

Introduction

The Super-Natural and Effectively Super-Natural SUSY

SUSY Dark Matter

The Generalized No-Scale  $\mathcal{F}$ - $SU(5)$

The Right-handed Slepton Bulk Region for Dark Matter in the pM

The Right-Handed Smuon NLSP Scenario

Conclusion

# The Right-Handed Slepton Bulk Region for Dark Matter in Generalized No-scale $\mathcal{F}$ - $SU(5)$ with Effective Super-Natural Supersymmetry

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# The Content of this Talk

- ▶ The Right-Handed Slepton Bulk Region for Dark Matter in Generalized No-scale  $\mathcal{F}$ - $SU(5)$  with Effective Super-Natural Supersymmetry.

The scenario can solve the supersymmetry electroweak fine-tuning problem.

- ▶ The Right-Handed Slepton Bulk Region for Dark Matter in the pMSSM.
- ▶ The Right-Handed Smuon NLSP Scenario.

## References:

- ▶ T. Leggett, T. Li, J. A. Maxin, D. V. Nanopoulos and J. W. Walker, arXiv:1403.3099 [hep-ph]; Phys. Lett. B **740**, 66 (2015) [arXiv:1408.4459 [hep-ph]].
- ▶ G. Du, T. Li, D. V. Nanopoulos and S. Raza, Phys. Rev. D **92**, no. 2, 025038 (2015) [arXiv:1502.06893 [hep-ph]].
- ▶ R. Ding, T. Li, F. Staub and B. Zhu, Phys. Rev. D **93**, no.9, 095028 (2016) [arXiv:1510.01328 [hep-ph]].
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- ▶ I. Khan, W. Ahmed, T. Li and S. Raza, Phys. Rev. D **109**, no.7, 075051 (2024) [arXiv:2312.07863 [hep-ph]].

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# The Standard Model

- ▶ The SM has been confirmed.
- ▶ However, it cannot be the final theory for particle physics.

# Motivation for New Physics beyond the Standard Model

## ▶ The convincing evidence

Dark energy; dark matter; neutrino masses and mixing; baryon asymmetry; inflation; ...

## ▶ Fine-tuning problems

cosmological constant problem; gauge hierarchy problem; strong CP problem; SM fermion masses and mixings; ...

## ▶ Aesthetic problems

Interaction and fermion unification; gauge coupling unification; charge quantization; too many parameters; ...

## ▶ The electroweak vacuum stability problem

The stability problem can be easily solved in the new physics models.

## ▶ New Physics beyond the SM!

## ▶ Question: why do we still believe in supersymmetry?

# Motivations for Supersymmetry

- ▶ Supersymmetric Algebra is a generalization of the Poincare Algebra; The most general symmetry of the S-matrix; The local supersymmetry includes gravity naturally, *i.e.*, supergravity, etc.
- ▶ Supersymmetry provides a natural solution to the gauge hierarchy problem.
- ▶ Supersymmetry partially solves the cosmological constant problem:  $M_{\text{Pl}} \rightarrow M_{\text{SUSY}}$ .
- ▶ Supersymmetry is a bridge between the promising low energy phenomenology and the high-energy fundamental physics such as the Grand Unified Theory and String Theory.



# The Supersymmetric Standard Models (SSMs)

- ▶ Solving the gauge hierarchy problem
- ▶ Gauge coupling unification
- ▶ Radiatively electroweak symmetry breaking
- ▶ Natural dark matter candidates
- ▶ Electroweak baryogenesis
- ▶ Electroweak precision: R parity
- ▶  $\mu$  problem in the MSSM:  $\mu H_d H_u$ .

# The Grand Unified Theories: $SU(5)$ and $SO(10)$

- ▶ Unification of the gauge interactions, and unifications of the SM fermions
- ▶ Charge quantization
- ▶ Gauge coupling unification in the MSSM, and Yukawa unification
- ▶ Radiative electroweak symmetry breaking due to the large top quark Yukawa coupling
- ▶ Weak mixing angle at weak scale  $M_Z$
- ▶ Neutrino masses and mixings by seesaw mechanism
- ▶ Prediction: dim-6 proton decay via heavy gauge boson exchange.

# Problems

- ▶ Gauge symmetry breaking
- ▶ Doublet-triplet splitting problem
- ▶ Proton decay problem
- ▶ Fermion mass problem:  $m_e/m_\mu = m_d/m_s$

# String Models

- ▶ Calabi-Yau compactification of heterotic string theory
- ▶ Orbifold compactification of heterotic string theory
- ▶ D-brane models on Type II orientifolds
- ▶ Free fermionic string model building
- ▶  $\mathcal{F}$ -Theory Model Building

**Supersymmetry is a bridge between the promising low energy phenomenology and high-energy fundamental physics.**

# Particle Physics Paradigm

String Theory  $\rightarrow$  String Models  $\rightarrow$  GUTs  $\rightarrow$  SSMs  $\rightarrow$  SM

# The LHC Supersymmetry Search Constraints:

- ▶ The gluino mass low bound is around 2.3 TeV in the CMSSM/mSUGRA
- ▶ The first two-generation squark mass low bounds are around 1.85 TeV.
- ▶ The stop/sbottom mass low bounds are around 1.3 TeV.  
**The SSMs are fine-tuned!!!**

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ATLAS SUSY Searches\* - 95% CL Lower Limits

