



# Development of first level track trigger at Belle II using Deep Neural Network

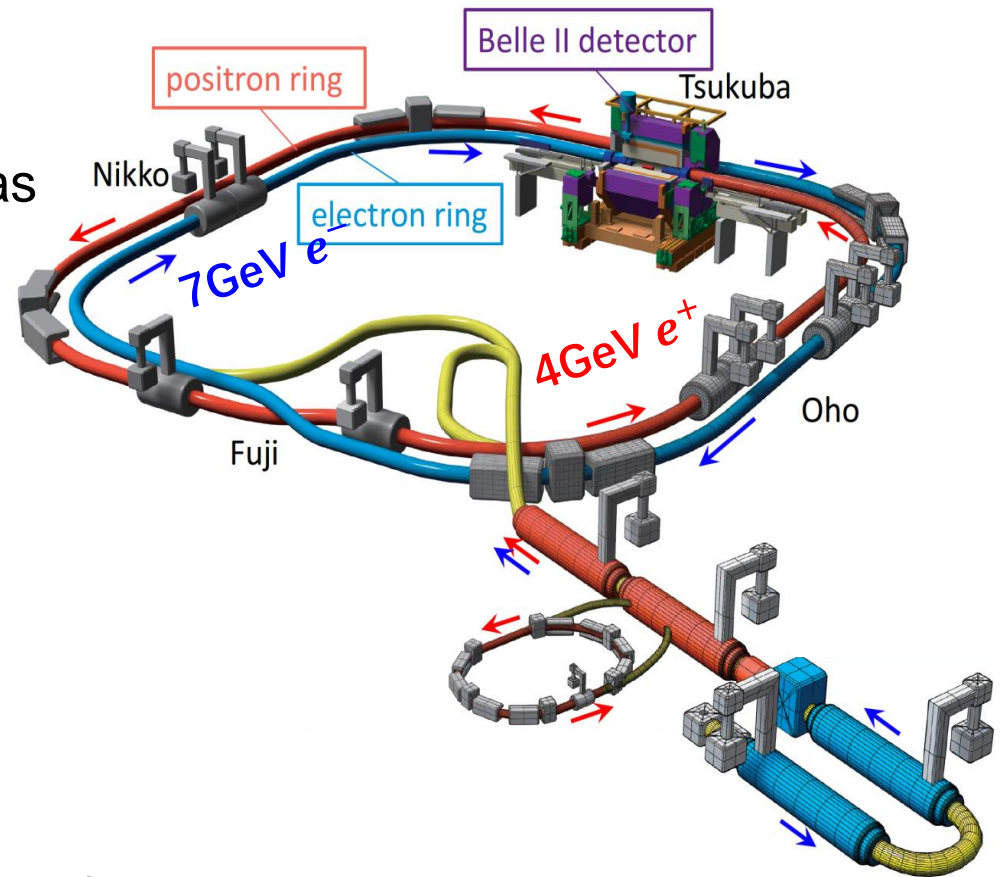
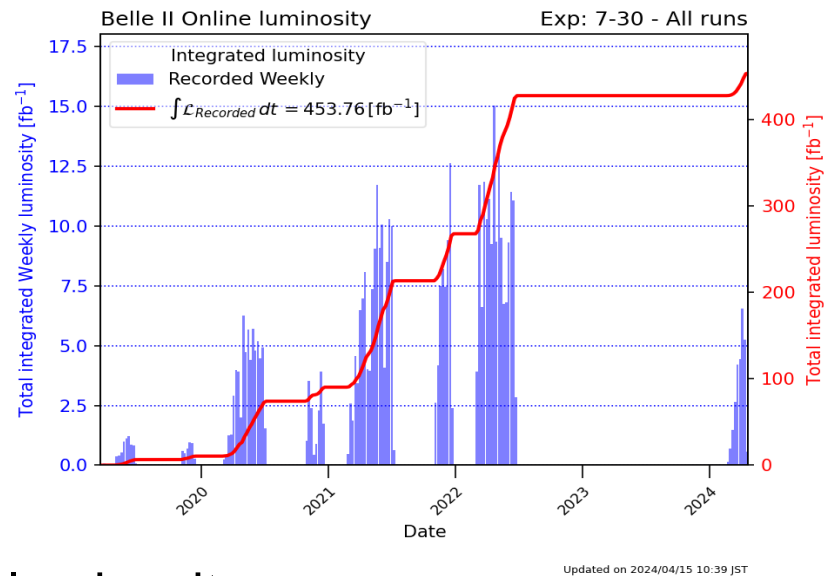
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Yuxin Liu, SOKENDAI(KEK)

18<sup>th</sup> May, Workshop of Tracking in Particle Physics Experiments

# SuperKEKB

- An asymmetric  $e^- e^+$  collider, Upgrade from KEKB. 7.0 GeV  $e^-$  and 4.0 GeV  $e^+$  for  $\Upsilon(4S)$
- SuperKEKB aimed for a peak luminosity of  $6 \times 10^{35} \text{ cm}^{-2} \text{ s}^{-1}$ , surpassing KEKB by 30 times and setting a world record; also with the integral luminosity as  $50 \text{ ab}^{-1}$  ;

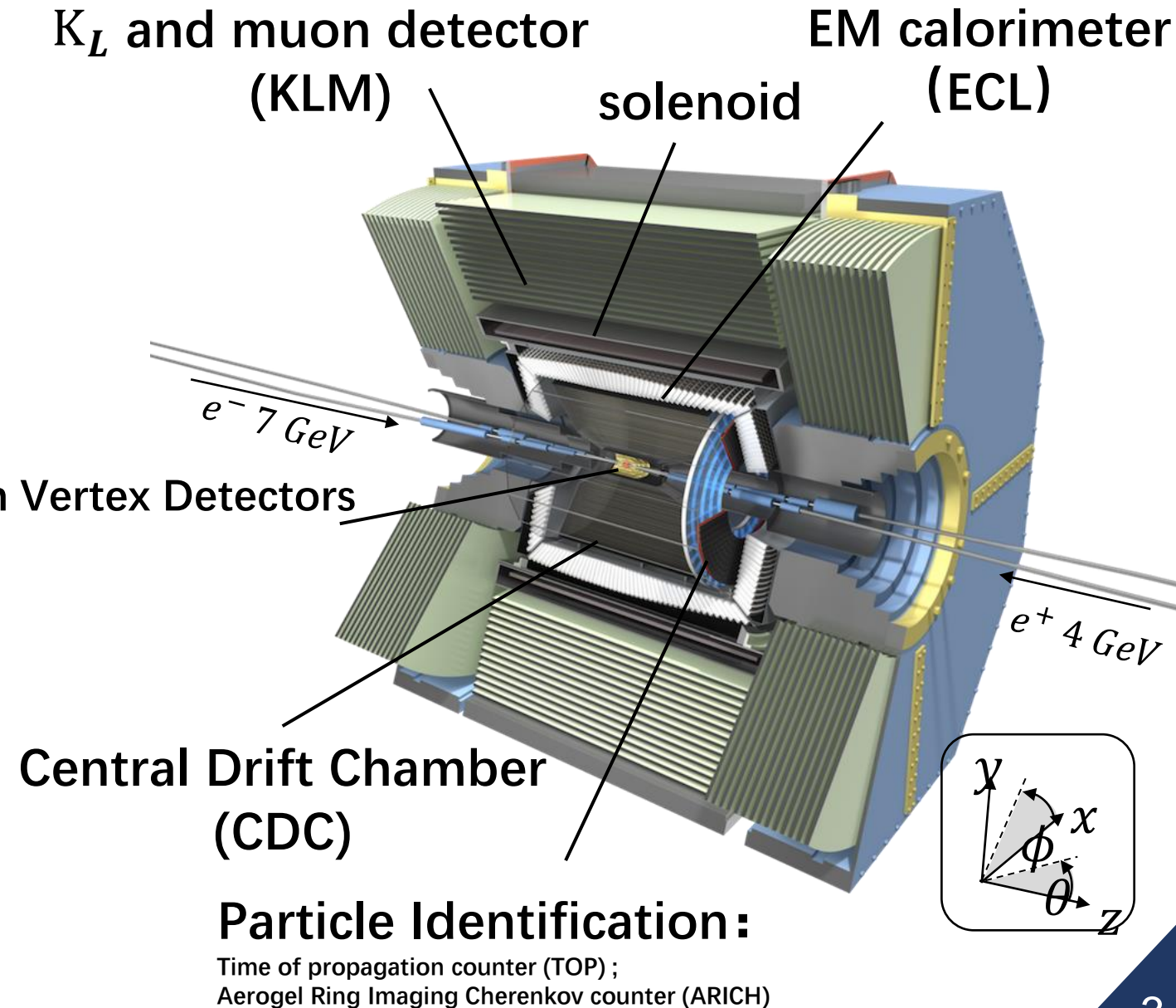


- Achieved luminosity:  
 $\mathcal{L}_{\text{peak}} = 4.65 \times 10^{34} \text{ cm}^{-2} \text{ s}^{-1}$ , two time of KEKB record  
 $\mathcal{L}_{\text{int}} = 453 \text{ fb}^{-1}$  ; till April 2024

# Belle II detectors

## Belle II including:

- Tracking: Vertex detectors and CDC.
- particle identification: TOP and ARICH.
- Calorimeter: ECL.
- KL and muon detector.
- First level (L1) trigger, High level trigger (HLT) and DAQ.

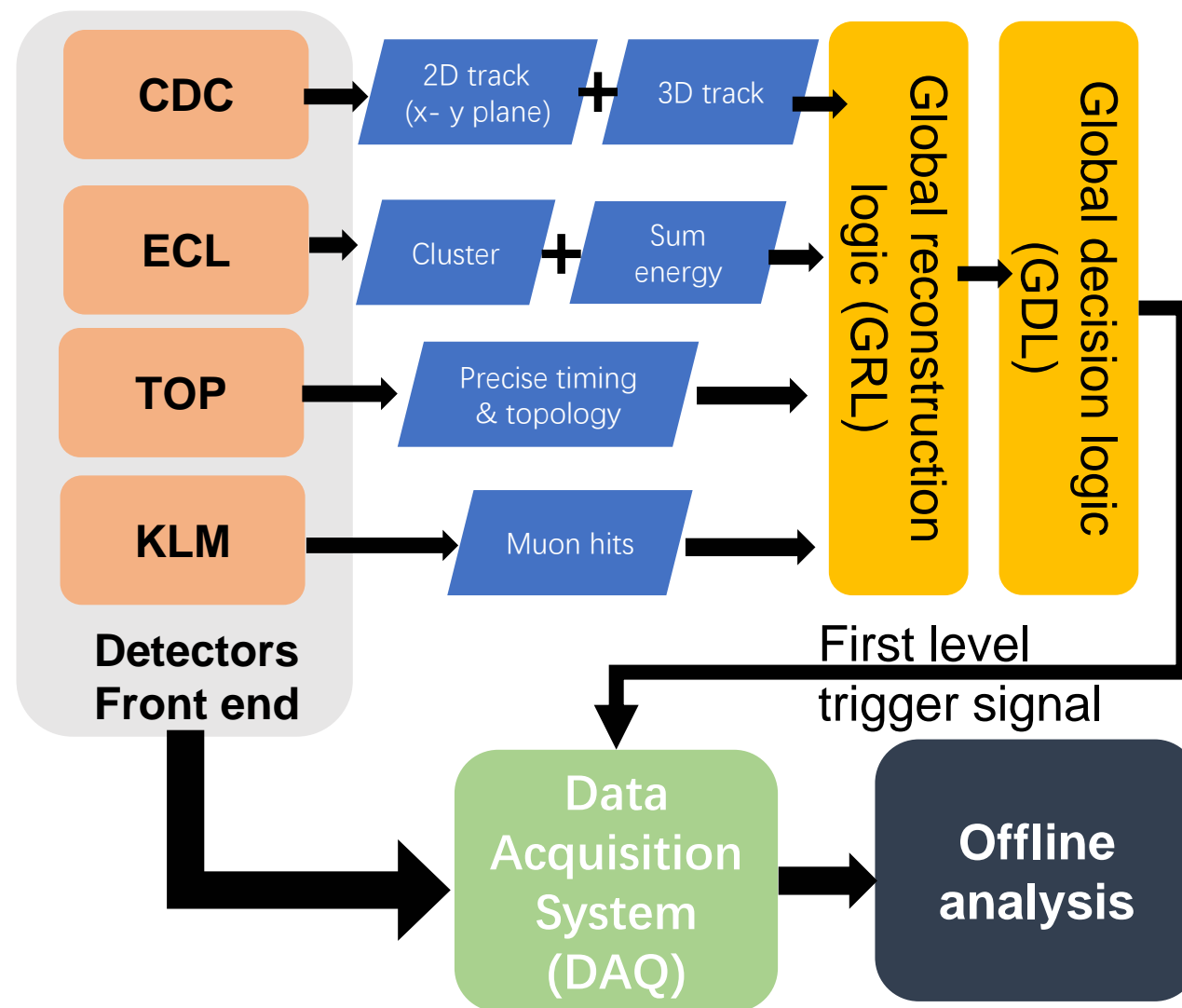


# First level trigger

- Collected small set of data from sub-detectors
- Process data in real-time; short dead time
- Decide to record the event or not with fixed latency

## Requirements for first level trigger system

1. High efficiency for hadronic events
2. A maximum average trigger rate of 30kHz
3. A fixed latency of about 4.4  $\mu$ s

