

第十七届粒子物理、核物理和宇宙学交叉学科前沿问题研讨会 (2024.07.12-  
2024.07.17, 贵州省、贵阳市、贵州财经大学)

# Axion-like particle triggered baryogenesis

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晁伟 (北京师范大学)

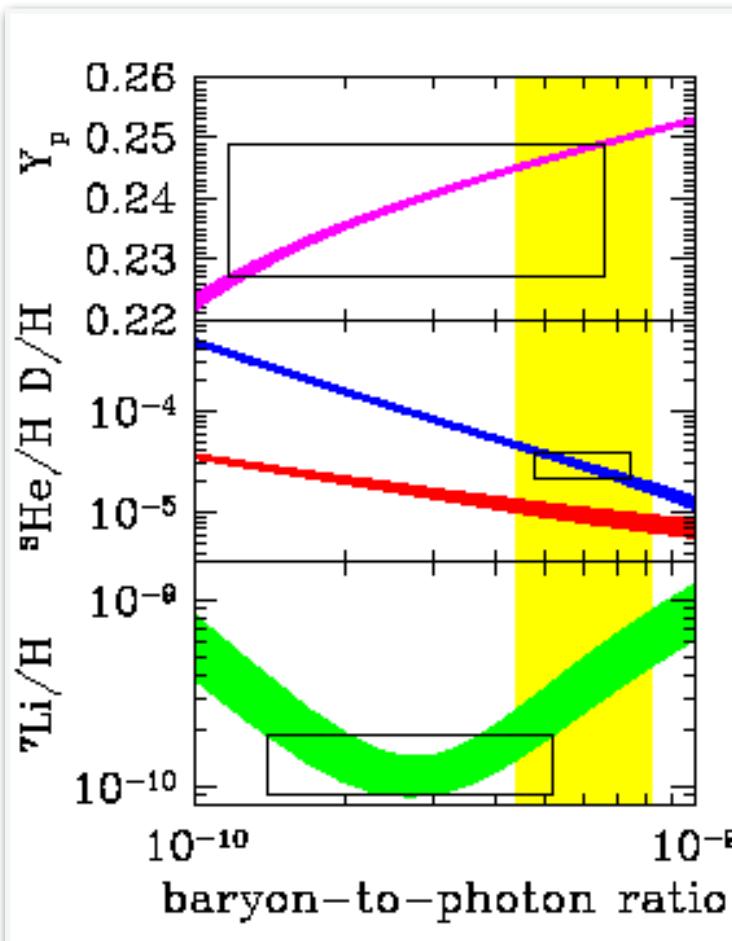
2024年07月13日

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# New physics—The Baryon asymmetry

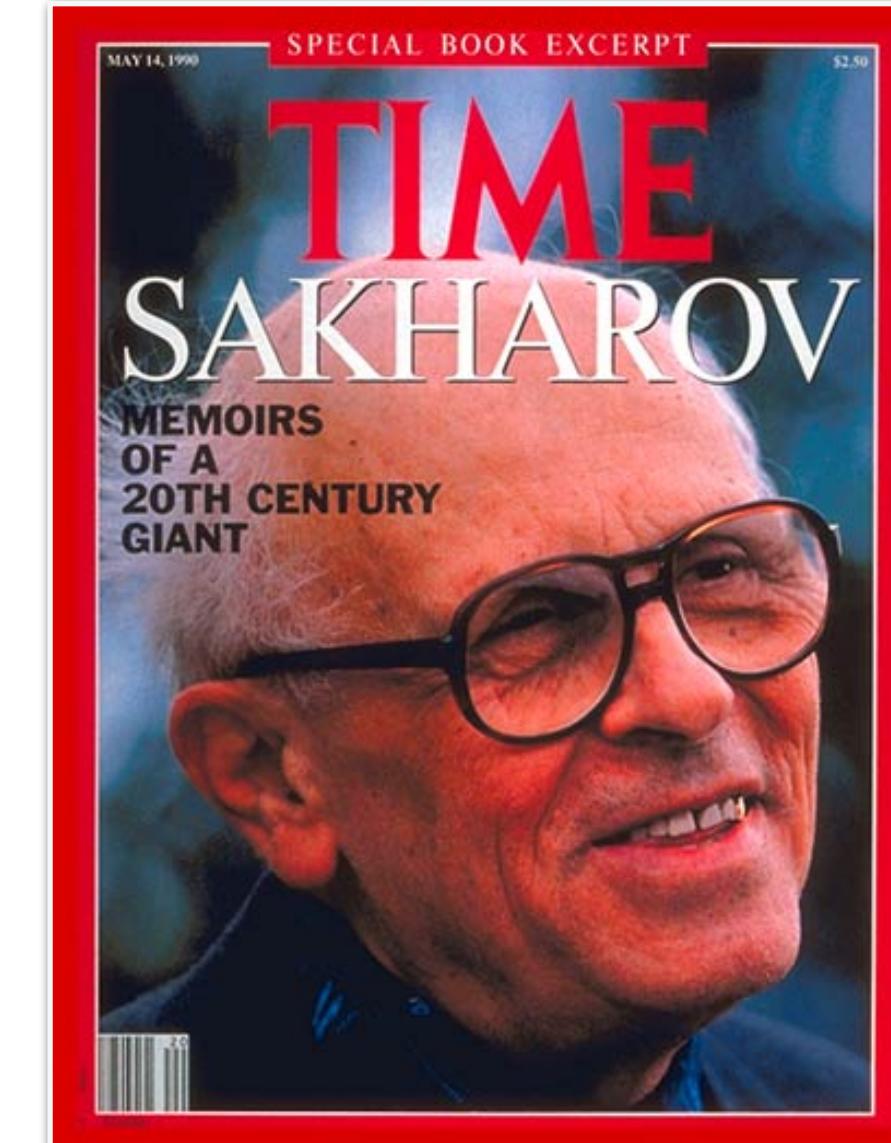
## Matter-antimatter asymmetry

- \* 没有观测到反物质星系，否则光学望远镜会观测到星系湮灭的射线
- \* 元素的原初丰度以及CMB功率谱的形状都依赖于重子数与光子数之比

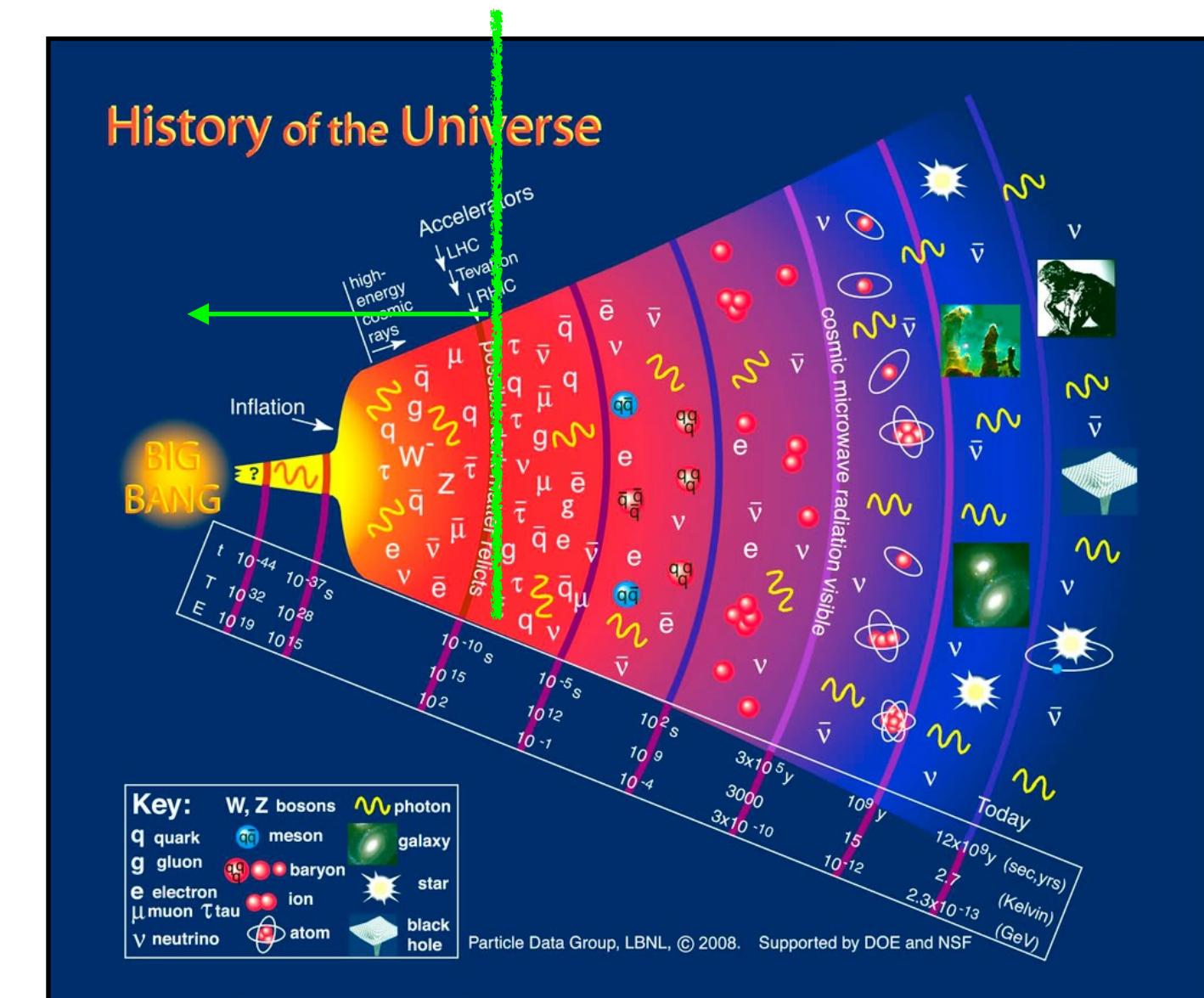


Baryon asymmetry:  $Y_B = \frac{\rho_B}{s} = (8.59 \pm 0.11) \times 10^{-11}$  Planck

## Baryogenesis



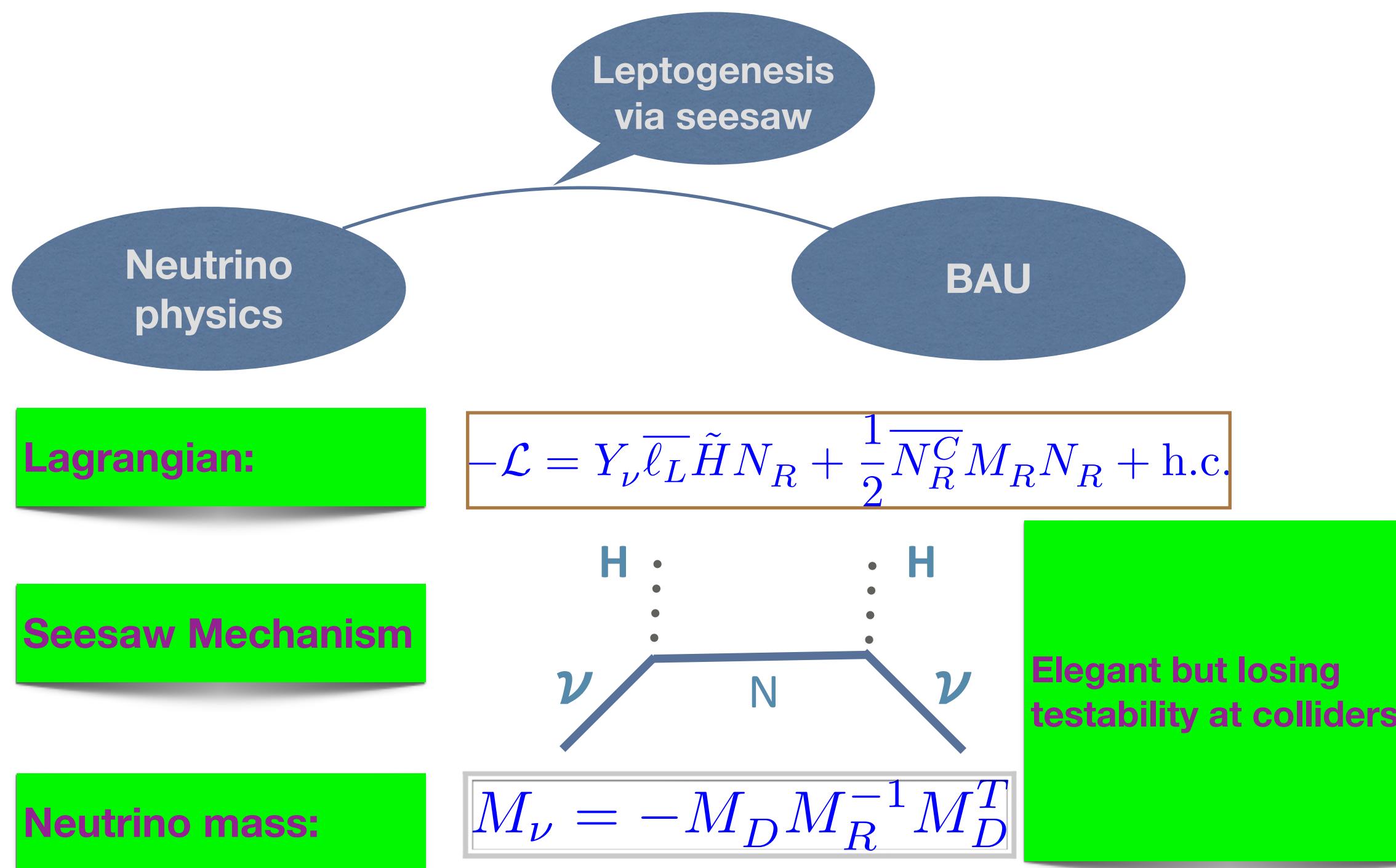
- ★ Baryon number violating
- ★ C&CP violation
- ★ Departure from equilibrium