March 2023

ATLAS Preliminary  
 $\sqrt{s} = 13$  TeV

Model	Signature	$\int \mathcal{L} dt$ ( $\text{fb}^{-1}$ )	Mass limit	Reference			
Inclusive Searches	$\tilde{g}\tilde{g} \rightarrow \gamma\tilde{g}^0$	$0 < \mu$	2-6 jets $E_{T,miss}^{>150}$	139	$\tilde{m}(\tilde{g}) > 400$ GeV $m(\tilde{g}) - m(\tilde{g}^0) > 5$ GeV	2010.14293 2102.18784	
	$\tilde{g}\tilde{g} \rightarrow \gamma\tilde{g}^0$	mono-jet	1-3 jets $E_{T,miss}^{>150}$	139	0.9	$m(\tilde{g}) > 1000$ GeV	2010.14293
	$\tilde{g}\tilde{g} \rightarrow \gamma\tilde{g}^0$	$0 < \mu$	2-6 jets $E_{T,miss}^{>150}$	139	Forbidden	$m(\tilde{g}) > 1000$ GeV	2010.14293
	$\tilde{g}\tilde{g} \rightarrow \gamma\tilde{g}^0 W \tilde{g}^0$	$1 < \mu$	2-6 jets $E_{T,miss}^{>150}$	139	Forbidden	$m(\tilde{g}) > 800$ GeV	2101.01629
	$\tilde{g}\tilde{g} \rightarrow \gamma\tilde{g}^0 W \tilde{g}^0$	$\nu\tau, \mu\mu$	2 jets $E_{T,miss}^{>150}$	139	2.2	$m(\tilde{g}) > 700$ GeV	2204.13072
	$\tilde{g}\tilde{g} \rightarrow \gamma\tilde{g}^0 W Z \tilde{g}^0$	$0 < \mu$	7-11 jets $E_{T,miss}^{>150}$	139	1.97	$m(\tilde{g}) > 800$ GeV	2008.06032
	$\tilde{g}\tilde{g} \rightarrow \gamma\tilde{g}^0 W Z \tilde{g}^0$	SS $\nu, \mu$	6 jets $E_{T,miss}^{>150}$	139	1.15	$m(\tilde{g}) - m(\tilde{g}^0) > 200$ GeV	1909.08457
	$\tilde{g}\tilde{g} \rightarrow \gamma\tilde{g}^0$	$0-1 < \mu$	3 b jets $E_{T,miss}^{>150}$	139	2.45	$m(\tilde{g}) > 500$ GeV	2211.08028
	$\tilde{g}\tilde{g} \rightarrow \gamma\tilde{g}^0$	SS $\nu, \mu$	6 jets $E_{T,miss}^{>150}$	139	1.25	$m(\tilde{g}) - m(\tilde{g}^0) > 300$ GeV	1909.08457
	3 $\gamma$ gen. squarks direct production	$\tilde{t}_1\tilde{t}_1$	$0 < \mu$	2 b jets $E_{T,miss}^{>150}$	139	1.255	$m(\tilde{t}_1) > 400$ GeV 10 GeV $< \Delta m(\tilde{t}_1, \tilde{t}_1^0) < 20$ GeV
$\tilde{t}_1\tilde{t}_1, \tilde{t}_1 \rightarrow \tilde{t}_1^0 b \rightarrow \tilde{t}_1^0 \tilde{t}_1^0$		$0 < \mu$	6 b jets $E_{T,miss}^{>150}$	139	Forbidden	$\Delta m(\tilde{t}_1^0, \tilde{t}_1^0) > 130$ GeV, $m(\tilde{t}_1^0) > 100$ GeV	1908.03122
$\tilde{t}_1\tilde{t}_1, \tilde{t}_1 \rightarrow \tilde{t}_1^0 b \rightarrow \tilde{t}_1^0 \tilde{t}_1^0$		$2 < \mu$	2 b jets $E_{T,miss}^{>150}$	139	0.13-0.85	$\Delta m(\tilde{t}_1^0, \tilde{t}_1^0) > 130$ GeV, $m(\tilde{t}_1^0) > 100$ GeV	2103.08189
$\tilde{t}_1\tilde{t}_1, \tilde{t}_1 \rightarrow \tilde{t}_1^0 b \rightarrow \tilde{t}_1^0 \tilde{t}_1^0$		$0-1 < \mu$	$\geq 1$ jet $E_{T,miss}^{>150}$	139	1.25	$m(\tilde{t}_1) > 1$ GeV	2004.14560, 2012.02769
$\tilde{t}_1\tilde{t}_1, \tilde{t}_1 \rightarrow W b \tilde{t}_1^0$		$1 < \mu$	3 jets/1 b $E_{T,miss}^{>150}$	139	Forbidden	$m(\tilde{t}_1) > 500$ GeV	2012.03769
$\tilde{t}_1\tilde{t}_1, \tilde{t}_1 \rightarrow \tilde{t}_1^0 b \nu, \tilde{t}_1 \rightarrow \tilde{t}_1^0 \tilde{t}_1^0$		$1-2 < \mu$	2 jets/1 b $E_{T,miss}^{>150}$	139	Forbidden	$m(\tilde{t}_1) > 800$ GeV	2108.07685
$\tilde{t}_1\tilde{t}_1, \tilde{t}_1 \rightarrow \tilde{t}_1^0 b \nu, \tilde{t}_1 \rightarrow \tilde{t}_1^0 \tilde{t}_1^0$		$0 < \mu$	2 $\nu$ jets $E_{T,miss}^{>150}$	36.1	0.55	$m(\tilde{t}_1) > 0$ GeV	1805.01649
$\tilde{t}_1\tilde{t}_1, \tilde{t}_1 \rightarrow \tilde{t}_1^0 b \nu, \tilde{t}_1 \rightarrow \tilde{t}_1^0 \tilde{t}_1^0$		$0 < \mu$	mono-jet $E_{T,miss}^{>150}$	139	0.85	$m(\tilde{t}_1) > m(\tilde{t}_1^0) > 5$ GeV	2102.10874
$\tilde{t}_1\tilde{t}_1, \tilde{t}_1 \rightarrow \tilde{t}_1^0 b \nu, \tilde{t}_1 \rightarrow Z/\tilde{H}^0 \tilde{t}_1^0$		$1-2 < \mu$	1-4 b jets $E_{T,miss}^{>150}$	139	0.067-1.18	$m(\tilde{t}_1) > 500$ GeV	2005.05880
$\tilde{t}_1\tilde{t}_1, \tilde{t}_1 \rightarrow \tilde{t}_1^0 b \nu, \tilde{t}_1 \rightarrow Z/\tilde{H}^0 \tilde{t}_1^0$		$3 < \mu$	1 b jets $E_{T,miss}^{>150}$	139	Forbidden	$m(\tilde{t}_1) > 360$ GeV, $m(\tilde{t}_1) - m(\tilde{t}_1^0) > 40$ GeV	2005.05880
EW direct	$\tilde{t}_1^0 \tilde{t}_1^0$ via WZ	Multiple $\ell$ /jets $\nu\tau, \mu\mu$	$\geq 1$ jet $E_{T,miss}^{>150}$	139	0.96	$m(\tilde{t}_1^0) > 0$ , wino-bino $m(\tilde{t}_1^0) - m(\tilde{t}_1^0) > 5$ GeV, wino-bino	2106.01676, 2108.07586 1911.12606
	$\tilde{t}_1^0 \tilde{t}_1^0$ via WW	Multiple $\ell$ /jets $\nu\tau, \mu\mu$	$\geq 1$ jet $E_{T,miss}^{>150}$	139	0.205	$m(\tilde{t}_1^0) > 0$ , wino-bino	1908.08215
	$\tilde{t}_1^0 \tilde{t}_1^0$ via WW	Multiple $\ell$ /jets $\nu\tau, \mu\mu$	$\geq 1$ jet $E_{T,miss}^{>150}$	139	Forbidden	$m(\tilde{t}_1^0) > 70$ GeV, wino-bino	2004.10894, 2108.07586
	$\tilde{t}_1^0 \tilde{t}_1^0$ via $WZ/\gamma$	Multiple $\ell$ /jets $\nu\tau, \mu\mu$	$\geq 1$ jet $E_{T,miss}^{>150}$	139	1.0	$m(\tilde{t}_1^0) > 0$ , wino-bino $m(\tilde{t}_1^0) > 50$ GeV, $m(\tilde{t}_1^0) - m(\tilde{t}_1^0) > 5$ GeV	1908.08215
	$\tilde{t}_1^0 \tilde{t}_1^0$ via $WZ/\gamma$	Multiple $\ell$ /jets $\nu\tau, \mu\mu$	$\geq 1$ jet $E_{T,miss}^{>150}$	139	0.16-0.3	$m(\tilde{t}_1^0) > 0$	1911.06650
	$\tilde{t}_1^0 \tilde{t}_1^0$ via $WZ/\gamma$	Multiple $\ell$ /jets $\nu\tau, \mu\mu$	$\geq 1$ jet $E_{T,miss}^{>150}$	139	0.7	$m(\tilde{t}_1^0) > 0$	1908.08215
	$\tilde{t}_1^0 \tilde{t}_1^0$ via $WZ/\gamma$	Multiple $\ell$ /jets $\nu\tau, \mu\mu$	$\geq 1$ jet $E_{T,miss}^{>150}$	139	0.255	$m(\tilde{t}_1^0) > 0$	1908.08215
	$\tilde{t}_1^0 \tilde{t}_1^0$ via $WZ/\gamma$	Multiple $\ell$ /jets $\nu\tau, \mu\mu$	$\geq 1$ jet $E_{T,miss}^{>150}$	139	0.13-0.23	$m(\tilde{t}_1^0) - m(\tilde{t}_1^0) > 10$ GeV	1908.08215
	$\tilde{t}_1^0 \tilde{t}_1^0$ via $WZ/\gamma$	Multiple $\ell$ /jets $\nu\tau, \mu\mu$	$\geq 1$ jet $E_{T,miss}^{>150}$	139	0.55	$BR(\tilde{t}_1^0 \rightarrow \tilde{t}_1^0 b) > 0$	1806.04200
	$\tilde{t}_1^0 \tilde{t}_1^0$ via $WZ/\gamma$	Multiple $\ell$ /jets $\nu\tau, \mu\mu$	$\geq 2$ large jets $E_{T,miss}^{>150}$	139	0.45-0.93	$BR(\tilde{t}_1^0 \rightarrow Z\tilde{t}_1^0) > 1$	2103.11684
$\tilde{t}_1^0 \tilde{t}_1^0$ via $WZ/\gamma$	Multiple $\ell$ /jets $\nu\tau, \mu\mu$	$\geq 2$ jets $E_{T,miss}^{>150}$	139	0.77	$BR(\tilde{t}_1^0 \rightarrow Z\tilde{t}_1^0) > 0.5$	2108.07586 2004.13072	
Long-lived particles	Direct $\tilde{t}_1^0 \tilde{t}_1^0$ prod., long-lived $\tilde{t}_1^0$	Disapp. 5%	1 jet $E_{T,miss}^{>150}$	139	0.66	Pure Wino Pure Higgsino	2001.02472 2201.02472
	Stable $\beta$ R-hadron	pixel dE/dx	$E_{T,miss}^{>150}$	139	0.21		
	Metastable $\beta$ R-hadron, $\beta \rightarrow \gamma\tilde{g}^0$ $Z\tilde{t}_1^0, \tilde{t}_1^0 \rightarrow \tilde{t}_1^0$	pixel dE/dx	$E_{T,miss}^{>150}$	139	2.05	$m(\tilde{t}_1^0) > 100$ GeV	2005.06013
RPV	$\tilde{t}_1^0 \tilde{t}_1^0$ via $WZ/\gamma$	Multiple $\ell$ /jets $\nu\tau, \mu\mu$	$\geq 1$ jet $E_{T,miss}^{>150}$	139	0.7	$m(\tilde{t}_1^0) > 0$ GeV	2011.07812
	$\tilde{t}_1^0 \tilde{t}_1^0$ via $WZ/\gamma$	Multiple $\ell$ /jets $\nu\tau, \mu\mu$	$\geq 1$ jet $E_{T,miss}^{>150}$	139	0.34	$m(\tilde{t}_1^0) > 0$ GeV	2011.07812
	$\tilde{t}_1^0 \tilde{t}_1^0$ via $WZ/\gamma$	Multiple $\ell$ /jets $\nu\tau, \mu\mu$	$\geq 1$ jet $E_{T,miss}^{>150}$	139	0.36	$m(\tilde{t}_1^0) > 10$ GeV	2305.05013
	$\tilde{t}_1^0 \tilde{t}_1^0$ via $WZ/\gamma$	Multiple $\ell$ /jets $\nu\tau, \mu\mu$	$\geq 1$ jet $E_{T,miss}^{>150}$	139	0.625	$m(\tilde{t}_1^0) > 200$ GeV	2011.05443
	$\tilde{t}_1^0 \tilde{t}_1^0$ via $WZ/\gamma$	Multiple $\ell$ /jets $\nu\tau, \mu\mu$	$\geq 1$ jet $E_{T,miss}^{>150}$	139	0.95	$m(\tilde{t}_1^0) > 200$ GeV	2103.11684
	$\tilde{t}_1^0 \tilde{t}_1^0$ via $WZ/\gamma$	Multiple $\ell$ /jets $\nu\tau, \mu\mu$	$\geq 1$ jet $E_{T,miss}^{>150}$	139	1.3	Large $A_{13}$	1804.02569
	$\tilde{t}_1^0 \tilde{t}_1^0$ via $WZ/\gamma$	Multiple $\ell$ /jets $\nu\tau, \mu\mu$	$\geq 1$ jet $E_{T,miss}^{>150}$	139	0.55	$m(\tilde{t}_1^0) > 200$ GeV, wino-bino	ATLAS-COUP-2018-003
	$\tilde{t}_1^0 \tilde{t}_1^0$ via $WZ/\gamma$	Multiple $\ell$ /jets $\nu\tau, \mu\mu$	$\geq 4$ jets $E_{T,miss}^{>150}$	139	0.95	$m(\tilde{t}_1^0) > 200$ GeV	2010.01015
	$\tilde{t}_1^0 \tilde{t}_1^0$ via $WZ/\gamma$	Multiple $\ell$ /jets $\nu\tau, \mu\mu$	2 jets + 2 b jets $E_{T,miss}^{>150}$	36.7	0.42	$m(\tilde{t}_1^0) > 200$ GeV	1710.07171
	$\tilde{t}_1^0 \tilde{t}_1^0$ via $WZ/\gamma$	Multiple $\ell$ /jets $\nu\tau, \mu\mu$	2 jets + 2 b jets $E_{T,miss}^{>150}$	36.1	0.4-1.45	$BR(\tilde{t}_1^0 \rightarrow \tilde{t}_1^0 b) > 20\%$	1710.02544
$\tilde{t}_1^0 \tilde{t}_1^0$ via $WZ/\gamma$	Multiple $\ell$ /jets $\nu\tau, \mu\mu$	2 jets + 2 b jets $E_{T,miss}^{>150}$	139	1.0	$BR(\tilde{t}_1^0 \rightarrow \tilde{t}_1^0 b) > 100\%$ , $\cos\theta > 1$	2003.11956	
$\tilde{t}_1^0 \tilde{t}_1^0$ via $WZ/\gamma$	Multiple $\ell$ /jets $\nu\tau, \mu\mu$	$\geq 6$ jets $E_{T,miss}^{>150}$	139	0.2-0.32	Pure Higgsino	2106.06030	