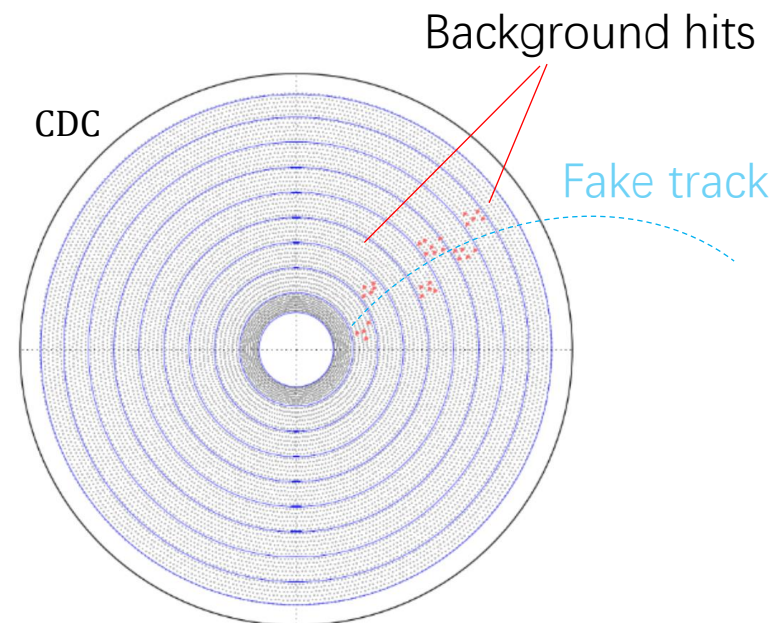
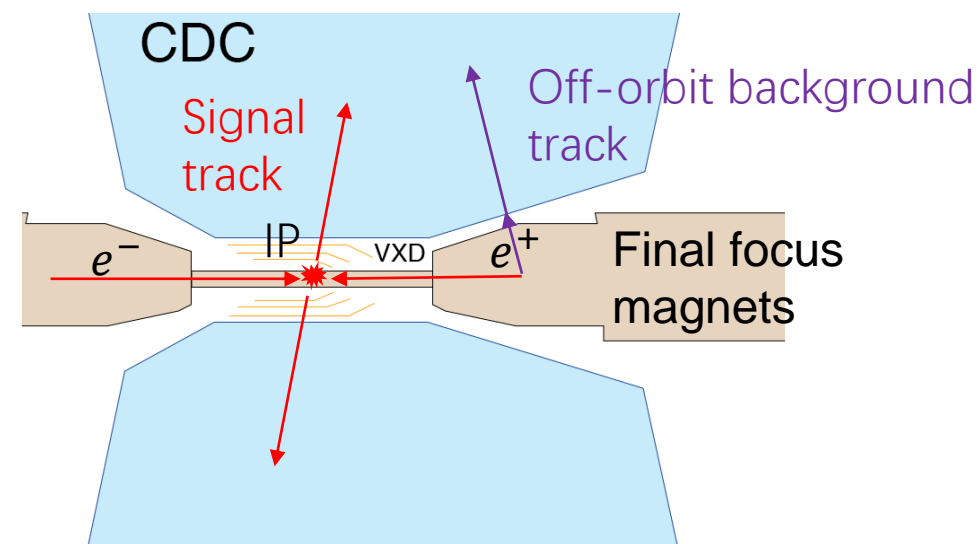
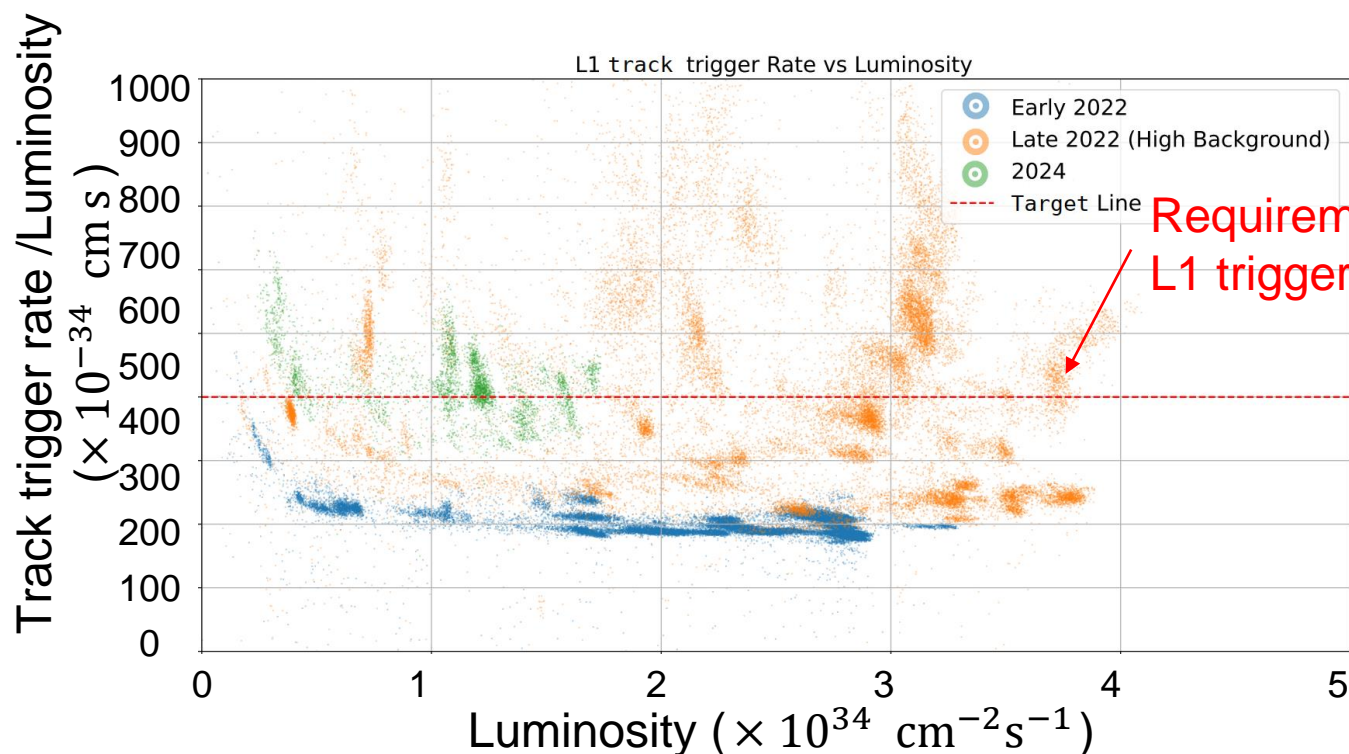




# Motivation for track trigger upgrading

## Requirements for first level trigger system

1. High efficiency for hadronic events
2. **A maximum average trigger rate of 30kHz**
3. A fixed latency of about 4.4  $\mu\text{s}$

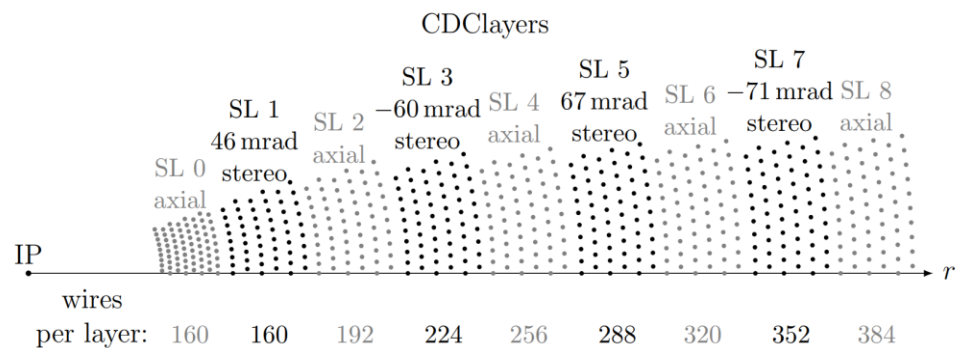
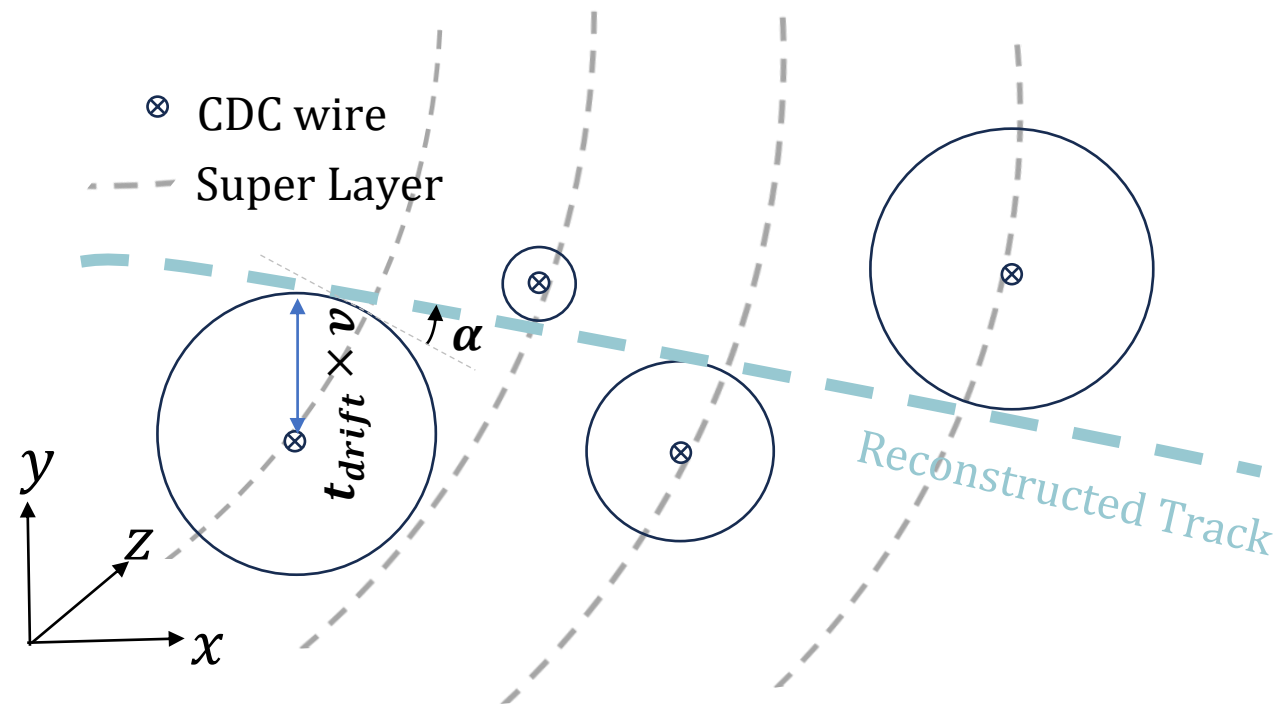
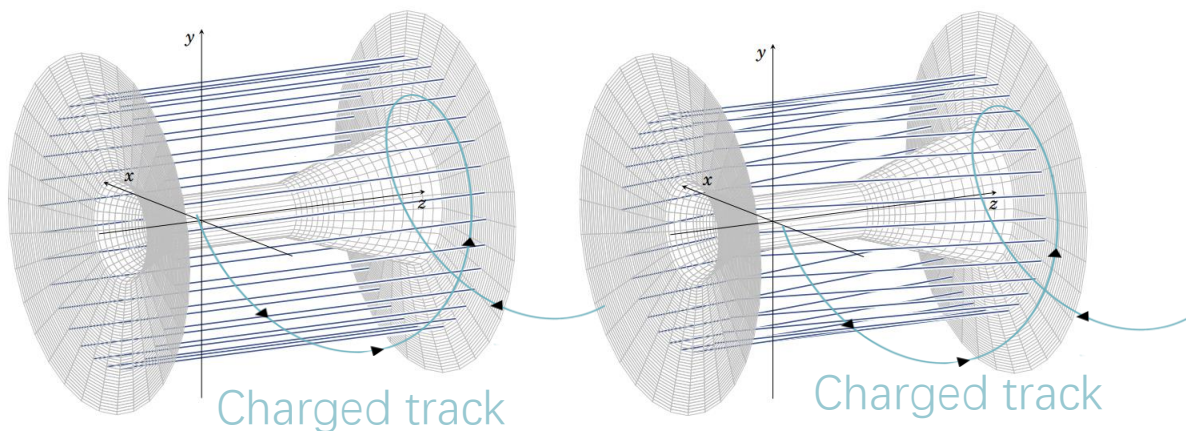


- we aim to decrease the track trigger rate, thereby lowering the overall trigger rate.

# Central drift chamber

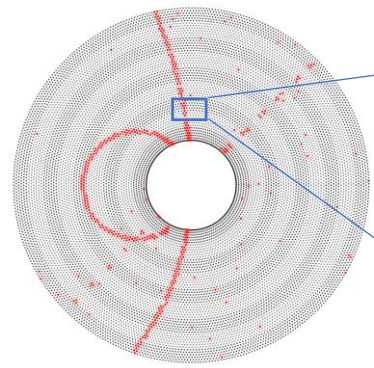
CDC Axial wires  
(parallel to beam direction)

CDC Stereo wires  
(oblique to beam direction)



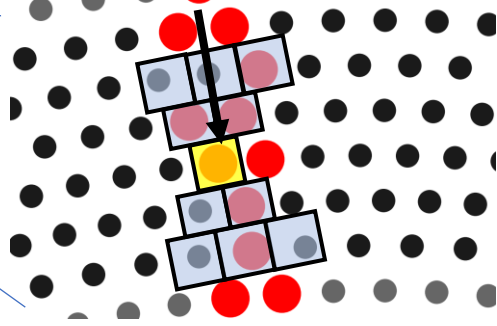
- Track reconstruction information: **location for CDC hits ( $\phi$  and  $r$ )** , **drift time ( $t_{drift}$ )**

