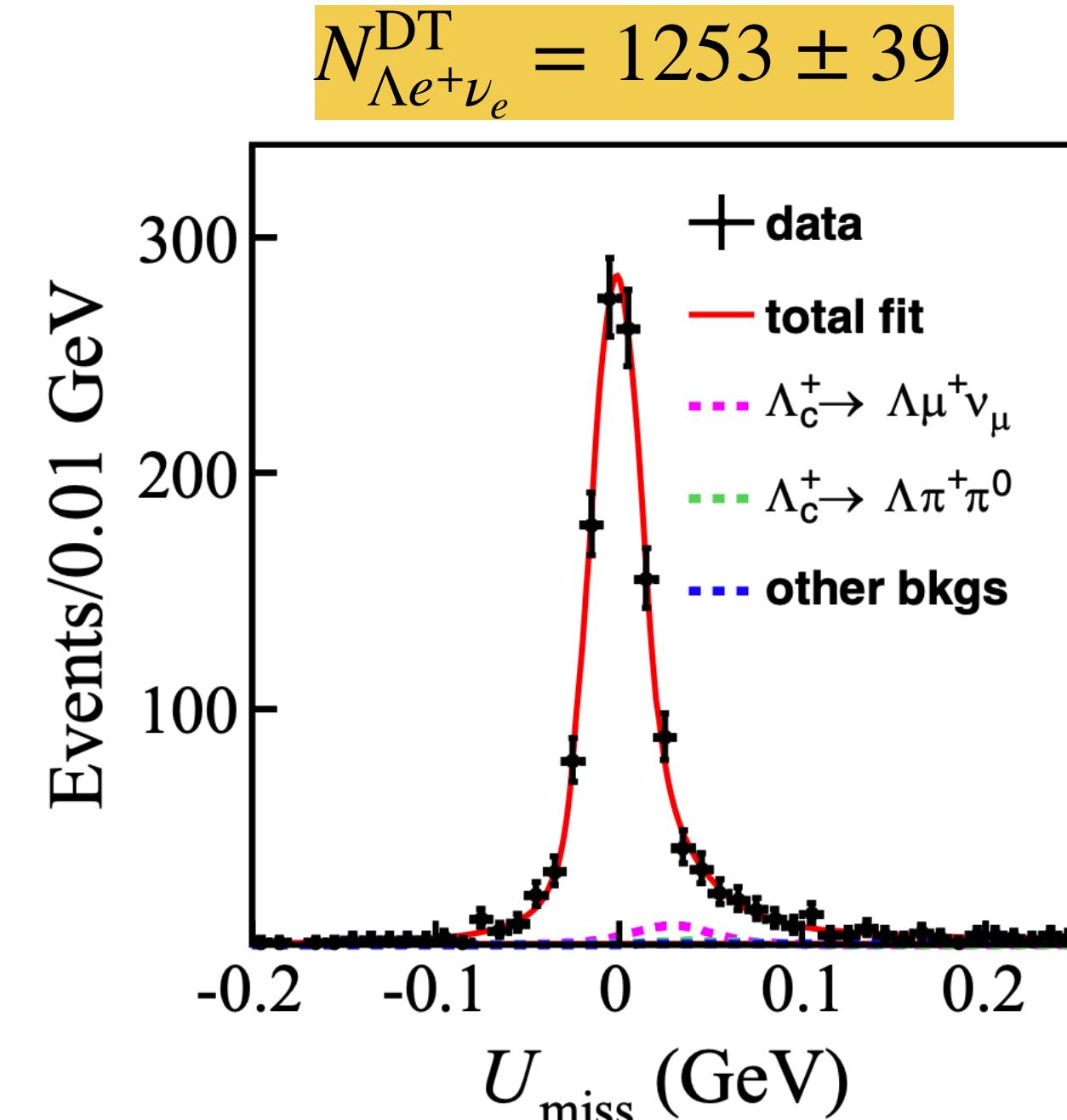
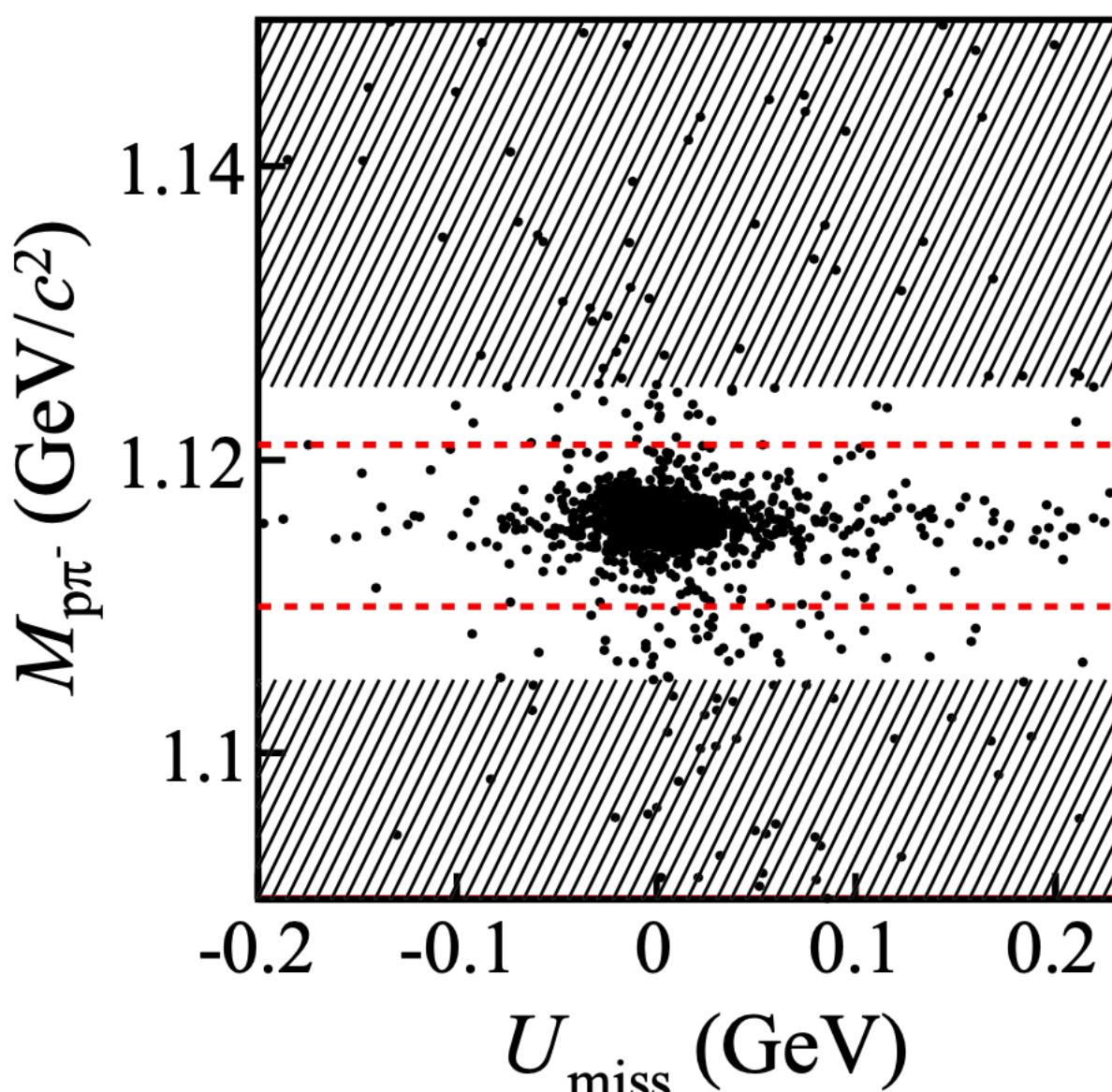
→ ST data set reconstructed by 14 hadronic Λ_c^+ decay mode

$$N_{\text{ST}} = 122268 \pm 474$$



Fits to M_{BC} distributions for different ST modes at $\sqrt{s} = 4.682 \text{ GeV}$

- Select signal Λ and e^+ in the recoiling side of $\bar{\Lambda}_c^-$
- Fit to U_{miss} distribution

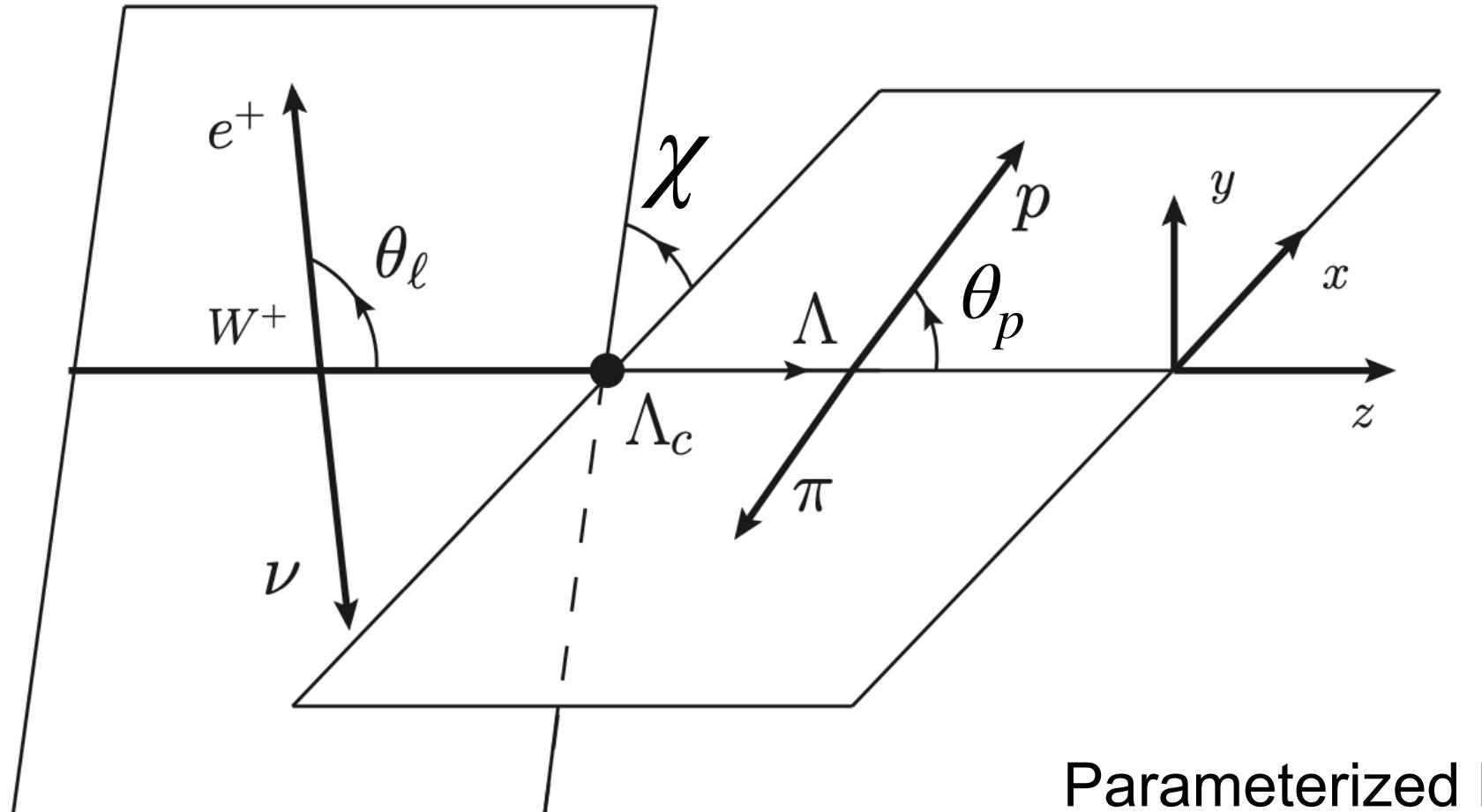


$$\mathcal{B}(\Lambda_c^+ \rightarrow \Lambda e^+ \nu_e) = (3.56 \pm 0.11_{\text{stat.}} \pm 0.07_{\text{syst.}}) \%$$

Precision improved

Decay dynamics of $\Lambda_c^+ \rightarrow \Lambda e^+ \nu_e$

Definition of the polar and the azimuthal angles



Differential decay width

$$\frac{d^4\Gamma}{dq^2 d\cos\theta_e d\cos\theta_p d\chi} = \frac{G_F^2 |V_{cs}|^2}{2(2\pi)^4} \cdot \frac{P q^2}{24 M_{\Lambda_c}^2} \left\{ \frac{3}{8} (1 - \cos\theta_e)^2 |H_{\frac{1}{2}1}|^2 (1 + \alpha_\Lambda \cos\theta_p) + \frac{3}{8} (1 + \cos\theta_e)^2 |H_{-\frac{1}{2}-1}|^2 (1 - \alpha_\Lambda \cos\theta_p) \right. \\ \left. + \frac{3}{4} \sin^2\theta_e [|H_{\frac{1}{2}0}|^2 (1 + \alpha_\Lambda \cos\theta_p) + |H_{-\frac{1}{2}0}|^2 (1 - \alpha_\Lambda \cos\theta_p)] + \frac{3}{2\sqrt{2}} \alpha_\Lambda \cos\chi \sin\theta_e \sin\theta_p \right\},$$

Neglect lepton mass term

Helicity amplitudes:

$$H_{\lambda_\Lambda \lambda_W} = H_{\lambda_\Lambda \lambda_W}^V - H_{\lambda_\Lambda \lambda_W}^A \quad \text{and} \quad H_{-\lambda_\Lambda - \lambda_W}^{V(A)} = +(-) H_{\lambda_\Lambda \lambda_W}^{V(A)}$$

Parameterized by “**Weinberg form factor**”

$$H_{\frac{1}{2}1}^V = \sqrt{2Q_-} [F_1^V(q^2) + \frac{(M_{\Lambda_c^+} + M_\Lambda)}{M_{\Lambda_c^+}} F_2^V(q^2)], \\ H_{\frac{1}{2}1}^A = \sqrt{2Q_+} [F_1^A(q^2) - \frac{(M_{\Lambda_c^+} - M_\Lambda)}{M_{\Lambda_c^+}} F_2^A(q^2)], \\ H_{\frac{1}{2}0}^V = \sqrt{\frac{Q_-}{q^2}} [(M_{\Lambda_c^+} + M_\Lambda) F_1^V(q^2) + \frac{q^2}{M_{\Lambda_c^+}} F_2^V(q^2)], \\ H_{\frac{1}{2}0}^A = \sqrt{\frac{Q_+}{q^2}} [(M_{\Lambda_c^+} - M_\Lambda) F_1^A(q^2) - \frac{q^2}{M_{\Lambda_c^+}} F_2^A(q^2)].$$

4D fit to extract FFs

- $e^+ \nu_e$ mass squared: q^2
- $\Lambda \rightarrow p \pi^-$ helicity angle: θ_p
- $W^+ \rightarrow e^+ \nu_e$ helicity angle: θ_e
- Acoplanarity angle between Λ and W^+ : χ

$$F_1^V(q^2) = \frac{1}{(M_{\Lambda_c^+} + M_\Lambda)^2 - q^2} [f_+(q^2)(M_{\Lambda_c^+} + M_\Lambda)^2 - f_\perp(q^2) \cdot q^2], \\ F_2^V(q^2) = \frac{M_{\Lambda_c^+} \cdot (M_{\Lambda_c^+} + M_\Lambda)}{(M_{\Lambda_c^+} + M_\Lambda)^2 - q^2} [f_\perp(q^2) - f_+(q^2)], \\ F_1^A(q^2) = \frac{1}{(M_{\Lambda_c^+} - M_\Lambda)^2 - q^2} [g_+(q^2)(M_{\Lambda_c^+} - M_\Lambda)^2 - g_\perp(q^2) \cdot q^2], \\ F_2^A(q^2) = \frac{M_{\Lambda_c^+} \cdot (M_{\Lambda_c^+} - M_\Lambda)}{(M_{\Lambda_c^+} - M_\Lambda)^2 - q^2} [g_+(q^2) - g_\perp(q^2)].$$

The relation between
“**Weinberg form factor**”
&
“**Helicity form factor**”

Parameterized by “**Helicity form factor**”

$$H_{\frac{1}{2}1}^V = \sqrt{2Q_-} f_\perp(q^2), \\ H_{\frac{1}{2}1}^A = \sqrt{2Q_+} g_\perp(q^2), \\ H_{\frac{1}{2}0}^V = \sqrt{Q_-/q^2} f_+(q^2)(M_{\Lambda_c} + M_\Lambda), \\ H_{\frac{1}{2}0}^A = \sqrt{Q_+/q^2} g_+(q^2)(M_{\Lambda_c} - M_\Lambda).$$

Following LQCD

Four-dimensional fit

- z -expansion: FF is q^2 dependent, refer to LQCD parameterization
 - ❖ Free parameters: a_0^f and α_1^f

$$f(q^2) = \frac{a_0^f}{1 - q^2/(m_{\text{pole}}^f)^2} [1 + \alpha_1^f \times z(q^2)]$$