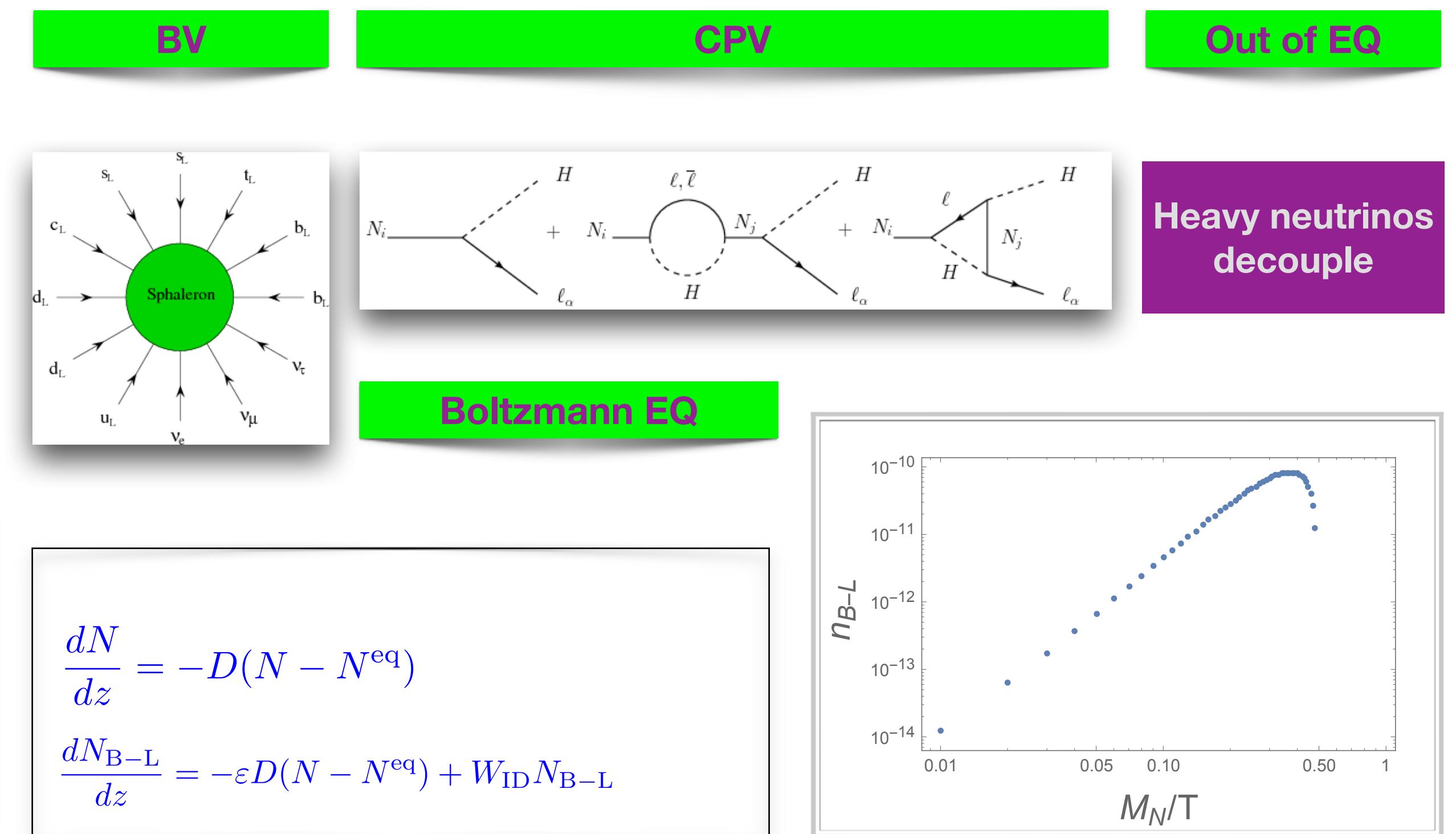
- Leptogenesis
- Electroweak Baryogenesis
- GUT Baryogenesis
- Afleck-Dine Baryogenesis
- Post-sphaleron baryogenesis

# History and development: Leptogenesis

轻子数破坏与 Leptogenesis (type-I seesaw case)

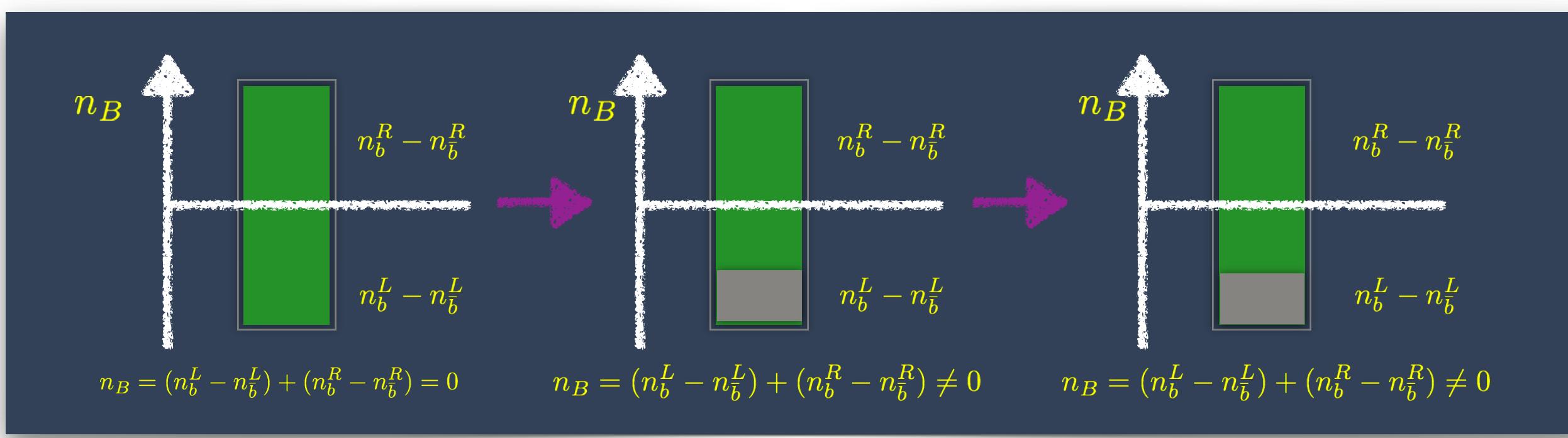
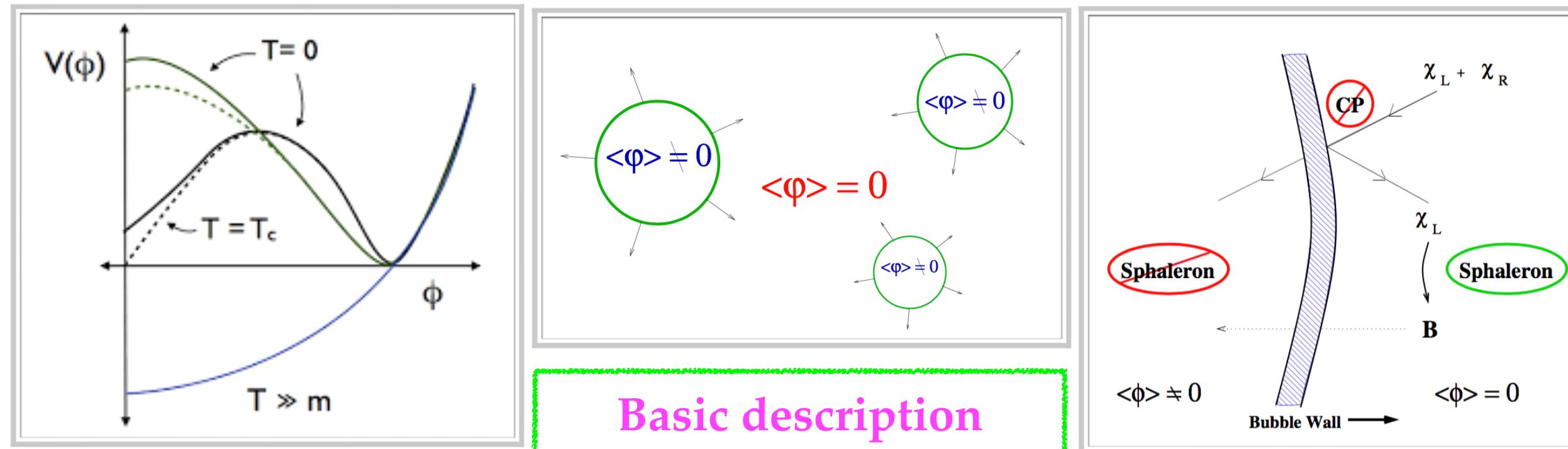


物理图像



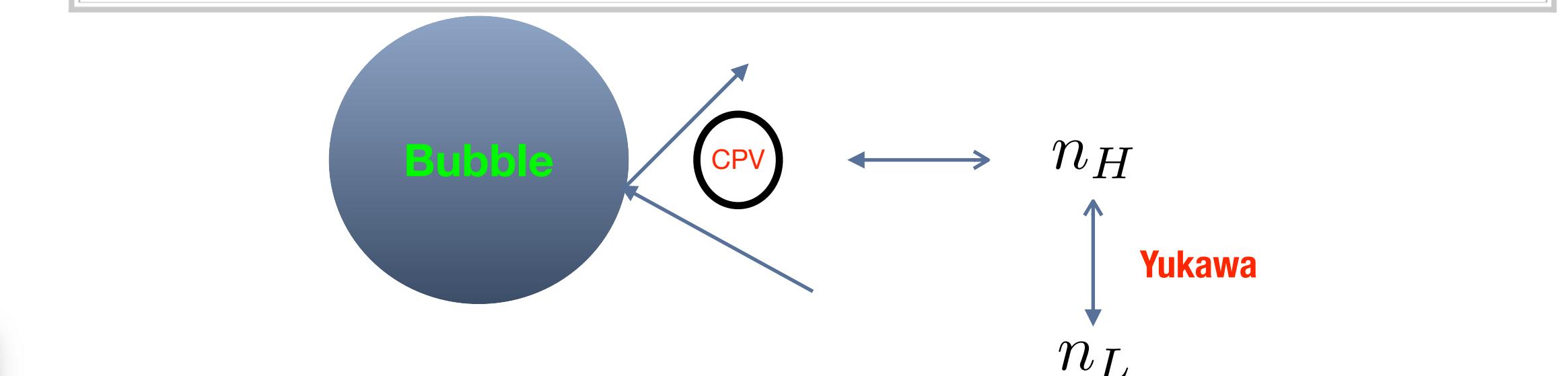
# History and development: EW Baryogenesis

EWBG



輸运方程

$$\frac{\partial n}{\partial t} + \nabla \cdot j(x) = - \int d^3z \int_{-\infty}^{x_0} dz^0 \text{Tr}[\Sigma^>(x, z)S^<(z, x) - S^>(x, z)\Sigma^<(z, x)] \\ + S^<(x, z)\Sigma^>(z, x) - \Sigma^<(x, z)S^>(z, x)]$$



$$\partial_\mu \psi_\mu = +\Gamma_\psi^+ \left( \frac{\chi}{k_\chi} + \frac{\psi}{k_\psi} \right) + \Gamma_\psi^- \left( \frac{\chi}{k_\chi} - \frac{\psi}{k_\psi} \right) + \left( \sum_i \Gamma_{y_i} \right) \left( \frac{\chi}{k_\chi} - \frac{H}{k_H} - \frac{\psi}{k_\psi} \right) + S_{\text{CP}}^\psi$$

$$\partial_\mu \chi_\mu = -\Gamma_\psi^+ \left( \frac{\chi}{k_\chi} + \frac{\psi}{k_\psi} \right) - \Gamma_\psi^- \left( \frac{\chi}{k_\chi} - \frac{\psi}{k_\psi} \right) - \left( \sum_i \Gamma_{y_i} \right) \left( \frac{\chi}{k_\chi} - \frac{H}{k_H} - \frac{\psi}{k_\psi} \right) - S_{\text{CP}}^\psi$$

$$\partial_\mu H_\mu = \Gamma_{Y_t} \left( \frac{T}{k_T} - \frac{H}{k_H} - \frac{Q}{k_Q} \right) + \left( \sum_i \Gamma_{y_i} \right) \left( \frac{\chi}{k_\chi} - \frac{H}{k_H} - \frac{\psi}{k_\psi} \right) - \Gamma_h \frac{H}{k_H},$$