\*Only a selection of the available mass limits on new states or parameters is shown. Many of these limits are based on



# Interesting Questions in Supersymmetry Phenomenology

- ▶ Can we solve the supersymmetry electroweak fine-tuning problem naturally?
- ▶ Do we still have the bulk region for dark matter?
- ▶ Can we probe this entire bulk region at the future experiments?



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# High Energy Fine-Tuning Definition

- ▶ Fine-tuning Definition <sup>1</sup>: the quantitative measure  $\Delta_{\text{FT}}^{\text{EENZ-BG}}$  for fine-tuning is the maximum of the logarithmic derivative of  $M_Z$  with respect to all the fundamental parameters  $a_i$  at the GUT scale

$$\Delta_{\text{FT}}^{\text{EENZ-BG}} = \text{Max}\{\Delta_i^{\text{GUT}}\}, \quad \Delta_i^{\text{GUT}} = \left| \frac{\partial \ln(M_Z)}{\partial \ln(a_i^{\text{GUT}})} \right|.$$

<sup>1</sup>J. R. Ellis, K. Enqvist, D. V. Nanopoulos and F. Zwirner, Mod. Phys. Lett. A **1**, 57 (1986); R. Barbieri and G. F. Giudice, Nucl. Phys. B **306**, 63 (1988).

## Question: Super-Natural Supersymmetry

Can we propose a supersymmetry scenario whose the EENZ-BG fine-tuning measure is automatically 1 or order 1 ( $\mathcal{O}(1)$ )?

Fundamental physics principles: simplicity and naturalness.

# Super-Natural Supersymmetry <sup>2</sup>

## ► Fine-Tuning Definition:

$$\Delta_{\text{FT}} = \text{Max}\{\Delta_i^{\text{GUT}}\}, \quad \Delta_i^{\text{GUT}} = \left| \frac{\partial \ln(M_Z)}{\partial \ln(a_i^{\text{GUT}})} \right|.$$

## ► Natural Solution:

$$M_Z^n = f_n \left( \frac{M_Z}{M_*} \right) M_*^n.$$

$$\frac{\partial \ln(M_Z^n)}{\partial \ln(M_*^n)} \simeq \frac{M_*^n}{M_Z^n} \frac{\partial M_Z^n}{\partial M_*^n} \simeq \frac{1}{f_n} \simeq \mathcal{O}(1).$$

## ► For no-scale supergravity and M-theory on $S^1/Z_2$ , we have $M_* = M_{1/2}$ and $M_* = M_{3/2}$ , respectively.

<sup>2</sup>T. Leggett, T. Li, J. A. Maxin, D. V. Nanopoulos and J. W. Walker, arXiv:1403.3099 [hep-ph]; Phys. Lett. B 740, 66 (2015) [arXiv:1408.4459 [hep-ph]]; G. Du, T. Li, D. V. Nanopoulos and S. Raza, Phys. Rev. D 92, no. 2

# The Super-Natural Supersymmetry and Its Generalizations

- ▶ The Kähler potential and superpotential can be calculated in principle or at least inspired from a fundamental theory such as string theory with suitable compactifications. In other words, one cannot add arbitrary high-dimensional terms in the Kähler potential and superpotential.
- ▶ There is one and only one chiral superfield or modulus whose F-term breaks supersymmetry. And all the supersymmetry breaking soft terms are obtained from the above Kähler potential and superpotential.
- ▶ All the other mass parameters, if there exist such as the  $\mu$  term in the MSSM, must arise from supersymmetry breaking.

# Effectively Super-Natural Supersymmetry <sup>3</sup>

**A supersymmetry breaking scenario is natural if all the fundamental parameters that have large EENZ-BG fine-tuning measures are correlated.**

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<sup>3</sup>R. Ding, T. Li, F. Staub and B. Zhu, Phys. Rev. D **93**, no.9, 095028 (2016) [arXiv:1510.01328 [hep-ph]].

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# SUSY Dark Matter Scenarios

## ▶ Bulk region

The sfermions (supersymmetric partners of the SM fermions) are light.

## ▶ The Z/Higgs funnels or Z/Higgs resonances

The LSP neutralino mass is about half of the masses of the Z boson, SM Higgs, CP-even Higgs  $H_0$ , or CP-odd Higgs  $A_0$ .

## ▶ Coannihilations

The sfermion masses are close to the LSP neutralino.

## ▶ Mixing scenario or well-tempered scenario

The LSP neutralino has enough Wino or Higgsino component to significantly increase the annihilation cross section.