# First level CDC track trigger

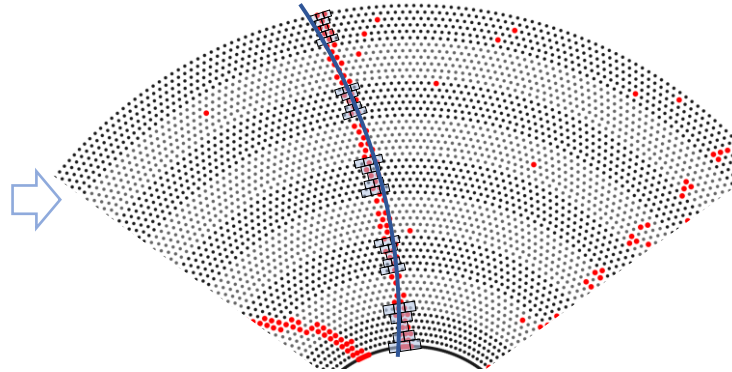


CDC raw hits

Priority wire

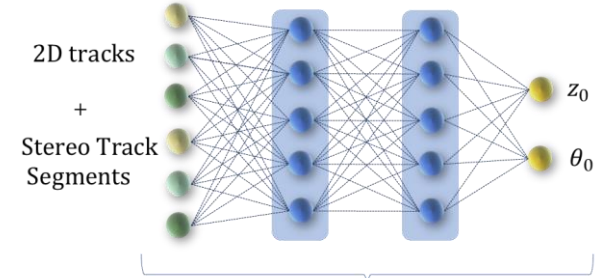


Built **Track Segment** (a set of CDC wires) in every super layer



Build **2D track** with **axial hits** using Hough transformation

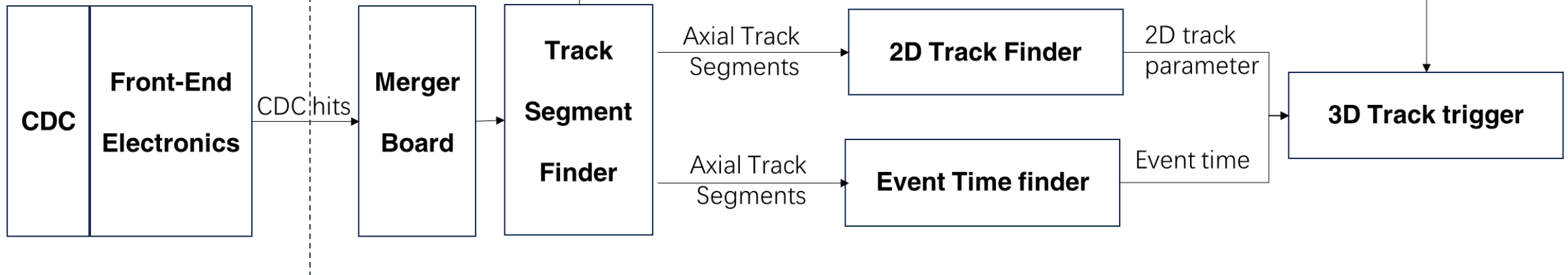
<https://arxiv.org/abs/2402.14962>



Neural Network

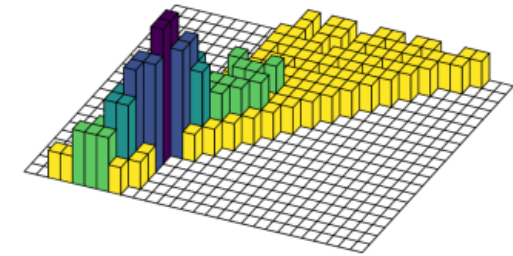
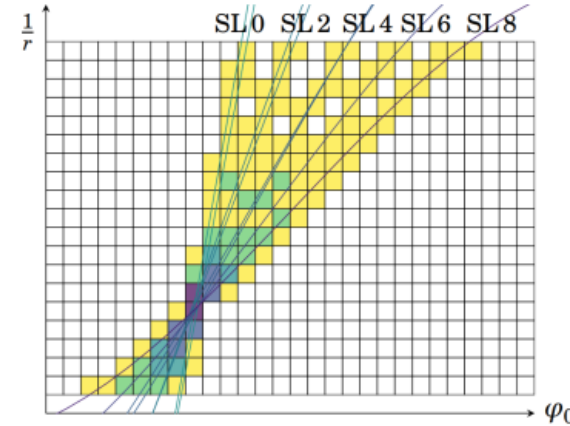
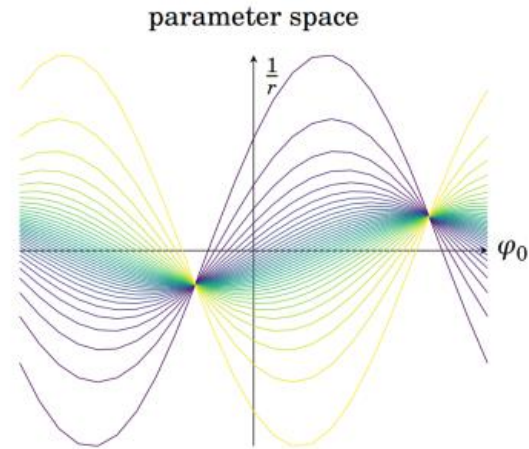
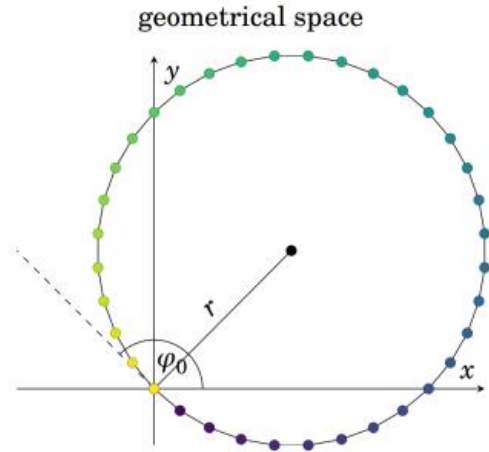
Build **3D track** with **stereo hits** and 2D track using **Neural network**

## CDC L1 trigger





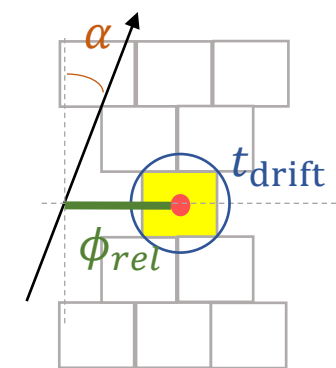
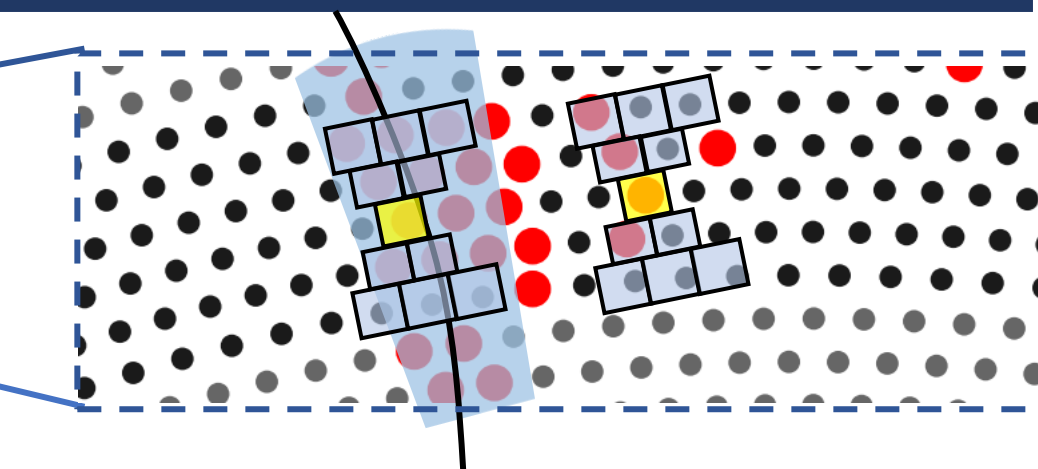
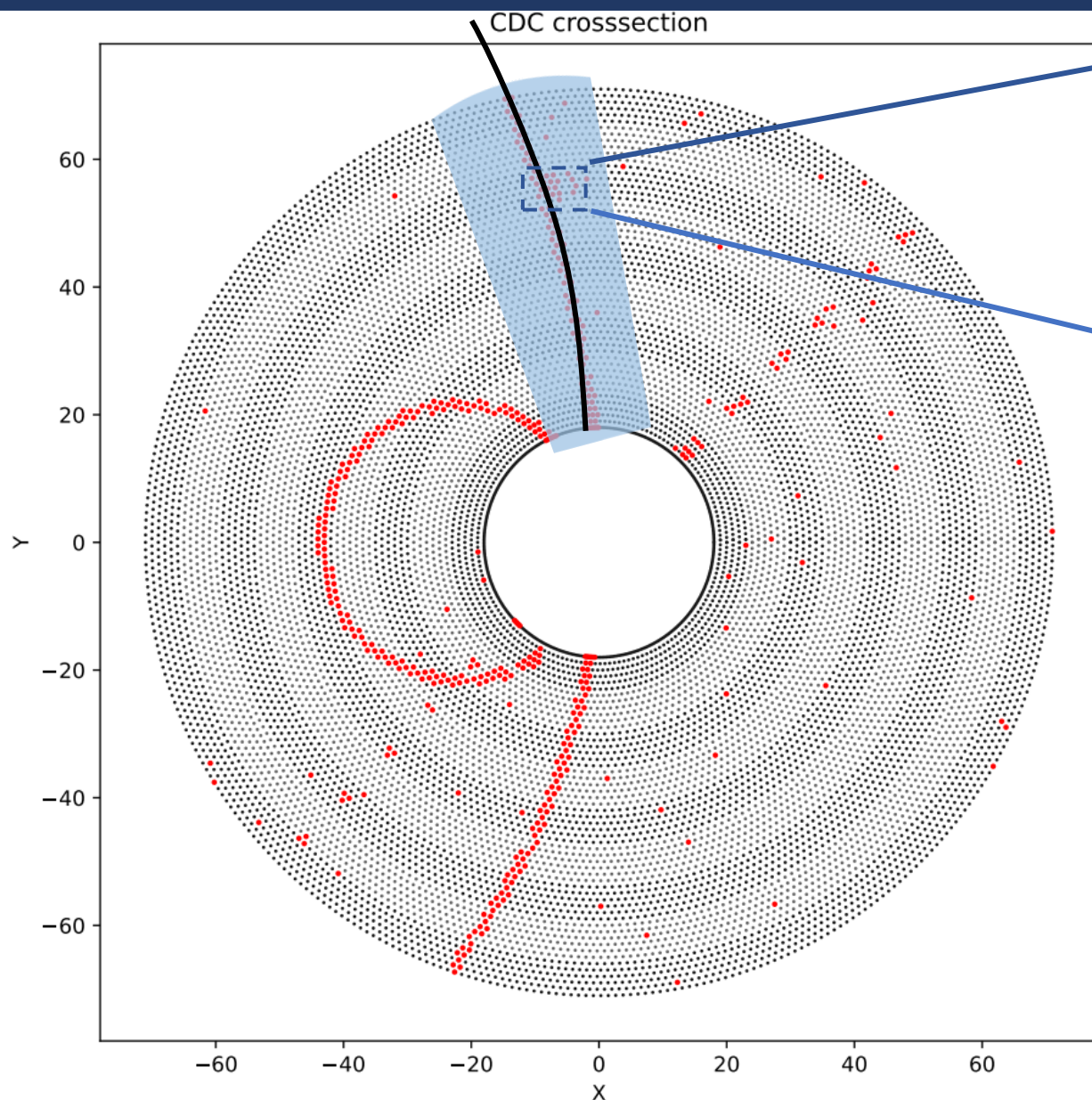
# 2D Hough transformation



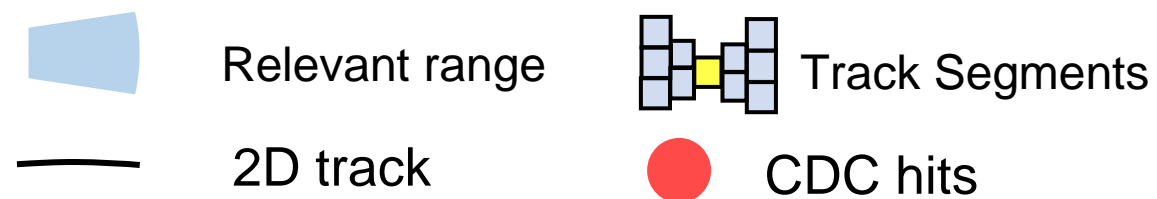
- Mapping points in the geometric space to a parameter space with :  $\rho(\phi) = \frac{2}{r_{TS}} \sin(\phi - \phi_{TS})$
- Implementing a grid separation on the Hough parameter space.
- Counting hits cell and take the cells exceeding threshold as a track



# Inputs selection



- Selected 1 Track Segments per one Super Layers
- Collected the  $\alpha$ ,  $t_{drift}$  and  $\phi_{rel}$  for each track segment

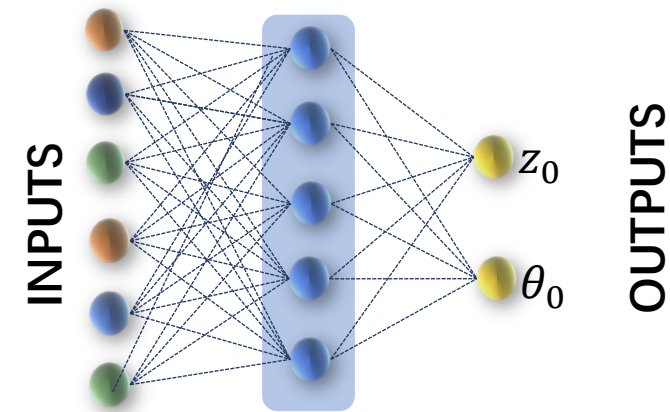


# Why use deep neural network

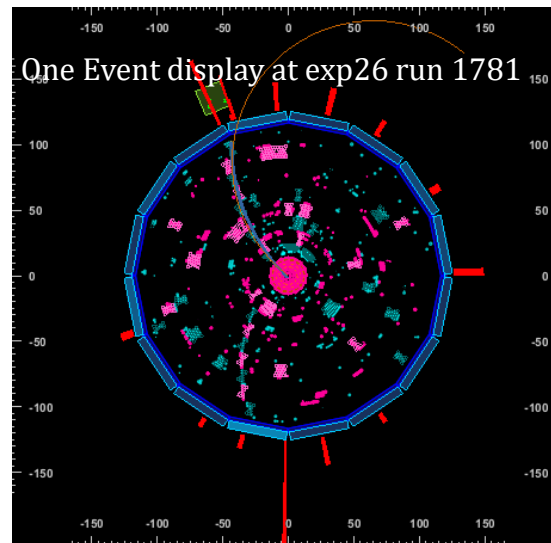
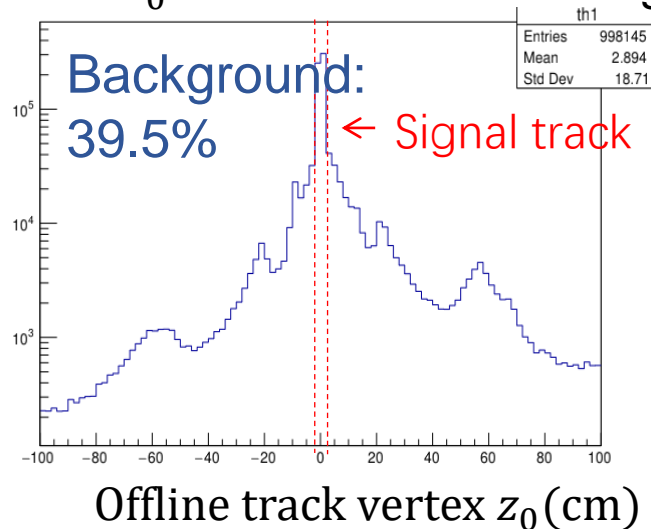
- Background ratio is still high
- Not only “Fitting”, but also “selection”
- Fake track problems

Current used MLP

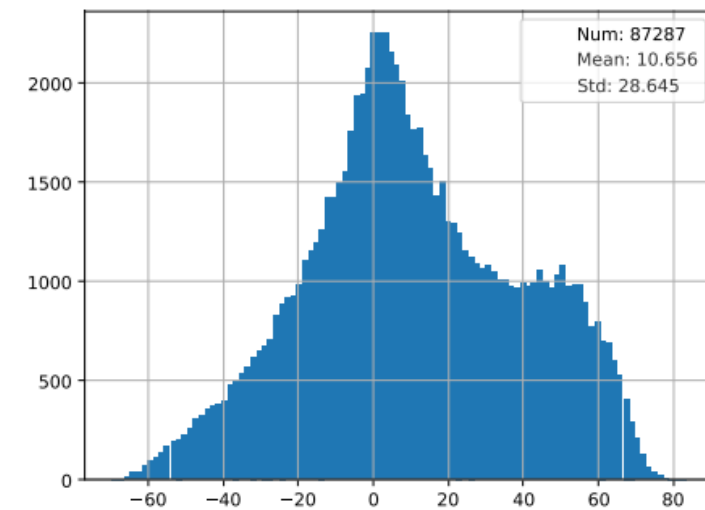
#nodes = 81



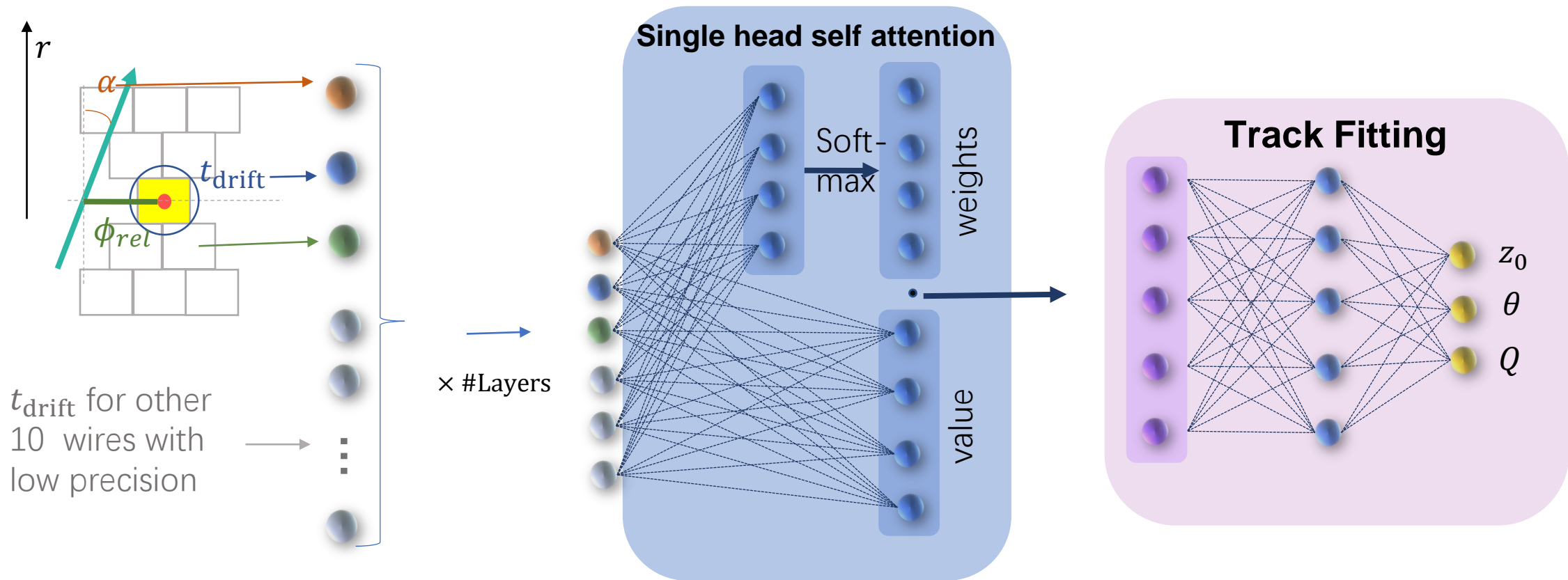
Tracks  $z_0$  distribution after L1 trigger