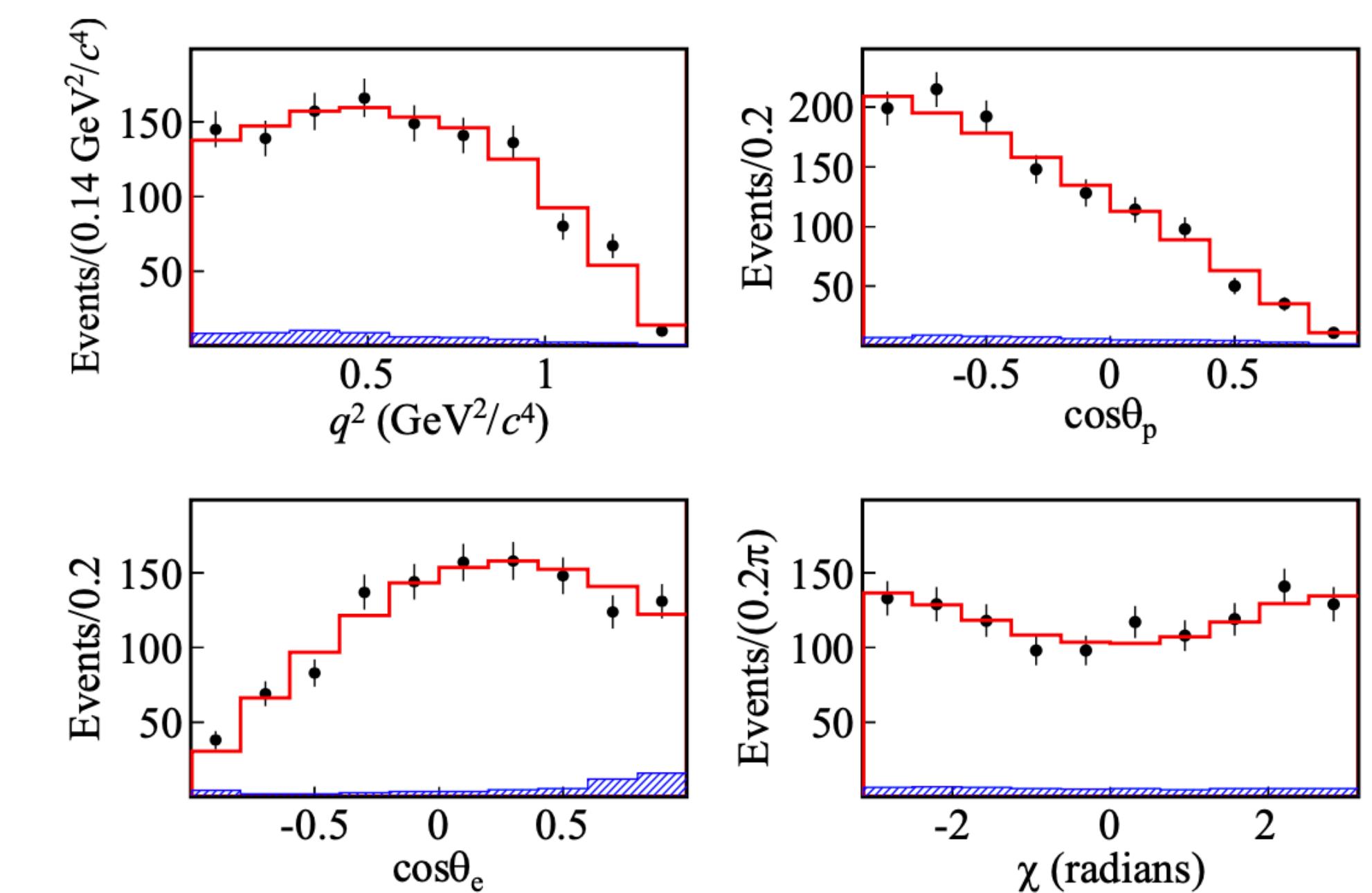
- Five independent free parameters in the fit: $a_1^{g_\perp}$, $a_1^{f_\perp}$, $r_{f_+} = a_0^{f_+}/a_0^{g_\perp}$, $r_{f_\perp} = a_0^{f_\perp}/a_0^{g_\perp}$, $r_{g_+} = a_0^{g_+}/a_0^{g_\perp}$

- ❖ Choose $a_0^{g_\perp}$ as the reference
- ❖ Set $a_1^{g_\perp} = a_1^{g_+}$ and $a_1^{f_\perp} = a_1^{f_+}$

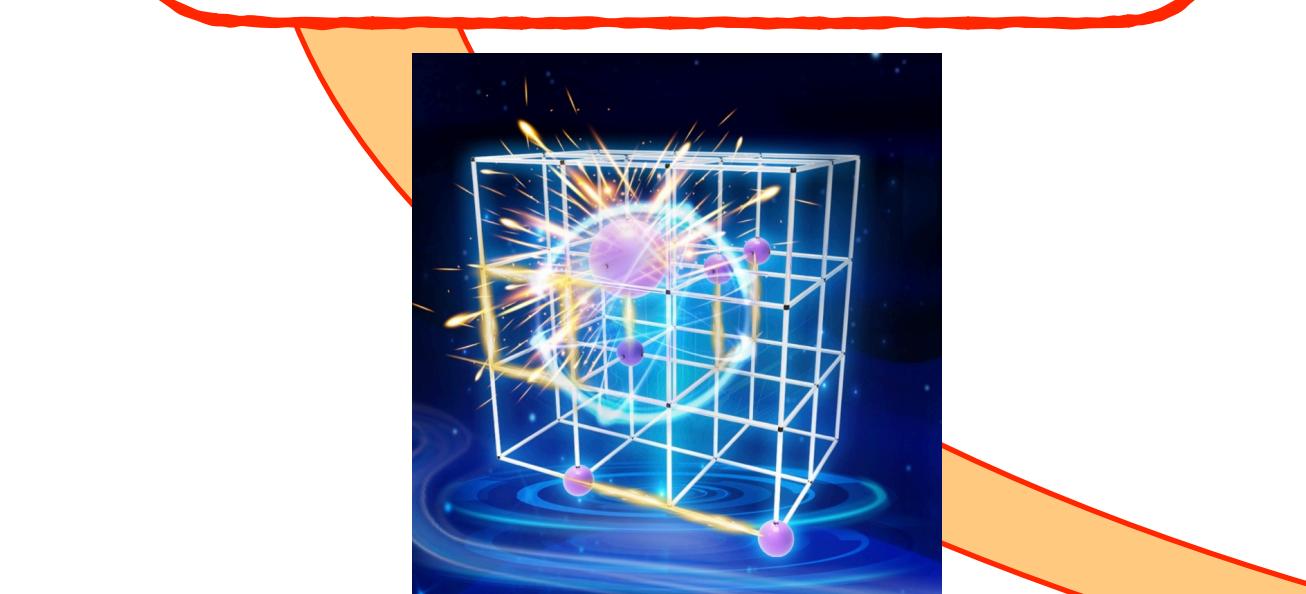
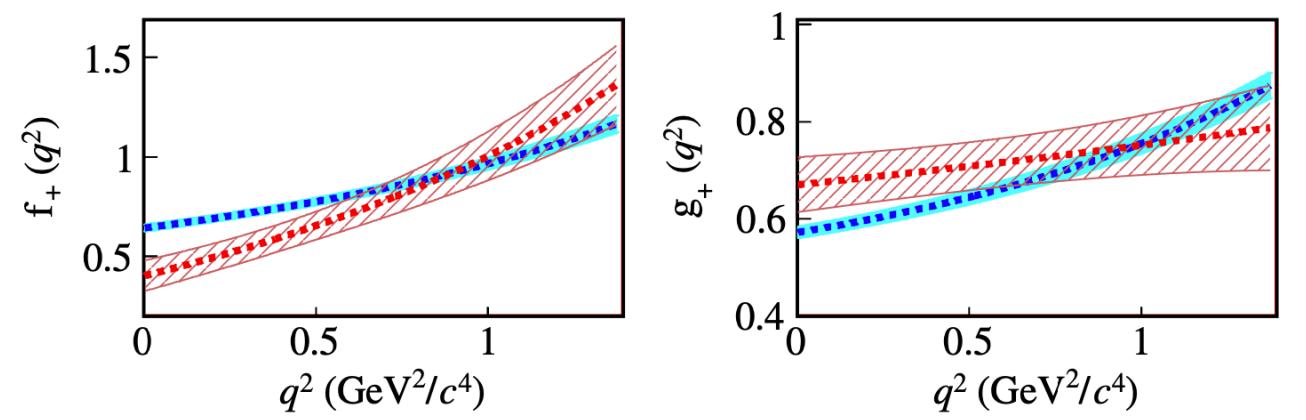
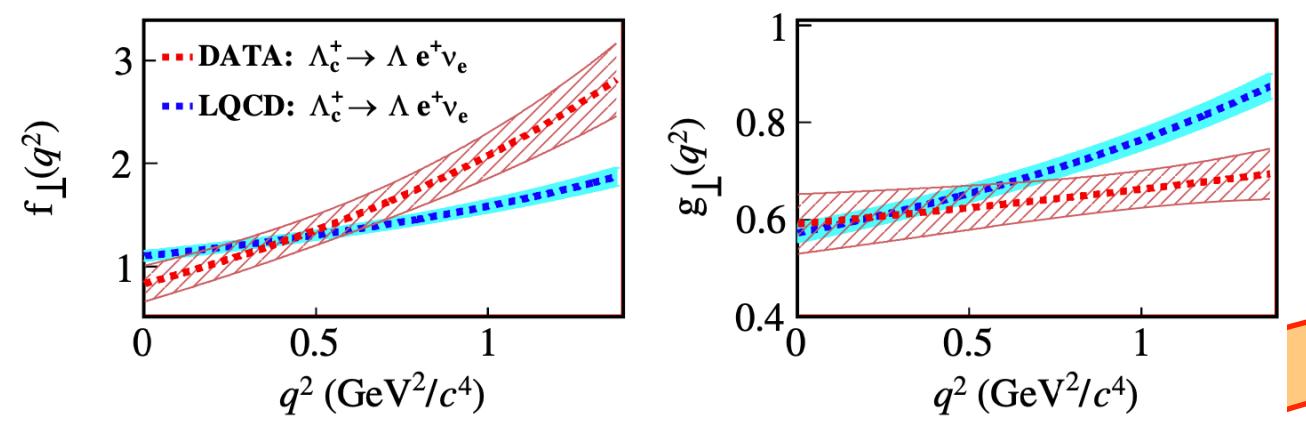
- Four-dimensional fit to events within $-0.06 < U_{\text{miss}} < 0.06$

- ❖ Normalization using BF: $a_0^{g_\perp} = 0.54 \pm 0.04_{\text{stat.}} \pm 0.01_{\text{syst.}}$

Parameters	$\alpha_1^{g_\perp}$	$\alpha_1^{f_\perp}$	r_{f_+}	r_{f_\perp}	r_{g_+}
Values	$1.43 \pm 2.09 \pm 0.16$	$-8.15 \pm 1.58 \pm 0.05$	$1.75 \pm 0.32 \pm 0.01$	$3.62 \pm 0.65 \pm 0.02$	$1.13 \pm 0.13 \pm 0.01$
Coefficients	$\alpha_1^{g_\perp}$	$\alpha_1^{f_\perp}$	r_{f_+}	r_{f_\perp}	r_{g_+}
$a_0^{g_\perp}$	-0.64	0.60	-0.66	-0.83	-0.40
$\alpha_1^{g_\perp}$		-0.63	0.62	0.53	-0.33
$\alpha_1^{f_\perp}$			-0.79	-0.67	-0.07
r_{f_+}				0.57	-0.09
r_{f_\perp}					0.39

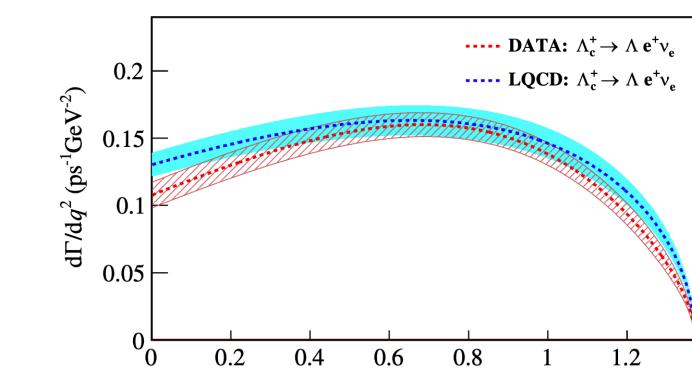
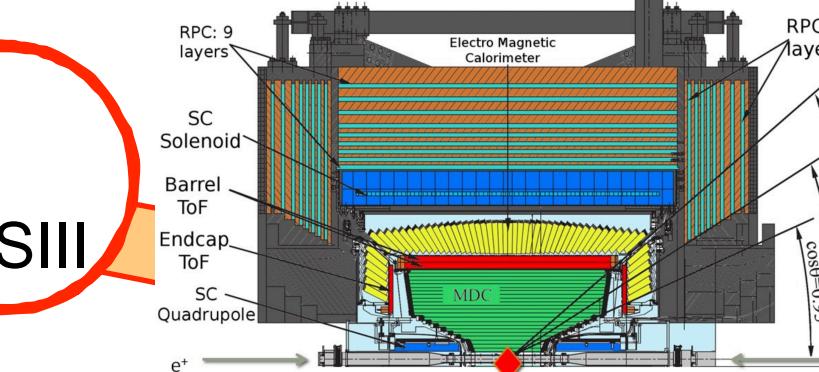


Indirect Test of SM



Branching Fraction

$$\mathcal{B}(\Lambda_c^+ \rightarrow \Lambda e^+ \nu_e) = (3.56 \pm 0.11 \pm 0.07) \% \text{ from BESIII}$$



Form Factor

Calculated from LQCD and models

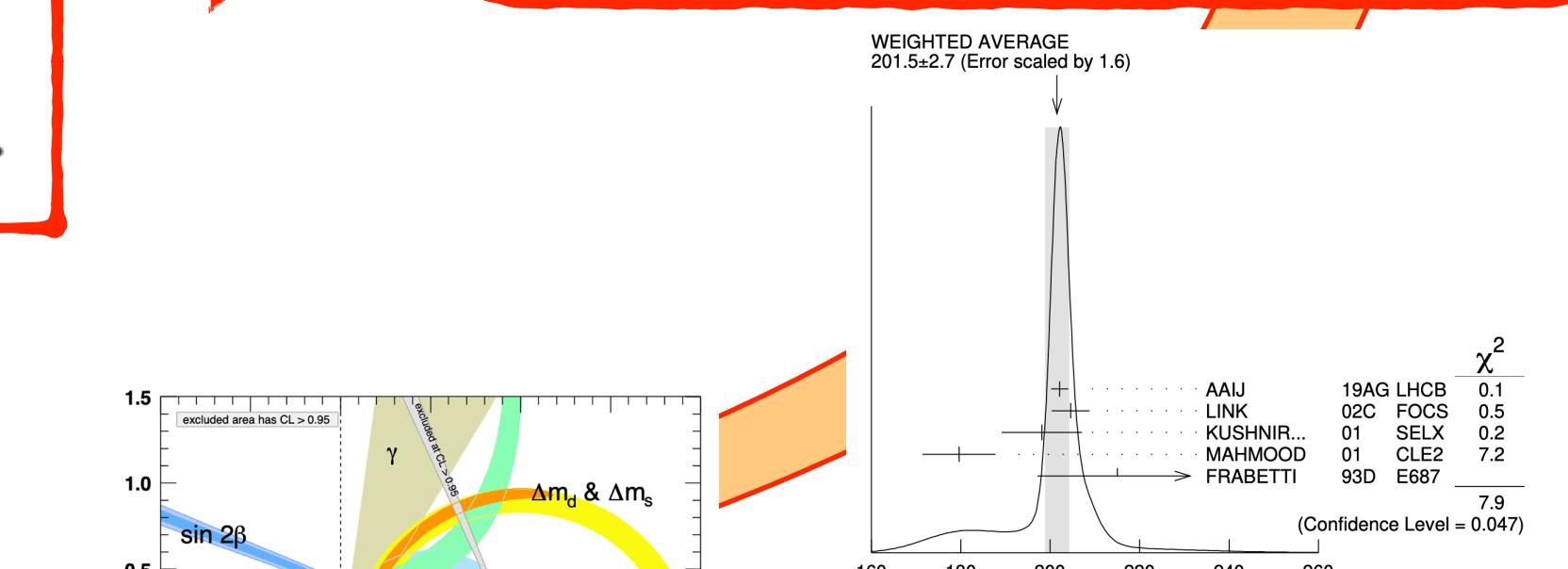
$$\int_0^{q_{\max}^2} \frac{d\Gamma}{dq^2} dq^2 = \frac{\mathcal{B}(\Lambda_c^+ \rightarrow \Lambda e^+ \nu_e)}{\tau_{\Lambda_c}},$$

$$\frac{d\Gamma}{dq^2} = \frac{G_F^2 |V_{cs}|^2}{192\pi^3 M_{\Lambda_c}^2} \times P q^2 \times [|H_{\frac{1}{2}1}|^2 + |H_{-\frac{1}{2}-1}|^2 + |H_{\frac{1}{2}0}|^2 + |H_{-\frac{1}{2}0}|^2].$$