# SUSY Dark Matter Scenarios

- ▶ The bulk region may be the most natural.
- ▶ Because the LHC SUSY searches have given strong constraints on the SUSY parameter space, the possible bulk region is the light right-handed sleptons and LSP neutralino annihilations.
- ▶ This is an interesting scenario for the SUSY searches at the FCC<sub>ee</sub> and CEPC.
- ▶ Question: Is it possible to have such kind of viable bulk region for dark matter in a natural SUSY scenario?

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## $\mathcal{F}$ -SU(5) Models

- ▶ The gauge group  $SU(5) \times U(1)_X$  can be embedded into  $SO(10)$  model.
- ▶ Generator  $U(1)_{Y'}$  in  $SU(5)$

$$T_{U(1)_{Y'}} = \text{diag} \left( -\frac{1}{3}, -\frac{1}{3}, -\frac{1}{3}, \frac{1}{2}, \frac{1}{2} \right) .$$

- ▶ Hypercharge

$$Q_Y = \frac{1}{5} (Q_X - Q_{Y'}) .$$

► SM fermions

$$F_i = (\mathbf{10}, \mathbf{1}), \quad \bar{f}_i = (\bar{\mathbf{5}}, -\mathbf{3}), \quad \bar{l}_i = (\mathbf{1}, \mathbf{5}),$$

$$F_i = (Q_i, D_i^c, N_i^c), \quad \bar{f}_i = (U_i^c, L_i), \quad \bar{l}_i = E_i^c.$$

► Higgs particles:

$$H = (\mathbf{10}, \mathbf{1}), \quad \bar{H} = (\bar{\mathbf{10}}, -\mathbf{1}), \quad h = (\mathbf{5}, -\mathbf{2}), \quad \bar{h} = (\bar{\mathbf{5}}, \mathbf{2}),$$

$$H = (Q_H, D_H^c, N_H^c), \quad \bar{H} = (\bar{Q}_{\bar{H}}, \bar{D}_{\bar{H}}^c, \bar{N}_{\bar{H}}^c),$$

$$h = (D_h, D_h, D_h, H_d), \quad \bar{h} = (\bar{D}_{\bar{h}}, \bar{D}_{\bar{h}}, \bar{D}_{\bar{h}}, H_u).$$

► Flip

$$U \leftrightarrow D, \quad N \leftrightarrow E, \quad H_d \leftrightarrow H_u.$$

## Symmetry breaking:

### ► Superpotential

$$W_{\text{GUT}} = \lambda_1 H H h + \lambda_2 \overline{H H h} + \Phi(\overline{H H} - M_{\text{H}}^2) .$$

- There is only one F-flat and D-flat direction along the  $N_H^c$  and  $\overline{N_H^c}$  directions:  $\langle N_H^c \rangle = \langle \overline{N_H^c} \rangle = M_{\text{H}}$ .
- The doublet-triplet splitting due to the missing partner mechanism
- No dimension-5 proton decay problem.

## Flipped $SU(5) \times U(1)_X$ Models: <sup>6</sup>

- ▶ Doublet-triplet splitting via missing partner mechanism <sup>4</sup>.
- ▶ No dimension-five proton decay problem.
- ▶ Little hierarchy problem in string models:  
 $M_{\text{String}} \sim 20 \times M_{\text{GUT}}$

$$M_{\text{String}} = g_{\text{String}} \times 5.27 \times 10^{17} \text{ GeV} .$$

- ▶ Testable flipped  $SU(5) \times U(1)_X$  models: TeV-scale vector-like particles <sup>5</sup>.

<sup>4</sup>I. Antoniadis, J. R. Ellis, J. S. Hagelin and D. V. Nanopoulos, Phys. Lett. B **194**, 231 (1987).

<sup>5</sup>J. Jiang, T. Li and D. V. Nanopoulos, Nucl. Phys. B **772**, 49 (2007).

<sup>6</sup>S. M. Barr, Phys. Lett. B **112**, 219 (1982); J. P. Derendinger, J. E. Kim and D. V. Nanopoulos, Phys. Lett. B **139**, 170 (1984).

# Flipped $SU(5) \times U(1)_X$ Models:

- ▶ Four-dimensional free-fermionic string construction <sup>7</sup>.
- ▶ F-theory model building <sup>8</sup>.
- ▶ Heterotic string constructions: Calabi-Yau <sup>9</sup>; Orbifold <sup>10</sup>.
- ▶ Orbifold GUTs <sup>11</sup>.

<sup>7</sup> J. L. Lopez, D. V. Nanopoulos and K. j. Yuan, Nucl. Phys. B **399**, 654 (1993).

<sup>8</sup> C. Beasley, J. J. Heckman and C. Vafa, JHEP **0901**, 059 (2009); J. Jiang, T. Li, D. V. Nanopoulos and D. Xie, Phys. Lett. B **677**, 322 (2009); Nucl. Phys. B **830**, 195 (2010).

<sup>9</sup> A. E. Faraggi, R. S. Garavuso and J. M. Isidro, Nucl. Phys. B **641**, 111 (2002)

<sup>10</sup> J. E. Kim and B. Kyae, Nucl. Phys. B **770**, 47 (2007).

<sup>11</sup> S. M. Barr and I. Dorsner, Phys. Rev. D **66**, 065013 (2002).

## $\mathcal{F}$ -SU(5) Models

- ▶ To achieve the string scale gauge coupling unification, we introduce sets of vector-like particles in complete  $SU(5) \times U(1)_X$  multiplets, whose contributions to the one-loop beta functions of the  $U(1)_Y$ ,  $SU(2)_L$  and  $SU(3)_C$  gauge symmetries,  $\Delta b_1$ ,  $\Delta b_2$  and  $\Delta b_3$  respectively, satisfy  $\Delta b_1 < \Delta b_2 = \Delta b_3$ .
- ▶ To avoid the Landau pole problem for the gauge couplings, we can only introduce the following two sets of vector-like particles around the TeV scale, which could be observed at the LHC

$$Z1 : XF = (\mathbf{10}, \mathbf{1}) \equiv (XQ, XD^c, XN^c), \quad \overline{XF} = (\overline{\mathbf{10}}, -\mathbf{1});$$

$$Z2 : XF, \overline{XF}, XI = (\mathbf{1}, -\mathbf{5}), \overline{XI} = (\mathbf{1}, \mathbf{5}) \equiv XE^c.$$



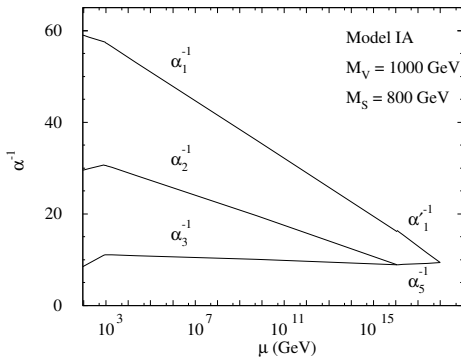


Figure: Gauge coupling unification in the Type IA model.

## No-Scale Supergravity <sup>12</sup>:

- ▶ The vacuum energy vanishes automatically due to the suitable Kähler potential.
- ▶ At the minimum of the scalar potential, there are flat directions which leave the gravitino mass  $M_{3/2}$  undertermined.
- ▶ The super-trace quantity  $\text{Str}\mathcal{M}^2$  is zero at the minimum.

$$K = -3\ln(T + \bar{T} - \sum_i \bar{\Phi}_i \Phi_i) .$$

<sup>12</sup>E. Cremmer, S. Ferrara, C. Kounnas and D. V. Nanopoulos, Phys. Lett. B **133**, 61 (1983); A. B. Lahanas and D. V. Nanopoulos, Phys. Rept. **145**, 1 (1987).

# No-Scale Supergravity

**No-scale supergravity can be realized in the compactification of the weakly coupled heterotic string theory <sup>13</sup> and the compactification of M-theory on  $S^1/Z_2$  at the leading order <sup>14</sup>.**

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<sup>13</sup>E. Witten, Phys. Lett. B **155**, 151 (1985).

<sup>14</sup>T. Li, J. L. Lopez and D. V. Nanopoulos, Phys. Rev. D **56**, 2602 (1997).