# History and development: Afleck-Dine

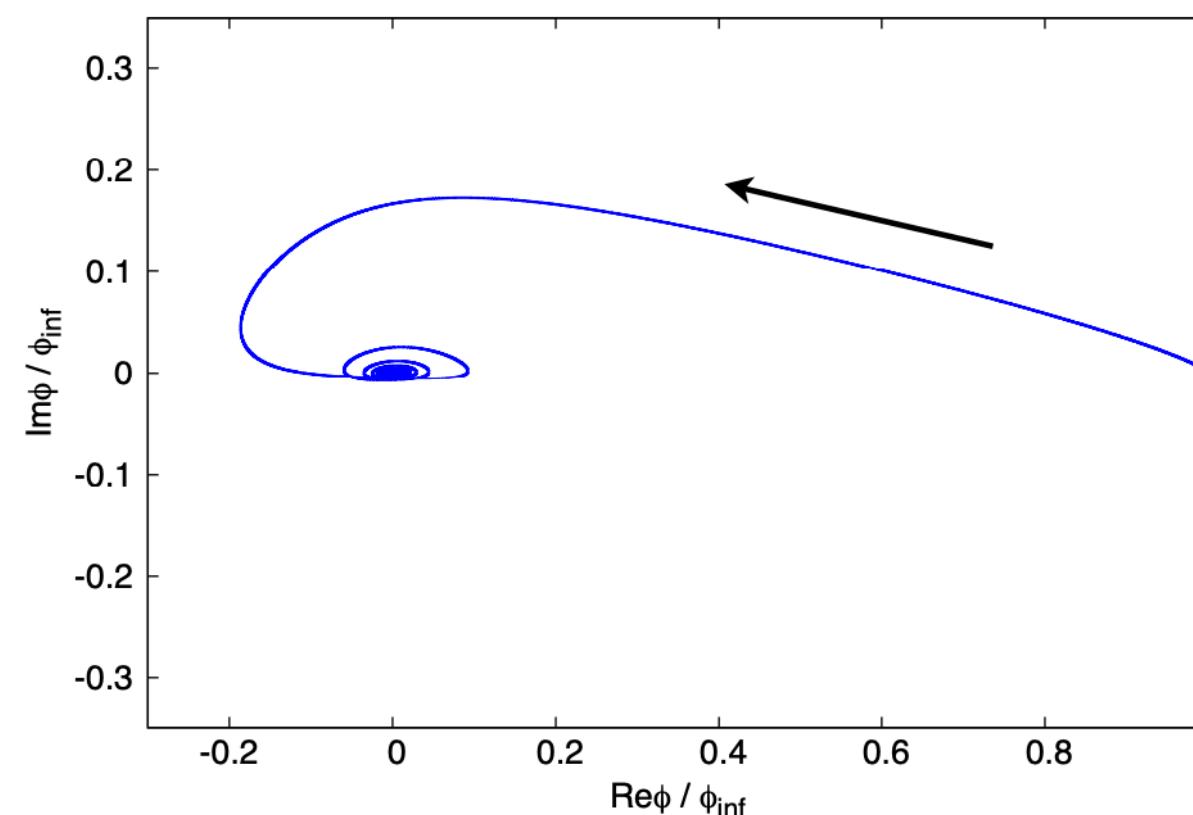
## Afleck-Dine Mechanism

Scalars carrying  
non-zero U(1)  
charges

Flat directions  
(AD fields)

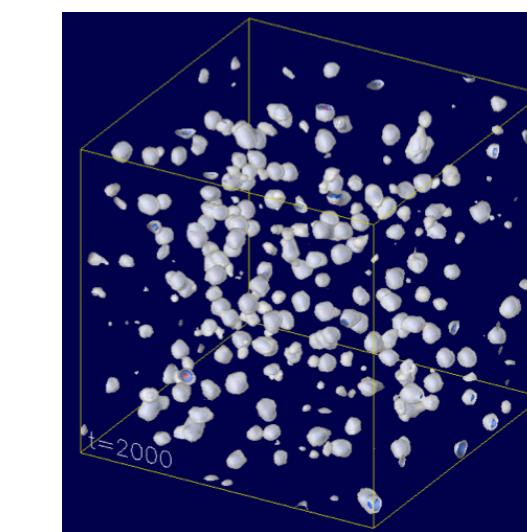
Lifting the potential  
via B/L violation  
operators

$$V = (m^2 - cH^2) |\phi|^2 + \lambda |\phi|^4 + \left( \frac{\phi^n}{M^{n-4}} + \text{h.c.} \right)$$



$$\dot{n}_{B,L} + 3Hn_{B,L} = 2\beta \text{Im} \left[ \frac{\partial V}{\partial \phi} \phi \right]$$

Q-ball formation (Non-topological soliton in scalar field theory)



Oscillation of AD field

Q-ball formation

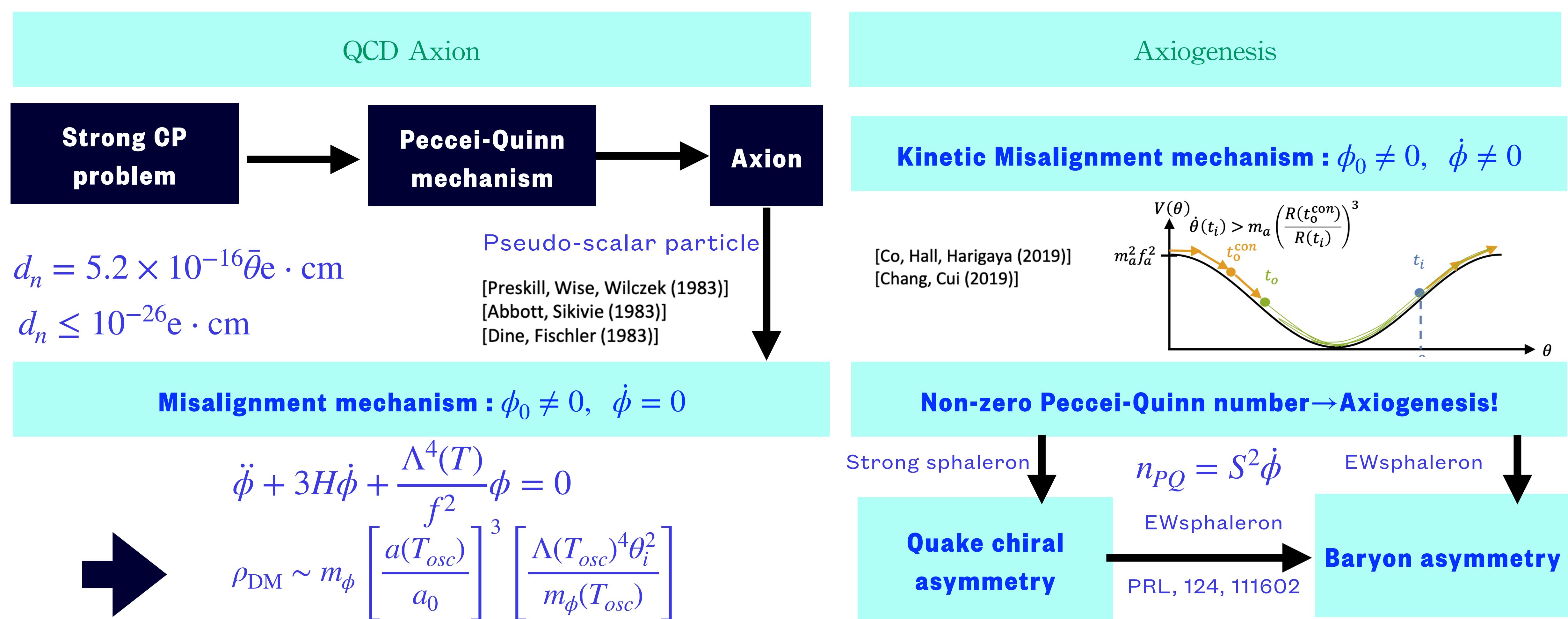
Long lived Q-ball

DM candidate

Evaporation

BAU when sphaleron  
erase is irrelevant

# History and development: Axiogenesis



# Two little works based on previous developments

- Axion-inflaton triggered baryogenesis



Axion-inflation triggered baryogenesis, Wei Chao, Y.H. Wang, C.H. Xie, in submission

- Majoron dark matter triggered baryogenesis

Axion-like dark matter from the type-II seesaw mechanism, Wei Chao, M.J. Jin, H.J. Li Y.Q. Peng, PRD

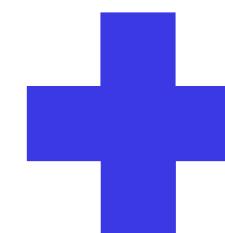
Majorana Majoron and the baryon asymmetry of the Universe, Wei Chao,Y.Q. Peng, in submission

# Axion-inflation triggered baryogenesis

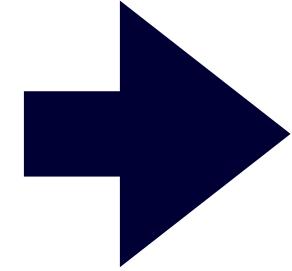
- Original idea : Alexander, Peskin, Sheikh-Jabbari, PRL 2004

$$S = \int \sqrt{-g} \left[ \frac{1}{2} \partial_\mu \phi \partial^\mu \phi - V(\phi) - F(\phi) R \tilde{R} \right]$$

**$R \tilde{R}$  production during axion inflation**



$$\partial_\mu J_l^\mu = \frac{3}{16\pi^2} R \tilde{R}$$



**Net lepton number density after inflation!**

- Net number densities of SM particles can be produced via the axion-inflaton that couples to the Hyper U(1) gauge field via the Chern-Simons interaction,  $g(\phi) F \tilde{F}$ .
- Hyper-magnetic field may survive to the EWPT, resulting in net BAU (JHEP12(2017)011)

# Axion-inflation triggered baryogenesis

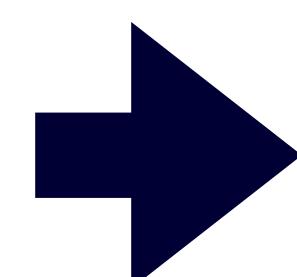
- Axion inflation with interactions

$$\mathcal{L}_{\text{int}} = \frac{\alpha}{4\pi} \frac{\phi}{f_a} F_{\mu\nu} \widetilde{F}^{\mu\nu}$$

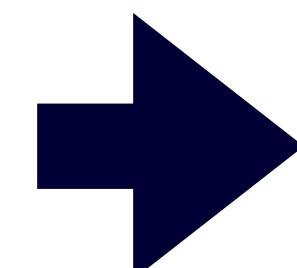
- Production of gauge fields during inflation:

$$\left( \square \eta^{\mu\nu} - a \frac{\alpha \dot{\phi}}{\pi f_a} \varepsilon^{0\mu\sigma\nu} \partial_\sigma \right) A_\nu = 0$$

$$A(\tau, x) = \sum_{\lambda=\pm} \int \frac{d^3 k}{(2\pi)^3} \left[ A_\lambda(\eta, k) \varepsilon_\lambda(k) a_\lambda(k) e^{ik \cdot x} + \text{h.c.} \right]$$



$$\left[ \frac{\partial^2}{\partial \eta^2} + k(k + 2\lambda\xi aH) \right] A_\lambda(\eta, k) = 0$$



$$A_\lambda^k(\tau) = \frac{e^{\lambda\pi\xi/2}}{\sqrt{2k}} W_{-i\lambda\xi, 1/2}(2ik\tau)$$

# Axion-inflation triggered baryogenesis

- Triangle anomalies for various  $U(1)$  gauge fields

scenario	symmetries	$Q_L$	$\ell_L$	$U_R$	$D_R$	$E_R$	$N_R$	$H$	$\psi_L$	$\psi_R$	$\chi_L$	$\chi_R$	$\eta_L$	$\eta_R$
(i)	$U(1)_{\mathbf{B-L}}$	$+\frac{1}{3}$	-1	$+\frac{1}{3}$	$+\frac{1}{3}$	-1	-1	0	×	×	×	×	×	×
(ii)	$U(1)_{\mathbf{R}}$	0	0	-1	+1	-1	+1	1	×	×	×	×	×	×
(iii)	$U(1)_{\mathbf{B}}$	$+\frac{1}{3}$	0	$+\frac{1}{3}$	$+\frac{1}{3}$	0	0	0	-1	+2	+2	-1	+2	-1
(iv)	$U(1)_{\mathbf{L}}$	0	+1	0	0	+1	+1	0	-1	+2	+2	-1	+2	-1

# Axion-inflation triggered baryogenesis

- **U(1)<sub>B-L</sub>**

$$\partial_\mu \left( j_{B,Q}^\mu \right) = \frac{1}{32\pi^2} \left( g^2 W \widetilde{W} + \frac{1}{9} g'^2 F \widetilde{F} + \frac{4}{9} g_{B-L}^2 F' \widetilde{F}' \right)$$