Lifetime

$$\tau_{\Lambda_c^+} = (202.4 \pm 3.1) \times 10^{-3} \text{ ps from PDG}$$

WEIGHTED AVERAGE 201.5±2.7 (Error scaled by 1.6)



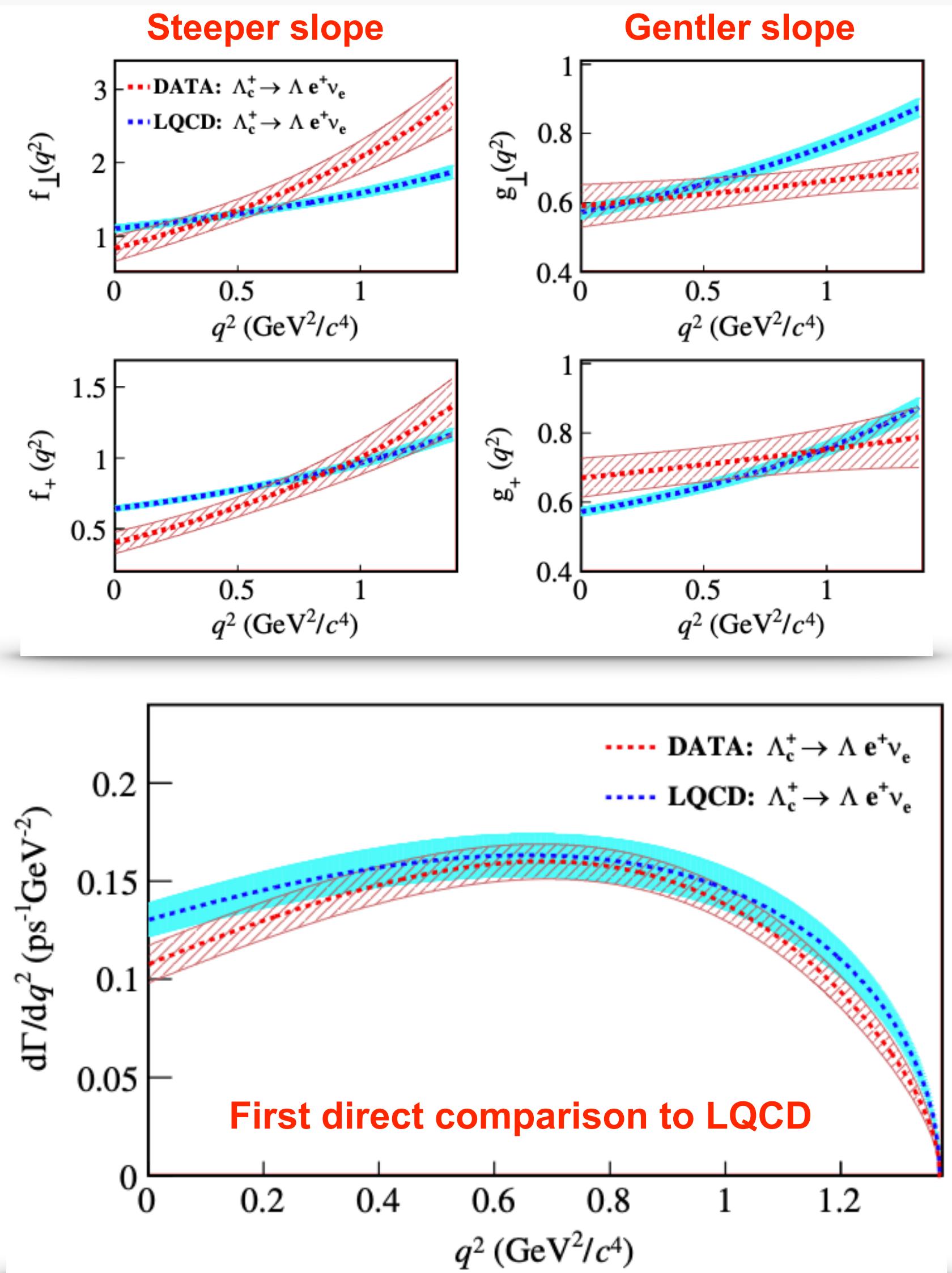
CKM unitarity

$$|V_{cs}| = 0.97320 \pm 0.00011 \text{ from CKM unitarity fit}$$

$$|V_{cs}| = 0.936 \pm 0.017 \quad \mathcal{B} \pm 0.024 \quad \text{LQCD} \pm 0.007 \quad \tau_{\Lambda_c}$$

Consistent with $|V_{cs}|$ measured in $D \rightarrow Kl\nu_l$

Comparison with theoretical predictions



No clear difference is observed within uncertainties
for the resulting differential decay rate of LQCD

TABLE III. Comparison of $\mathcal{B}(\Lambda_c^+ \rightarrow \Lambda e^+ \nu_e)$ from theoretical calculations and our measurement.

	$\mathcal{B}(\Lambda_c^+ \rightarrow \Lambda e^+ \nu_e)$ (%)	Differ by $> 2\sigma$
Constituent quark model (HONR) [9]	4.25	
Light-front approach [10]	1.63	
Covariant quark model [11]	2.78	
Relativistic quark model [12]	3.25	
Non-relativistic quark model [13]	3.84	
Light-cone sum rule [14]	3.0 ± 0.3	
Lattice QCD [15]	3.80 ± 0.22	
$SU(3)$ [16]	3.6 ± 0.4	
Light-front constituent quark model [17]	3.36 ± 0.87	
MIT bag model [17]	3.48	
Light-front quark model [18]	4.04 ± 0.75	
This Letter	$3.56 \pm 0.11 \pm 0.07$	

LFU test in $\Lambda_c^+ \rightarrow \Lambda\mu^+\nu_\mu$

→ Improved measurement of $\mathcal{B}(\Lambda_c^+ \rightarrow \Lambda\mu^+\nu_\mu) = (3.48 \pm 0.14_{\text{stat.}} \pm 0.10_{\text{syst.}}) \%$

- ◆ 3 times more precise than prior results

- ◆ $\mathcal{B}(\Lambda_c^+ \rightarrow \Lambda e^+\nu_e)/\mathcal{B}(\Lambda_c^+ \rightarrow \Lambda\mu^+\nu_\mu) = 0.98 \pm 0.05_{\text{stat.}} \pm 0.03_{\text{syst.}}$ consistent with LQCD (0.97)

→ **Differential decay rates** in separate four-momentum transfer regions

$$\Delta\Gamma_i = \int_i \frac{d\Gamma}{dq^2} dq^2 = \sum_{j=1}^{N_{\text{bins}}} (\epsilon^{-1})_{ij} N_{\text{DT}}^j / (\tau_{\Lambda_c} \times N^{\text{ST}})$$

- ◆

- ◆ ϵ_{ij} : efficiency matrix for reconstruction efficiency and migration effects across q^2 bins

→ **Model-independent forward-backward asymmetries** for lepton system and $p\pi^-$ system

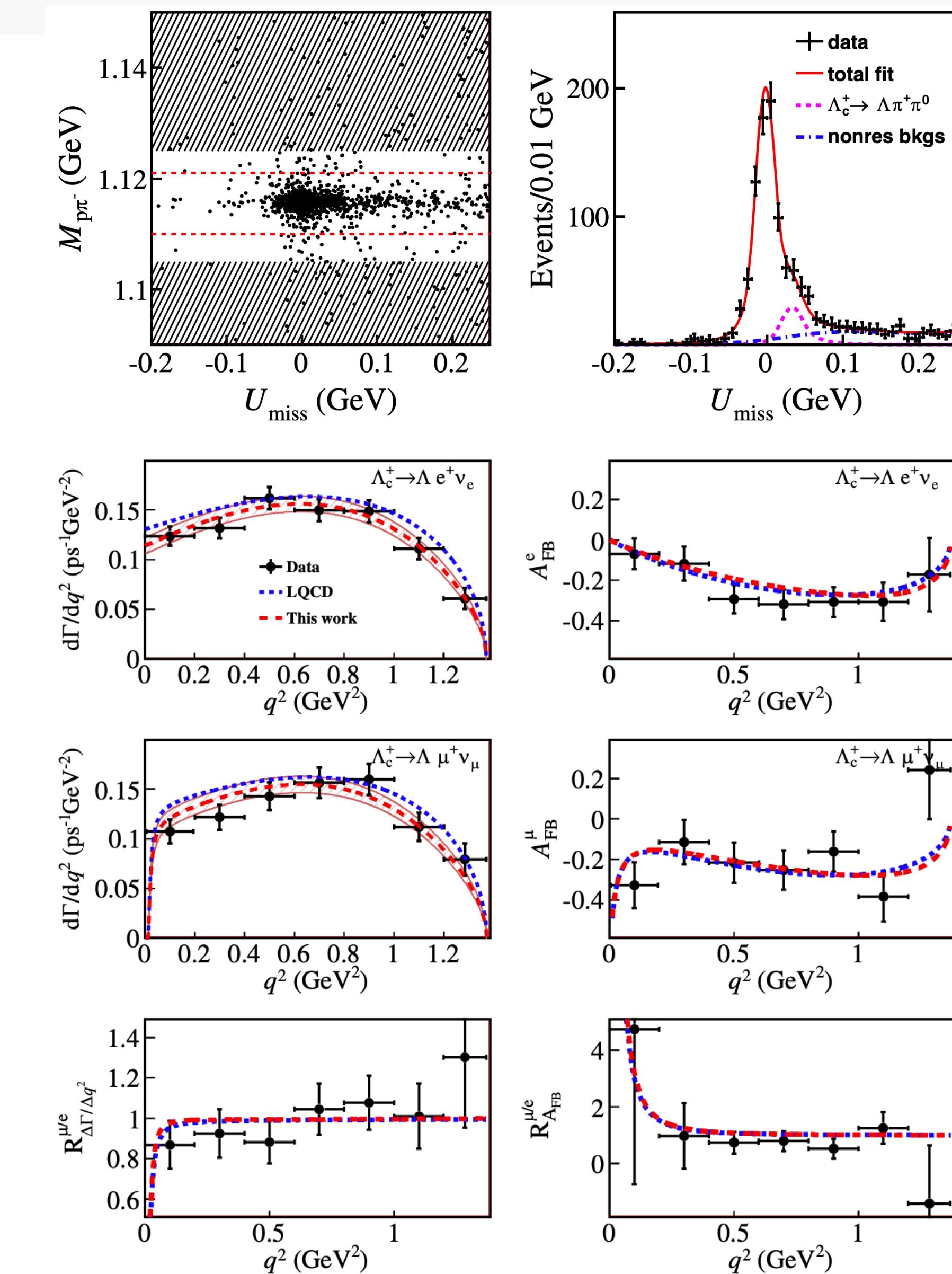
$$A_{\text{FB}}^{\ell,p}(q^2) = \frac{\int_0^1 \frac{d^2\Gamma}{dq^2 d\cos\theta_{\ell,p}} d\cos\theta_{\ell,p} - \int_{-1}^0 \frac{d^2\Gamma}{dq^2 d\cos\theta_{\ell,p}} d\cos\theta_{\ell,p}}{\int_0^1 \frac{d^2\Gamma}{dq^2 d\cos\theta_{\ell,p}} d\cos\theta_{\ell,p} + \int_{-1}^0 \frac{d^2\Gamma}{dq^2 d\cos\theta_{\ell,p}} d\cos\theta_{\ell,p}}$$

- ◆

- ◆ Average lepton FB asymmetry: $\langle A_{\text{FB}}^e \rangle = -0.24 \pm 0.03_{\text{stat.}} \pm 0.01_{\text{syst.}}$

- ◆ $\langle A_{\text{FB}}^\mu \rangle = -0.22 \pm 0.04_{\text{stat.}} \pm 0.01_{\text{syst.}}$

→ **No evidence for a violation of LFU**



Decay asymmetry and New physics search in $\Lambda_c^+ \rightarrow \Lambda l^+ \nu_l$

→ Decay asymmetry α_{Λ_c} vs Forward-backward asymmetry A_{FB}^p $\alpha_{\Lambda_c}(q^2) = \frac{2}{\alpha_\Lambda} [A_{\text{FB}}^p(q^2)]$

- ❖ Model-dependent determination:

$$\alpha_{\Lambda_c} = \frac{|H_{1/2\ 1}|^2 - |H_{-1/2\ -1}|^2 + |H_{1/2\ 0}|^2 - |H_{-1/2\ 0}|^2}{|H_{1/2\ 1}|^2 + |H_{-1/2\ -1}|^2 + |H_{1/2\ 0}|^2 + |H_{-1/2\ 0}|^2}$$

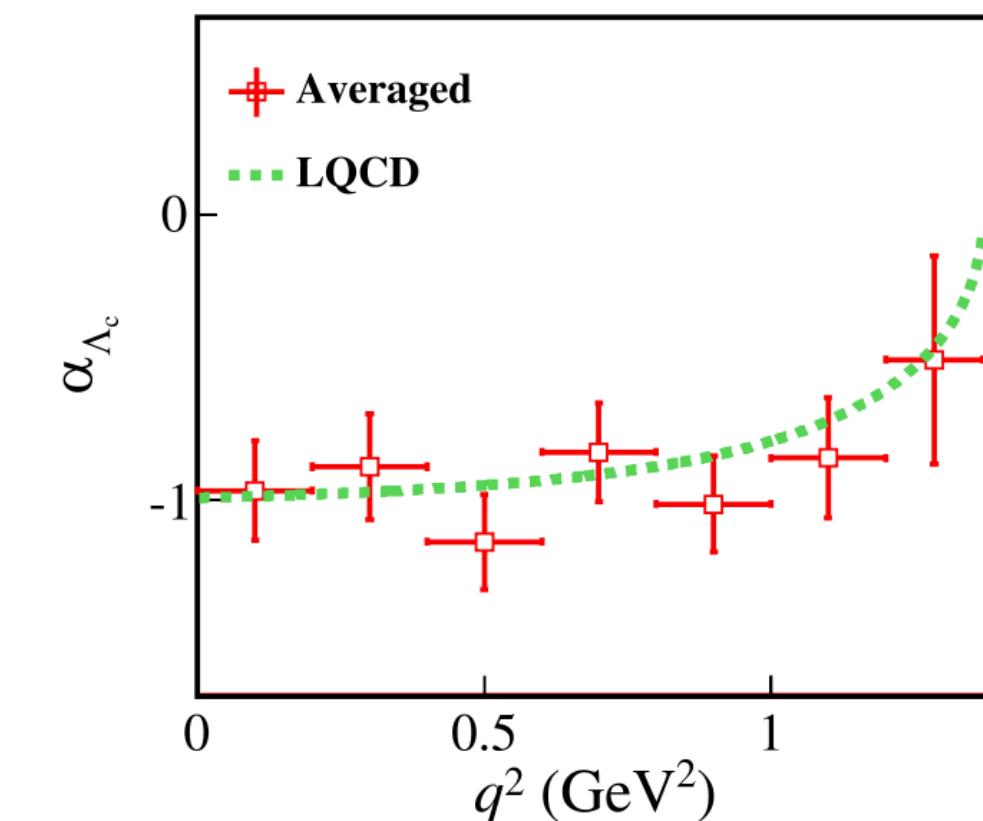
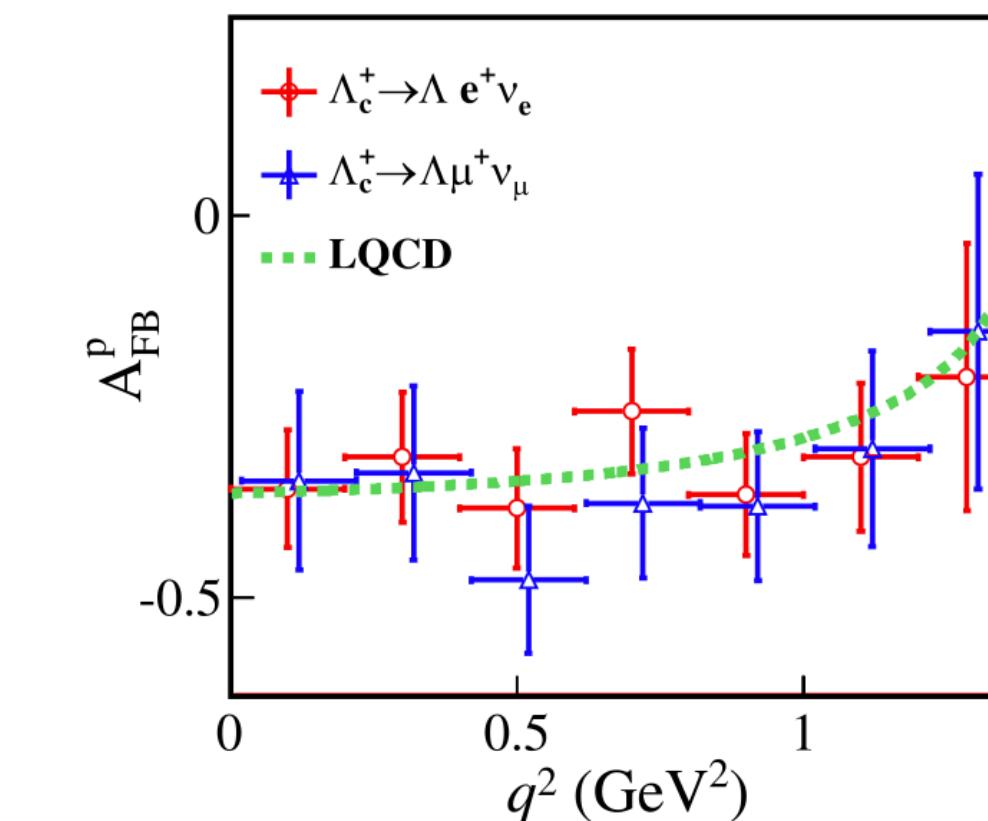
- ❖ First model-independent determination of $\alpha_{\Lambda_c}(q^2)$