## No-Scale Supergravity:

- ▶ mSUGRA/CMSSM:  $M_{1/2}, M_0, A, \tan \beta, \text{sign}(\mu)$ .
- ▶ No-scale boundary condition:  $M_{1/2} \neq 0, M_0 = A = B_\mu = 0$
- ▶ Natural solution to CP violation and FCNC problem.
- ▶ Disfavored by phenomenology

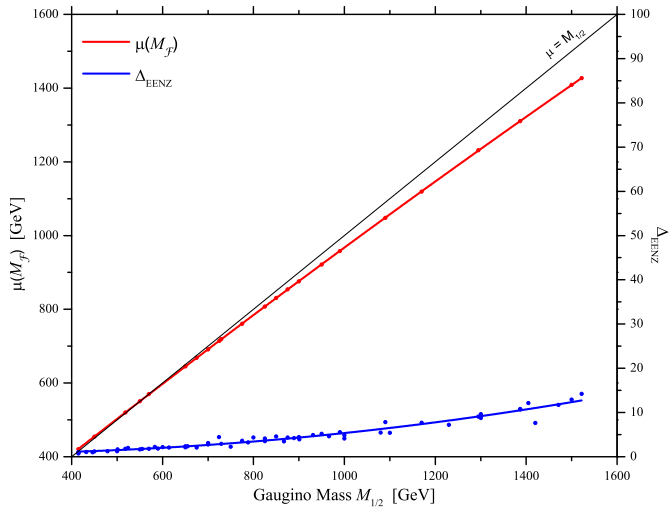
The light stau is the LSP if we run the RGEs from the traditional GUT scale.

- ▶ No-scale  $\mathcal{F}$ - $SU(5)$

**The Bino dominant neutralino is the LSP if we run the RGEs from the string scale.**

# Miracle of Vector-Like Particles

- ▶ String-scale gauge coupling unification.
- ▶ Lifting the lightest CP-even Higgs boson mass.
- ▶ The proton decay  $p \rightarrow e^+ \pi^0$  from the heavy gauge boson exchange is within the reach of the future Hyper-Kamiokande experiments for a majority of the most plausible parameter space.
- ▶ Explaining the muon anomalous magnetic moment easily due to the chirality flip if it is needed.
- ▶ Special sparticle spectra.



# The No-Scale Supergravity and Its Generalization

- ▶ No-Scale Supergravity is only valid at tree level.
- ▶ There exist corrections to the gauge kinetic functions and Kähler potential at one loop.
- ▶ The Generalized No-Scale Supergravity:  $M_{1/2} \neq 0$ ,  
 $M_0 \sim \mathcal{O}(10^{-2})M_{1/2}$ ,  $A \sim \mathcal{O}(10^{-2})M_{1/2}$ ,  $B_\mu \sim \mathcal{O}(10^{-2})M_{1/2}$ .

# The Generalized No-Scale Supergravity for $\mathcal{F}$ - $SU(5)$

- ▶ At the  $SU(5) \times U(1)_X$  unification scale (string scale), we vary the  $SU(5)$  gaugino mass  $M_5$  from 1200 GeV to 5000 GeV, yielding a large gluino mass.
- ▶ To produce a light Bino, we vary the  $U(1)_X$  gaugino mass  $M_{1X}$  from 100 GeV to 600 GeV.
- ▶ Note that No-Scale SUGRA is obtained at tree level and can be violated at one loop, so we assume the universal supersymmetry breaking soft mass  $M_0$  and trilinear soft term  $A$  are smaller than about 1% of  $M_5$ . For simplicity, we take  $A = 0$ .
- ▶ We span  $\tan\beta$  from 2 to 65, and the vector-like particle mass scale  $M_V$  from 1 TeV to 10 TeV.



## The Bino Mass

$$\frac{M_1}{\alpha_1} \equiv \frac{24}{25} \frac{M_{1X}}{\alpha_{1X}} + \frac{1}{25} \frac{M_5}{\alpha_5},$$

where  $\alpha_i$  are the gauge couplings at their respective scales.

# Effective Super-Natural SUSY

- ▶ A supersymmetry breaking scenario is natural if all the fundamental parameters that have large EENZ-BG fine-tuning measures are correlated.
- ▶ In our generalized No-Scale SUGRA, the fine-tuning measures for the SUSY breaking soft terms  $M_{1X}$ ,  $M_0$ , and  $A_0$  are all small, and only  $M_5$  might have a large fine-tuning measure.
- ▶ Our generalized No-Scale SUGRA is approximately **Super-Natural SUSY**, and thus indeed natural.

More specifically, it is only a small deviation from Super-Natural SUSY, and hence the simplest scenario for Effective Super-Natural SUSY.

## Experimental Constraints

- ▶ Require neutralino LSP
- ▶ Constraints on the masses of the gluino and first/second generation squarks:  $m_{\tilde{g}} \gtrsim 2.2 \text{ TeV}$ ,  $m_{\tilde{q}} \gtrsim 2.0 \text{ TeV}$ .
- ▶ Rare B-meson decay constraint  $1.6 \times 10^{-9} \leq \text{BR}(B_s^0 \rightarrow \mu^+ \mu^-) \leq 4.2 \times 10^{-9}$  and branching ratio of rare b-quark decay of  $2.99 \times 10^{-4} \leq \text{BR}(b \rightarrow s\gamma) \leq 3.87 \times 10^{-4}$ .
- ▶ The Higgs boson mass range  $122 \text{ GeV} \leq m_h \leq 128 \text{ GeV}$ .
- ▶ Constraints on spin-independent DM-nuclei cross sections from the XENONnT and LUX-ZEPLIN experiments.
- ▶ Relic density of cold DM measured by the  $5\sigma$  Planck 2018 of  $0.114 \leq \Omega_{\text{DM}} h^2 \leq 0.126$  where below this range is regarded as under-saturated and above is over-saturated.

## Suppression of Coannihilation

With the absent of coannihilation, we have

$$\Omega_{\tilde{B}} h^2 = 1.3 \times 10^{-2} \left( \frac{m_{\tilde{e}_R}}{100\text{GeV}} \right)^2 \frac{(1+r)^4}{r(1+r^2)} \left( 1 + 0.07 \log \frac{\sqrt{r} 100\text{GeV}}{m_{\tilde{e}_R}} \right),$$

where  $r \equiv M_1^2 / m_{\tilde{e}_R}^2$ .

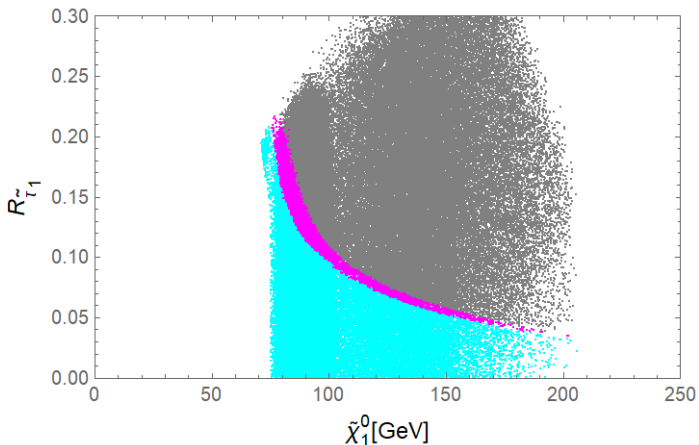
- ▶ MicrOMEGAs 2.1, with and without coannihilation
- ▶  $\mathcal{R}_\phi \equiv (m_\phi - m_{\tilde{\chi}_1^0}) / m_{\tilde{\chi}_1^0}$  with  $\phi = \tilde{e}_R$  or  $\tilde{\tau}_1$ .
- ▶  $\mathcal{R}_\phi = 5 - 8\%$ , deviates from the coannihilation  $\geq 50\%$ .
- ▶  $\mathcal{R}_\phi = 10 - 12\%$ , co-annihilation 20 - 30%, annihilation 70 - 80%.

## Bulk Region Condition

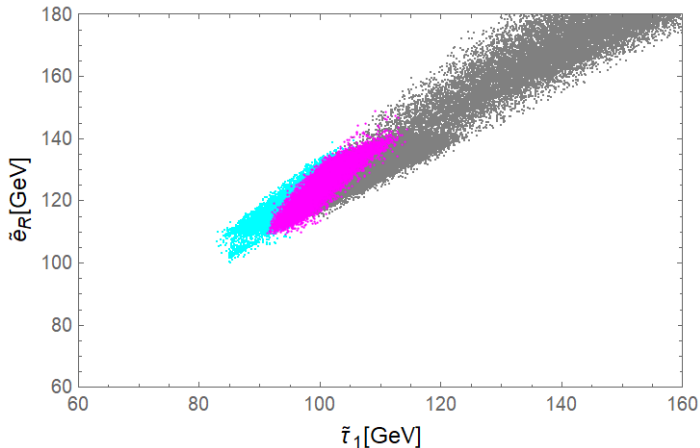
- ▶ 99.9% Bino-like LSPs are selected to prohibit large annihilation cross sections induced by Higgsino or Wino components.
- ▶  $2m_{\tilde{\chi}_1^0} \ll m_{H^0}, m_{A^0}$  and  $2m_{\tilde{\chi}_1^0} \gg m_h$  are enforced to avoid the "Higgs funnel".
- ▶  $\tilde{\tau}_1$  and  $\tilde{e}_R$  are naturally light, so coannihilation processes are negligible when  $\mathcal{R}_{\tilde{\tau}_1} \equiv \frac{m_{\tilde{\tau}_1} - m_{\tilde{\chi}_1^0}}{m_{\tilde{\chi}_1^0}} \gtrsim 10\%$  and
 
$$\mathcal{R}_{\tilde{e}_R} \equiv \frac{m_{\tilde{e}_R} - m_{\tilde{\chi}_1^0}}{m_{\tilde{\chi}_1^0}} \gtrsim 10\%.$$
- ▶ Require the SM Higgs resonance to vanish, which transpires when  $|\mu|^2 \gg M_Z^2$ , via the coupling  $g_{h\tilde{\chi}_1^0\tilde{\chi}_1^0} \propto \frac{M_Z(2\mu\cos\beta + M_1)}{\mu^2 - M_1^2}$ .