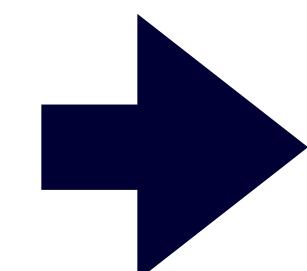
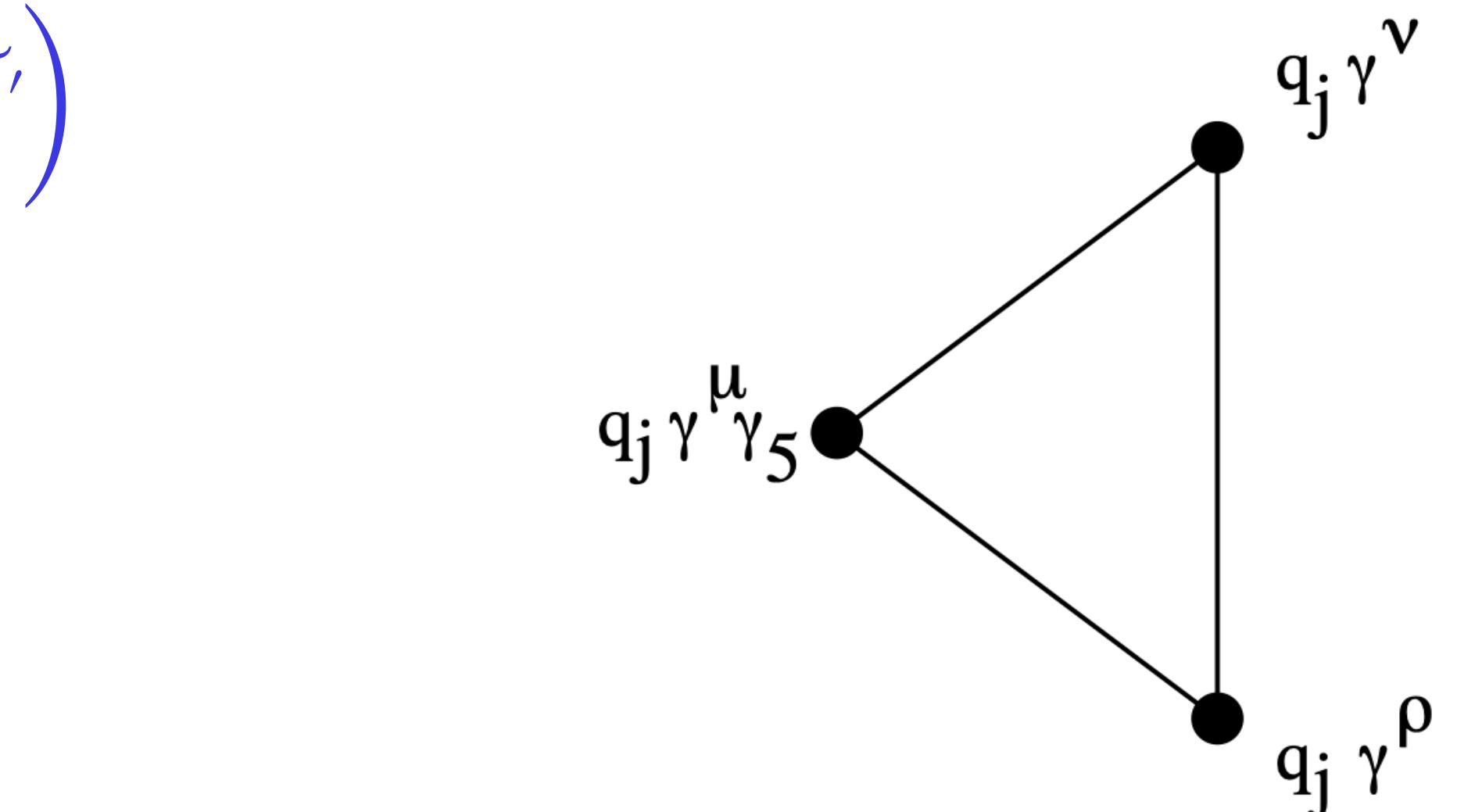
$$\partial_\mu \left( j_{B,u}^\mu \right) = \frac{1}{16\pi^2} \left( -\frac{4}{9} g'^2 F \widetilde{F} - \frac{1}{9} g_{B-L}^2 F' \widetilde{F}' \right)$$

$$\partial_\mu \left( j_{B,d}^\mu \right) = \frac{1}{16\pi^2} \left( -\frac{1}{9} g'^2 F \widetilde{F} - \frac{1}{9} g_{B-L}^2 F' \widetilde{F}' \right)$$

$$\partial_\mu \left( j_{L,\ell}^\mu \right) = \frac{1}{32\pi^2} \left( g^2 W \widetilde{W} + g'^2 F \widetilde{F} + 4 g_{B-L}^2 F' \widetilde{F}' \right)$$

$$\partial_\mu \left( j_{L,E}^\mu \right) = \frac{1}{16\pi^2} \left( -g'^2 F \widetilde{F} - g_{B-L}^2 F' \widetilde{F}' \right)$$

$$\partial_\mu \left( j_{L,N}^\mu \right) = \frac{1}{16\pi^2} \left( -g_{B-L}^2 F' \widetilde{F}' \right)$$



$$\partial_\mu \left( j_B^\mu - j_L^\mu \right) = \partial_\mu j_N^\mu = \frac{-g_{B-L}^2}{16\pi^2} F' \widetilde{F}'$$

Key-point of this study!

# Axion-inflation triggered baryogenesis

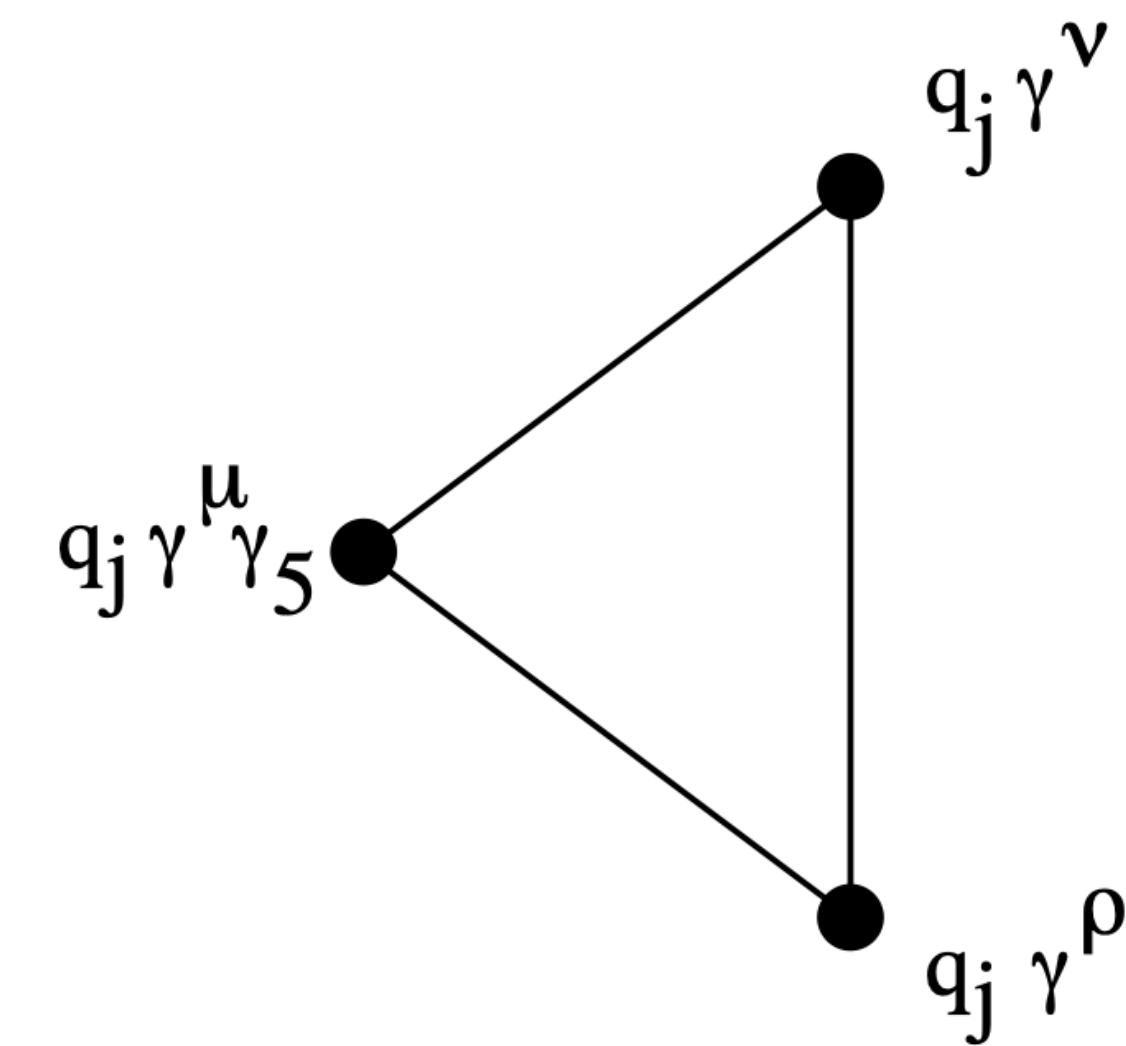
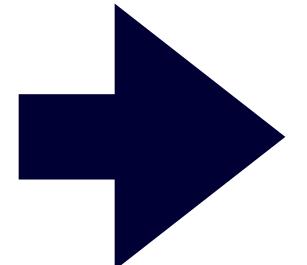
- $\mathbf{U(1)_R}$

$$\partial_\mu \left( j_{B,u}^\mu \right) = \frac{1}{16\pi^2} \left( -\frac{4}{9} g'^2 F \widetilde{F} - g_R^2 F' \widetilde{F}' \right)$$

$$\partial_\mu \left( j_{B,d}^\mu \right) = \frac{1}{16\pi^2} \left( -\frac{1}{9} g'^2 F \widetilde{F} - g_R^2 F' \widetilde{F}' \right)$$

$$\partial_\mu \left( j_{L,E}^\mu \right) = \frac{1}{16\pi^2} \left( -g'^2 F \widetilde{F} - g_R^2 F' \widetilde{F}' \right)$$

$$\partial_\mu \left( j_{L,N}^\mu \right) = \frac{1}{16\pi^2} \left( -g_R^2 F' \widetilde{F}' \right)$$



$$\boxed{\partial_\mu \left( j_B^\mu - j_L^\mu \right) = \partial_\mu j_N^\mu = \frac{-g_{B-L}^2}{16\pi^2} F' \widetilde{F}'}$$

# Axion-inflation triggered baryogenesis

- **U(1)<sub>B</sub>:**
- **current equations for quarks are the same as these in the U(1)<sub>B-L</sub>**
- **current equations for leptons are the same as these in the SM**

$$\partial_\mu \left( j_{\psi_L}^\mu \right) = + \frac{1}{32\pi^2} \left( g^2 W \widetilde{W} + g'^2 F \widetilde{F} + 4g_B^2 F' \widetilde{F}' \right)$$

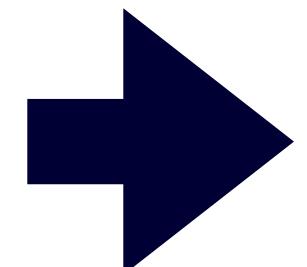
$$\partial_\mu \left( j_{\chi_L}^\mu \right) = + \frac{1}{16\pi^2} \left( g'^2 F \widetilde{F} + 4g_B^2 F' \widetilde{F}' \right)$$

$$\partial_\mu \left( j_{\eta_L}^\mu \right) = + \frac{1}{4\pi^2} \left( g_B^2 F' \widetilde{F}' \right)$$

$$\partial_\mu \left( j_{\psi_R}^\mu \right) = - \frac{1}{32\pi^2} \left( g^2 W \widetilde{W} + g'^2 F \widetilde{F} + 16g_B^2 F' \widetilde{F}' \right)$$

$$\partial_\mu \left( j_{\chi_R}^\mu \right) = - \frac{1}{16\pi^2} \left( g'^2 F \widetilde{F} + g_B^2 F' \widetilde{F}' \right)$$

$$\partial_\mu \left( j_{\eta_R}^\mu \right) = - \frac{1}{16\pi^2} \left( g_B^2 F' \widetilde{F}' \right)$$

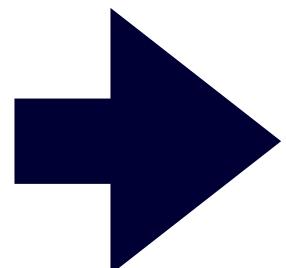


$$\partial_\mu \left( j_{\psi_L}^\mu + j_{\psi_R}^\mu + j_{\chi_L}^\mu + j_{\chi_R}^\mu + j_{\eta_L}^\mu + j_{\eta_R}^\mu \right) = 0$$

$$\partial_\mu \left( j_B^\mu - j_L^\mu \right) = 0!$$

# Axion-inflation triggered baryogenesis

- **$U(1)_L$ :**
- **current equations for quarks are the same as these in the SM**
- **current equations for leptons are the same as these in the  $U(1)_{B-L}$**
- **current equations for new fermions are the same as these in the  $U(1)_B$**



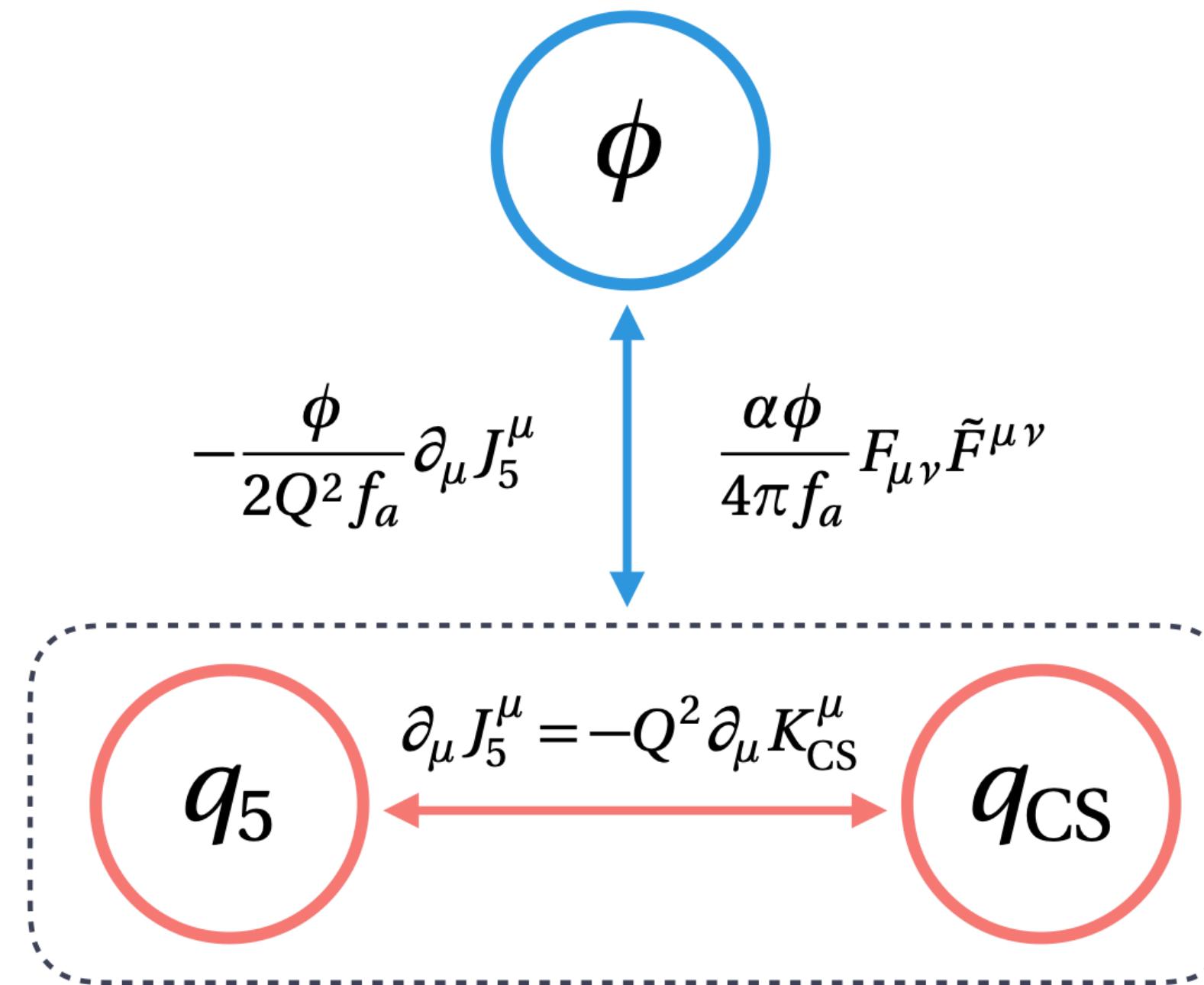
$$\partial_\mu \left( j_{\psi_L}^\mu + j_{\psi_R}^\mu + j_{\chi_L}^\mu + j_{\chi_R}^\mu + j_{\eta_L}^\mu + j_{\eta_R}^\mu \right) = 0$$