- ❖ q^2 averaged asymmetry

$\langle A_{\text{FB}}^p \rangle = -0.33 \pm 0.03_{\text{stat.}} \pm 0.01_{\text{syst.}}$ Only for $\Lambda_c^+ \rightarrow \Lambda e^+ \nu_e$

$\langle A_{\text{FB}}^p \rangle = -0.37 \pm 0.04_{\text{stat.}} \pm 0.01_{\text{syst.}}$ Only for $\Lambda_c^+ \rightarrow \Lambda \mu^+ \nu_\mu$

$\langle \alpha_{\Lambda_c} \rangle = -0.94 \pm 0.07_{\text{stat.}} \pm 0.03_{\text{syst.}}$ Combine e and μ channels



→ New physics search: T asymmetry parameter \mathcal{T}_p

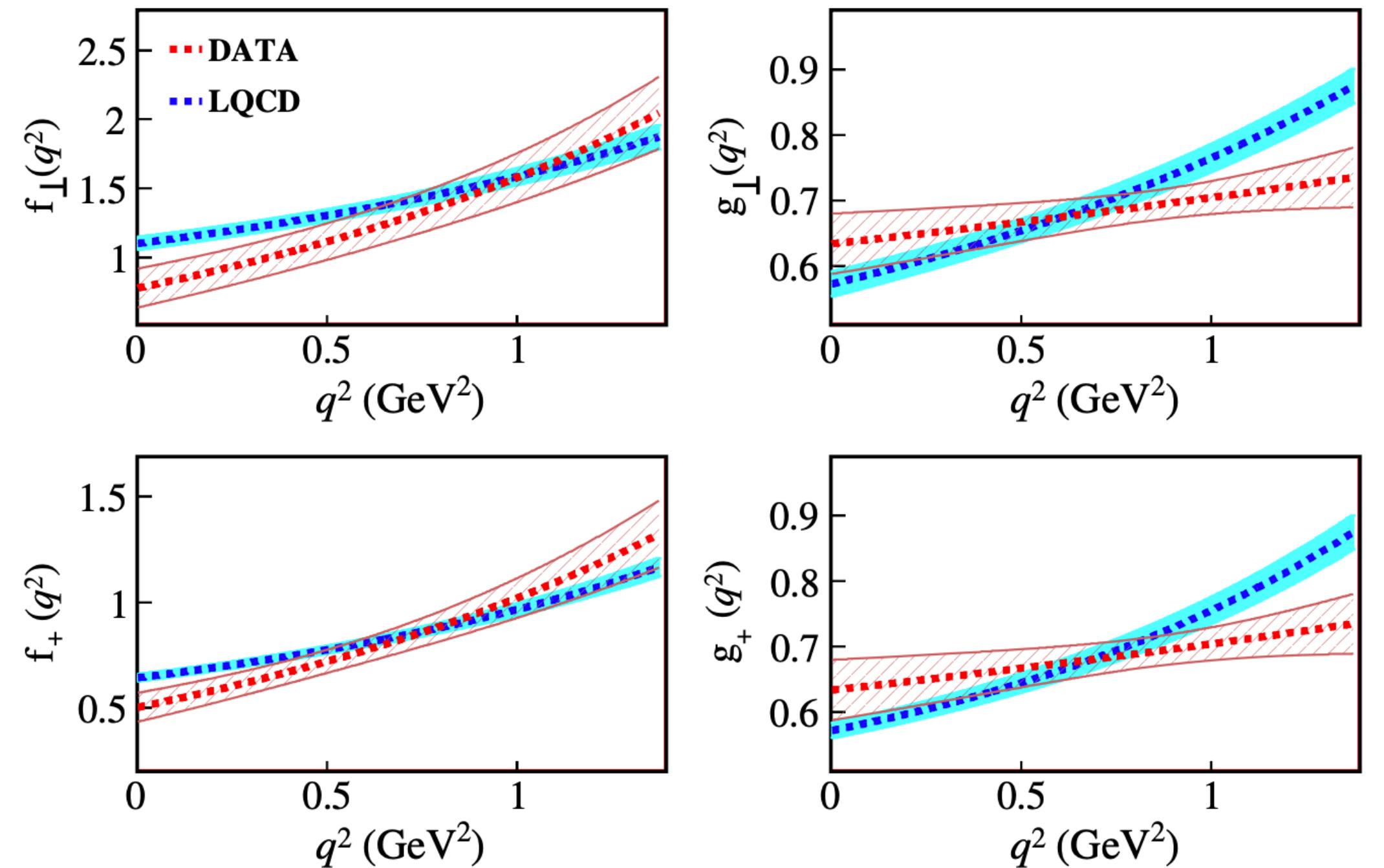
- ❖ Consistent with zero as predicted from the SM

- ❖ No indication of new physics in $\Lambda_c^+ \rightarrow \Lambda l^+ \nu_l$ decays

$$\mathcal{T}_p = \frac{[(\int_{-\pi}^0 - \int_0^\pi) d\chi][(\int_0^1 - \int_{-1}^0) d \cos \theta_p] \Gamma_{\chi, \cos \theta_p}^\ell}{\alpha_\Lambda \Gamma^\ell}$$

$$\begin{aligned} \mathcal{T}_p(\Lambda_c^+ \rightarrow \Lambda e^+ \nu_e) &= -0.021 \pm 0.041_{\text{stat.}} \pm 0.001_{\text{syst.}} \\ \mathcal{T}_p(\Lambda_c^+ \rightarrow \Lambda \mu^+ \nu_\mu) &= 0.068 \pm 0.055_{\text{stat.}} \pm 0.002_{\text{syst.}} \end{aligned}$$

Improvement of $\Lambda_c^+ \rightarrow \Lambda$ FF parameters



$$\frac{d^4\Gamma}{dq^2 d\cos\theta'_\ell d\cos\theta_p d\chi} = \frac{G_F^2 |V_{cs}|^2}{2(2\pi)^4} \cdot \frac{P q^2 (1 - m_\ell^2/q^2)^2}{24 M_{\Lambda_c}^2} \left\{ \begin{aligned} & \frac{3}{8} (1 - \cos\theta'_\ell)^2 |H_{\frac{1}{2}1}|^2 (1 + \alpha_\Lambda \cos\theta_p) \\ & + \frac{3}{8} (1 + \cos\theta'_\ell)^2 |H_{-\frac{1}{2}-1}|^2 (1 - \alpha_\Lambda \cos\theta_p) \\ & + \frac{3}{4} \sin^2\theta'_\ell [|H_{\frac{1}{2}0}|^2 (1 + \alpha_\Lambda \cos\theta_p) + |H_{-\frac{1}{2}0}|^2 (1 - \alpha_\Lambda \cos\theta_p)] + \frac{3}{2\sqrt{2}} \alpha_\Lambda \cos\chi \sin\theta'_\ell \sin\theta_p \\ & \times [(1 - \cos\theta'_\ell) H_{-\frac{1}{2}0} H_{\frac{1}{2}1} + (1 + \cos\theta'_\ell) H_{\frac{1}{2}0} H_{-\frac{1}{2}-1}] + \mathcal{H}_{m_\ell^2} \end{aligned} \right\},$$

$$\begin{aligned} H_{\frac{1}{2}1}^{V/A} &= \sqrt{2Q_\mp} f_\perp / g_\perp(q^2), \\ H_{\frac{1}{2}0}^{V/A} &= \sqrt{Q_\mp/q^2} f_+ / g_+(q^2) (M_{\Lambda_c} \pm M_\Lambda), \\ H_{\frac{1}{2}t}^{V/A} &= \sqrt{Q_\pm/q^2} f_0 / g_0(q^2) (M_{\Lambda_c} \mp M_\Lambda), \end{aligned}$$

- Improve measurement of the FF parameters in the $\Lambda_c^+ \rightarrow \Lambda$ transition
- Differential decay width formula needs to consider lepton mass term
- Test and calibrate LQCD

Comparison with theoretical calculations

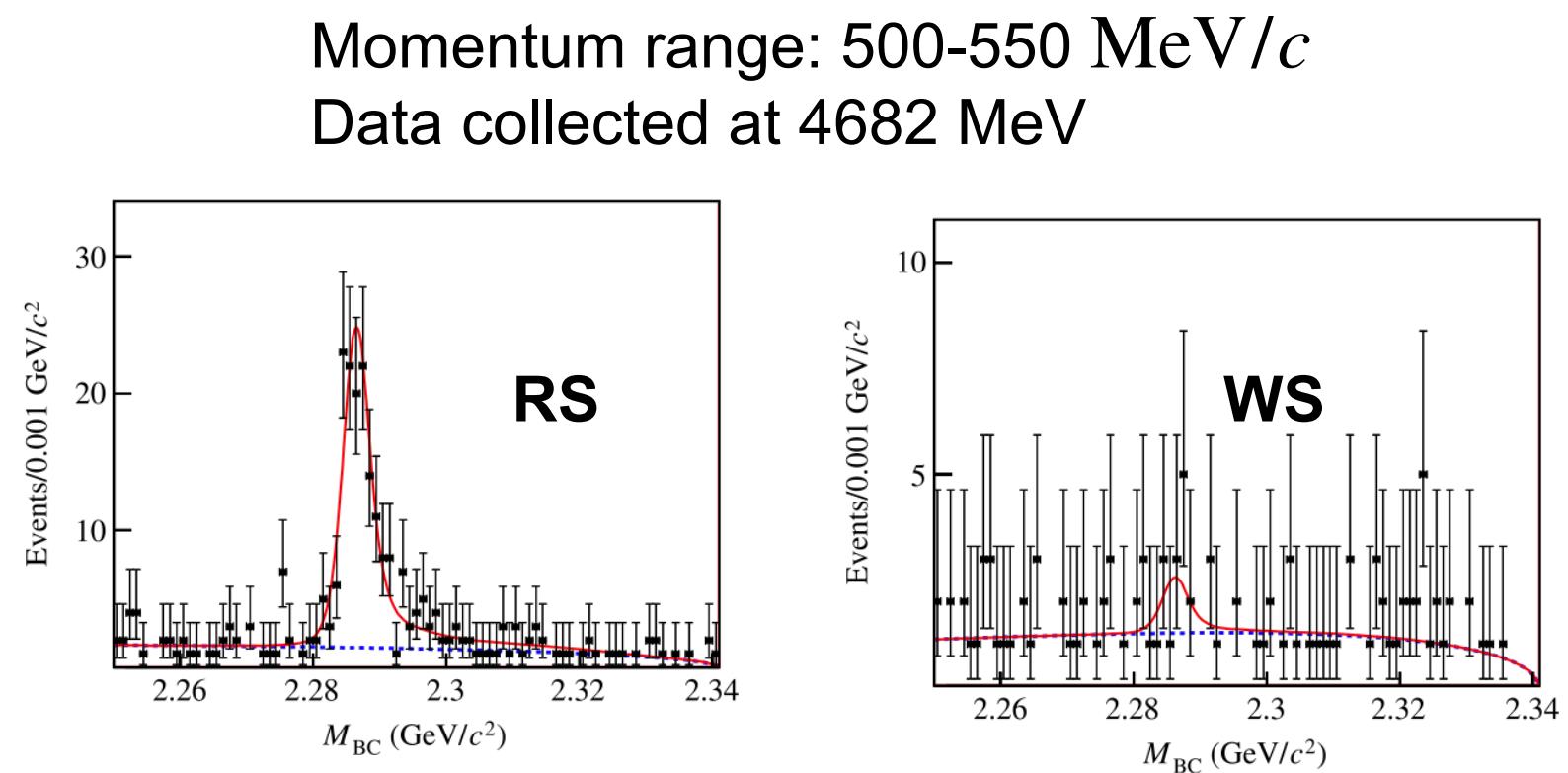
TABLE I. Comparisons of $\mathcal{B}(\Lambda_c^+ \rightarrow \Lambda\mu^+\nu_\mu)$ (in %), $\langle\alpha_{\Lambda_c}\rangle$, $\langle A_{FB}^e\rangle$, and $\langle A_{FB}^\mu\rangle$ from theories and measurement.

	$\mathcal{B}(\Lambda_c^+ \rightarrow \Lambda\mu^+\nu_\mu)$	$\langle\alpha_{\Lambda_c}\rangle$	$\langle A_{FB}^e\rangle$	$\langle A_{FB}^\mu\rangle$
CQM [20]	2.69	-0.87	-0.2	-0.21
RQM [21]	3.14	-0.86	-0.209	-0.242
CQM(HONR) [49]	4.25			
NRQM [50]	3.72			
HBM [24]	3.67 ± 0.23	-0.826	-0.176(5)	-0.143(6)
LQCD [28]	3.69 ± 0.22	-0.874(10)	-0.201(6)	-0.169(7)
LCSR [51]	3.0 ± 0.3			
$SU(3)$ [25]	3.6 ± 0.4	-0.86(4)		
LFCQM [27]	3.21 ± 0.85	-0.97(3)		
MBM [27]	3.38	-0.83		
LFQM [22]	3.90 ± 0.73	-0.87(9)	0.20(5)	0.16(4)
LFCQM [26]	3.40 ± 1.02	-0.97(3)		
$SU(3)$ [52]	3.45 ± 0.30			
This work	3.48 ± 0.17	-0.94(8)	-0.24(3)	-0.22(4)

- $\mathcal{B}(\Lambda_c^+ \rightarrow \Lambda\mu^+\nu_\mu)$: Disfavor Refs. [20,49] based on CQM at a confidence level of more than 95%
- Decay asymmetry: consistent with all theoretical prediction and model-dependent measurement by CLEO
- Lepton forward-backward asymmetry: clearly differ from Ref. [22] based on LFQM

$$\Lambda_c^+ \rightarrow X e^+ \nu_e$$

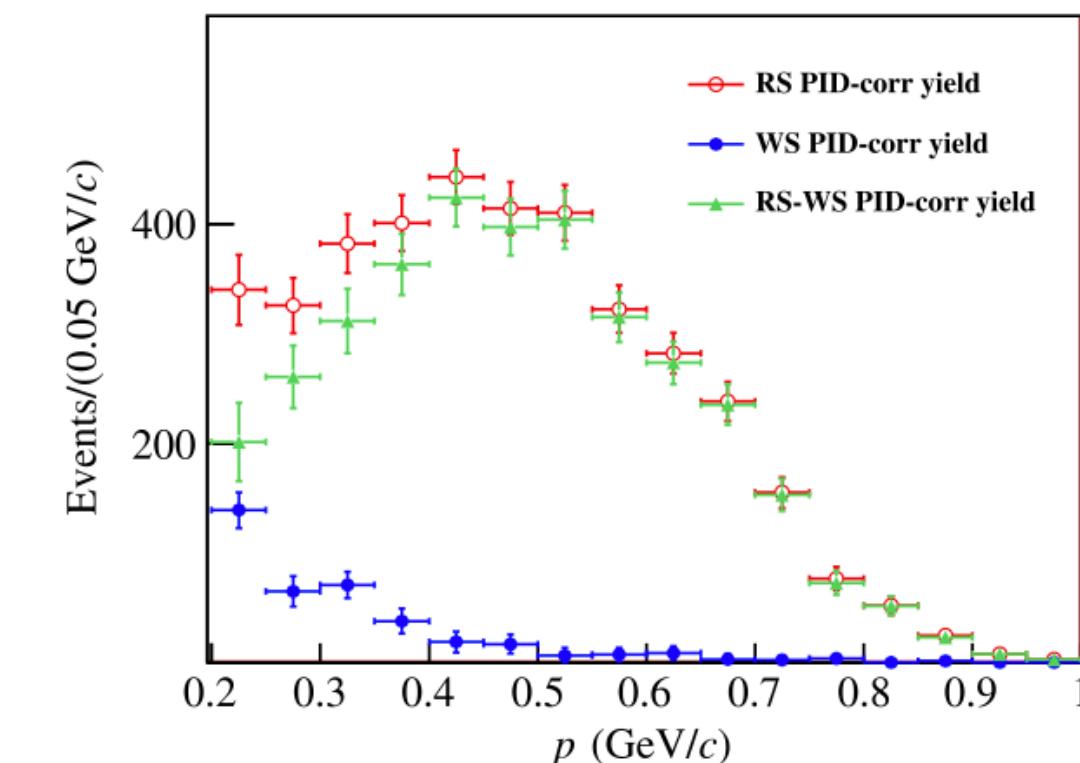
WS technique is used to subtract charge symmetric backgrounds in each momentum bin, e.g., $\pi^0 \rightarrow \gamma e^+ e^-$



$$\begin{bmatrix} N_e^{\text{obs}} \\ N_{\pi}^{\text{obs}} \\ N_K^{\text{obs}} \\ N_p^{\text{obs}} \end{bmatrix} = \begin{bmatrix} P_{e \rightarrow e} & P_{\pi \rightarrow e} & P_{K \rightarrow e} & P_{p \rightarrow e} \\ P_{e \rightarrow \pi} & P_{\pi \rightarrow \pi} & P_{K \rightarrow \pi} & P_{p \rightarrow \pi} \\ P_{e \rightarrow K} & P_{\pi \rightarrow K} & P_{K \rightarrow K} & P_{p \rightarrow K} \\ P_{e \rightarrow p} & P_{\pi \rightarrow p} & P_{K \rightarrow p} & P_{p \rightarrow p} \end{bmatrix} \begin{bmatrix} N_e^{\text{true}} \\ N_{\pi}^{\text{true}} \\ N_K^{\text{true}} \\ N_p^{\text{true}} \end{bmatrix}$$