# The Criteria for Right-Handed Slepton Bulk Region

- ▶ The ratio of the mass difference  $\mathcal{R}_\phi \equiv (m_\phi - m_{\tilde{\chi}_1^0})/m_{\tilde{\chi}_1^0}$  is more important than the absolute mass difference, where  $\phi$  is  $\tilde{\tau}_1$  (light stau) or  $\tilde{e}_R$  (light selectron).
- ▶ Comprehensive numerical studies that we present in this work show that  $\mathcal{R}_\phi \gtrsim 10\%$  is a conservative criterion to formulate the bulk region, *i.e.*, the observed dark matter density is obtained via traditional annihilations, not from coannihilations or resonances, etc.

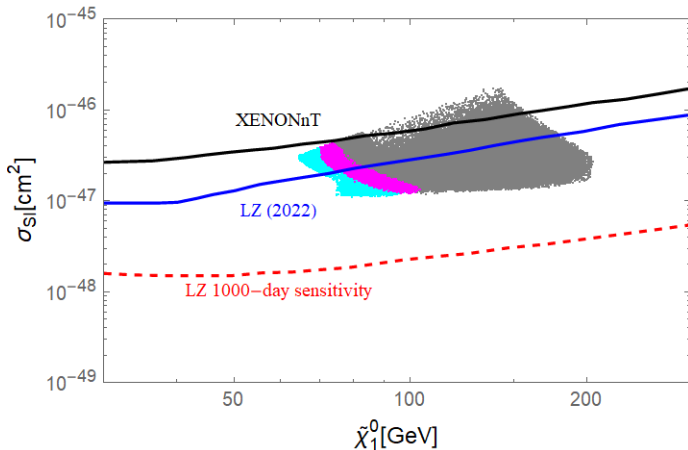


**Figure:** Bulk region in Generalized No-Scale  $\mathcal{F}$ -SU(5). Cyan, magenta, gray points correspond to under-saturated, saturated, over-saturated DM relic density.



**Figure:** Light right-handed slepton masses in the Generalized No-Scale  $\mathcal{F}$ - $SU(5)$  bulk region. Cyan, magenta, gray points correspond to under-saturated, saturated, over-saturated DM relic density with  $\mathcal{R}_{\tilde{\tau}_1} \gtrsim 10\%$ .





**Figure:** Generalized No-Scale  $\mathcal{F}$ -SU(5) bulk region LSPs plot in reference to spin-independent DM-nuclei cross sections from XENONnT and LUX-ZEPLIN. Cyan, magenta, gray points correspond to under-saturated, saturated, over-saturated DM relic density with  $\mathcal{R}_{\tilde{\tau}_1} \gtrsim 10\%$ . We underscore the significance of the 1000-day LUX-ZEPLIN run that should fully probe the  $\mathcal{F}$ -SU(5) bulk and about 50% of the pMSSM bulk (not shown).

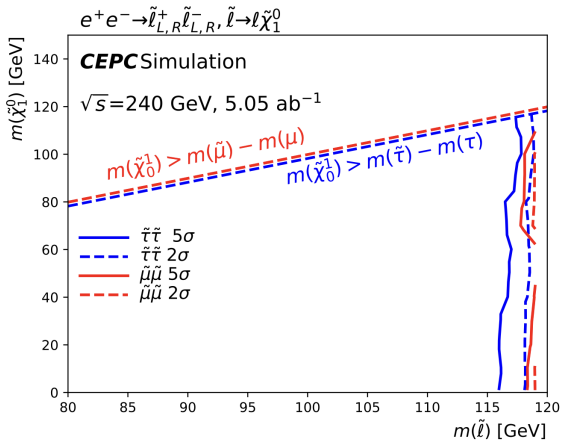


Figure: CEPC sensitivity.

# The Light Right-Handed Stau Bulk Region in $\mathcal{F}$ - $SU(5)$

- ▶ The LSP neutralino is Bino dominant.
- ▶ The mass hierarchy in  $\mathcal{F}$ - $SU(5)$  is  $m_{\tilde{\chi}_1^0} < m_{\tilde{\tau}_1} < m_{\tilde{e}_R} = m_{\tilde{\mu}_R}$ .
- ▶ If the Bino contributes all the DM abundance, the ratio  $\mathcal{R}_{\tilde{\tau}_1} \gtrsim 10\%$  implies  $m_{\tilde{\chi}_1^0} \leq 103.0$  GeV.
- ▶ The upper bounds on  $\tilde{\tau}_1$  and  $\tilde{e}_R$  are around 115 GeV and 150 GeV, respectively.

## The Light Right-Handed Stau Bulk Region in $\mathcal{F}-SU(5)$

- ▶ The entire viable parameter space can be probed by the the 1000-day LUX-ZEPLIN experiment within the next a few years.
- ▶ The proton lifetime via dimension-six proton decay is around  $3 - 4 \times 10^{34}$  years, so it is within reach of the future Hyper-Kamiokande experiment.
- ▶ The entire viable parameter space can be probed by the Future Circular Collider (FCC-ee) at CERN, Circular Electron Positron Collider (CEPC)
- ▶ The pure supersymmetry contribution to the muon anomalous magnetic moment  $\Delta a_\mu$  is small, around  $5 \times 10^{-11}$ , which is consistent with the BMW results.  $\Delta a_\mu$  can be explained via vectot-like particles if it is needed.

$M_5$	3996	2591
$M_{1X}$	473	268
$M_0$	23.15	21.49
$A_0$	0	0
$\tan\beta$	3.04	2.53
$M_V$	9063	4603
$m_h$	125.43	123.06
$m_A$	7325	5395
$m_{\tilde{\chi}_1^0}$	161.3	92.3
$m_{\tilde{\tau}_1}$	169.6	103.4
$m_{\tilde{e}_R}$	216.1	130.1
$m_{\tilde{t}_1}$	4273	2747
$m_{\tilde{g}}$	4986	3259
$m_{\tilde{u}_R}$	6798	4606
$\text{BR}(B_S^0 \rightarrow \mu^+ \mu^-) \times 10^{-9}$	3.03	3.05
$\text{BR}(b \rightarrow s\gamma) \times 10^{-4}$	3.61	3.61
$\sigma_{\text{SI}} \times 10^{-12} \text{pb}$	6.28	17.10
$\tau_p \times 10^{34} \text{yrs}$	5.01	3.95
$\mathcal{R}_{\tilde{\tau}_1}$	5%	12%
$\Omega_{\tilde{\chi}} h^2$	0.1256	0.118
$\Omega_{\tilde{\chi}} h^2 (\text{No co-annihilation})$	0.386	0.147
co-annihilation rate	> 50%	~ 20%

Figure: Two benchmark points for Generalized No-Scale  $\mathcal{F}$ -SU(5). All masses are in GeV.