$$\partial_\mu \left( j_B^\mu - j_L^\mu \right) = \partial_\mu j_N^\mu \neq 0!$$

If neutrinos are Dirac particles which means that its Yukawa interaction never reach equilibrium, then we have the source of the BAU for the  $U(1)_{B-L}$ ,  $U(1)_R$  and  $U(1)_L$  cases!

# Axion-inflation triggered baryogenesis

- Axion inflation  $\rightarrow q_{CS} \rightarrow q_5$



- Chern Simons number:

$$n_{CS} \equiv \frac{1}{(2\pi)^2} \mathcal{K}(\xi) a^3 H^3$$

$$= \frac{1}{(2\pi)^2} \sum_{\lambda=\pm} \lambda e^{i\kappa_\lambda \pi} \int \tilde{\tau}^3 d \ln \tilde{\tau} W_{\kappa_\lambda, \mu}^*(-2i\tilde{\tau}) W_{\lambda_\sigma, \mu}(-2i\tilde{\tau}) a^3 H^3$$

- Chiral fermion asymmetry during reheating

$$n_{f,\sigma} = -\epsilon_\sigma N_{f,\sigma} \frac{g_X^2}{8\pi^2 a^3} n_{CS} = -\epsilon_i N_i \frac{g_X^2}{2(2\pi)^4} H^3 \mathcal{K}(\xi)$$

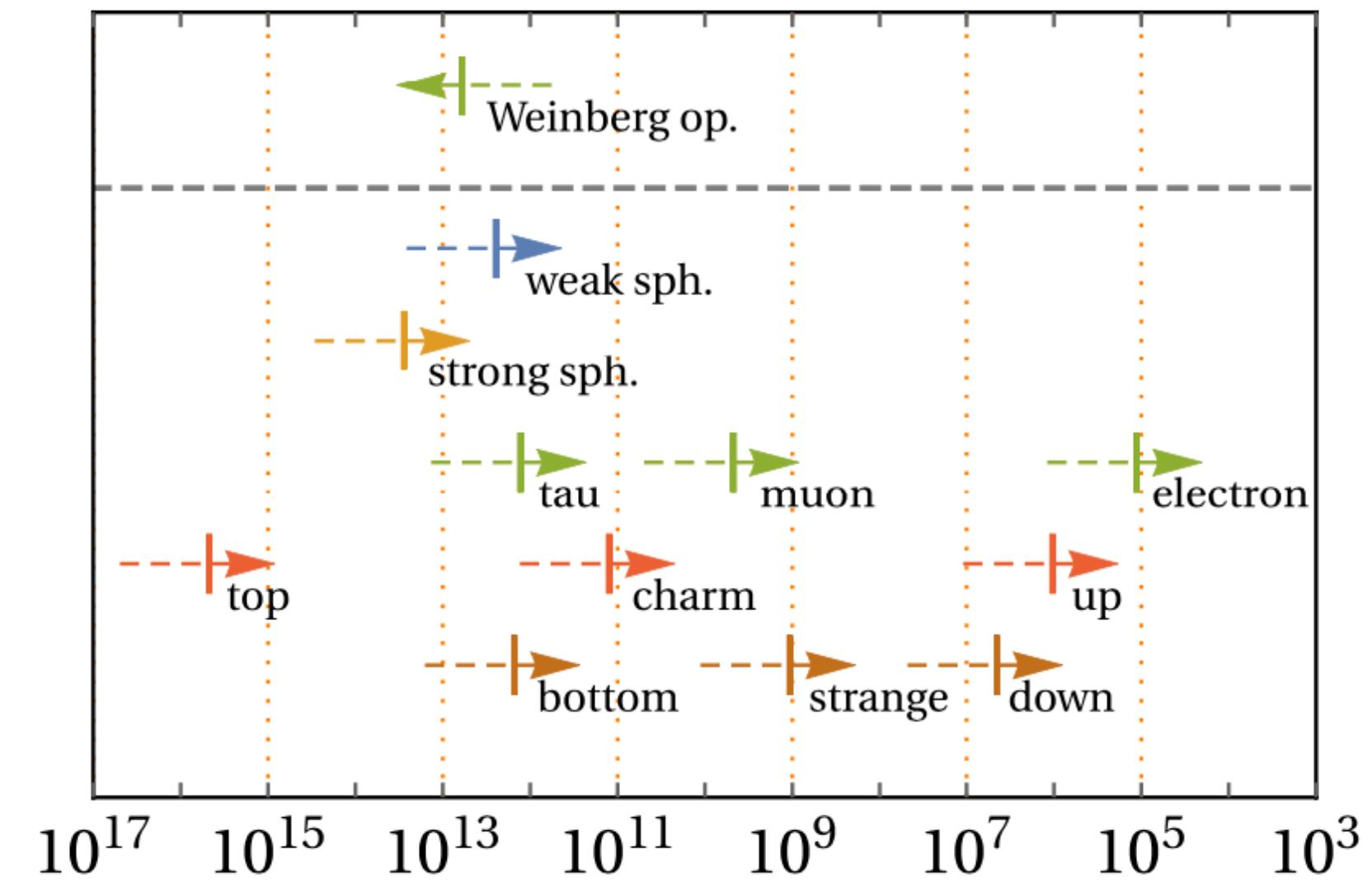
# Axion-inflation triggered baryogenesis

- From chiral fermion asymmetries to the BAU

**Transport equations:**

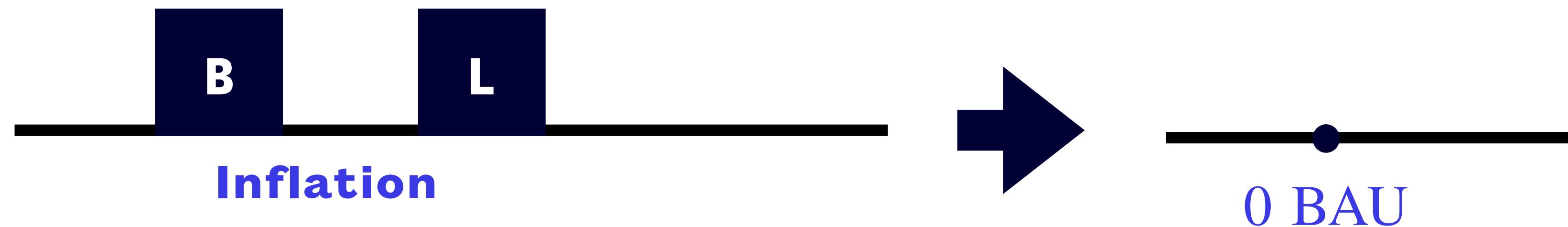
$$-\frac{d}{d \ln T} \left( \frac{\mu_i}{T} \right) = -\frac{1}{g_i} \sum_{\alpha} n_i^{\alpha} \frac{\gamma_{\alpha}}{H} \left[ \sum_j n_j^{\alpha} \left( \frac{\mu_j}{T} \right) \right],$$

Interaction	WS	SS	$Y_e$	$Y_{\mu}$	$Y_{\tau}$
$\Gamma_{\alpha}/T^4$	$\frac{1}{2}\kappa_{WS}\alpha_2^5$	$\frac{1}{2}\kappa_{SS}\alpha_3^5$	$\kappa_{Y_e} y_e^2$	$\kappa_{Y_{\mu}} y_{\mu}^2$	$\kappa_{Y_{\tau}} y_{\tau}^2$
$T_{\alpha}$ [GeV]	$6.0 \times 10^{12}$	$2.5 \times 10^{12}$	$2.8 \times 10^{13}$	$1.1 \times 10^5$	$4.7 \times 10^9$
Interaction	$Y_u$	$Y_c$	$Y_t$	$Y_d$	$Y_s$
$\Gamma_{\alpha}/T^4$	$\kappa_{Y_u} y_u^2$	$\kappa_{Y_u} y_c^2$	$\kappa_{Y_t} y_t^2$	$\kappa_{Y_d} y_d^2$	$\kappa_{Y_d} y_s^2$
$T_{\alpha}$ [GeV]	$1.0 \times 10^6$	$1.2 \times 10^{11}$	$4.7 \times 10^{15}$	$4.5 \times 10^6$	$1.1 \times 10^9$

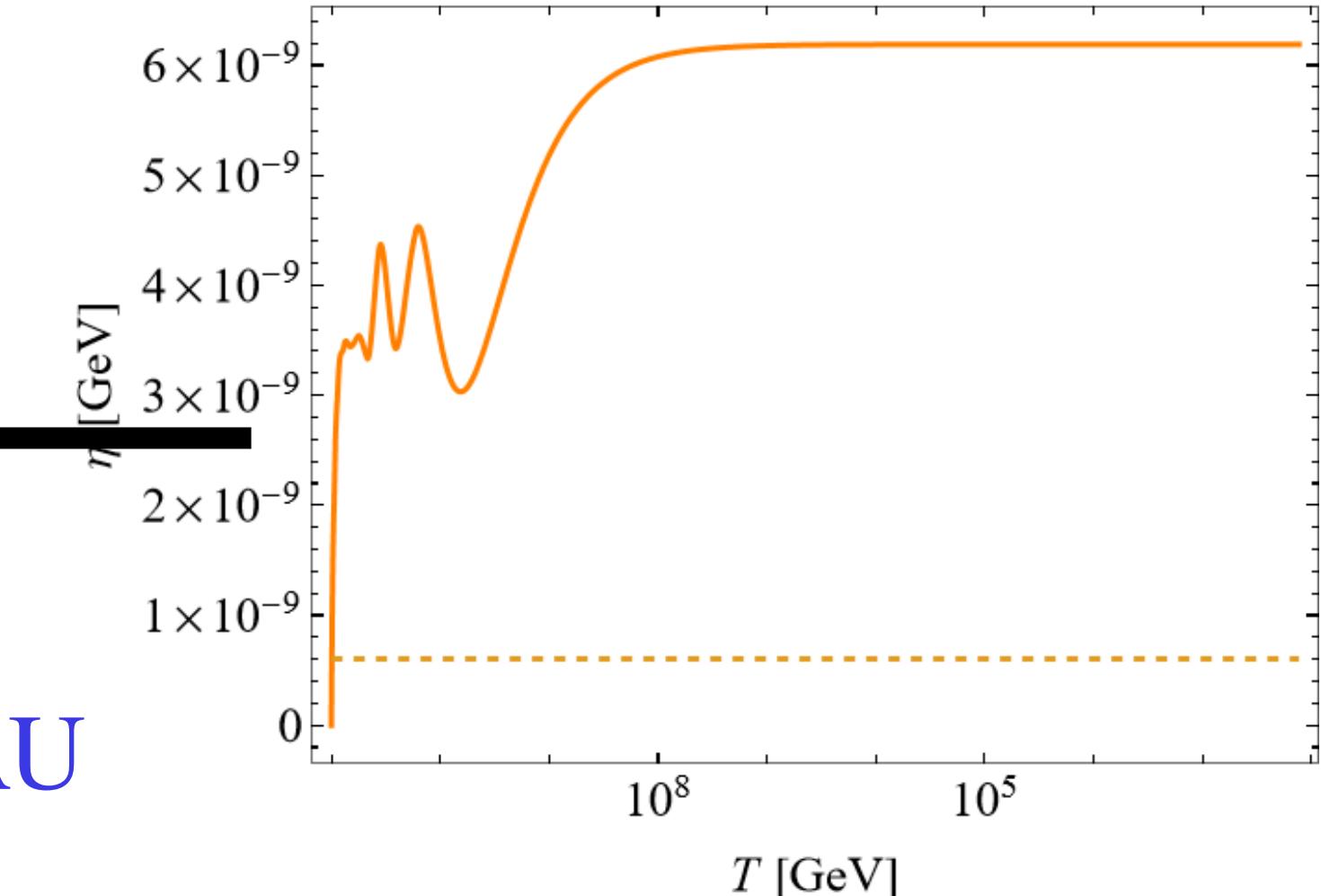
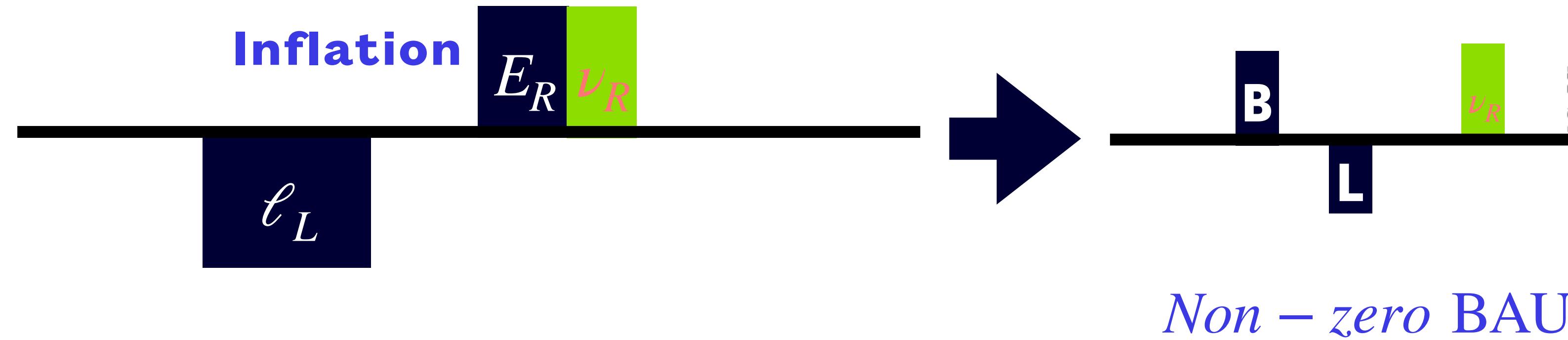