PID migration matrix

Contamination of other particle types (p, π^+, K^+)



Reconstruct RS and WR sample
In different momentum bin

PID unfolding

WS subtraction

$$\mathcal{B}(\Lambda_c^+ \rightarrow X e^+ \nu_e) = (4.06 \pm 0.10_{\text{stat}} \pm 0.09_{\text{syst}})\%.$$

$$\frac{\Gamma(\Lambda_c^+ \rightarrow X e^+ \nu_e)}{\Gamma(D \rightarrow X e^+ \nu_e)} = 1.28 \pm 0.05$$

Compared with HQE(1.2), EQM(1.67)

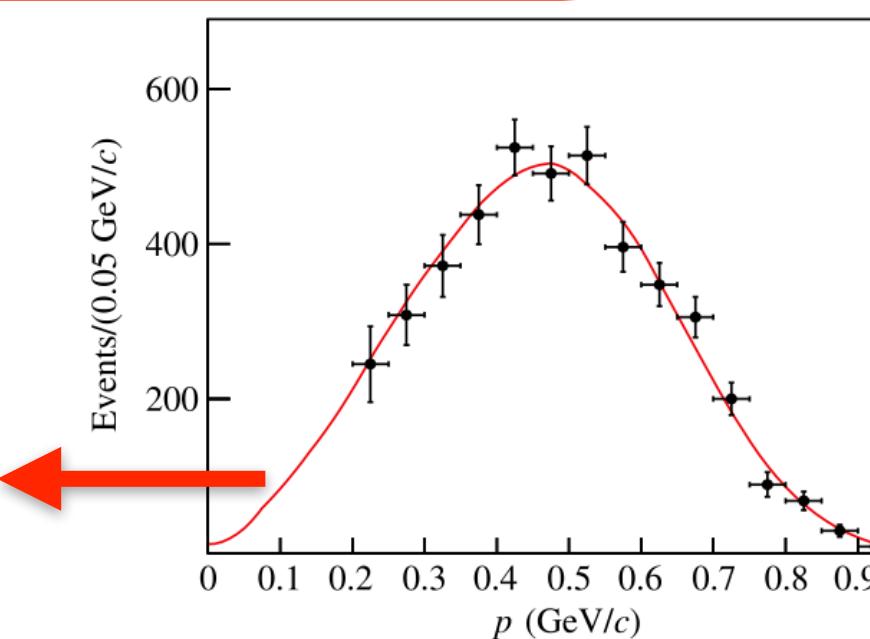
BF determination

PHSP Extrapolation

Tracking efficiency unfolding

Decay	\mathcal{B} [%]	Model
$\Lambda_c^+ \rightarrow \Lambda e^+ \nu_e$	$3.56 \pm 0.11 \pm 0.07$	References [6]
$\Lambda_c^+ \rightarrow p K^- (n \bar{K}^0) e^+ \nu_e$	$0.088 \pm 0.017 \pm 0.007$	PHSP [7]
$\Lambda_c^+ \rightarrow \Lambda(1405) e^+ \nu_e$	0.24	HQET [27,28]
$\Lambda_c^+ \rightarrow \Lambda(1520) e^+ \nu_e$	0.06	HQET [27,28]
$\Lambda_c^+ \rightarrow n e^+ \nu_e$	0.20	Quark model [29]

Based on our knowledge of MC model



$$N_e^{\text{true}}(i) = \sum_j A_{\text{TRK}}(e|i, j) N_e^{\text{prod}}(j)$$

- Geometrical acceptance
- Track reconstruction efficiency
- Resolution smearing

$$\Lambda_c^+ \rightarrow p K^- e^+ \nu_e$$

→ ST data set is same with last analysis

→ Select signal pK^-e^+ in the recoiling side of $\bar{\Lambda}_c^-$

→ Background veto

- ❖ Suppress $\Lambda_c^+ \rightarrow pK^-\pi^+$: $M_{pK^-e^+} < 2.15 \text{ GeV}/c^2$

- ❖ Suppress $\Lambda_c^+ \rightarrow pK^-\pi^+\pi^0$: Additional π^0 search and veto M_{BC} signal region

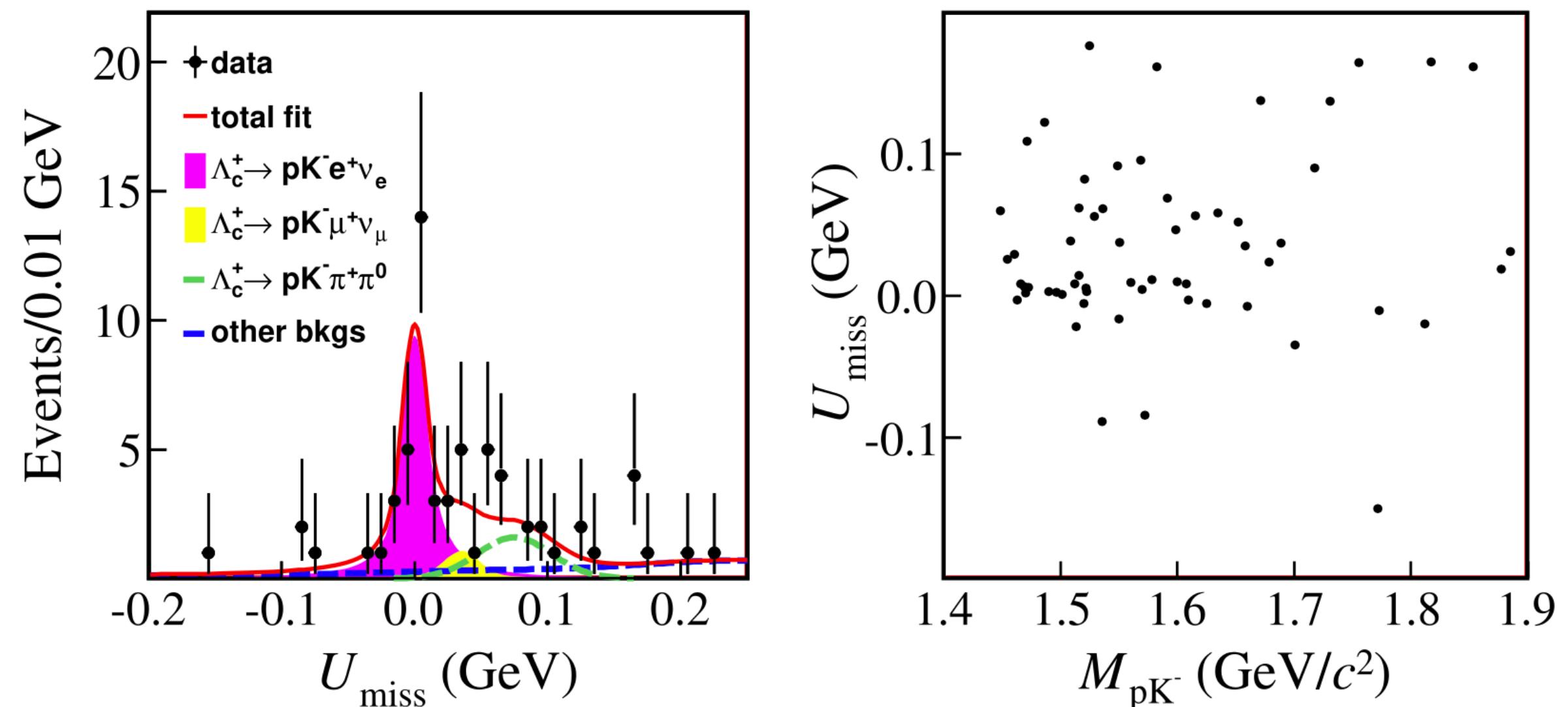
→ $\Lambda_c^+ \rightarrow pK^-e^+\nu_e$ is firstly observed with significance of 8.2σ !

- ❖ $\mathcal{B}(\Lambda_c^+ \rightarrow pK^-e^+\nu_e) = (0.82 \pm 0.15 \pm 0.06) \times 10^{-3}$

→ The only observed SL channel beyond $\Lambda_c^+ \rightarrow \Lambda l^+\nu_l$

- ❖ $\frac{\mathcal{B}(\Lambda_c^+ \rightarrow pK^-e^+\nu_e)}{\mathcal{B}(\Lambda_c^+ \rightarrow X e^+\nu_e)} = (2.1 \pm 0.4_{\text{stat.}} \pm 0.1_{\text{syst.}}) \times 10^{-3}$

$$N_{pK^-e^+\nu_e}^{\text{DT}} = 33.5 \pm 6.3$$



- Signal: Gaussian core + power law tail (ISR & FSR)
- BKG: $\Lambda_c^+ \rightarrow pK^-\pi^+\pi^0$ and $\Lambda_c^+ \rightarrow pK^-\mu^+\nu_\mu$

Yield of $\Lambda_c^+ \rightarrow pK^-\mu^+\nu_\mu$ is fixed

$$N_{\text{DT}}^{pK^-\mu^+\nu_\mu} = N_{\text{DT}}^{pK^-e^+\nu_e} \times R_\epsilon \times R_{\mathcal{B}}$$

$$R_{\mathcal{B}} = \frac{\mathcal{B}(\Lambda_c^+ \rightarrow pK^-\mu^+\nu_\mu)}{\mathcal{B}(\Lambda_c^+ \rightarrow pK^-e^+\nu_e)} = 0.88 \pm 0.03$$

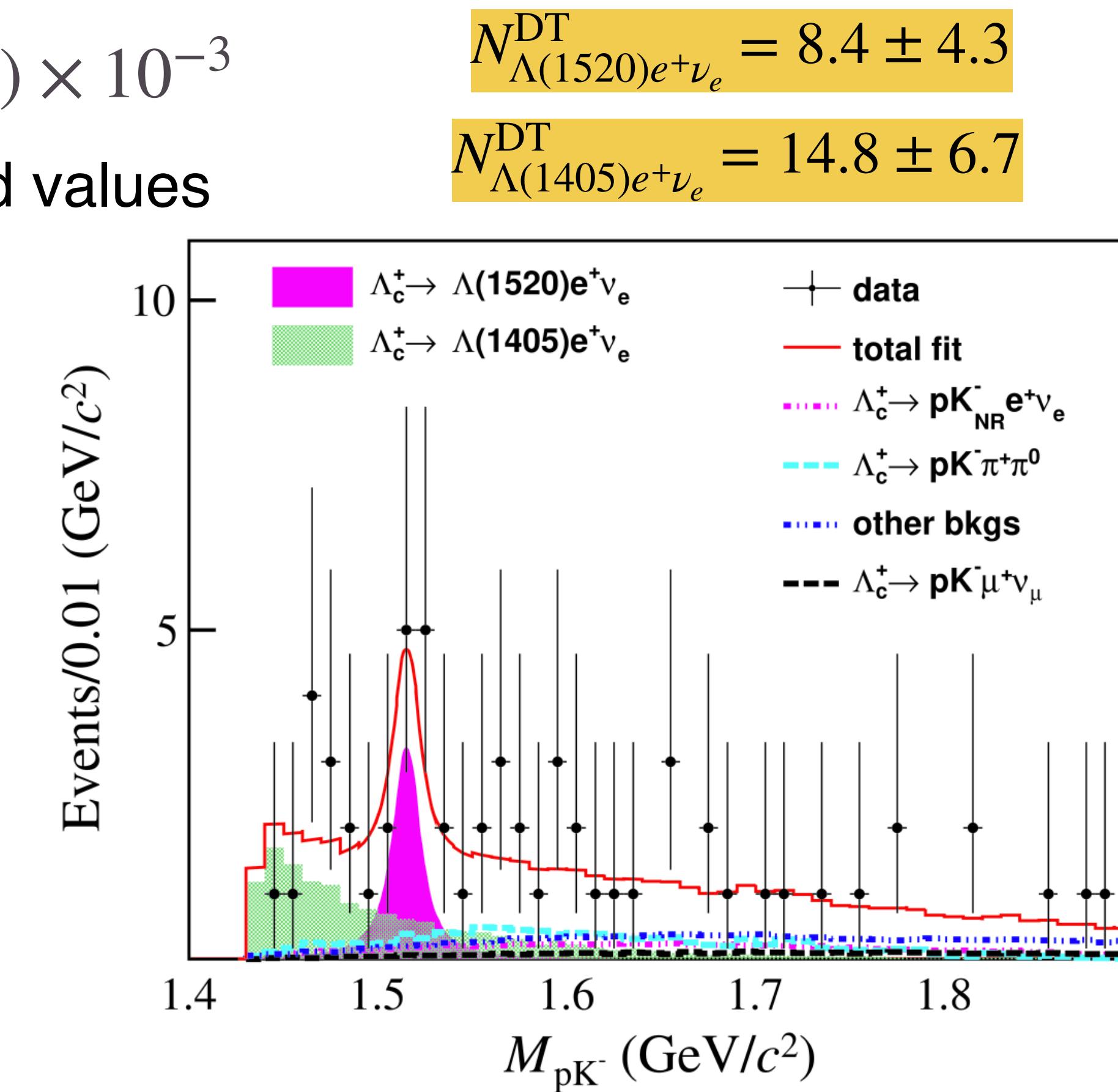
Relative detection efficiency $R_\epsilon = 0.15$

Search for $\Lambda(1405)$ and $\Lambda(1520)$ in pK^- spectrum

- 2D fit is performed to the M_{pK^-} and U_{miss} distributions
- Evidence of $\Lambda_c^+ \rightarrow \Lambda(1520)e^+\nu_e$ (3.3σ) & $\Lambda_c^+ \rightarrow \Lambda(1405)e^+\nu_e$ (3.2σ)
 - ❖ $\mathcal{B}(\Lambda_c^+ \rightarrow \Lambda(1520)e^+\nu_e) = (1.02 \pm 0.52_{\text{stat.}} \pm 0.11_{\text{syst.}}) \times 10^{-3}$
 - ❖ $\mathcal{B}(\Lambda_c^+ \rightarrow \Lambda(1405)[\rightarrow pK^-]e^+\nu_e) = (0.42 \pm 0.19_{\text{stat.}} \pm 0.04_{\text{syst.}}) \times 10^{-3}$
- Comparisons of $\mathcal{B}(\Lambda_c^+ \rightarrow \Lambda(1520)/\Lambda(1405)e^+\nu_e)$ with predicted values from theoretical models and LQCD
 - ❖ Consistent within two standard deviations
- Prospects
 - ❖ Amplitude analysis of pK^- mass spectrum to study Λ^*
 - ❖ Extraction of $\Lambda_c^+ \rightarrow \Lambda(1520)$ FF

TABLE I. Comparison of $\mathcal{B}(\Lambda_c^+ \rightarrow \Lambda(1520)/\Lambda(1405)e^+\nu_e)$ [in $\times 10^{-3}$] between theoretical calculations and this measurement. The BF of $\Lambda(1405) \rightarrow pK^-$ is unknown [2].