Fake track

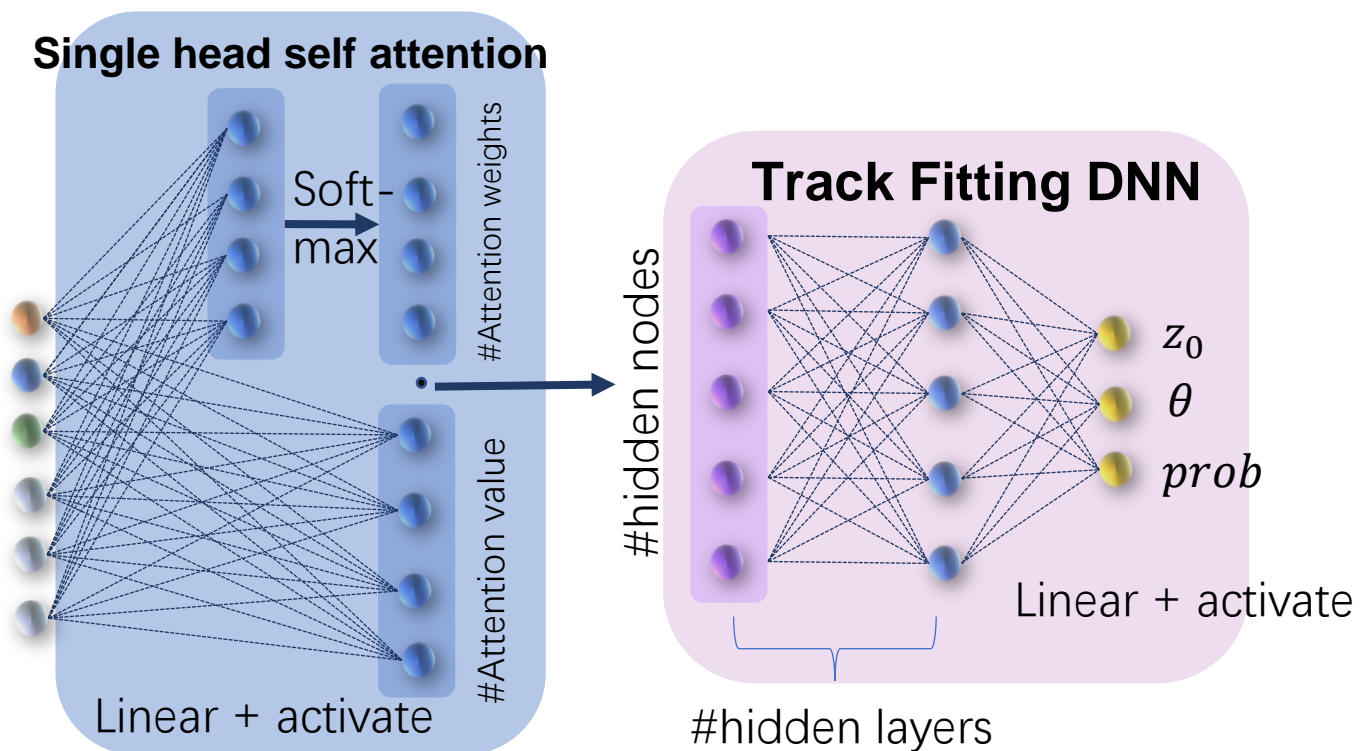


# Neural-network inputs and architecture upgrade

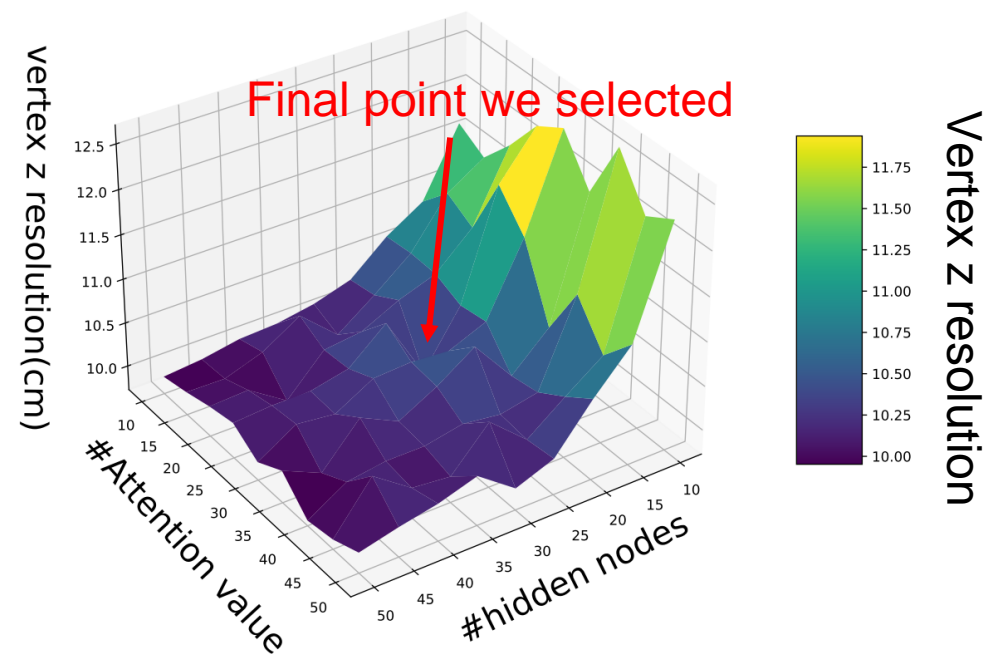




- Inputs: **Drift time**  $t_{\text{drift}}$ , **wires relative location**  $\phi_{\text{rel}}$ , **Crossing angle**  $\alpha$  for priority wires + **Drift time** for all other wires
- Introduce the **self-attention architecture** to “focus” on certain inputs
- Output track vertex  $z_0$ , track  $\theta$  and **classifier output**  $Q$

# Neural-network training, optimization, quantization



Snapshot of optimization process



- Data: real physics run data with high background in late 2022.
- Using  PyTorch lib for model building and training,  OPTUNA for parameters optimization

Parameter	#Attention value	#hidden nodes	#hidden layer	activate	precision	Total multiplier
Values	27	27	2	Leaky Relu	Float 16	4,185



# Field Programmable Gate Arrays (FPGA)

## FPGA contains:

-IOBs : Programmable in/out pins

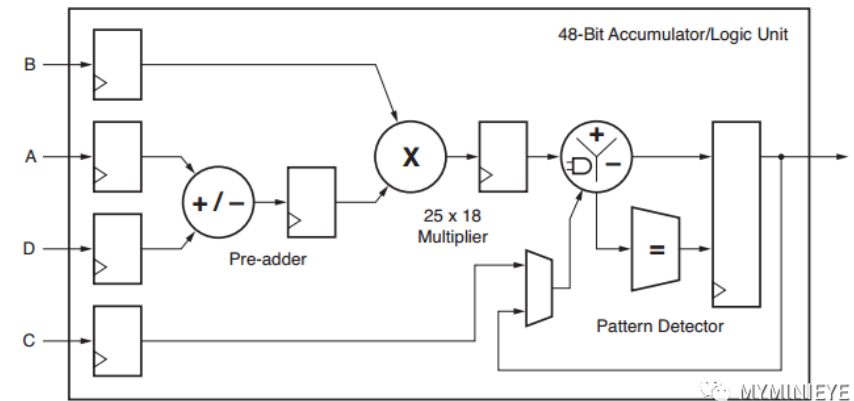
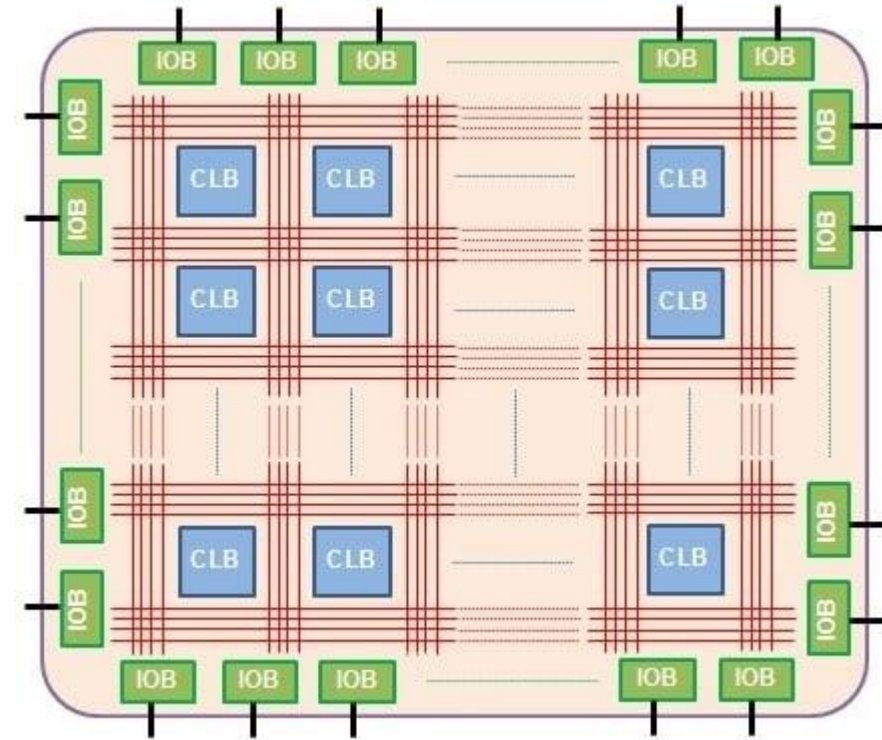
-CLBS : Configurable Logic Blocks

 : Programmable interconnect

## FPGA Advantage:

- Flexibility
- Extremely fast ( $\sim$  ns)
- Fixed latency

**DSP: a logic unit to process Multiply And Accumulate (MAC)**



Digital Signal Processing (DSP) 48E1

# Deep neural-network implementation

Upgrade



Universal Trigger board (UT) generation	3rd	4th
FPGA	Virtex 6 XC6VHX380	Virtex UltraScale XCVU160
DSP	864	1560
Logic gates	380k	2026k
Optical bandwidth	530 Gbps	1300 Gbps

Requirements for implementation:

- Latency: ~300ns (3rd) and ~600ns (4th)
- DSP limitation: 864 (3rd) and 1560 (4th)
- More than 5 times logic gates, can be used for multiply

Belle II UT3



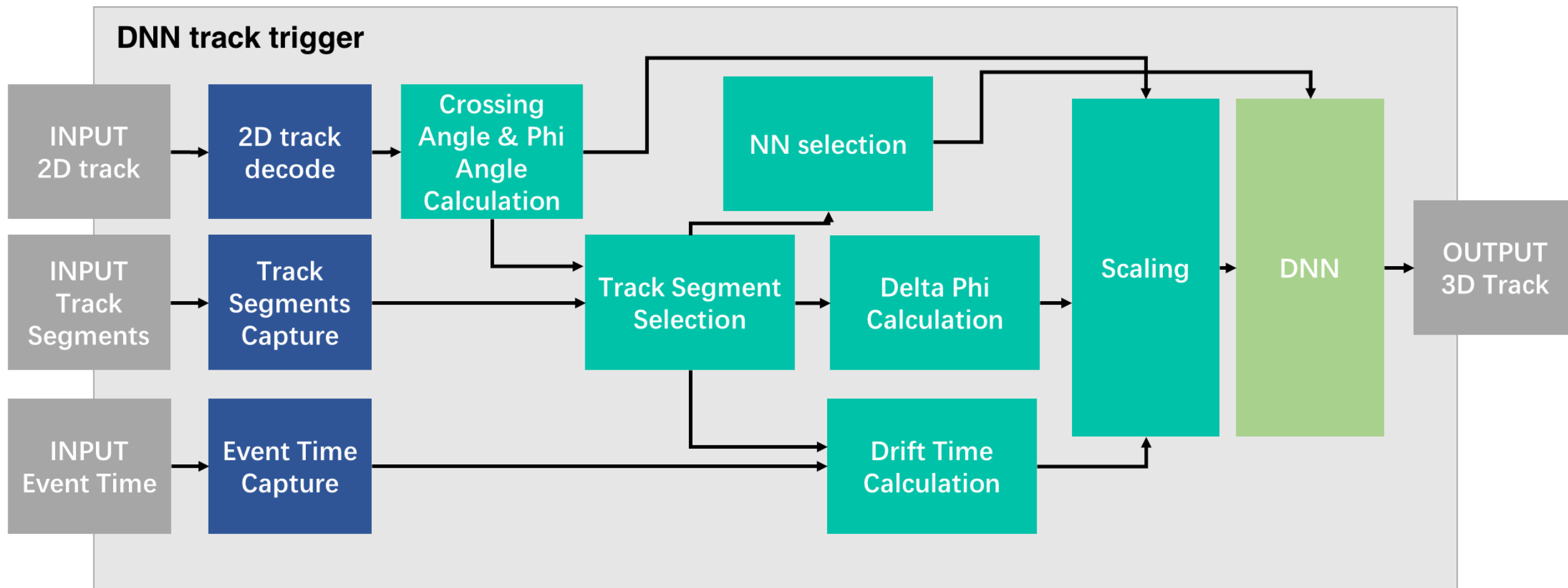
Xilinx Virtex-6  
xc6vhx380t, xc6vhx565t  
11.2 Gbps with 64B/66B