# Axion-inflation triggered baryogenesis

- $F\tilde{F}$ :  $U(1)_B$  gauge field  $\times$  (or require exotic mechanism!)

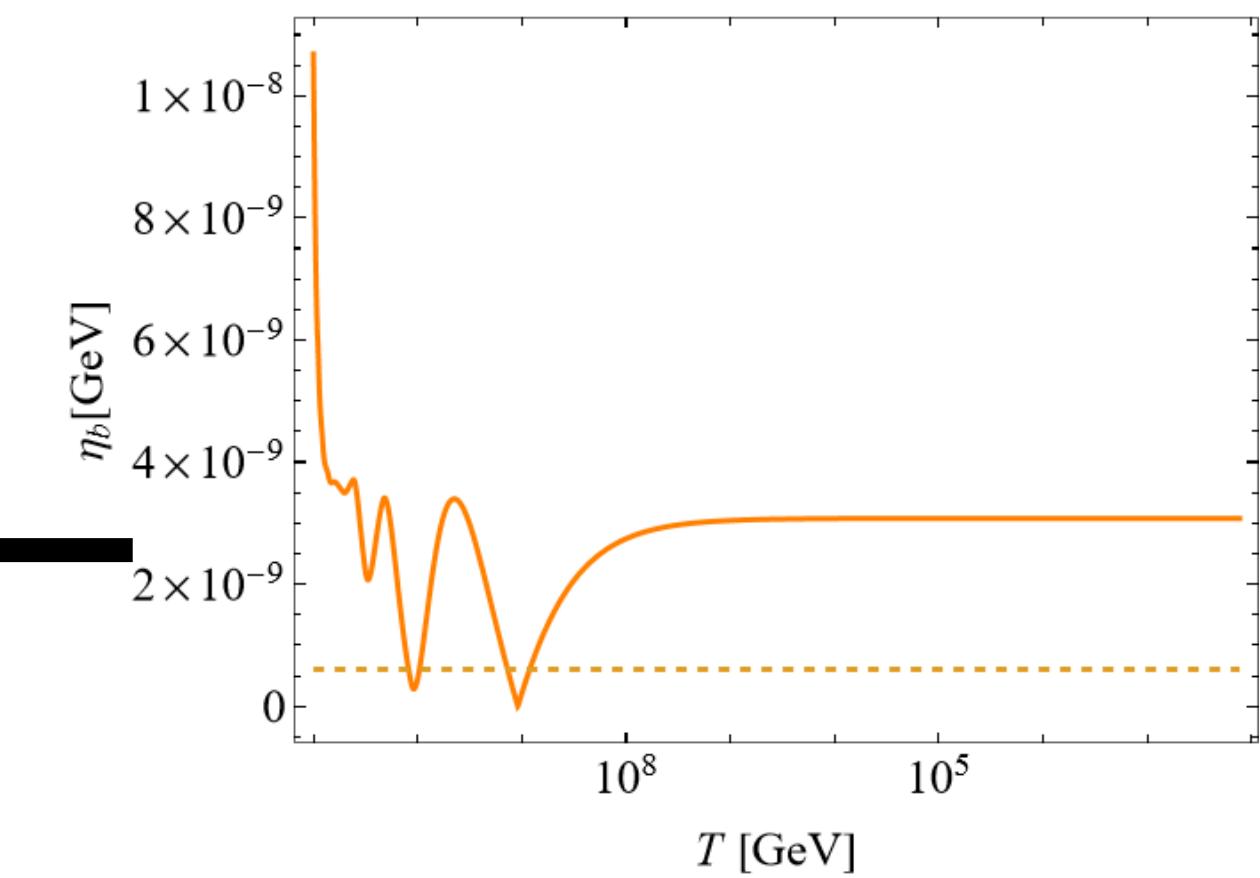
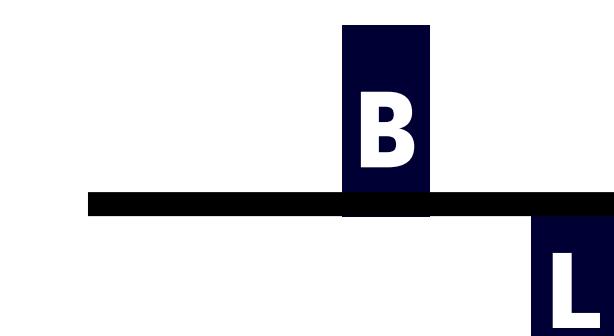
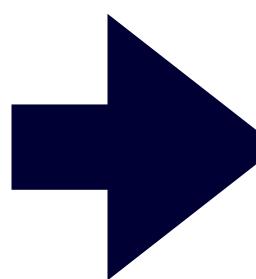


- $F\tilde{F}$ :  $U(1)_L$  gauge field ✓

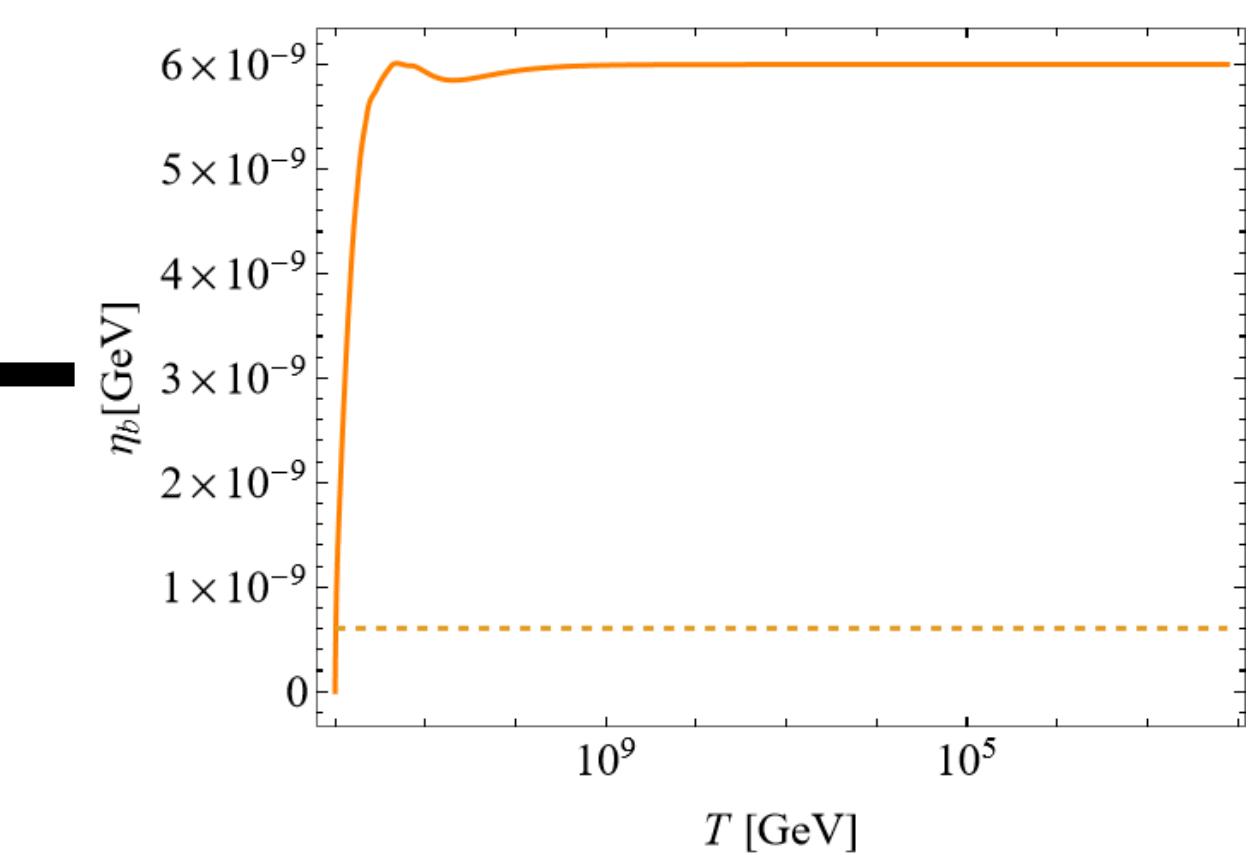
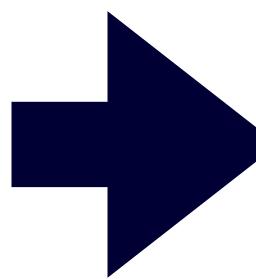
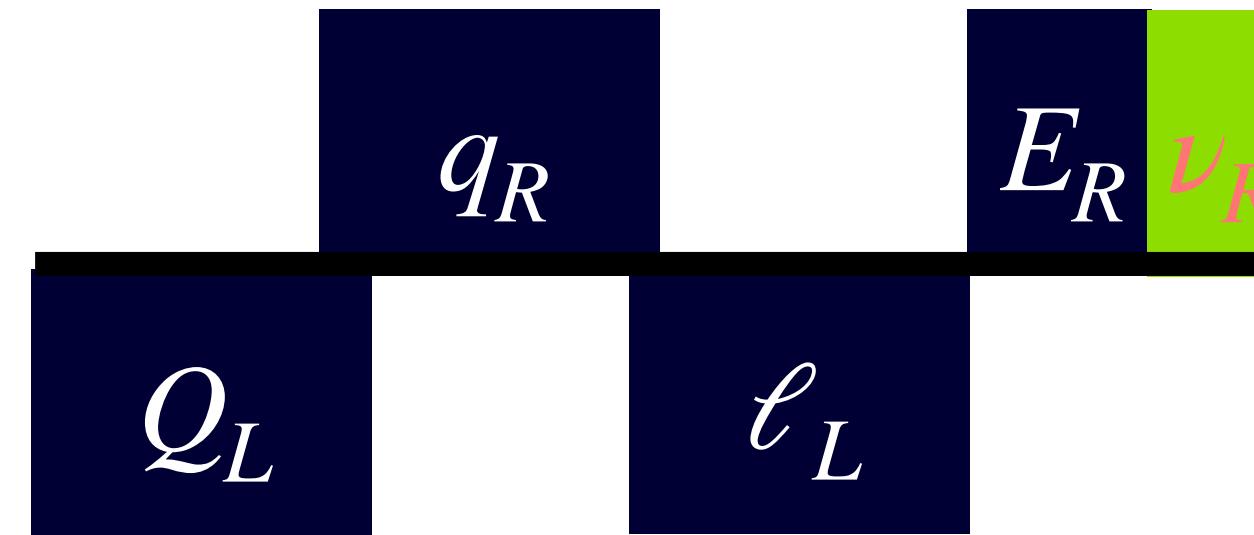


# Axion-inflation triggered baryogenesis

- $F\tilde{F}$ :  $\mathbf{U(1)_R}$  gauge field ✓



- $F\tilde{F}$ :  $\mathbf{U(1)_{B-L}}$  gauge field ✓



# Two little works based on previous developments

- Axion-inflaton triggered baryogenesis

Axion-inflation triggered baryogenesis, Wei Chao, Y.H. Wang, C.H. Xie, in submission

- Majoron dark matter triggered baryogenesis



Axion-like dark matter from the type-II seesaw mechanism, Wei Chao, M.J. Jin, H.J. Li Y.Q. Peng, PRD

Majorana Majoron and the baryon asymmetry of the Universe, Wei Chao,Y.Q. Peng, in submission

# Majoron & neutrino mass via type-I seesaw

Type-I seesaw + spontaneous breaking  $U(1)_L$  symmetry

$$\mathcal{L}_{\text{BSM}} = \left( \partial_\mu \Phi \right)^\dagger (\partial^\mu \Phi) + \mu_\Phi^2 \Phi^\dagger \Phi - \lambda_1 (\Phi^\dagger \Phi)^2 - \lambda_2 (\Phi^\dagger \Phi) (H^\dagger H) - \left[ Y_N \overline{\ell}_L \tilde{H} N_R + \frac{1}{2} \overline{N}_R^C \left( Y_M \Phi + m \right) N_R + \text{h.c.} \right]$$

$$H = \begin{pmatrix} \phi^+ \\ \frac{\nu_\phi + \phi + i\chi}{\sqrt{2}} \end{pmatrix}$$

$$\Phi = \frac{\nu_s + \tilde{s} + i\tilde{a}}{\sqrt{2}}$$

$\tilde{a}$  : Majoron

LNV term!