	$\mathcal{B}(\Lambda_c^+ \rightarrow \Lambda(1520)e^+\nu_e)$	$\mathcal{B}(\Lambda_c^+ \rightarrow \Lambda(1405)e^+\nu_e)$
Constituent quark model [8]	1.01	3.04
Molecular state [9]	...	0.02
Nonrelativistic quark model [10]	0.60	2.43
Lattice QCD [12,13]	0.512 ± 0.082	...
Measurement	$1.02 \pm 0.52 \pm 0.11$	$\frac{0.42 \pm 0.19 \pm 0.04}{\mathcal{B}(\Lambda(1405) \rightarrow pK^-)}$

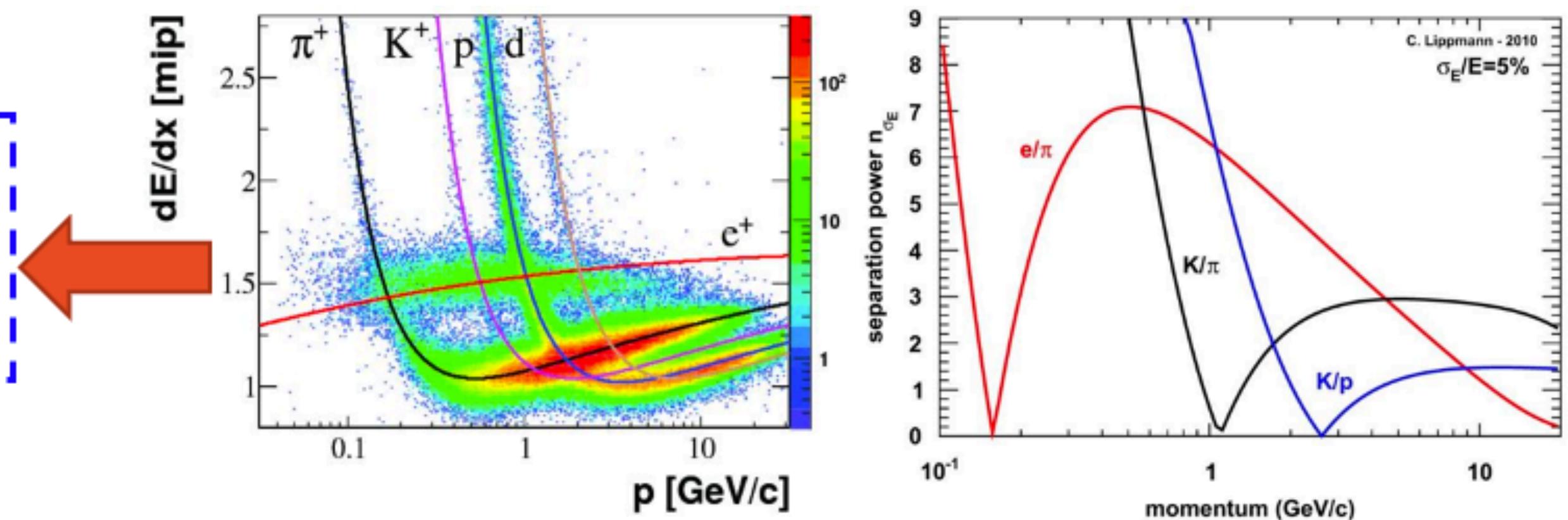


$$\Lambda_c^+ \rightarrow \Lambda\pi^+\pi^-e^+\nu_e, pK_S^0\pi^-e^+\nu_e$$

- Search for $\Lambda_c^+ \rightarrow \Lambda^* e^+ \nu_e$: $\Lambda\pi^+\pi^-$ and $pK_S^0\pi^-$ are used to tag Λ^*
 - ❖ $\mathcal{B}(\Lambda(1520) \rightarrow \Lambda\pi^+\pi^-) = (10 \pm 1)\%$
 - ❖ Higher excited Λ^* states may decay to $pK^*(892)^-, K^*(892)^- \rightarrow K_S^0\pi^-$

- ST data set reconstructed by 12 hadronic $\bar{\Lambda}_c^-$ decay mode
- Reconstruct $\Lambda [\rightarrow p\pi^-]\pi^+\pi^-e^+$ and $pK_S^0 [\rightarrow \pi^+\pi^-]\pi^-e^+$ in the recoiling side of $\bar{\Lambda}_c^-$
- Challenge from misID between e and π

- ✓ The phase space of 5-body decay is very small
- ✓ Low momentum of e/π causes serious misidentification



Background Study

→ Tight PID requirement to generally improve PID ability

- ❖ Valid e EMC hit information
- ❖ Tight $\text{Prob}(e)/[\text{Prob}(e)+\text{Prob}(\pi)+\text{Prob}(K)]$ requirement

→ γ -conversion background

- ❖ $\Lambda_c^+ \rightarrow \Lambda \pi^+ \pi^0, \Sigma^0 \pi^+ \pi^0 (pK_S^0 \pi^0, pK_S^0 \eta), \pi^0/\eta \rightarrow \gamma\gamma$
- ❖ Under the action of the nucleus, γ converts into electron-positron pair
- ❖ Require a large angle between e and π

→ $\Lambda \pi^+ \pi^- \pi^+ (pK_S^0 \pi^- \pi^+)$ background

- ❖ Veto $M_{\Lambda \pi^+ \pi^- e(\pi)^+} (M_{pK_S^0 \pi^- e(\pi)^+})$, where $e(\pi)^+$ means that M_{e^+} is replaced by M_{π^+}

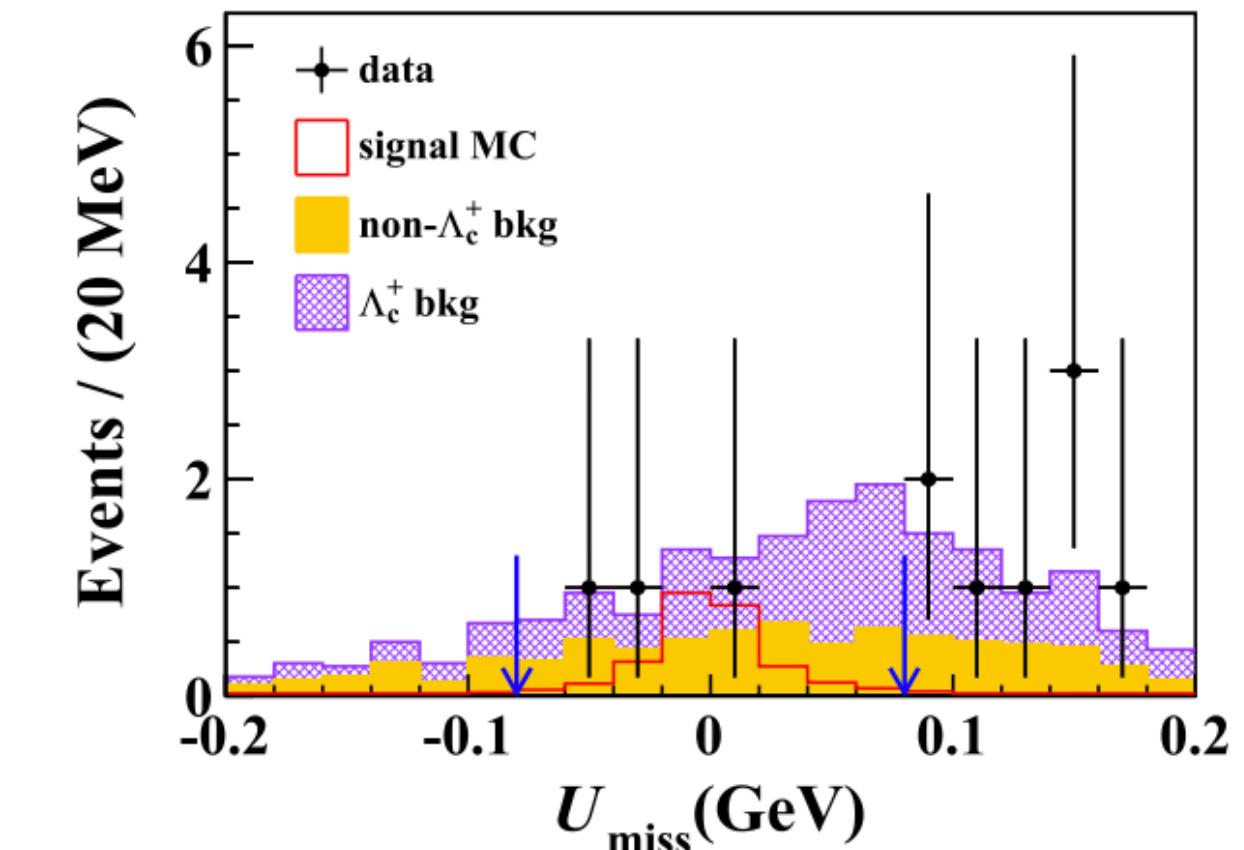
→ Miss- $\pi^0(\gamma)$ background

- ❖ $\Lambda_c^+ \rightarrow \Lambda \pi^+ \omega/\eta, \omega/\eta \rightarrow \pi^+ \pi^- \pi^0$ or $\Sigma^0 \pi^+ \pi^- \pi^+, \Sigma^0 \rightarrow \gamma \Lambda,$
 $\Lambda_c^+ \rightarrow pK_S^0 \eta, \eta \rightarrow \pi^+ \pi^- \pi^0$ or $\eta \rightarrow \gamma e^+ e^-$

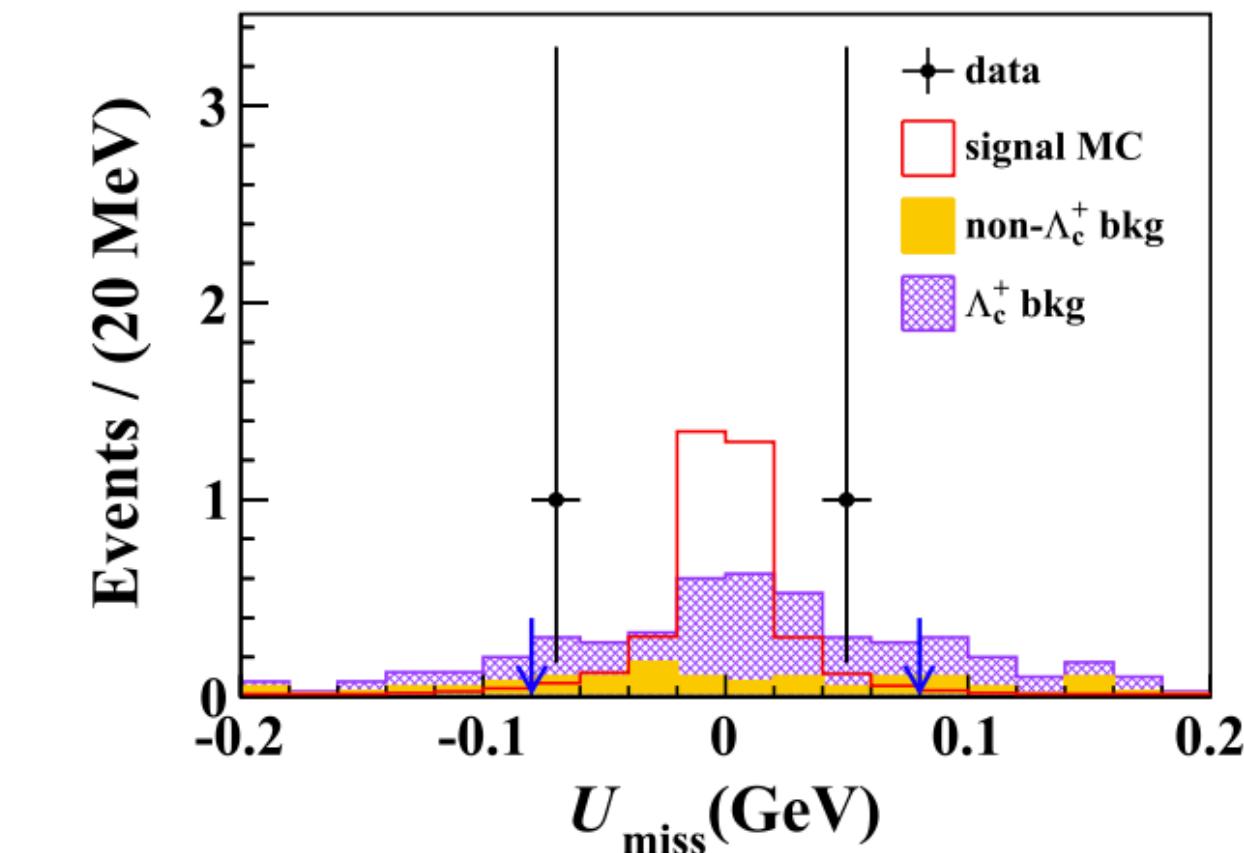
- ❖ Require a large angle between P_{miss} and the most energetic shower



U_{miss} distribution after all cuts



$$\Lambda_c^+ \rightarrow \Lambda \pi^+ \pi^- e^+ \nu_e$$



$$\Lambda_c^+ \rightarrow pK_S^0 \pi^- e^+ \nu_e$$

Upper limits

- Profile likelihood method
- Joint likelihood

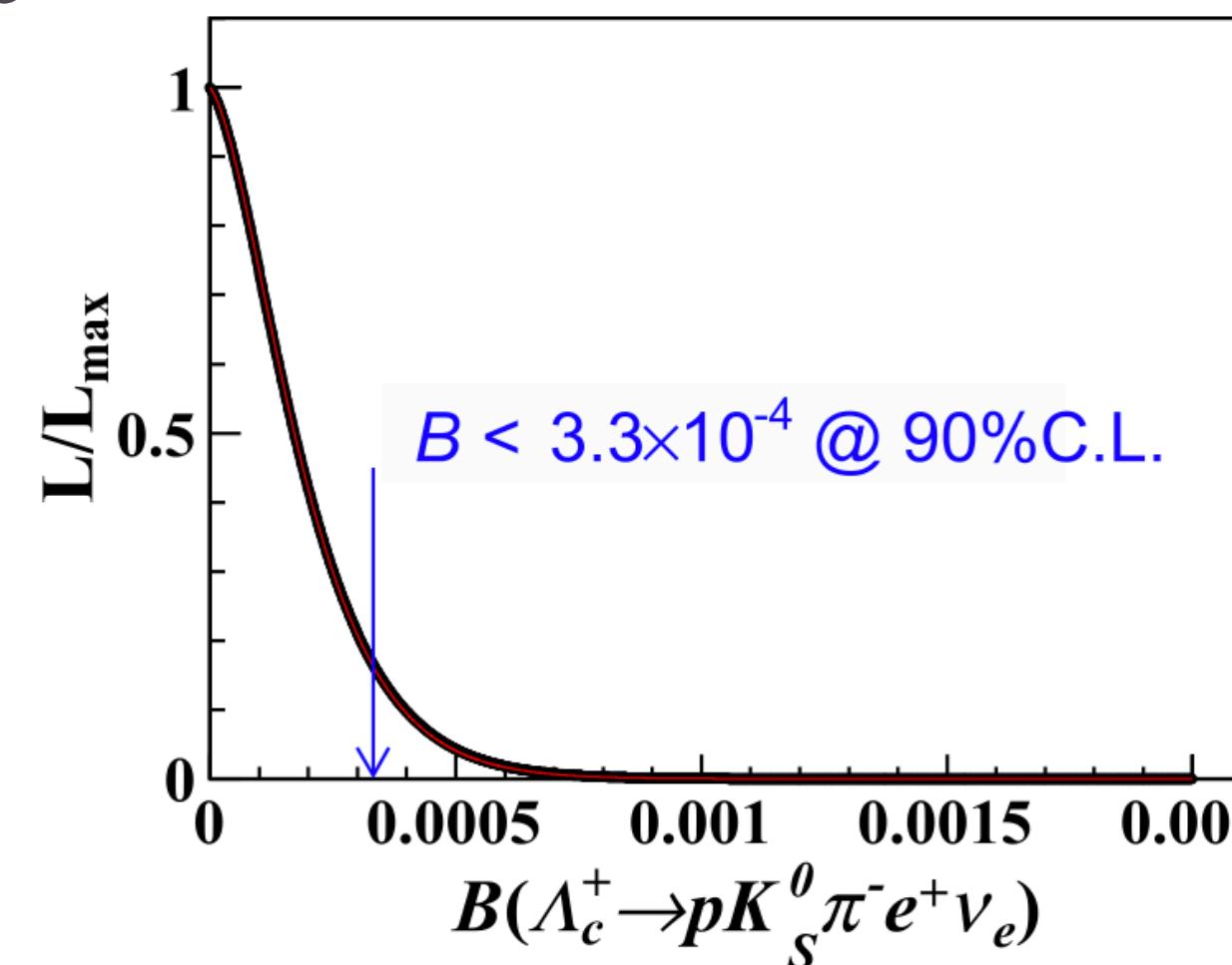
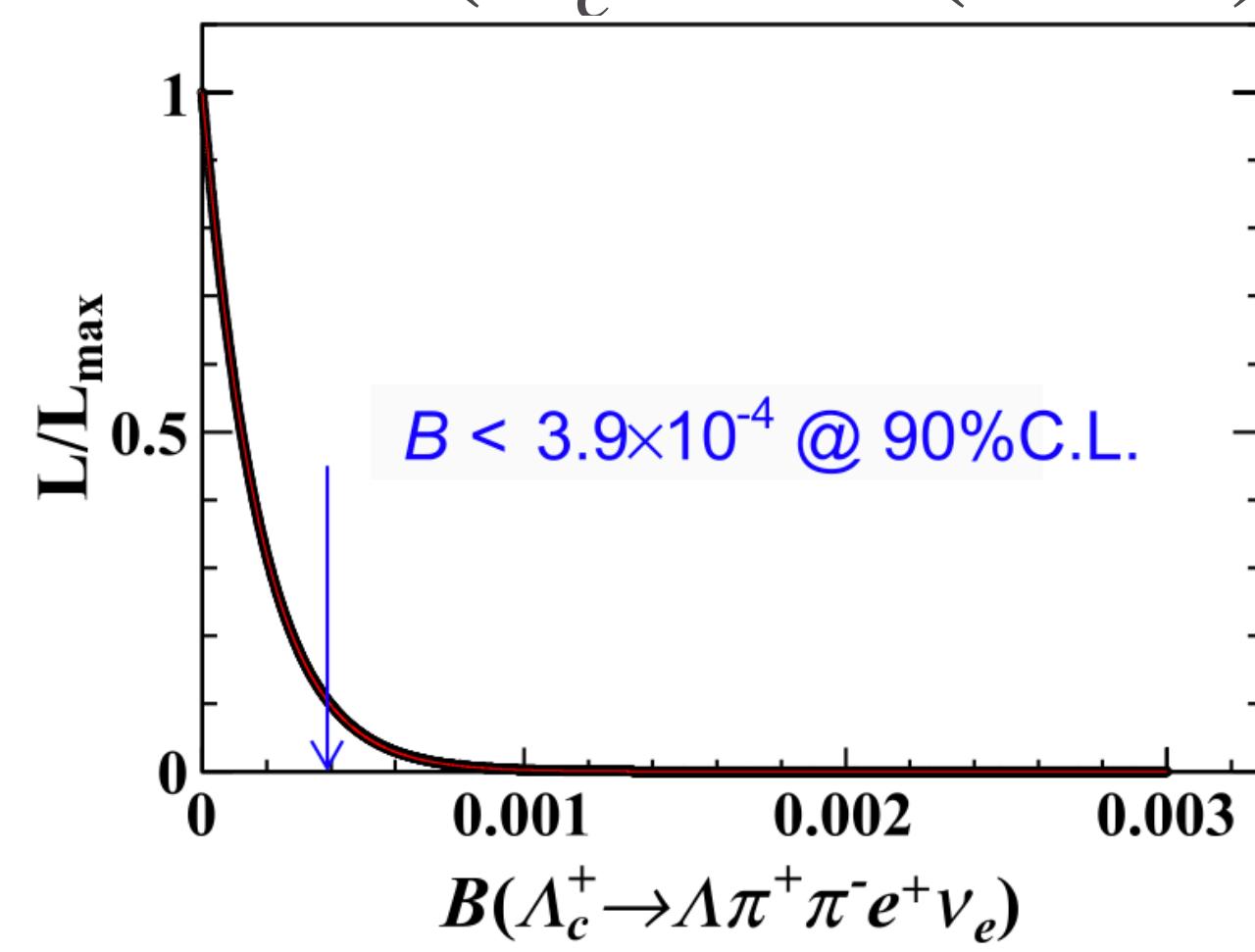
$$\begin{aligned} \mathcal{L} = & \mathcal{P}(N^{\text{obs}} | N^{\text{eff}} \cdot \mathcal{B} + N_{\text{bkg1}} + N_{\text{bkg2}}) \\ & \cdot \mathcal{G}(N^{\text{eff}} | \mathcal{B}^{\text{inter}} \cdot N^{\text{ST}} \cdot \varepsilon^{\text{sig}}, \mathcal{B}^{\text{inter}} \cdot N^{\text{ST}} \cdot \varepsilon^{\text{sig}} \cdot \sigma) \\ & \cdot \mathcal{P}(N_{\text{bkg1}}^{\text{SB}} | N_{\text{bkg1}} / r) \\ & \cdot \mathcal{G}(N_{\text{bkg2}} | N_{\text{bkg2}}^{\text{MC}}, \sigma_{\text{bkg2}}^{\text{MC}}). \end{aligned}$$