Belle II UT4



Xilinx UltraScale  
XCVU080, XCVU160  
25 Gbps with 64B/66B

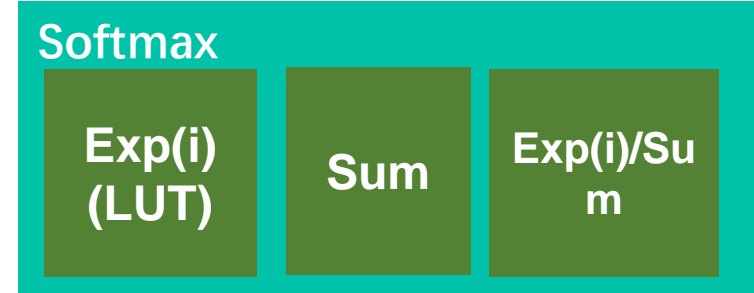
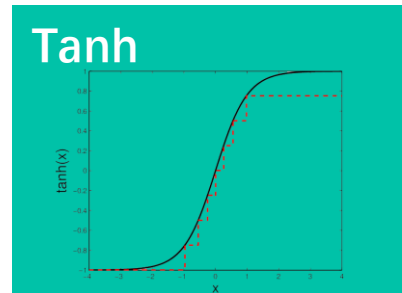
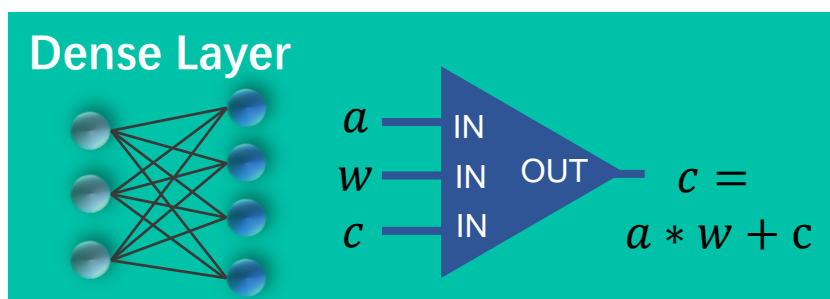
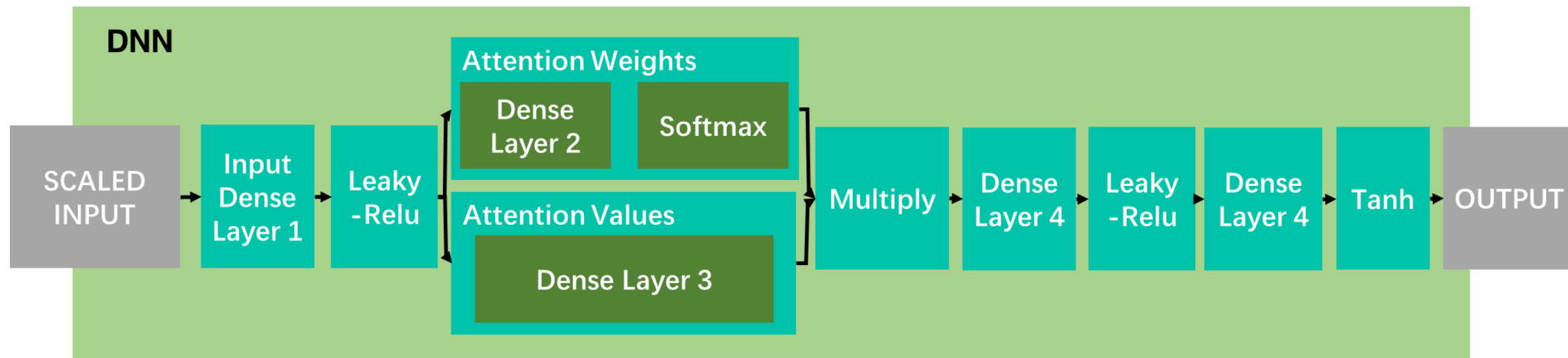
# DNN track trigger firmware architecture




- Input 2D track, track segments and event time pre-processing them to get scaled input for DNN.

- Pre-processing & interface using , Core DNN logic using 

# Firmware architecture for DNN TRG



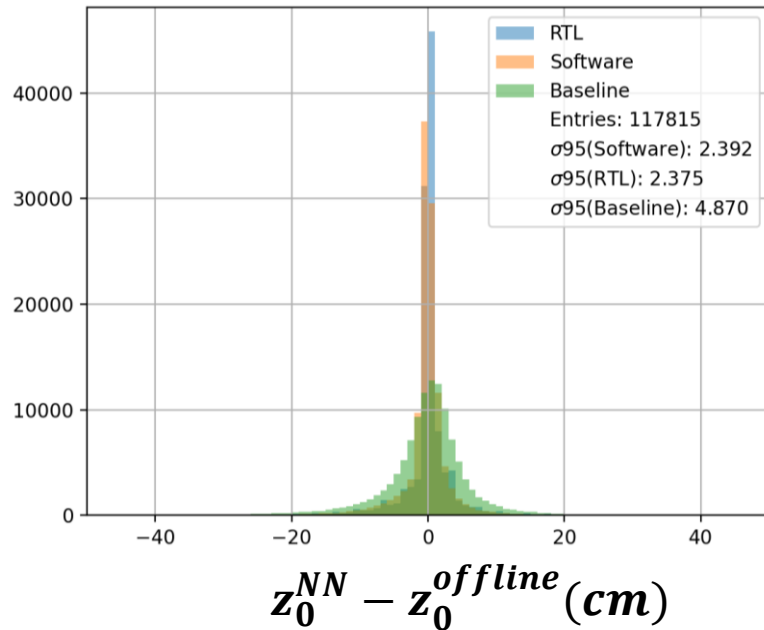
- Using look up table with 18 bits precision for  $\exp(x)$  &  $\tanh(x)$ , refer to the function in 
- Directly use DSP for Leaky ReLU
- For Dense layer, using specific strategy to fit the requirements (next page)



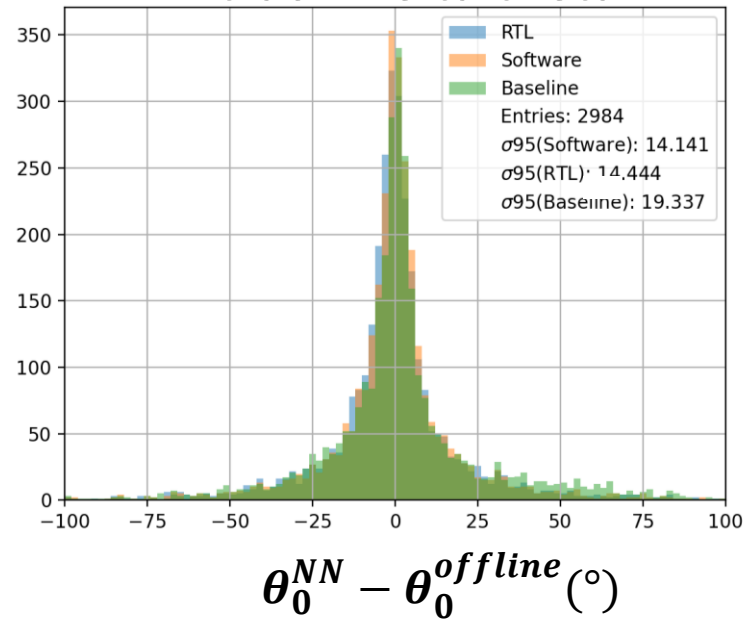
# Performance: Register-transfer level (RTL) simulation

- Performance RTL simulation and comparing performance with pytorch results

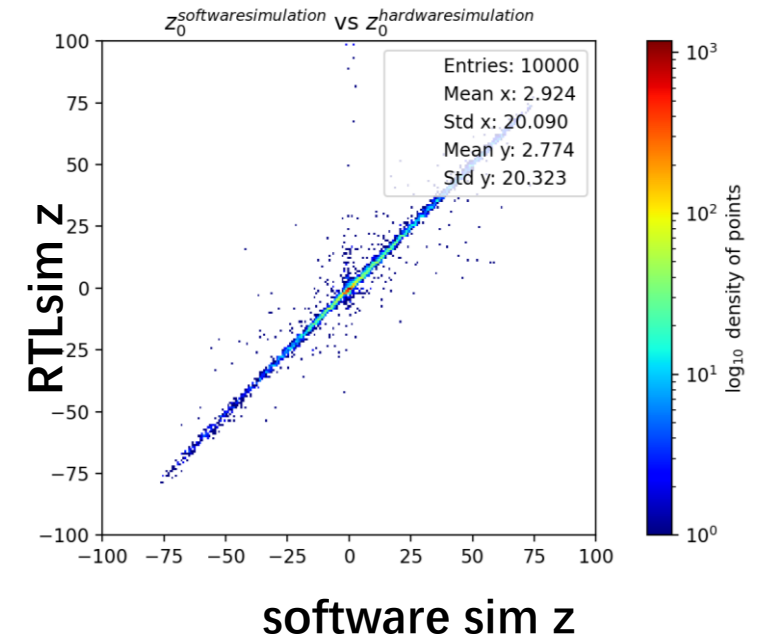
track Delta z



track Delta theta



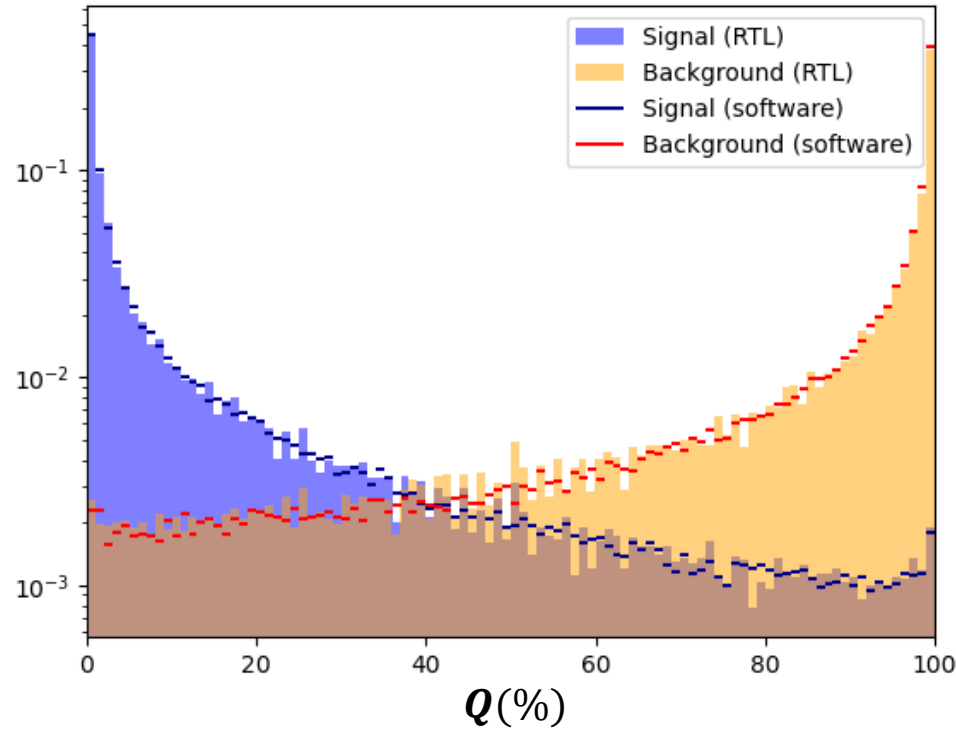
RTL co-sim vs software sim



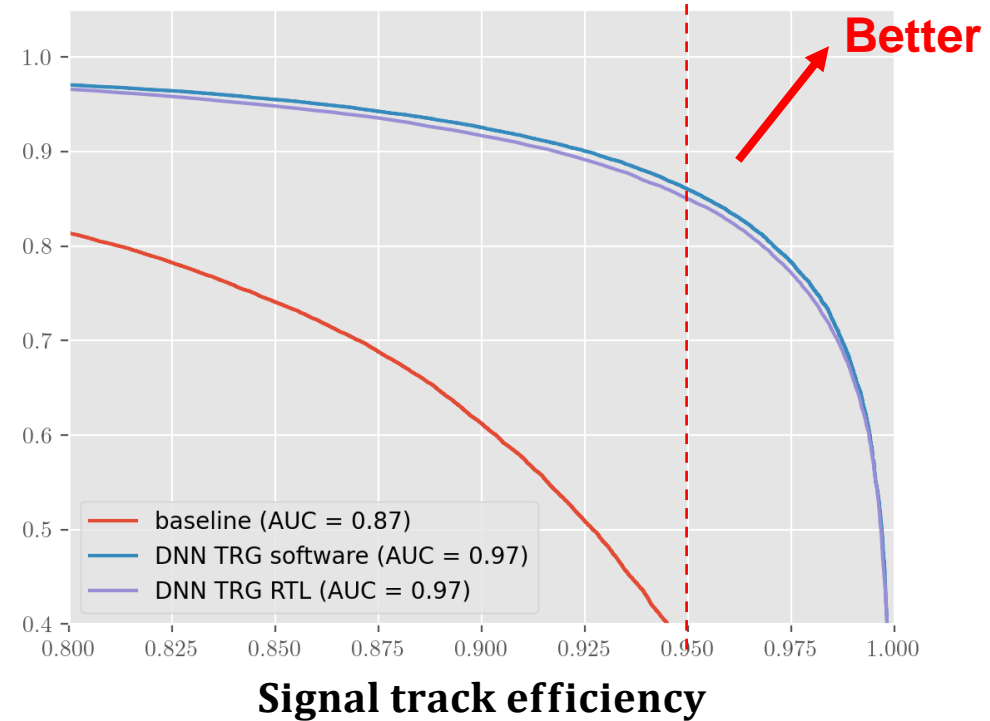
- $\sigma^{z_0} = 2.4 \text{ cm}$ , about  $\frac{1}{2}$  as the baseline  $\sigma^{z_0} = 4.9 \text{ cm}$ ; and  $\sigma^\theta = 14^\circ$  (baseline:  $\sigma^\theta = 19^\circ$ )
- RTL and software simulation matched. Reducing precision did not loss the resolution.