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# The pMSSM

The methodology just discussed is extended to include the much less constrained generic pMSSM. The pMSSM contains 22 free parameters, and we input  $M_A$  and  $\mu$  in lieu of  $m_{H_u}^2$  and  $m_{H_d}^2$ . The scanning ranges of the pMSSM parameters are as follows:

$$20 \text{ GeV} \leq M_1 \leq 1000 \text{ GeV}$$

$$2 \leq \tan\beta \leq 65$$

$$1000 \text{ GeV} \leq M_2 \leq 5000 \text{ GeV}$$

$$1000 \text{ GeV} \leq M_A, \mu \leq 6000 \text{ GeV}$$

$$1200 \text{ GeV} \leq M_3 \leq 5000 \text{ GeV}$$

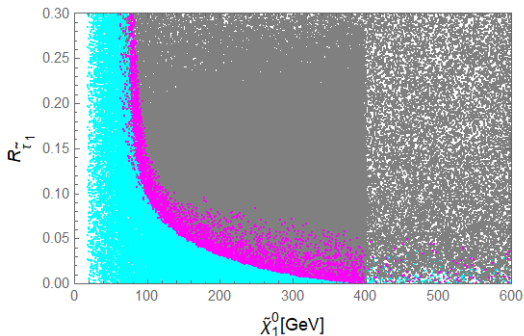
$$M_1 \leq m_{\tilde{e}_R}, m_{\tilde{\tau}_R} \leq 2M_1$$

$$2500 \text{ GeV} \leq m_{\tilde{q}}, m_{\tilde{Q}}, m_{\tilde{u}_R}, m_{\tilde{t}_R}, m_{\tilde{d}_R}, m_{\tilde{b}_R} \leq 5000 \text{ GeV}$$

$$700 \text{ GeV} \leq m_{\tilde{l}} \leq 2000 \text{ GeV}$$

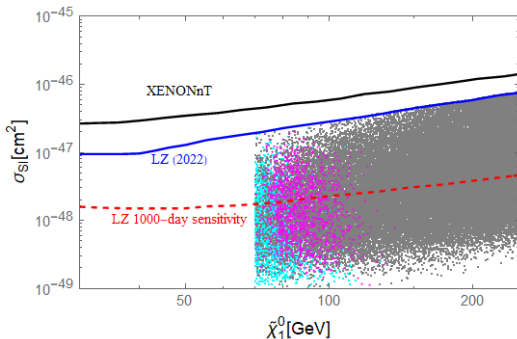
$$1200 \text{ GeV} \leq m_{\tilde{L}} \leq 5000 \text{ GeV}$$

$$-5000 \text{ GeV} \leq A_u, A_d, A_e, A_t, A_b, A_\tau \leq 5000 \text{ GeV}$$

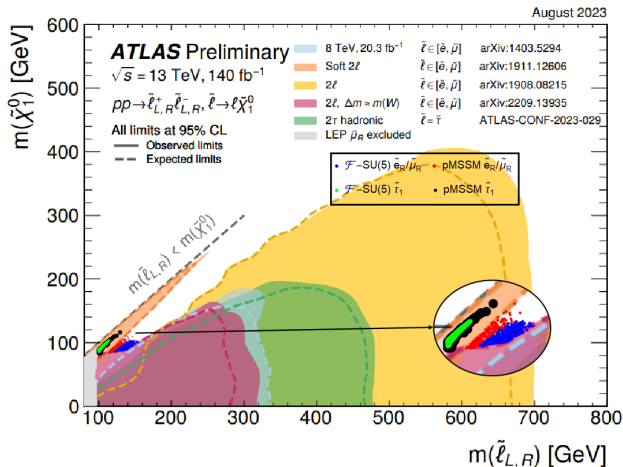


**Figure:** Bulk region in pMSSM. Cyan, magenta, gray points correspond to under-saturated, saturated, over-saturated DM relic density.

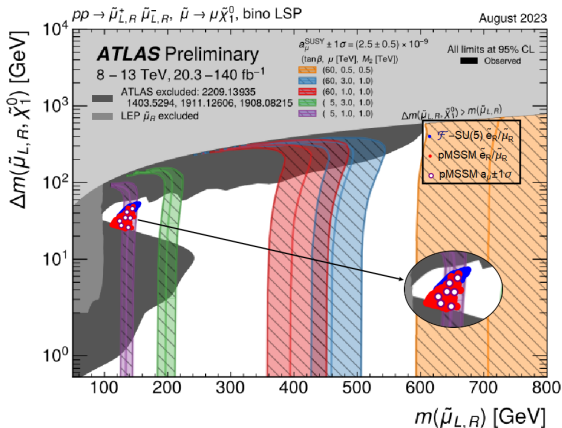




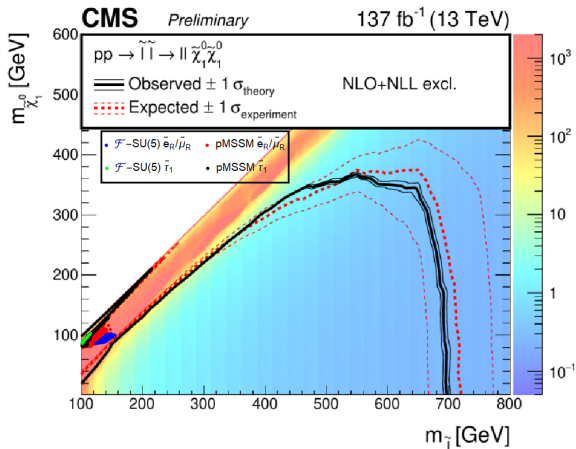
**Figure:** The pMSSM bulk region LSPs plot in reference to spin-independent DM-nuclei cross sections from XENONnT and LUX-ZEPLIN. Cyan, magenta, gray points correspond to under-saturated, saturated, over-saturated DM relic density with  $\mathcal{R}_{\tilde{\tau}_1} \gtrsim 10\%$ . The LUX-ZEPLIN 1000-day should fully probe about 50% of the pMSSM bulk.



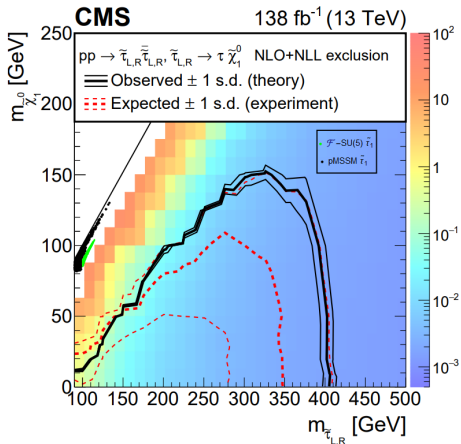
**Figure:** Generalized No-Scale  $\mathcal{F}$ -SU(5) and pMSSM bulk regions superimposed over the August 2023 ATLAS Summary Plot [?] of SUSY searches for electroweak production of sleptons.



**Figure:** Generalized No-Scale  $\mathcal{F}$ -SU(5) and pMSSM bulk regions superimposed over the August 2023 ATLAS Summary Plot of SUSY searches for electroweak production of smuons, plot here in terms of  $\Delta m = (\tilde{\mu}_{L,R}, \tilde{\chi}_1^0)$  for a Bino LSP, emphasizing consistency of the bulk with recent muon anomalous magnetic moment measurements. The inset is a zoom of the bulk.



**Figure:** Generalized No-Scale  $\mathcal{F}$ -SU(5) and pMSSM bulk regions consistent with the CMS SUSY searches for the sleptons.



**Figure:** Generalized No-Scale  $\mathcal{F}\text{-SU}(5)$  and pMSSM bulk regions consistent with the CMS SUSY searches for the light stau.

# The Light Right-Handed Stau Bulk Region in the pMSSM

- ▶ All pMSSM points with an  $\tilde{e}_R$  NLSP are excluded by the ATLAS soft lepton SUSY search.
- ▶ Therefore, like Generalized No-Scale  $\mathcal{F}$ - $SU(5)$ , the only viable pMSSM region in the bulk is for the case
 
$$m_{\tilde{\chi}_1^0} < m_{\tilde{\tau}_1} < m_{\tilde{e}_R} = m_{\tilde{\mu}_R}.$$
- ▶ Numerical findings disclose the ratio  $\mathcal{R}_{\tilde{\tau}_1} \gtrsim 10\%$  implies  $m_{\tilde{\chi}_1^0} \leq 117.7$  GeV. The upper bound on the light stau mass is about 129.3 GeV.
- ▶ The bulk alone can explain recent muon anomalous magnetic moment measurements.

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# The Right-Handed Smuon NLSP Scenario

- ▶ Dark matter.
- ▶ The muon anomalous magnetic moment.
- ▶ Consider gauge coupling unification and radiative electroweak gauge symmetry breaking, but neglect the fine-tuning issue.
- ▶ The SUSY scenario with minimal light sparticles.