Use Bayesian statistics



- Based on the Bayesian statistics, the likelihood distribution as a function of BF is obtained
- The ULs at the 90% confidence level (CL) are determined
 - ❖ Assuming that all the $\Lambda\pi^+\pi^-$ combinations come from $\Lambda(1520)/\Lambda(1600)$,
 - $\mathcal{B}(\Lambda_c^+ \rightarrow \Lambda(1520)e^+\nu_e) < 4.3 \times 10^{-3}$ @ 90 % CL
 - $\mathcal{B}(\Lambda_c^+ \rightarrow \Lambda(1600)e^+\nu_e) < 9.0 \times 10^{-3}$ @ 90 % CL



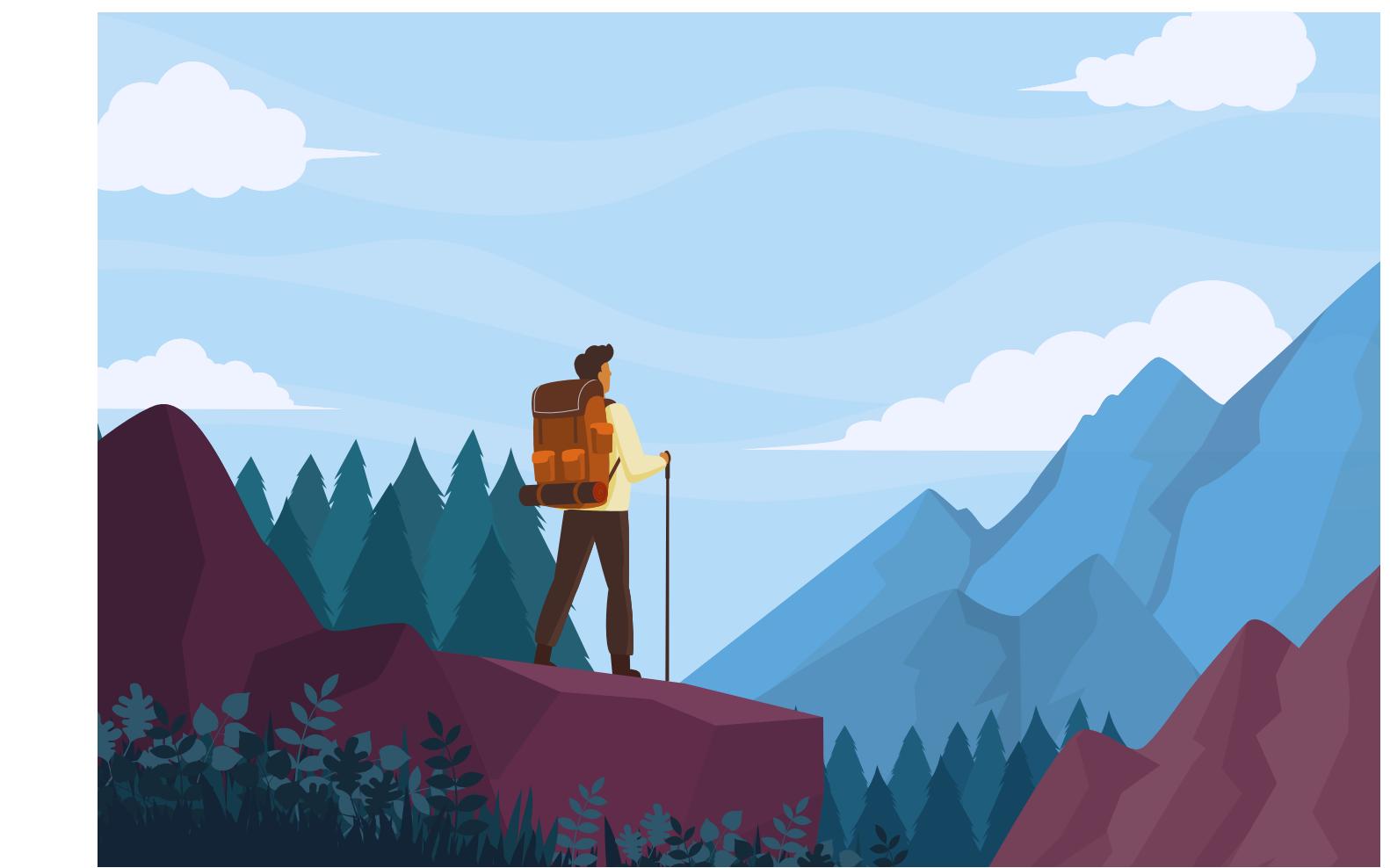
Λ^* state	CQM [8]	NRQM [9]	LFQM [10]	LQCD [11]
$\Lambda(1520)$	10.00	5.94	--	5.12 ± 0.82
$\Lambda(1600)$	4.00	1.26	(0.7 ± 0.2)	--
$\Lambda(1890)$	--	3.16×10^{-2}	--	--
$\Lambda(1820)$	--	1.32×10^{-2}	--	--

Limited sensitivity to identify different theoretical calculations

Other ongoing analysis

Roadmap of $\Lambda_c^+ SL$

- $\mathcal{B}(\Lambda_c^+ \rightarrow X e^+ \nu_e) = (4.06 \pm 0.10_{\text{stat.}} \pm 0.09_{\text{syst.}}) \%$
- $\mathcal{B}(\Lambda_c^+ \rightarrow \Lambda e^+ \nu_e) = (3.56 \pm 0.11_{\text{stat.}} \pm 0.07_{\text{syst.}}) \%$
- $\mathcal{B}(\Lambda_c^+ \rightarrow p K^- e^+ \nu_e) = (0.82 \pm 0.15 \pm 0.06) \times 10^{-3}$
- ❖ $\mathcal{B}(\Lambda_c^+ \rightarrow \Lambda(1520) e^+ \nu_e) = (1.02 \pm 0.52_{\text{stat.}} \pm 0.11_{\text{syst.}}) \times 10^{-3}$



- $\frac{\mathcal{B}(\Lambda_c^+ \rightarrow \Lambda e^+ \nu_e) + \mathcal{B}(\Lambda_c^+ \rightarrow p K^- e^+ \nu_e)}{\mathcal{B}(\Lambda_c^+ \rightarrow X e^+ \nu_e)} = (89.7 \pm 4.3) \% \Rightarrow (85.4 \sim 94.0) \%$
- $\mathcal{B}(\Lambda_c^+ \rightarrow \text{non}[\Lambda, pK^-] e^+ \nu_e) = (4.18 \pm 1.75) \times 10^{-3} \Rightarrow (2.43 \sim 5.93) \times 10^{-3}$

- $\Lambda^* e^+ \nu_e: \Sigma \pi e^+ \nu_e, n \bar{K}^0 e^+ \nu_e$
- $N^{(*)} e^+ \nu_e: n e^+ \nu_e, N(1535) e^+ \nu_e$

Next stage

sub- 10^{-3} level rooms

Stay tuned

$$\rightarrow \Lambda_c^+ \rightarrow n e^+ \nu_e$$

- ❖ Singly Cabibbo-suppressed transition $c \rightarrow d$
- ❖ Various theoretical-model calculations
- ❖ Challenge in experimental study
 - Two missing particles: n and ν_e
 - Huge background from $\Lambda_c^+ \rightarrow \Lambda e^+ \nu_e$

$$\rightarrow \Lambda_c^+ \rightarrow \Sigma \pi e^+ \nu_e$$

- ❖ $\mathcal{B}(\Lambda(1405) \rightarrow \Sigma \pi) \approx 100\%$ and $\mathcal{B}(\Lambda(1520) \rightarrow \Sigma \pi) \approx (42 \pm 1)\%$

- ❖ Search for Λ^* in $\Sigma \pi$ invariant mass spectrum

- ❖ Nature of $\Lambda(1405)$?

- uds bound state, dynamically generated molecular state, multi-quark state

$$\rightarrow \Lambda_c^+ \rightarrow p \pi^- (\text{non-}\Lambda) e^+ \nu_e$$

- ❖ Singly Cabibbo-suppressed transition to nucleon excited states $c(\Lambda_c^+) \rightarrow d(N^*)$

- ❖ $\mathcal{B}(\Lambda_c^+ \rightarrow N^*(1535) e^+ \nu_e)$: 4.03×10^{-5} (8.06×10^{-5})^[1], 6.4×10^{-3} (7.7×10^{-4})^[2]

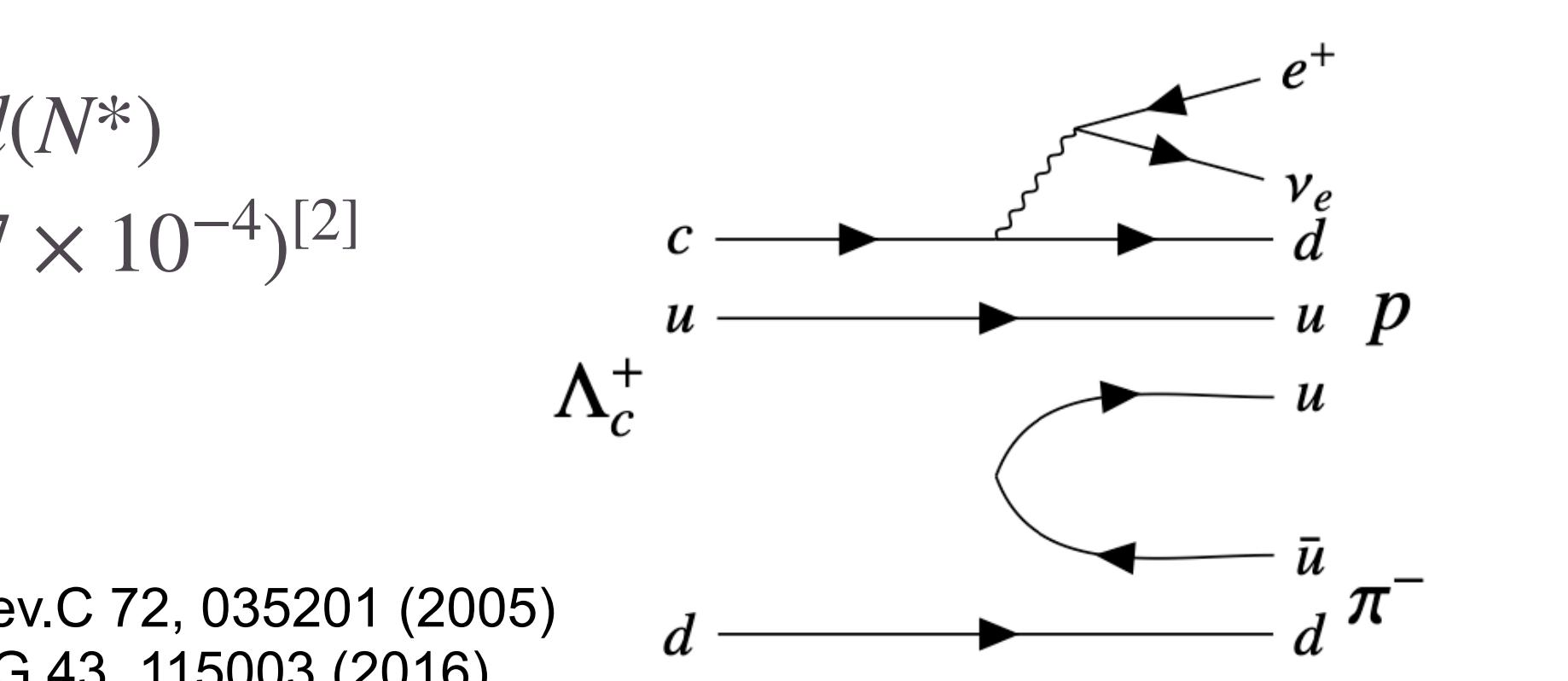
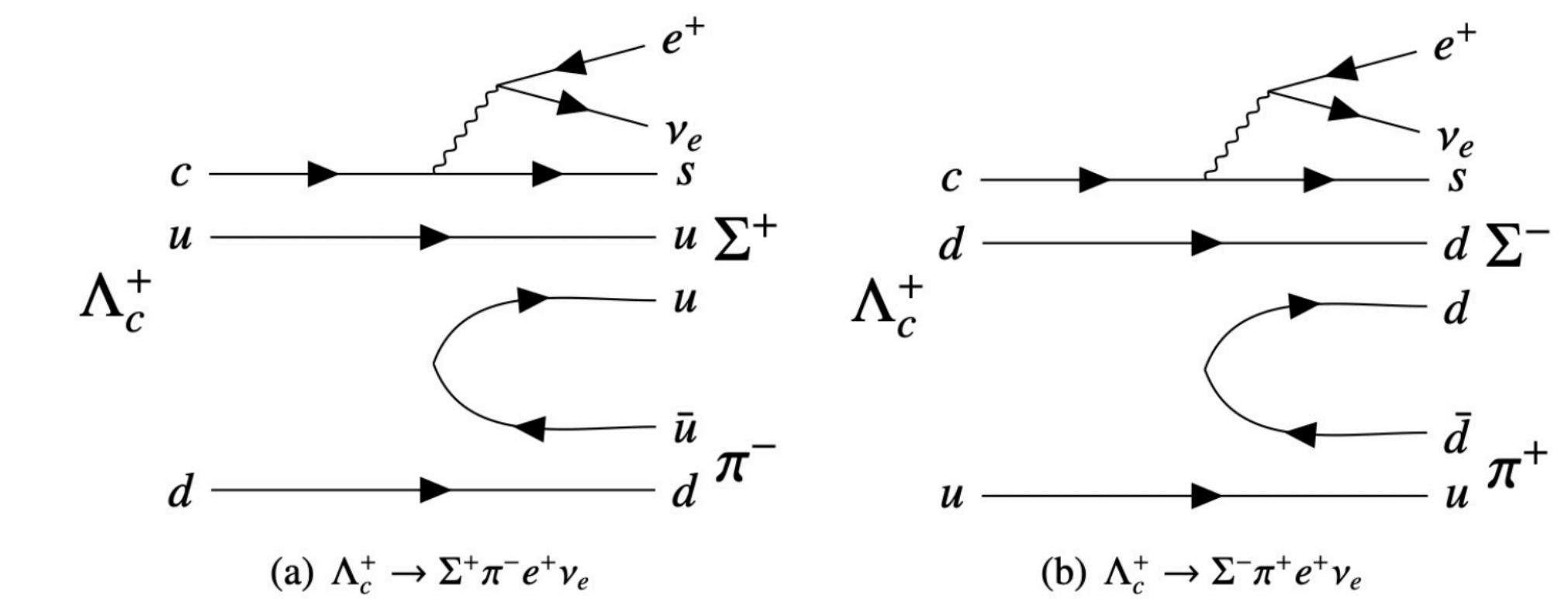
$$\rightarrow \Lambda_c^+ \rightarrow n K_S^0 e^+ \nu_e$$