# Performance: Register-transfer level (RTL) simulation

## Classifier output

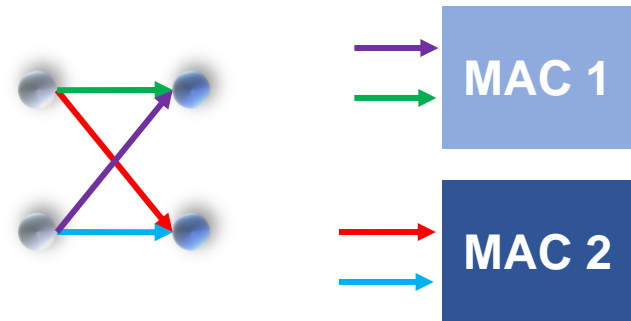


## background track rejection rate



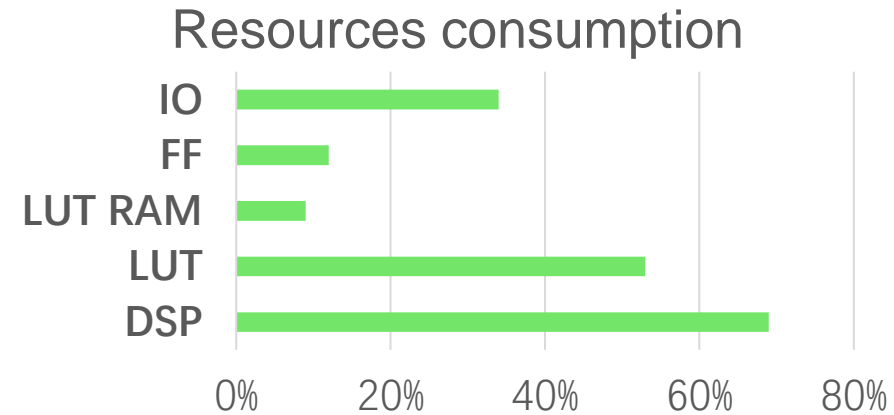
- $Q$  output got consistent with software result
- AUC do not get large drop comparing RTL and software simulation
- At signal track efficiency at  $\sim 95\%$  :  
Background rejection rate: **NN track trigger (baseline): 39%**; **DNN track trigger: 85%**

# Implementation result



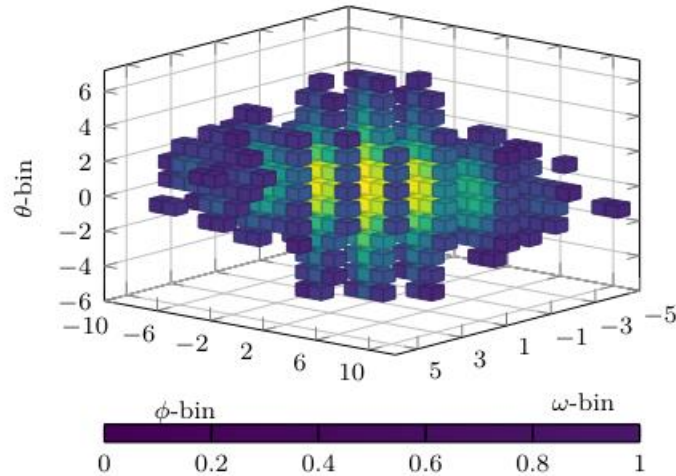
Reuse every multiplier by twice

- **4000** multiplier v.s. **1600** DSP
- Using both LUT and DSP to perform Multiply And Accumulate (MAC)
- Reuse each MAC twice.

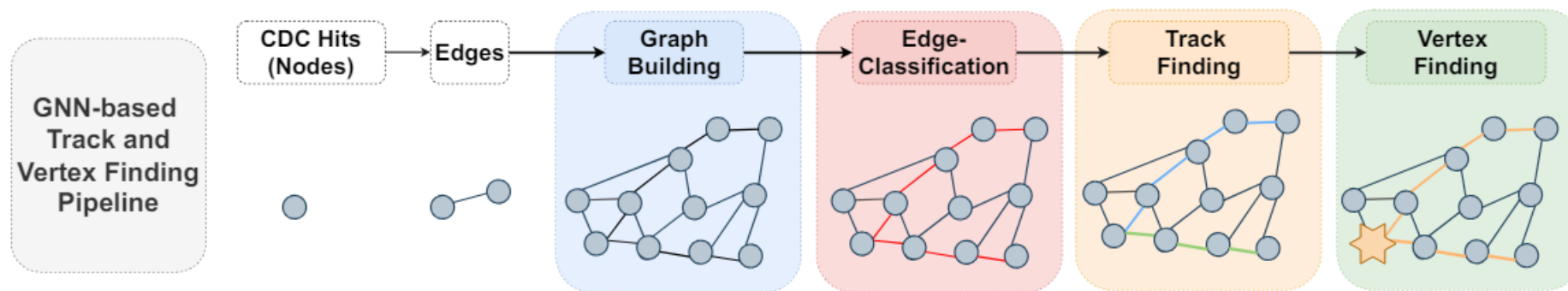


- Resource matched requirements, not timing violation
- Latency : 76 clock = 592.8 ns ;require: < 600ns
- Pipeline Interval (dead time) = 32ns ;require: 32ns

# Next step: 3D Hough and GNN



3D Hough Transformation  
 $(\theta, \phi, \omega)$



GNN track finding



# Summary

- The upgrade of Belle II first level track trigger is on-going
- We examined the performance for upgrade trigger with both software and RTL simulation, and achieved a 2.2 times background rejection rate improvement.
- We successfully implemented the DNN track trigger with UT4 module and fulfill the requirements with latency  $\sim 600\text{ns}$  and II  $\sim 4$  clock.
- We are working on the commission work for the DNN track trigger

## Next Step

- 3D Hough transformation and GNN



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**Thanks for your attention**



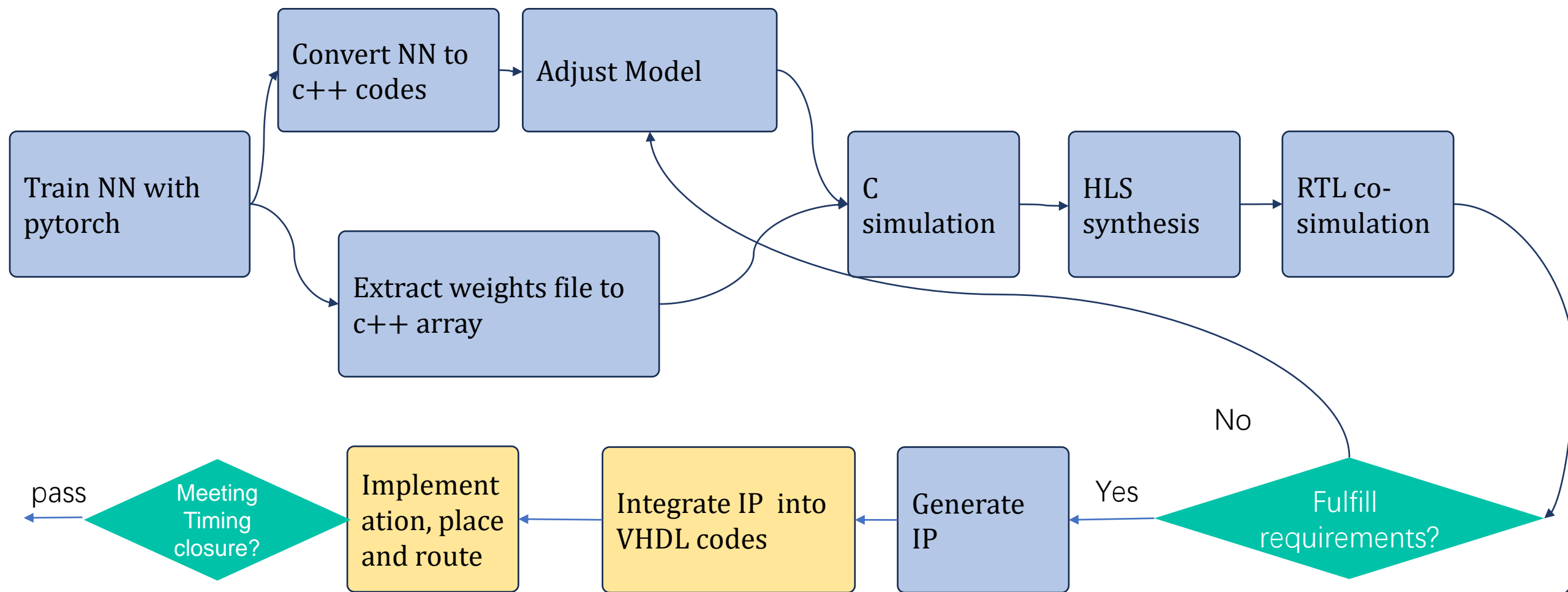


**Backup**

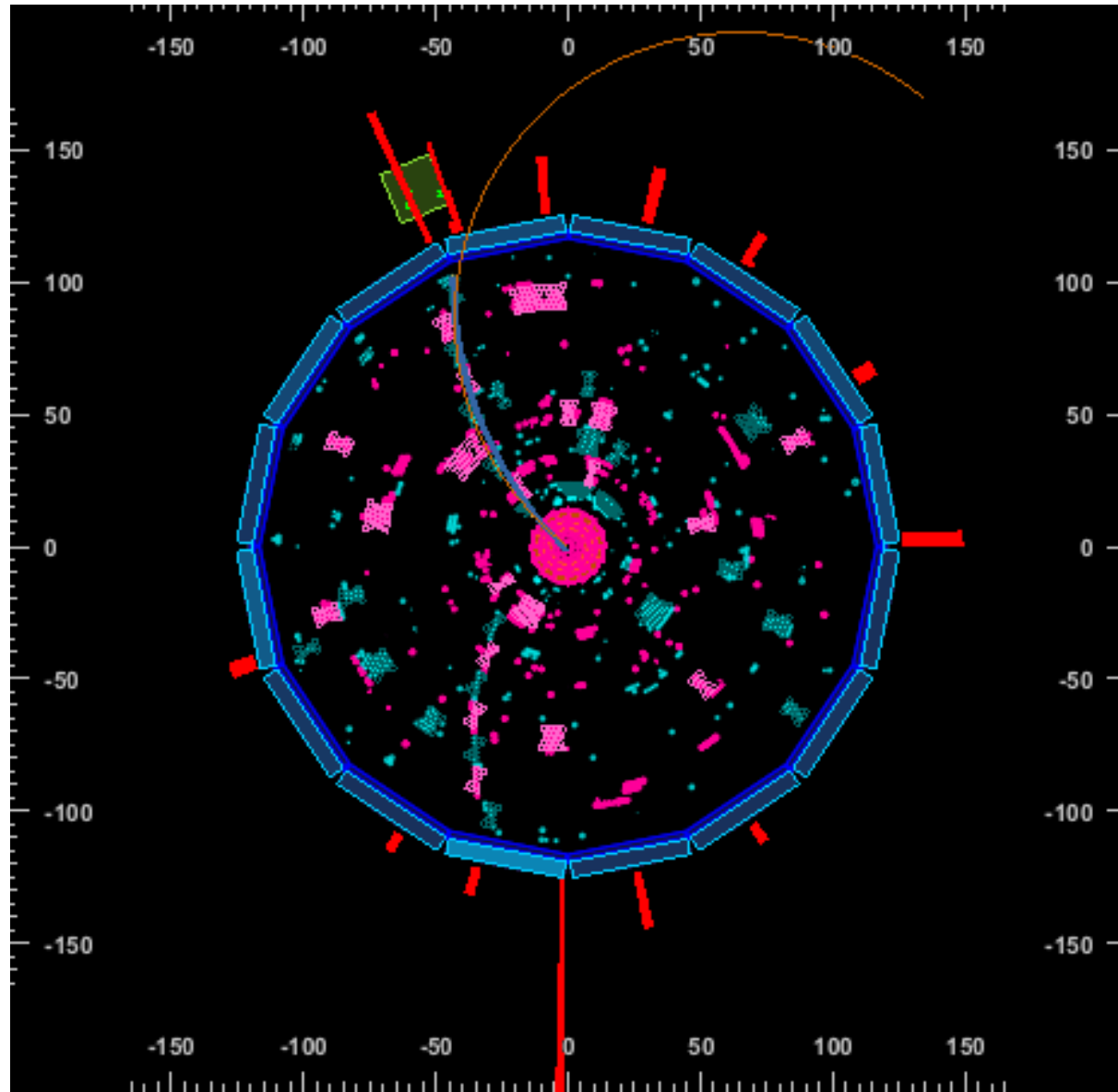
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# Workflow with HLS