# Scan Range

$$20 \text{ GeV} \leq M_1 \leq 400 \text{ GeV}$$

$$2 \leq \tan\beta \leq 65$$

$$1000 \text{ GeV} \leq M_2 \leq 5000 \text{ GeV}$$

$$1000 \text{ GeV} \leq M_A, \mu \leq 6000 \text{ GeV}$$

$$1200 \text{ GeV} \leq M_3 \leq 5000 \text{ GeV}$$

$$M_1 \leq m_{\tilde{\mu}_R} \leq 700 \text{ GeV}$$

$$2500 \text{ GeV} \leq m_{\tilde{q}}, m_{\tilde{Q}}, m_{\tilde{u}_R}, m_{\tilde{t}_R}, m_{\tilde{d}_R}, m_{\tilde{b}_R} \leq 5000 \text{ GeV}$$

$$700 \text{ GeV} \leq m_{\tilde{e}_L}, m_{\tilde{e}_R}, m_{\tilde{\mu}_L}, m_{\tilde{\tau}_L}, m_{\tilde{\tau}_R} \leq 2000 \text{ GeV}$$

$$-5000 \text{ GeV} \leq A_u, A_d, A_e, A_t, A_b, A_\tau \leq 5000 \text{ GeV}$$

## Experimental Constraints

- ▶ Gluino, squarks, sleptons, and Higgs mass constraints
- ▶ muon  $g - 2$

$$\Delta a_{\mu}^{\text{BNL+FNAL}} = (24.9 \pm 4.8) \times 10^{-10}$$

- ▶ Dark matter relic density constraint within the Planck 2018 experiment

$$0.114 \leq \Omega_{\text{DM}} h^2 \leq 0.126$$

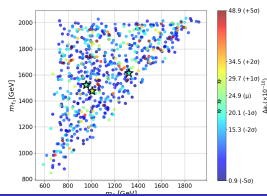
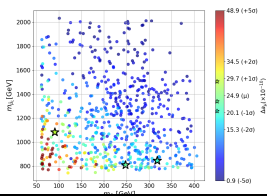
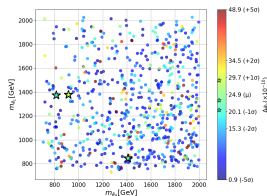
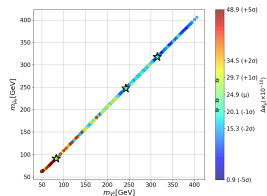
- ▶ Spin-independent DM-proton scattering cross-section from the LUX-ZEPLIN (LZ) experiment, future LZ 1000-day experiment, and spin-dependent scattering cross-sections from PICO-60  $C_3F_8$  and IceCube.

## Split the first and second family sleptons

- ▶  $m_{\tilde{\mu}_R} \neq m_{\tilde{e}_R}$ , all sparticles are heavy except Bino and right-handed smuon
- ▶ The relic density constraint become more strict compared to the degenerate case.
- ▶ Use SPheno 4.15.3 to compute the mass spectrum and experimental observable, and MicrOMEGAs 5.0 to calculate the DM relic density

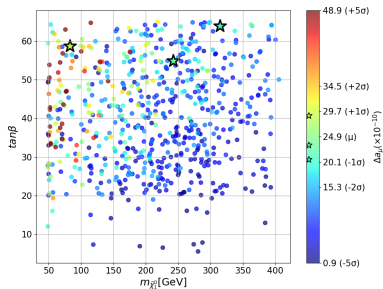
# Slepton mass

Every solid point is color coded to this  $\Delta a_\mu$  color scale.



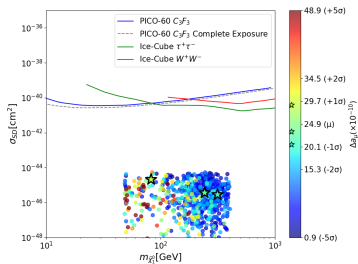
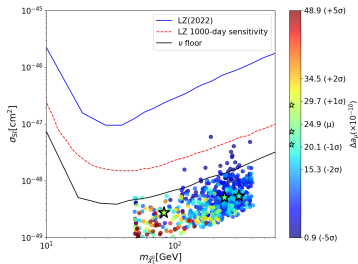
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$\tan\beta$



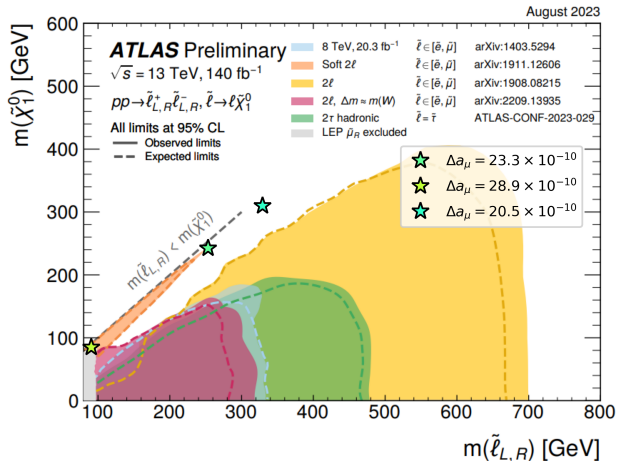
## DM SI/SD cross section

Spin-independent and Spin-dependent DM detection cannot cover large  $\Delta a_\mu$ , leaving this compressed mass region to be explored by colliders



## Collider Slepton Search

- ▶ NLSP:  $\tilde{\mu}_R; m_{\tilde{e}_L}, m_{\tilde{e}_R}, m_{\tilde{\mu}_L}, m_{\tilde{\tau}_1}, m_{\tilde{\tau}_2} > 700$  GeV.
- ▶ The LHC SUSY search constraints are for degenerate case for the left-handed and right-handed selectrons and smuons, and the mass bound is around 240 GeV.
- ▶ What is the LHC SUSY constraints on the right-handed smuon mass? If it is smaller than 180 GeV, this scenario might be probed by the FCC<sub>ee</sub> and CEPC.
- ▶ Using the ATLAS SUSY search constraints, the bulk point (bottom left corner) has been excluded, and the remaining two points are for co-annihilation.





Input	★	Output	★
$M_1$	246	$m_h, m_H, m_{H^\pm}$	123, 4827, 4828
$M_2$	3337	$m_{\tilde{\chi}_{1,2}^0}$	242.1, 2851.6
$M_3$	4214	$m_{\tilde{\chi}_{3,4}^0}$	2859.1, 3330.4
$\tan\beta$	54.86	$m_{\tilde{\chi}_{1,2}^\pm}$	2852.1, 3330.5
$M_A$	4827	$m_{\tilde{g}}$	4323.1
$\mu$	2870	$m_{\tilde{u}_{L,R}, \tilde{d}_{L,R}}$	3584.1, 3558.1, 3585, 3556.3
$m_{\tilde{q}, \tilde{Q}}$	3419, 2325	$m_{\tilde{t}_{1,2}, \tilde{b}_{1,2}}$	2523.5, 4967, 2521.4, 4437.6
$m_{\tilde{u}_R, \tilde{d}_R}$	3419, 3419	$m_{\tilde{\nu}_{e,\mu,\tau}}$	841.1, 805.2, 989.6
$m_{\tilde{t}_R, \tilde{b}_R}$	4906, 4347	$m_{\tilde{e}_{L,R}}$	845.2, 1408.5
$m_{\tilde{e}_L, \tilde{e}_R}$	780, 1407.73	$m_{\tilde{\mu}_{L,R}}$	809.9, 247.4
$m_{\tilde{\mu}_L, \tilde{\mu}_R}$	742, 249.71	$m_{\tilde{\tau}_{1,2}}$	954.3, 1523.8
$m_{\tilde{\tau}_L, \tilde{\tau}_R}$	957, 1542.28	$\Delta a_\mu \times 10^{-10}$	23.3
$A_{u,d}$	-3258, -184	$\Omega_{\tilde{\chi}} h^2$	0.122
$A_{t,b}$	-3018, -2905	$\sigma_{SI} \times 10^{-12} [\text{pb}]$	0.508
$A_{e,\tau}$	849, 1921	$\sigma_{SD} \times 10^{-8} [\text{pb}]$	0.0378

Figure: The benchmark point for the NLSP smuon.

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## Summary

- ▶ We propose Generalized No-Scale Supergravity, the simplest scenario for Effective Super-Natural Supersymmetry, which solve the supersymmetry electroweak fine-tuning problem naturally.
- ▶ A light right-handed slepton bulk region is realized in the Generalized No-Scale  $\mathcal{F}$ - $SU(5)$  and the pMSSM.
- ▶ The bulk region may be beyond the LHC reach, though can be probed at the 1000-day LUX-ZEPLIN, Future Circular Collider (FCC-ee) at CERN, Circular Electron Positron Collider (CEPC), and Hyper-Kamiokande experiments.

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Thank You Very Much  
for Your Attention!