- ❖ Isospin-symmetric channel to $p K^-$

- ❖ Similar challenge with $n e^+ \nu_e$: two missing particles

Chin.J.Phys. 78, 324 (2022)

Process	NRQM [232]	RQM [236]	RQM [237]	QSR [243]	QSR [244]	CQM [238]	LQCD [248, 249]	LFQM [227]	SU(3) [251]	Expt [31]	
$\Lambda_c^+ \rightarrow \Lambda^0 e^+ \nu_e$	3.0 (2.2)	1.4	3.25	2.6 ± 0.4	3.0 ± 0.3	2.78	3.8 ± 0.2	4.04	3.6 ± 0.4	3.6 ± 0.4	
			-0.812	-1	-0.88 ± 0.03				-0.86 ± 0.03	-0.86 ± 0.04	
$\Lambda_c^+ \rightarrow \Lambda^0 \mu^+ \nu_\mu$				3.14				3.7 ± 0.2	3.90	3.6 ± 0.4	3.5 ± 0.5
$\Lambda_c^+ \rightarrow n e^+ \nu_e$	0.22 (0.34)	0.26	0.268			0.20	0.41			-0.86 ± 0.04	0.49 ± 0.05
											-0.89 ± 0.04



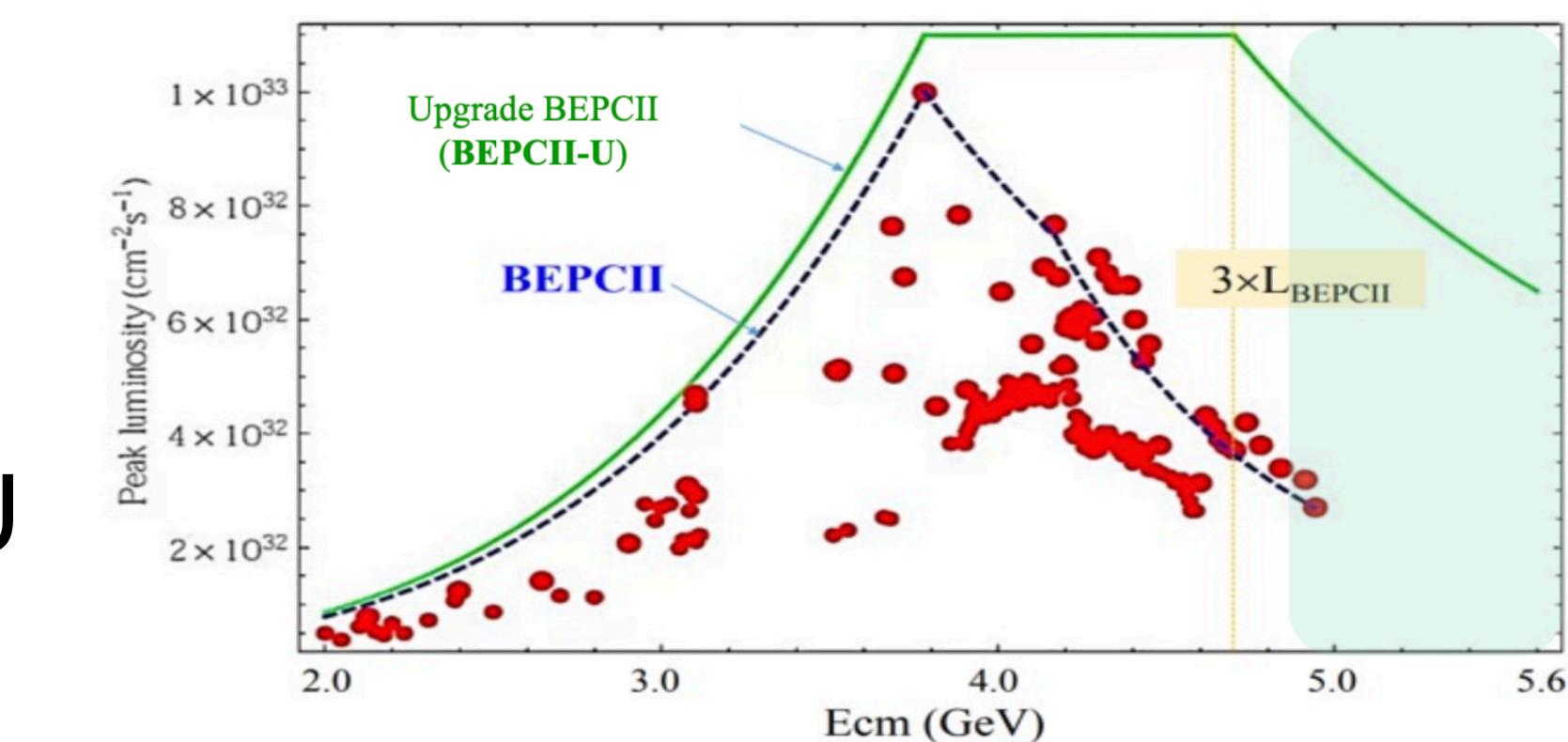
- [1] *Phys.Rev.C* 72, 035201 (2005)
 [2] *J.Phys.G* 43, 115003 (2016)

Summary

Summary & outlook

- Semi-leptonic Λ_c^+ decays provide good opportunities to study the dynamics of charm baryons, test Standard Model and probe new physics
- Improved measurement of $\Lambda_c^+ \rightarrow \Lambda l^+ \nu_l$ and $\Lambda_c^+ \rightarrow X e^+ \nu_e$
- First search for $\Lambda_c^+ \rightarrow \Lambda^* e^+ \nu_e$ in pK^- , $\Lambda\pi^+\pi^-$, $pK_S^0\pi^-$ channels
- More physics results coming soon
- Larger data samples will be collected at BESIII after BEPCII-U

Thanks for your attention!



Backup

z -expansion

→ z -expansion: FF is q^2 dependent, refer to LQCD parameterization

- ❖ m_{pole}^f : pole mass, $m_{\text{pole}}^{f_+, f_\perp} = 2.112 \text{ GeV}/c^2$ and $m_{\text{pole}}^{g_+, g_\perp} = 2.460 \text{ GeV}/c^2$
- ❖ a_0^f and α_1^f : free parameters
- ❖ $z(q^2) = [(\sqrt{t_+ - q^2} - \sqrt{t_+ - t_0}) / (\sqrt{t_+ - q^2} + \sqrt{t_+ - t_0})]$ with
 $t_0 = q_{\max}^2 = (m_{\Lambda_c} - m_\Lambda)^2$, $t_+ = (m_D - m_K)^2$
- ❖ $m_D = 1.870 \text{ GeV}/c^2$ and $m_K = 0.494 \text{ GeV}/c^2$

$$f(q^2) = \frac{a_0^f}{1 - q^2 / (m_{\text{pole}}^f)^2} [1 + \alpha_1^f \times z(q^2)]$$

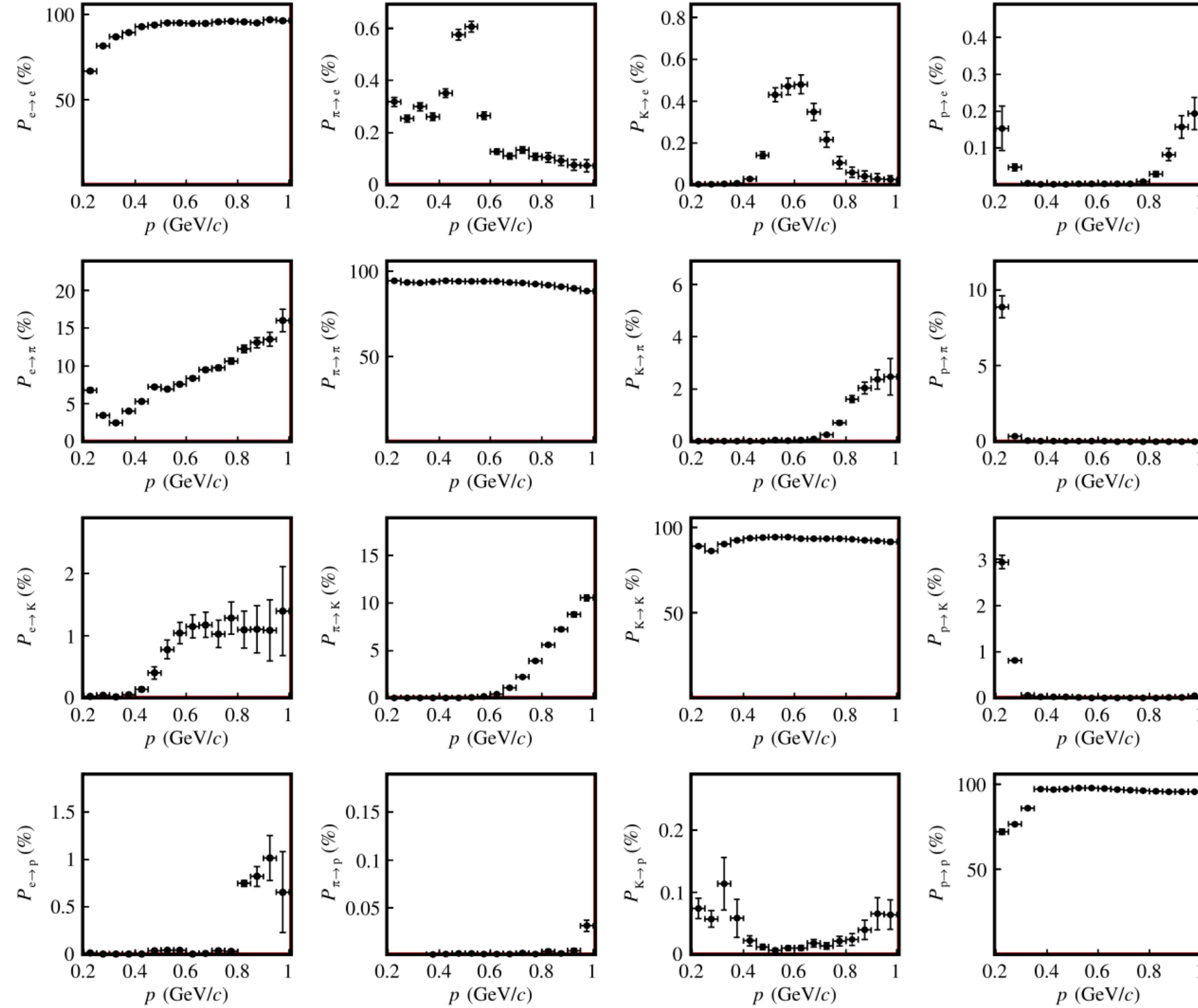
$$\Lambda_c^+ \rightarrow X e^+ \nu_e$$
FIG. 4. PID efficiencies as a function of momentum used to populate the A_{PID} matrices.

TABLE I. Positron yield in data after each procedure. The listed uncertainties are statistical.

Correction (see text)	RS yields	WS yields
Observed yields	3706 ± 71	394 ± 31
PID unfolding yields	3865 ± 80	376 ± 33
WS subtraction	3489 ± 87	
Tracking unfolding yields	4333 ± 107	
Extrapolation	4692 ± 117	

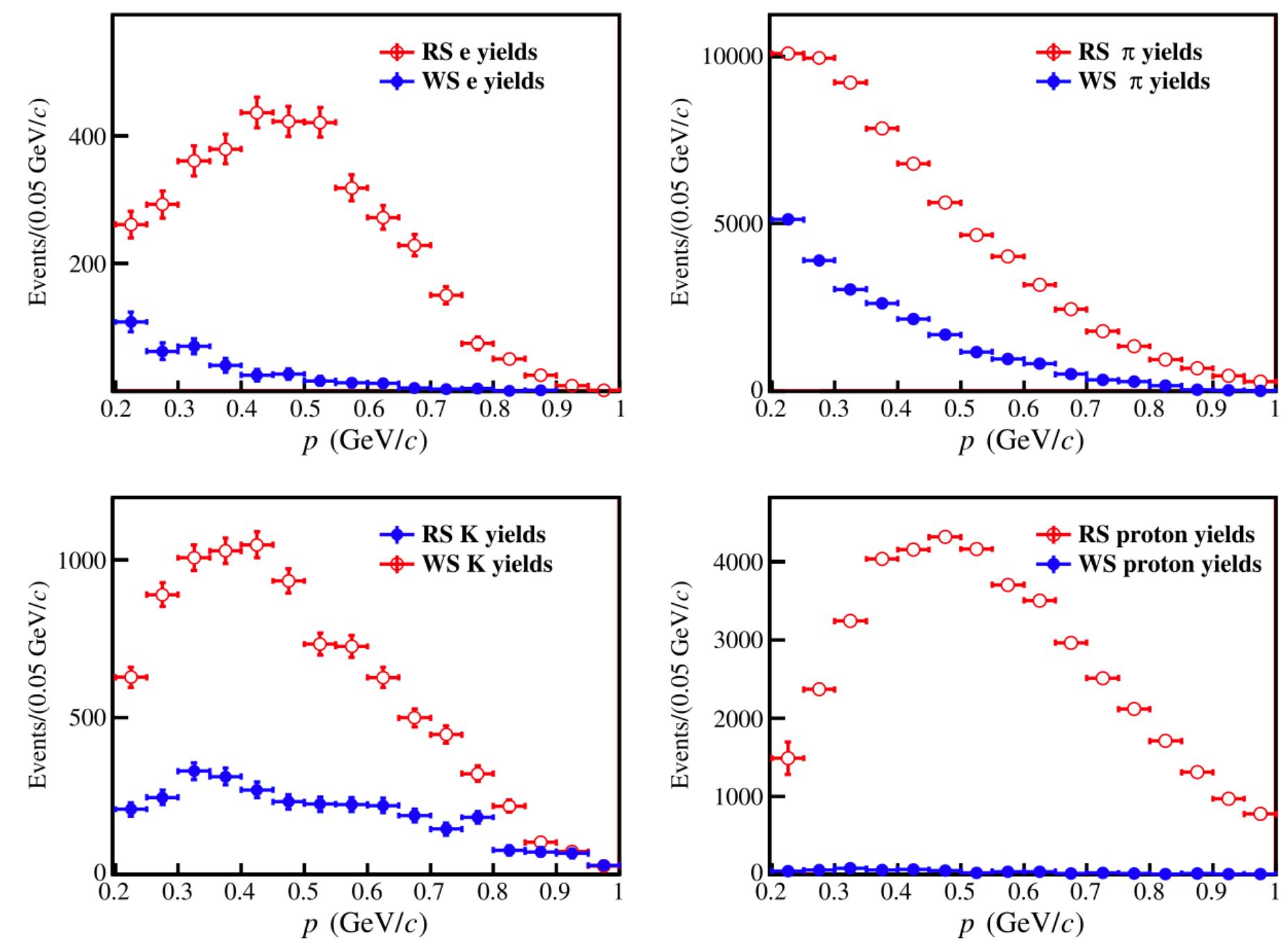


FIG. 3. Measured RS (blue) and WS (red) yields for each particle category as a function of momentum.

$\Lambda_c^+ \rightarrow \Lambda\pi^+\pi^-e^+\nu_e, pK_S^0\pi^-e^+\nu_e$ Signal yields & BKG number estimation

→ No signals observed on data, plan to setting upper limits (ULs) on BFs 😞

→ The backgrounds separated into two categories:

- ❖ Non- Λ_c^+ background, denoted as bkg1 ⇒ Estimated by data sideband region
- ❖ Λ_c^+ background, denoted as bkg2 ⇒ Estimated by MC simulation

→ The observed events N^{obs} follows a Poisson distribution(\mathcal{P})

- ❖ $N^{\text{obs}} \sim \mathcal{P}(N^{\text{obs}} | N_{\text{sig}} + N_{\text{bkg1}} + N_{\text{bkg2}})$

→ The signal event number $N_{\text{sig}} = \mathcal{B}_{\text{sig}} \cdot \mathcal{B}^{\text{inter}} \cdot N^{\text{ST}} \cdot \varepsilon^{\text{sig}} = \mathcal{B}_{\text{sig}} \cdot N^{\text{eff}}$

- ❖ $N^{\text{eff}} \sim \mathcal{G}(N^{\text{eff}} | \mathcal{B}^{\text{inter}} \cdot N^{\text{ST}} \cdot \varepsilon^{\text{sig}}, \mathcal{B}^{\text{inter}} \cdot N^{\text{ST}} \cdot \varepsilon^{\text{sig}} \cdot \sigma)$ ⇒ Rely on systematic uncertainty study