\*include some function  
from hls4ml lib



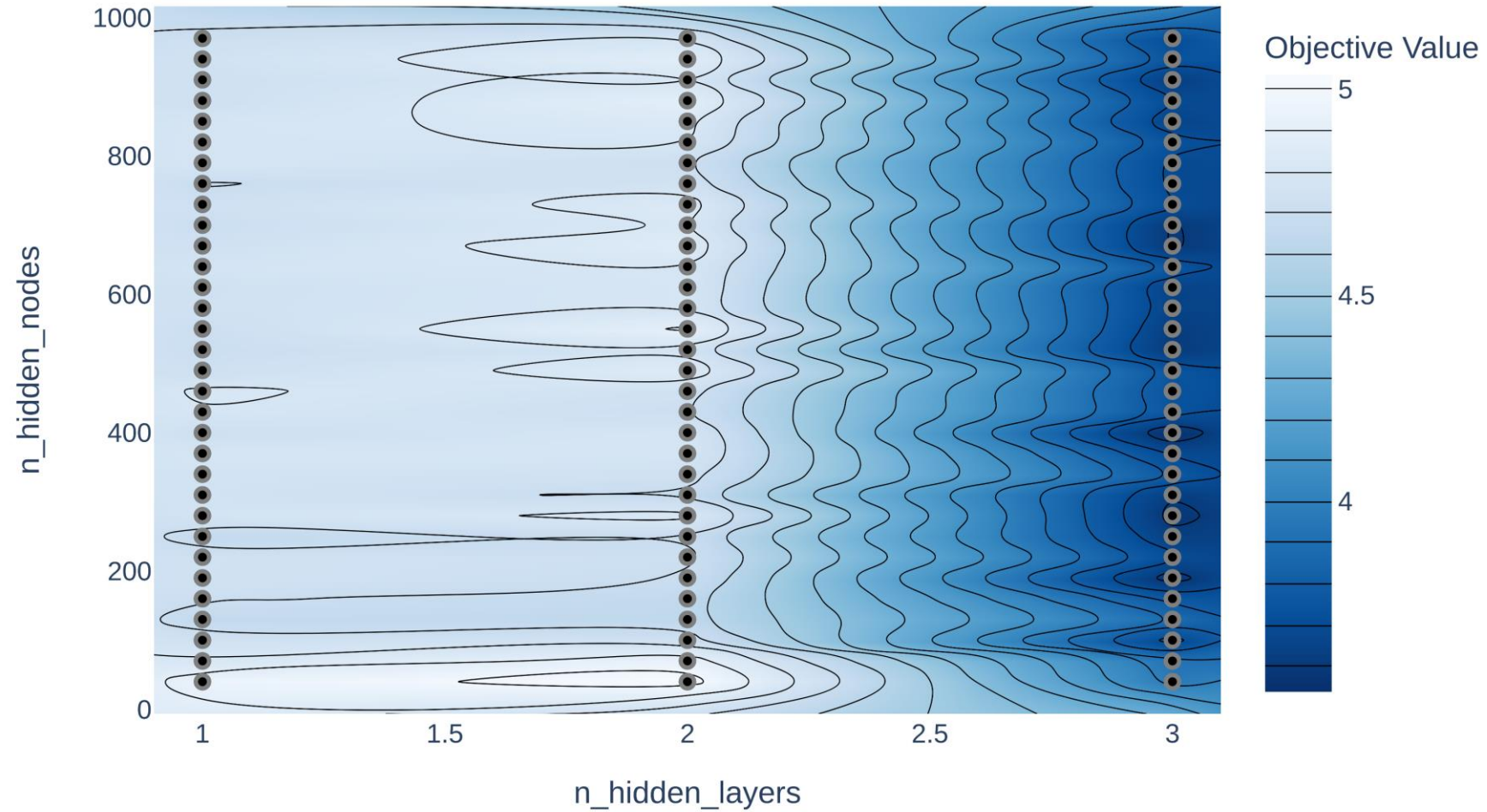
# General physics events shape





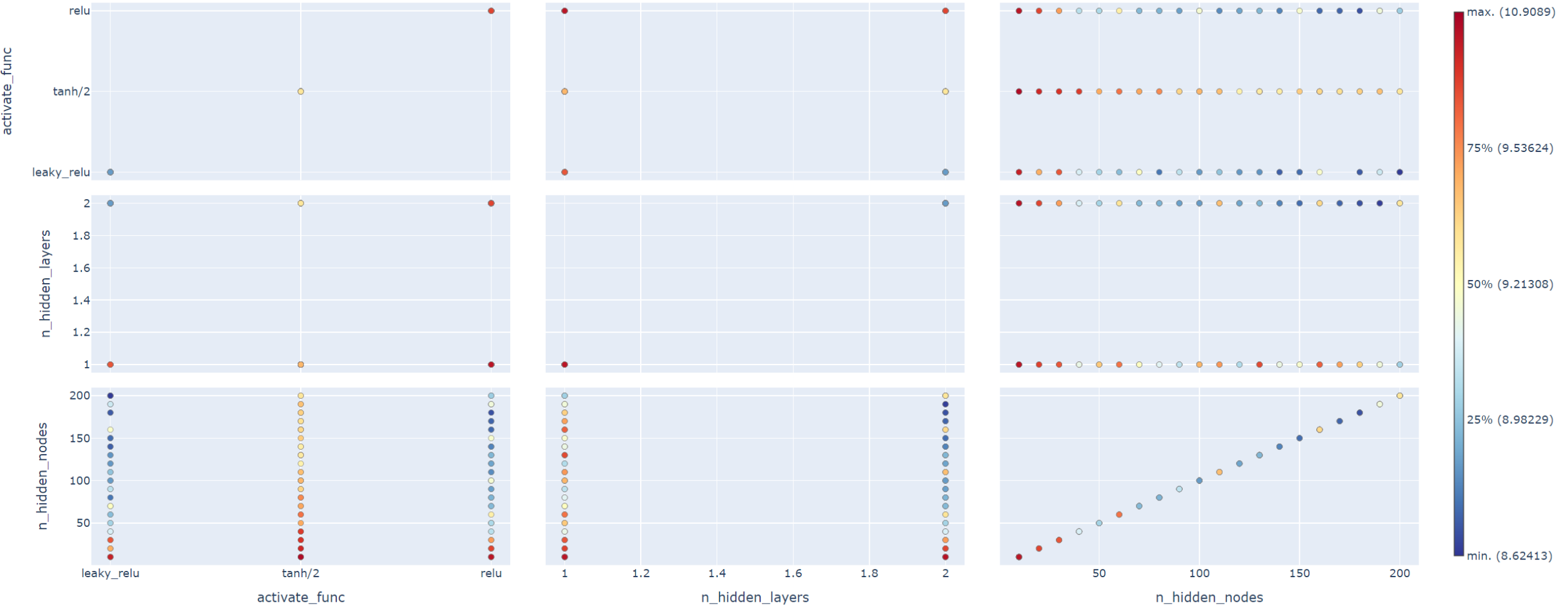
# Depth is much more powerful than width

Contour Plot

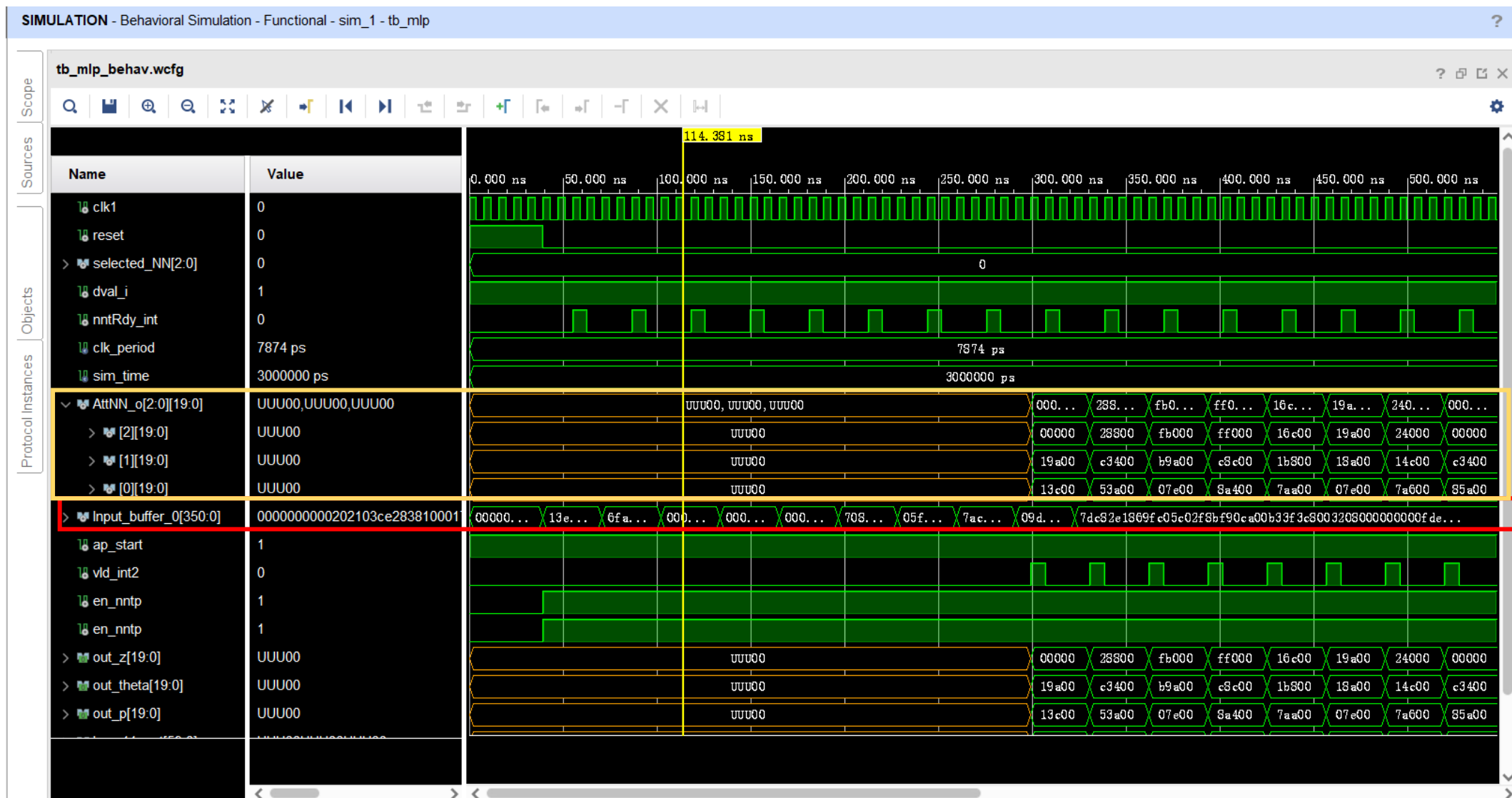


# Optimization for Self-attention MLP

Rank (Objective Value)



# Core Logic vivado simulation pass



Output: after  
~600ns

Input: every 4  
clock a new input

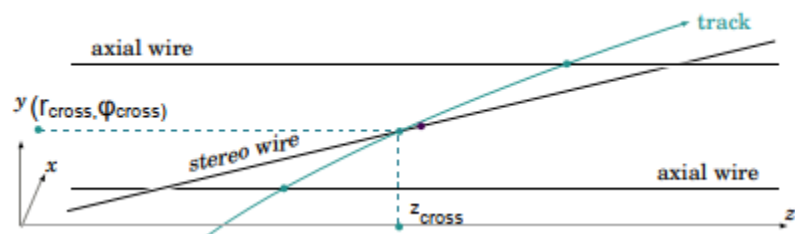
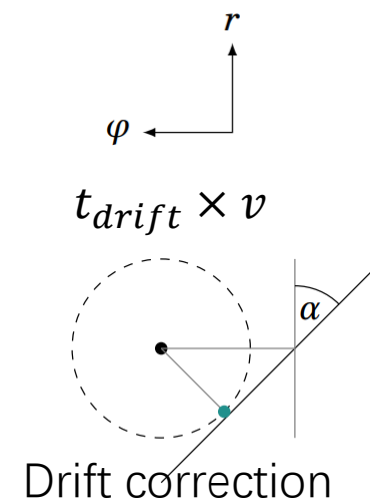
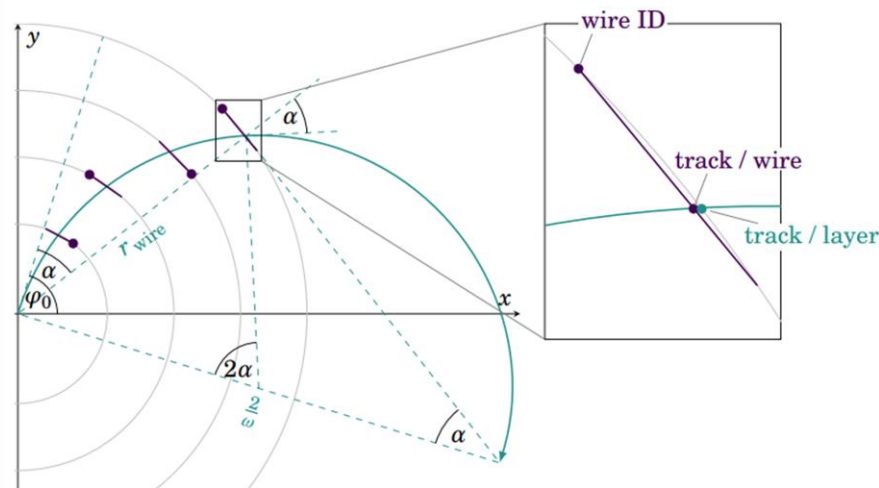
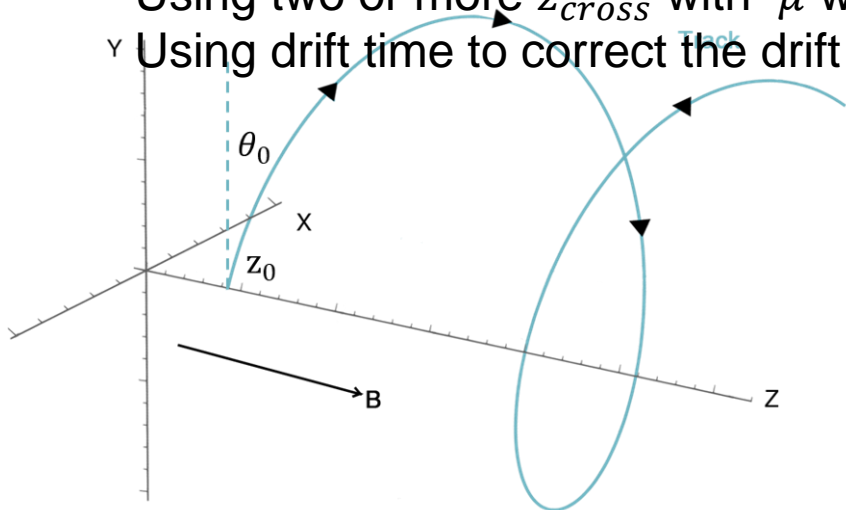
# Introduction CDC trigger - 3D reconstruction

Only  $\theta_0$  and  $z_0$  remain unknown for 3D tracks.

With Crossing angle  $\phi_{cross}$  for stereo wire we can get  $z_{cross}$ .

Using two or more  $z_{cross}$  with  $\mu$  we can fit the linear track in  $\mu - z$  plane and obtain  $\theta_0$  and  $z_0$ .

Using drift time to correct the drift distance.



$$\begin{pmatrix} x(\mu) \\ y(\mu) \\ z(\mu) \end{pmatrix} = \begin{pmatrix} r \cdot (\sin(\mu/r - \phi_0) + \sin \phi_0 + x_0) \\ r \cdot (\cos(\mu/r - \phi_0) - \cos \phi_0 + y_0) \\ \cot \theta_0 \cdot \mu + z_0 \end{pmatrix}$$

# Requirement for new developed NN

Parameters	Target
$z_0$ resolution at IP ( $\sigma_{95}^{IP}$ )	<2 cm
Trigger efficiency	>95%
Extra background rejection rate	>50%

- Reduce the  $z_0$  resolution for signal track to less 2 cm
- Keep same efficiency as before (>95%) and restrict cut to reject further half of background events, which were kept by current trigger.

	CDC $B\bar{B}$ bits	CDC $\tau$ & dark bits
Current CDC Background raw trigger rate	2.15 kHz	1.91 kHz
Required CDC Background raw trigger rate	1.07 kHz	0.9 kHz

- New NN algorithm can be implemented on new universal trigger board (called UT4) ,which has about 4 times more logic gates than previous one.



# Performance evaluation – Training, validation and testing sample

Data sample generate from special physics run data taken without HLT trigger.

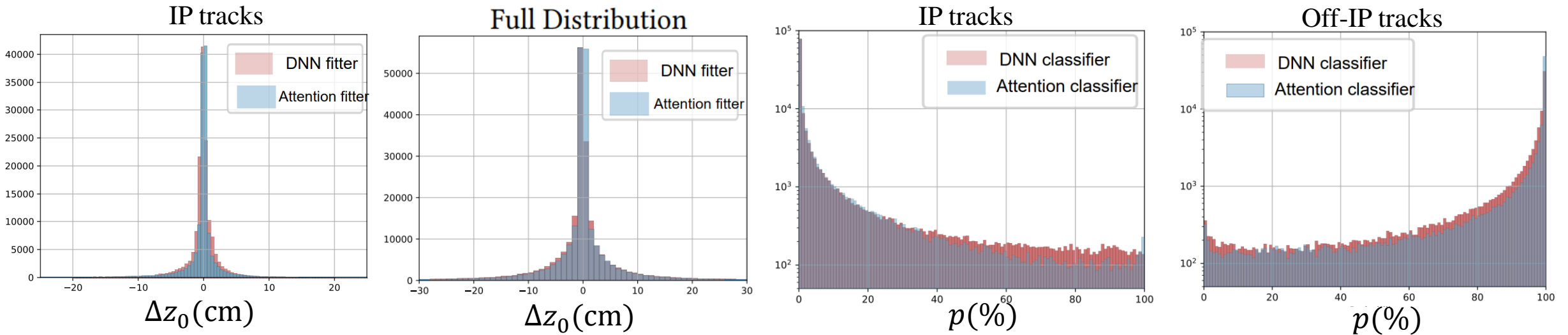
Target  $z_0$  and  $\theta_0$  of Tracks are got from offline reconstruction and fed for training

Randomly separate full sample in training validation and test:

	#Signal Tracks	# Off-IP Tracks	#Fake Tracks
Training sample	935K	284K	0
Validation sample	282K	85K	0
Test sample	180k	53k	87k

Fake tracks are only included in test sample -- No target  $z_0$  and  $\theta_0$

# Performance evaluation – Attention based NN



	Cut	$\sigma_{95}^{IP}$ (cm)	signal track efficiency (%)	off-IP track reject rate(%)	
Neurotrigger	$ z_0^{NN}  < 15$	5.53	93.5	52.0	
DNN fitter	$ z_0^{NN}  < 15$	2.34	97.5	56.7	6%↑
<b>Attention fitter</b>	$ z_0^{NN}  < 15$	<b>1.84</b>	<b>97.8</b>	<b>59.4</b>	
DNN classifier	$p < 65$	/	95.1	84.4	12%↑
<b>Attention classifier</b>	$p < 65$	/	<b>96.6</b>	<b>86.2</b>	