**Yukawa Interaction**

$$- Y_N \overline{\ell}_L \tilde{H} N_R \rightarrow M_D = Y_N \nu / \sqrt{2}$$

**Key term:**

$$m \overline{N}_R^C N_R + \text{h.c.}$$

Quantum Gravity effect!

# Majoron interactions and Majoron mass

## Field-dependent phase transformation

$$\left. \begin{array}{l} \ell_L \rightarrow e^{-\frac{ia}{2f}} \ell_L \quad S \rightarrow e^{+\frac{ia}{f}} S \\ \\ E_R \rightarrow e^{-\frac{ia}{2f}} E_R \quad H \rightarrow H \end{array} \right\} \quad \begin{aligned} \mathcal{L} &\rightarrow \mathcal{L} - \frac{a}{2f} \partial_\mu \left( \overline{\ell}_L \gamma^\mu \ell_L + \overline{E}_R \gamma^\mu E_R \right) \\ &= \mathcal{L} - \frac{a}{2f} \partial_\mu J_\mu^L \\ &= \mathcal{L} + \frac{a}{2f} \frac{N_f}{32\pi^2} \left( g^2 W_{\mu\nu}^a \widetilde{W}^{\mu\nu,a} - g'^2 B_{\mu\nu} \widetilde{B}^{\mu\nu} \right) \end{aligned}$$

$\xrightarrow{\hspace{10em}}$

$$\frac{1}{2} e^{-i\theta} \overline{N}_R^C m N_R + h.c.$$

# Majoron interactions and Majoron mass

$$\frac{1}{2} e^{-i\theta} \overline{N_R^C} m N_R + h.c. \longrightarrow$$

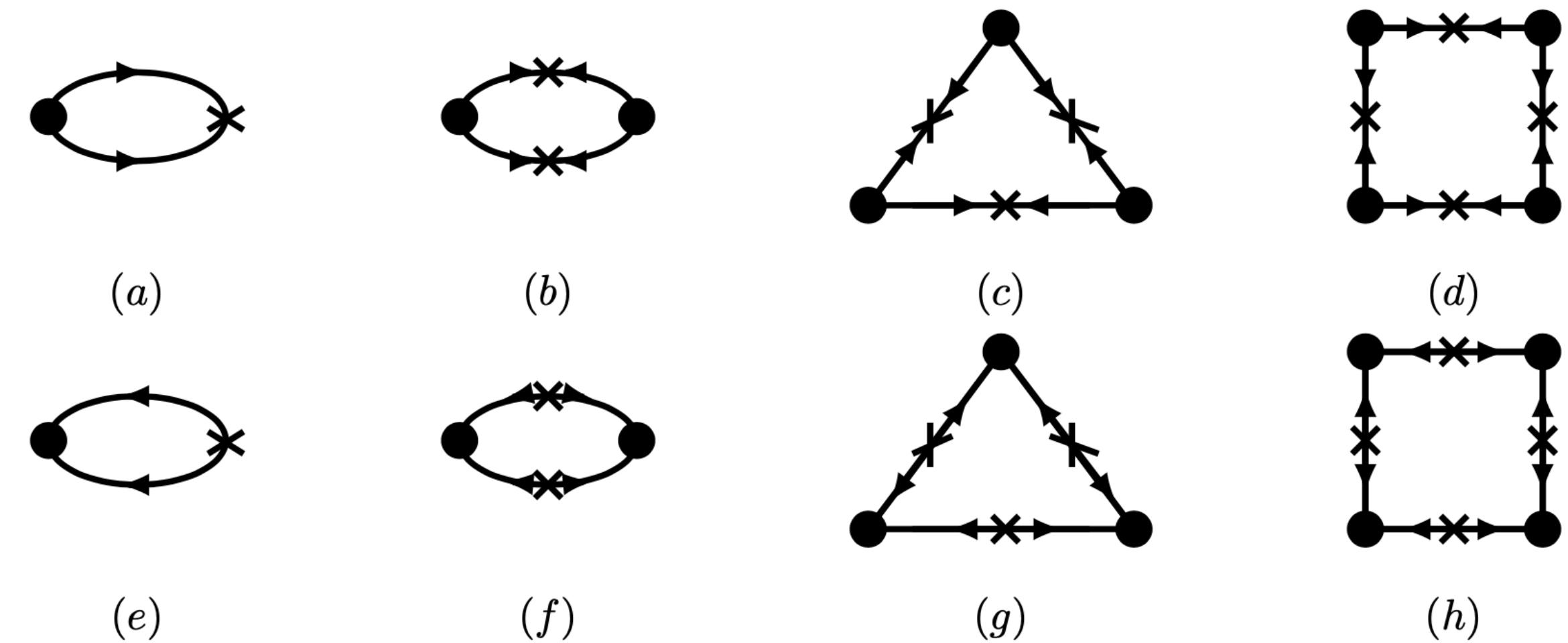
**Mass insertion of right-handed neutrino masses:**

**Before symmetry breaking:**  $M = m$

**After symmetry breaking:**

$$M = f_a Y_M / \sqrt{2} + m$$

$$V_a \sim -\frac{1}{16\pi^2} \sum_{n=1}^4 a_n \cos n\theta.$$



$a_1$	$a_2$	$a_3$	$a_4$
$m M^3 \left( 1 - \log \frac{M^2}{M_{pl}^2} \right)$	$2m^2 M^2 \log \frac{M^2}{M_{pl}^2}$	$-m^3 M$	$m^4 / 3$

# Majoron mass and its relic density

**Majoron mass:**

$$m_a^2 = \frac{1}{f_a^2} \frac{d^2 V}{d\theta^2} = \frac{1}{16\pi^2 f_a^2} \left| a_1 + 4a_2 + 9a_3 + 16a_4 \right|.$$

**Initial velocity:**  
**(From Noether theorem)**

$$\partial_\mu j^\mu = \left( \frac{\partial V}{\partial \phi} \right) \phi - \phi^\dagger \left( \frac{\partial V}{\partial \phi^\dagger} \right)$$

**In the traditional misalignment mechanism**

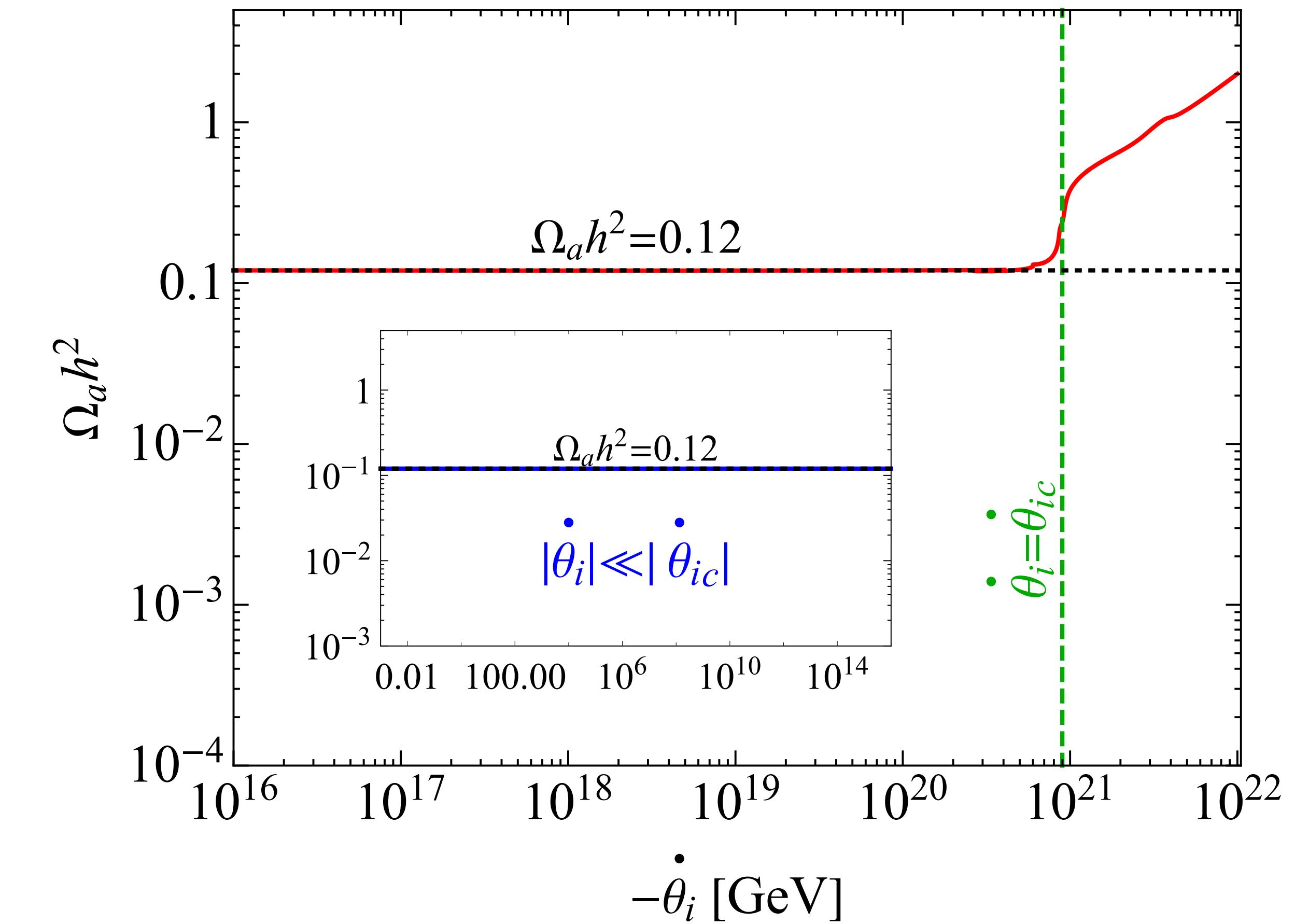
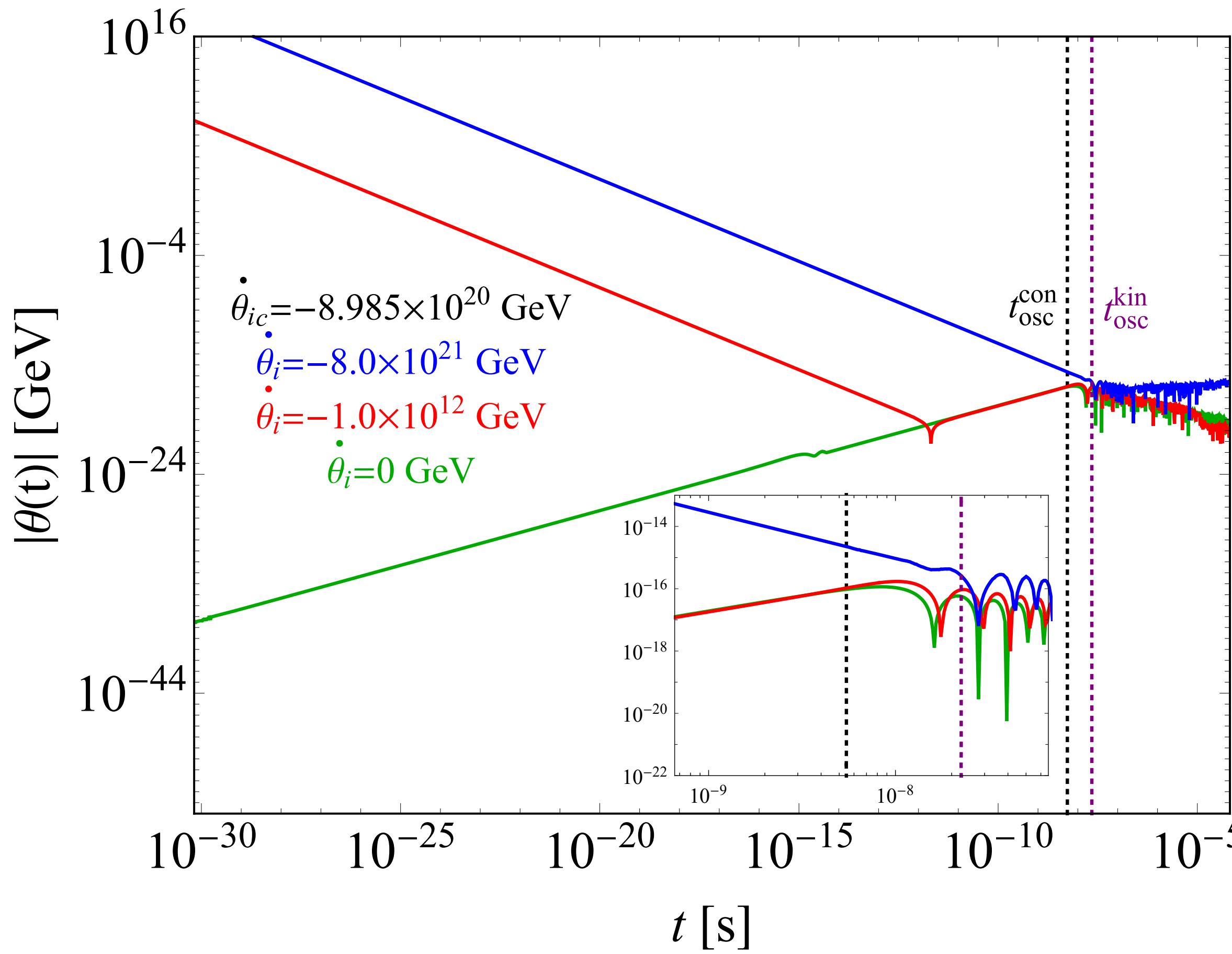
$$\dot{\theta}_i = 0$$

**EOM**

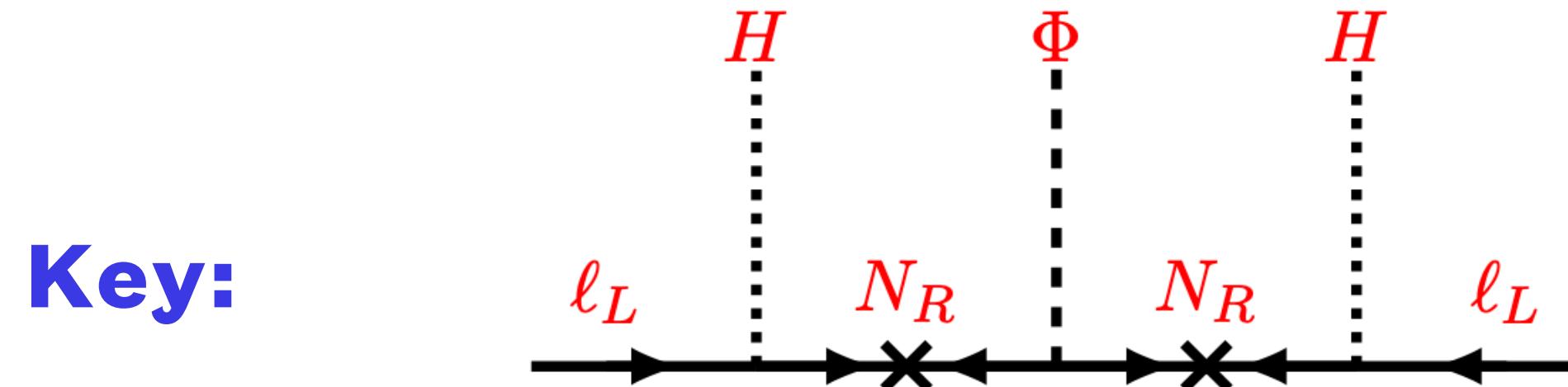
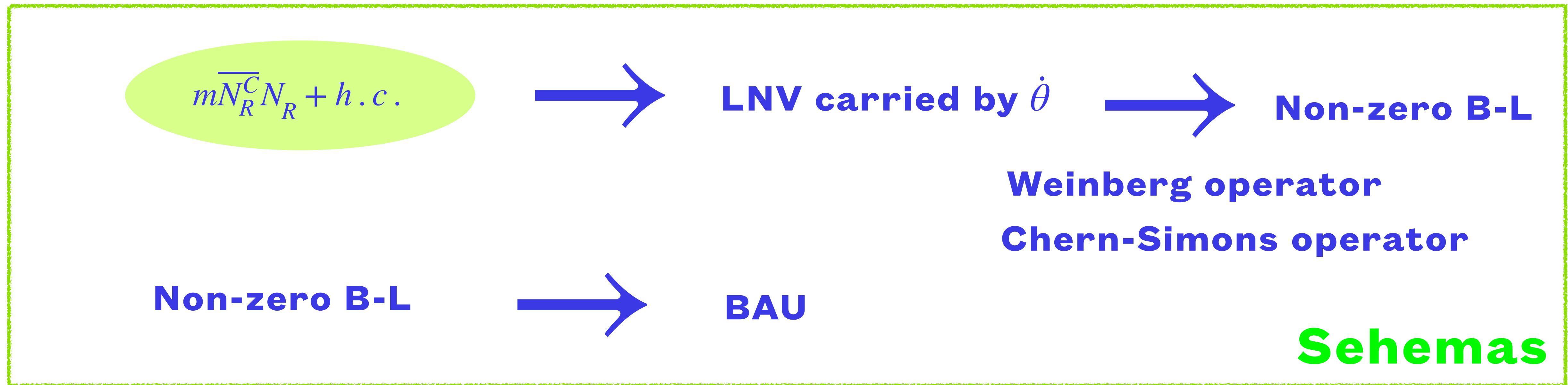
$$\ddot{\theta} + 3H\dot{\theta} + \frac{1}{f_a^2} \frac{dV_a}{d\theta} = 0,$$

**Different oscillation temperature**

# Majoron mass and its relic density



# Baryon asymmetry of the universe



$$\mathcal{L}_{\text{int}} \supset \frac{1}{2M} \frac{a}{f_a} \ell \ell H H,$$

$$\mathcal{L}_{\text{int}} \supset \frac{3g^2}{64\pi^2} \frac{a}{f_a} W \widetilde{W}$$

# Baryon asymmetry of the universe

**Transport equations:**

$$-\frac{d}{d \ln T} \left( \frac{\mu_i}{T} \right) = -\frac{1}{g_i} \sum_{\alpha} n_i^{\alpha} \frac{\gamma_{\alpha}}{H} \left[ \sum_j n_j^{\alpha} \left( \frac{\mu_j}{T} \right) - n_S^{\alpha} \frac{\dot{\theta}(T)}{T} \right],$$

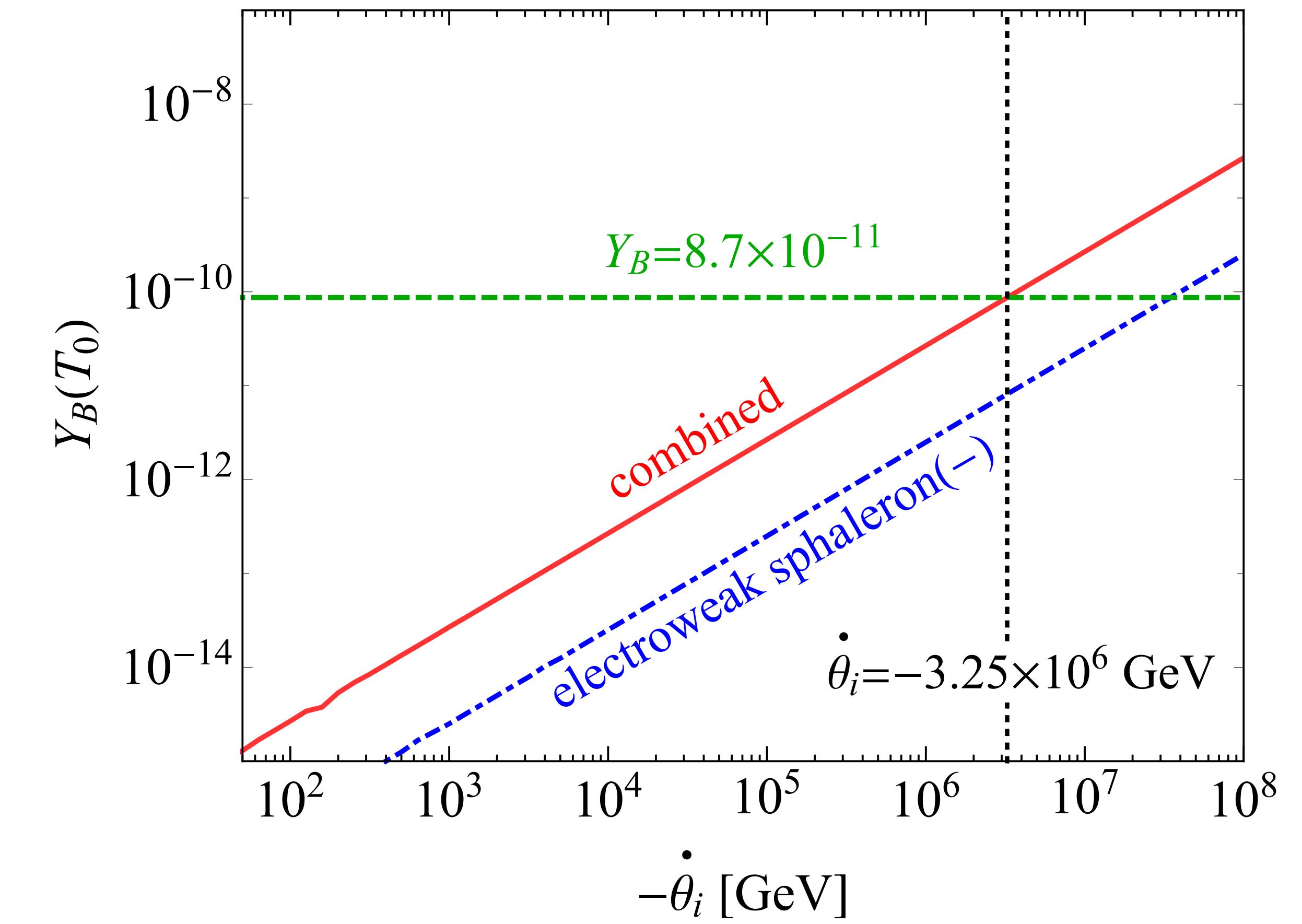
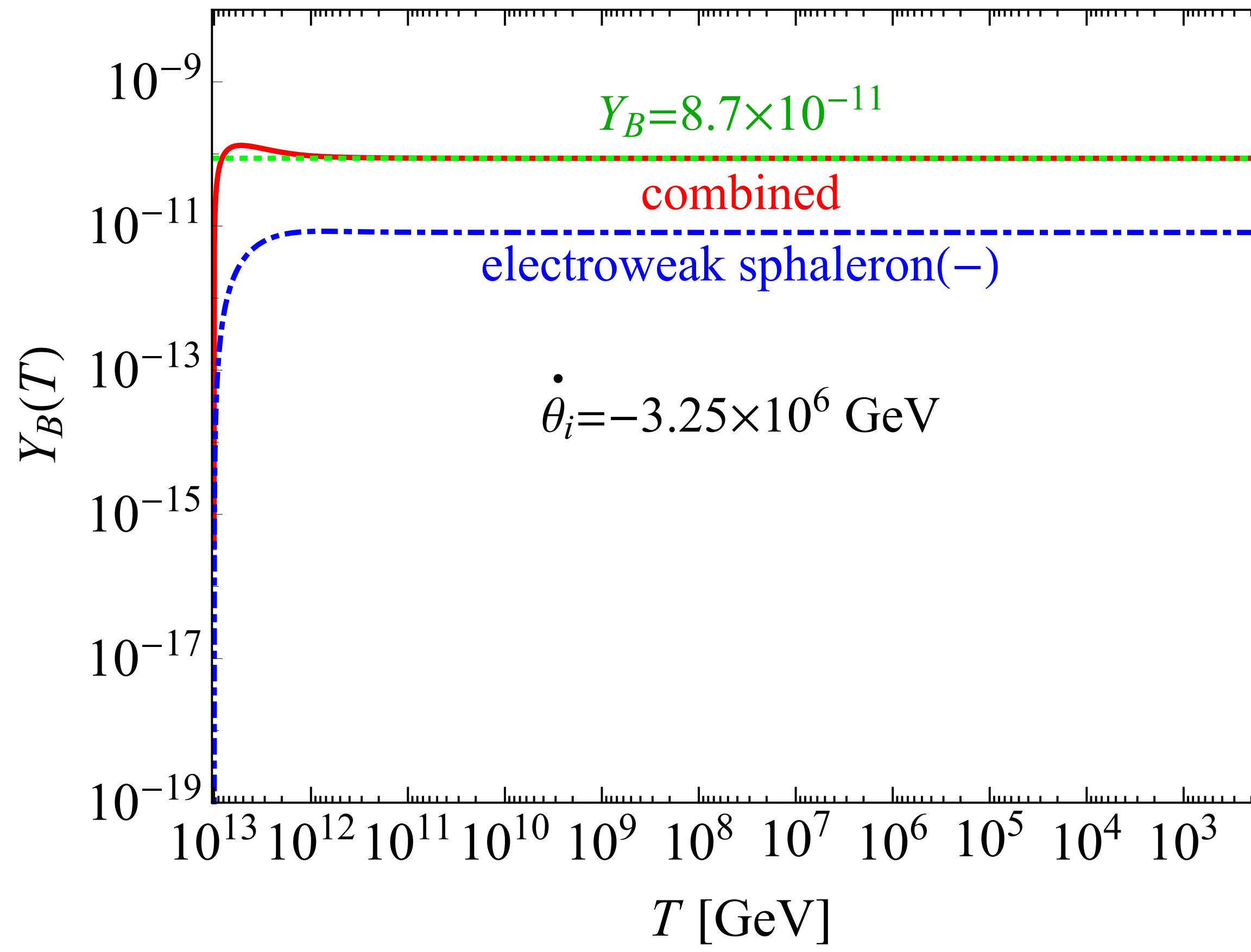
**Source term:**

$$\left( n_S^{WS}, n_S^{W_{12}}, n_S^{W_3}, n_S^{SS}, n_S^{Y_{\tau}}, n_S^{Y_t}, n_S^{Y_b} \right) = \left( \frac{3}{2}, 1, 1, 0, 0, 0, 0 \right).$$

**Weinberg operator decoupling temperature:**

$$T_W \simeq 6 \times 10^{12} \text{ GeV} \times \left( \frac{0.05 \text{ eV}}{m_{\nu}} \right)^2.$$

# Baryon asymmetry of the universe



# Summary

**Dark matter and the baryon asymmetry of the universe are two solid hints of new physics beyond the SM.**

**They can be explained simultaneously in a simple theory.**

**We have proposed two possible solutions to the baryon asymmetry based on axion-like dark matter or inflation theories.**

**Thank you for your attention!**