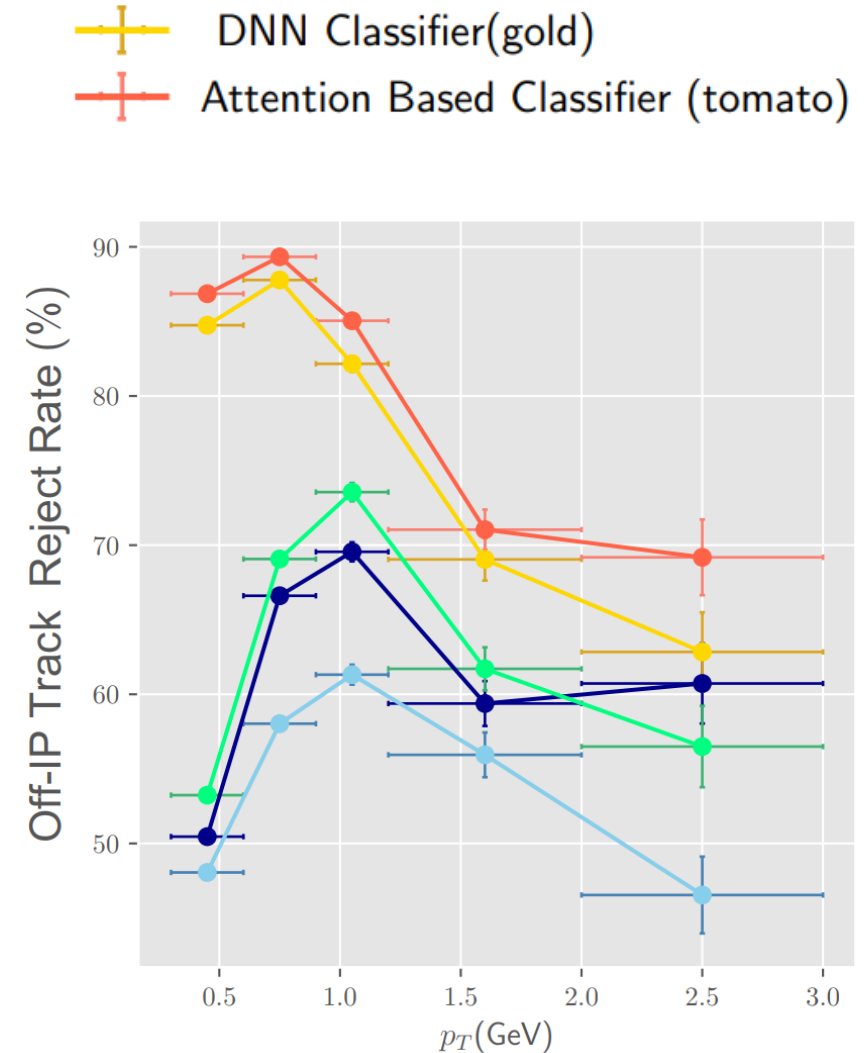
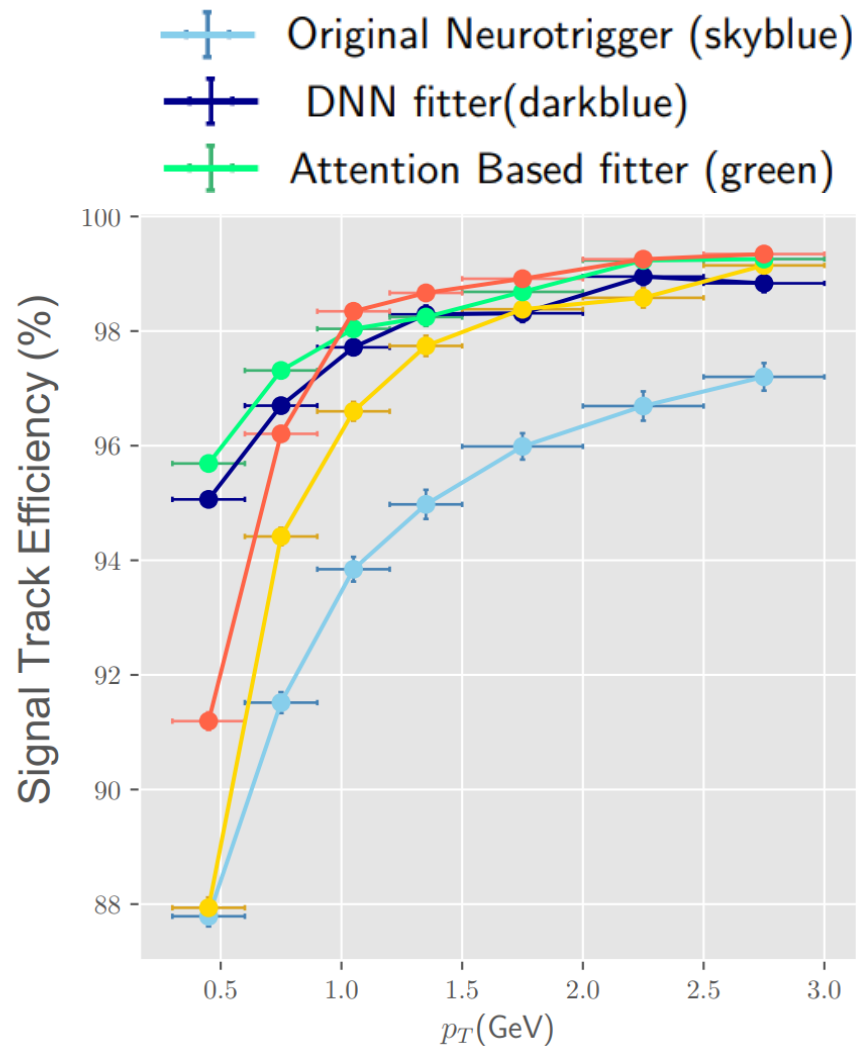
Attention NN gain 0.5 cm IP resolution and ~12% reject rate improvement comparing with DNN

# Performance evaluation – Transverse momentum dependency

Check the efficiency and reject rate dependency of Transverse momentum ( $p_T$ )

Cut:  $p < 65$  OR  $|z_0^{NN}| < 15$

- All new model have better efficiency & reject rate at any  $p_T$
- Classifiers improve low  $p_T$  reject rate by 30%, while have lower efficiency comparing with fitters



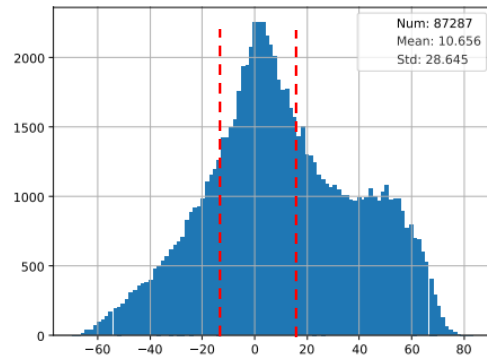
# Performance evaluation – Fake track

**Classifiers** can identify fake track well which mainly **concentrate at  $p \sim 100$**

For **Fitters**, Fake track have a certain  $z_0^{NN}$  distribution **centering at  $\sim 0$** .

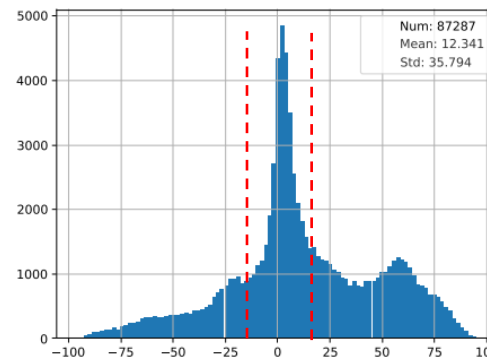
With Cut:  $p < 65$  OR  $|z_0^{NN}| < 15$

Original Neurotrigger



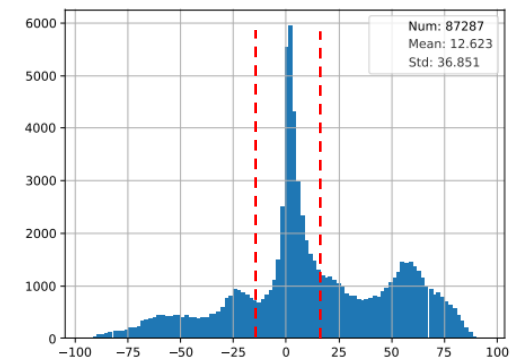
$z_0^{NN}$  (cm)

DNN fitter



$z_0^{NN}$  (cm)

Attention based fitter

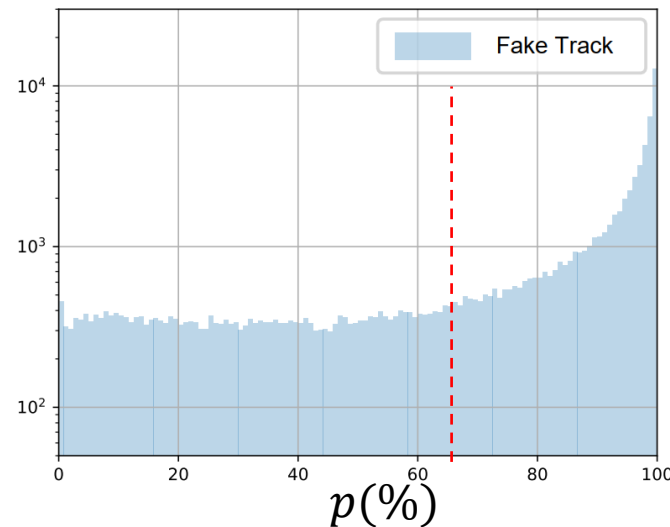


$z_0^{NN}$  (cm)

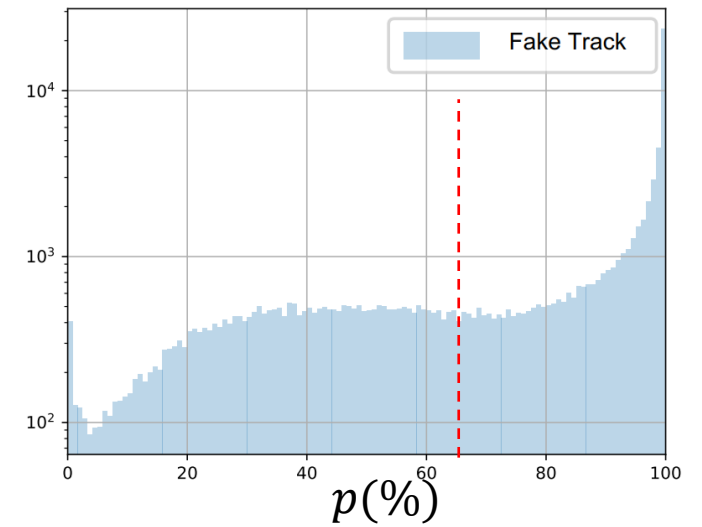
**Fake tracks reject rate**

Original Neurotrigger	60.4%
DNN fitter	58.5%
Attention based fitter	59.8%
DNN classifier	68.5%
Attention based classifier	66.5%

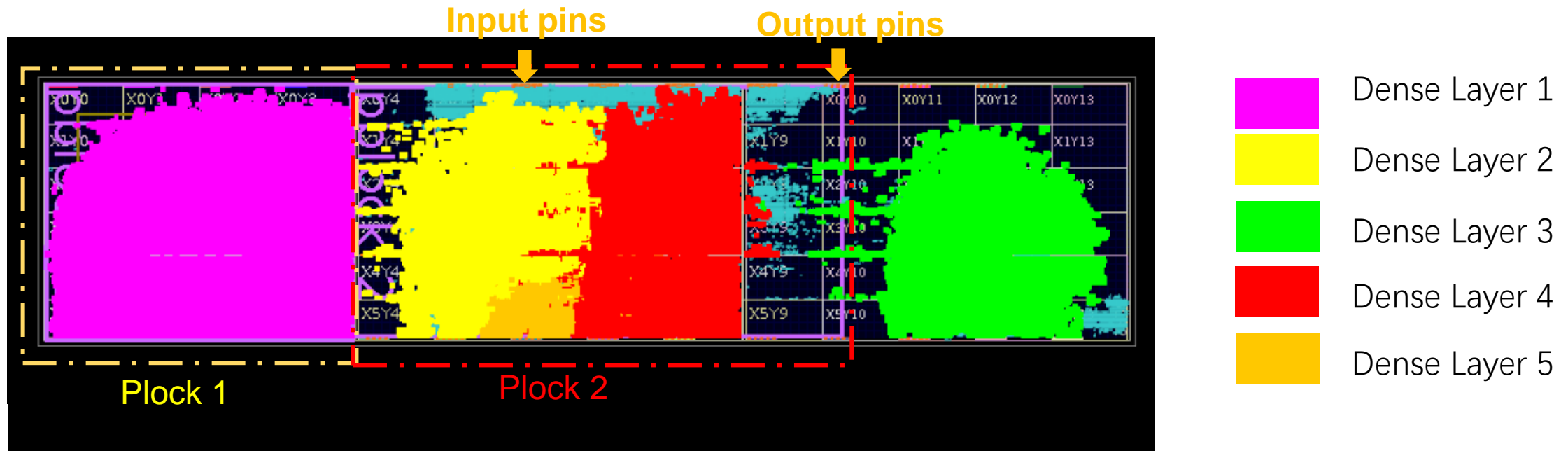
DNN classifier



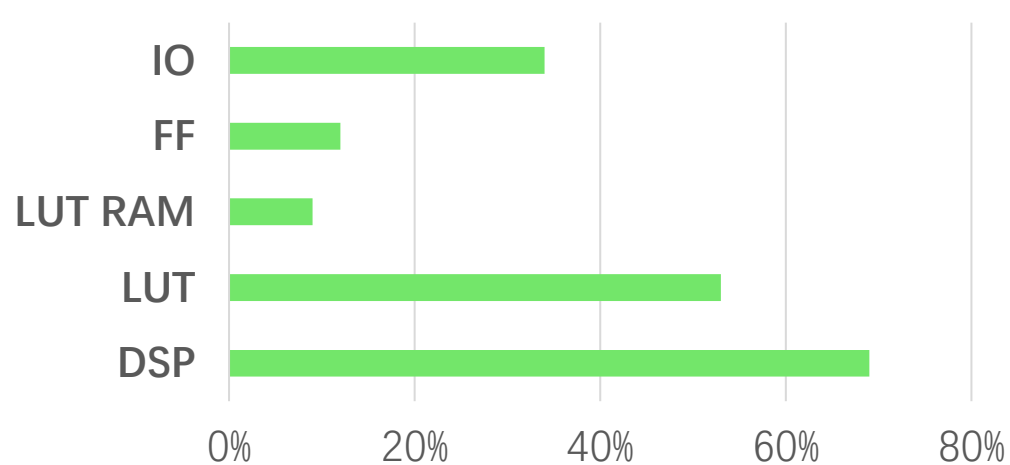
Attention based classifier



# Floor planning and Implementation result



Resources consumption



- Floor planning the dense layers :
- Resource matched requirements, not timing violation
- Latency : 76 clock = 592.8 ns ;require: < 600ns
- Initial Interval = 4 clocks ;require: 4 clocks